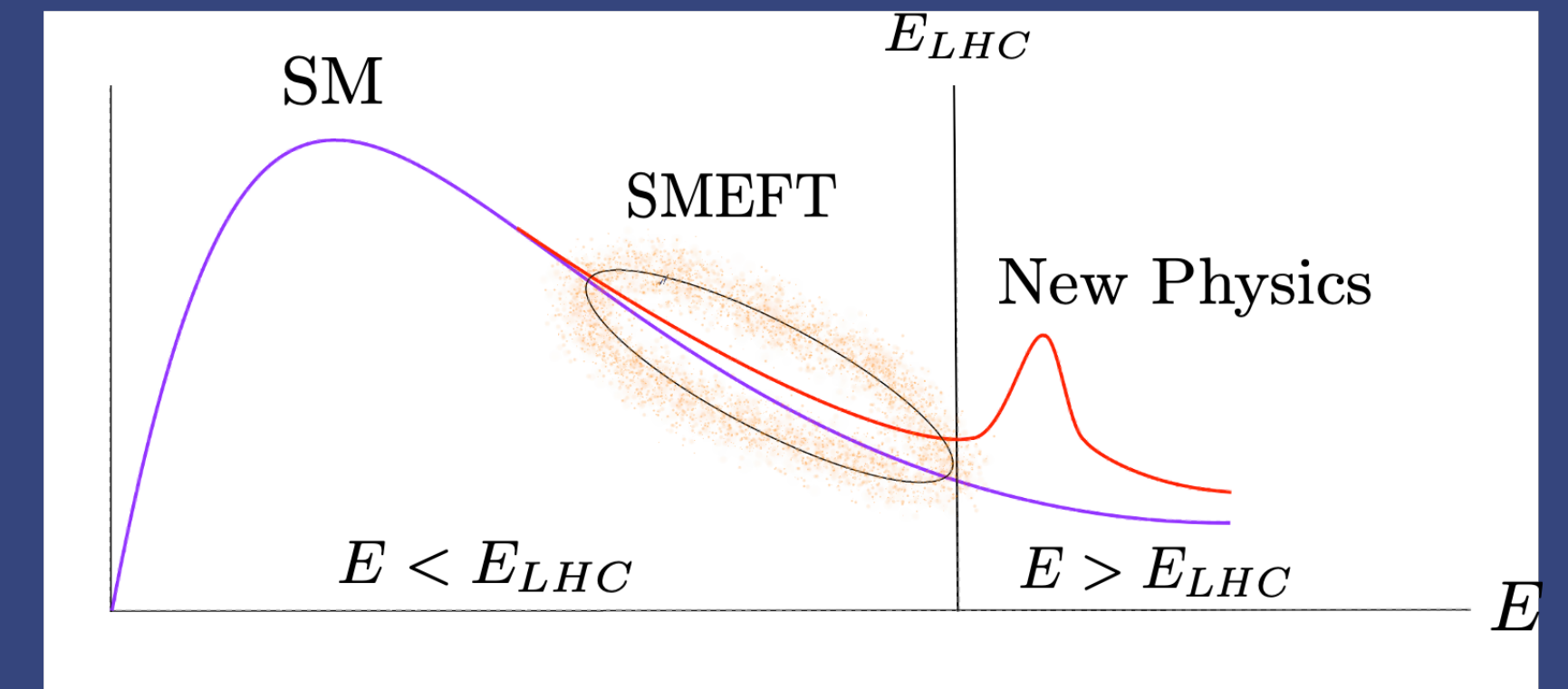


# Advancing SMEFT Global Analyses

## RGE effects and flavour physics

In collaboration with Anke Biekötter and Tobias Hurth (arxiv:2311.04963)

DISCRETE 2024, Ljubljana, 4 December 2024



# Outline

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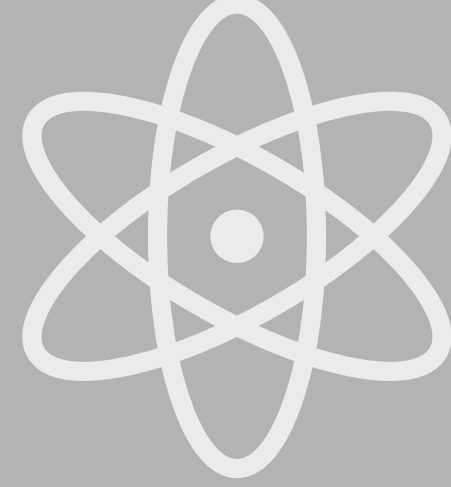
1. Global analyses in the flavour symmetric SMEFT

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1. Global analyses in the flavour symmetric SMEFT
2. Global analysis with LO predictions (and Dijets+ $\gamma$ )

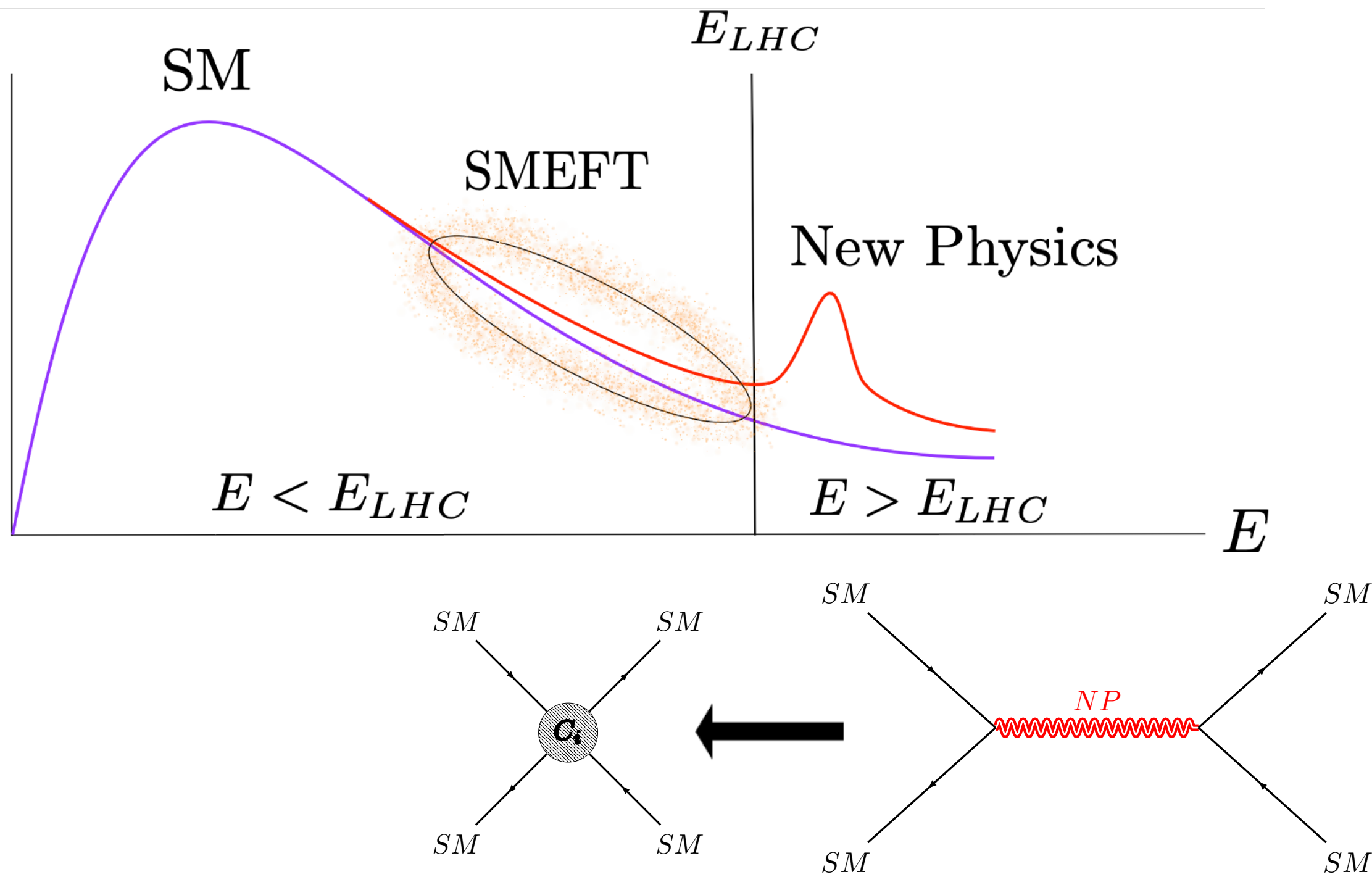
# Outline

1. Global analyses in the flavour symmetric SMEFT
2. Global analysis with LO predictions (and Dijets+ $\gamma$ )
3. RGE effects on the global analysis



# Global analyses in the flavour symmetric SMEFT

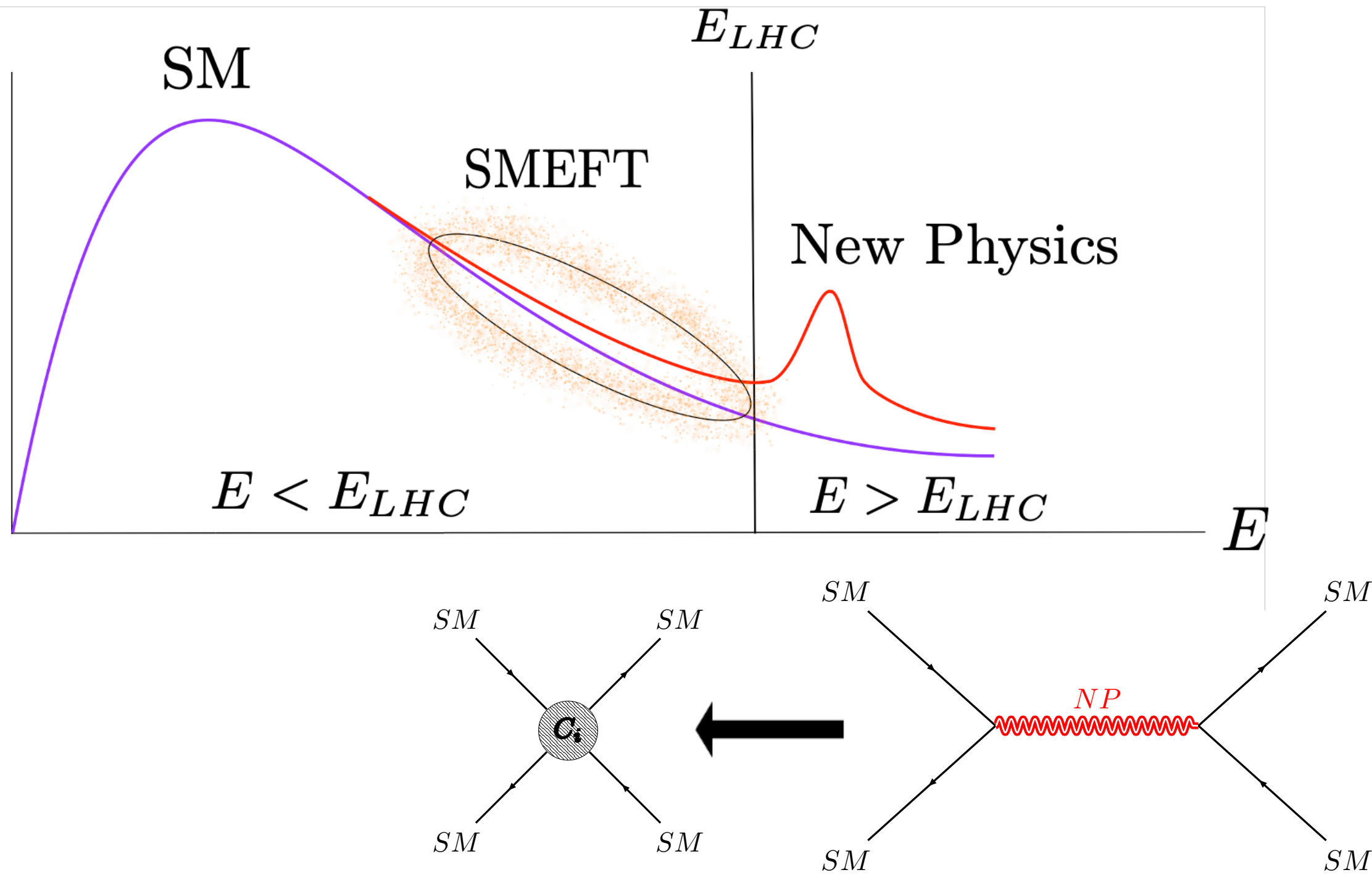
# SMEFT and flavour symmetry



**SMEFT: EFT for heavy NP model-agnostic study**

$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM} + \sum_i \frac{C_i^{(6)}}{\Lambda^2} O_i^{(6)} + \dots \quad \begin{array}{l} \text{2499 operators} \\ \text{[1008.4884, Grzadkowski et al.]} \end{array}$$

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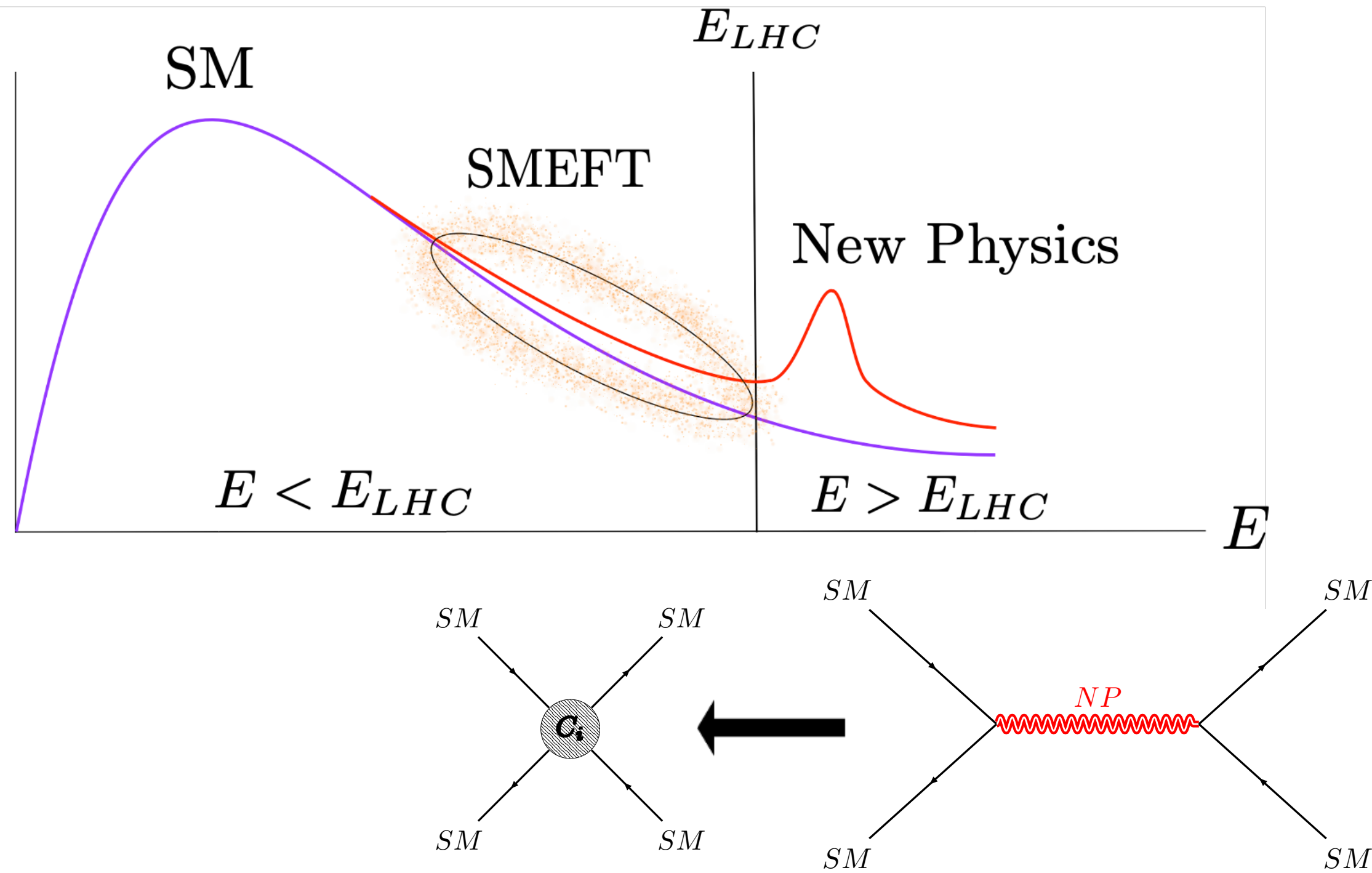
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**SMEFT observables are given by:**

$$\sigma \propto |\mathcal{A}|^2 = \underbrace{|\mathcal{A}_{SM}|^2}_{\text{SM background}} + \underbrace{\frac{2C_6}{\Lambda^2} \text{Re}(\mathcal{A}_{d6} \mathcal{A}_{SM}^*)}_{\text{signal}} + \underbrace{\frac{C_6^2}{\Lambda^4} |\mathcal{A}_{d6}|^2 + \frac{2C_8}{\Lambda^4} \text{Re}(\mathcal{A}_{d8} \mathcal{A}_{SM}^*)}_{\text{theoretical uncertainty}} + \dots$$



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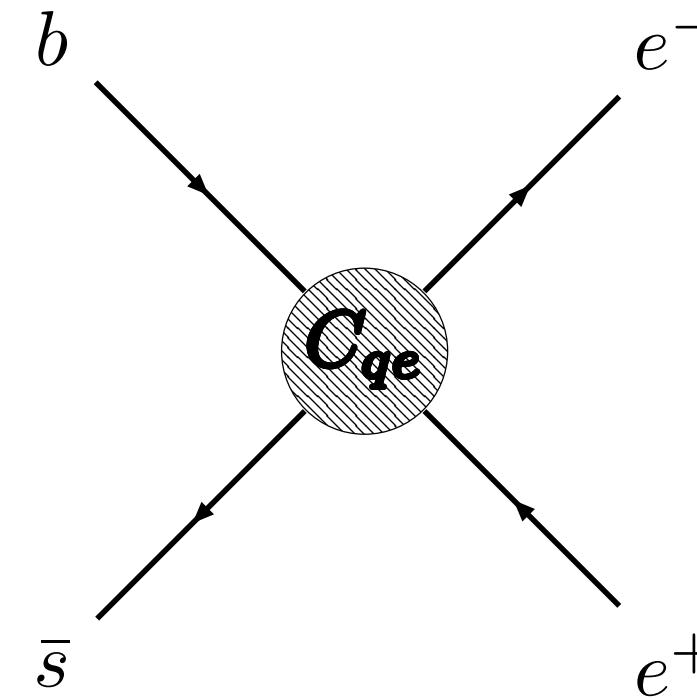
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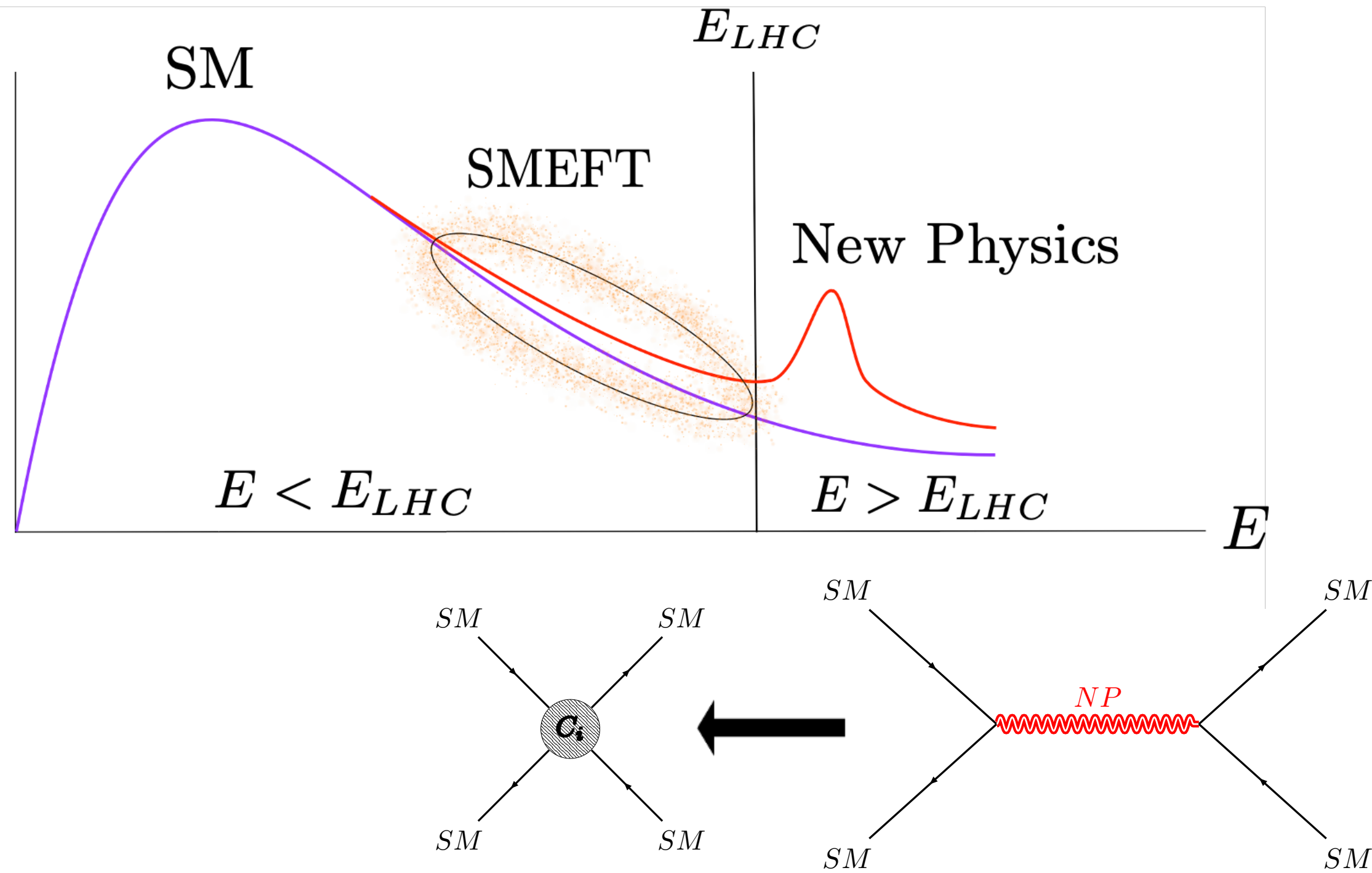
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**Symmetry assumption on NP:**

$$U(3)^5 = U(3)_\ell \times U(3)_q \times U(3)_e \times U(3)_u \times U(3)_d$$



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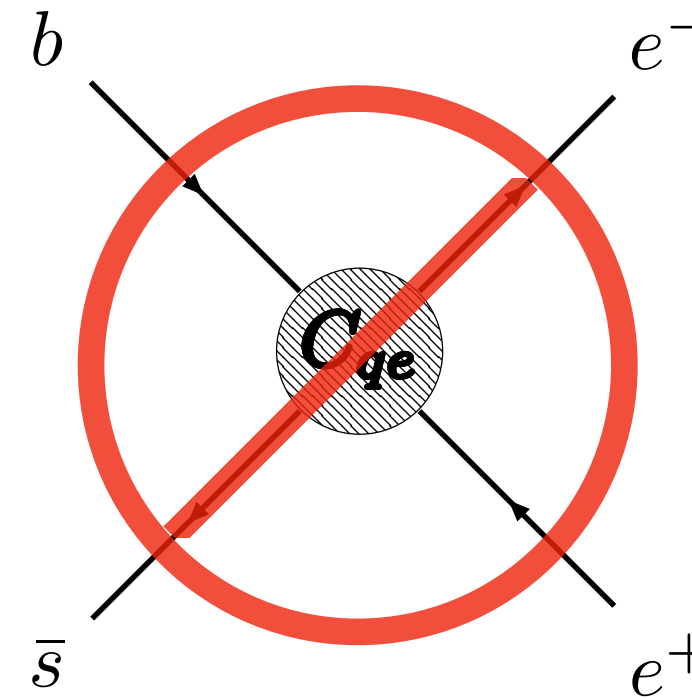
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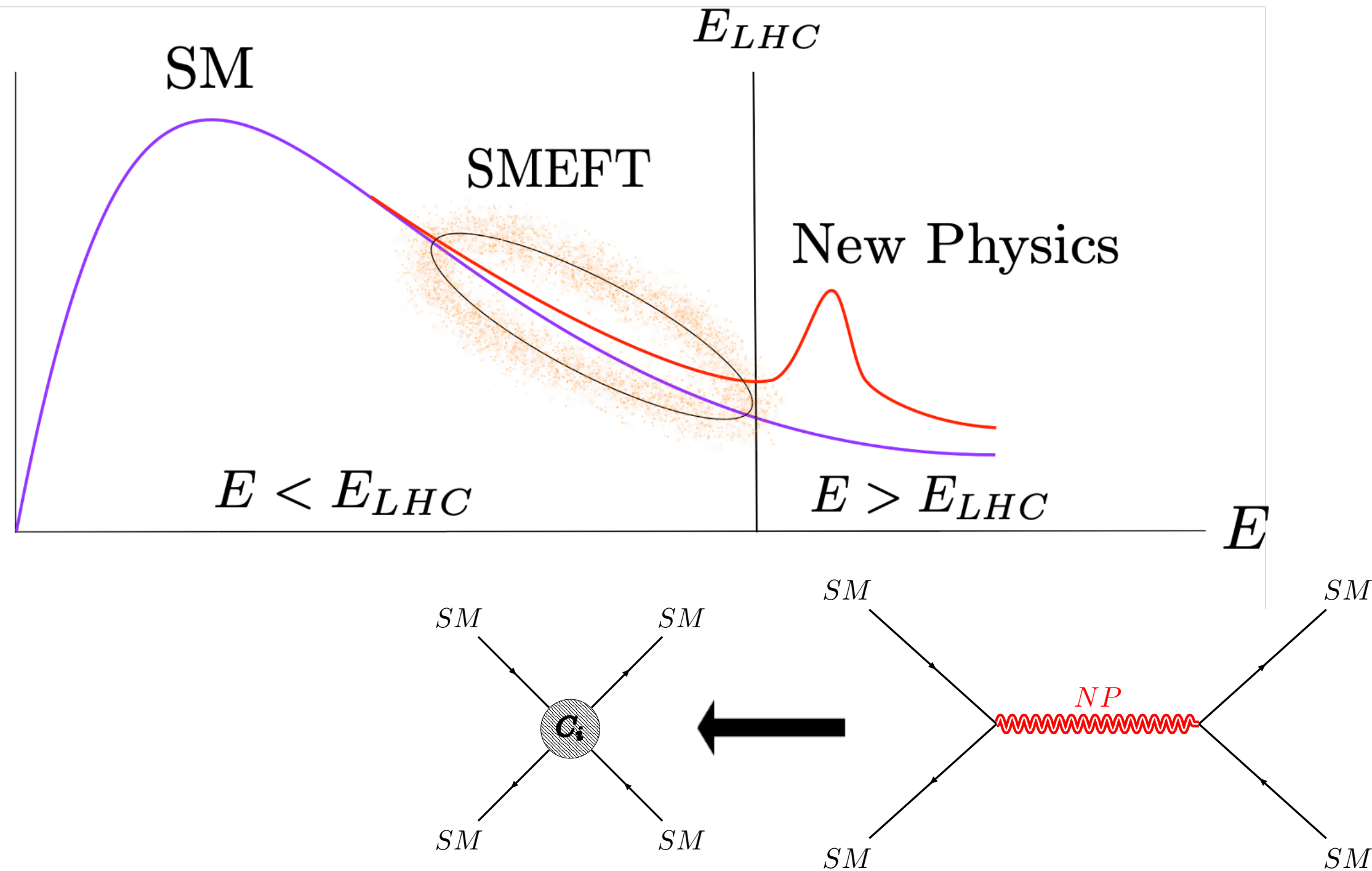
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From 2499 dimension six operators to 41 (CP even)

[2005.05366: Faroughy, Isidori, Wilsch, Yamamoto]

