

A WEAKLY PARAMETRIC APPROACH TO STOCHASTIC BACKGROUND IN LISA

[arXiv:2311.12111](https://arxiv.org/abs/2311.12111)

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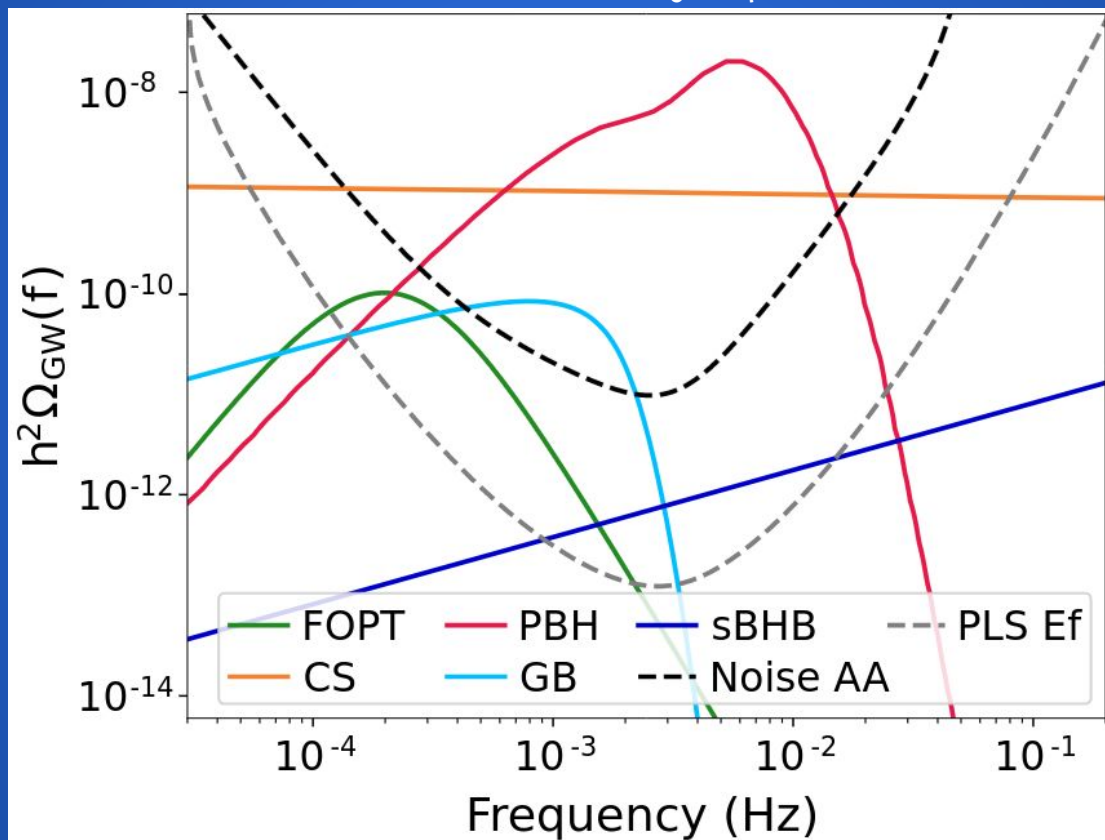
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11th LISA CosWG - 19/6/2024



STOCHASTIC BACKGROUND IN LISA

LISA Definition Study Report



SEARCHING BACKGROUND IN LISA -CHALLENGES

NOISE

SIGNAL

$$C(f) = S_n(f) + R(f)S_h(f)$$

SEARCHING BACKGROUND IN LISA -CHALLENGES

$$C(f) = S_n(f) + R(f)S_h(f)$$

- Non-Stationarity (gaps, glitches, ...)
- Noise Uncertainties
- Correlation between TDI channels
- likely non-existing null channel

