

ML in Data Analysis: Systematic Uncertainties with ML

Lecture 4

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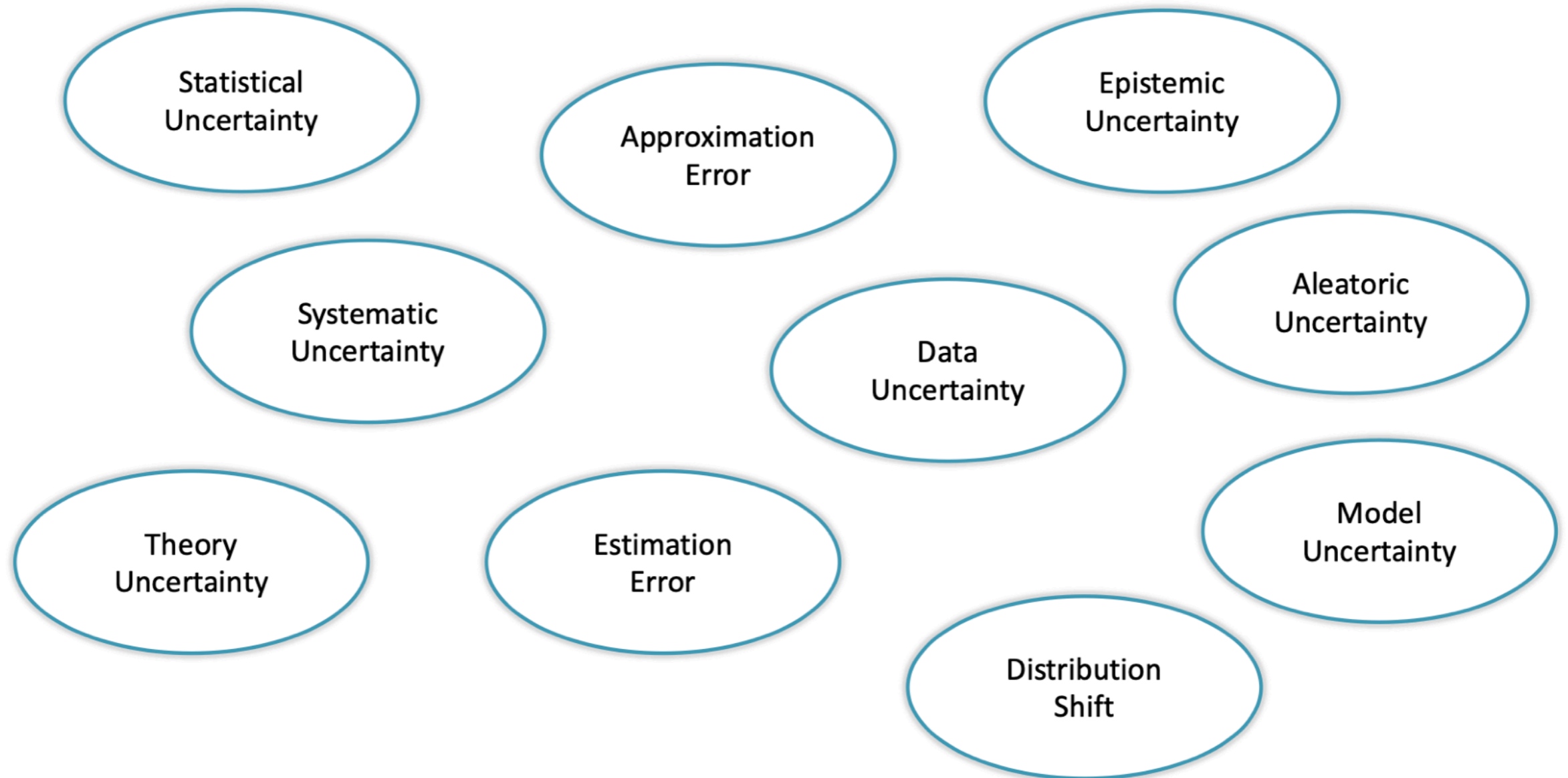
Thematic CERN School of Computing on Machine Learning
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Introduction

Many Terminologies Around Uncertainty

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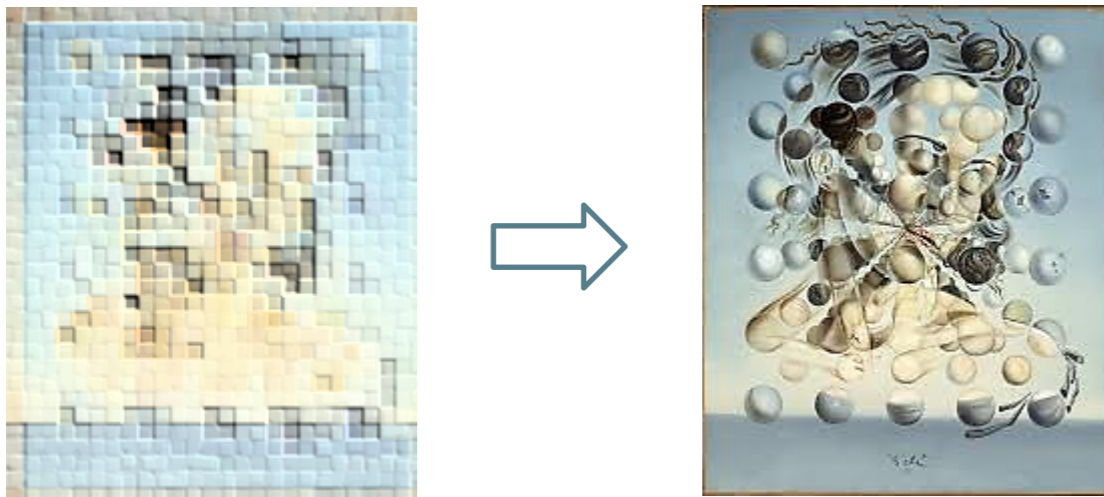
Goal of today's lecture: understand the different concepts and link them together

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Introduction: Why systematics are important?

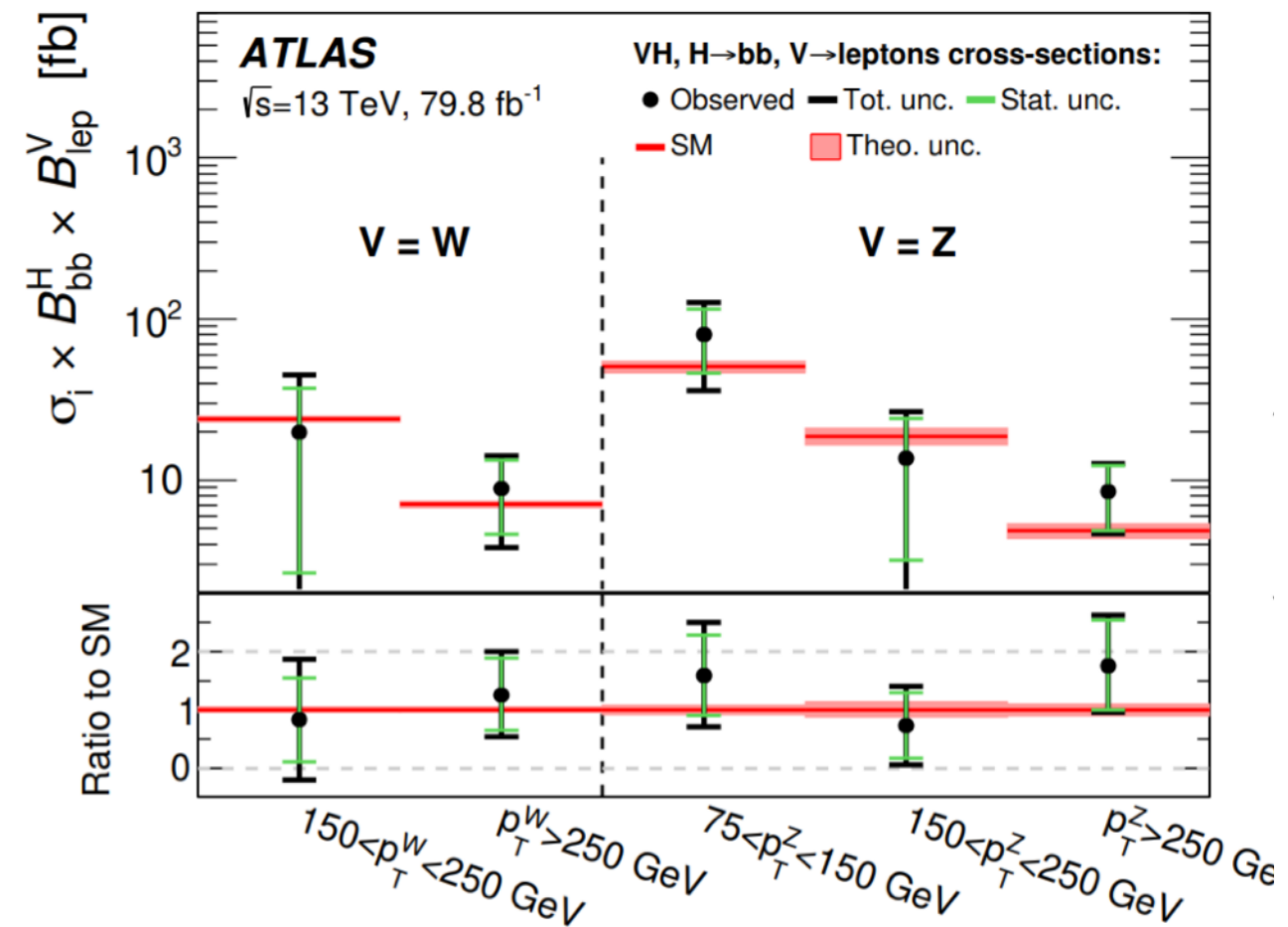
We are entering in a new era:

After the Higgs boson discovery, the focus shifted toward the **measurement of its properties**:



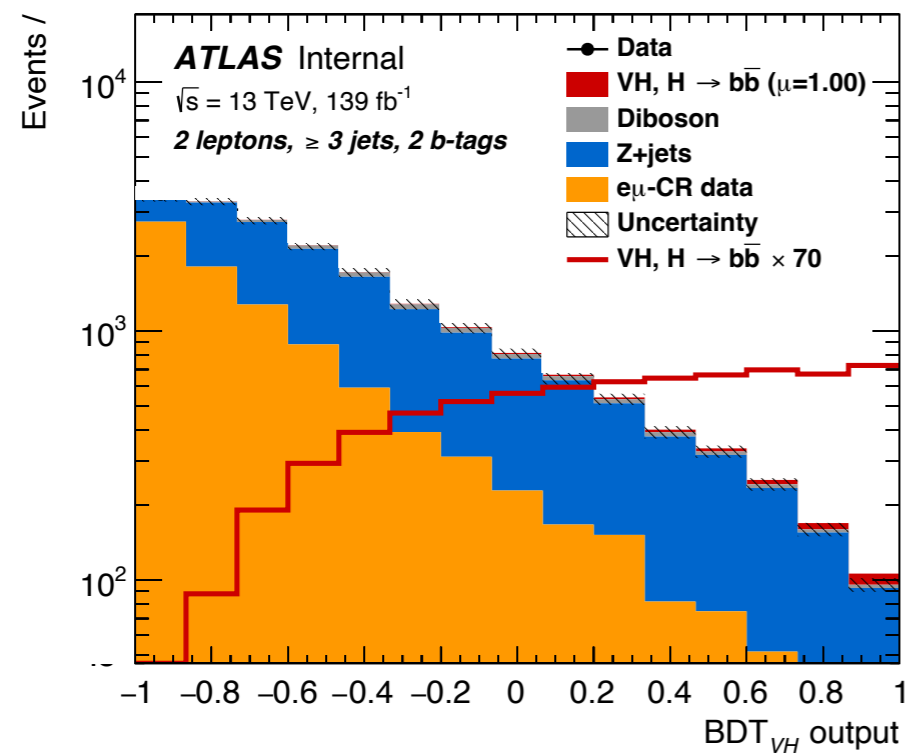
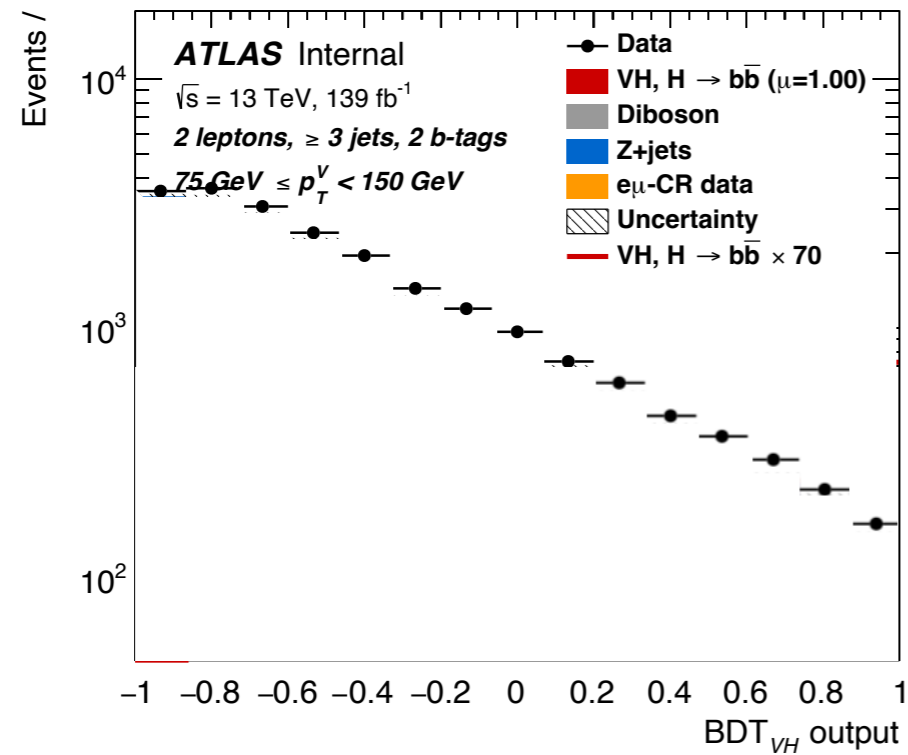
Is this “the Higgs”?

“precise” Higgs measurements → reduce the uncertainties to **increase the sensitivity** to tiny BSM induced anomalies.

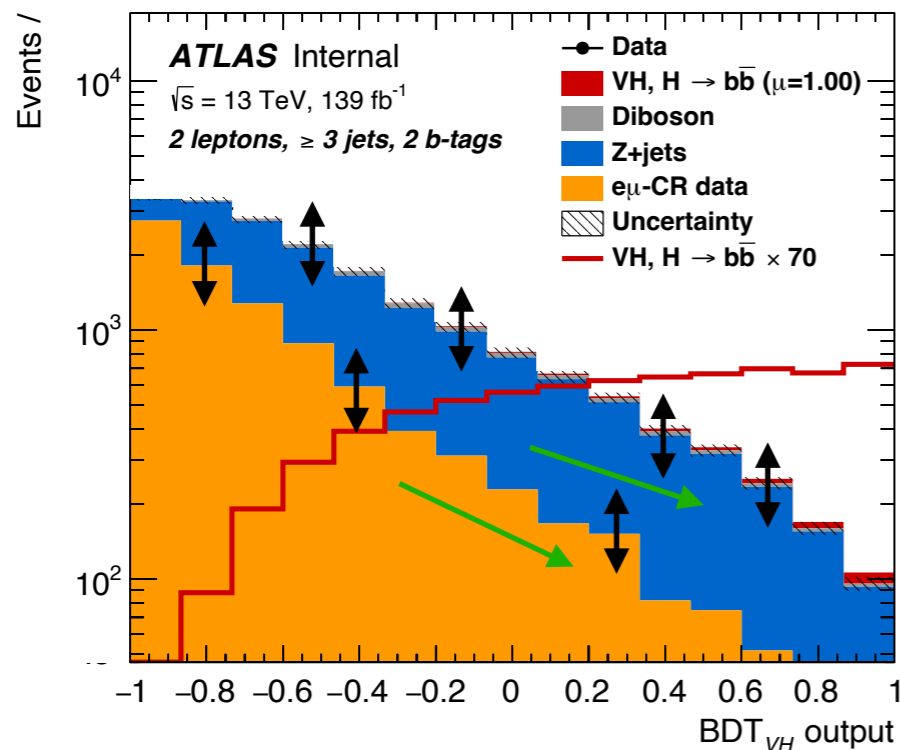
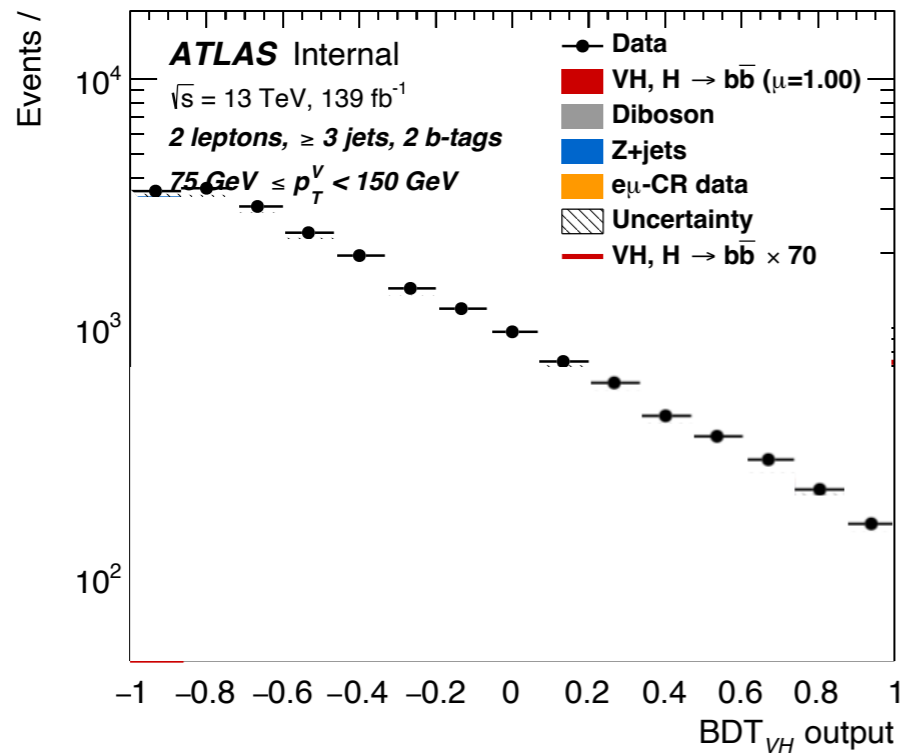