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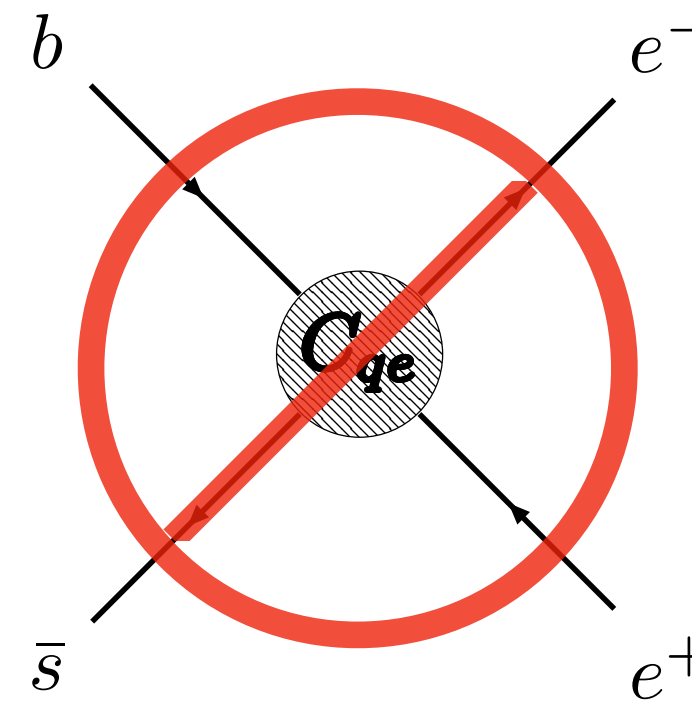
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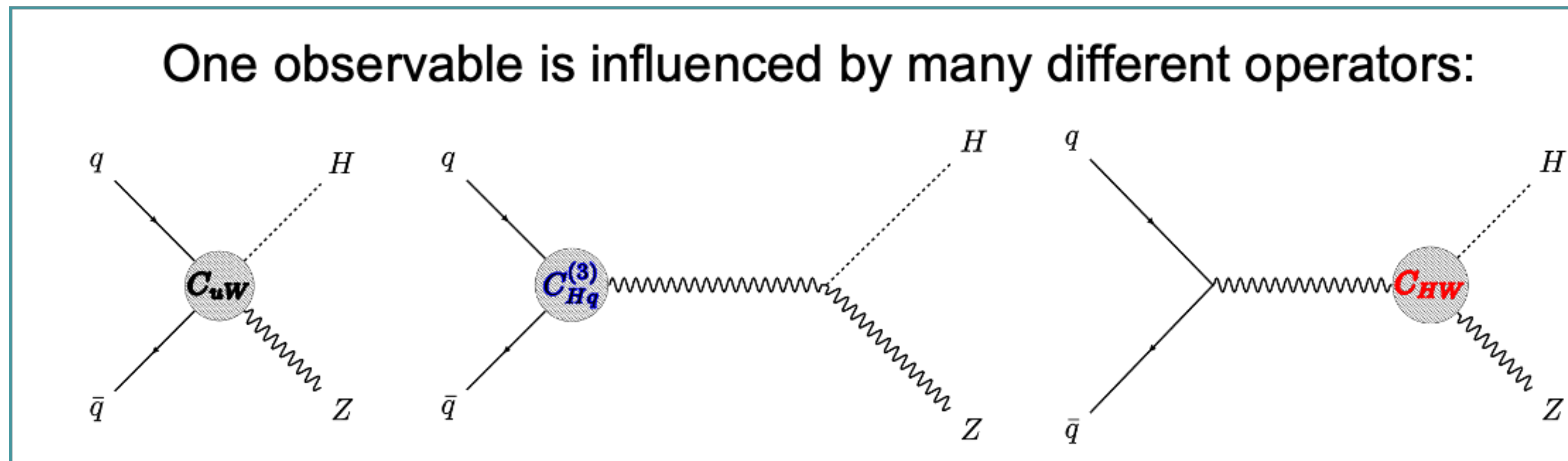
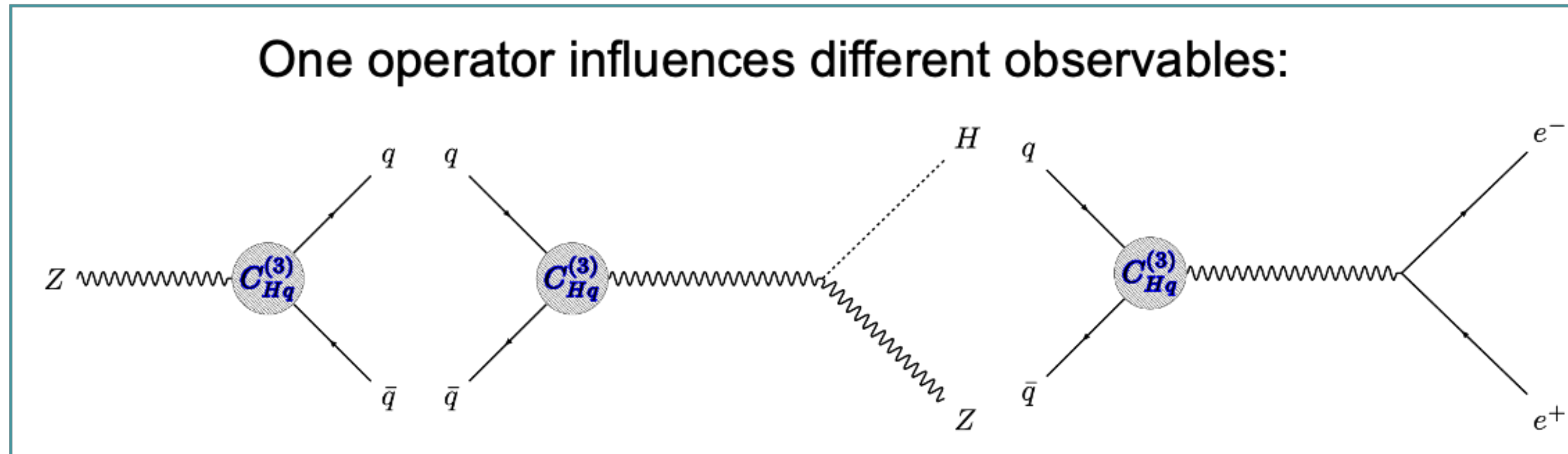
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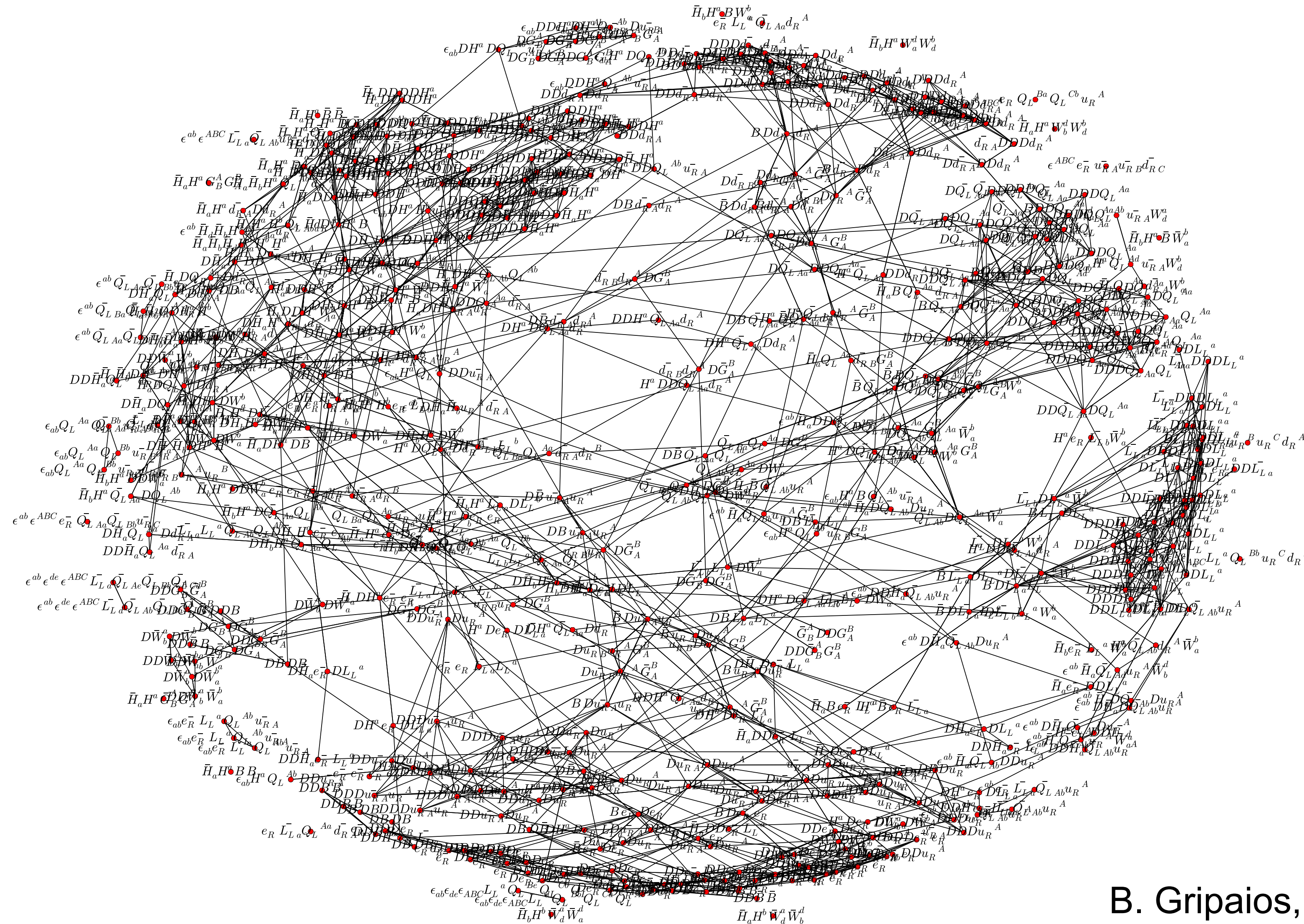
This assumption corresponds to minimal version of MFV: it contains the minimum and non-removable amount of flavour violation.

# Global analyses in the SMEFT

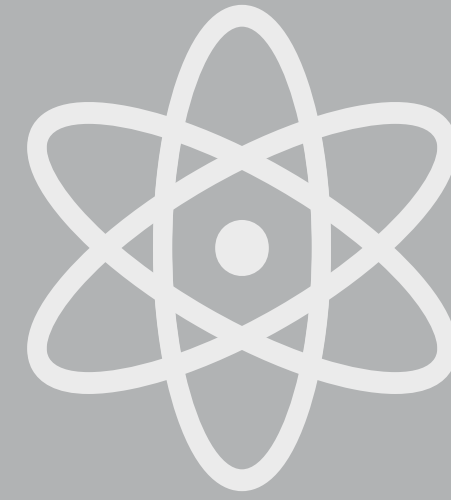
Wilson coefficients in SMEFT are **highly correlated** and only **global analysis** can give meaningful results.



# Global analyses in the SMEFT



B. Gripaios, HEFT 2018



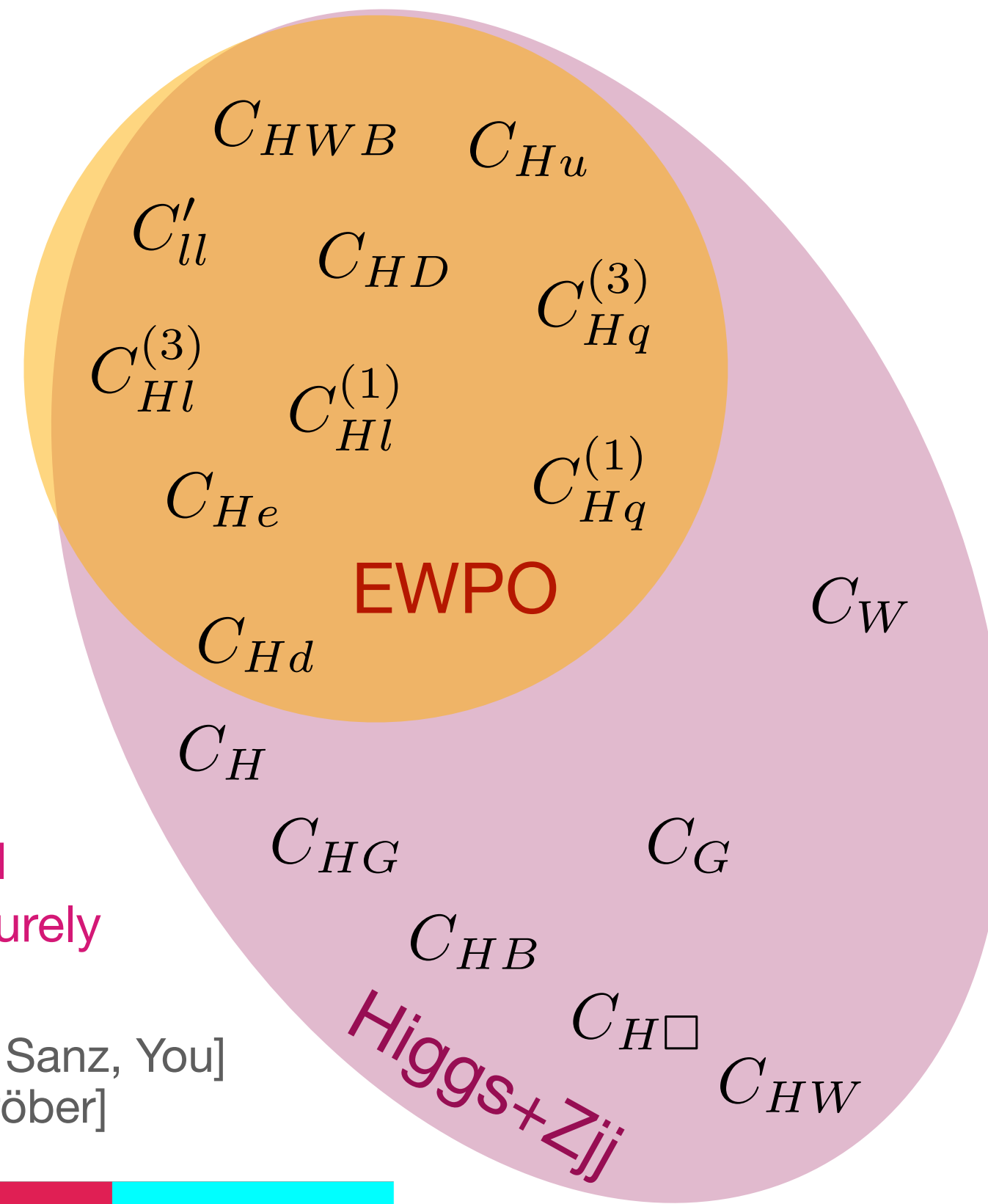
# Global analysis with LO predictions

# Datasets

## EWPO:

Dominantly constrain these 10 operators, but leaves two flat directions.

[1909.02000: Dawson, Giardino]



## Higgs:

Breaks EW flat directions and constrains some additional purely boson operators.

[2012.02779: Ellis, Madigan, Mimasu, Sanz, You]

[2202.02333: Alasfar, de Blas, Gröber]

**Constrained operators: 17**

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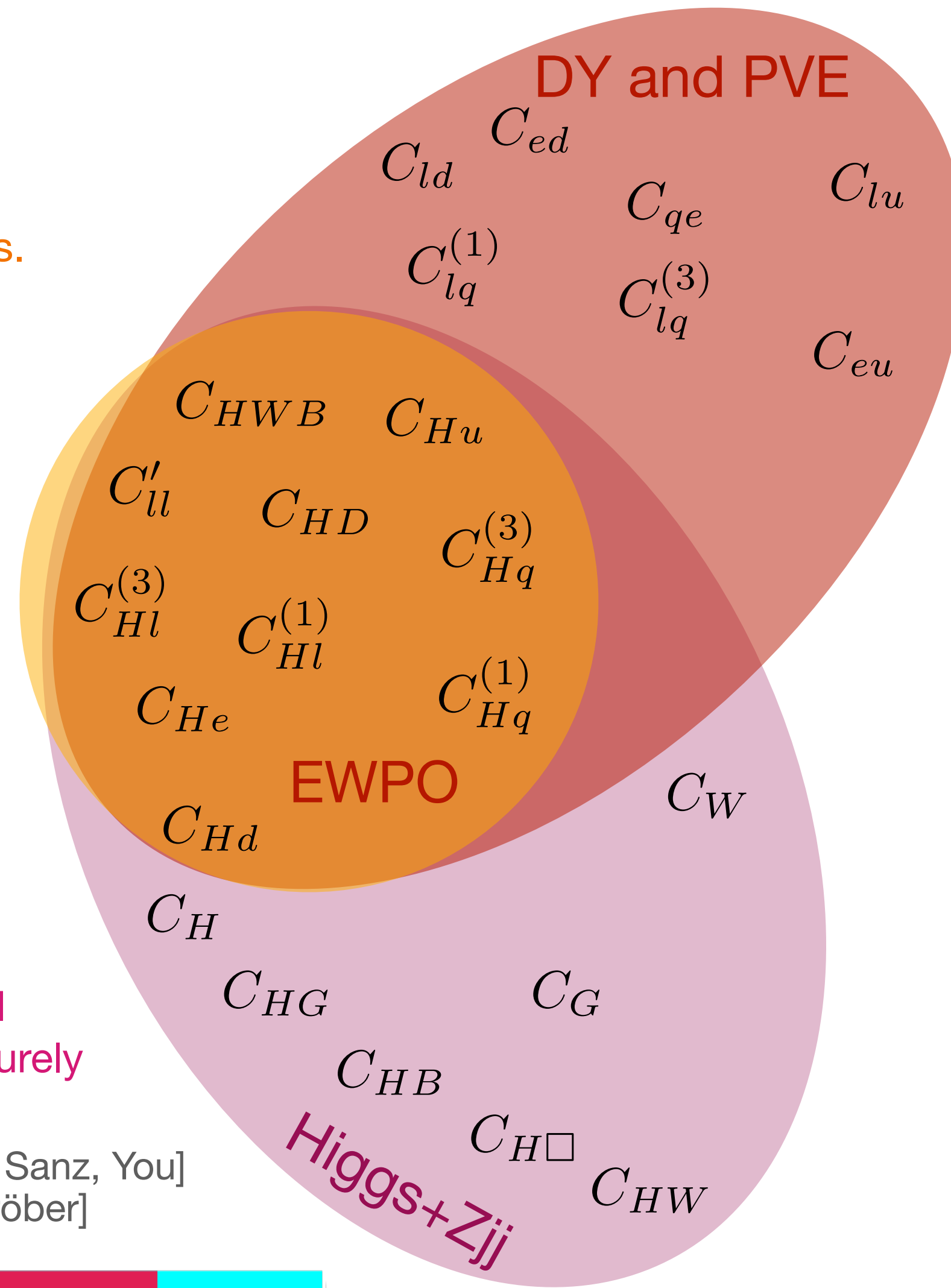
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Their interplay is needed in order to constrain semi-leptonic operators.

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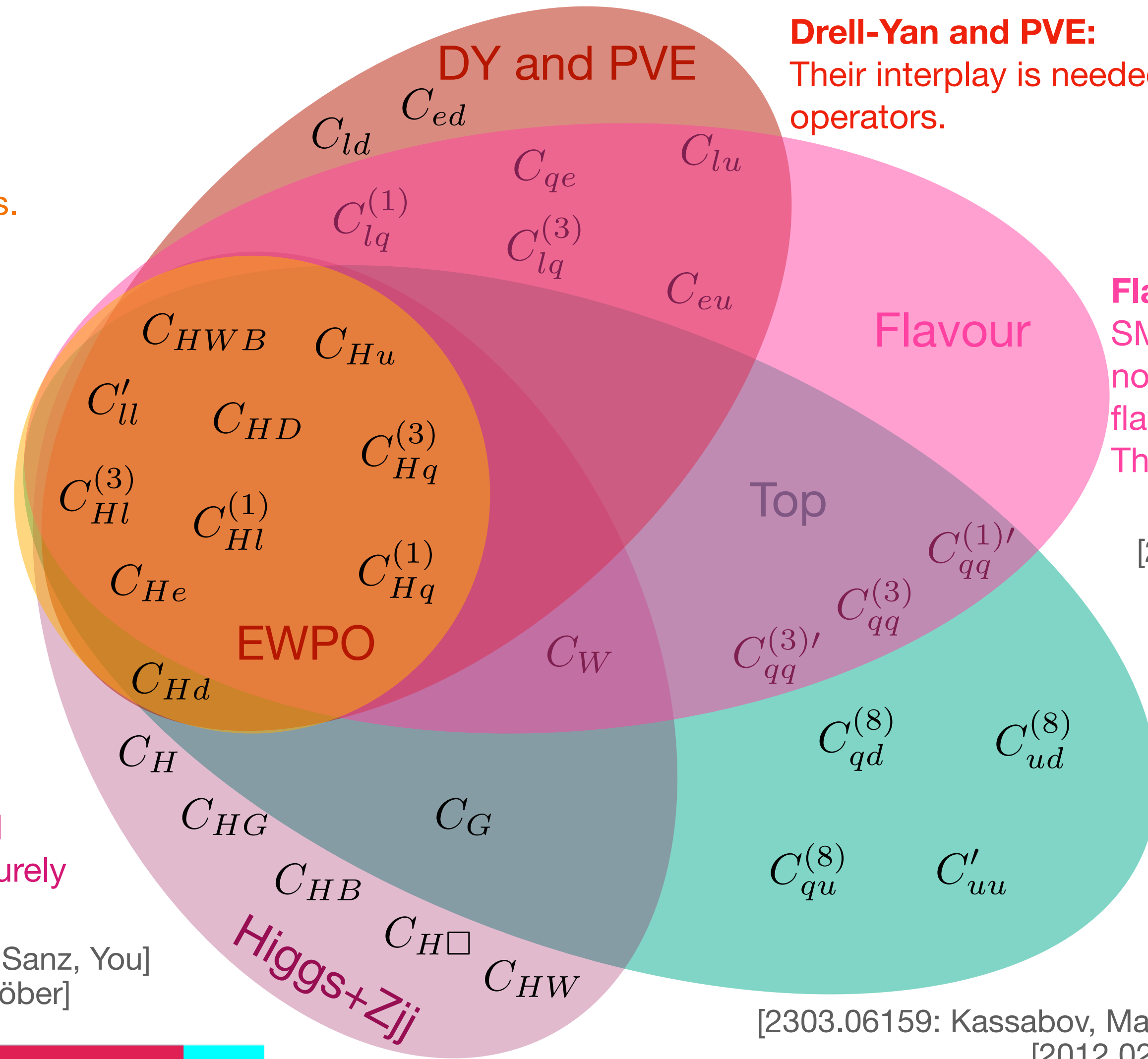
[2202.02333: Alasfar, de Blas, Gröber]

**Constrained operators: 24**



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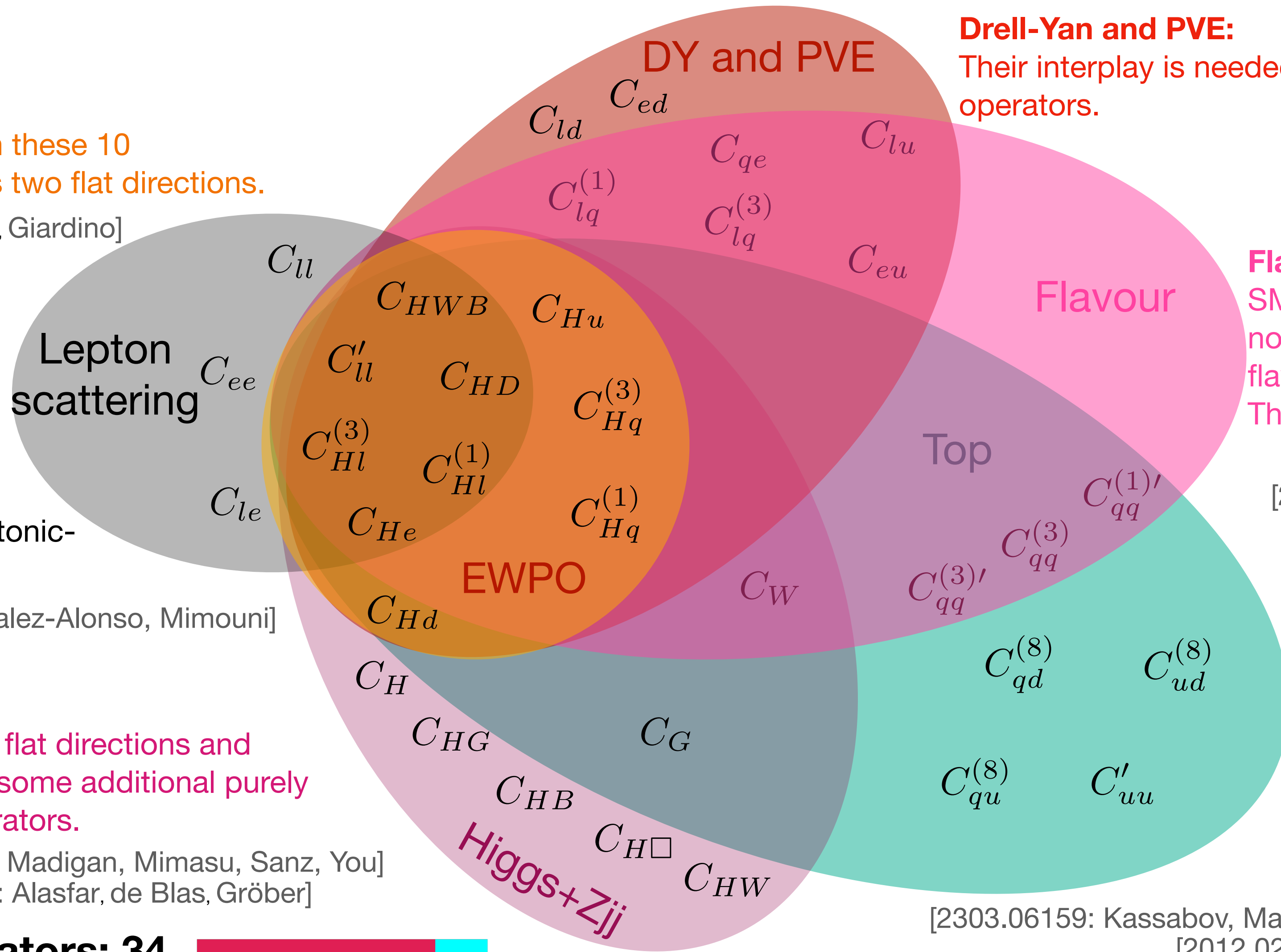
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**Constrained operators: 31**

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**Flavour:**  
 SMEFT operators are flavour symmetric, nonetheless Yukawa couplings give rise to flavour violating observables via loop. These bounds lift correlations present in Top.  
 [1810.08132: Straub]  
 [2003.05432: Aoude, Hurth, Renner, Shepherd]

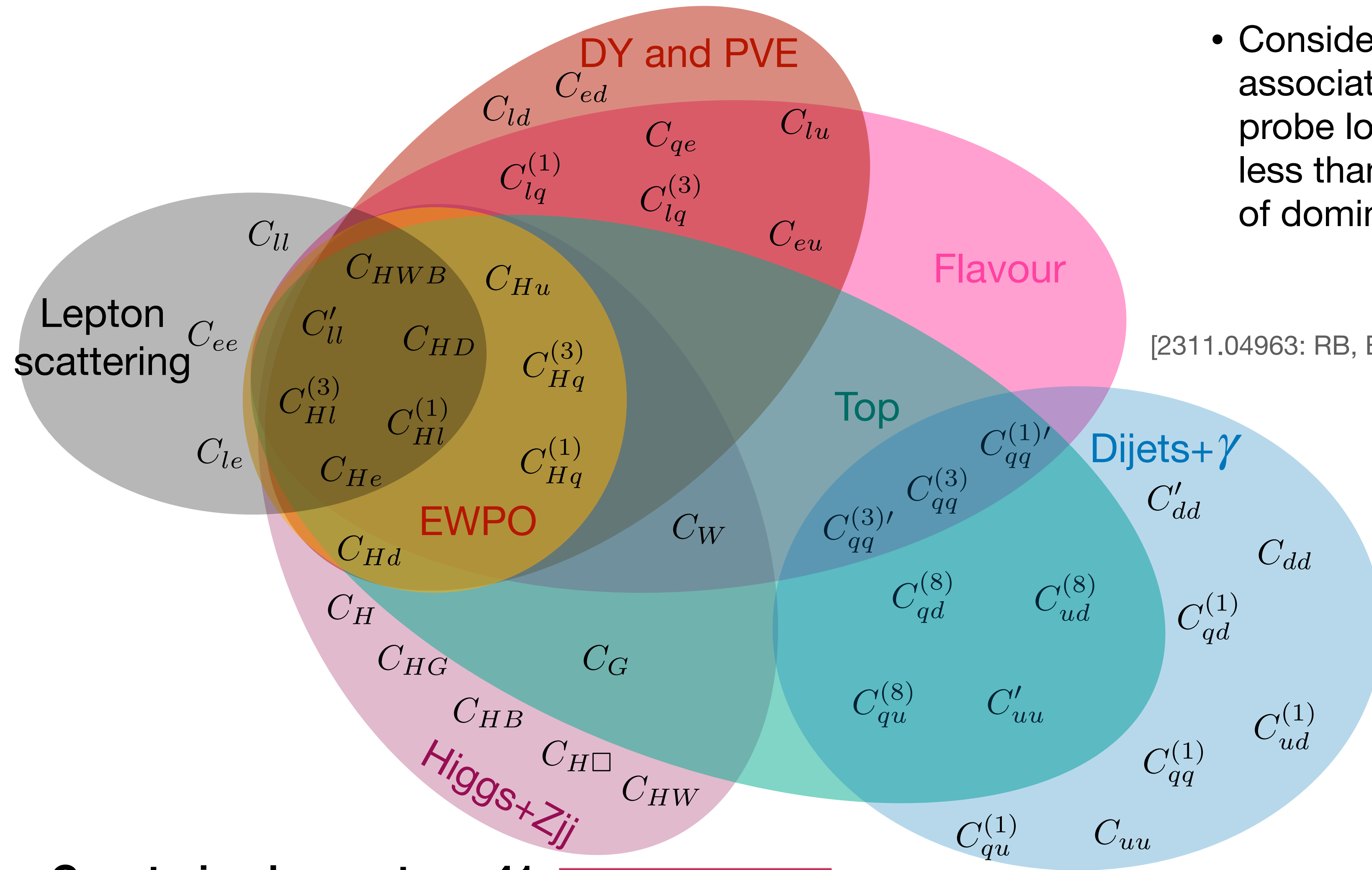
**Top:**  
 Put constraints on 4-quark operators involving up-type quark. Some operators suffer from correlations.  
 [2303.06159: Kassabov, Madigan, Mantani, Moore, Alvarado, Rojo, Ubiali]  
 [2012.02779: Ellis, Madigan, Mimasu, Sanz, You]

**Lepton scattering:**  
 Constrain mainly purely leptonic operators  
 [1706.03783: Falkowski, Gonzalez-Alonso, Mimouni]

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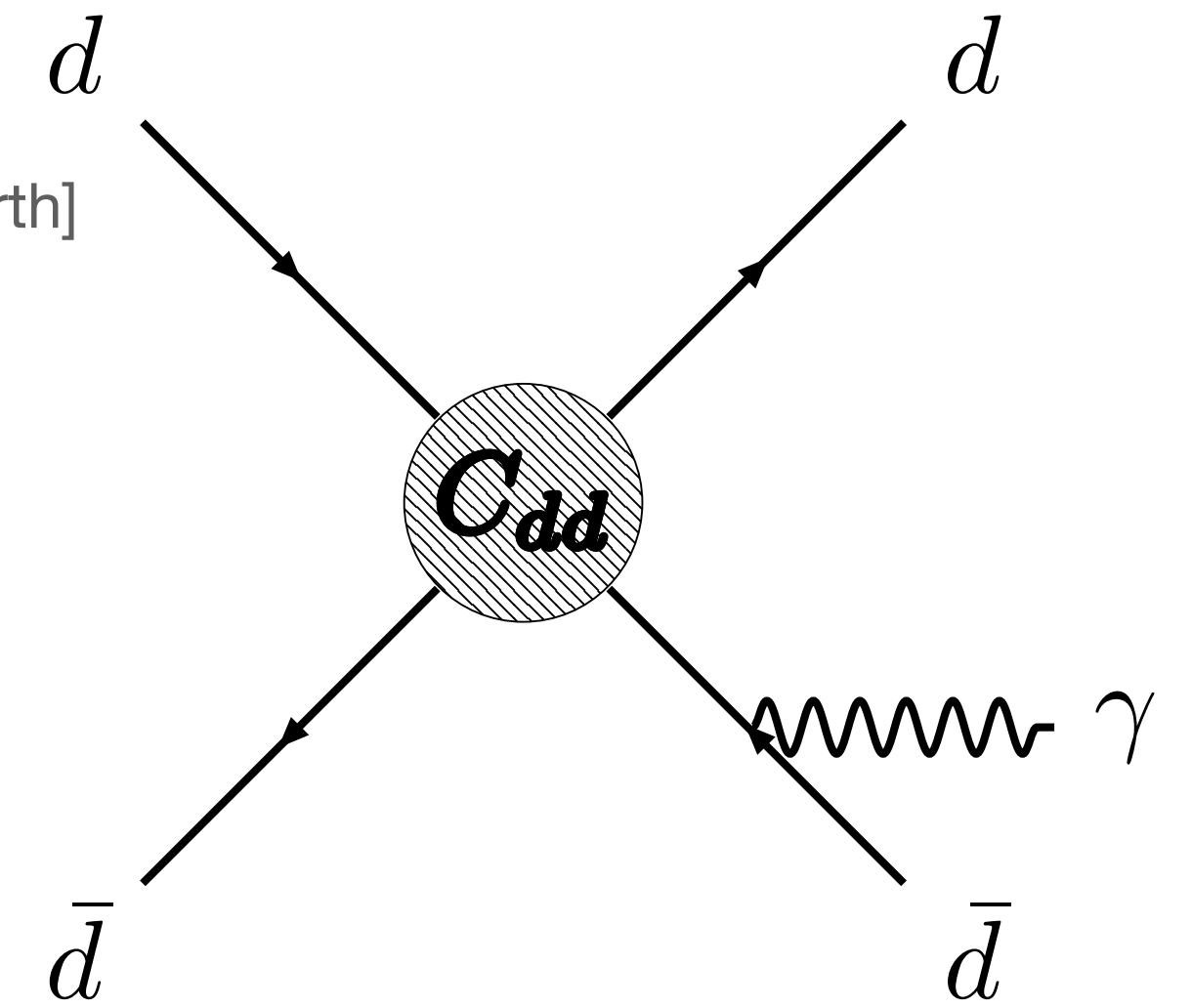
**Constrained operators: 34**





- Considering the production of two jets in association with a photon enables us to probe lower dijet invariant-mass ranges less than 1.1 TeV and circumvent the issue of dominant quadratic terms.

