

EFT Highlights from CMS

8th General Meeting of the LHC EFT Working Group

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Analyses covered in this talk

Differential Higgs Combination

- CMS-PAS-HIG-23-013: «Combination and interpretation of fiducial differential Higgs boson production cross sections at $\sqrt{s} = 13$ TeV»

Combination across multiple sectors

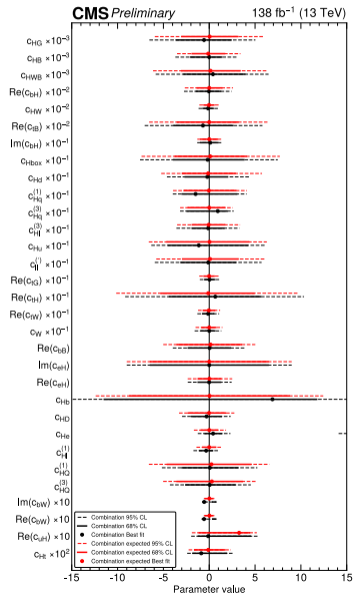
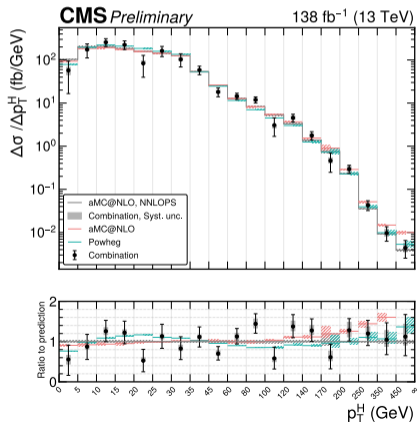
- CMS-PAS-SMP-24-003: «Combined effective field theory interpretation of Higgs boson, electroweak vector boson, top quark, and multi-jet measurements»

Differential Higgs Combination

CMS-PAS-HIG-23-013: «Combination and interpretation of fiducial differential Higgs boson production cross sections at $\sqrt{s} = 13$ TeV»

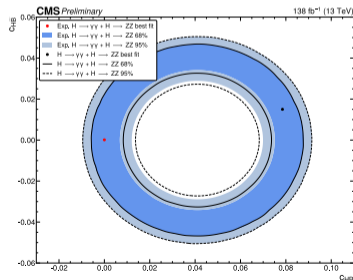
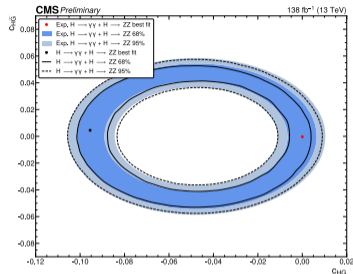
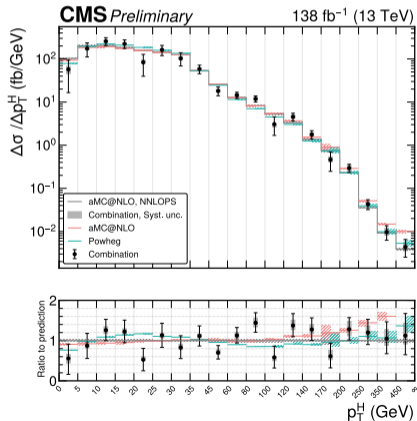
Differential Higgs combination

- Combination of fiducial differential Higgs measurements using the $H \rightarrow \gamma\gamma, ZZ, WW, \tau\tau$ channels
- 31 dim-6 operators considered (CP-even and CP-odd)
- 1-dimensional scans
- 2-d scans of CP-even and CP-odd pairs



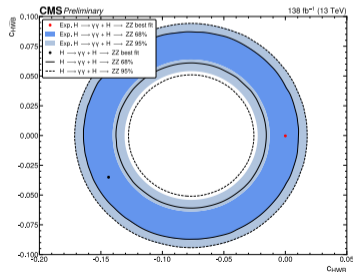
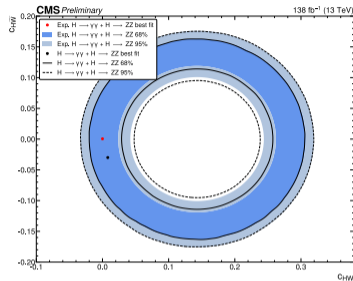
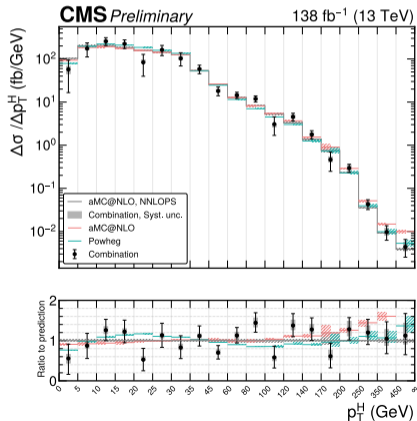
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Principal Component Analysis

