

# Constraints on the Symmetry Energy from the Dipole Polarizability



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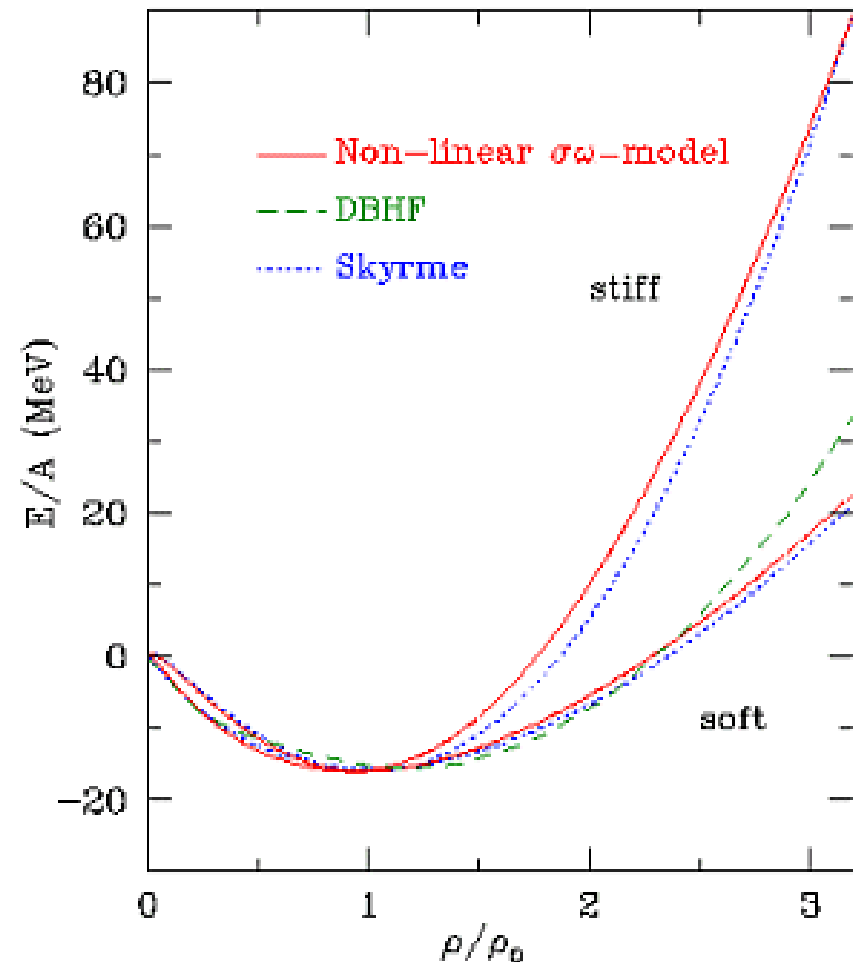
- Equation of State, symmetry energy, neutron skin and dipole polarizability
- Extraction of the E1 strength and dipole polarizability from small-angle ( $p, p'$ ) scattering
- Constraints from density functional theory
- Constraints from *ab initio* calculations
- Constraints from systematics

Supported by DFG under contract SFB 1245 (project id 279384907)



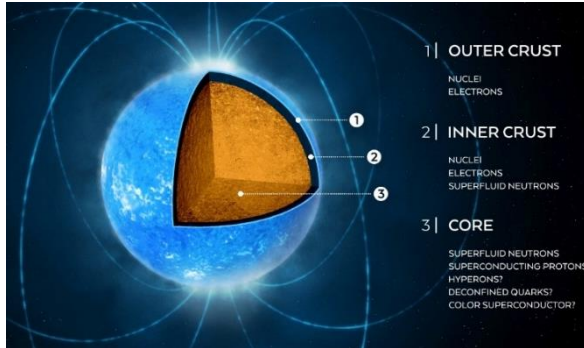
# Nuclear Matter Equation of State (EOS)

- Energy as a function of density (or pressure)
- Well defined at  $\rho/\rho_0 = 1$  by properties of stable nuclei
- Large differences of models at high densities: stiff or soft?



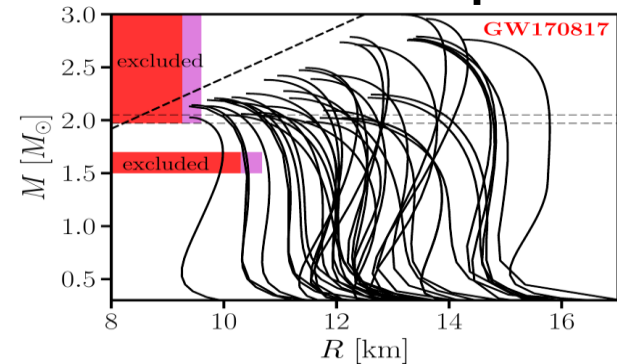
# EoS of Neutron-Rich Matter

## Neutron Stars



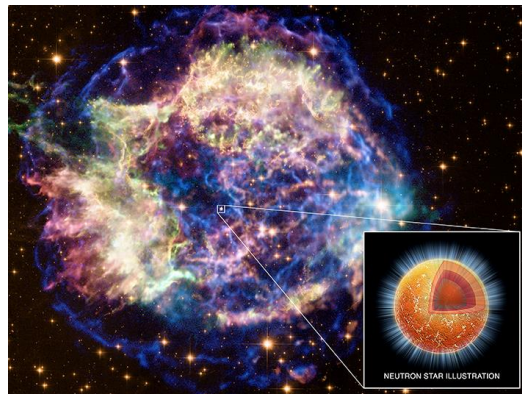
A. Watts et al., RMP 88, 021001 (2016)

## Neutron Star Properties



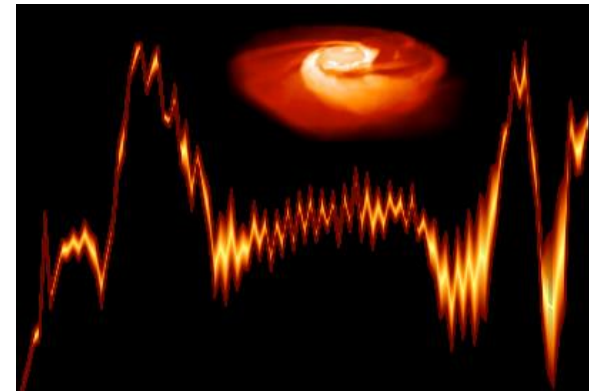
A. Bauswein et al., ApJ Lett. 885, L34 (2017)

## Core-Collapse Supernovae



H. Yasin et al., PRL 124, 092701 (2020)

## Neutron Star Mergers

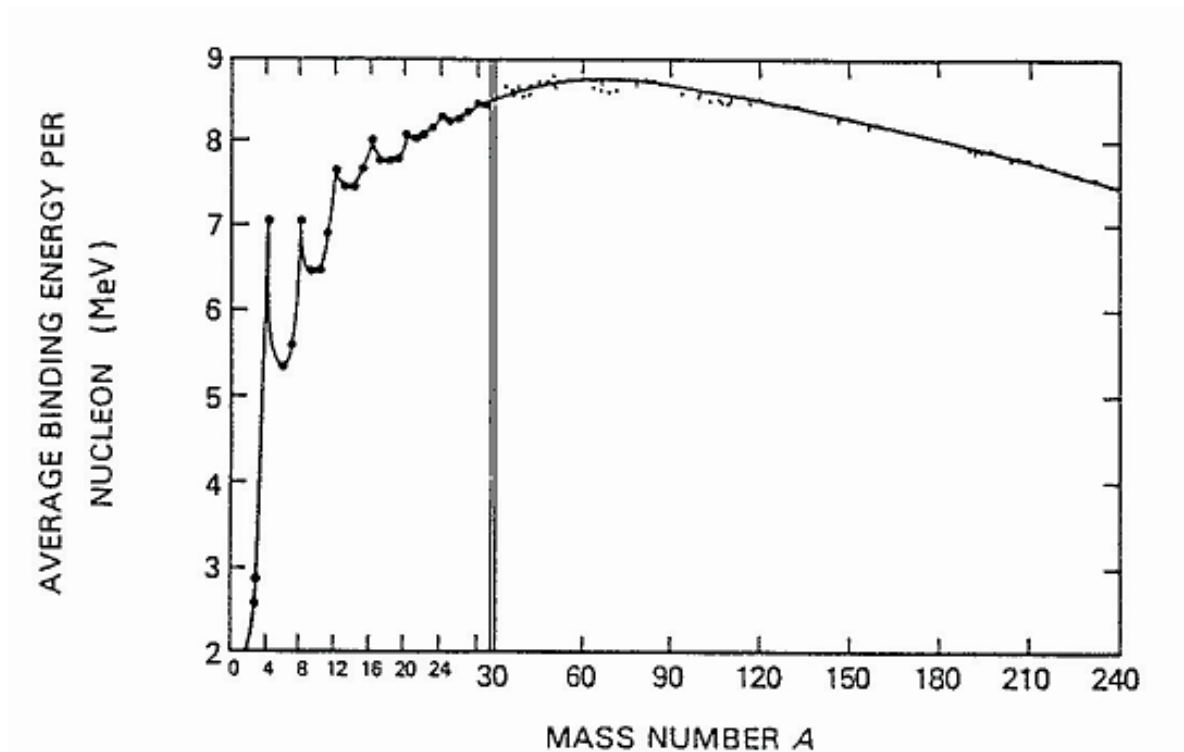


B.P. Abbott et al., PRL 119, 161101 (2017)

# Binding Energy of Nuclei

$$B(A, Z) = a_v A - a_s A^{2/3} - a_c Z(Z-1)/A^{1/3} - a_{sym} (A-2Z)^2/A + \delta$$

volume surface Coulomb symmetry pairing




# Binding Energy of (Infinite) Neutron-Rich Matter



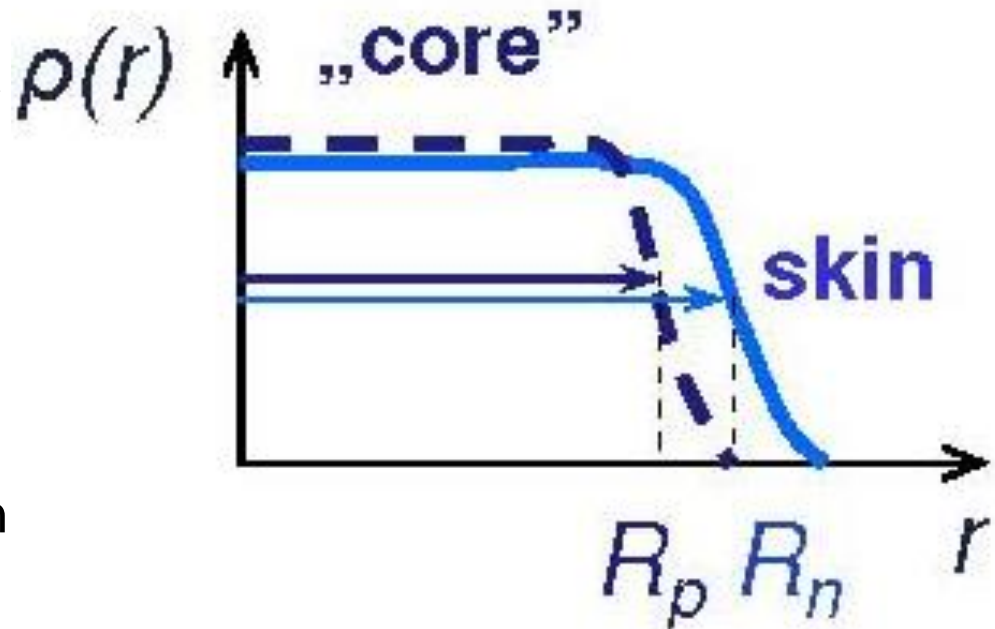
$$B(A, Z) = a_v A - a_s A^{2/3} - a_c Z(Z-1)/A^{1/3} - a_{sym} (A - 2Z)^2 / A + a_p$$

volume    ~~surface~~    Coulomb    symmetry    ~~pairing~~

- For (infinite) neutron matter only volume and symmetry term contribute to the energy of the system.
  - The volume term can be estimated from the saturation properties
- 
- The symmetry energy represents the largest uncertainty for the EOS of neutron-rich matter.

