

Charm production in the dipole approach

Introduction

Charm structure function

Charm pt distribution in eA

Charm production in pp and pA

Summary

(focus on saturation effects)

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IFUSP / BRAZIL

Introduction

Why charm ?

Heavy enough for perturbative QCD

Light enough to be abundant

more important at low x $F_2^c \cong 0.25 F_2$

$m_c \sim Q_s$ saturation effects ?

How to calculate ?

Collinear factorization + DGLAP evolution

KT factorization + unintegrated gluon densities

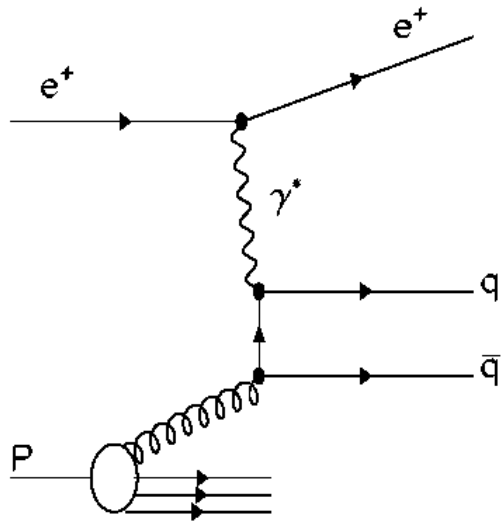
Color dipole + dipole cross section

Zotov's talk

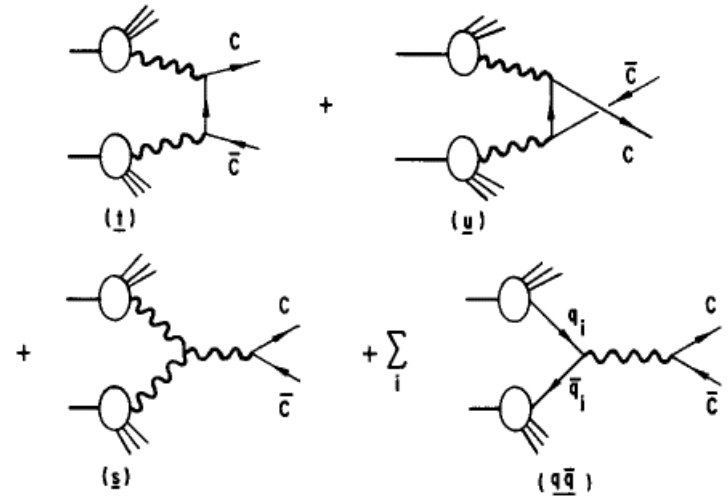
Dipoles: **easy inclusion of saturation effects**

Nikolaev, Zakharov (1991),
A. Müller (1994)

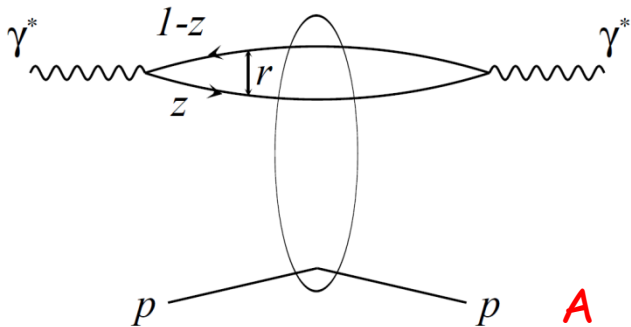
ep: boson-gluon fusion



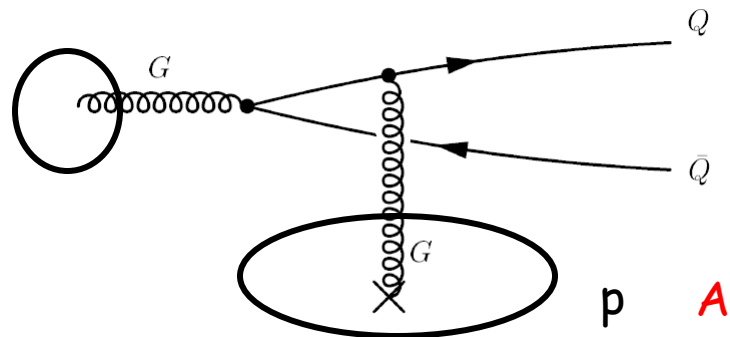
pp: gluon-gluon fusion



color (singlet) dipole



color (octet) dipole



Charm structure function in eA

$$F_2^A(x, Q^2) = \frac{Q^2}{4\pi^2 \alpha_{em}} (\sigma_T + \sigma_L)$$

Albacete's talk

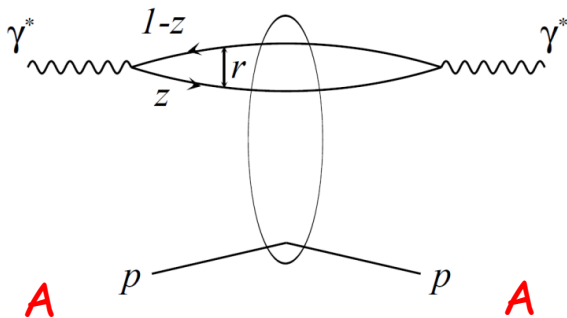
Stasto's talk

$$\sigma_{T,L} = \int d^2r d\alpha |\Psi_{T,L}(r, \alpha, Q^2)|^2 \sigma_{dA}(x, r)$$

$$\sigma_{dA}(x, r) = 2 \int d^2b N_A(x, r, b)$$

$$N_A(x, r, b) = 1 - \exp \left[-\frac{1}{2} \sigma_{dp}(x, r) T_A(b) \right]$$

Armesto (2002)



QCD input: in the dipole - proton cross section !

Dipole - proton cross section

Golec-Biernat - Wüsthoff	GBW (1998)
Bartels - Golec-Biernat - Kowalski	BGK (2002)
Kowalski - Teaney	IPsat (2003)
Iancu - Itakura - Munier	IIM (2004)
Kharzeev - Kovchegov - Tuchin	KKT (2004)
Kowalski - Motyka - Watt	bCGC (2006)
Dumitru - Hayashigaki - Jalilian-Marian	DHJ (2006)
Gonçaves - Kugeratski - Machado - Navarra	GKMN (2006)
Marquet - Peshanski - Soyez	MPS (2007)
Boer - Utermann - Wessels	BUW (2008)
Albacete - Armesto - Milhano - Salgado	rcBK (2009)

(and others...sorry for omissions)

Linear limit with dipoles

dp

GBW	$N(x, r) = 1 - \exp \left\{ -\frac{1}{4} (r^2 Q_s^2) \right\}$	$r \rightarrow 0$ 	$N(x, r) \cong \frac{1}{4} (r^2 Q_s^2)$
KKT	$N(x, r) = 1 - \exp \left\{ -\frac{1}{4} (r^2 Q_s^2)^\gamma \right\}$		$N(x, r) \cong \frac{1}{4} (r^2 Q_s^2)^\gamma$
IIM	$N(x, r) = \begin{cases} N_0 \left(\frac{r Q_s}{2} \right)^{2 \gamma_{eff}} \\ 1 - \exp[-a \ln^2(b r Q_s)] \end{cases}$	$r Q_s < 2$ $r Q_s > 2$	<p style="color: red;">linear</p> <p style="color: red;">saturation</p>
rcBK	(all numerical)		

dA

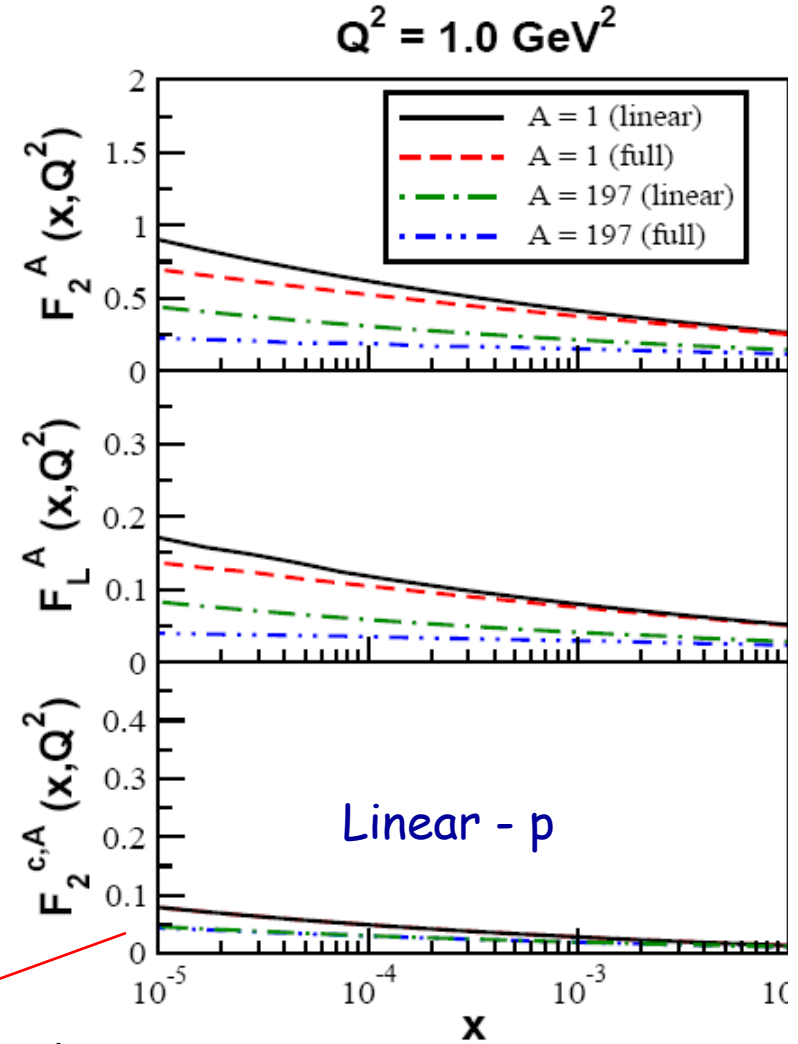
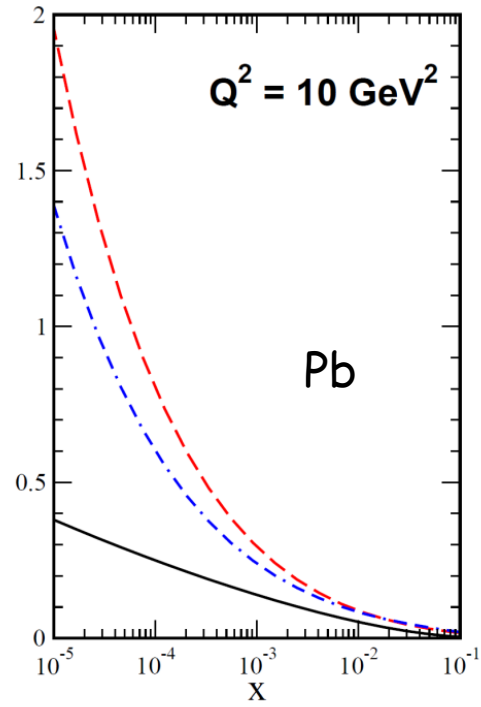
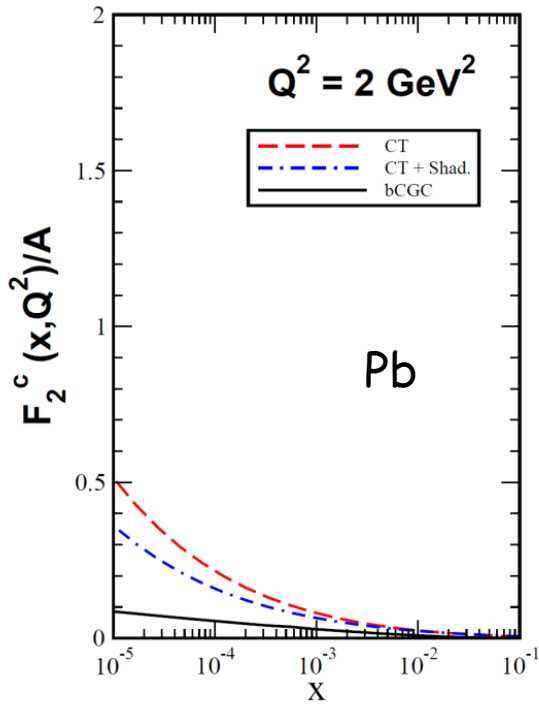
Mixed description: $\sigma_{dA}(x, r^2) = \frac{\pi^2}{3} r^2 \alpha_s x g_A(x, Q^2)$

{	$x g_A(x, Q^2) = A x g_N(x, Q^2)$	}	Color transparency (CT)
	g_N from GRV98		
{	$x g_A(x, Q^2) = A R_g(x, Q^2) x g_N(x, Q^2)$	}	Color transparency + Shadowing (CT + Shad)
	R_g from EKS98		

Linear - p:

$$N_A(x, r, b) = 1 - \exp\left[-\frac{1}{2} \sigma_{dp}(x, r) T_A(b)\right] \quad \sigma_{dp} = \text{linear}$$

Charm structure function in eA



Gonçalves, Kugerastski, Navarra (2010)

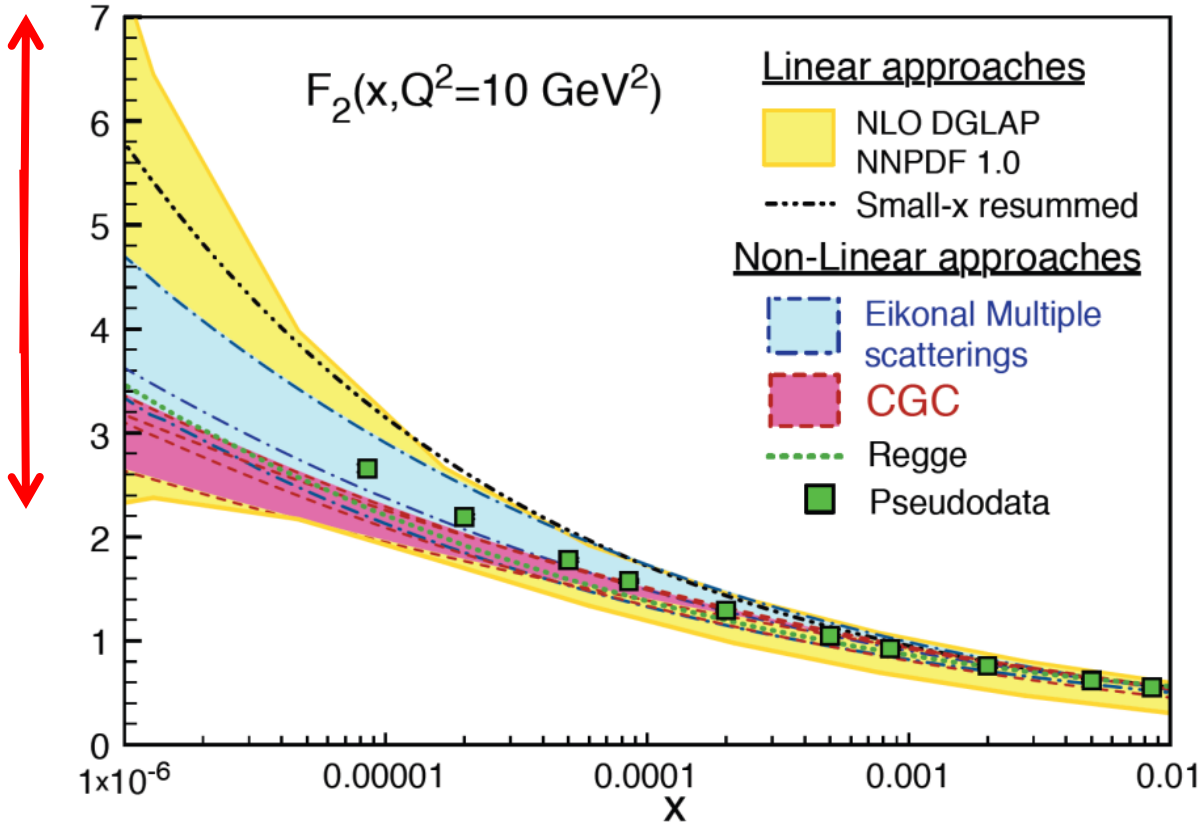
Saturation: reduction by a factor 3 to 4 at $x = 10^{-5}$

Almost no reduction

Gonçalves, Kugerastski, Navarra (2005)

Linear - p

Linear limit without dipoles



Saturation: reduction by a factor ~ 2

Stasto's talk

Linear limit without dipoles

Collinear factorization approach:

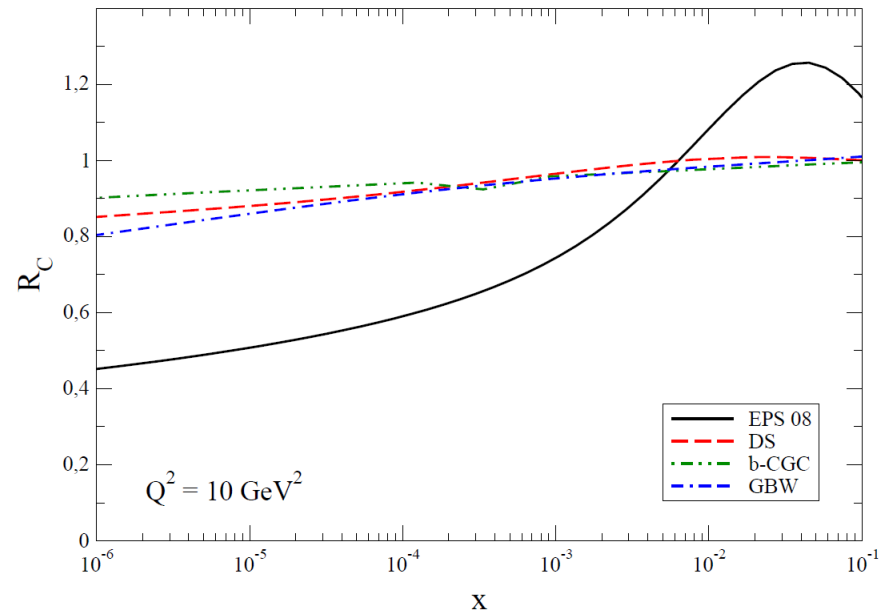
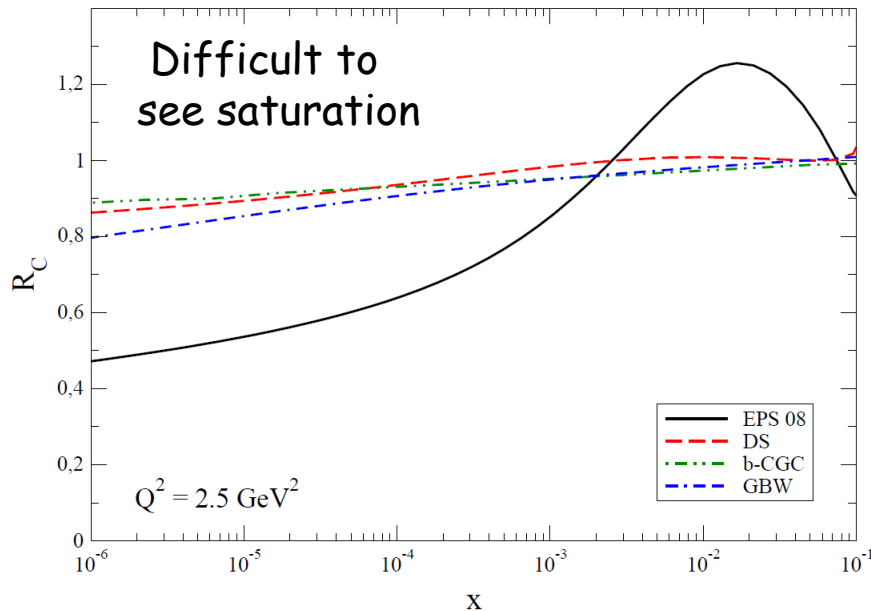
$$R_c = \frac{F_2^{cA}}{A F_2^{cp}}$$

$$\frac{1}{x} F_2^c(x, Q^2, m_c) = e_c^2 \frac{\alpha_s(\mu^2)}{2\pi} \int_{ax}^1 \frac{dy}{y} C\left(\frac{x}{y}, \xi\right) g(x, \mu^2)$$

$C(z, \xi) =$ Coefficient function from pQCD

$$x g_A(x, Q^2) = \begin{cases} \text{DS: de Florian, Sassot (2004)} \\ \text{EPS: Eskola, Paukkunen, Salgado (2008)} \end{cases}$$

Cazaroto, Gonçalves, Carvalho, Navarra (2009)



eA

Heavy quark pt distribution

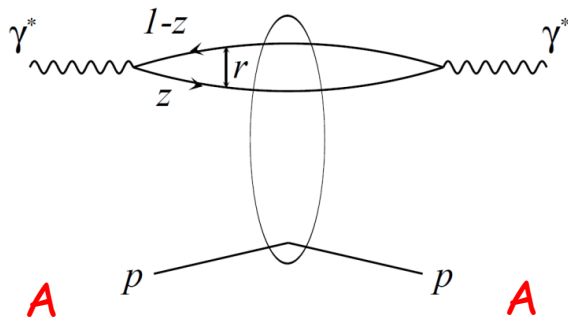
$$\frac{d\sigma(\gamma^* A \rightarrow Q X)}{d^2p_Q^\perp} = \frac{6e_Q^2\alpha_{em}}{(2\pi)^2} \int d\alpha \left\{ \left[m_Q^2 + 4Q^2\alpha^2(1-\alpha)^2 \right] \left[\frac{I_1}{p_Q^{\perp 2} + \epsilon^2} - \frac{I_2}{4\epsilon} \right] + \left[\alpha^2 + (1-\alpha)^2 \right] \left[\frac{p_Q^\perp \epsilon I_3}{p_Q^{\perp 2} + \epsilon^2} - \frac{I_1}{2} + \frac{\epsilon I_2}{4} \right] \right\}$$

$$I_1 = \int dr r J_0(p_Q^\perp r) K_0(\epsilon r) \sigma_{dA}(\mathbf{r})$$

$$I_2 = \int dr r^2 J_0(p_Q^\perp r) K_1(\epsilon r) \sigma_{dA}(\mathbf{r})$$

$$I_3 = \int dr r J_1(p_Q^\perp r) K_1(\epsilon r) \sigma_{dA}(\mathbf{r})$$

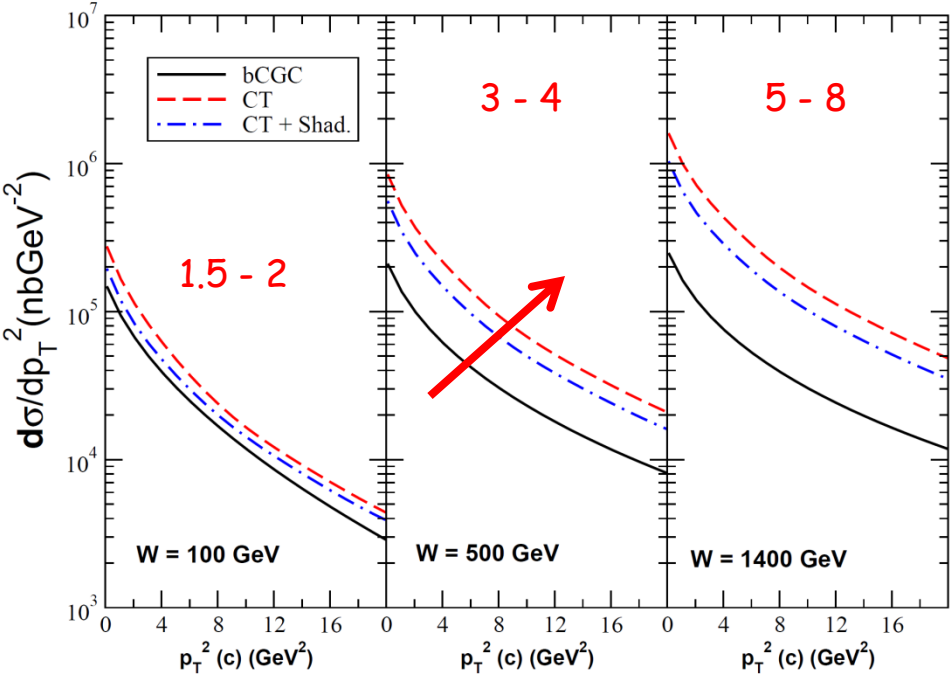
Flöter, Kopeliovich,
Pirner, Raufeisen
(2007)



$$\epsilon = \alpha(1-\alpha)Q^2 + m^2$$

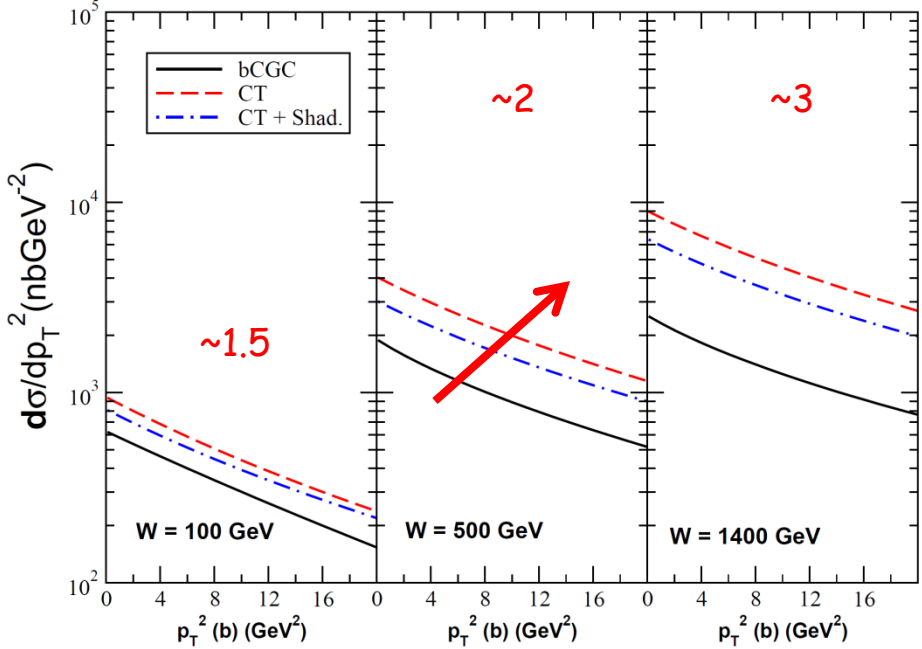
eA

$$Q^2 = 2 \text{ GeV}^2$$



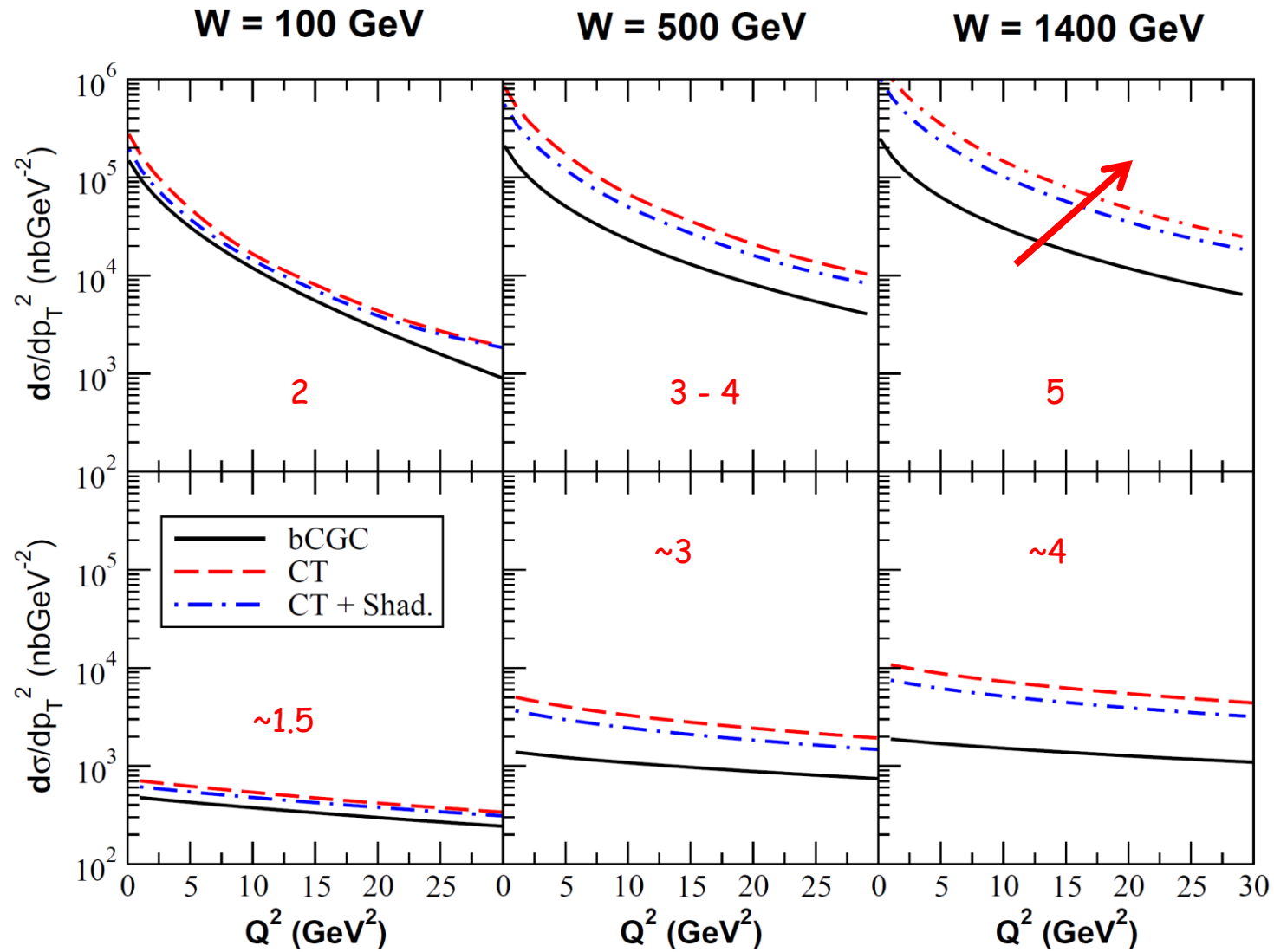
charm

Gonçalves,
Kugerastski,
Navarra
(2010)



bottom

eA



charm

Gonçalves,
Kugerastski,
Navarra
(2010)

bottom

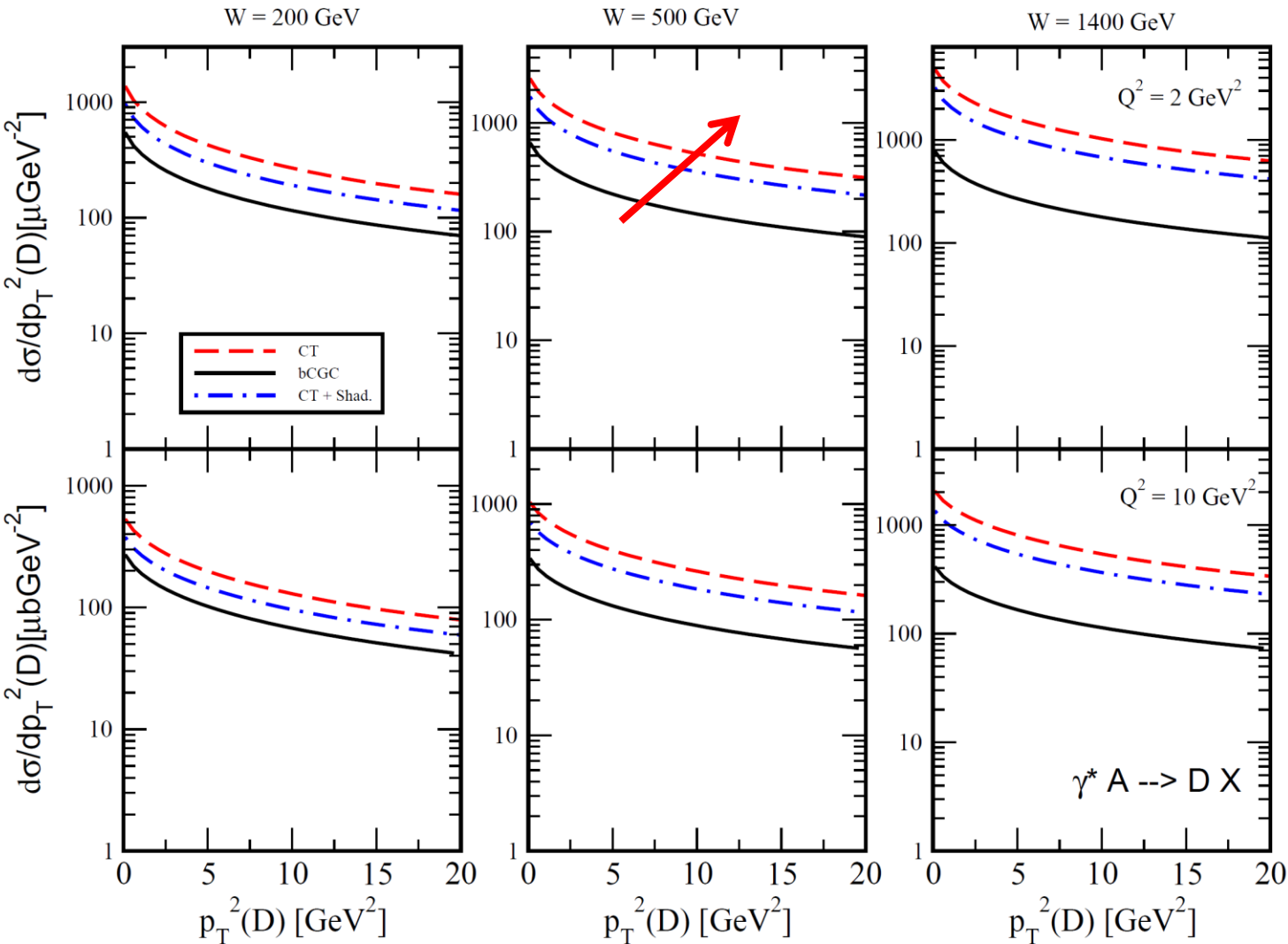
$$p_T^2 = 4 \text{ GeV}^2$$

eA

D meson pt distribution

$$\frac{d\sigma(\gamma^* A \rightarrow DX)}{dz d^2p_D^\perp} = \int \frac{dp_c^\perp d\alpha}{\alpha} \frac{d\sigma(\gamma^* A \rightarrow cX)}{d^2p_c^\perp d\alpha} D_D^c\left(\frac{z}{\alpha}\right) \delta\left(p_D^\perp - \frac{z}{\alpha} p_c^\perp\right)$$

Peterson fragment.



