

# Searching for proton decay with paleo-detectors

based on “The Final Frontier for Proton Decay” arXiv:2405.15845  
with Sebastian Baum, Cassandra Little, Paola Sala and Joshua Spitz

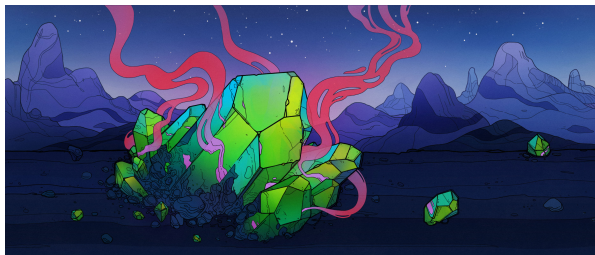


Figure: Olena Shmahalo/Quanta Magazine

 **Jožef Stefan  
Institute  
Ljubljana, Slovenia**



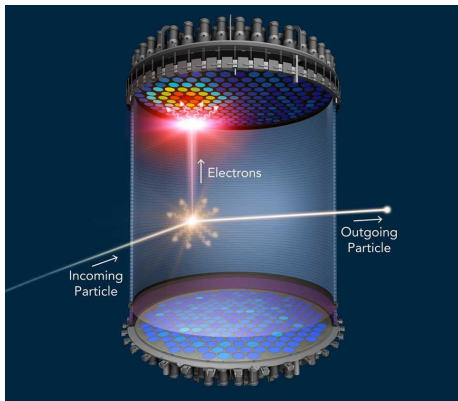
**SMASH**  
machine learning for science and humanities postdoctoral program



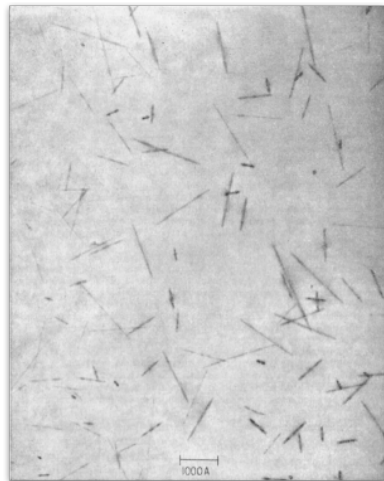
**Co-funded by  
the European Union**

This project has received funding from the European Union's Horizon Europe research and innovation programme under the Marie Skłodowska-Curie grant agreement No. 101081355.

# Damage features from recoils in ancient minerals

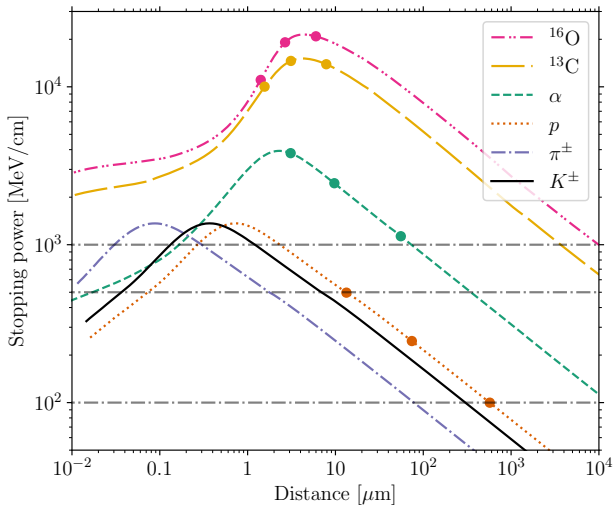
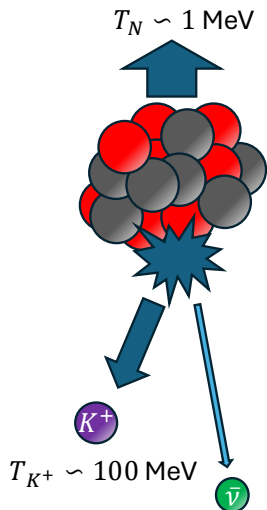


**Figure:** LUX-ZEPLIN (LZ) Collaboration / SLAC National Accelerator Laboratory

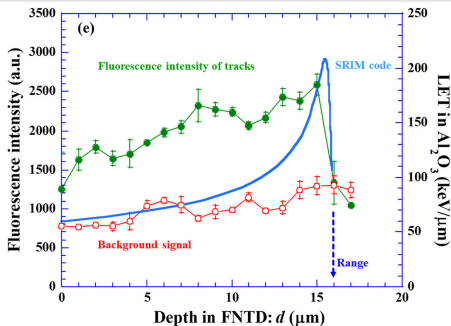
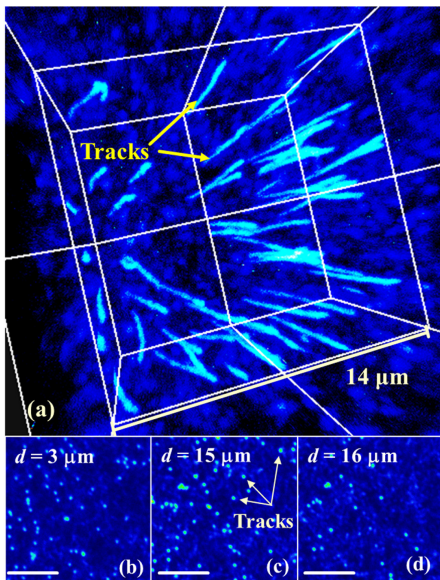


**Figure:** Price+Walker (1963)

# Large exposure from small target $\Rightarrow$ kg Gyr = 1 Mton yr



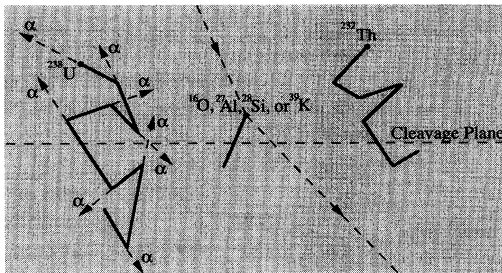
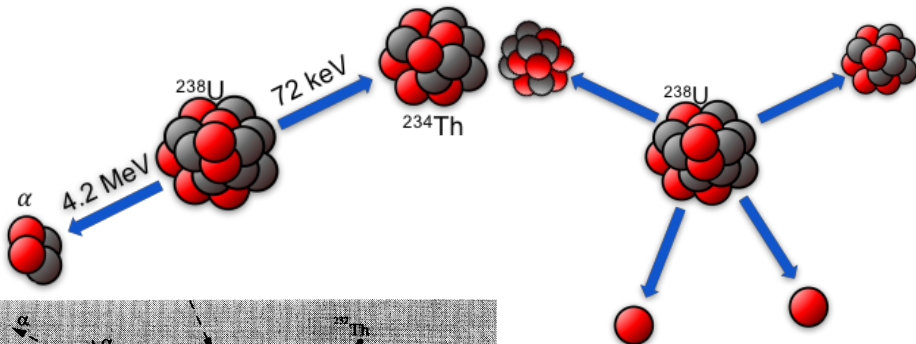
# Fluorescent nuclear track detectors for $K^+$ endpoints



Figures from Kusumoto et al. (2022) show proton tracks in doped sapphire

- Theory of track formation?
- Are tracks robust to annealing?
- Use  $dE/dx$  proxy for tracks

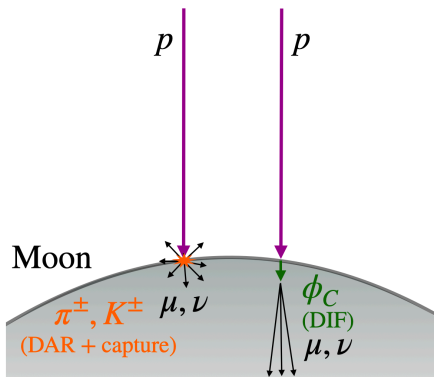
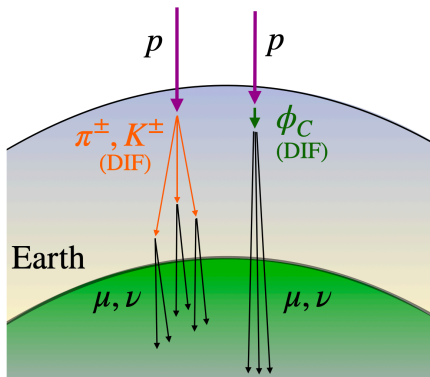
# Nuclear recoils from $\alpha$ -decays and spontaneous fission