SEARCHING BACKGROUND IN LISA -CHALLENGES

$$C(f) = S_n(f) + R(f)S_h(f)$$

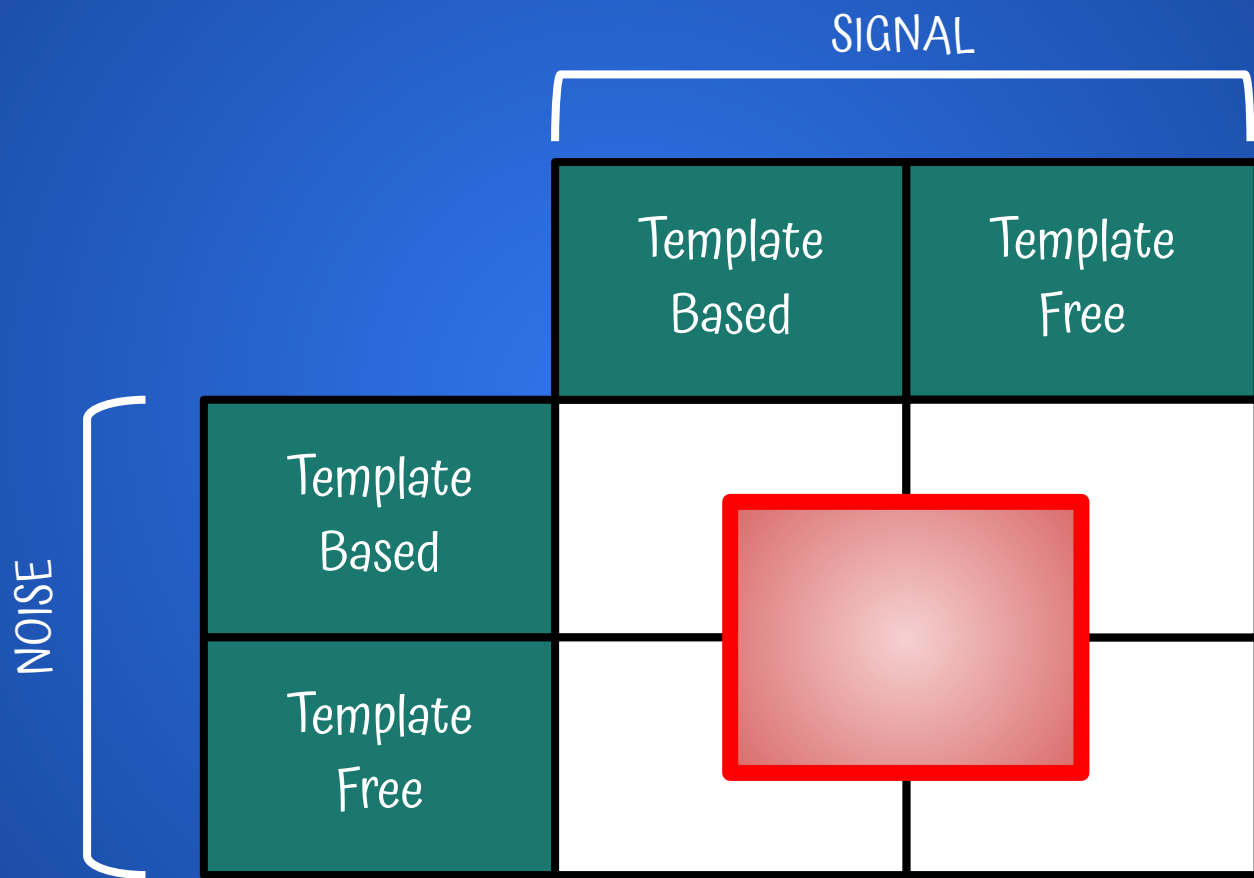
- Non-stationarity, Anisotropy, Non-Gaussianity
- Overlapping signals
- Astrophysical Models depend on populations
- Cosmological Models depend on fundamental physics

SEARCHING BACKGROUND IN LISA - MODELS

		SIGNAL	
		Template Based	Template Free
NOISE	Template Based	Boileau 23 Adam 14	Caprini 19 Flauger 21
	Template Free	Baghi 23 Muratore 23	?

What do we propose?

SEARCHING BACKGROUND IN LISA - MODELS



MODELLING WITH GP - PRELIMINARY ASSUMPTION

→ Fourier Domain

MODELLING WITH GP - PRELIMINARY ASSUMPTION

- *Fourier Domain*
- *GENERATION 1.5 TDI (Unequal and constants LISA arms) and AET variables*

MODELLING WITH GP - PRELIMINARY ASSUMPTION

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- Whittle Likelihood

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- Model Signal and Noise strain:

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- Model Signal and Noise strain:

+ We assume perfect knowledge of TDI transfer matrix (*)

$$S_{n,\alpha\beta}(f) = \frac{1}{2} S_n(f) M_{\alpha i, \text{TDI}}(f) M_{i\beta, \text{TDI}}^*(f)$$

*Note: OMS and Acceleration noise components have different transfer function

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$$S_{h,\alpha\beta}(f) = R_{\alpha\beta}(f) S_h(f)$$

