

EPIC 2024

Calaserena Resort, Sardinia, Italy

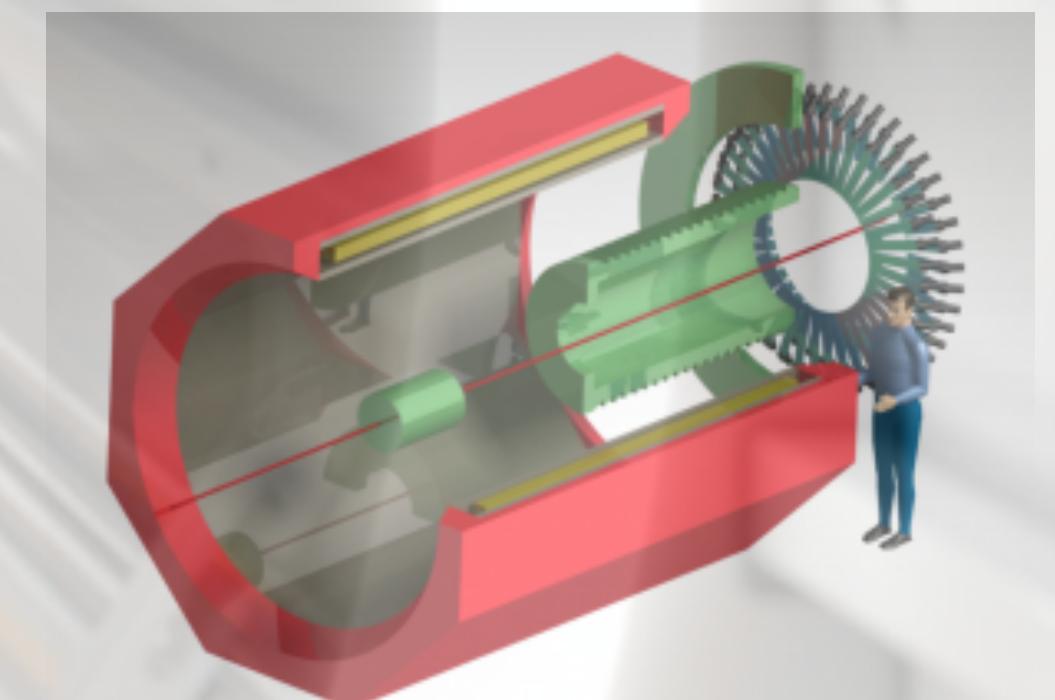
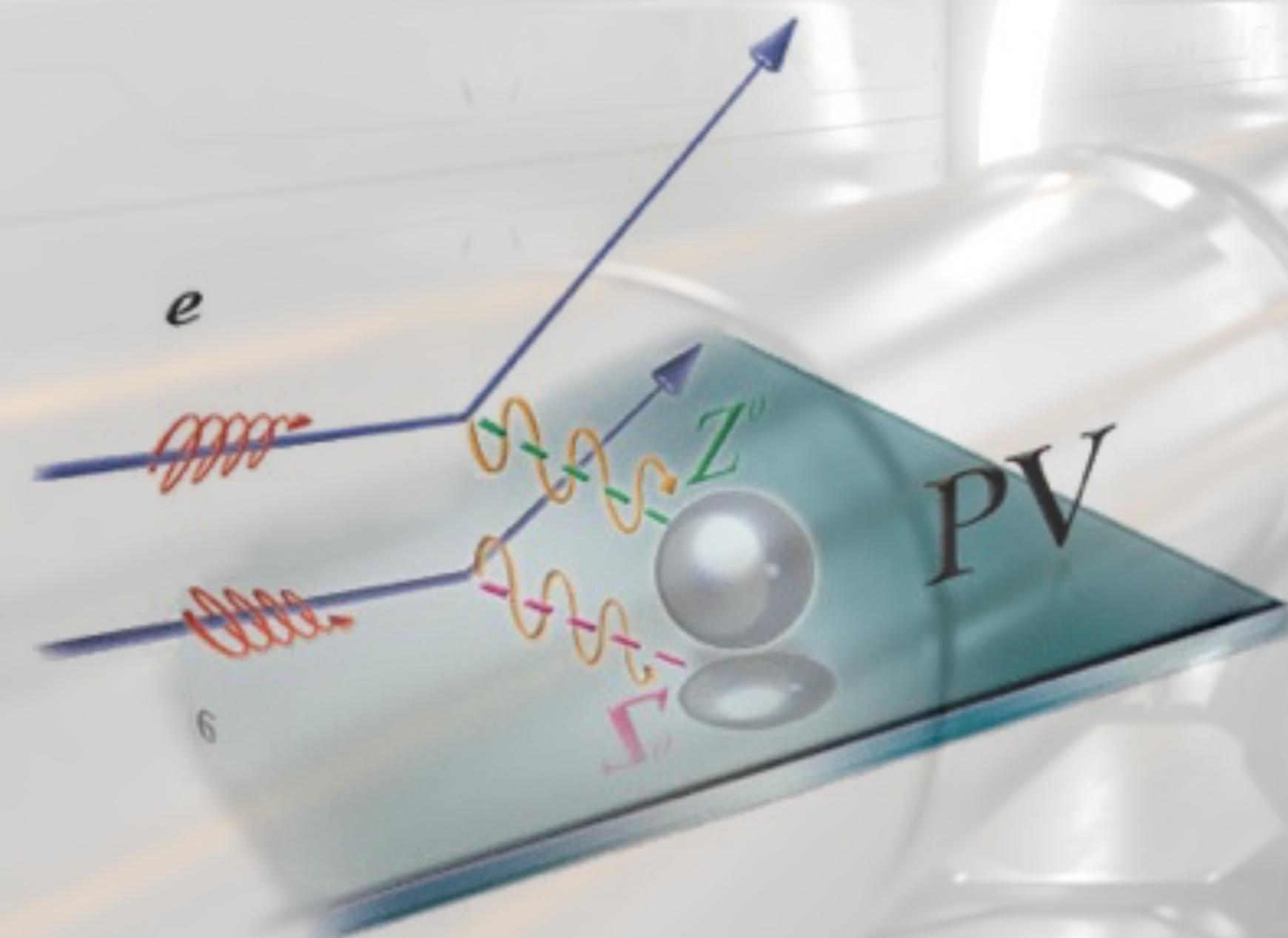
September 23, 2024