Need very radiopure minerals

**Ultra-basic rocks** formed in the mantle with  $C^{238} \gtrsim 0.01$  ppb

# Atmospheric neutrinos induce $\mathcal{O}(100) K^+ / 100 \text{ g/Gyr}$



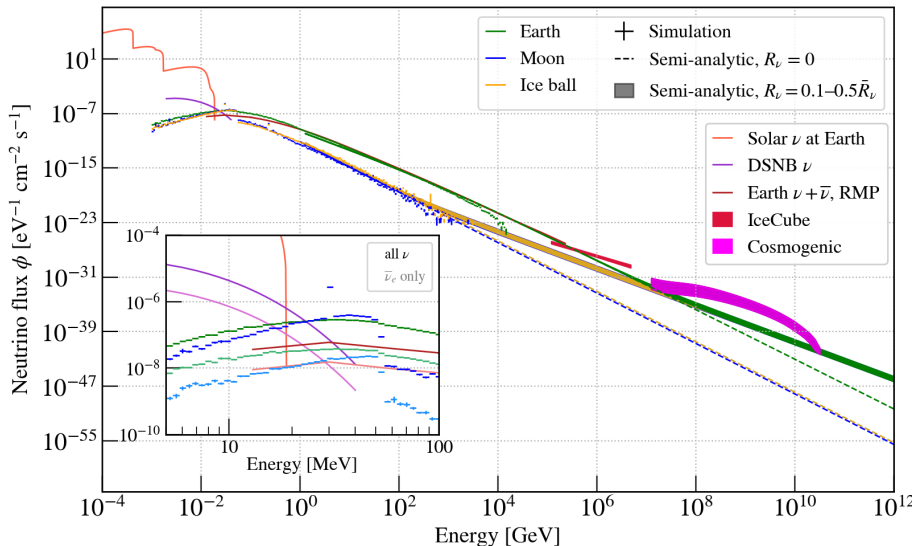
Figures from arXiv:2411.09634

- Conventional secondary mesons **decay in flight** on Earth
- Prompt fluxes from short-lived mesons decaying in flight

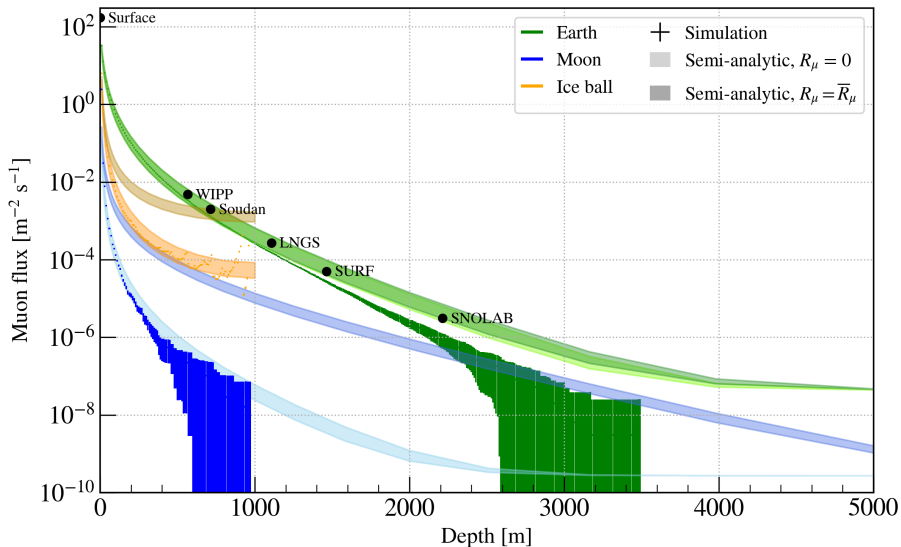
Suppression of lunar  $\mu$  and  $\nu$  fluxes

- Conventional secondary mesons **decay at rest** on the Moon
- Less suppression of short-lived mesons decaying in flight

# Lunar neutrinos induce $\sim 0.5 K^+ / 100 \text{ g} / \text{Gyr}$ in Olivine

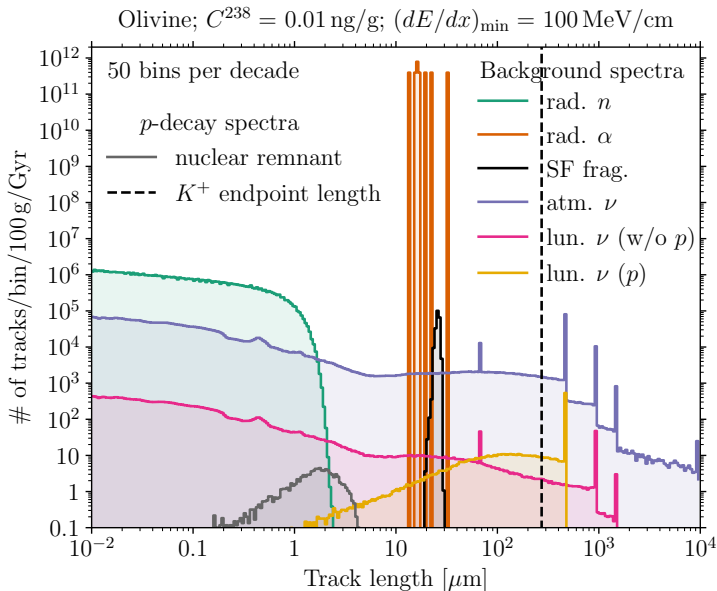


# Lunar muons induce $\sim 0.1 K^+ / 100 \text{ g} / \text{Gyr}$ at $\sim 5 \text{ km}$ depth





Expect  $\lesssim 6 K^+ / 100 \text{ g} / \text{Gyr}$  for  $\tau(p \rightarrow \bar{\nu} K^+) > 5.9 \times 10^{33} \text{ yr}$



## Astrophysics &gt; Cosmology and Nongalactic Astrophysics

*[Submitted on 2 May 2024]***Mineral Detection of Neutrinos and Dark Matter 2024. Proceedings**

Sebastian Baum, Patrick Huber, Patrick Stengel, Natsue Abe, Daniel G. Ang, Lorenzo Apollonio, Gabriela R. Araujo, Levente Balogh, Pranshu Bhaumik Yilda Boukhtouchen, Joseph Bramante, Lorenzo Caccianiga, Andrew Calabrese-Day, Qing Chang, Juan I. Collar, Reza Ebadi, Alexey Elykov, Katherine Freese, Audrey Fung, Claudio Galelli, Arianna E. Gleason, Mariano Guerrero Perez, Janina Hakenmüller, Takeshi Hanyu, Noriko Hasebe, Shigenobu Hirose, Shunsaku Horiuchi, Yasushi Hoshino, Yuki Ido, Vsevolod Ivanov, Takashi Kamiyama, Takenori Kato, Yoji Kawamura, Chris Kelso, Giti A. Khodaparast, Emilie M. LaVoie-Ingram, Matthew Leybourne, Xingxin Liu, Thalles Lucas, Brenden A. Magill Federico M. Mariani, Charlotte Mkhonto, Hans Pieter Mumm, Kohta Murase, Tatsuhiro Naka, Kenji Oguni, Kathryn Ream, Kate Scholberg, Maximilian Shen, Joshua Spitz, Katsuhiko Suzuki, Alexander Takla, Jiashen Tang, Natalia Tapia-Arellano, Pieter Vermeesch, Aaron C. Vincent, Nikita Vladimirov, Ronald Walsworth, David Waters, Greg Wurtz, Seiko Yamasaki, Xianyi Zhang

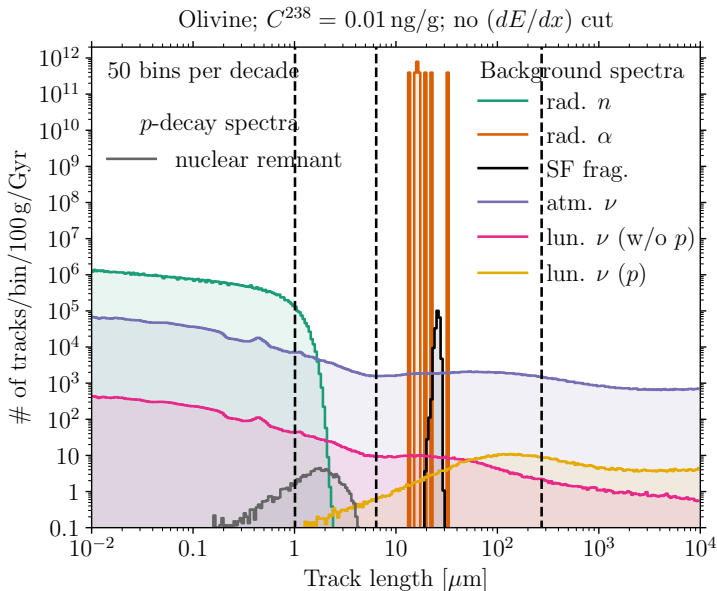
**MD $\nu$ DM community**

- Groups across Europe, North America and Japan
- Astroparticle theorists, experimentalists, geologists, and materials scientists

