Collider Feasibility of the Dynamical Scotogenic Model

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Particle content and symmetries of the model

- The SM leptons only couple to the dark sector through the Yukawa couplings (y_{ij}) .
- The new fermion sector includes the following terms in the Lagrangian:

$$
\mathcal{L}_F = y_{ij}\bar{\ell}_i \tilde{\eta} N_j + \kappa_{ij} \overline{N_i}^c \sigma N_j + \text{h.c.} \tag{1}
$$

- The σ VEV allows the Majorana fermions (N_i) to acquire mass. In this case, κ_{ij} is a 3×3 matrix, that we will consider diagonal for our study without any loss of
- The potential reads:

$$
\mathcal{V} = m_H^2 H^{\dagger} H + m_\eta^2 \eta^{\dagger} \eta + m_\sigma^2 \sigma^{\dagger} \sigma + \frac{\lambda_1}{2} (H^{\dagger} H)^2 + \frac{\lambda_2}{2} (\eta^{\dagger} \eta)^2 + \frac{\lambda_\sigma}{2} (\sigma^{\dagger} \sigma)^2 \n+ \lambda_3 (H^{\dagger} H)(\eta^{\dagger} \eta) + \lambda_3^{H \sigma} (H^{\dagger} H)(\sigma^{\dagger} \sigma) + \lambda_3^{ \eta \sigma} (\eta^{\dagger} \eta) (\sigma^{\dagger} \sigma) + \lambda_4 (H^{\dagger} \eta) (\eta^{\dagger} H) \n+ \frac{\lambda_5}{2} [(H^{\dagger} \eta)^2 + (\eta^{\dagger} H)^2]
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$$

• After the Kibble parametrization

$$
H = \left(\frac{H^+}{\sqrt{2}}(v + S_H + iP_H)\right);
$$

\n
$$
\sigma = \frac{1}{\sqrt{2}}(v_\sigma + S_\sigma + iP_\sigma);
$$

\n
$$
\eta = \left(\frac{\eta^+}{\sqrt{2}}(\eta_R + i\eta_I)\right),
$$

\n(2)

Figure: Representation of the Kibble parametrization of a scalar around the VEV topology.

one finds that the quadratic parts of the coupling potential between H^0 and σ take the form

$$
\mathcal{V}_{H^0\sigma} = \frac{1}{2} \operatorname{Re} \{\varphi_i\} (\mathcal{M}_R^2)_{ij} \operatorname{Re} \{\varphi_j\} + \frac{1}{2} \operatorname{Im} \{\varphi_i\} (\mathcal{M}_I^2)_{ij} \operatorname{Im} \{\varphi_j\}; \quad \varphi = (H^0, \sigma) \tag{3}
$$

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$$
f_{\rm{max}}
$$

• The mass matrices, \mathcal{M}_R and \mathcal{M}_I are given by

$$
\mathcal{M}_{R}^{2} = \begin{pmatrix} m_{H}^{2} + \frac{3}{2}\lambda_{1}v^{2} + \frac{\lambda_{3}^{H\sigma}}{2}v_{\sigma}^{2} & \lambda_{3}^{H\sigma}vv_{\sigma} \\ \lambda_{3}^{H\sigma}vv_{\sigma} & m_{\sigma}^{2} + \frac{3}{2}\lambda_{\sigma}v_{\sigma}^{2} + \frac{\lambda_{3}^{H\sigma}}{2}v^{2} \end{pmatrix}
$$
(4)

$$
\mathcal{M}_{I}^{2} = \begin{pmatrix} m_{H}^{2} + \frac{\lambda_{1}}{2}v^{2} + \frac{\lambda_{3}^{H\sigma}}{2}v_{\sigma}^{2} & 0 \\ 0 & m_{\sigma}^{2} + \frac{\lambda_{\sigma}}{2}v_{\sigma}^{2} + \frac{\lambda_{3}^{H\sigma}}{2}v^{2} \end{pmatrix}
$$
(5)