Systematic uncertainties in HEP

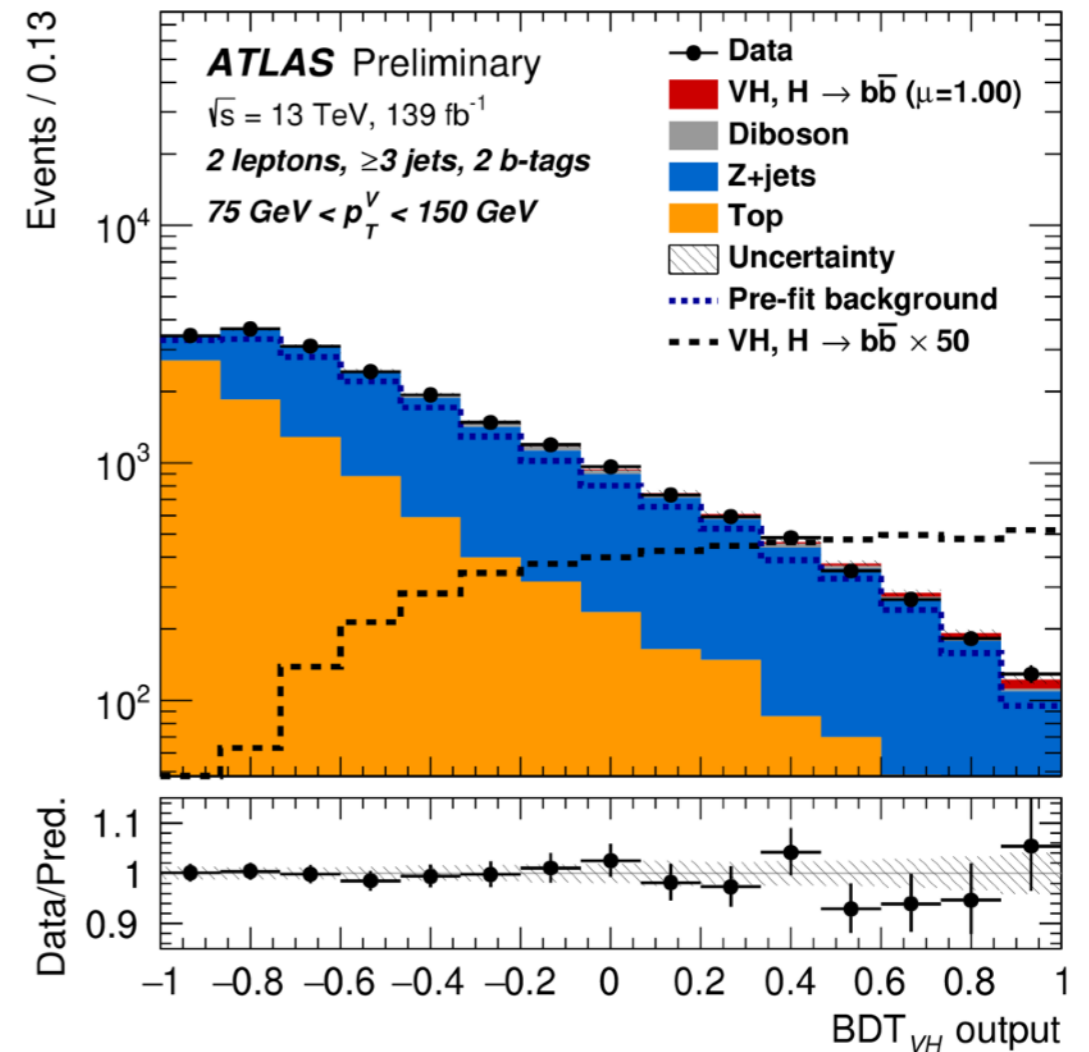
How does a fit (usually) work in HEP?



How does a fit (usually) work in HEP?



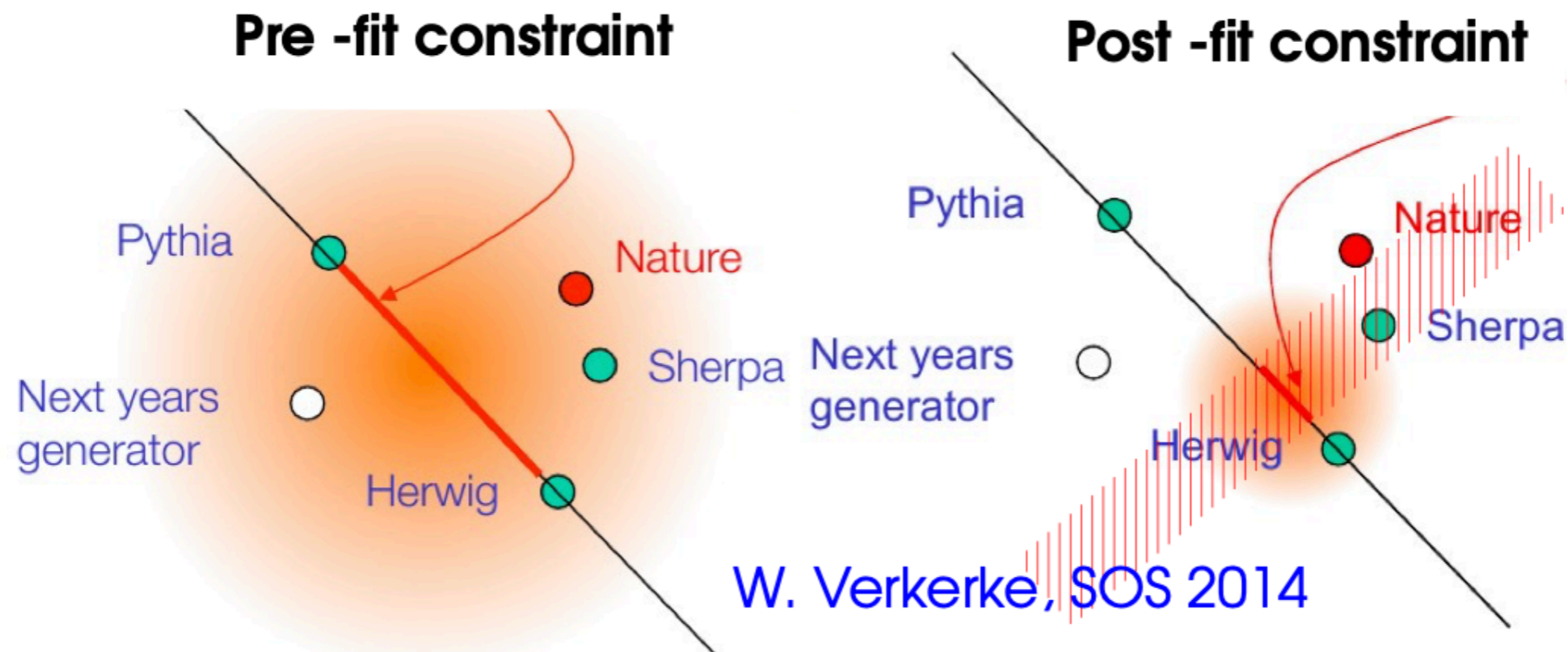
Note: sometimes the Montecarlo can be replaced by a certain function, like for example for $H \rightarrow \gamma\gamma$



Maximise the likelihood
..within some boundaries

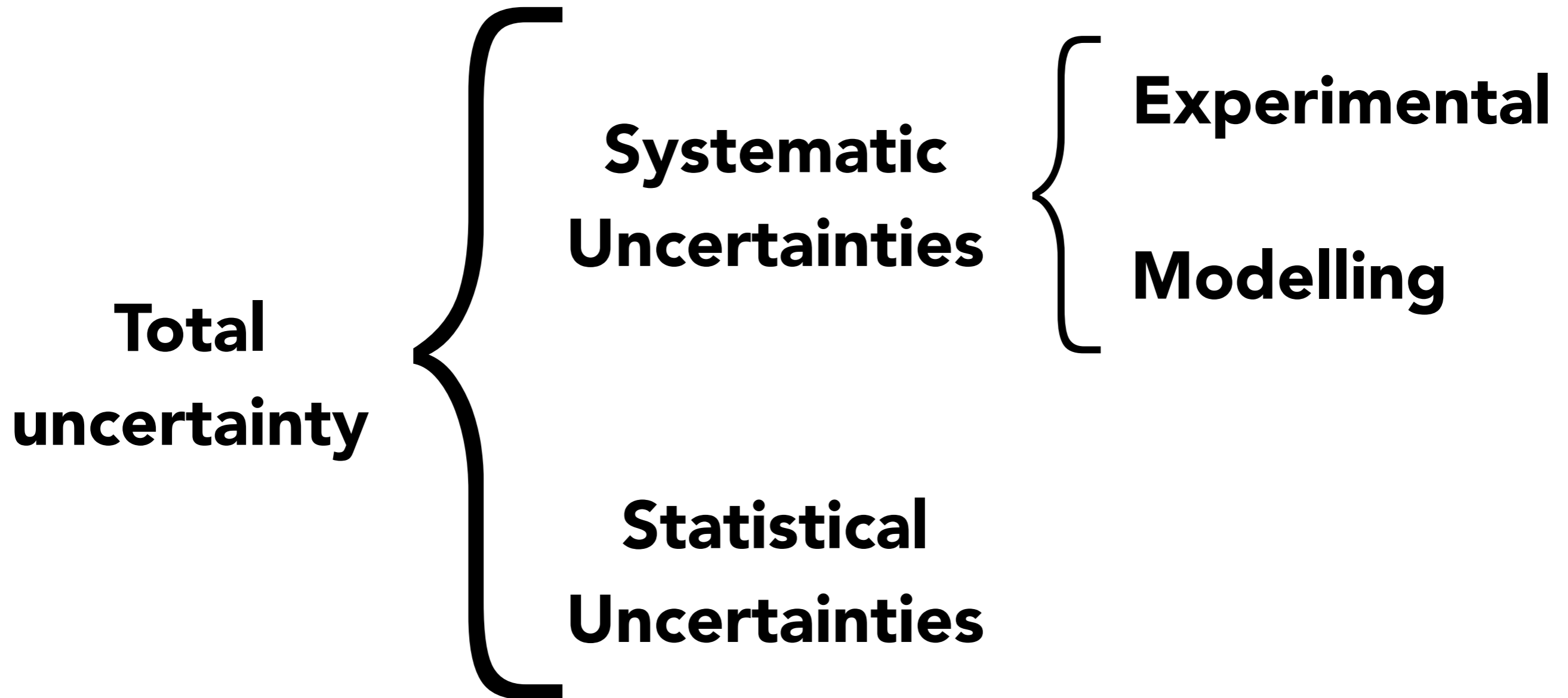
Nuisance parameters

These boundaries are called “nuisance parameters” and define our level of uncertainty on the montecarlo

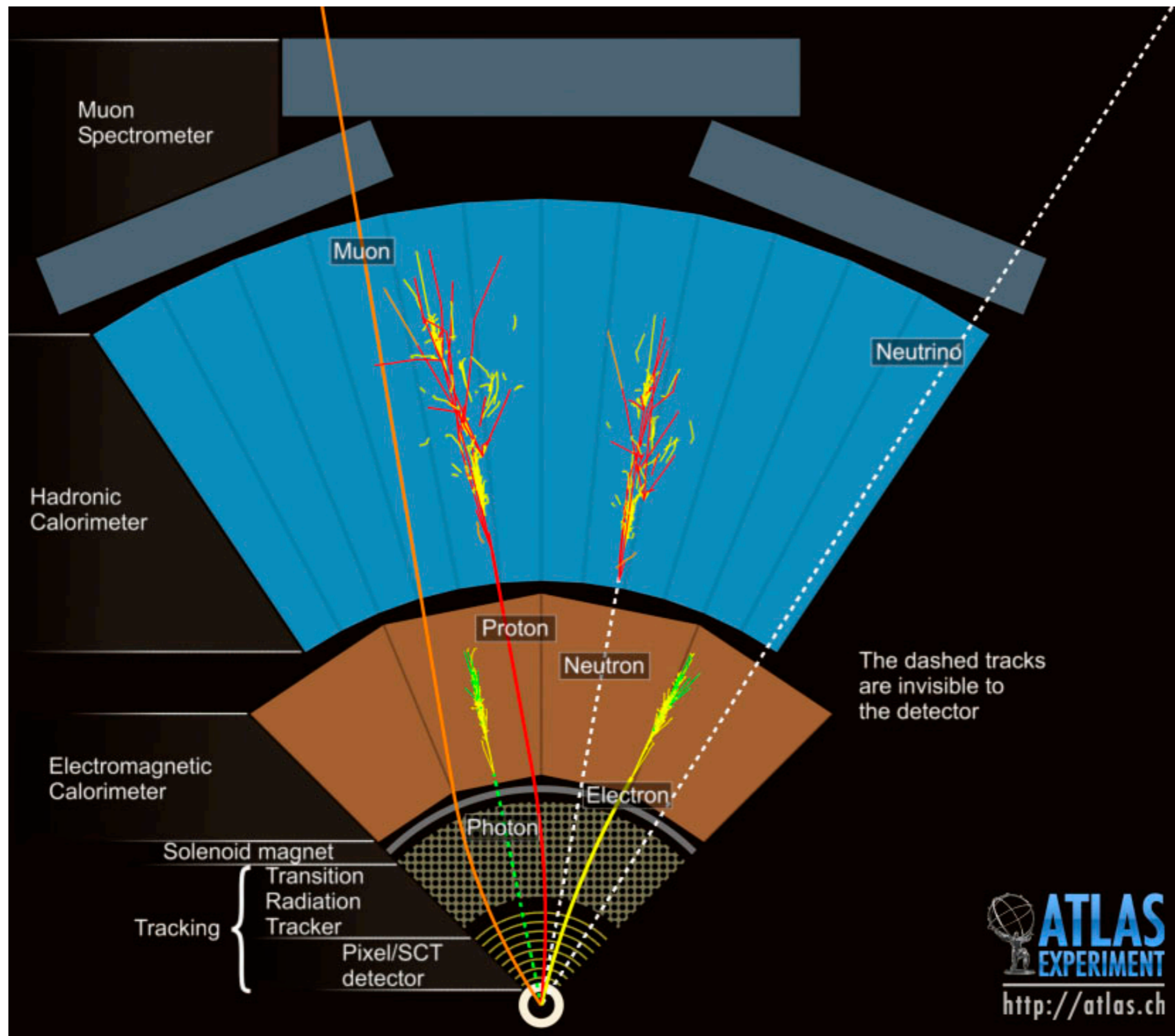


- Account for shape differences
- Account for normalisation effects
- Account for uncertainties in the applied corrections or in the theory
- Account for uncertainties associated with limited data

Types of uncertainty



Experimental uncertainties



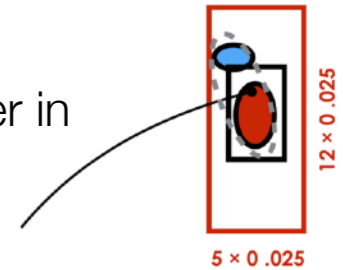
Muons:

Match tracks in the MS and in the ID (combined muons)

$$\chi^2_{match}$$

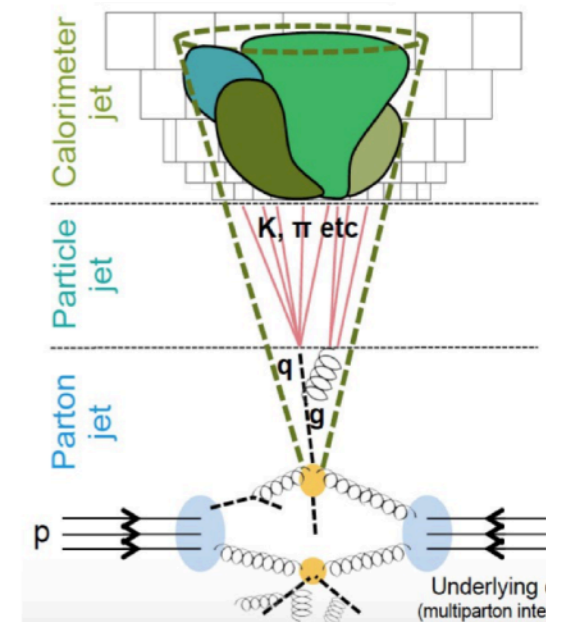
Electrons:

match a cluster in ECAL with an ID track



Jets:

Reconstructed from clusters in the ECAL+HCAL
Anti- k_T algorithm

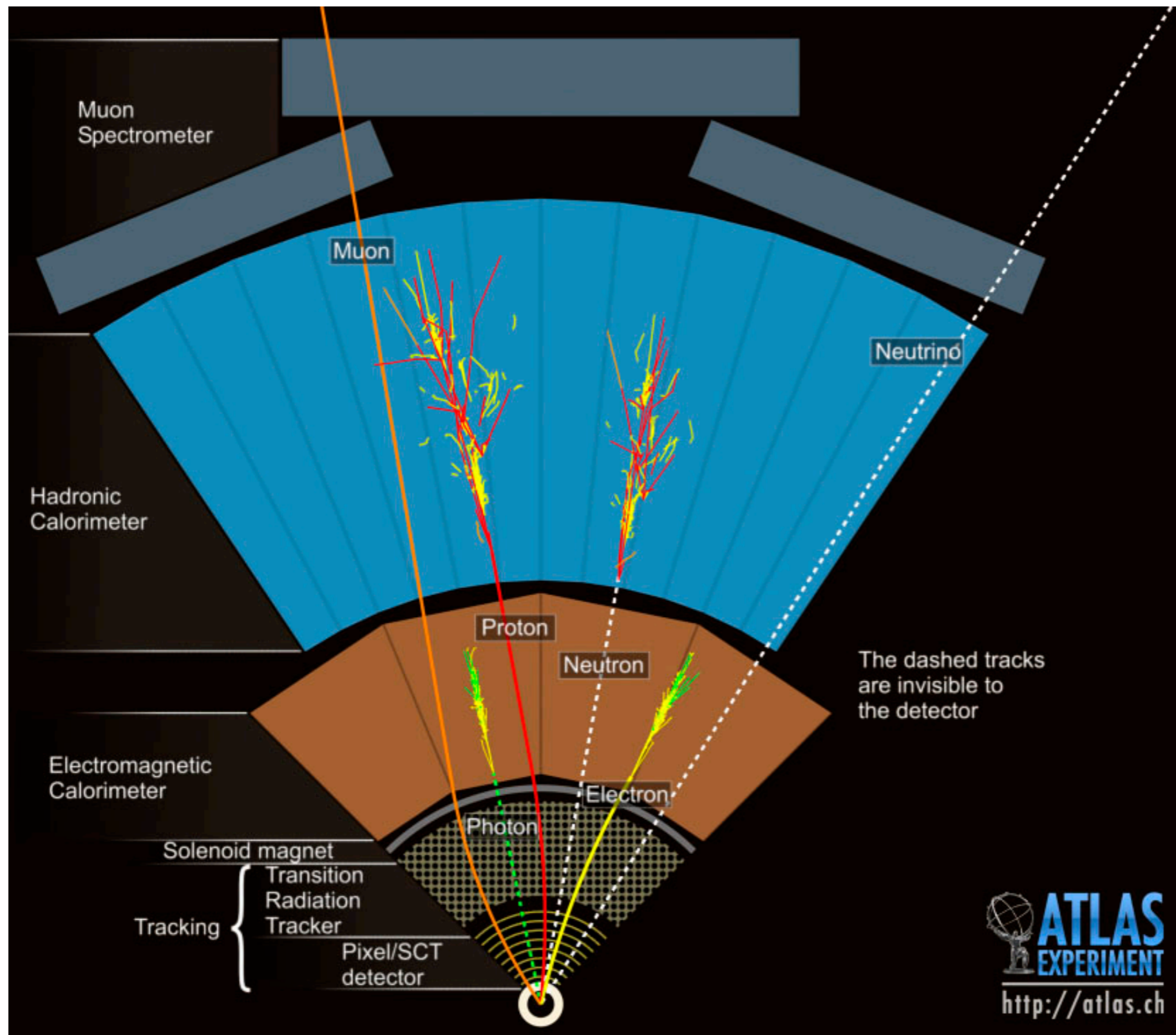


E_T miss:

Missing Transv. Momentum
Momentum imbalance in the transverse plane:

$$\vec{E}_T^{miss} = - \sum_{i \in obj.} \vec{p}_T^i$$

Experimental uncertainties



Some examples:

- Calibrations
- Identification
- Trigger uncertainties

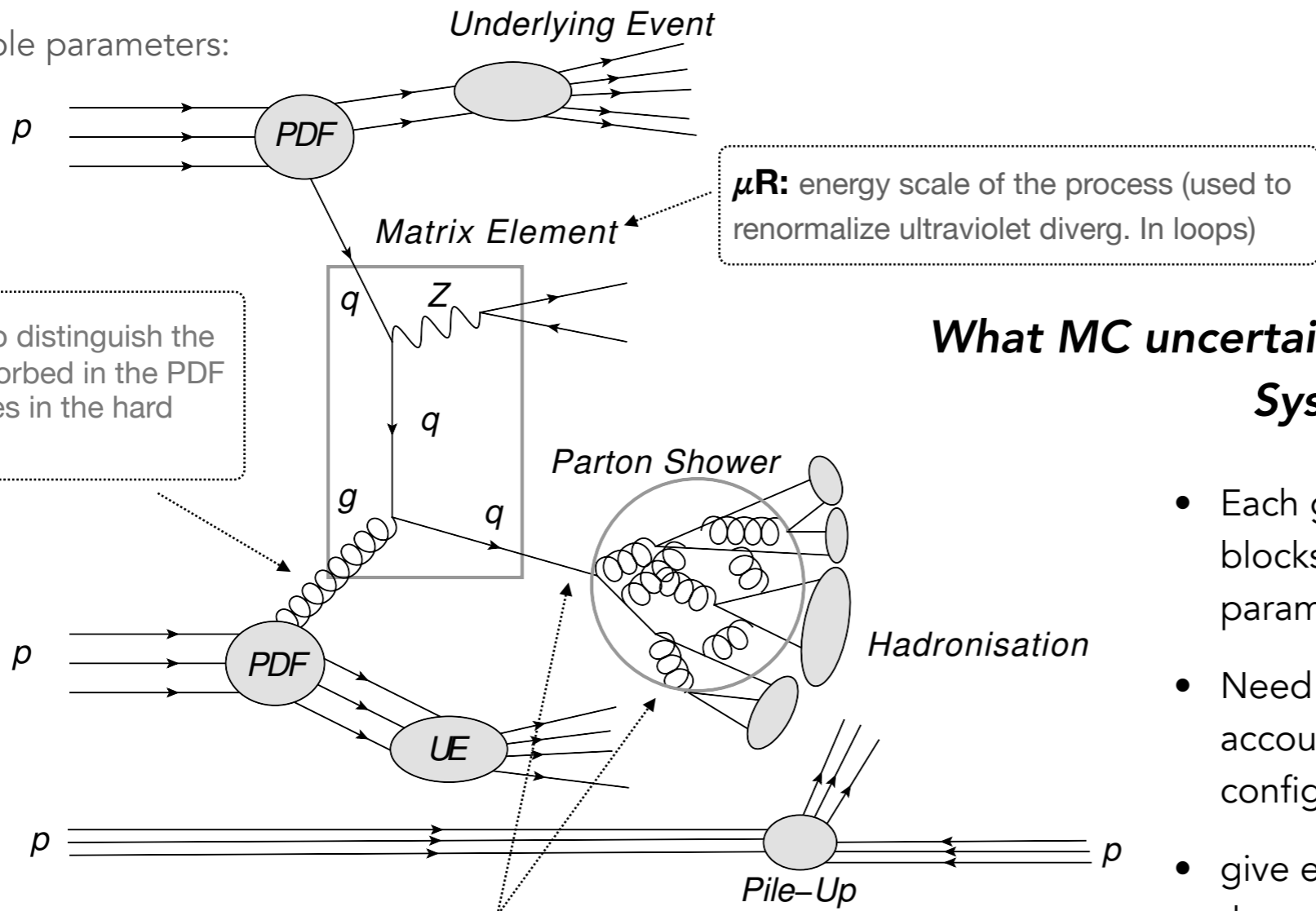
- Jet energy scales
- Flavour tagging

- Energy corrections

Modelling uncertainties

Start building the MC Systematic Model

Configurable parameters:



What MC uncertainties should we consider in our Systematic Model?

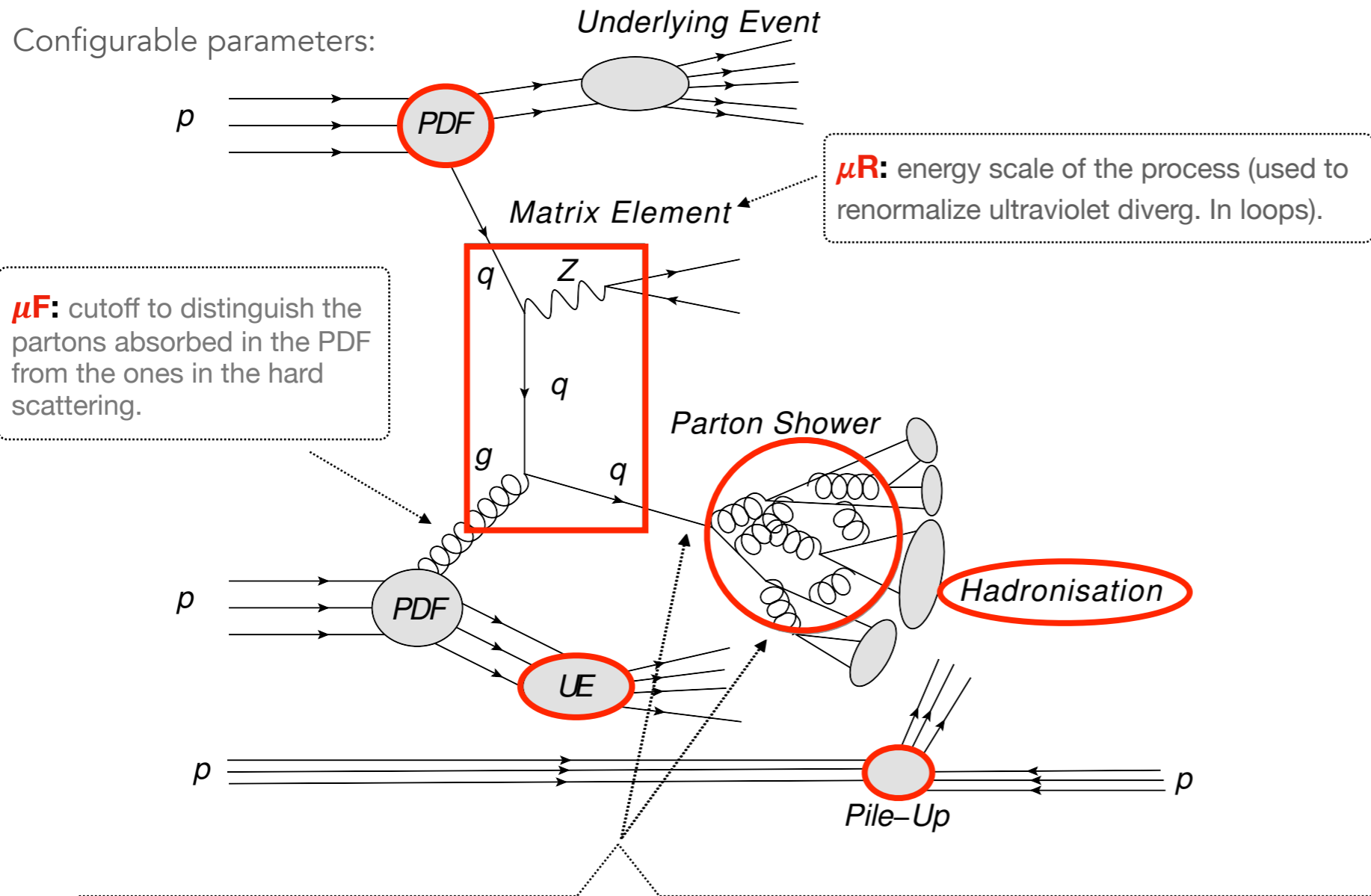
- Each generator is made up of building blocks tuned using an array of configurable parameters.
- Need to build our systematic model to account for the uncertainties on these configurable parameters.
- give enough freedom to the fit to absorb these potential Data/MC differences.

Matrix element matching scale (CKKW): the scale taken for the calculation of the overlap between jets from the matrix element and the parton shower.

Resummation scale (QSF): the scale used for the resummation of soft gluon emissions.

Modelling uncertainties

Start building the MC Systematic Model



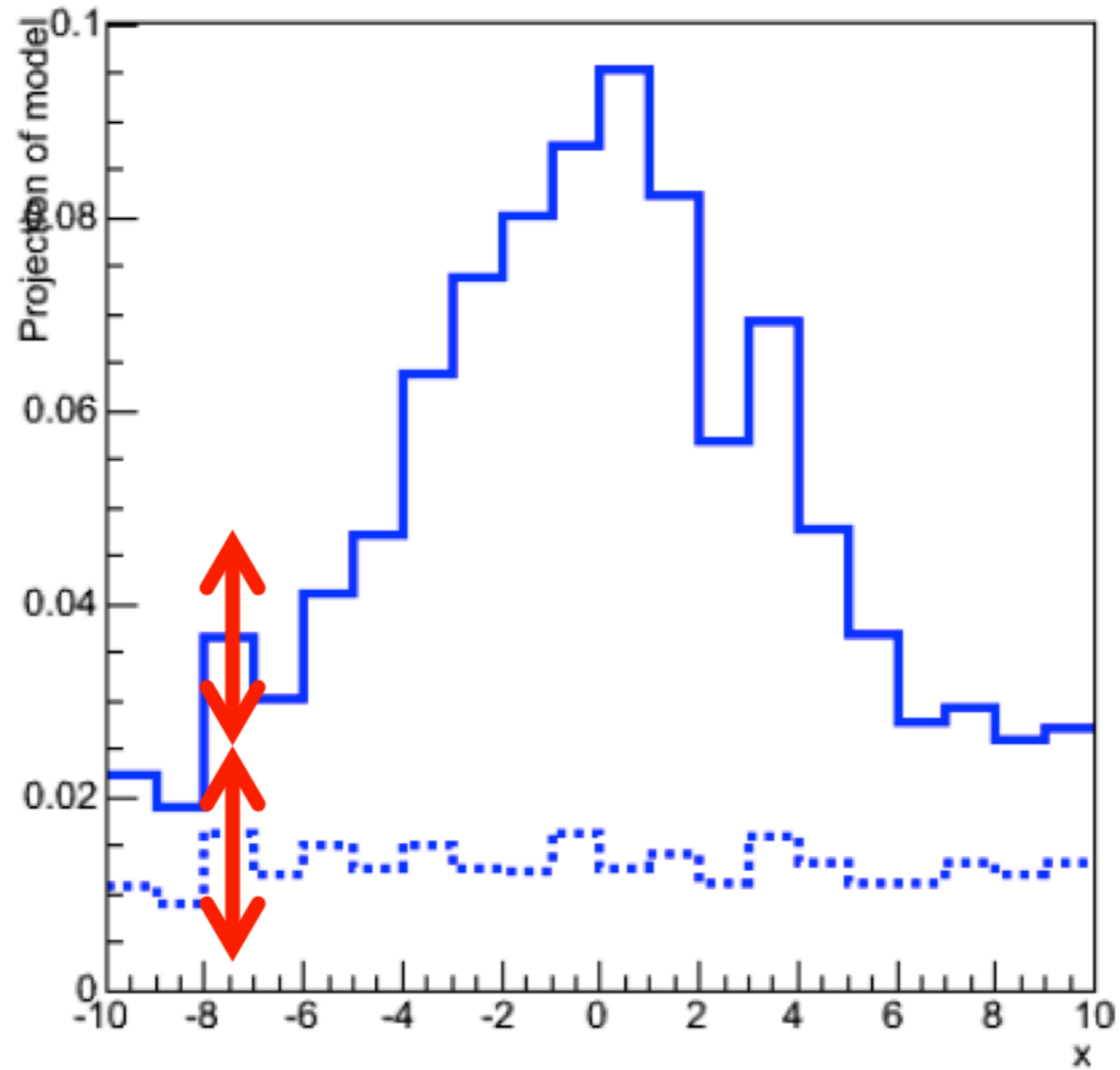
Consider one effect at a time:

- PDF
- Renormalization scale (μ_R)
- Factorisation scale (μ_F)
- Matrix Element
- Parton Shower
- Resummation Scale (QSF)
- CKKW
- Underlying Event
- Pile-up (not covered)
- EW corrections (not covered)
- Radiation High/Low

Matrix element matching scale (CKKW): the scale taken for the calculation of the overlap between jets from the matrix element and the parton shower.

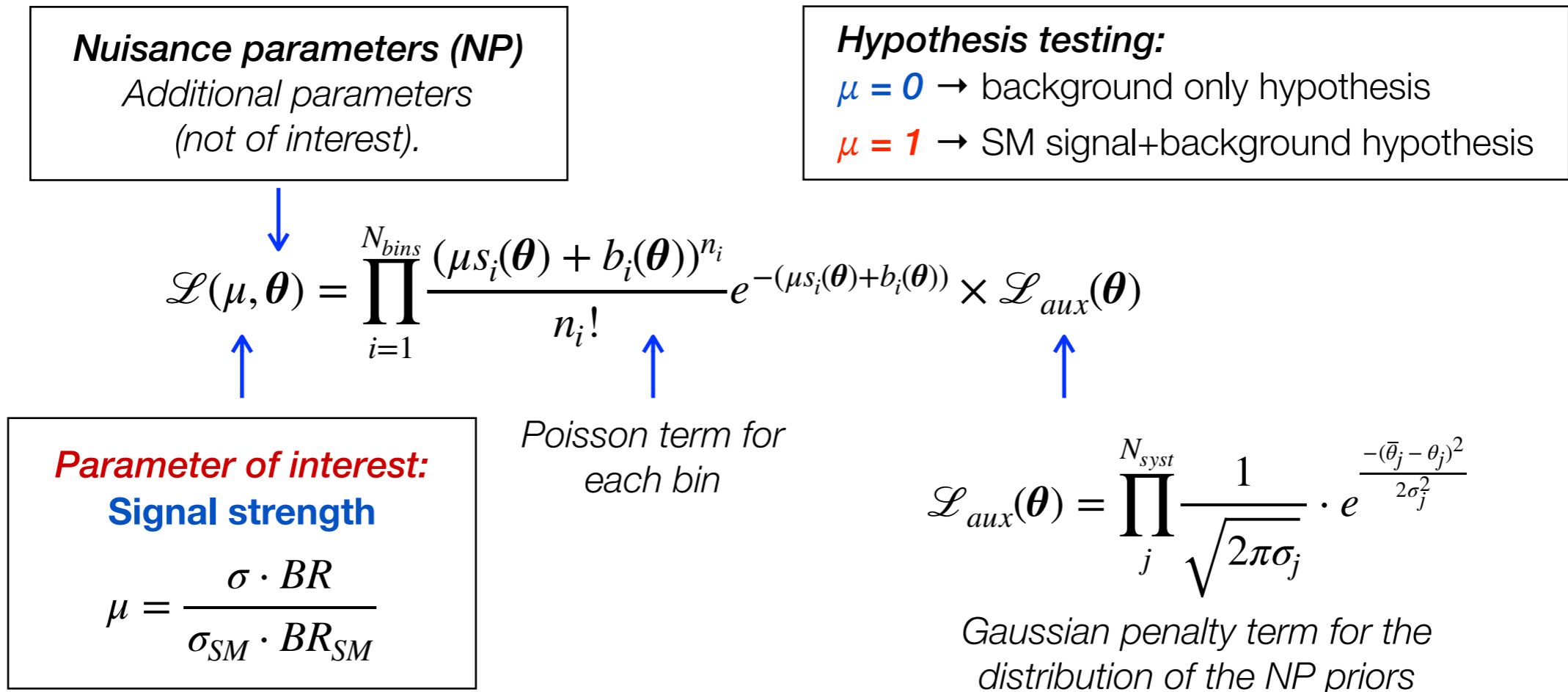
Resummation scale (QSF): the scale used for the resummation of soft gluon emissions.

