

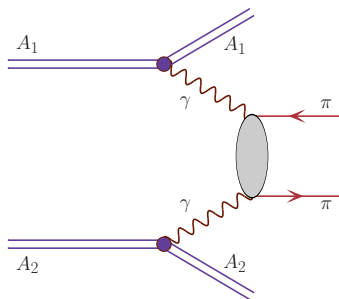


Institute of Nuclear Physics PAN, PL-31-342 Cracow, Poland

Exclusive production of pion pairs in large invariant mass  
in nucleus-nucleus collisions

Mariola Kłusek-Gawenda

In collaboration with prof. A. Szczurek



### Accelerator LHC:

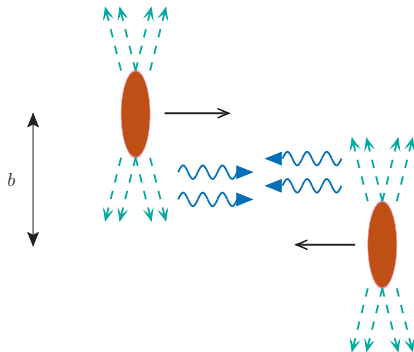
- nuclei: Pb-Pb
- $\sqrt{s_{NN}} = 3.5$  TeV
- $\gamma_{cm} = 2\,932$  GeV

$$PbPb \rightarrow PbPb\pi^0\pi^0$$

$$PbPb \rightarrow PbPb\pi^+\pi^-$$

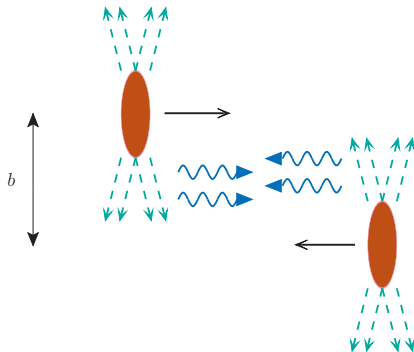
- 1 Equivalent photon approximation
  - Form factor
    - Realistic
    - Monopole
- 2  $\gamma\gamma \rightarrow \pi\pi$ 
  - pQCD Brodsky-Lepage
  - Hand-bag
- 3 Nuclear cross section
- 4 Conclusions

## Equivalent photon approximation (EPA)



The strong electromagnetic field is used as a source of photons to induce electromagnetic reactions.

## Equivalent photon approximation (EPA)



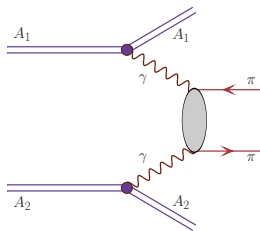
The strong electromagnetic field is used as a source of photons to induce electromagnetic reactions.

Peripheral collisions:

$$b > R_1 + R_2 \cong 14 \text{ fm}$$

# The total cross section in EPA

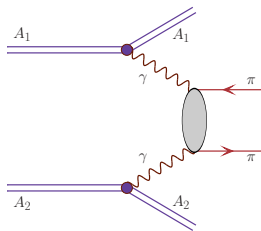
$$\begin{aligned} &\sigma(PbPb \rightarrow PbPb\pi\pi; s_{NN}) \\ &= \int \hat{\sigma}(\gamma\gamma \rightarrow \pi\pi; x_1 x_2 s_{NN}) dn_{\gamma\gamma}(x_1, x_2, \mathbf{b}) \end{aligned}$$



# The total cross section in EPA

$$\begin{aligned} &\sigma(PbPb \rightarrow PbPb\pi\pi; s_{NN}) \\ &= \int \hat{\sigma}(\gamma\gamma \rightarrow \pi\pi; x_1 x_2 s_{NN}) dn_{\gamma\gamma}(x_1, x_2, \mathbf{b}) \end{aligned}$$

- $x_{1,2} = \frac{\omega_{1,2}}{\gamma M_A}$



## Photons flux

$$dn_{\gamma\gamma}(x_1, x_2, \mathbf{b}) = \int \frac{1}{\pi} d^2\mathbf{b}_1 |\mathbf{E}(x_1, \mathbf{b}_1)|^2 \frac{1}{\pi} d^2\mathbf{b}_2 |\mathbf{E}(x_2, \mathbf{b}_2)|^2$$

$$\times S_{abs}^2(\mathbf{b}) \delta^{(2)}(\mathbf{b} - \mathbf{b}_1 + \mathbf{b}_2) \frac{dx_1}{x_1} \frac{dx_2}{x_2}$$

- $\mathbf{E}(x, \mathbf{b}) = Z\sqrt{4\pi\alpha_{em}} \int \frac{d^2\mathbf{q}}{(2\pi^2)} e^{-i\mathbf{b}\mathbf{q}} \frac{\mathbf{q}}{q^2 + x^2 M_A^2} F_{em}(q^2 + x^2 M_A^2)$
  - $S_{abs}^2(\mathbf{b}) \cong \theta(\mathbf{b} - 2R_A)$
- 
- $\frac{1}{\pi} \int d^2\mathbf{b} |\mathbf{E}(x, \mathbf{b})|^2 = \int d^2\mathbf{b} N(\omega, \mathbf{b})$
  - $d\omega_1 d\omega_2 \rightarrow dW_{\gamma\gamma} dY$