# Symmetry Energy and Neutron Skin of Nuclei

- Nuclear force leads to constant density in the interior (saturation)
- Stable heavy nuclei have  $N > Z$  because the symmetry energy is balanced by the Coulomb repulsion between protons
- Extra neutrons concentrate on the surface  
→ formation of a neutron skin
- Neutron skin thickness depends on the parameters of the symmetry energy



$$\begin{aligned}\mathcal{E}(\rho, \alpha) &= \mathcal{E}_{\text{SNM}}(\rho) + \alpha^2 \mathcal{S}_2(\rho) + \dots \\ &= \left( \varepsilon_0 + \frac{1}{2} K_0 x^2 + \dots \right) + \alpha^2 \left( J + Lx + \frac{1}{2} K_{\text{sym}} x^2 + \dots \right) + \dots\end{aligned}$$

*Note: In the original image, green arrows point from the  $\alpha^2$  term to  $J$  and  $Lx$ , and a green 'X' is placed over  $K_{\text{sym}}$ .*

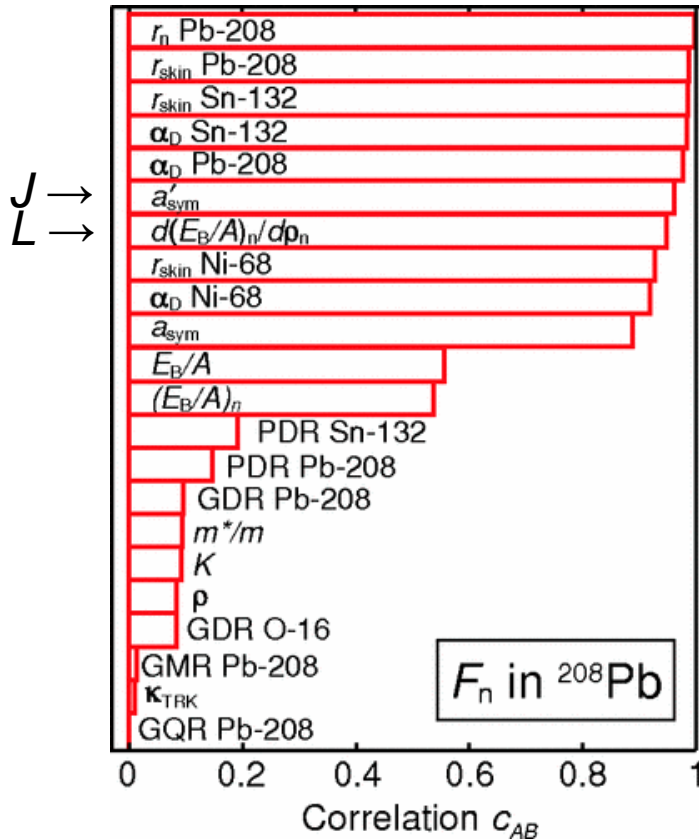
$$\boxed{P_{\text{PNM}}(\rho_0) = \frac{1}{3} \rho_0 L} \quad \left[ \alpha = (N - Z) / A; \quad x = (\rho - \rho_0) / 3\rho_0 \right]$$

- Symmetry energy determined by  $J$  and  $L$
- $L$  describes density dependence (stiff or soft EoS)

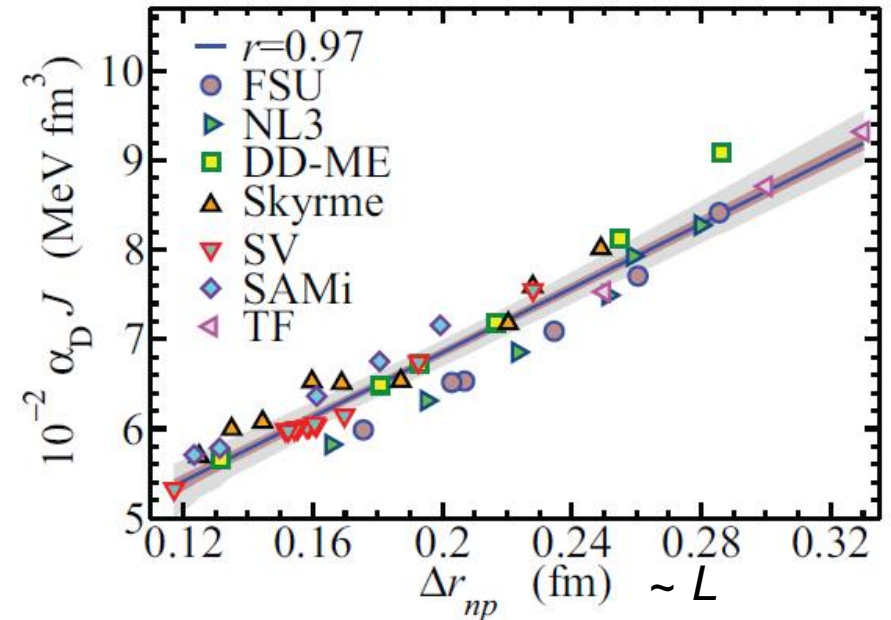
# Polarizability, Neutron Skin and Symmetry Energy

- Static nuclear dipole polarizability

$$\alpha_D = \frac{\hbar c}{2\pi^2} \int \frac{\sigma_{abs}^{E1}}{E^2} dE$$



P.-G. Reinhard and W. Nazarewicz,  
PRC 81, 051303(R) (2010)

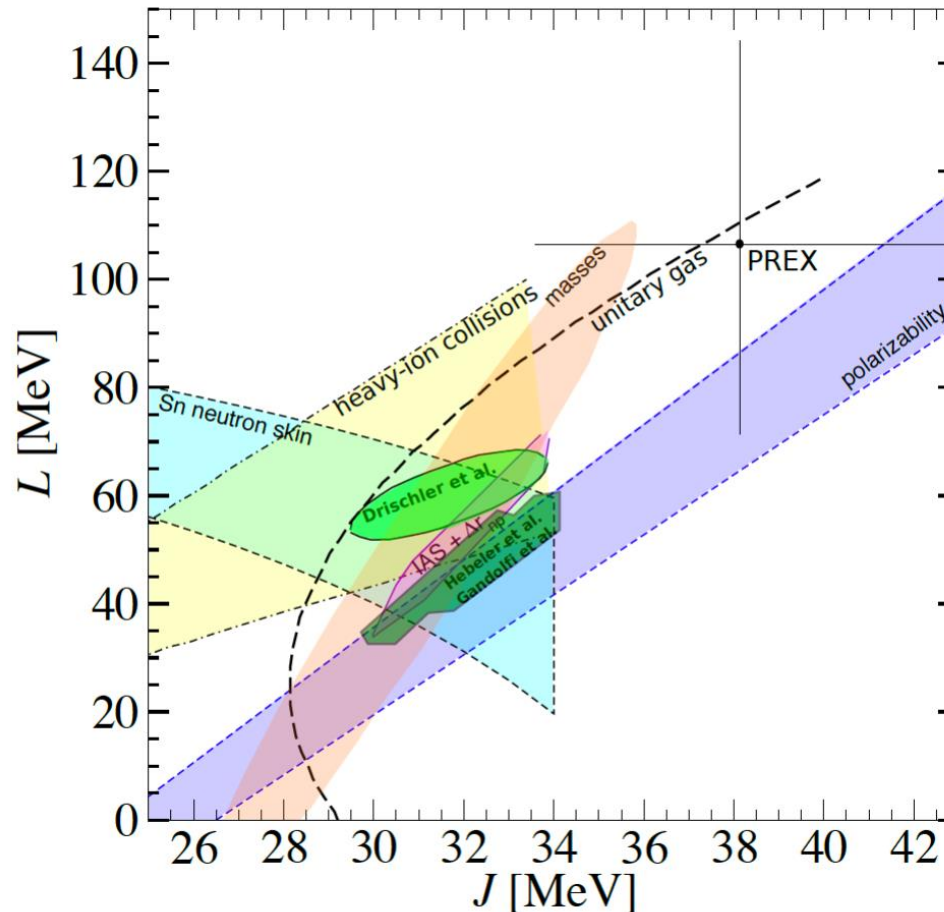


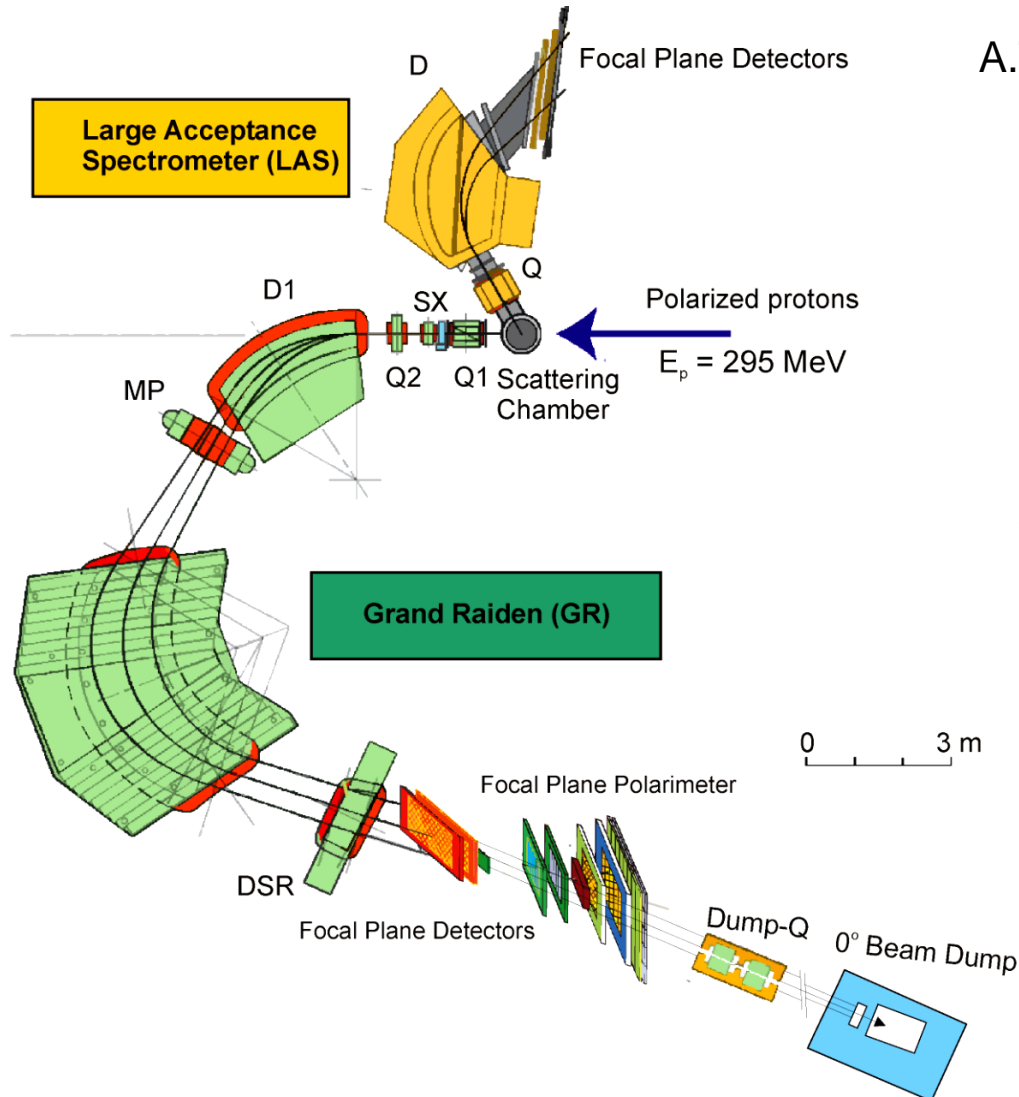
X. Roca-Maza et al., PRC 88, 024316 (2013)