Statistical uncertainties



The fit model:

Simultaneous binned Likelihood fit built across multiple analysis categories:



Systematic uncertainties are parametrized by **nuisance parameters (NPs)**, constrained with priors:

- ▶ *JES, JER, MET*
- ▶ *Lepton reco, ID, iso, calibration*
- ▶ *b-tagging uncertainties*
- ▶ *Lumi, pile-up*
- ▶ *Shapes and relative normalizations across regions*
- ▶ *Flavor composition uncertainties*
- ▶ *Theory uncertainties: PDF, scales, PS/UE*
- ▶ *...*

A concrete example:

Z + jets	
Z + ll normalisation	18%
Z + cl normalisation	23%
Z + HF normalisation	Floating (2-jet, 3-jet)
Z + bc-to-Z + bb ratio	30 – 40%
Z + cc-to-Z + bb ratio	13 – 15%
Z + bl-to-Z + bb ratio	20 – 25%
0-to-2 lepton ratio	7%
m_{bb}, p_T^V	S
W + jets	
W + ll normalisation	32%
W + cl normalisation	37%
W + HF normalisation	Floating (2-jet, 3-jet)
W + bl-to-W + bb ratio	26% (0-lepton) and 23% (1-lepton)
W + bc-to-W + bb ratio	15% (0-lepton) and 30% (1-lepton)
W + cc-to-W + bb ratio	10% (0-lepton) and 30% (1-lepton)
0-to-1 lepton ratio	5%
W + HF CR to SR ratio	10% (1-lepton)
m_{bb}, p_T^V	S
$t\bar{t}$ (all are uncorrelated between the 0+1- and 2-lepton channels)	
$t\bar{t}$ normalisation	Floating (0+1-lepton, 2-lepton 2-jet, 2-lepton 3-jet)
0-to-1 lepton ratio	8%
2-to-3-jet ratio	9% (0+1-lepton only)
W + HF CR to SR ratio	25%
m_{bb}, p_T^V	S
Single top-quark	
Cross-section	4.6% (<i>s</i> -channel), 4.4% (<i>t</i> -channel), 6.2% (<i>Wt</i>)
Acceptance 2-jet	17% (<i>t</i> -channel), 55% (<i>Wt(bb)</i>), 24% (<i>Wt(other)</i>)
Acceptance 3-jet	20% (<i>t</i> -channel), 51% (<i>Wt(bb)</i>), 21% (<i>Wt(other)</i>)
m_{bb}, p_T^V	S (<i>t</i> -channel, <i>Wt(bb)</i> , <i>Wt(other)</i>)
Multi-jet (1-lepton)	
Normalisation	60 – 100% (2-jet), 90 – 140% (3-jet)
BDT template	S

A concrete example:

Z + jets	
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Z + cl normalisation	23%
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m_{bb}, p_T^V	S

W + jets	
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W + bc-to-W + bb ratio	15% (0-lepton) and 30% (1-lepton)
W + cc-to-W + bb ratio	10% (0-lepton) and 30% (1-lepton)
0-to-1 lepton ratio	5%
W + HF CR to SR ratio	
m_{bb}, p_T^V	

$t\bar{t}$ (all are uncorrelated between)	
$t\bar{t}$ normalisation	Floating
0-to-1 lepton ratio	
2-to-3-jet ratio	
W + HF CR to SR ratio	
m_{bb}, p_T^V	

Single-jet	
Cross-section	4.6%
Acceptance 2-jet	17% (t)
Acceptance 3-jet	20% (t)
m_{bb}, p_T^V	

Multi-jet (1-lepton)	
Normalisation	60 – 100% (2-jet), 90 – 140% (3-jet)
BDT template	S

Signal	
Cross-section (scale)	0.7% (qq), 27% (gg)
Cross-section (PDF)	1.9% (qq → WH), 1.6% (qq → ZH), 5% (gg)
H → b \bar{b} branching fraction	1.7%
Acceptance from scale variations	2.5 – 8.8%
Acceptance from PS/UE variations for 2 or more jets	2.9 – 6.2% (depending on lepton channel)
Acceptance from PS/UE variations for 3 jets	1.8 – 11%
Acceptance from PDF + α_s variations	0.5 – 1.3%
m_{bb}, p_T^V , from scale variations	S
m_{bb}, p_T^V , from PS/UE variations	S
m_{bb}, p_T^V , from PDF + α_s variations	S
p_T^V from NLO EW correction	S

A concrete example:

Z + jets	
Z + ll normalisation	18%
Z + cl normalisation	23%
Z + HF normalisation	Floating (2-jet, 3-jet)
Z + bc-to-Z + bb ratio	30 – 40%
Z + cc-to-Z + bb ratio	13 – 15%
Z + bl-to-Z + bb ratio	20 – 25%
0-to-2 lepton ratio	7%
m_{bb}, p_T^V	S
W + jets	
W + ll normalisation	32%
W + cl normalisation	37%
W + HF normalisation	Floating (2-jet, 3-jet)
W + bl-to-W + bb ratio	26% (0-lepton) and 23% (1-lepton)
W + bc-to-W + bb ratio	15% (0-lepton) and 30% (1-lepton)
W + cc-to-W + bb ratio	10% (0-lepton) and 30% (1-lepton)
0-to-1 lepton ratio	5%
W + HF CR to SR ratio	
m_{bb}, p_T^V	
$t\bar{t}$ (all are uncorrelated between)	
$t\bar{t}$ normalisation	Floating
0-to-1 lepton ratio	
2-to-3-jet ratio	
W + HF CR to SR ratio	
m_{bb}, p_T^V	
	Singl
Cross-section	4.6%
Acceptance 2-jet	17% (t
Acceptance 3-jet	20% (t
m_{bb}, p_T^V	
Multi-jet (1-lepton)	
Normalisation	60 – 100% (2-jet), 90 – 140% (3-jet)
BDT template	S

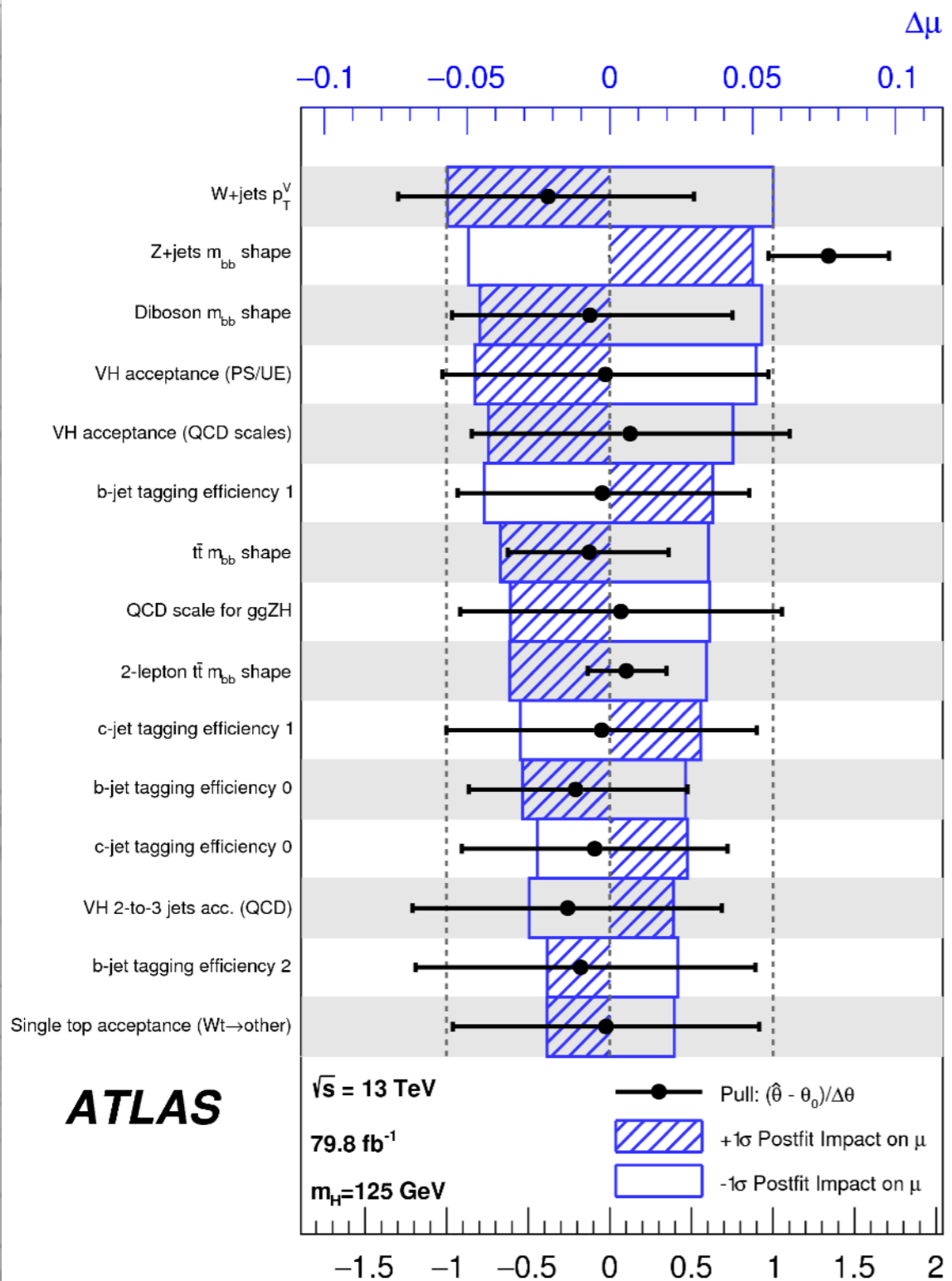
ZZ	
Normalisation	20%
0-to-2 lepton ratio	6%
Acceptance from scale variations	10 – 18%
Acceptance from PS/UE variations for 2 or more jets	6%
Acceptance from PS/UE variations for 3 jets	7% (0-lepton), 3% (2-lepton)
m_{bb}, p_T^V , from scale variations	S (correlated with WZ uncertainties)
m_{bb}, p_T^V , from PS/UE variations	S (correlated with WZ uncertainties)
m_{bb} , from matrix-element variations	S (correlated with WZ uncertainties)
WZ	
Normalisation	26%
0-to-1 lepton ratio	11%
Acceptance from scale variations	13 – 21%
Acceptance from PS/UE variations for 2 or more jets	4%
Acceptance from PS/UE variations for 3 jets	11%
m_{bb}, p_T^V , from scale variations	S (correlated with ZZ uncertainties)
m_{bb}, p_T^V , from PS/UE variations	S (correlated with ZZ uncertainties)
m_{bb} , from matrix-element variations	S (correlated with ZZ uncertainties)
WW	
Normalisation	25%
Acceptance from scale variations	2.9 – 6.2% (depending on lepton channel)
Acceptance from PS/UE variations for 2 or more jets	1.8 – 11%
Acceptance from PS/UE variations for 3 jets	0.5 – 1.3%
Acceptance from PDF + α_s variations	
m_{bb}, p_T^V , from scale variations	S
m_{bb}, p_T^V , from PS/UE variations	S
m_{bb}, p_T^V , from PDF + α_s variations	S
p_T^V from NLO EW correction	S

gg)	
Cross-section (scale)	
Cross-section (PDF)	
H → bb branching fraction	
Acceptance from scale variations	
Acceptance from PS/UE variations for 2 or more jets	
Acceptance from PS/UE variations for 3 jets	
Acceptance from PDF + α_s variations	
m_{bb}, p_T^V , from scale variations	S
m_{bb}, p_T^V , from PS/UE variations	S
m_{bb}, p_T^V , from PDF + α_s variations	S
p_T^V from NLO EW correction	S

A concrete example:

Z + jets		Source of uncertainty		σ_μ
Z + ll normalisation	18%	Total		0.259
Z + cl normalisation	23%	Statistical		0.161
Z + HF normalisation	Floating (2-jet, 3-jet)	Systematic		0.203
Z + bc-to-Z + bb ratio	30 – 40%	Experimental uncertainties		
Z + cc-to-Z + bb ratio	13 – 15%	Jets		0.035
Z + bl-to-Z + bb ratio	20 – 25%	E_T^{miss}		0.014
0-to-2 lepton ratio	7%	Leptons		0.009
m_{bb}, p_T^V	S	b-tagging	b-jets	0.061
W + jets			c-jets	0.042
W + ll normalisation	32%		light-flavour jets	0.009
W + cl normalisation	37%		extrapolation	0.008
W + HF normalisation	Floating (2-jet, 3-jet)	Pile-up		0.007
W + bl-to-W + bb ratio	26% (0-lepton) and 23% (1-lepton)	Luminosity		0.023
W + bc-to-W + bb ratio	15% (0-lepton) and 30% (1-lepton)	Theoretical and modelling uncertainties		
W + cc-to-W + bb ratio	10% (0-lepton) and 30% (1-lepton)	Signal		0.094
0-to-1 lepton ratio	5%	Floating normalisations		0.035
W + HF CR to SR ratio		Z + jets		0.055
m_{bb}, p_T^V		W + jets		0.060
$t\bar{t}$ (all are uncorrelated between)		$t\bar{t}$		0.050
$t\bar{t}$ normalisation	Floating	Single top quark		0.028
0-to-1 lepton ratio		Diboson		0.054
2-to-3-jet ratio		Multi-jet		0.005
W + HF CR to SR ratio		MC statistical		0.070
m_{bb}, p_T^V				
Single-jet (1-lepton)				
Cross-section	4.6%			
Acceptance 2-jet	17% ($t\bar{t}$)			
Acceptance 3-jet	20% ($t\bar{t}$)			
m_{bb}, p_T^V				
Multi-jet (1-lepton)				
Normalisation	60 – 100% (2-jet), 90 – 140% (3-jet)			
BDT template	S			

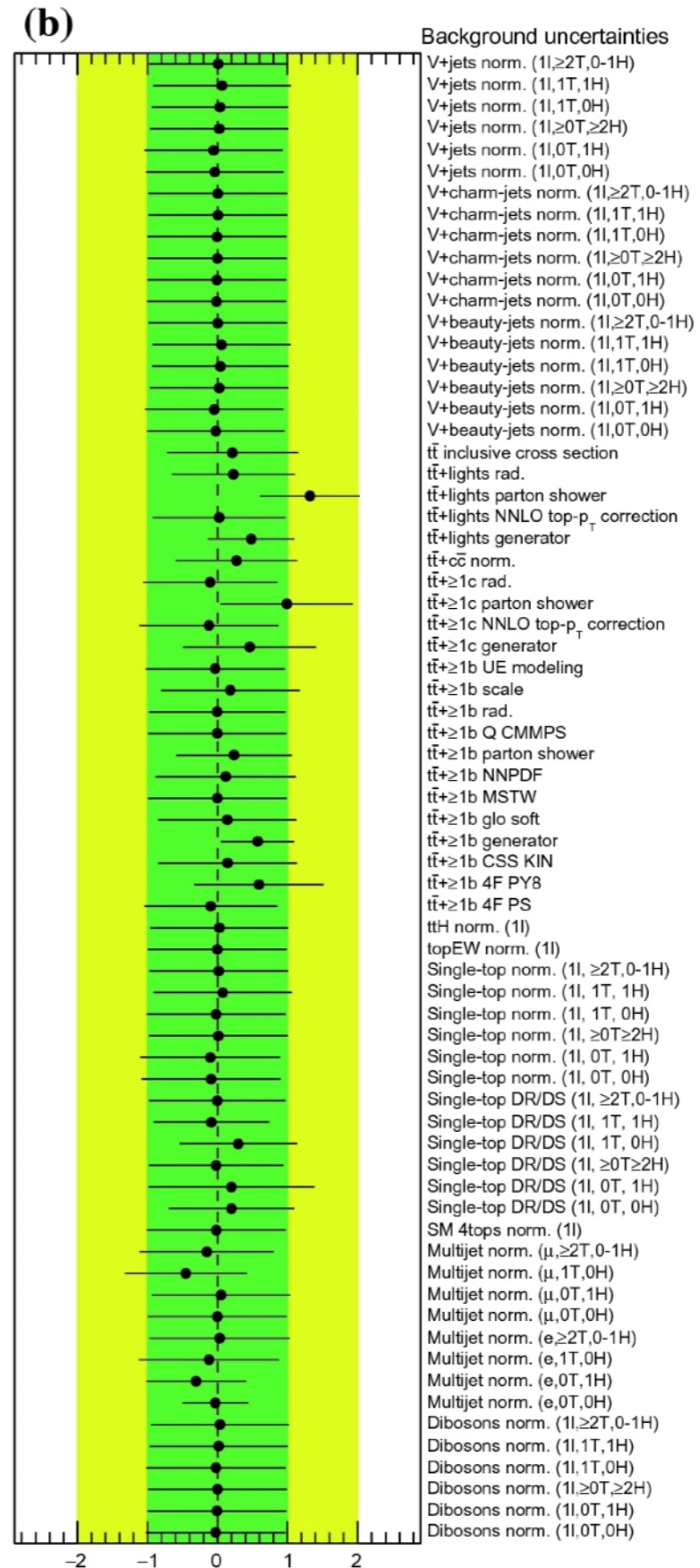
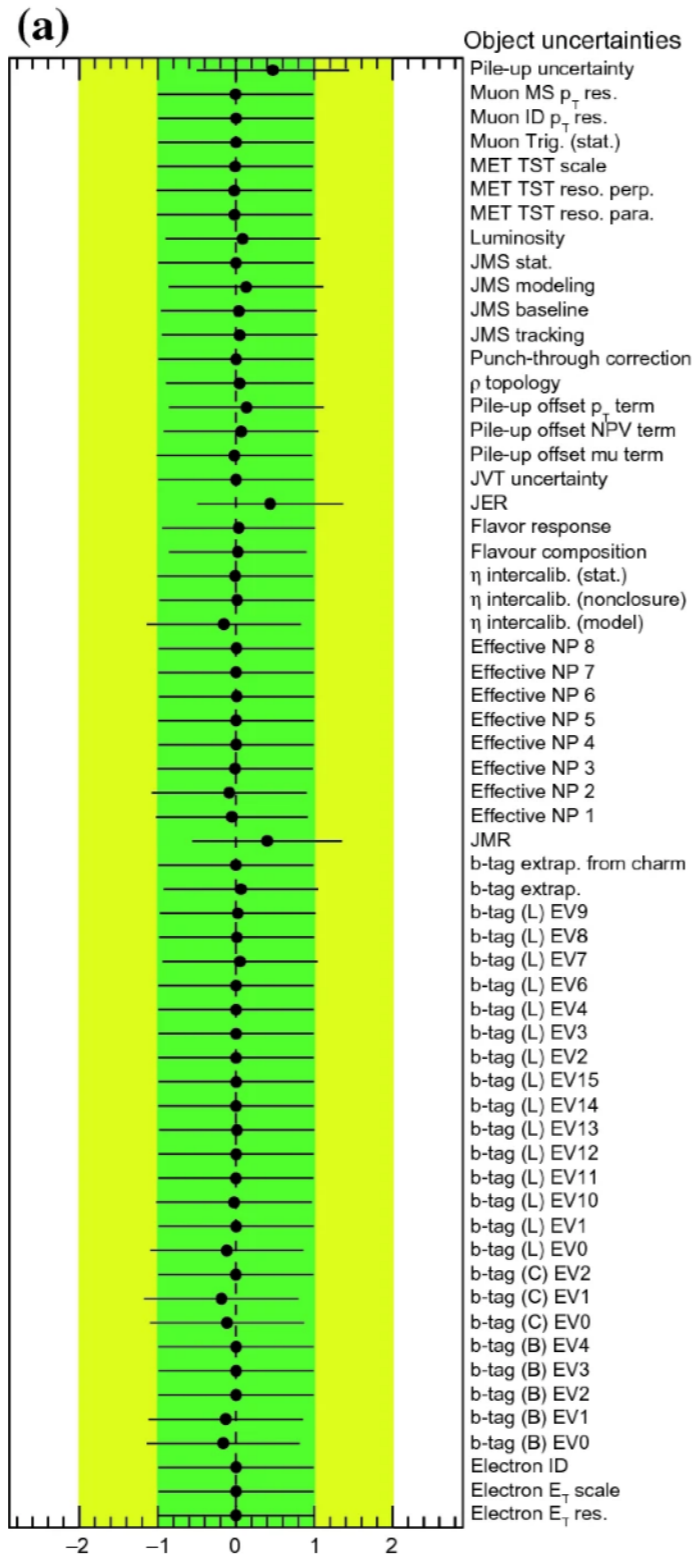
A concrete example:



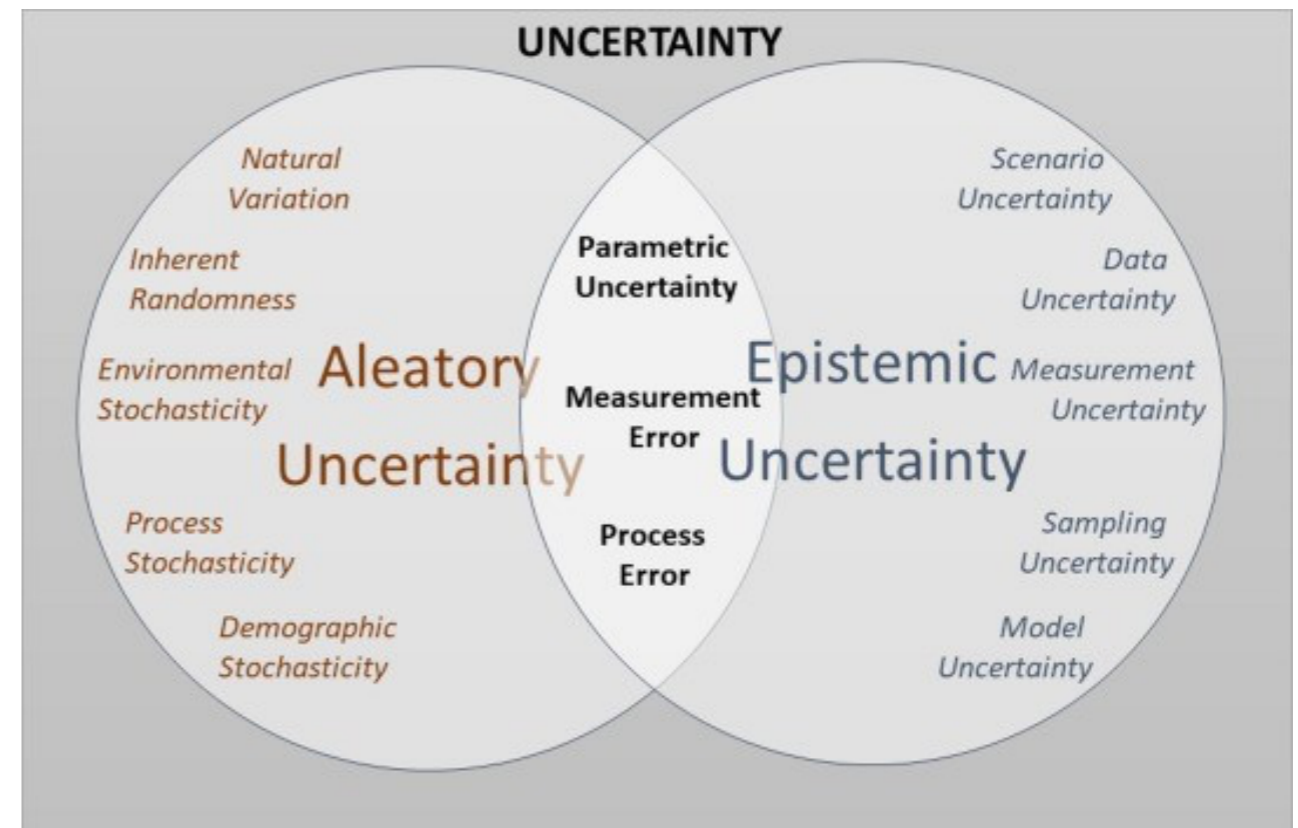
Source of uncertainty	σ_μ	
Total	0.259	
Statistical	0.161	
Systematic	0.203	
Experimental uncertainties		
Jets	0.035	
E_T^{miss}	0.014	
Leptons	0.009	
b -tagging	b -jets	0.061
	c -jets	0.042
	light-flavour jets	0.009
	extrapolation	0.008
Pile-up	0.007	
Luminosity	0.023	
Theoretical and modelling uncertainties		
Signal	0.094	
Floating normalisations		
$Z + \text{jets}$	0.055	
$W + \text{jets}$	0.060	
$t\bar{t}$	0.050	
Single top quark	0.028	
Diboson	0.054	
Multi-jet	0.005	
MC statistical	0.070	

A concrete example:

The "pull plot"



Uncertainties in Machine Learning



Introduction

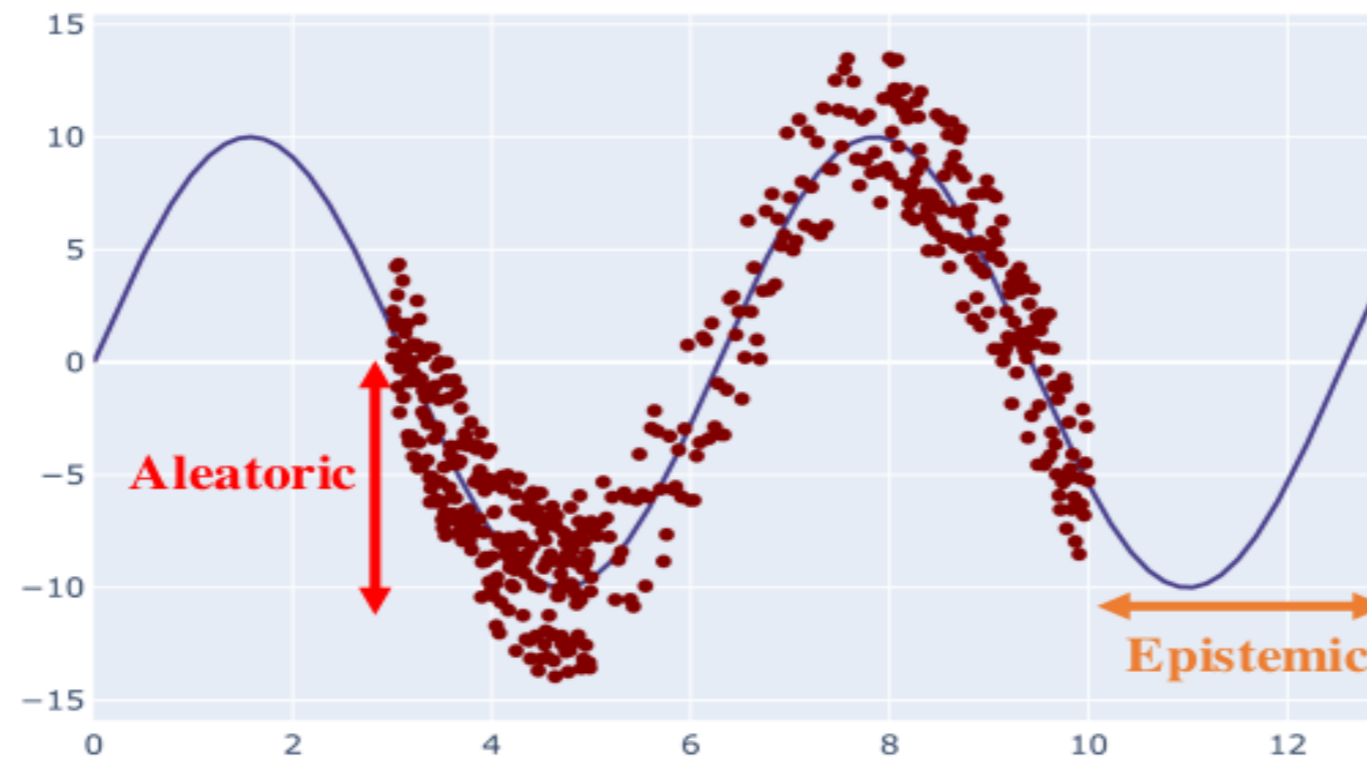
Let x an input point, f_ω a predictive model with parameters ω

Objective: Quantifying the uncertainty on the prediction $f_\omega(x)$

Predictive uncertainty

Aleatoric uncertainty
Uncertainty related to the data

Epistemic uncertainty
Uncertainty related to the model



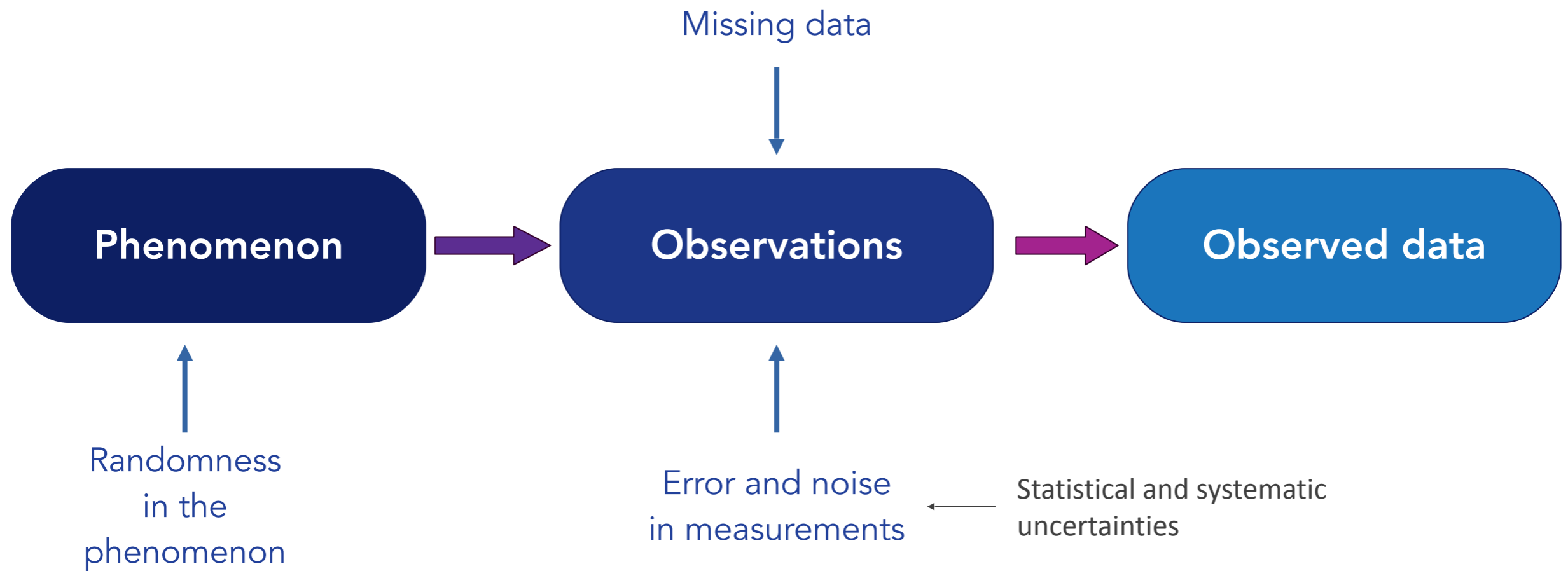
Representation of the total predictive uncertainty by a probability distribution

$$p(y^* | x, D) = \int_{\omega} \underbrace{p(y^* | x, \omega)}_{\text{Aleatoric}} \underbrace{p(\omega | D)}_{\text{Epistemic}} d\omega$$

x : input data point
 ω : model parameters
 y^* : possible output
 D : Training dataset

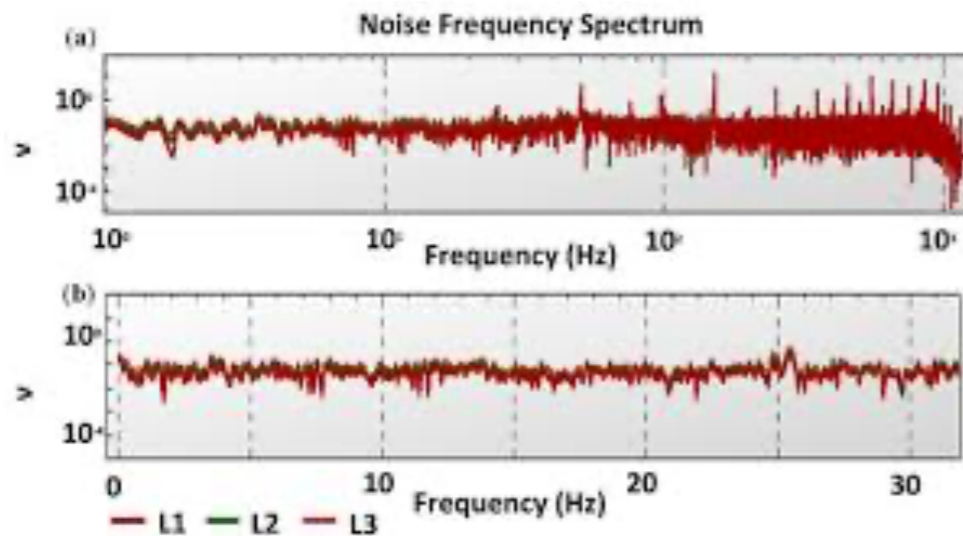
Aleatoric uncertainties

Uncertainty intrinsic within the data, irreducible by improving the model or increasing the dataset
**A larger dataset does not reduce aleatoric uncertainty,
but it helps to give a better estimation!**

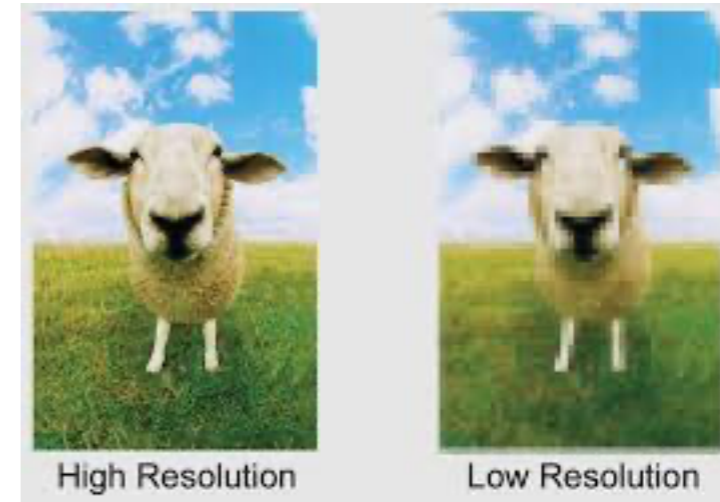


We can reduce the aleatoric uncertainty **by improving the measurement (reducing the error or noise)** for instance.

Aleatoric uncertainties: examples



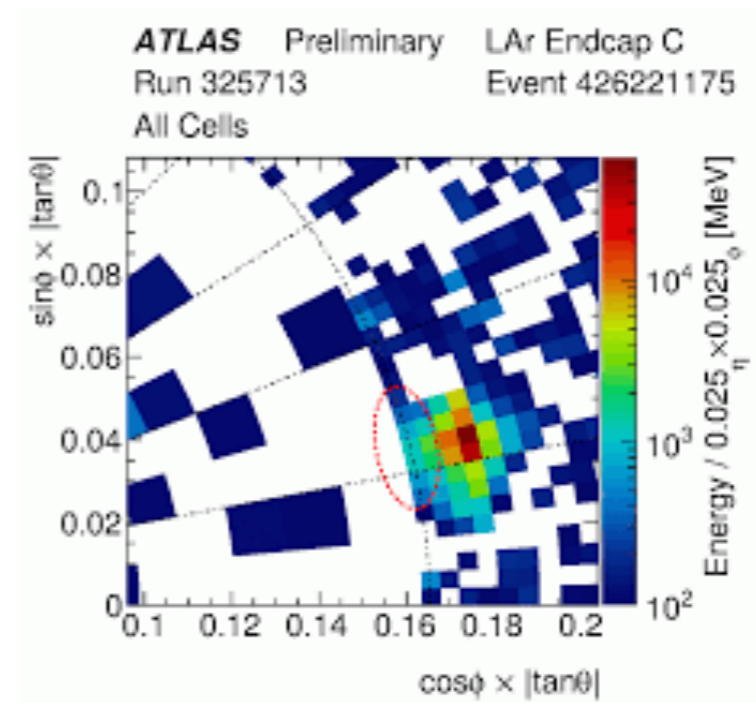
Noisy spectra



Noisy images



Text from social media



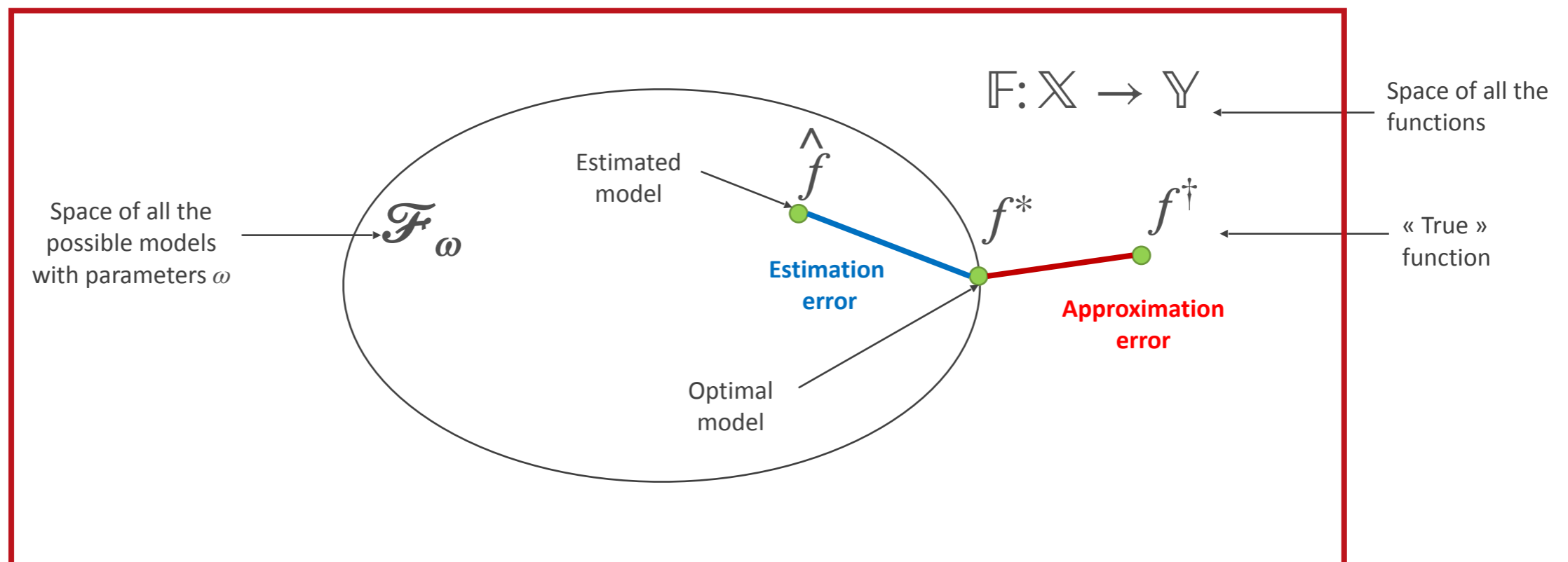
Noisy detector channels
(e.g. for reconstruction)

Epistemic uncertainties

Represents the lack of « knowledge » or « understanding » of a model on a specific input data point

Two main origins of epistemic uncertainty for machine learning models:

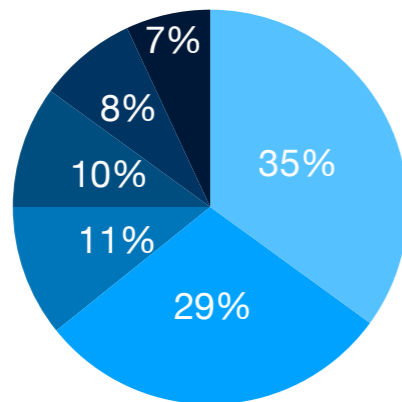
- **Estimation error:** the training dataset is just a sample of all the possible observable data
- **Approximation error:** no model can approximate perfectly the unknown « true » function



It can be possible to reduce epistemic uncertainty by using more data and increasing the model complexity

Epistemic uncertainties: examples

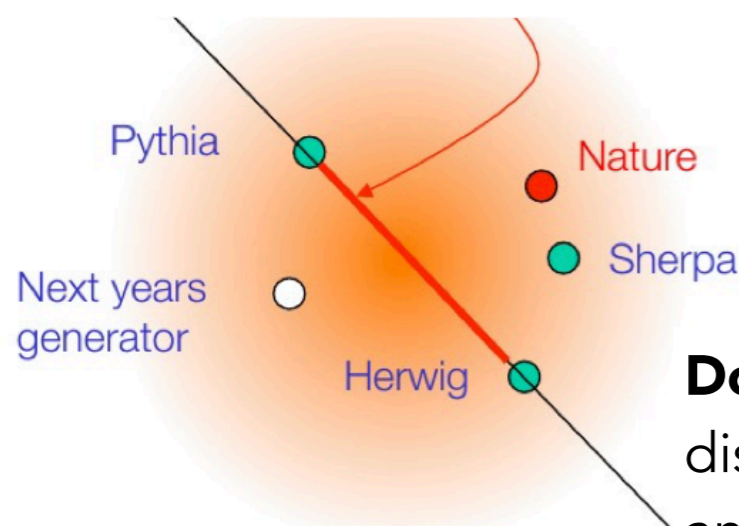
Epistemic uncertainty refers to the uncertainty of the model (epistemology is the study of knowledge) and is **often due to a lack of training data**.