## The cross section in EPA

## Nuclear cross section – EPA

$$\begin{aligned} \sigma(PbPb \rightarrow \pi\pi PbPb; s_{NN}) &= \\ &= \int \hat{\sigma}(\gamma\gamma \rightarrow \pi\pi; W_{\gamma\gamma}) \theta(|\mathbf{b}_1 - \mathbf{b}_2| - 2R_A) \\ &\times N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_1) 2\pi b_m db_m d\bar{b}_x d\bar{b}_y \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY \end{aligned}$$

***The details of derivation:***

Antoni Szczurek, M.K-G; Phys. Rev. **C82** (2010) 014904,  
 "Exclusive muon-pair productions in ultrarelativistic heavy-ion collisions: Realistic nucleus charge form factor and differential distributions"



## Form factor

MONOPOLE  $F_{em}$ 

$$F(q^2) = \frac{\Lambda^2}{\Lambda^2 + q^2}$$

$$\Lambda = \sqrt{\frac{6}{\langle r^2 \rangle}}$$

## Form factor

MONOPOLE  $F_{em}$ 

$$F(q^2) = \frac{\Lambda^2}{\Lambda^2 + q^2}$$

$$\Lambda = \sqrt{\frac{6}{\langle r^2 \rangle}}$$

- $^{197}\text{Au} \Rightarrow \sqrt{\langle r^2 \rangle} = 5.3 \text{ fm}, \Lambda = 0.091 \text{ GeV},$
- $^{208}\text{Pb} \Rightarrow \sqrt{\langle r^2 \rangle} = 5.5 \text{ fm}, \Lambda = 0.088 \text{ GeV}.$

## Form factor

MONOPOLE  $F_{em}$ 

$$F(q^2) = \frac{\Lambda^2}{\Lambda^2 + q^2}$$

$$\Lambda = \sqrt{\frac{6}{\langle r^2 \rangle}}$$

- $^{197}\text{Au} \Rightarrow \sqrt{\langle r^2 \rangle} = 5.3 \text{ fm}, \Lambda = 0.091 \text{ GeV},$
- $^{208}\text{Pb} \Rightarrow \sqrt{\langle r^2 \rangle} = 5.5 \text{ fm}, \Lambda = 0.088 \text{ GeV}.$

In the literature:

$$\Lambda = (0.08 - 0.09) \text{ GeV}$$

## Form factor

MONOPOLE  $F_{em}$ 

$$F(q^2) = \frac{\Lambda^2}{\Lambda^2 + q^2}$$

$$\Lambda = \sqrt{\frac{6}{\langle r^2 \rangle}}$$

- $^{197}\text{Au} \Rightarrow \sqrt{\langle r^2 \rangle} = 5.3 \text{ fm}, \Lambda = 0.091 \text{ GeV},$
- $^{208}\text{Pb} \Rightarrow \sqrt{\langle r^2 \rangle} = 5.5 \text{ fm}, \Lambda = 0.088 \text{ GeV}.$

In the literature:

$$\Lambda = (0.08 - 0.09) \text{ GeV}$$

REALISTIC  $F_{em}$ 

$$F(q) = \int \frac{4\pi}{q} \rho(r) \sin(qr) r dr$$

## Form factor

MONOPOLE  $F_{em}$ 

$$F(q^2) = \frac{\Lambda^2}{\Lambda^2 + q^2}$$

$$\Lambda = \sqrt{\frac{6}{\langle r^2 \rangle}}$$

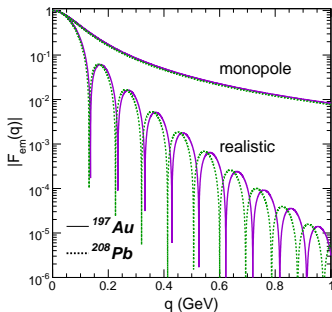
- $^{197}\text{Au} \Rightarrow \sqrt{\langle r^2 \rangle} = 5.3 \text{ fm}, \Lambda = 0.091 \text{ GeV},$
- $^{208}\text{Pb} \Rightarrow \sqrt{\langle r^2 \rangle} = 5.5 \text{ fm}, \Lambda = 0.088 \text{ GeV}.$

In the literature:

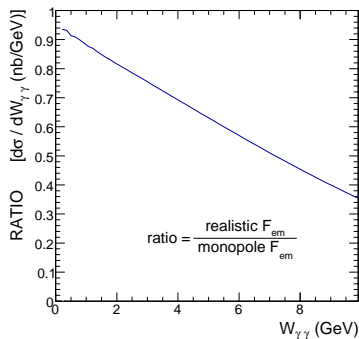
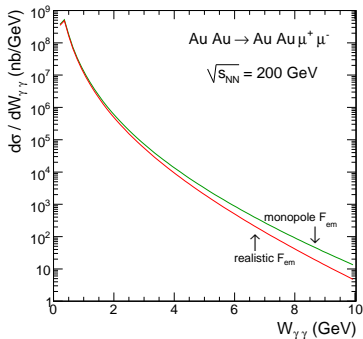
$$\Lambda = (0.08 - 0.09) \text{ GeV}$$

REALISTIC  $F_{em}$ 

$$F(q) = \int \frac{4\pi}{q} \rho(r) \sin(qr) r dr$$

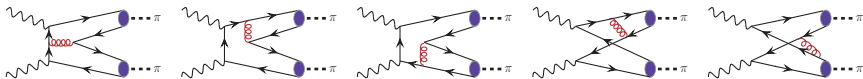


# Realistic vs monopole form factor



Elementary cross section for  $\gamma\gamma \rightarrow \pi\pi$ The  $\gamma\gamma \rightarrow (q\bar{q})(q\bar{q}) \rightarrow \pi\pi$  amplitude in the LO pQCD

$$\mathcal{M}(\lambda_1, \lambda_2) = \int_0^1 dx \int_0^1 dy \phi_\pi(x, \mu_x^2) T_H^{\lambda_1 \lambda_2}(x, y, \mu^2) \phi_\pi(y, \mu_y^2) \times F_{reg}^{pQCD}(t, u)$$

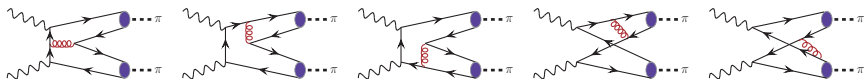


- $\mu_x = \min(x, 1-x) \sqrt{s(1-z^2)}$ ,
- $z = \cos \theta$ ,  $\rightarrow$  A. Szczurek, J. Speth, Nucl.Phys. **A728**(2003)182
- $F_{reg}^{pQCD}(t, u) = \left[ 1 - \exp\left(\frac{t-t_m}{\Lambda_{reg}^2}\right) \right] \left[ 1 - \exp\left(\frac{u-u_m}{\Lambda_{reg}^2}\right) \right]$

# Elementary cross section for $\gamma\gamma \rightarrow \pi\pi$

The  $\gamma\gamma \rightarrow (q\bar{q})(q\bar{q}) \rightarrow \pi\pi$  amplitude in the LO pQCD

$$\begin{aligned} \mathcal{M}(\lambda_1, \lambda_2) &= \int_0^1 dx \int_0^1 dy \phi_\pi(x, \mu_x^2) T_H^{\lambda_1 \lambda_2}(x, y, \mu^2) \phi_\pi(y, \mu_y^2) \\ &\times F_{reg}^{pQCD}(t, u) \end{aligned}$$



Total cross section

$$\sigma(\gamma\gamma \rightarrow \pi\pi) = \int \frac{2\pi}{4 \cdot 64\pi^2 W^2} \frac{p}{q} \sum_{\lambda_1, \lambda_2} |\mathcal{M}(\lambda_1, \lambda_2)|^2 dz$$



## The quark distribution amplitude of the pion

$$\phi_\pi(x, \mu^2) = \frac{f_\pi}{2\sqrt{3}} 6x(1-x) \sum_{n=0}^{\infty'} C_n^{3/2} (2x-1) a_n(\mu^2)$$

$$a_n(\mu^2) = \frac{2}{3} \frac{2n+3}{(n+1)(n+2)} \left( \frac{\alpha_s(\mu^2)}{\alpha_s(\mu_0^2)} \right)^{-\frac{C_F}{\beta_0} \left[ 3 + \frac{2}{(n+1)(n+2)} - 4 \sum_{k=1}^{n+1} \frac{1}{k} \right]}$$

$$\times \int_0^1 dx C_n^{3/2} (2x-1) \phi_\pi(x, \mu_0^2)$$

- $\alpha_s(\mu^2) = \frac{4\pi}{\beta_0 \ln \frac{\mu^2}{\Lambda_{QCD}^2}}$

- $\beta_0 = \frac{11}{3} C_A - \frac{2}{3} N_F$

# The quark distribution amplitude of the pion

PHYSICAL REVIEW D 82, 034024 (2010)

Implication on the pion distribution amplitude from the pion-photon transition form factor with the new BABAR data

Xing-Gang Wu<sup>\*</sup>

*Department of Physics, Chongqing University, Chongqing 400044, People's Republic of China*

Tao Huang<sup>†</sup>

*Institute of High Energy Physics and Theoretical Physics Center for Science Facilities, Chinese Academy of Sciences, Beijing 100049, People's Republic of China*

(Received 19 May 2010; published 19 August 2010)