Gonçalves,
Kugerastski,
Navarra
(2010)

Charm production in pA collisions

Kopeliovich,
Tarasov
(2002)

$$\frac{d\sigma\{p p \rightarrow Q\bar{Q} X\}}{dy} = x_1 G(x_1, \mu^2) \sigma\{g p \rightarrow Q\bar{Q} X\}$$

$$\sigma\{g N \rightarrow Q\bar{Q} X\} = \int_0^1 d\alpha \int_0^1 d^2\rho |\Psi_{g \rightarrow Q\bar{Q}}(\alpha, \rho)|^2 \sigma_{gq\bar{q}}(\alpha, \rho)$$

$$|\Psi_{g \rightarrow Q\bar{Q}}(\alpha, \rho)|^2 = \frac{\alpha_s(\mu^2)}{(2\pi)^2} \{ m_Q^2 K_0^2(m_Q \rho) + (\alpha^2 + \bar{\alpha}^2) m_Q^2 K_1^2(m_Q \rho) \}$$

$$\sigma_{gq\bar{q}}(\alpha, \rho) = \frac{9}{8} [\sigma_{dp}(\alpha\rho) + \sigma_{dp}(\bar{\alpha}\rho)] - \frac{1}{8} \sigma_{dp}(\rho)$$

$$\sigma\{p p \rightarrow Q\bar{Q} X\} = 2 \int_0^{\ln(\sqrt{s}/2m_Q)} dy x_1 G(x_1, \mu^2) \sigma\{g p \rightarrow Q\bar{Q} X\}$$

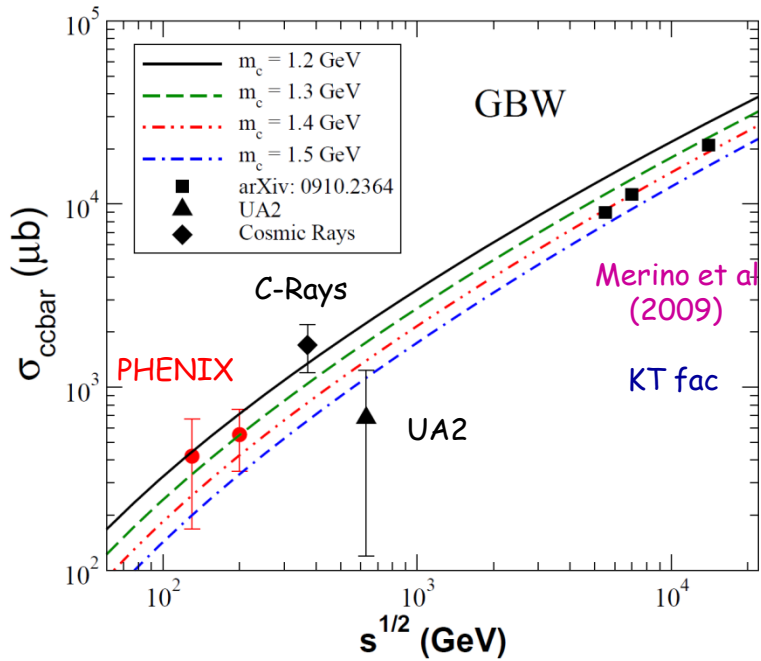
$$G(x_1) = \text{GRV 98} \quad \mu^2 = m_c^2$$

$$x_1 = \frac{2 m_Q e^y}{\sqrt{s}}$$

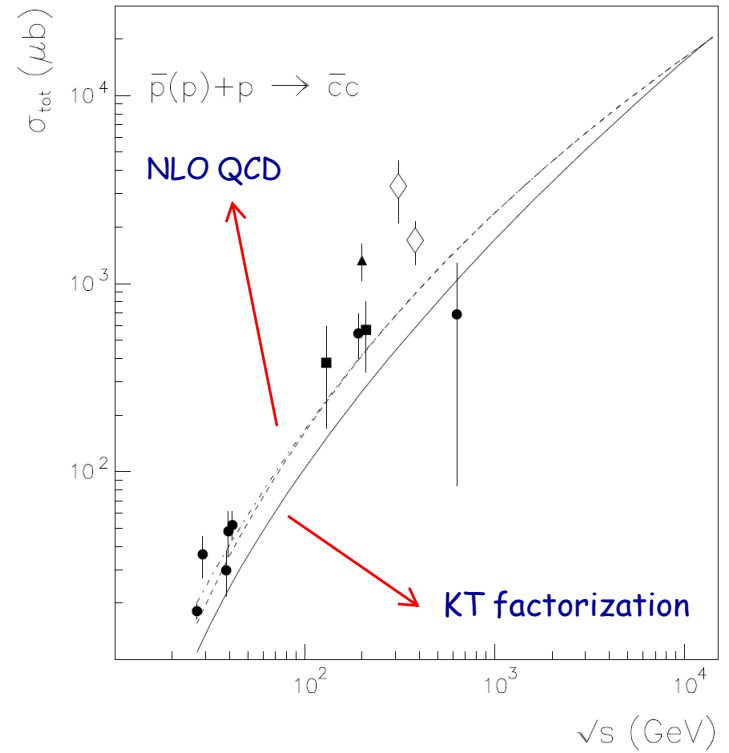
$$x_2 = \frac{2 m_Q e^{-y}}{\sqrt{s}}$$

$$y = \frac{1}{2} \ln \left(\frac{x_1}{x_2} \right)$$

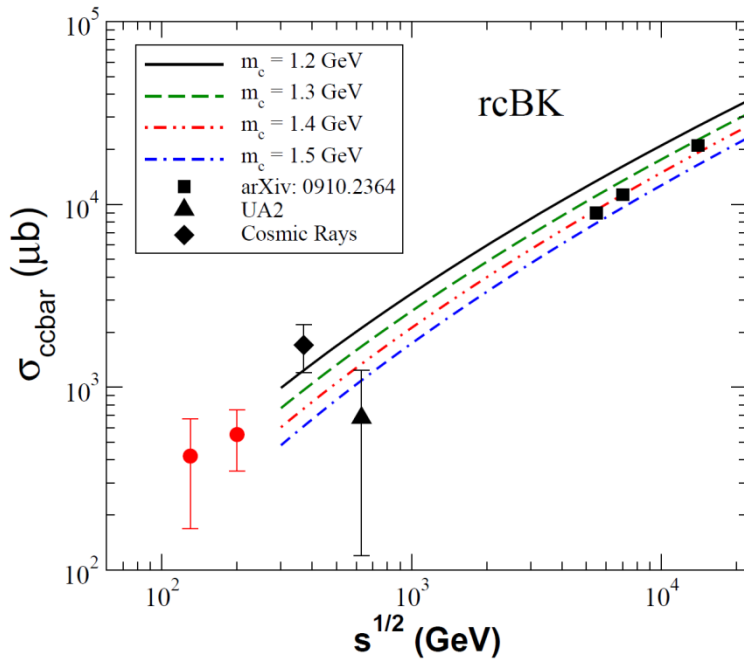
pp



C-Rays
nucl-ex/0607015



Merino,Pajares,Ryzhinskiy,
Shabelski,Shuvaev,
arXiv:0910.2364



Cazaroto,
Gonçalves,
Navarra
in progress

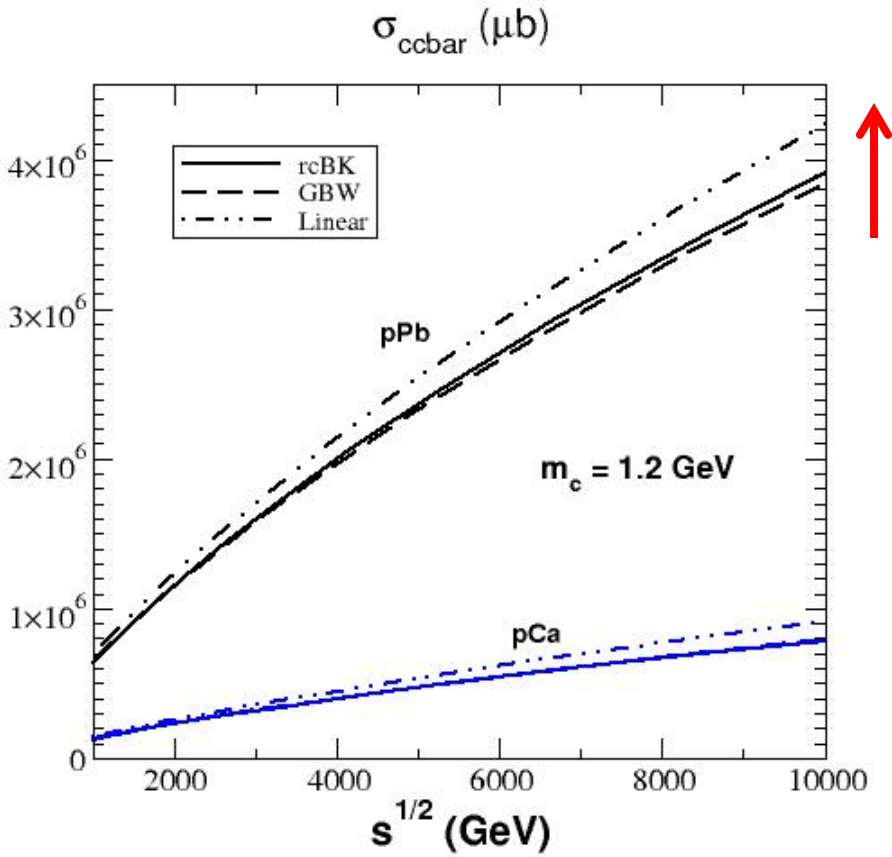
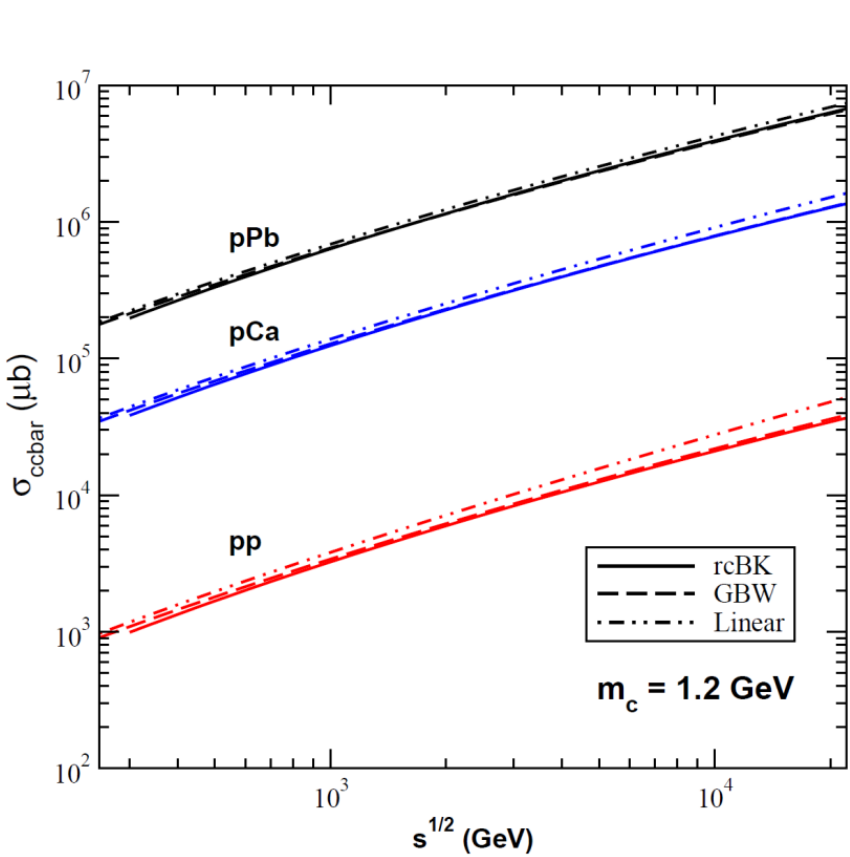
pA

Total cross section

$$\sigma_{dA} = 2 \pi \int_0^{R_A} d b b [2 (1 - \exp [- \frac{1}{2} \sigma_{dp} T_A(b)])]$$

linear p

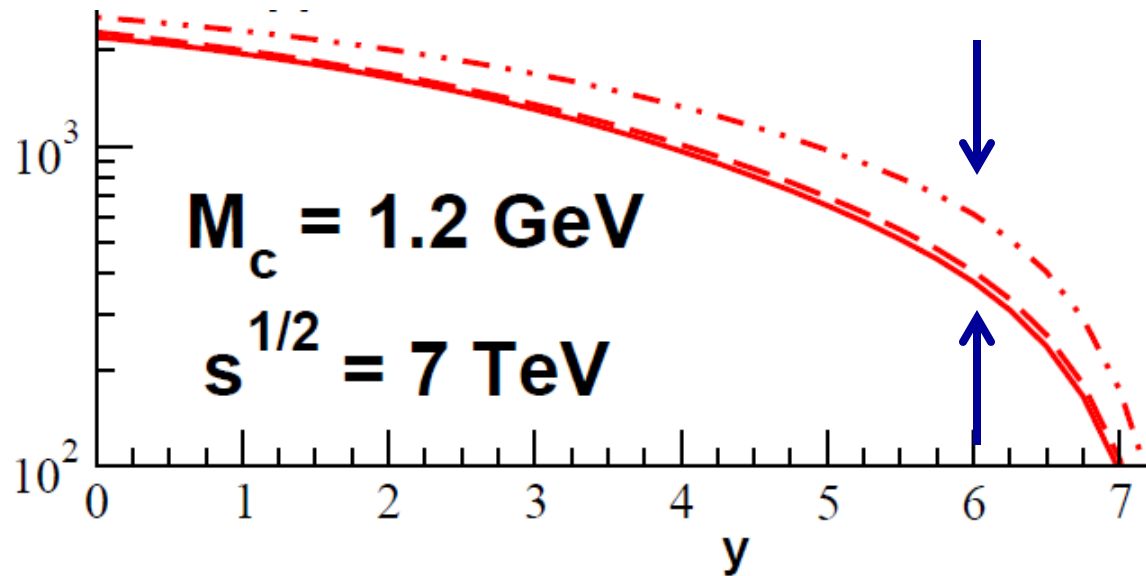
$$\sigma_{dp} = \frac{\sigma_0}{4} Q_s^2 \rho^2$$



Saturation: reduction by 10 % with x going down to $x_2 = 10^{-6}$

Rapidity distribution

$$\frac{d\sigma\{pp \rightarrow Q\bar{Q}X\}}{dy}$$



Saturation: reduction by 1.7 at $y = 6$

Summary

Well established dipole model for charm production in ep, eA, pp and pA

Different ways to estimate the linear predictions in eA and pA:

{ CT (overestimates linear regime)
CT+Shad
Linear p (underestimates linear regime)

F2c: almost no suppression with (linear-p)

F2c: large suppression factors (3 - 4) with (CT, CT+Shad)

Rc: no sign of saturation

F2c: large suppression factors (2) in other approaches

eA @ 1TeV: large suppression factors (1.5 - 8) in dN/d pt (CT, CT+Shad)

Dipole models reproduce well the data on $\sigma(p + p \rightarrow Q \bar{Q} + X)$

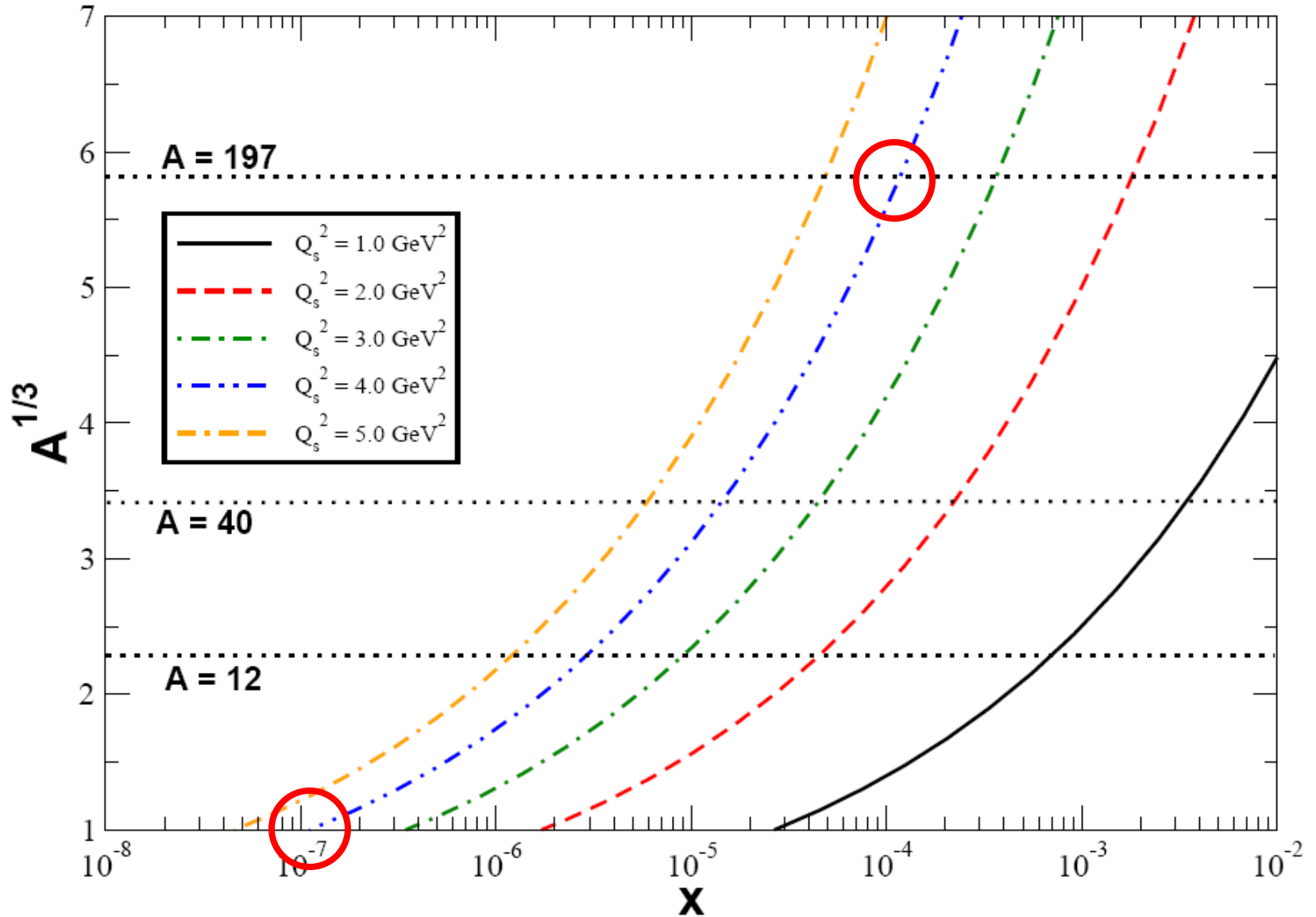
pA @ 10 TeV: reduction by 10 % (or 1.1) in the total cross section (linear-p)

