

SO(10) Model of pseudo-Goldstone Dark Matter, Gravitational Waves from Walls Bounded by Strings and PTA data

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CTPU - CGA

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- 2 Model of Pseudo-Goldstone Dark Matter (pGDM)
- 3 Formation of Domain Walls Bounded by Strings
- 4 Gravitational Wave Background from WBS
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1 *Introduction*

Standard Model ($SU(2)_L \otimes U(1)_Y \otimes SU(3)_C$)

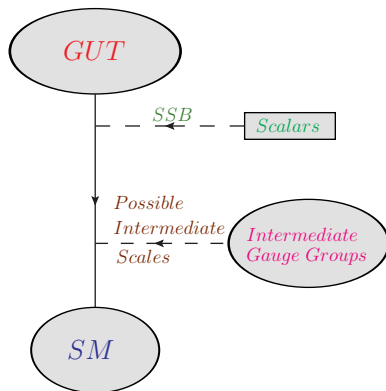
		Fields	Quantum numbers
Spin- $\frac{1}{2}$	Quarks	$Q_g^{i\alpha} = \left\{ \begin{pmatrix} u^\alpha \\ d^\alpha \end{pmatrix}_L, \begin{pmatrix} c^\alpha \\ s^\alpha \end{pmatrix}_L, \begin{pmatrix} t^\alpha \\ b^\alpha \end{pmatrix}_L \right\}$	$(2, \frac{1}{6}, 3)$
		$u_{\alpha L}^C, c_{\alpha L}^C, t_{\alpha L}^C$	$(1, -\frac{2}{3}, \bar{3})$
		$d_{\alpha L}^C, s_{\alpha L}^C, b_{\alpha L}^C$	$(1, \frac{1}{3}, \bar{3})$
Spin- $\frac{1}{2}$	Leptons	$\ell_g^i = \left\{ \begin{pmatrix} \nu_e \\ e \end{pmatrix}_L, \begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}_L, \begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}_L \right\}$	$(2, -\frac{1}{2}, 1)$
		$e_{\alpha L}^C, \mu_{\alpha L}^C, \tau_{\alpha L}^C$	$(1, 1, 1)$
Spin-1	$SU(2)_L$	W_μ^a	$(3, 0, 1)$
	$U(1)_Y$	B_μ	$(1, 0, 1)$
	$SU(3)_C$	G_μ^a	$(1, 0, 8)$
Spin-0	Higgs	$\Phi^i = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$	$(2, \frac{1}{2}, 1)$

Table: Fields in the Standard Model.

Grand Unification beyond the SM

- The basic idea in a Grand Unified Theory (GUT) is that the SM, $SU(2)_L \otimes U(1)_Y \otimes SU(3)_C$, is embedded in a larger simple group, \mathcal{G} .

Schematic view



- $SU(5)$ (rank = 4): $\bar{5} + 10 \Rightarrow$ SM fermions.

Georgi, Glashow, PRL **32**, 438 (1974)

- $SO(10)$ (rank = 5): $16 \Rightarrow$ SM fermions $\oplus \nu_L^C$.

Fritzsch, Minkowski, Ann. Phys. **93**, 93-266 (1975)

- $E(6)$ (rank = 6): $27 \Rightarrow$ SM fermions $\oplus \nu_L^C \oplus$

$$\underbrace{\left(2, \pm \frac{1}{2}, 1\right) + \left(1, -\frac{1}{3}, 3\right) + \left(1, \frac{1}{3}, \bar{3}\right) + (1, 0, 1)}_{\text{Exotic fermions}}$$

Exotic fermions

Gursey, Ramond, Sikivie, PLB **60** (1976) 177

Shafi, PLB **79** (1978) 301

2 *Model of Pseudo-Goldstone Dark Matter (pGDM)*

Model of Pseudo-Goldstone Dark Matter (pGDM)

- Introduce a complex singlet scalar S and a softly broken global $U(1)$ symmetry $S \rightarrow e^{i\alpha} S$.
- $V = -\mu_h^2 |H|^2 - \mu_s^2 |S|^2 + \lambda_h |H|^4 + \lambda_{hs} |H|^2 |S|^2 + \lambda_s |S|^4 - \mu_s'^2 (S^2 + \text{h.c.})$
- The **last term** explicitly breaks $U(1) \rightarrow \mathbb{Z}_2$.
- As the radial component of S gets a VEV, its angular component will be a **pseudo Nambu-Goldstone boson (pNGB)** due the **spontaneous and explicit breaking of the $U(1)$ symmetry**.
- Becomes a viable dark matter candidate stabilized by the symmetry $S \rightarrow S^*$.