The new BABAR data on the pion-photon transition form factor arouses people's interest for the determination of the pion distribution amplitude. To explain the data, we take both the leading valence quark state's and the nonvalence quark state's contributions into consideration, where the valence quark part up to next-to-leading order is presented and the nonvalence quark part is estimated by a phenomenological model based on its limiting behavior at both  $Q^2 \rightarrow 0$  and  $Q^2 \rightarrow \infty$ . Our results show that to be consistent with the new BABAR data at the large  $Q^2$  region, a broader amplitude other than the asymptoticlike pion distribution amplitude should be adopted. The broadness of the pion distribution amplitude is controlled by a parameter  $B$ . It has been found that the new BABAR data at low and high energy regions can be explained simultaneously by setting  $B$  to be around 0.60, in which the pion distribution amplitude is closed to the Chernyak-Zhitnitsky form.

DOI: 10.1103/PhysRevD.82.034024

$$F_{\pi\gamma}(Q^2) = F_{\pi\gamma}^{(V)}(Q^2) + F_{\pi\gamma}^{(NV)}(Q^2)$$

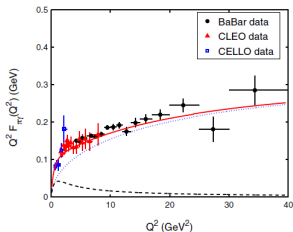


FIG. 5 (color online).  $Q^2 F_{\pi\gamma}(Q^2)$  with the model wave function (3) by taking  $m_q = 0.30$  GeV and  $B = 0.60$ . The solid, the dotted, and the dashed lines are for the total contribution, the leading valence quark contribution, and the nonvalence quark contribution to the form factor, respectively.

# The quark distribution amplitude of the pion

PHYSICAL REVIEW D 82, 034024 (2010)

Implication on the pion distribution amplitude from the pion-photon transition form factor with the new BABAR data

Xing-Gang Wu\*

Department of Physics, Chongqing University, Chongqing 400044, People's Republic of China

Tao Huang†

Institute of High Energy Physics and Theoretical Physics Center for Science Facilities,  
Chinese Academy of Sciences, Beijing 100049, People's Republic of China

(Received 19 May 2010; published 19 August 2010)

The new BABAR data on the pion-photon transition form factor arouses people's interest for the determination of the pion distribution amplitude. To explain the data, we take both the leading valence quark state's and the nonvalence quark state's contributions into consideration, where the valence quark part up to next-to-leading order is presented and the nonvalence quark part is estimated by a phenomenological model based on its limiting behavior at both  $Q^2 \rightarrow 0$  and  $Q^2 \rightarrow \infty$ . Our results show that to be consistent with the new BABAR data at the large  $Q^2$  region, a broader amplitude other than the asymptoticlike pion distribution amplitude should be adopted. The broadness of the pion distribution amplitude is controlled by a parameter  $B$ . It has been found that the new BABAR data at low and high energy regions can be explained simultaneously by setting  $B$  to be around 0.60, in which the pion distribution amplitude is closed to the Chernyak-Zhitnitsky form.

DOI: 10.1103/PhysRevD.82.034024

$$F_{\pi\gamma}(Q^2) = F_{\pi\gamma}^{(V)}(Q^2) + F_{\pi\gamma}^{(NV)}(Q^2)$$

$$\Psi_{q\bar{q}}(x, \mathbf{k}_\perp) = \sum_{\lambda_1 \lambda_2} \chi^{\lambda_1 \lambda_2} \Psi_{q\bar{q}}^R(x, \mathbf{k}_\perp)$$

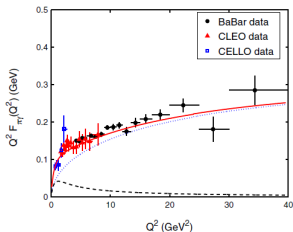


FIG. 5 (color online).  $Q^2 F_{\pi\gamma}(Q^2)$  with the model wave function (3) by taking  $m_q = 0.30$  GeV and  $B = 0.60$ . The solid, the dotted, and the dashed lines are for the total contribution, the leading valence quark contribution, and the nonvalence quark contribution to the form factor, respectively.

# The quark distribution amplitude of the pion

PHYSICAL REVIEW D 82, 034024 (2010)

Implication on the pion distribution amplitude from the pion-photon transition form factor with the new BABAR data

Xing-Gang Wu\*

Department of Physics, Chongqing University, Chongqing 400044, People's Republic of China

Tao Huang†

Institute of High Energy Physics and Theoretical Physics Center for Science Facilities, Chinese Academy of Sciences, Beijing 100049, People's Republic of China

(Received 19 May 2010; published 19 August 2010)

The new BABAR data on the pion-photon transition form factor arouses people's interest for the determination of the pion distribution amplitude. To explain the data, we take both the leading valence quark state's and the nonvalence quark state's contributions into consideration, where the valence quark part up to next-to-leading order is presented and the nonvalence quark part is estimated by a phenomenological model based on its limiting behavior at both  $Q^2 \rightarrow 0$  and  $Q^2 \rightarrow \infty$ . Our results show that to be consistent with the new BABAR data at the large  $Q^2$  region, a broader amplitude other than the asymptoticlike pion distribution amplitude should be adopted. The broadness of the pion distribution amplitude is controlled by a parameter  $B$ . It has been found that the new BABAR data at low and high energy regions can be explained simultaneously by setting  $B$  to be around 0.60, in which the pion distribution amplitude is closed to the Chernyak-Zhitnitsky form.

