### Monte-Carlo developments and Electroweak/mixed QCD-EW corrections

Marco Zaro LHC EWWG, July 2024







#### Outline

- Recent progress in the computation of EW corrections
  - Introduction on EW and mixed QCD-EW corrections
  - EW corrections in the high-energy limit
  - The problem of PS matching
  - Mixed QCD/EW corrections to Drell-Yan at NNLO
- Recent and future developments in MC tools
  - NNLO+PS predictions
  - Techniques for the reduction of negative weights in MC@NLO-type matching
  - GPU/AI related developments





### EW corrections and mixed-coupling expansion





$$\sigma_{pp \to X}(s) = \sum_{ab} \int dx_1 dx_2 f_a(x_1) f_b(x_2) \hat{\sigma}_{ab \to X}(\hat{s} = x_1 x_2 s)$$





• The way we do precise predictions: perturbation theory

Probability of finding a parton into the proton

$$\sigma_{pp\to X}(s) = \sum_{ab} \int dx_1 dx_2 f_a(x_1) f_b(x_2) \hat{\sigma}_{ab\to X}(\hat{s} = x_1 x_2 s)$$
Parton distribution functions:

Parton distribution functions: must be fit to data, process independent





#### • The way we do precise predictions: perturbation theory

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must be fit to data, process independent

Partonic cross section: can be computed in perturbation theory, process dependent





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LO
NLO
strong coupling, ~0.1





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NNLO
strong coupling, ~0.1
NLO
NLO











#### • The way we do precise predictions: perturbation theory



• Going higher orders, the complexity of the computation explodes

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#### Electroweak corrections: a multi-coupling expansion

- If EW corrections come into play, one must carry the expansion both in a and as
- The structure of a given process are something like







Some comments







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- The presence of different powers of  $\alpha$  and  $\alpha_s$  hints at a power-counting estimate for the contributions. Such an estimate is often misleading!





Some comments



- For IR-finiteness, contributions of QCD and EW origin to a given contribution must *both* be included
- The presence of different powers of  $\alpha$  and  $\alpha_s$  hints at a power-counting estimate for the contributions. Such an estimate is often misleading!
- Predictions including all the contributions at LO/NLO/... are typically called "Complete-LO/NLO/..."
   NLO EW and Complete-NLO predictions can be obtained with automatic (and mostly public) tools

Collier, GoSam, MG5\_aMC, Recola, Sherpa+Collier/OpenLoops/OpenLoops2/...



#### Coupling-hiearchy violation Drell-Yan



Dittmaier et al, 0911.2329



- Because of photon radiation from events on the peak, the region M(e<sup>+</sup>e<sup>-</sup>)<m<sub>Z</sub> receives huge EW corrections
- NLO QCD corrections remain fairly stable across the peak







#### Coupling-hiearchy violation VBS

Biedermann et al, 1708.00268





- In VBS, EW and QCD induced production modes comparable at LO
- NLO EW corrections to EW-induced mode (NLO<sub>4</sub>) are by far the dominant NLO contribution
- Not only for ssWW, but general feature of VBS processes
   WZ: Denner et al, 1904.00882





### **Coupling-hiearchy violation**







- 4top production receives contributions induced by  $y_t$  which ends up in (N)LO<sub>2</sub> $\rightarrow$ ...
- Despite being subleading by power-counting, even  $NLO_4$  can amount to some 10%s wrt  $LO_1$
- Accidental cancelations occur among the various contributions with the complete-NLO being very close to  $LO_1$ +NLO<sub>1</sub> (NLO QCD)
- A non-SM y<sub>t</sub> will spoil these cancelations
  - 4top as BSM probe





### Approximate EW corrections in the high-energy limit



### Approximate EW corrections in the high-energy limit



- EW corrections show universal behaviour when all invariants are large
   Logarithmic enhancement are gue to would be IR siggularities related to W and Z masses, the so-called Sudakov logs
- In this limit, the logarithmic 'c' <u>other building</u> pe control to the state of t
- This can be very helpful if EVV corrections for a given process are dominated by Sudakov logs, if the large-invariants regime is considered, and if the process is not mass-suppressed