# Symmetry Energy Constraints

F. Gulminelli and A.F. Fantina, Nucl. Phys. News 31(2), 9 (2021)



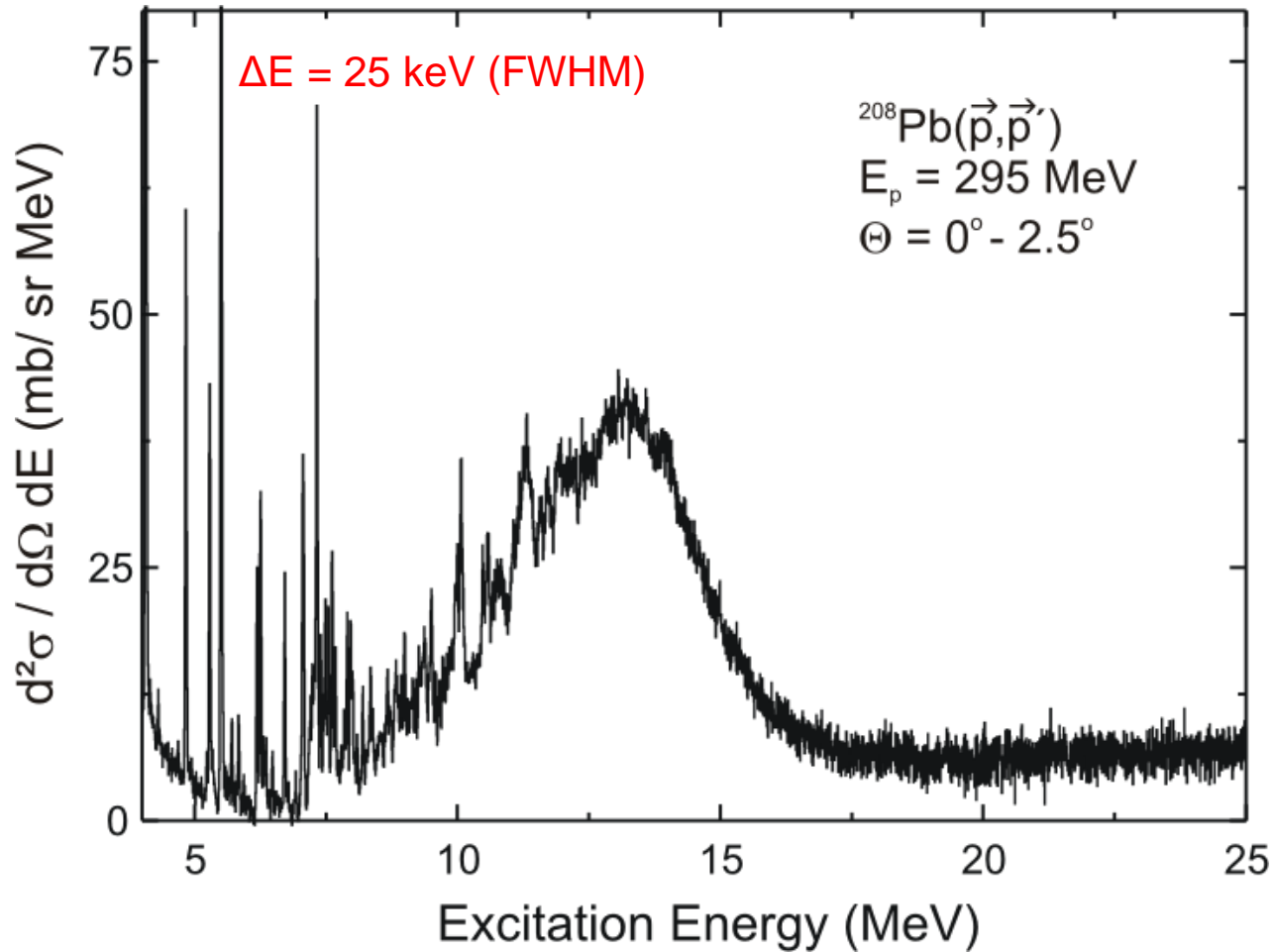


A.Tamii et al., NIMA 605, 326 (2009)

## Measured observables

- $d\sigma/d\Omega$  - angular distributions  
( $0^\circ \leq \Theta \leq 10^\circ$ )
- $A_y$  - asymmetry
- $D_{SS}$  at  $0^\circ$  - sideways polarization
- $D_{LL}$  at  $0^\circ$  - longitudinal polarization

