

## STCF tracking with ACTS

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## Super Tau-Charm Facility (STCF) physics goals

- A future e+e- collider in China operating at tau-charm region ( $\sqrt{s} = 2^7$  GeV) with peak lumi of 0.5 × 10<sup>35</sup> cm<sup>-2</sup> s<sup>-1</sup> (>x50 of current BEPCII collider)
  - A factory of charmonium (J/ $\psi$ ,  $\psi$ (3686), ...), open charm meson,  $\tau$  ...
- Physics topics:
  - QCD and Hadron spectroscopy (new hadrons, e.g. glueballs, hybrid hadrons...)
  - Flavor physics and CP violation
  - Exotic decays and new physics



#### The detector and performance requirements



See an overview in J.B. Liu's talk

#### ITK (cylindrical MPGD/ CMOS MAPS)

Material < 0.01 X0,  $\sigma_{xv}$  < 100 um

#### **MDC** (drift chamber)

- Material < 0.05 X0
- $\sigma_{xy}$  < 130 um,  $\sigma_p/p$  < 0.5% at 1 GeV/c dE/dx resolution < 6%

#### **RICH** (CsI-MPGD) & **DTOF** (DIRC-like TOF)

PID  $\pi/K$  PID efficiency > 97% up to 2 GeV/c @mis-ID rate 2%

EMC (pure Csl + APD)

 $\sigma_{\rm E}^{}$  < 2.5%,  $\sigma_{
m pos}^{}$  < 5 mm,  $\sigma_{
m t}^{}$  < 300 ps @ 1 GeV

#### **MUD** (RPC + scintillator strips)

 $\mu$  PID efficiency > 95% with  $\pi \rightarrow \mu$  mis-ID rate < 3.3% (a) p = 1 GeV/c

## STCF tracking system



## **ACTS tracking geometry**

- Working approaches to transform full G4 simulation geometry (described with DD4hep) into ACTS geometry through:
  - ACTS TGeo plugin (DD4hep plugin should also work)
  - Acts::KDTreeTrackingGeometryBuilder





- ⇒ 3 MPGD layers  $\rightarrow$  3 layers (one ACTS::CylinderSurface for each layer)
- $\circ \quad 48 \text{ straw layers} \rightarrow 48 \text{ layers with} \\ \text{composed of ACTS::LineSurface} \\$

#### STCF tracking challenges

- Most physics processes have charged particles with  $p_{\tau} < 500$  MeV/c
  - $\circ$  More material effects  $\rightarrow$  worse resolution
  - Looping tracks with  $p_T < 130 \text{ MeV/c} \rightarrow \text{fake/duplicate tracks}$
- Long-lived particles ( $\Lambda$ , K<sub>s</sub>, ...) can decay outside ITK





## ACTS tracking strategy

- ACTS has been integrated into STCF offline software
  - Hough + GenFit has been well optimized
  - ACTS seeding + ACTS CKF is used as second tracking option at STCF (No ambiguity Resolving yet)
  - Hough (as seeding) + ACTS CKF is also being studied for long-lived particle tracking







Details about Hough + GenFit in <u>H. Zhou's CHEP2024 talk</u>

## Performance for non-displaced tracks



#### Particle $\cos\theta$ vs. $p_{\tau}$

 $\mu, \psi$ (3686) $\rightarrow \pi^{+}\pi^{-}J/\psi(\rightarrow \mu^{+}\mu^{-})$ 



π, ψ**(3686)**→ π<sup>+</sup>π<sup>-</sup>J/ψ(→ μ<sup>+</sup>μ<sup>-</sup>)



### Seeding efficiency



>96% seeding efficiency for particles in the

Particle requirements: nHits>=5,  $|\cos\theta|<0.94$ 

## Tracking (seeding + CKF) efficiency



## Tracking fake rate

Almost zero fake rates W/O backgrounds  $\rightarrow$  become non negligible W/ backgrounds



# Performance for displaced tracks



#### Particle $cos\theta$ vs. $p_{\tau}$



## Particle displacement V\_{\_{xy}} vs. p\_{\_{T}}

#### A considerable amount of particles decay outside of first layer of ITK





#### Zero seeding efficiency if $nHits_{ITK} < 3$



Backgrounds not included

## Hough Transform for seeding

- Hough transform is more robust against local hit loss/inefficiency
- ACTS has slightly better seeding efficiency if there are enough hits



