

Studies of CP violation at Belle and Belle II

Radek Žlebčik

on behalf of the Belle II collaboration

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DISCRETE 2024

Ljubljana, Slovenia

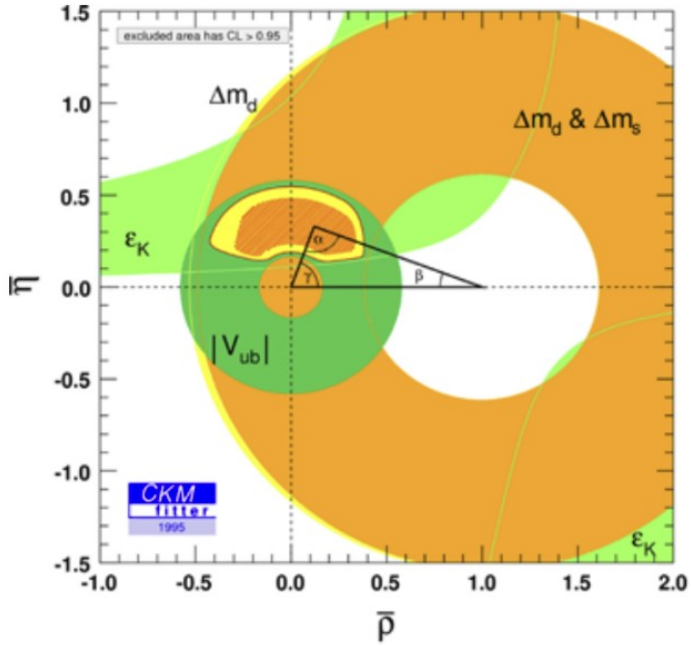


Unitarity triangle : 30 years of development

- Unitarity Triangle constructed from CKM matrix has angles and sides which are well-defined (physics) quantities

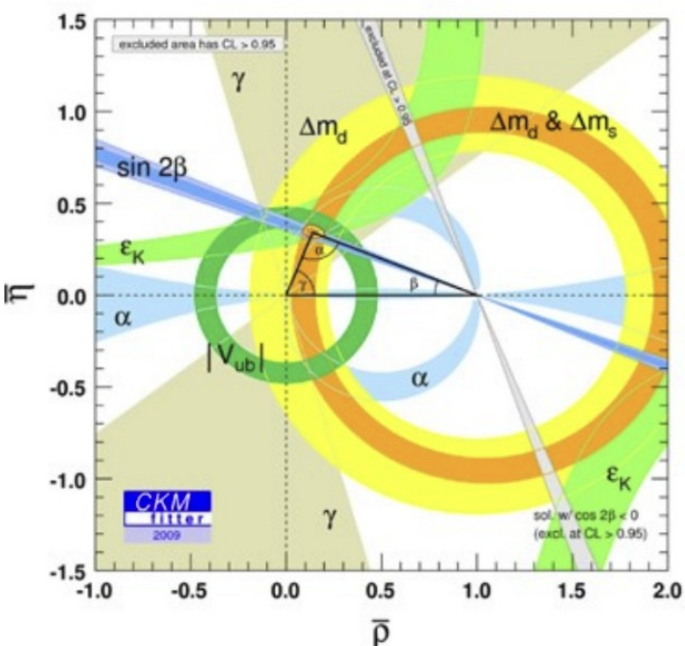
$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

1995



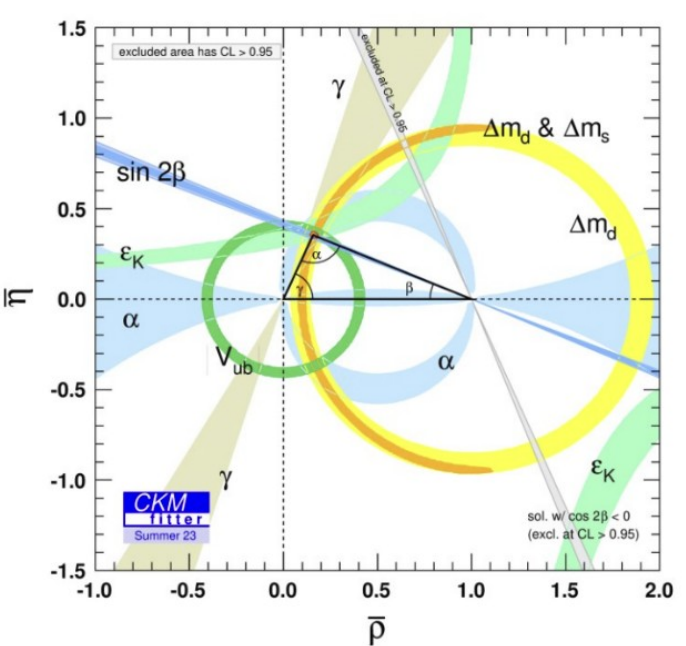
Pre 1st generation *B* factories

2009



Post 1st generation *B* factories
+ CDF *B*_s mixing

2023

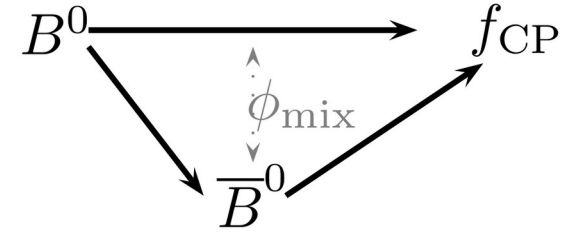


Today
+ LHCb and improved theory

6 ways of (over)constraining the Apex of the Unitarity Triangle

CP violation in interference of mixing and decay

- The S measurable from the time-dependent asymmetry between $B^0 \rightarrow f_{CP}$ and $\bar{B}^0 \rightarrow f_{CP}$

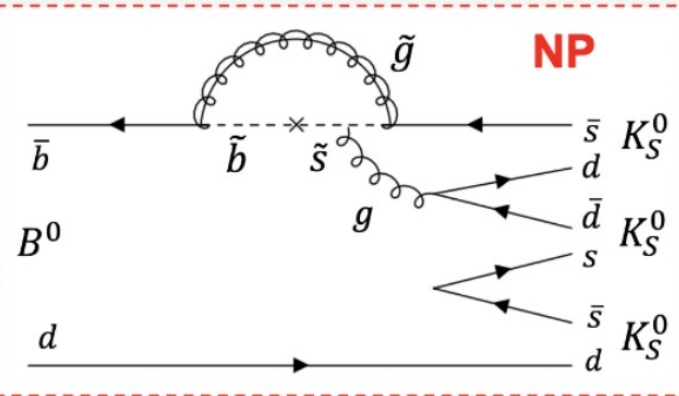
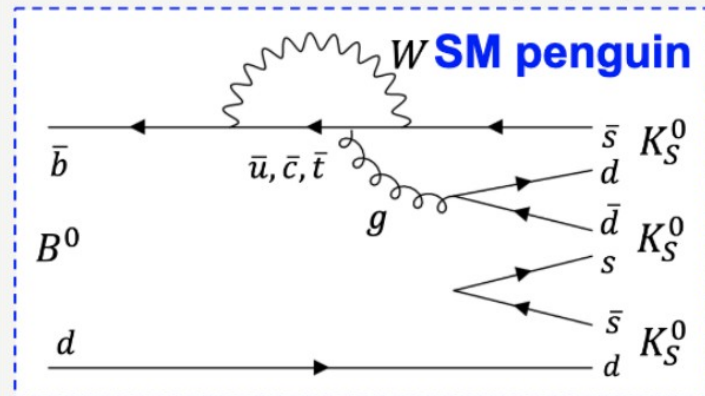


$$A_{CP}(\Delta t) = \frac{\mathcal{B}(\bar{B}^0 \rightarrow f_{CP})(\Delta t) - \mathcal{B}(B^0 \rightarrow f_{CP})(\Delta t)}{\mathcal{B}(\bar{B}^0 \rightarrow f_{CP})(\Delta t) + \mathcal{B}(B^0 \rightarrow f_{CP})(\Delta t)} = S \sin(\Delta m_d \Delta t) - C \cos(\Delta m_d \Delta t)$$

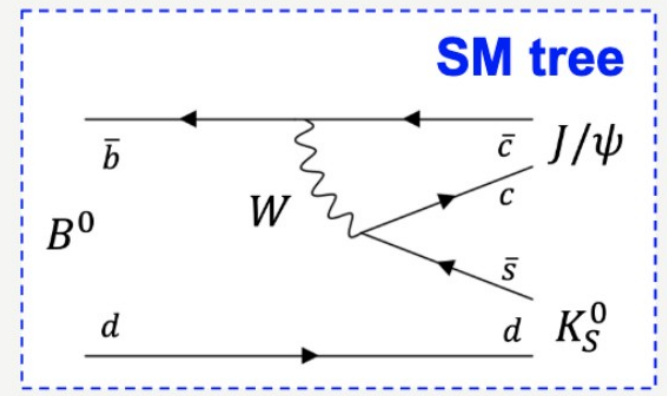
Mixing-induced CPV

Direct CPV

$$S_{K_S^0 K_S^0 K_S^0} = -\sin 2\phi_1 + \Delta S$$



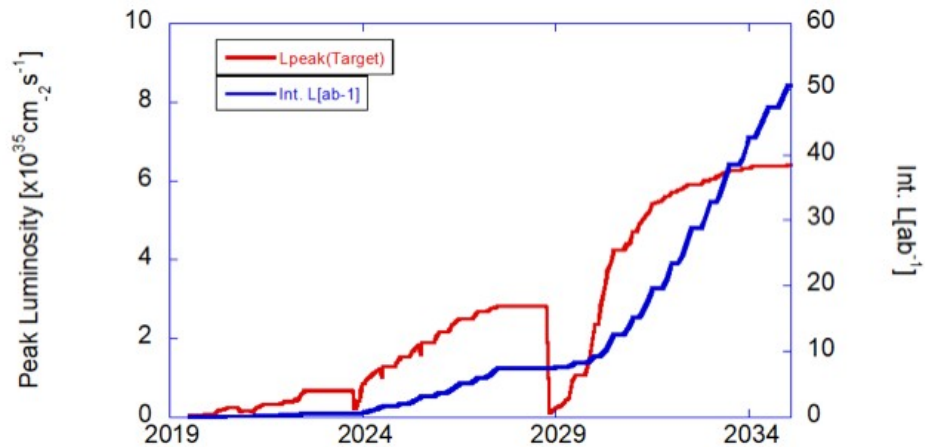
$$S_{J/\psi K_S^0} = \sin 2\phi_1$$



Belle2 & SuperKEKB status



- 550 fb⁻¹ of integrated luminosity collected so far (most analyses based on 365 fb⁻¹ of Run 1 4S data)
- World record instantaneous luminosity 0.47x10³⁵ cm⁻² s⁻¹
→ target 6x10³⁵ cm⁻² s⁻¹