• Both matrices can be reduced after inserting the tadpole equations of the potential

$$
\frac{\partial V_{H^0\sigma}}{\partial H^0}|_{H^0 = \langle H^0 \rangle} = m_H^2 \frac{v}{\sqrt{2}} + \frac{\lambda_1}{2\sqrt{2}} v^3 \lambda_1 + \frac{\lambda_3^{H\sigma}}{2\sqrt{2}} v v_\sigma^2 = 0
$$
\n
$$
\frac{\partial V_{H^0\sigma}}{\partial \sigma}|_{\sigma = \langle \sigma \rangle} = \frac{v_\sigma}{\sqrt{2}} m_\sigma^2 + \frac{\lambda_\sigma}{2\sqrt{2}} v_\sigma^3 + \frac{\lambda_3^{H\sigma}}{2\sqrt{2}} v_\sigma v^2 = 0.
$$
\n(7)

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• \mathcal{M}_I^2 becomes exactly zero, allowing us to identify P_H as the SM neutral Goldstone boson from the parametrization

$$
H = \begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}}(v + S_H + iP_H) \end{pmatrix}; \quad \sigma = \frac{1}{\sqrt{2}}(v_\sigma + S_\sigma + iP_\sigma);
$$

- $P_{\sigma} = J$ remains a physical state of the theory, the Majoron.
- \mathcal{M}_R^2 reduces to

$$
\mathcal{M}_R^2 = \begin{pmatrix} \lambda_1 v^2 & \lambda_3^{H\sigma} v v_{\sigma} \\ \lambda_3^{H\sigma} v v_{\sigma} & \lambda_{\sigma} v_{\sigma}^2 \end{pmatrix},\tag{8}
$$

which is still non diagonal. To find the mass eigenstates, and the mass values, we must diagonalize.

• Eigenvalues are given by

$$
m_{h_2/h_1}^2 = \frac{\lambda_1}{2}v^2 + \frac{\lambda_\sigma}{2}v_\sigma^2 \pm \frac{1}{2}\sqrt{(2\lambda_3^{H\sigma}vv_\sigma)^2 + (\lambda_1v^2 - \lambda_\sigma v_\sigma^2)^2},\tag{9}
$$

• Additionally, the eigenstates can be obtained via change of basis

$$
\begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = R \cdot \begin{pmatrix} S_H \\ S_\sigma \end{pmatrix},\tag{10}
$$

where R is obtained from

$$
\begin{pmatrix} m_{h_1}^2 & 0 \\ 0 & m_{h_2}^2 \end{pmatrix} = R \mathcal{M}_R^2 R^T; \quad R = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \in \text{SO}(2).
$$

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• Now, neutrino masses can be generated via the Yukawa term $-\mathcal{L} \supset y_{ij} \bar{\ell}_i \tilde{\eta} N_j + \kappa_{ij} \bar{N}_i^c \sigma N_j$. Which induces the 1-loop correction

$$
(\mathcal{M}_{\nu})_{ij} = \sum_{k=1}^{3} \frac{y_{ki} y_{kj}}{32\pi^2} M_{N_k^0} \left[\frac{m_{\eta_R^2}}{m_{\eta_R^2}^2 - M_{N_k^0}^2} \ln \left(\frac{m_{\eta_R^2}^2}{M_{N_k^0}^2} \right) - \frac{m_{\eta_I}^2}{m_{\eta_I}^2 - M_{N_k^0}^2} \ln \left(\frac{m_{\eta_I}^2}{M_{N_k^0}^2} \right) \right],
$$
 (11)
where $M_{N_i^0} = \sqrt{2} \kappa_{ii} v_\sigma$
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Constraints