#### Hough Transform + CKF performance

Efficiency loss can be recovered by using Hough as seeding



Particle requirements: nHits>=5, |cosθ|<0.94 Track requirements: nHits>=5, matchingProb > 0.5 18

Backgrounds not included

#### Summary

- ACTS has been used as one of the tracking methods at STCF
  - $\circ$  Encouraging performance even at  $p_T$  below 100 MeV
- Obvious seeding efficiency loss for long-lived particles at STCF
  - Hough transform as a global track finding algorithm can recover the seeding efficiency loss
- Non-negligible amount of fake (and also duplicate) tracks exist
- Next:
  - Investigate ML ambiguity resolver to remove fake/duplicate tracks

## backup

## Hough Transform at STCF



#### Backgrounds

#### **Touschek effect**

- · Scattering between inner beam particles
- Generation rate  $\propto N_{\text{bunch}}$ , beam size<sup>-1</sup>, energy<sup>-3</sup>
- Main Background



#### Beam-gas effect

- · Effect with residual gas in the beam pipe
- Coulomb scattering, bremsstrahlung

e±

ITK3

8.2

Ν

60.3

Generation ∝ pressure \_\_\_\_\_

ITK1

37.3

ITK2

13.6

Yupeng Pei

#### Luminosity-related background

• Radiative Bhabha:  $e^+e^- \rightarrow e^+e^-\gamma$ 

• Two-photon process:  $e^+e^- \rightarrow e^+e^-\gamma^*\gamma^* \rightarrow e^+e^-e^+e^-$ 



MDC7

30.8

MDC8

30.0

5

#### Other background

Injection

Background hits count per event

24.8

25.1

MDC1 MDC2 MDC3 MDC4

42.4

· Synchrotron radiation

MDC5 MDC6

67.8

60.0











E			т	τ, ψ <b>(36</b>	686)→	π <sup>+</sup> π <sup>-</sup> <b>J</b> /ι	ψ <b>(</b> → μ	.⁺μ <b>⁻</b> )		45				
ł	W/ backgrounds													
	9.42	10.56	9.69	9.82	9.65	9.39	8.77	7.97						
	13.34	15.89	18.83	17.97	14.96	14.23	11.99	8.93	_	35				
	16.79	26.24	28.97	27.94	20.60	16.90	13.45	9.81						
	18.14	29.37	31.56	31.75	30.32	20.54	13.71	11.25						
5	19.77	32.53	35.32	35.29	37.04	32.74	13.79	10.76		30				
	19.39	33.24	36.89	38.34	40.66	39.71	26.59	11.86						
	18.00	31.25	37.92	40.92	43.30	44.54	35.18	12.18		25				
	17.47	31.96	38.25	40.80	43.87	45.68	43.32	12.90		20				
	18.70	33.14	38.24	40.08	43.46	45.63	43.67	18.20						
	20.78	33.60	37.84	40.11	43.13	45.55	44.63	21.96	_	20				
	21.79	33.89	37.68	39.98	43.80	45.40	43.71	27.00						
	17.80	32.56	38.24	40.79	43.42	45.00	44.37	16.50		15				
	18.73	32.57	37.77	41.03	43.21	44.97	42.77	14.43		15				
	17.58	32.35	39.26	40.68	43.25	42.97	36.50	12.73						
5	19.02	32.88	38.71	39.36	40.54	40.86	23.44	11.37	_	10				
5	18.91	31.33	35.00	35.48	36.84	31.61	13.31	11.49		10				
	17.88	29.50	32.11	31.98	30.70	19.07	14.28	10.00						
	17.13	26.30	29.20	27.54	20.60	16.09	14.28	9.54	-	5				
	13.21	15.85	18.97	17.50	15.15	15.35	11.38	8.79						
4	9.51	10.87	9.69	9.77	9.64	9.19	8.38	7.73		0				
, 9.51   10.87   9.69   9 5 0.1 0.15 0.2	10.87   9.69   9 1 0.15 0.2	15 0.2	.2	.77 0.	25 0	.3 0. F	35 0 eco p_	4 0.4 [GeV/c]	45	0				