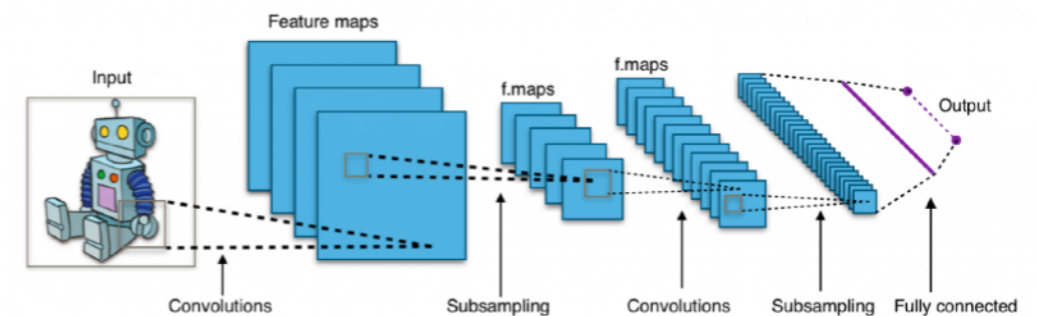
Rare or underrepresented occurrences in a dataset



Rare words in a text dataset



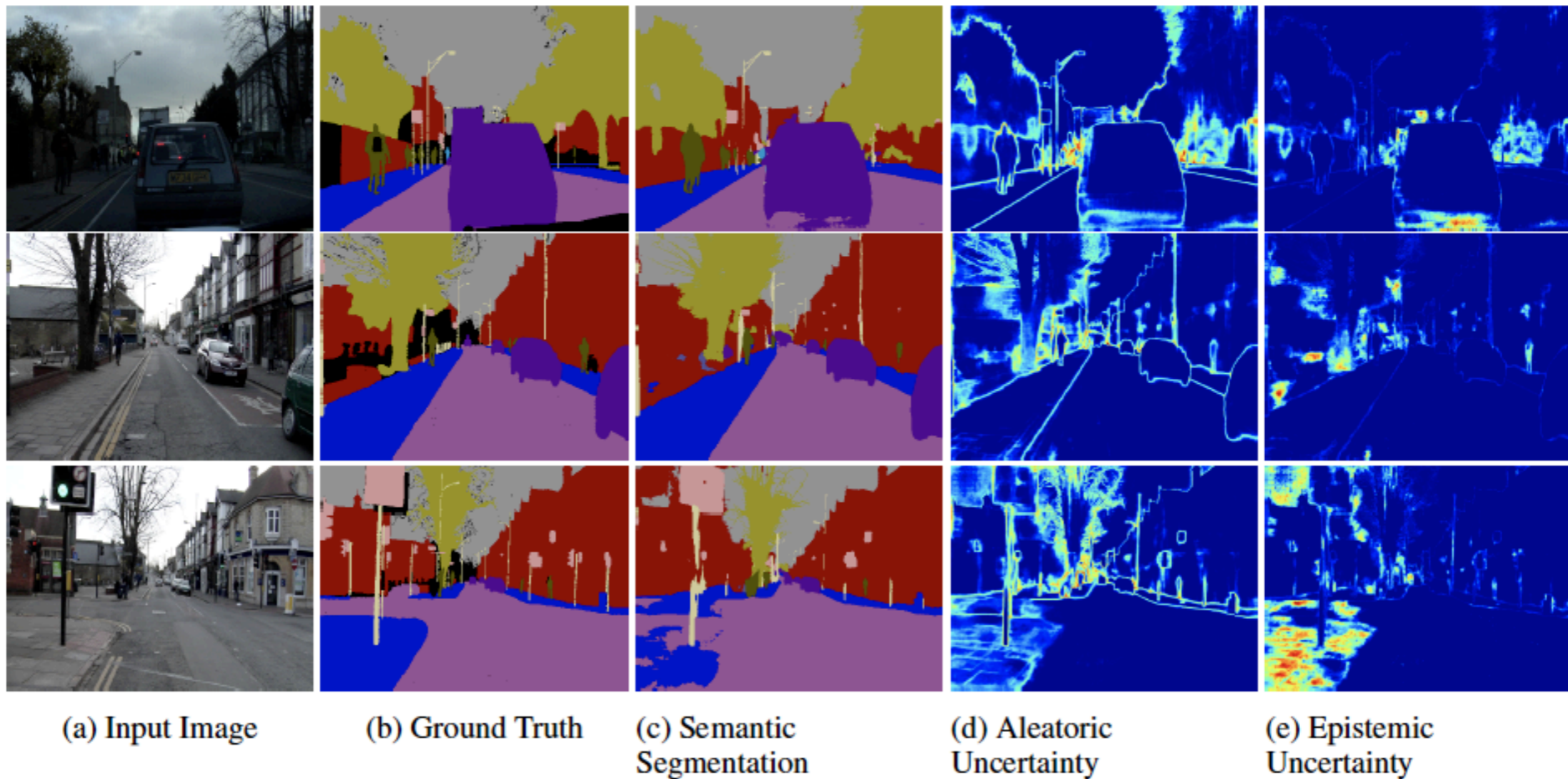
Domain shift: differences in distribution between data and Montecarlo or between test and training datasets



Choice of the ML architecture

Uncertainties example

the model fails to segment the footpath due to increased epistemic uncertainty, but not aleatoric uncertainty



Can we match these uncertainties with what we have seen in HEP analyses?

- Aleatoric uncertainties
- Epistemic uncertainties

- Experimental uncertainties
- Modelling uncertainties
 - Shape uncertainties (change in distribution)
 - From limited knowledge of the distribution
- Statistical uncertainties

Final answer (debatable, but still..):

Machine Learning

Aleatoric uncertainty

- “Statistical” / “Data” Uncertainty
- Uncertainty Inherent to data
- Not reduced w/ more data

Epistemic uncertainty

- “Model” Uncertainty
- Uncertainty from Imperfect knowledge
- Reduces with more data

Domain Shift

- Imperfect model of data generation process

HEP

Detector Noise Resolutions

Stat. errors in HEP

Systematic errors induced by ML model training on finite stats.

Systematic Uncertainties from data / simulation differences

*Even within the ML community, these terms can be ambiguous

How to reduce uncertainties:

Confidential - Google DeepMind

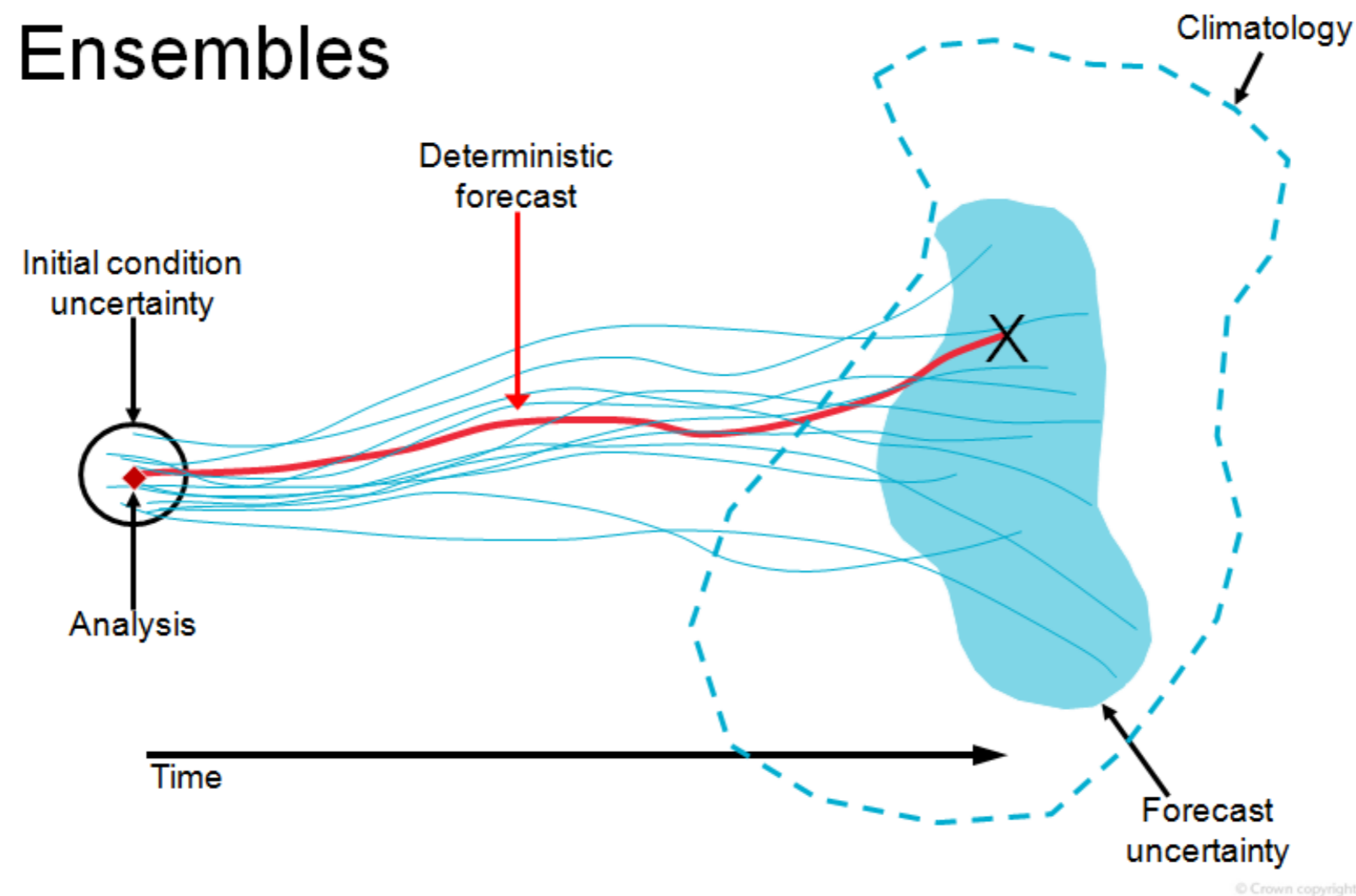
How might we **reduce** uncertainty? (ML perspective)

Uncertainty <i>about</i> the model (its structure and parameters)	Initial condition uncertainty	Uncertainty due to limitations of the model (modelled as stochastic dynamics)
<p>Use more historical data and compute for model selection and parameter learning.</p> <p>More data-efficient and compute-efficient model architectures and learning methods</p>	<p>Assimilate more observations (and more precise obs)</p> <p>Better assimilation methods (could be ML-based)</p> <p>Better models used for assimilation (see <-- and -->)</p>	<p><i>Subject to enough data:</i> allow the model more:</p> <ul style="list-style-type: none">● Learning capacity (parameter count, ...)● Computational capacity (resolution, latent size, message-passing steps, ...)● State representation capacity (resolution, latent size, ...)

Limits of predictability: we expect some uncertainty is irreducible, for anything short of a perfect model and perfect initial conditions

Deterministic vs stochastic models

- For ML models, stochasticity is bound up with physical realism.
- Much easier to produce realistic outputs from a stochastic ML model ('generative model') than a deterministic ML model.
- Technical tip: Deterministic ML loss functions without physical constraints will tend to blurry the hedge of uncertainty



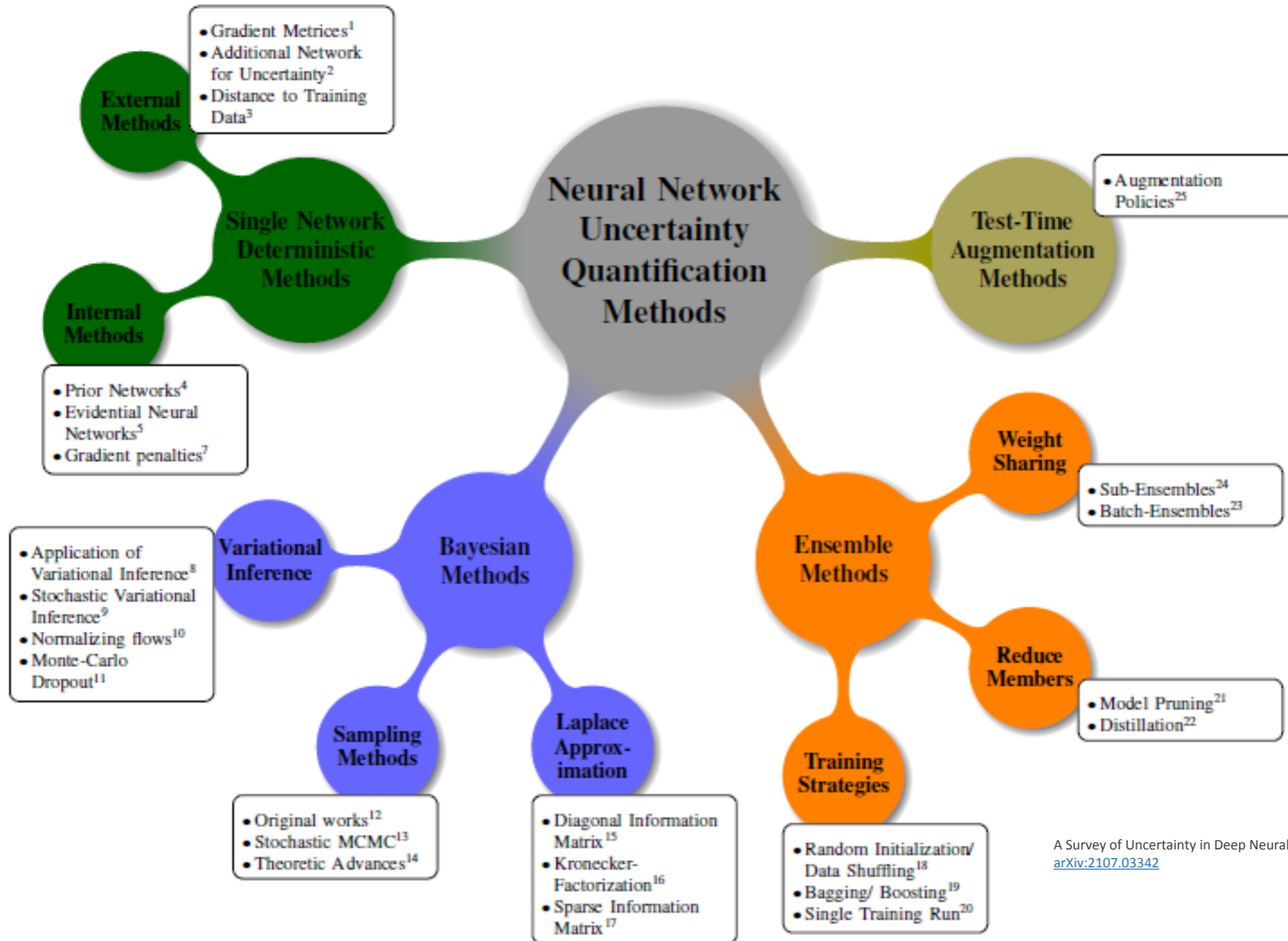
How to represent uncertainties

Confidential - Google DeepMind

How might we **represent** uncertainty? (ML perspective)

Uncertainty <i>about</i> the model (its structure and parameters)	Initial condition uncertainty	Uncertainty <i>due to</i> limitations of the model (modelled as stochastic dynamics)
Bayesian ML methods: <ul style="list-style-type: none">● to obtain approximate posterior over parameters or over model structures Ad-hoc multi-model ensembles: <ul style="list-style-type: none">● trained from multiple random initializations● trained on different resampled datasets ...	Ensemble data assimilation Ad-hoc initial perturbations End-to-end ML model conditioning directly on obs ...	Probabilistic generative models (Diffusion, GANs, VAEs, flows, scoring-rule minimization, ...) Ad-hoc perturbations at each timestep ...