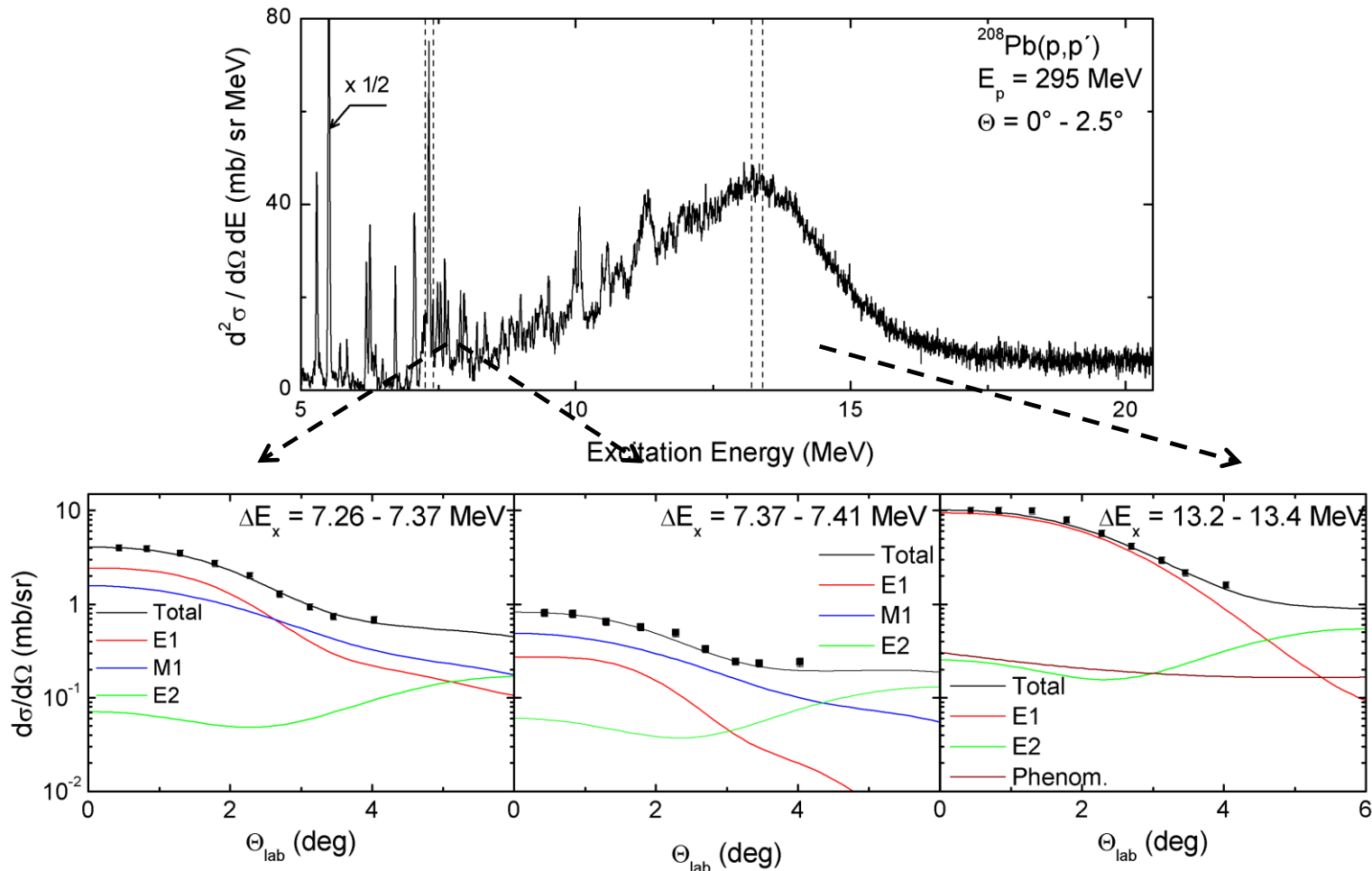
# Measured Spectrum



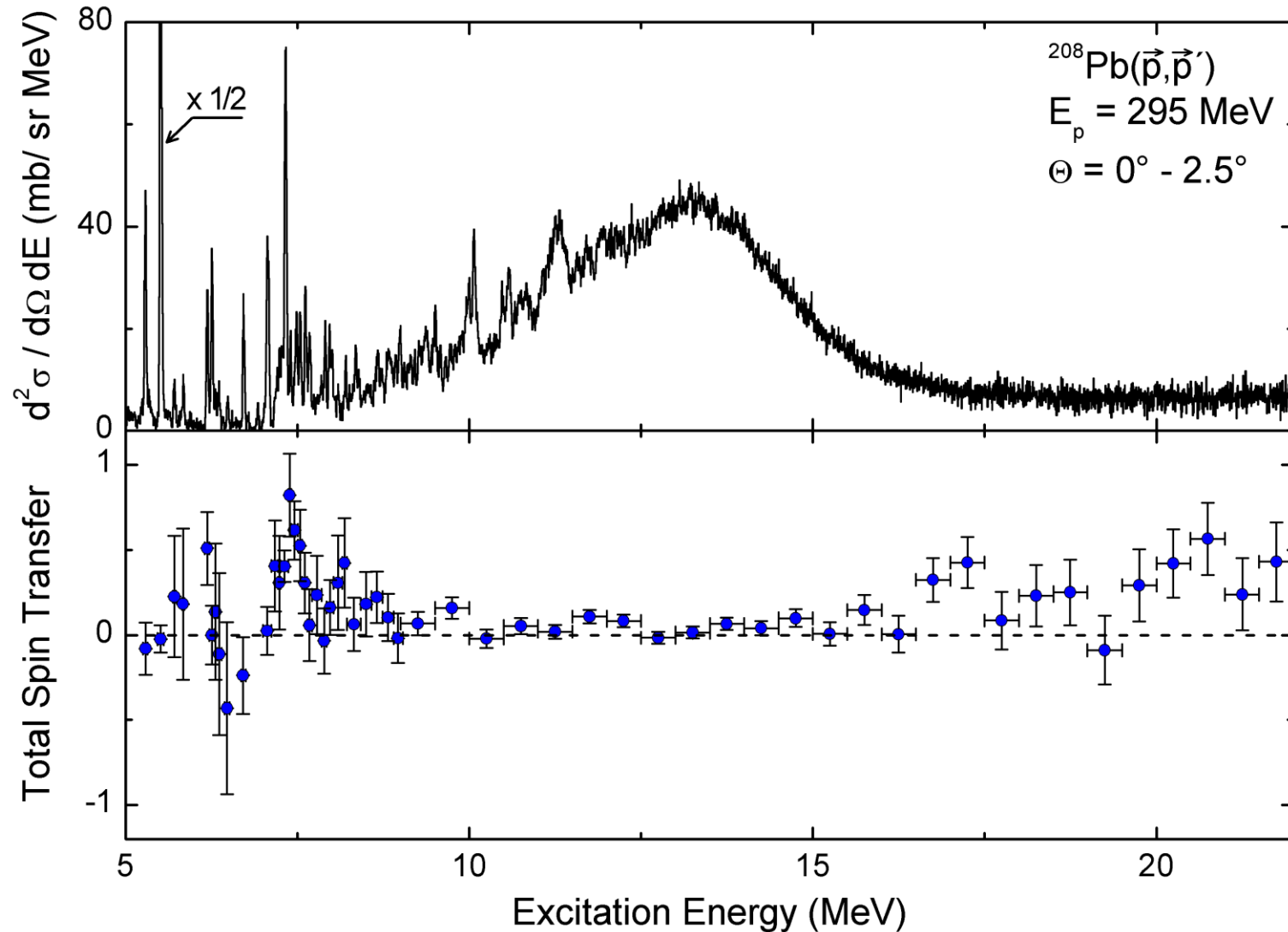
- Dominance of relativistic Coulomb excitation

# Multipole Decomposition of Angular Distributions

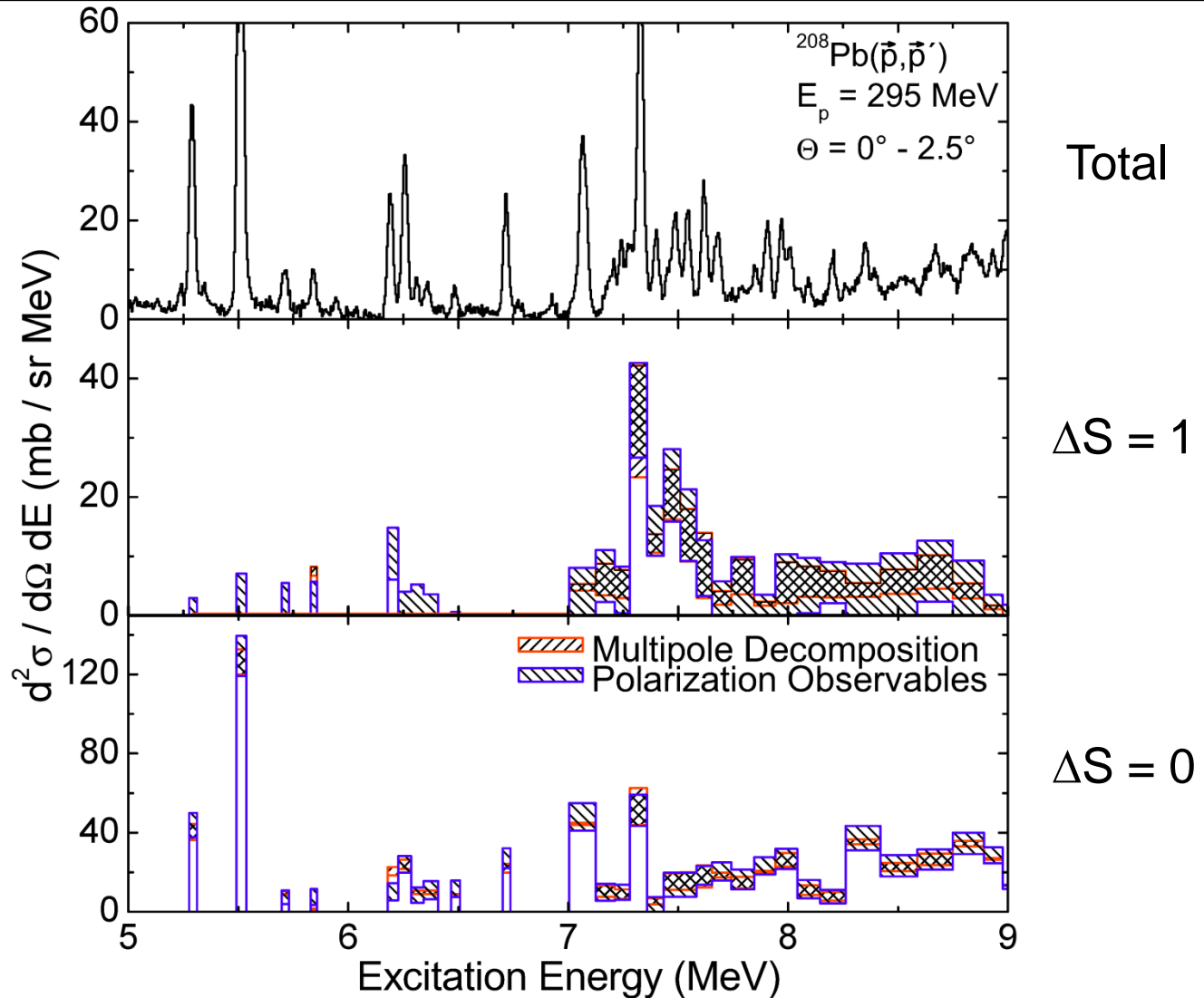
I. Poltoratska et al., PRC 85, 041304(R) (2012)



