

# On the SMEFT Basis for aQGCs

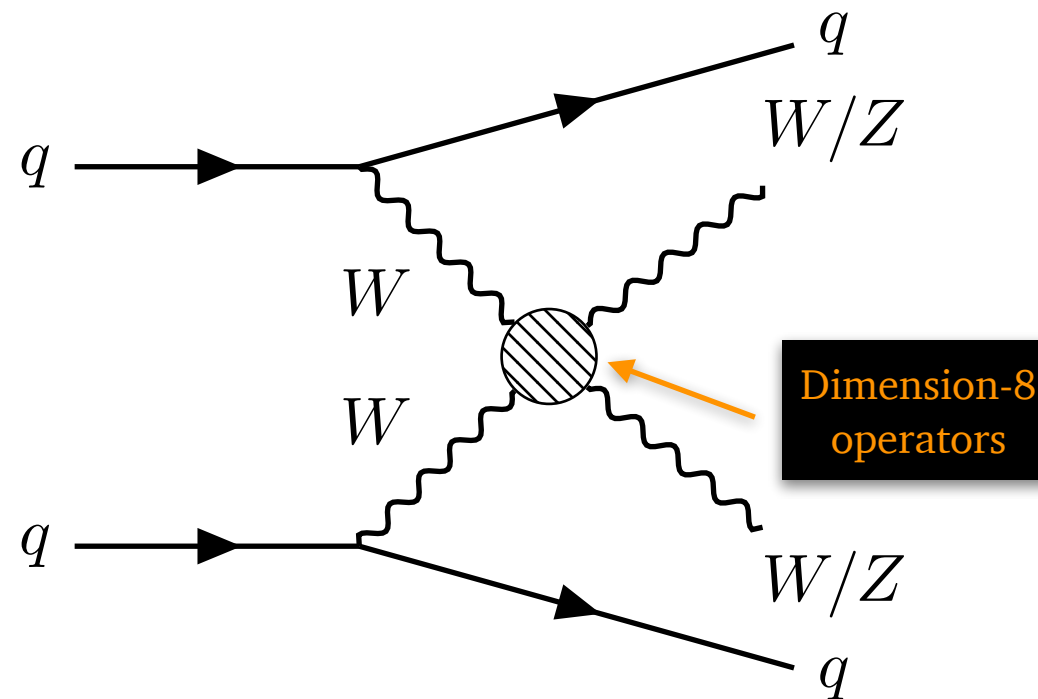
[2411.02483 w/ Durieux, Remmen, Éboli, Gonzalez-Garcia, Kondo, Murayama, Okabe]



# Motivation

Dim-8 SMEFT allows anomalous quartic gauge couplings\*

[Eboli, Gonzalez-Garcia,  
Mizukoshi 2006]



aQGCs modify SM couplings (e.g.  $W^4$ ) and induce new ones (e.g.  $Z^4$ )

\*Dim-6 contributions strongly  
constrained by triple gauge  
couplings, e.g. [Butter+ 2006]

# Motivation

Improvements are a clear target for HL LHC

**Evidence for Electroweak Production of  $W^\pm W^\pm jj$  in  $pp$  Collisions at  $\sqrt{s} = 8$  TeV with the ATLAS Detector**

[ATLAS 2014] - sensitive to  $WWWW$

**Evidence for electroweak production of two jets in association with a  $Z\gamma$  pair in  $pp$  collisions at  $\sqrt{s} = 13$  TeV with the ATLAS detector**

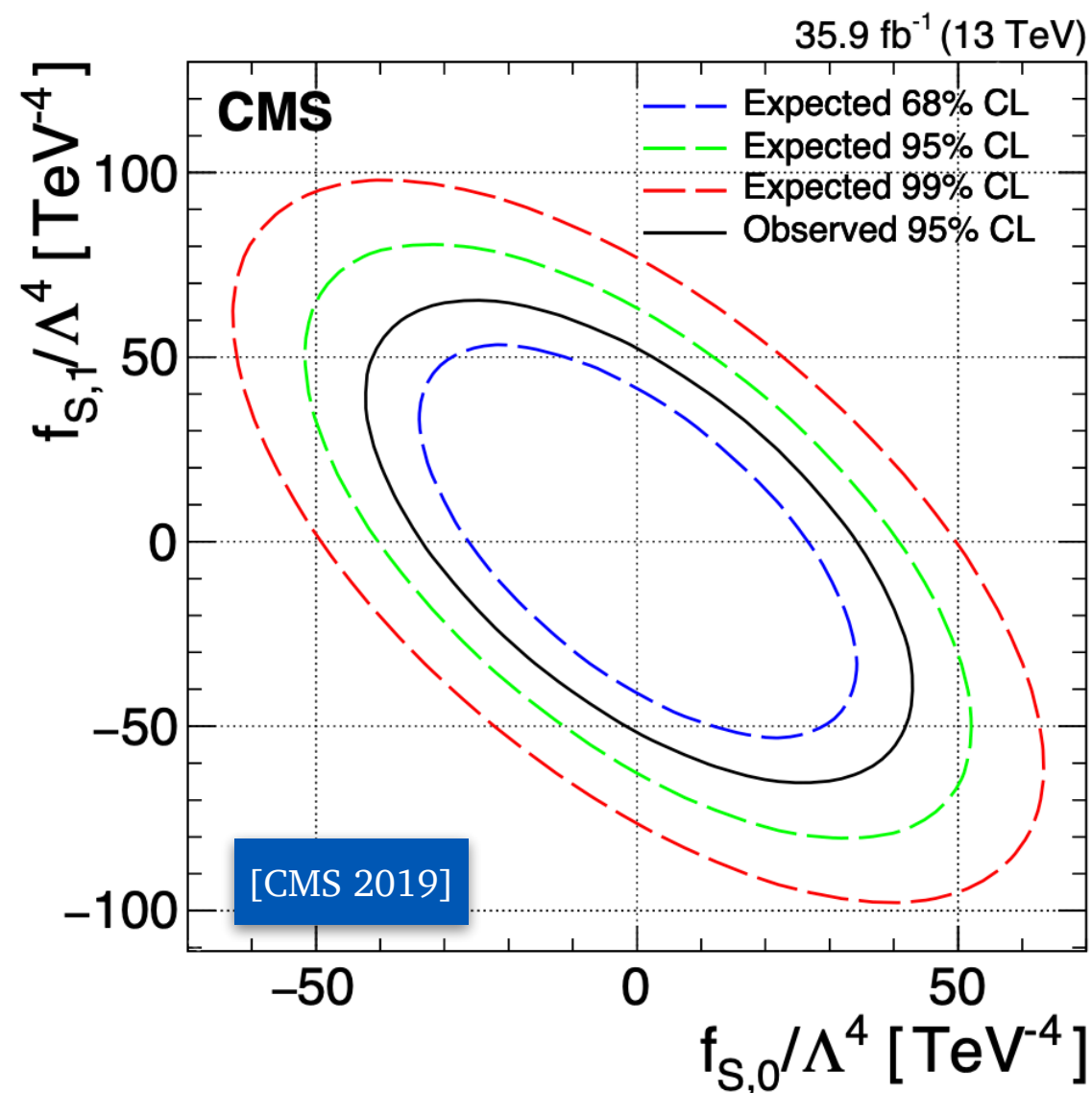
[ATLAS 2020] - sensitive to  $WWZ\gamma$

**Observation of electroweak production of two jets and a Z-boson pair with the ATLAS detector at the LHC**

[ATLAS 2020] - sensitive to  $WWZZ$

**Observation of photon-induced  $W^+W^-$  production in  $pp$  collisions at  $\sqrt{s} = 13$  TeV using the ATLAS detector**

