



# Walking in the Hidden Valley

Exploring near-conformal dark sectors

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(Paper to appear!)

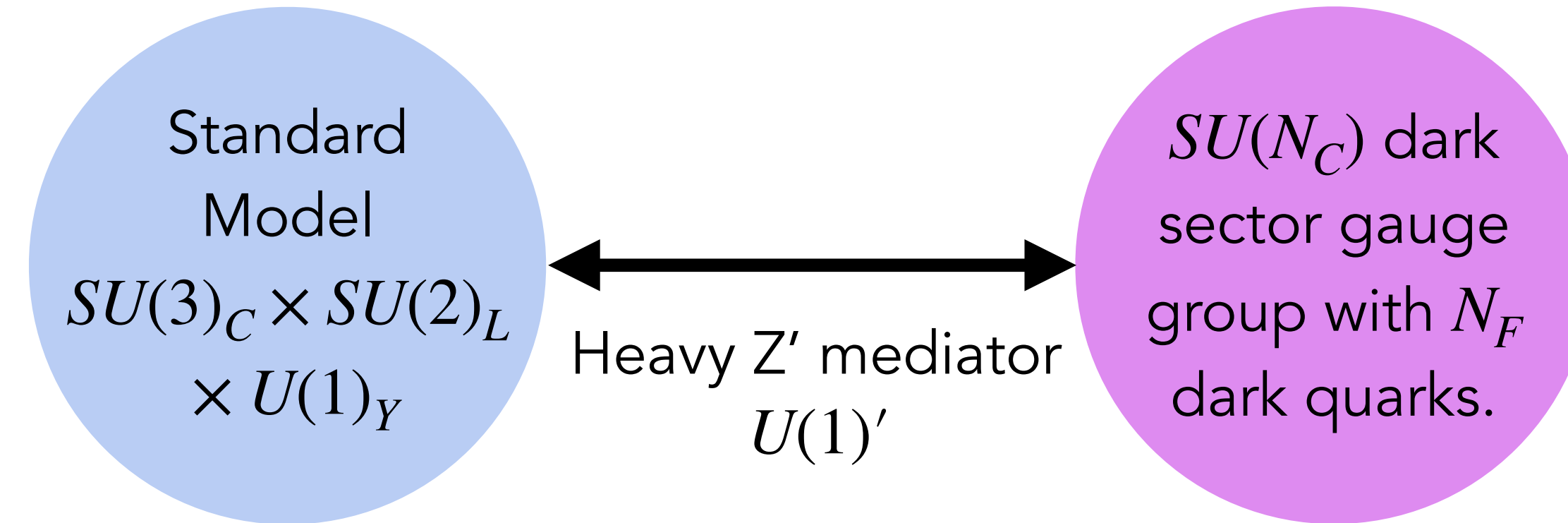
# Confining dark sector models

arXiv:0604261, M.J. Strassler et al.

arXiv:1502.05409, P. Schwaller et al.

arXiv:1503.00009, T. Cohen et al.

arXiv:0712.2041, T. Han et al.



- Hidden Valley models that extend the SM with a new confining dark sector resembling QCD present exciting opportunities for new physics discovery. We will focus on light dark quarks; Dirac fermions in the fundamental representation of  $SU(N_C)$ .
- At colliders, these dark quarks undergo parton showering, hadronisation and decay giving rise to anomalous jet signatures (e.g. emerging or semi-visible jets) that are well-known at small  $N_F/N_C$ . Large  $N_F/N_C$  dark sectors are a largely undeveloped area of theory space and could give rise to distinct signatures.
- There is a plethora of work focused on the non-perturbative structure and the low-energy effective descriptions of large  $N_F/N_C$  theories; can be used to build up near-conformal dark sector models in the future.

arXiv:2306.07236, A. Hasenfratz et al.

arXiv:1610.01752, M. Golterman et al.