DOI: 10.1103/PhysRevD.82.034024

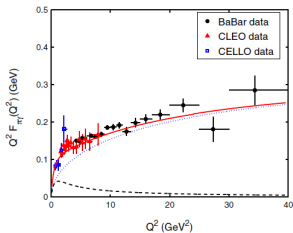


FIG. 5 (color online).  $Q^2 F_{\pi\gamma}(Q^2)$  with the model wave function (3) by taking  $m_q = 0.30$  GeV and  $B = 0.60$ . The solid, the dotted, and the dashed lines are for the total contribution, the leading valence quark contribution, and the nonvalence quark contribution to the form factor, respectively.

$$F_{\pi\gamma}(Q^2) = F_{\pi\gamma}^{(V)}(Q^2) + F_{\pi\gamma}^{(NV)}(Q^2)$$

$$\Psi_{q\bar{q}}(x, \mathbf{k}_\perp) = \sum_{\lambda_1 \lambda_2} \chi^{\lambda_1 \lambda_2} \Psi_{q\bar{q}}^R(x, \mathbf{k}_\perp)$$

Based on the BHL prescription:

$$\Psi_{q\bar{q}}^R(x, \mathbf{k}_\perp) = A \varphi_\pi(x) \times \exp\left[-\frac{\mathbf{k}_\perp + m_q^2}{8\beta^2 x(1-x)}\right]$$

$$\bullet \varphi_\pi(x) = \left(1 + B C_2^{3/2} (2x - 1)\right)$$

## The quark distribution amplitude of the pion

PHYSICAL REVIEW D 82, 034024 (2010)

Implication on the pion distribution amplitude from the pion-photon transition form factor with the new BABAR data

Xing-Gang Wu\*

Department of Physics, Chongqing University, Chongqing 400044, People's Republic of China

Tao Huang†

Institute of High Energy Physics and Theoretical Physics Center for Science Facilities,  
Chinese Academy of Sciences, Beijing 100049, People's Republic of China

(Received 19 May 2010; published 19 August 2010)

The new BABAR data on the pion-photon transition form factor arouses people's interest for the determination of the pion distribution amplitude. To explain the data, we take both the leading valence quark state's and the nonvalence quark state's contributions into consideration, where the valence quark part up to next-to-leading order is presented and the nonvalence quark part is estimated by a phenomenological model based on its limiting behavior at both  $Q^2 \rightarrow 0$  and  $Q^2 \rightarrow \infty$ . Our results show that to be consistent with the new BABAR data at the large  $Q^2$  region, a broader amplitude other than the asymptoticlike pion distribution amplitude should be adopted. The broadness of the pion distribution amplitude is controlled by a parameter  $B$ . It has been found that the new BABAR data at low and high energy regions can be explained simultaneously by setting  $B$  to be around 0.60, in which the pion distribution amplitude is closed to the Chernyak-Zhitnitsky form.

DOI: 10.1103/PhysRevD.82.034024

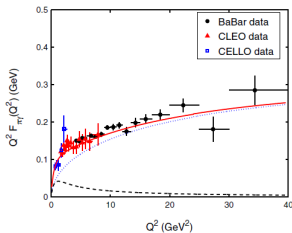


FIG. 5 (color online).  $Q^2 F_{\pi\gamma}(Q^2)$  with the model wave function (3) by taking  $m_q = 0.30$  GeV and  $B = 0.60$ . The solid, the dotted, and the dashed lines are for the total contribution, the leading valence quark contribution, and the nonvalence quark contribution to the form factor, respectively.

$$F_{\pi\gamma}(Q^2) = F_{\pi\gamma}^{(V)}(Q^2) + F_{\pi\gamma}^{(NV)}(Q^2)$$

$$\Psi_{q\bar{q}}(x, \mathbf{k}_\perp) = \sum_{\lambda_1 \lambda_2} \chi^{\lambda_1 \lambda_2} \Psi_{q\bar{q}}^R(x, \mathbf{k}_\perp)$$

Based on the BHL prescription:

$$\Psi_{q\bar{q}}^R(x, \mathbf{k}_\perp) = A \varphi_\pi(x) \times \exp\left[-\frac{\mathbf{k}_\perp + m_q^2}{8\beta^2 x(1-x)}\right]$$

$$\bullet \varphi_\pi(x) = (1 + B C_2^{3/2} (2x - 1))$$

$$\phi_\pi(x, \mu_0^2) = \frac{2\sqrt{3}}{f_\pi} \int_{|\mathbf{k}_\perp|^2 \leq \mu_0^2} \frac{d^2 \mathbf{k}_\perp}{16\pi^3} \Psi_{q\bar{q}}(x, \mathbf{k}_\perp)$$