Electroweak fit

Jens Erler



JOHANNES GUTENBERG
UNIVERSITÄT MAINZ

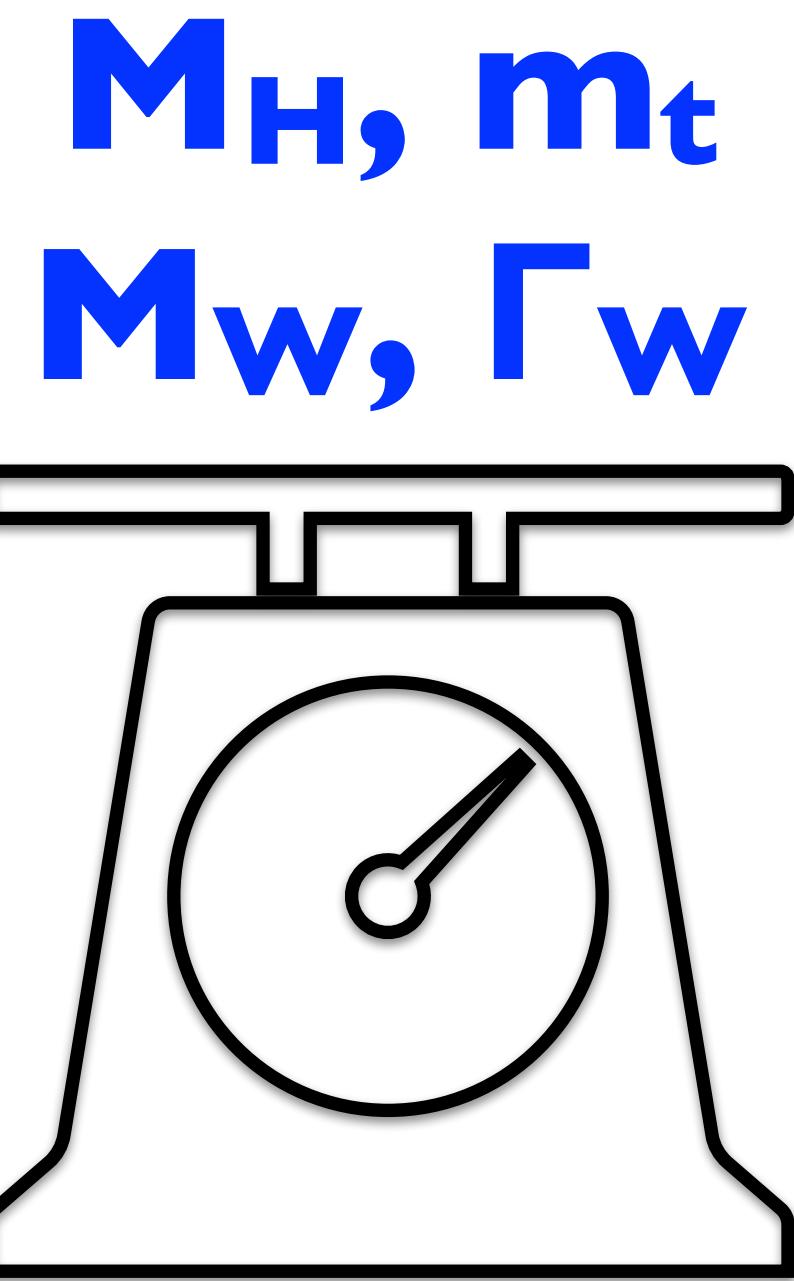
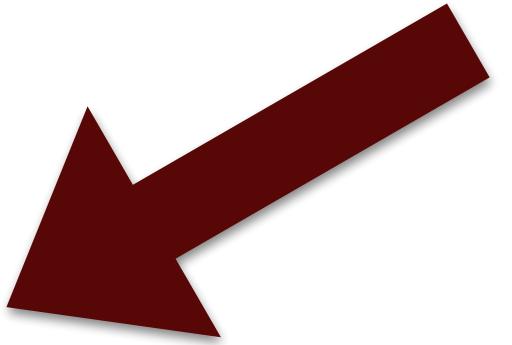
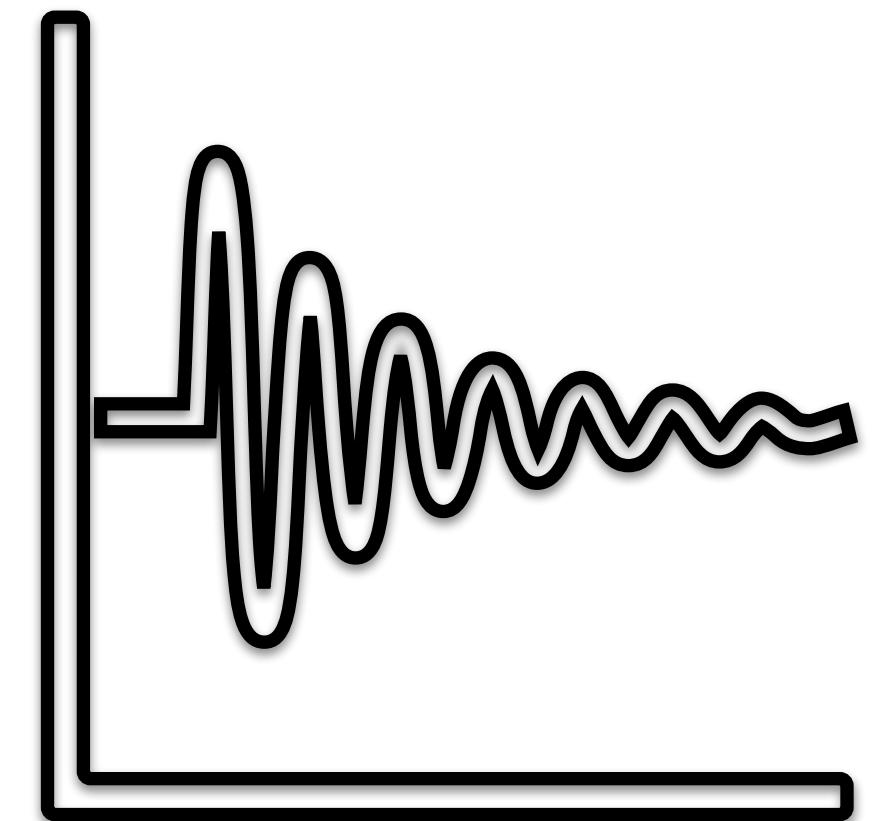
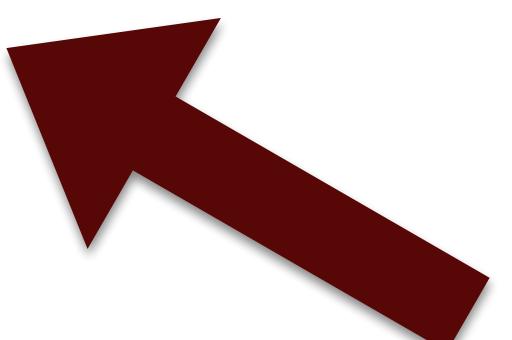
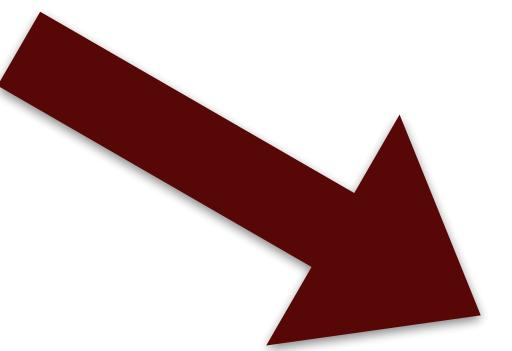
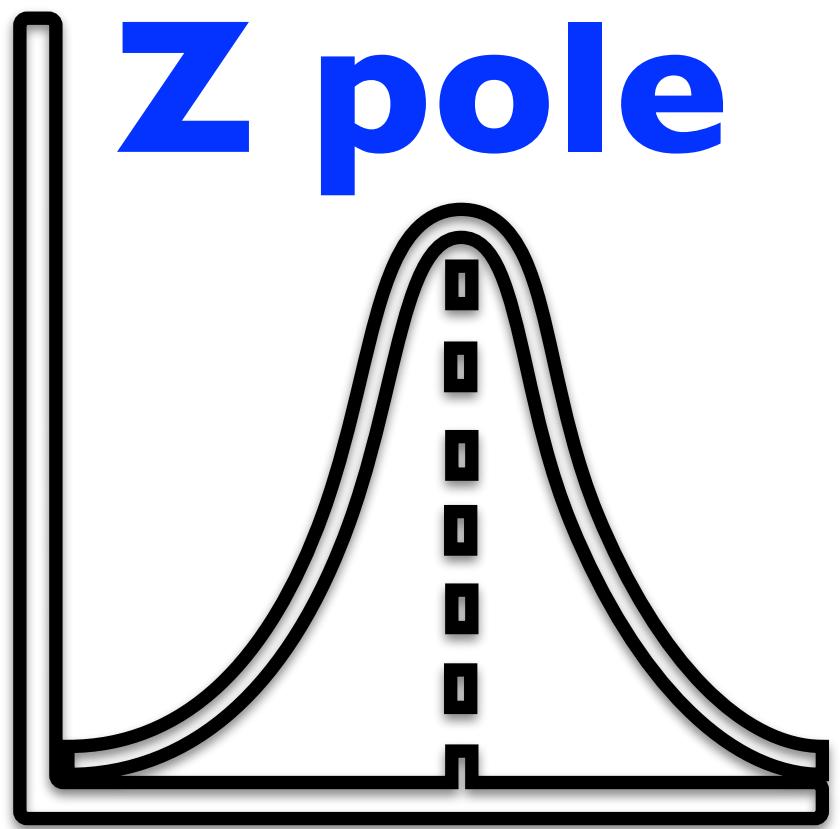
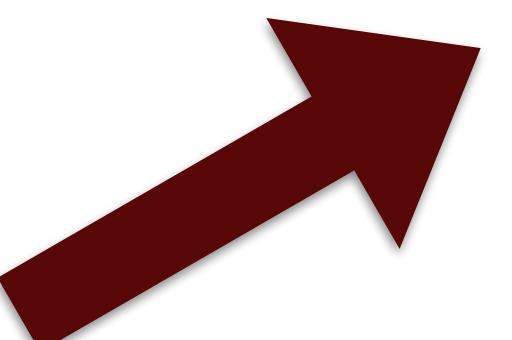
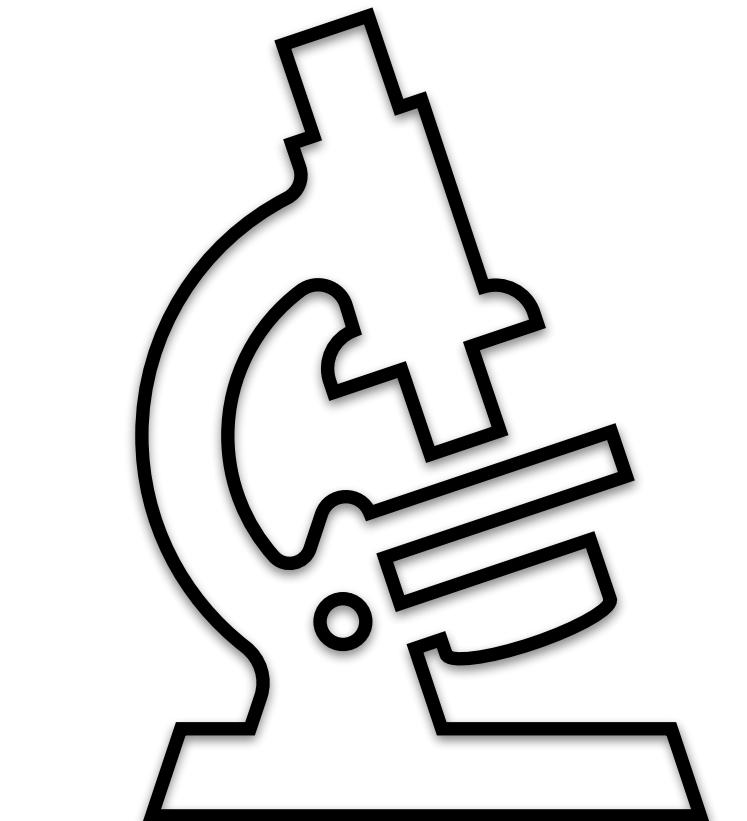


Overview

- * Introduction
 - * the over-constrained Standard Model
 - * the weak mixing angle
- * Latest developments
 - * M_Z (CDF)
 - * M_W (ATLAS and CDF)
 - * Γ_W (update)
- * Hadronic vacuum polarization
 - * $\alpha(M_Z)$
 - * $\sin^2\theta_W(0)$
 - * $g-2$
- * α_S and N_V from the Z pole

The over-constrained SM

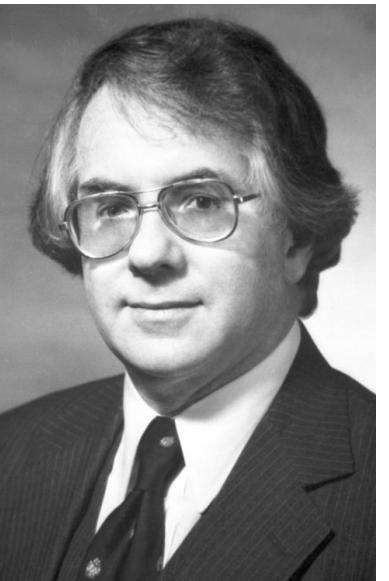
**low-energy
precision**



M_H, m_t
 M_w, Γ_w

$m_c, m_b, \Delta a \dots$

The $E = mc^2$ of the SM

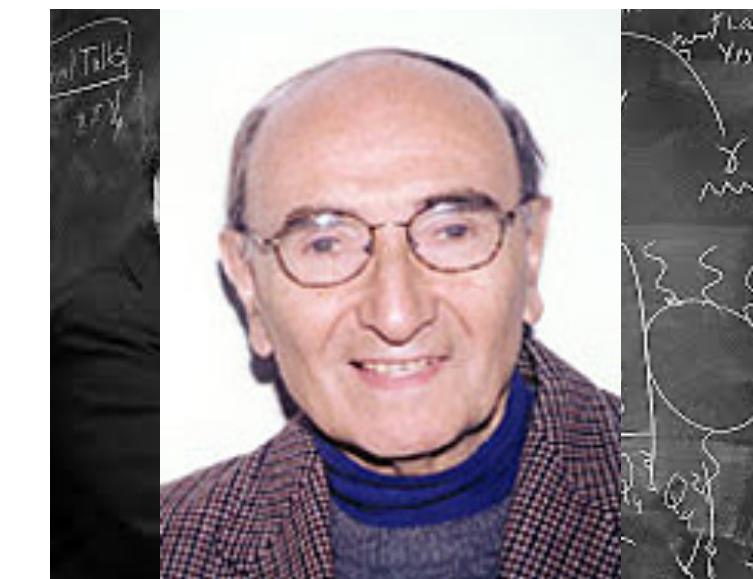
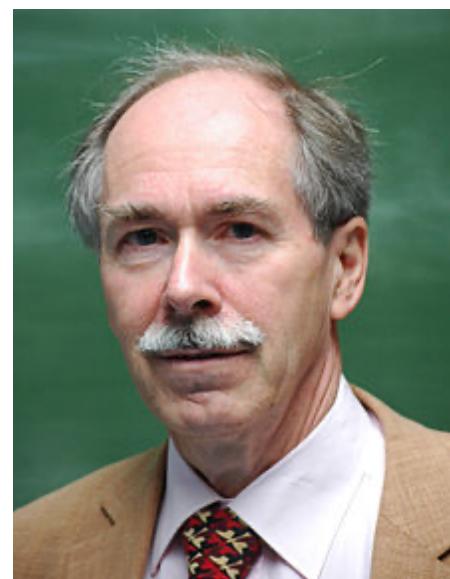


$$\sin^2 \theta_W = \frac{g'^2}{g^2 + g'^2} = 1 - \frac{M_W^2}{M_Z^2} = \frac{\pi \alpha}{\sqrt{2} G_F M_W^2}$$