[2311.04963: RB, Biekötter, Hurth]



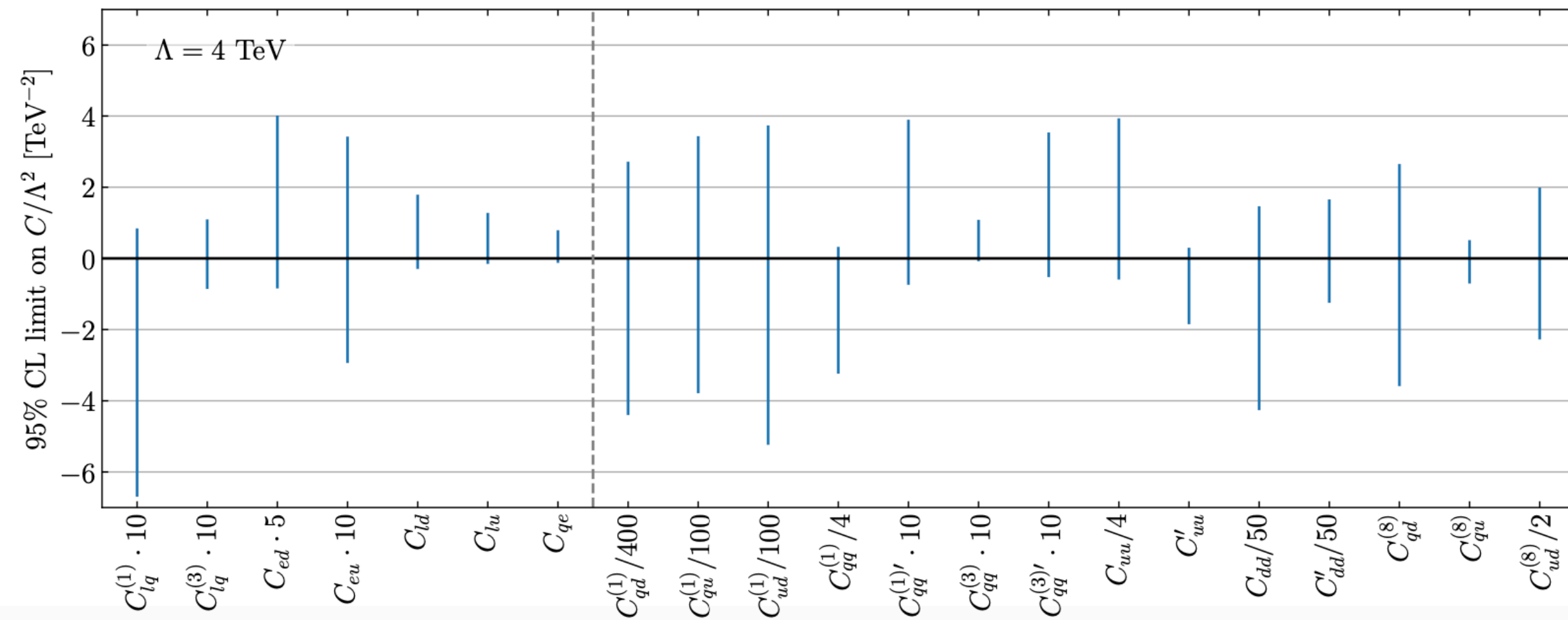
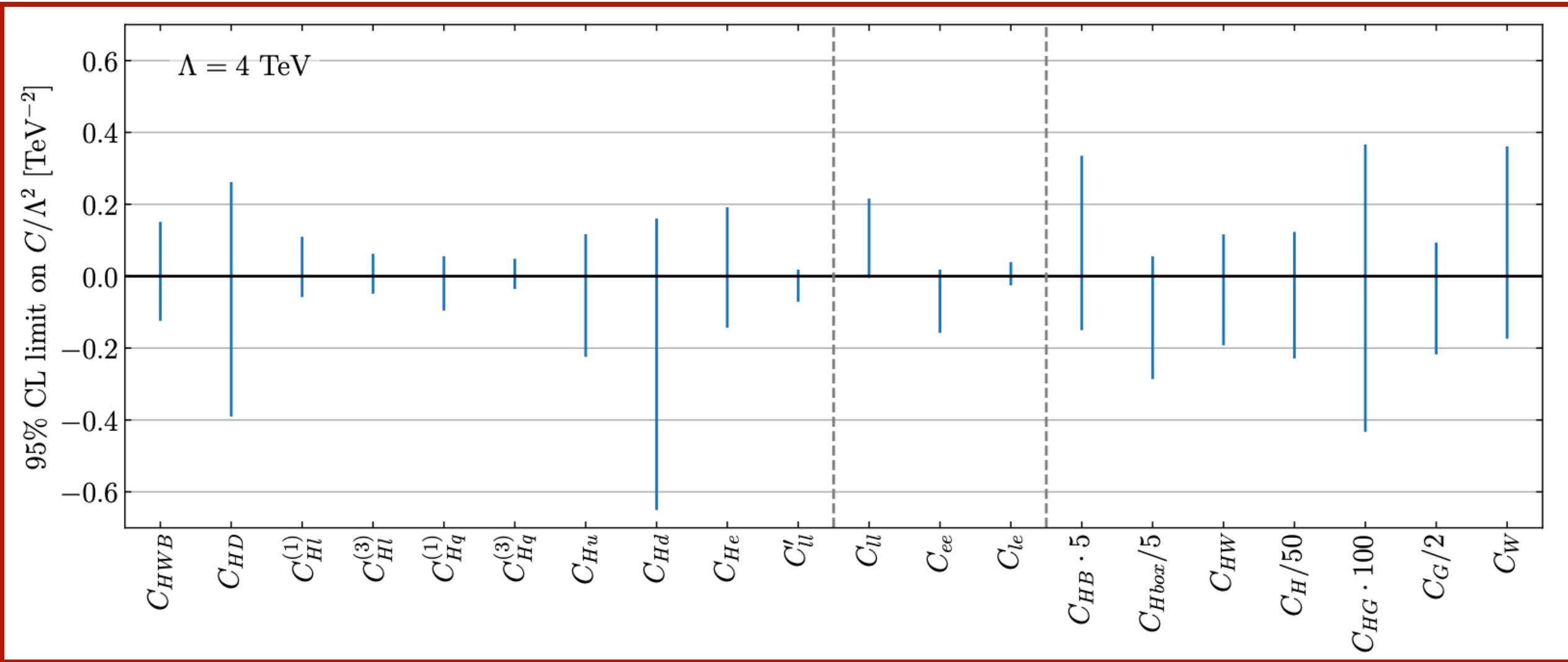
Dijet mass range: 225 GeV - 1.1 TeV

[ATLAS: 1901.10917]

**Constrained operators: 41**

# LO fit results

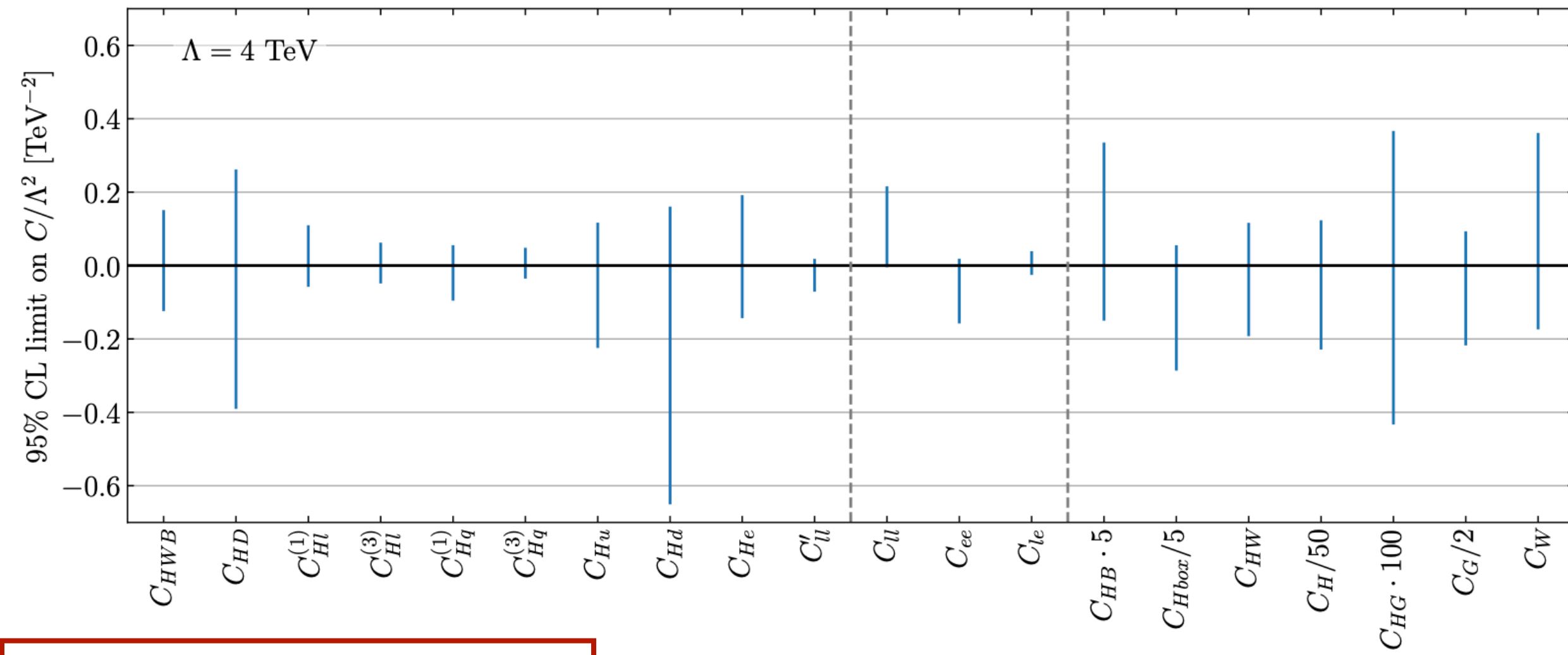
EW-Higgs operators



Comments:

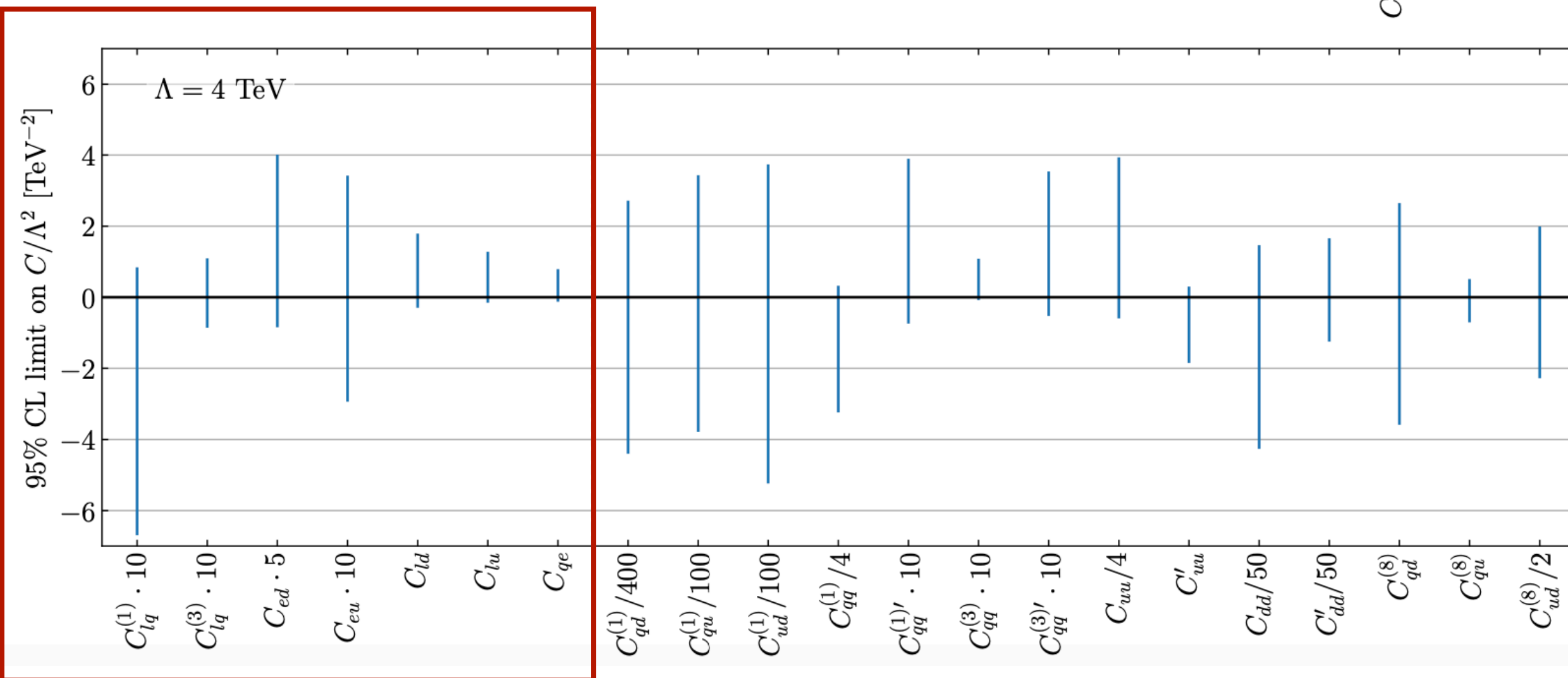
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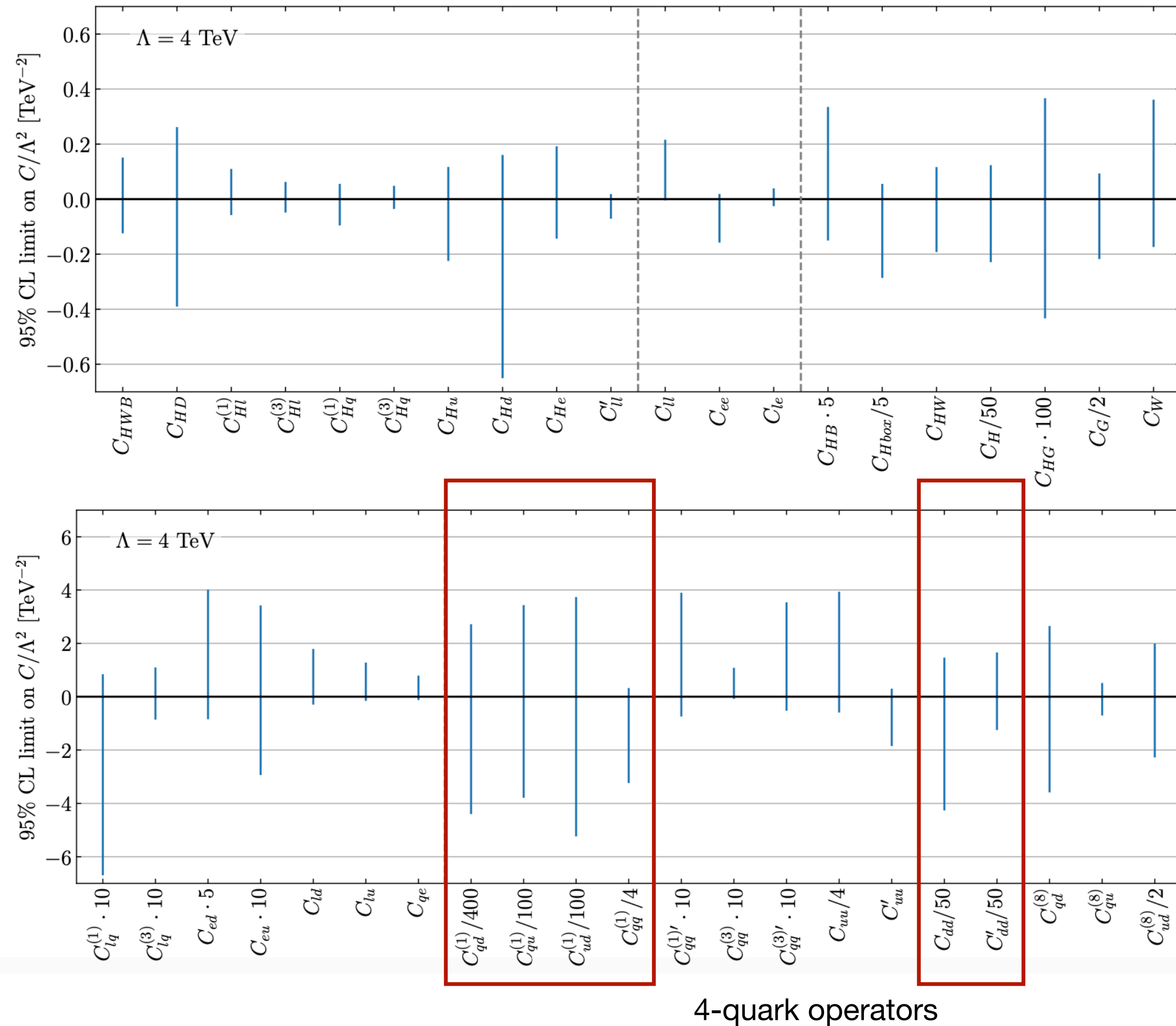
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semileptonic operators

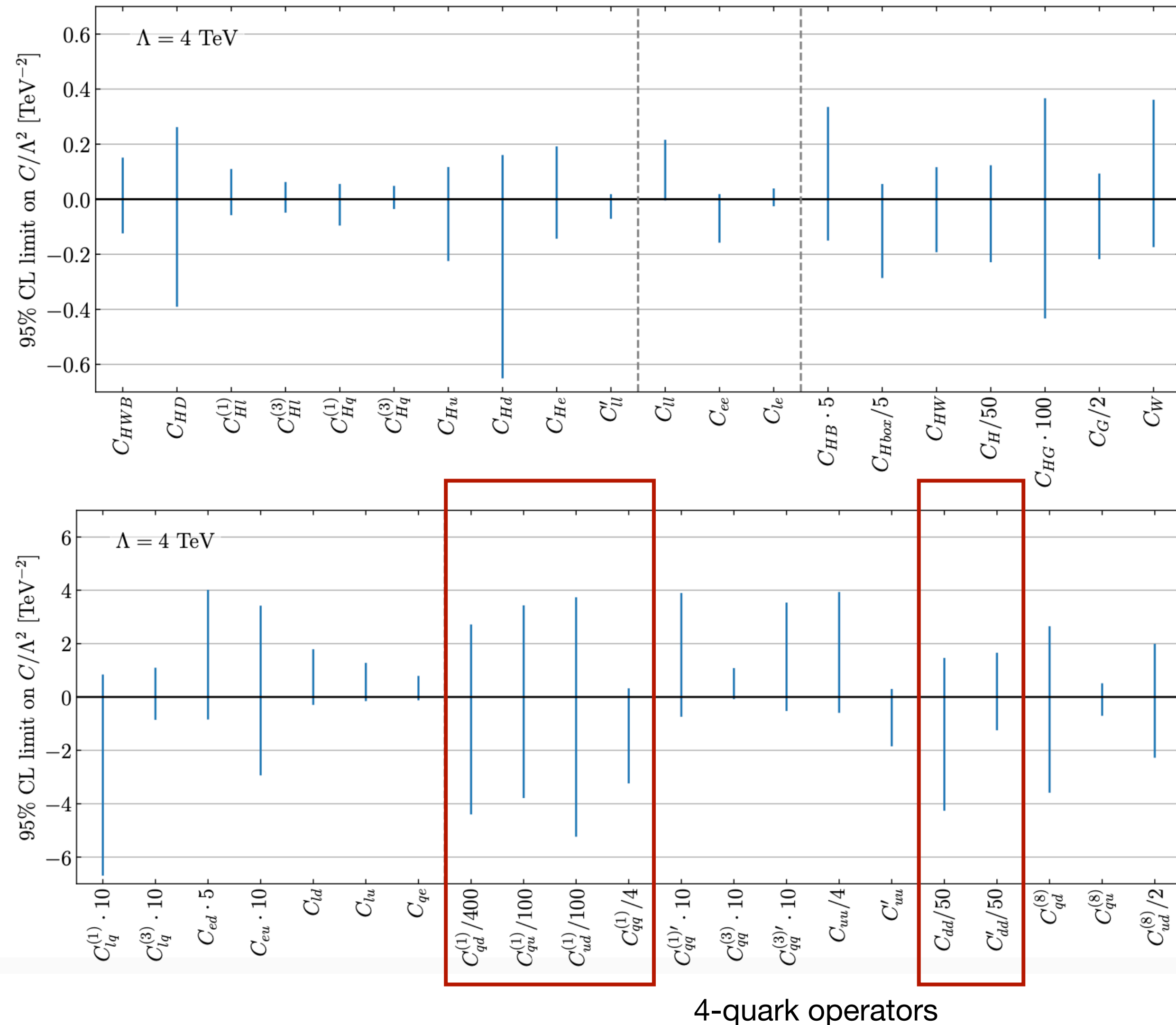
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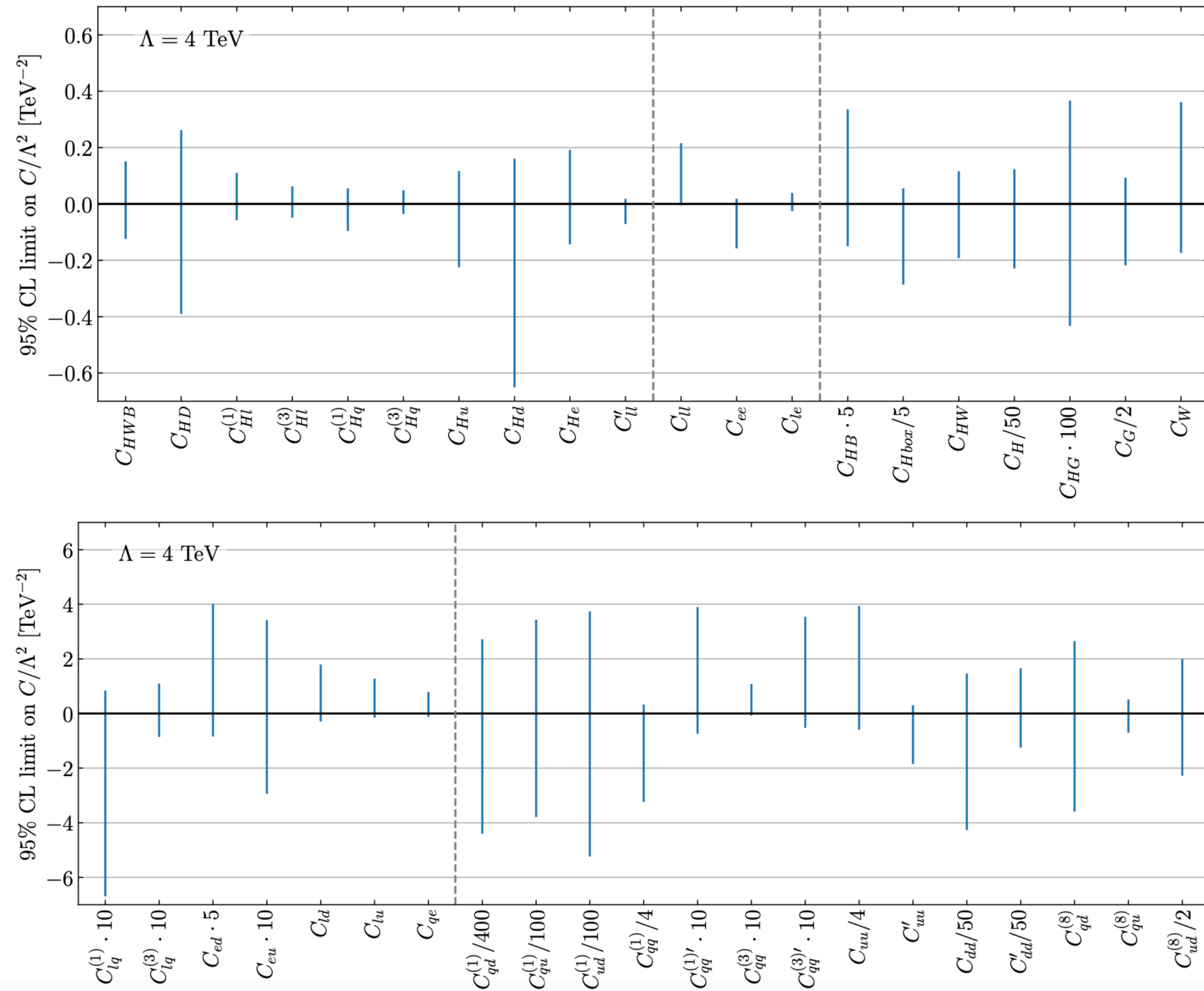


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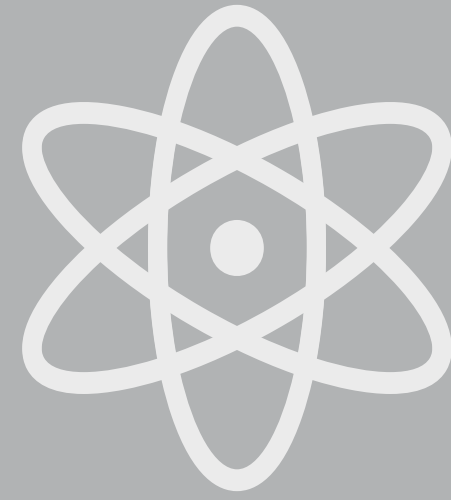


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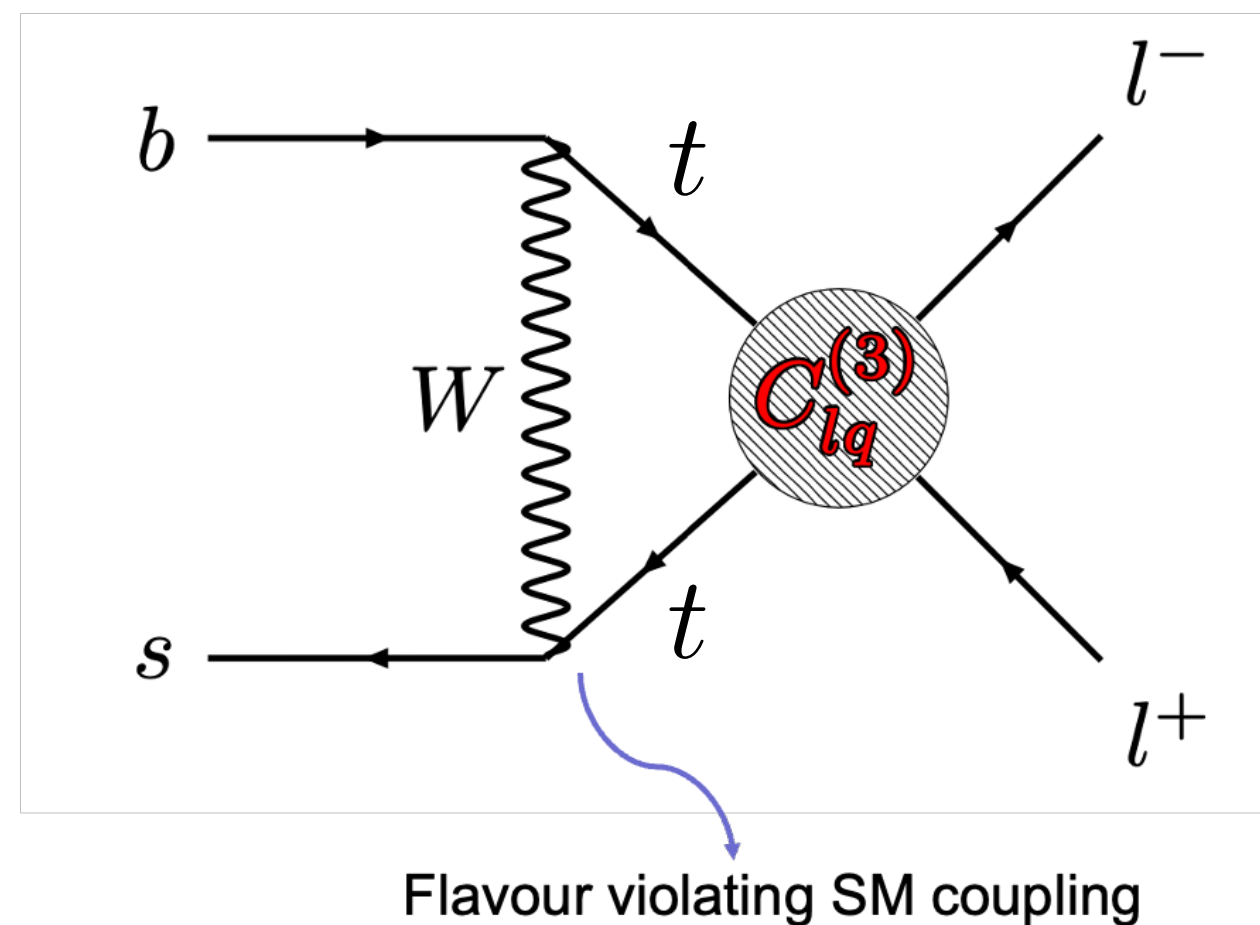
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- There are no coefficients deviating more than 2 sigma from the SM



# **RGE effects on the global analysis**

# Flavour violation in MFV SMEFT

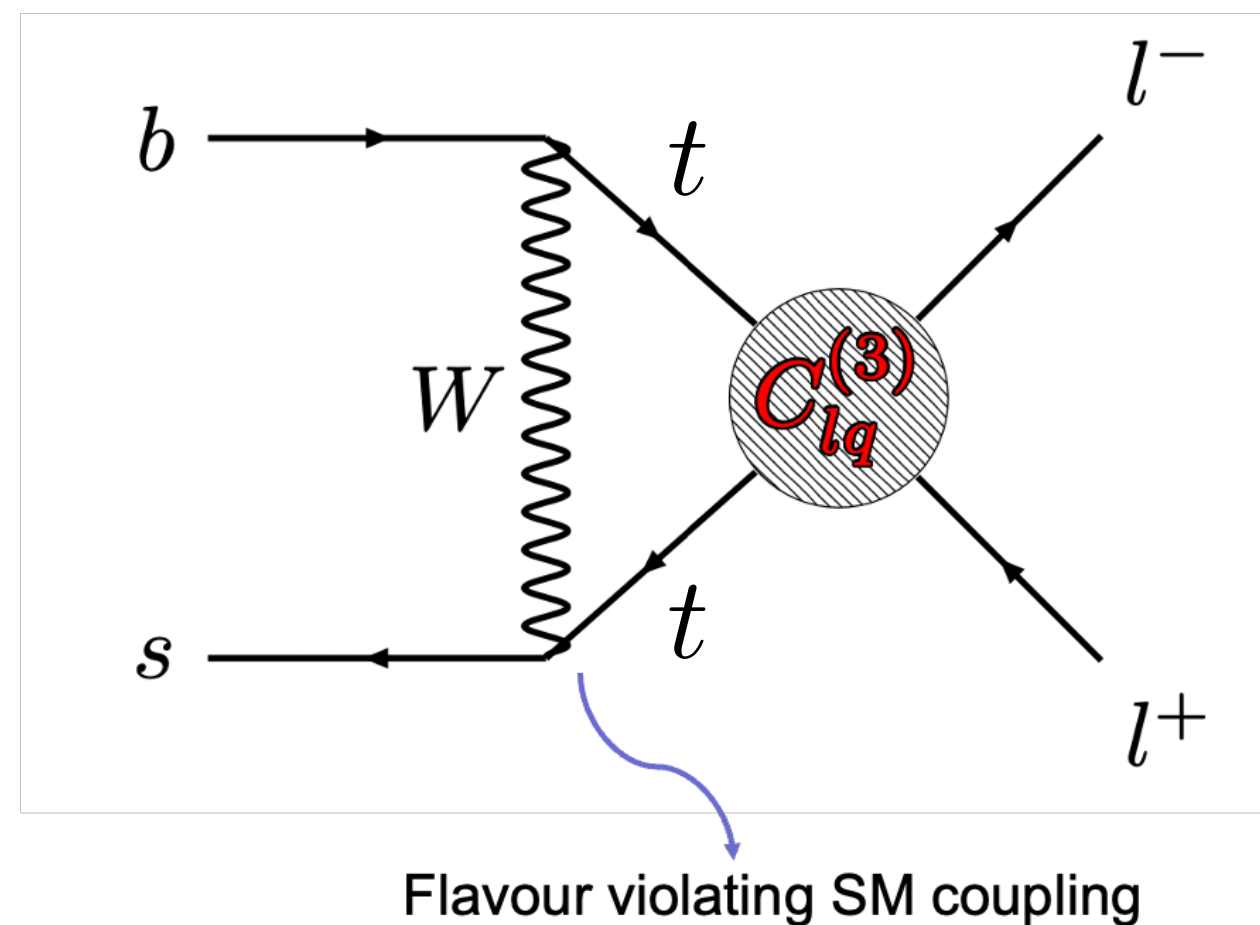
NP operators are flavour symmetric, but SM Yukawa couplings break this symmetry. **RGE** generates also **flavour violating contributions** depending on flavour-symmetric coefficients.