Reco cos0



Reco cos0

$ \begin{array}{c} 0.3 \ \end{array}{c} 0.3 \ \begin{array}{c} 0.3 \ \begin{array}{c} 0.3 \ \begin{array}{c} 0.3 \ \end{array}{c} 0.3 \ \end{array}{c} 0.3 \ \begin{array}{c} 0.3 \ \begin{array}{c} 0.3 \ \end{array}{c} 0.3$		ourity 1	cos0		_				π, ι	ψ <b>(3</b>	686	)→	π <sup>+</sup> π <sup>-</sup> J	/ψ <b>(</b> →	,	ι⁺μ <sup>-</sup> )	)	_	0.9 c
$ \begin{array}{c} 0.8 \\ \hline \\ 0.8 \\ \hline \\ 0.7 \\ 0.6 \\ 0.6 \\ 0.6 \\ 0.5 \\ 0.6 \\ 0.5 \\ 0.6 \\ 0.7 \\ 0.6 \\ 0.5 \\ 0.8 \\ 0.8 \\ 0.9 \\ 0.8 \\ 0.9 \\ 0.8 \\ 0.9 \\ 0.9 \\ 0.8 \\ 0.9 \\ 0.9 \\ 0.8 \\ 0.9 \\ 0.$		0.90	00		-							W	// back	grou	Ine	ds			2.0.2 
$ \begin{array}{c} 0.7 \\ 0.7 \\ 0.6 \\ 0.5 \\ 0.6 \\ 0.7 \\ 0.6 \\ 0.7 \\ 0.6 \\ 0.7 \\ 0.6 \\ 0.7 \\ 0.8 \\ 0.8 \\ 0.9 \\ 0.8 \\ 0.9 \\ 0.8 \\ 0.9 $		0.8 2	Re	1	0.90		0.90	0.85		0.86	C	.87	0.86	0.8	36	0.	.83	_	0.8
$ \begin{array}{c} 0.7 \\ 0.6 \\ 0.5 \\ 0.8 \\ 0.8 \\ 0.8 \\ 0.8 \\ 0.8 \\ 0.9 \\ 0.8 \\ 0.8 \\ 0.9 \\ 0.8 \\ 0.9 $		-10.0			0.93		0.95	0.94		0.90	C	.88	0.88	0.8	34	0	.81		
$ \begin{array}{c} 0.7 \\ 0.6 \\ 0.5 \\ 0.7 \\ 0.6 \\ 0.7 \\ 0.8 \\ 0.7 \\ 0.8 \\ 0.7 \\ 0.8 \\ 0.7 \\ 0.8 \\ 0.9 $		0.7			- 0.88		0.93	0.95		0.96	C	0.90	0.90	0.8	37	0.	.84	-	0.7
$ \begin{array}{c} 0.6 \\ 0.5 \\ 0.6 \\ 0.78 \\ 0.90 \\ 0.91 \\ 0.80 \\ 0.91 \\ 0.94 \\ 0.94 \\ 0.96 \\ 0.97 \\ 0.97 \\ 0.97 \\ 0.97 \\ 0.98 \\ 0.98 \\ 0.99 \\ 0.97 \\ 0.98 \\ 0.99 \\ 0.97 \\ 0.98 \\ 0.99 \\ 0.97 \\ 0.98 \\ 0.99 \\ 0.97 \\ 0.98 \\ 0.99 \\ 0.97 \\ 0.98 \\ 0.99 \\ 0.97 \\ 0.98 \\ 0.99 \\ 0.97 \\ 0.98 \\ 0.99 \\ 0.97 \\ 0.98 \\ 0.99 \\ 0.97 \\ 0.98 \\ 0.99 \\ 0.97 \\ 0.99 \\ 0.98 \\ 0.99 \\ 0.97 \\ 0.99 \\ 0.98 \\ 0.99 \\ 0.97 \\ 0.99 \\ 0.98 \\ 0.99 \\ 0.98 \\ 0.99 \\ 0.98 \\ 0.99 \\ 0.98 \\ 0.99 \\ 0.98 \\ 0.99 \\ 0.98 \\ 0.99 \\ 0.98 \\ 0.99 \\ 0.98 \\ 0.98 \\ 0.99 \\ 0.98 \\ 0.99 \\ 0.98 \\ 0.98 \\ 0.99 \\ 0.98 \\ 0.98 \\ 0.98 \\ 0.99 \\ 0.91$		0.7			_ 0.84		0.92	0.95		0.96	0	0.96	0.91	0.8	36	0.	.85		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$			0.	.5	0.84		0.92	0.95		0.96	C	).97	0.95	0.8	37	0.	.86		0.6
$ \begin{array}{c} 0.5 \\ 0.6 \\ 0.4 \\ 0.3 \\ 0.2 \\ 0.1 \\ 0.6 \\ 0.1 \\ 0.6 \\ 0.5 \\ 0.7 \\ 0.8 \\ 0.8 \\ 0.9 \\ 0.8 \\ 0.9 $	-	0.6			0.82		0.92	0.94		0.96	C	).97	0.97	0.9	92	0.	.83	-	0.0
$ \begin{array}{c} 0.5 \\ 0.4 \\ 0.3 \\ 0.2 \\ 0.1 \\ 0.1 \\ 0.2 \\ 0.1 $					- 0.78		0.90	0.94		0.96	C	).98	0.98	0.9	95	0.	.88		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		0.5		-	_ 0.78		0.90	0.95		0.97	C	.98	0.98	0.9	97	0.	.84		0.5