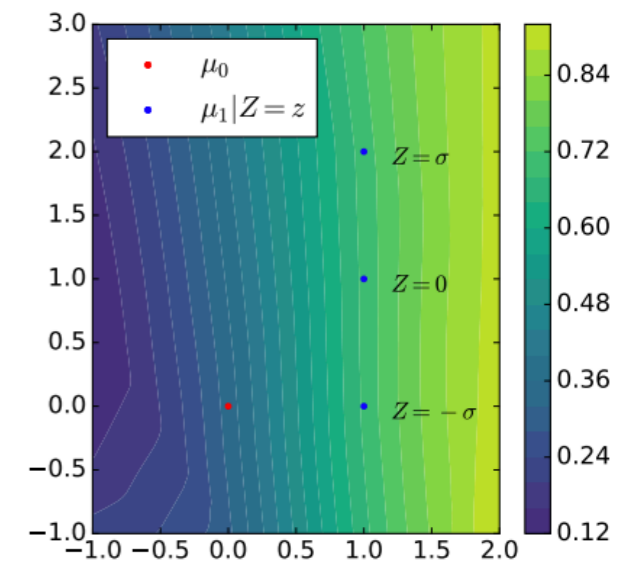
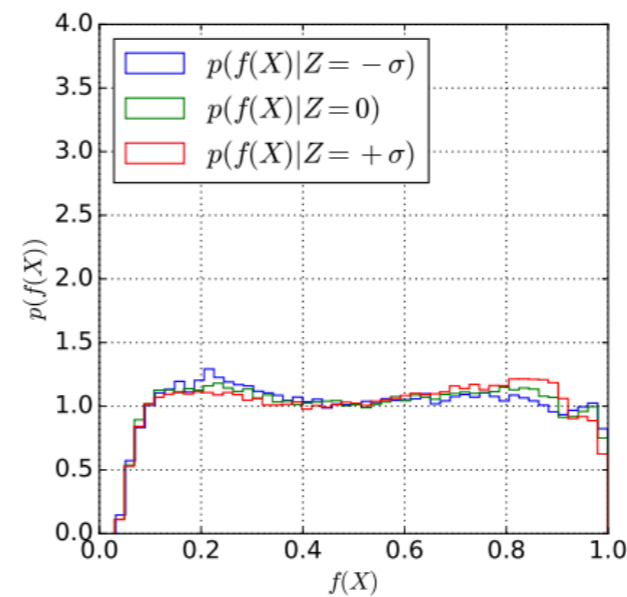
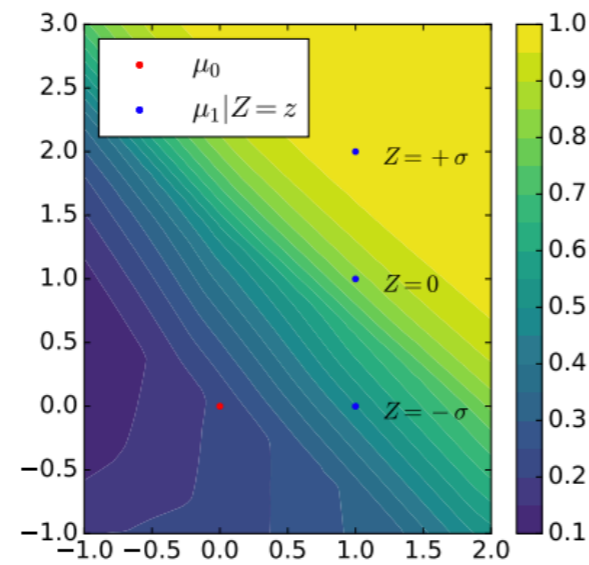
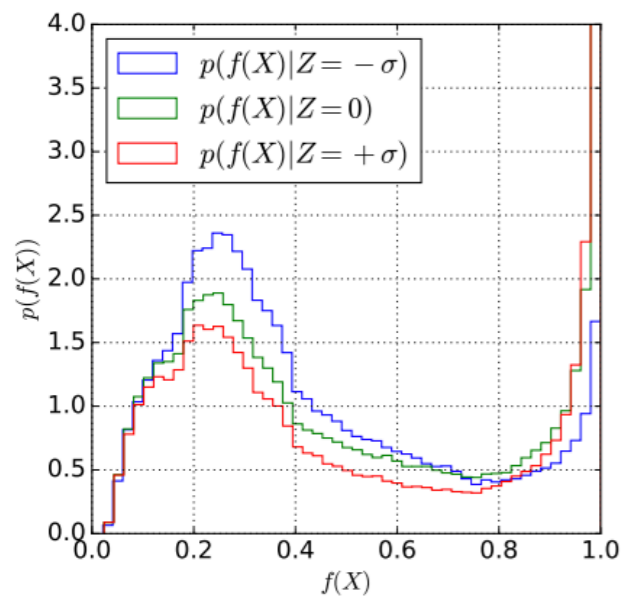
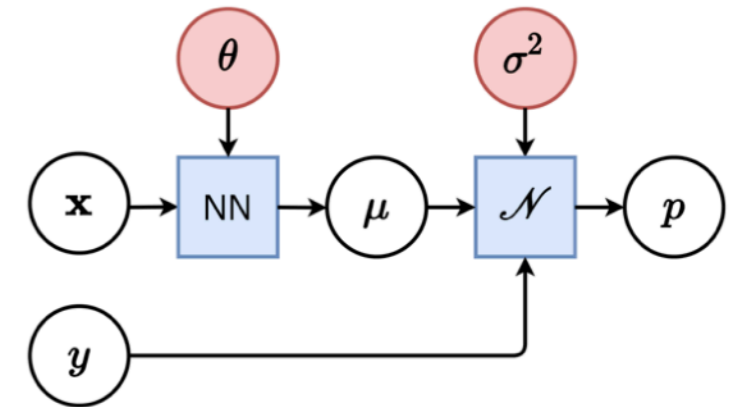
A list



A Survey of Uncertainty in Deep Neural Networks, J. Gawlikowski et al., [arXiv:2107.03342](https://arxiv.org/abs/2107.03342)

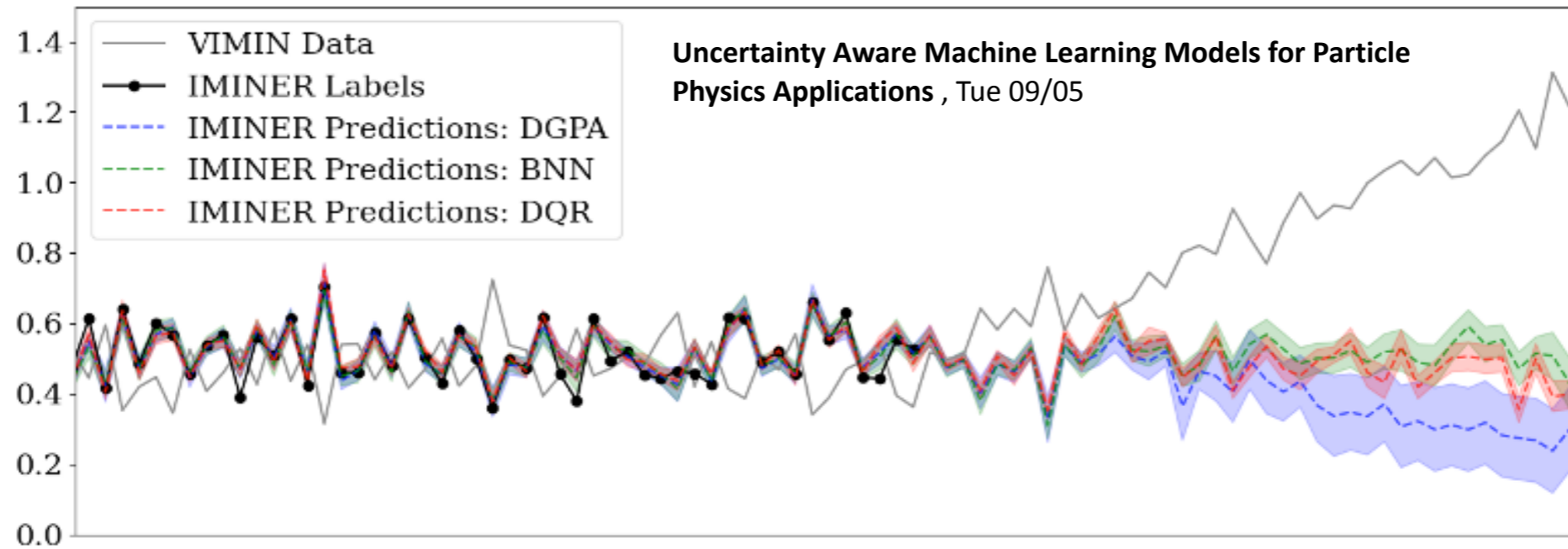
Example: Learning Systematics

- **Ex. Regression:** model aleatoric uncertainty in the output by modelling the conditional distribution as a Normal distribution
- Generative models –based uncertainty learning

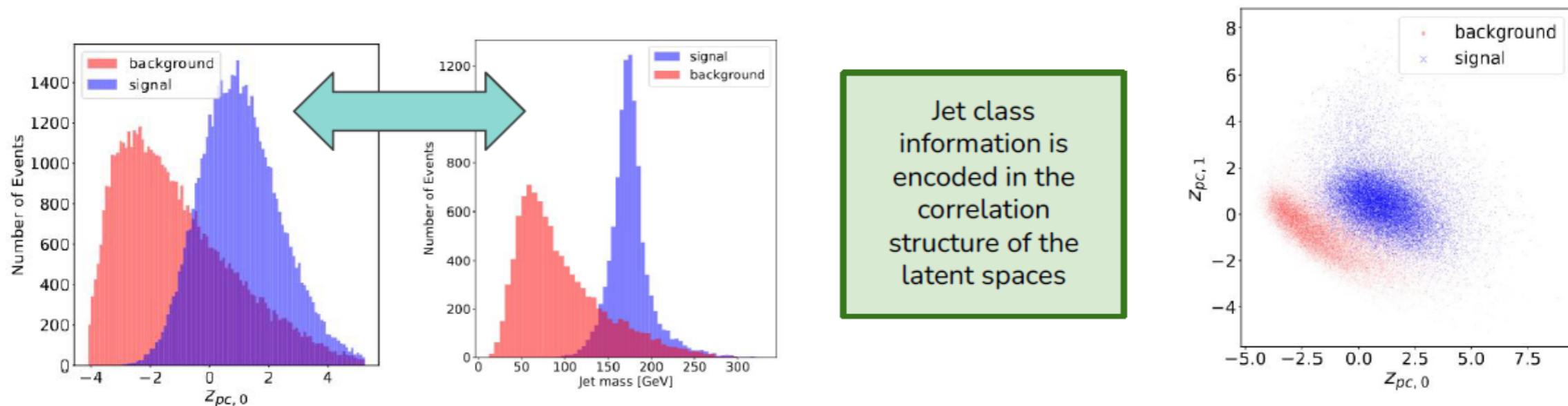


Loupe, Gilles, Michael Kagan, and Kyle Cranmer. "Learning to pivot with adversarial networks." arXiv:1611.01046 (2016).

Interpretability



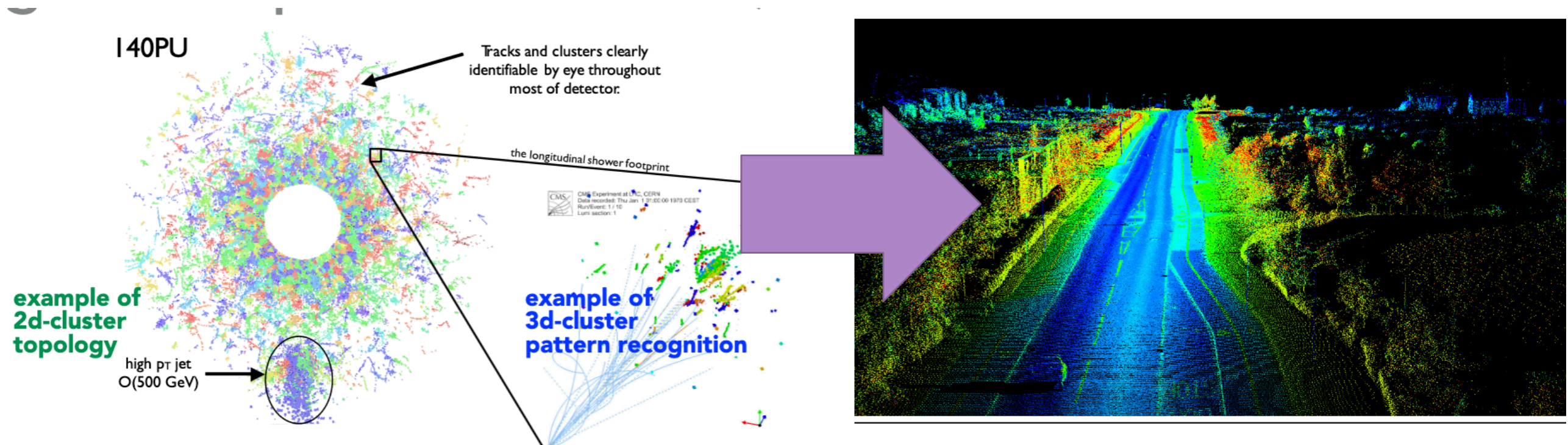
Interpretability Inspires: Explainable AI for DNN Top Taggers, CHEP2023



FAIR principles

FAIR:

Findability, **A**ccessibility, **I**nteroperability, and **R**euse of digital assets



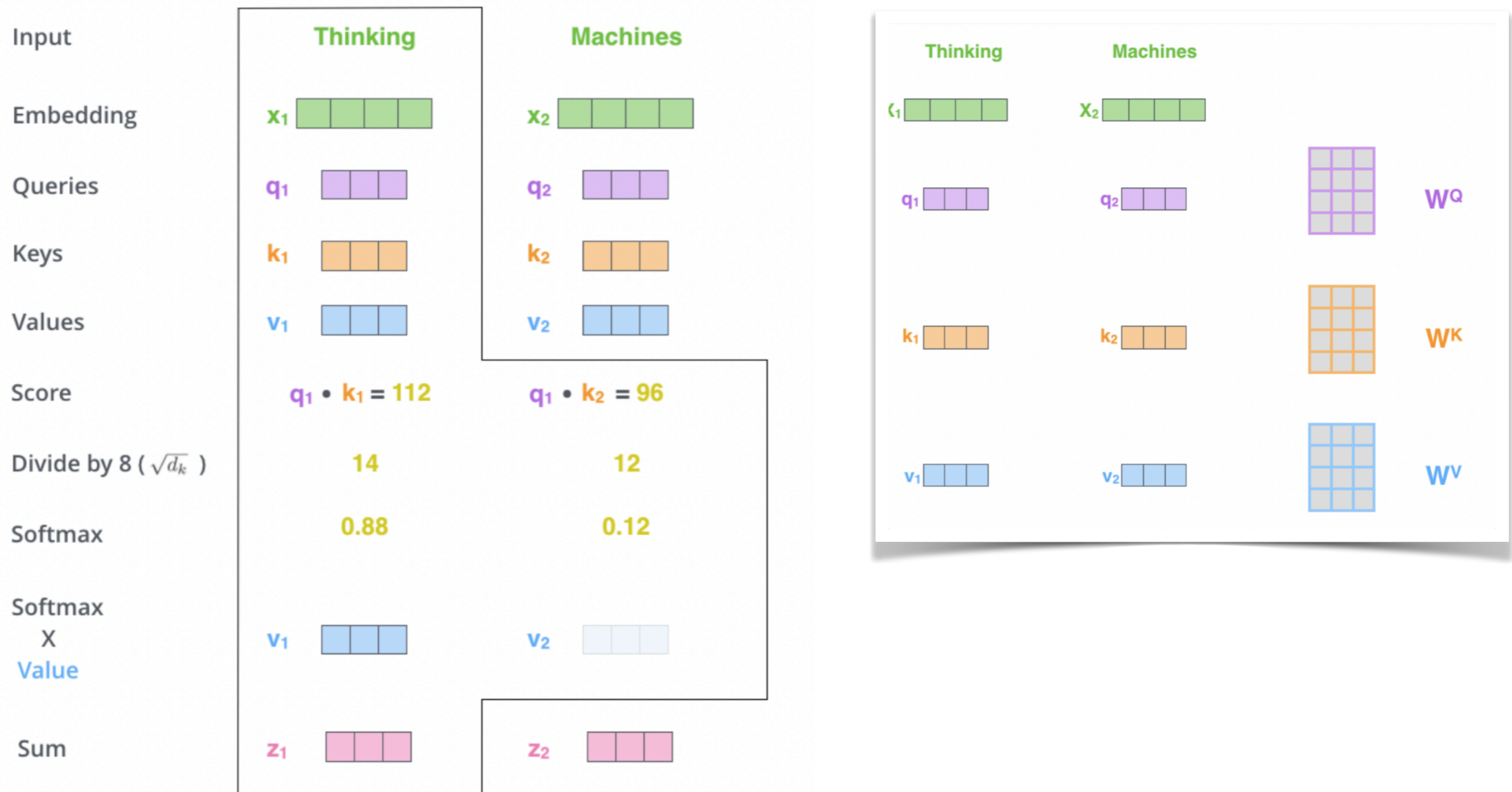
Some resources:

- PHYSTAT seminar: On relating Uncertainties in Machine Learning and HEP [[link](#)]
- [Uncertainties workshop](#) at Learning to Discover
- Great new ML review in PDG: [[Cranmer, Seljak, Terao, 2021](#)]
- Snowmass paper on uncertainty for ML in HEP: [[2208:03284](#)]
- Book Chapter: [[Dorigo, de Castro Manzano](#)]

Backup

Keys, queries, values

<http://jalammar.github.io/illustrated-transformer/>



Multiplying x_1 by the W^Q weight matrix produces q_1 , the "query" vector associated with that word. We end up creating a "query", a "key", and a "value" projection of each word in the input sentence.

Transformers

<http://jalammar.github.io/illustrated-transformer/>

1) This is our input sentence*

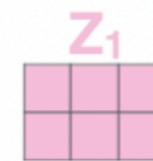
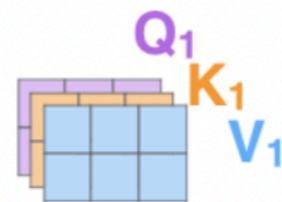
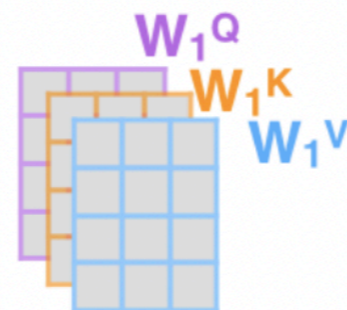
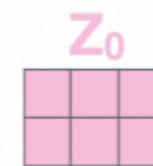
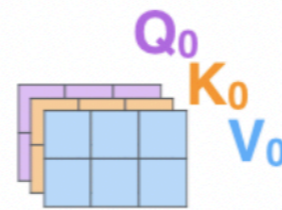
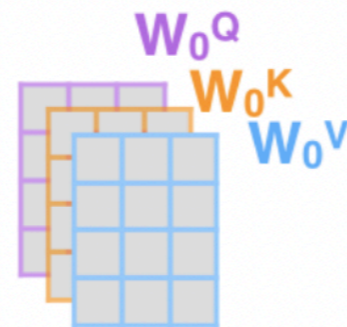
2) We embed each word*

3) Split into 8 heads. We multiply X or R with weight matrices

4) Calculate attention using the resulting $Q/K/V$ matrices

5) Concatenate the resulting Z matrices, then multiply with weight matrix W^O to produce the output of the layer

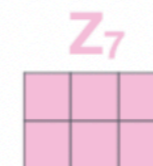
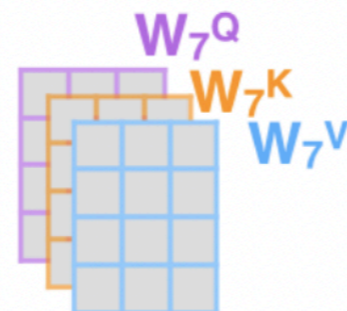
Thinking Machines



...