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MODELLING WITH GP

We employ the expectation value of Gaussian Process to model the PSD

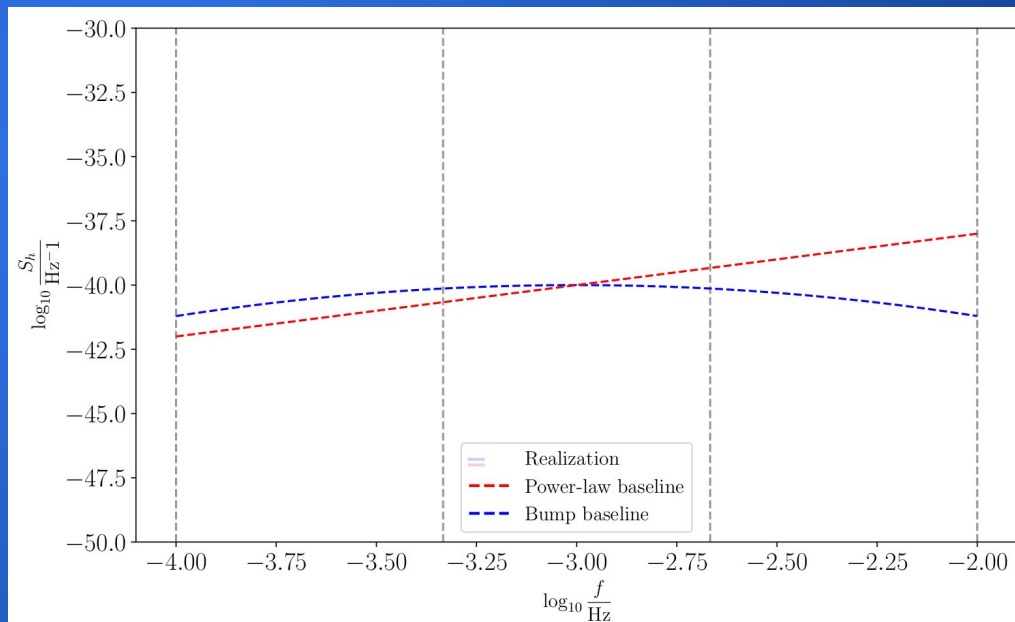
$$\mu(X_* | X) = \mu(X_*) + \Sigma(X_*, X)\Sigma(X, X)^{-1}(g(X) - \mu(X))$$

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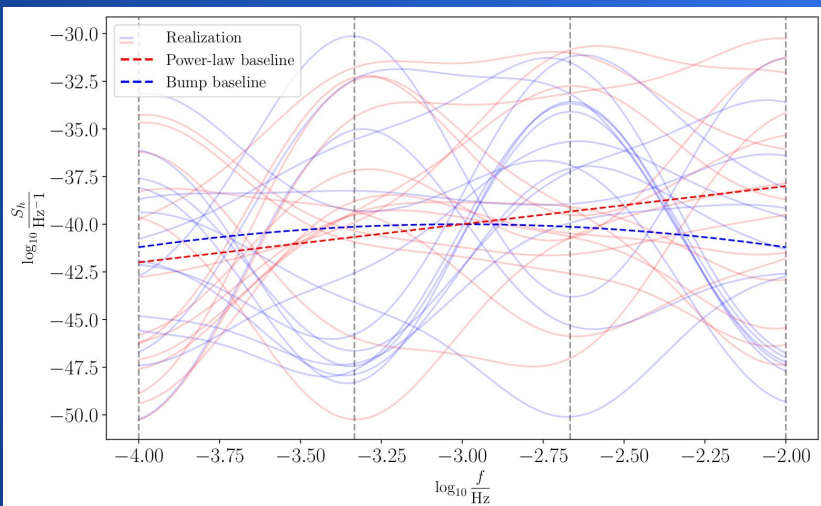
BASELINE



MODELLING WITH GP

We employ the expectation value of Gaussian Process to model the PSD

$$\mu(X_* | X) = \mu(X_*) + \Sigma(X_*, X)\Sigma(X, X)^{-1}(g(X) - \mu(X))$$



DEVIATION FROM THE
BASELINE AT KNOTS
where

$$\Sigma_{ij}^{RBF}(X, Y) = k_{RBF}(x_i, y_j) = \exp\left(-\frac{|x_i - y_j|^2}{2\sigma^2}\right)$$

MODELLING WITH GP

We employ the expectation value of Gaussian Process (EGP) to model the PSD

$$\mu(X_* | X) = \underbrace{\mu(X_*)}_{\text{BASELINE}} + \underbrace{\Sigma(X_*, X)\Sigma(X, X)^{-1}(g(X) - \mu(X))}_{\text{DEVIATION FROM THE BASELINE AT KNOTS}}$$