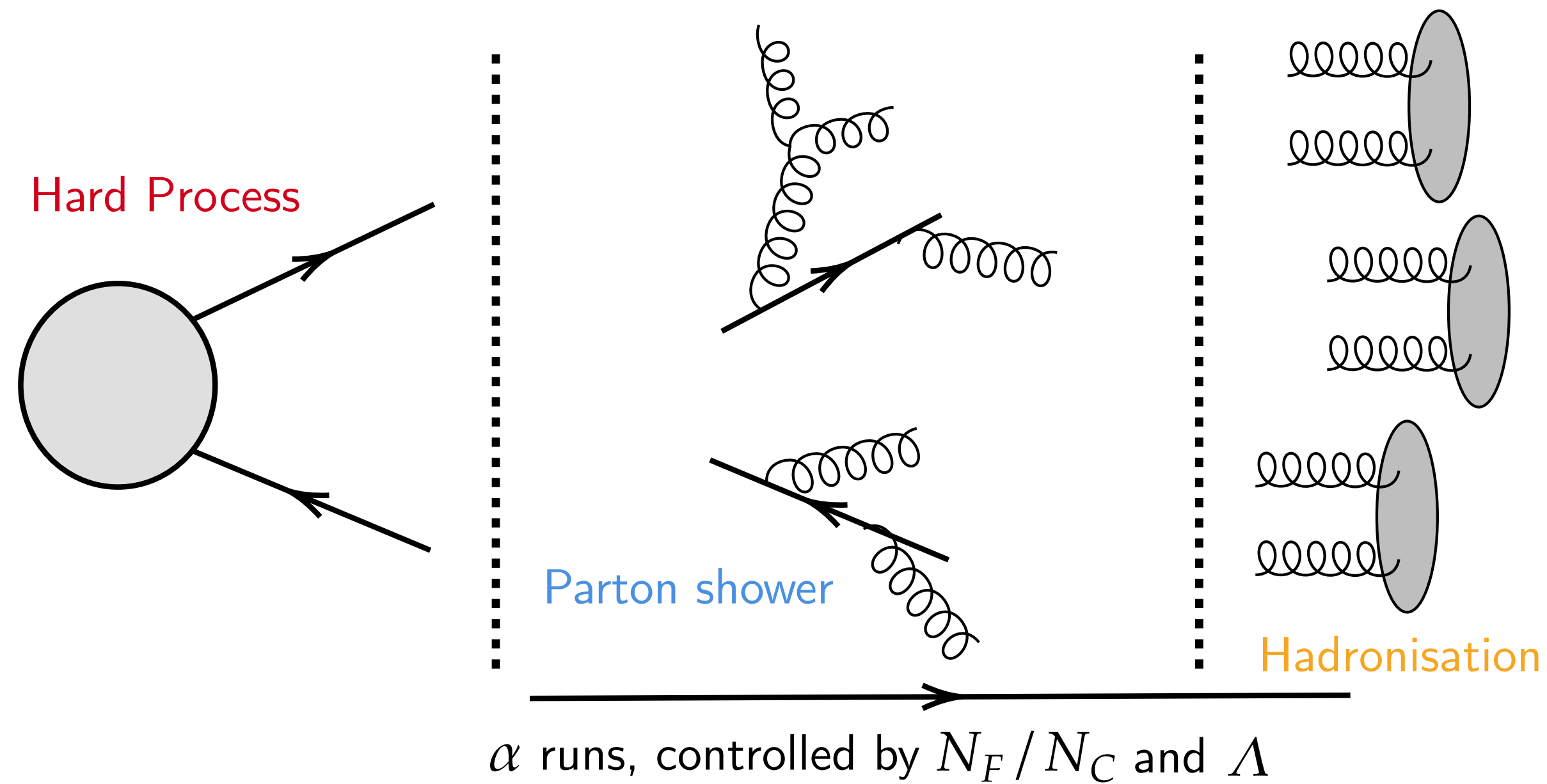
arXiv:2305.03665, T. Appelquist et al.

arXiv:2312.08332, A. Pomarol et al.

arXiv:2312.13761, R. Zwicky

arXiv:2404.07601, T. Appelquist et al.

# Dark parton showering



$$\mu^2 \frac{d\alpha}{d\mu^2} = \beta(\alpha) = -\alpha^2 (\beta_0 + \beta_1 \alpha) \quad (\text{at 2-loop})$$

$$N_C \alpha = f(N_F/N_C, \mu/\Lambda) + \mathcal{O}(N_F/N_C^3) \text{ corrections}$$

Non-trivial fixed point:  $\alpha_* = -\frac{\beta_0}{\beta_1} ; > 0 \text{ for } N_F/N_C \gtrsim 2.7$