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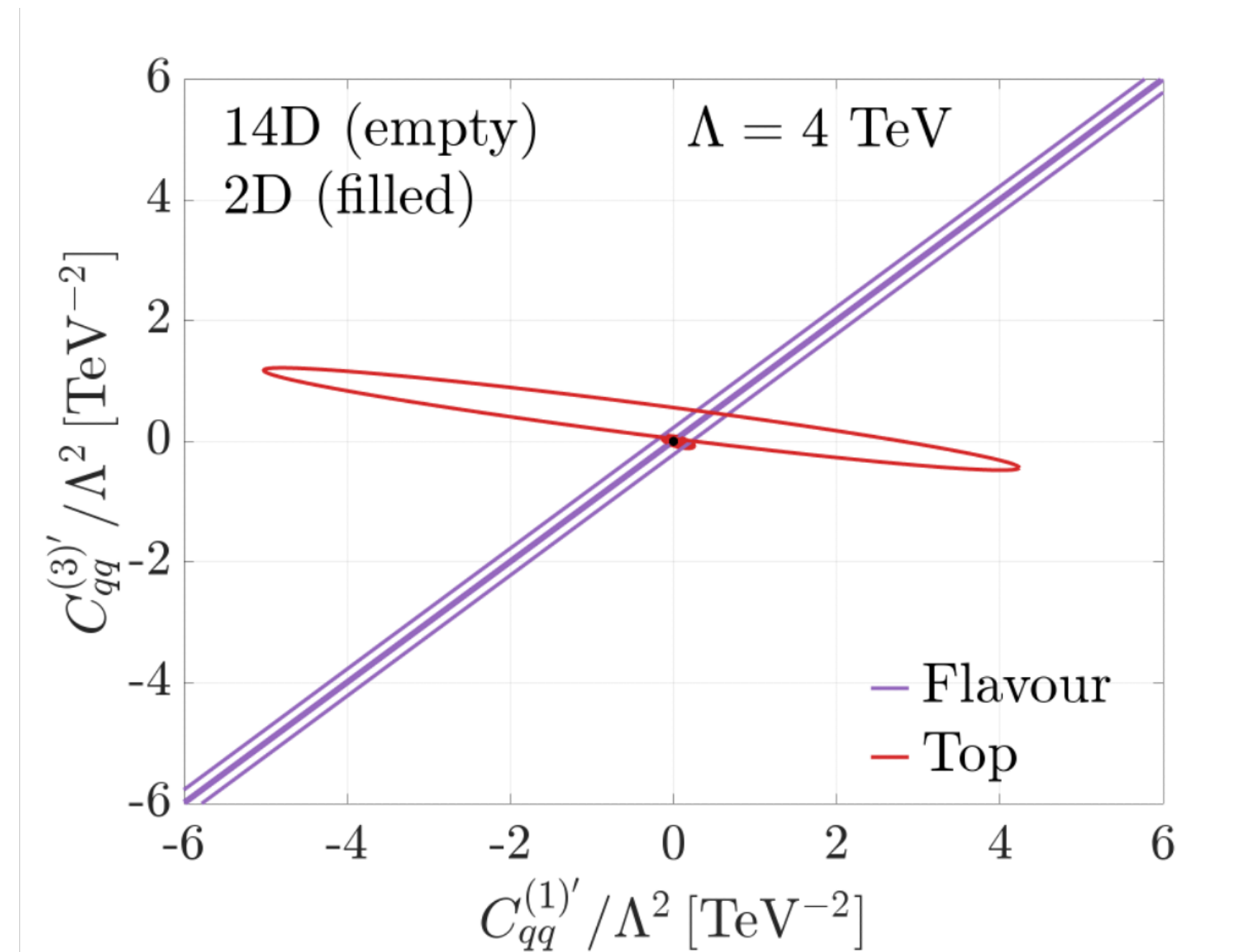
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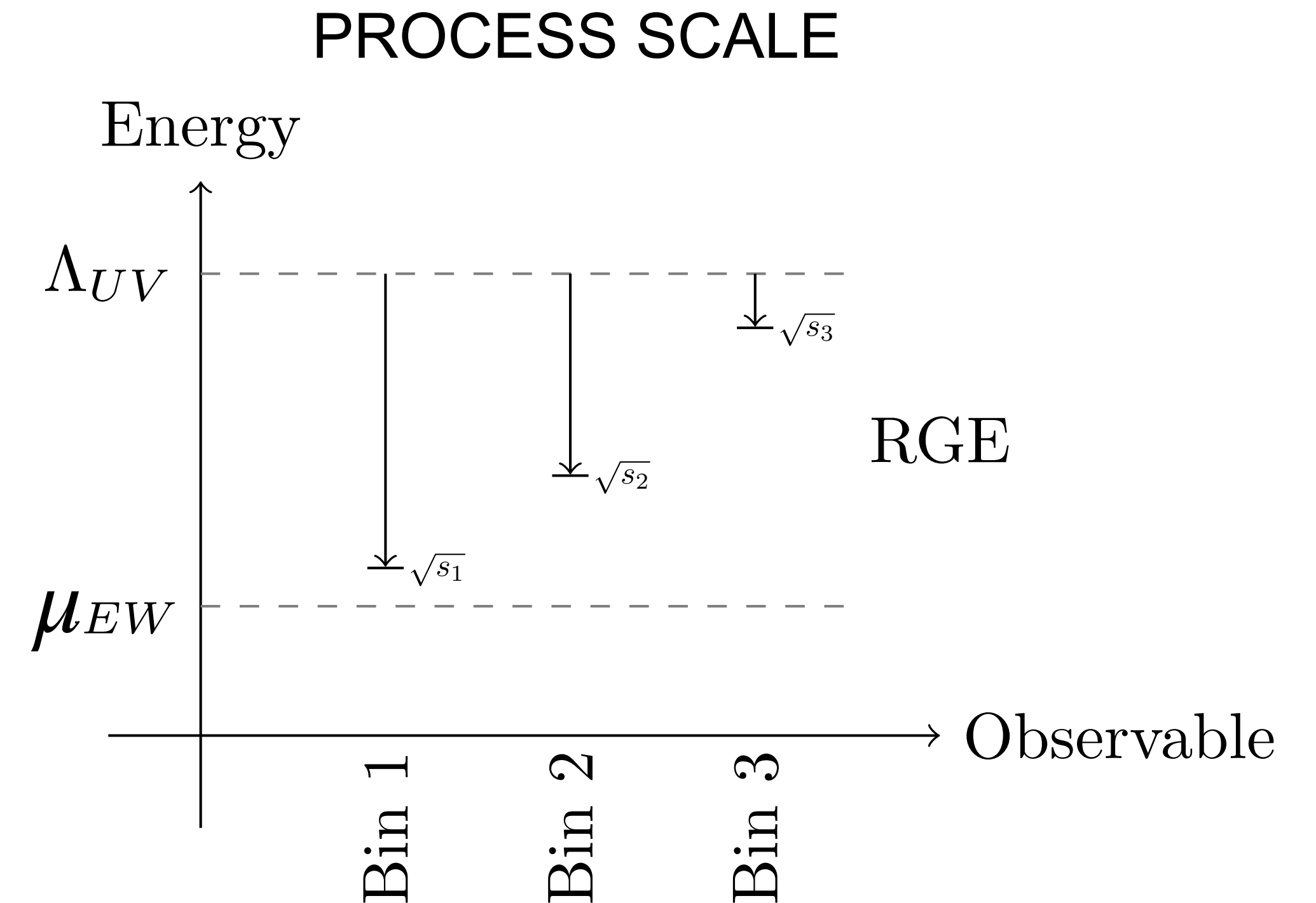
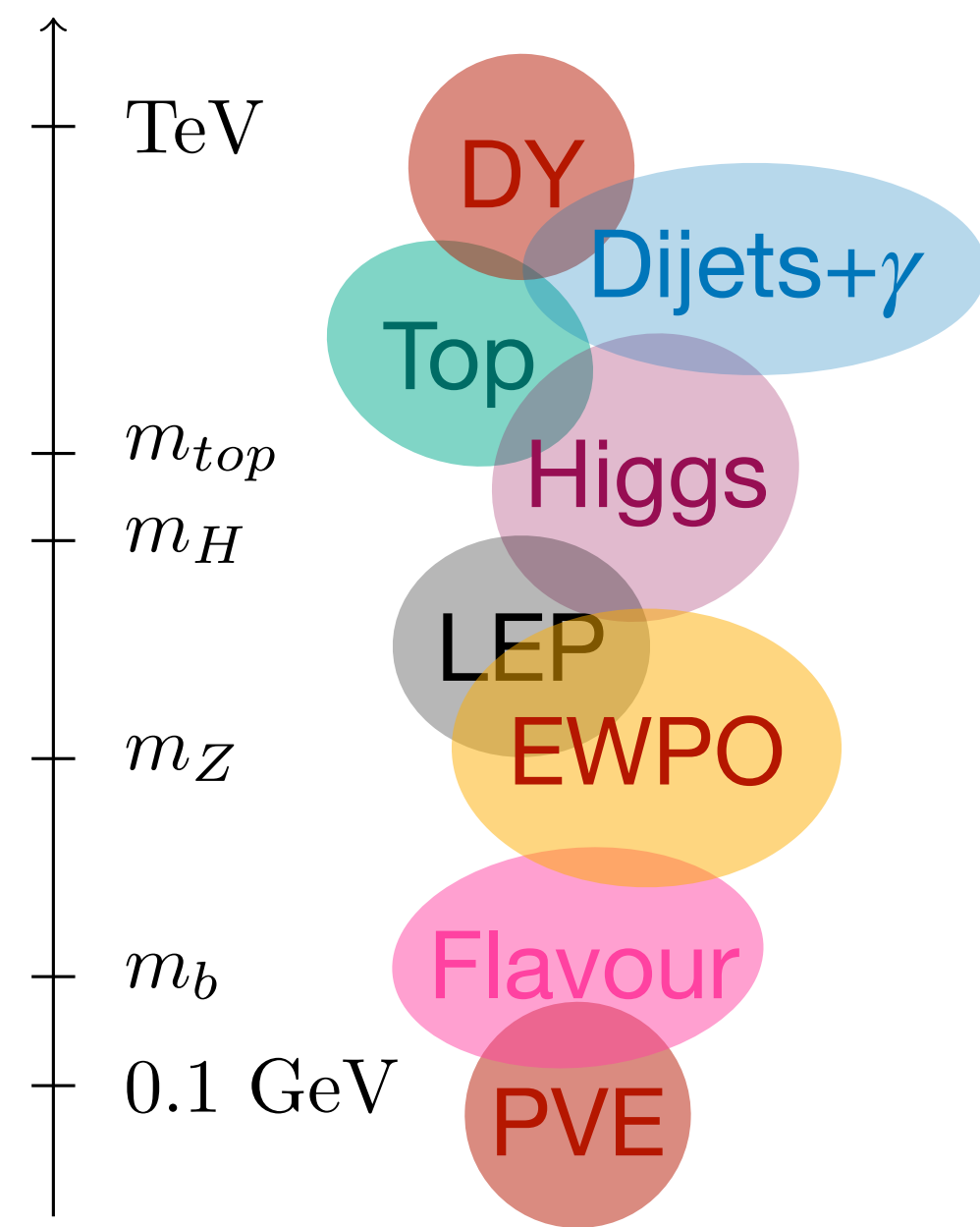
Even if suppressed flavour observables constrain **different directions** of the parameter space compared to top, thus improving significantly the bounds.



[2311.04963: RB, Biekötter, Hurth]

# Fixed scale VS Process scale

Collider observables span a wide range of energies, therefore running and mixing effects depend on the renormalisation scale choice.



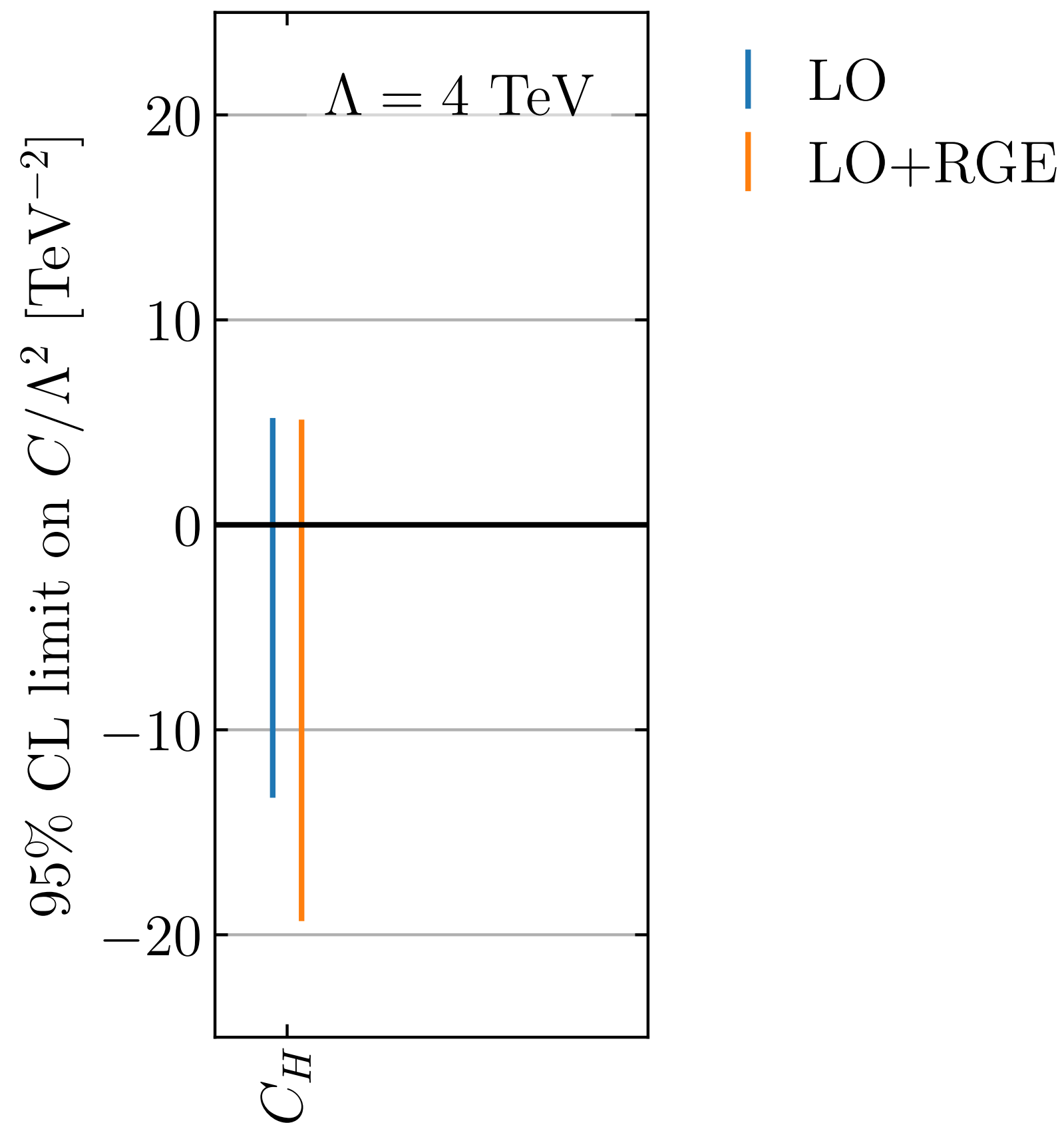
Choosing a dynamical scale instead of a fixed scale can sizeably influence the constraints on the Wilson coefficients.

[2212.05067: Aoude et al.]  
[2409.19578: Heinrich and Lang]  
[2312.11327: Di Noi, Gröber]

# RGE effects on the global analysis

## Diagonal running effect:

There are operators like  $C_H$  that run diagonally bringing to different bounds between the fit with no running and the fit with running.



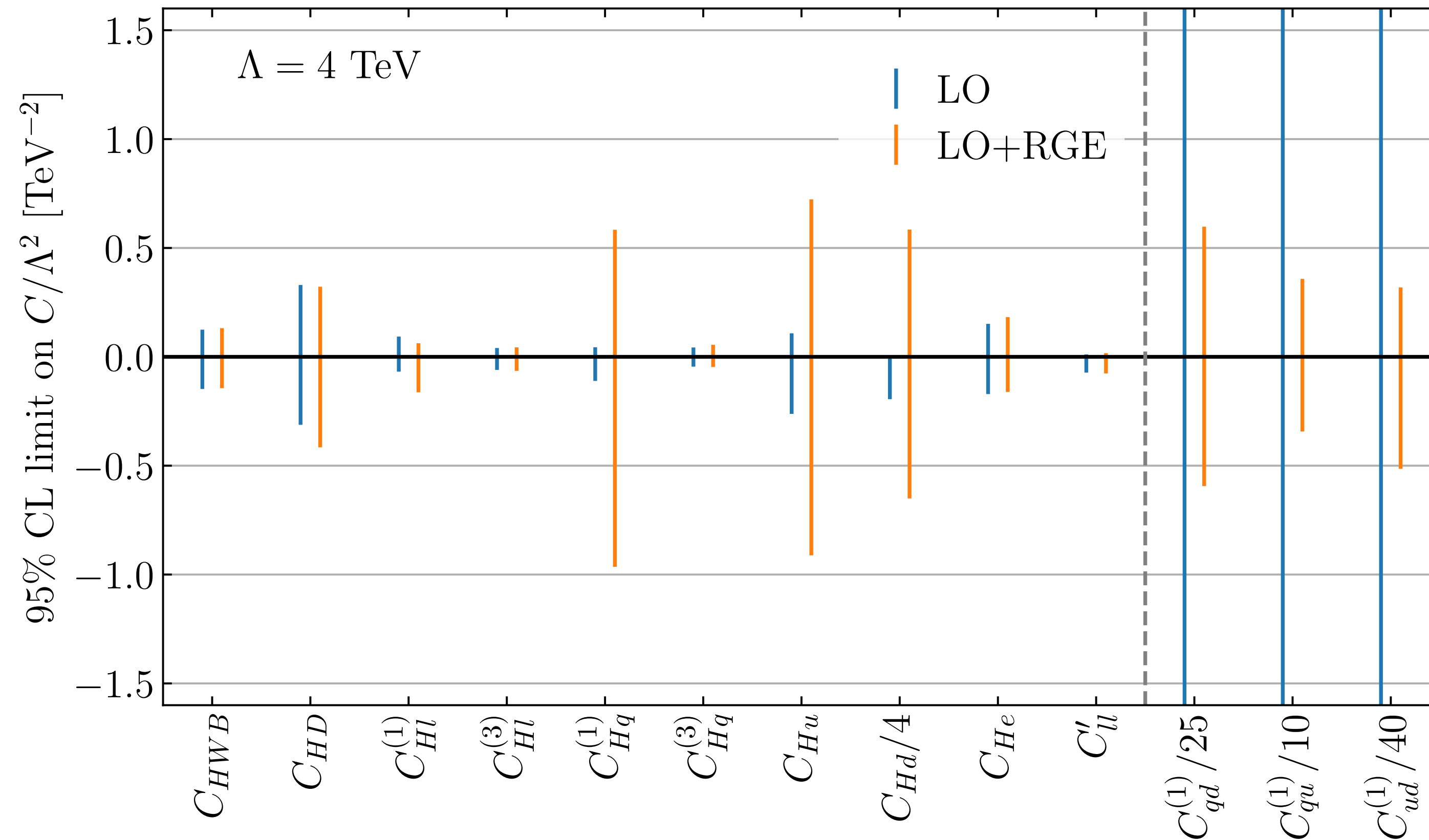
$$C_H(\mu_{EW}) = 0.65 C_H(\mu_\Lambda)$$

The operator  $C_H$  at the EW scale is 35% smaller than the same operator at the NP scale. Since this operator is constrained almost independently in di-Higgs production, its bound is weakened of this factor.

# RGE and correlations

Non-diagonal running effect:

$$C_{ed}(\mu_{EW}) = 0.02 C_{ud}^{(1)}(\mu_{\Lambda}) + 0.01 C_{qd}^{(1)}(\mu_{\Lambda})$$

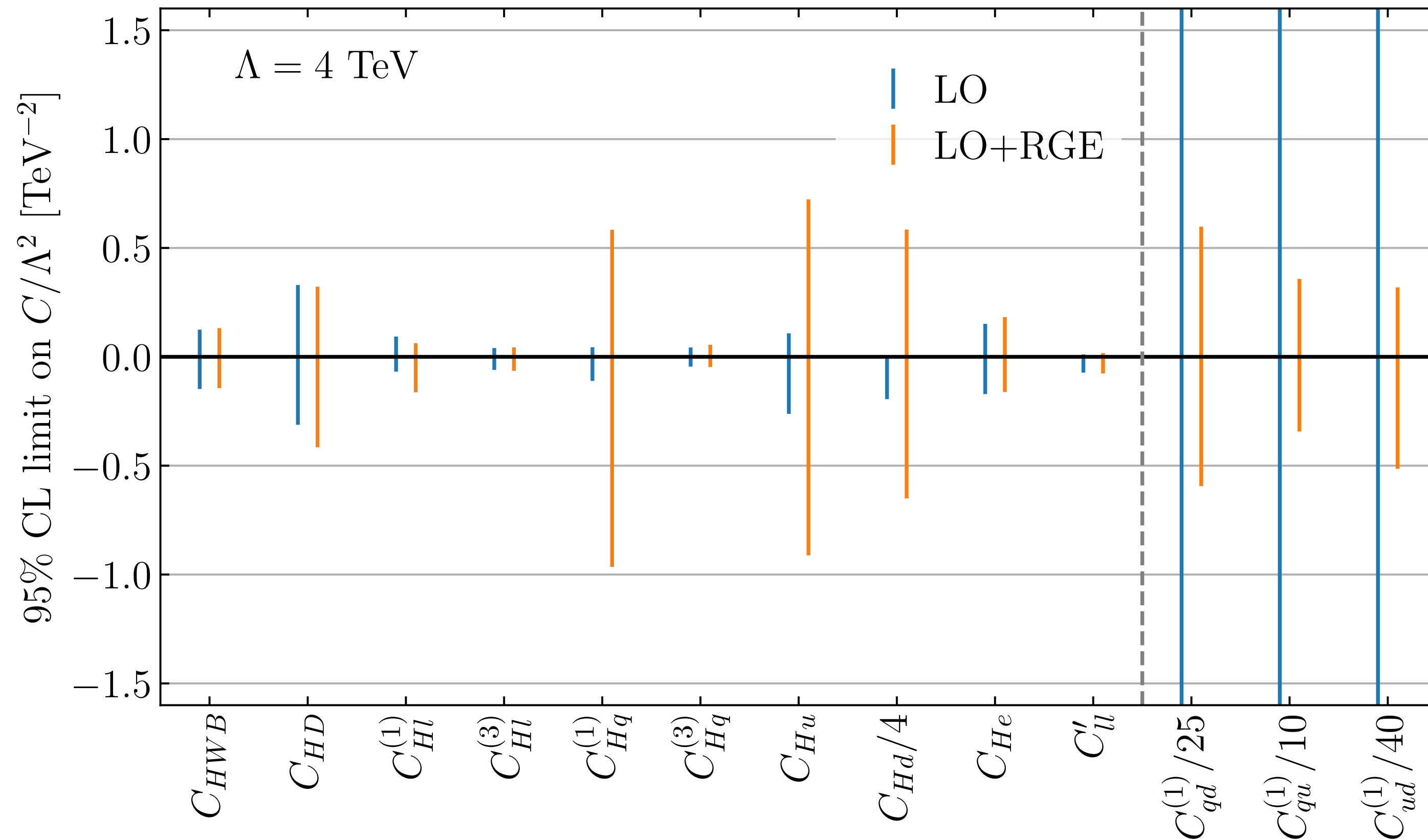


Including the RGE effects influences significantly EWPO operators

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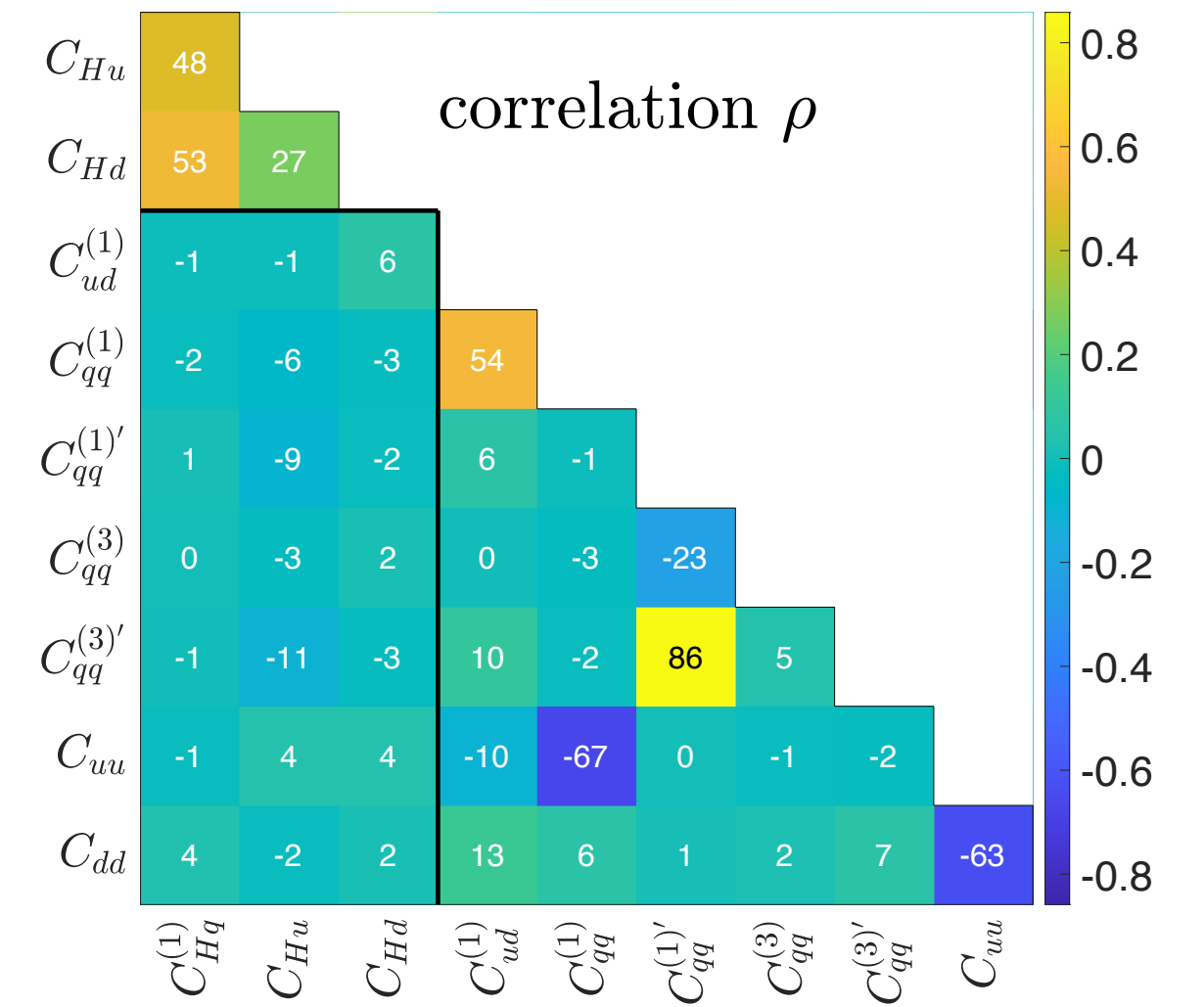
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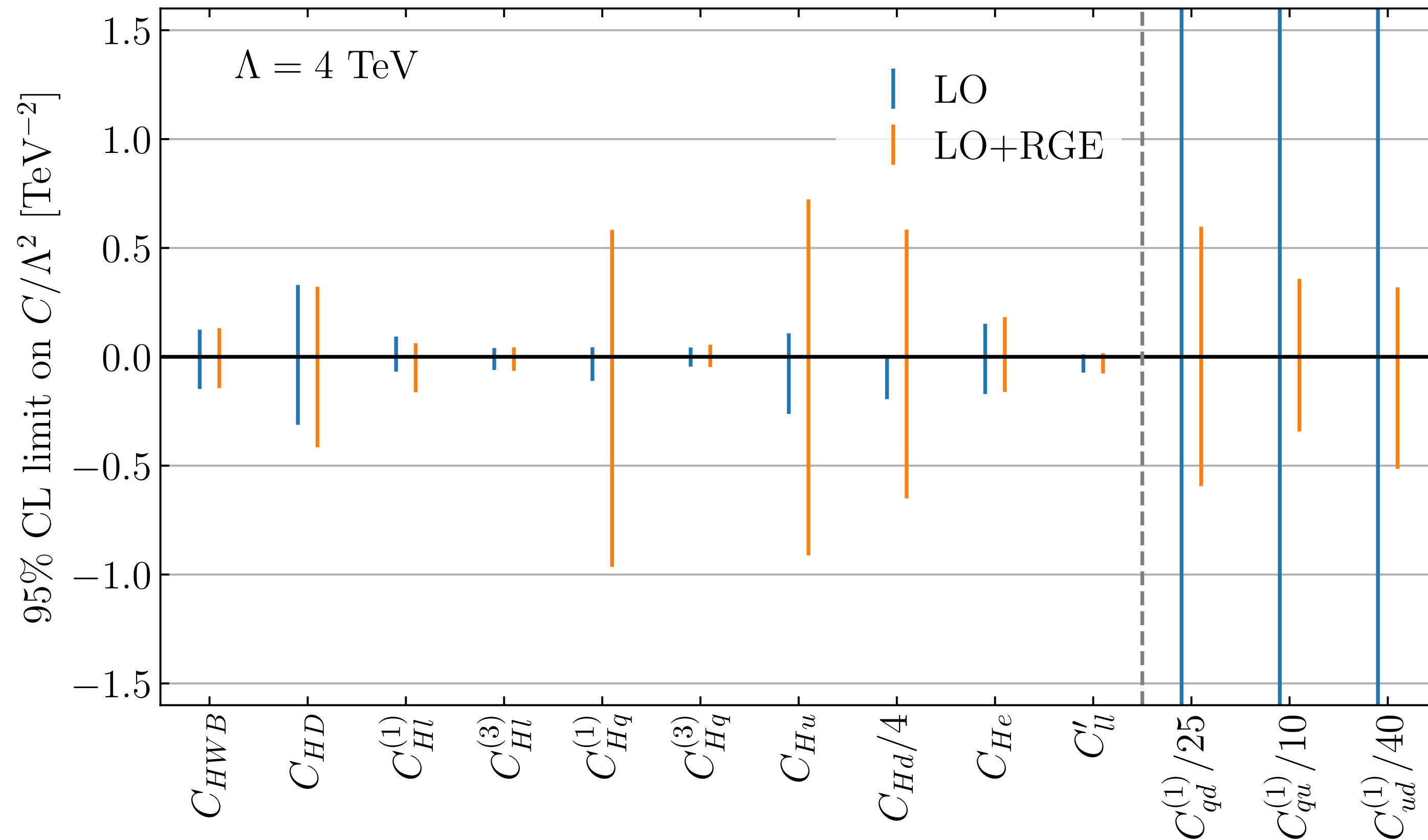