Crucial for Δt measurement

Pixel Detector (PXD)

Silicon Vertex Detector (SVD)

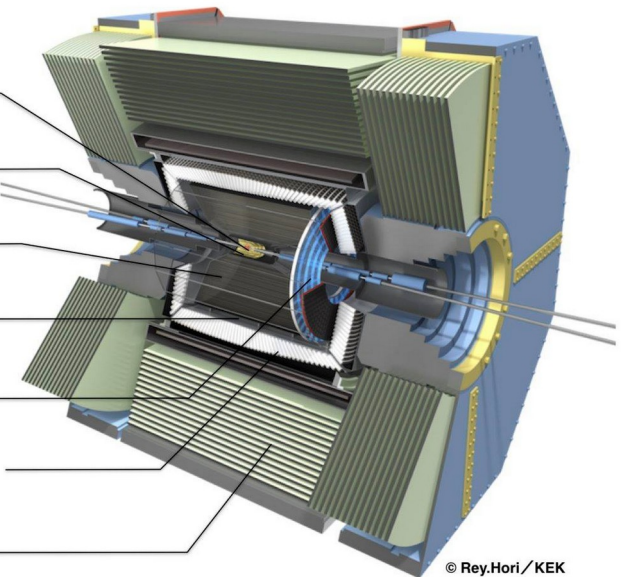
Central Drift Chamber (CDC)

TOP counter (TOP)

Aerogel RICH counter (ARICH)

Electromagnetic Calorimeter (ECL)

K_L⁰/Muon Detector (KLM)



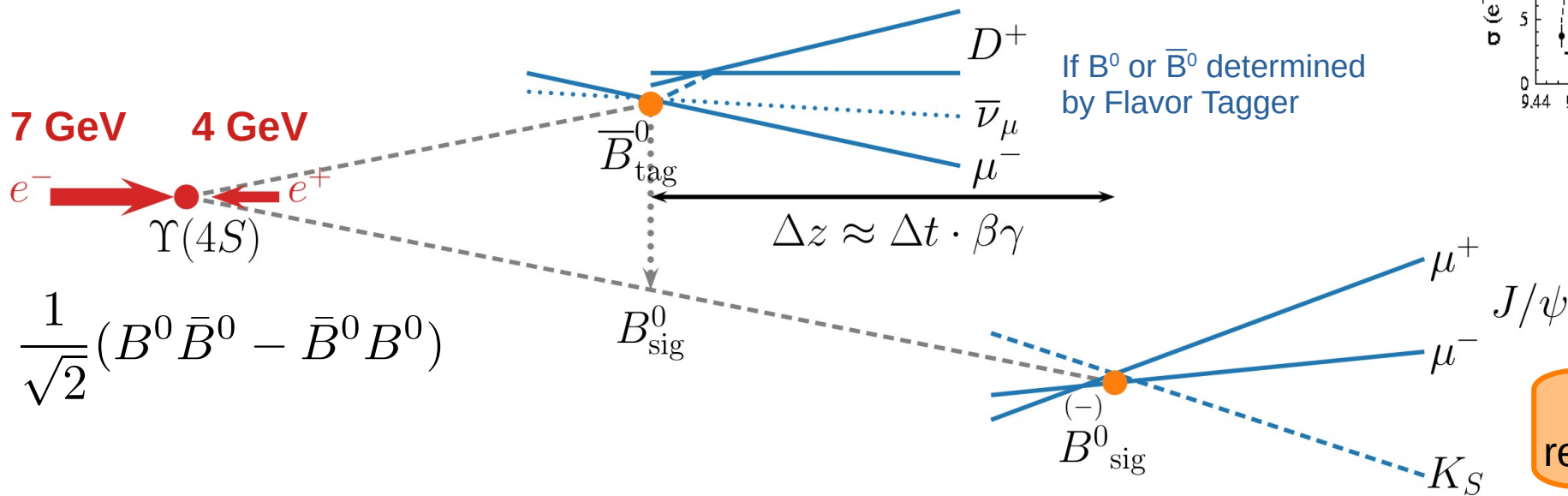
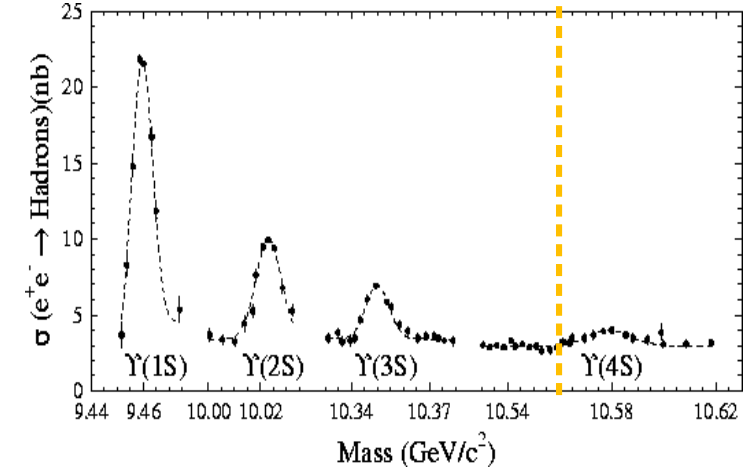
© Rey,Hori/KEK

Frequent beam instabilities has resulted in smaller integrated luminosity, and even to preventive turn-off of PXD in 2024
→ Most of the 2024 runtime dedicated to accelerator studies

Measuring time-dep. CPV at Belle II

- Collisions energy just above $B^0\bar{B}^0$ production threshold
- Due to the asymmetric beam energies B-mesons fly in the direction of the e^- beam

$B^0\bar{B}^0$ mass



Belle II : $\Delta z \approx 130 \mu\text{m}$
 Belle : $\Delta z \approx 200 \mu\text{m}$

$$\beta\gamma = 0.288$$

Fully reconstructed From rest of event

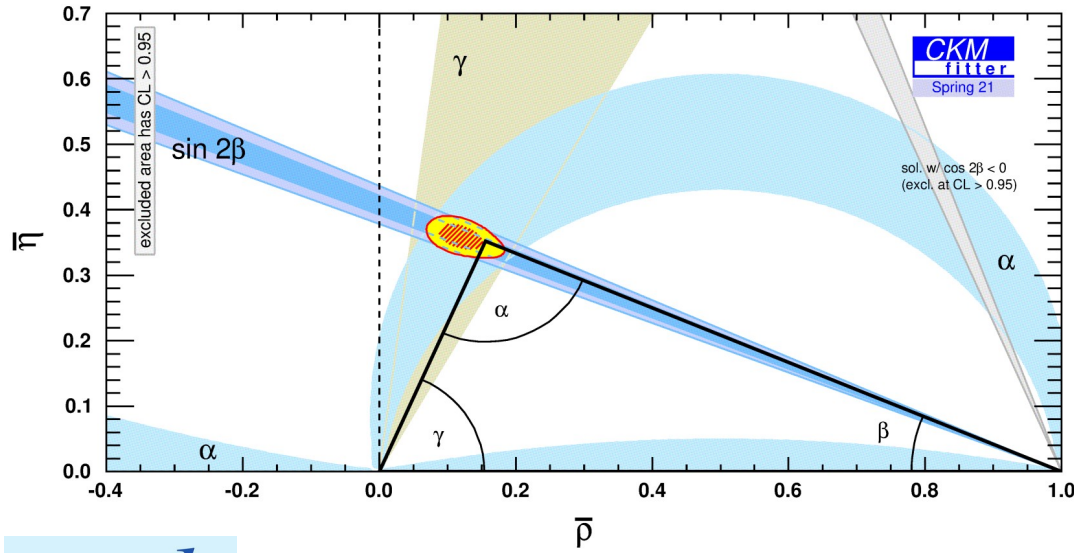
$$\Delta t = \frac{(\vec{v}_{\text{sig}} - \vec{v}_{\text{tag}}) \cdot \vec{n}_{\text{boost}}}{\gamma\beta c}$$

In this talk

Global average dominated by...