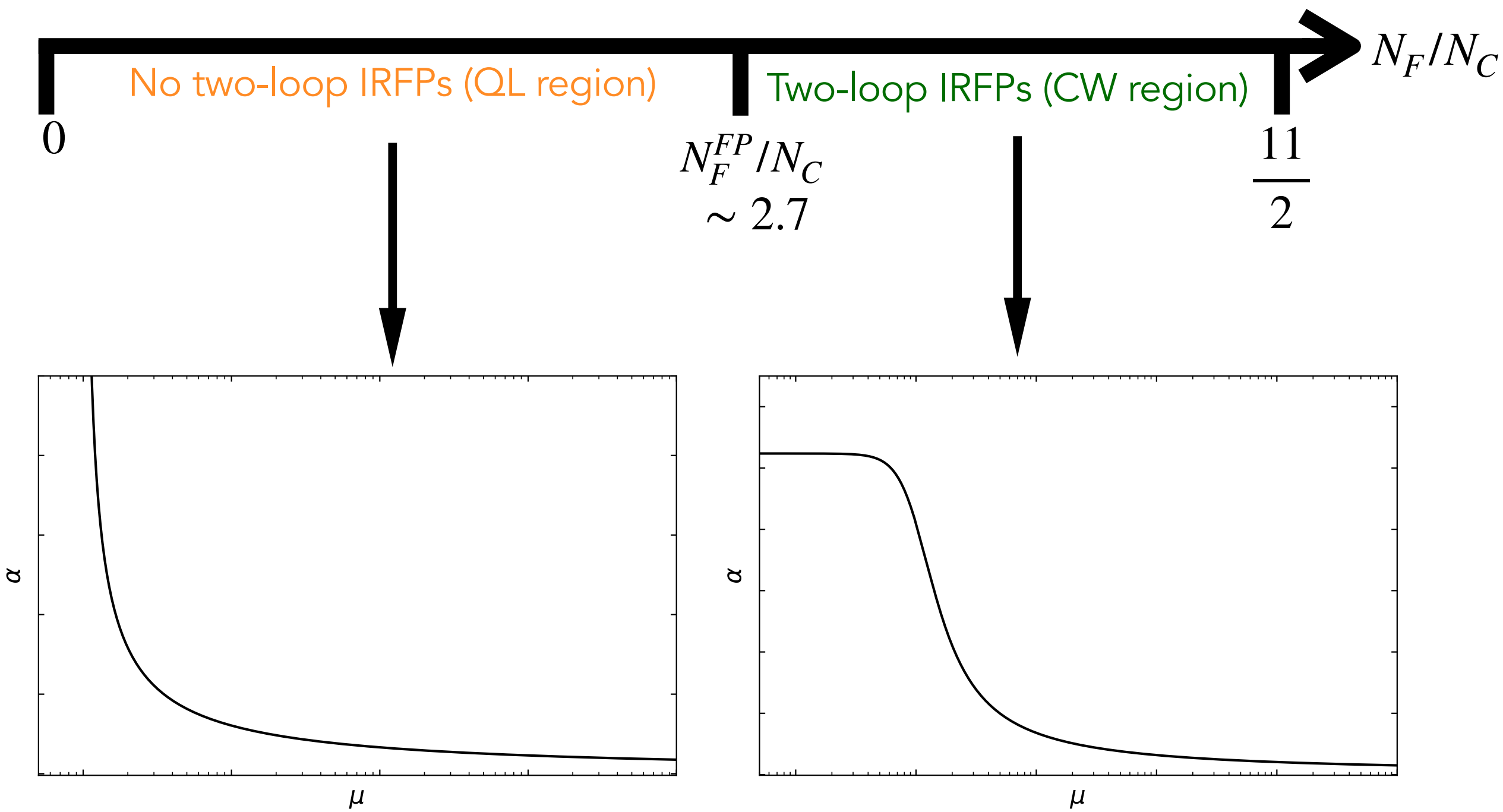
- First, we'll focus on dark parton showering; hadronisation details not yet fully understood. Dark parton showering is governed by the t' Hooft gauge coupling,  $N_C \alpha$  with  $\alpha$  in turn being governed by the Renormalisation Group Equations (RGE). G. 't Hooft Nucl. Phys. B ('74)
- Parton shower ends near scale  $\Lambda$ , this scale characterises the breakdown of the perturbative expansion of  $\alpha$  and is a good proxy for the scale of the theory. Up to corrections, the t' Hooft gauge coupling is governed solely by  $N_F/N_C$  and  $\mu/\Lambda$ .
- At two-loop, for  $N_F/N_C \gtrsim 2.7$ ,  $\alpha$  flows to a non-trivial infra-red fixed point (IRFP); as  $N_F/N_C$  increases  $\alpha$  begins to slow down. New procedures are needed to understand parton showering within this region. T. Banks., A. Zaks, Nucl.Phys.B 196 ('82)

