Higgs decays into lepton pairs and a photon

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Based on [2001.06516, 2109.04426 (with Kachanovich, Nierste), 2405.16239 (with Kachanovich)]

DISCRETE 2024 in Ljubljana November 4, 2024 Portrait of $H \to \ell^- \ell^+ \gamma$, $\ell = e, \mu$

• We studied $H \to \ell^- \ell^+ \gamma$ process, with $\ell = e, \mu$, including a new one-loop calculation of the amplitude and decay rates

Dominated by electroweak loops, nonvanishing even for $m_\ell=0$

Probing chirality-conserving Higgs couplings to leptons

Consequently:

$$\begin{split} \Gamma(H \to e^- e^+ \gamma) \gg \Gamma(H \to e^- e^+), & \text{while} \\ \Gamma(H \to \mu^- \mu^+ \gamma) \simeq 1/3 \, \Gamma(H \to \mu^- \mu^+) \end{split}$$

Branching fractions:

$$B(H \to e^- e^+ \gamma) = 5.8 \cdot 10^{-5}, \qquad B(H \to \mu^- \mu^+ \gamma) = 6.4 \cdot 10^{-5}$$

with minimal cuts: $s, t, u > (0.1 \, m_H)^2$, $E_{\gamma} > 5 \, \text{GeV}$, $(E_1 > 7 \, \text{GeV}, E_2 > 25 \, \text{GeV})$ or $(E_1 > 25 \, \text{GeV}, E_2 > 7 \, \text{GeV})_{2/17}$

Sample set of diagrams:



• Tree-level contribution is negligible for $H \to e^- e^+ \gamma$, but notable for $H \to \mu^- \mu^+ \gamma$

$$\frac{d^2\Gamma}{ds\,dt} = \begin{cases} \frac{d^2\Gamma_{\mathrm{loop}}}{ds\,dt}, & \text{for } \ell = e, \\ \frac{d^2\Gamma_{\mathrm{loop}}}{ds\,dt} + \frac{d^2\Gamma_{\mathrm{tree}}}{ds\,dt}, & \text{for } \ell = \mu. \end{cases}$$

(negligible tree-loop interference)

What makes this process interesting?

We identify three milestones expected from measurements of $H \rightarrow \ell^- \ell^+ \gamma$:

- Discovery of $H \to Z\gamma$
- Observation of $H \to \mu^- \mu^+ \gamma$ at tree level driven by muon's Yukawa coupling
- \blacksquare Search for deviations from SM both in $H\mathchar`-Z\mathchar`-\gamma$ and nonresonant $H\mathchar`-\ell^+\gamma$

Why perform a new calculation?

Previous calculations:

Analytic expressions derived in:

[1] Abbasabadi, Bowser-Chao, Dicus, Repko (9611209)

[2] Sun, Chang, Gao (1303.2230)

New calculations:

[4] Passarino (1308.0422)

[5] Han, Wang (1705.00790)

- Significant discrepancies between previous results for $d\Gamma(H \to \ell^- \ell^+ \gamma)/dm_{\ell\ell}$ prompted our independent calculation.
- To provide expressions that could prove useful in experimental studies

Our calculation

- We used linear R_{ξ} gauge, resulting with $\mathcal{O}(10^2)$ loop diagrams
- Analytic check of gauge invariance and UV/IR finiteness

Classes of one-loop diagrams:



- $H \to Z^*[\to \ell^+ \ell^-]\gamma$ (a)
- $H \to \gamma^* [\to \ell^+ \ell^-] \gamma$ (a)
- Others, including nonresonant box diagrams (b,c)

- Individual classes of diagrams exhibit ξ -dependence in the linear R_{ξ} gauge.
- Specifically, the ξ -dependence in the $H \to Z^*(\ell \ell) \gamma$ class cancels with contributions from other diagrams, including box diagrams.
- Multiplying this contribution by the Breit-Wigner distribution to study $H \rightarrow Z\gamma$ yields an unphysical result [Passarino, 1308.0422].
- $H \to Z \gamma$ is well-defined only for on-shell Z boson

Achieving the three goals requires a clear separation of contributions performed in a gauge-invariant manner.