[ATLAS 2021] - sensitive to  $WW\gamma\gamma$

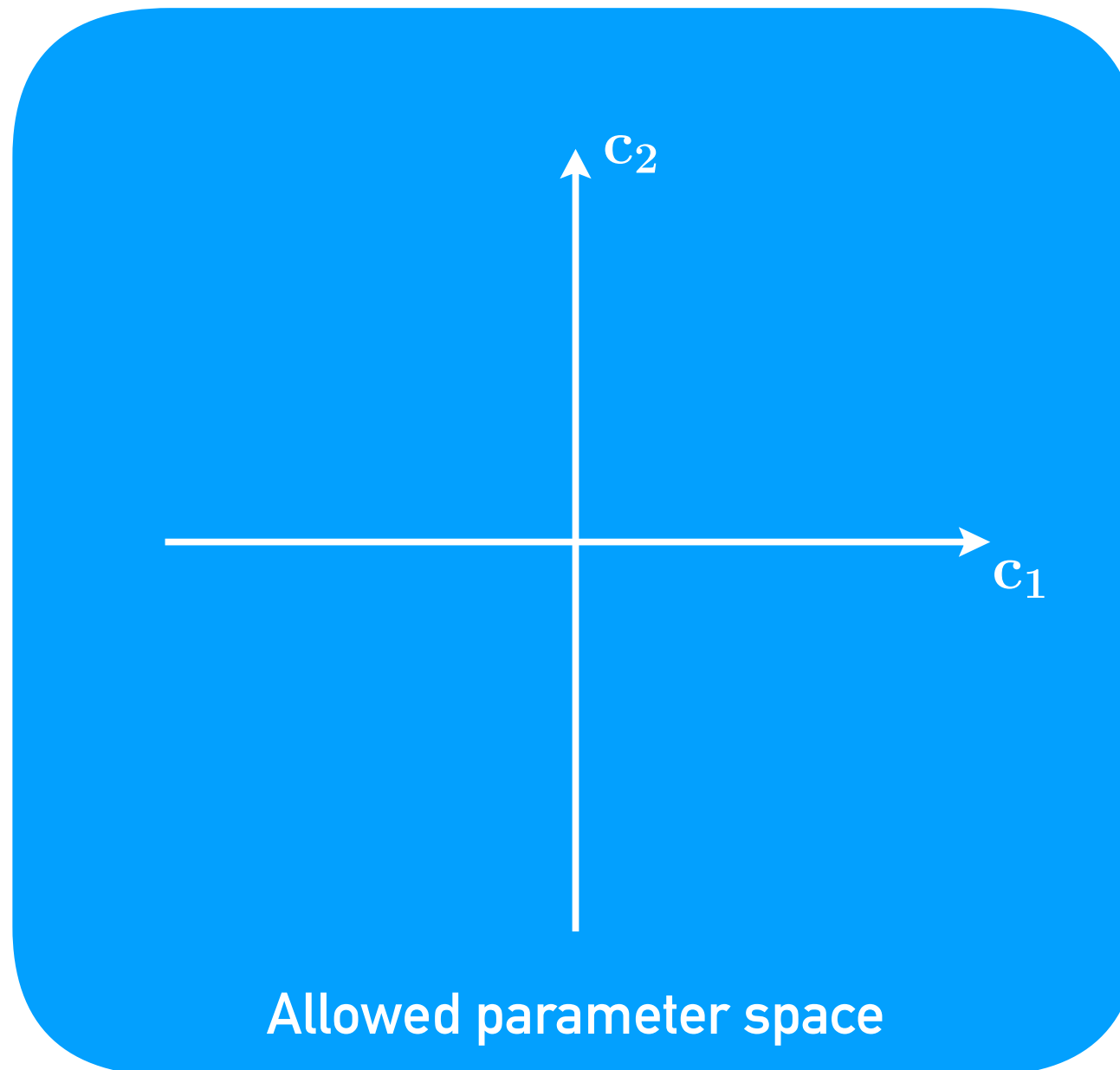


Very incomplete list!

# Motivation

Theoretically very interesting due to **positivity bounds**

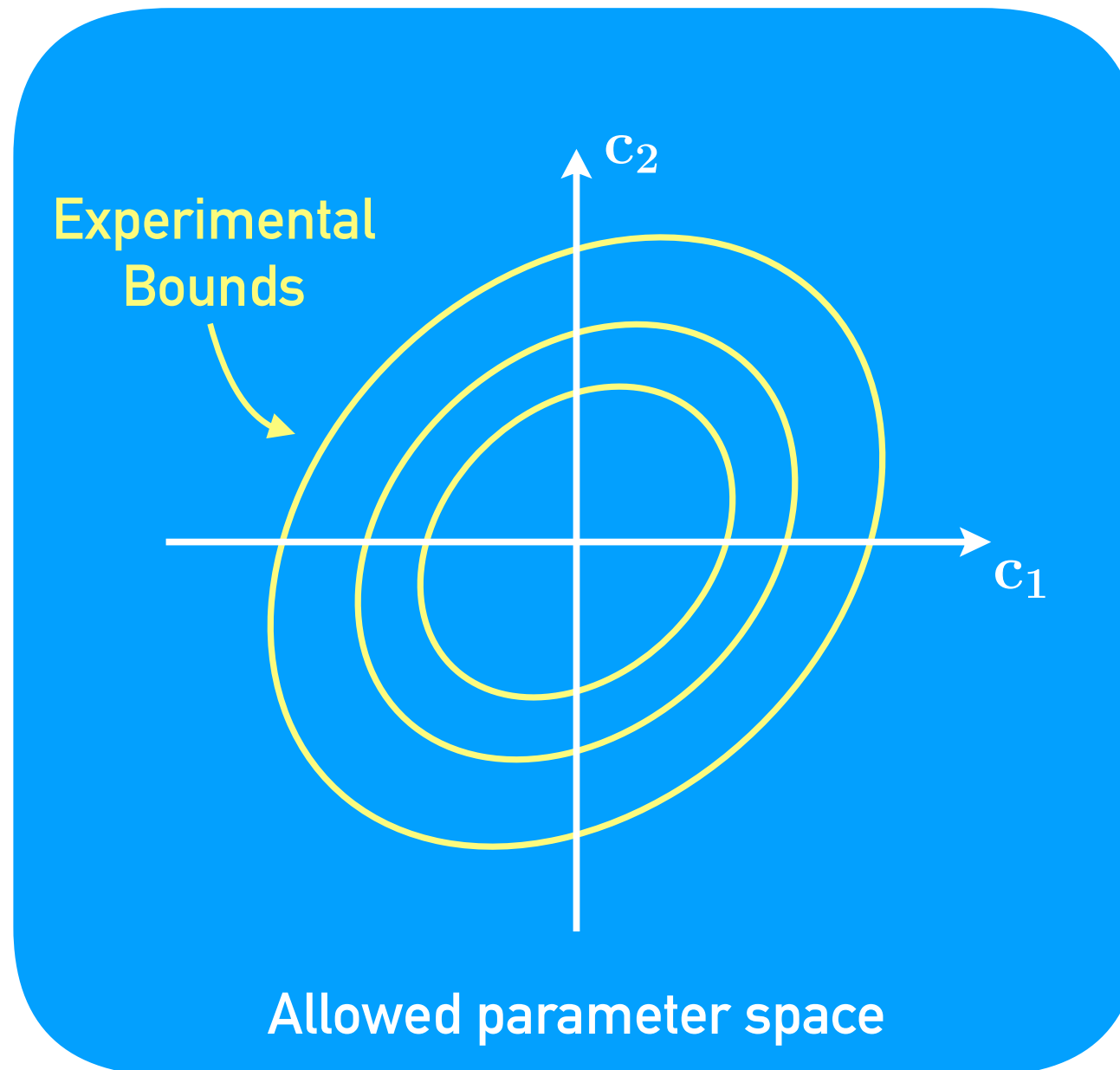
Application to the SMEFT,  
e.g. [Remmen, NLR 2019],  
[Zhang, Zhou 2020]