# The quark distribution amplitude of the pion

PHYSICAL REVIEW D 82, 034024 (2010)

## Implication on the pion distribution amplitude from the pion-photon transition form factor with the new BABAR data

Xing-Gang Wu\*

Department of Physics, Chongqing University, Chongqing 400044, People's Republic of China

Tao Huang†

Institute of High Energy Physics and Theoretical Physics Center for Science Facilities, Chinese Academy of Sciences, Beijing 100049, People's Republic of China

(Received 19 May 2010; published 19 August 2010)

The new BABAR data on the pion-photon transition form factor arouses people's interest for the determination of the pion distribution amplitude. To explain the data, we take both the leading valence quark state's and the nonvalence quark state's contributions into consideration, where the valence quark part up to next-to-leading order is presented and the nonvalence quark part is estimated by a phenomenological model based on its limiting behavior at both  $Q^2 \rightarrow 0$  and  $Q^2 \rightarrow \infty$ . Our results show that to be consistent with the new BABAR data at the large  $Q^2$  region, a broader amplitude other than the asymptoticlike pion distribution amplitude should be adopted. The broadness of the pion distribution amplitude is controlled by a parameter  $B$ . It has been found that the new BABAR data at low and high energy regions can be explained simultaneously by setting  $B$  to be around 0.60, in which the pion distribution amplitude is closed to the Chernyak-Zhitnitsky form.

DOI: 10.1103/PhysRevD.82.034024

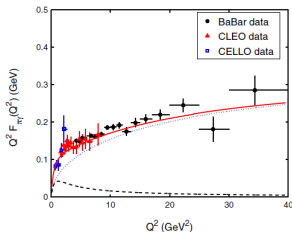


FIG. 5 (color online).  $Q^2 F_{\pi\gamma}(Q^2)$  with the model wave function (3) by taking  $m_q = 0.30$  GeV and  $B = 0.60$ . The solid, the dotted, and the dashed lines are for the total contribution, the leading valence quark contribution, and the nonvalence quark contribution to the form factor, respectively.

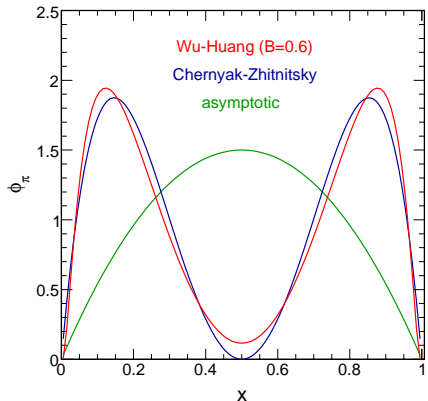
$$\begin{aligned} \phi_\pi(x, \mu_0^2) &= \\ &= \frac{\sqrt{3} A m_q \beta}{2\sqrt{2}\pi^{3/2} f_\pi} \sqrt{x(1-x)} \\ &\times \left( 1 + B \times C_2^{3/2} (2x-1) \right) \\ &\times \left( \operatorname{erf} \left[ \sqrt{\frac{m_q^2 + \mu_0^2}{8\beta^2 x(1-x)}} \right] \right. \\ &\left. - \operatorname{erf} \left[ \sqrt{\frac{m_q^2}{8\beta^2 x(1-x)}} \right] \right) \end{aligned}$$

- $B = 0.6$
- $m_q = 0.3$  GeV
- $A = 16.62$  GeV<sup>-1</sup>
- $\beta = 0.745$  GeV

## The quark distribution amplitude of the pion

$$\phi_\pi(x)_{\text{CZ}} = 30x(1-x)(2x-1)^2$$

$$\phi_\pi(x)_{\text{as}} = 6x(1-x)$$



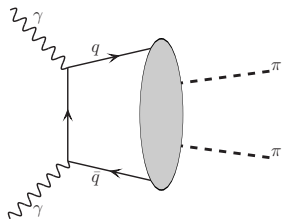
$$\begin{aligned} & \phi_\pi(x, \mu_0^2)_{\text{WH}} = \\ & = \frac{\sqrt{3} A m_q \beta}{2\sqrt{2}\pi^{3/2} f_\pi} \sqrt{x(1-x)} \\ & \times \left( 1 + B \times C_2^{3/2} (2x-1) \right) \\ & \times \left( \operatorname{erf} \left[ \sqrt{\frac{m_q^2 + \mu_0^2}{8\beta^2 x(1-x)}} \right] \right. \\ & \left. - \operatorname{erf} \left[ \sqrt{\frac{m_q^2}{8\beta^2 x(1-x)}} \right] \right) \end{aligned}$$