Loop amplitude:

$$\mathcal{A}_{\mathsf{loop}} = \left[(k_{\mu} \, p_{1\nu} - g_{\mu\nu} \, k \cdot p_1) \bar{u}(p_1) \big(a_1 \gamma^{\mu} P_R + b_1 \gamma^{\mu} P_L \big) v(p_2) \right. \\ \left. + (k_{\mu} \, p_{2\nu} - g_{\mu\nu} \, k \cdot p_2) \bar{u}(p_1) \big(a_2 \gamma^{\mu} P_R + b_2 \gamma^{\mu} P_L \big) v(p_2) \right] \varepsilon^{\nu \, *}(k) \,,$$

determined in terms of two loop coefficients a_1 , b_1 , due to

$$a_2(t, u) = a_1(u, t), \qquad b_2(t, u) = b_1(u, t)$$

with $s = (p_1 + p_2)^2$, $t = (p_1 + k)^2$, $u = (p_2 + k)^2$

• We provide compact expressions for $a_1(u,t)$ and $b_1(u,t)$, reduced to scalar one-loop functions

Tools: Feynarts, Feyncalc, Feynhelpers, PackageX, Collier

Separation of resonant and nonresonant contributions

• Loop coefficients take the form:

$$a_1(s,t) = \widetilde{a}_1(s,t) + \frac{\alpha(s)}{s - m_Z^2 + im_Z\Gamma_Z}$$

Setting $s = m_Z^2$ in $\alpha(s)$, $\beta(s)$ isolates the gauge-invariant resonant contribution from the nonresonant components:

$$a_1(s,t) = a_1^{nr}(s,t) + a_1^{res}(s)$$

where:

$$a_1^{nr}(s,t) = \tilde{a}_1(s,t) + \frac{\alpha(s) - \alpha(m_Z^2)}{s - m_Z^2 + im_Z\Gamma_Z}, \quad a_1^{res}(s) = \frac{\alpha(m_Z^2)}{s - m_Z^2 + im_Z\Gamma_Z}$$

(The residue of the Z-propagator is gauge-invariant.)

Implementing a discovery strategy for $H \to Z\gamma$:

• Using data on the double differential decay width, $\frac{d^2\Gamma}{ds dt}$, perform a fit to extract the following three quantities:

$$\begin{split} & \left[\alpha(m_Z^2)\right]^2 + \left[\beta(m_Z^2)\right]^2, \quad |a_1^{nr}|^2 + |b_1^{nr}|^2 \quad \text{and} \quad |a_2^{nr}|^2 + |b_2^{nr}|^2 \\ & \bullet \text{ targeting } \left[\alpha(m_Z^2)\right]^2 + \left[\beta(m_Z^2)\right]^2 \neq 0 \text{ at } 5\sigma \text{ significance.} \end{split}$$

(with negligible resonant-nonresonant interference)

- Using the measured value of this quantity, relate $d\Gamma_{res}/ds$ to $\Gamma(H \to Z\gamma)$ under the narrow width approximation.
- To faciliate this, we provide numerical easy-to-use expressions for $a_{1,2}^{nr}$ and $b_{1,2}^{nr}$.

Differential distributions over dilepton mass:



Peaks at the Z-pole and photon pole; for muons, the tree-level contribution rises towards the spectrum's endpoint.

 \blacksquare Nonresonant loop contributions are prominent between the photon and Z poles.

To devise kinematic cuts for separating contributions, we examine Dalitz plots



Loop contributions (resonant and nonresonant) are sensitive to the cuts on s near the peaks, but insensitive to t and u near the edges

 \blacksquare Tree-level contribution peaks at low t and low u

For generic cuts, nonresonant and tree contributions constitute significant fractions of the rate

s _{min}	s_{max}	$ ilde{t}_{min}, ilde{u}_{min}$	$\Gamma_{res}({ m keV})$	$\Gamma_{nr}({ m keV})$	$\Gamma_{tree}({ m keV})$	$\Gamma_{tot}({ m keV})$
$(0.1 m_H)^2$	$(120GeV)^2$	$(0.1 m_H)^2$	0.202	0.042	0.026	0.270
$(0.1 m_H)^2$	$(120GeV)^2$	$(0.2 m_H)^2$	0.165	0.037	0.013	0.215

Strategy for the separation of contributions:

- **Resonant contribution:** *s* around the *Z*-peak, excluding regions with significant tree-level effects; requires tighter cuts on *t* and *u*.
- Nonresonant contribution: *s* in the intermediate range between the photon and *Z*-peaks.
- **Tree-level contribution:** s above the Z-peak, with looser cuts on t and u.