- The available data do not contain enough information to constrain all Wilson coefficients in a simultaneous fit; unconstrained degrees of freedom (flat directions in the likelihood)
- Principal component analysis (PCA) is a useful tool to identify linear combinations of WCs that can be constrained:
 - Obtain the Hessian matrix of the likelihood parametrized in terms of the Wilson coefficients,

$$\mathcal{H} \approx C_{\text{SMEFT}}^{-1} = P^T C^{-1} P,$$

where C is the covariance matrix between the measurement bins, and P is the matrix of the linear SMEFT parameterization

$$P_{ij} = A_j^i, \quad \text{where } (\sigma \times \mathcal{B})_{\text{SMEFT}}^i = (\sigma \times \mathcal{B})_{\text{SM}}^i \left(1 + \sum_j A_j^i c_j + \sum_{j,k} B_{jk}^i c_j c_k \right)$$

- Eigendecomposition of C_{SMEFT}^{-1} yields the eigenvectors (which are used to write linear combinations of Wilson coefficients, EVi), the corresponding eigenvalues λ_i and variances $1/\lambda_i$
- Linear combinations with small eigenvalue $\lambda_i \rightarrow 0$ correspond to flat directions and are fixed to their SM value of 0

Combination across multiple sectors

CMS-PAS-SMP-24-003: «Combined effective field theory interpretation of Higgs boson, electroweak vector boson, top quark, and multi-jet measurements»

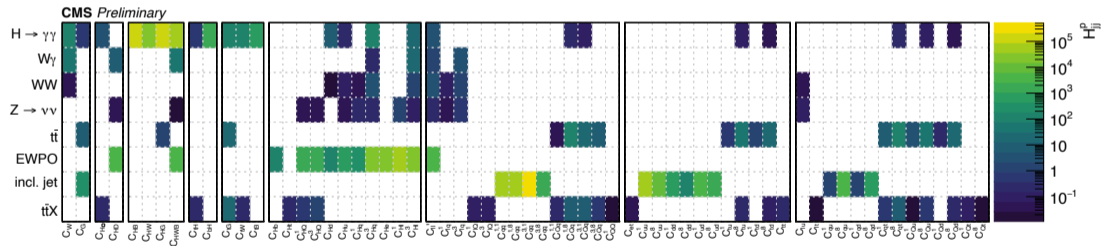
Inputs to the combination

- **Combined SMEFT interpretation of data from four sectors of the SM (Higgs, Top, Electroweak, QCD):** Seven CMS measurements + EWPO from LEP and SLC
- Inputs chosen to provide sensitivity to broad set of dim-6 SMEFT operators (64 in total), negligible overlap in event selections, small backgrounds (or estimated from data)

Analysis	Type of measurement	Observables used	Experimental likelihood
$H \rightarrow \gamma\gamma$	Diff. cross sections	STXS bins [41]	✓
$W\gamma$	Fid. diff. cross sections	$p_T^\gamma \times \phi_f $	✓
WW	Fid. diff. cross sections	$m_{\ell\ell}$	✓
$Z \rightarrow \nu\nu$	Fid. diff. cross sections	p_T^Z	✓
$t\bar{t}$	Fid. diff. cross sections	$M_{t\bar{t}}$	×
EWPO	Pseudo-observables	$\Gamma_Z, \sigma_{\text{had}}^0, R_\ell, R_c, R_b, A_{FB}^{0,\ell}, A_{FB}^{0,c}, A_{FB}^{0,b}$	×
Inclusive jet	Fid. diff. cross sections	$p_T^{\text{jet}} \times y^{\text{jet}} $	×
$t\bar{t}X$	Direct EFT	Yields in regions of interest	✓

Inputs to the combination

- **Combined SMEFT interpretation of data from four sectors of the SM (Higgs, Top, Electroweak, QCD):** Seven CMS measurements + EWPO from LEP and SLC
- Inputs chosen to provide sensitivity to broad set of dim-6 SMEFT operators (64 in total), negligible overlap in event selections, small backgrounds (or estimated from data)
- Which input channel is sensitive to which operators?



- plot shows diagonal entries of the Hessian matrix, $H_{jk} = \frac{\partial^2 \ln \mathcal{L}}{\partial c_j \partial c_k}$
 - $(H_{jj}^p)^{-1/2}$: estimate of half the expected 68% confidence interval on Wilson coefficient c_j/Λ^2 , evaluated with input channel p

SMEFT parameterization

- Scattering cross section is proportional to matrix element squared

$$\sigma = |\mathcal{M}_{\text{SM}} + \sum_j \frac{c_j}{\Lambda^2} \mathcal{M}_j|^2 = |\mathcal{M}_{\text{SM}}|^2 + 2 \sum_j \frac{c_j}{\Lambda^2} \text{Re}(\mathcal{M}_j \mathcal{M}_{\text{SM}}^*) + \sum_{j,k} \frac{c_j c_k}{\Lambda^4} \text{Re}(\mathcal{M}_j \mathcal{M}_k^*)$$

- This means that cross section of process p in kinematic bin i can be written as

$$\sigma_{\text{SMEFT}}^{i,p} = \sigma_{\text{SM}}^{i,p} + \sigma_{\text{int.}}^{i,p}(\vec{c}) + \sigma_{\text{BSM}}^{i,p}(\vec{c}) = \sigma_{\text{SM}}^{i,p} \left(1 + \sum_j A_j^{i,p} \frac{c_j}{\Lambda^2} + \sum_{j,k} B_{jk}^{i,p} \frac{c_j c_k}{\Lambda^4} \right)$$

