



LHC Heavy Flavour WG topical meeting: $b \rightarrow sll$
CERN

Angular Analysis of $B_d^0 \rightarrow K^{*0} \mu\mu$ at ATLAS

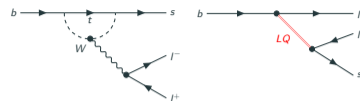


Pavel Řezníček (Charles University) for the ATLAS Collaboration
14th May 2024

Angular analysis of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ decays in pp collisions at $\sqrt{s} = 8 \text{ TeV}$
with the ATLAS detector (Run 1 data)

JHEP 10 (2018) 047

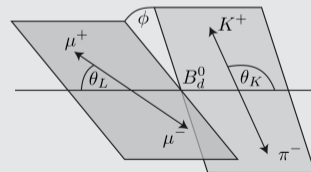
- Analysis of the decay angles in the $B^0 \rightarrow K^{*0} \mu \mu$ system, $m(\mu\mu)$ dependent
- ATLAS Run 1 data at $\sqrt{s} = 8$ TeV



Measurement

$$\mathcal{L} = \frac{e^{-N}}{n!} \prod_{i=1}^n \sum_j n_j P_{ij}(m_{K\pi\mu\mu}, \cos\theta_K, \cos\theta_L, \phi; \hat{p}, \hat{\theta})$$

- Extended unbinned maximum likelihood fit of the 3D decay angles distribution (and B -candidate mass and its uncertainty) in q^2 bins
 - Ignored range above $c\bar{c}$
- Blinded fit results
- Study of number of potential backgrounds from radiative resonant decays and other semileptonic rare decays
 - Treated in systematics, no need to include in default fit
- Detector acceptance from MC, factorized in all the three angles
- No K/π separation in ATLAS \implies 11% wrong tag of B -flavor



Low statistics (~ 340 signal events) does not allow full fit \implies simplifications:

Angular distribution folding

- Full angular distribution \rightarrow four simpler distributions
- Lost sensitivity to S_6 and S_9

$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d \cos \theta_L d \cos \theta_K d\phi dq^2} = \frac{9}{32\pi} \left[\frac{3(1-F_L)}{4} \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1-F_L}{4} \sin^2 \theta_K \cos 2\theta_L \right. \\ \left. - F_L \cos^2 \theta_K \cos 2\theta_L + S_3 \sin^2 \theta_K \sin^2 \theta_L \cos 2\phi \right. \\ \left. + S_4 \sin 2\theta_K \sin 2\theta_L \cos \phi + S_5 \sin 2\theta_K \sin \theta_L \cos \phi \right. \\ \left. + S_6 \sin^2 \theta_K \cos \theta_L + S_7 \sin 2\theta_K \sin \theta_L \sin \phi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_L \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_L \sin 2\phi \right]$$

\Downarrow

$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d \cos \theta_\ell d \cos \theta_K d\phi dq^2} = \frac{9}{8\pi} \left[\frac{3(1-F_L)}{4} \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1-F_L}{4} \sin^2 \theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi \right. \\ \left. + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi \right]$$

$$F_L, S_3, S_5, P'_5 : \begin{cases} \phi \rightarrow -\phi & \text{for } \phi < 0 \\ \theta_L \rightarrow \pi - \theta_L & \text{for } \theta_L > \frac{\pi}{2} \end{cases} \implies$$

Low statistics (~ 340 signal events) does not allow full fit \implies simplifications:

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B -candidate mass distribution pre-fits

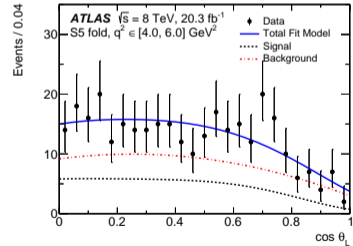
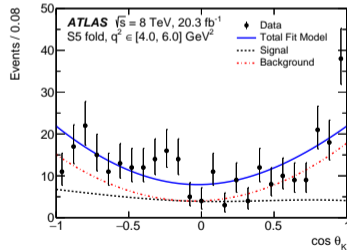
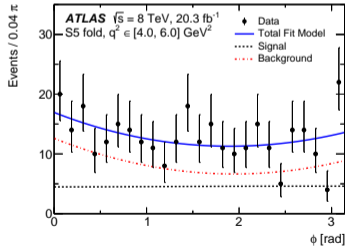
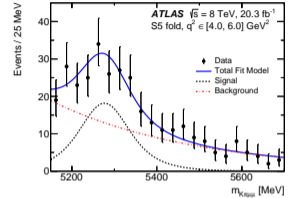
- B -candidate mass distribution pre-fitted and fixed in the angular fit
- Mass nuisance parameters extract from fits to control channels ($B^0 \rightarrow J/\psi K^*$, $B^0 \rightarrow \psi(2S)K^*$)
- Procedure feasibility validated with toy-MC