Radiative corrections

$$\frac{\sin^2 \theta_{\text{eff}}^e}{1 + \Delta \hat{k}} = \frac{\hat{g}'^2}{\hat{g}^2 + \hat{g}'^2} = 1 - \frac{(1 - \Delta \hat{\rho}) M_W^2}{M_Z^2} = \frac{\alpha \frac{\alpha m_t^2}{M_W^2}}{(1 - \Delta \hat{r}) \sqrt{2} G_F M_W^2} + \dots$$

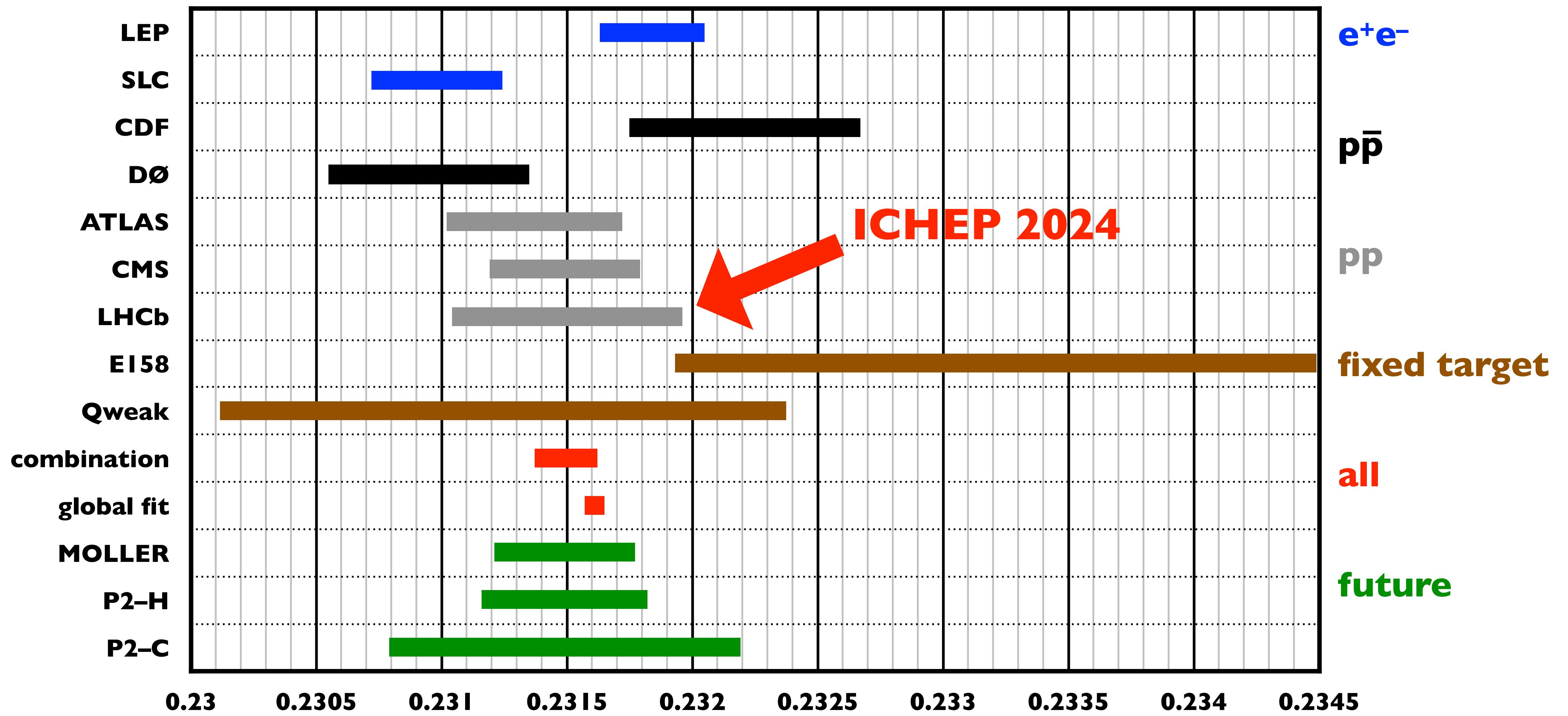
$\uparrow \pi \alpha$
 $\uparrow \alpha \frac{\alpha m_t^2}{M_W^2}$



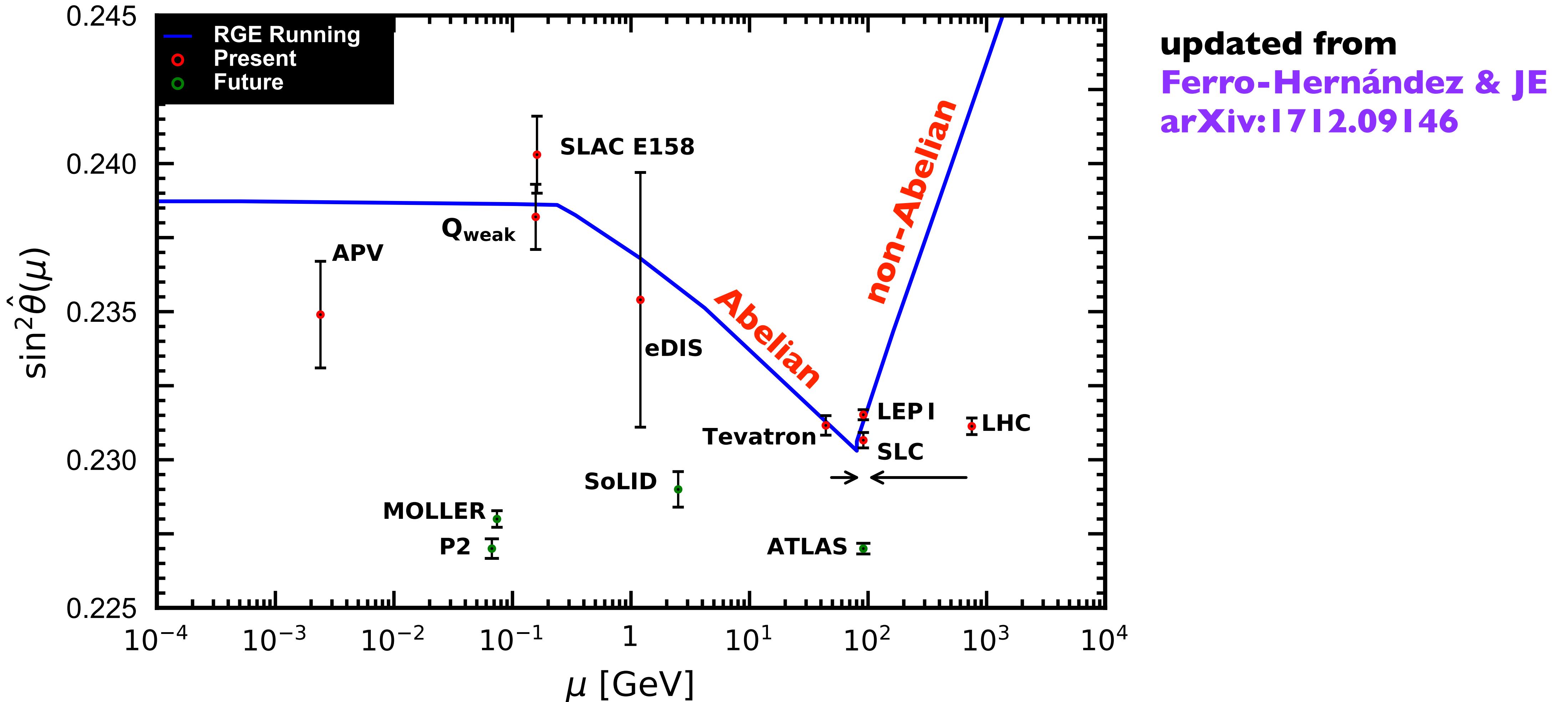
High-precision era

- 😊 Standard Model correct to lowest order and at the level of quantum corrections
- ➡ Global analysis of precision observables at ultra-high precision
- * General remark: the higher the precision, the more physics issues will enter in the interpretation of precision measurements
 - ➡ **Atomic physics** (e.g., transition matrix elements), **nuclear physics** (e.g., neutron skin), hadron physics (e.g., form factors), **QCD** (e.g., PDFs), **QED** (e.g., initial-state radiation)
 - * Obstacle when looking at single observables
 - * A feature in global analyses:
Someones bottleneck may be somebody else's opportunity → **this Workshop**

