

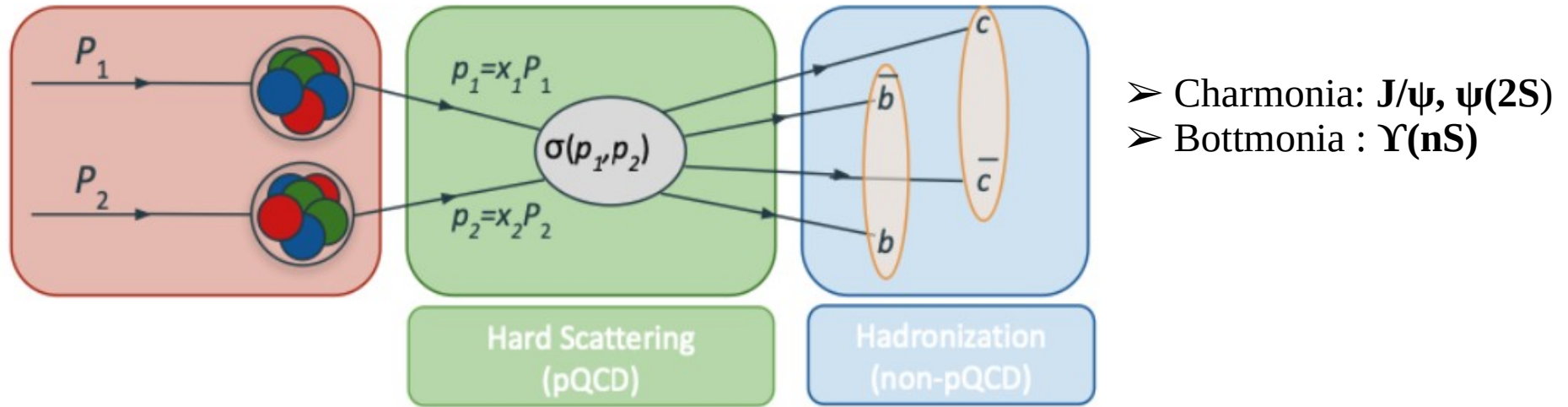


$\Upsilon(nS)$ cross section measurement in pp collisions @ 13TeV

Subikash Choudhury
Jadavpur University

ALICE-STAR India Collaboration meeting, IOP, Bhubaneswar
June 24-27, 2024

Introduction



Quarkonium production in pp collisions:

- Initial heavy quark production (sensitive to pQCD)
- Formation of bound quarkonium states (non perturbative QCD)
- Constrain model calculations (CO/CS mechanism)
- Reference measurement for heavy-ion system

Motivation and Analysis Details

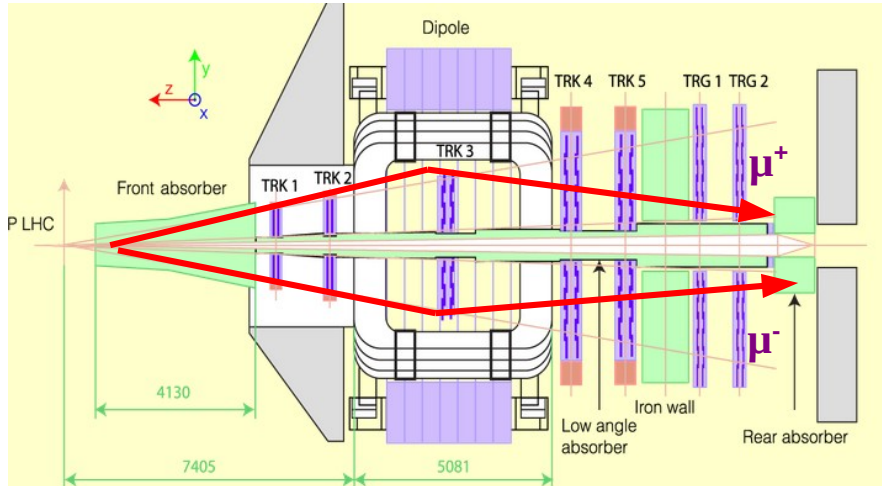
Physics motivation of this analysis:

- Benefit from highest statistics Run 2 data to do precise measurements $\Upsilon(nS)$ cross-sections in finer p_T and y bins
- Extend to $\Upsilon(3S)$ in ALICE
- Facilitate more stringent test QCD
- Benchmark for RUN3 analyses and complementary to LHCb

Trigger selection : CMUL7-NOPF-MUFAST

Physics selection : kMuonUnlikePt7 (LHC17 and LHC18) or kMUU7 (LHC16)

Total Analysed Events: ~ 647 M



Single muon track selection

1. Muon tracking-trigger matching.
2. $-4.0 < \eta_\mu < -2.5$
3. $17.6 < R_{abs} < 89$ cm
4. pDCA cuts

Muon pair selection

1. $2.5 < y^{\mu^+\mu^-} < 4$
2. Opposite sign charges
3. $0 < p_T < 30$ GeV/c

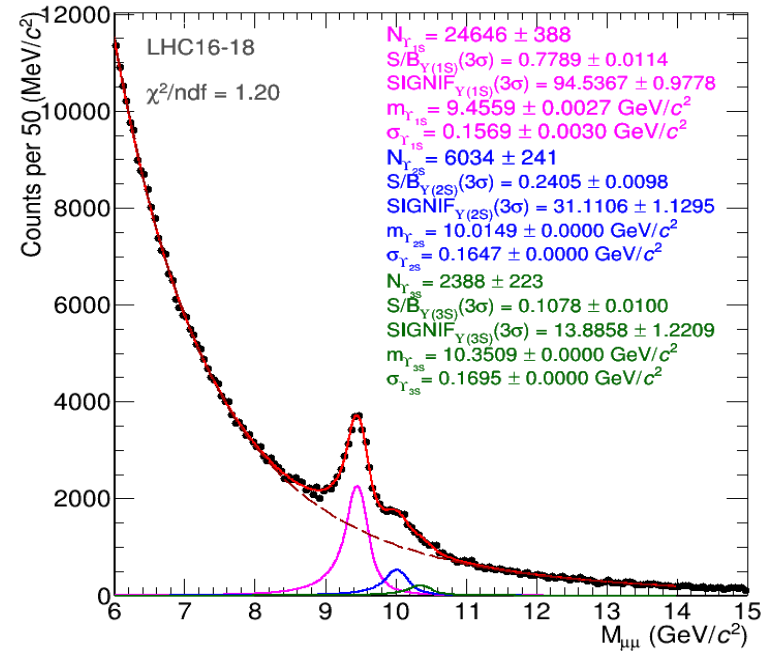
Signal Extraction

1. Obtain di-muon invariant mass spectra
2. Fit mass spectra with a combination of signal+ background function
 - **Signal: Crystal Ball (An exponential tail + Gaussian core)**
 - **Background: DE, DP, VWG (Pl. See back up)**
3. Determine tail parameters
4. Refit invariant mass spectra keeping tail parameters fixed

Parameter initialization and constrains:

- **Mass of $\Upsilon(1S)$ is kept free**
- **Sigma of $\Upsilon(1S)$ is kept free**

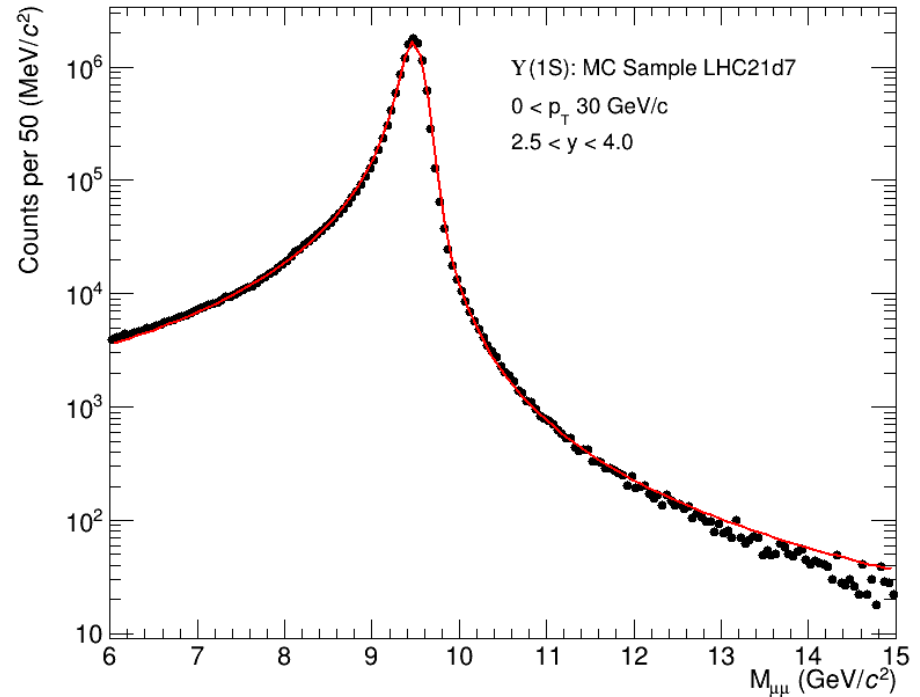
$$m_{\Upsilon(nS)} = m_{\Upsilon(1S)} + (m_{\Upsilon(nS)}^{\text{PDG}} - m_{\Upsilon(1S)}^{\text{PDG}}), \quad \sigma_{\Upsilon(nS)} = \sigma_{\Upsilon(1S)} \times \frac{\sigma_{\Upsilon(nS)}^{\text{MC}}}{\sigma_{\Upsilon(1S)}^{\text{MC}}}$$



Tail Extraction from Monte Carlo

- Invariant mass distribution is fitted with CB2
- No background
- p_T and rapidity inclusive