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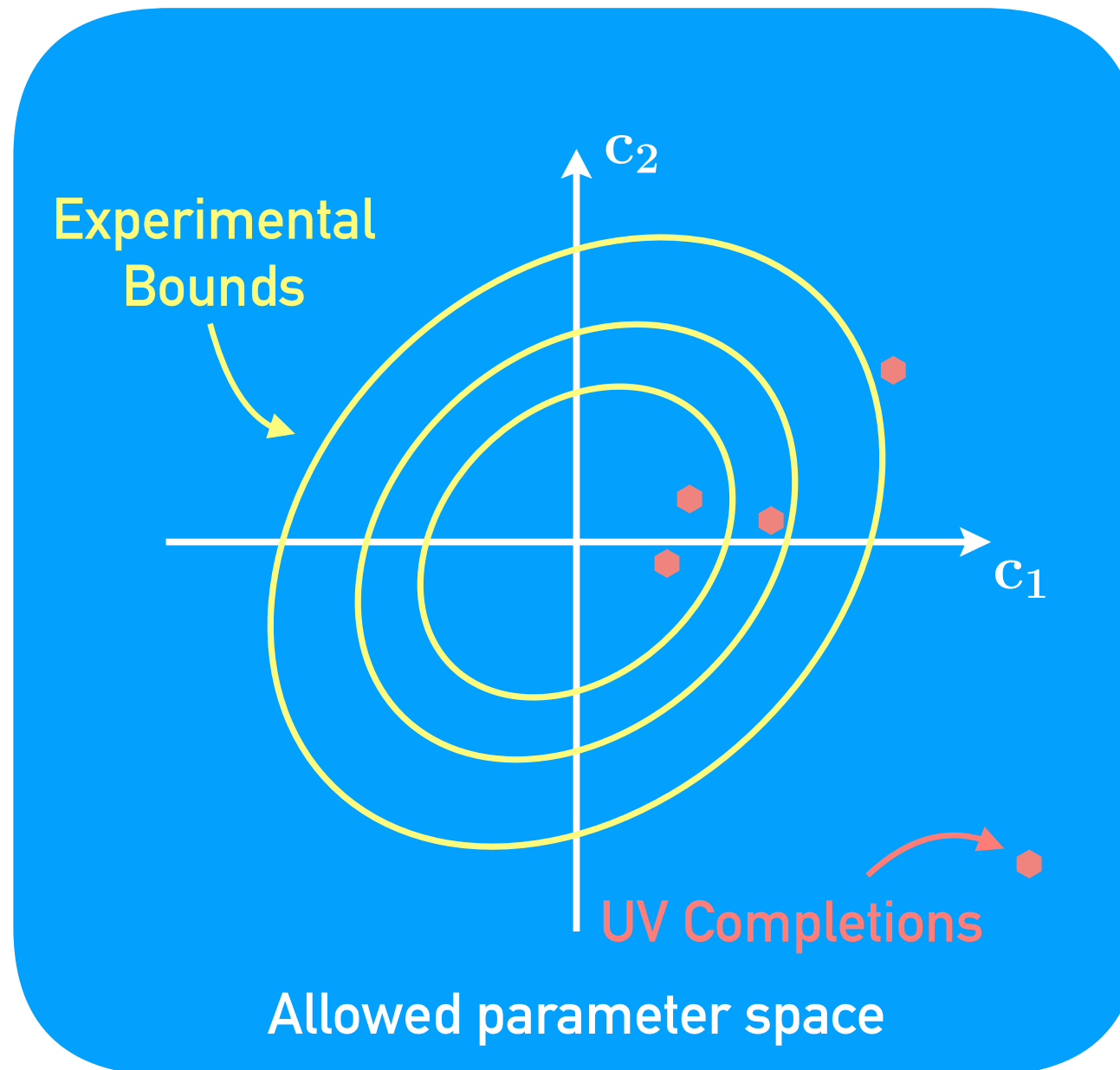
Application to the SMEFT,  
e.g. [Remmen, NLR 2019],  
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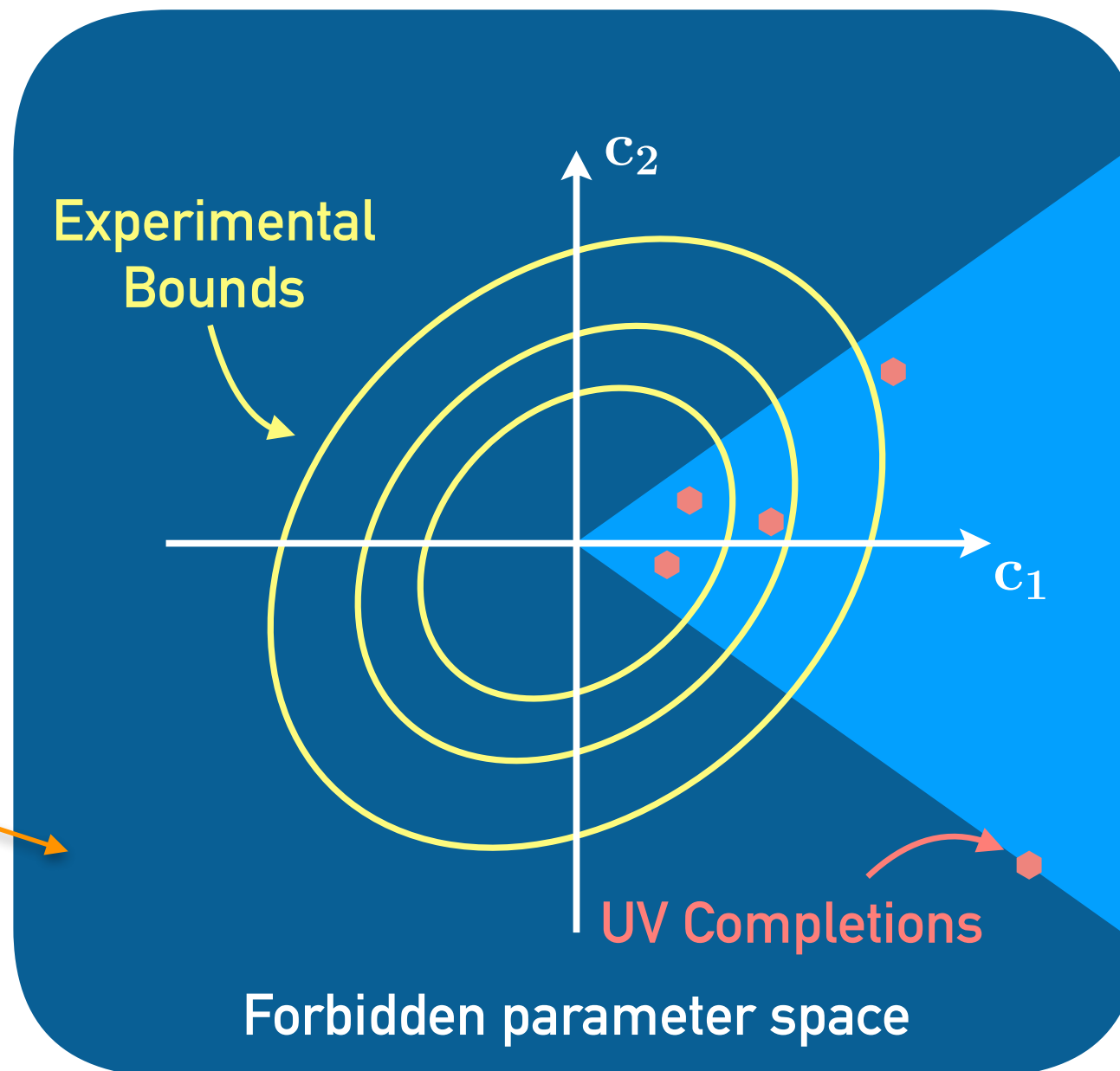