$\sin^2\theta_{\text{eff}}$ anno 2024

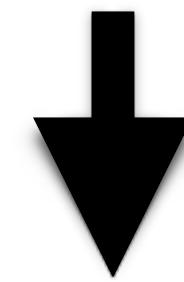


Running $\overline{\text{MS}}$ weak mixing angle

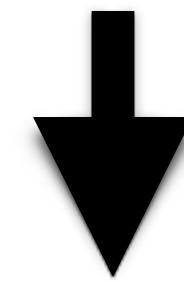


SMEFT@ D = 6

38 four-Fermi-operators



$3 L^4 + 13 L^2 Q^2 + 8 LQ^3 (\Delta B \neq 0) + 14 Q^4$ operators

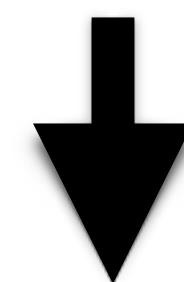


$3 L^4 = e_V e_V + e_A e_V$ (*MOLLER*) + $e_A e_A$

$$\psi_V = \bar{\psi} \gamma^\mu \psi$$

$$\psi_A = \bar{\psi} \gamma^\mu \gamma^5 \psi$$

$13 L^2 Q^2 = 7$ vector and axial-vector combinations + 4 scalar + 2 tensor

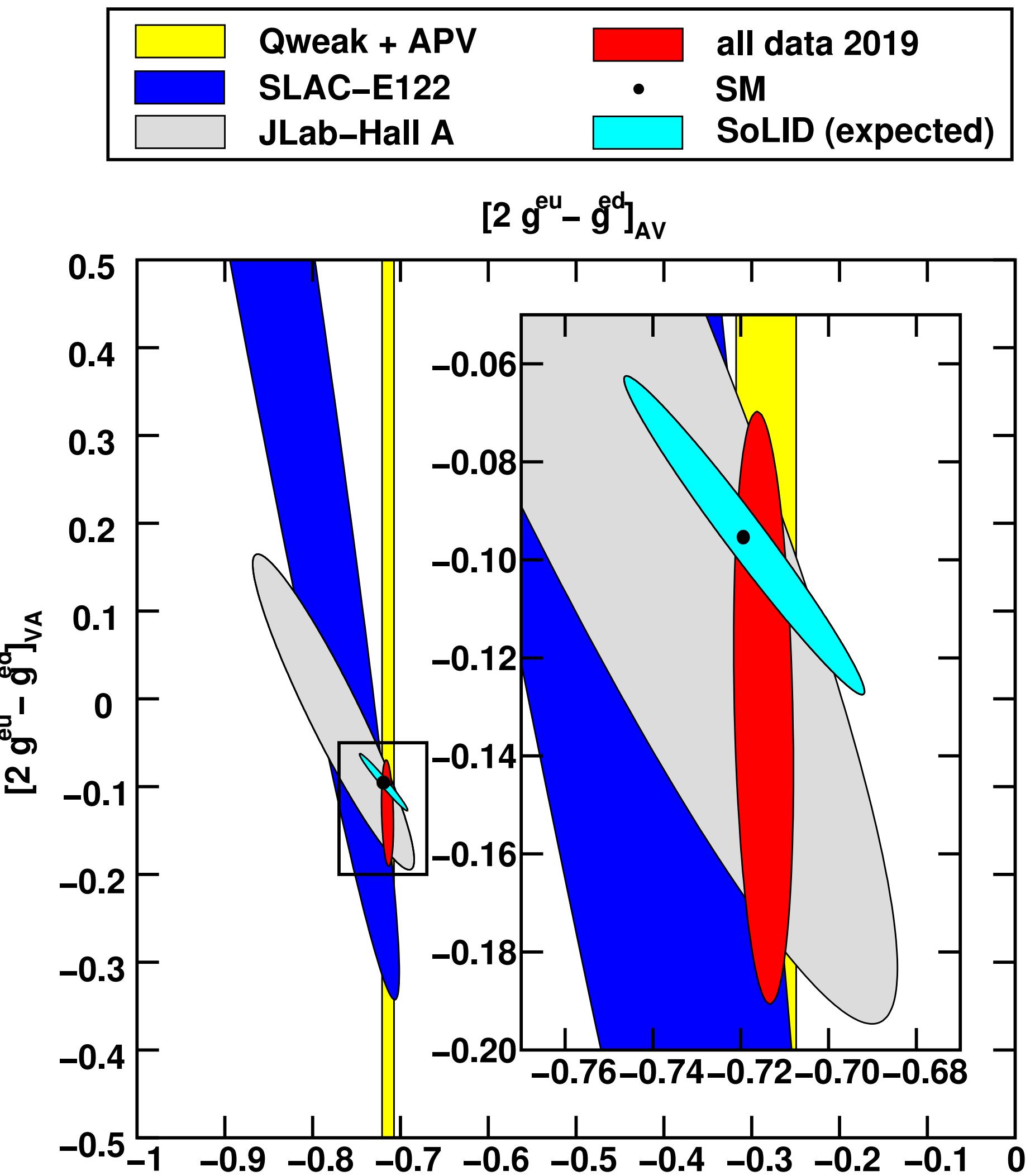
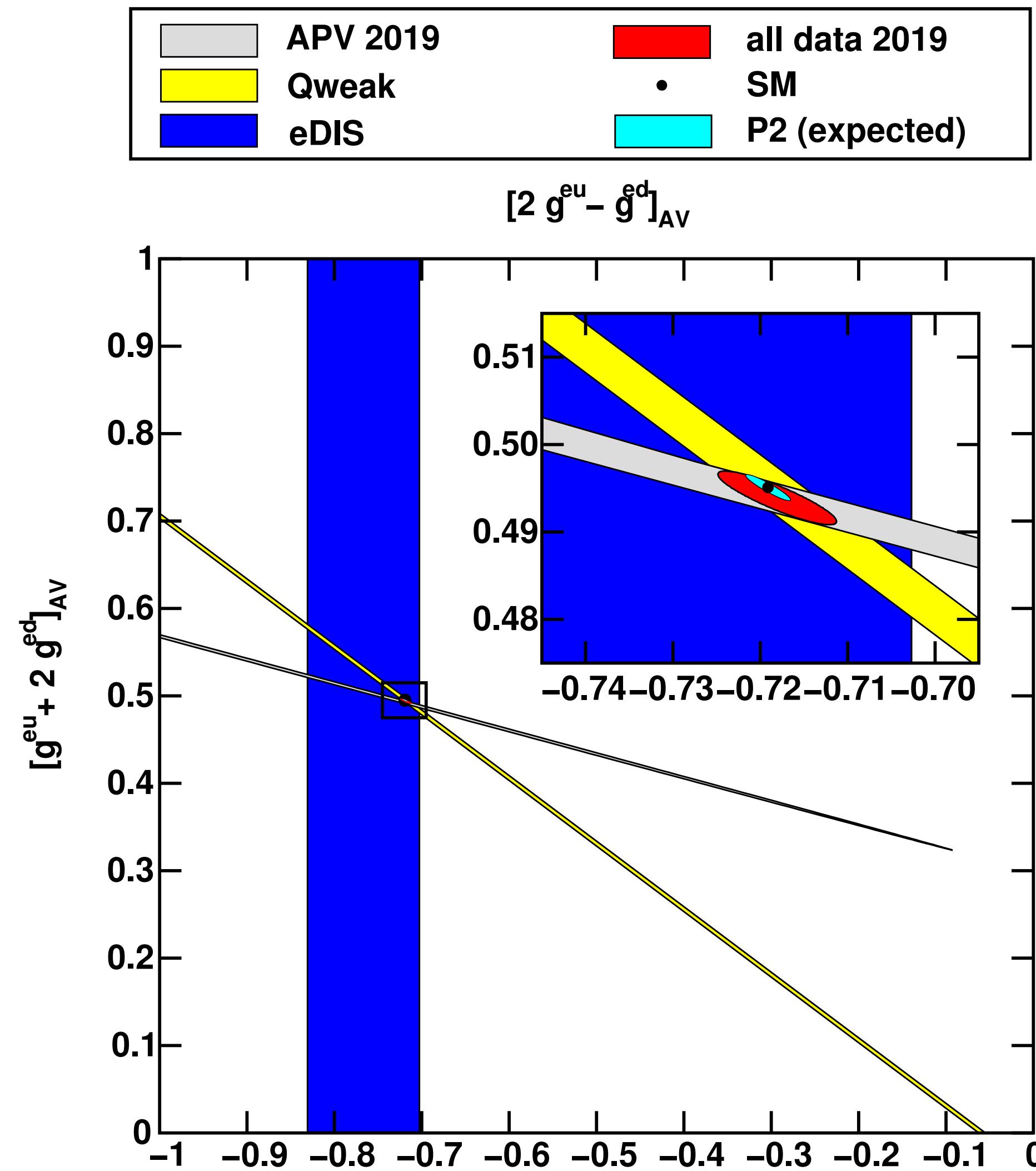


$2 e_V q_V (C_0) + 2 e_A q_V (C_1)$ (*APV, Qweak, P2*) + $2 e_V q_A (C_2)$ (*SLAC-EI22, PVDIS, SoLID*)

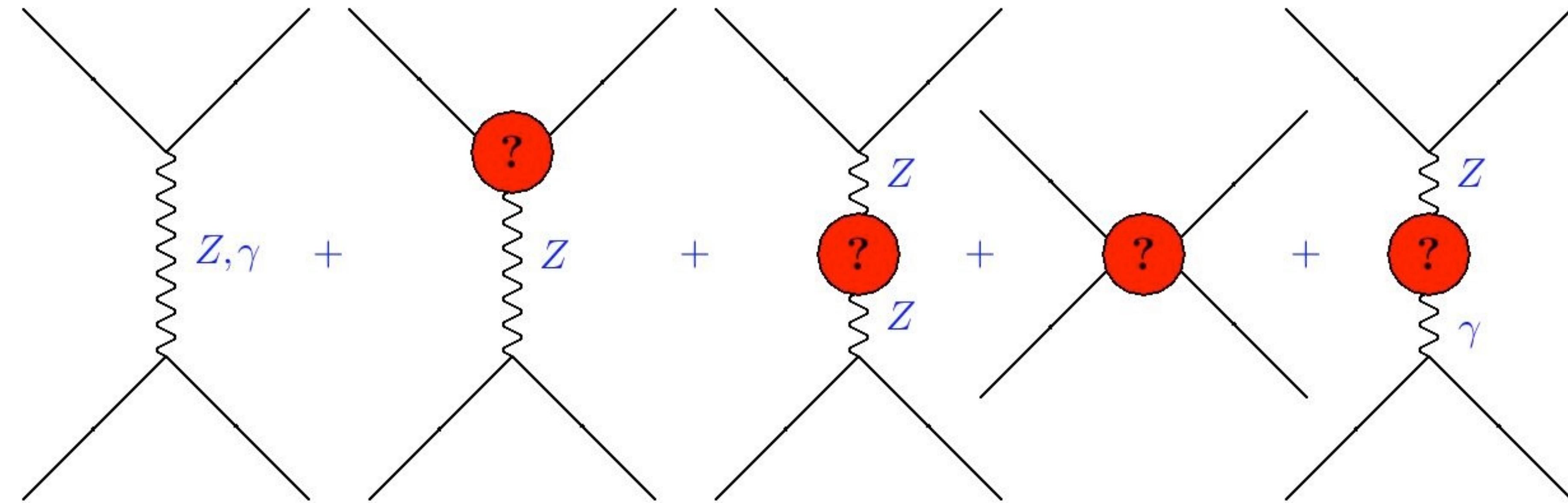
+ $2 e_A q_A (C_3)$ (*e+@SoLID*)

- 1 constraint: $(\bar{u}_L \gamma^\mu u_L - \bar{d}_L \gamma^\mu d_L) \bar{e}_R \gamma_\mu e_R = 0$