- Automated by 3 different collaborations Sherpa: Bothmann et al, 2006.14635; Sc G5 aMC Pagani, MZ, 2110.037, 4; OpenLoops: Lindert et al, 2312.07927
- They provide easy solutions to difficult problems:
  - Much more stable and faster than EW corrections
  - Possibility to combine approximate-EW corrections with NLO-QCD predictions matched to PS (possibly in multijet-merged samples)
     Bothmann et al, 2111.13453; Pagani, Vitos, MZ, 2309.00452
  - They exponentiate and can be resummed to all-orders
- However, one should always check whether the Sudakov approx holds against the exact EW corrections

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### Don't buy everything they sell

• In ZHH production, at *large*  $p_T(Z)$ , EWSLs fail to reproduce EW corrections







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#### Resummation of EW Sudakov logs

- Denner, Rode, 2402.10503
- Since EW corrections are non-diagonal wrt flavour, exponentiation of Sudakov-logs is highly non-trivial
- Seminal studies for 2-loop amplitudes suggested to exponentiate separately weak and QED terms, and about their order Denner et al, hep-ph/0301241
- Resummation achieved using the EW version of SCET, included in a fullydifferential MC
- Results presented for CLIC@3TeV and FCC-hh@100TeV



While the resummation of large EW logarithms is a must at future high-energy colliders, the application of the  $SCET_{EW}$  formalism to realistic diboson processes is nontrivial and requires a number of approximations that need to be carefully checked.

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### Matching with parton shower?

- EW corrections matched with PS still not available for general processes
  - Approximate approaches exist, only including n-body contribution ("EWvirt" or EWSL). Accuracy depends on kinematics region
     EWVirt: VV(J): Brauer et al, 2005.12128; top: Gutschov et al, 1803.00950; V+jets: Kallweit et al, 1511.08692, ...

 Exact matching performed only for processes with just LO<sub>1</sub> (in the Powheg scheme)
 DY: Barzè et al, 1302.4606; HV(J): Granata et al, 1706.03522;
 VBS: Chiesa et al, 1906.01863, VV: Chiesa et al, 2005.12146;
 WZ@NNLO+PS: Lindert et al, 2208.12660

 Main issue: how to assign colour-flows to interferences (LO<sub>2</sub> is mostly an interference contribution) Some ideas: Frixione et al, 2106.13471







#### Attaining the highest precision: Drell-Yan NNLO QCD×EW





#### Attaining the highest precision: Drell-Yan NNLO QCD×EW

- Lepton-pair production (Drell-Yan) is a highprecision probe of the EW sector (M<sub>W</sub>, sinθ<sub>W</sub>, ...)
- NNLO QCD+NLO EW not enough for current and upcoming exp. data
- NNLO<sub>2</sub> has been the frontier for long time:
  - Historically, different approaches have been pursued for the pole vs large-m(l<sup>+</sup>l<sup>-</sup>) region
  - Complicated topologies (massive double box)
- Recently, full computations of NNLO<sub>2</sub> have become available, both for NC and CC process
- I will briefly review these works, focusing on pheno results







2106.11953

#### Mixed QCD-EW corrections to NC Drell-Yan

Mixed Strong-Electroweak Corrections to the Drell-Yan Process

Roberto Bonciani<sup>®</sup>,<sup>1,\*</sup> Luca Buonocore<sup>®</sup>,<sup>2,†</sup> Massimiliano Grazzini<sup>®</sup>,<sup>2,‡</sup> Stefan Kallweit<sup>®</sup>,<sup>3,§</sup> Narayan Rana<sup>®</sup>,<sup>4,||</sup> Francesco Tramontano<sup>®</sup>,<sup>5,¶</sup> and Alessandro Vicini<sup>®</sup>,<sup>4,\*\*</sup>

- First computation of NNLO<sub>2</sub> (with massive leptons)
  - Amplitues computed with semi-analytical approach
  - IR Subtraction with Matrix Grazzini et al, 1711.06631
- Comparison with pole approx and naive factorisation of K-factors



- Peak region: excellent agreement with PA. Very large effects due to radiation. Naive factorisation fails
- Large inv.mass: O(0.5%) difference wrt PA and naive fact, due to genuinely nonfactorisable contributions
- NNLO<sub>2</sub> corrections at the 1% level in the large inv.mass region

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#### Mixed QCD-EW corrections at large mariant mass