$ \begin{array}{c} -0.4 \\ 0.4 \\ 0.3 \\ -0.2 \\ 0.1 \\ 0.$		0.0			- 0.80		0.91	0.94		0.96	C	0.98	0.99	0.9	97	0.	.84		
$ \begin{array}{c} 0.4 \\ 0.3 \\ 0.2 \\ 0.1 \\ 0.1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ $		~ .		0	0.81		0.91	0.94		0.96	C	).97	0.99	0.9	98	0.	.89		0.4
$ \begin{array}{c} 0.3 \\ 0.2 \\ 0.1 \\ 0.1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ $	-	0.4		Ĭ	- 0.84		0.91	0.94		0.96	C	.98	0.98	0.9	97	0.	.92		0.4
$ \begin{array}{c} 0.3 \\ 0.2 \\ 0.1 \\ 0.1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ $					0.80		0.90	0.94		0.96	C	0.98	0.98	0.9	98	0.	.84		
$ \begin{array}{c} -0.2 \\ -0.5 \\ -0.8 \\ 0.8 \\ 0.9 \\ 0.8 \\ 0.9 \\ 0$	_	0.3			0.80		0.91	0.94		0.96	C	).97	0.98	0.9	97	0.	.87		0.3
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$					_ 0.79		0.91	0.95	65 - C	0.96	C	0.98	0.97	0.9	95	0.	.85		
$ \begin{array}{c} 0.2 \\ 0.1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ $		0.0	-0	5	0.81		0.91	0.95		0.96	C	0.97	0.98	0.8	39	0.	.82		02
$ \begin{array}{c} -0.1 \\ \hline 0.1 \\ \hline 0.05 \\ 0.05 \\ 0.05 \\ 0.1 \\ \hline 0.05 \\ 0.1 \\ \hline 0.05 \\ 0.1 \\ \hline 0.05 \\ 0.1 \\ 0.05 \\ 0.1 \\ 0.05 \\ 0.1 \\ 0.05 \\ 0.1 \\ 0.05 \\ 0.15 \\ 0.95 \\ 0.95 \\ 0.95 \\ 0.96 \\ 0.91 \\ 0.96 \\ 0.96 \\ 0.91 \\ 0.96 \\ 0.96 \\ 0.91 \\ 0.96 \\ 0.96 \\ 0.91 \\ 0.96 \\ 0.96 \\ 0.91 \\ 0.96 \\ 0.96 \\ 0.91 \\ 0.96 \\ 0.96 \\ 0.91 \\ 0.96 \\ 0.96 \\ 0.91 \\ 0.96 \\$		0.2	0.		_ 0.83		0.91	0.95		0.96	C	).97	0.95	0.8	36	0.	.84		0.2
$ \begin{array}{c} 0.1 \\ \begin{array}{c} 0.88 \\ 0.93 \\ 0.93 \\ 0.94 \\ 0.94 \\ 0.94 \\ 0.90 \\ 0.88 \\ 0.88 \\ 0.88 \\ 0.88 \\ 0.88 \\ 0.88 \\ 0.85 \\ 0.79 \\ 0.85 \\ 0.95 \\ 0.1 \\ 0.15 \\ 0.2 \\ 0.25 \\ 0.3 \\ 0.35 \\ 0.45 \\ $					0.86		0.92	0.95		0.96	C	0.96	0.91	0.8	36	0.	.82		
$ \begin{array}{c} 0.93 \\ 0.94 \\ 0.94 \\ 0.90 \\ 0.88 \\ 0.88 \\ 0.88 \\ 0.88 \\ 0.88 \\ 0.88 \\ 0.88 \\ 0.85 \\ 0.85 \\ 0.85 \\ 0.85 \\ 0.85 \\ 0.88 \\ 0.85 \\ 0$	_	0.1			0.88		0.93	0.96		0.95	(	0.91	0.88	0.8	38	0.	.83		0.1
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$					_ 0.93		0.94	0.94		0.90	C	.88	0.88	0.8	35	0.	.79		
$5^{\circ}$ 0.05 0.1 0.15 0.2 0.25 0.3 0.35 0.4 0.45		0	_	_1	0.91	r L r	<b>9.90</b>	0.86	1.1.1	0.86		.86	0.87	0.8	35	<u>9</u>	.85		0
Booo n (Co)//ol	5	0		0:0	)5	0.1	0.	15	0.2	0	.25		0.3 0	.35	C	1.4	<u>0.4</u>	45	0
Reco p <sub>1</sub> [Gev/c]														Reco	p_	[Ge	eV/c]		