# Near-conformal dark sector models

arXiv:2008.12223, J.W. Lee

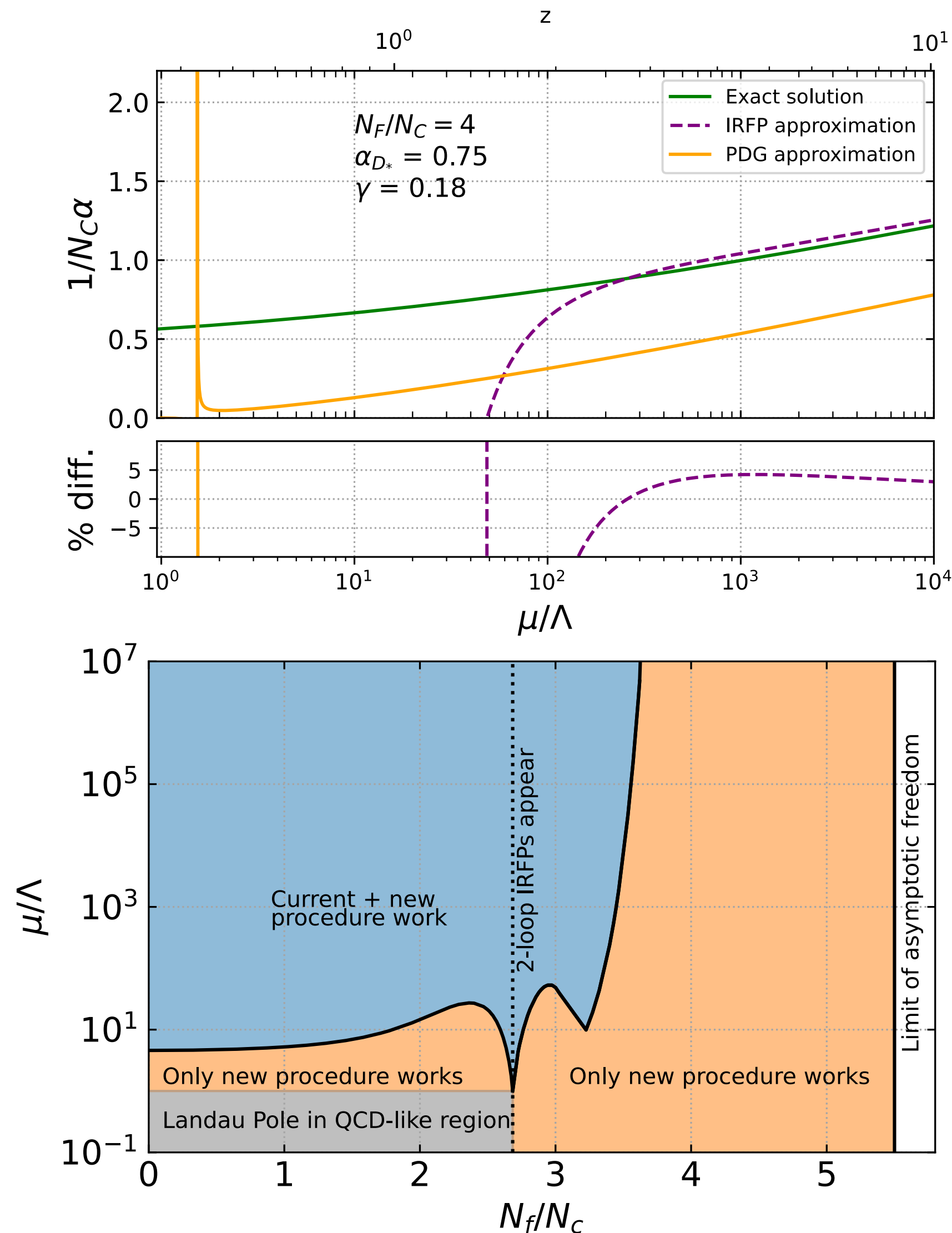
Two-loop perturbative description

Non-perturbative description



- Within the conformal window, chiral symmetry is restored and the infra-red theory is conformal. Lattice calculations suggest  $N_F^c/N_C = 3 - 4$ . arXiv:2004.00754, A. Hasenfratz et al.
- Since  $\alpha$  flows from a weakly coupled value in the UV, we automatically lose scale invariance. The dark quark mass ( $m_q$ ) additionally deforms the IR conformal symmetry. These ensure any signatures are not purely missing energy.

# Modelling of dark parton showers



- The current approximation used within event generators (the PDG formula) is insufficient to describe two-loop  $\alpha$  for high  $N_F/N_C$  since it neglects effects of the IRFP.
- By taking this IRFP into account, we establish a framework of two solutions to the RGE that allow for parton showering to be simulated across a wide range of parameter space.

$$\alpha = \alpha_* \left[ W_{-1} \left( -\frac{1}{e} \left( \frac{\mu^2}{\Lambda^2} \right)^{\beta_0 \alpha_*} \right) + 1 \right]^{-1} \quad ; \quad \alpha = \alpha_* \left[ W_0 \left( \frac{1}{e} \left( \frac{\mu^2}{\Lambda^2} \right)^{\beta_0 \alpha_*} \right) + 1 \right]^{-1}$$

QL region (no IRFPs)

CW region (IRFPs)

- This procedure defines  $\Lambda$  within the IRFP region as the scale at which power-law running takes over from logarithmic running.

arXiv:9602385, T. Appelquist et al.    arXiv:1406.2337, D. Litim et al.

arXiv:9810192 - E. Gardi et al.

# The Sudakov veto algorithm at two-loop

- To generate some scale  $Q_i^2$  given some initial scale  $Q_{i-1}^2$ , Pythia generates a random number  $R_1$  and solves for  $\Delta(Q_i^2, Q_{i-1}^2) = R_1$ .  $\Delta$  is the Sudakov form factor, the probability of no parton emissions between  $Q_{i-1}^2$  and  $Q_i^2$ .

arXiv:0603175 - T. Sjöstrand et al.

arXiv:1102.2126 - W. Giele et al.

arXiv:1101.2599 - A. Buckley et al.