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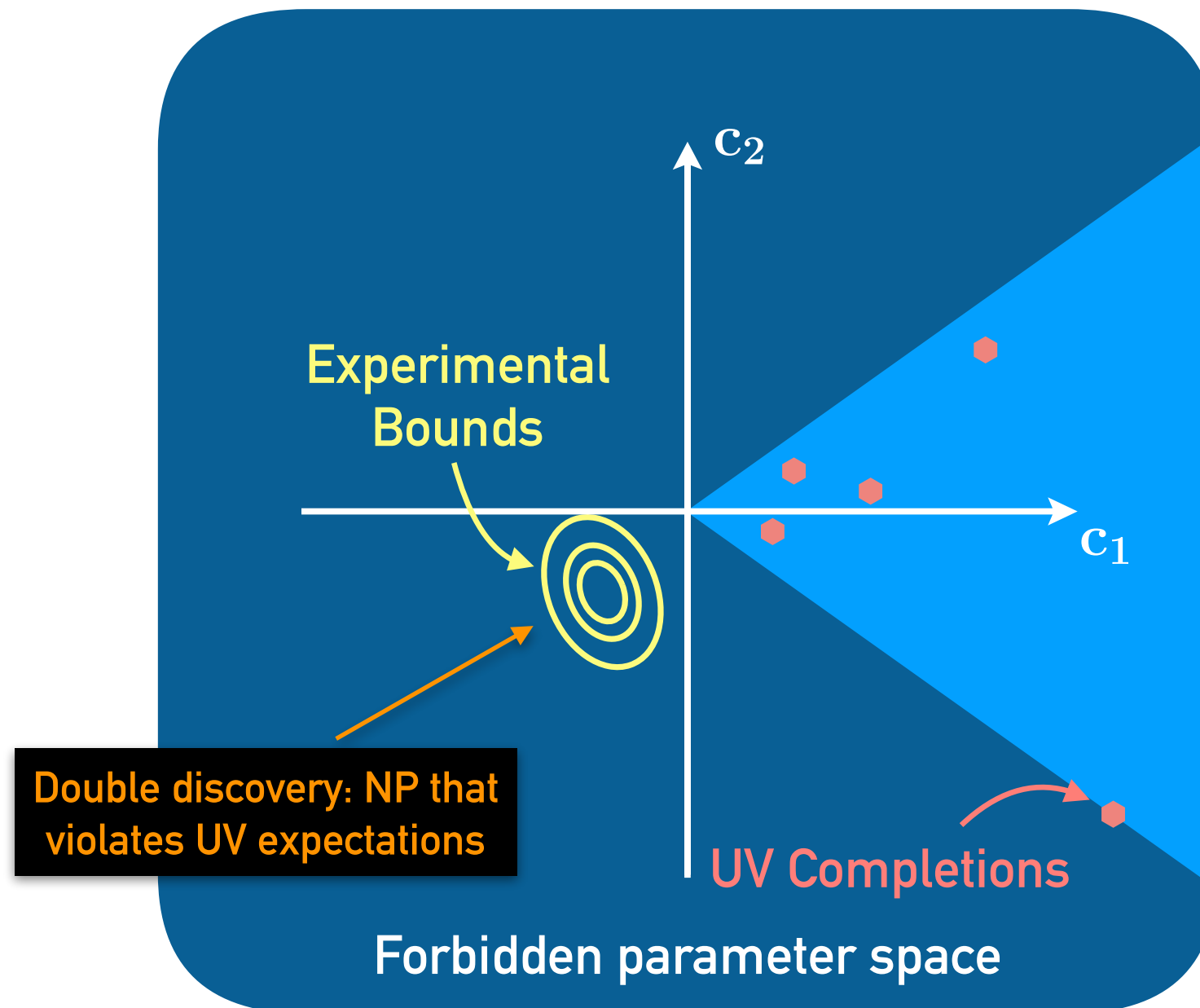


Forbidden if assume  
UV obeys unitarity,  
locality, and causality

# Motivation

Theoretically very interesting due to **positivity bounds**

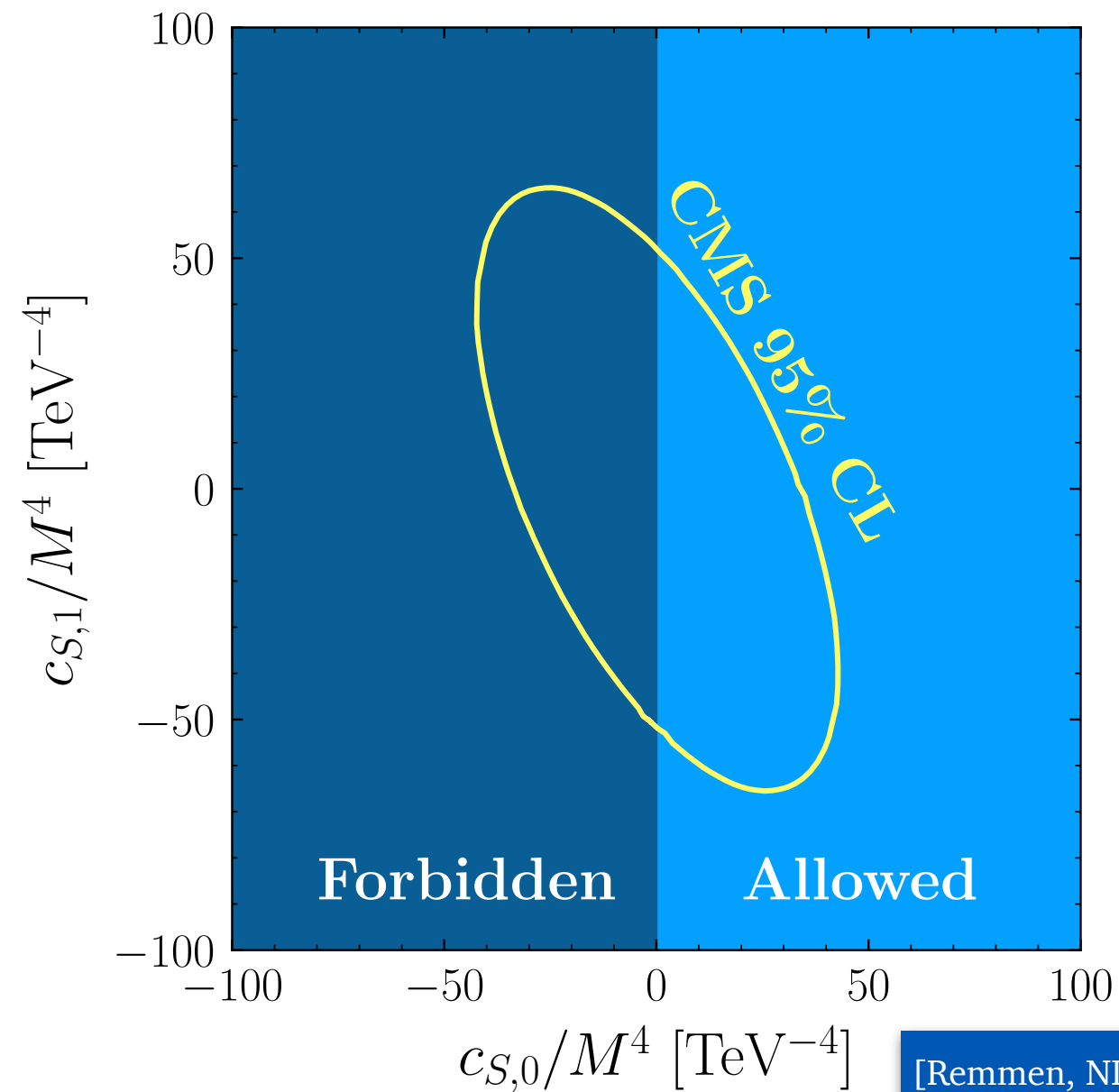
Application to the SMEFT,  
e.g. [Remmen, NLR 2019],  
[Zhang, Zhou 2020]





# Motivation

aQGCs ideal target for positivity



[Remmen, NLR 2019]

# Motivation

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Step 0 in accessing all of this physics:  
complete EFT basis for aQGCs

# The Basis

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Three types of operators:

Scalar (S-type):  $(\partial H)^4$

Mixed (M-type):  $(\partial H)^2 F^2$

Tensor (T-type):  $F^4$

*But how many of each?*

Notation from  
[Eboli+ 2006]

# The Basis

There has been several attempts

- Almeida, Éboli, Gonzalez-Garcia, Mizukoshi 06, 16, 20
  - Redundancies and omissions corrected in 16 and 20
  - Focused on C-even and P-even operators
  - *Two C-odd & P-odd operators missing*
- Remmen, NLR 19
  - CP-even and -odd all listed and distinguished
  - *CP properties misidentified on 3 operators*
- Murphy 20 (see also Li, Ren, Shu, Xiao, Yu, Zheng 20)
  - same operators as RR, but different naming
  - *CP-even and -odd operators not distinguished*
- Kondo, Murayama, Okabe 22
  - CP-even & odd operators counted using Hilbert series
  - *Misidentified two explicit CP-even vs. odd operators*