Reco cos0

					μ	,ψ(	368	6)→ W	π⁺г / <b>ba</b>	t <sup>-</sup> J/ψ ckg	(→ rour	µ⁺µ` nds	.)		ck purity
2 1	0.936	0.970	0.917	0.888	0.887	0.899	0.895	0.892	0.890	0.905	0.879	0.862	0.865		088
	0.858	0.963	0.987	0.991	0.984	0.930	0.884	0.900	0.904	0.908	0.905	0.888	0.870		<sup>0.0</sup> ⊢
	0.853	0.866	0.906	0.963	0.994	0.997	0.994	0.960	0.923	0.926	0.929	0.898	0.883		07
	0.868	0.884	0.885	0.892	0.941	0.993	0.998	0.997	0.984	0.940	0.948	0.936	0.900		0.7
05	0.867	0.882	0.888	0.905	0.909	0.941	0.994	0.998	0.997	0.992	0.949	0.945	0.891		
0.5	0.864	0.877	0.888	0.897	0.920	0.934	0.953	0.993	0.998	0.998	0.996	0.933	0.885	-	0.6
	0.882	0.888	0.899	0.915	0.919	0.929	0.952	0.975	0.998	0.999	0.998	0.985	0.949		
	0.880	0.893	0.910	0.912	0.918	0.934	0.956	0.967	0.997	0.999	0.999	0.998	0.966		05
	0.867	0.876	0.904	0.914	0.919	0.915	0.907	0.943	0.994	0.998	0.999	0.997	0.987		0.5
0	0.881	0.893	0.915	0.920	0.929	0.906	0.953	0.936	0.984	0.997	0.997	0.997	0.988		0.4
Ű	0.882	0.890	0.910	0.917	0.923	0.940	0.935	0.948	0.987	0.998	0.999	0.998	0.990		0.4
	0.881	0.876	0.892	0.920	0.910	0.900	0.926	0.967	0.993	0.997	0.998	0.998	0.988		
	0.885	0.880	0.895	0.896	0.937	0.916	0.920	0.934	0.993	0.998	0.998	0.996	0.981	-	0.3
	0.871	0.883	0.906	0.903	0.902	0.929	0.956	0.981	0.997	0.998	0.998	0.993	0.936		
-0.5	0.861	0.884	0.911	0.902	0.905	0.919	0.955	0.995	0.998	0.997	0.993	0.940	0.897		02
	0.872	0.890	0.889	0.907	0.913	0.935	0.993	0.998	0.998	0.992	0.950	0.912	0.907		0.2
	0.864	0.875	0.895	0.900	0.930	0.992	0.998	0.997	0.984	0.938	0.934	0.926	0.882		~ 1
	0.840	0.864	0.898	0.969	0.994	0.996	0.992	0.939	0.904	0.923	0.932	0.900	0.870		0.1
	0.847	0.957	0.988	0.990	0.982	0.935	0.922	0.899	0.906	0.906	0.905	0.865	0.864		
-1	0.946	0.972	0.916	0.886	0.887	0.892	0.882	0.899	0.886	0.894	0.8/3	0.858	0.855		0
	' 0.6 0.8 1 1.2 1.4 1.6 1.8 Recop <sub>T</sub> [GeV/c]												8	-	