α_L	1.016
n_L	2.035
α_R	2.063
n_R	2.247

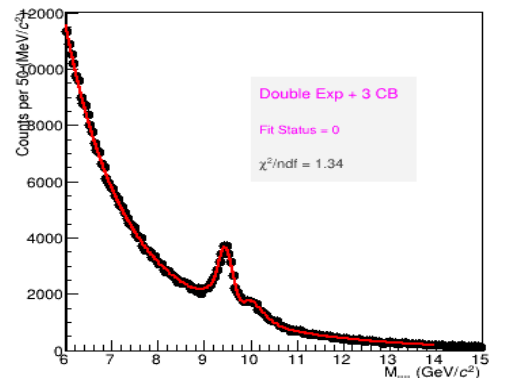
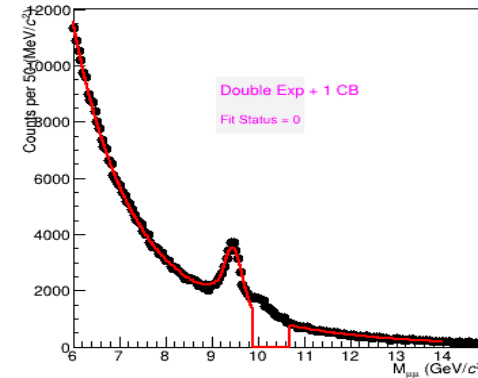
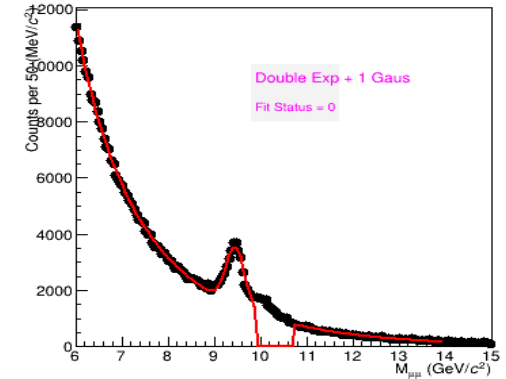
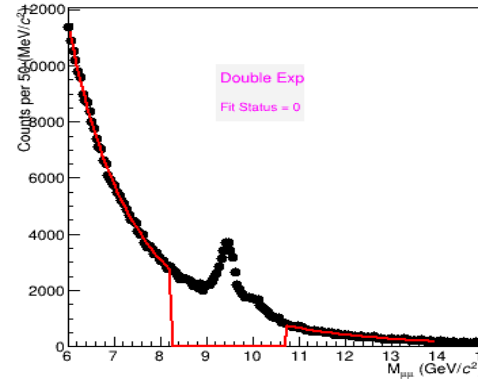


Data driven tail extraction

Steps of extraction

1. A bkg function is fitted excluding at least $\pm 5\sigma$ around $\Upsilon(1S)$ mass peak
2. Bkg+Gaus is fitted excluding $\Upsilon(2S)$ and $\Upsilon(3S)$
3. Bkg+1CB2 taking mass and σ of 1S from step2, excluding 2s and 3s, and bkg params are fixed
4. Bkg + 2CB2 excluding 3s, bkg params fixed
5. Bkg + 3CB2, bkg params fixed
6. Mass and sigma of $\Upsilon(1S)$ and, tail parameters are always kept free

Graphical demonstration



Data driven tail extraction

Steps of Extraction

1. A bkg function is fitted excluding at least $\pm 5\sigma$ around Υ_{1s} mass peak
2. Bkg+Gaus is fitted excluding Υ_{2s} and Υ_{3s}
3. Bkg+1CB2 taking mass and σ of 1s from step2, excluding 2s and 3s, and bkg params are fixed
4. Bkg + 2CB2 excluding 3s, bkg params fixed
5. Bkg + 3CB2, bkg params fixed
6. Mass and sigma of Υ_{1s} and, tail parameters are always kept free

Systematics are done repeating 1-5 for following conditions

Bkg Functions	1. Double Exponential 2. Sum of two power law 3. Variable Width Gaussian
Fit ranges	6-13, 7-14, 5-12
Exclusion region around $\Upsilon(1S)$ mass peak	$\pm 5\sigma$, $\pm 6\sigma$, $\pm 8\sigma$

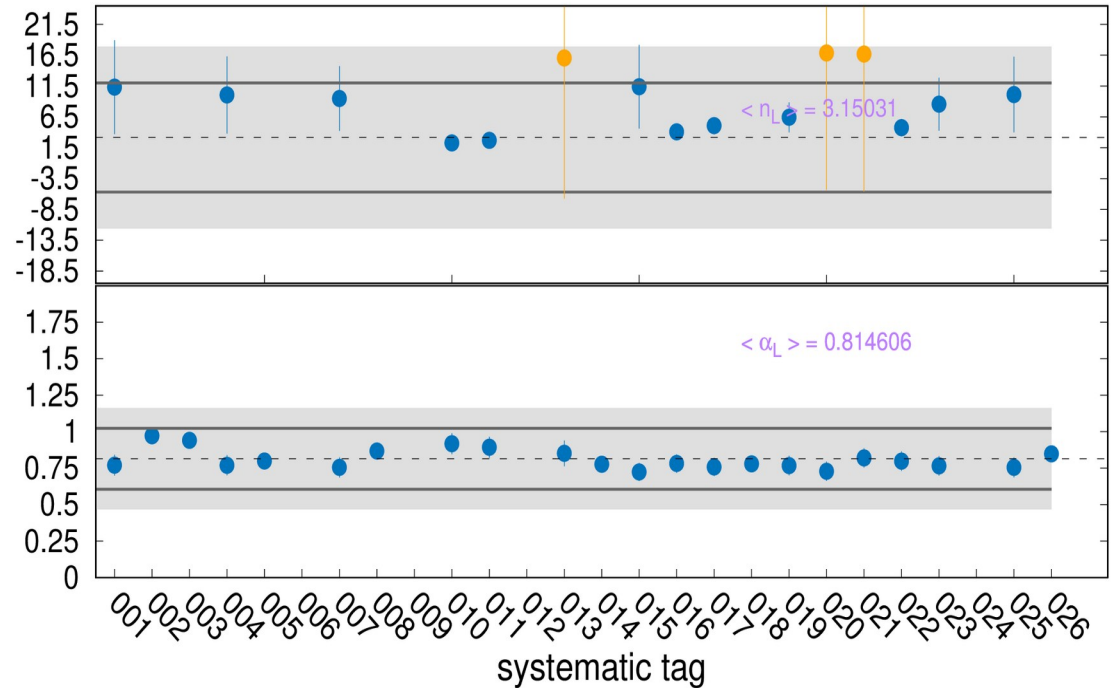
Left Tail Parameters (α_L and n_L)

Gray band $\pm 5\sigma$ around global mean

Black solid lines $\pm 3\sigma$ around global mean

Orange markers, data points $\pm 3\sigma$ away from global mean

Blue markers, data points within $\pm 3\sigma$ of global mean



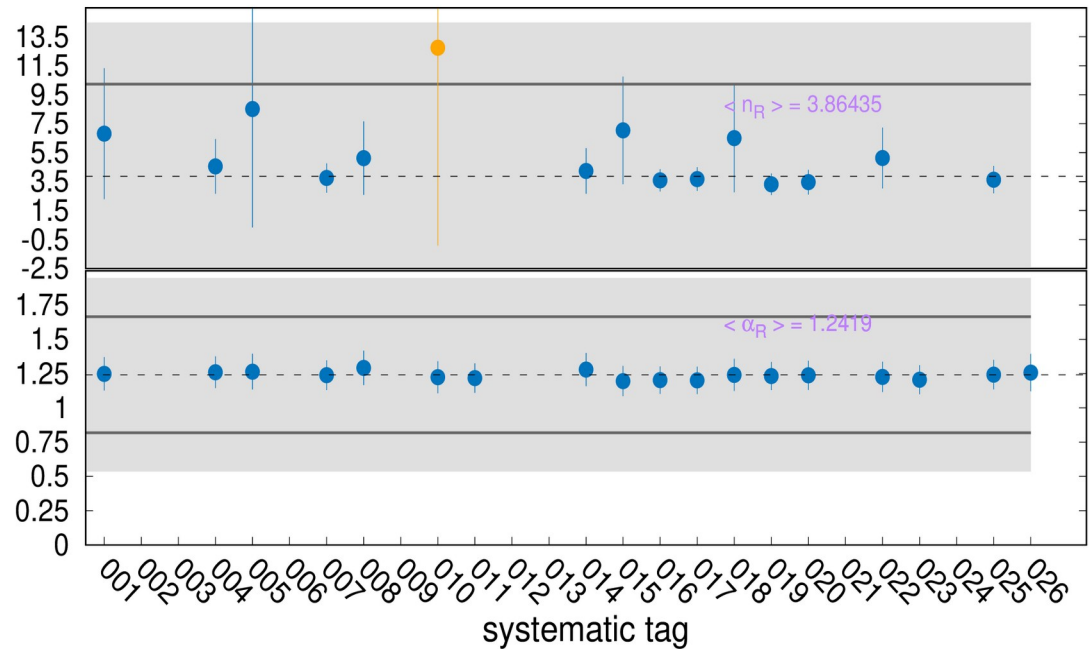
Right Tail Parameters (α_R and n_R)

Gray band $\pm 5\sigma$ around global mean

Black solid lines $\pm 3\sigma$ around global mean

Orange markers, data points $\pm 3\sigma$ away from global mean

Blue markers, data points within $\pm 3\sigma$ of global mean

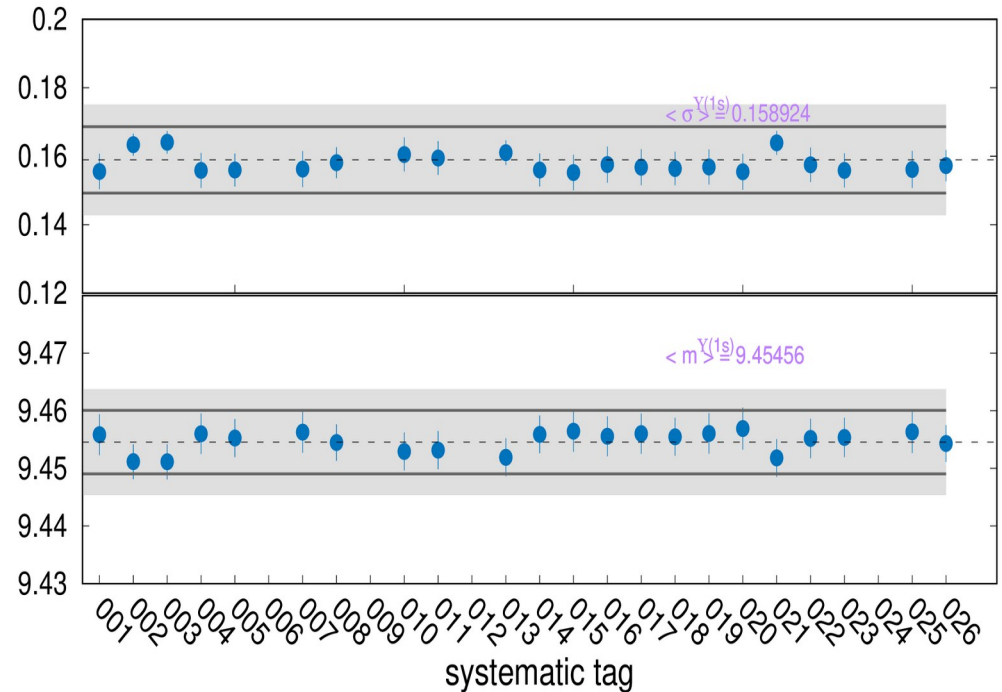


Final Tail Parameters (data)

Data driven tail parameters are extracted averaging over those fits that have converged