# Decomposition into Spinflip / Non-Spinflip Cross Sections

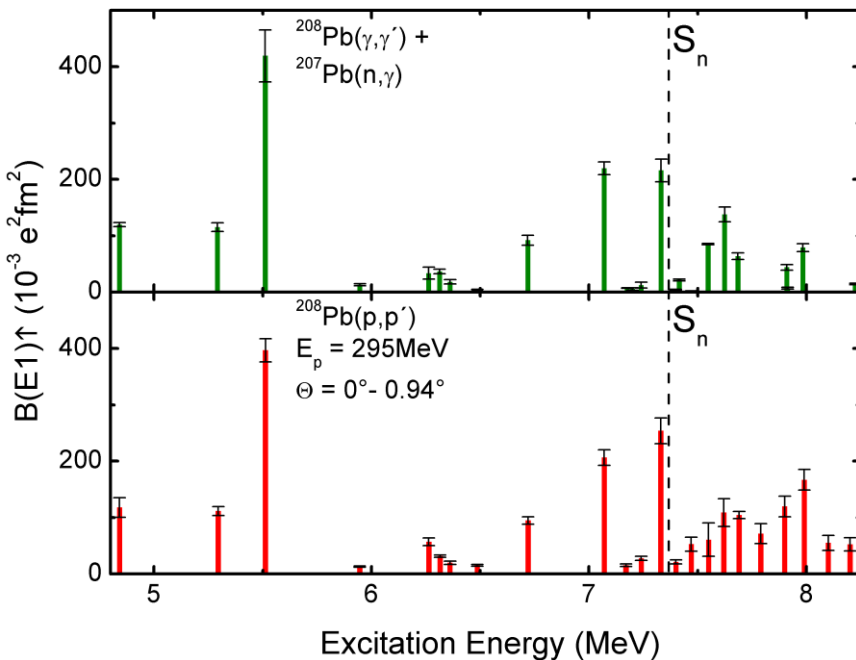


# Comparison of Both Methods

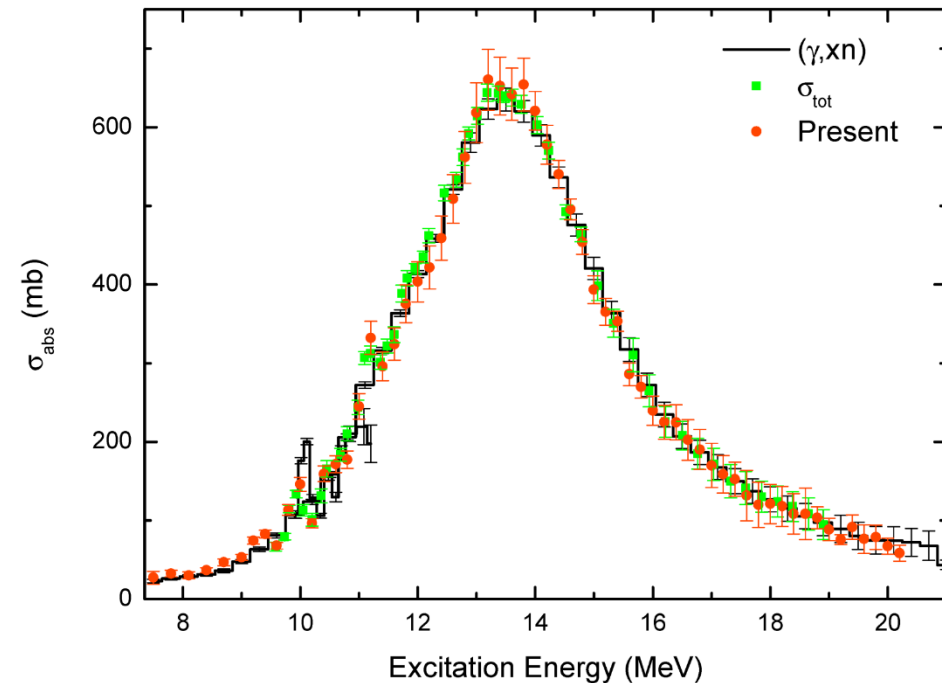


# E1 Strength in $^{208}\text{Pb}$

I. Poltoratska et al., PRC 85 (2012) 041304(R)

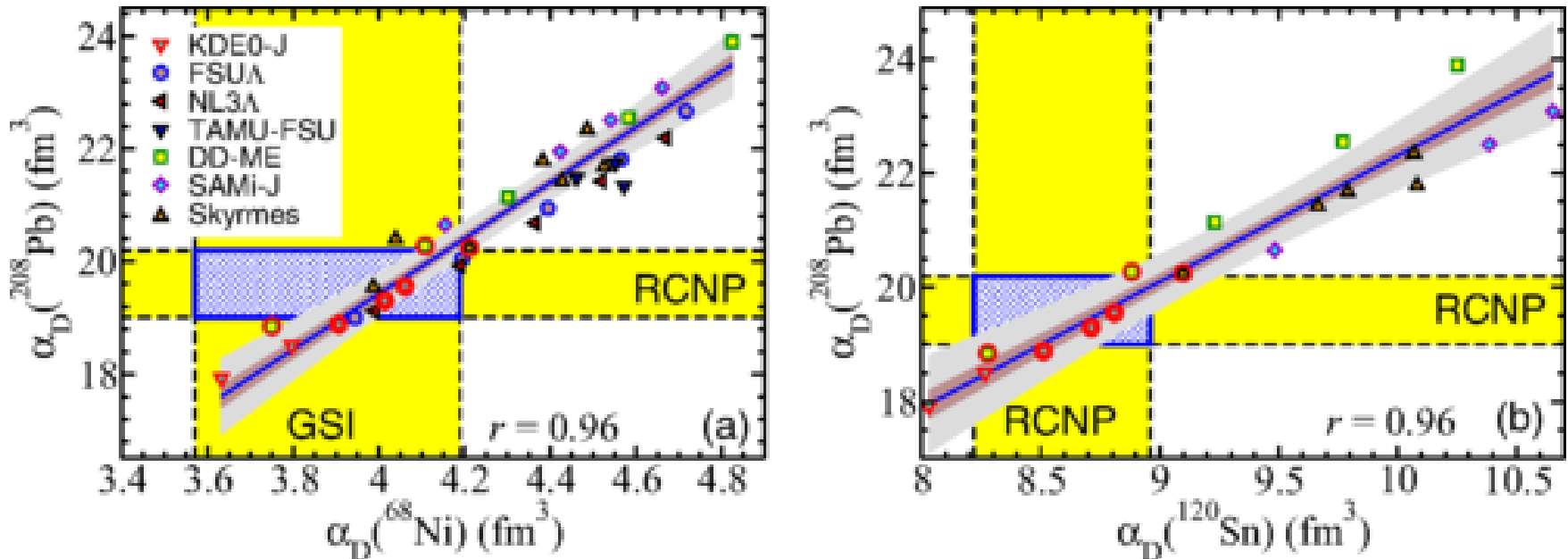


A. Tamii et al., PRL107, 062502 (2011)



# Constraints on EDFs from $^{208}\text{Pb}$ , $^{120}\text{Sn}$ and $^{68}\text{Ni}$

X. Roca-Maza et al., PRC 92, 064304 (2015)

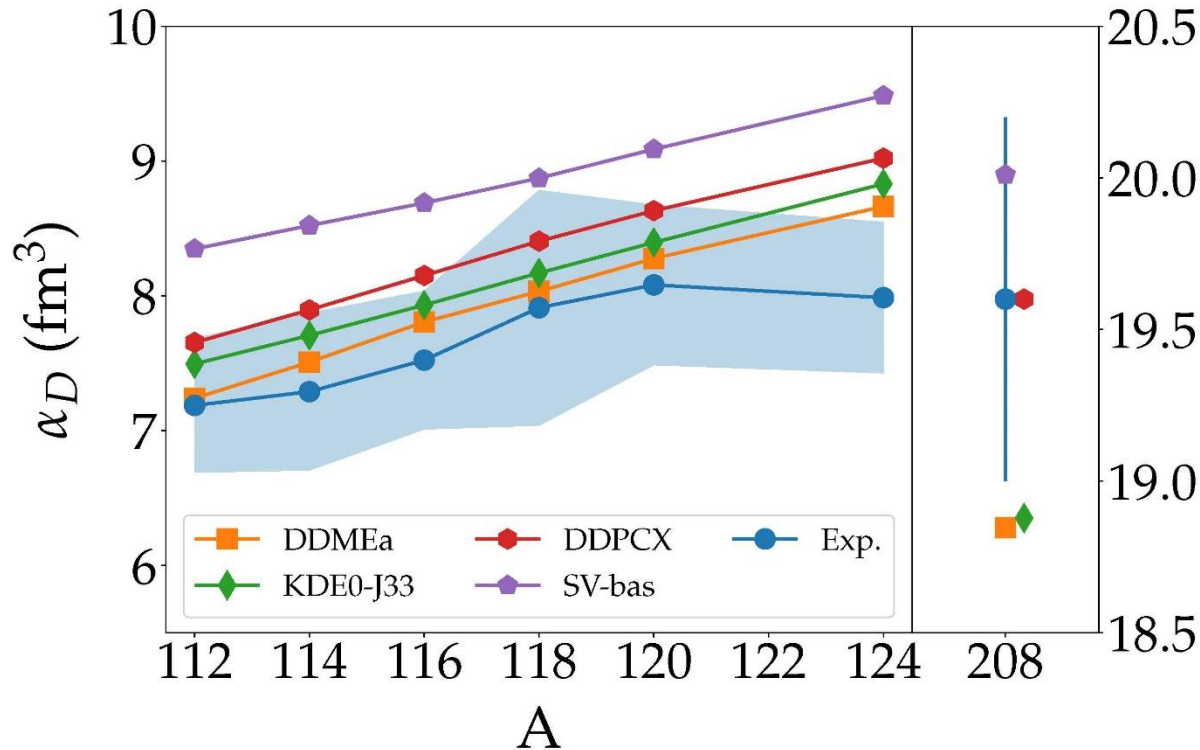


- Only a handful of EDFs can describe all 3 data
- Constraints on symmetry energy:  $J = 30 - 35 \text{ MeV}$   $L = 20 - 66 \text{ MeV}$



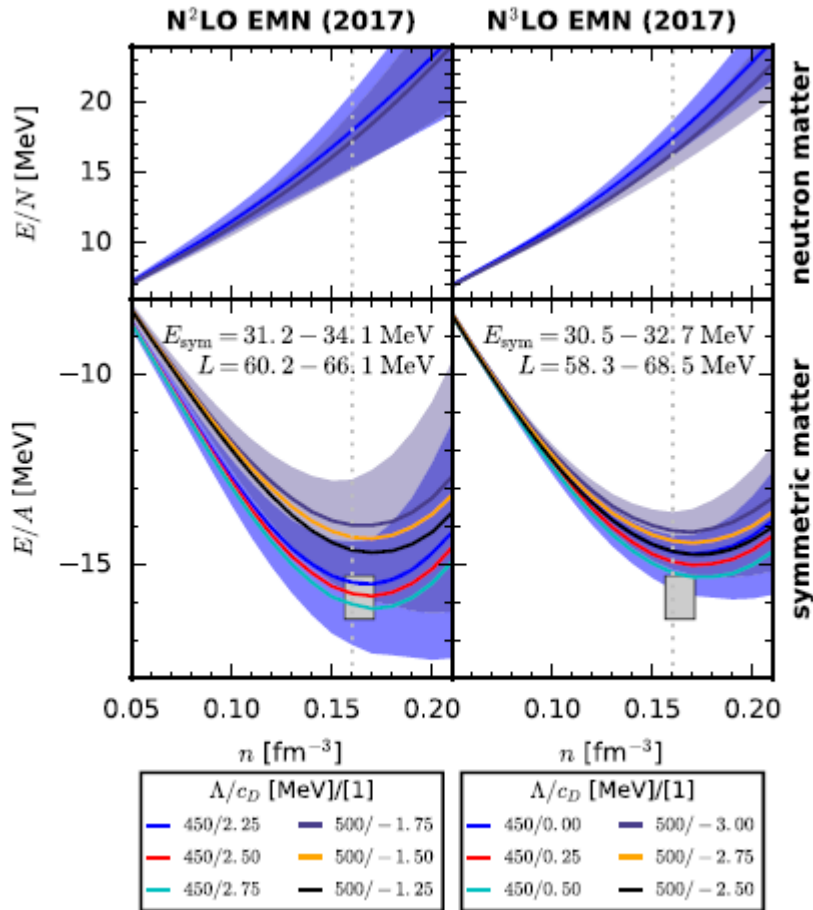
# Polarizability: Systematics in the Sn Chain

S. Bassauer et al., PLB 810, 135804 (2020)



- Simultaneous description with of  $\alpha_D(^{208}\text{Pb})$  difficult

# Ab Initio Calculations

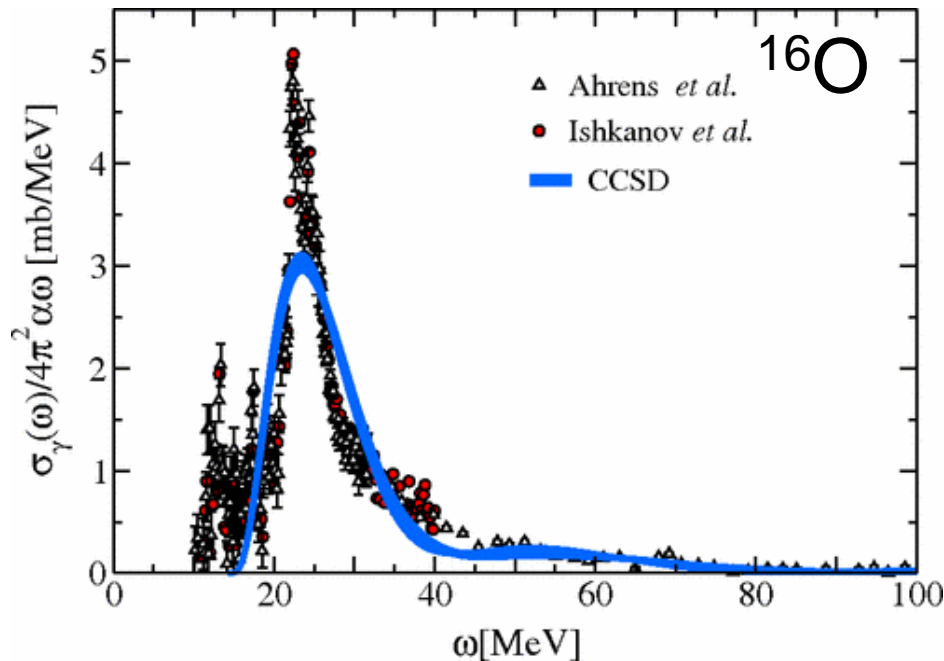


C. Drischler, K. Hebeler, and A. Schwenk,  
Phys. Rev. Lett. 122, 042501 (2019)

- Same interactions can be used to calculate nuclear matter
- Polarizability provides constraints for neutron matter