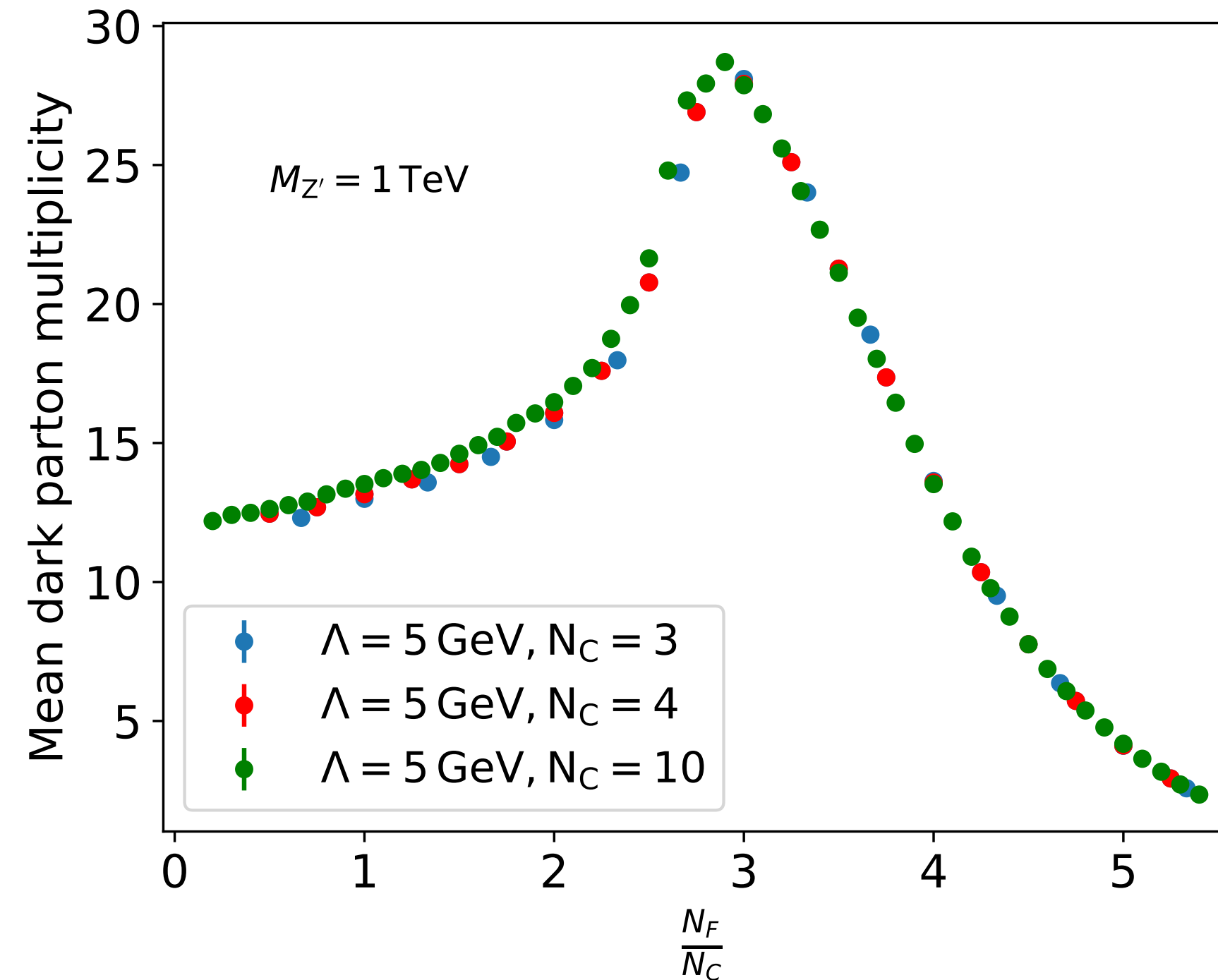
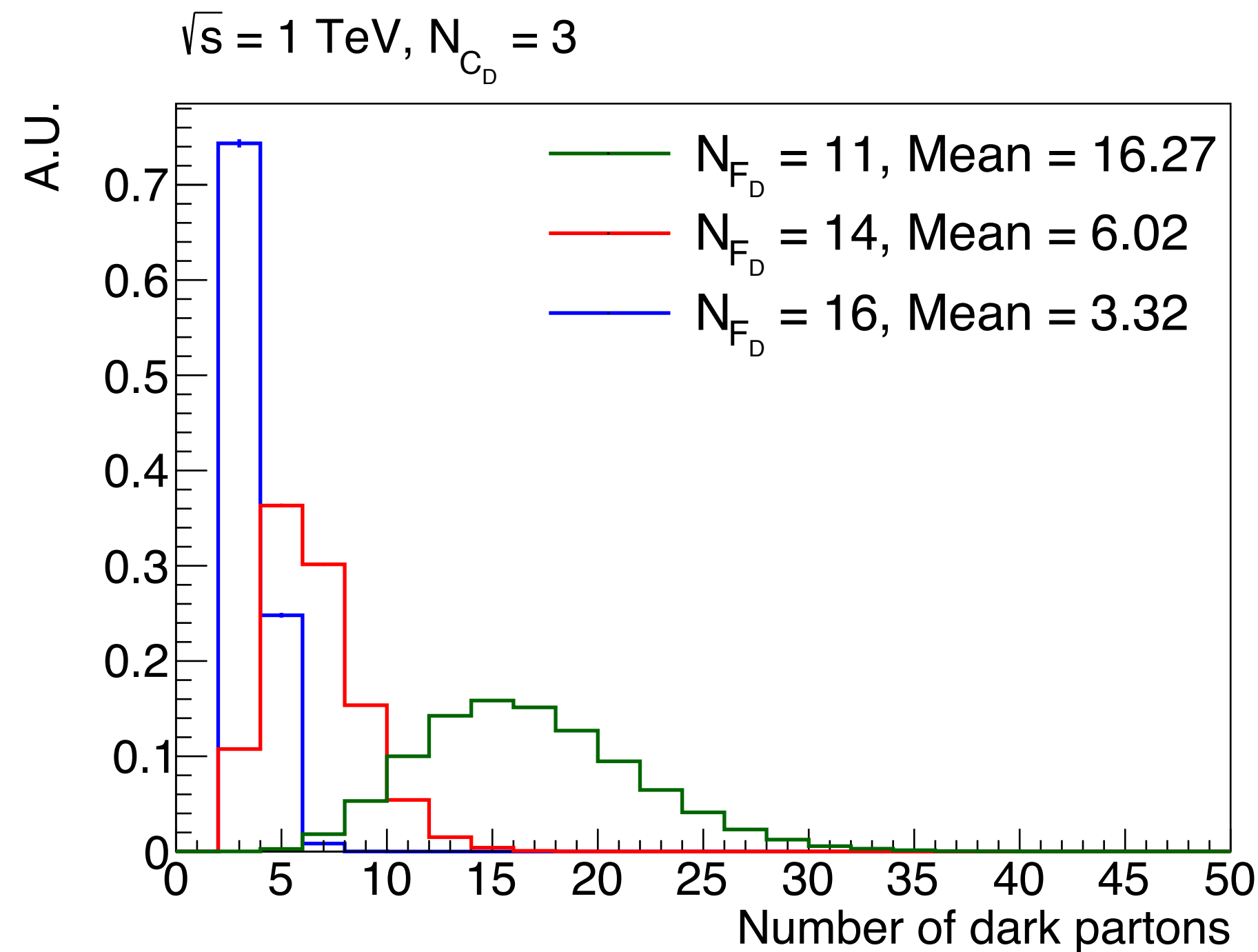
arXiv:1211.7204 - L. Lonnblad et al.