Challenge primarily in identifying the properties of operators under C

# The Basis

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Situation had become murky: many papers with wrong basis

Solution: bring all relevant authors together, resolve the issue and publicize that resolution to the community

# The Basis

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## LHC EFT WG Note:

## Basis for Anomalous Quartic Gauge Couplings

*Gauthier Durieux,<sup>1,\*</sup> Grant N. Remmen,<sup>2,\*</sup> Nicholas L. Rodd,<sup>3,\*</sup> O. J. P. Éboli,<sup>4</sup>  
M. C. Gonzalez-Garcia,<sup>5,6</sup> Dan Kondo,<sup>7</sup> Hitoshi Murayama,<sup>3,7</sup> Risshin Okabe<sup>7</sup>*

*\*Editors*

- Minimal basis containing all operators, both CP-even and CP-odd, with all CP properties identified and explained
- Approved by the LHC WG - *thanks for feedback, especially the conveners I. Brivio, K. Potamianos, M. Presilla, D. Sutherland*
- UFO implementation made publicly available here:
  - <https://github.com/gdurieux/aqgc>

# The Basis

aQGC Operator Basis	C P	Almeida, Éboli, Gonzalez-Garcia [3]	Remmen & Rodd [4]	Murphy [6]
$\mathcal{O}_0^S$	++	$\mathcal{O}_{S,0}$	$\mathcal{O}_2^{H^4}$	$Q_{H^4}^{(2)}$
$\mathcal{O}_1^S$	++	$\mathcal{O}_{S,1}$	$\mathcal{O}_3^{H^4}$	$Q_{H^4}^{(3)}$
$\mathcal{O}_2^S$	++	$\mathcal{O}_{S,2}$	$\mathcal{O}_1^{H^4}$	$Q_{H^4}^{(1)}$
$\mathcal{O}_0^M$	++	$\mathcal{O}_{M,0}$	$\frac{1}{2}\mathcal{O}_2^{H^2W^2}$	$\frac{1}{2}Q_{W^2H^2D^2}^{(2)}$
$\mathcal{O}_1^M$	++	$\mathcal{O}_{M,1}$	$-\frac{1}{2}\mathcal{O}_1^{H^2W^2}$	$-\frac{1}{2}Q_{W^2H^2D^2}^{(1)}$
$\mathcal{O}_2^M$	++	$\mathcal{O}_{M,2}$	$\mathcal{O}_2^{H^2B^2}$	$Q_{B^2H^2D^2}^{(2)}$
$\mathcal{O}_3^M$	++	$\mathcal{O}_{M,3}$	$-\mathcal{O}_1^{H^2B^2}$	$-Q_{B^2H^2D^2}^{(1)}$
$\mathcal{O}_4^M$	++	$\mathcal{O}_{M,4}$	$\mathcal{O}_1^{H^2BW}$	$Q_{WBH^2D^2}^{(1)}$
$\mathcal{O}_5^M$	++	$\mathcal{O}_{M,5}$	$\mathcal{O}_3^{H^2BW}$	$Q_{WBH^2D^2}^{(4)}$
$\mathcal{O}_7^M$	++	$\mathcal{O}_{M,7}$	$\frac{1}{4}\mathcal{O}_1^{H^2W^2} - \frac{1}{2}\mathcal{O}_3^{H^2W^2}$	$\frac{1}{4}Q_{W^2H^2D^2}^{(1)} - \frac{1}{2}Q_{W^2H^2D^2}^{(4)}$
$\mathcal{O}_8^M$	--	---	$\tilde{\mathcal{O}}_2^{H^2BW}$	$Q_{WBH^2D^2}^{(5)}$
$\mathcal{O}_9^M$	--	---	$\tilde{\mathcal{O}}_2^{H^2W^2}$	$Q_{W^2H^2D^2}^{(5)}$
$\mathcal{O}_0^T$	++	$\mathcal{O}_{T,0}$	$\frac{1}{4}\mathcal{O}_1^{W^4}$	$\frac{1}{4}Q_{W^4}^{(1)}$
$\mathcal{O}_1^T$	++	$\mathcal{O}_{T,1}$	$\frac{1}{4}\mathcal{O}_3^{W^4}$	$\frac{1}{4}Q_{W^4}^{(3)}$
$\mathcal{O}_2^T$	++	$\mathcal{O}_{T,2}$	$\frac{1}{16}\mathcal{O}_1^{W^4} + \frac{1}{16}\mathcal{O}_3^{W^4} + \frac{1}{16}\mathcal{O}_4^{W^4}$	$\frac{1}{16}Q_{W^4}^{(1)} + \frac{1}{16}Q_{W^4}^{(3)} + \frac{1}{16}Q_{W^4}^{(4)}$
$\mathcal{O}_3^T$	++	$\mathcal{O}_{T,3}$	$\frac{1}{8}\mathcal{O}_3^{W^4} + \frac{1}{16}\mathcal{O}_2^{W^4}$	$\frac{1}{8}Q_{W^4}^{(3)} + \frac{1}{16}Q_{W^4}^{(2)}$
$\mathcal{O}_4^T$	++	$\mathcal{O}_{T,4}$	$\frac{1}{8}\mathcal{O}_2^{B^2W^2} + \frac{1}{4}\mathcal{O}_3^{B^2W^2}$	$\frac{1}{8}Q_{W^2B^2}^{(2)} + \frac{1}{4}Q_{W^2B^2}^{(3)}$
$\mathcal{O}_5^T$	++	$\mathcal{O}_{T,5}$	$\frac{1}{2}\mathcal{O}_1^{B^2W^2}$	$\frac{1}{2}Q_{W^2B^2}^{(1)}$
$\mathcal{O}_6^T$	++	$\mathcal{O}_{T,6}$	$\frac{1}{2}\mathcal{O}_3^{B^2W^2}$	$\frac{1}{2}Q_{W^2B^2}^{(3)}$
$\mathcal{O}_7^T$	++	$\mathcal{O}_{T,7}$	$\frac{1}{8}\mathcal{O}_1^{B^2W^2} + \frac{1}{8}\mathcal{O}_3^{B^2W^2} + \frac{1}{8}\mathcal{O}_4^{B^2W^2}$	$\frac{1}{8}Q_{W^2B^2}^{(1)} + \frac{1}{8}Q_{W^2B^2}^{(3)} + \frac{1}{8}Q_{W^2B^2}^{(4)}$
$\mathcal{O}_8^T$	++	$\mathcal{O}_{T,8}$	$\mathcal{O}_1^{B^4}$	$Q_{B^4}^{(1)}$
$\mathcal{O}_9^T$	++	$\mathcal{O}_{T,9}$	$\frac{1}{2}\mathcal{O}_1^{B^4} + \frac{1}{4}\mathcal{O}_2^{B^4}$	$\frac{1}{2}Q_{B^4}^{(1)} + \frac{1}{4}Q_{B^4}^{(2)}$