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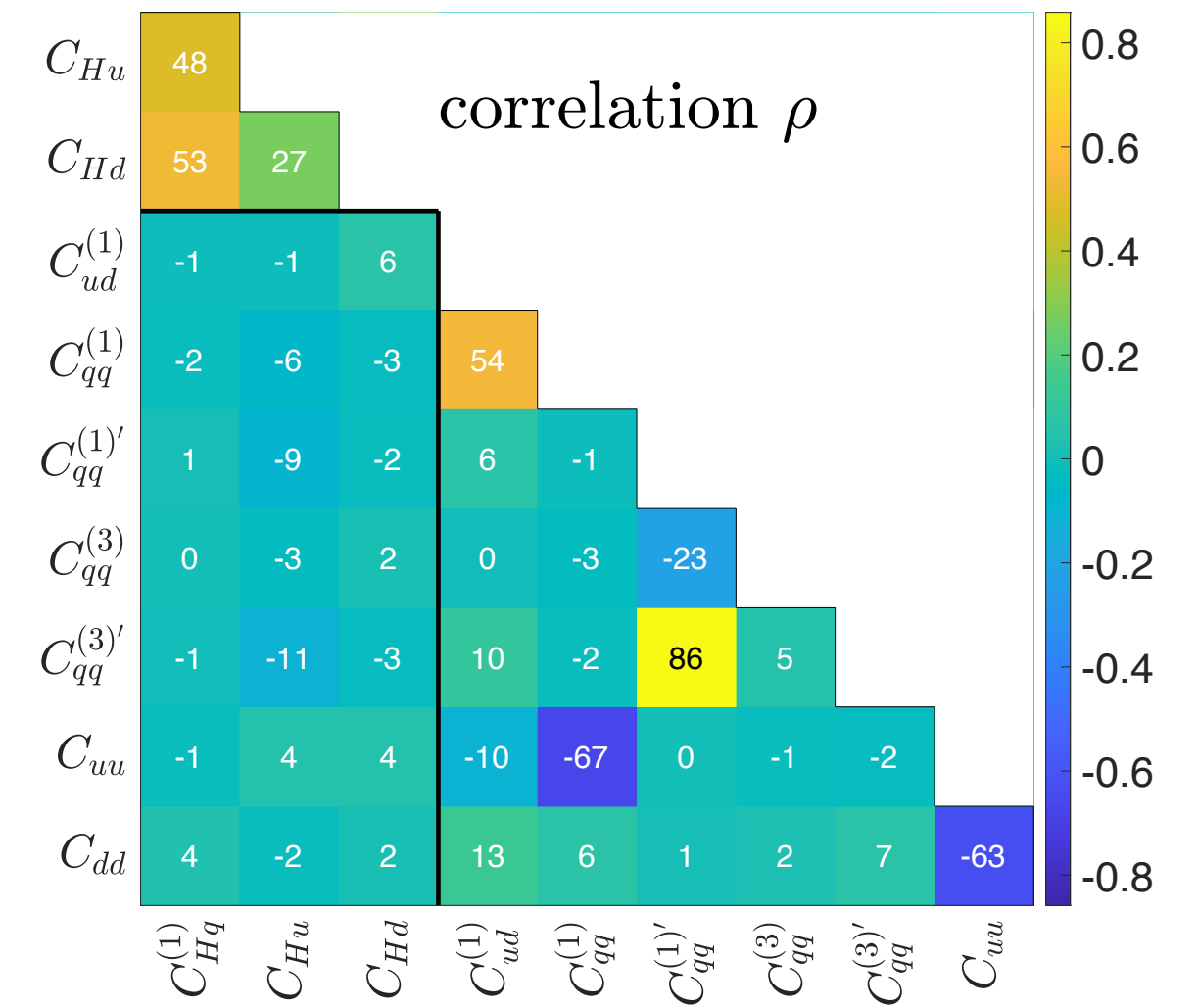
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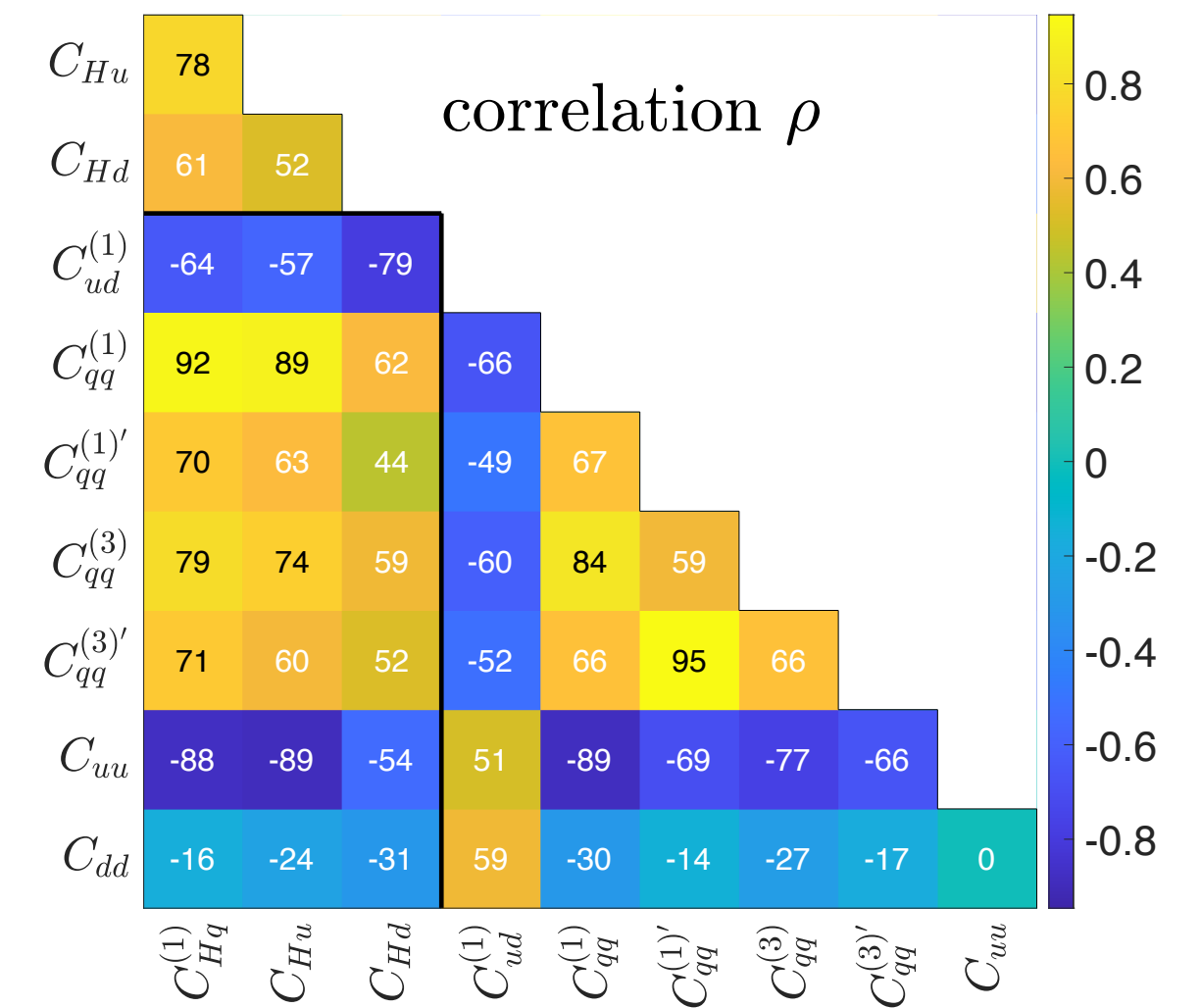


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LO



LO+RGE



# Summary and outlook

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Under this assumption, all the operators can be bounded without surviving flat directions

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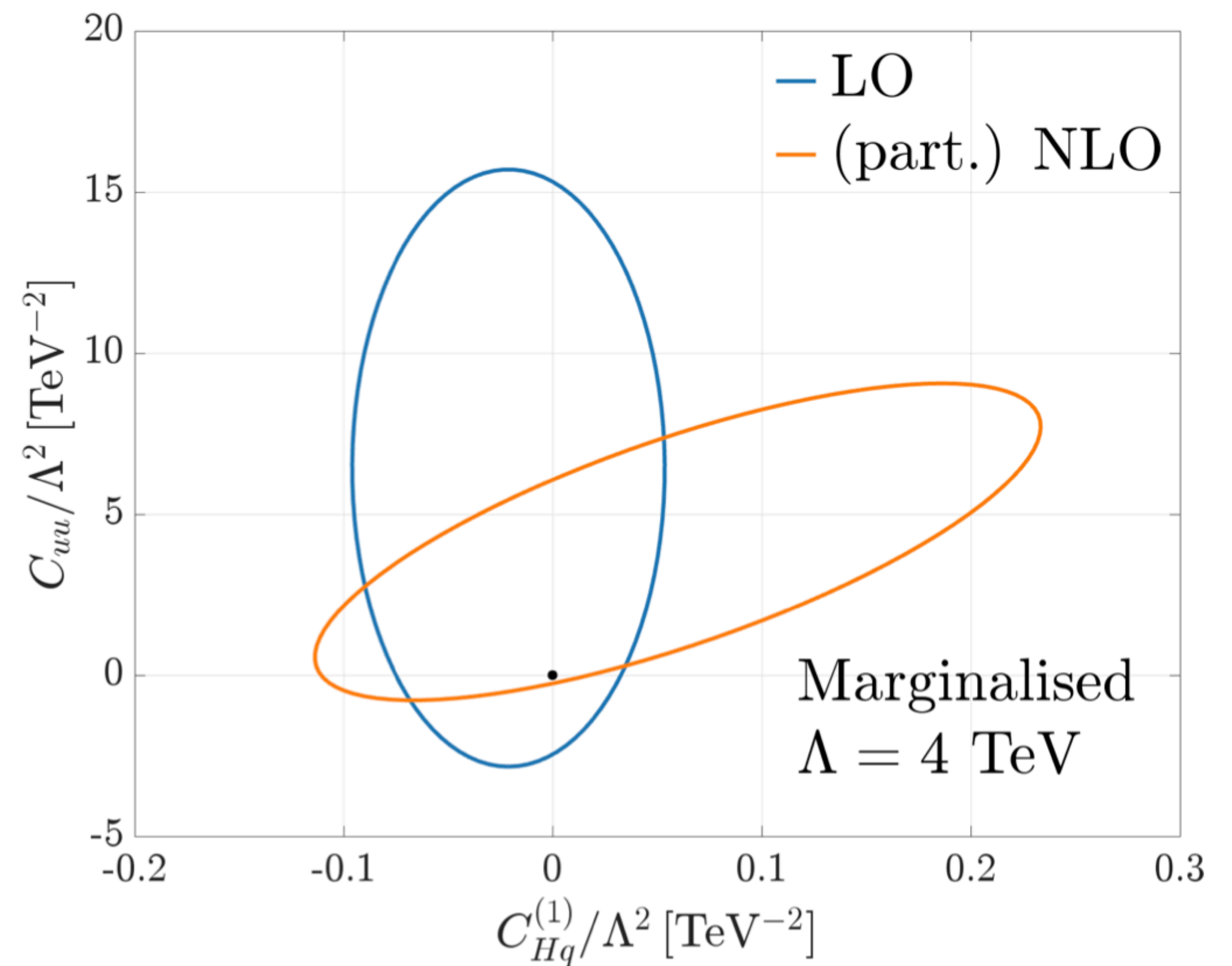
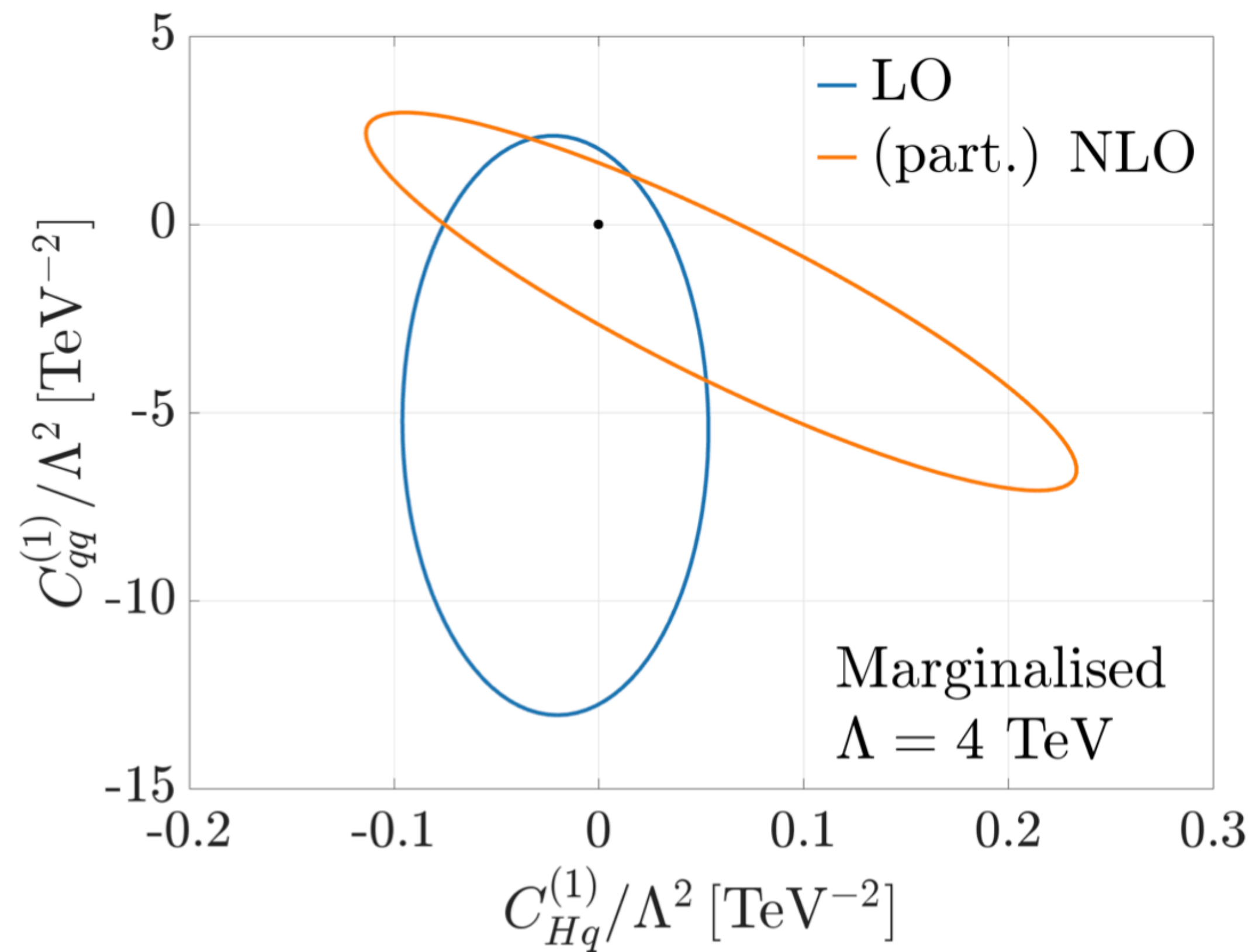
**Thank you for your attention!**



**Back up slides**

# The $C_{Hq}^{(1)}$ case

The only weakened bound with NLO contributions is  $C_{Hq}^{(1)}$ . At LO there are no visible correlations with four-quark operators, but at NLO there is a strong correlation with  $C_{uu}$  and  $C_{qq}^{(1)}$  due to EWPO.

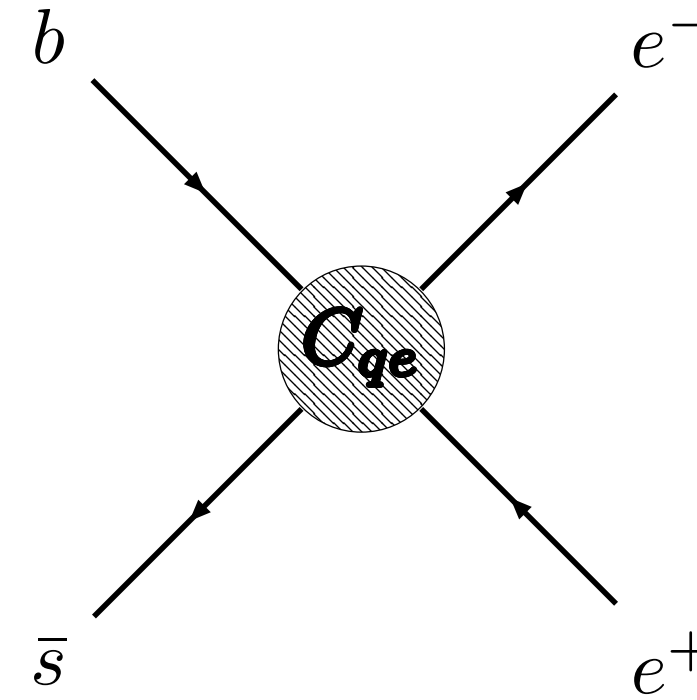




# SMEFT and flavour symmetry

Symmetry assumption on NP:

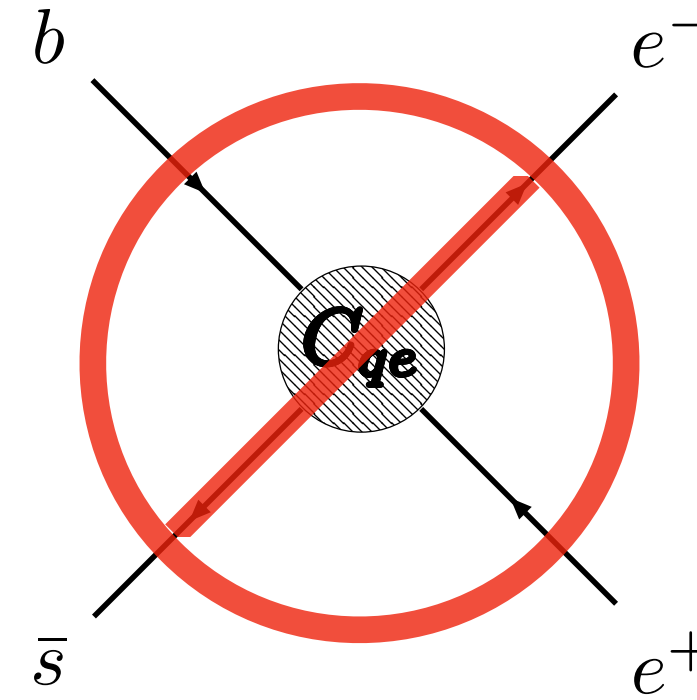
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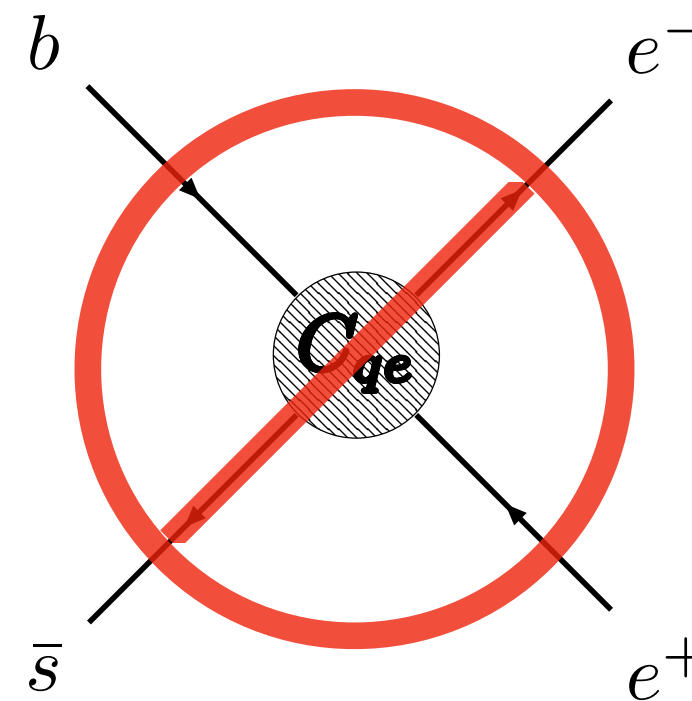
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$$U(3)^5 = U(3)_\ell \times U(3)_q \times U(3)_e \times U(3)_u \times U(3)_d$$



From 2499 dimension six operators to 41 (CP even)

[2005.05366: Faroughy, Isidori, Wilsch, Yamamoto]

- According to this assumption also Yukawa-like operators are excluded because they add additional source of flavour violation BSM.

	$\psi^2 \varphi^3$
$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$

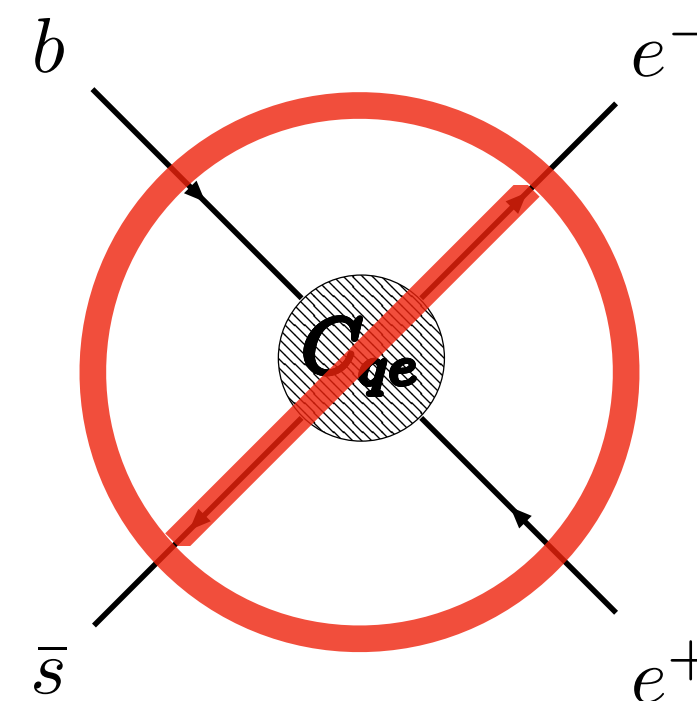
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- For some 4-fermion operators there are two independent ways to contract the flavour indices to get a flavour conserving operator.

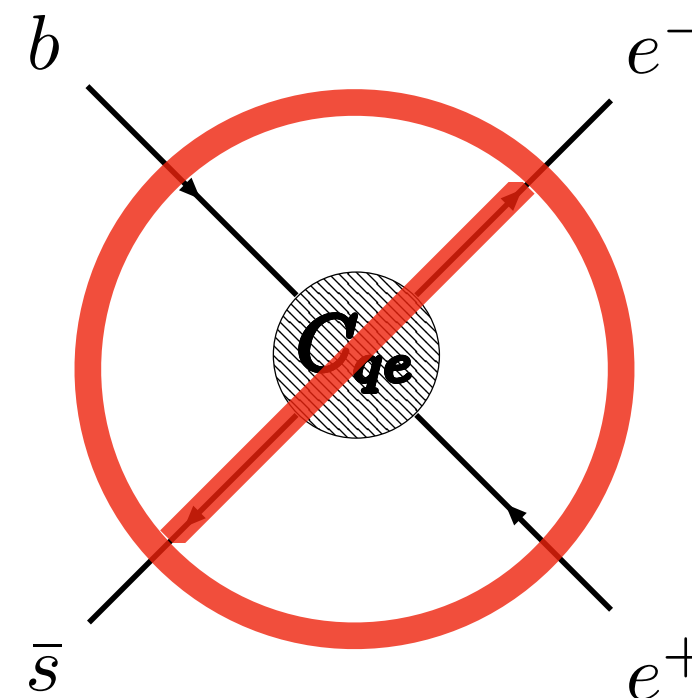
$$Q_{ll} = (\bar{l}_i \gamma_\mu l_j)(\bar{l}_k \gamma^\mu l_l)$$

$$C_{ll} \delta_{ij} \delta_{lk} \quad \text{and} \quad C'_{ll} \delta_{ik} \delta_{jl}.$$

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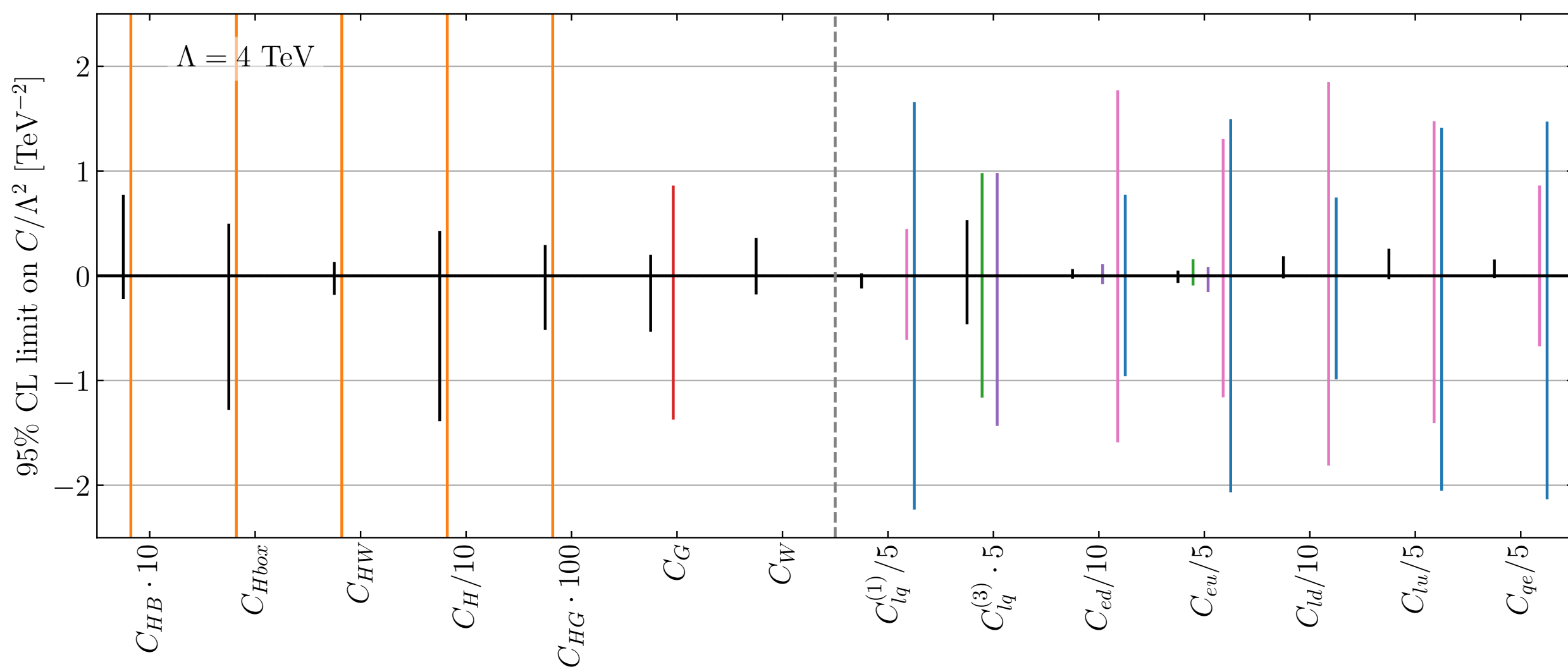
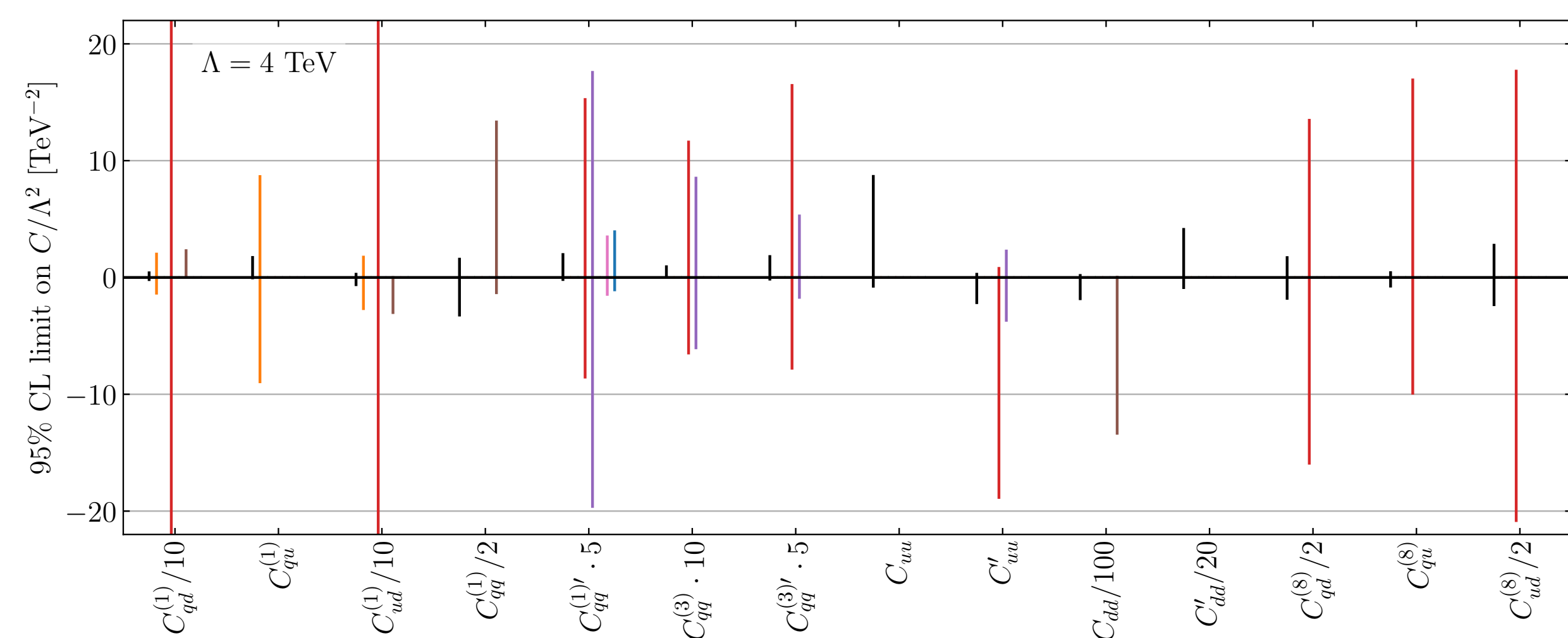
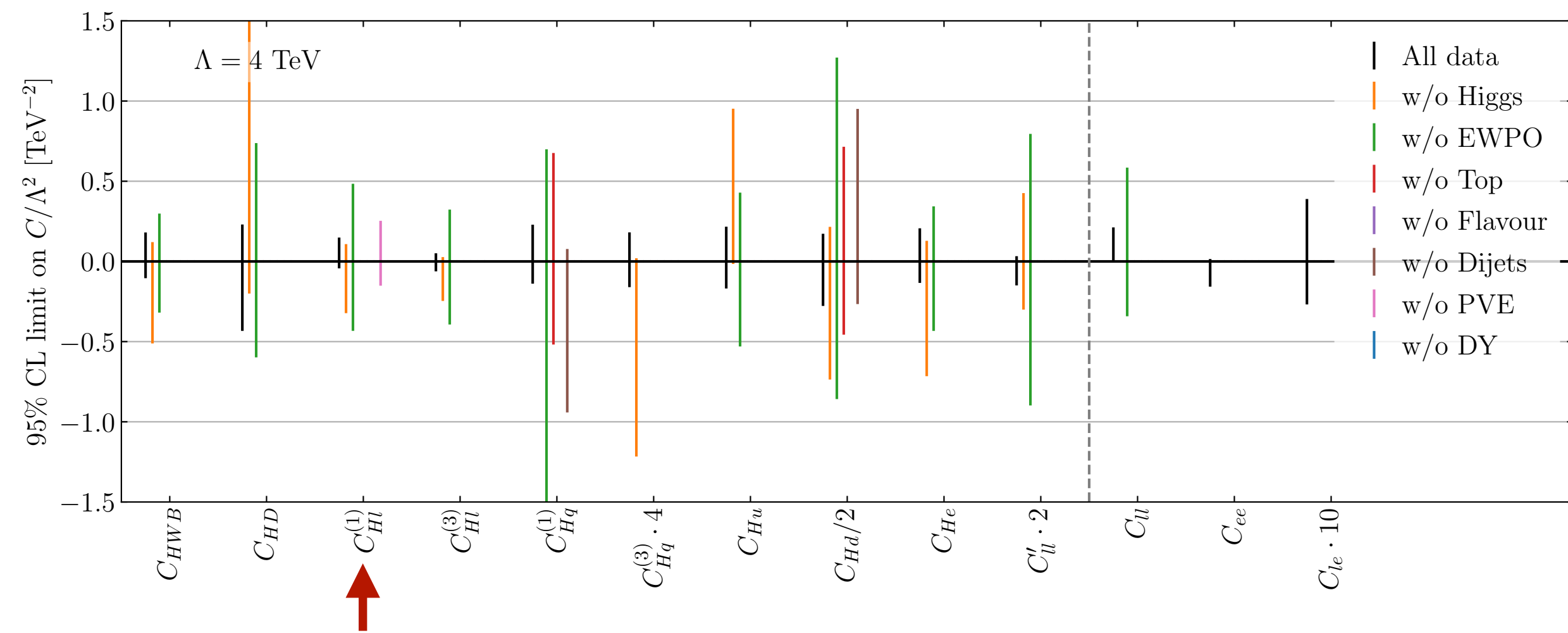
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$$C_{ll} \delta_{ij} \delta_{lk} \quad \text{and} \quad C'_{ll} \delta_{ik} \delta_{jl}.$$

This assumption corresponds to minimal version of MFV: it contains the minimum and non-removable amount of flavour violation.