pA @ 10 TeV: reduction by 1.7 in dN/dy at large y (linear-p)

$$Q_s^2 = A^{1/3} Q_0^2 \left(\frac{x_0}{x} \right)^\lambda$$

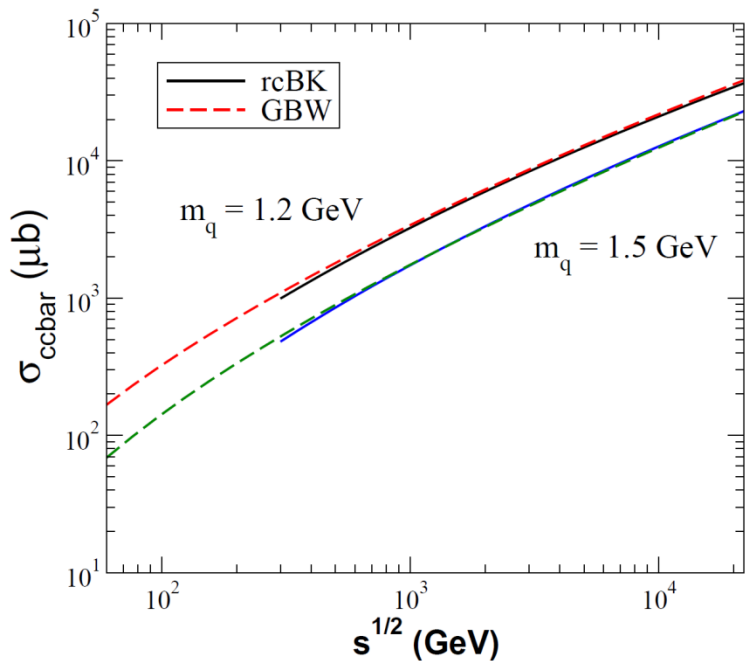
$$Q_0^2 = 1.0 \text{ GeV}^2 \quad \lambda = 0.253$$

$$x_0 = 0.267 \times 10^{-4}$$

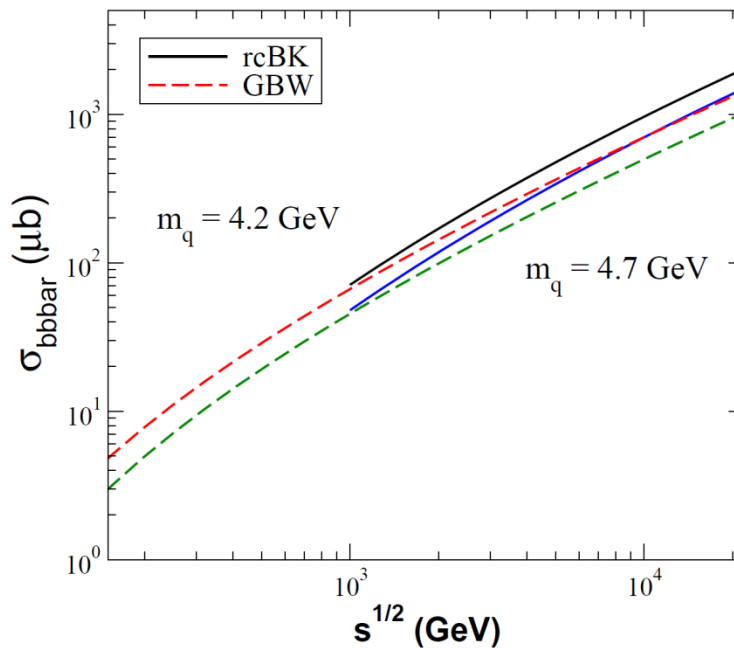


pp

Not so small r



Very small r



GBW

$$N(x, r) = 1 - \exp \left\{ -\frac{1}{4} (r^2 Q_s^2) \right\}$$

$r \rightarrow 0$
 \longrightarrow

$$N(x, r) \cong \frac{1}{4} (r^2 Q_s^2)$$

rcBK (?)

$$N(x, r) = 1 - \exp \left\{ -\frac{1}{4} (r^2 Q_s^2)^\gamma \right\}$$

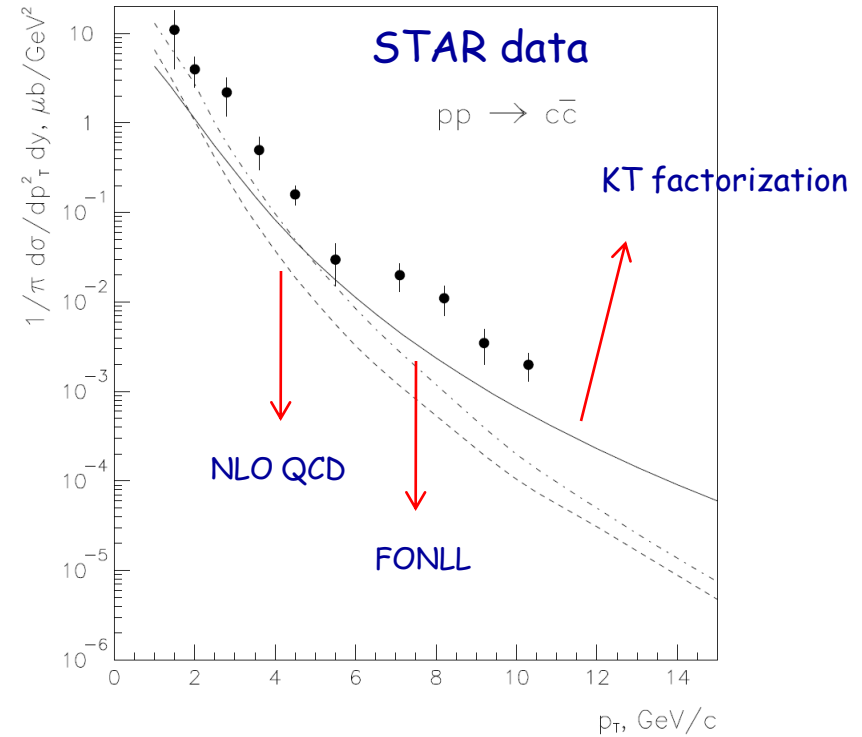
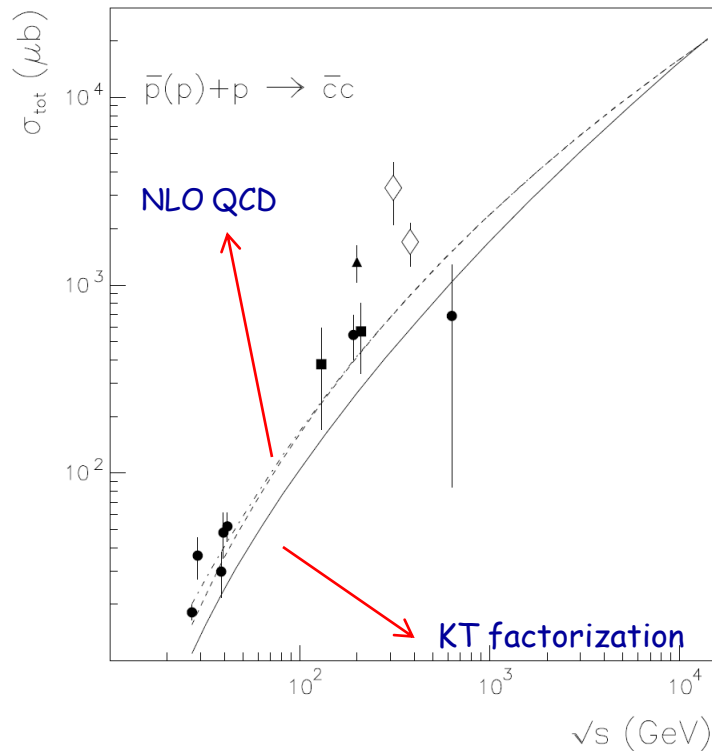
\longrightarrow

$$N(x, r) \cong \frac{1}{4} (r^2 Q_s^2)^\gamma$$

Discussion

On charm production in pp and AA :

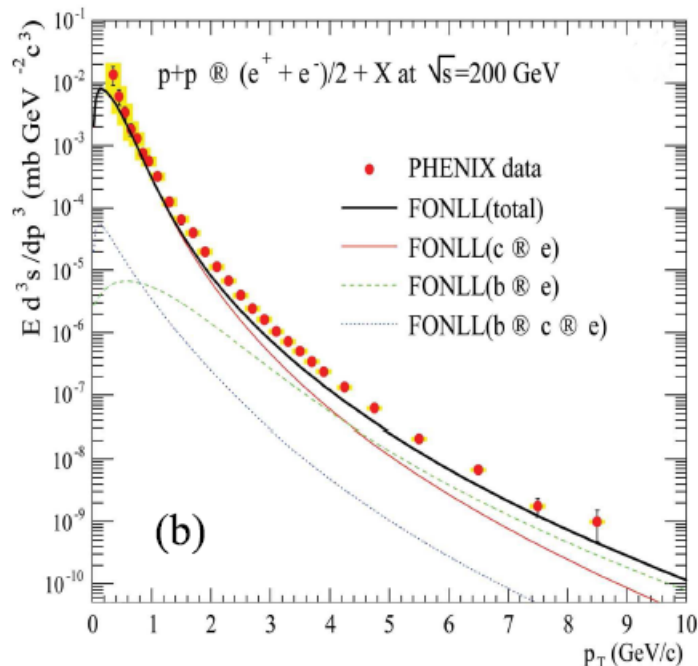
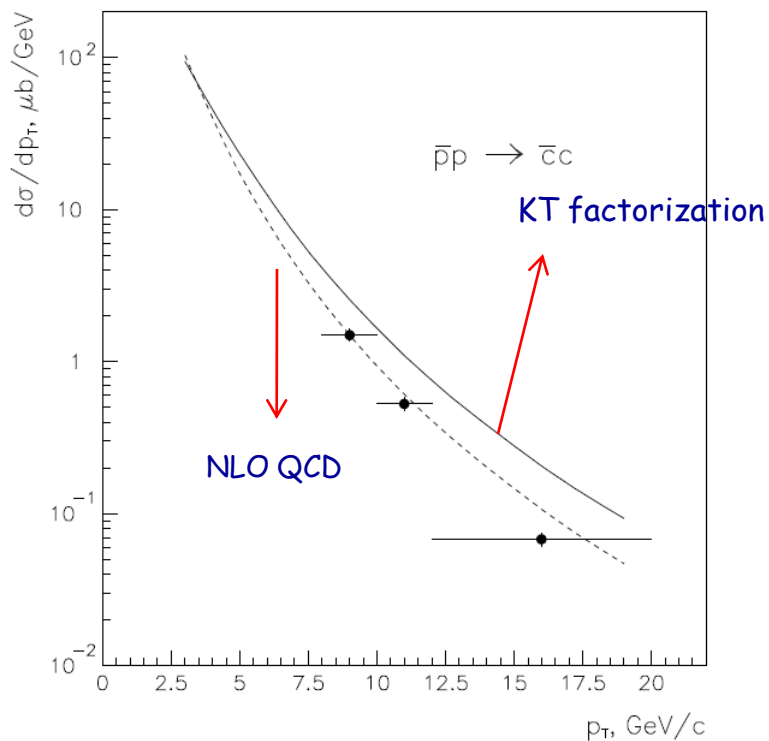
Merino,Pajares,Ryzhinskiy,
Shabelski,Shuvaev,
arXiv:0910.2364



Will we have data on total cross section from Tevatron?

Disagreement between PHENIX and STAR is gone ?

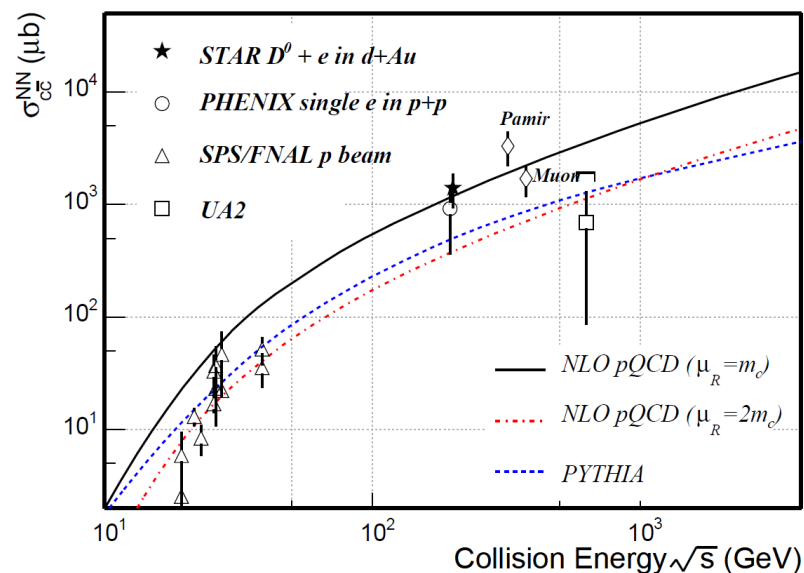
Tevatron data



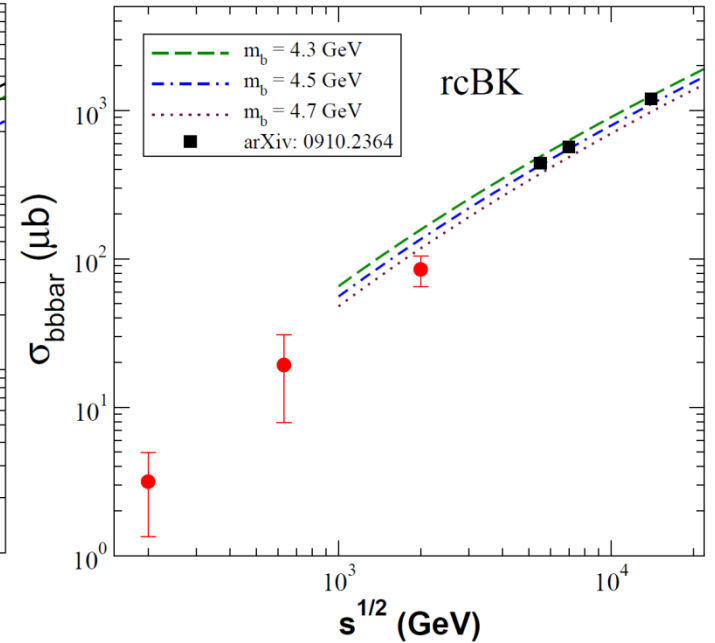
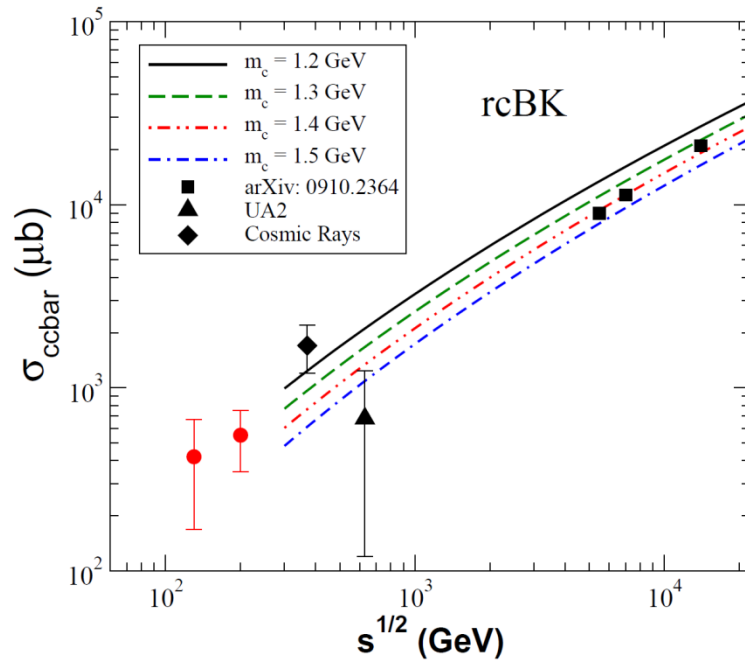
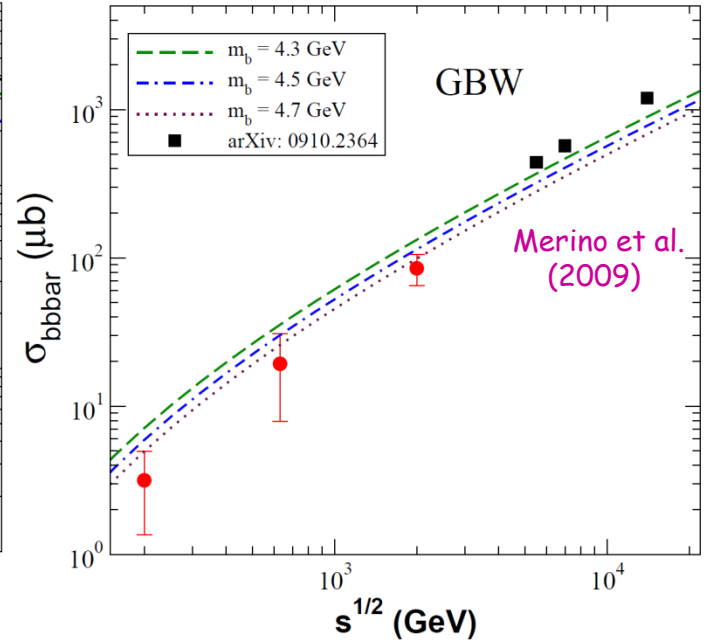
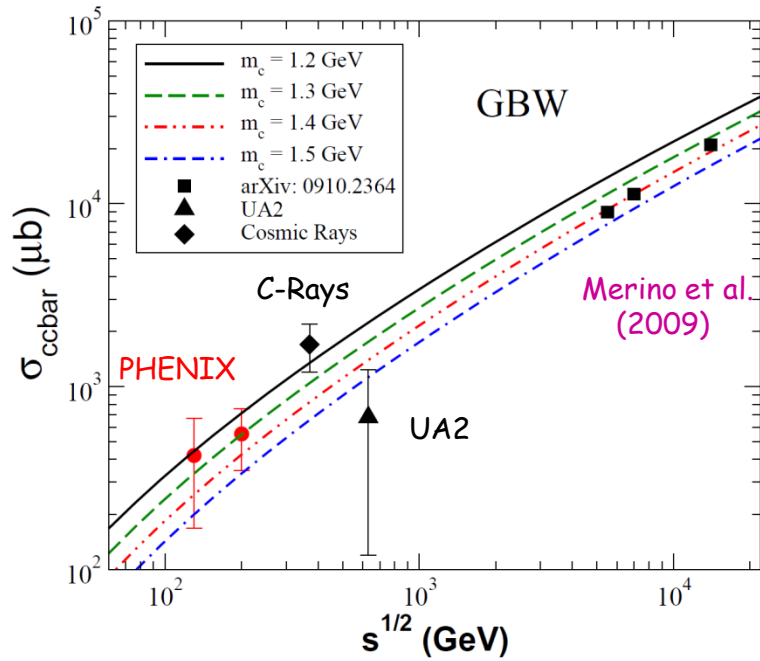
Fragmentation ?