Rough q^2 binning

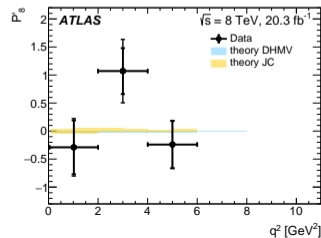
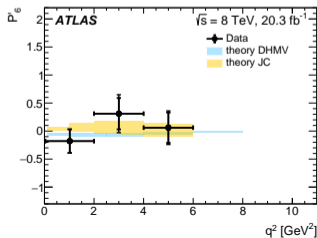
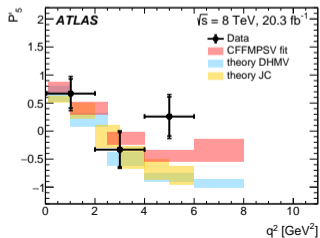
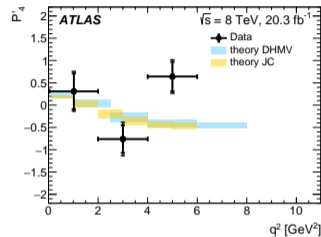
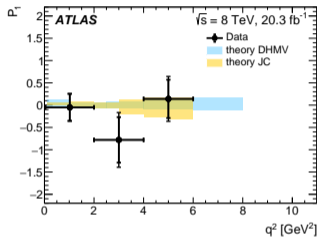
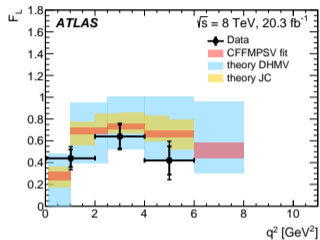
- 3 bins only in q^2 [GeV²]: (0.04 - 2), (2.0 - 4.0), (4.0 - 6.0)

Extended unbinned maximum likelihood fit

- Left sideband cut to avoid contrib. from partially reconstructed B -decays
- Extracting S_i parameters \rightarrow transformed to P'_i (including correlations)
- Dilution correction applied post-fit to S_5, S_8



- Results \sim compatible with SM, largest (local) deviations of 2.7σ for P'_5 and P'_4
- Run 2 analysis in progress, similar analysis approach



- Ongoing and future analyses expected to follow the binned approach, possibly extract more parameters, wider q^2 range, and make technical improvements (selection, fits)
- Binning driven by available statistics, but no problem to accommodate any agreed bin-edges
- Possible deviations: resolution drives bin edges near resonances ($\phi \rightarrow \mu\mu$ veto, distance from $c\bar{c}$)

Thank you

Pavel Řezníček

pavel.reznicek@cern.ch

Name of the project: Fundamental constituents of matter through frontier technologies (FORTE)

Registration number: CZ.02.01.01/00/22_008/0004591

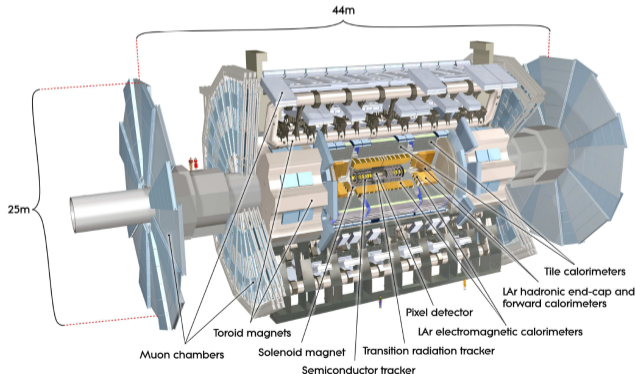
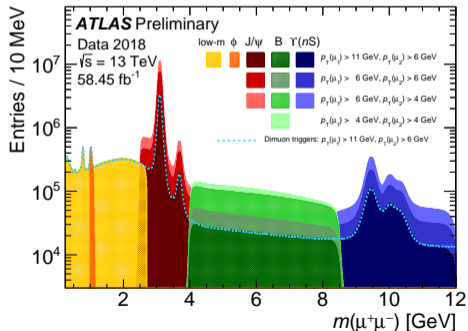