...

...



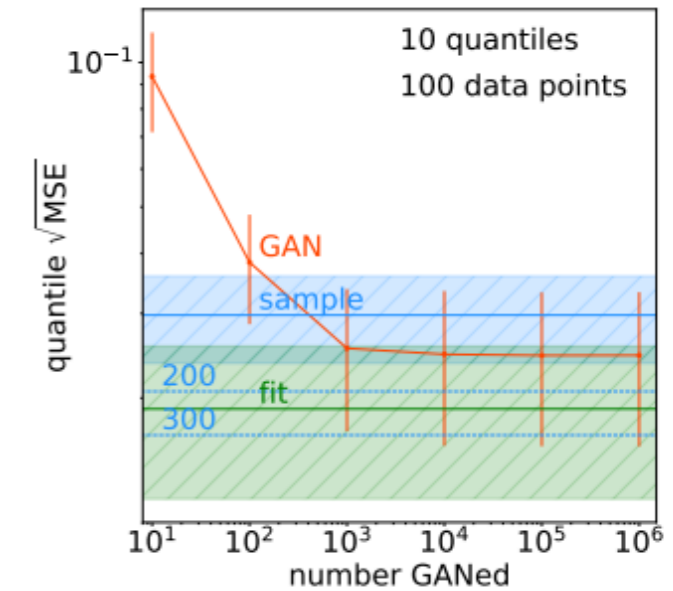
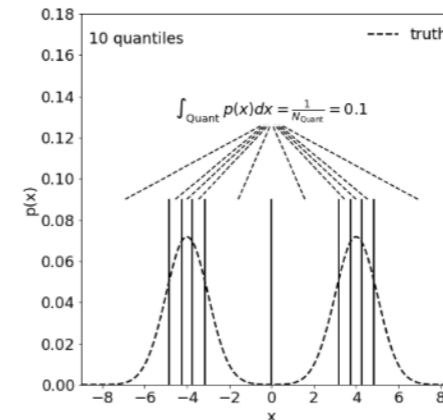
* In all encoders other than #0, we don't need embedding. We start directly with the output of the encoder right below this one



Systematics: training dataset size

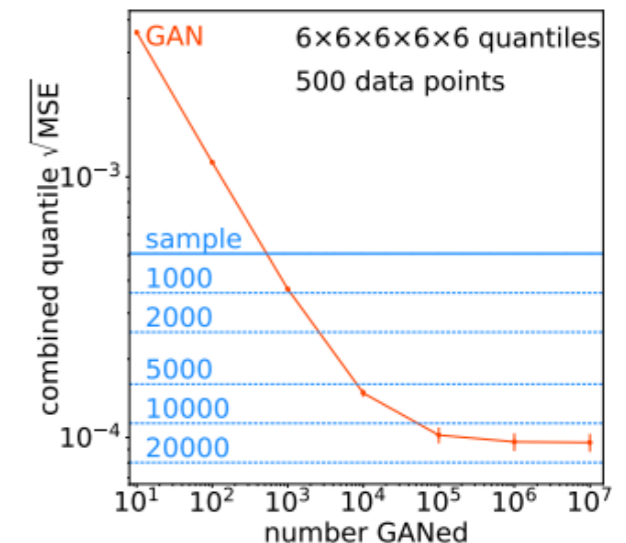
arxiv:2008.06545
NEW: arxiv:2202.073

- If a GAN is trained on **N** data points, how many **new** points can be drawn?
- GAN can describe distribution better than training data
- Needs 10,000 GAN points to match 150 true points
- In terms of **information**:
 - **sample**: only data points
 - **fit**: data + true function
 - **GAN**: data + smooth, continuous function

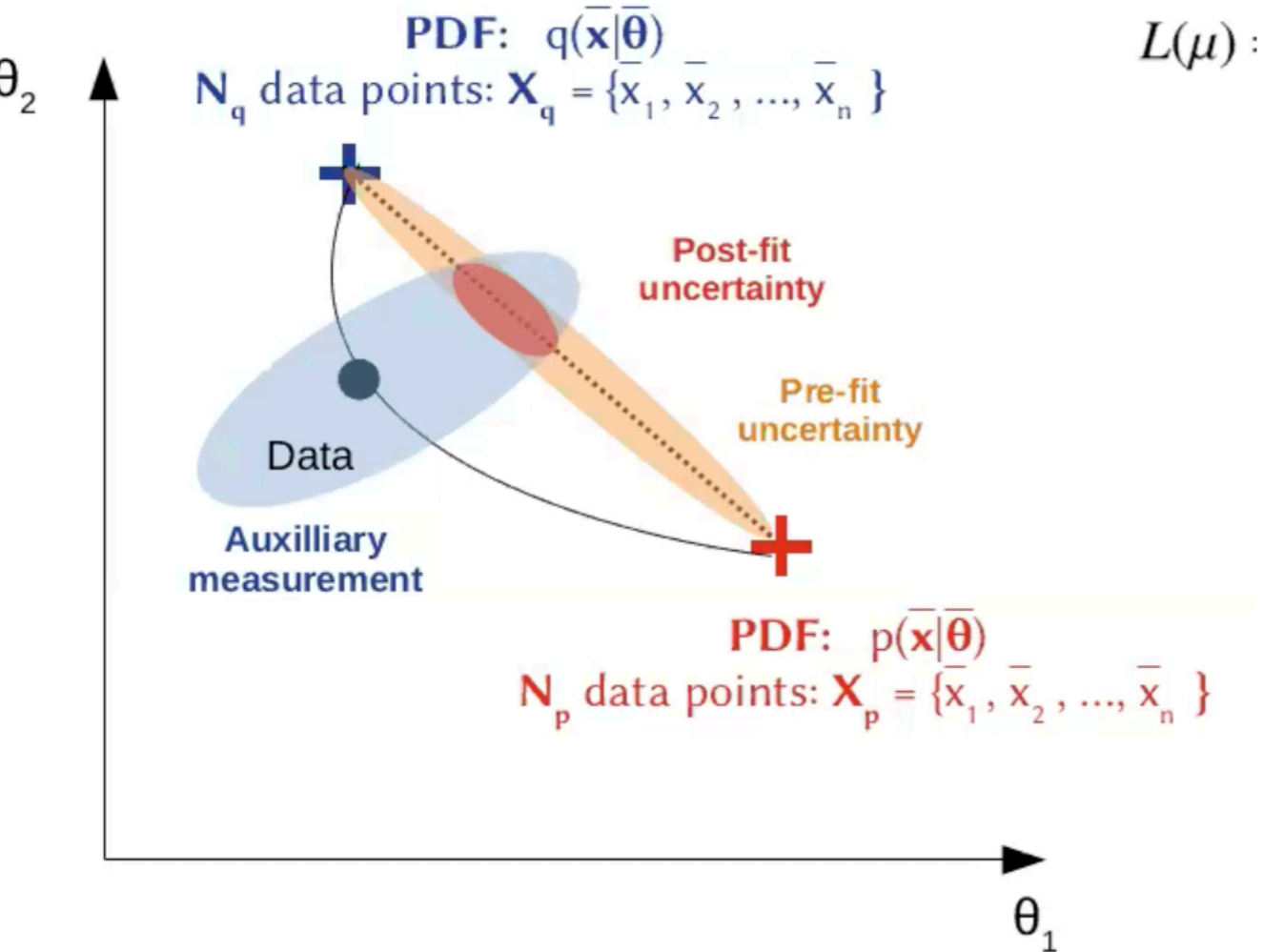


Generalisation
to multi-
dimensional
problem

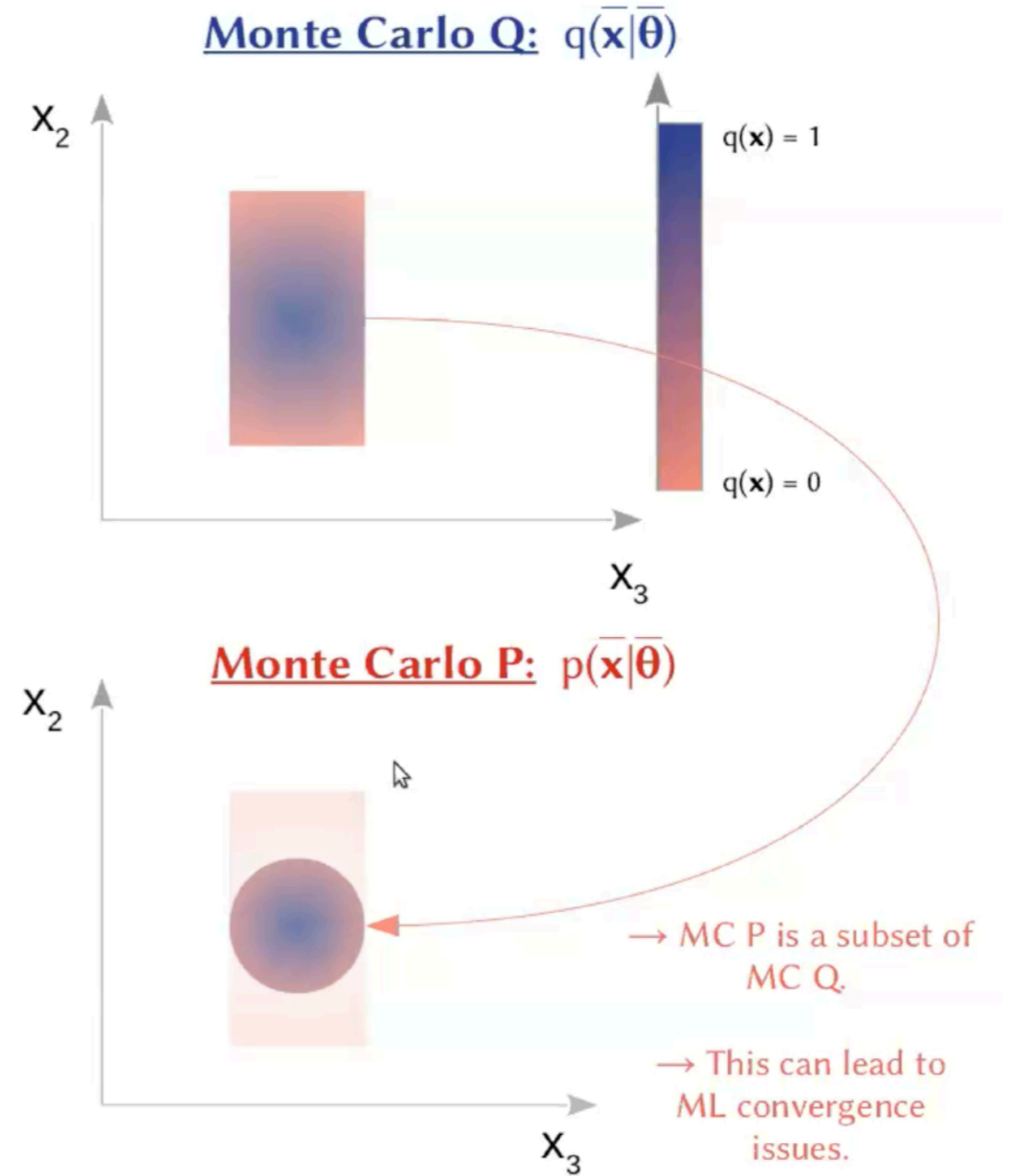
Most physics data sets described by continuous function →
GAN can interpolate



Bonus: Montecarlo reweighting with NN



$L(\mu) :$



Systematic uncertainties: image similarity

GAN can exhibit **mode-collapse** or **mode-drop**

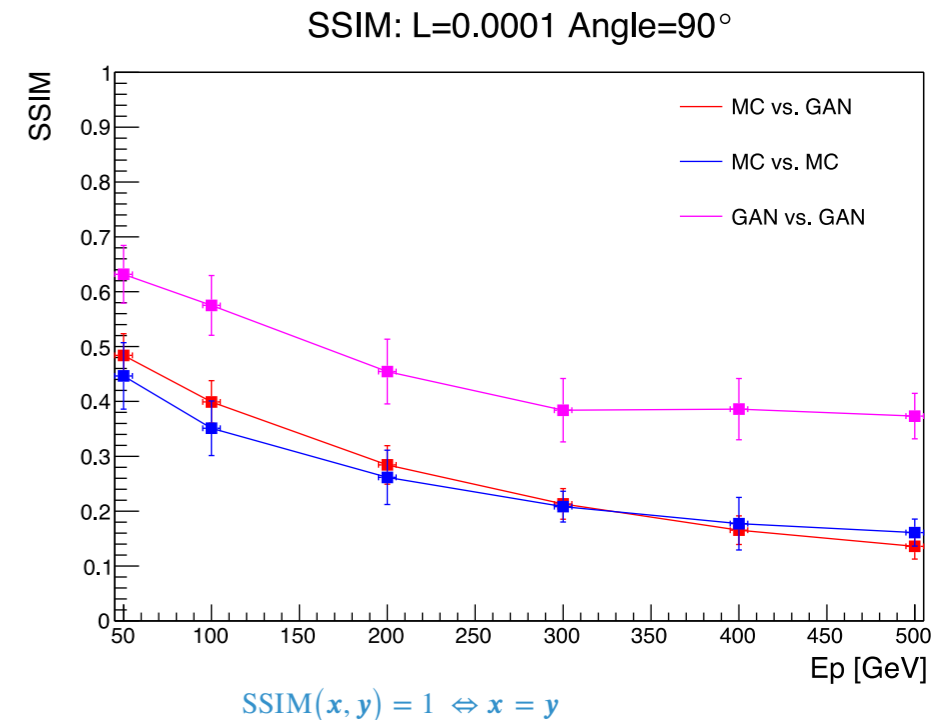
How much **diversity** in the generated sample?

- Use the **Structural Similarity Index**

$$\text{SSIM}(x, y) = \frac{(2\mu_x\mu_y + C_1)(2\sigma_{xy} + C_2)}{(\mu_x^2 + \mu_y^2 + C_1)(\sigma_x^2 + \sigma_y^2 + C_2)}$$

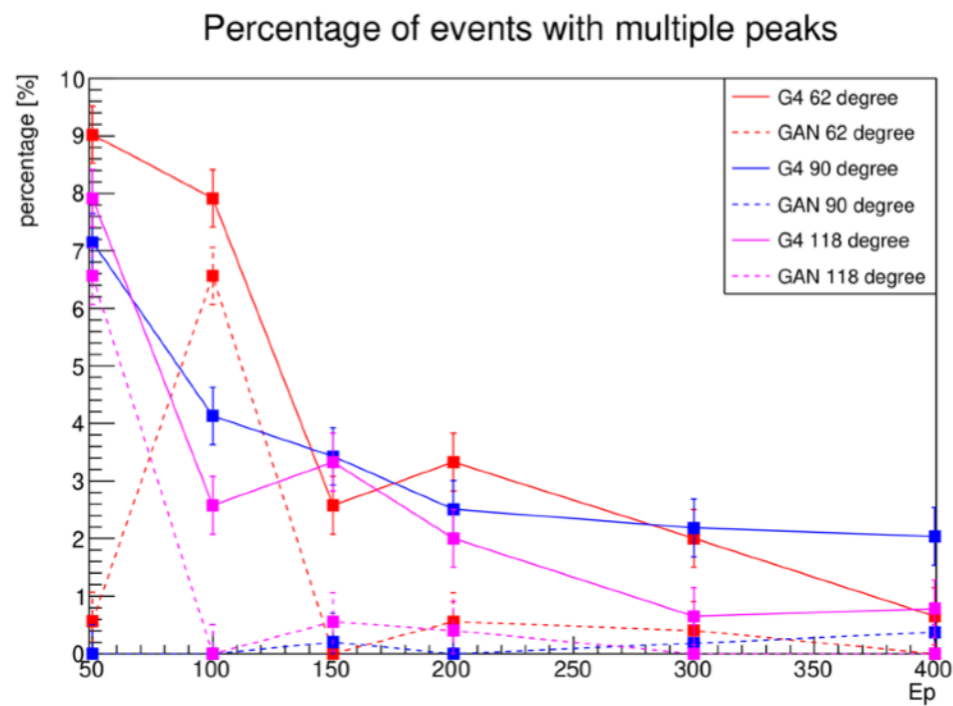
where x, y are two samples to be compared

- Calculated on sliding windows, then averaged.
- Ours is a 3D problem: SSIM computed in **xy plane**, 3rd dimension is **channel**
- Adjust C1-C2 to the pixel dynamic range



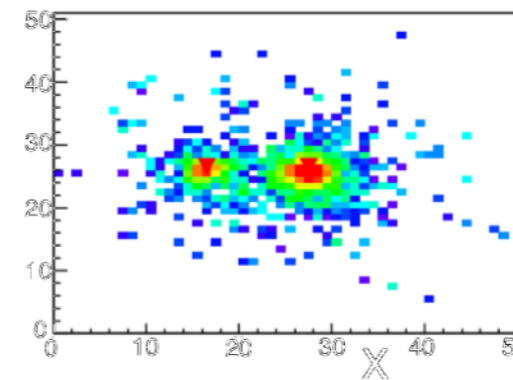
Systematics: rare events

It is important to reproduce correctly the topology and occurrence of rare events



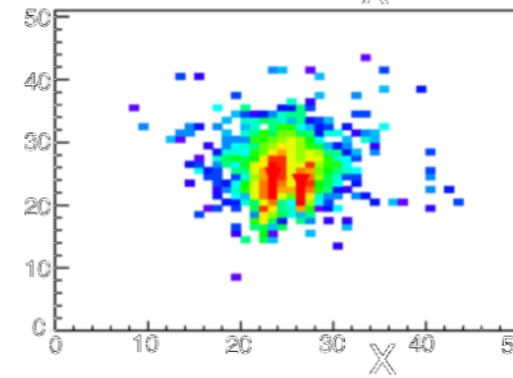
MC

Y



GAN Y

Y



“Standard”