- This inversion is complicated, so  $\Delta$  is usually overestimated with a much simpler  $\tilde{\Delta}$ . The overestimate is then corrected for through the Sudakov veto algorithm. At two-loop, the inverse can be performed exactly as,

$$Q_i^2 = \Lambda^2 \left( \frac{Q_{i-1}^2}{\Lambda^2} \right)^{\tilde{\Delta}^{2\pi\beta_0/\epsilon}} \left[ \tilde{\Delta}^{2\pi\beta_0/\epsilon} \left( \mp e W_n \left( \mp \frac{1}{e} \left( \frac{Q_{i-1}^2}{\Lambda^2} \right)^{\beta_0\alpha_*} \right) \right)^{1 - \tilde{\Delta}^{2\pi\beta_0/\epsilon}} \right]^{1/\beta_0\alpha_*}; \quad \epsilon = \int_{\tilde{\xi}_{min}}^{\tilde{\xi}_{max}} \tilde{P}_{a \rightarrow bc}(\xi') d\xi'; \quad \mp, n = \begin{cases} -, -1 & \text{(QL region)} \\ +, 0 & \text{(CW region)} \end{cases}$$

- Previous two-loop efforts relied on a separate veto algorithm that corrected one-loop showering with two-loop effects - a method which did not converge for the entire  $N_F/N_C - \mu/\Lambda$  space. The new implementation now even provides a way to simulate below  $\mu/\Lambda = 1$  in the CW region.
- The Lambert W function is put within Pythia through a combination of approximation and interpolation.