Parity-violating 4-fermion electron-quark couplings



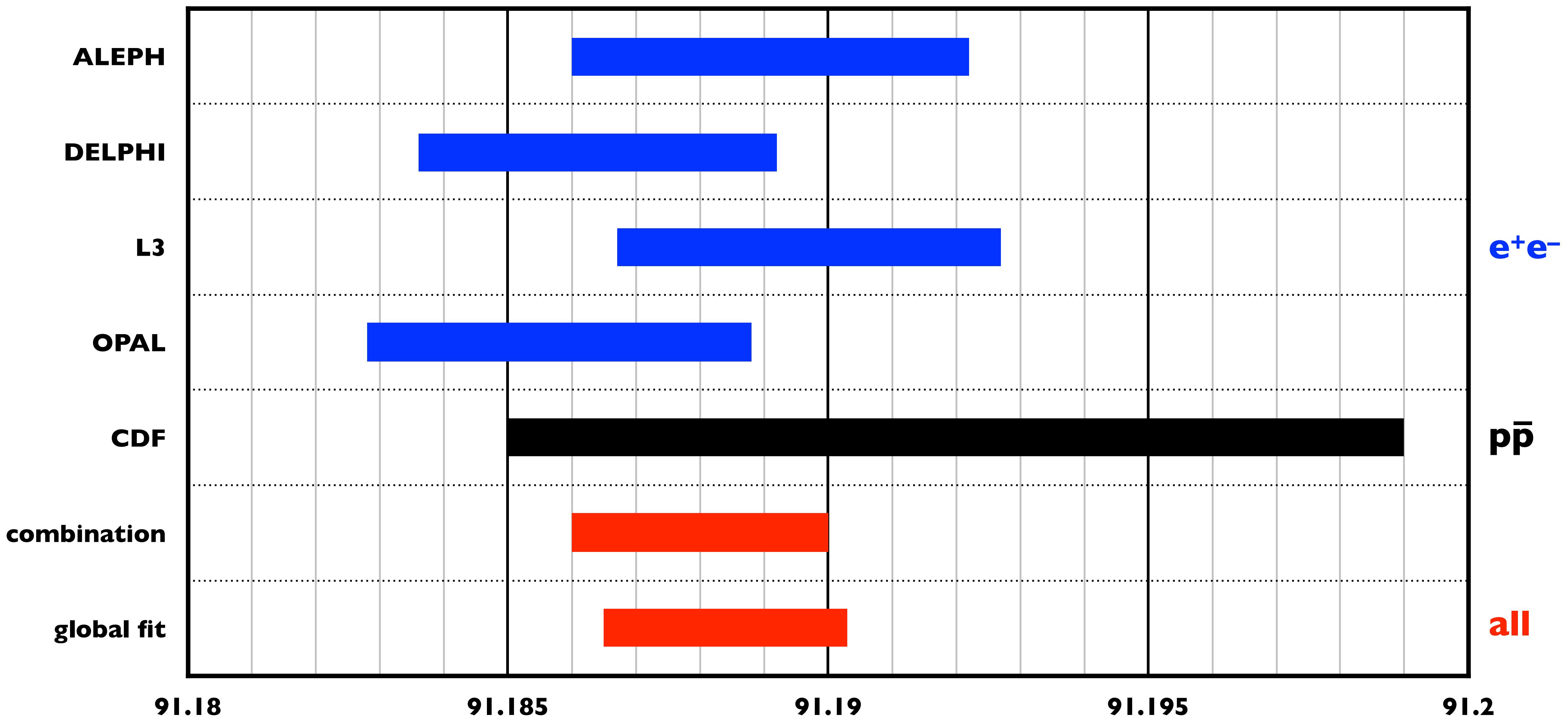
Discriminating new physics



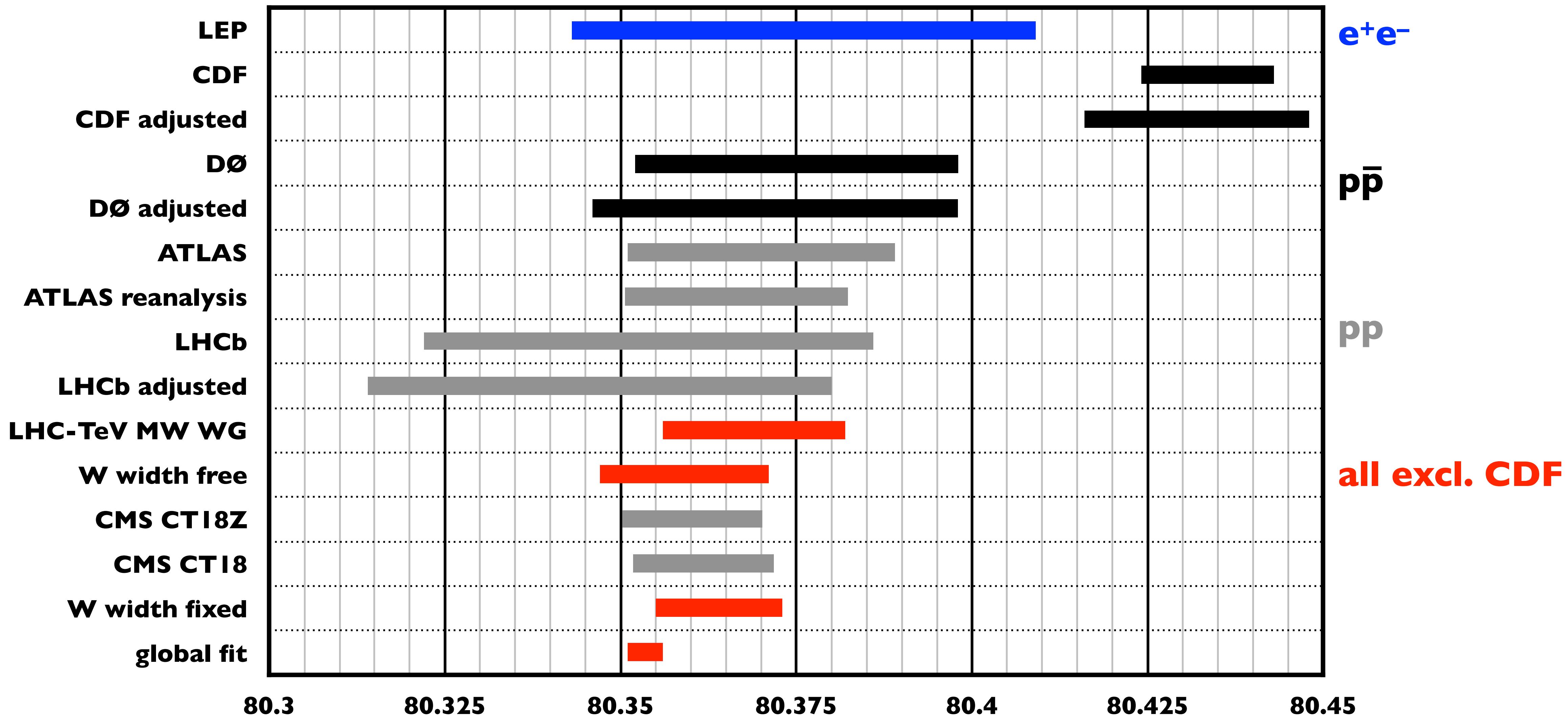
- * **Z-Z' mixing:** modification of Z vector coupling
- * **oblique parameters:** STU (also need M_W and Γ_Z)
- * **new amplitudes:** off- versus on-Z pole measurements (e.g. heavy Z')
- * **dark Z:** renormalization group evolution (low versus very low energy measurements)

Latest developments

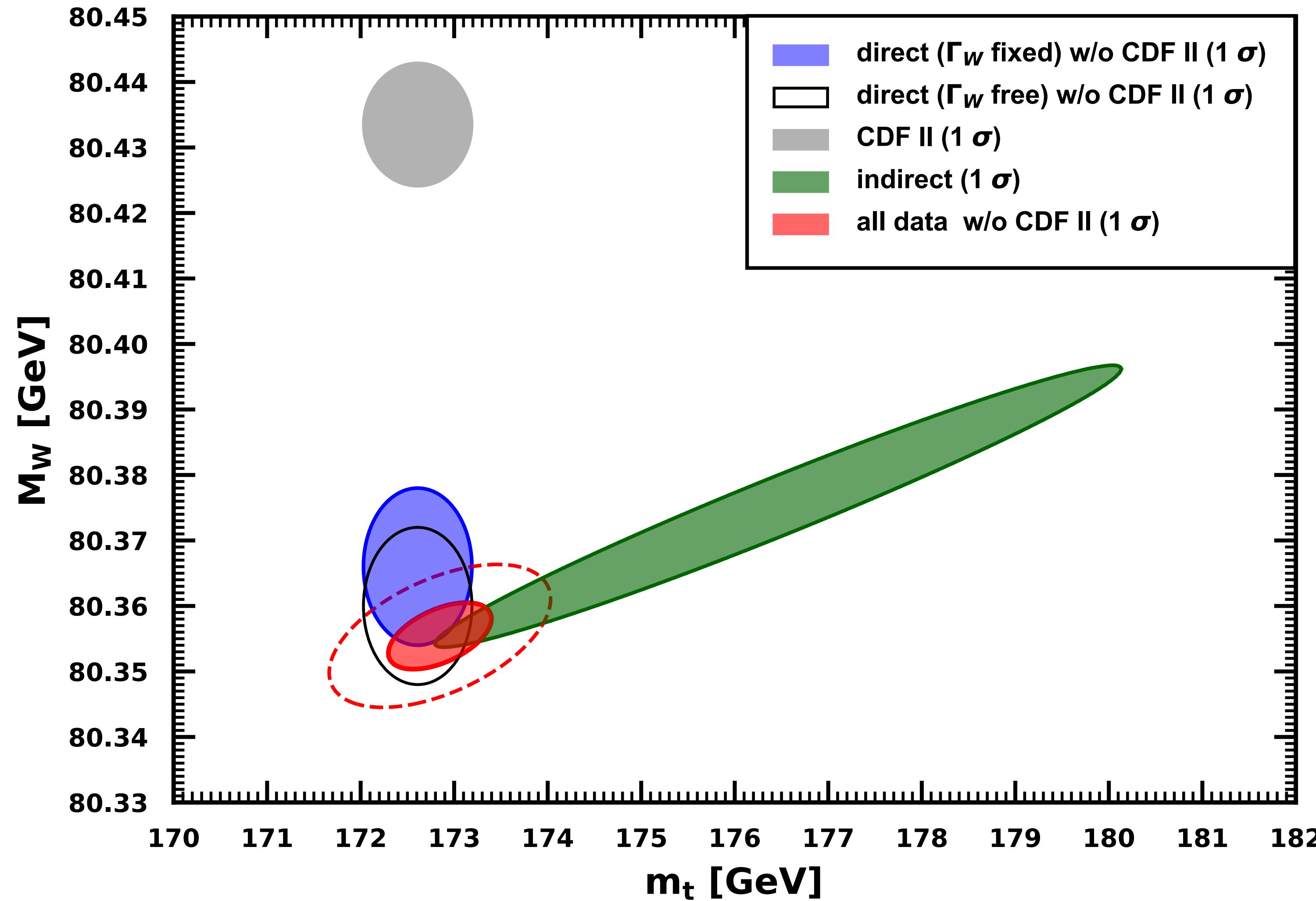
M_Z anno 2024 [GeV]