$\alpha/\phi_2 = (84 \pm 4)^\circ$:
 $B^0 \rightarrow \pi^0 \pi^0$
 $B^0 \rightarrow \pi^+ \pi^-$
 $B^+ \rightarrow \pi^+ \pi^0$
 $B^0 \rightarrow \rho^+ \rho^-$



$\beta/\phi_1 = (22.6 \pm 0.5)^\circ$ $b \rightarrow c$:
 $B^0 \rightarrow J/\psi K_s^0$
 $B^0 \rightarrow J/\psi \pi^0$

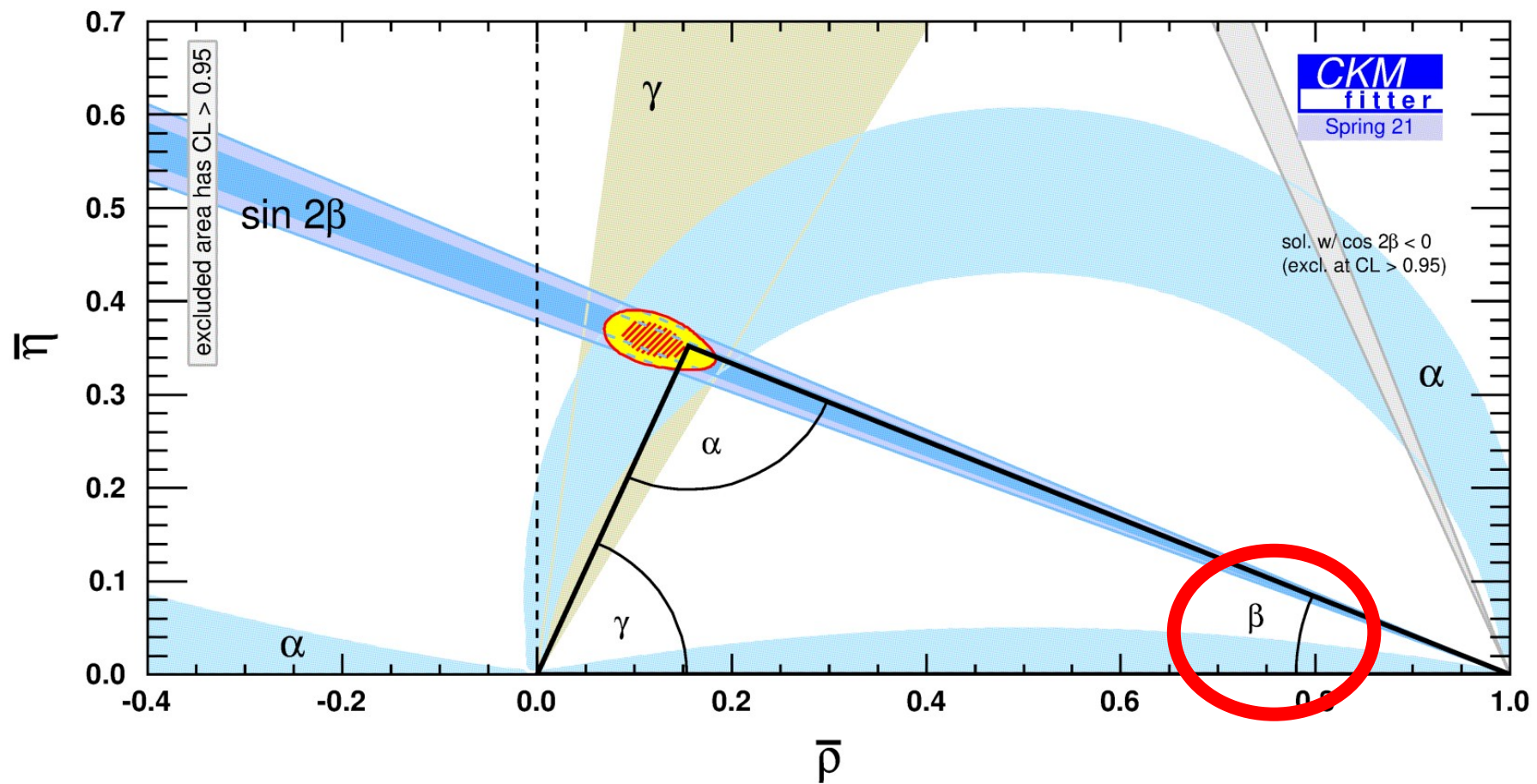


$\gamma/\phi_3 = (66 \pm 3)^\circ$



$\beta/\phi_1 = (20.4 \pm 1.4)^\circ$ $b \rightarrow s$:
 $B^0 \rightarrow \eta' K_s^0$
 $B^0 \rightarrow \phi K_s^0$
 $B^0 \rightarrow K_s^0 K_s^0 K_s^0$

$$\phi_1 = \beta$$



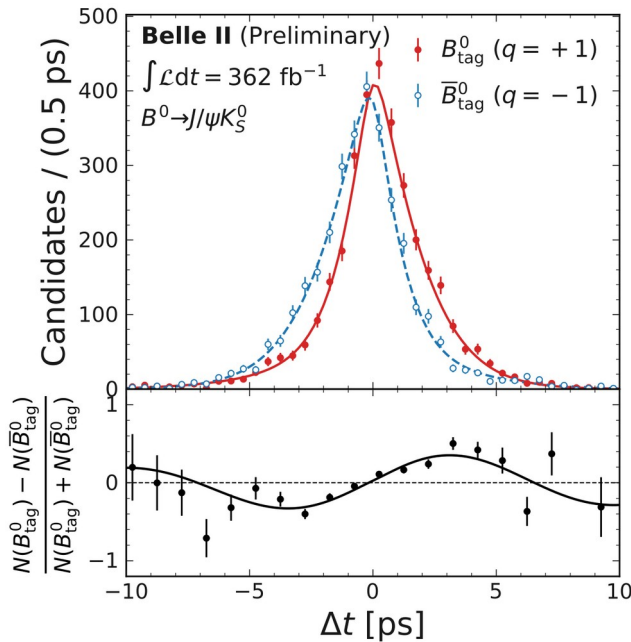
GNN-based Flavor tagger and $B^0 \rightarrow J/\psi K_s^0$

- The Graph Neural Network based Flavor tagger leads to $\sim 20\%$ gain in the effective statistics compared to category-based FT
- FT tested in $B^0 \rightarrow J/\psi K_s^0$, the golden channel for the $S \sim \sin 2\phi_1$ measurement

Phys.Rev.D 110 (2024)

$$\epsilon_{\text{tag}}^{\text{eff}} (\text{CB}) = (31.7 \pm 0.5 \pm 0.4)\%$$

$$\epsilon_{\text{tag}}^{\text{eff}} (\text{GFlaT}) = (37.4 \pm 0.4 \pm 0.3)\%$$

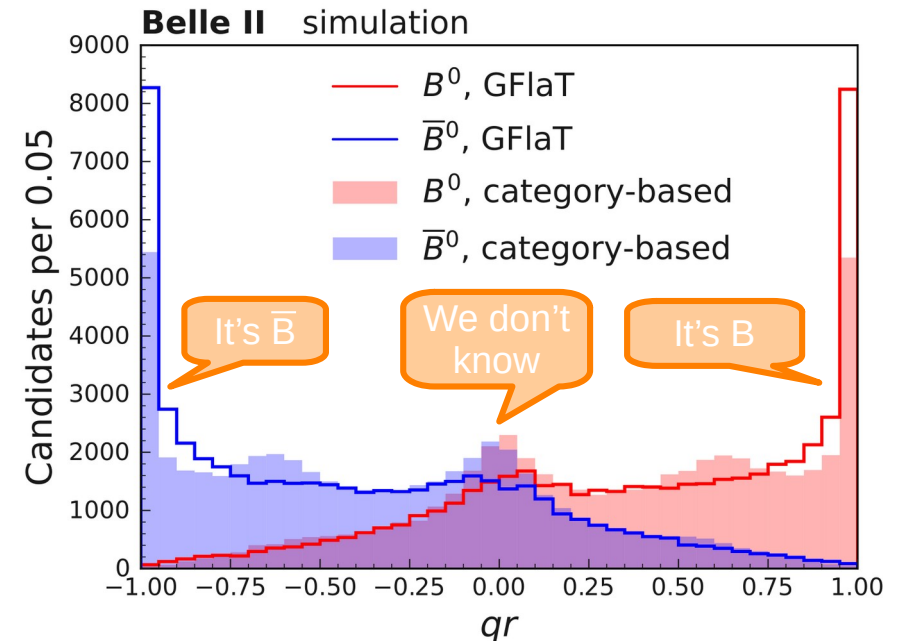


$$S = +0.724 \pm 0.035 \pm 0.009$$

$$C = -0.035 \pm 0.026 \pm 0.029$$

Latest LHCb result
Phys.Rev.Lett. 132 (2024) 2
 $S = +0.726 \pm 0.014$

Important validation of time-dep. CPV machinery, already more precise than BaBar.