If STAR was right enhanced production might have non-pert. origin: strong fields

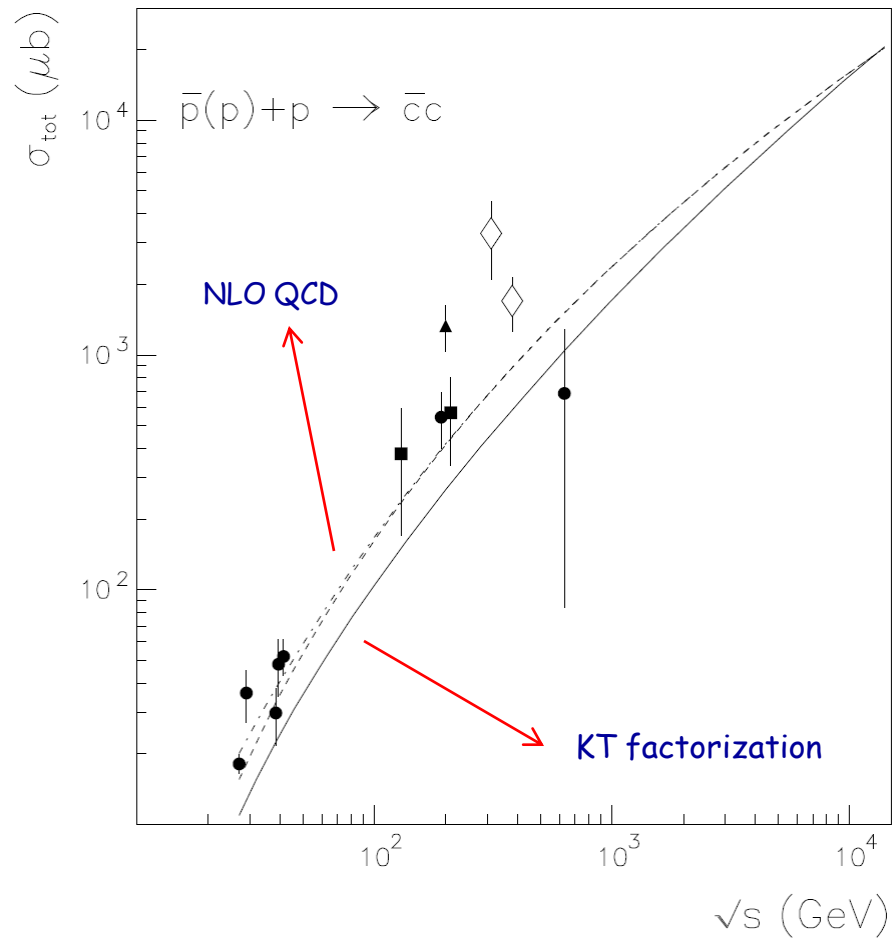
Should we prefer KT factorization?



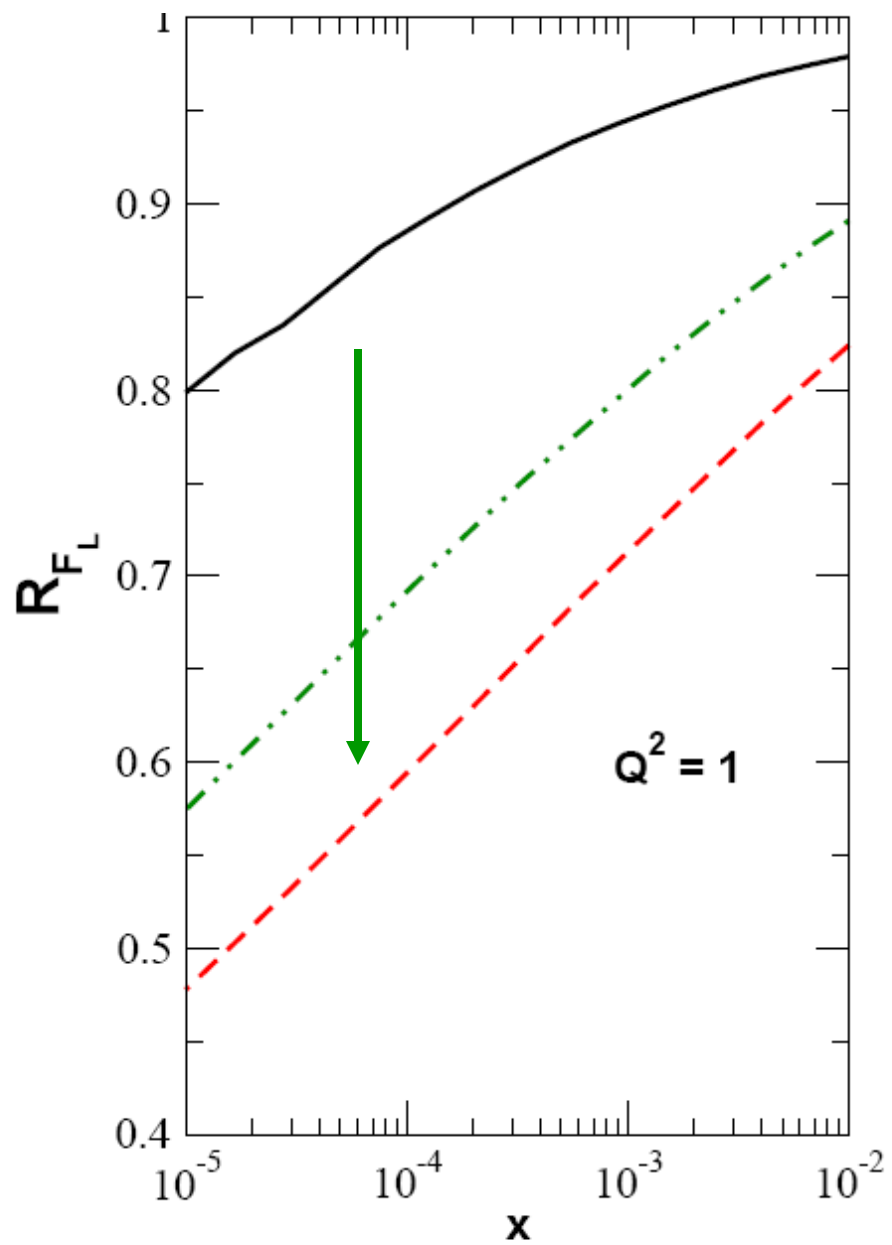
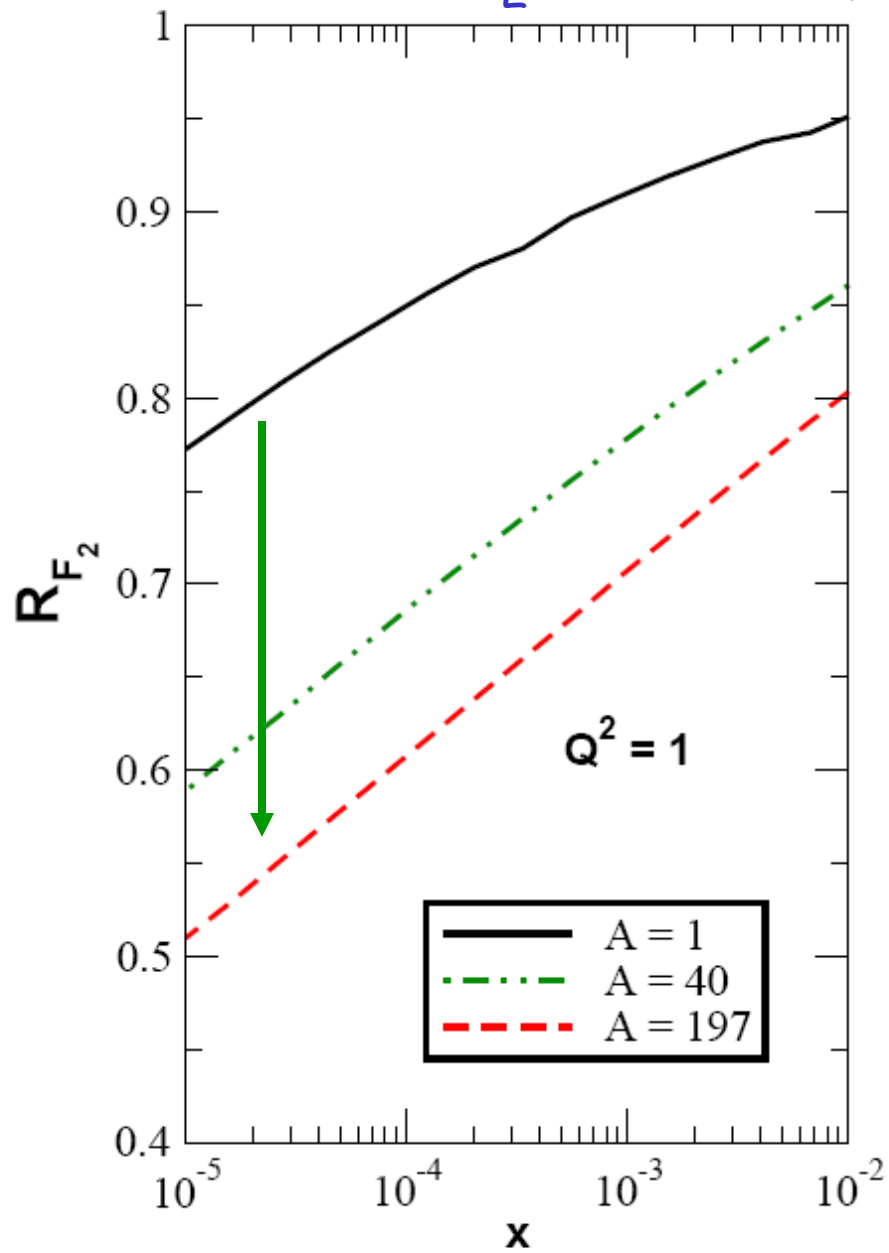
pp

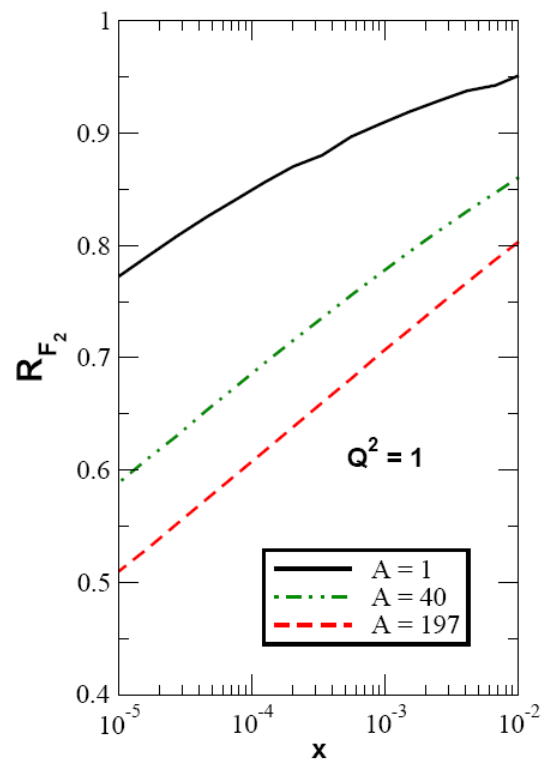
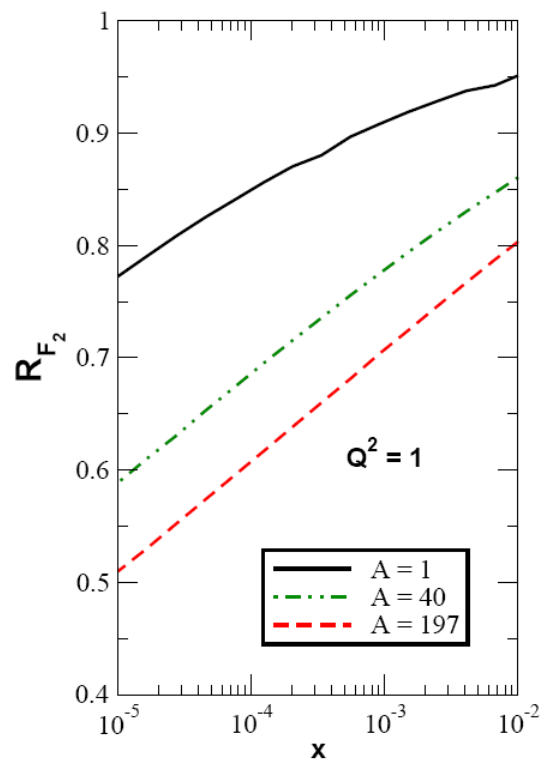


Cazaroto,
Gonçalves,
Navarra
in progress



Merino, Pajares, Ryzhinskiy,
Shabelski, Shuvaev,
arXiv:0910.2364

F_2 $R = \text{full} / \text{linear}$ 



Charm structure function in the KLN model

$$\frac{1}{x} F_2^c(x, Q^2, m_c) = e_c^2 \frac{\alpha_s(\mu^2)}{2\pi} \int_{a_x}^1 \frac{dy}{y} C\left(\frac{x}{y}, \xi\right) g(x, \mu^2)$$

Glück, Reya,
Stratmann (1994)

Glück, Reya,
Vogt (1995)

