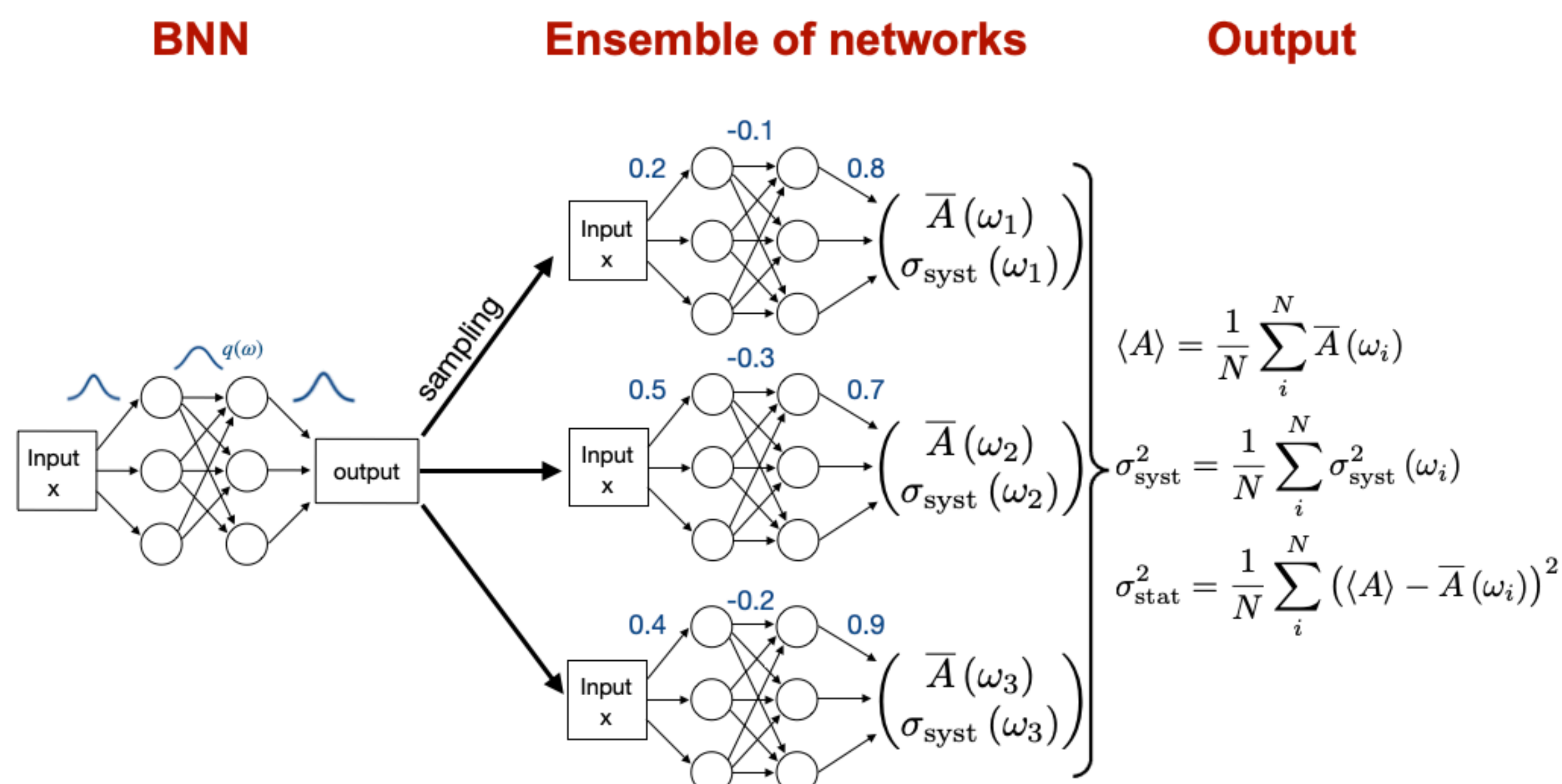