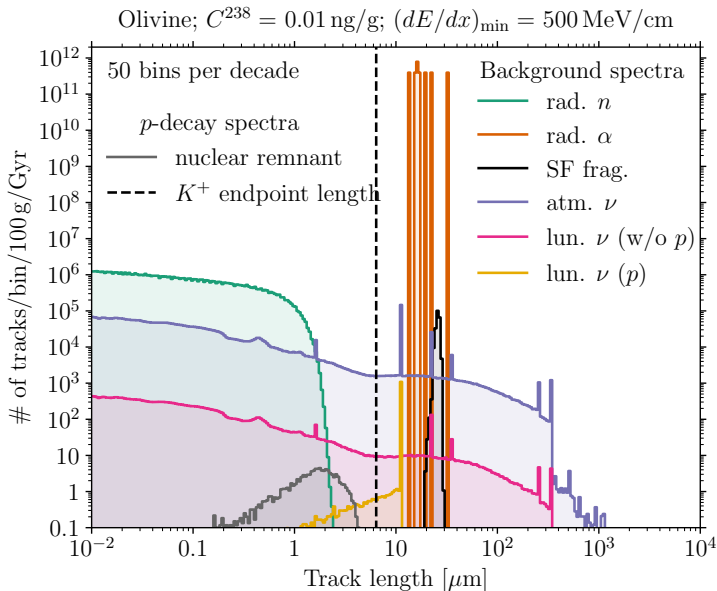
**Also check out our whitepaper!**  
arXiv:2301.07118, 2405.01626

- History of mineral detectors
- Review of scientific potential for particle physics, reactor neutrinos and geoscience

# Trade-off between read-out resolution and exposure



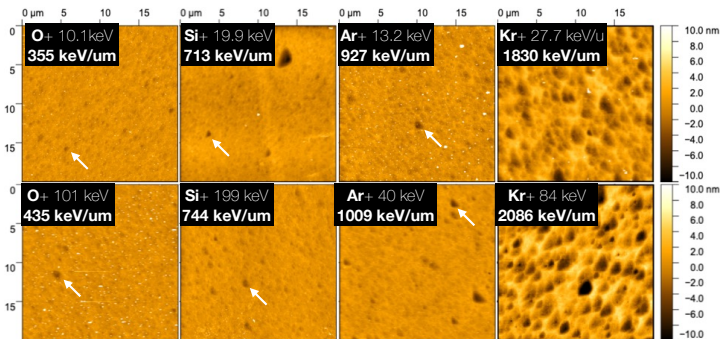
# Trade-off between read-out resolution and exposure



# New techniques allow for much larger readout capacity



Irradiation dose is 80 ions per field of view (20umx20um).



proxy	DM scattering	alpha recoils
pit formation efficiency	several to 10 %	~ 100%

# Cleaving and etching limits $\epsilon$ and can only reconstruct 2D

## Readout scenarios for different $x_T$

- HIBM+pulsed laser could read out 10 mg with nm resolution
- SAXs at a synchrotron could resolve 15 nm in 3D for 100 g

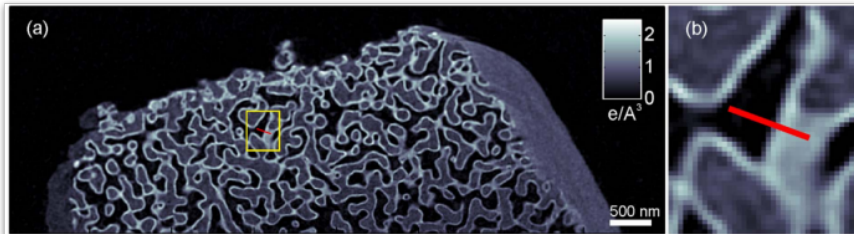
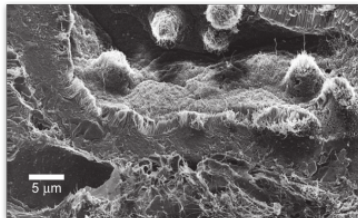
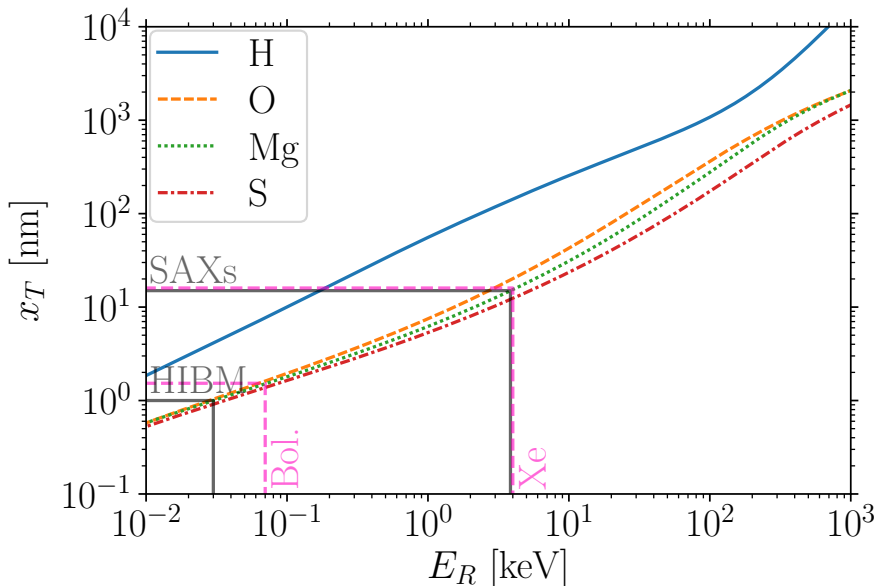
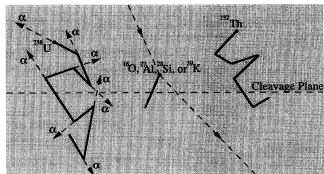


Figure: HIM rodent kidney Hill+ '12, SAXs nanoporous glass Holler+ '14

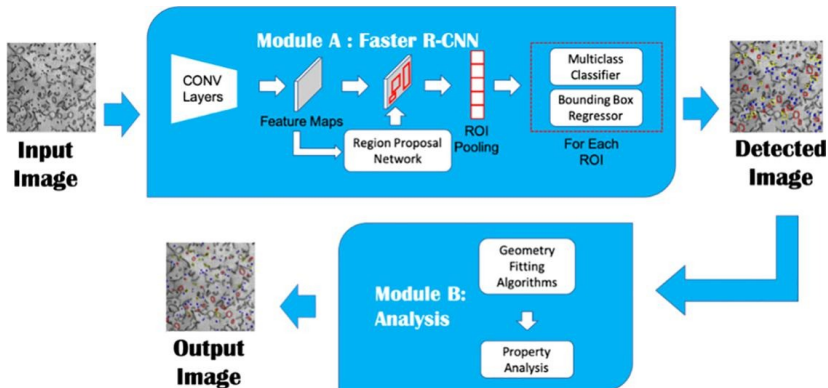
# Integrate stopping power to estimate track length



# Recognition of sparse tracks is a data analysis challenge



- 15 nm resolution of 100 g sample  
 $\Rightarrow 10^{19}$  mostly empty voxels
- 1 Gyr old with  $C^{238} = 0.01$  ppb  
 $\Rightarrow 10^{13}$  voxels for  $\alpha$ -recoil tracks





# Scattering cross sections $\Rightarrow$ scattering rates

$$\frac{d^2\sigma}{dq^2 d\Omega_q} = \frac{d\sigma}{dq^2} \frac{1}{2\pi} \delta\left(\cos\theta - \frac{q}{2\mu_{\chi T} v}\right) \simeq \frac{\sigma_0 F(q)^2}{8\pi\mu_{\chi T}^2 v} \delta\left(v \cos\theta - \frac{q}{2\mu_{\chi T}}\right)$$

$$\frac{d^2R}{dE_R d\Omega_q} = 2M_T \frac{N_T}{M_T N_T} \int \frac{d^2\sigma}{dq^2 d\Omega_q} n_X v f(v) d^3v \simeq \frac{\sigma_0 F(q)^2}{4\pi\mu_{\chi T}} n_X \hat{f}(v_q, \hat{q})$$