# The Basis

Follow AEG as already widely used - mapping to other bases provided

aQGC Operator Basis	C P	Almeida, Éboli, Gonzalez-Garcia [3]	Remmen & Rodd [4]	Murphy [6]
$\mathcal{O}_0^S$	++	$\mathcal{O}_{S,0}$	$\mathcal{O}_2^{H^4}$	$Q_{H^4}^{(2)}$
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$\mathcal{O}_2^S$	++	$\mathcal{O}_{S,2}$	$\mathcal{O}_1^{H^4}$	$Q_{H^4}^{(1)}$
$\mathcal{O}_0^M$	++	$\mathcal{O}_{M,0}$	$\frac{1}{2}\mathcal{O}_2^{H^2W^2}$	$\frac{1}{2}Q_{W^2H^2D^2}^{(2)}$
$\mathcal{O}_1^M$	++	$\mathcal{O}_{M,1}$	$-\frac{1}{2}\mathcal{O}_1^{H^2W^2}$	$-\frac{1}{2}Q_{W^2H^2D^2}^{(1)}$
$\mathcal{O}_2^M$	++	$\mathcal{O}_{M,2}$	$\mathcal{O}_2^{H^2B^2}$	$Q_{B^2H^2D^2}^{(2)}$
$\mathcal{O}_3^M$	++	$\mathcal{O}_{M,3}$	$-\mathcal{O}_1^{H^2B^2}$	$-Q_{B^2H^2D^2}^{(1)}$
$\mathcal{O}_4^M$	++	$\mathcal{O}_{M,4}$	$\mathcal{O}_1^{H^2BW}$	$Q_{WBH^2D^2}^{(1)}$
$\mathcal{O}_5^M$	++	$\mathcal{O}_{M,5}$	$\mathcal{O}_3^{H^2BW}$	$Q_{WBH^2D^2}^{(4)}$
$\mathcal{O}_7^M$	++	$\mathcal{O}_{M,7}$	$\frac{1}{4}\mathcal{O}_1^{H^2W^2} - \frac{1}{2}\mathcal{O}_3^{H^2W^2}$	$\frac{1}{4}Q_{W^2H^2D^2}^{(1)} - \frac{1}{2}Q_{W^2H^2D^2}^{(4)}$
$\mathcal{O}_8^M$	--	---	$\tilde{\mathcal{O}}_2^{H^2BW}$	$Q_{WBH^2D^2}^{(5)}$
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$\mathcal{O}_0^T$	++	$\mathcal{O}_{T,0}$	$\frac{1}{4}\mathcal{O}_1^{W^4}$	$\frac{1}{4}Q_{W^4}^{(1)}$
$\mathcal{O}_1^T$	++	$\mathcal{O}_{T,1}$	$\frac{1}{4}\mathcal{O}_3^{W^4}$	$\frac{1}{4}Q_{W^4}^{(3)}$
$\mathcal{O}_2^T$	++	$\mathcal{O}_{T,2}$	$\frac{1}{16}\mathcal{O}_1^{W^4} + \frac{1}{16}\mathcal{O}_3^{W^4} + \frac{1}{16}\mathcal{O}_4^{W^4}$	$\frac{1}{16}Q_{W^4}^{(1)} + \frac{1}{16}Q_{W^4}^{(3)} + \frac{1}{16}Q_{W^4}^{(4)}$
$\mathcal{O}_3^T$	++	$\mathcal{O}_{T,3}$	$\frac{1}{8}\mathcal{O}_3^{W^4} + \frac{1}{16}\mathcal{O}_2^{W^4}$	$\frac{1}{8}Q_{W^4}^{(3)} + \frac{1}{16}Q_{W^4}^{(2)}$
$\mathcal{O}_4^T$	++	$\mathcal{O}_{T,4}$	$\frac{1}{8}\mathcal{O}_2^{B^2W^2} + \frac{1}{4}\mathcal{O}_3^{B^2W^2}$	$\frac{1}{8}Q_{W^2B^2}^{(2)} + \frac{1}{4}Q_{W^2B^2}^{(3)}$
$\mathcal{O}_5^T$	++	$\mathcal{O}_{T,5}$	$\frac{1}{2}\mathcal{O}_1^{B^2W^2}$	$\frac{1}{2}Q_{W^2B^2}^{(1)}$
$\mathcal{O}_6^T$	++	$\mathcal{O}_{T,6}$	$\frac{1}{2}\mathcal{O}_3^{B^2W^2}$	$\frac{1}{2}Q_{W^2B^2}^{(3)}$
$\mathcal{O}_7^T$	++	$\mathcal{O}_{T,7}$	$\frac{1}{8}\mathcal{O}_1^{B^2W^2} + \frac{1}{8}\mathcal{O}_3^{B^2W^2} + \frac{1}{8}\mathcal{O}_4^{B^2W^2}$	$\frac{1}{8}Q_{W^2B^2}^{(1)} + \frac{1}{8}Q_{W^2B^2}^{(3)} + \frac{1}{8}Q_{W^2B^2}^{(4)}$
$\mathcal{O}_8^T$	++	$\mathcal{O}_{T,8}$	$\mathcal{O}_1^{B^4}$	$Q_{B^4}^{(1)}$
$\mathcal{O}_9^T$	++	$\mathcal{O}_{T,9}$	$\frac{1}{2}\mathcal{O}_1^{B^4} + \frac{1}{4}\mathcal{O}_2^{B^4}$	$\frac{1}{2}Q_{B^4}^{(1)} + \frac{1}{4}Q_{B^4}^{(2)}$

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$\mathcal{O}_0^M$	++	$\mathcal{O}_{M,0}$	$\frac{1}{2}\mathcal{O}_2^{H^2W^2}$	$\frac{1}{2}Q_{W^2H^2D^2}^{(2)}$
$\mathcal{O}_1^M$	++	$\mathcal{O}_{M,1}$	$-\frac{1}{2}\mathcal{O}_1^{H^2W^2}$	$-\frac{1}{2}Q_{W^2H^2D^2}^{(1)}$
$\mathcal{O}_2^M$	++	$\mathcal{O}_{M,2}$	$\mathcal{O}_2^{H^2B^2}$	$Q_{B^2H^2D^2}^{(2)}$
$\mathcal{O}_3^M$	++	$\mathcal{O}_{M,3}$	$-\mathcal{O}_1^{H^2B^2}$	$-Q_{B^2H^2D^2}^{(1)}$
$\mathcal{O}_4^M$	++	$\mathcal{O}_{M,4}$	$\mathcal{O}_1^{H^2BW}$	$Q_{WBH^2D^2}^{(1)}$
$\mathcal{O}_5^M$	++	$\mathcal{O}_{M,5}$	$\mathcal{O}_3^{H^2BW}$	$Q_{WBH^2D^2}^{(4)}$
$\mathcal{O}_7^M$	++	$\mathcal{O}_{M,7}$	$\frac{1}{4}\mathcal{O}_1^{H^2W^2} - \frac{1}{2}\mathcal{O}_3^{H^2W^2}$	$\frac{1}{4}Q_{W^2H^2D^2}^{(1)} - \frac{1}{2}Q_{W^2H^2D^2}^{(4)}$
$\mathcal{O}_8^M$	--	---	$\tilde{\mathcal{O}}_2^{H^2BW}$	$Q_{WBH^2D^2}^{(5)}$
$\mathcal{O}_9^M$	--	---	$\tilde{\mathcal{O}}_2^{H^2W^2}$	$Q_{W^2H^2D^2}^{(5)}$
<p><math>\mathcal{O}_6^M</math> in original AEG basis, but redundant  <math>\mathcal{O}_{8,9}^M</math> are new, C&amp;P odd</p>		$\mathcal{O}_{T,0}$	$\frac{1}{4}\mathcal{O}_1^{W^4}$	$\frac{1}{4}Q_{W^4}^{(1)}$
		$\mathcal{O}_{T,1}$	$\frac{1}{4}\mathcal{O}_3^{W^4}$	$\frac{1}{4}Q_{W^4}^{(3)}$
		$\mathcal{O}_{T,2}$	$\frac{1}{16}\mathcal{O}_1^{W^4} + \frac{1}{16}\mathcal{O}_3^{W^4} + \frac{1}{16}\mathcal{O}_4^{W^4}$	$\frac{1}{16}Q_{W^4}^{(1)} + \frac{1}{16}Q_{W^4}^{(3)} + \frac{1}{16}Q_{W^4}^{(4)}$
		$\mathcal{O}_{T,3}$	$\frac{1}{8}\mathcal{O}_3^{W^4} + \frac{1}{16}\mathcal{O}_2^{W^4}$	$\frac{1}{8}Q_{W^4}^{(3)} + \frac{1}{16}Q_{W^4}^{(2)}$
		$\mathcal{O}_{T,4}$	$\frac{1}{8}\mathcal{O}_2^{B^2W^2} + \frac{1}{4}\mathcal{O}_3^{B^2W^2}$	$\frac{1}{8}Q_{W^2B^2}^{(2)} + \frac{1}{4}Q_{W^2B^2}^{(3)}$
		$\mathcal{O}_{T,5}$	$\frac{1}{2}\mathcal{O}_1^{B^2W^2}$	$\frac{1}{2}Q_{W^2B^2}^{(1)}$
		$\mathcal{O}_{T,6}$	$\frac{1}{2}\mathcal{O}_3^{B^2W^2}$	$\frac{1}{2}Q_{W^2B^2}^{(3)}$
		$\mathcal{O}_{T,7}$	$\frac{1}{8}\mathcal{O}_1^{B^2W^2} + \frac{1}{8}\mathcal{O}_3^{B^2W^2} + \frac{1}{8}\mathcal{O}_4^{B^2W^2}$	$\frac{1}{8}Q_{W^2B^2}^{(1)} + \frac{1}{8}Q_{W^2B^2}^{(3)} + \frac{1}{8}Q_{W^2B^2}^{(4)}$
		$\mathcal{O}_{T,8}$	$\mathcal{O}_1^{B^4}$	$Q_{B^4}^{(1)}$
		$\mathcal{O}_{T,9}$	$\frac{1}{2}\mathcal{O}_1^{B^4} + \frac{1}{4}\mathcal{O}_2^{B^4}$	$\frac{1}{2}Q_{B^4}^{(1)} + \frac{1}{4}Q_{B^4}^{(2)}$