- $B = 0.6$
- $m_q = 0.3 \text{ GeV}$
- $A = 16.62 \text{ GeV}^{-1}$
- $\beta = 0.745 \text{ GeV}$

$$\gamma\gamma \rightarrow \pi\pi$$

$$PbPb \rightarrow PbPb\pi\pi$$

# Hand-bag model

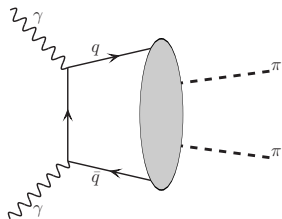


M. Diehl, P. Kroll and C. Vogt,  
Phys. Lett. **B532** (2002) 99;

M. Diehl and P. Kroll,  
Phys. Lett. **B683** (2010) 165.



# Hand-bag model



M. Diehl, P. Kroll and C. Vogt,  
Phys. Lett. **B532** (2002) 99;

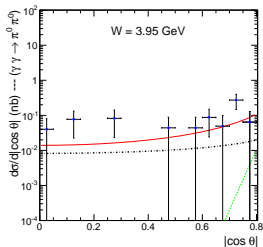
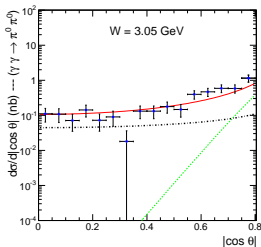
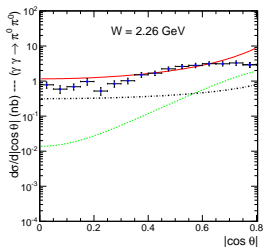
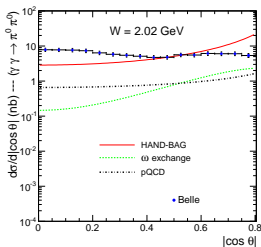
M. Diehl and P. Kroll,  
Phys. Lett. **B683** (2010) 165.

$$\mathcal{A}_{+-} = \mathcal{A}_{-+} = -4\pi_{em} \frac{s^2}{tu} R_{\pi\pi}(s) \propto \frac{1}{\sin^2\theta}$$

$$R_{\pi\pi}(s) = \frac{5}{9s} a_u \left(\frac{s_0}{s}\right)^{n_u} + \frac{1}{9s} a_s \left(\frac{s_0}{s}\right)^{n_s}$$

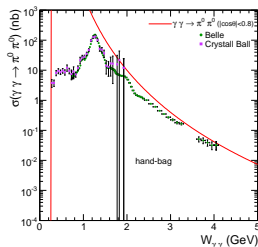
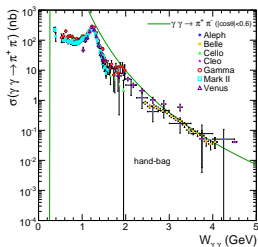
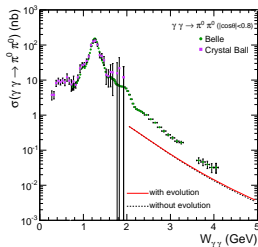
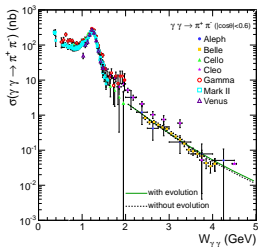
- $s_0 = 9 \text{ GeV}^2$
- $a_u = 1.375 \text{ GeV}^2$
- $a_s = 0.5025 \text{ GeV}^2$
- $n_u = 0.4175$
- $n_s = 1.195$

$$\sigma(\gamma\gamma \rightarrow \pi^+\pi^-) = \frac{4\pi\alpha_{em}^2}{s} \left( \frac{\cos\theta_0}{\sin^2\theta_0} + \frac{1}{2} \ln \frac{1 + \cos\theta_0}{1 - \cos\theta_0} \right) |R_{\pi\pi}(s)|^2$$

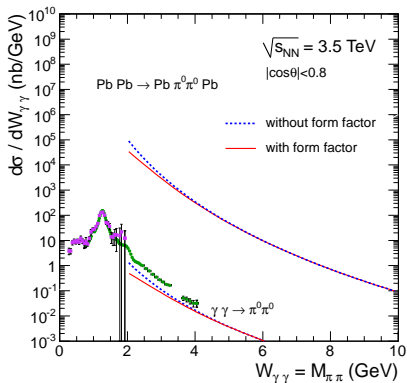
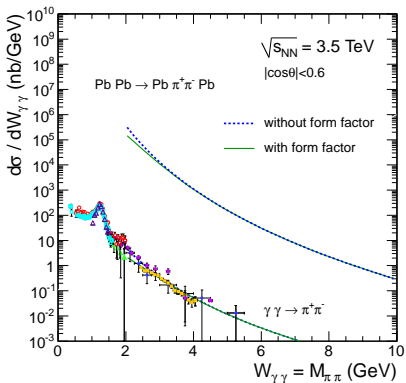
$$\frac{d\sigma(\gamma\gamma \rightarrow \pi^0\pi^0)}{dz} \implies \text{pQCD vs hand-bag vs } \omega \text{ exchange}$$