# Ab Initio Calculations of the Polarizability

S. Bacca et al., PRL 111, 122502 (2013)

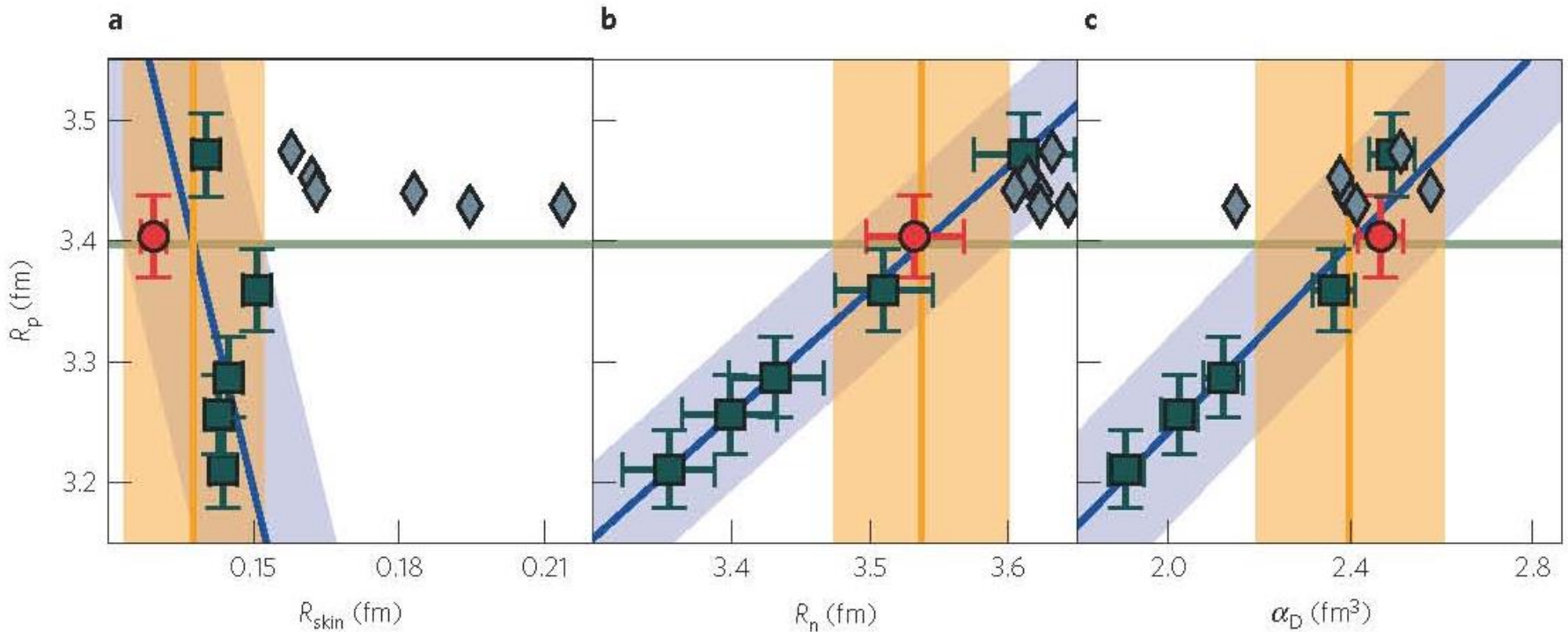


- Based on interactions derived from  $\chi$ EFT
- Combines Lorentz Integral Transform (LIT) with Coupled Cluster (CC) technique

→ next talk by Francesca Bonaiti

# The Case of $^{48}\text{Ca}$ : $\chi\text{EFT}$ versus EDFs

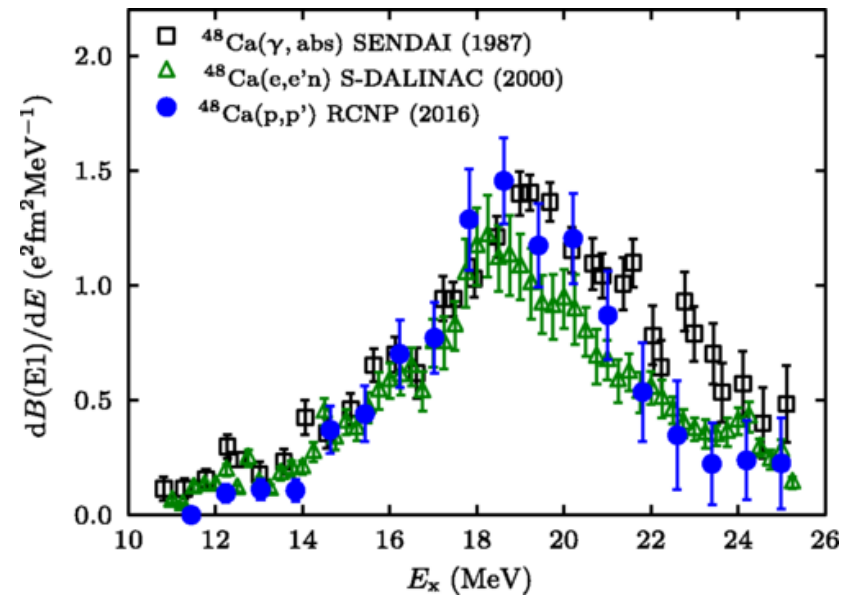
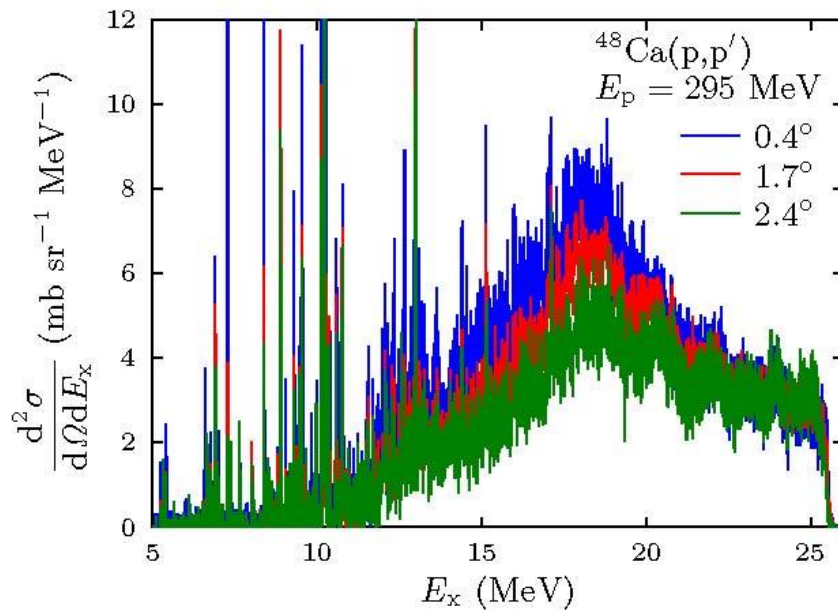
G. Hagen et al., Nat. Phys. 12, 186 (2016)



- Small neutron skin predicted by EFT
- Different correlation between  $R_p$  and  $R_n$

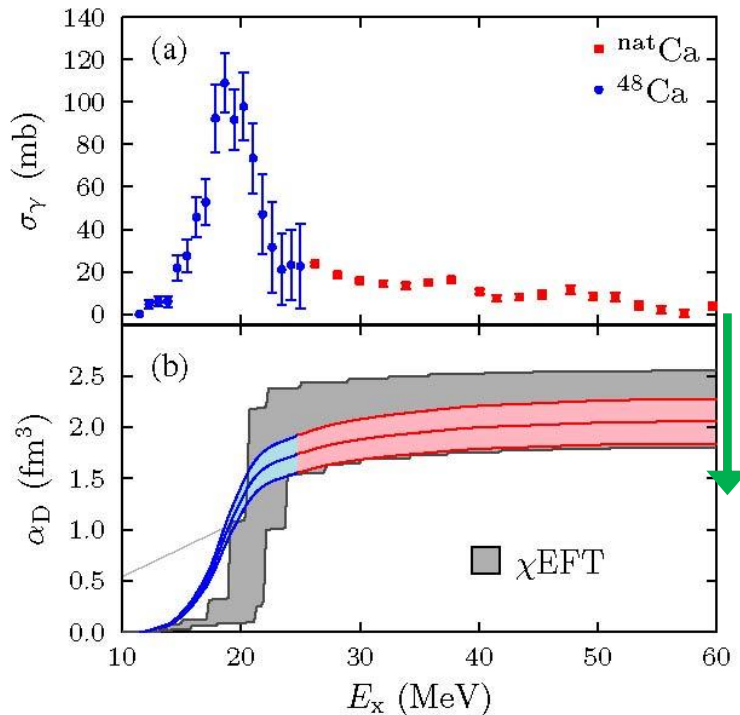
# Polarizability of $^{48}\text{Ca}$

J. Birkhan et al., PRL 118, 252501 (2017)

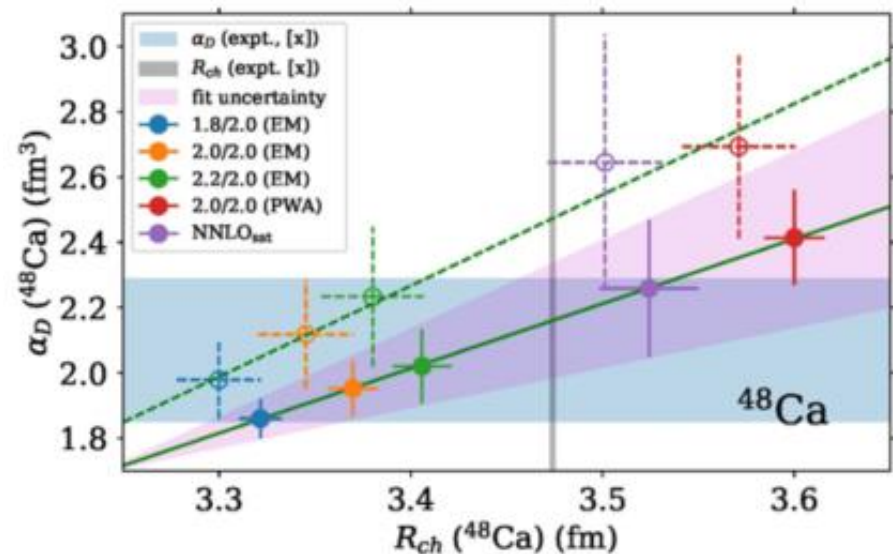


# Polarizability of $^{48}\text{Ca}$

J. Birkhan et al., PRL 118, 252501 (2017)

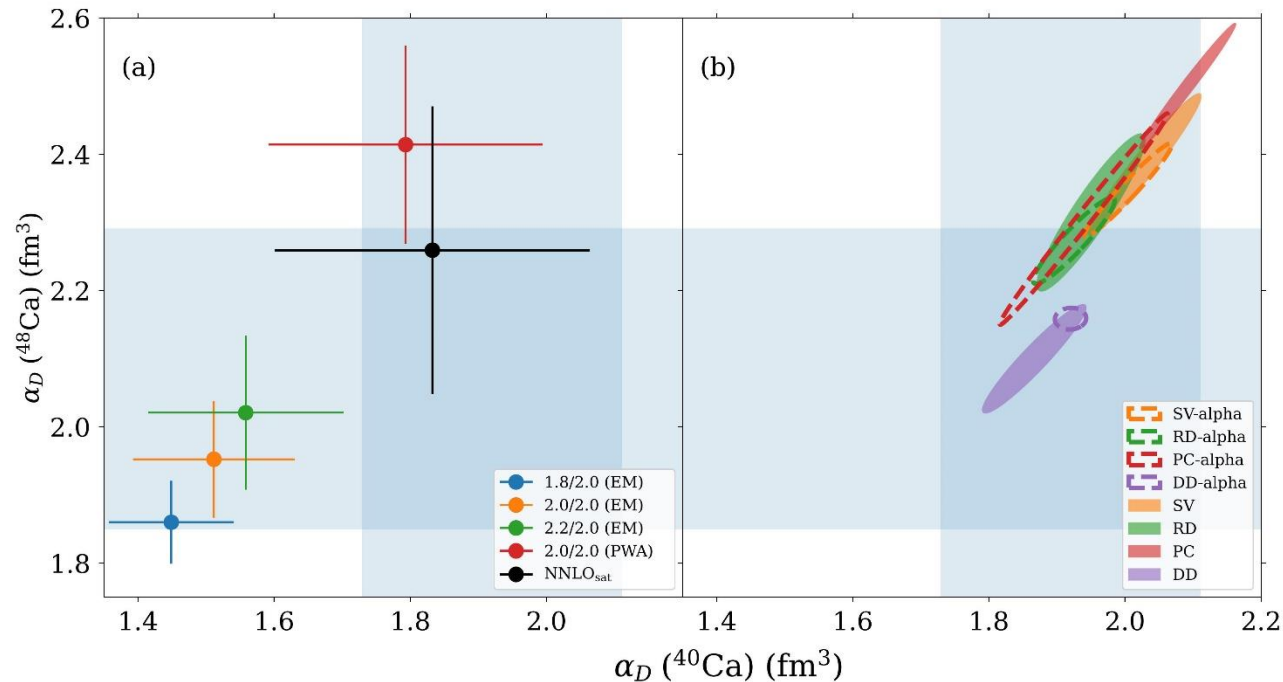


M. Miorelli et al., PRC 98, 014324 (2018)



- Uncertainty larger than in  $^{208}\text{Pb}$  due to unknown parametrization of the nuclear background
- Triple correlations important