$C(z, \xi) =$ Coefficient function from pQCD

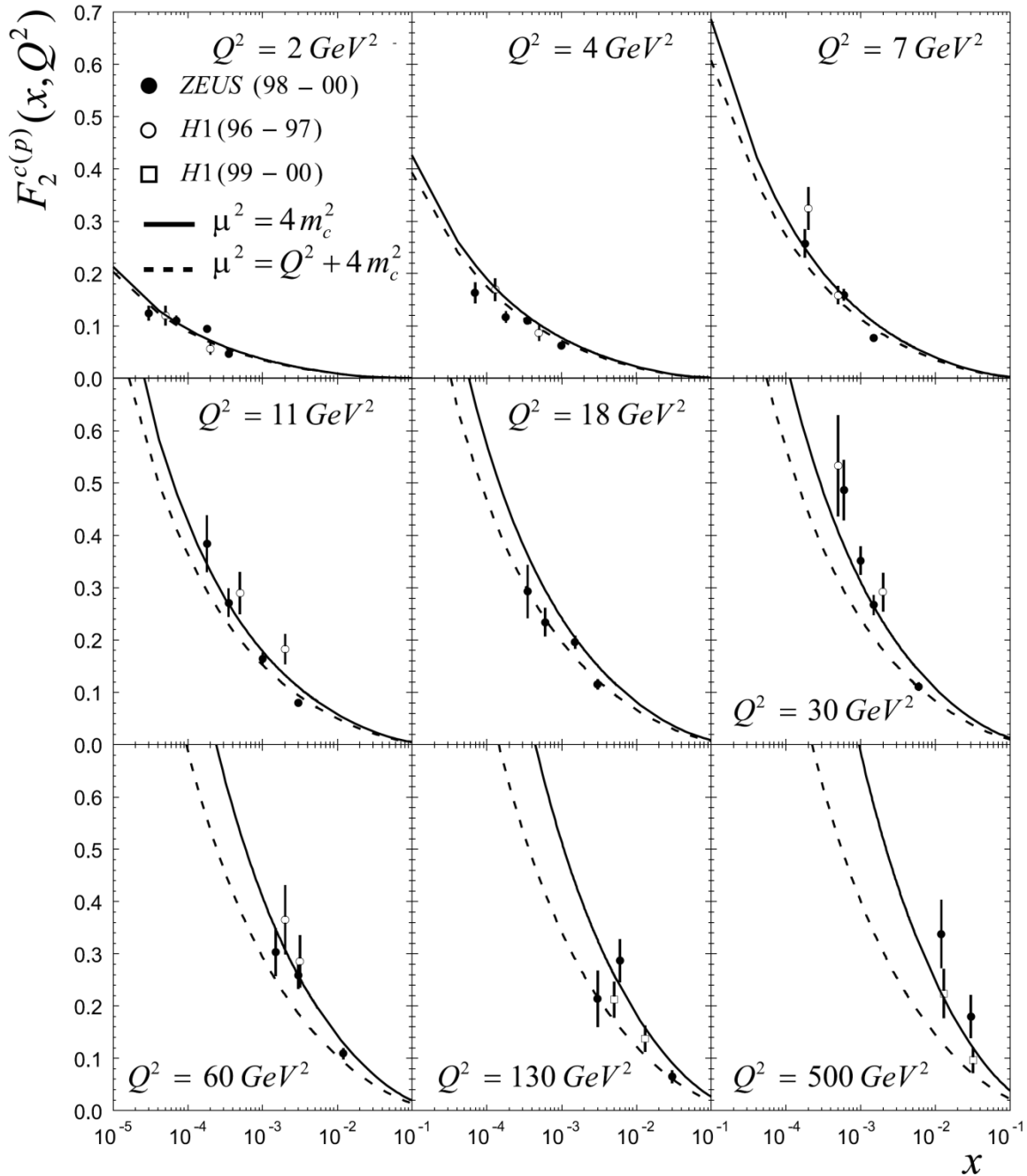
$$a = 1 + \frac{m_c^2}{Q^2} \quad \mu^2 = 4m_c^2 \quad \mu^2 = 4m_c^2 + Q^2 \quad m_c = 1.2 \text{ GeV}$$

$$x g(x, \mu^2) = \begin{cases} \frac{\kappa_0}{\alpha_s(Q_s^2)} S Q^2 (1-x)^4 & Q^2 < Q_s^2 & \text{saturation} \\ \frac{\kappa_0}{\alpha_s(Q_s^2)} S Q_s^2 (1-x)^4 & Q^2 > Q_s^2 & \text{linear} \end{cases}$$

$$Q_s^2 = Q_0^2 \left(\frac{x_0}{x}\right)^\lambda \quad S = \pi R^2$$

Kharzeev, Levin,
Nardi (2001)

ep



$$Q_0^2 = 0.34 \text{ GeV}^2$$

$$x_0 = 3 \times 10^{-3}$$

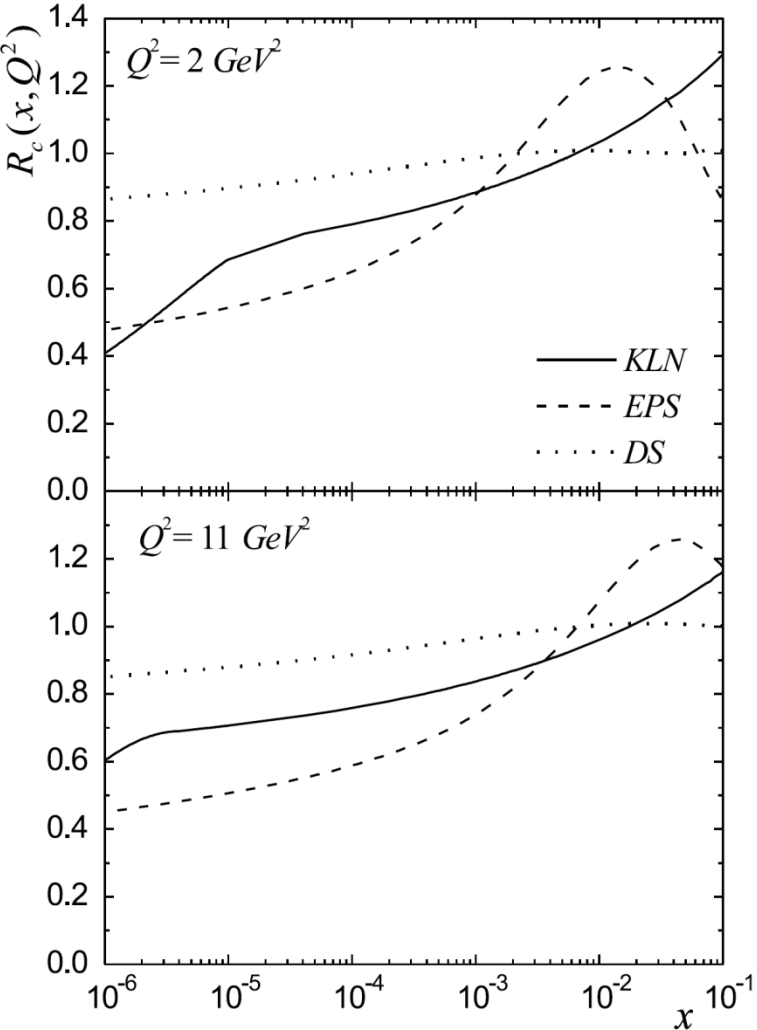
$$\lambda = 0.25$$

Carvalho, Durães
Navarra, Szpigel
(2009)

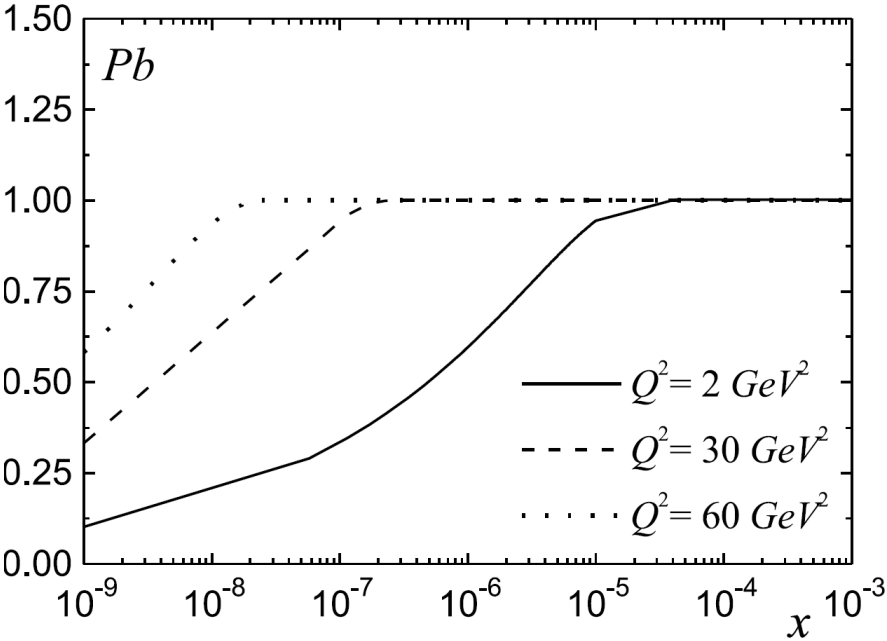
eA

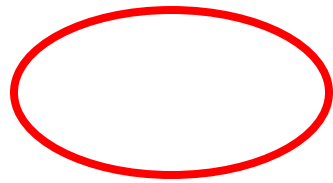
$$R_c = \frac{F_2^{cA}}{A F_2^{cp}}$$

$$\left\{ \begin{array}{l} g(x, \mu^2) \rightarrow g^A(x, \mu^2) \\ S \rightarrow S^A = A^{2/3} S \\ Q_s^2 \rightarrow Q_s^{2A} = A^{1/3} Q_s^2 \end{array} \right.$$



$$R_{FL} = \frac{\text{full}}{\text{linear}}$$





Charm production in pA collisions

Kopeliovich,
Tarasov
(2002)

$$\sigma(GN \rightarrow \{Q\bar{Q}\}X) = \int_0^1 d\alpha \int d^2\rho |\Psi_{G \rightarrow Q\bar{Q}}(\alpha, \rho)|^2 \sigma_{q\bar{q}G}(\alpha, \rho)$$

$$\sigma_{q\bar{q}G}(\alpha, \rho) = \frac{9}{8} [\sigma_{q\bar{q}}(\alpha\rho) + \sigma_{q\bar{q}}(\bar{\alpha}\rho)] - \frac{1}{8} \sigma_{q\bar{q}}(\rho)$$

$$|\Psi_{G \rightarrow Q\bar{Q}}(\alpha, \rho)|^2 = \frac{\alpha_S(\mu_R)}{(2\pi)^2} \{m_Q^2 K_0(m_Q\rho_1) K_0(m_Q\rho_2) + [\alpha^2 + \bar{\alpha}^2] m_Q^2 \frac{\vec{\rho}_1 \cdot \vec{\rho}_2}{\rho_1 \rho_2} K_1(m_Q\rho_1) K_1(m_Q\rho_2)\}$$

$$\frac{d\sigma(pp \rightarrow \{Q\bar{Q}\}X)}{dy} = x_1 G(x_1, \mu_F^2) \sigma(GN \rightarrow \{Q\bar{Q}\}X)$$

$$\sigma_{tot}(pp \rightarrow \{Q\bar{Q}\}X) = 2 \int_0^{-\ln(2m_Q/\sqrt{s})} dy x_1 G(x_1, \mu_F) \sigma(GN \rightarrow \{Q\bar{Q}\}X)$$

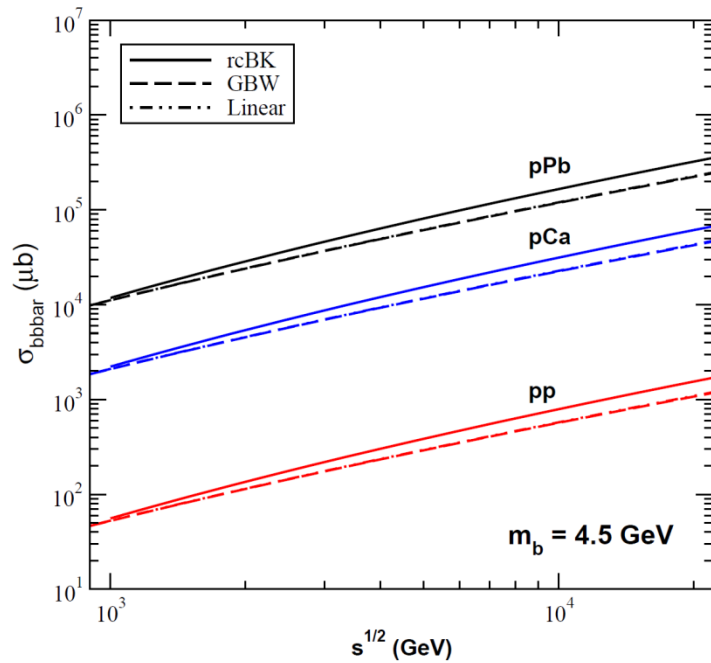
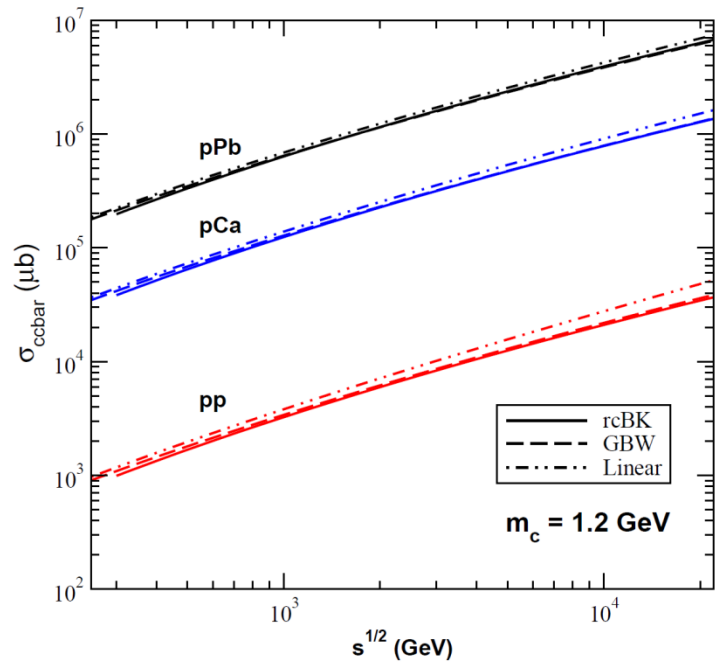
$$x_1 = \frac{2m_Q e^y}{\sqrt{s}}$$