M_w anno 2024 [GeV]



$M_W - m_t$



$m_t = 174.8 \pm 1.4 \text{ GeV}$
(indirect)

1.5 σ above

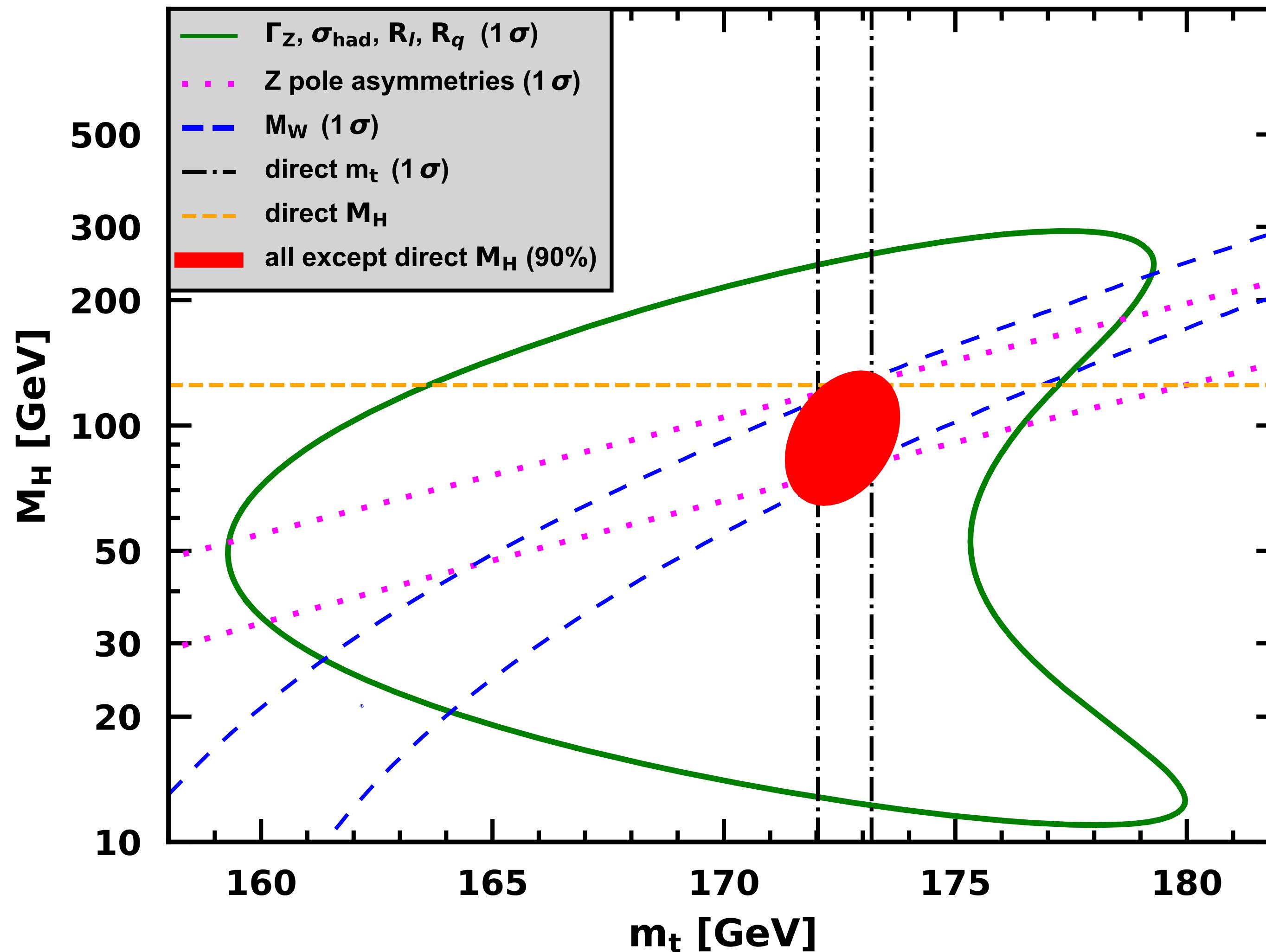
$m_t = 172.61 \pm 0.58 \text{ GeV}$
(Tevatron + LHC)

$M_W = 80353 \pm 6 \text{ GeV}$
(indirect)

$M_W = 80364 \pm 9 \text{ MeV}$
(direct)

Freitas & JE, PDG (2024)
figure: Rodolfo Ferro

$M_H - m_t$ EPIC update



$\chi^2/\text{d.o.f.} = 45.5/48$
 $(\text{p-value} = 57\%)$

$M_H = 97 (99)^{+15}_{-14} \text{ GeV}$

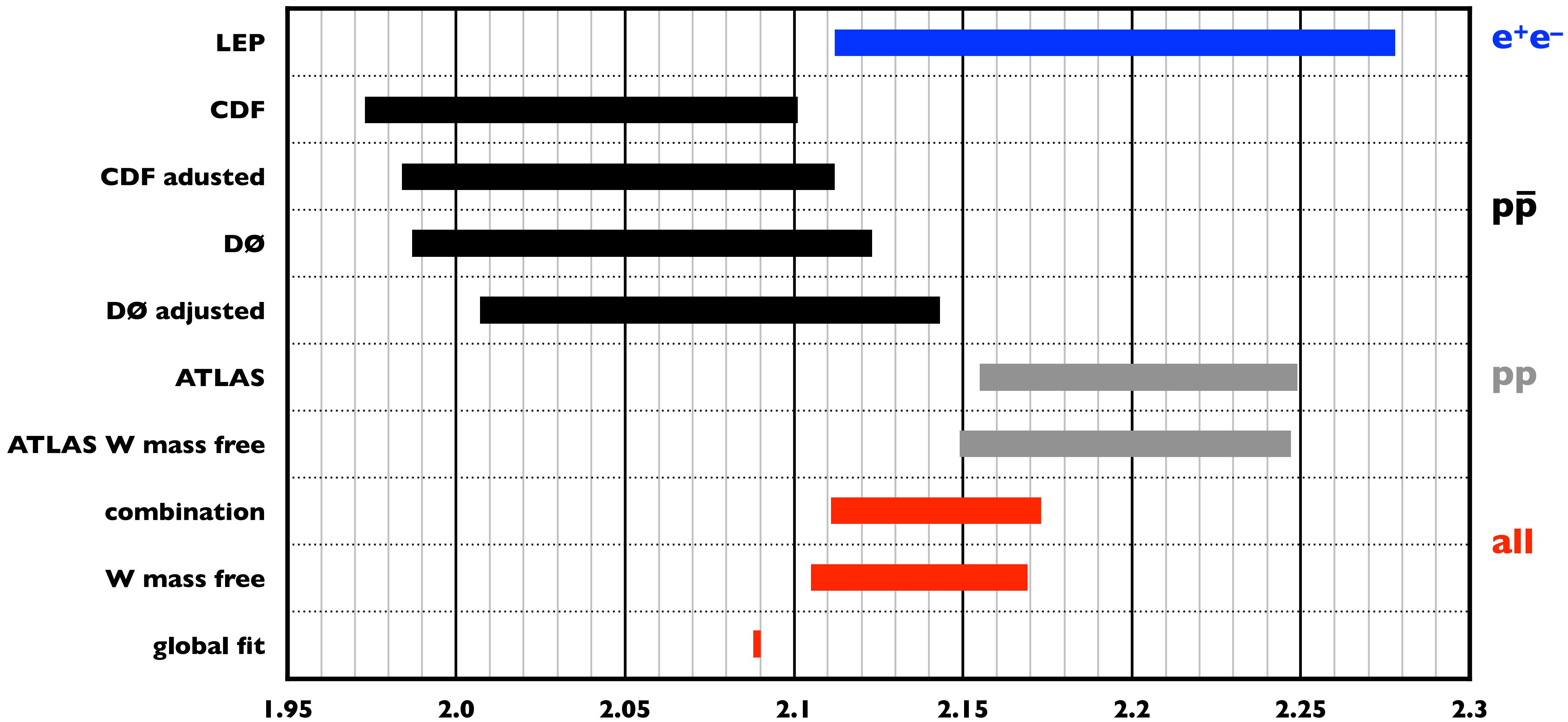
indirect (including Γ_H)