CPV in $B^0 \rightarrow J/\psi \pi^0$

arXiv:2410.08622

- Color suppressed $b \rightarrow c\bar{c}d$ tree-level decay
→ loop contribution plays a role
- Important input to correct for the penguin contamination in the $B^0 \rightarrow J/\psi K_s^0$ (tree only: $S = -\sin 2\phi_1 \sim -0.71$)

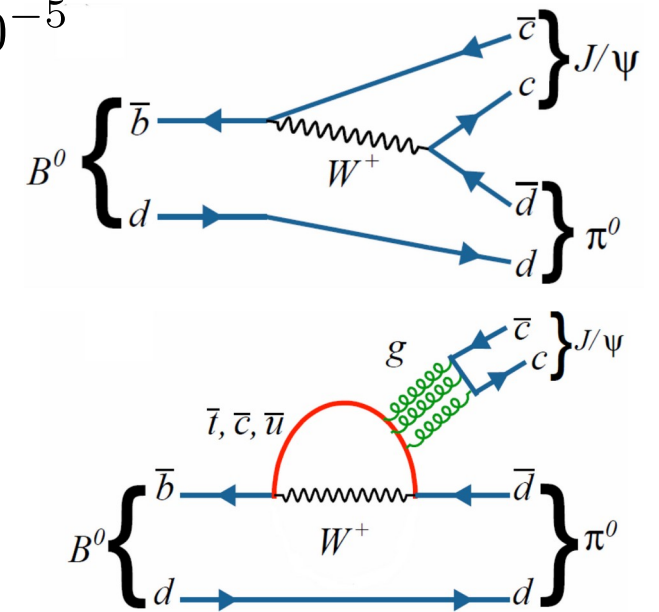
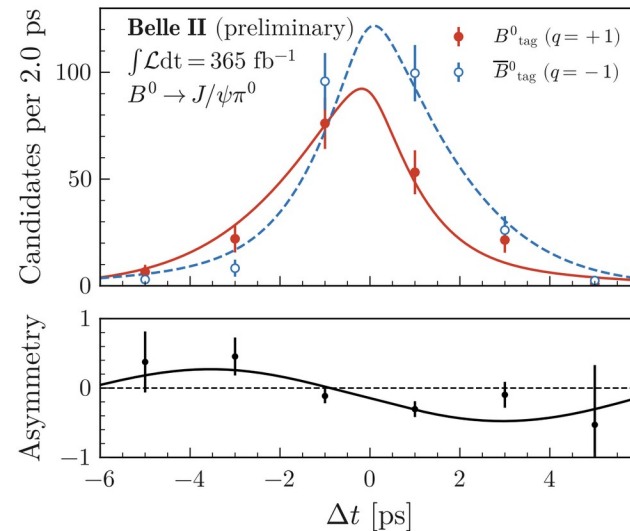
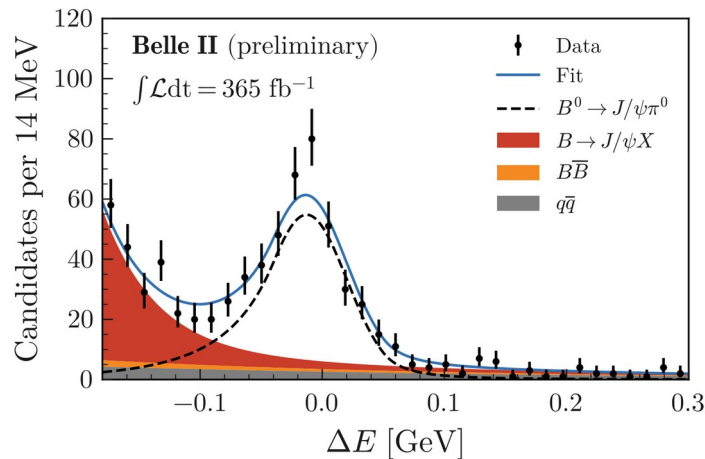
203 ± 17 ($J/\psi \rightarrow \mu\mu$)

186 ± 16 ($J/\psi \rightarrow ee$)

$$S = -0.88 \pm 0.17 \pm 0.03$$

$$\text{BR} = (2.00 \pm 0.12 \pm 0.10) \pm 10^{-5}$$

$$C = +0.13 \pm 0.12 \pm 0.03$$



[PhysRevD.98.112008](#)

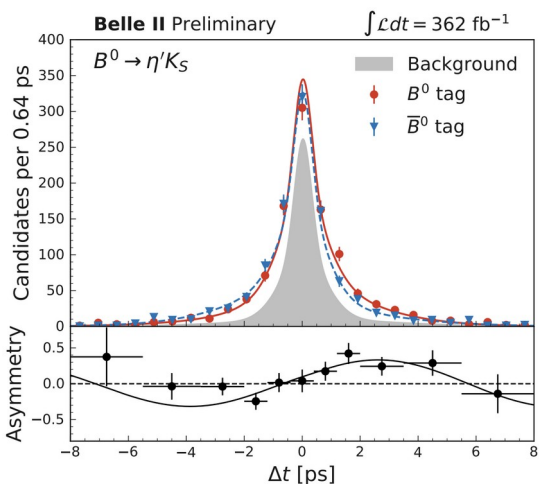
The world's most precise measurement of this mode
(higher precision than Belle)

$\phi_1 = \beta$ from Penguin $b \rightarrow s$ transitions

[arXiv:2402.03713](https://arxiv.org/abs/2402.03713)



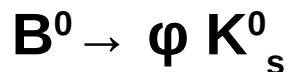
- $\eta' \rightarrow \eta(\rightarrow \gamma\gamma)\pi^+\pi^-$
 $\eta' \rightarrow \rho\gamma$
- ~800 signal events



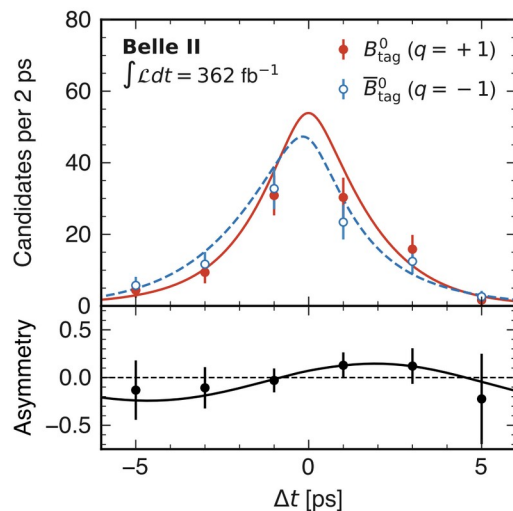
$$S = +0.67 \pm 0.10 \pm 0.04$$

$$C = -0.19 \pm 0.08 \pm 0.03$$

[Phys.Rev.D 108 \(2023\) 7](https://arxiv.org/abs/2308.11111)



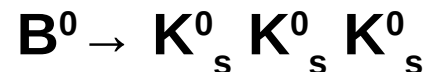
- Major challenge is from non-resonant $B^0 \rightarrow K^+ K^- K_s^0$ background with opposite CP
- ~160 signal events



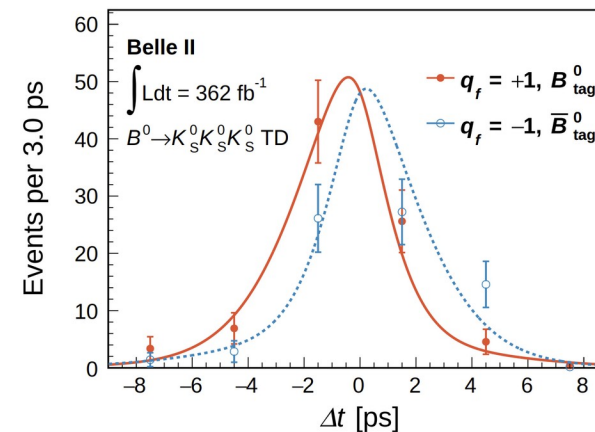
$$S = +0.54 \pm 0.26^{+0.06}_{-0.08}$$

$$C = -0.31 \pm 0.20 \pm 0.05$$

[Phys.Rev.D 109 \(2024\) 11](https://arxiv.org/abs/2402.03713)



- Major challenge is to reconstruct B^0 vertex from three K_s^0 “tracks”
- ~160 signal events