$$\gamma\gamma \rightarrow \pi\pi$$

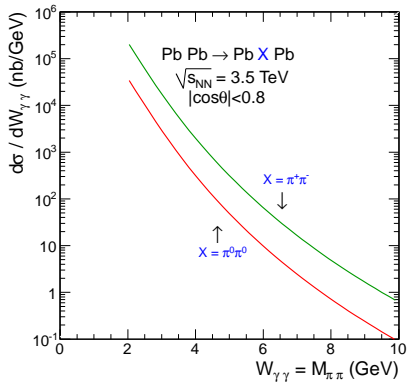
$$PbPb \rightarrow PbPb\pi\pi$$

$$\sigma(\gamma\gamma \rightarrow \pi^+\pi^-) \text{ \& \ } \sigma(\gamma\gamma \rightarrow \pi^0\pi^0) \implies \text{pQCD vs hand-bag}$$


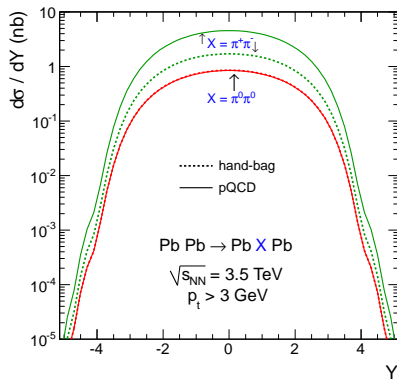
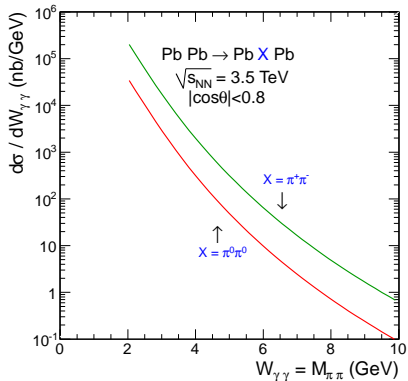
# Nuclear cross section



# Nuclear cross section



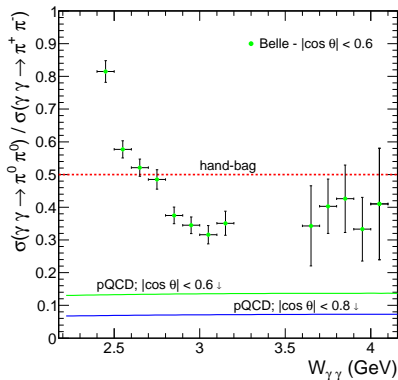
# Nuclear cross section



# Conclusions

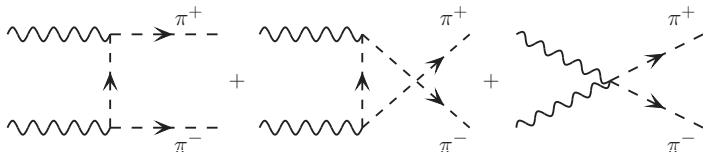
$$\frac{\sigma(\gamma\gamma \rightarrow \pi^0\pi^0)}{\sigma(\gamma\gamma \rightarrow \pi^+\pi^-)}$$

pQCD vs hand-bag mechanism

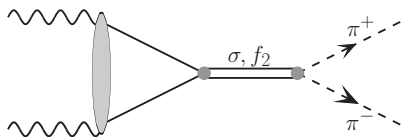


# Other mechanisms

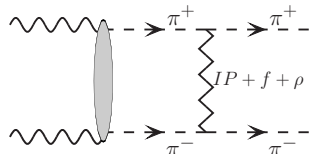
- Pion exchange



- Resonances



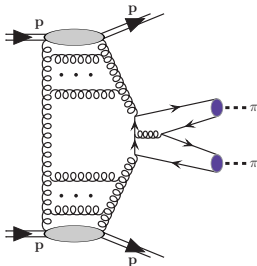
- High-energy  $\pi\pi$  rescattering



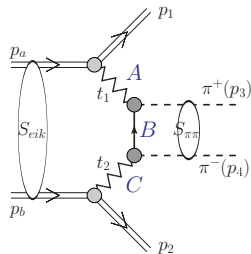


## Some other related works

- A new pQCD mechanism:  
L. A. Harland-Lang,  
V. A. Khoze,  
M. G. Ryskin and  
W. J. Stirling,  
[arXiv: 1105.1626 \[hep-ph\]](https://arxiv.org/abs/1105.1626)



- But here  
non-perturbative mechanism:  
P. Lebiedowicz,  
R. Pasechnik and  
A. Szczurek,  
[arXiv: 1103.5642 \[hep-ph\]](https://arxiv.org/abs/1103.5642)



$$\gamma\gamma \rightarrow \pi\pi$$

$$PbPb \rightarrow PbPb\pi\pi$$

# Thank You For Attention