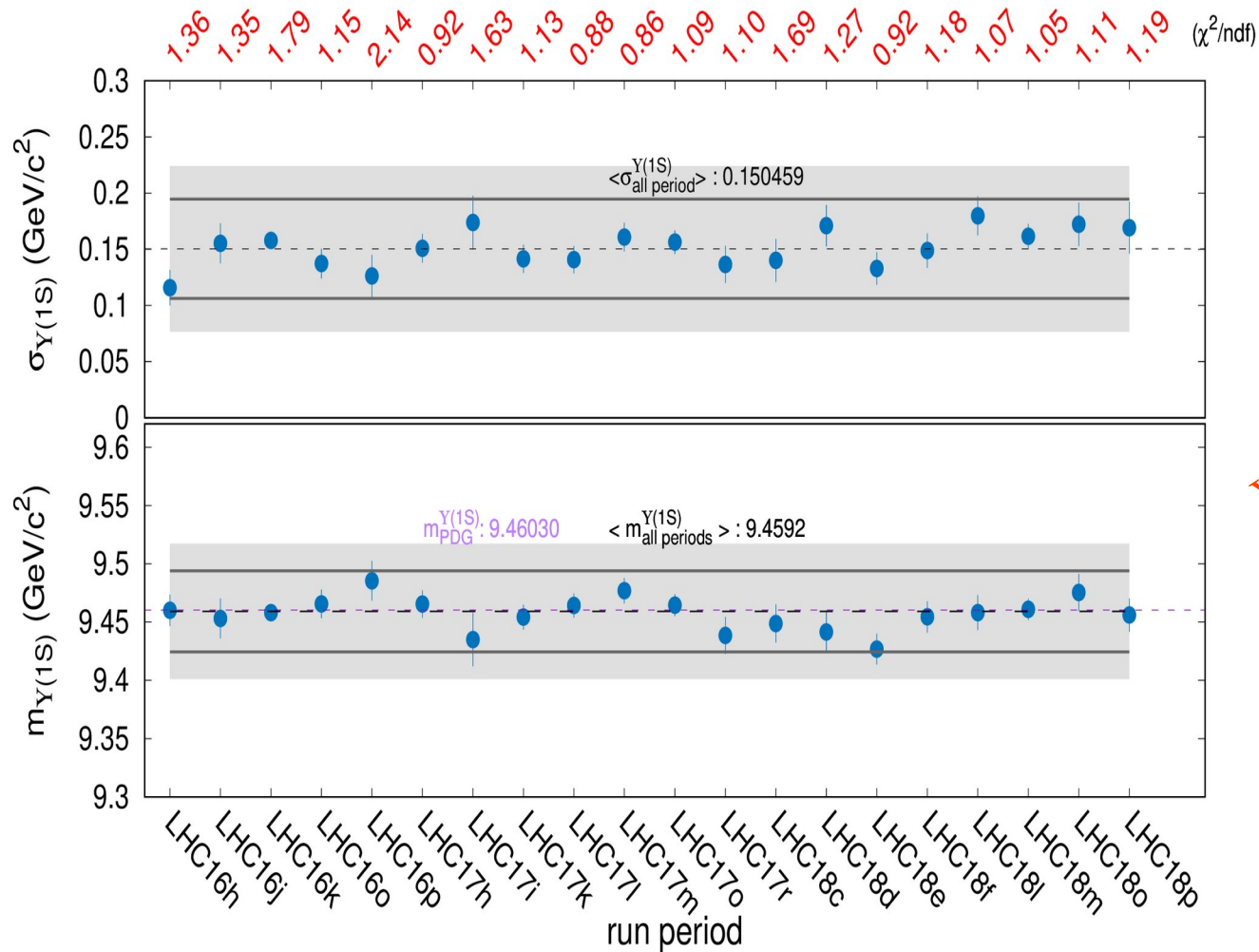
α_L	0.814
n_L	3.150
α_R	1.242
n_R	3.864

No explicit cut over χ^2/ndf is applied



Mass and σ of $\Upsilon(1S)$ of corresponding fits

Mass and Sigma of $\Upsilon(1S)$ across different run-periods with data-driven tail params

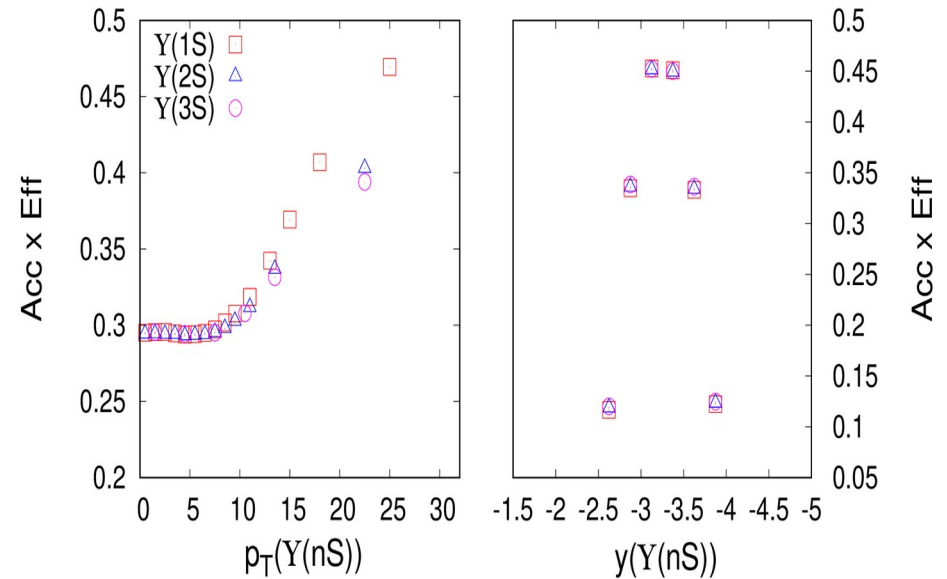
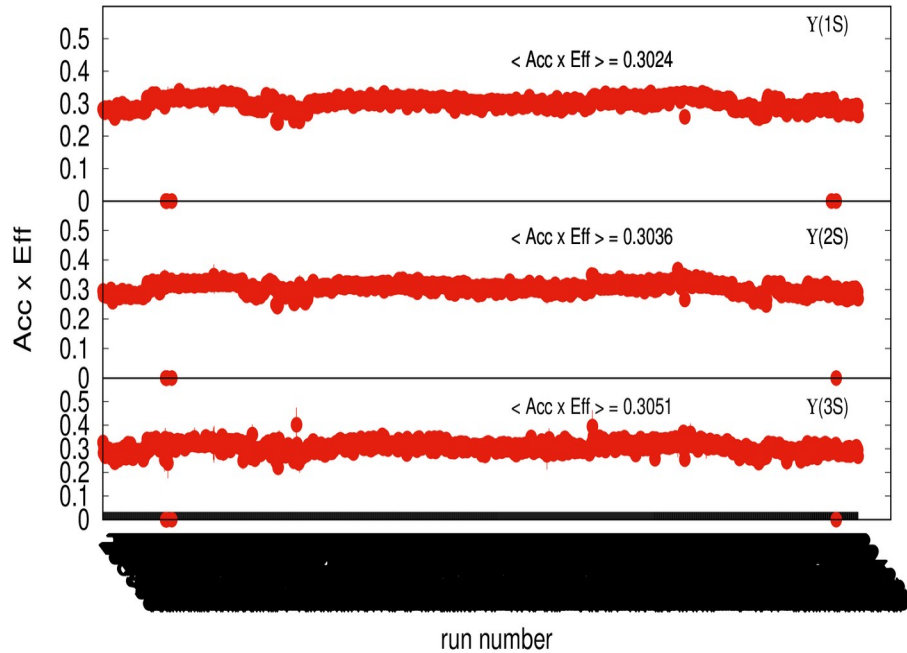


Variation across run-periods within 3σ

Acceptance and Efficiency corrections [$\Upsilon(nS)$]

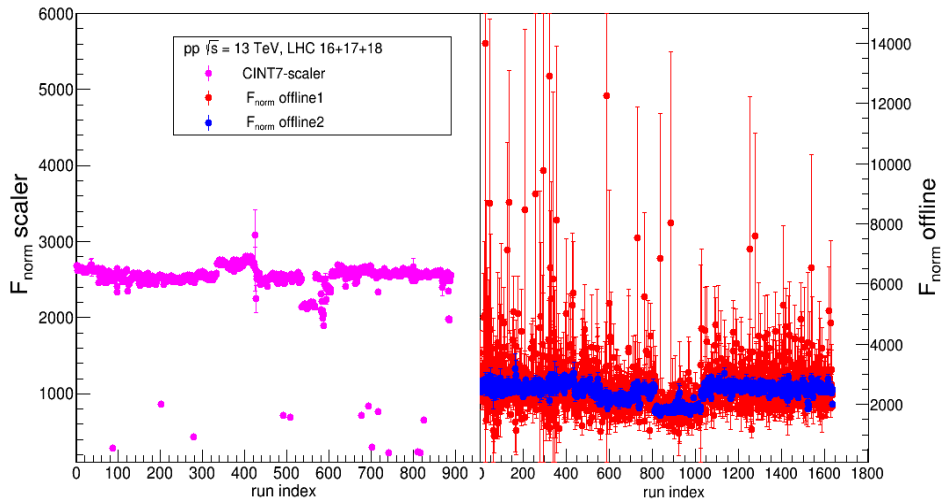
MC sample:
tuned on LHCb data @ 13TeV
LHC21d7
LHC22d4

$$\langle A\varepsilon \rangle = \frac{N_{\text{reconstructed}}}{N_{\text{generated}}}$$