BASELINE

DEVIATION FROM THE
BASELINE AT KNOTS

The model depends on 2 hyperparameters:

- the number of knots
- kernel lengthscale

MODELLING WITH GP

We employ the expectation value of Gaussian Process (EGP) to model the PSD

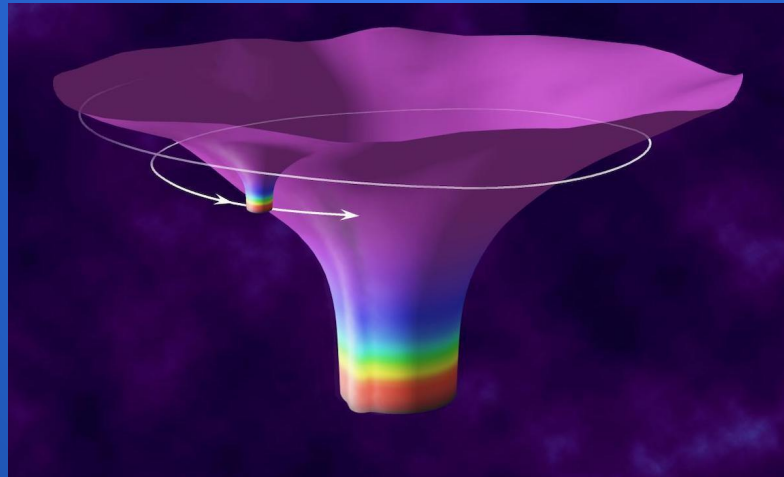
$$\mu(X_* | X) = \mu(X_*) + \Sigma(X_*, X)\Sigma(X, X)^{-1}(g(X) - \mu(X))$$

SIGNAL with power-law as
baseline

NOISE with fixed baseline at
SciRD level

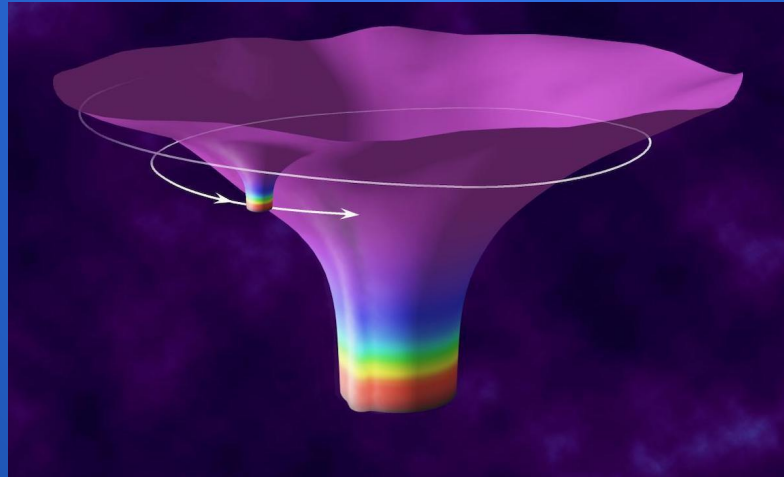
*Number of knots can be different for noise and signal

RESULTS - APPLICATION TO EMRI



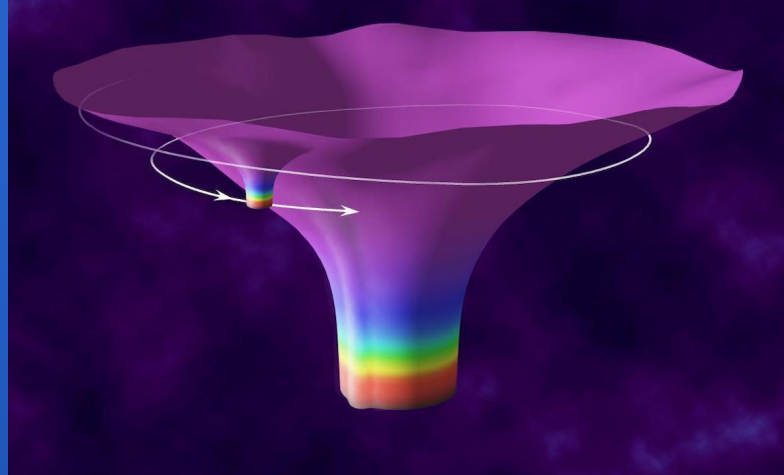
RESULTS - APPLICATION TO EMRI

- The largest majority of EMRIs will be undetectable \longrightarrow Possible SGWB