## Differential cross section

- $\delta$ -function imposes **kinematics**
- $\sigma_0$  is velocity and momentum independent cross section for **scattering off pointlike nucleus**

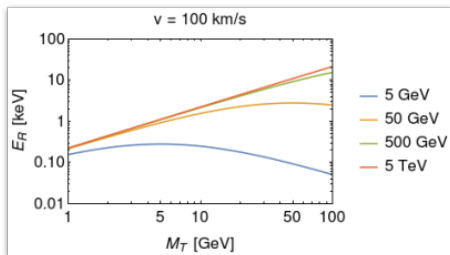
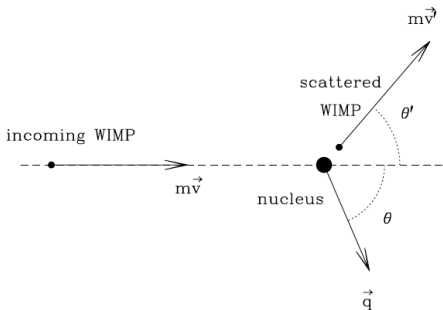
$$F(q) \simeq \frac{9 [\sin(qR) - qR \cos(qR)]^2}{(qR)^6}$$

## Differential scattering rate

- Rate per unit time per unit **detector mass** for **all nuclei**
- Convolute cross section with **astrophysical WIMP flux**

$$\sigma_0^{SI} = \frac{4}{\pi} \mu_{\chi T}^2 [Z f_s^p + (A - Z) f_s^n]^2$$

# Nuclear recoils induced by elastic WIMP-nucleus scattering



Rate per unit time per unit mass

$$\frac{dR}{dE_R} = \frac{n_X}{2} \frac{\sigma_{Xp}^{SI}}{\mu_{Xp}^2} A^2 F(q)^2 \eta(v_q)$$

Scattering kinematics  $\Rightarrow$  event rate

- Account for **finite size** of nucleus
- Convolute with **WIMP flux**
- Write **cross section** in terms of WIMP-nucleon interaction

# WIMP velocity distribution and induced recoil spectra

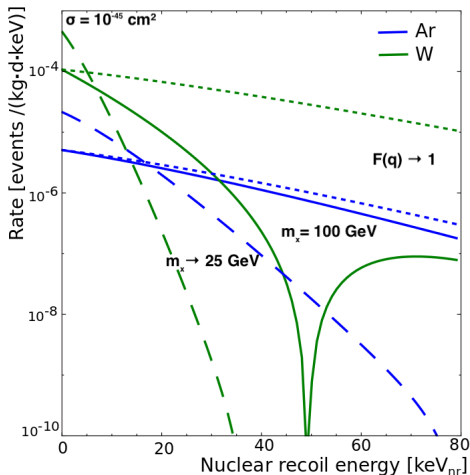
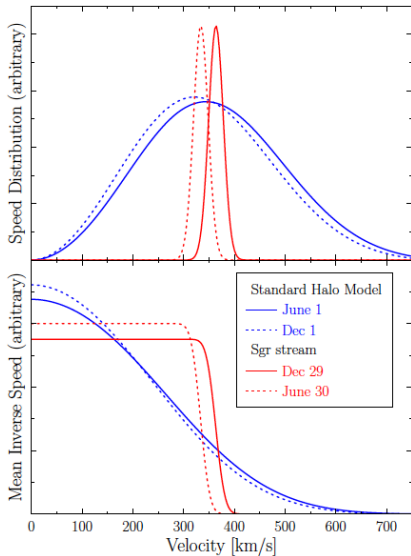


Figure: (left) 1209.3339 (right) 1509.08767

# Mineral detectors used to constrain WIMPs before

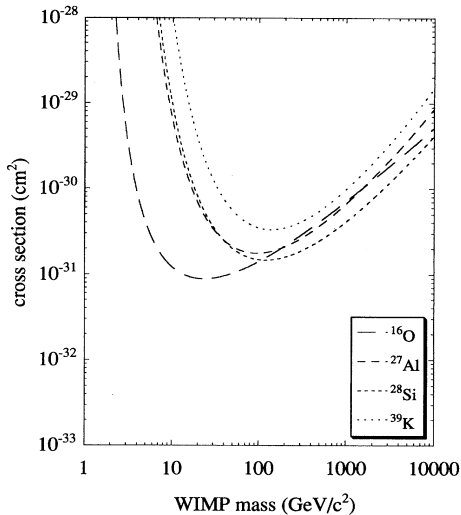
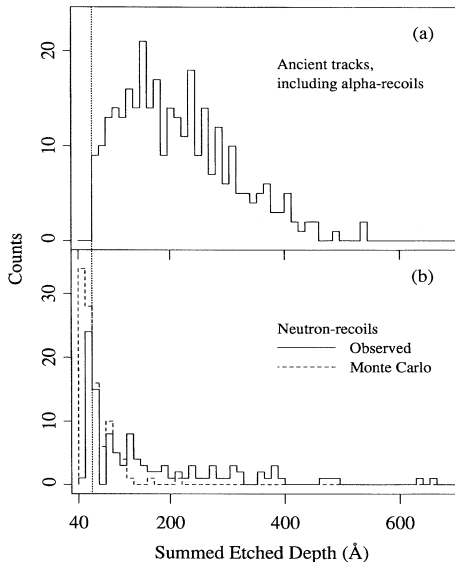
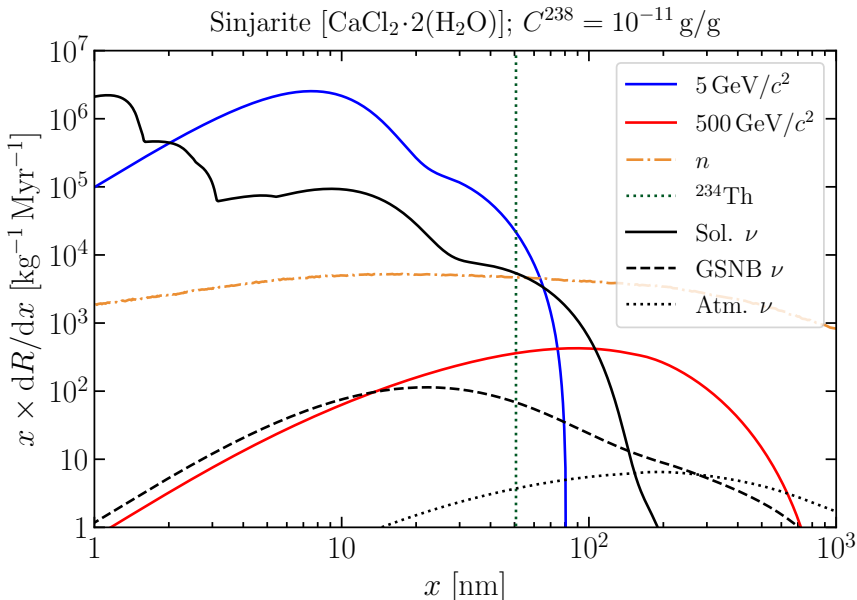
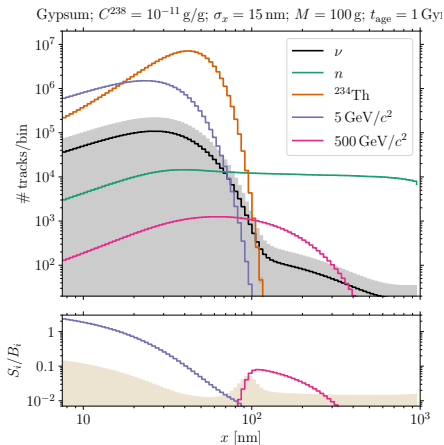
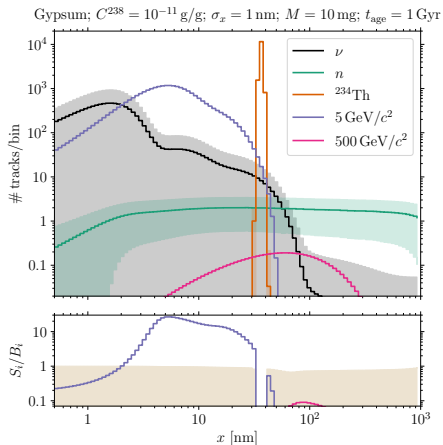