Luminosity

For systematics two methods are used to determine F_{norm} : offline (direct & indirect)



$$F_{\text{norm}} \text{ offline1 (direct)} = 2467.04 \pm 13.36$$

$$F_{\text{norm}} \text{ offline2 (indirect)} = 2400.25 \pm 1.34$$

$$\Delta F_{\text{norm}} = 66.79 \text{ (2.78\% [syst])}$$

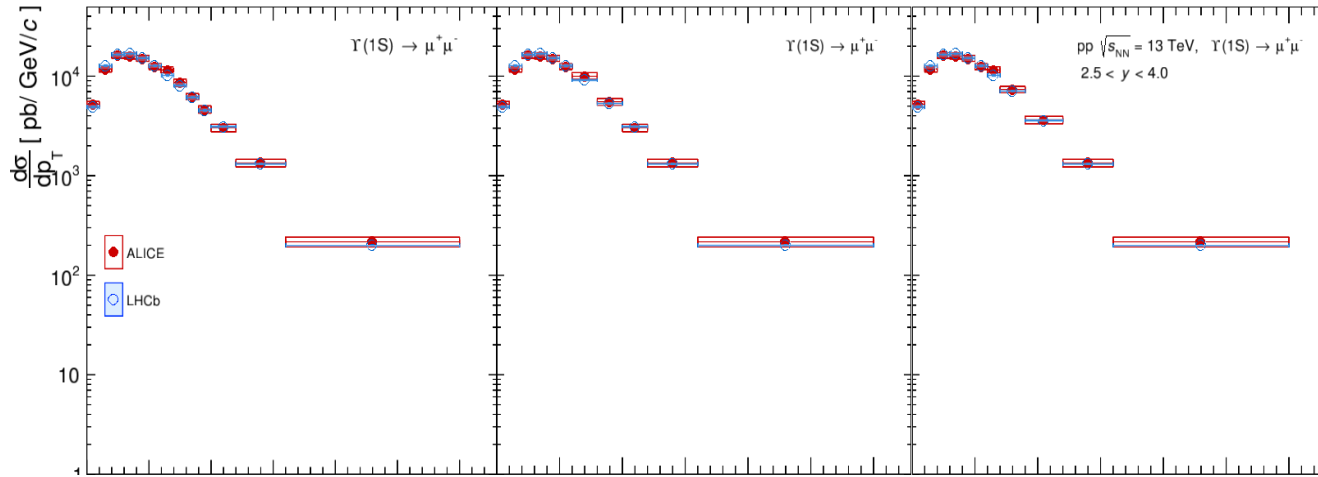
$$\Delta \sigma_{v0} = 2.0 \%$$

$$\text{Total uncertainty} = 3.46\%$$

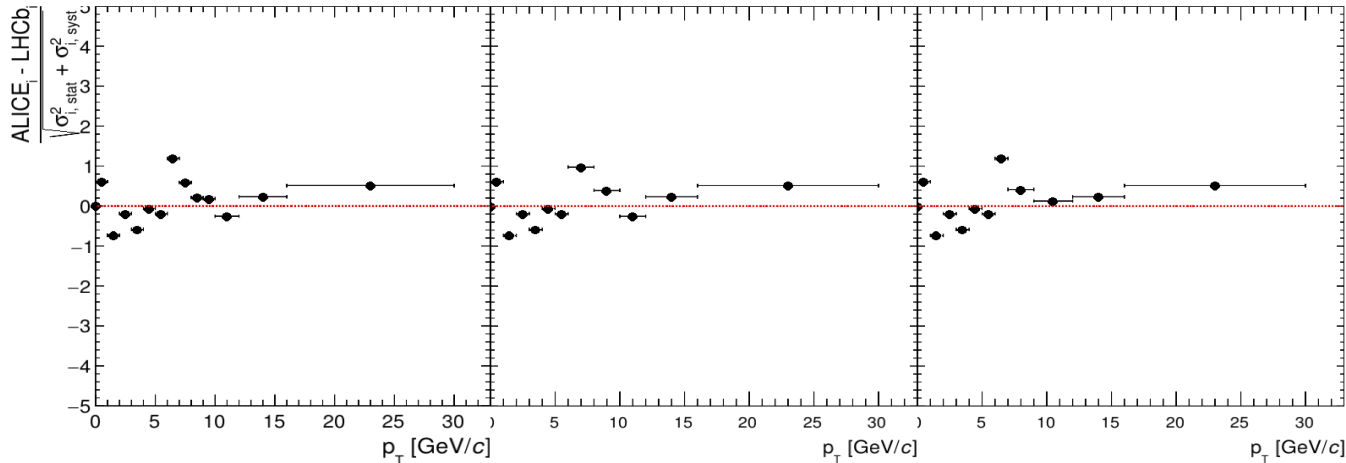
$$L_{\text{int}} = \frac{N_{\text{CMUL7,PS}} \times F_{\text{norm}}}{\sigma_{VdM} \text{ (57.8 } \pm 1.2 \text{ mb)}}$$

Taking $F_{\text{norm}} \text{ offline2}$ as default choice, integrated luminosity $26.87 \pm 0.037\%$ (stat) $\pm 3.46\%$ (syst) pb^{-1}

p_T differential $\Upsilon(1S)$ cross sections

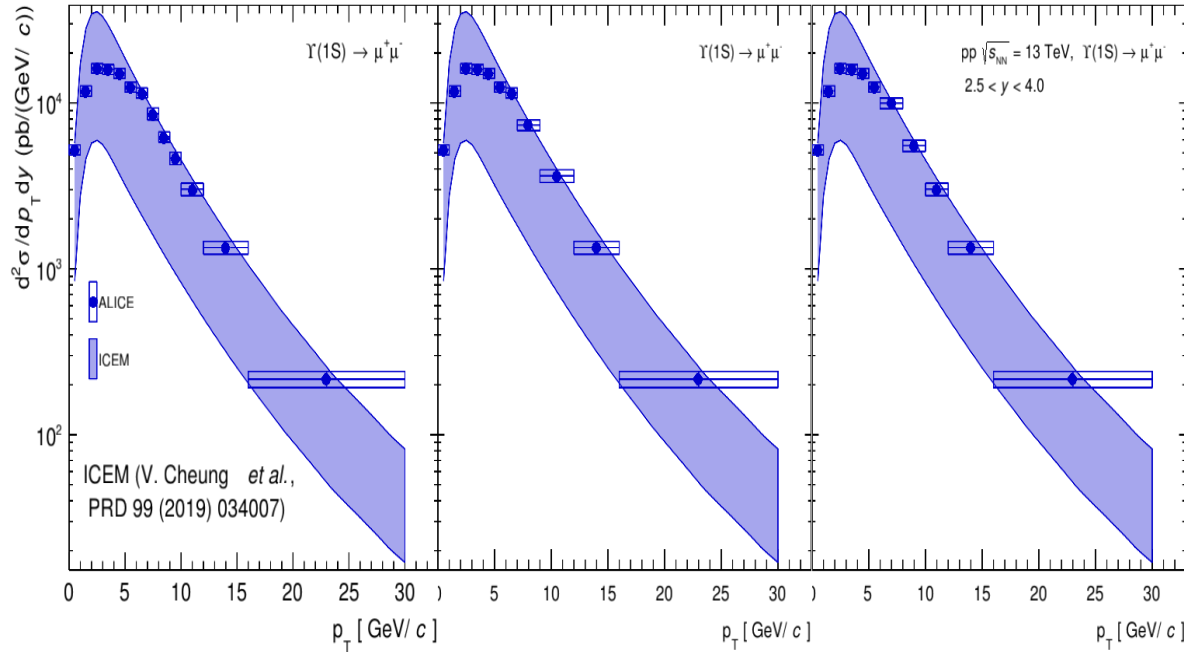


$$\frac{d^2\sigma_{\Upsilon(nS)}}{dydp_T} = \frac{N_{\Upsilon(nS)}}{A \times \varepsilon} \frac{1}{BR_{\Upsilon(nS) \rightarrow \mu^+\mu^-}} \frac{1}{\mathcal{L}_{\text{int}}} \frac{1}{\Delta y \Delta p_T}$$



$\Upsilon(1S)$ cross sections
are in good agreement
between ALICE & LHCb
→ Mostly within 1σ

p_T differential $\Upsilon(1S)$ cross sections compared to ICEM



$$\frac{d\sigma_\psi(P)}{d^3P} = F_\psi \int_{2m_c}^{2M_D} dM \frac{d\sigma_{c\bar{c}}(M, P)}{dM d^3P}$$

Colour Evaporation model

- A fixed fraction of QQbar pairs form J/ψ or $\Upsilon(nS)$, provided mass of QQbar pair $< D/B$ -meson mass threshold
- CEM is in general successful in describing quarkonium production
- A flaw in the approach: ratios of two charmonium states are independent of kinematics.

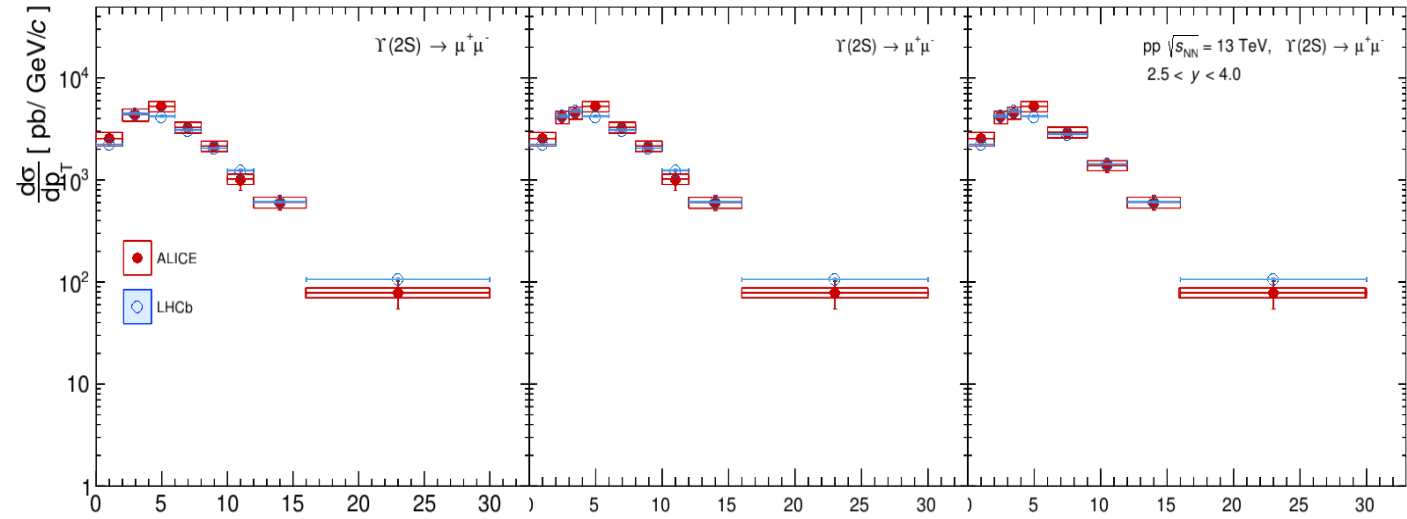
$$\frac{d\sigma_\psi(P)}{d^3P} = F_\psi \int_{M_\psi}^{2M_D} d^3P' dM \frac{d\sigma_{c\bar{c}}(M, P')}{dM d^3P'} \delta^3(P - \frac{M_\psi}{M} P')$$

Improved Colour Evaporation Model:

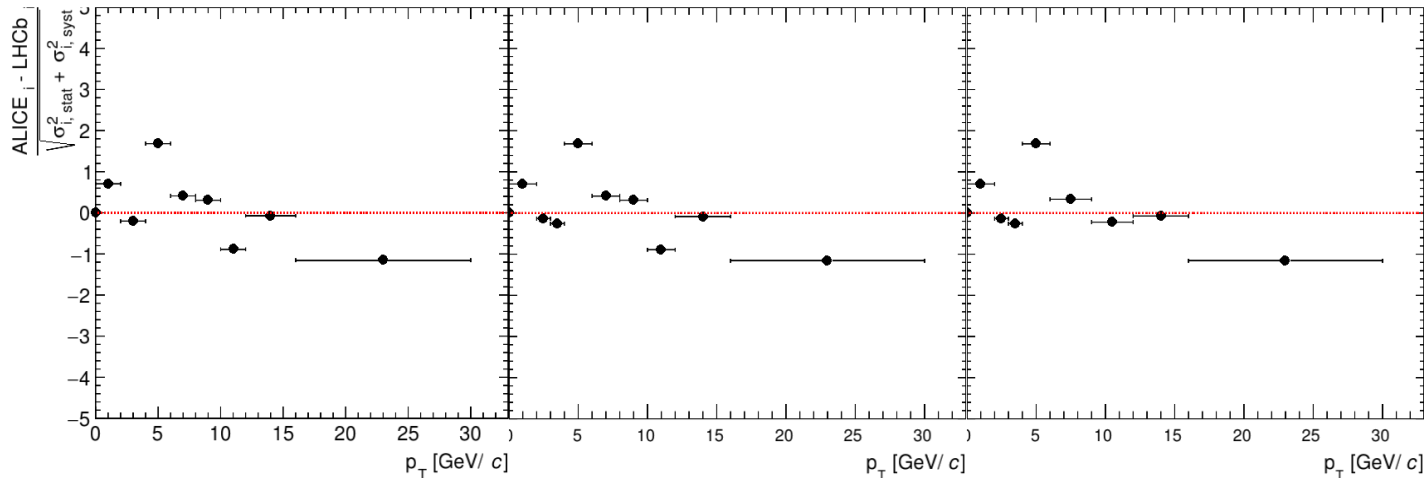
- Incorporates the kinematic dependence

In general good agreement within uncertainties

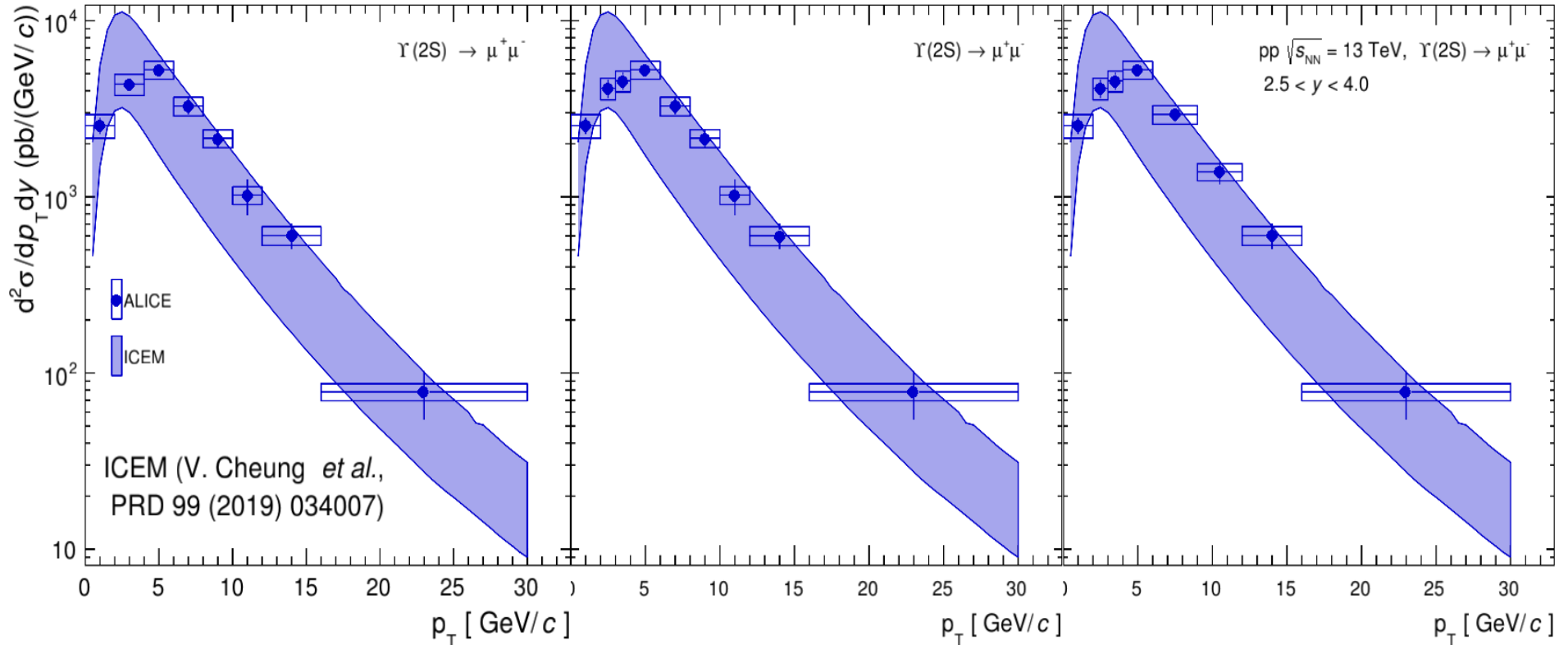
p_T differential $\Upsilon(2S)$ cross sections



$\Upsilon(2S)$ cross sections
 are in good agreement
 between ALICE & LHCb
 → Mostly within 1σ

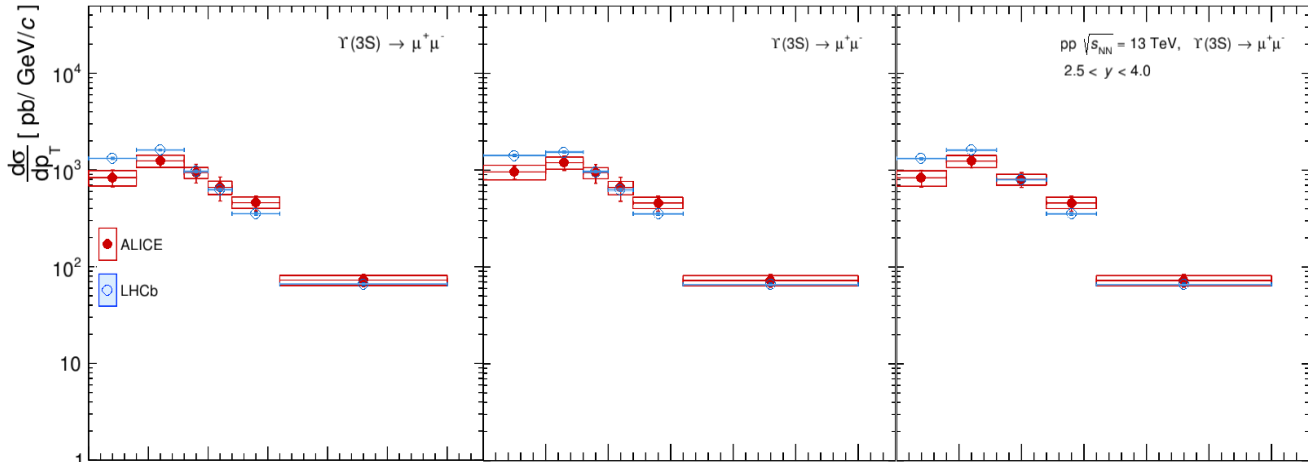


p_T differential $\Upsilon(2S)$ cross sections compared to ICEM

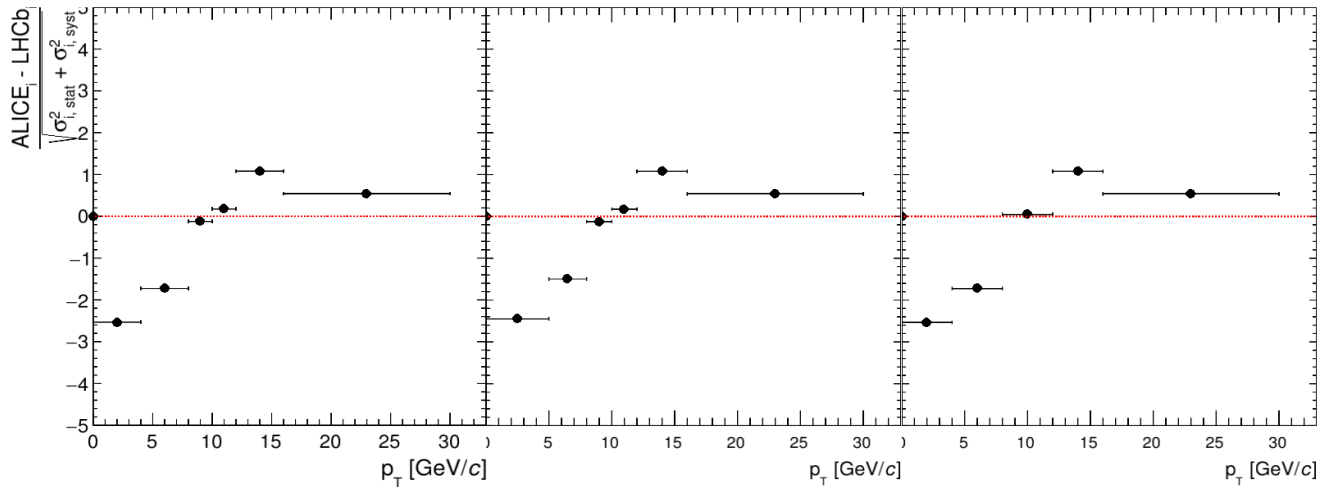


In general good agreement within uncertainties

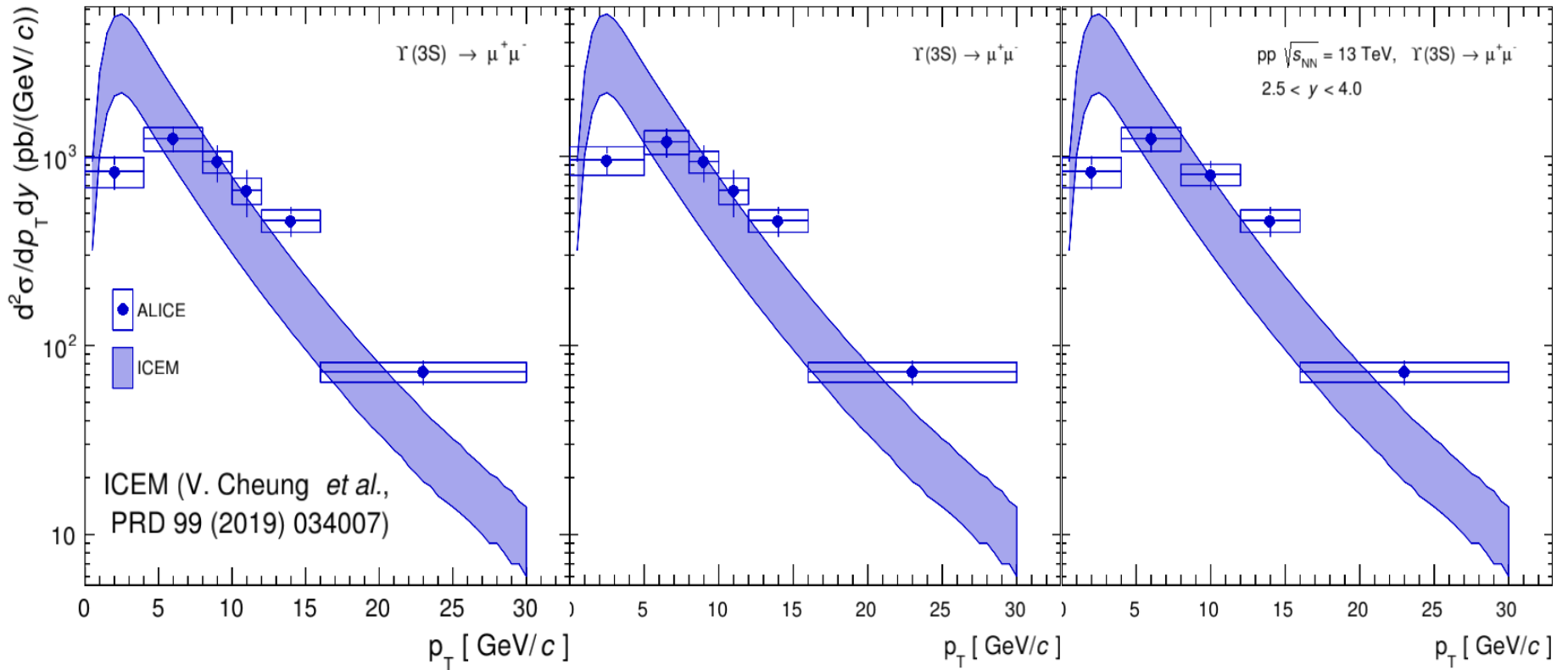
p_T differential $\Upsilon(3S)$ cross sections