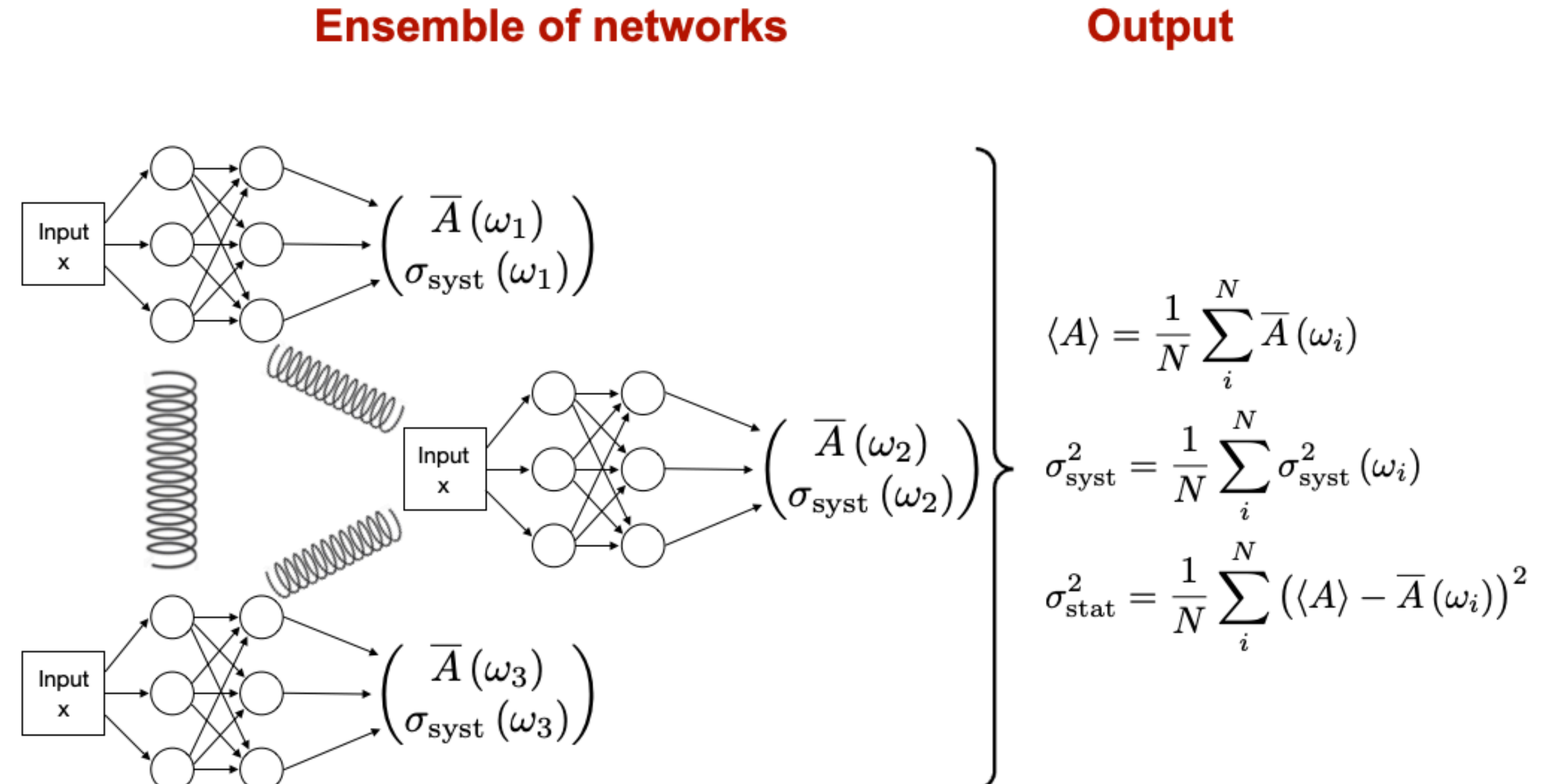