Figure: Snowden-Ifft et al. (1995)

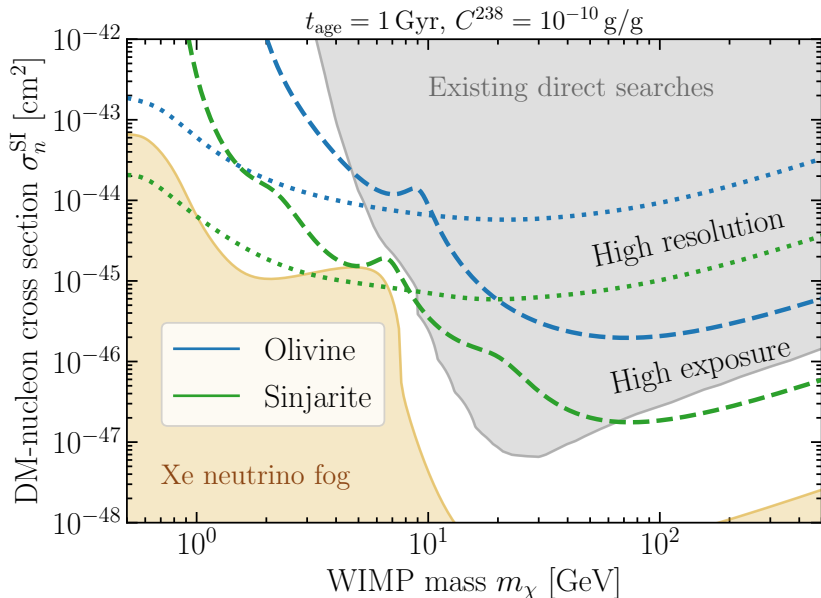
# Use track length spectra to pick out WIMP signal



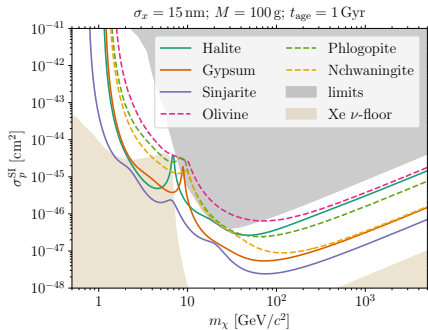
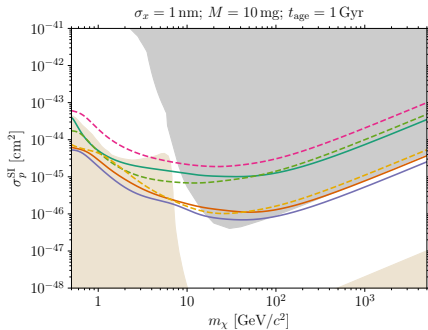
# Track length spectra after smearing by readout resolution



# Trade-off between read-out resolution and exposure



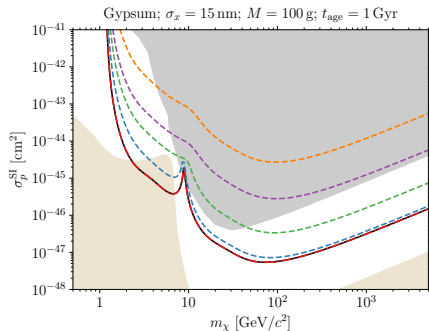
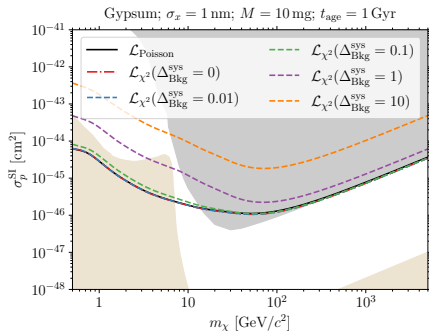
# Sensitivity for different targets



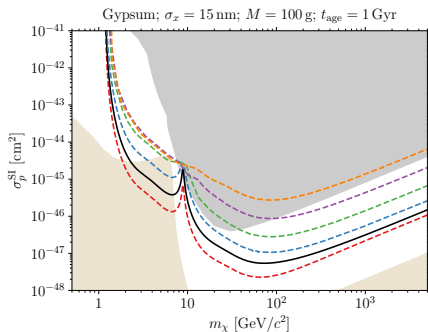
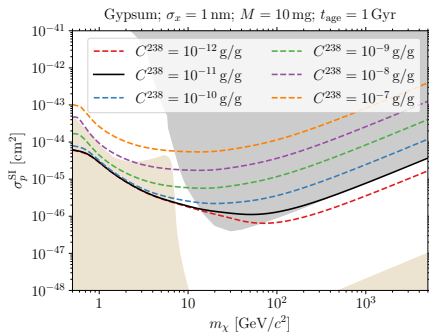
Halite	NaCl	$C^{238} = 10^{-11} \text{ g/g}$
Gypsum	$\text{Ca}(\text{SO}_4) \cdot 2(\text{H}_2\text{O})$	$C^{238} = 10^{-11} \text{ g/g}$
Sinjarite	$\text{CaCl}_2 \cdot 2(\text{H}_2\text{O})$	$C^{238} = 10^{-11} \text{ g/g}$
Olivine	$\text{Mg}_{1.6}\text{Fe}_{0.4}^{2+}(\text{SiO}_4)$	$C^{238} = 10^{-10} \text{ g/g}$
Phlogopite	$\text{KMg}_3\text{AlSi}_3\text{O}_{10}\text{F}(\text{OH})$	$C^{238} = 10^{-10} \text{ g/g}$
Nchwangingite	$\text{Mn}_2^{2+}\text{SiO}_3(\text{OH})_2 \cdot (\text{H}_2\text{O})$	$C^{238} = 10^{-10} \text{ g/g}$



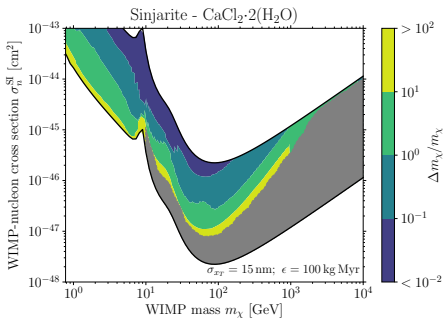
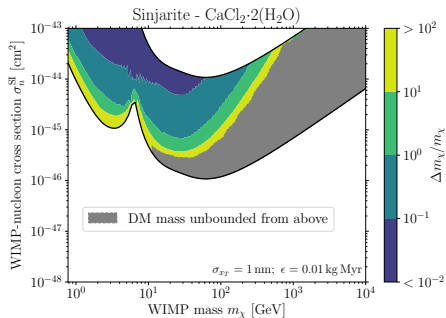
# Effects of background shape systematics



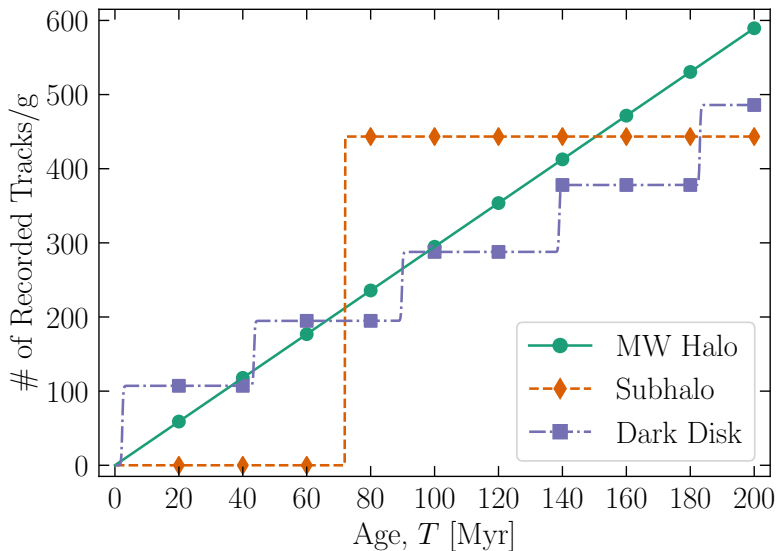
# Sensitivity for different $^{238}\text{U}$ concentrations