- The following discussion considers both scalar and fermionic DM scenarios.
- Neutrino oscillation data can be implemented via a modified Casas-Ibarra parametrization

$$
y = \sqrt{\Lambda^{-1}} O \sqrt{\hat{M}_{\nu}} U^{\dagger}, \qquad (12)
$$

where O is a 3×3 orthogonal matrix, U is the PMNS matrix containing all the experimental oscillation data, and $\Lambda = \text{Diag}(\Lambda_i)$ is the matrix containing loop functions:

$$
\Lambda_{i} = \frac{M_{N_{i}^{0}}}{32\pi^{2}} \left[\frac{m_{\eta_{R}}^{2}}{m_{\eta_{R}}^{2} - M_{N_{i}^{0}}^{2}} \ln\left(\frac{m_{\eta_{R}}^{2}}{M_{N_{i}^{0}}^{2}}\right) - \frac{m_{\eta_{I}}^{2}}{m_{\eta_{I}}^{2} - M_{N_{i}^{0}}^{2}} \ln\left(\frac{m_{\eta_{I}}^{2}}{M_{N_{i}^{0}}^{2}}\right) \right]
$$
(13)

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• The DM candidate particle must comply with the current relic density value measured by PLANCK:

 $\Omega_{\chi} h^2 = 0.120 \pm 0.0036$

- To analyze the parameter space that complies with all the constraints we used a Markov Chain Monte Carlo scan.
- Two different m_{h_2} were considered∼ 246 GeV, and 500 GeV

Figure: Projection of the relic density on the dark matter mass, for the two different candidates for dark matter.

• We first analyze the behavior of the DM relic density for the three different v_{σ} cases, independent of the compressed mass spectrum.

Figure: DM relic density as function of the DM mass. Left: Distribution with the different VEV values. Right:Distribution for the two possible DM candidate . Green band: PLANCK results.

• Without imposing any conditions on the $\Delta m = |m_{N_1} - m_{\eta^0}| \rightarrow 89\%$ of all points are $N₁$

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Impact of a compressed mass spectrum

• We now impose $\Delta m = |m_{N_1} - m_{\eta^0}| < 50$ GeV to check the impact of the Δm in the relic density distribution.

Figure: DM relic density as a function of the DM candidate mass. Red dots are solution to DM relic density and green band: PLANCK results. Results are given for $v_{\sigma} = 9 \text{ TeV}$

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- De Romeri, et. al: Considering $\Delta m(N_1, \eta_R)$ very close in mass values (Compressed Mass Spectrum) inside the coannihililation region implies that DM could be produced via DY processes at the LHC!
- Idea: Produce the η as shown in the diagram and let them decay after

considering each DM possibility Figure: Drell-Yan production of a pair of η scalars.

- In the case of Fermion DM production, as it does not couple directly to the SM gauge bosons, we consider $p + p \to \eta^+ + \eta^-$ and allow the $\eta^{\pm} \to N + \ell$ decay.
- We considered the cases $m_{h_2} = 246 \text{ GeV}, 500 \text{ GeV}$ and $v_{\sigma} = 1 \text{ TeV}, 2$, TeV, 3 TeV, 4 TeV, 5 TeV, 6 TeV, and 9 TeV. Additionally, we considered different compressed mass spectra $\sim \Delta m < 20$ GeV, 50 GeV.
- Model was implemented in FeynRules to ensure full compatibility between UFO and MadGraph
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• Dominant intermediate topologies for each scenario:

1. Scalar DM:
$$
p + p \rightarrow \eta_I + \eta_R
$$

2. Fermion DM: $p + p \rightarrow \eta^+ + \eta^-$

Figure: Feynman diagram corresponding to the Drell-Yan production of the components of the η doublet for each DM case before decay. Left: Production of $\eta_I + \eta_R$ for Scalar DM. Right: Production of of $\eta^+ + \eta^-$ for fermion DM.

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- The considered decay chains for the η components were:
	- 1. Scalar DM: $\eta_R \to W^{\pm} + N_i + \ell$ via decay of a η^{\pm} .
	- 2. Fermion DM: $\eta^{\pm} \to N_i \ell$

Figure: Example topology for the decay chain considered for cross section calculation. Left: Example topology for scalar DM production via Drell-Yan. Right: Example topology for fermion DM production via Drell-Yan.