# Learning Uncertainties using Amplitude regression

## Bayesian Neural Network (BNN)



## Repulsive Ensemble (RE)

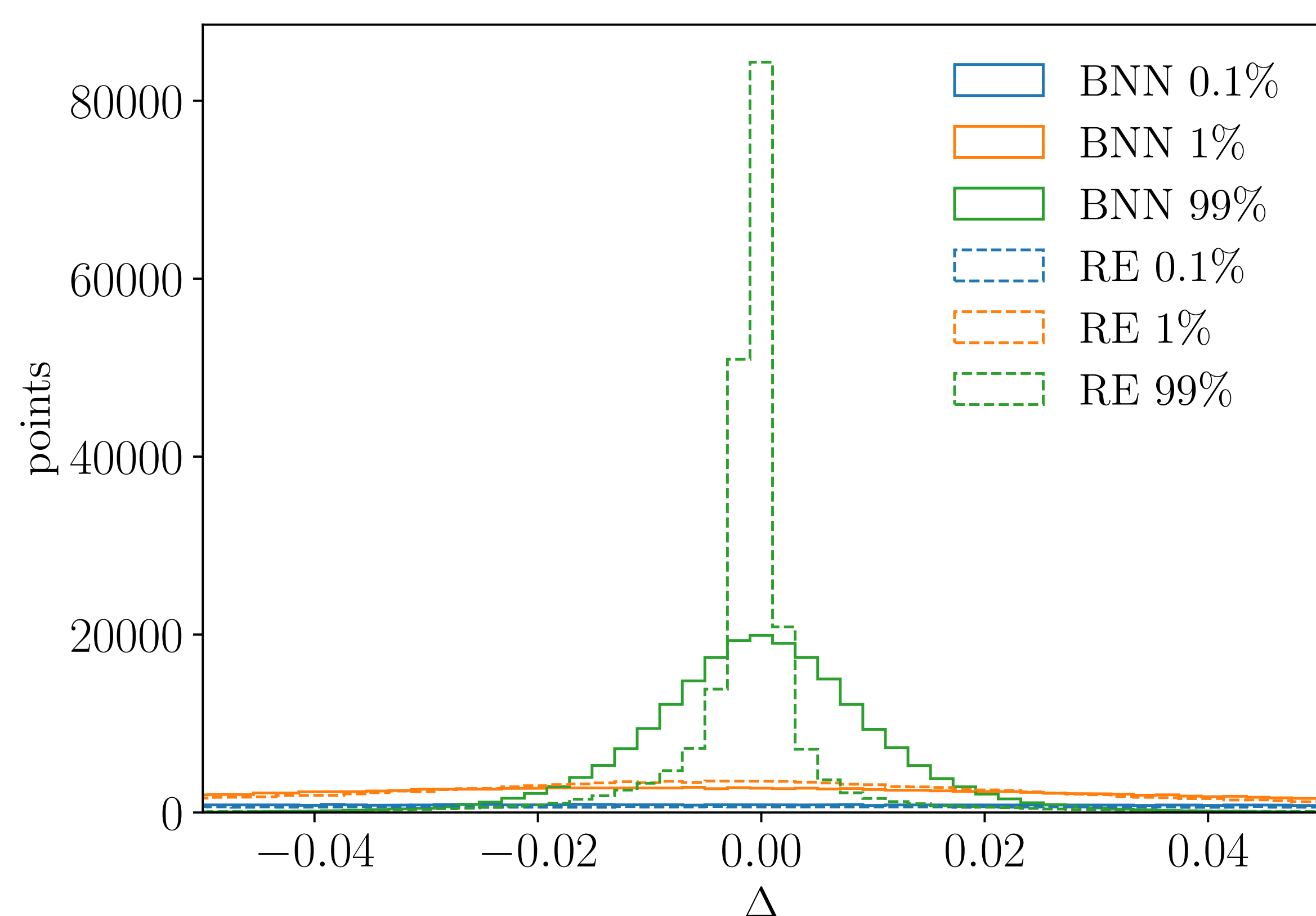
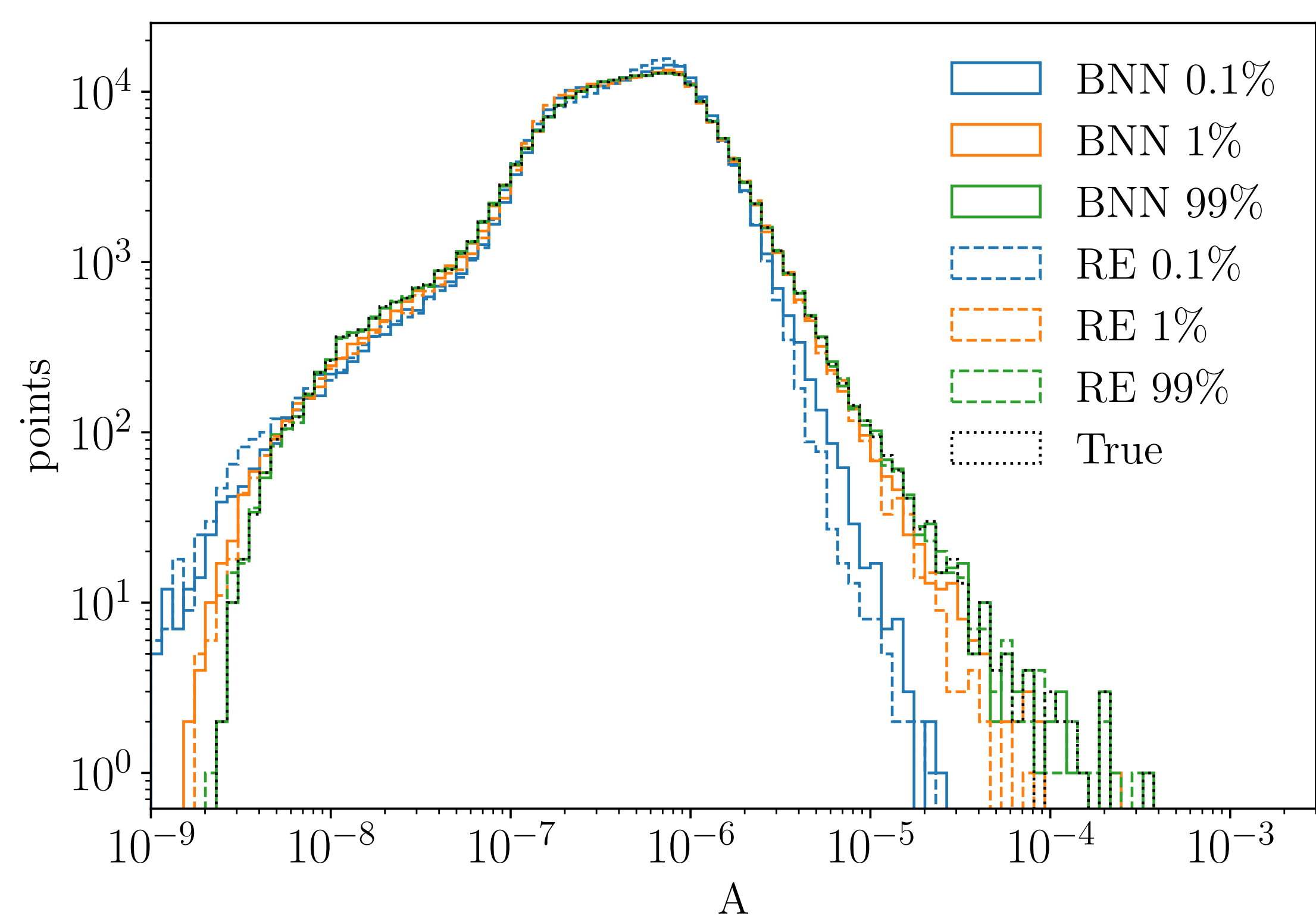