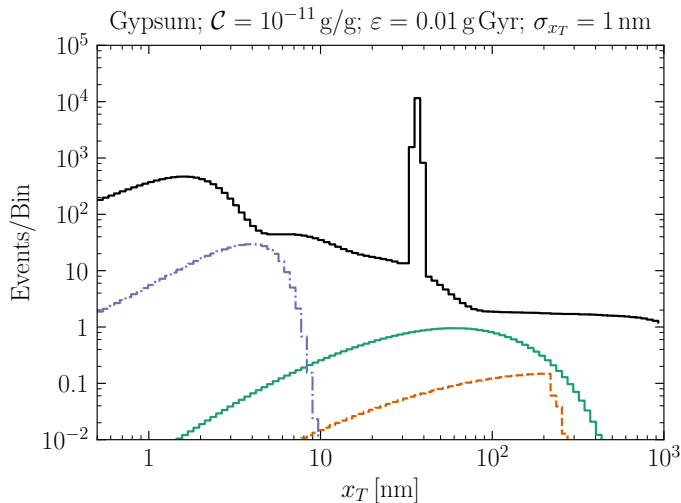
# Multiple nuclei and large $\epsilon$ allow for optimal $\Delta m_\chi/m_\chi$



# Mineral detectors can look for signals “averaged” over geological timescales or for time-varying signals

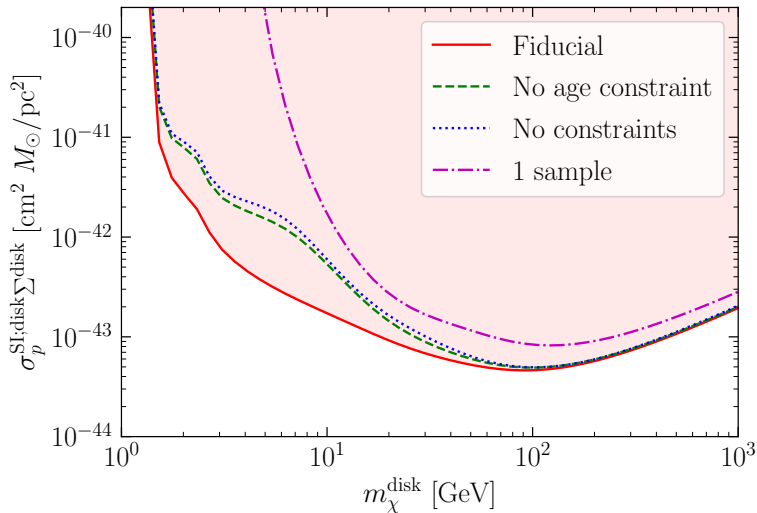


# Multiple samples to detect dark disk transit every $\sim 45$ Myr



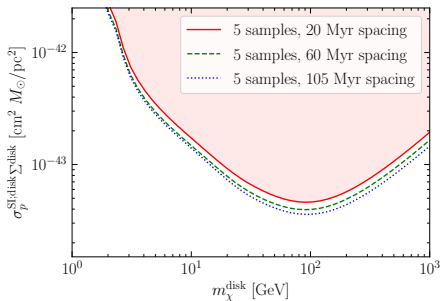
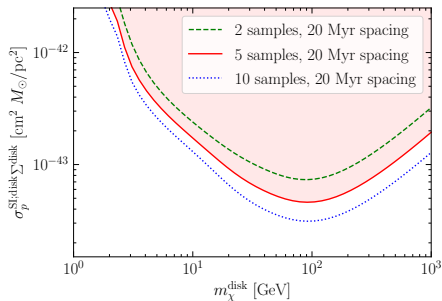
$$m_X^{\text{disk}} = 100 \text{ GeV} \quad \sigma_{Xp}^{\text{disk}} = 10^{-43} \text{ cm}^2 \quad m_X = 500 \text{ GeV} \quad \sigma_{Xp} = 5 \times 10^{-46} \text{ cm}^2$$

# Distinguish from halo with 20, 40, 60, 80, 100 Myr samples

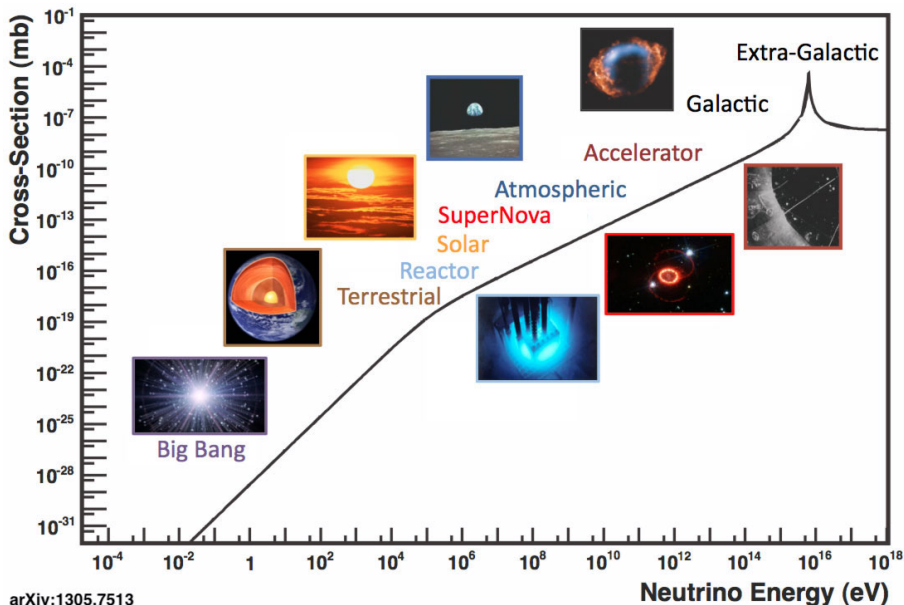


**Systematic uncertainties**  $\Delta_t = 5\%$   $\Delta_M = 0.1\%$   $\Delta_C = 10\%$   $\Delta_\Phi = 100\%$

# Change number of samples and sample spacing in time



# Neutrinos come from a variety of sources



arXiv:1305.7513



# Nuclear recoil spectrum depends on neutrino energy

$$\frac{dR}{dE_R} = \frac{1}{m_T} \int dE_\nu \frac{d\sigma}{dE_R} \frac{d\phi}{dE_\nu}$$

- **Quasi-elastic** for  $E_\nu \gtrsim 100$  MeV
- **Resonant  $\pi$  production** at  $E_\nu \sim$  GeV
- **Deep inelastic** for  $E_\nu \gtrsim 10$  GeV

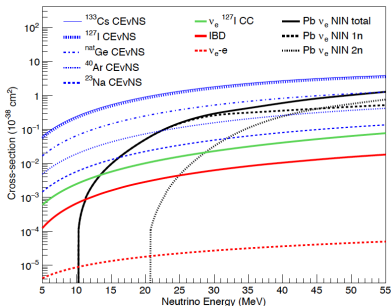


Figure: COHERENT, 1803.09183

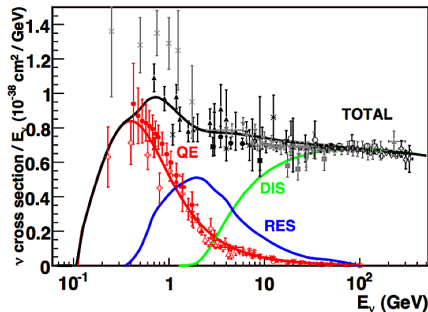
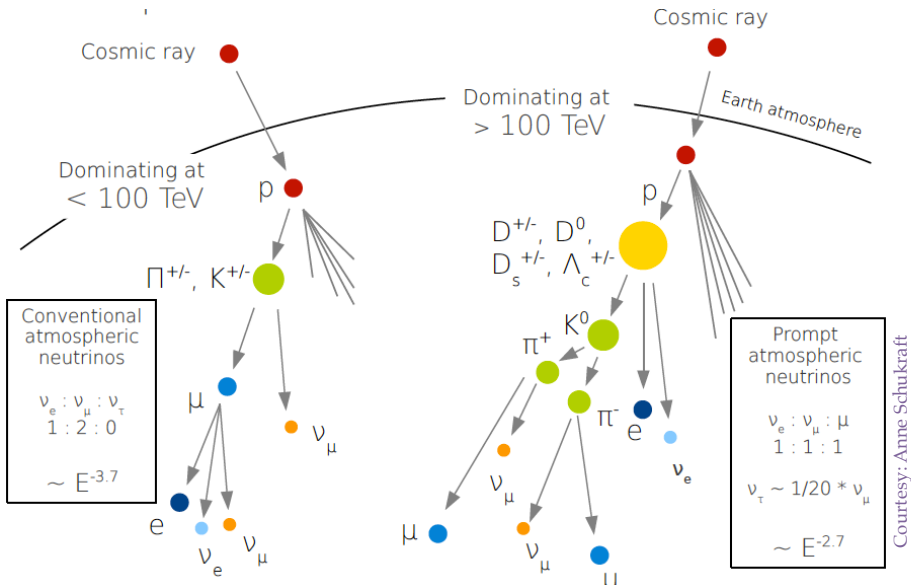