R.W. Fearick et al., PRR 5, L022044 (2023)

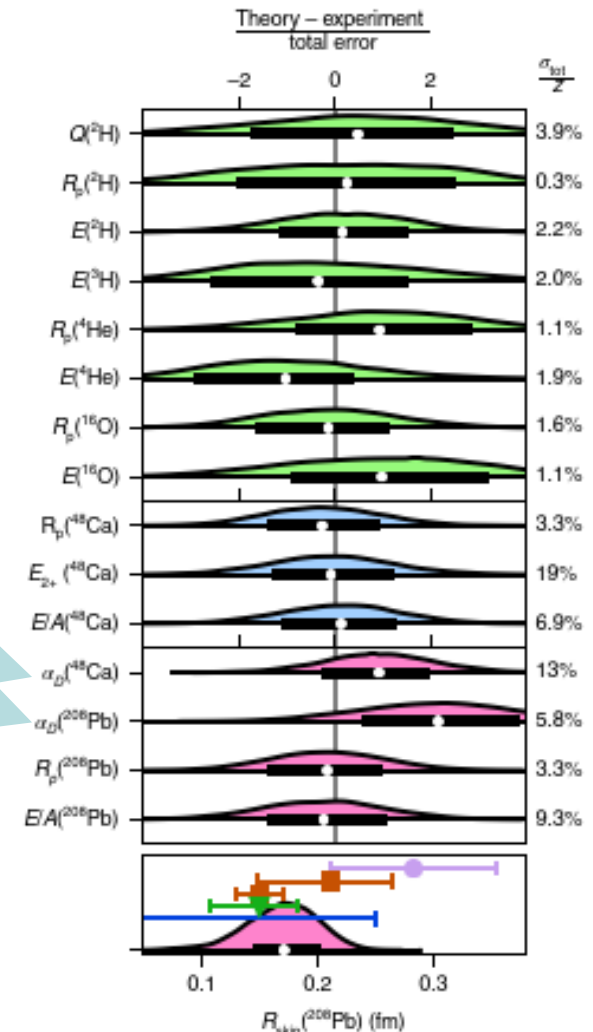


- Constraints from  $\chi\text{EFT}$ :  $J = 27\text{--}33$  MeV,  $L = 41\text{--}49$  MeV
- Constraints from EDFs:  $J = 30\text{--}35$  MeV,  $L = 32\text{--}82$  MeV  
 $J = 30\text{--}32$  MeV,  $L = 35\text{--}52$  MeV [ $\alpha_D(^{208}\text{Pb})$  included]

# New Ab Initio Calculation of $^{208}\text{Pb}$ and $^{48}\text{Ca}$

B. Hu et al, Nat. Phys. 18, 1196 (2022)

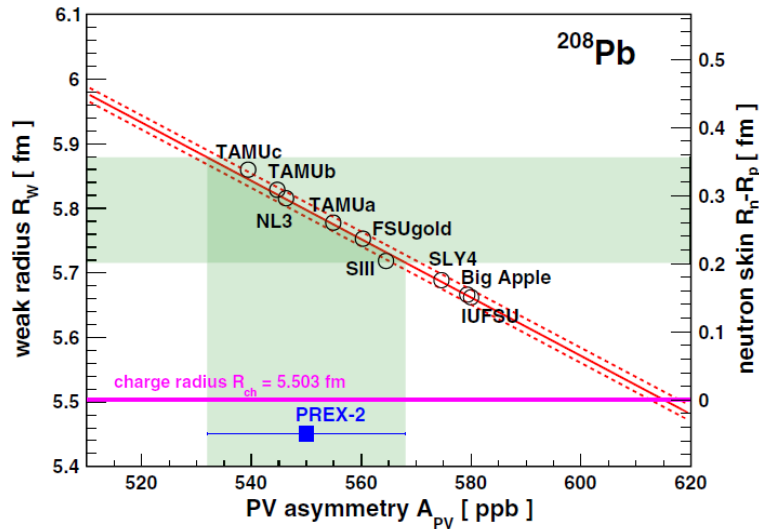
- Unknown LECs constrained by nucleon scattering data and selected observables in light nuclei
- Reasonable agreement for  $\alpha_D$  results (slightly too high)
- Constraints on symmetry energy:  
 $J = 27 - 31 \text{ MeV}$   $L = 37 - 66 \text{ MeV}$



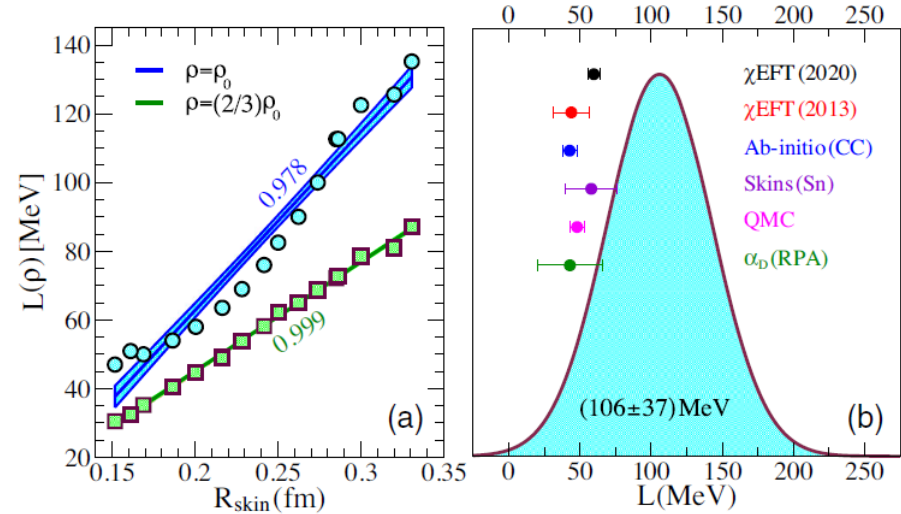


# PREX Constraints on Neutron Skin and Density Dependence of the Symmetry Energy

D. Adhikari et al., PRL 126, 172502 (2021)



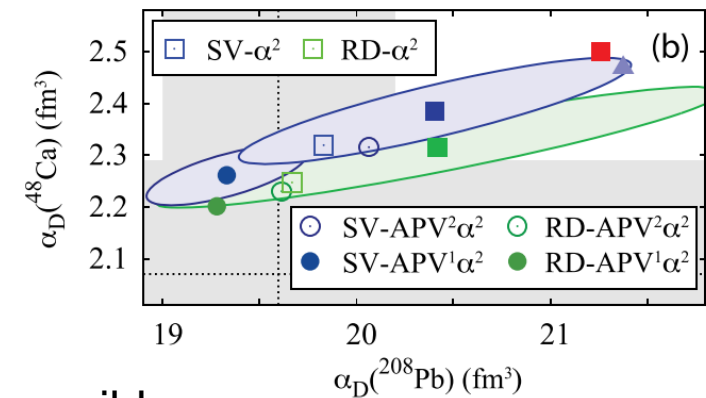
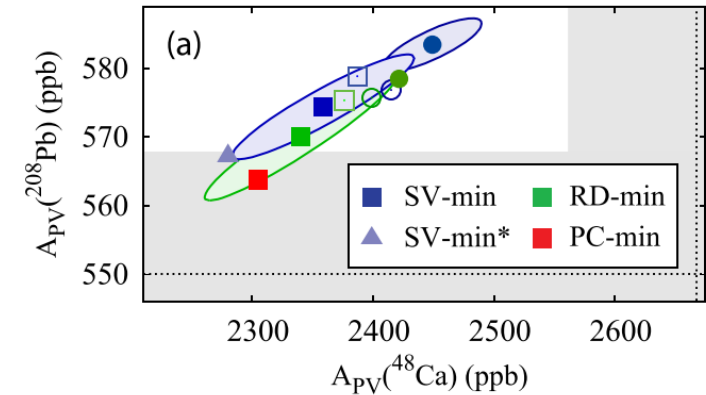
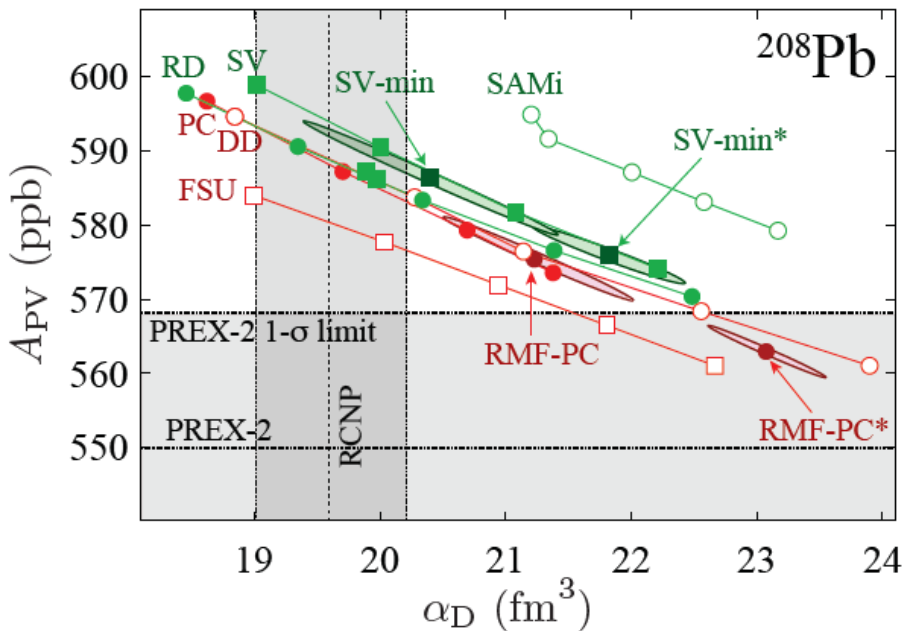
B.T. Reed et al., PRL 126, 172503 (2021)



- Derived density dependence of the symmetry energy  $L = 106(37)$  MeV

# PREX and CREX versus Dipole Polarizability

P.-G. Reinhard, X. Roca-Maza and W. Nazarewicz, PRL 127, 232501 (2021); PRL 129, 232501 (2022)



- No consistent description of  $A_{PV}$  and  $\alpha_D$  for  $^{208}\text{Pb}$  possible