# Simulation of dark parton showers

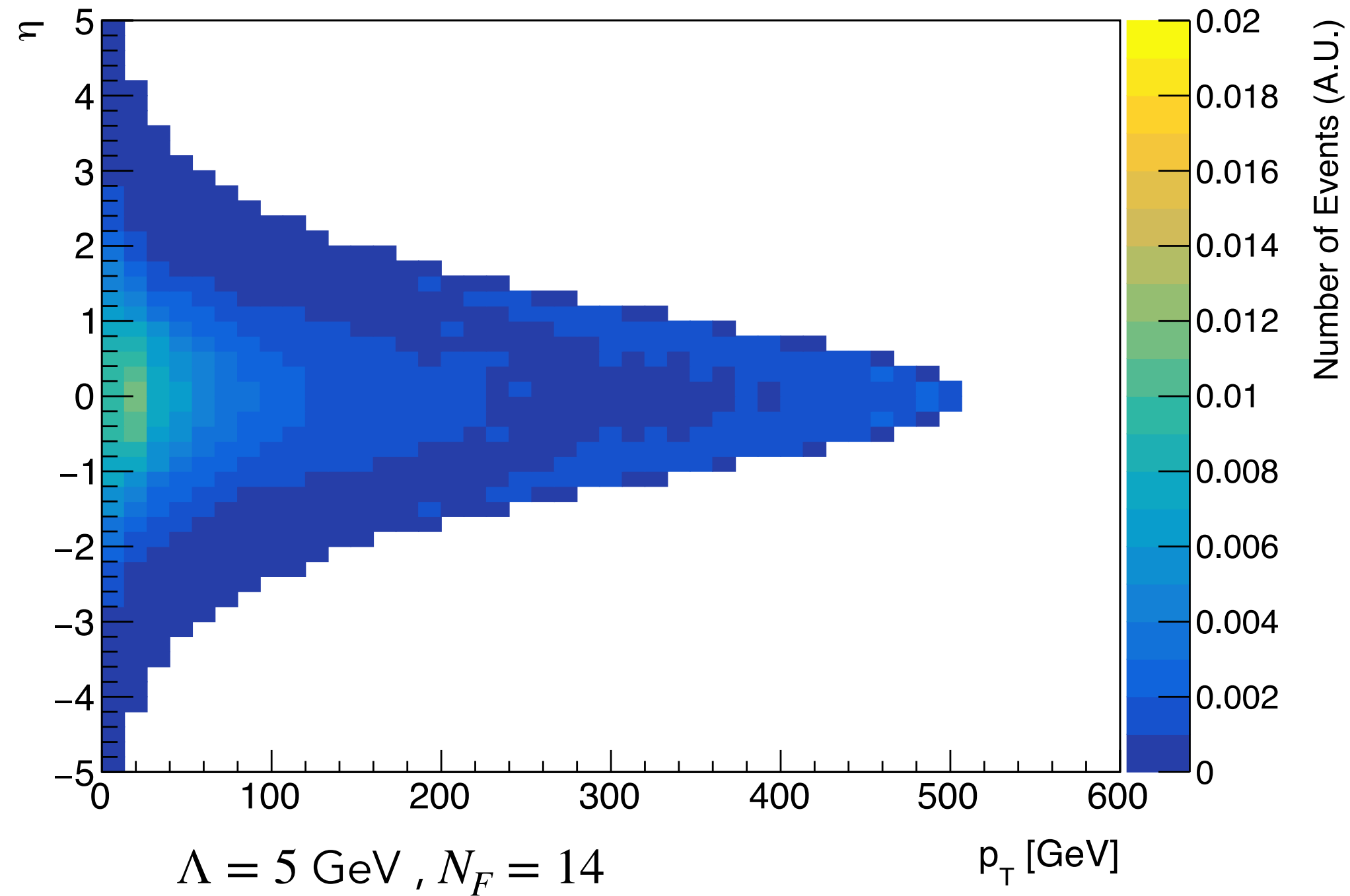


Simulated with a custom Pythia 8.307 with benchmark:  
 $e^+e^- \rightarrow Z' \rightarrow q_D \bar{q}_D$ ,  $\sqrt{s} = M_{Z'} = 1$   
 TeV, hadronisation off,  $\Lambda = 5$   
 GeV,  $N_C = 3$ .