Forward-backward asymmetry:



Interesting asymmetry w.r.t. $\cos \theta^{(\mu)}$ - angle between lepton and photon (in Higgs boson RF)

$$\mathcal{A}_{\mathsf{FB}}^{(\ell)} = \frac{\int_{-1}^{0} \frac{d\Gamma}{d\cos\theta^{(\ell)}} - \int_{0}^{1} \frac{d\Gamma}{d\cos\theta^{(\ell)}}}{\int_{-1}^{0} \frac{d\Gamma}{d\cos\theta^{(\ell)}} + \int_{0}^{1} \frac{d\Gamma}{d\cos\theta^{(\ell)}}}$$

$$\mathcal{A}_{\mathsf{FB}}^{(e)} = 0.343, \qquad \mathcal{A}_{\mathsf{FB}}^{(\mu)} = 0.255$$

Brief Overview of $H \rightarrow \nu \bar{\nu} \gamma$ [2405.16239]

- Non-resonant box contributions important for high photon energies with off-shell Z bosons.
- Potentially relevant for dark sector searches, especially at future lepton colliders.



Somewhat larger branching fraction:

$$B(H \to \nu \bar{\nu} \gamma) = 3.2 \cdot 10^{-4}$$

Summary

- Performed a new calculation of $H \to \ell^- \ell^+ \gamma$ ($\ell = e, \mu$) with compact expressions fully reduced to scalar one-loop functions, with analytic checks of ξ -independence, UV- and IR finiteness
- Evaluated differential decay rates and branching fractions
- Suggested a gauge-invariant separation of resonant contribution, enabling the determination of $\Gamma(H\to Z\gamma)$
- Separation of resonant, non-resonant, and tree-level contributions can be obtained by using the kinematic cuts
- We use $\alpha^{-1} = \frac{\pi}{\sqrt{2}G_F m_W^2 \sin^2 \theta_W} = 132$, compare to $\alpha^{-1} = 128$. Ambiguity in numerical inputs for α can only be resolved through a NLO calculation
- \blacksquare Performed one-loop calculation of $H \rightarrow \nu \bar{\nu} \gamma$ process

Additional Details on the Cuts

Resonant contribution

s_{min}	s _{max}	$ ilde{t}_{min}, ilde{u}_{min}$	$\Gamma_{res} \ (keV)$	$\Gamma_{nr}(\text{keV})$	$\Gamma_{tree}({ m keV})$	$\Gamma_{tot}({ m keV})$
$(70 GeV)^2$	$(100GeV)^2$	$(0.1 m_H)^2$	0.195	0.002	0.007	0.204
$(70GeV)^2$	$(100 GeV)^2$	$(0.2 m_H)^2$	0.160	0.001	0.004	0.165

Nonresonant contribution

s_{min}	s_{max}	$ ilde{t}_{min}, ilde{u}_{min}$	$\Gamma_{res}({ m keV})$	${f \Gamma_{nr}}({ m keV})$	$\Gamma_{tree}({ m keV})$	$\Gamma_{tot}({ m keV})$
$(10GeV)^2$	$(40GeV)^2$	$(0.1 m_H)^2$	$3.53\cdot 10^{-4}$	$3.78 \cdot 10^{-2}$	$1.02\cdot 10^{-3}$	$3.92\cdot10^{-2}$
$(20GeV)^2$	$(40GeV)^2$	$(0.1m_H)^2$	$3.33\cdot 10^{-4}$	$1.75 \cdot 10^{-2}$	$8.12\cdot 10^{-4}$	$1.87\cdot10^{-2}$

Tree-level contribution

s_{min}	s_{max}	$ ilde{t}_{min}, ilde{u}_{min}$	$\Gamma_{res}({ m keV})$	$\Gamma_{nr}(\text{keV})$	$\Gamma_{tree}(\text{keV})$	$\Gamma_{tot}({ m keV})$
$(100GeV)^2$	$(120GeV)^2$	$(0.1 m_H)^2$	$1.93\cdot 10^{-3}$	$7.51\cdot10^{-5}$	$1.5 \cdot 10^{-2}$	$1.70 \cdot 10^{-2}$
$(100GeV)^2$	$(120GeV)^2$	$(0.2 m_H)^2$	$1.40\cdot10^{-3}$	$5.28\cdot10^{-5}$	$\boldsymbol{6.06\cdot 10^{-3}}$	$7.51 \cdot 10^{-3}$