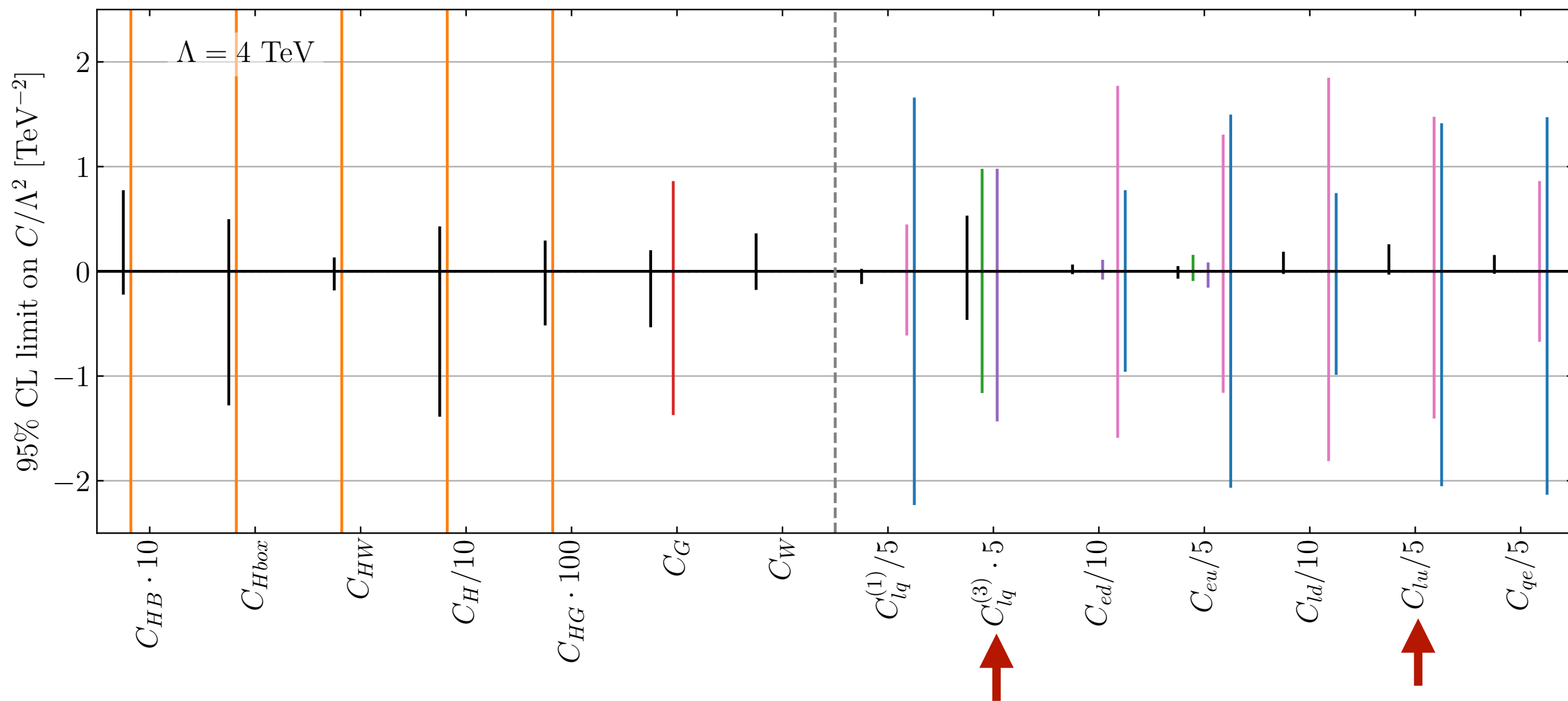
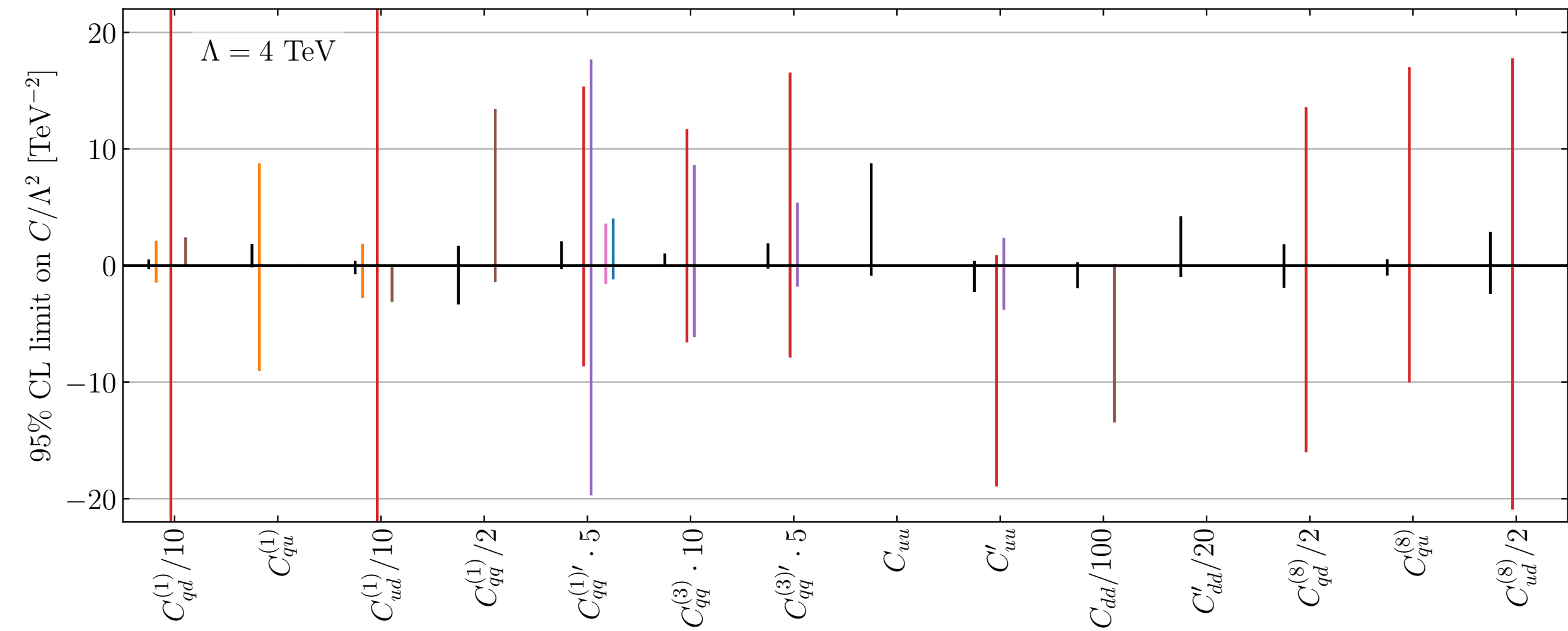
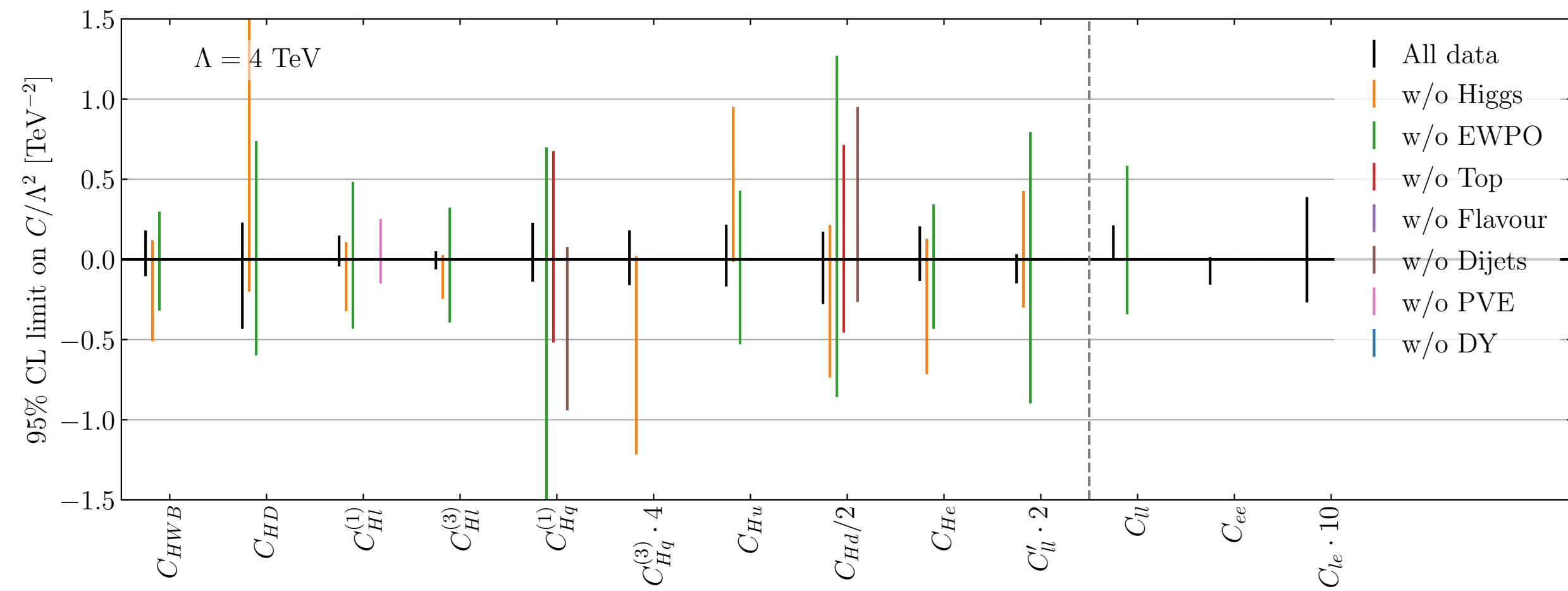
# Full results removing datasets



- PVE impact on  $C_{HI}^{(1)}$  and  $C_{qq}^{(1)'}$

[2311.04963: RB, Biekötter, Hurth]

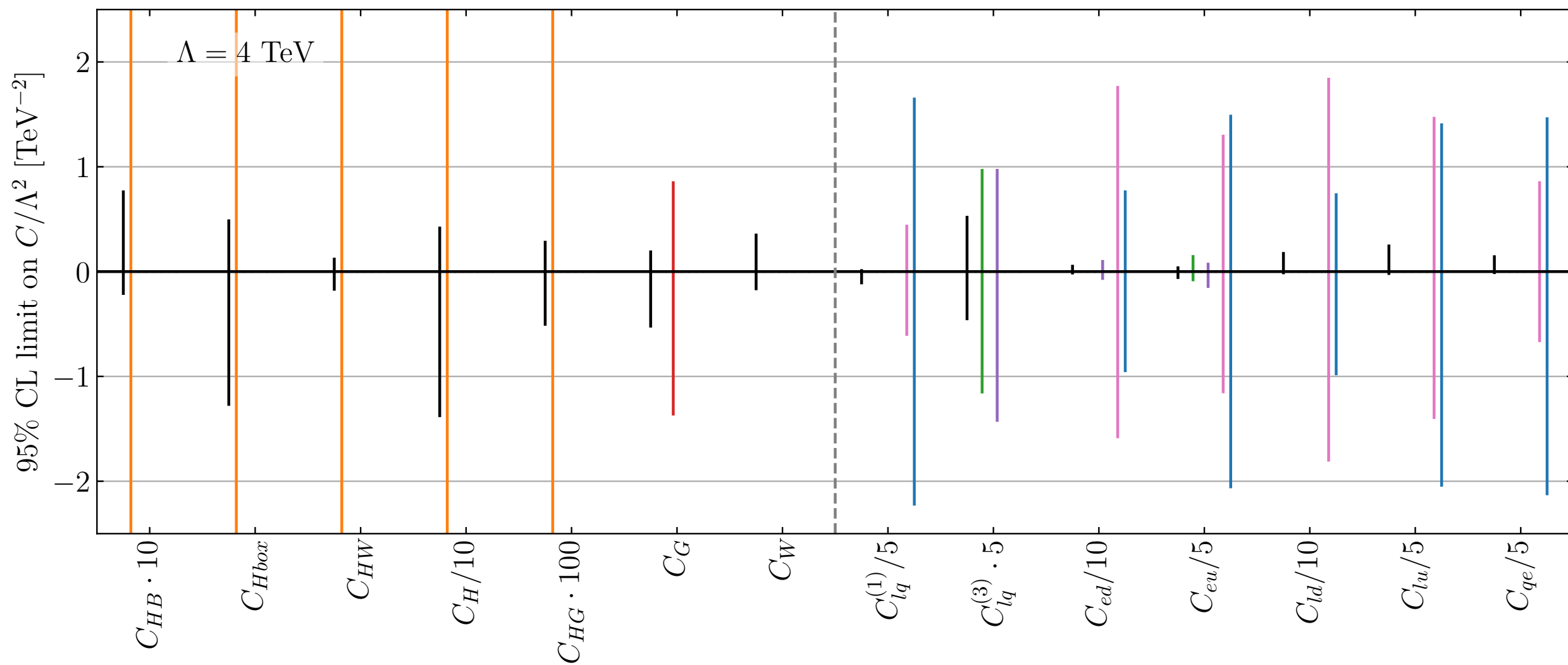
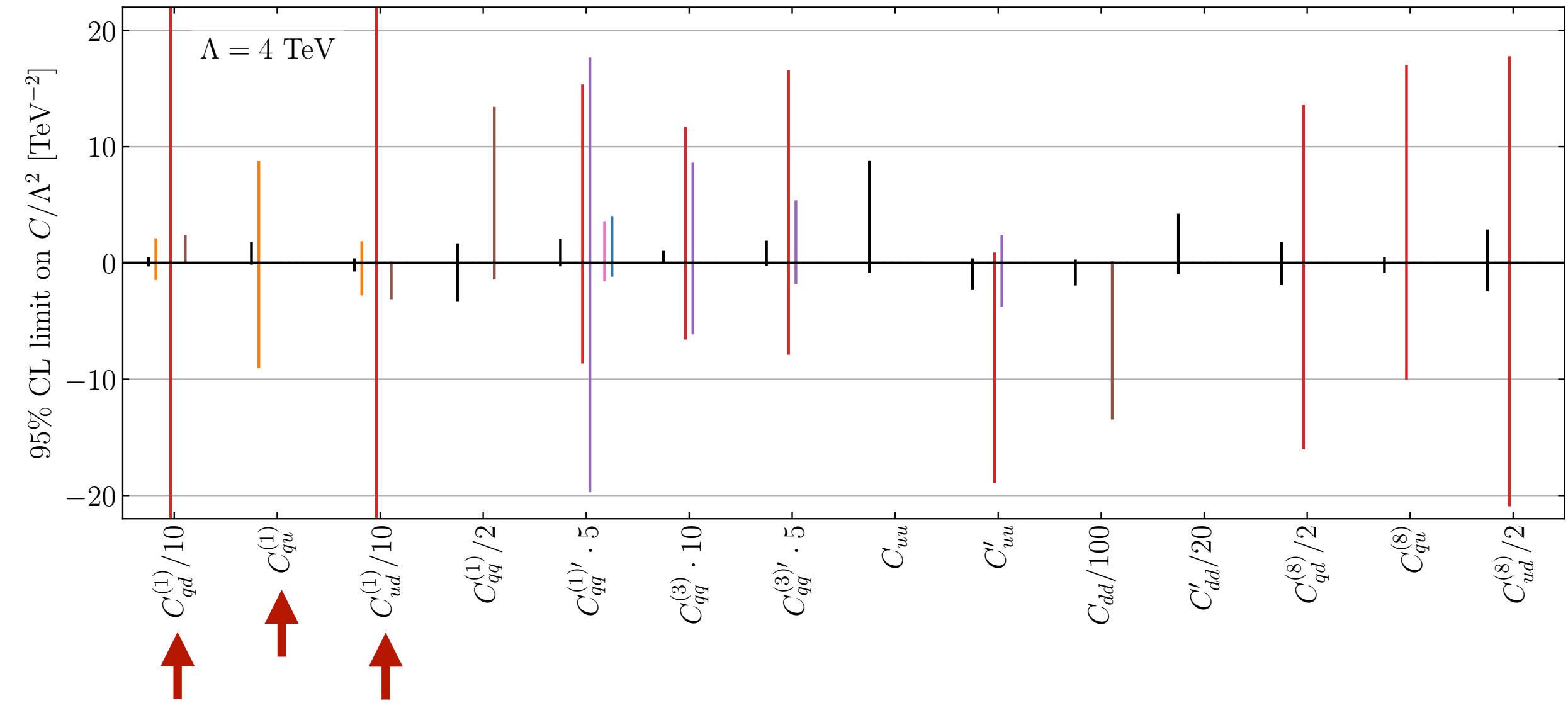
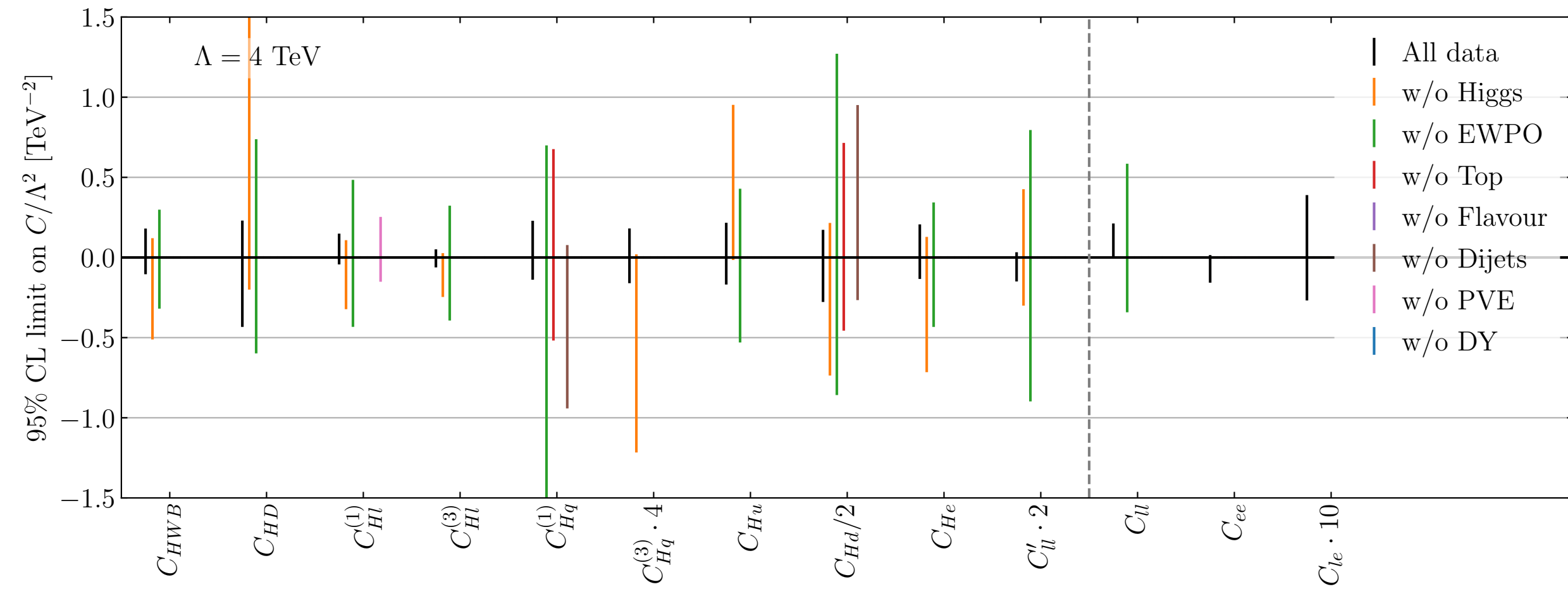
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- PVE impact on  $C_{Hl}^{(1)}$  and  $C_{qq}^{(1)'}$
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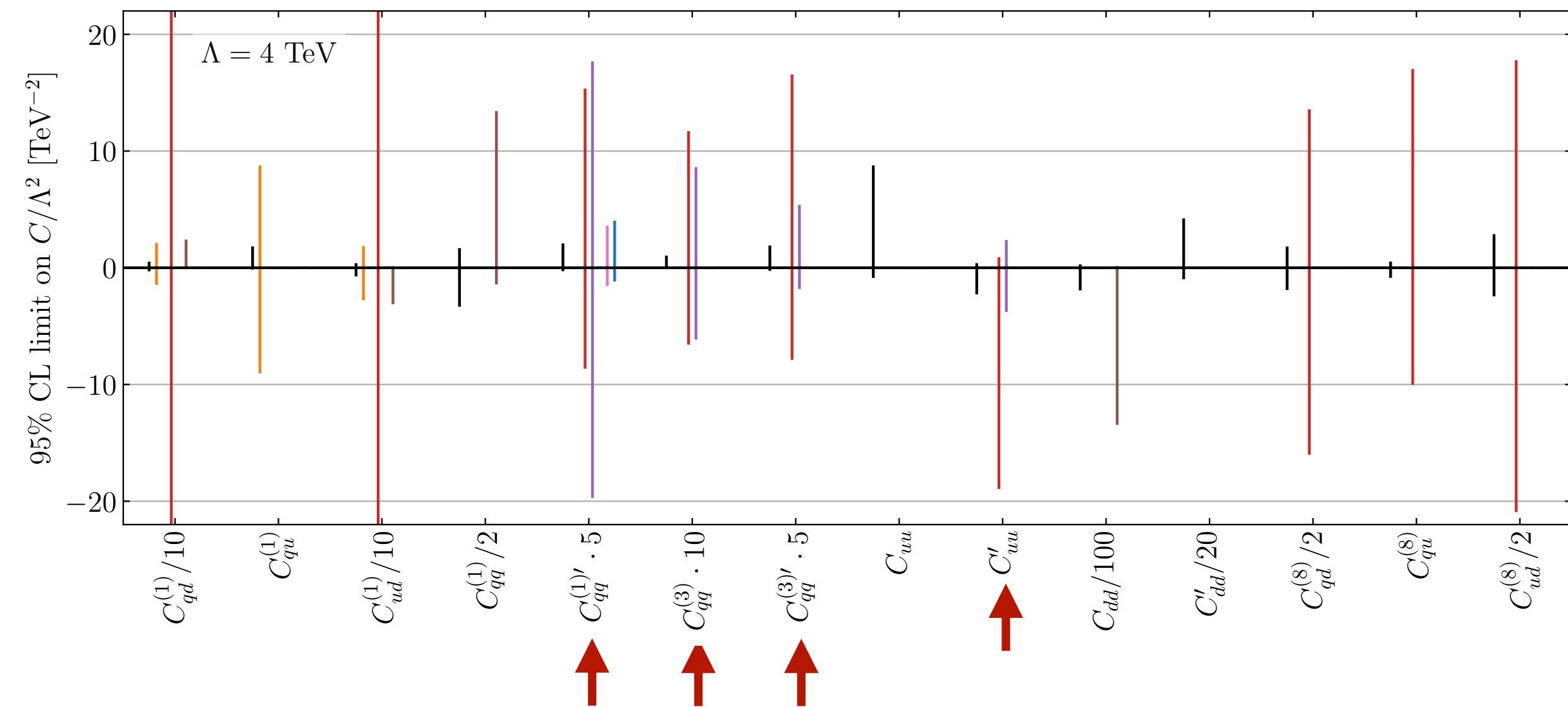
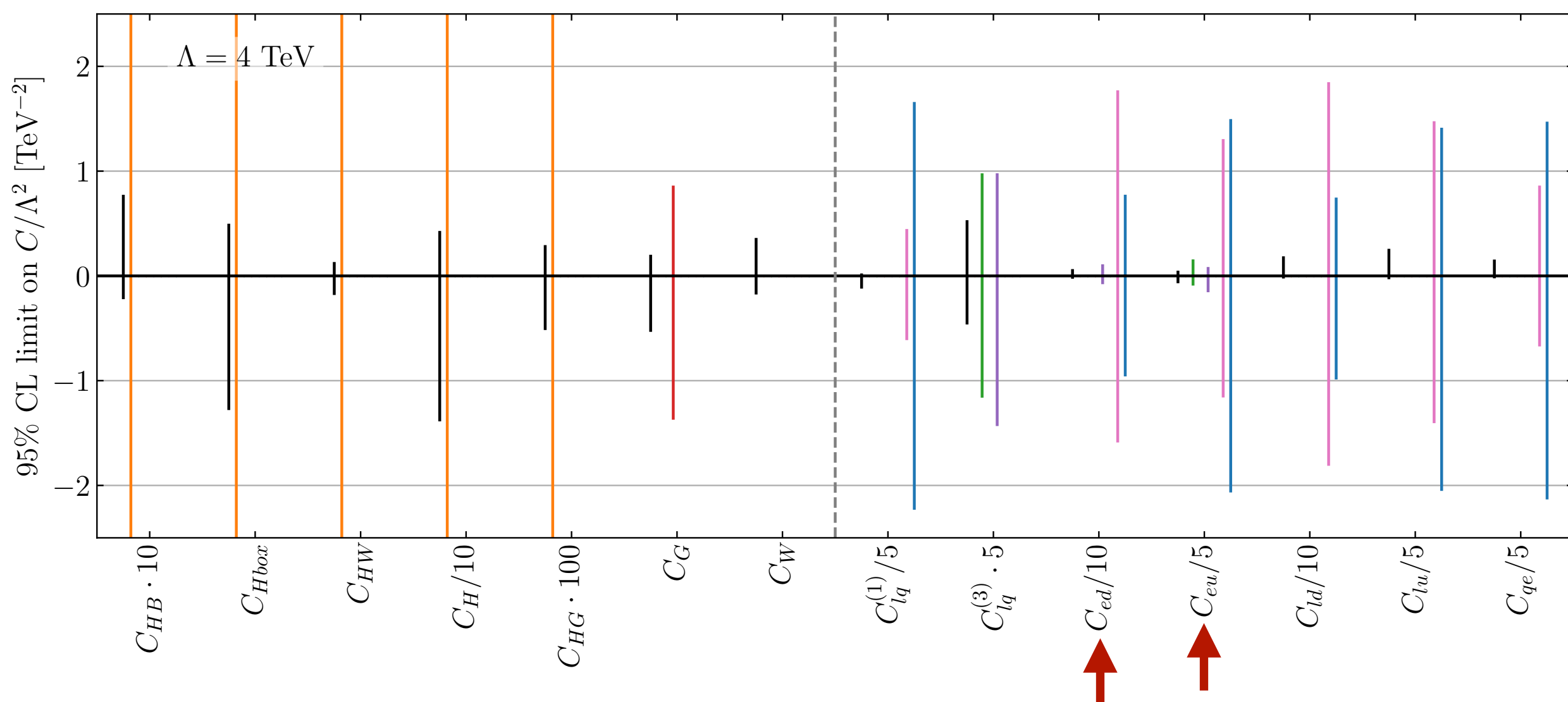
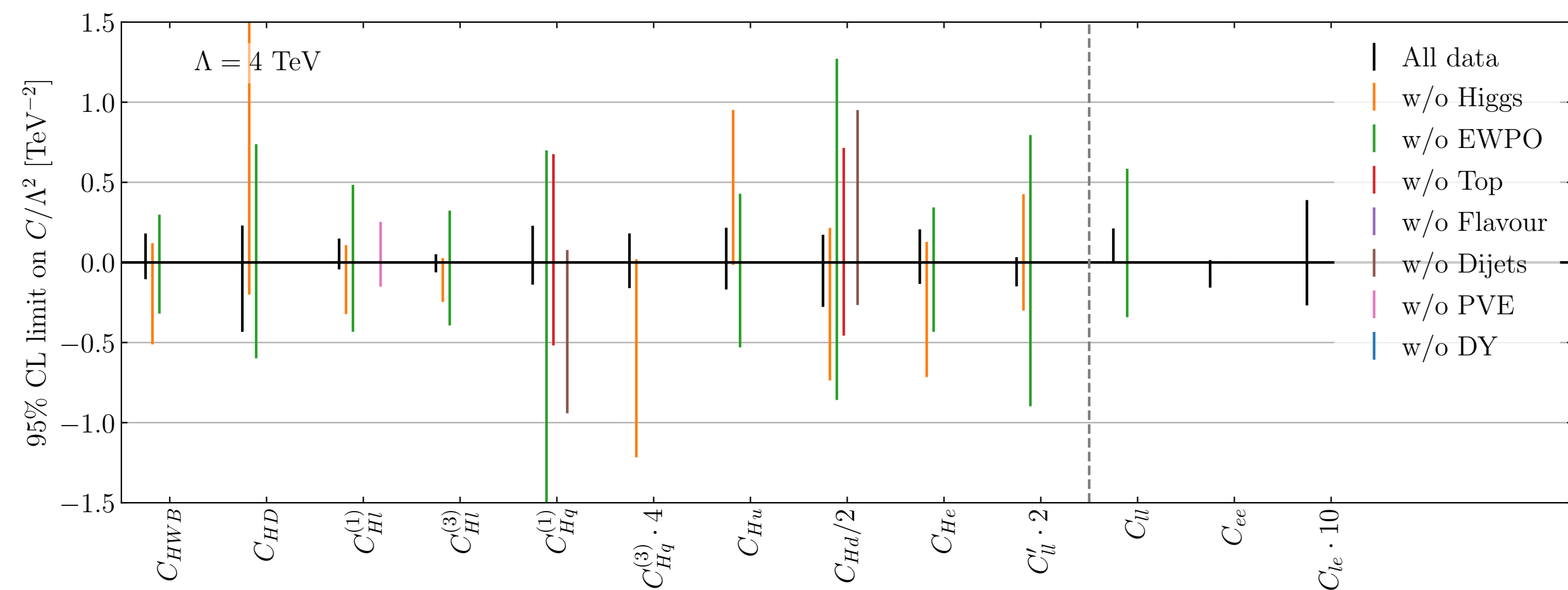


- PVE impact on  $C_{Hl}^{(1)}$  and  $C_{qq}^{(1)'}$
- NLO EWPO impact on  $C_{lq}^{(3)}$  and  $C_{lu}$
- NLO Top and Higgs impact on  $C_{qd}^{(1)}$ ,  $C_{qu}^{(1)}$  and  $C_{ud}^{(1)}$

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# Full results removing datasets