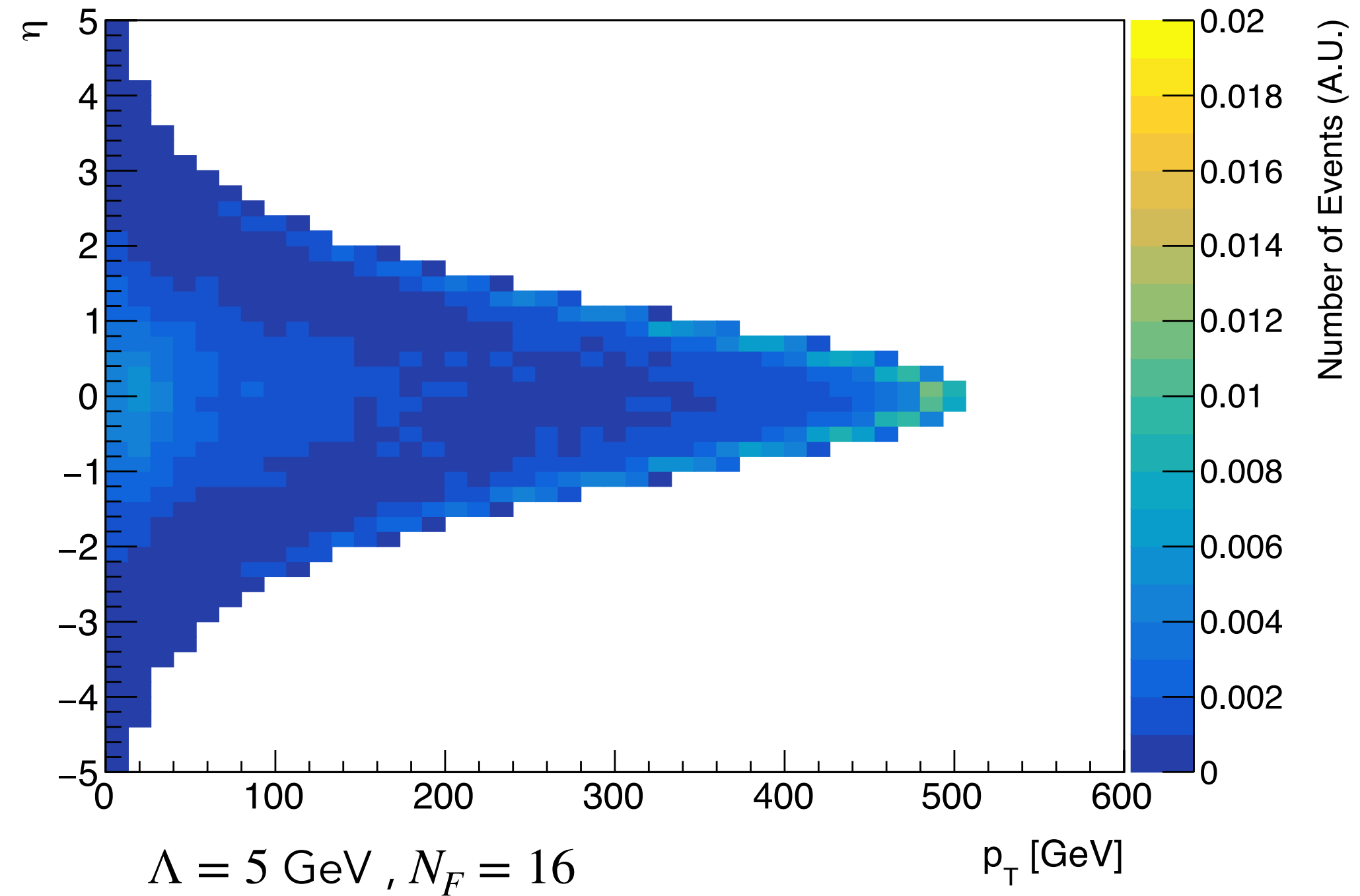
- Theories with large IRFPs ( $\alpha_* \gg 1$ ) (around  $N_F/N_C \sim 3$ ) have similar parton showering behaviour to those without IRFPs, having a overall large multiplicity of soft partons. Theories with small IRFPs ( $\alpha_* \ll 1$ ) (around  $N_F/N_C \sim 5$ ) have both hard and soft partons; having an overall small multiplicity of hard partons.
- Since parton splitting probability is proportional to  $\alpha$ , it thus vanishes as  $N_F/N_C \rightarrow 5.5$ . Hence there is very little splitting at  $N_F/N_C \sim 5$  and average parton multiplicity is almost 2 - the 2 initial dark quarks.

# Simulation of dark parton showers

Showered dark parton  $p_T$  and  $\eta$  distribution



Showered dark parton  $p_T$  and  $\eta$  distribution



Simulated with a custom Pythia 8.307 with benchmark:  
 $e^+e^- \rightarrow Z' \rightarrow q_D \bar{q}_D$ ,  
 $\sqrt{s} = M_{Z'} = 1 \text{ TeV}$ ,  
hadronisation off,  
 $\Lambda = 5 \text{ GeV}$ ,  $N_C = 3$ .

- At around  $N_F/N_C \sim 5$ , there is a transition in the  $p_T$  —  $\eta$  plane from the majority of partons being soft to a majority being hard, reflecting how branching probability is negligible and the majority of partons are initial dark quarks.
- This new procedure allows for the simulation of the anomalous jets signatures of near-conformal Hidden Valley theories. Motivates further investigations into the hadronisation and subsequent decay of near-conformal bound states, as this could have an additionally large influence on the dark shower phenomenology.





Thank you!  
Questions?