1.7σ below

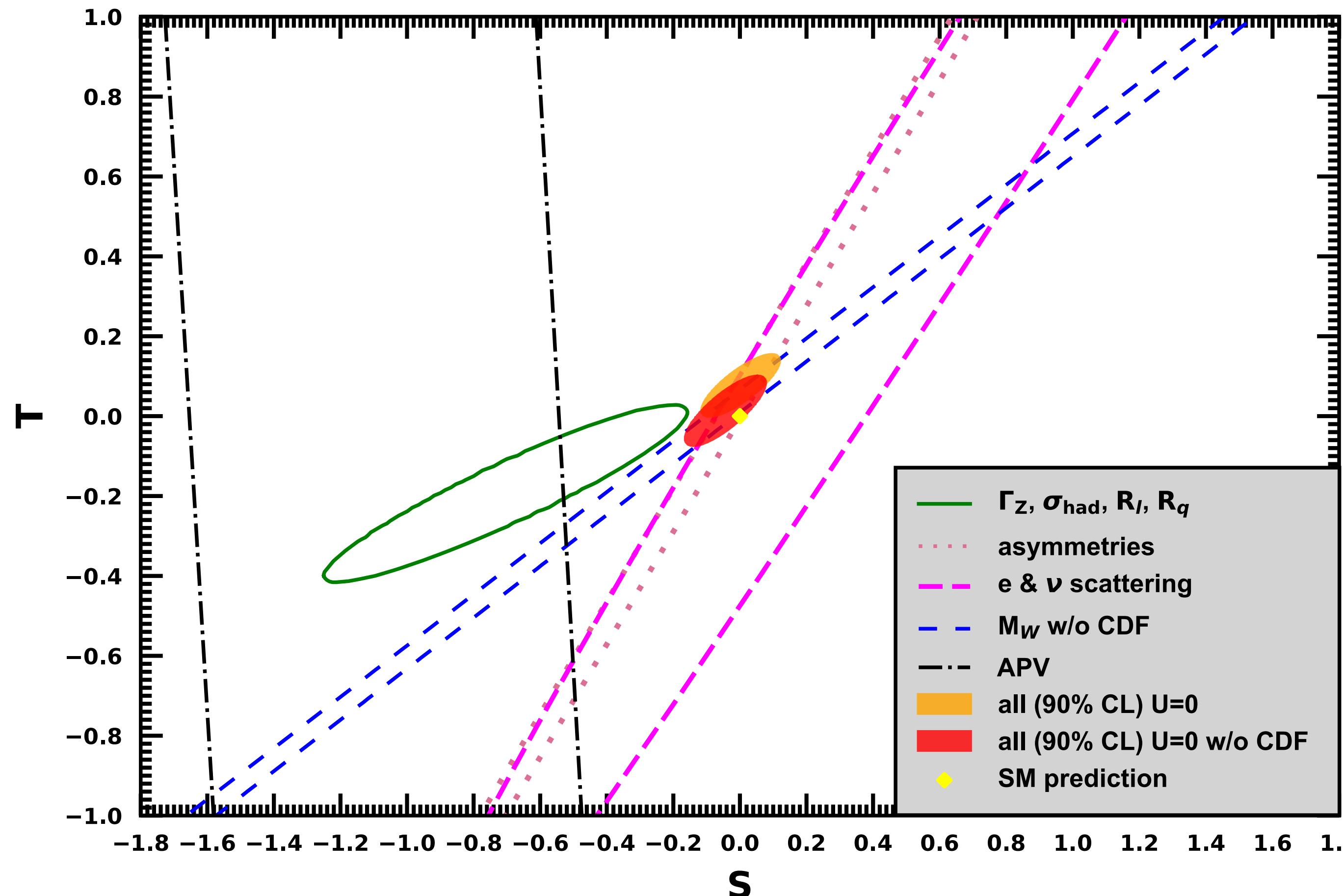
$M_H = 125.10 \pm 0.09 \text{ GeV}$
(LHC)

Freitas & JE, PDG (2024)
figure: Rodolfo Ferro

Γ_W anno 2024 [GeV]



S – T EPIC update



Freitas & JE, PDG (2024)
figure: Rodolfo Ferro

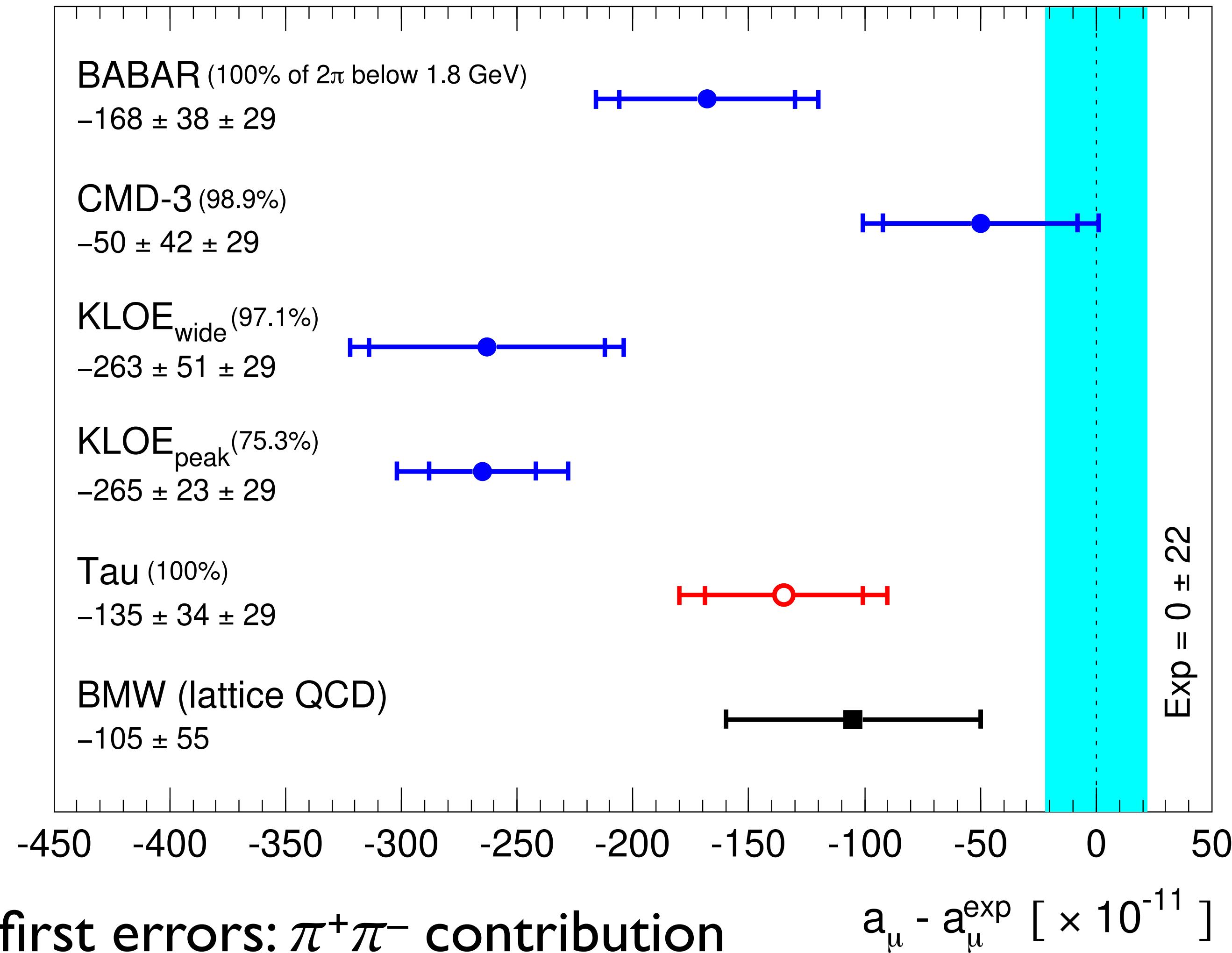
S	-0.06 ± 0.07
T	-0.01 ± 0.05

S	0 (fixed)
T	$+0.03 \pm 0.02$

$$(2 \text{ GeV})^2 < \sum_i \frac{N_C^i}{3} \Delta m_i^2 < (44 \text{ GeV})^2$$

Hadronic vacuum polarization

Hadronic vacuum polarization



**BaBar and earlier data based on
Davier et al. arXiv:1908.00921**

**CMD-3 and figure from
Davier et al., arXiv:2312.02053**

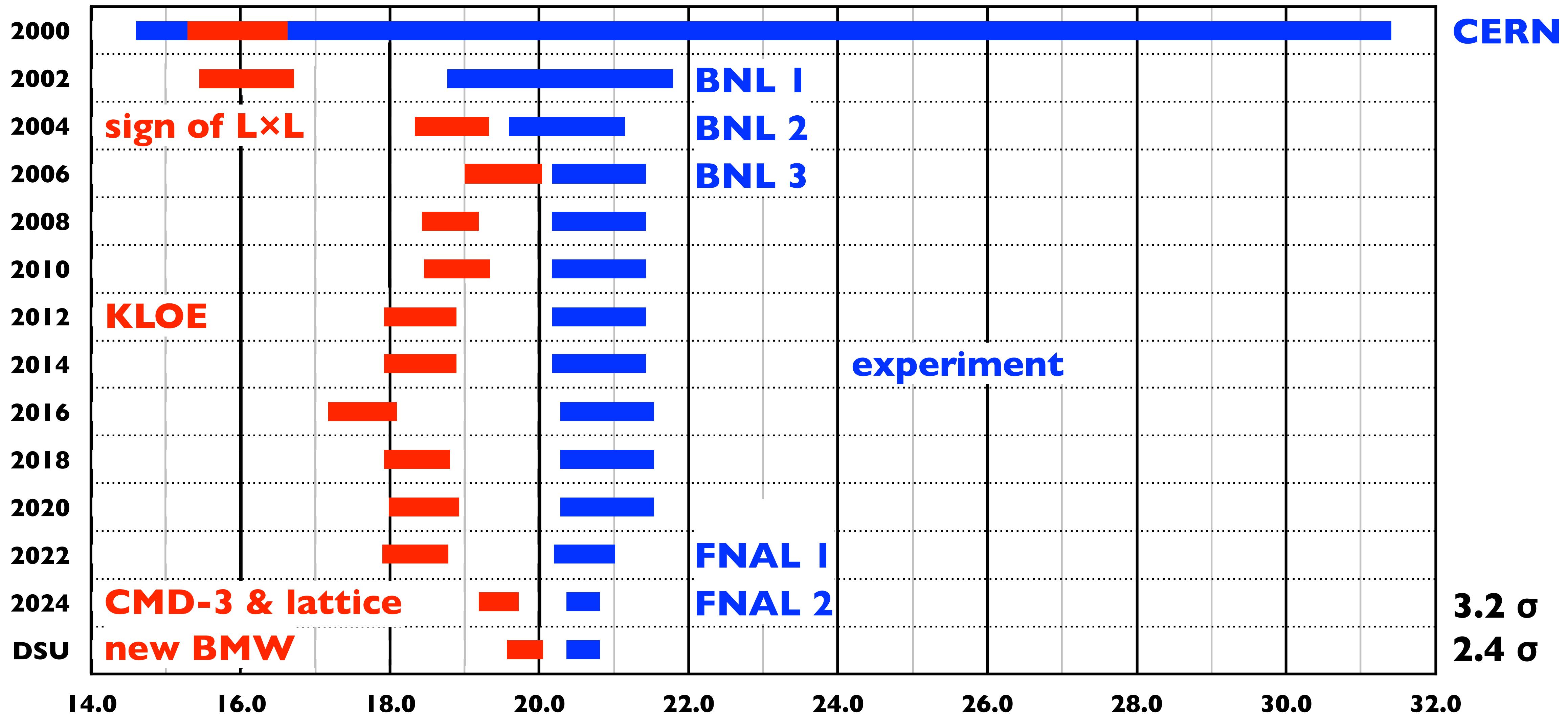
**KLOE based on
Davier et al. arXiv:1908.00921**