$\Upsilon(3S)$ cross sections
are in low p_T bins have large
disagreement between
ALICE & LHCb
→ Agreement at high p_T is better

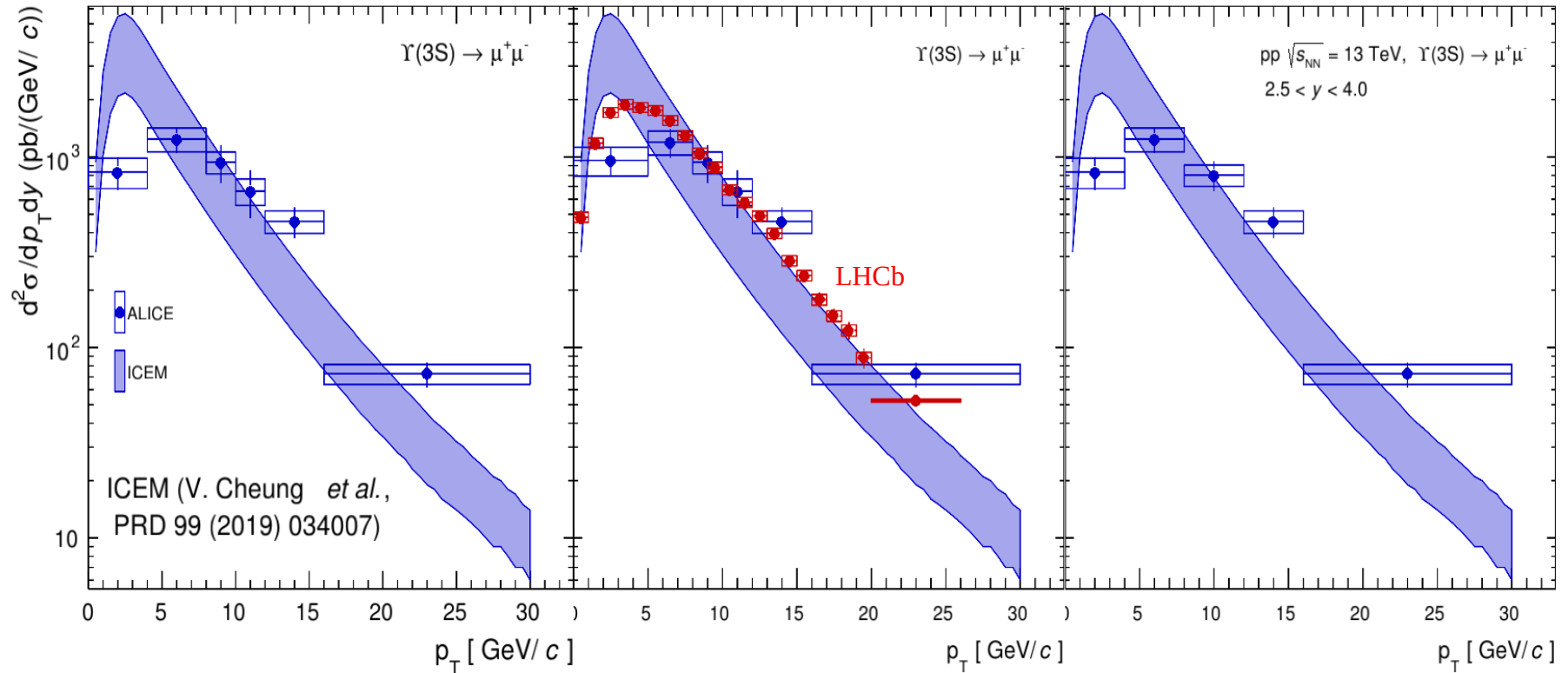


p_T differential $\Upsilon(3S)$ cross sections compared to ICEM



ICEM calculations not in a good agreement even within uncertainties

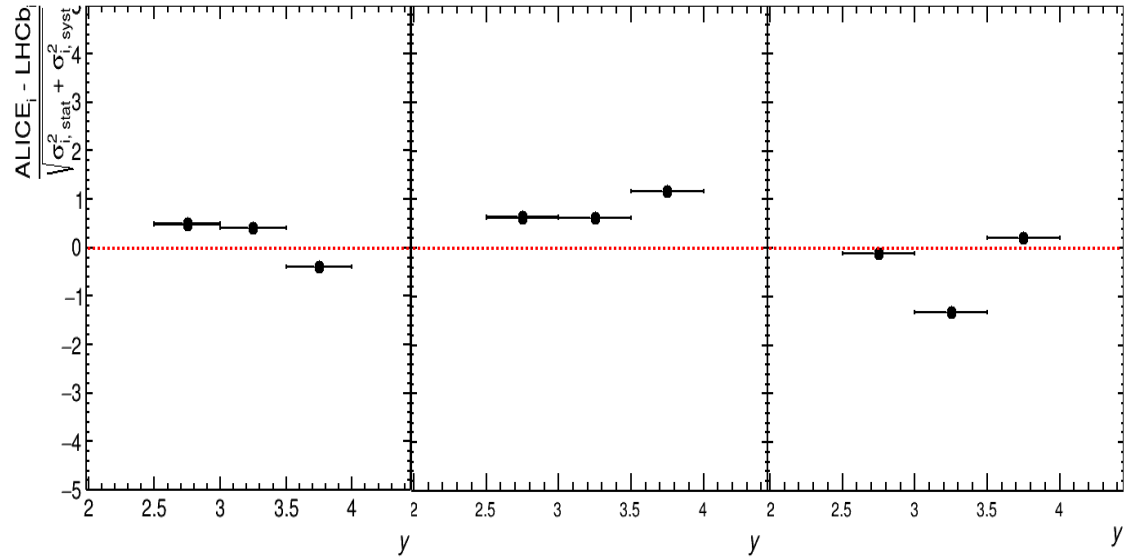
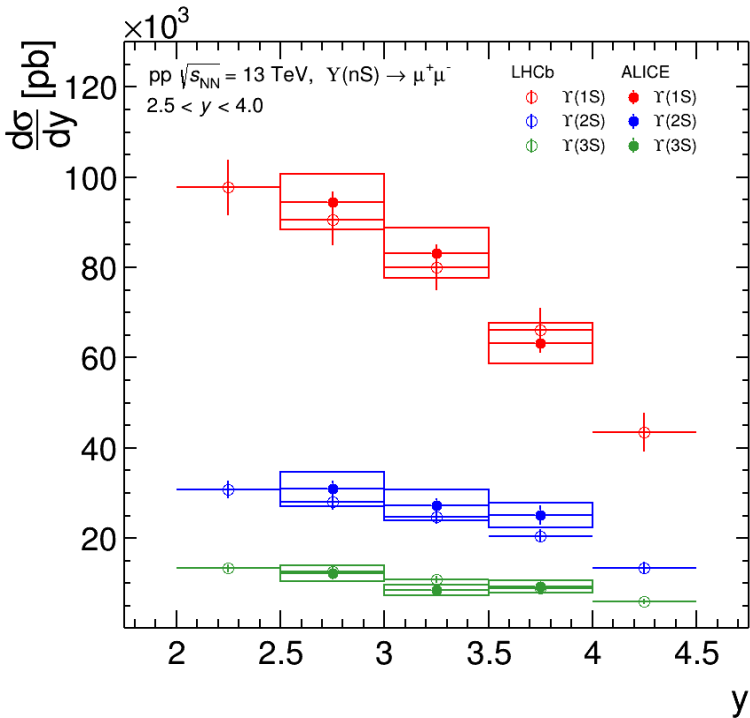
p_T differential $\Upsilon(3S)$ cross section compared to ICEM



In general not a very good agreement even within uncertainties

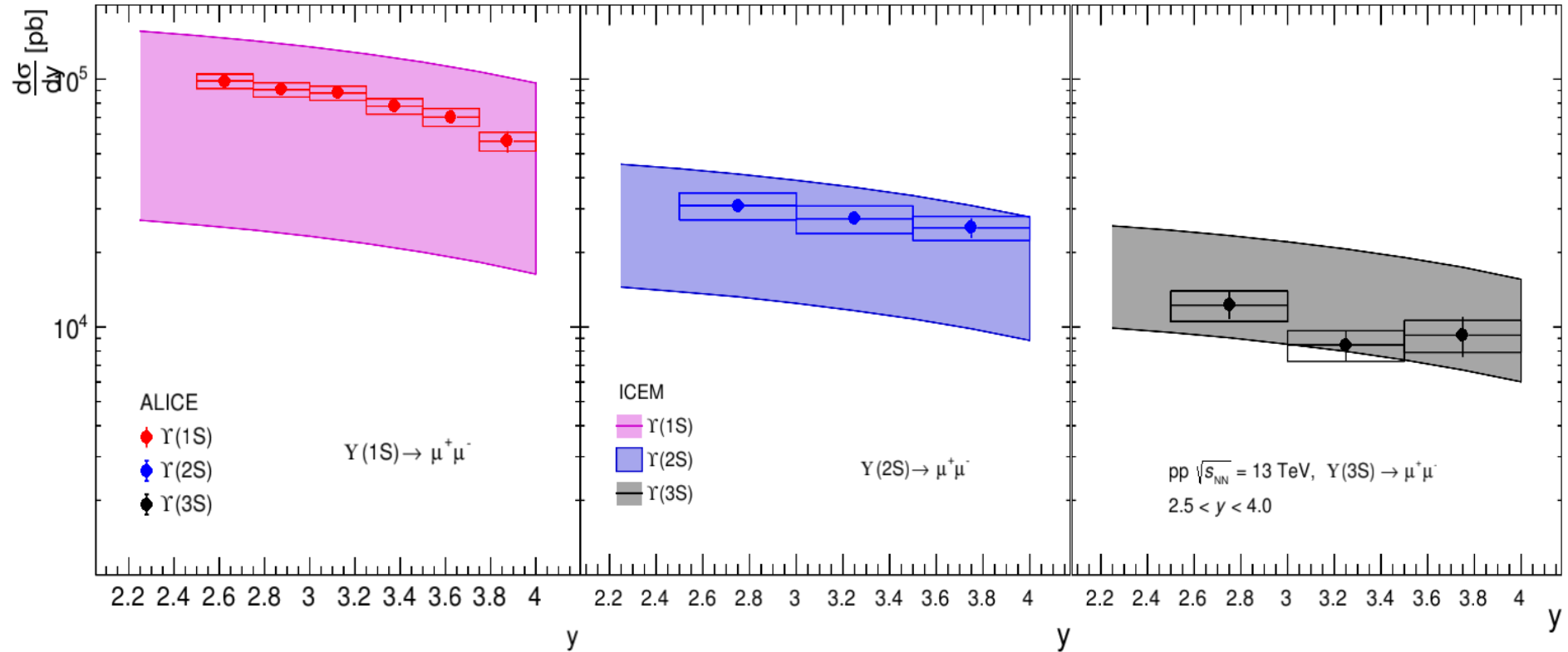
y differential $\Upsilon(nS)$ cross sections