Reco cos0

	_				μ	,ψ(	368	6)→ ₩	π⁺π /Ω h	τ <b>΄ J</b> /ψ	(→	µ⁺µ`	)	_	1 purity 1
1	0.000	0.000	0.002	0.092	0.069	0.079	0.096	0.052	0.051		grui	1 000	1 000		g, j
	0.999	0.999	1 000	1 000	1 000	0.970	0.900	0.952	0.931	0.904	0.950	0.900	0.944	_	0.8 🛎
1	0.946	0.975	0.991	0.999	1.000	1.000	1.000	0.999	0.965	0.980	0.955	0.944	0.931		
3	0.980	0.991	0.952	0.971	0.994	1.000	1.000	1.000	1.000	0.995	0.987	1.000	0.969	_	0.7
~ -	0.940	0.987	0.996	0.978	0.990	0.990	0.999	1.000	1.000	1.000	0.986	0.980	1.000		
0.5	0.910	0.939	0.995	0.990	0.991	1.000	1.000	1.000	1.000	1.000	1.000	0.980	0.891		0.6
	0.972	0.957	0.996	0.993	0.991	0.997	0.996	0.999	1.000	1.000	1.000	0.999	1.000		0.0
	0.965	0.944	0.994	0.998	0.994	1.000	0.994	1.000	1.000	1.000	1.000	1.000	1.000		0.5
	0.951	0.978	1.000	0.991	1.000	0.999	0.969	1.000	1.000	1.000	1.000	1.000	1.000		0.5
0	0.953	0.963	0.988	0.974	0.994	0.986	0.988	1.000	1.000	1.000	1.000	1.000	1.000		
U	0.948	0.958	0.987	0.990	0.990	0.989	1.000	1.000	1.000	1.000	1.000	1.000	1.000	-	0.4
	0.948	0.980	0.992	0.996	0.993	0.991	0.978	1.000	0.998	1.000	1.000	1.000	0.996		
	0.989	0.904	0.991	0.990	0.994	0.988	1.000	0.996	1.000	1.000	1.000	0.999	1.000	_	0.3
	0.954	0.988	0.987	0.983	1.000	0.986	0.993	1.000	1.000	1.000	1.000	1.000	1.000		
-0.5	0.978	0.978	0.988	0.992	0.983	0.997	0.996	1.000	1.000	1.000	1.000	0.996	1.000		0.2
0.0	0.951	0.979	0.990	0.997	0.997	0.994	1.000	1.000	1.000	1.000	0.995	0.979			0.2
1	0.953	0.977	0.993	0.988	0.995	1.000	1.000	1.000	0.999	0.990	0.962	1.000	1.000		
	0.949	0.967	0.974	0.998	1.000	1.000	1.000	0.996	0.987	0.931	0.981	0.778	0.936		0.1
	0.975	0.998	1.000	1.000	0.999	0.995	0.961	0.934	0.914	0.895	0.889		1.000		
-1	0.998	1.000	0.995	0.962	0.985	0.958	0.975	0.955	0.949	1.000	<u> </u>	0.944	0.833		0
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$													8	

Reco cos0