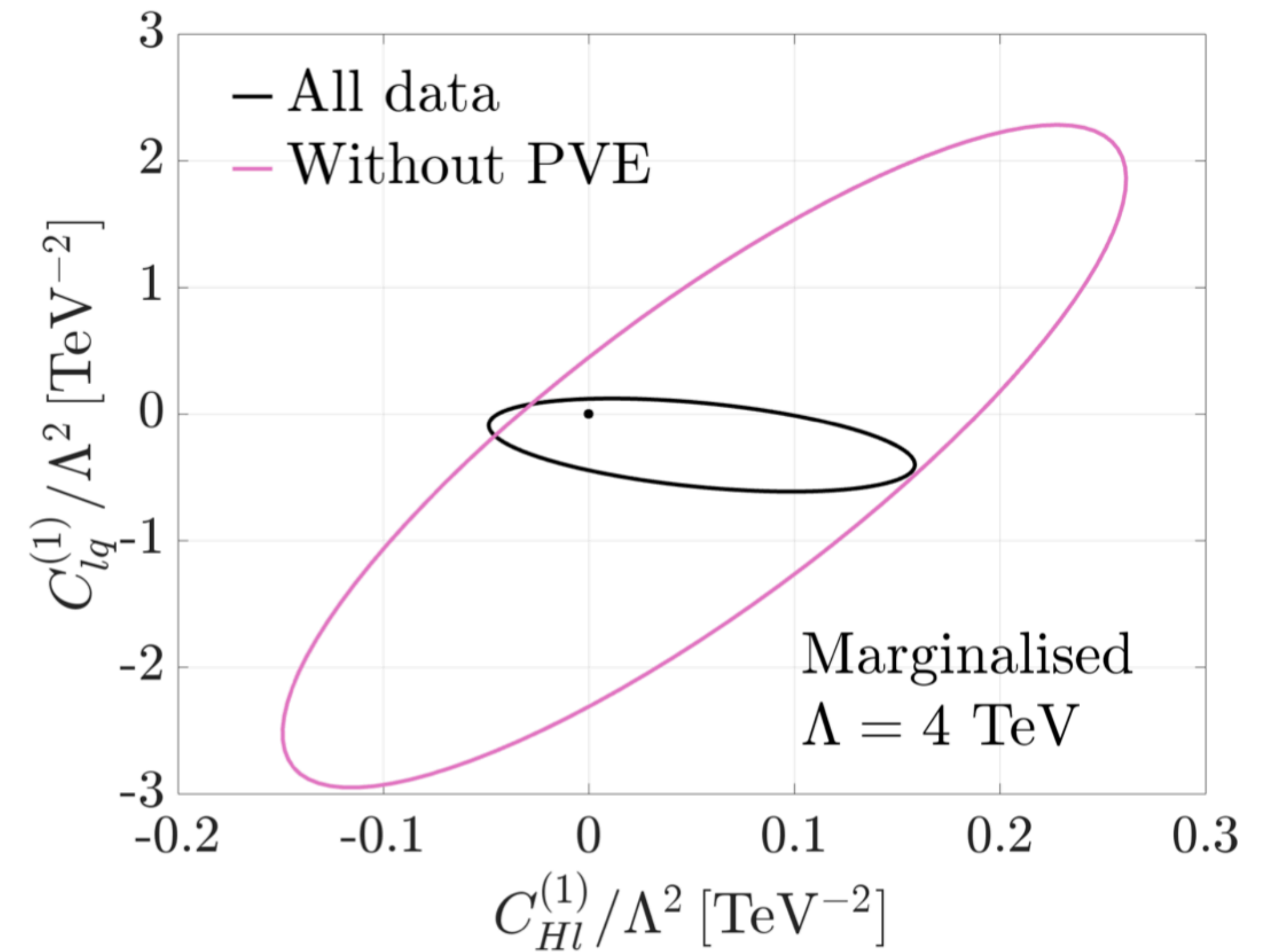
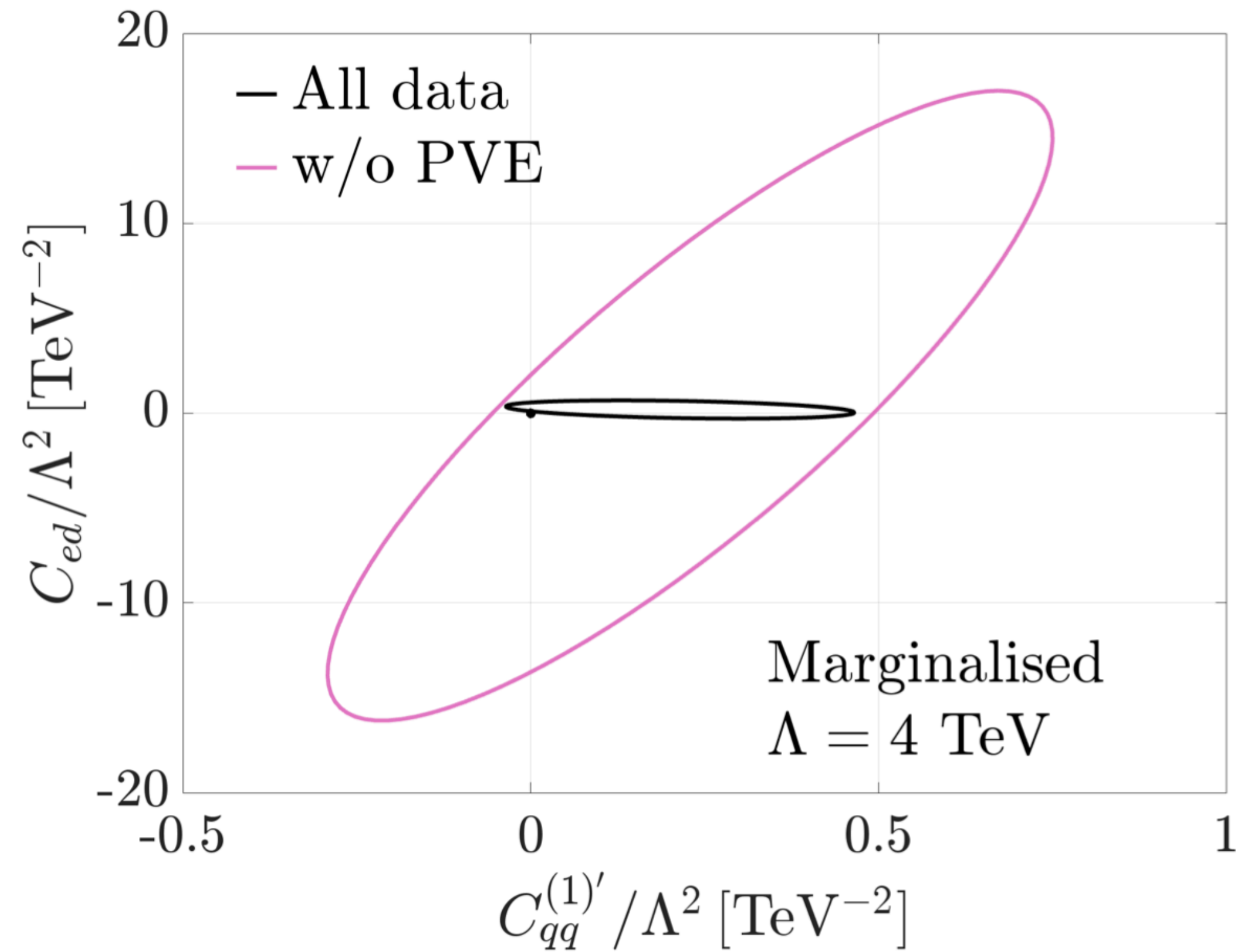


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- Flavour impact on semi-leptonic and 4-quark operators (more details later)

[2311.04963: RB, Biekötter, Hurth]

# PVE effects on the global fit

PVE bounds on  $C_{ed}$  and  $C_{lq}^{(1)}$  lifts the correlation of these operators with  $C_{qq}^{(1)'}$  and  $C_{Hl}^{(1)}$ .



# Warsaw basis

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
		$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		B-violating			
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s^k q_t^j)$	$Q_{duq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^{\gamma j})^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	$Q_{qqu}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jn} \varepsilon_{km} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{duu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$				

# Global analyses in the SMEFT

Many different global analyses have been performed:

## Combinations:

[arXiv:2304.12837: Grunwald, Hiller, Kröninger, Nollen]

[arXiv:1909.13632: Bißmann, Erdmann, Grunwald, Hiller, Kröninger]

[arXiv:2012.02779: Ellis, Madigan, Mimasu, Sanz, You]

[arXiv:2105.00006: Ethier et al.]

## Low energy:

[1706.03783: Falkowski, González-Alonso, Mimouni]

## Higgs-EW:

[1812.07587: Biekötter, Corbett, Plehn]

[1908.03952: Kraml, Quang Loc, Thi Nhung, Duc Ninh]

[2007.01296: Dawson, Homiller, D. Lane]

[2007.01296: Eduardo da Silva Almeida, et al.]

## Top:

[arXiv:1512.03360: Andy Buckley, et al.]

[arXiv:1802.07237: J. A. Aguilar Saavedra, et al.]

[arXiv:1910.03606: I. Brivio, et al.]

[arXiv:2212.05067: Brivio et al.]

## Flavour:

[arXiv:2101.07273: Bruggisser, Schäfer, van Dyk, Westhoff]

[arXiv:2003.05432: Aoude, Hurth, Renner, Shepherd]

## Experiments:

ATL-PHYS-PUB-2022-037

CMS-PAS-SMP-24-003

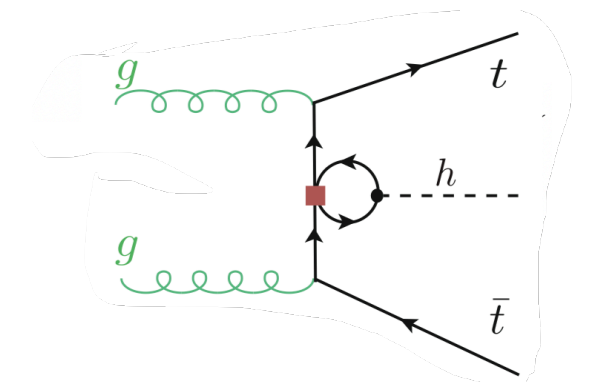
and many others...

In particular in this talk:

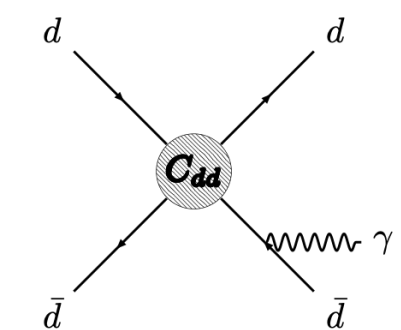
- The operator selection comes purely from symmetry assumptions

$$U(3)^5 = U(3)_\ell \times U(3)_q \times U(3)_e \times U(3)_u \times U(3)_d$$

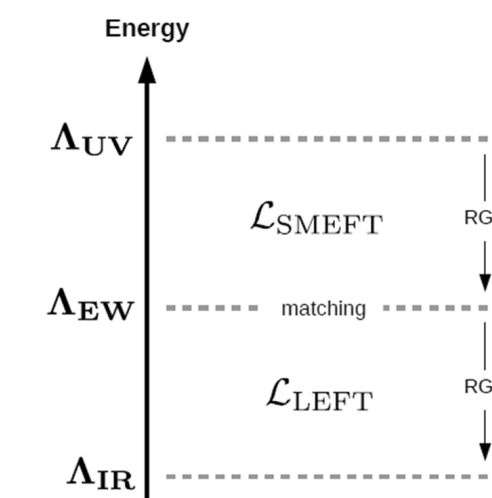
- Inclusion of NLO observables in a global fit without flat directions



- Inclusion of dijet observables below 1.1 TeV



- Inclusion of RGE effects in global analysis.



# Flavour symmetris in the SMEFT

Class	Operators	No symmetry				$U(3)^5$					
		3 Gen.		1 Gen.		Exact		$\mathcal{O}(Y_{e,d,u}^1)$		$\mathcal{O}(Y_e^1, Y_d^1 Y_u^2)$	
1–4	$X^3, H^6, H^4 D^2, X^2 H^2$	9	6	9	6	9	6	9	6	9	6
5	$\psi^2 H^3$	27	27	3	3	–	–	3	3	4	4
6	$\psi^2 X H$	72	72	8	8	–	–	8	8	11	11
7	$\psi^2 H^2 D$	51	30	8	1	7	–	7	–	11	1
8	$(\bar{L}L)(\bar{L}L)$	171	126	5	–	8	–	8	–	14	–
	$(\bar{R}R)(\bar{R}R)$	255	195	7	–	9	–	9	–	14	–
	$(\bar{L}L)(\bar{R}R)$	360	288	8	–	8	–	8	–	18	–
	$(\bar{L}R)(\bar{R}L)$	81	81	1	1	–	–	–	–	–	–
	$(\bar{L}R)(\bar{L}R)$	324	324	4	4	–	–	–	–	4	4
<b>total:</b>		1350	1149	53	23	41	6	52	17	85	26

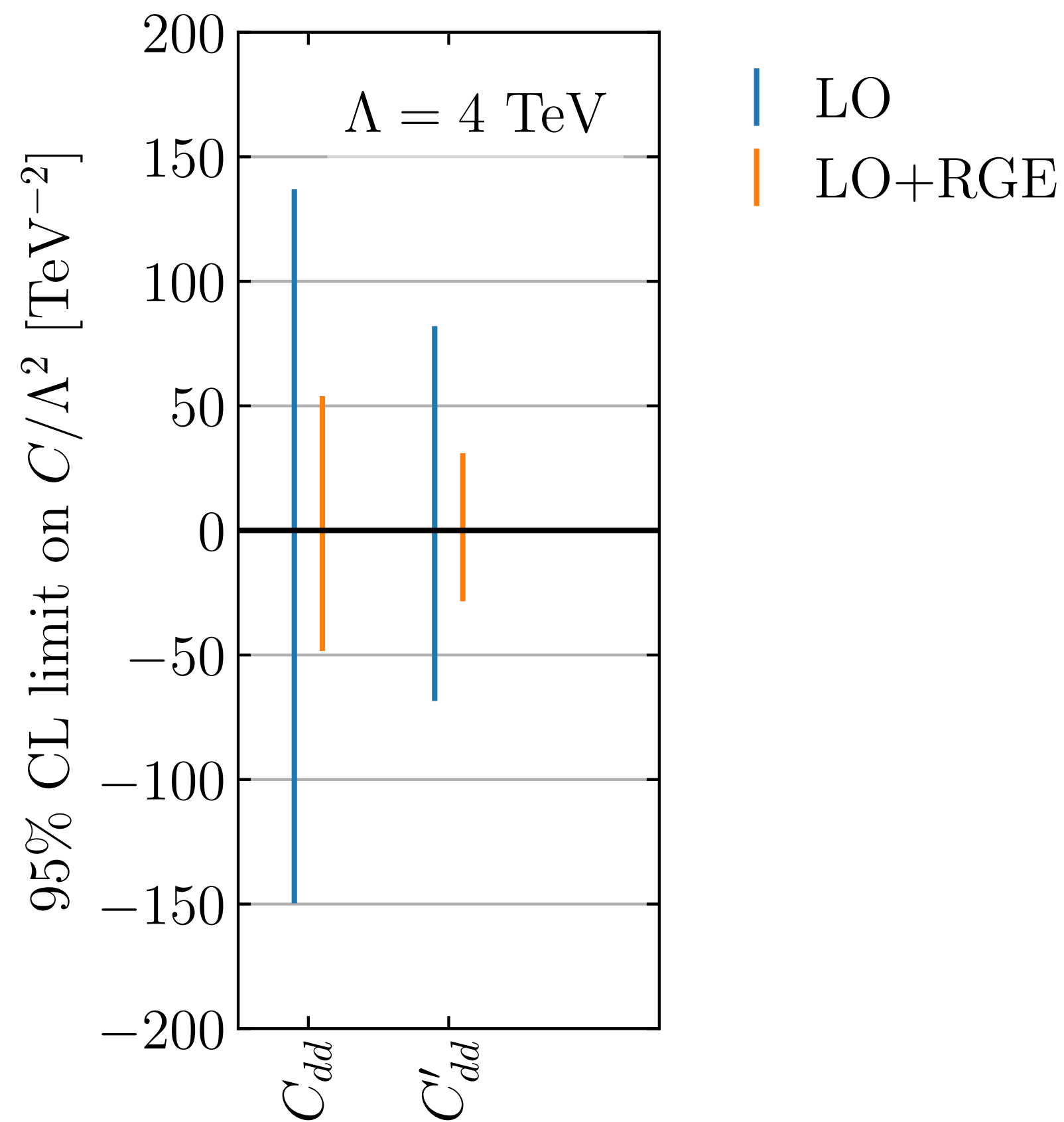
Table 1: Number of independent operators in  $U(3)^5$ , MFV and without symmetry. In each column the left (right) number corresponds to the number of CP-even (CP-odd) coefficients.  $\mathcal{O}(X^n)$  stands for including terms up to  $\mathcal{O}(X^n)$ .

[2005.05366: Faroughy, Isidori, Wilsch, Yamamoto]

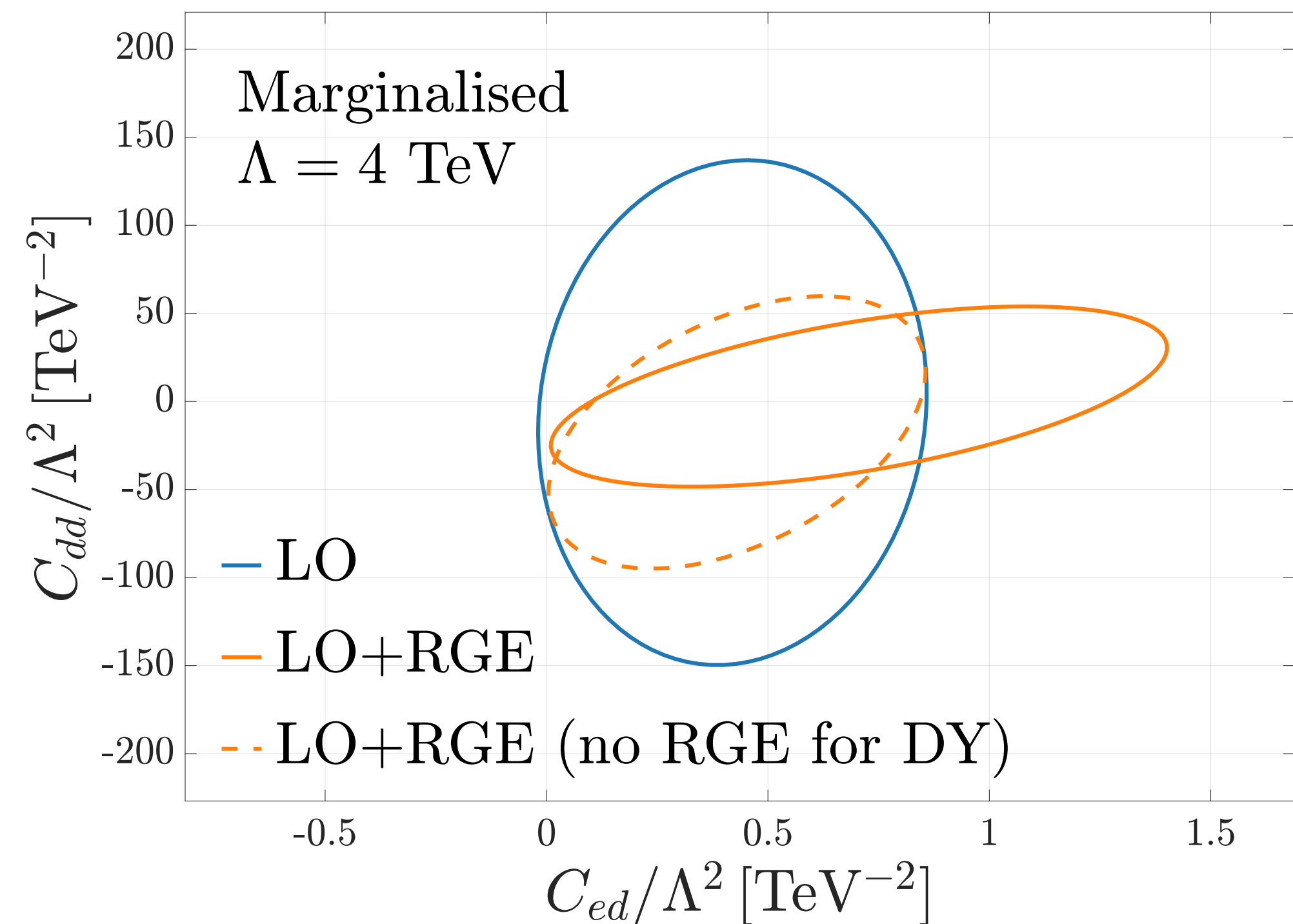
# RGE effects on the global analysis

## Non-diagonal running effect:

The weakly constrained operators  $C_{dd}$  and  $C'_{dd}$  run in the operators  $C_{ed}$  and  $C_{ld}$  which are well constrained by Drell-Yan.



$$C_{ed}(\mu_{EW}) = -0.03 C_{dd}(\mu_{\Lambda}) - 0.01 C'_{dd}(\mu_{\Lambda})$$



# Models compatible with our assumption

These scalar extensions of the SM match at 1-loop only on flavour symmetric operators:

**Complex colour sextet, isospin singlet:**  $\chi_3 \equiv (6_C, 1_L, -\frac{2}{3}|_Y)$

$$\mathcal{L}_{\chi_3} = \mathcal{L}_{\text{SM}}^{d \leq 4} + (D_\mu \chi_3)^\dagger (D^\mu \chi_3) - m_{\chi_3}^2 \chi_3^\dagger \chi_3 - \eta_{\chi_3} H^\dagger H \chi_3^\dagger \chi_3 - \lambda_{\chi_3} (\chi_3^\dagger \chi_3)^2 \\ - \left\{ y_{\chi_3} \left( d_R^{\{A\}} \right)^T C (\chi_3^{AB})^\dagger d_R^{\{B\}} + \text{h.c.} \right\} \square$$

**Complex Singlet:**  $\mathcal{S}_2 \equiv (1_C, 1_L, 2|_Y)$

$$\mathcal{L}_{\mathcal{S}_2} = \mathcal{L}_{\text{SM}}^{d \leq 4} + (D_\mu \mathcal{S}_2)^\dagger (D^\mu \mathcal{S}_2) - m_{\mathcal{S}_2}^2 \mathcal{S}_2^\dagger \mathcal{S}_2 - \eta_{\mathcal{S}_2} |H|^2 |\mathcal{S}_2|^2 - \lambda_{\mathcal{S}_2} |\mathcal{S}_2|^4 \\ - \left\{ y_{\mathcal{S}_2} e_R^T C e_R \mathcal{S}_2 + \text{h.c.} \right\} \square$$

**Complex colour triplet, isospin singlet:**  $\varphi_2 \equiv (3_C, 1_L, -\frac{4}{3}|_Y)$

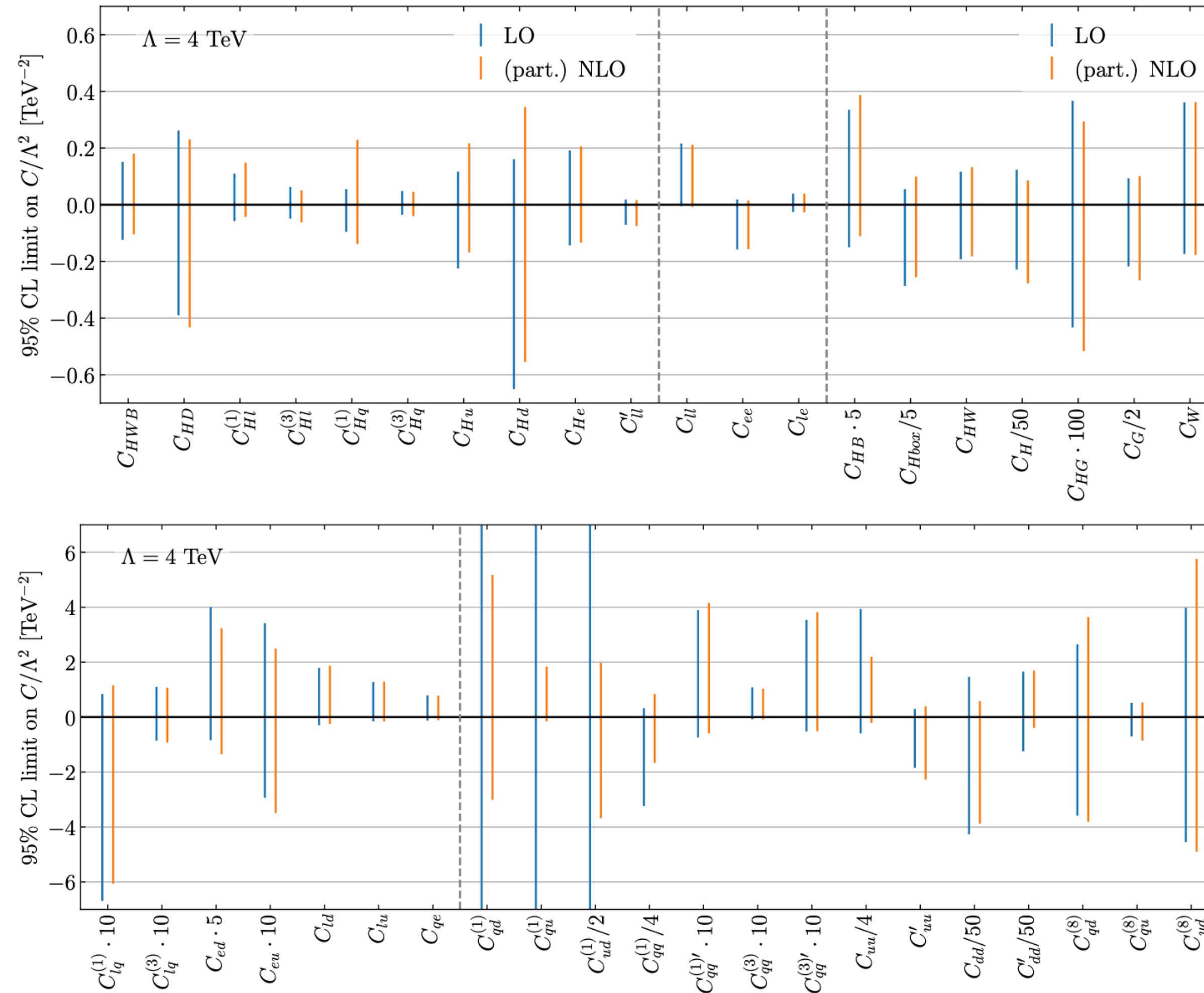
$$\mathcal{L}_{\varphi_2} = \mathcal{L}_{\text{SM}}^{d \leq 4} + (D_\mu \varphi_2)^\dagger (D^\mu \varphi_2) - m_{\varphi_2}^2 \varphi_2^\dagger \varphi_2 - \eta_{\varphi_2} H^\dagger H \varphi_2^\dagger \varphi_2 - \lambda_{\varphi_2} (\varphi_2^\dagger \varphi_2)^2 \\ + \left\{ y_{\varphi_2} \varphi_2^{\alpha \dagger} d_R^{\alpha T} C e_R + \text{h.c.} \right\} \square$$

[arXiv:2111.05876: Anisha, Das Bakshi, Banerjee, Biekötter, Chakraborty, Patra, Spannowsky]

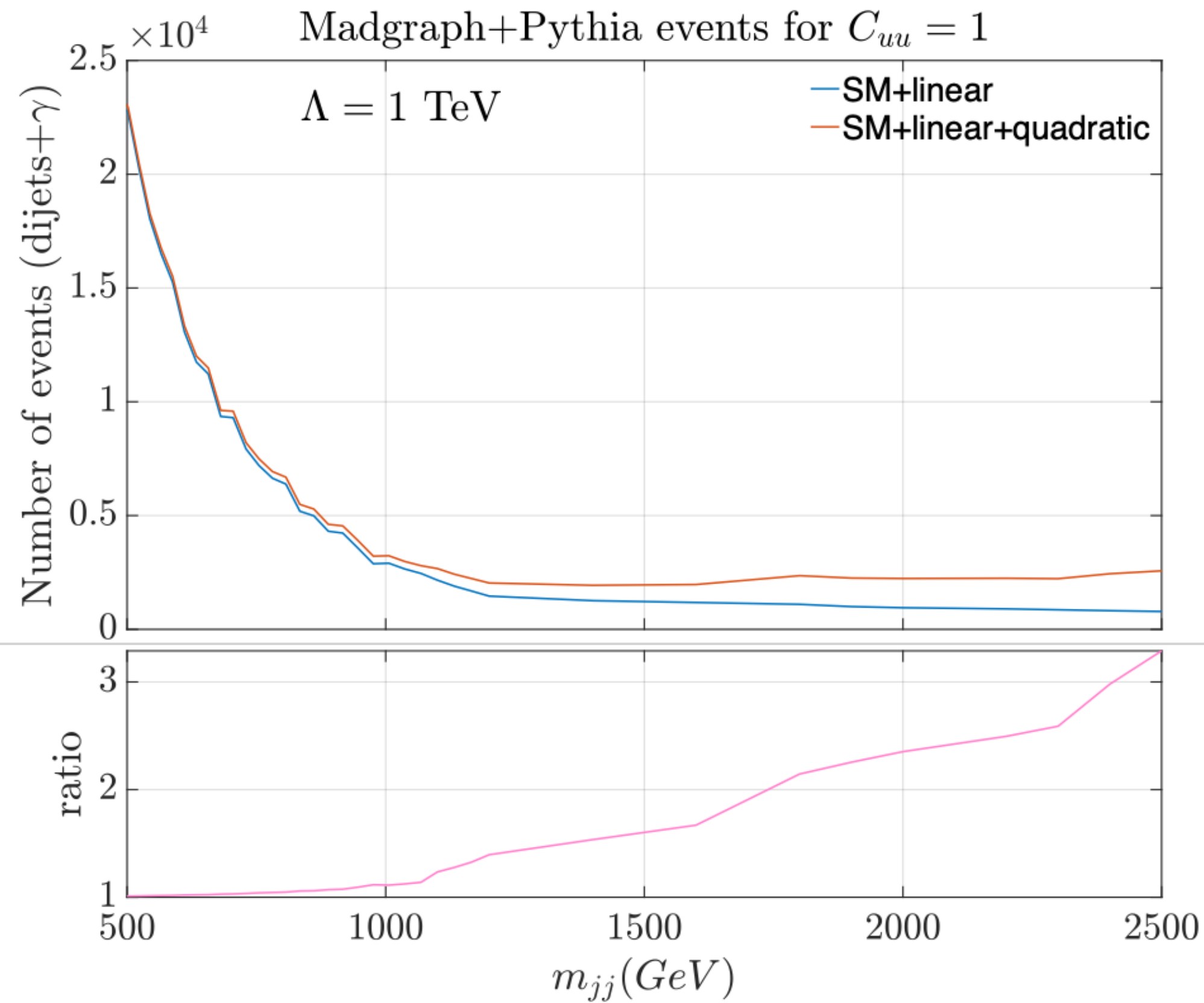




# Full LO vs NLO results



While dijets are powerful for probing the unbounded 4-quark operators, due to trigger thresholds at LHC **only very high energy** data are available.

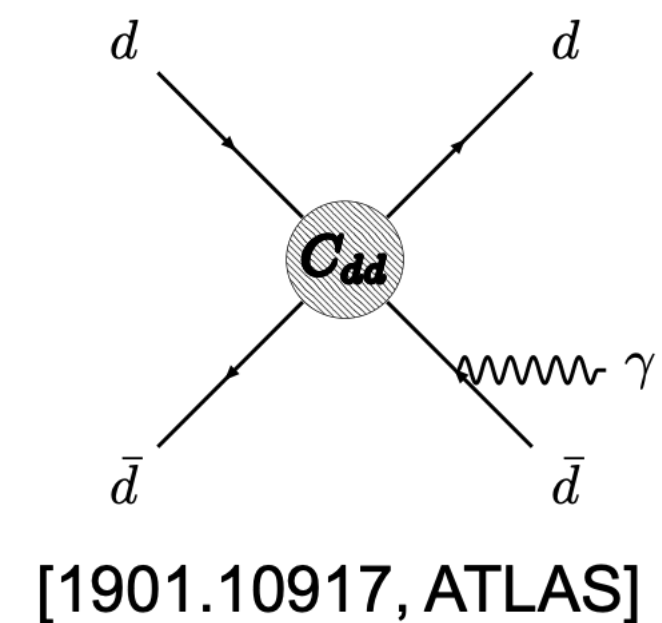


$$\sigma \propto \frac{|C_{dd}|^2}{\Lambda^4} s$$

Energy squared enhancement for quadratic contributions

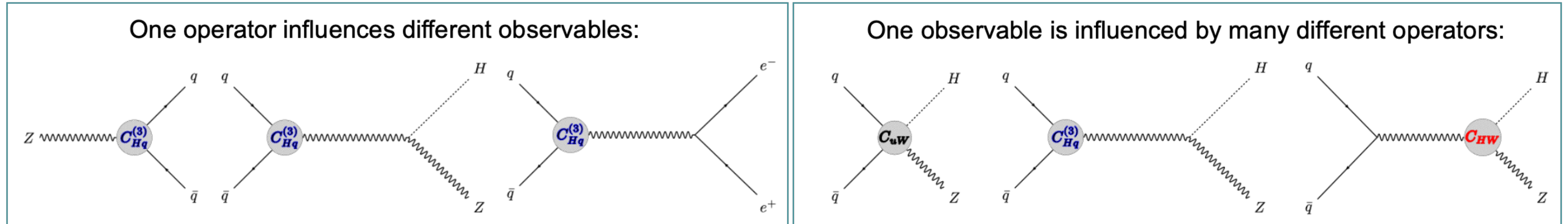
At high energies, it is no longer possible to neglect  $1/\Lambda^4$  terms, and dimension 8 operators also become relevant

Therefore, we utilise a different process: **dijets+ $\gamma$**  production. This allows us probe the dijet invariant mass range **below 1.1 TeV**.