**after isospin rotation according to
Davier et al., arXiv:2312.02053**

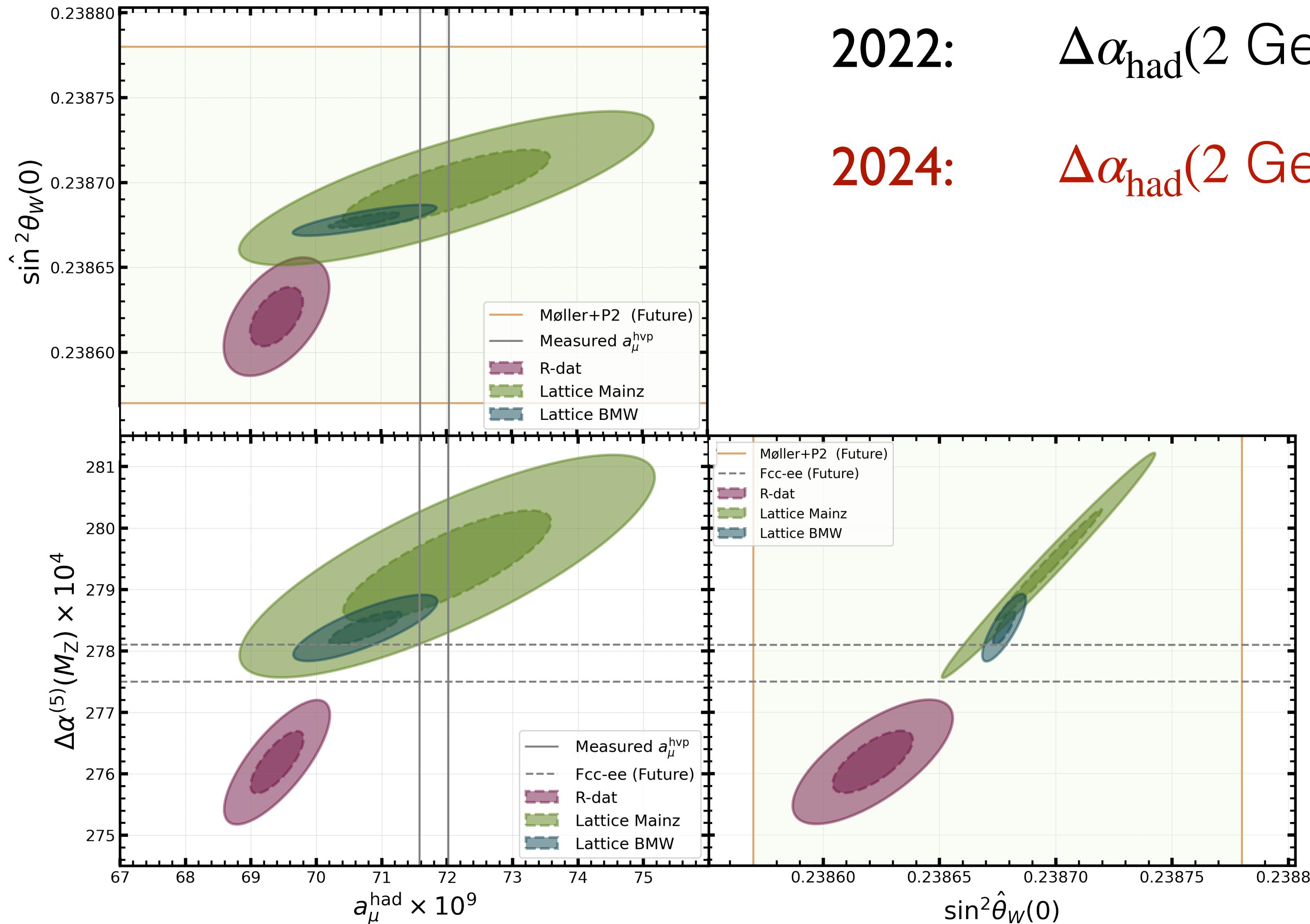
Borsanyi et al., arXiv:2002.12347

**$\Delta\alpha$ from Cè et al., arXiv:2203.08676
also enters through correlations**

chronology of a_μ [$\times 10^9 - 1165900$]

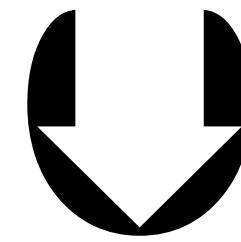


$g_\mu - 2$, $\alpha(M_Z)$ and $\sin^2\theta_W(0)$



2022: $\Delta\alpha_{\text{had}}(2 \text{ GeV}) = (58.84 \pm 0.51) \times 10^{-4}$

2024: $\Delta\alpha_{\text{had}}(2 \text{ GeV}) = (60.30 \pm 0.43) \times 10^{-4}$



$$\Delta M_W = -2.7 \text{ MeV}$$

$$\Delta M_H = -7.0 \text{ MeV}$$

Ferro-Hernández, Kuberski
& JE, arXiv:2406.16691

...if there is time...

α_s from the Z pole

observable	$\alpha_s(M_Z)$	comment
$\Gamma_Z = 2495.5 \pm 2.3 \text{ MeV}$	0.1215 ± 0.0048	update: $\Gamma_Z = +0.3 \text{ MeV}$
$\sigma_{\text{had}} = 41.481 \pm 0.033 \text{ nb}$	0.1201 ± 0.0065	update: $\Delta\sigma_{\text{had}} = -60 \text{ pb}$
$R_e = \Gamma_{\text{had}}/\Gamma_e = 20.804 \pm 0.050$	0.1295 ± 0.0082	
$R_\mu = \Gamma_{\text{had}}/\Gamma_\mu = 20.784 \pm 0.034$	0.1264 ± 0.0054	$m_\mu \neq 0$
$R_\tau = \Gamma_{\text{had}}/\Gamma_\tau = 20.764 \pm 0.045$	0.1157 ± 0.0072	$m_\tau \neq 0$
$B_W(\text{had}) = 0.6736 \pm 0.0018$	0.098 ± 0.025	recent (LEP 2 + CMS)
combination	0.1223 ± 0.0028	future lepton collider $\sim 10^{-4}$
global fit	0.1185 ± 0.0016	includes τ decays

electromagnetic beam-beam effects
improved Bhabha X section (luminosity)

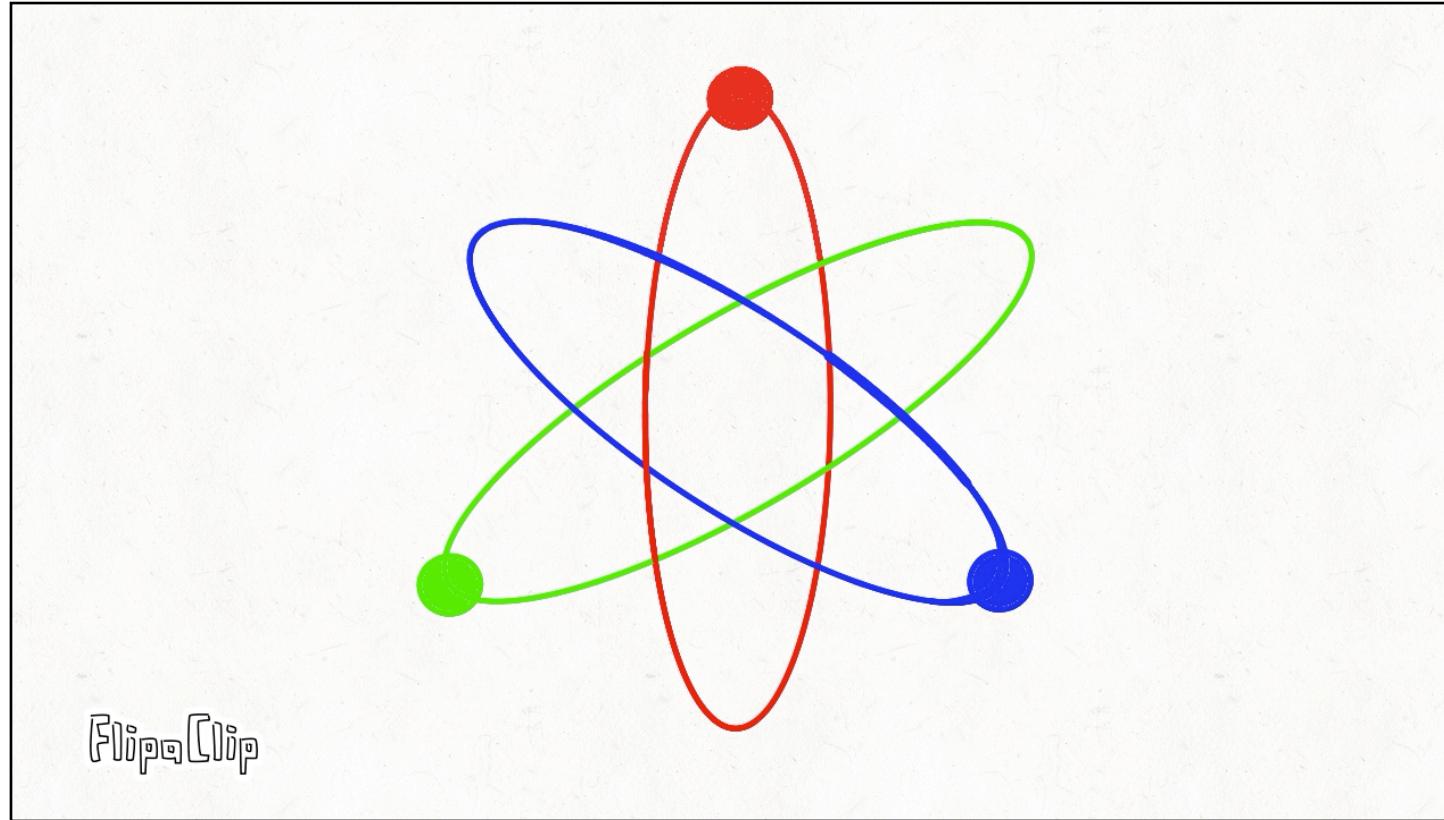
Voutsinas et al., arXiv:1908.01704
Janot & Jadach, arXiv:1912.02067

Conclusions

- * *after more than 50 years of electroweak precision physics, still no conclusive evidence for BSM*
- * M_W, M_Z, m_t, M_H (and m_c) have all been successfully **predicted** before their discoveries
- * the infamous conflict in **muon g–2** reduced to about 2.4σ
- * recent *LEP* luminosity update confirms $N_\nu = 3$ active neutrinos, but α_s somewhat high
- * new CDF M_W result $\sim 7\sigma$ **higher** than other measurements !!!
- * *outlook*
 - * high precision PVES (*P2, MOLLER, SoLID*) competitive alternatives to high energy frontier
 - * leap in precision expected from future lepton collider(s)
ILC, CEPC, FCC–ee, CLIC, μ collider

Discussion Topics

- * How difficult would be the atomic theory calculation for the $7s$ to $6d_{3/2}$ transition in Ra^+ ?
What uncertainty could be expected?
- * Is the muon $g-2$ deviation gone (nominally $2.4\ \sigma$)?
Trust dispersion analysis or lattice?
- * What should be done about the M_W from CDF, given that their M_Z agrees well with LEP?
Are we central limit or even confirmation biased?



Thank You