$$\frac{d\sigma_{\Upsilon(nS)}}{dy} = \frac{N_{\Upsilon(nS)}}{A \times \varepsilon} \frac{1}{BR_{\Upsilon(nS) \rightarrow \mu^+ \mu^-}} \frac{1}{\mathcal{L}_{int}} \frac{1}{\Delta y}$$



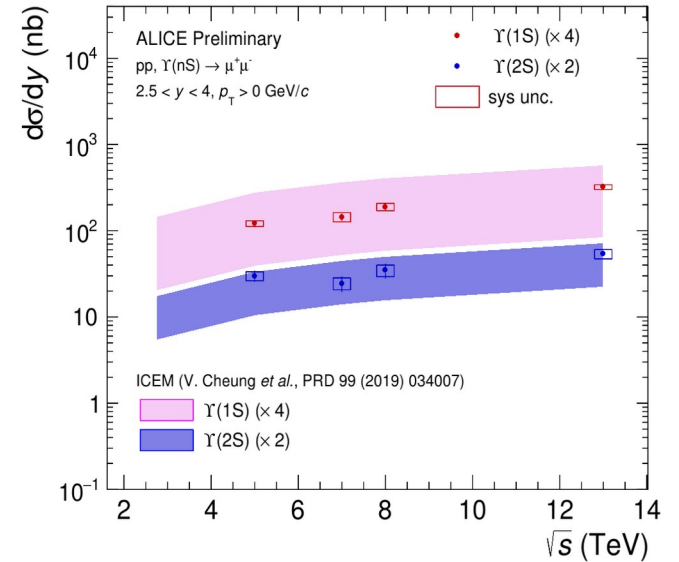
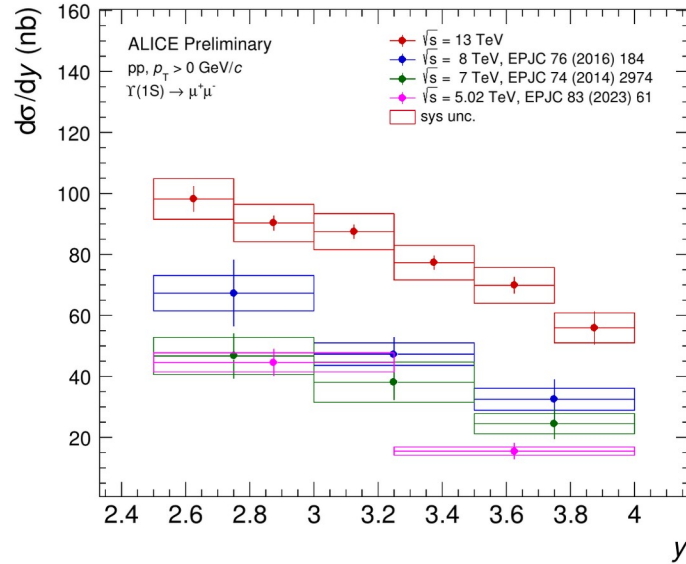
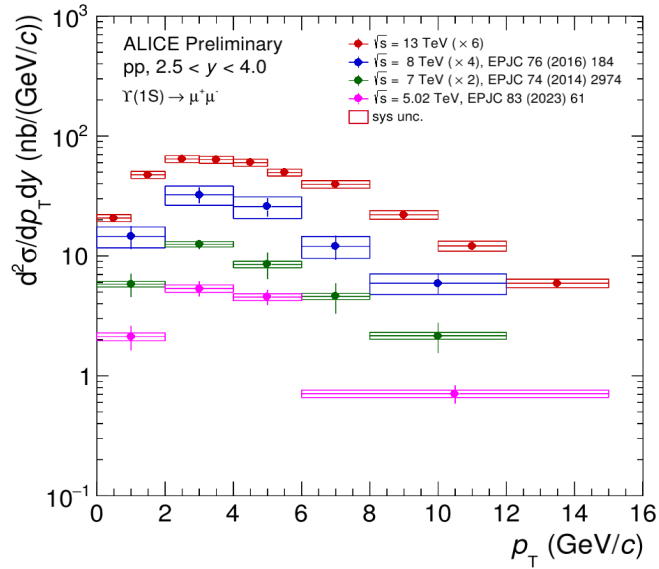
$\Upsilon(nS)$ cross sections in general have good agreement
 → Mostly within 1σ

y differential $\Upsilon(nS)$ cross sections compared to ICEM



Good agreement within uncertainties

$\Upsilon(1S \text{ \& } 2S)$ cross sections with \sqrt{s}



The cross sections of $\Upsilon(1S)$ at different collision energies are shown as functions of p_T and y .
 → ICEM model can describe the energy dependence of the production of $\Upsilon(nS)$

Integrated $\Upsilon(nS)$ cross section compared to ICEM

p_T GeV/c	$d\sigma_{\Upsilon(1S)}/dp_T \pm \text{stat [nb]}$	p_T GeV/c	$d\sigma_{\Upsilon(2S)}/dp_T \pm \text{stat [nb]}$	p_T GeV/c	$d\sigma_{\Upsilon(3S)}/dp_T \pm \text{stat [nb]}$
0-1	5.22 ± 0.32	0-2	2.54 ± 0.25	0-4	0.83 ± 0.16
1-2	11.83 ± 0.50	2-3	4.13 ± 0.49	4-8	1.24 ± 0.18
2-3	16.19 ± 0.60	3-4	4.55 ± 0.49	8-10	0.94 ± 0.21
3-4	15.94 ± 0.59	4-6	5.26 ± 0.35	10-12	0.66 ± 0.18
4-5	15.09 ± 0.57	6-8	3.28 ± 0.32	12-16	0.46 ± 0.08
5-6	12.48 ± 0.52	8-10	2.15 ± 0.26	16-30	0.07 ± 0.01
6-8	9.97 ± 0.33	10-12	1.02 ± 0.23		
8-10	5.53 ± 0.25	12-16	0.60 ± 0.09		
10-12	3.02 ± 0.21	16-30	0.08 ± 0.02		
12-16	1.34 ± 0.08				
16-30	0.21 ± 0.02				
0-30	$\sigma_{\Upsilon(1S)} = 122.09 \pm 1.64$	-	$\sigma_{\Upsilon(2S)} = 40.70 \pm 1.52$	-	$\sigma_{\Upsilon(3S)} = 14.30 \pm 1.16$

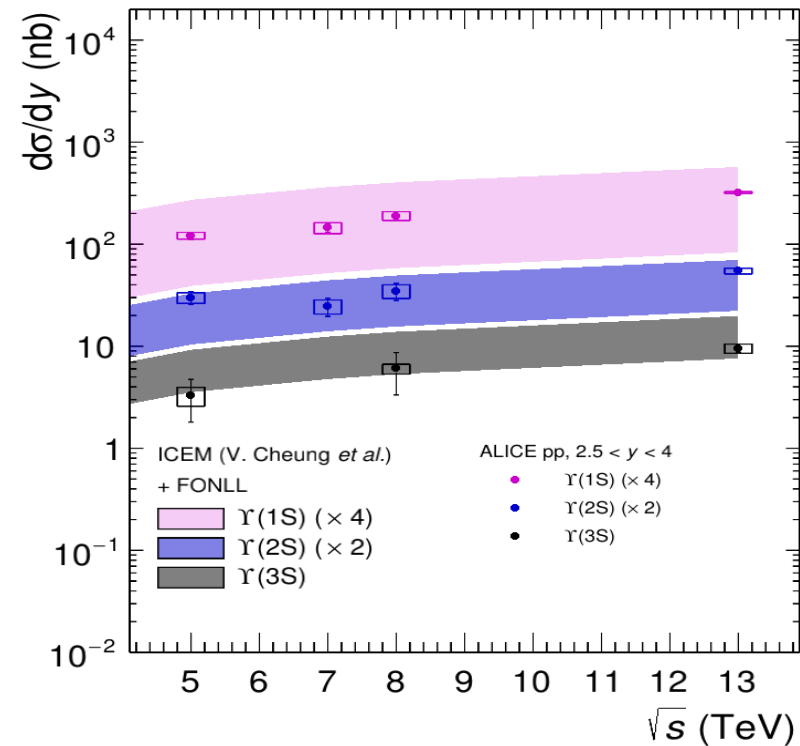
Table 9: p_T -differential cross sections of $\Upsilon(nS)$, shown in Fig 17 are tabulated here.

y	$d\sigma_{\Upsilon(1S)}/dy \pm \text{stat [nb]}$	y	$d\sigma_{\Upsilon(2S)}/dy \pm \text{stat [nb]}$	$d\sigma_{\Upsilon(3S)}/dy \pm \text{stat [nb]}$
2.5-2.75	98.22 ± 4.20	2.5-3.0	30.90 ± 1.87	12.25 ± 1.47
2.75-3.0	90.63 ± 2.46	3.0-3.5	27.31 ± 1.44	8.46 ± 1.13
3.0-3.25	87.84 ± 2.24	3.5-4.0	25.13 ± 2.18	9.27 ± 1.65
3.25-3.50	77.76 ± 2.28			
3.50-3.75	70.24 ± 2.71			
3.75-4.00	56.14 ± 5.40			
2.5-4.0	$\sigma_{\Upsilon(1S)} = 120.21 \pm 2.09$	-	$\sigma_{\Upsilon(2S)} = 41.67 \pm 1.60$	$\sigma_{\Upsilon(3S)} = 14.99 \pm 1.24$

Table 10: Rapidity-differential cross sections of $\Upsilon(nS)$ as shown in left panel of Fig. 19

$\Upsilon(nS)$	$N_{\text{raw}} \pm \text{stat} \pm \text{syst}$	$A\epsilon$	BR	Lum [pb^{-1}]	$\sigma \pm \text{stat} \pm \text{syst [nb]}$
1S	$24,314 \pm 332 \pm 499$	0.3024	0.0248	26.87	$120.65 \pm 1.65 \pm 2.49$
2S	$6408 \pm 231 \pm 416$	0.3036	0.0193	-	$40.70 \pm 1.47 \pm 2.65$
3S	$2478 \pm 206 \pm 256$	0.3051	0.0213	-	$14.27 \pm 1.18 \pm 1.47$

Table 11: Integrated cross sections obtained independently from the fit to inclusive mass spectra.