Training: prior **independent**  
uncertainties and mean for different prior widths

$\sigma_{\text{wb}}$	$10^{-2}$	1	1000
mean	$4.63 \cdot 10^{-7}$	$4.64 \cdot 10^{-7}$	$4.63 \cdot 10^{-7}$
$\sigma_{\text{syst}}$	$6.10 \cdot 10^{-8}$	$6.09 \cdot 10^{-8}$	$6.02 \cdot 10^{-8}$
$\sigma_{\text{stat}}$	$4.24 \cdot 10^{-8}$	$4.17 \cdot 10^{-8}$	$4.05 \cdot 10^{-8}$
$\sigma_{\text{tot}}$	$7.48 \cdot 10^{-8}$	$7.45 \cdot 10^{-8}$	$7.33 \cdot 10^{-8}$

Data:

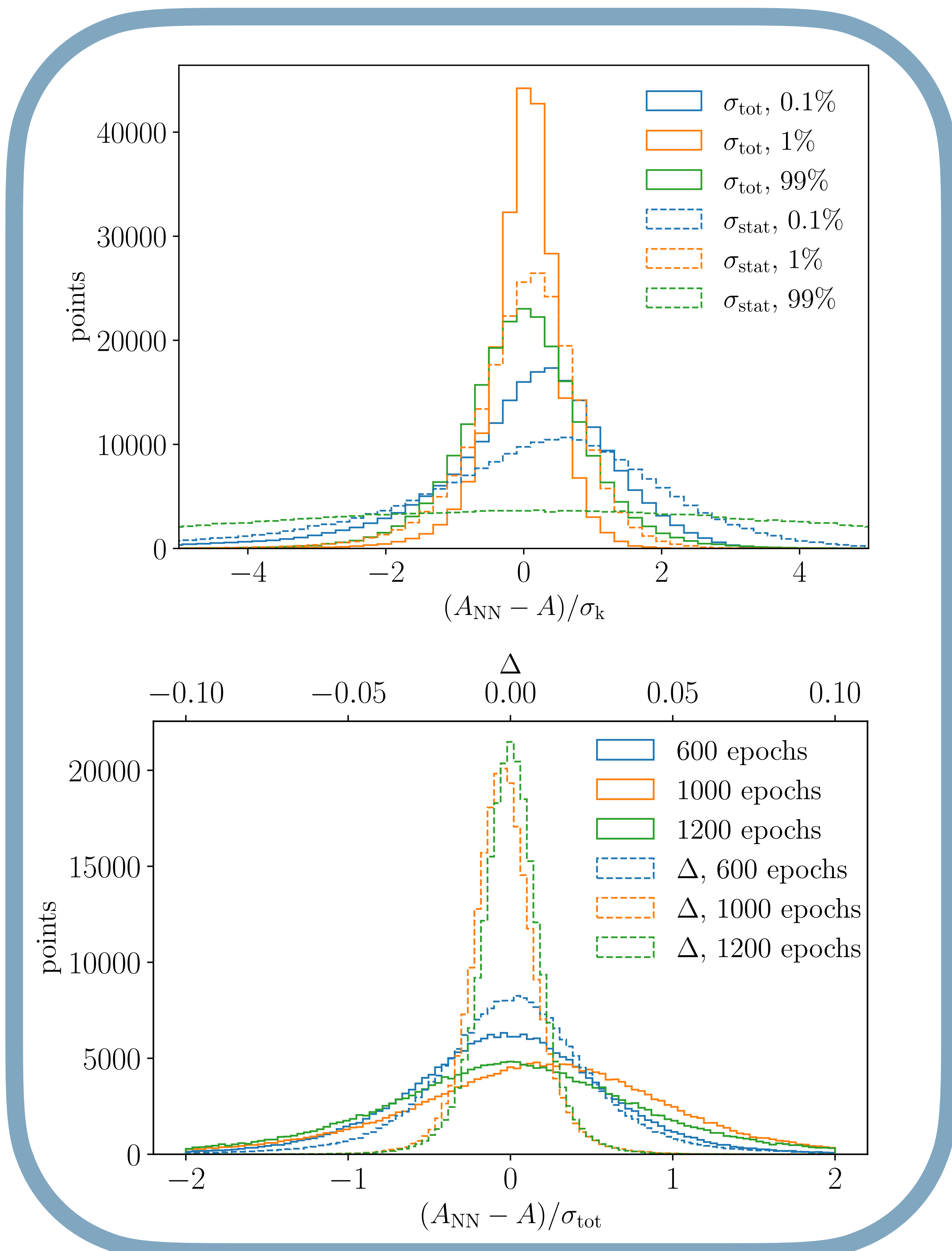
- **Amplitude regression:  $gg \rightarrow \gamma\gamma g$**



comparing BNN and RE for different training sizes  
with  $\Delta = (A - A_{\text{NN}})/A$

Results:

- BNNs with regularization and RE with ensemble training **more efficient** than normal neural net
- small training: good estimation of amplitudes
- BNNs:  $\sigma_{\text{tot}}$ : good estimation,  $\sigma_{\text{stat}}$ : underestimated for large training
- RE: overconfident in uncertainties



both BNN,  $\Delta = (A - A_{\text{NN}})/A$

upper: Pull for different training sizes

lower: 99% training data for various epochs

**IMPRS**

for Precision Tests of  
Fundamental Symmetries  
INTERNATIONAL MAX PLANCK  
RESEARCH SCHOOL



Uncertainty-aware Machine Learning for the LHC

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