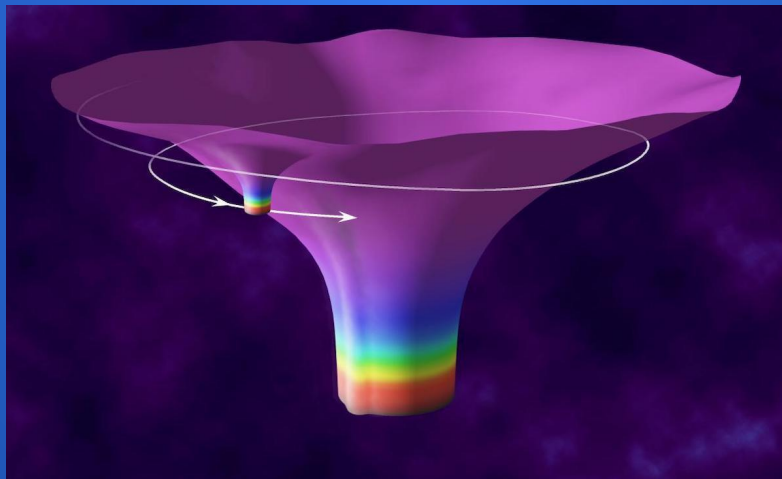
RESULTS - APPLICATION TO EMRI

- The largest majority of EMRIs will be undetectable \longrightarrow Possible SGWB
- EMRI are extremely complex objects, both for the GW waveform and population



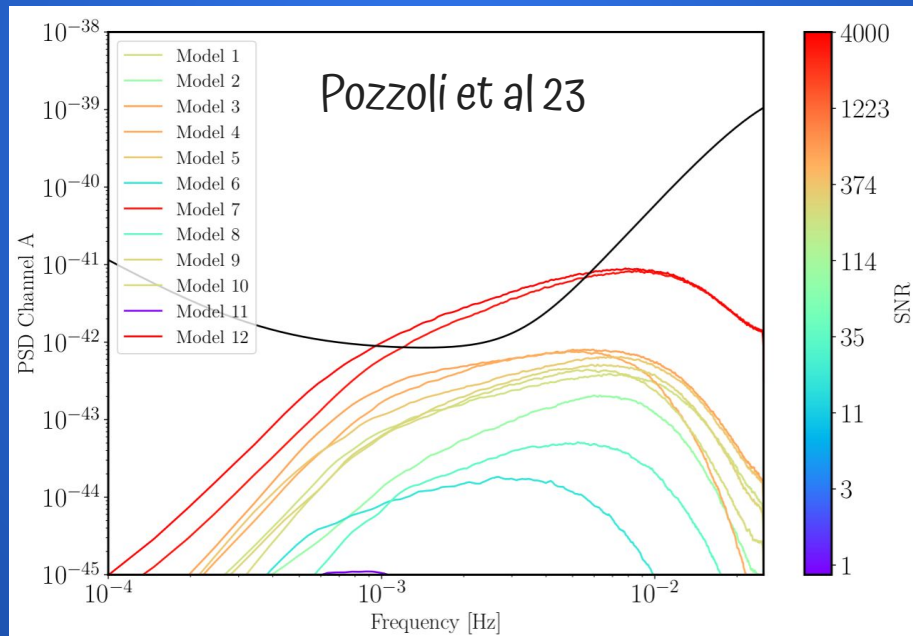
RESULTS - APPLICATION TO EMRI

- The largest majority of EMRIs will be undetectable → Possible SGWB
- EMRI are extremely complex objects, both for the GW waveform and population
- A lot of uncertainties in the SGWB



RESULTS - APPLICATION TO EMRI

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RESULTS - APPLICATION TO EMRI