- Spectrum points considered for the cross section calculation \rightarrow compatible with the DM relic density for each candidate scenario.
- Cross section exhibits some randomness whihe arises when including Y_N , λ_i , cos α , etc \rightarrow Random from the MCMC.
- We define a new parameter that contains all the, BRs and interference terms:

$$
\beta = \frac{\sigma(p + p \to N + W^{\pm} + \ell + \eta_I)}{\sigma(p + p \to \eta_R + \eta_I)}
$$
 (Scalar DM)

$$
\beta = \frac{\sigma(p + p \to N + \ell + N + \ell)}{\sigma(p + p \to \eta^+ + \eta^-)}
$$
 (Fermion DM)

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DY-Cross section calculation: Scalar sector

• We calculated the cross section values $@ 1.69$ significance for $\mathcal{L} = \{137, 300, 3000\}$ fb⁻¹ in an optimistic scenario with 20% background, 20% systematic uncertainties and 10% acceptance.

Figure: Behavior of the $p + p \rightarrow \eta_I + W^{\pm} + N_i + \ell$ cross section as a function of the DM candidate particle mass, in the scalar sector, for $\Delta m < 30$ GeV and both m_{h_2} scenarios.

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DY-Cross section calculation: Fermionic sector

- As the final states considered in our analysis are similar to those shown in [arXiv:1911.12606v2\[hep-ex\]](arXiv:1911.12606v2 [hep-ex]) (SUSY), we interpreted their results and applied them to estimate sensitivity for our analysis in scenarios with $\mathcal{L} = \{300, 3000\}$ fb⁻¹.
- The maximum and minimum β values were used to estimate a region where all plausible points of our scan would fall when considering larger statistics.

Figure: Behavior of the $p + p \rightarrow N_i + \ell + N_i + \ell$ cross section as a function of the fermionic DM mass, for $\Delta m < 30$ GeV and both m_{h_2} scenarios. Dashed lines denote the experimental limits taken from ATLAS SUSY studies in compressed mass spectra models.

• One way to probe the purely neutral production of the DM candidates is via Vector Boson Fusion (VBF) or VBF-like processes.

Figure: Feynman diagrams illustrating the production of DM via vector boson fusion (VBF) processes. The scalar DM channel is depicted on the left, while the fermionic channel is shown on the right

- Scenarios with $\Delta m < 50$ GeV were considered to compare results with CMS SUSY results (see [arXiv:1905.13059\[hep-ex\]](arXiv:1905.13059 [hep-ex])).
- CMS results were also used to estimate sensitivity in $\mathcal{L} = \{300, 3000\}$ fb⁻¹ scenarios.

Figure: Left: Analysis performed considering the DM particle as the pseudo-scalar η_I . Right: Analysis performed considering the fermionic DM particle N_1 .

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- Scalar DM production via DY processes at the LHC can not be performed due to very small σ values.
- \bullet σ values obtained for fermionic DM production via DY processes could be probed for M_{DM} between 150 and 220 GeV in future luminosity scenarios at the LHC.
- VBF production of scalar DM could be probed at the LHC for M_{DM} between 150 and 350 GeV in future high luminosity scenarios.
- Fermionic DM production via VBF processes can not be probed at the LHC due to the smallness of the cross section values, showing complementarity between the considered production mechanisms.

Questions and comments

¡Muchas gracias!

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Our study is based on previous work from Valentina De Romeri and collaborators.

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• In this study we fix the masses of the scalars h_1 and h_2 , to 125 GeV and 500 GeV respectively, with the following parametrization of the couplings

$$
\lambda_1 = (m_{h_1}^2 \cos^2 \alpha + m_{h_2}^2 \sin^2 \alpha)/v^2
$$

\n
$$
\lambda_3^{H\sigma} = (m_{h_1}^2 \cos \alpha \sin \alpha - m_{h_2}^2 \cos \alpha \sin \alpha)/vv_{\sigma}
$$

\n
$$
\lambda_{\sigma} = (m_{h_1}^2 \sin^2 \alpha + m_{h_2}^2 \cos^2 \alpha)/v_{\sigma}^2
$$

• The rest of the free parameters of the model have been varied within the same ranges consider by De Romeri et. al.