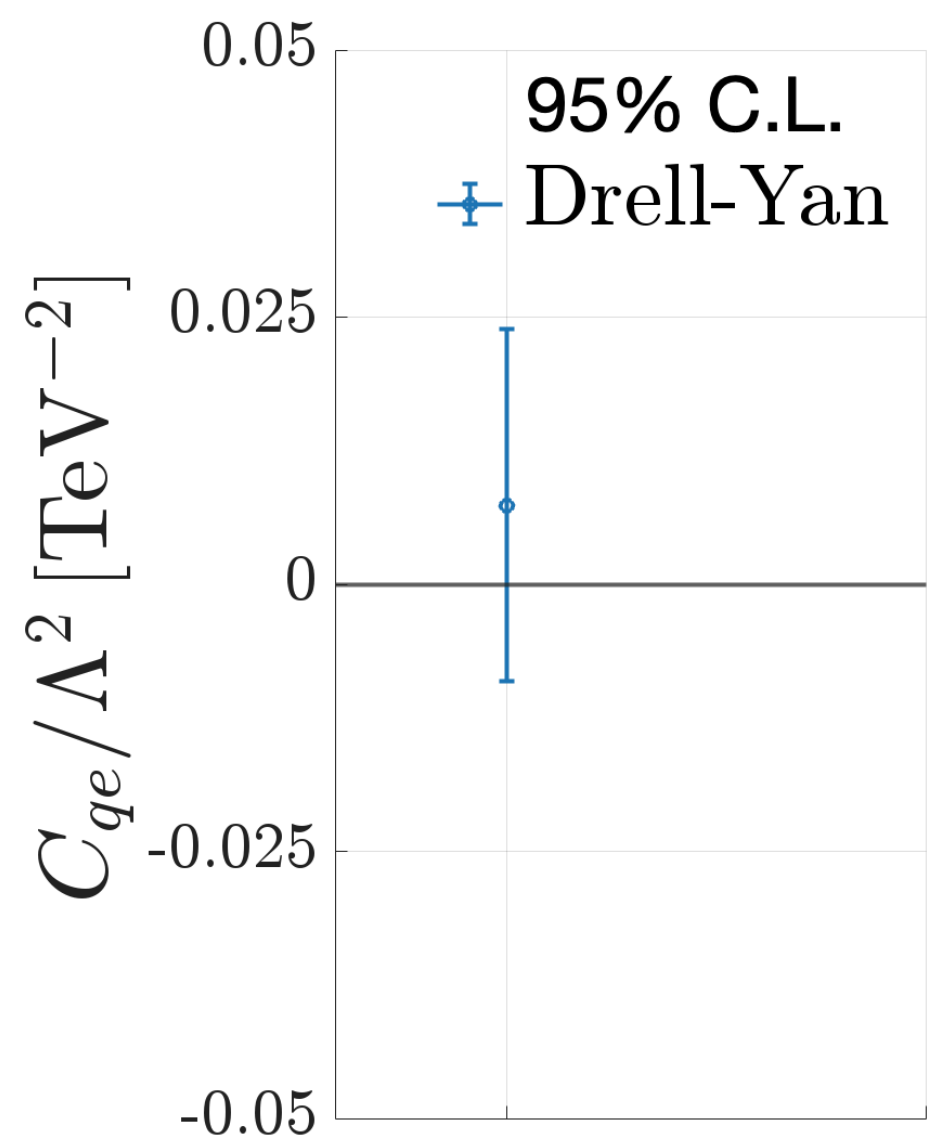
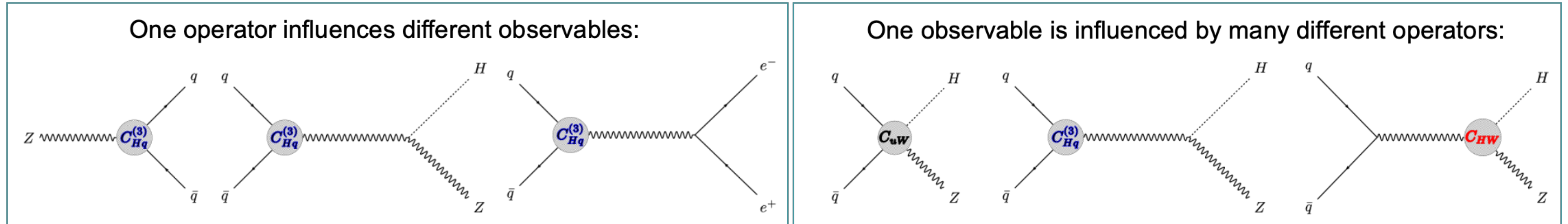
# Global analyses in the SMEFT

Wilson coefficients in SMEFT are **highly correlated** and only **global analysis** can give meaningful results.



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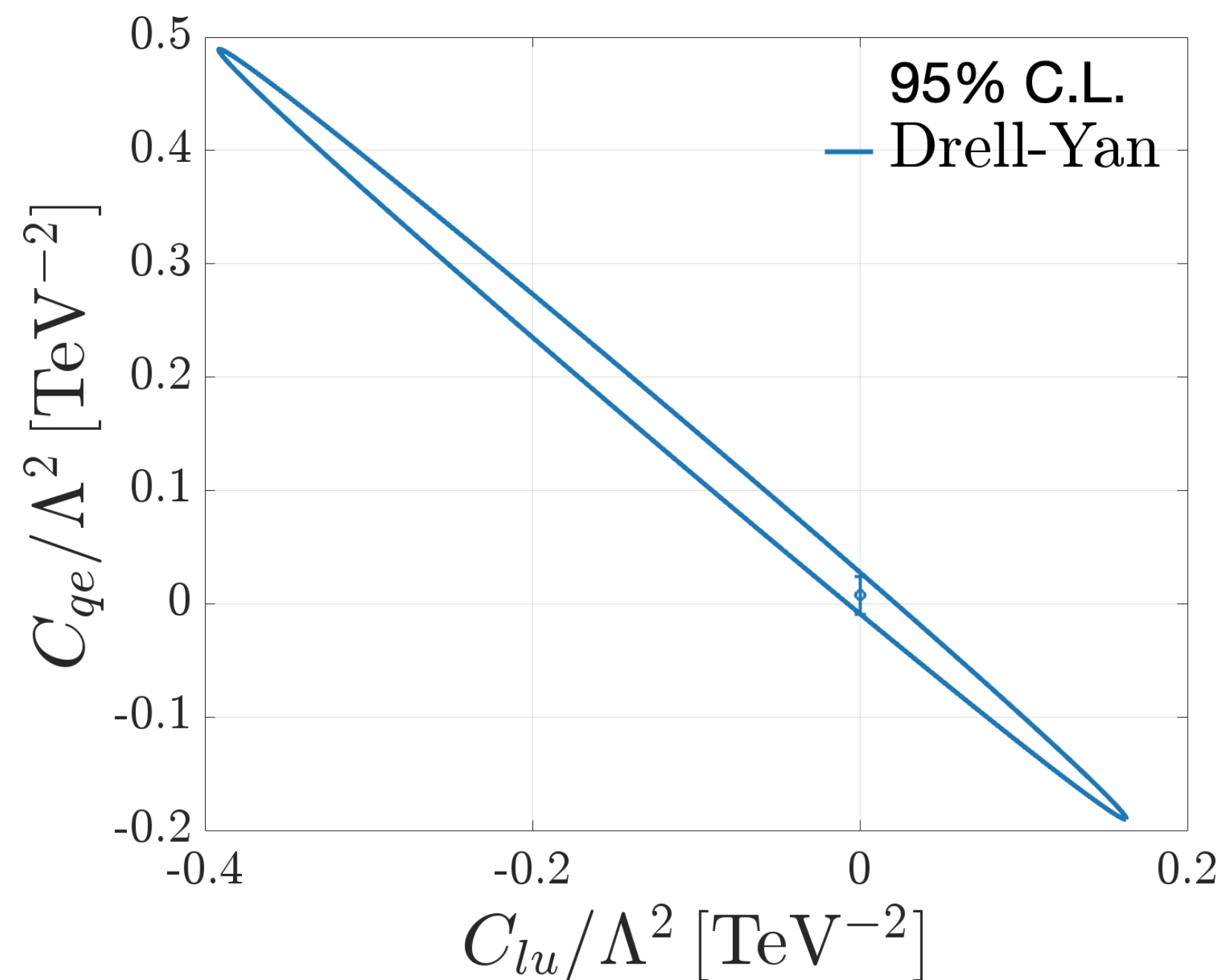
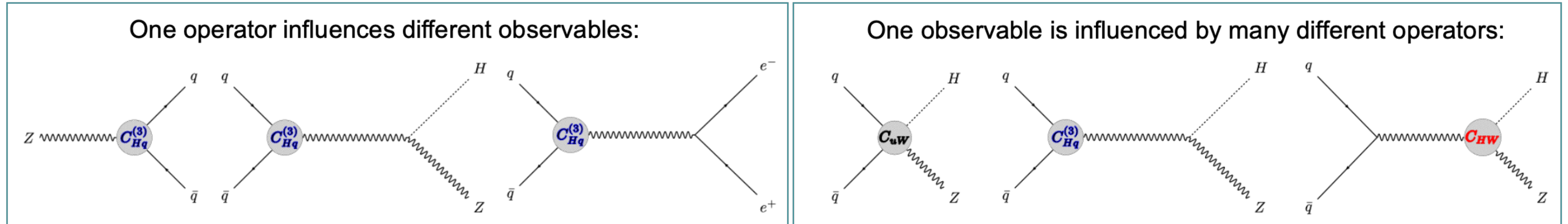
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[2311.04963: RB, Biekötter, Hurth]  
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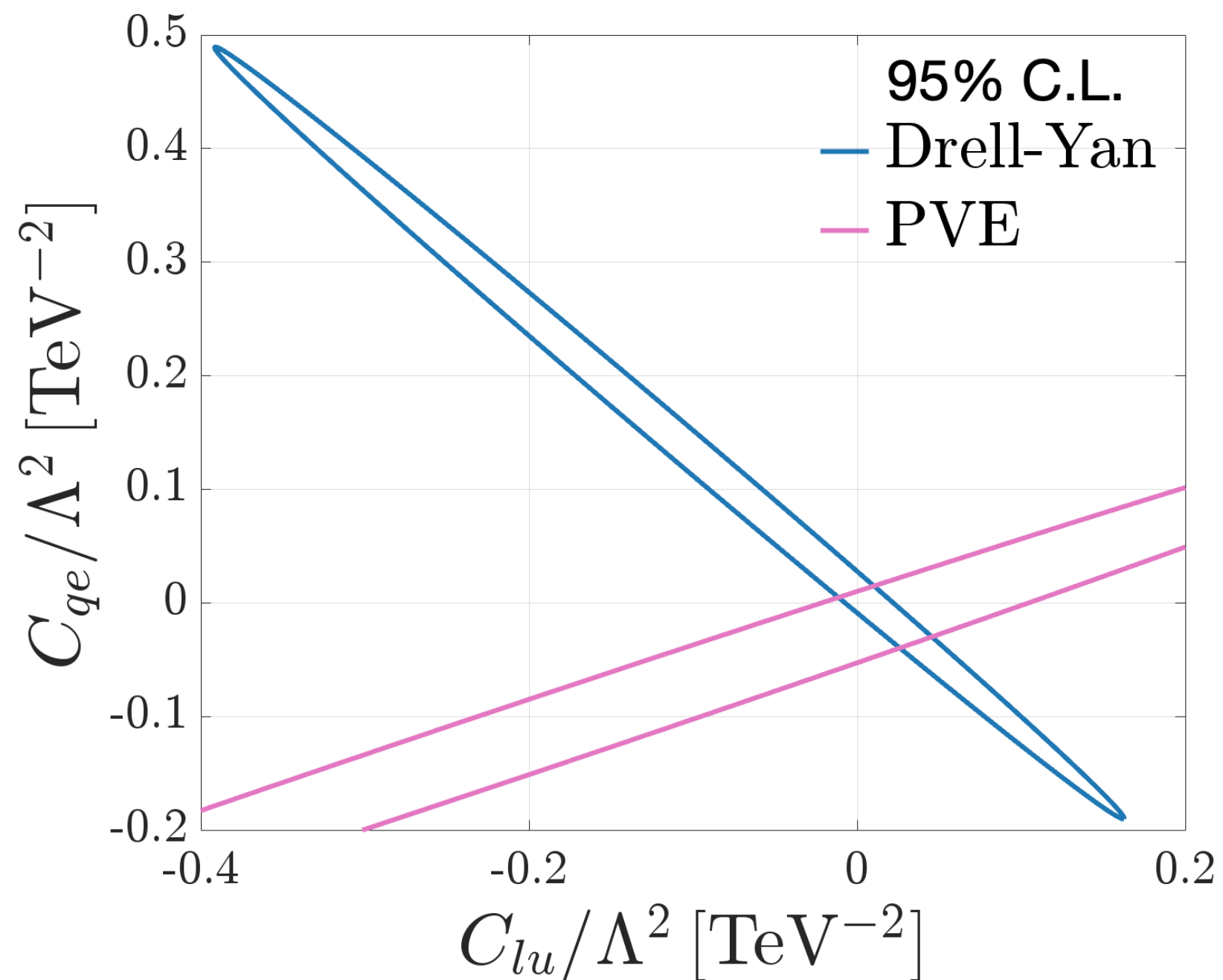
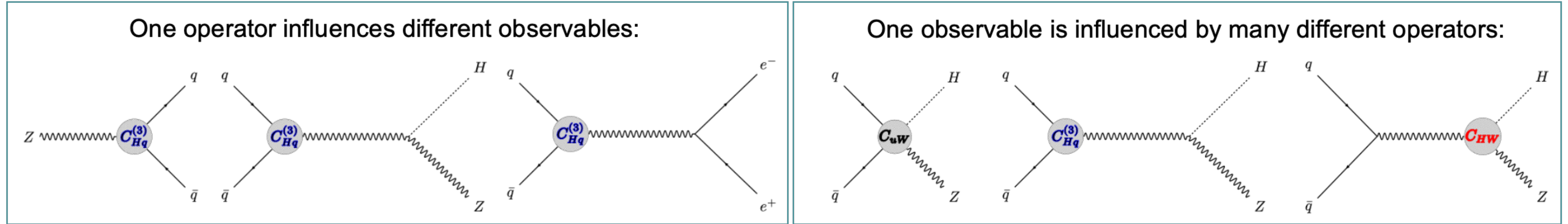
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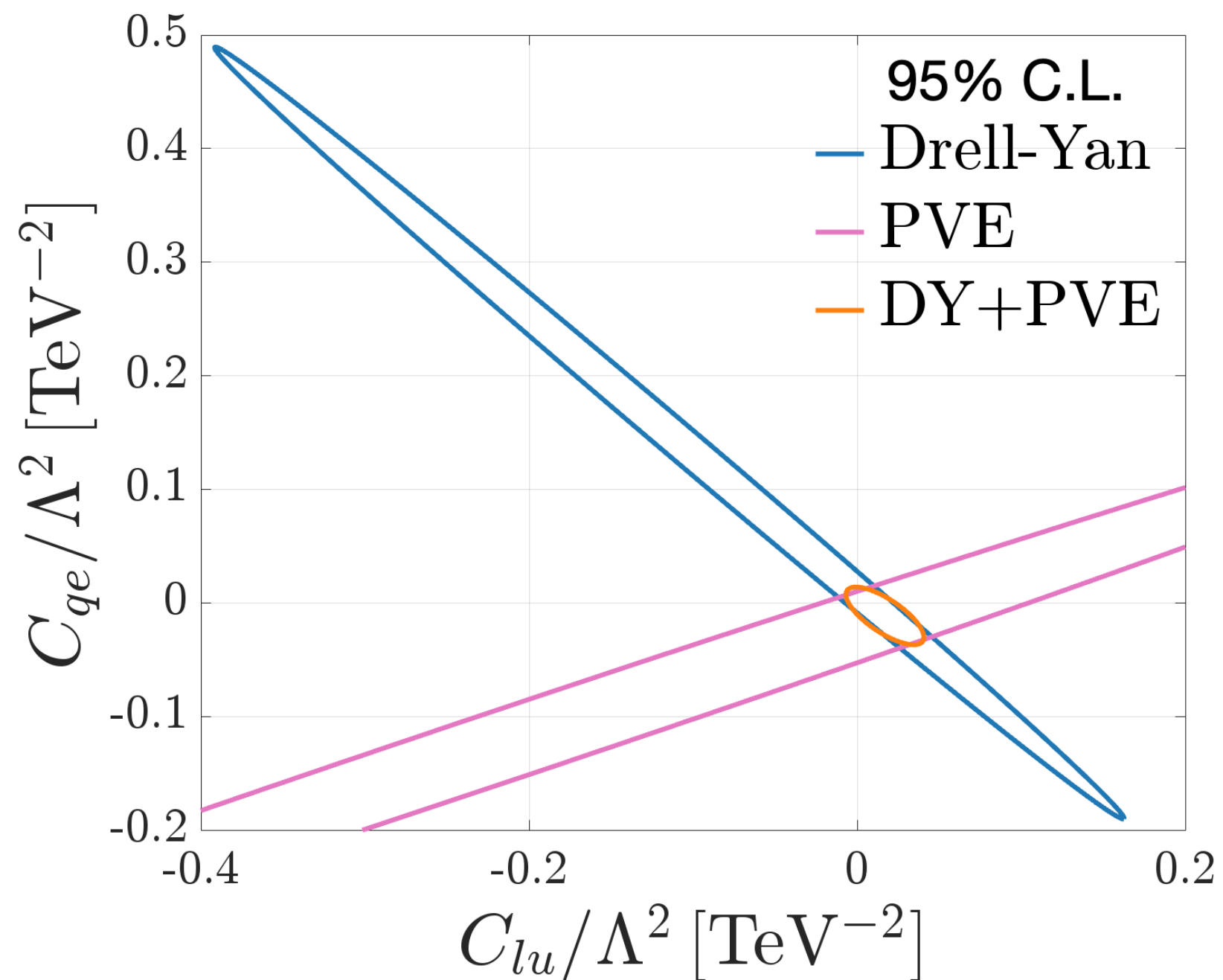
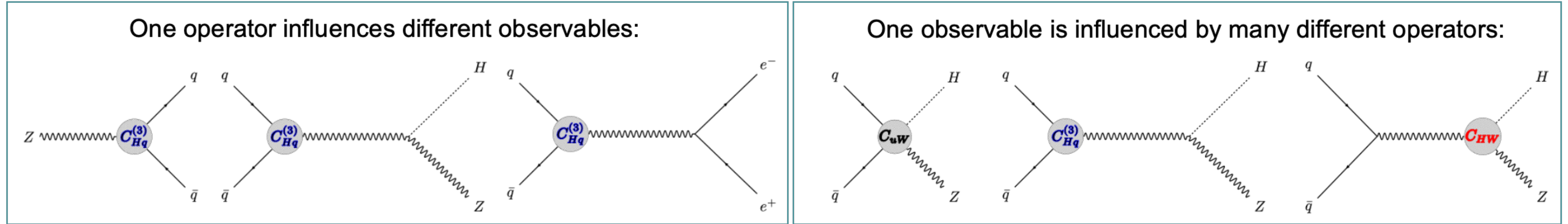
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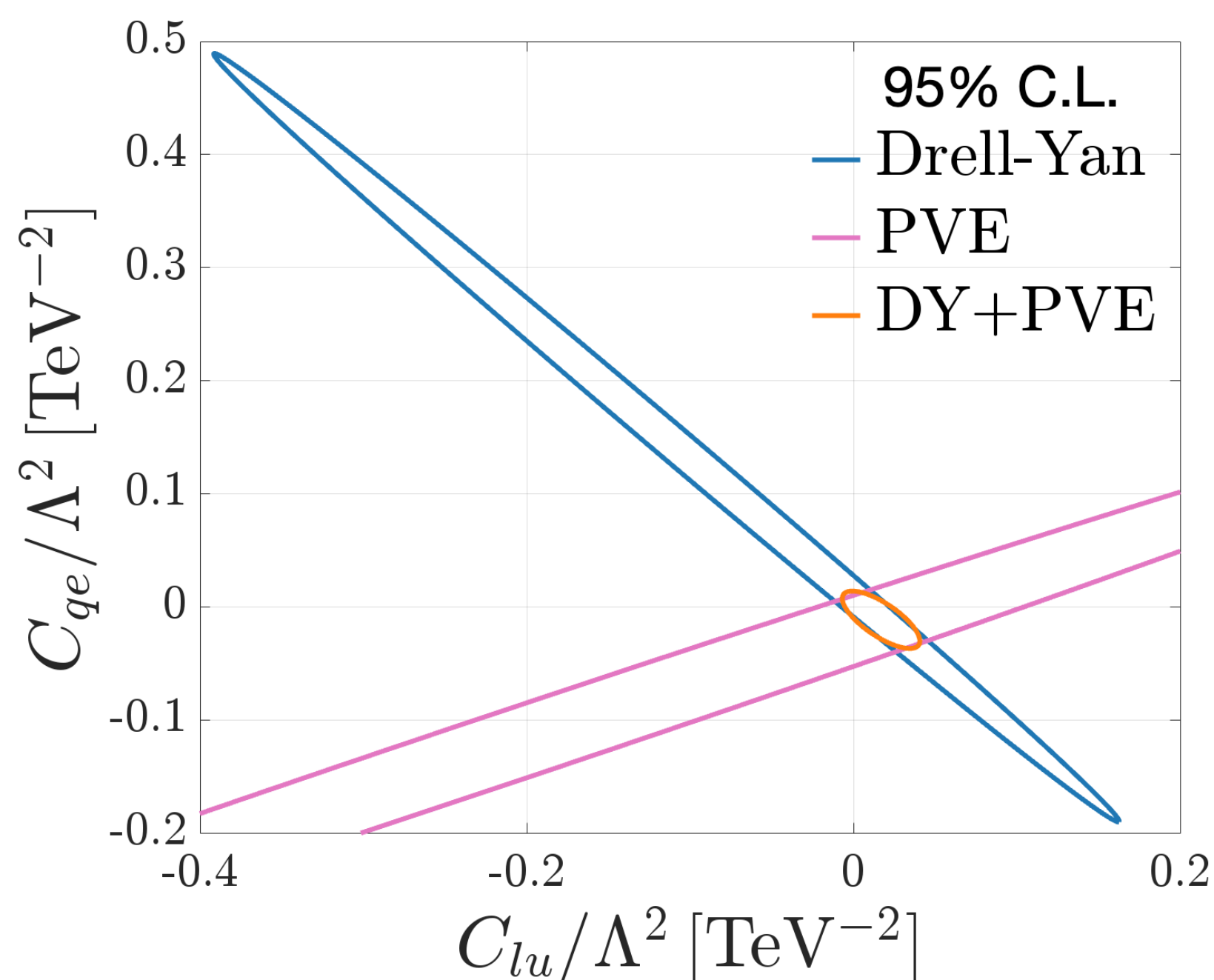
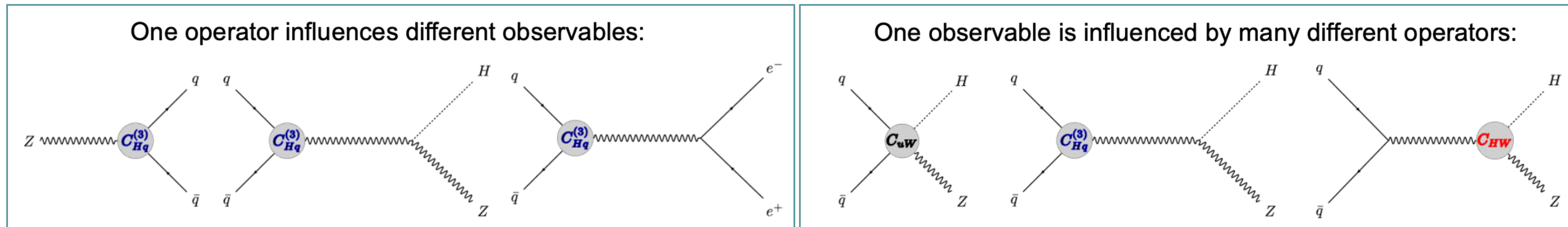
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**Goal:** Constrain all the possible directions  
(linear combinations of Wilson coefficients)

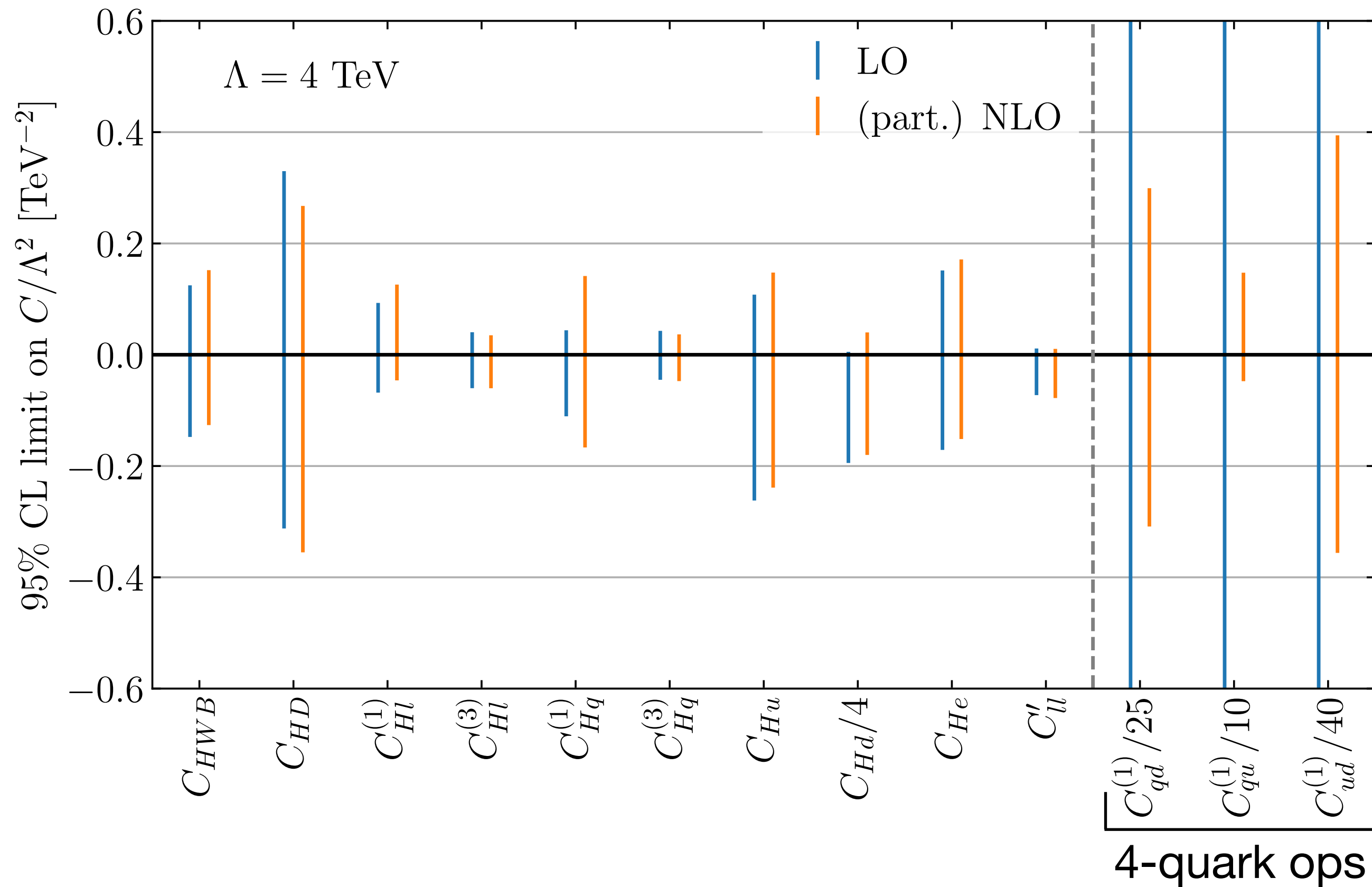
High and low  
energy data

Identify  
correlations



# LO vs NLO fit

[2311.04963: RB, Biekötter, Hurth]



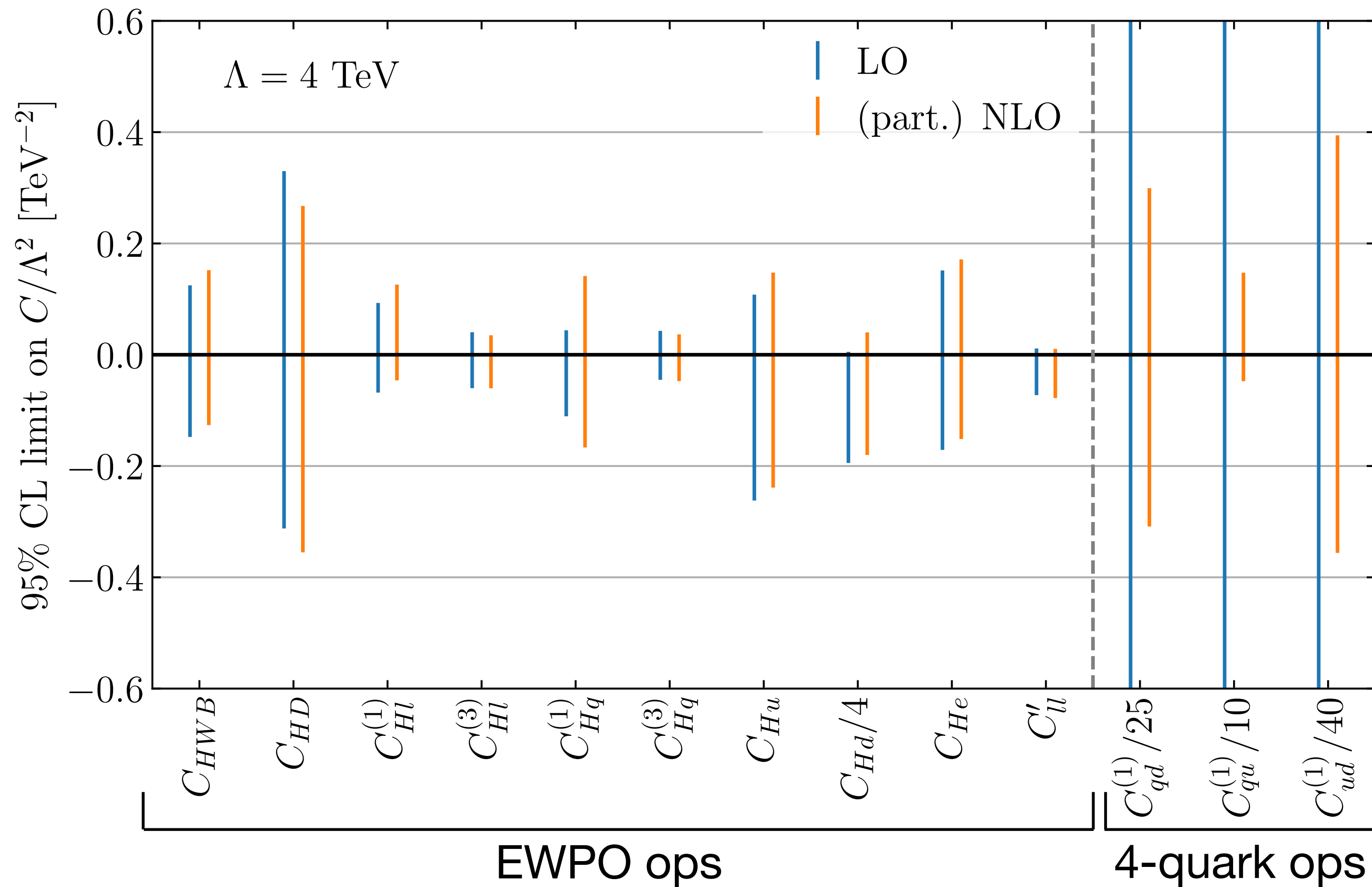
- Some operators, poorly constrained using only LO observables, result much better bounded when NLO observables are included.

Constraints on  $C_{qu}^{(1)}$  at LO: Dijets

Constraints on  $C_{qu}^{(1)}$  at LO+NLO: Dijets, Higgs, EWPO, Top

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Constraints on  $C_{qu}^{(1)}$  at LO+NLO: Dijets, Higgs, EWPO, Top

- Even after the inclusion of NLO predictions for EWPO observables, the bounds on EW operators did not significantly change.

Number of operators occurring in EWPO at LO: 10

Number of operators occurring in EWPO at NLO: 35

# RGE impact on 1D bounds