# Next Steps

*With the basis resolved, we can get back to physics*

**Minimal example:** custodially symmetric Higgs sector

Rewrite three Higgs aQGCs as follows

$$\mathcal{O}_+ = \frac{1}{2}(\mathcal{O}_0^S + \mathcal{O}_2^S)$$

$$\mathcal{O}_- = \frac{1}{2}(\mathcal{O}_0^S - \mathcal{O}_2^S)$$

$$\mathcal{O}_\times = \mathcal{O}_1^S$$

# Next Steps

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Rewrite three Higgs aQGCs as follows

$$\mathcal{O}_+ = \frac{1}{2}(\mathcal{O}_0^S + \mathcal{O}_2^S)$$

~~$$\mathcal{O}_- = \frac{1}{2}(\mathcal{O}_0^S - \mathcal{O}_2^S)$$~~

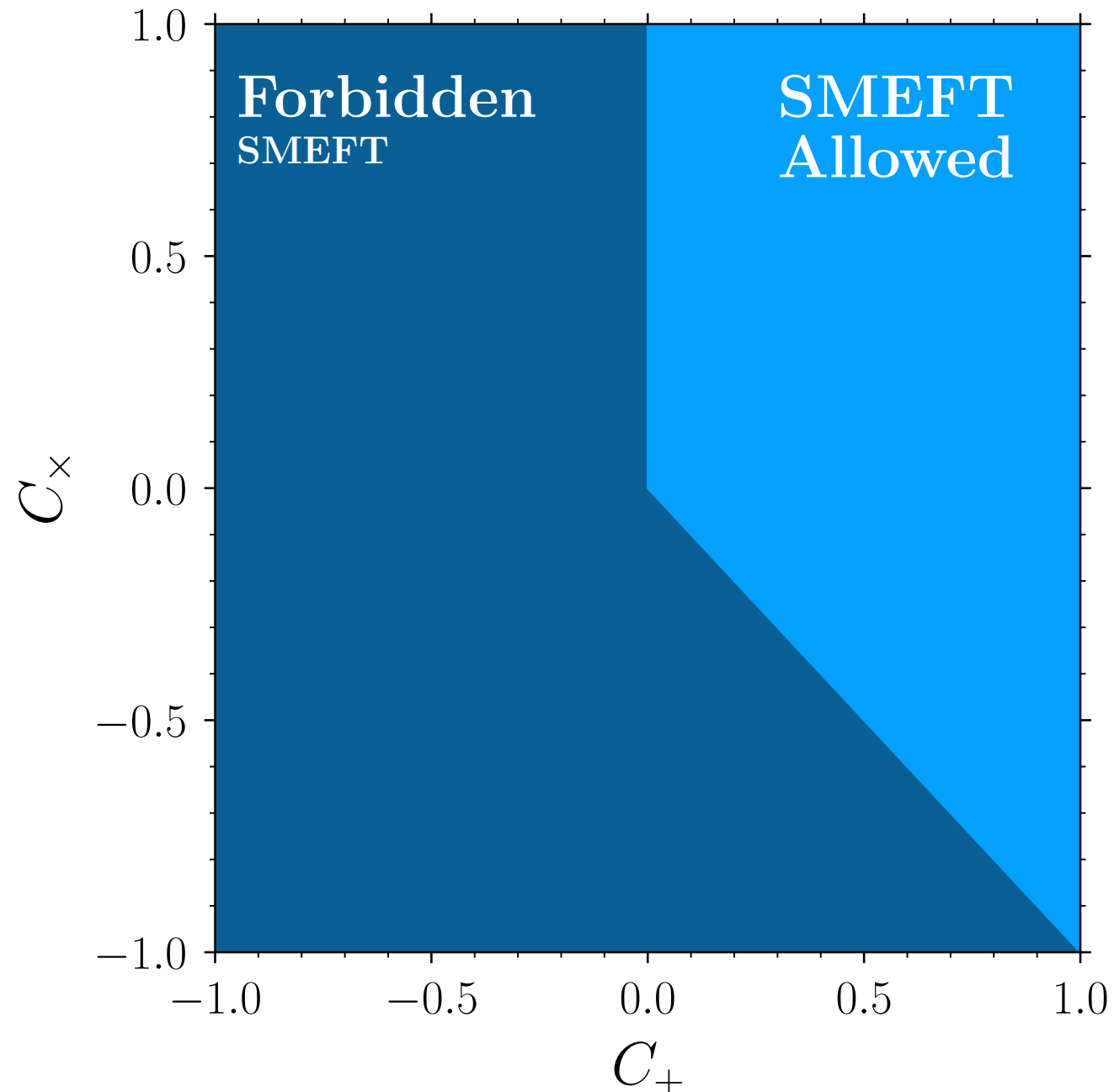
$$\mathcal{O}_\times = \mathcal{O}_1^S$$