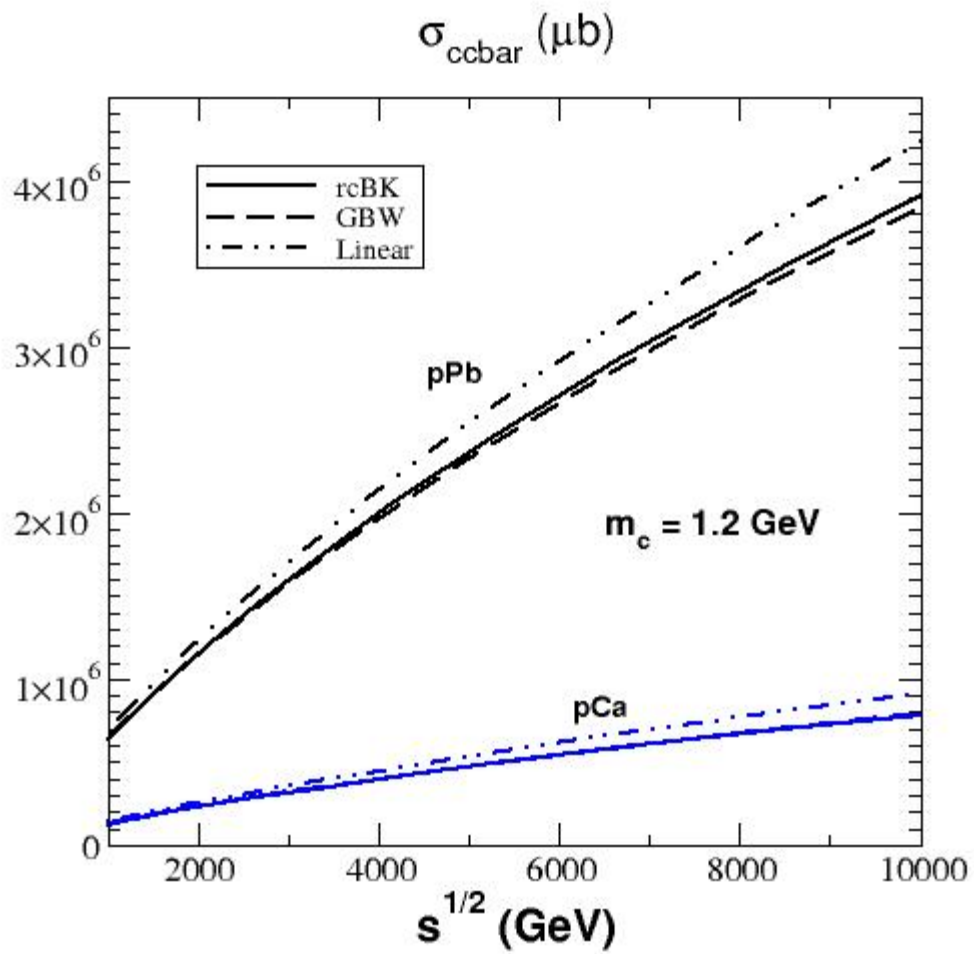
$$x_2 = \frac{2m_Q e^{-y}}{\sqrt{s}}$$

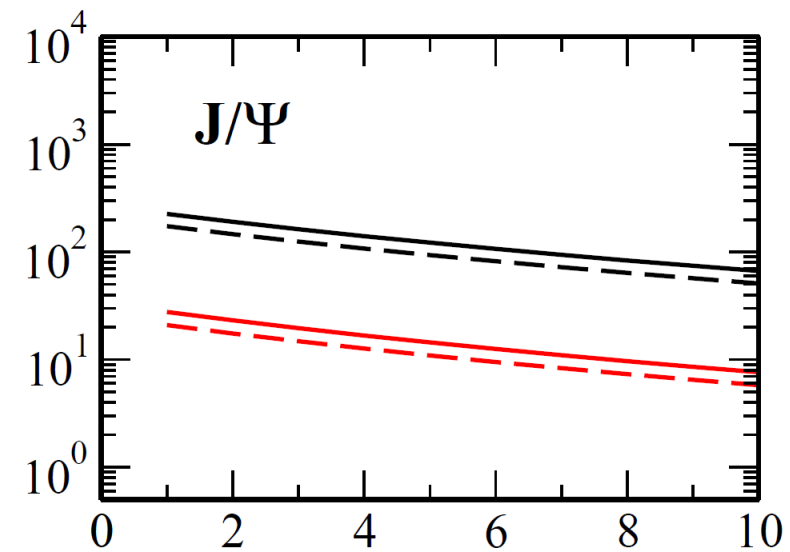
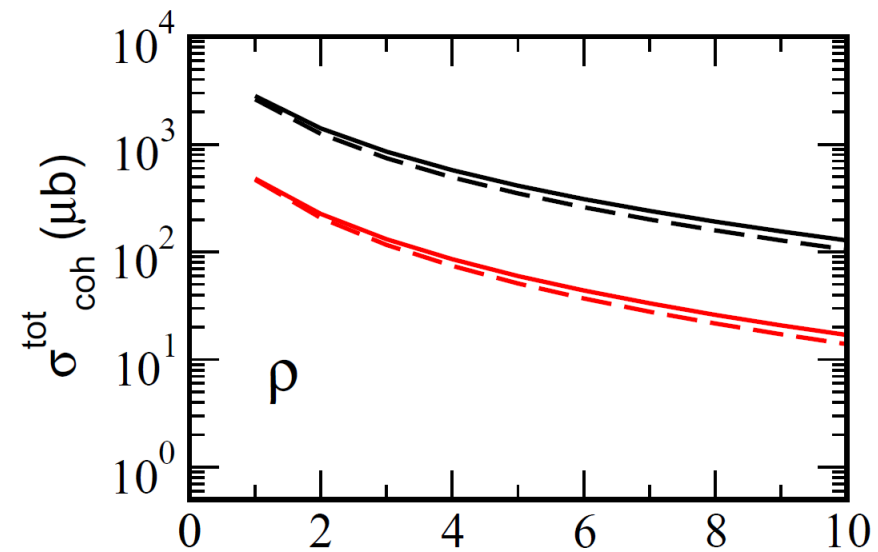
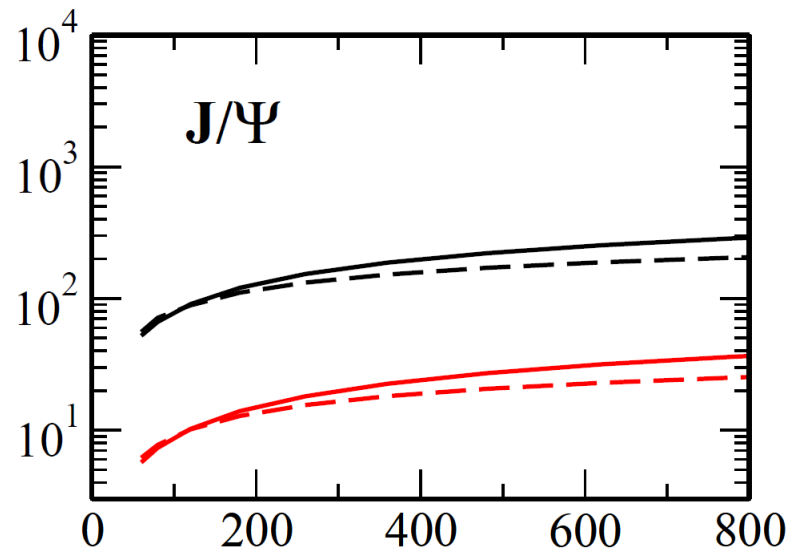
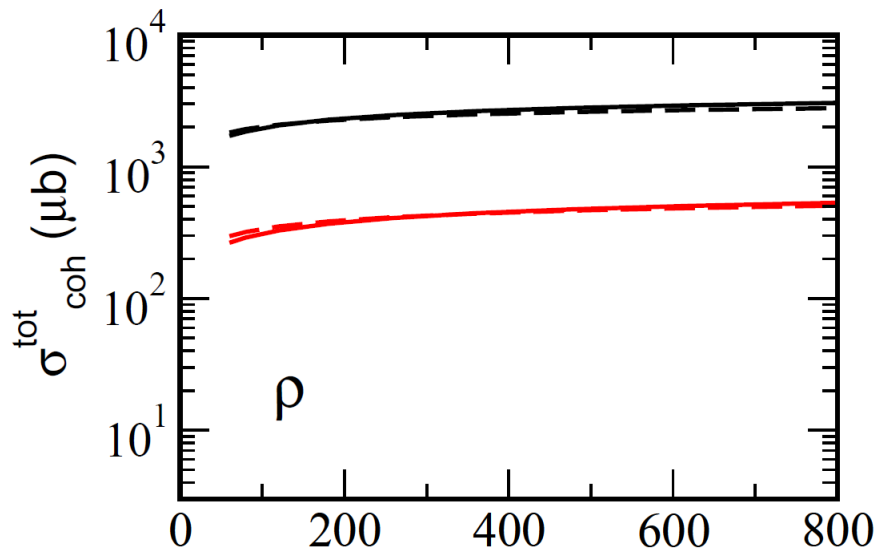
$$\sigma_{q\bar{q}-A} = 2\pi \int_0^{R_A} dbb \left[2 \left(1 - e^{-\frac{1}{2} \sigma_{q\bar{q}} T_A(b)} \right) \right]$$

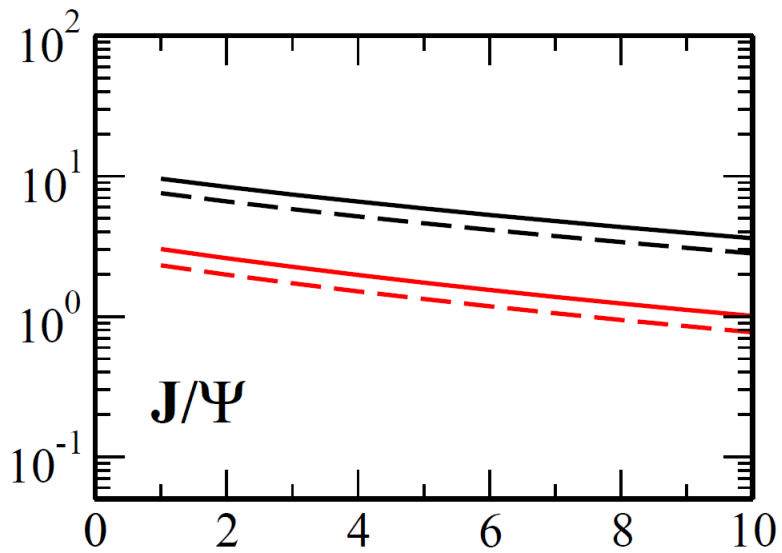
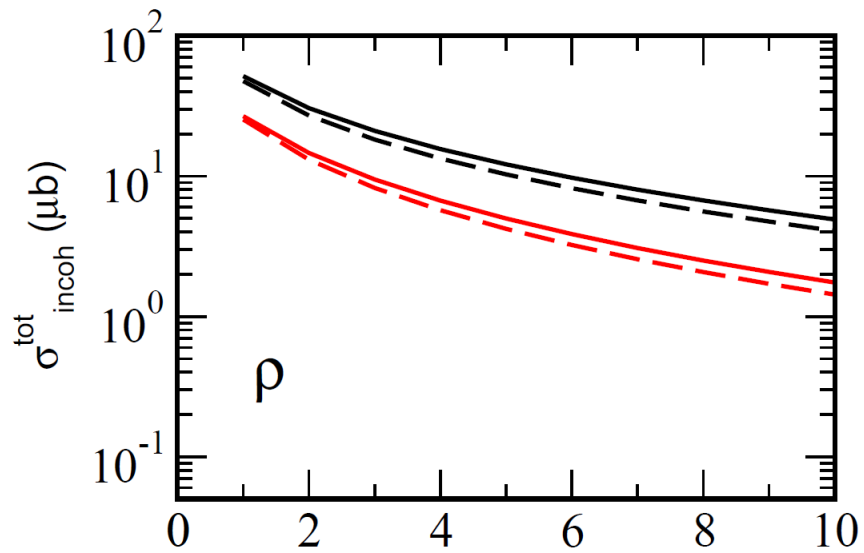
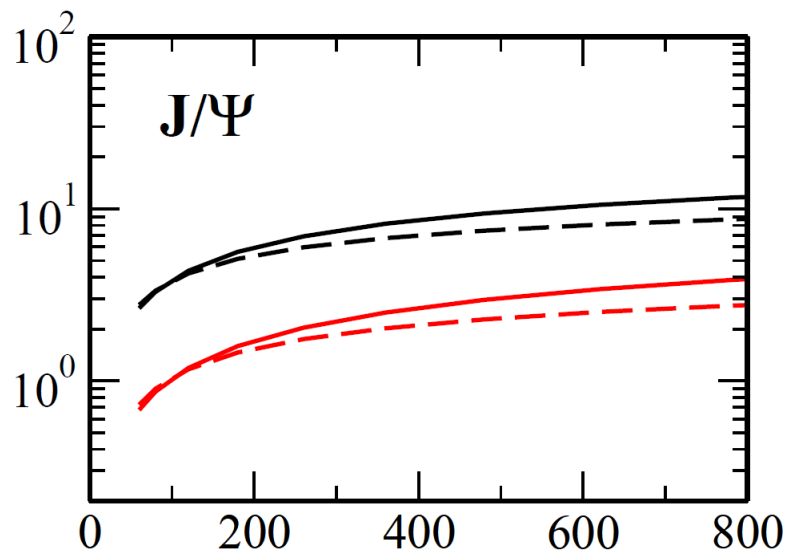
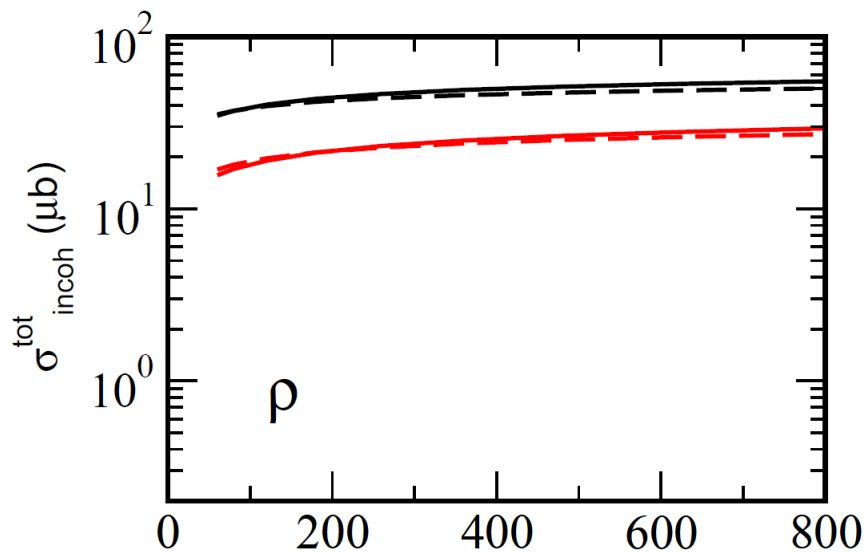
$$y = 1/2 \ln(x_1/x_2)$$

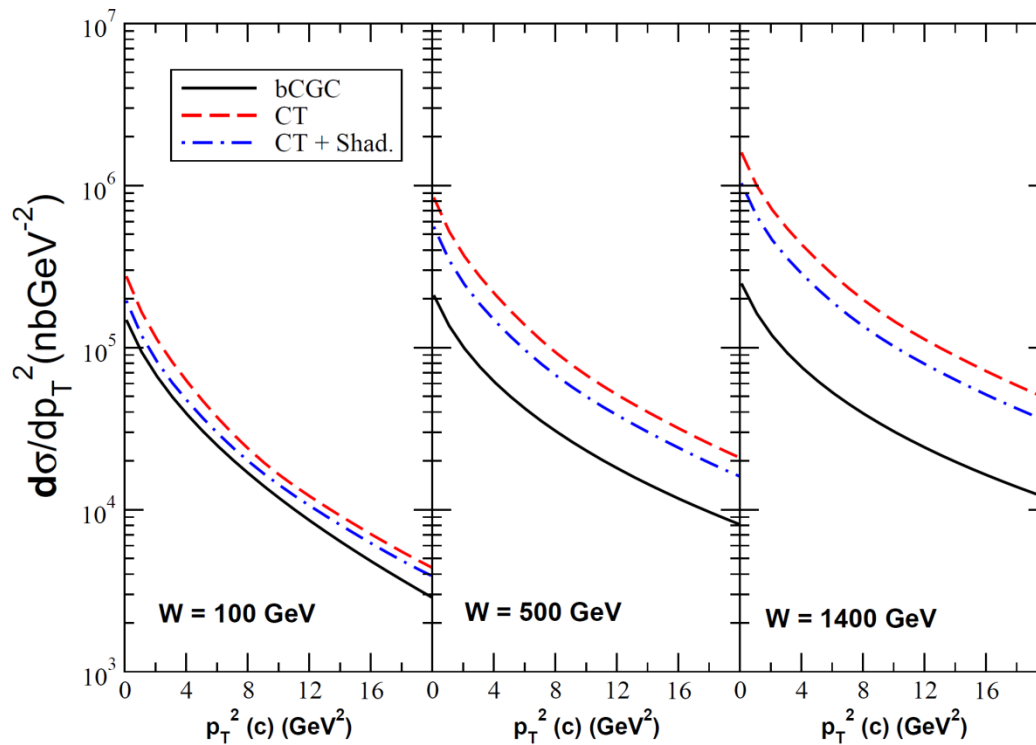
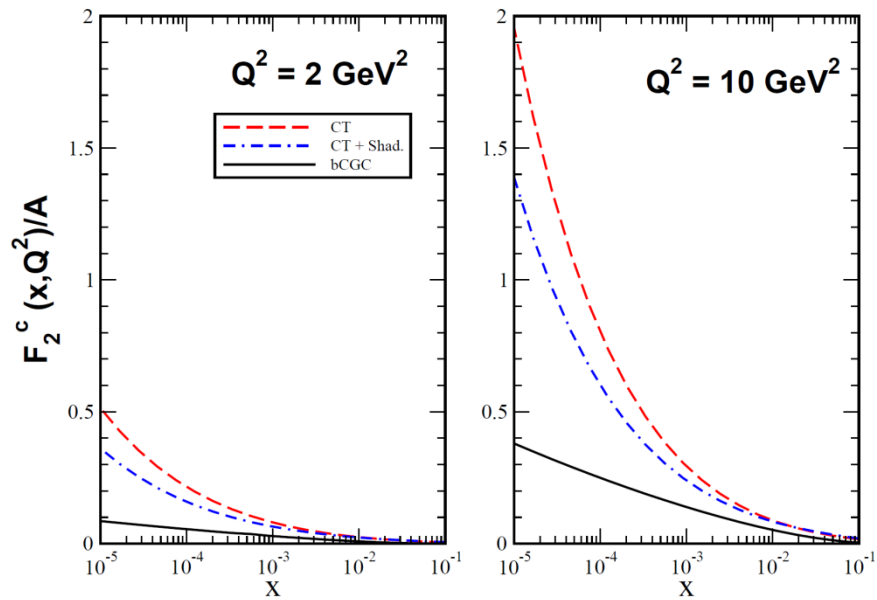
Back ups











Introduction

NLO collinear factorization

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Color dipole formalism

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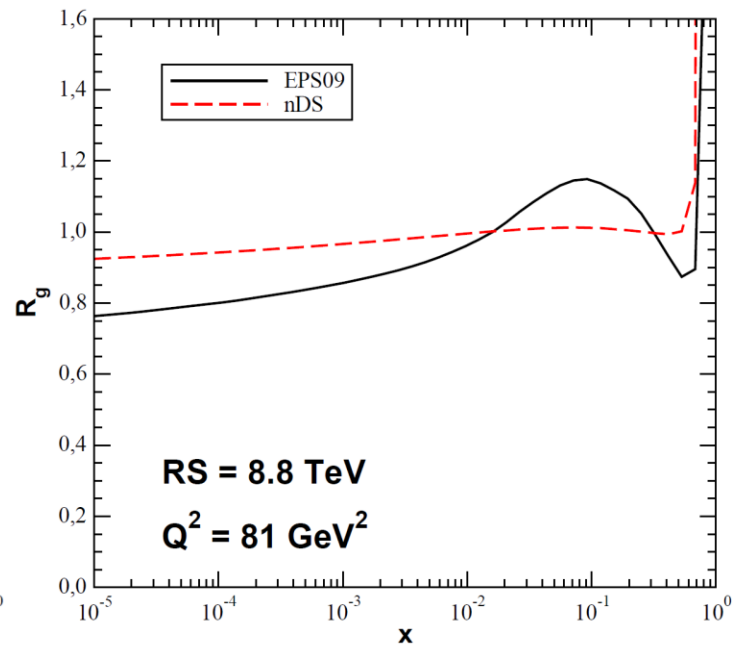
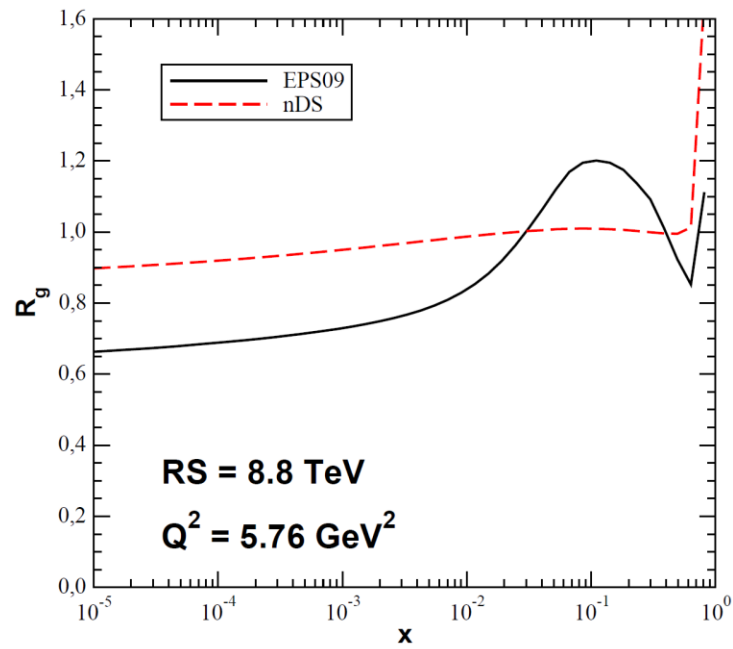
$$F_2^A(x, Q^2) = \frac{Q^2}{4\pi^2\alpha_{em}} \sigma_{tot}(x, Q^2)$$