- Two-loop amplitudes computed in 2020, without widths Heller et al, 2012.05918
- IR subtraction with nested softcollinear scheme Caola et al, 1702.01352
- Computation with massless leptons (recombination needed)
- NNLO<sub>2</sub> corrections at the 1% level wrt NLO<sub>QCD+EW</sub> in the large inv.mass region (up to 1 TeV)
- Growth with invariant mass due to Sudakov effects, up to 3% at 3 TeV
- Surprisingly large size in the TeV region wrt to power counting

Mixed QCD-electroweak corrections to dilepton production at the LHC in the high invariant mass region

Federico Buccioni,<sup>*a*</sup> Fabrizio Caola,<sup>*a,b*</sup> Herschel A. Chawdhry,<sup>*a*</sup> Federica Devoto,<sup>*a*</sup> Matthias Heller,<sup>*c*</sup> Andreas von Manteuffel,<sup>*d*</sup> Kirill Melnikov,<sup>*e*</sup> Raoul Röntsch<sup>*f*</sup> and Chiara Signorile-Signorile<sup>*e,g*</sup> 2303.1237





### From NC to CC

Armadillo, Bonciani, Devoto, Rana, Vicini, 2405.00612

- The CC case requires new topologies wrt the NC one
  - Most complicated: double-box, with 2 different internal masses
  - Solved by in-house package for differential equations, based on LiteRed and SeaSyde (series expansion wrt invariants)
  - Boundary condition evaluated with AMFlow
  - Checked that the result matches the equal-masses topology
  - Complex-mass scheme and lepton mass≠0
- Results available as a grid, including full dependence on W mass

LiteRed: Lee, 1310.1145; AMFlow: Liu et al, 2201.1/1669; SeaSyde: Armadillo et al, 2205.03345

и W и d d Ζ μ 60 101.0 0.50.0 cosl 60 -0.580  $\sqrt{s} [G_{eV]}$ 100 120 - 1.0



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### Resummation of QED effects

Buonocore, Rottoli, Torrielli, 2404.15112

- Soft QED and mixed effects added on top of QCD ones, within the Radish framework Monni et al, 1604.02191
- QED soft effects due to correlations with final-state leptons included
  - See also earlier work with stable W/Z Autieri et al, 2302.05403
     N311' OCD
     N11' MIX Gemon Lm+n

$$R(k_{t1}) = \left[ R(k_{t1}) \right]_{\text{eq.}(2.4)} + R^{\text{QED}}(k_{t1}) + R^{\text{MIX}}(k_{t1}) + \frac{\alpha_s}{2\pi} \frac{\alpha}{2\pi} B^{(1,1)} L$$







### Part 2 Recent and planned developments for MC tools





### NNLO+PS predictions





#### MiNNLO+PS

- NLO QCD+PS has been the golden standard for long time  $\hat{\sigma}_{ab \to X} = \hat{\sigma}_{ab \to X}^{(0)} + LO$ MG5 aMC/Sherpa/Powheg
- Going beyond NLO: NNLO
  - NNLO+PS relies on rather mature technology (MiNNLOPS) Monni et al. 1908.06987
  - All currently-available NNLO QCD computation can (in principle) be included into a NNLO+PS generator
  - Implementation is still process-dependent, and mostly done by hand

bbH: Biello et al, 2402.04025; b prod: Mazzitelli et al, 2302.01645; WZ (+EW) Lindert et al, 2208.12660; ZH (SMEFT): Haisch et al, 2204.00663; top: Mazzitelli et al, 2112.12135, ...



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#### NNLO+PS in Geneva

- The Geneva method combines NNLO+PS with N-jettiness resummation at NNLL' Alioli et al, 1211.7049
- $_{\gamma\gamma}W\gamma$  Implomented and validated for several color-singlet processes



- New developments:
  - Resumming second jet resolution at NLL'
  - Extension towards color-singlet+jet processes WIP





# Reduction of negative weights in MC@NLO-type matching





- MC@NLO-matched MCs affected by negative weights
  - Reduce the statistical quality of the event sample
  - More events need to be generated than with positiveonly events
- Recent progress both in Sherpa and MG5\_aMC:
  - MG5\_aMC: modify the matching by a term which improves the IR behaviour of the MC counterterms Frederix et al, 2002.12716