Violates custodial symmetry

Minimal basis for studying positivity

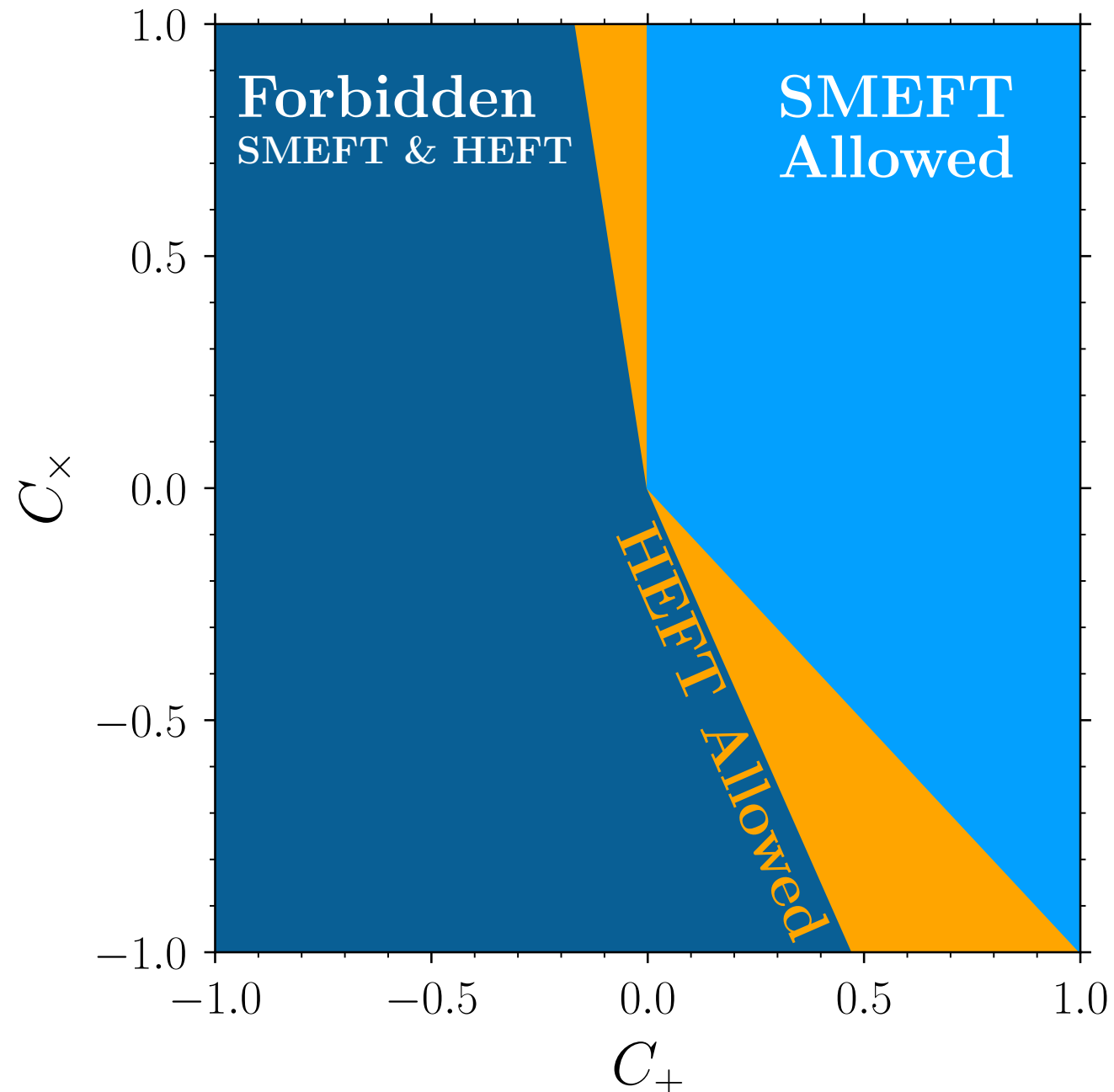
# Next Steps

Discovery in the forbidden region: perverse UV or wrong EFT?



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Discovery in the forbidden region: perverse UV or wrong EFT?



# Next Steps

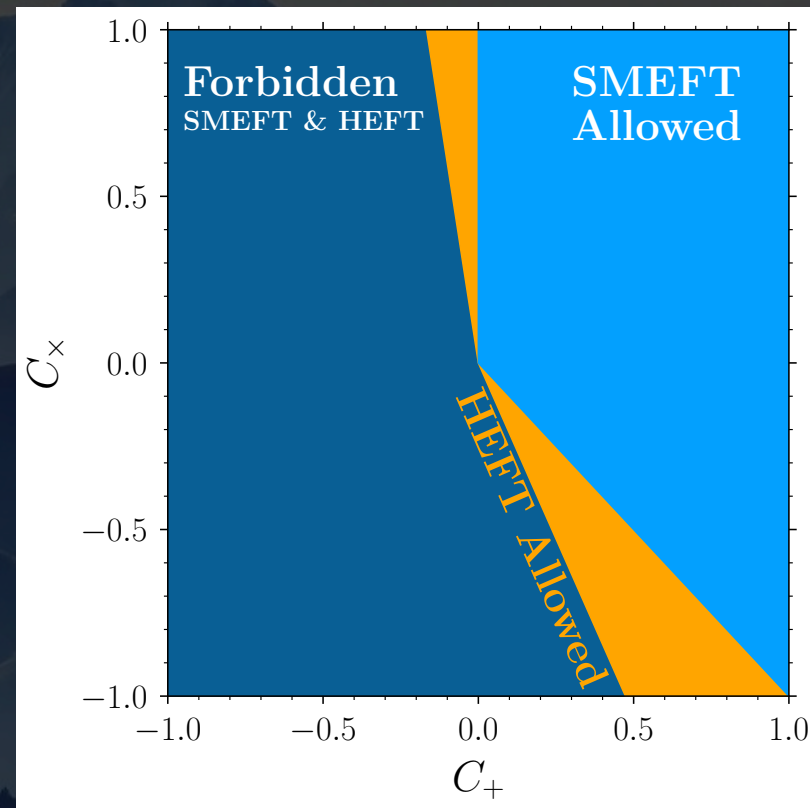
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More broadly, ultimate goal is to incorporate positivity bounds into future aQGC searches at the LHC



# Conclusion

With the aQGC basis resolved,  
time to get back to physics!



Backup Slides

# CP Odd Operators

aQGC Operator Basis		C	P	AEG [3]	RR [4]	M [6]
$\mathcal{O}_1^M$	$[D^\mu H^\dagger D_\mu H] B_{\nu\rho} \tilde{B}^{\nu\rho}$	+	-	N/A	$\tilde{\mathcal{O}}_1^{H^2 B^2}$	$Q_{B^2 H^2 D^2}^{(3)}$
$\mathcal{O}_2^M$	$[D^\mu H^\dagger \tau^I D_\mu H] B_{\nu\rho} \tilde{W}^{I\nu\rho}$	+	-	N/A	$\tilde{\mathcal{O}}_1^{H^2 BW}$	$Q_{WBH^2 D^2}^{(2)}$
$\mathcal{O}_3^M$	$i[D^\mu H^\dagger \tau^I D^\nu H] (B_{\mu\rho} W_\nu^{I\rho} - B_{\nu\rho} W_\mu^{I\rho})$	-	+	N/A	$\mathcal{O}_2^{H^2 BW}$	$Q_{WBH^2 D^2}^{(3)}$
$\mathcal{O}_4^M$	$[D^\mu H^\dagger \tau^I D^\nu H] (B_{\mu\rho} \tilde{W}_\nu^{I\rho} + B_{\nu\rho} \tilde{W}_\mu^{I\rho})$	+	-	N/A	$\tilde{\mathcal{O}}_3^{H^2 BW}$	$Q_{WBH^2 D^2}^{(6)}$
$\mathcal{O}_5^M$	$[D^\mu H^\dagger D_\mu H] W_{\nu\rho}^I \tilde{W}^{I\nu\rho}$	+	-	N/A	$\tilde{\mathcal{O}}_1^{H^2 W^2}$	$Q_{W^2 H^2 D^2}^{(3)}$
$\mathcal{O}_6^M$	$i\epsilon^{IJK} [D^\mu H^\dagger \tau^I D^\nu H] (W_{\mu\rho}^J \tilde{W}_\nu^{K\rho} + \tilde{W}_{\mu\rho}^J W_\nu^{K\rho})$	+	-	N/A	$\tilde{\mathcal{O}}_3^{H^2 W^2}$	$Q_{W^2 H^2 D^2}^{(6)}$
$\mathcal{O}_1^T$	$B_{\mu\nu} B^{\mu\nu} B_{\rho\sigma} \tilde{B}^{\rho\sigma}$	+	-	N/A	$\tilde{\mathcal{O}}_1^{B^4}$	$Q_{B^4}^{(3)}$
$\mathcal{O}_2^T$	$B_{\mu\nu} \tilde{B}^{\mu\nu} W_{\rho\sigma}^I W^{I\rho\sigma}$	+	-	N/A	$\tilde{\mathcal{O}}_1^{B^2 W^2}$	$Q_{W^2 B^2}^{(5)}$
$\mathcal{O}_3^T$	$B_{\mu\nu} B^{\mu\nu} W_{\rho\sigma}^I \tilde{W}^{I\rho\sigma}$	+	-	N/A	$\tilde{\mathcal{O}}_2^{B^2 W^2}$	$Q_{W^2 B^2}^{(6)}$
$\mathcal{O}_4^T$	$B_{\mu\nu} W^{I\mu\nu} B_{\rho\sigma} \tilde{W}^{I\rho\sigma}$	+	-	N/A	$\tilde{\mathcal{O}}_3^{B^2 W^2}$	$Q_{W^2 B^2}^{(7)}$
$\mathcal{O}_5^T$	$W_{\mu\nu}^I W^{I\mu\nu} W_{\rho\sigma}^J \tilde{W}^{J\rho\sigma}$	+	-	N/A	$\tilde{\mathcal{O}}_1^{W^4}$	$Q_{W^4}^{(5)}$
$\mathcal{O}_6^T$	$W_{\mu\nu}^I W^{J\mu\nu} W_{\rho\sigma}^I \tilde{W}^{J\rho\sigma}$	+	-	N/A	$\tilde{\mathcal{O}}_2^{W^4}$	$Q_{W^4}^{(6)}$