→ new MREX experiment important

## ■ Data

- $^{208}\text{Pb}$ : A. Tamii et al., PRL 107, 062502 (2011)
- $^{120}\text{Sn}$ : T. Hashimoto et al., PRC 92, 031305(R) (2015)
- $^{112,114,116,118,120,124}\text{Sn}$ : S. Bassauer et al., PLB 810, 135804 (2020)
- $^{90}\text{Zr}$ : T. Klaus, PhD thesis, TU Darmstadt (2020)
- $^{68}\text{Ni}$ : D.M. Rossi et al., PRL 111, 242503 (2013)
- $^{58}\text{Ni}$ : I. Brandherm et al., in preparation (2024)
- $^{48}\text{Ca}$ : J. Birkhan et al., PRL 118, 252501 (2017)
- $^{40}\text{Ca}$ : R.W. Fearick et al., PRR 5, L022044 (2023)
- $^{27}\text{Al}, ^{16}\text{O}$ : J. Ahrens et al., NPA 251, 479 (1975)

# Systematics: Migdal Model

- ▶ Hydrodynamic model with interpenetrating proton and neutron fluids

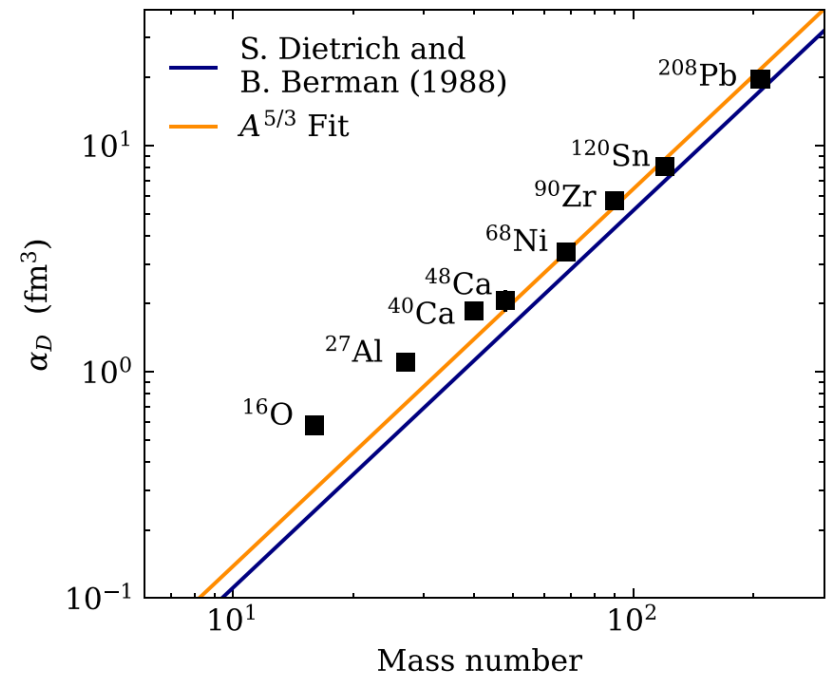
$$\alpha_D = \frac{e^2 R^2 A}{40 \cdot a_{\text{sym}}} \propto A^{5/3} \text{ fm}^3$$

- ▶  $a_{\text{sym}}$ : Symmetry energy parameter in the Bethe-Weizsäcker mass formula

- ▶ S. Dietrich and B. Berman,  
[At. Data Nucl. Data Tables 38, 199 \(1988\)](#)

$$\alpha_D = 2.4 \times 10^{-3} \cdot A^{5/3} \text{ fm}^3$$

- ▶ Fit:  $\alpha_D = 3.0(3) \times 10^{-3} \cdot A^{5/3} \text{ fm}^3$



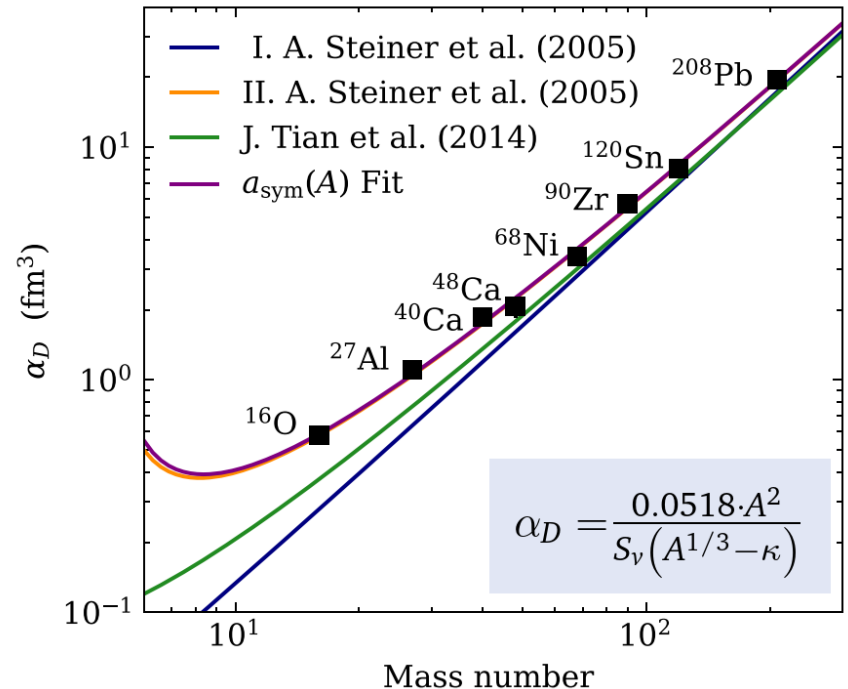
# Systematics: Volume and Surface Contributions



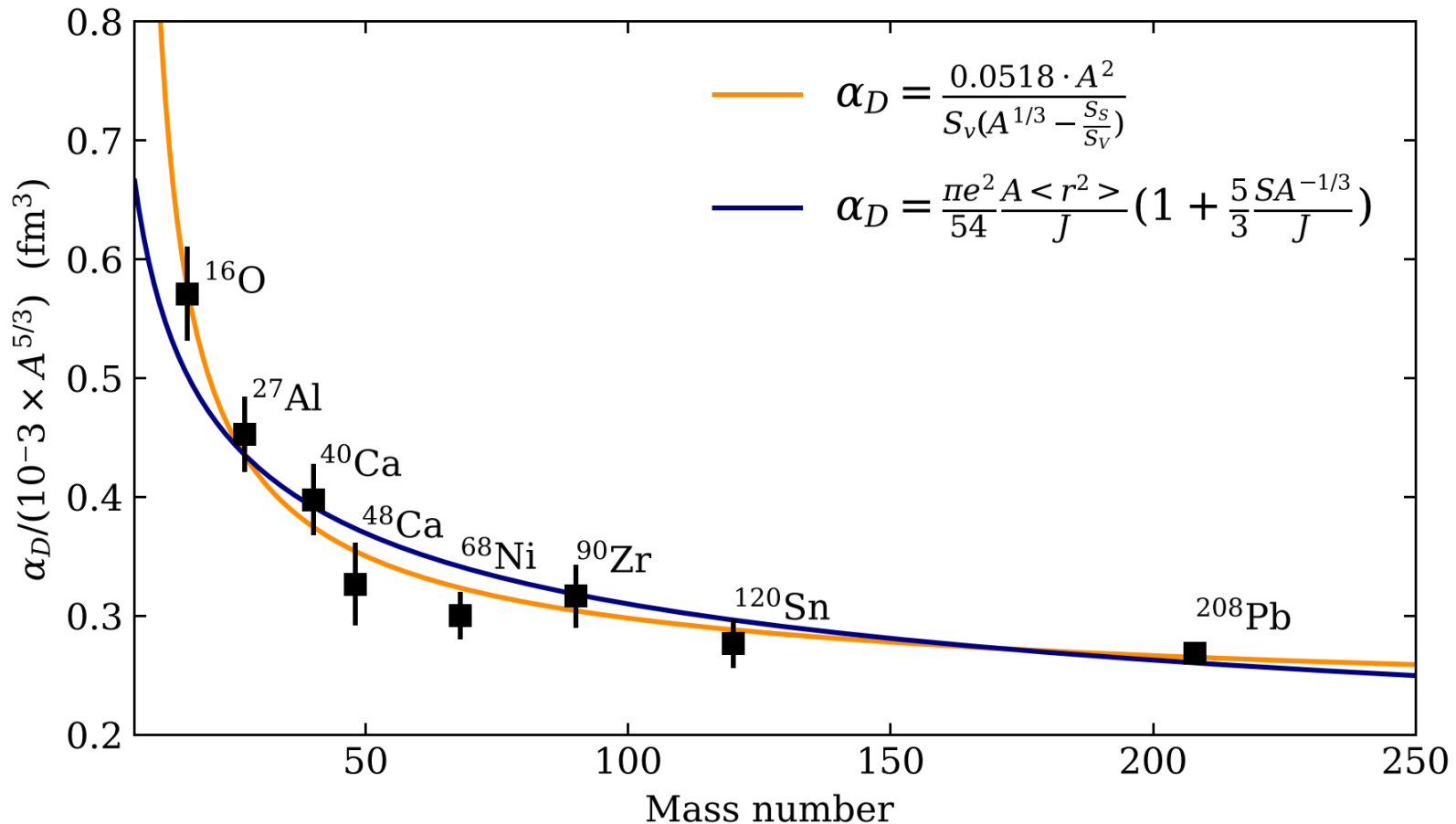
► Refined model:  $a_{\text{sym}}$  mass dependent

$$a_{\text{sym}}(A) = S_v \left( 1 - \frac{\kappa}{A^{1/3}} \right), \quad \kappa = \frac{S_s}{S_v}$$

J. Tian et al., <a href="#">Phys. Rev. C 90, 024313 (2014)</a>	$S_v = 28.3 \text{ MeV}$ $\kappa = 1.27$
(I.) A.W. Steiner et al., <a href="#">Phys. Rep. 411, 325 (2005)</a>	$S_v = 24.1 \text{ MeV}$ $\kappa = 0.545$
(II.) A.W. Steiner et al., <a href="#">Phys. Rep. 411, 325 (2005)</a>	$S_v = 27.3 \text{ MeV}$ $\kappa = 1.68$
Fit	$S_v = 27.3(8) \text{ MeV}$ $\kappa = 1.69(6)$



# Constraints on $J$ and $L$ from Droplet Model



■ Work in progress .....

- Proton scattering at and close to  $0^\circ$  - a versatile experimental tool to extract the polarizability
- Constraints on the symmetry energy from EDFs
  - correlation  $\alpha_D \cdot J \sim L$
  - Systematics dramatically reduce number of suitable interactions
- Constraints on the symmetry energy from  $\chi$ EFT
  - good description for  $^{40,48}\text{Ca}$  and  $^{208}\text{Pb}$
  - $L$  values derived significantly smaller than those derived from PREX
- Constraints on the symmetry energy from systematics
  - volume and surface contributions can be separated
  - relation to  $J$  and  $L$  within the droplet model?

- How important would be results with improved accuracy (in particular in lighter nuclei)?
- Extension of EFT calculations to open-shell nuclei?
- Importance of experiments in very neutron-rich nuclei?



## Special thanks to

Sergej Bassauer, Jonny Birkhan, Isabelle Brandherm  
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