Co-funded by
the European Union



Backup

- Producing 2.5 M $b\bar{b}$ pairs/second, B_s , B_c , Λ_b , etc. available
- Program focused mostly on muonic final states, fully reconstructable
- Typical trigger: low- p_T di-muons at low invariant mass, using information from tracker and muon detectors
- B-physics trigger rate up to ~ 200 Hz



Triggers

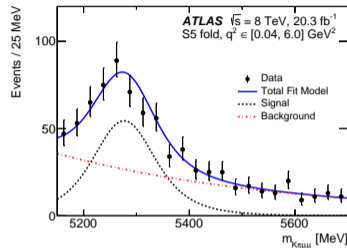
- Limited by rate of HW-based L1 system
- Combination of 19 single-/di-/tri-muon triggers
- Dimuon typically with 4(6) GeV thresholds

Offline selection optimized on MC (cherry pick)

- B -decay vertex reconstruction, $\chi^2/\text{ndf} < 2$
- B -hadron decay time significance $\tau/\sigma_\tau > 12.25$
- B -momentum pointing to collision vertex $\cos\theta > 0.999$
- Radiative tail cut: $|(m(B)-m_{\text{pdg}}(B)) - (m(\mu\mu)-m_{\text{pdg}}(J/\psi))| < 130 \text{ MeV}$

Multiple candidates

- Candidates from different tracks \rightarrow pick smallest vertex $\chi^2/\text{ndf} < 2$
- Same tracks $\Rightarrow B$ or \bar{B} ? \rightarrow pick smallest $|m(K^*)-m_{\text{pdg}}(K^*)|/\sigma_{m(K^*)}$



q^2 [GeV^2]	n_{signal}	$n_{\text{background}}$
[0.04, 2.0]	128 ± 22	122 ± 22
[2.0, 4.0]	106 ± 23	113 ± 23
[4.0, 6.0]	114 ± 24	204 ± 26
[0.04, 4.0]	236 ± 31	233 ± 32
[1.1, 6.0]	275 ± 35	363 ± 36
[0.04, 6.0]	342 ± 39	445 ± 40

Angular distribution foldings (complete)

- Not enough statistics for full 3D angular fit \implies fold distributions, but lost sensitivity to S_6 (A_{FB}) and S_9

$$F_L, S_3, S_4, P'_4 : \begin{cases} \phi \rightarrow -\phi & \text{for } \phi < 0 \\ \phi \rightarrow \pi - \phi & \text{for } \theta_L > \frac{\pi}{2} \\ \theta_L \rightarrow \pi - \theta_L & \text{for } \theta_L > \frac{\pi}{2} \end{cases} \quad \frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d\cos\theta_\ell d\cos\theta_K d\phi dq^2} = \frac{9}{8\pi} \left[\frac{3(1-F_L)}{4} \sin^2\theta_K + F_L \cos^2\theta_K + \frac{1-F_L}{4} \sin^2\theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2\theta_K \cos 2\theta_\ell + S_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi \right. \\ \left. + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi \right]$$

$\cos\theta_L \in [0, 1], \cos\theta_K \in [-1, 1]$ and $\phi \in [0, \pi]$

$$F_L, S_3, S_5, P'_5 : \begin{cases} \phi \rightarrow -\phi & \text{for } \phi < 0 \\ \theta_L \rightarrow \pi - \theta_L & \text{for } \theta_L > \frac{\pi}{2} \end{cases} \quad \frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d\cos\theta_\ell d\cos\theta_K d\phi dq^2} = \frac{9}{8\pi} \left[\frac{3(1-F_L)}{4} \sin^2\theta_K + F_L \cos^2\theta_K + \frac{1-F_L}{4} \sin^2\theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2\theta_K \cos 2\theta_\ell + S_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi \right. \\ \left. + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi \right]$$