C. Gross, O. Lebedev and T. Toma, Phys. Rev. Lett. **119** (2017) 191801

Domain Wall Problem

- The VEV of S spontaneously breaks \mathbb{Z}_2 .
- Breaking of exact \mathbb{Z}_2 produces topologically stable domain walls.
- The domain walls gradually dominate the energy density of the universe ($t \sim m_{\text{Pl}}^2 / \langle S \rangle^3$) and the scale factor $a(t) \propto t^2$.
- Contradict the standard cosmology.

Zeldovich, Kobzarev, Okun, Zh. Eksp. Teor. Fiz. **67**, 3-11 (1974)

Gauge $U(1)_{B-L}$ Model of pGDM

- A $U(1)_{B-L}$ gauge symmetry and two complex scalars S and Φ carrying one and two units of $B - L$ charges respectively.
- Trilinear interaction Lagrangian: $\beta(\Phi^\dagger S^2 + \text{h.c.})$.
- The spontaneous breaking of $U(1)_{B-L}$ gauge symmetry by the Φ VEV leaves a remnant gauge \mathbb{Z}_2 symmetry and generates the soft breaking term from the trilinear term.

Abe, Toma, Tsumura JHEP **05** (2020) 057

Okada, Raut, Shafi, PRD **103** (2021) 055024

$SO(10)$ model of pGDM

- A unified approach is based on $SO(10)$ with $S \in 16_H$ and $\Phi \in \overline{126}_H$.
- Trilinear term arising from the coupling $\overline{126}_H(16_H)^2 + \text{h.c.}$ in the scalar potential.
- The dark matter candidate is the pseudo-Goldstone mode coming from a linear combination of the CP-odd components of the SM singlets.

Abe, Toma, Tsumura, Yamatsu, PRD **104** (2021) 035011

Okada, Raut, Shafi, Thapa, PRD **104** (2021) 095002

Phenomenological Implications of $SO(10)$ pGDM

- The dark matter can decay via gauge interactions.
- The VEV along the SM singlet direction in 126_H should be above 10^{11} GeV in order to satisfy the lifetime bound, $\tau_{\text{DM}} \gtrsim 10^{27}$ sec, for decaying dark matter.
- $\langle 126_H \rangle \gtrsim 10^{11}$ GeV coincides with the requirement from the fitting of neutrino oscillation data in the minimal $SO(10)$ GUT.
- A VEV $\sim 10^2$ GeV of 16_H gives a viable pNGB thermal dark matter.

Baring, Ghosh, Queiroz, Sinha, PRD **93** (2016) 103009

Abe, Toma, Tsumura, Yamatsu, PRD **104** (2021) 035011

Okada, Raut, Shafi, Thapa, PRD **104** (2021) 095002

3 *Formation of Domain Walls Bounded by Strings*

Formation of Domain Walls Bounded by Strings

$$\underbrace{SO(10) \rightarrow \dots \rightarrow \mathcal{G}_I}_{\text{rank}=5} \xrightarrow[M_R(\nu_L^C)]{\langle \Phi \in \overline{126} \rangle \gtrsim 10^{11} \text{ GeV}} \underbrace{SM \times \mathbb{Z}_2}_{\text{rank}=4} \xrightarrow[\simeq 10^2 - 10^5 \text{ GeV}]{\langle S \in 16 \rangle} SM$$

- $\langle 126_H \rangle \gtrsim 10^{11} \text{ GeV}$ leaves an unbroken \mathbb{Z}_2 and therefore generates topologically stable cosmic strings.

Kibble, Lazarides, Shafi, Phys. Lett. B **113** (1982)

- The VEV $\langle 16_H \rangle \simeq [10^2, 10^5] \text{ GeV}$, breaks this \mathbb{Z}_2 symmetry, which leads to the formation of domain walls bounded by strings.

RM, Park, Shafi, Phys.Lett.B **845** (2023) 138127

Kibble, Lazarides, Shafi, Phys. Rev. D **26** (1982), 435

- String has a tension $\mu \sim \langle 126_H \rangle^2$ and wall has a tension $\sigma \sim \langle 16_H \rangle^3$.

④ *Gravitational Wave Background from WBS*

Timescale for String Network

- Strings formed at time t_F form a network and domain walls are formed at a later time t_{dw} with the strings as their boundary.
- For a wall bounded by a string of radius of curvature R , the force per unit length on the string boundary $\sim \mu/R$ dominates over the wall tension σ for $R < \boxed{R_c = \mu/\sigma}$.
- String dynamics dominates till R_c if $R_c > t_{dw}$.
- For $t_{dw} > R_c$, the domain wall dynamics starts dominating right after their formation.