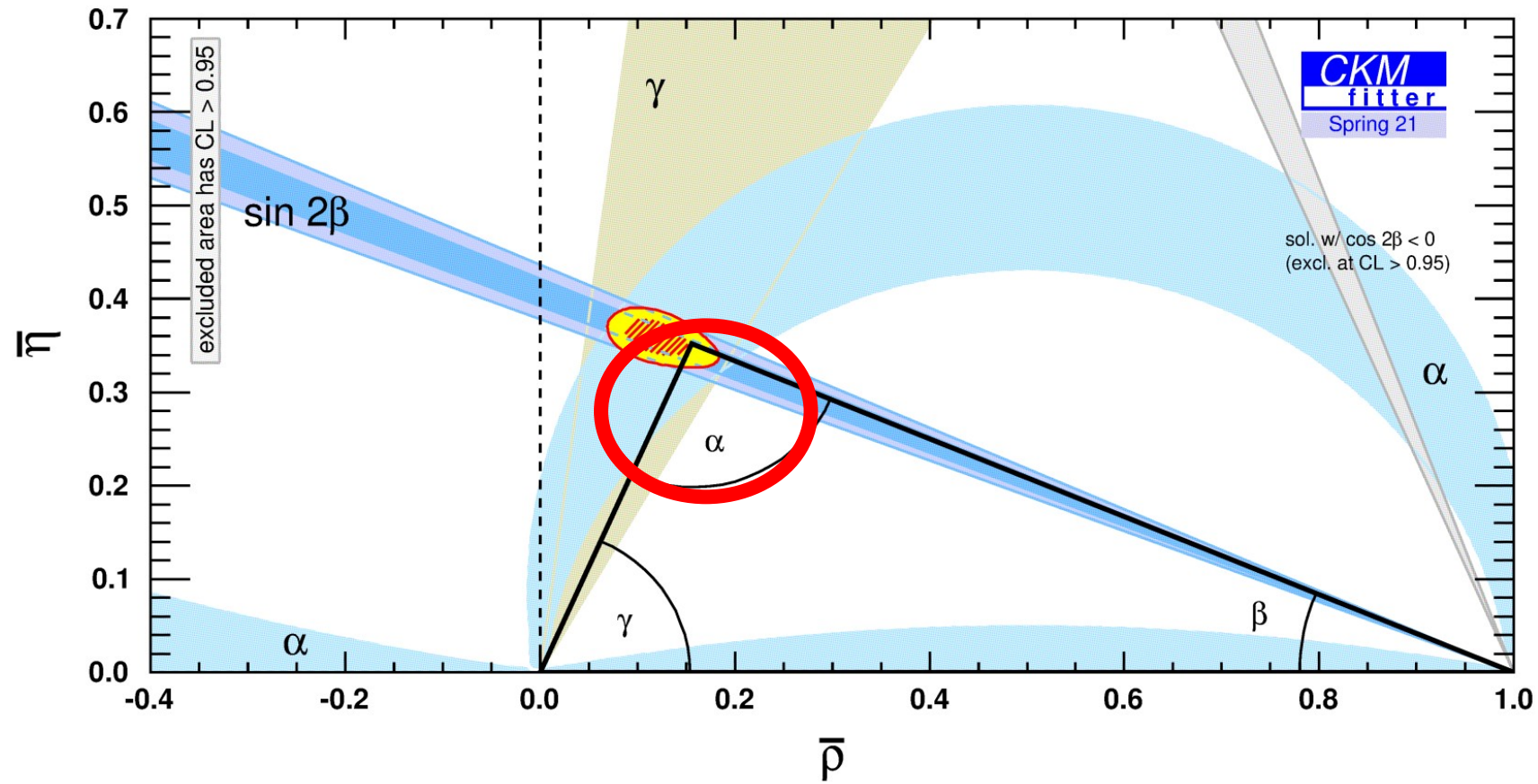


$$S = -1.37^{+0.35}_{-0.45} \pm 0.03$$

$$C = -0.07 \pm 0.20 \pm 0.05$$

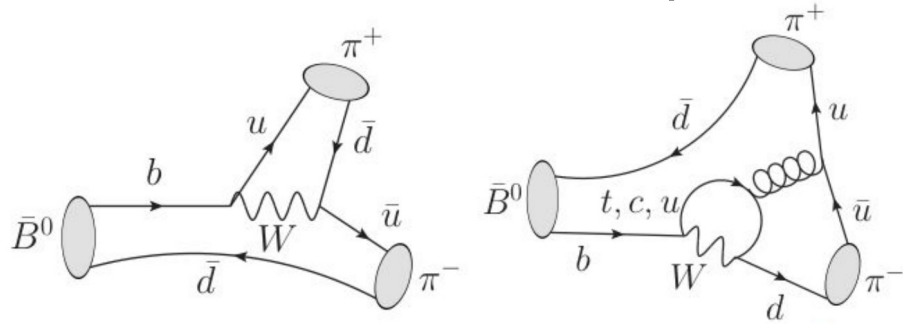
Results compatible with World Average, not at the Belle precision yet.

$$\phi_2 = \alpha$$



Experimental framework

- For $B^0 \rightarrow \pi^+ \pi^-$ and $B^0 \rightarrow \pi^0 \pi^0$ the tree-level and loop contribution have similar size, but different phase



- Need for
- All branching fractions
 - Direct CP asymmetries $C^{00} C^{+-}$
 - TD CP asymmetries $S^{00} S^{+-}$

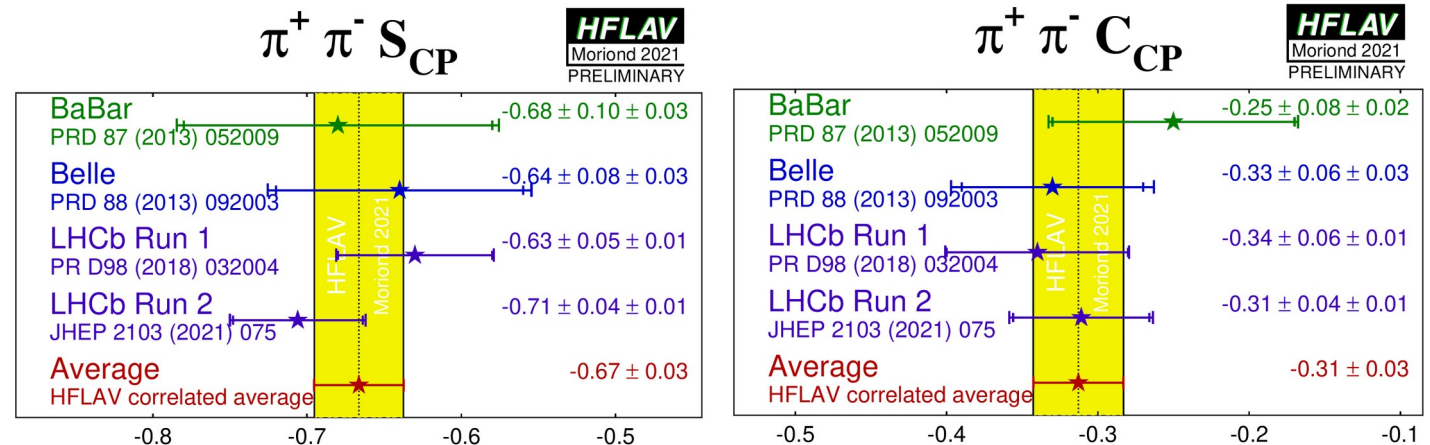
Projected Belle II sensitivity for α is 1% (currently 5%)

- Usage of Gronau-London isospin relations for $B \rightarrow \pi\pi$ to disentangle the effects (CKMfitter, UTfit)

$$A^{+0} = A^{+-} / \sqrt{2} + A^{00}$$

$$\bar{A}^{+0} = \bar{A}^{+-} / \sqrt{2} + \bar{A}^{00}$$

$$|A^{+0}| = |\bar{A}^{+0}|$$



Can be also done with $B \rightarrow \rho\rho$

Time integrated $B^0 \rightarrow \pi^0 \pi^0$

- Very difficult for LHCb, important constraint of penguin component
- Time-integrated analysis
→ getting π^0 vertices is difficult
- BG e.g. from $B^+ \rightarrow \rho^+(\rightarrow \pi^+\pi^0) \pi^0$
- 4D unbinned fit in M_{bc} , ΔE , continuum suppression (C) and wrong tag probability (w)

$$B = (1.26 \pm 0.20 \pm 0.11) \times 10^{-6}$$

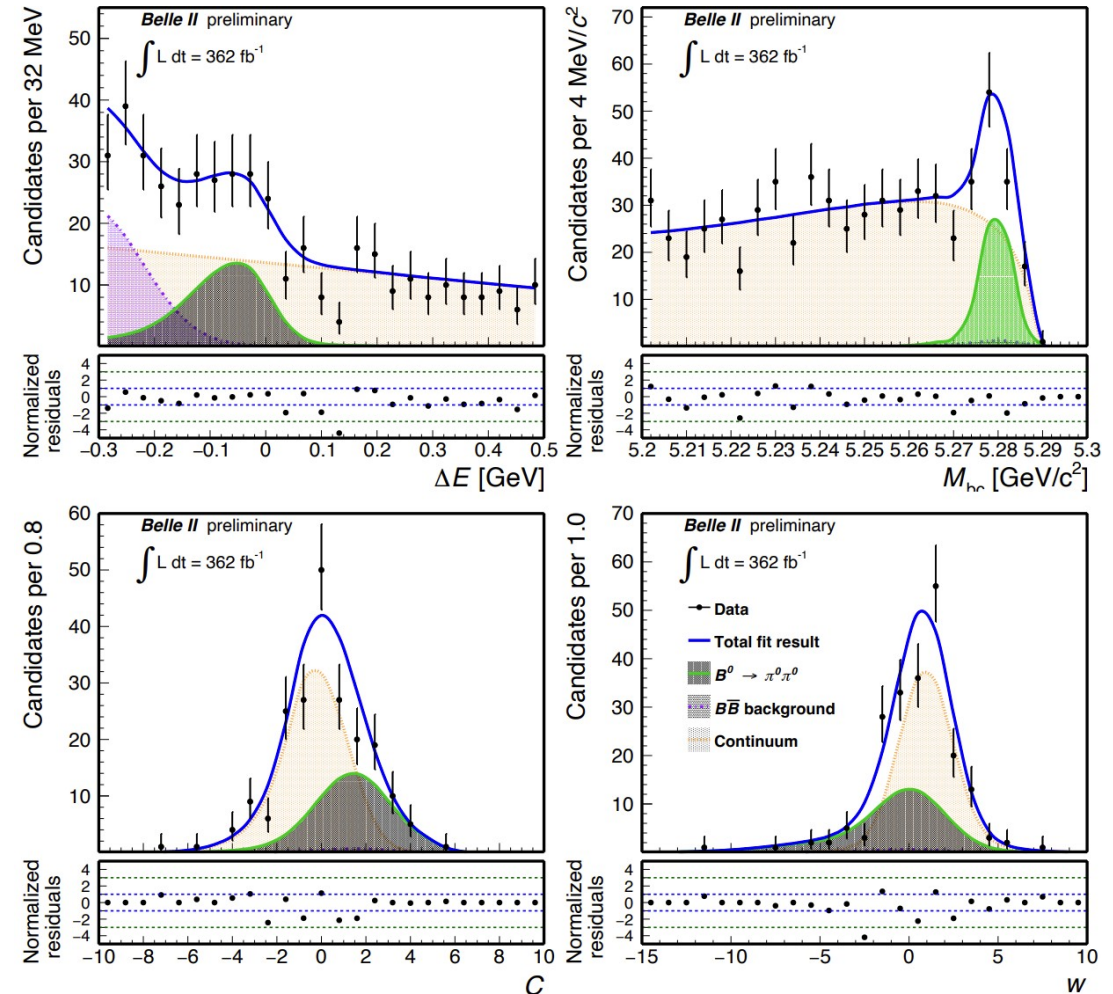
$$A_{CP} = +0.06 \pm 0.30 \pm 0.06$$

World average:

$$B = (1.59 \pm 0.26) \times 10^{-6}$$

$$A_{CP} = 0.30 \pm 0.20$$

126±20 signal events

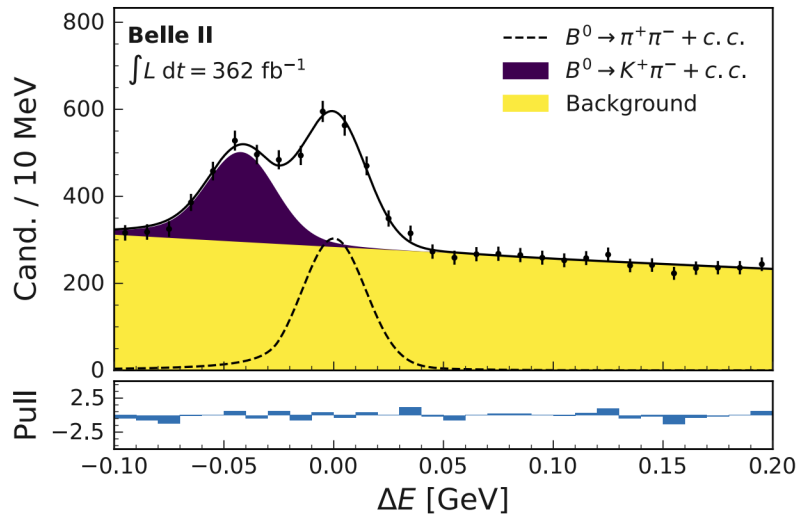


World best measurement of B and C

Time integrated $B^0 \rightarrow \pi^+ \pi^-$ and $B^+ \rightarrow \pi^+ \pi^0$

- All decay modes are still stat-dominated since the π^0 efficiency systematics will improve with more data
- Measurement of the $B^0 \rightarrow \pi^+ \pi^-$ CP asymmetries in the pipe-line

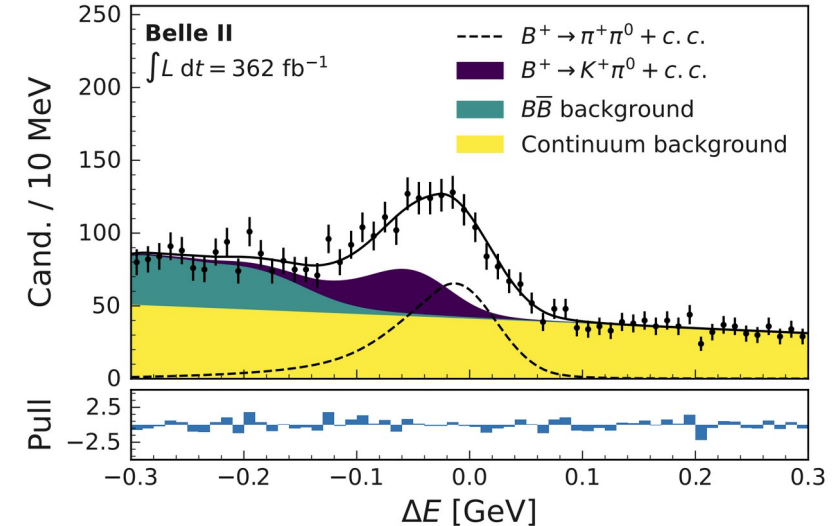
~1500 $B^0 \rightarrow \pi^+ \pi^-$ events



$$B = (5.83 \pm 0.22 \pm 0.17) \times 10^{-6}$$

World best

~900 $B^+ \rightarrow \pi^+ \pi^0$ events

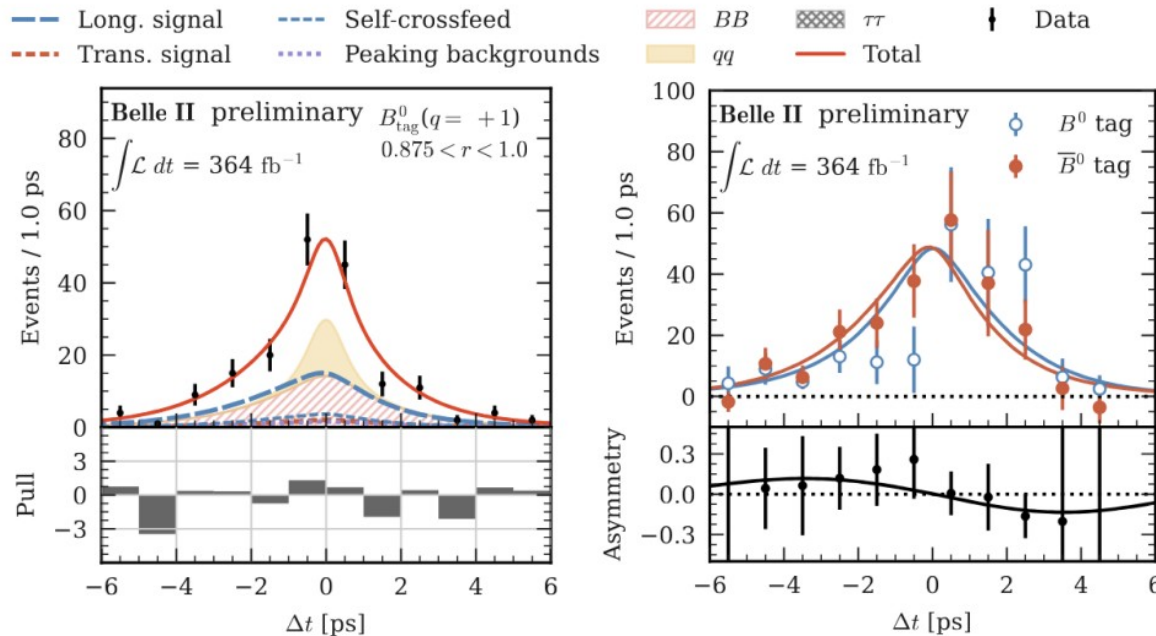
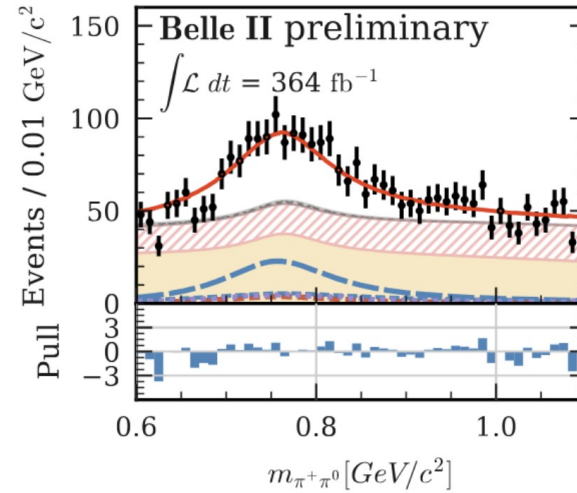


$$B = (5.10 \pm 0.29 \pm 0.32) \times 10^{-6}$$

$$A_{CP} = (-0.081 \pm 0.054 \pm 0.008) \times 10^{-6}$$

Time-dependent CPV in $B^0 \rightarrow \rho^+ \rho^-$

- The $P \rightarrow VV$ decay, i.e. full angular analysis needed for polarization extraction, notice $\rho^+ \rightarrow \pi^+ \pi^0$
- Two soft π^0 in the final state
→ difficult for LHCb
- 6D time-dependent fit for signal extraction



	$\mathcal{B}(10^{-6})$	f_L
Belle II	$29.0^{+2.3}_{-2.2} {}^{+3.1}_{-3.0}$	$0.921^{+0.024}_{-0.025} {}^{+0.017}_{-0.015}$
Belle	$28.3 \pm 1.5 \pm 1.5$	$0.988 \pm 0.012 \pm 0.006$
BABAR	$25.5 \pm 2.1 {}^{+3.6}_{-3.9}$	$0.992 \pm 0.024 {}^{+0.026}_{-0.013}$

	S	C
Belle II	$-0.26 \pm 0.19 \pm 0.08$	$-0.02 \pm 0.12 {}^{+0.06}_{-0.05}$
Belle	$-0.13 \pm 0.15 \pm 0.05$	$0.00 \pm 0.10 \pm 0.06$
BABAR	$-0.17 \pm 0.20 {}^{+0.05}_{-0.06}$	$0.01 \pm 0.15 \pm 0.06$

All parameters are measured with precision better than BaBar but worse than Belle
→ extract ϕ_2 using new data

Impact on the ϕ_2/α

- The world average of ϕ_2 is dominated by B factories and $B \rightarrow \pi\pi$ & $B \rightarrow \rho\rho$ decay modes
- The $B \rightarrow \rho\rho$ only world average:

$$\phi_2 = (91.5^{+4.5}_{-5.4})^\circ$$

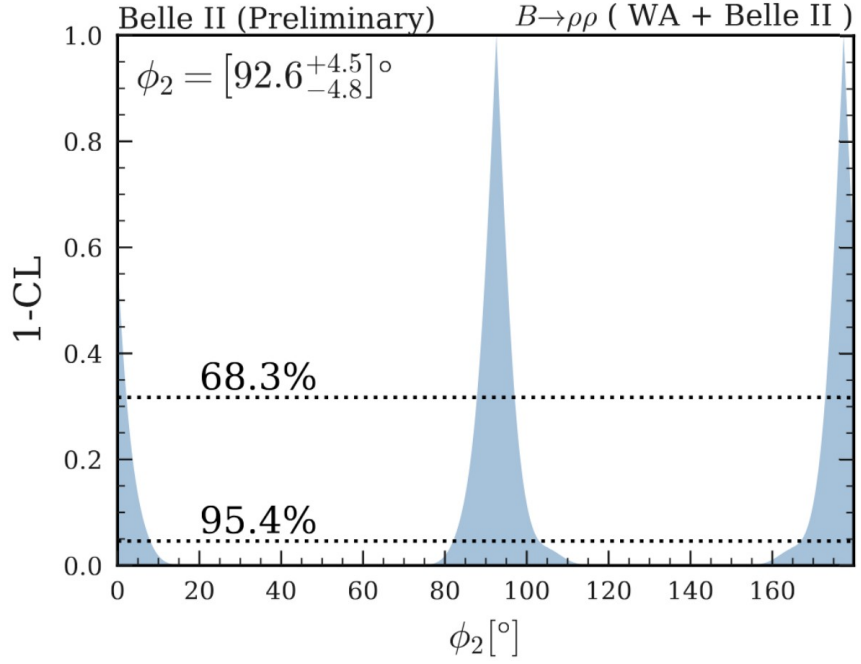
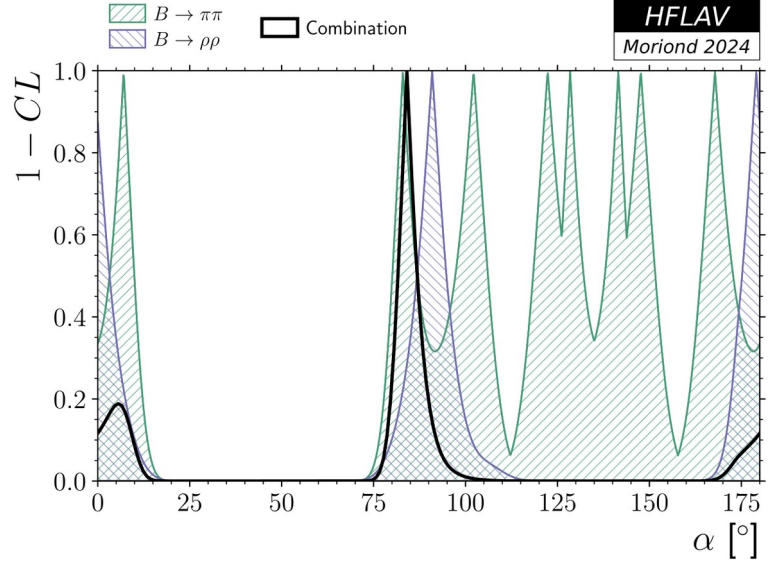
- The $B \rightarrow \rho\rho$ only world average (+ Belle II $B^0 \rightarrow \rho^+\rho^-$)

$$\phi_2 = (92.6^{+4.5}_{-4.8})^\circ$$

7% improvement in the ϕ_2 precision.
 The fit dominated by $S(\rho^+\rho^-)$ and $S(\rho^0\rho^0)$, both only measured at B factories.

The ρ -based estimate is slightly higher than π -based but still consistent within 2σ .

Current world average:
 $\phi_2 = (84.1^{+4.5}_{-3.8})^\circ$

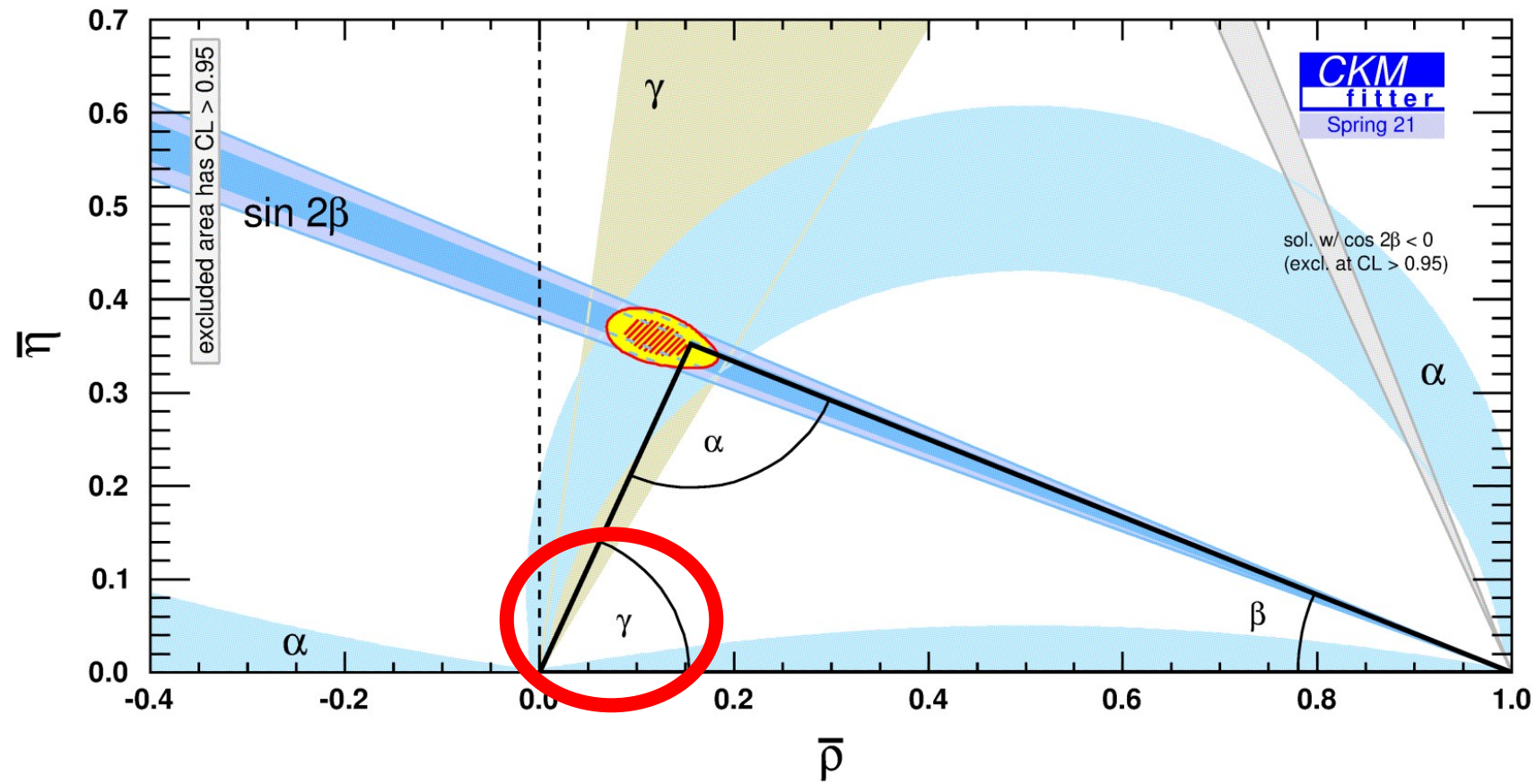


Conclusion

- Broad CPV physics program at Belle II
 - **Precise** measurements of Unitarity Triangle angles
 - CPV in **rare** $b \rightarrow s$ decays sensitive to New Physics
- The Run I Belle II dataset similar to BaBar but often the precision is better:
 - Smaller interaction region
 - Better vertex resolution
 - The GNN-based B flavor tagging
- After LS1 (Spring 2024) Belle II continues in data taking
 - Exceeding Belle statistics in one or two years

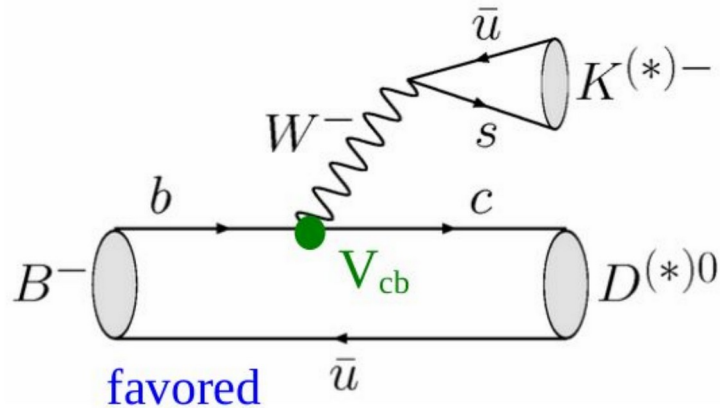
Backup

$$\phi_3 = \gamma$$

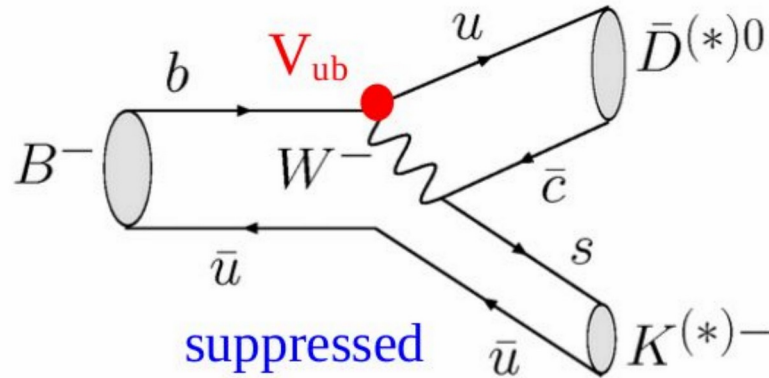


Combined Belle & Belle II fit

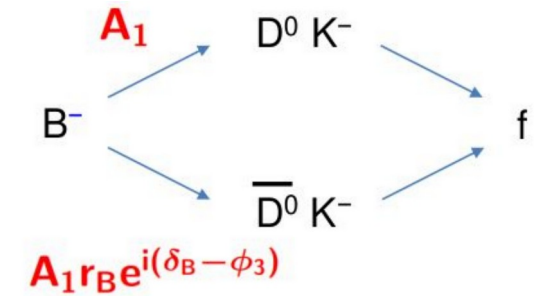
- Interference between $b \rightarrow c\bar{u}s$ and $b \rightarrow \bar{c}u s$



$$B^- \rightarrow D^0 K^- \approx V_{cb} V_{us}^* A_1$$



$$B^- \rightarrow \bar{D}^0 K^- \approx V_{ub} V_{cs}^* A_1 r_B e^{i(\delta_B - \phi_3)}$$