→ Free Template algorithm is necessary to study this kind of SGWB

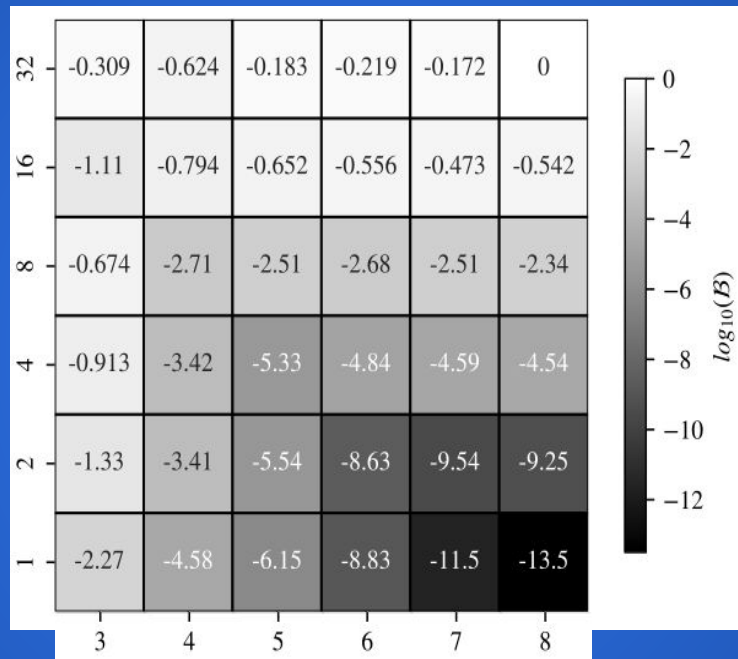
- We inject noise + EMRI realization M1 from Pozzoli et al 23
- We recover noise with EGP using 3 knots
- We recover signal exploring different combination of hyperparameters