Timescale for String Network

- $t_* = \max[R_c, t_{\text{dw}}]$ to be the maximum timescale for domination by the string dynamics.
- The cosmic strings inter-commute, form loops before t_* with $R < t_*$ and can produce gravitational waves.

$$f = \frac{2n}{l(t)} \frac{a(t)}{a_0}$$

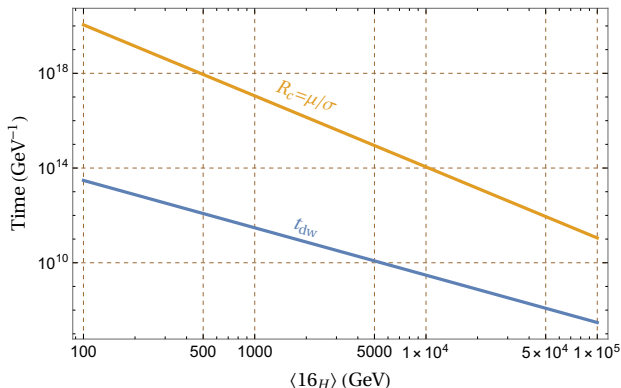
- The domain wall dynamics become dominant for $t > t_*$, and the string-wall networks collapse as the walls pull the strings.

Vilenkin, Everett, PRL **48** (1982) 1867

Martin, Vilenkin, PRL **77** (1996) 2879

Dunsky et. al., PRD **106** (2022) 075030

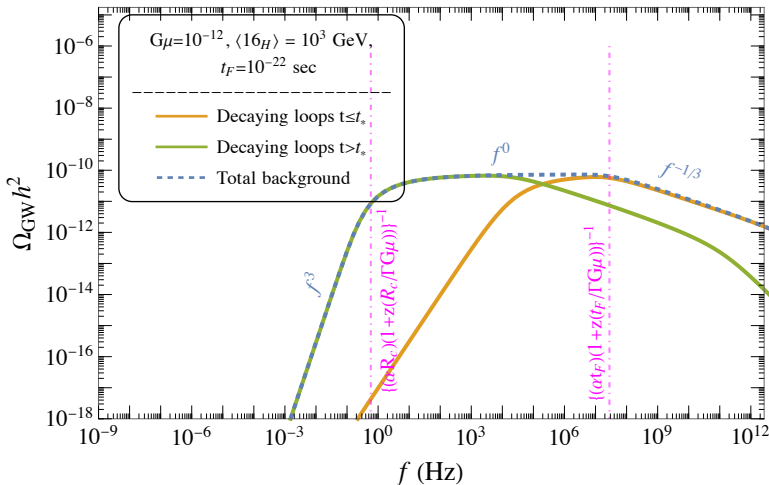
Timescale for String Network



- $R_c \gg t_{dw}$ for pGDM implies $t_* = R_c$, and the gravitational wave background is dominated by string loops.

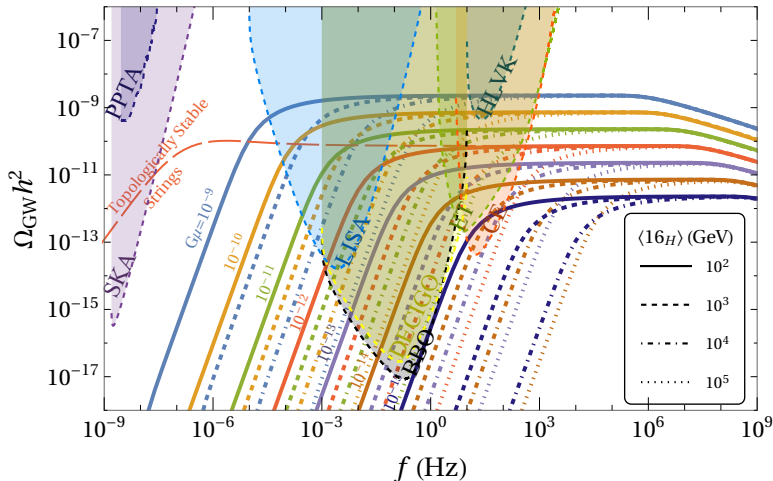
RM, Park, Shafi, Phys.Lett.B 845 (2023) 138127