- The amplitude ratio r_B and strong phase δ_B are model dependent
 → There are several methods of determining γ

B decay	D decay	Method	Data set (Belle + Belle II)[fb ⁻¹]
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 \pi^0, K^- K^+$	GLW	711 + 189
$B^+ \rightarrow Dh^+$	$D \rightarrow K^+ \pi^-, K^+ \pi^- \pi^0$	ADS	711 + 0
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 K^- \pi^+$	GLS	711 + 362
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 h^- h^+$	BPGGSZ (m.i.)	711 + 128
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 \pi^- \pi^+ \pi^0$	BPGGSZ (m.i.)	711 + 0
$B^+ \rightarrow D^* K^+$	$D^* \rightarrow D\pi^0, D \rightarrow K_S^0 \pi^0, K_S^0 \phi, K_S^0 \omega,$ $K^- K^+, \pi^- \pi^+$	GLW	210+0
$B^+ \rightarrow D^* K^+$	$D^* \rightarrow D\pi^0, D\gamma, D \rightarrow K_S^0 \pi^- \pi^+$	BPGGSZ (m.d.)	605 + 0

$B^+ \rightarrow D^0 (K_S h^+ h^-) h^+$

- Model-independent BPGGSZ method using Dalitz-binned D^0 amplitudes:
 - NN-based K_S reconstruction
 - Considering $h=\pi, K$

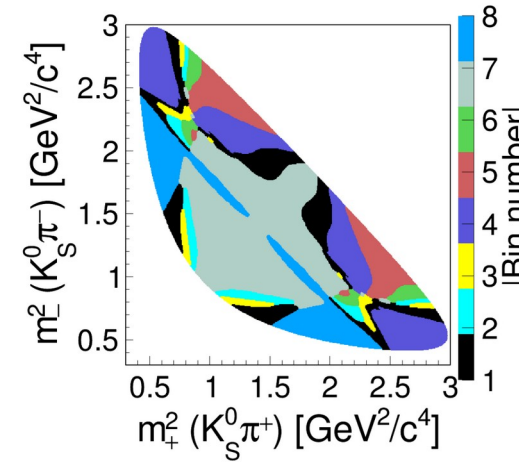
$$A_{B^+}(m_-^2, m_+^2) \propto A_{\bar{D}}(m_-^2, m_+^2) + r_B^{DK} e^{i(\delta_B^{DK} - \phi_3)} A_D(m_-^2, m_+^2)$$

$$\gamma = 78.4 \pm 11.4(\text{stat}) \pm 0.5(\text{syst}) \pm 1.0(\text{ext}) \text{ deg}$$

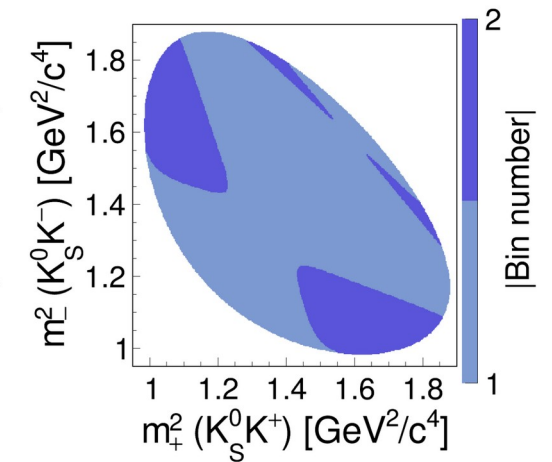
Strong D^0 - \bar{D}^0 phases from CLEO & BESIII

BaBar: $\gamma = (69 \pm 17) \text{ deg}$

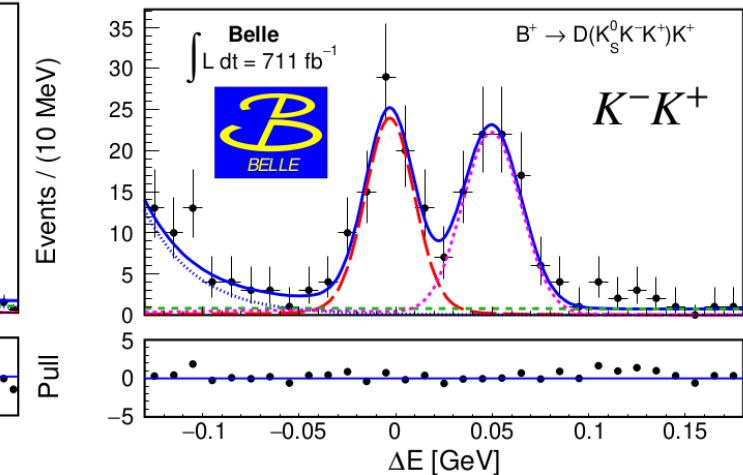
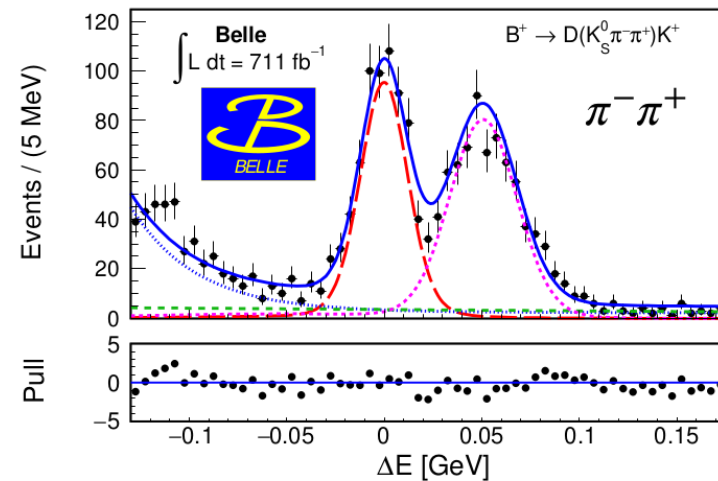
$D^0 \rightarrow K_S \pi^+ \pi^-$



$D^0 \rightarrow K_S K^+ K^-$



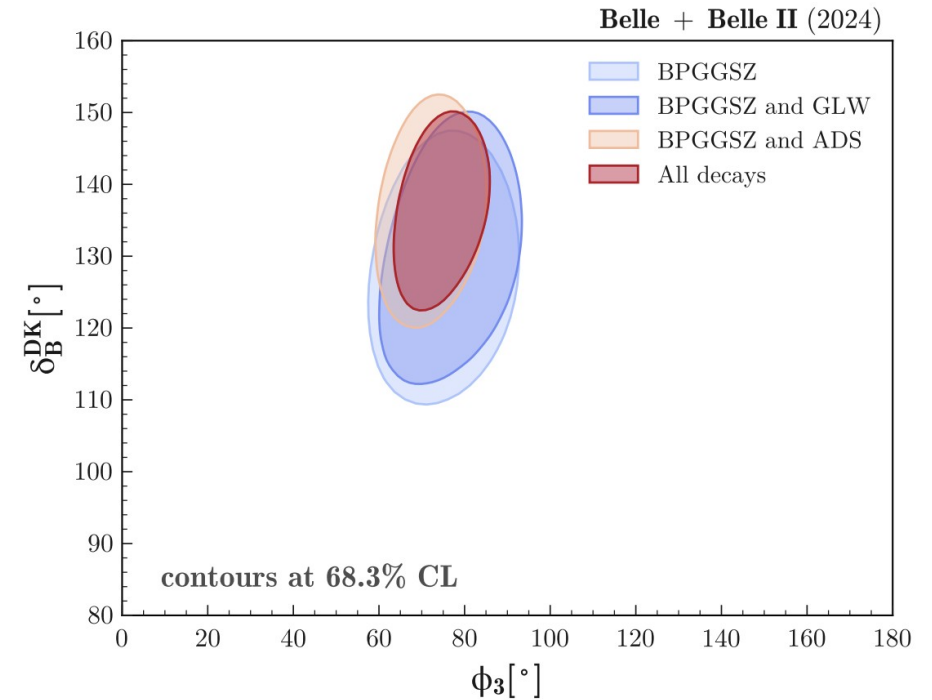
Bins from BESIII & CLEO



Combined Belle & Belle II fit: Results

JHEP 10 (2024) 143

- Fitted combined likelihood with 18 free parameters, inputs:
 - 45 Belle/Belle II data points
 - 14 “external inputs” (D decays)
- Consistent results for various methods and various decay modes, good fit quality (chi2/ndf = 38 / 41)
- Small correlations between Φ_3 and the strong phases δ_B & amplitude ratios r_B



Belle II result:
 $\Phi_3 = (75.2 \pm 7.6)^\circ$

LHCb result:
 $\Phi_3 = (64.6 \pm 2.8)^\circ$

B decay	D decay	Method	Data set (Belle + Belle II)[fb ⁻¹]
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 \pi^0, K^- K^+$	GLW	711 + 189
$B^+ \rightarrow Dh^+$	$D \rightarrow K^+ \pi^-, K^+ \pi^- \pi^0$	ADS	711 + 0
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 K^- \pi^+$	GLS	711 + 362
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 h^- h^+$	BPGGSZ (m.i.)	711 + 128
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 \pi^- \pi^+ \pi^0$	BPGGSZ (m.i.)	711 + 0
$B^+ \rightarrow D^* K^+$	$D^* \rightarrow D \pi^0, D \rightarrow K_S^0 \pi^0, K_S^0 \phi, K_S^0 \omega,$ $K^- K^+, \pi^- \pi^+$	GLW	210+0
$B^+ \rightarrow D^* K^+$	$D^* \rightarrow D \pi^0, D \gamma, D \rightarrow K_S^0 \pi^- \pi^+$	BPGGSZ (m.d.)	605 + 0