Integrated cross sections agree well with differential estimations

Summary

1. $\Upsilon(nS)$ cross sections are measured as a function of $p_T (< 30 \text{ GeV})$ and y
2. Cross sections are compared to LHCb, agreement within 1σ in most bins
3. Compared with ICEM model calculations, $\Upsilon(1S \text{ and } 2S)$ agrees well

Ongoing work:

Systematic error calculations related to track and trigger matching efficiency

Remaining task:

1. Comparison to other model calculations

Paper proposal:

1. Merged paper proposal of THIS analysis + $\Upsilon(1S)$ polarization anticipated soon

Thank you

Fit Functions

$$f(x; \mu, \sigma, \alpha_L, n_L, \alpha_R, n_R) = N \cdot \begin{cases} \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right) & \text{for } \alpha_R > \frac{x-\mu}{\sigma} > -\alpha_L \\ A \cdot \left(B - \frac{x-\mu}{\sigma}\right)^{-n_L} & \text{for } \frac{x-\mu}{\sigma} \leq -\alpha_L \\ C \cdot \left(D + \frac{x-\mu}{\sigma}\right)^{-n_R} & \text{for } \frac{x-\mu}{\sigma} \geq \alpha_R \end{cases}$$

$$A = \left(\frac{n_L}{|\alpha_L|}\right)^{n_L} \cdot \exp\left(-\frac{|\alpha_L|^2}{2}\right)$$

$$B = \frac{n_L}{|\alpha_L|} - |\alpha_L|$$

$$C = \left(\frac{n_R}{|\alpha_R|}\right)^{n_R} \cdot \exp\left(-\frac{|\alpha_R|^2}{2}\right)$$

$$B = \frac{n_R}{|\alpha_R|} - |\alpha_R|$$

Double Exponential

The following Double Exponential (DE) function have been used to fit the background of dimuon spectrum,

$$f(x) = e^{a_1+b_1x} + e^{a_2+b_2x}$$

where a_1, a_2, b_1, b_2 are fitting parameters.

Double Power Law

The second function which have been used for background estimation is Double Power Law (DP),

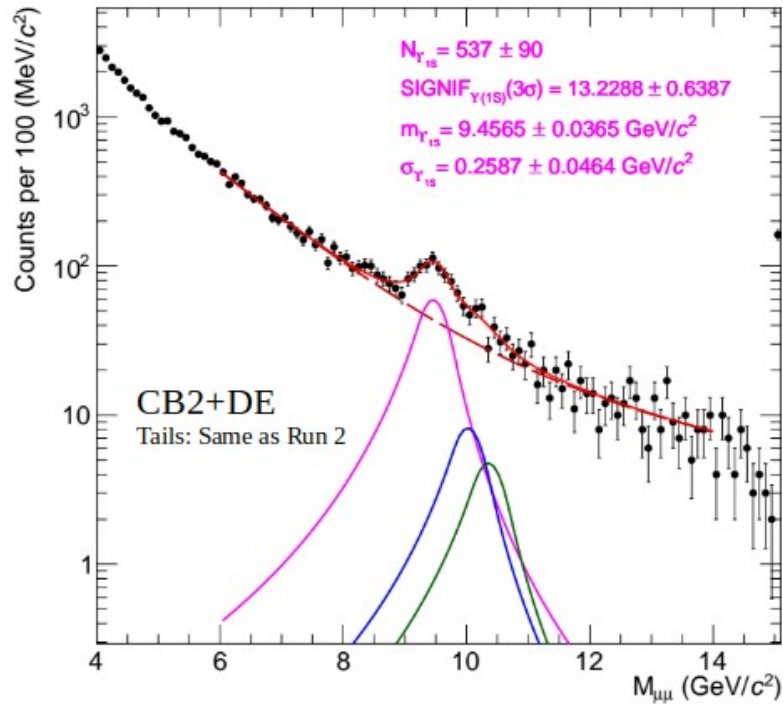
$$f(x) = N_1 \cdot x^{a_1} + N_2 \cdot x^{a_2}$$

Systematic tags

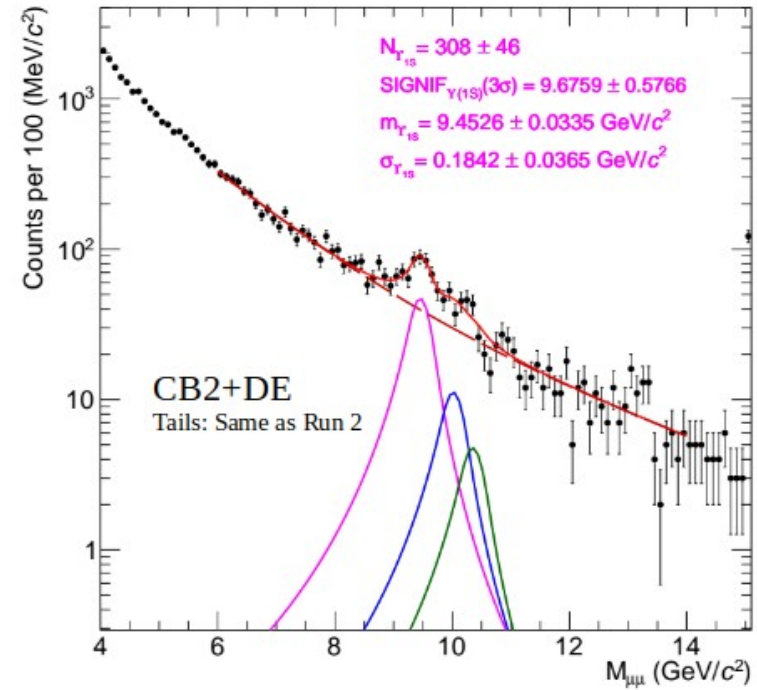
Bkg. Func	Fit Range	Tail type	Tag
DE	6-14	data	000
	7-12		001
	5-14		002
DP	6-14	data	003
	7-12		004
	5-14		005
VWG	6-14	data	006
	7-12		007
	5-14		008

Bkg. Func	Fit Range	Tail type	Tag
DE	6-14	MC	009
	7-12		010
	5-14		011
DP	6-14	MC	012
	7-12		013
	5-14		014
VWG	6-14	MC	015
	7-12		016
	5-14		017

Invariant mass distribution @ 13.6 TeV



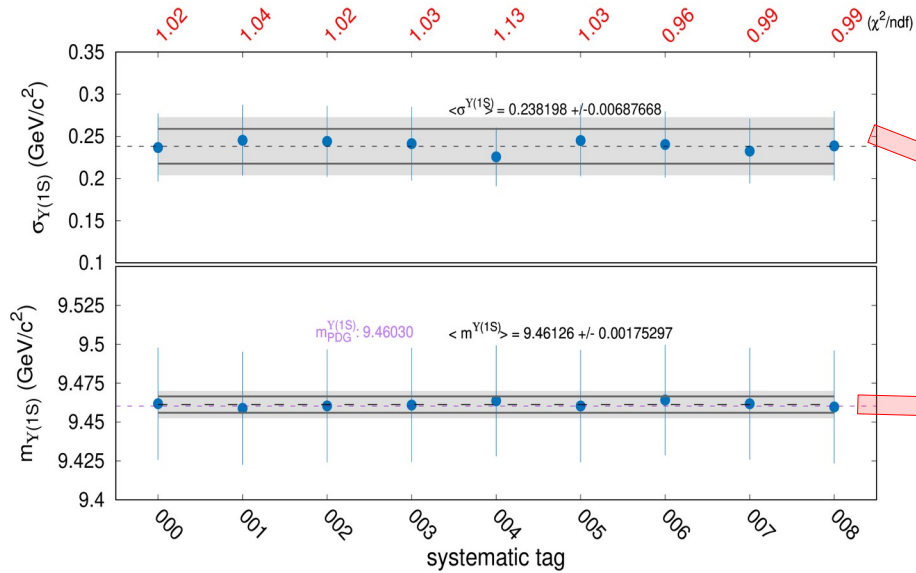
standard track association



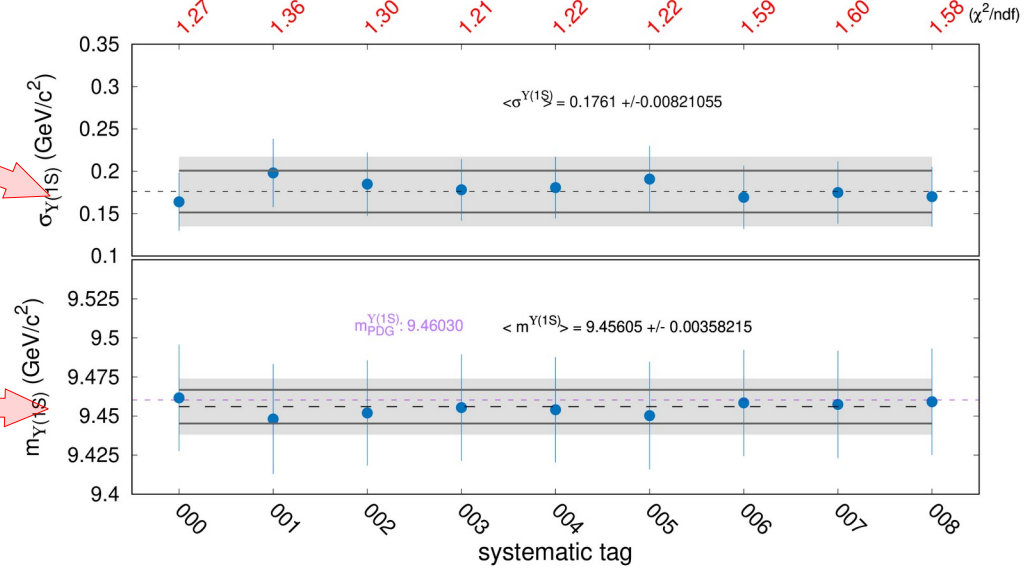
time compatible track association (2σ)

- Improvement in mass resolution
- Mass position remains same

Systematics of mass position resolution



standard track association



time compatible track association (2 σ)

- Improvement in mass resolution is apparent for all variations in fit
- Statistics is however, limited