Gravitational Waves from WBS



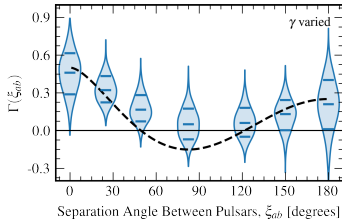
RM, Park, Shafi, Phys.Lett.B 845 (2023) 138127

GWs from WBS and Observational Prospects



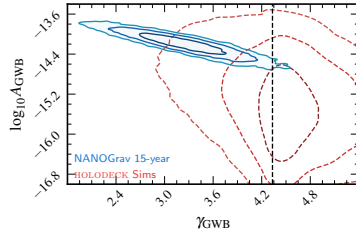
RM, Park, Shafi, Phys.Lett.B 845 (2023) 138127

Evidence of GWB in PTA

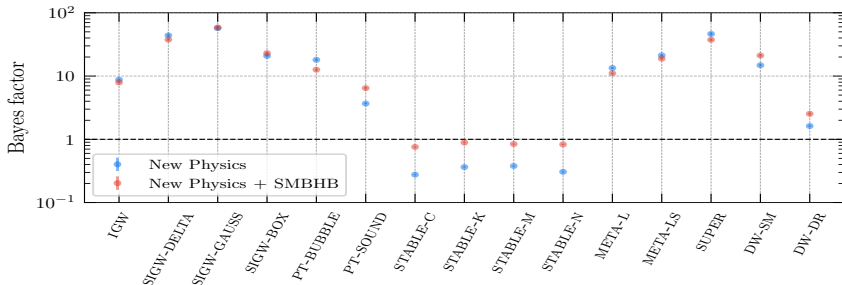


NG15:2306.16219,...

Mergers of SMBHBs?

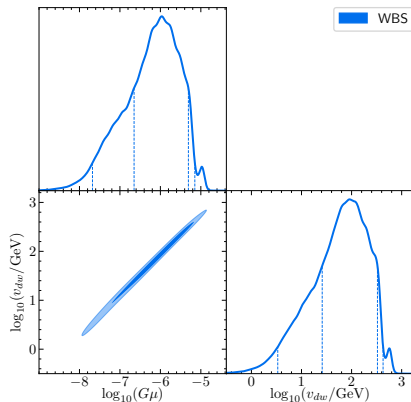
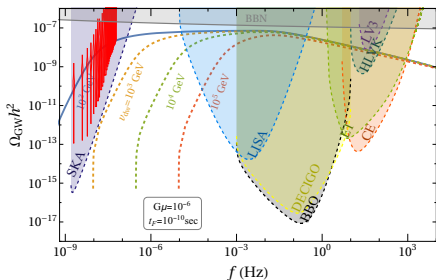


Cosmological Origin? New Physics?



WBS and NANOGrav data

Parameters	Bayesian Credible Intervals	
	68%	95%
$\log_{10}(G\mu)$	$[-6.65, -5.31]$	$[-7.68, -5.15]$
$\log_{10}(v_{dw}/\text{GeV})$	$[1.41, 2.52]$	$[0.53, 2.63]$



Lazarides, **RM**, Shafi, *Phys. Rev. D* **108** (2023) 095041

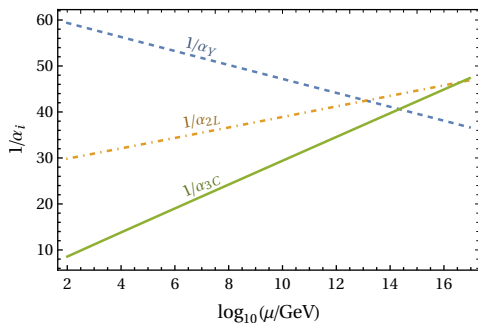
5 *Summary*

- PGDM models based on realistic grand unified gauge symmetries such as $SO(10)$ predict the existence of composite topological structures known as ‘walls bounded by strings’.
- Gravitational wave spectrum produced by this string-wall system will be accessible in the foreseeable future at a number of proposed experiments.
- We note that the PTA data has a strong evidence of GWs background from the string-wall composite structures with $G\mu \sim 10^{-6}$ and $v_{dw} \sim 10^2$ GeV.

Thank You

Back up slides

Motivation towards the Grand Unification



- Renormalization Group Evolution of Standard Model gauge couplings gives the hint of the possibility of the Grand Unified Theories.

- Imposition of higher symmetry may constraint some free parameters.
- All fermions including $(\nu^c)_L$ can be put in one representation in GUT.
- One way to understand the charge quantization.