Alternatively, spread the Born over the radiative PS in order to compensate for over-cancelation of local CTs or negative virtuals Frederix, Torrielli, 2310.04160

- Sherpa: use leading-colour approximation+move Kfactor to low-mult. processes in merged samples Danzinger et al, 2110.15211
- Other approaches (MC-agnostic):
  - Positive resampler: resample cross section to eliminate negative weights Andersen et al, 2005.09375



	MC@NLO	MC@NLO- $\Delta$
$pp \rightarrow e^+e^-$	3.5%~(1.2)	2.4% (1.1)
$pp \rightarrow e^+ \nu_e$	3.8%~(1.2)	2.5%~(1.1)
$pp \to H$	4.9%~(1.2)	2.0% (1.1)
$pp \to H b \bar{b}$	38.4% (19)	32.6%~(8.2)
$pp \to W^+ j$	16.5%~(2.2)	7.9%~(1.4)
$pp \to W^+ t \bar{t}$	15.2% (2.1)	11.9% (1.7)
$pp \to t \bar{t}$	20.2% (2.8)	9.3%~(1.5)





 $d\sigma/dp_{\perp}(jet 1) [pb/GeV]$ 

#### Results



#### 2110.15211 (Z+jets)







# Towards the usage of GPUs and AI in the MG5\_aMC framework





#### Improving computing performances

- Computing demand requires more efficient and smarter handling of resources
- On one side, move away from multi-threading in favour of multiprocessing (SIMD/OpenMP), suitable for GPUs
  - This requires rewriting and rethinking our (old) codes
- On the other, benefit from AI to improve some specific aspects (integration/event-gen./...)

#### • See also:

"Event Generators for High-Energy Physics Experiments", 2203.11110 "Machine learning and LHC event generation", 2203.07460 "Challenges in Monte Carlo event generator software for High-Luminosity LHC", 2004.13687





#### Towards MG5\_aMC on GPU

#### MadFlow: Carrazza, Cruz-Martinez, Rossi, MZ, 2106.10279



Process	MadFlow $\mathrm{CPU}$	${\tt MadFlow}~{\rm GPU}$	MG5_aMC
$gg \to t\bar{t}$	$9.86 \ \mu s$	$1.56 \ \mu s$	$20.21~\mu{\rm s}$
$pp \to t\bar{t}$	$14.99~\mu { m s}$	$2.20~\mu{ m s}$	$45.74~\mu{\rm s}$
$pp \to t\bar{t}g$	$57.84 \ \mu s$	$7.54~\mu { m s}$	$93.23~\mu{ m s}$
$pp \rightarrow t\bar{t}gg$	$559.67~\mu\mathrm{s}$	121.05 $\mu {\rm s}$	$793.92~\mu\mathrm{s}$

#### MG5onGPU: Valassi et al, 2106.12631, 2303.18244, 2312.02898





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# Using NN's for importance sampling



- Use NN to overcome some limitations of VEGAS
- Do not reinvent the wheel:
  - Pre-training with VEGAS (fast) used as starting point of normalizing-flow
  - Use NF on top of known analytical mappings
  - NF adjust the weight of each channel
- Important improvement both on variance and on unweighting efficiency, even for large multiplicities



All figures by R.Winterhalder

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Conclusions



- Kinematics, couplings (e.g. Yukawa), radiative return, EWSL
- EW corrections are moving beyond NLO
  - Drell-Yan corrections available for NNLO2, both NC and CC
  - Resummation available both for soft γs (jointly with QCD) and for EWSLs
- Still, we miss a general procedure for PS matching at NLO
  - EWSL approximation +PS seems a good compromise
  - But the validity of EWSL approximation (both in principle and in practice) should always be checked
- Lot of progress also beyond LHC physics (e<sup>+</sup>e<sup>-</sup>/ μ<sup>+</sup>μ<sup>-</sup>colliders, g-2) not covered in this talk





- Understanding and improving MC tools is crucial for a proper and efficient collaboration between theory and experiments
- Lot of recent activity, only a glimpse of it in these slides
  - Inclusion of higher orders beyond NLO QCD
  - Reduction of negative weights leads to reduction in needed n of events. Some methods already implemented in public tools
  - Faster simulations can profit of modern hardwares (GPUs) and of AI for integration/event generation. At the moment most WIP, but stay tuned!