$\cos\theta_L \in [0, 1], \cos\theta_K \in [-1, 1]$ and $\phi \in [0, \pi]$

$$F_L, S_3, S_7, P'_6 : \begin{cases} \phi \rightarrow \pi - \phi & \text{for } \phi > \frac{\pi}{2} \\ \phi \rightarrow -\pi - \phi & \text{for } \phi < -\frac{\pi}{2} \\ \theta_L \rightarrow \pi - \theta_L & \text{for } \theta_L > \frac{\pi}{2} \end{cases} \quad \frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d\cos\theta_\ell d\cos\theta_K d\phi dq^2} = \frac{9}{8\pi} \left[\frac{3(1-F_L)}{4} \sin^2\theta_K + F_L \cos^2\theta_K + \frac{1-F_L}{4} \sin^2\theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2\theta_K \cos 2\theta_\ell + S_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi \right. \\ \left. + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi \right]$$

$\cos\theta_L \in [0, 1], \cos\theta_K \in [-1, 1]$ and $\phi \in [-\pi/2, \pi/2]$

$$F_L, S_3, S_8, P'_8 : \begin{cases} \phi \rightarrow \pi - \phi & \text{for } \phi > \frac{\pi}{2} \\ \phi \rightarrow -\pi - \phi & \text{for } \phi < -\frac{\pi}{2} \\ \theta_L \rightarrow \pi - \theta_L & \text{for } \theta_L > \frac{\pi}{2} \\ \theta_K \rightarrow \pi - \theta_K & \text{for } \theta_L > \frac{\pi}{2} \end{cases} \quad \frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d\cos\theta_\ell d\cos\theta_K d\phi dq^2} = \frac{9}{8\pi} \left[\frac{3(1-F_L)}{4} \sin^2\theta_K + F_L \cos^2\theta_K + \frac{1-F_L}{4} \sin^2\theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2\theta_K \cos 2\theta_\ell + S_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi \right]$$

$\cos\theta_L \in [0, 1], \cos\theta_K \in [-1, 1]$ and $\phi \in [-\pi/2, \pi/2]$

- Large stat. errors \implies can afford very conservative approach to systematics
- Largest systematics from backgrounds modeling

Source	F_L	S_3	S_4	S_5	S_7	S_8
Combinatoric $K\pi$ (fake K^*) background	0.03	0.03	0.05	0.04	0.06	0.16
D and B^+ veto	0.11	0.04	0.05	0.04	0.01	0.06
Background pdf shape	0.04	0.04	0.03	0.03	0.03	0.01
Acceptance function	0.01	0.01	0.07	0.01	0.01	0.01
Partially reconstructed decay background	0.03	0.05	0.02	0.08	0.05	0.06
Alignment and B field calibration	0.02	0.04	0.05	0.04	0.04	0.04
Fit bias	0.01	0.01	0.02	0.03	0.01	0.05
Data/MC differences for p_T	0.02	0.02	0.01	0.01	0.01	0.01
S -wave	0.01	0.01	0.01	0.01	0.01	0.03
Nuisance parameters	0.01	0.01	0.01	0.01	0.01	0.01
Λ_b , B^+ and B_s background	0.01	0.01	0.01	0.01	0.01	0.01
Misreconstructed signal	0.01	0.01	0.01	0.01	0.01	0.01
Dilution	—	—	—	< 0.01	—	< 0.01

- $|\cos \theta_K| < 0.9$
- veto B^+ or D hypothesis
- expo. / pol3
- factorization, signal MC test
- left B-mass sideband variation
- track p_T smearing
- toy-MC pulls
- data/MC $B - p_T$ weights
- $B \rightarrow K\pi\mu\mu$, 5% fed to toy-MC
- control sample fit uncertainties
- toy-MC with peak. backgrounds
- B fit with \bar{B} acceptance
- MC stat., ω vs $\bar{\omega}$

Backgrounds from long-list found to have non-negligible contributions

- $B^+ \rightarrow K^{*+} \mu \mu$
- $B^+ \rightarrow K^+ \mu \mu$
- $B_s^0 \rightarrow \phi \mu \mu$
- $\Lambda_b \rightarrow \Lambda(1520) \mu \mu$
- $\Lambda_b \rightarrow p K^- \mu \mu$
- $B^+ \rightarrow K \mu \mu, \pi \mu \mu$ peaking at $\cos(\theta_K) \sim 1.0$
- $B \rightarrow DX$ in left B -mass sideband peaking at $\cos(\theta_L) \sim 0.7$