A Minimal Yukawa Sector in $SO(10)$

- The Lagrangian for the Yukawa interactions:

$$y_{10}\psi_{16}^T \mathcal{C}\phi_{10}\psi_{16} + y_{126}\psi_{16}^T \mathcal{C}\phi_{126}^\dagger\psi_{16} + \text{H.c.},$$

- SM Higgs doublet (H) is a linear combination of bi-doublets from complex 10_H and $\overline{126}_H$.

Lazarides, Shafi, Wetterich, NPB **181** (1981) 287

Babu, Mohapatra, PRL **70** (1993) 2845

- A VEV (v_R) along the SM singlet direction of $\overline{126}_H$ breaks a diagonal generator orthogonal to the hypercharge (Y).

$$\underbrace{SO(10) \rightarrow \dots \rightarrow \mathcal{G}_I}_{\text{rank}=5} \xrightarrow{\langle \overline{126}_H \rangle} \underbrace{SM \times \mathbb{Z}_2}_{\text{rank}=4}.$$

- Example: $SU(2)_L \times SU(2)_R \times U(1)_{B-L} \rightarrow SU(2)_L \times U(1)_Y$, where $T_{3R} - \frac{B-L}{2}$ is broken.

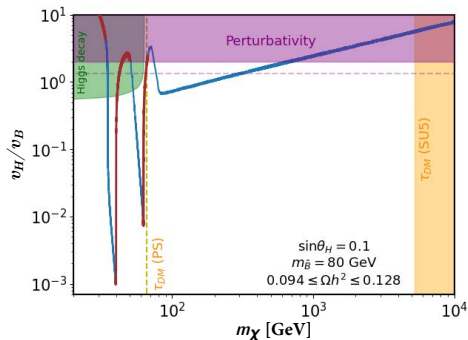
Right-handed Neutrino Mass in Minimal $SO(10)$

- The Majorana mass matrix of the RHNs: $M_R = y_{126} v_R$.
- Fit to the quark and lepton mass and mixing parameters requires $v_R \gtrsim 10^{11} \text{ GeV}$.
- For example, predicted physical masses of the RHNs from two recent fittings:
 - $\{4.36 \times 10^9, 1.97 \times 10^{11}, 8.66 \times 10^{11}\} \text{ GeV}$ [Mummidi, Patel, JHEP 12 \(2021\)](#)
 - $\{1.87 \times 10^{10}, 4.46 \times 10^{11}, 2.36 \times 10^{12}\} \text{ GeV}$ [Ohlsson, Pernow, JHEP 06 \(2019\)](#)
- Compatible with gauge coupling unification.

[Chakraborty, RM, King, Phys. Rev. D 99 \(2019\) 095008](#)

[Lazarides, RM, Roshan, Shafi, JCAP 12 \(2022\), 009](#)

Phenomenological Implications of $SO(10)$ pGDM



- The VEV of 16_H is $\sim 10^2$ GeV for a viable pNGB thermal dark matter.
- It could be $\sim 10^5$ GeV or so near the resonance.
- Namely, $\langle 16_H \rangle / v_H \simeq [1, 10^3]$, with v_H being the VEV of the SM Higgs.

Okada, Raut, Shafi, Thapa, PRD **104** (2021) 095002

$$\underbrace{SO(10) \rightarrow \dots \rightarrow \mathcal{G}_I}_{\text{rank}=5} \xrightarrow[M_R(\nu_L^C)]{\langle \Phi \in \overline{126} \rangle \gtrsim 10^{11} \text{ GeV}} \underbrace{SM \times \mathbb{Z}_2 \xrightarrow[\simeq 10^2 - 10^5 \text{ GeV}]{\langle S \in 16 \rangle}}_{\text{rank}=4} SM$$

Predictions of GUTs: Topological Defects

- Topological defects may appear during the SSB of a group \mathcal{G} down to its subgroup \mathcal{H} .
- Non-trivial homotopy group $\Pi_k(\mathcal{M})$ of the vacuum manifold ($\mathcal{M} = \mathcal{G}/\mathcal{H}$) implies formation of topological defects.
- Various types of topological defects which can be formed are : domain walls ($k = 0$), cosmic strings ($k = 1$), monopoles ($k = 2$) etc

$$n_{rm}(l, t > t_{eq} > t_M) = \frac{0.18 t_{eq}^{1/2} \Theta(0.1 t_M - l - \Gamma G \mu (t - t_M))}{t^2 (l + \Gamma G \mu t)^{5/2}} \quad (1)$$