Figure: Inclusive CC  $\sigma_{\nu N}$ , 1305.7513

# Atmospheric $\nu$ 's originating from CR interactions



Courtesy: Anne Schukraft

# Atmospheric $\nu$ 's originating from CR interactions

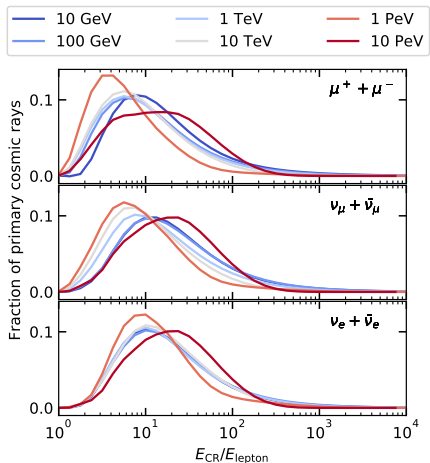


Figure:  $E_{CR}$  to leptons, 1806.04140

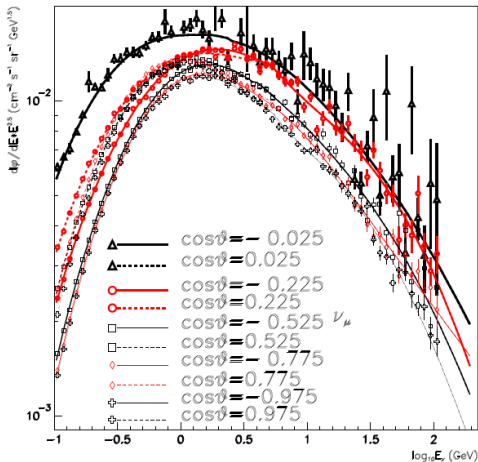


Figure: FLUKA simulation of  $\nu_\mu$  flux at SuperK for solar max, hep-ph/0207035

# Geomagnetic field deflects lower energy CR primaries

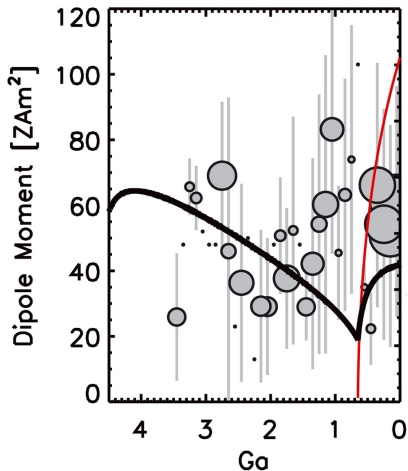
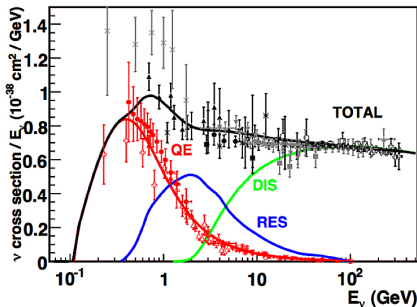


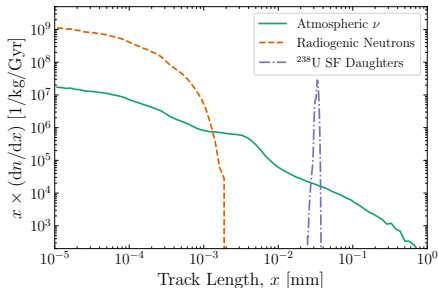
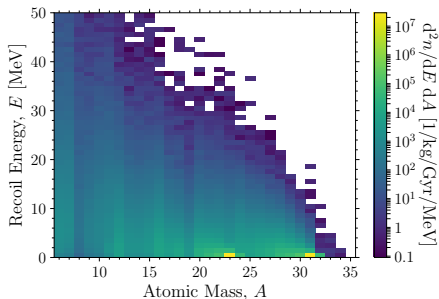
Figure: Driscoll, P. E. (2016),  
*Geophys. Res. Lett.*, 43, 5680-5687

Rigidity  $p_{CR}/Z_{CR} \simeq E_{CR}$  for CR protons

- Rigidity cutoff  $\propto M_{dip}$  truncates atmospheric  $\nu$  spectrum at low  $E_\nu$
- Maximum cutoff today  $\sim 50$  GV
- Recall CR primary  $E_{CR} \gtrsim 10 E_\nu$



# Recoil spectra from atmospheric $\nu$ 's incident on NaCl(P)



## Recoils of many different nuclei

- Low energy peak from QE neutrons scattering  $^{23}\text{Na}$ ,  $^{31}\text{P}$
- High energy tail of lighter nuclei produced by DIS

## Background free regions for $\gtrsim 1 \mu\text{m}$

- Radiogenic n-bkg confined to low  $x$ , regardless of target
- Subdominant systematics from atmosphere, heliomagnetic field

# Galactic contribution to $\nu$ flux over geological timescales

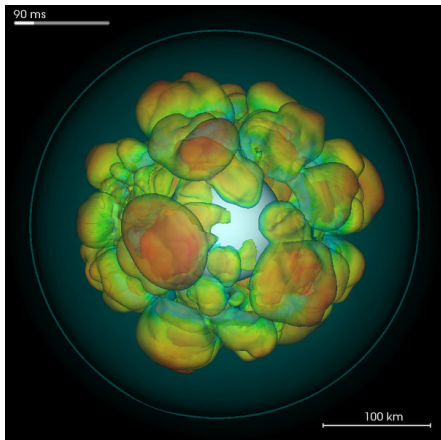


Figure: Supernova simulation after CC

Only  $\sim 2$  SN 1987A events/century

- Measure galactic CC SN rate
- Traces star formation history

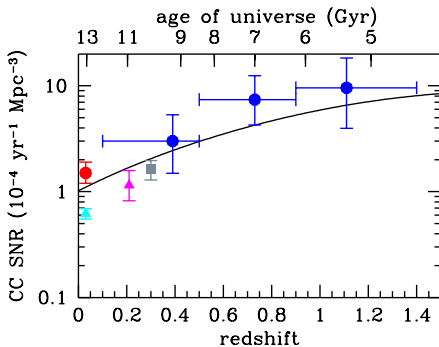


Figure: Cosmic CC SNR, 1403.0007

# Galactic contribution to $\nu$ flux over geological timescales

$$\frac{d\phi}{dE_\nu} = \dot{N}_{\text{CC}}^{\text{gal}} \frac{dn}{dE_\nu} \int_0^\infty dR_E \frac{f(R_E)}{4\pi R_E^2}$$

Only  $\sim 2$  SN 1987A events/century

- Measure galactic CC SN rate
- Traces star formation history

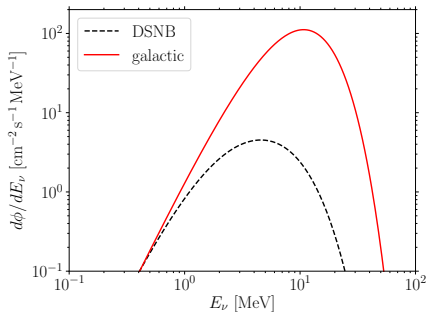
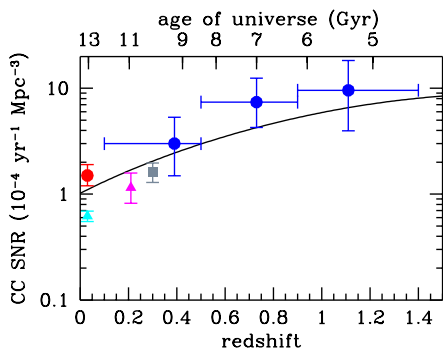
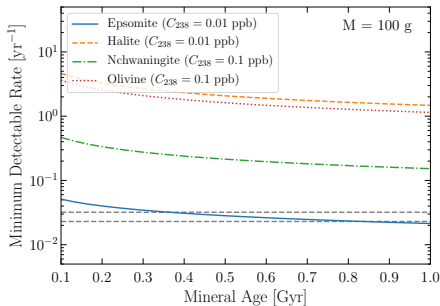
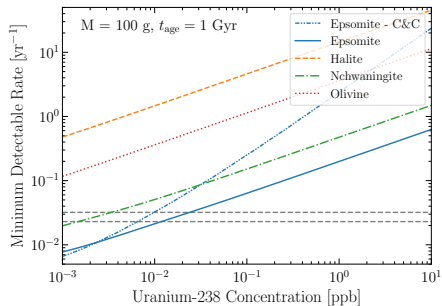