RESULTS - APPLICATION TO EMRI

STIFFNESS - GLOBAL



Lengthscale of Kernel



$\log_{10}(B)$

BETTER FIT

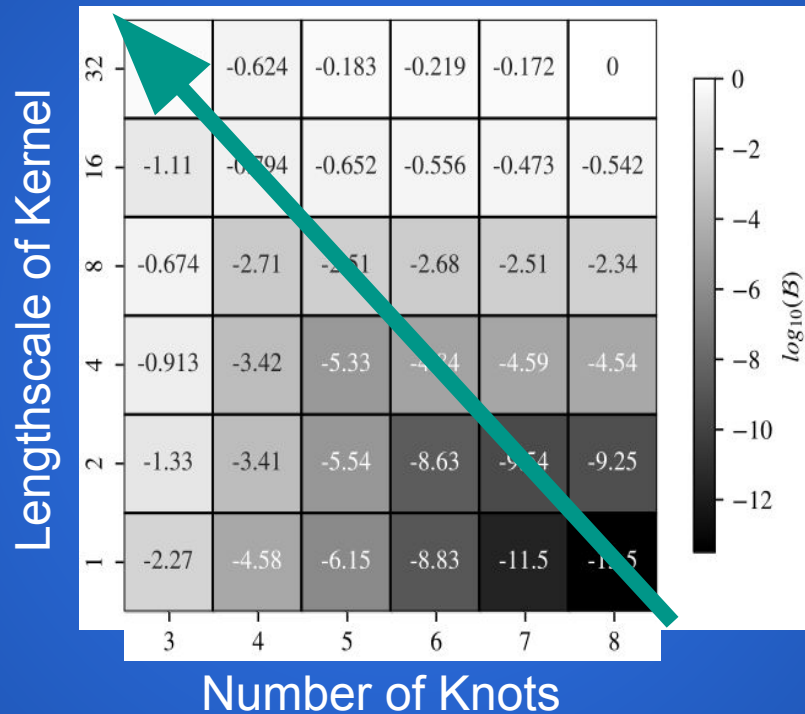


Number of Knots



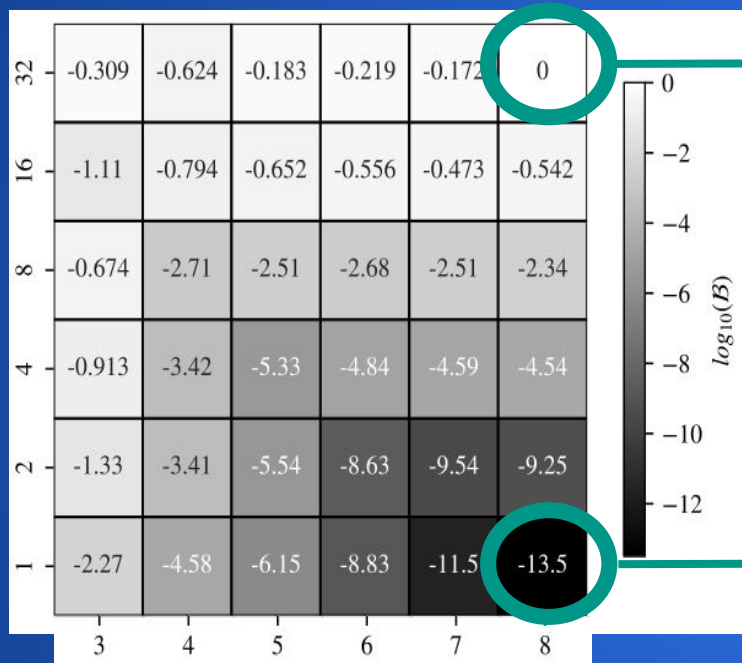
GRANULARITY - LOCAL

RESULTS - APPLICATION TO EMRI

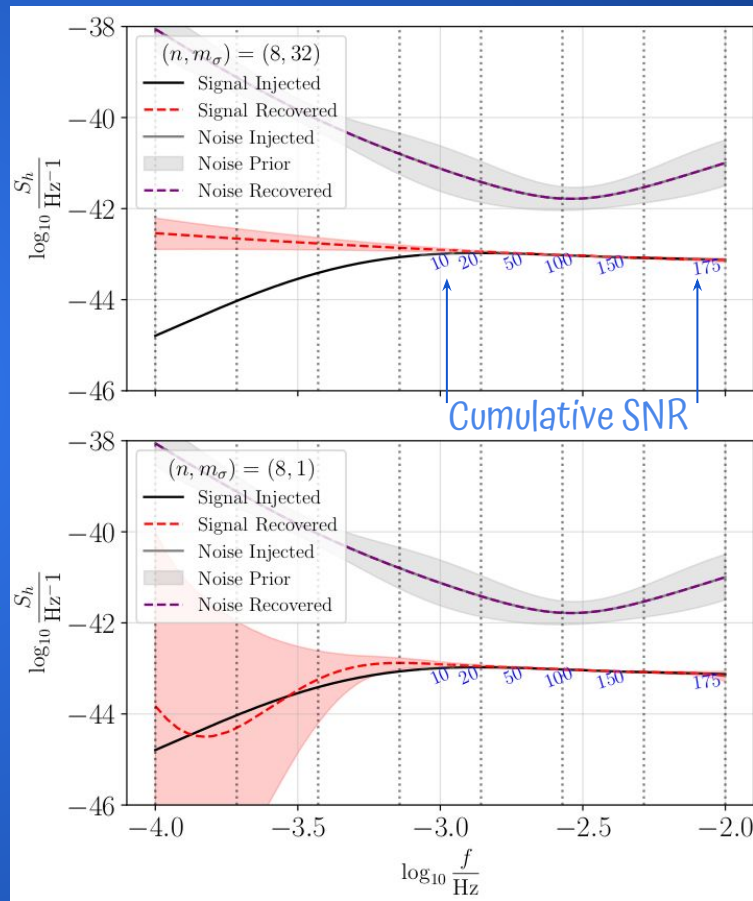


RESULTS - APPLICATION TO EMRI

Lengthscale of Kernel



Number of Knots



CONCLUSIONS & OUTLOOKS

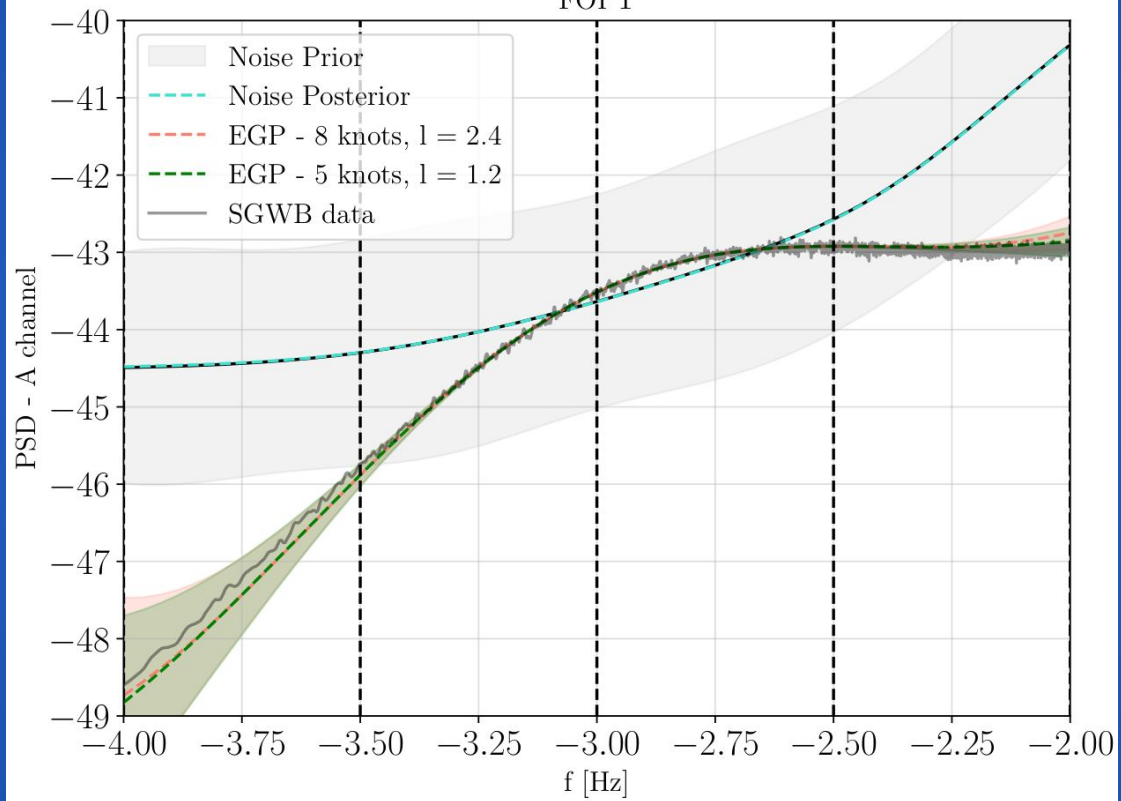
In this work, we introduce a new flexible method for the simultaneous inference of SGWB and LISA noise.