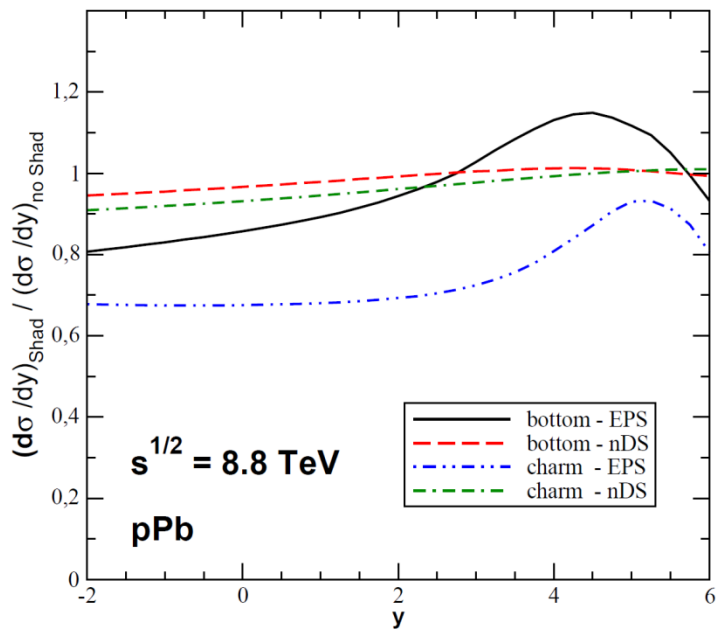
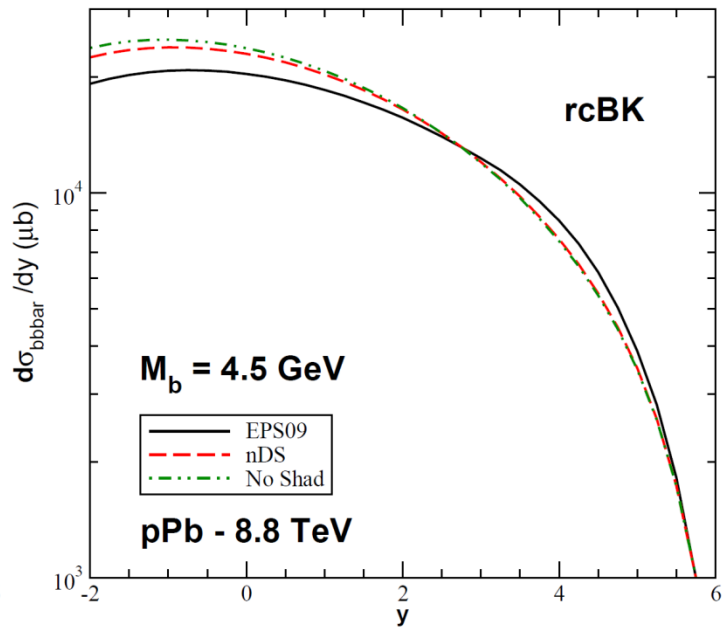
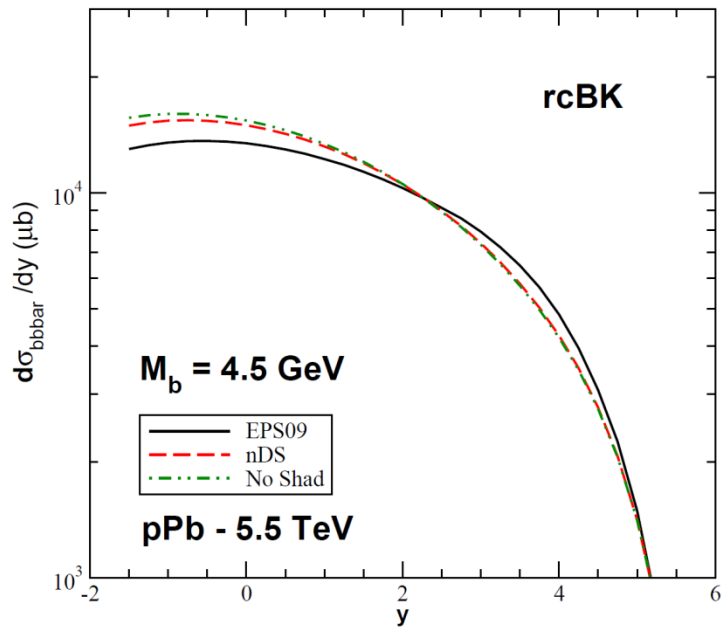
$$\sigma_{tot} = \sigma_T + \sigma_L \text{ and } \sigma_{T,L} = \int d^2\mathbf{r} dz |\Psi_{T,L}(\mathbf{r}, z, Q^2)|^2 \sigma_{dA}(x, \mathbf{r})$$

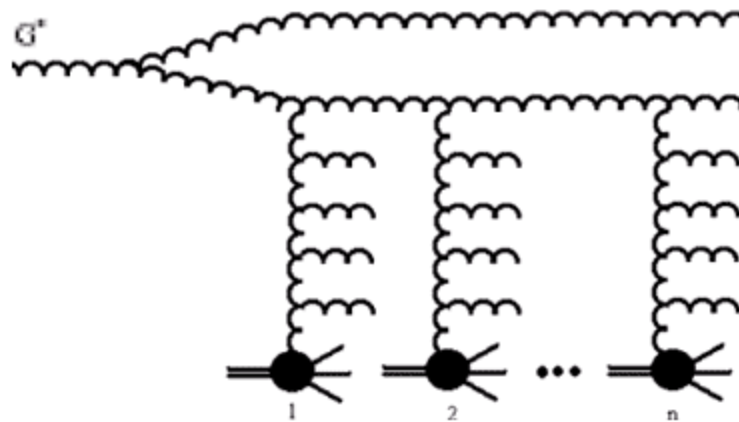
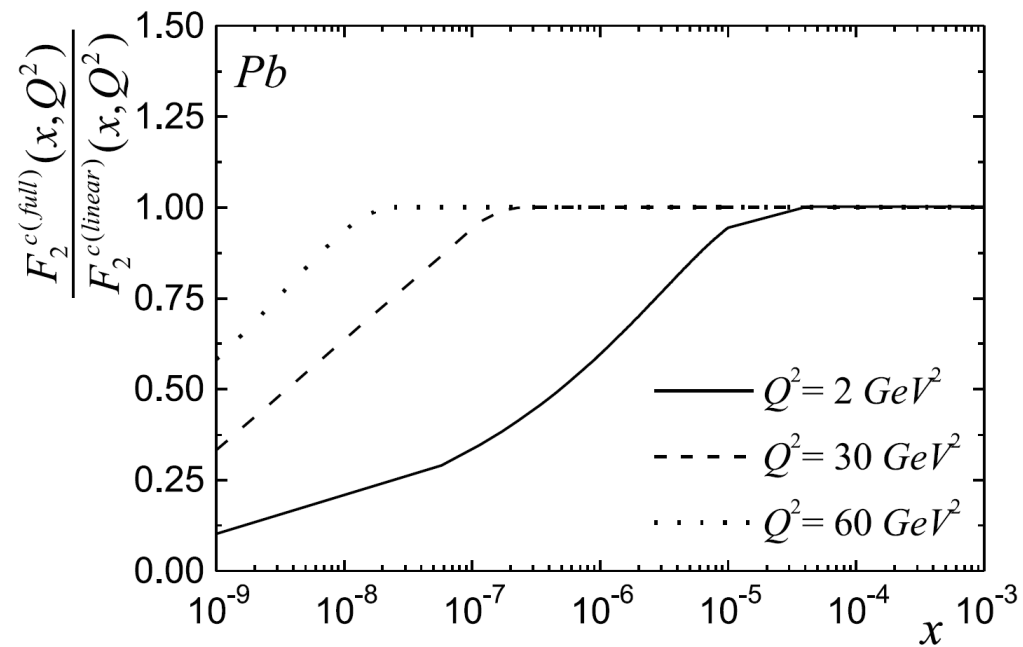
$$D_Q^h(z^*) = \frac{n(h)}{z^* \left[1 - \frac{1}{z^*} - \frac{\epsilon_Q}{1-z^*}\right]^2}$$

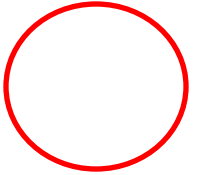
$$\sigma_{dp}^{bCGC}(x, \mathbf{r}^2) \equiv \int d^2\bar{\mathbf{b}} \frac{d\sigma_{dp}}{d^2\bar{\mathbf{b}}}$$

$$\frac{d\sigma_{dp}}{d^2\bar{\mathbf{b}}} = 2 \mathcal{N}^p(x, \mathbf{r}, \bar{\mathbf{b}}) = 2 \times \begin{cases} \mathcal{N}_0 \left(\frac{r Q_s}{2}\right)^{2\left(\gamma_s + \frac{\ln(2/r Q_s)}{\kappa \lambda Y}\right)} & r Q_s \leq 2 \\ 1 - \exp\left[-a \ln^2(b r Q_s)\right] & r Q_s > 2 \end{cases}$$

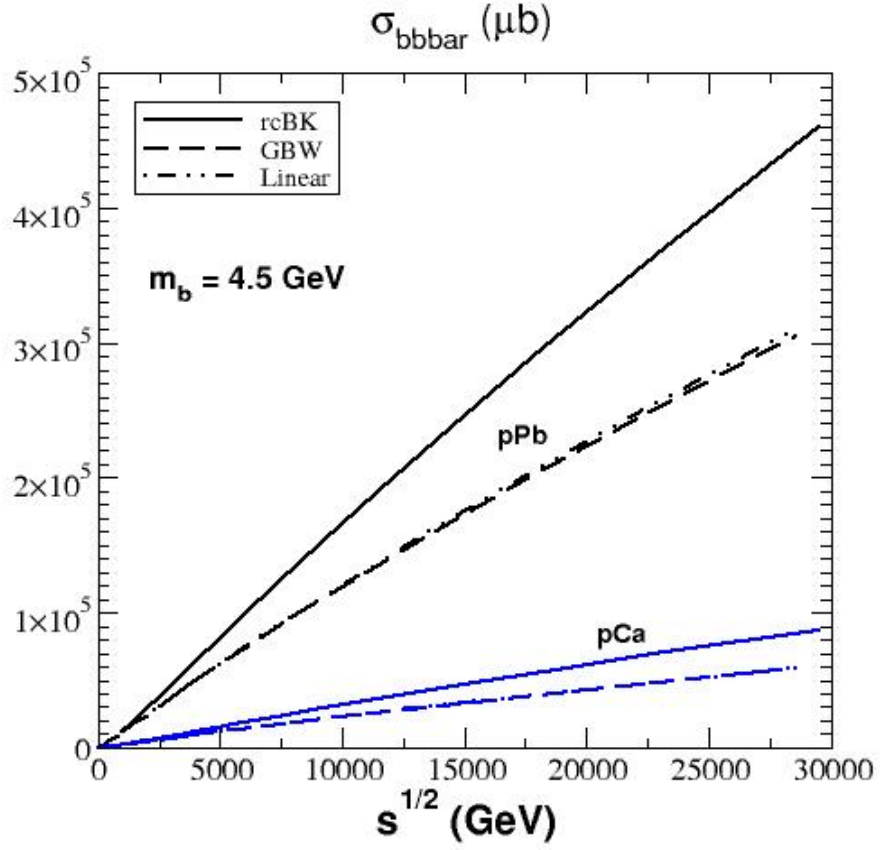
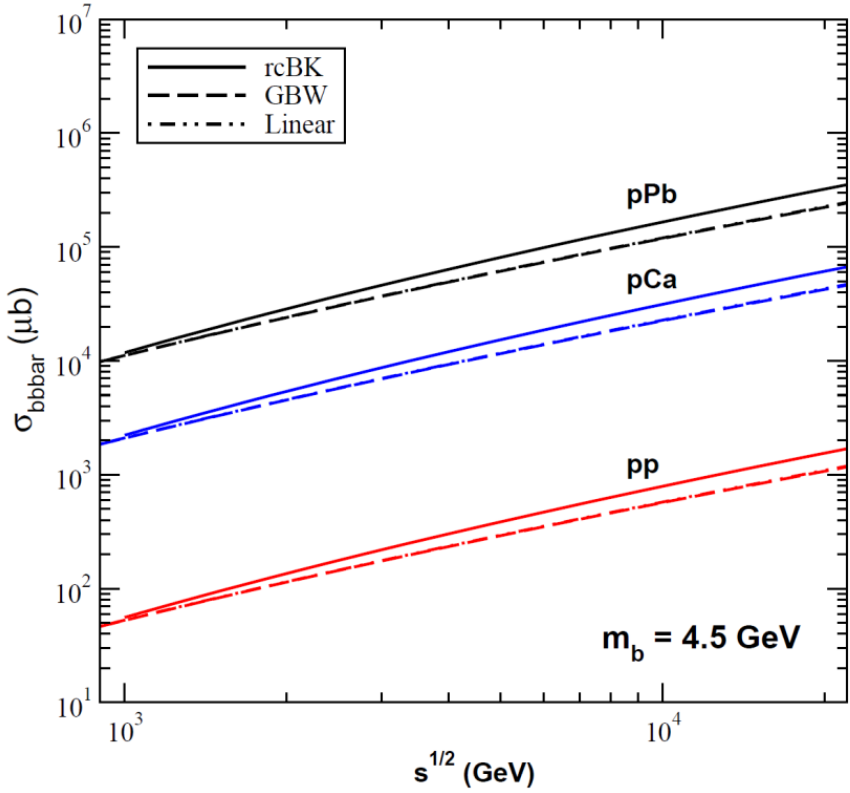






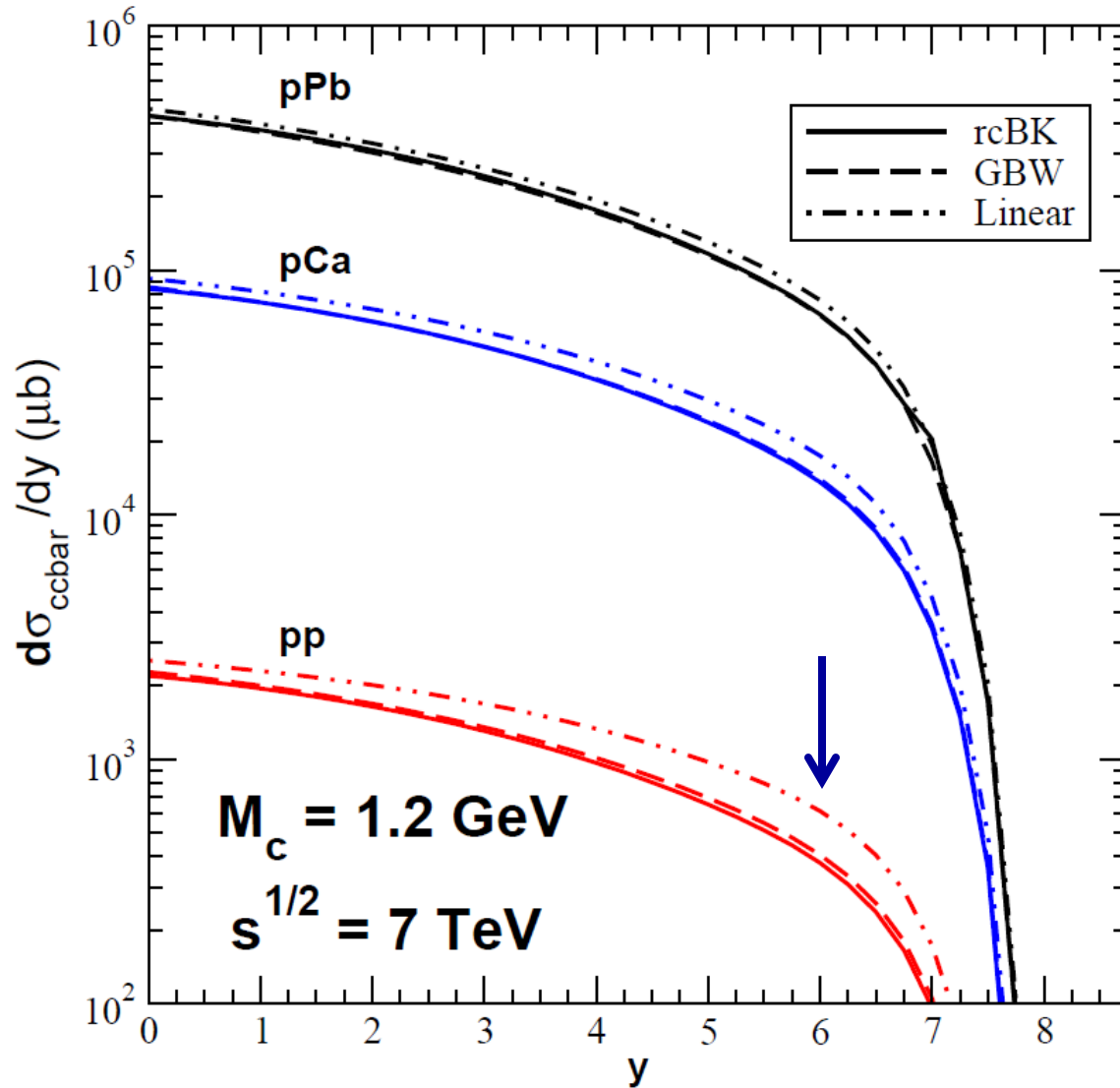


pA



pA

Rapidity distribution



Saturation: reduction by 1.7 at $y = 6$