Figure: Cosmic CC SNR, 1403.0007

# Sensitivity to galactic CC SN rate depends on $C^{238}$



Epsomite [ $\text{Mg}(\text{SO}_4) \cdot 7(\text{H}_2\text{O})$ ]

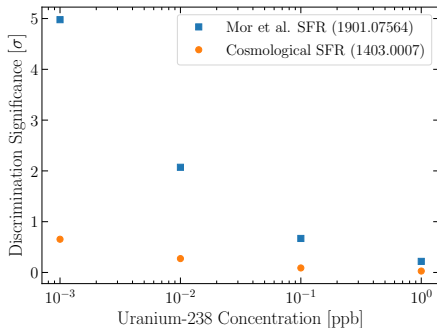
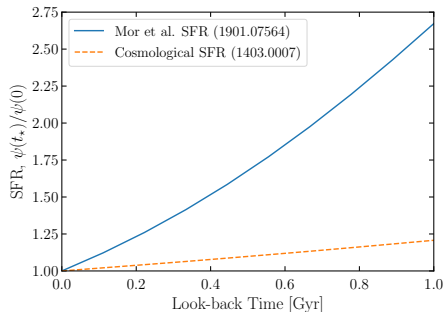
Halite [ $\text{NaCl}$ ]

Nchwangingite [ $\text{Mn}_2^+ \text{SiO}_3(\text{OH})_2 \cdot (\text{H}_2\text{O})$ ]

Olivine [ $\text{Mg}_{1.6}\text{Fe}_{0.4}^{2+}(\text{SiO}_4)$ ]



# Difficult to pick out time evolution of galactic CC SN rate



## Coarse grained cumulative time bins

- 10 Epsomite paleo-detectors
- 100 g each,  $\Delta t_{\text{age}} \simeq 100$  Myr

## Determine $\sigma$ rejecting constant rate

Could only make discrimination at  $3\sigma$  for  $\mathcal{O}(1)$  increase in star formation rate with  $C^{238} \lesssim 5$  ppt

# Solar $\nu$ 's produced in fusion chains from H to He

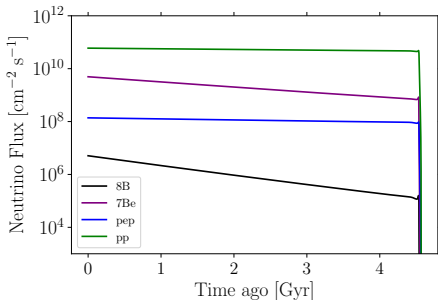
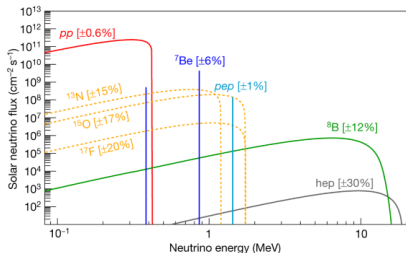
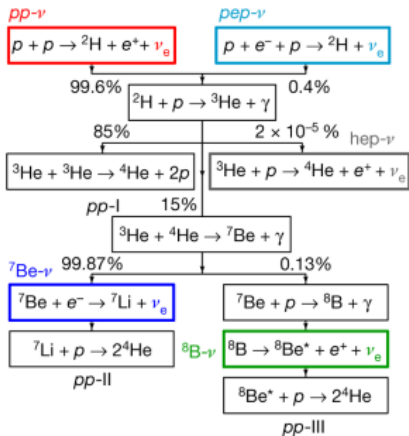
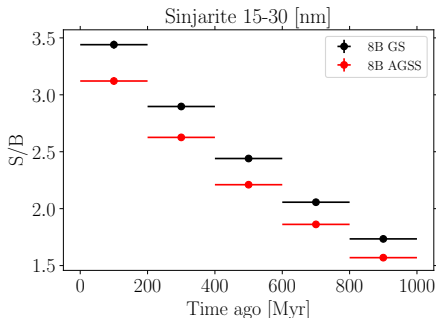
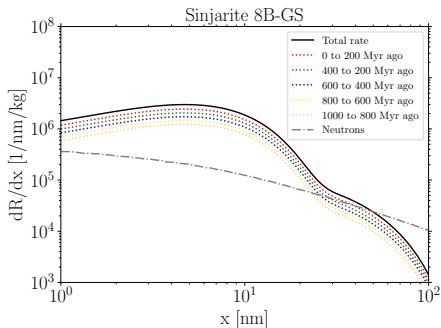


Figure: Today's flux at Borexino (Nature, 2018) and time dependence of GS metallicity model, 2102.01755

# Could use large exposure to differentiate between scenarios



## Could measure $^8B$ flux over time

- Higher  $E_\nu \Rightarrow$  longer tracks
- Highly dependent on solar core temperature with flux  $\propto T^{24}$
- Sensitive to metallicity model

## 100 g samples with 15 nm resolution

- Look in single bin 15 – 30 nm
- Assume  $\Delta_t \sim 10\%$ ,  $\Delta_C = 10\%$
- $N_{\text{tot}}^{\text{GS}} \sim (1.63 \pm 0.05) \times 10^6$
- $N_{\text{tot}}^{\text{AGSS}} \sim (1.52 \pm 0.05) \times 10^6$

# Reactor $\nu$ 's produced in $\beta$ decays of fission fragments

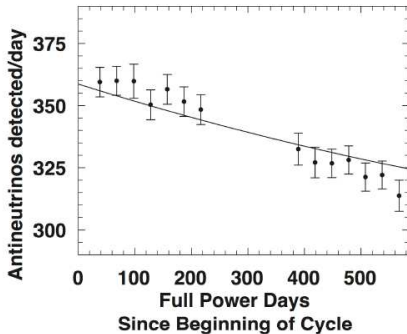
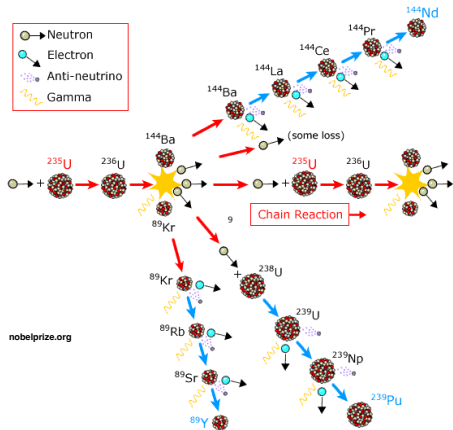


Figure: Processes yielding reactor  $\nu$ 's and time dependence over the course of reactor fuel cycle for  $^{239}\text{Pu}$  (1605.02047)

## Nuclear non-proliferation safeguards

- Measure soft nuclear recoils
- Passive and robust detectors operable at room temperature

# Semi-analytic range calculations and SRIM agree with data

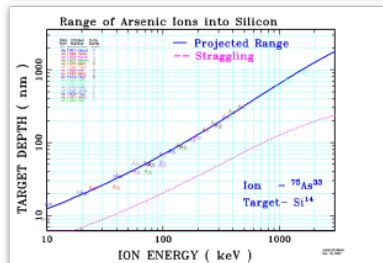
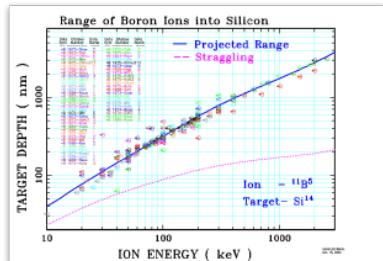
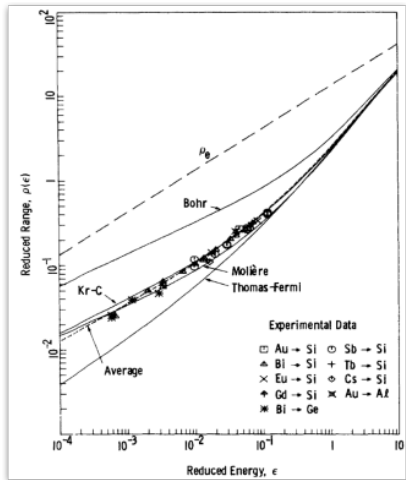


Figure: Wilson, Hagmark+ '76