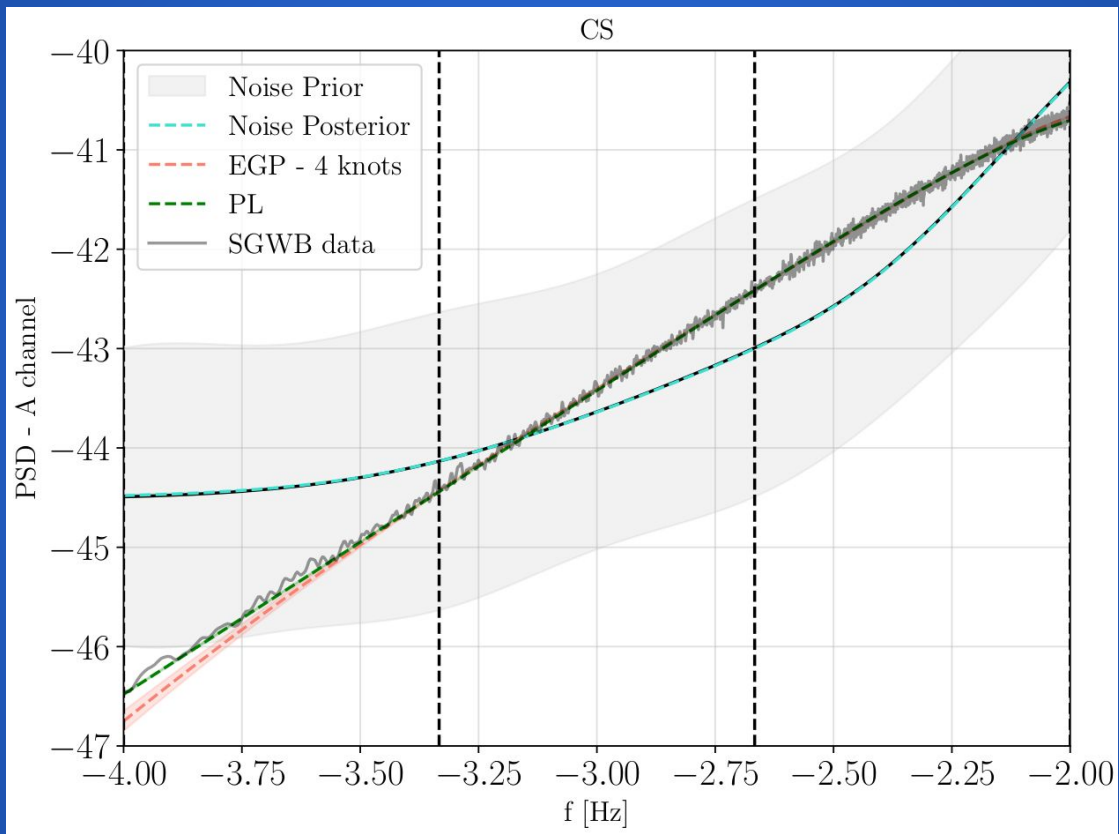
FUTURE EXTENSIONS:

- *Multiple Backgrounds Injection*
- *Include correlation terms in TDI matrix*
- *Transdimensional Sampler*
- *Non-Stationary Signal (e.g., MW Foreground)*

THANK YOU!

FOPT





$$C(f, f') = \sum_{n=-8}^{n=8} B_n S_h \left(\frac{f' + f}{2} \right) \delta \left(f - f' + \frac{n}{T} \right)$$