- Majority of results we report use parameterizations truncated at $\mathcal{O}(c/\Lambda^2)$ (linear terms)
- $A_j^{i,p}, B_{jk}^{i,p}$ computed using MG5_aMC@NLO+Pythia+SMEFTsim3 (SMEFT@NLO for $gg \rightarrow H, ZH$)
- SMEFT modifications of masses and decay widths also taken into account
- For $H \rightarrow \gamma\gamma$ decay and EWPO, analytic calculations are used

Modifications to input analyses and likelihood model

Likelihood model:

- Combined likelihood model:

$$\mathcal{L}(\text{data}; \vec{c}, \vec{\nu}) = \mathcal{L}^{\text{expt}}(\vec{c}, \vec{\nu}) \mathcal{L}^{\text{simpl}}(\vec{c})$$

- «experimental likelihood»:

$$\mathcal{L}^{\text{expt}}(\vec{c}, \vec{\nu}) = \prod_i \text{Poisson}(n_i | \sum_j \mu'^j(\vec{c}) s_i^j(\vec{\nu}) + b_i(\vec{\nu})) \prod_k p_k(y_k | \nu_k)$$

- covers the $H \rightarrow \gamma\gamma$, $W\gamma$, WW , and $Z \rightarrow \nu\nu$ measurements
- in the $t\bar{t}X$ measurement, instead of $\sum_j \mu'^j(\vec{c}) s_i^j(\vec{\nu})$, signal yield takes the form $\sum_j s_i^j(\vec{\nu}, \vec{c})$

- «simplified likelihood»:

$$\mathcal{L}^{\text{simpl}}(\vec{c}) = \frac{\exp(-\frac{1}{2}(\vec{\mu}(\vec{c}) - \hat{\vec{\mu}})^T V^{-1}(\vec{\mu}(\vec{c}) - \hat{\vec{\mu}}))}{\sqrt{(2\pi)^m \det(V)}}$$

- covers the EWPO, $t\bar{t}$, and inclusive jet measurements

Modifications to input analyses and likelihood model

Likelihood model:

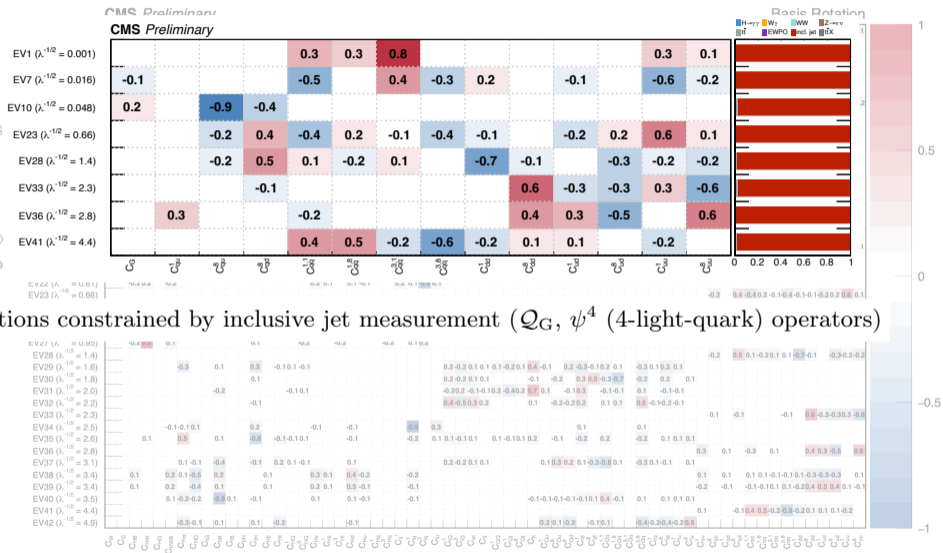
- Combined likelihood model: $\mathcal{L}(\text{data}; \vec{c}, \vec{\nu}) = \mathcal{L}^{\text{expt}}(\vec{c}, \vec{\nu}) \mathcal{L}^{\text{simpl}}(\vec{c})$
- $\mathcal{L}^{\text{expt}}(\vec{c}, \vec{\nu}) = \prod_i \text{Poisson}(n_i | \sum_j \mu'^j(\vec{c}) s_i^j(\vec{\nu}) + b_i(\vec{\nu})) \prod_k p_k(y_k | \nu_k)$ (H, $W\gamma$, WW, Z, $t\bar{t}X$)
- $\mathcal{L}^{\text{simpl}}(\vec{c}) = \exp(-\frac{1}{2}(\vec{\mu}(\vec{c}) - \hat{\vec{\mu}})^T V^{-1}(\vec{\mu}(\vec{c}) - \hat{\vec{\mu}})) / \sqrt{(2\pi)^m \det(V)}$ ($t\bar{t}$, inclusive jet, EWPO)

Modifications to input measurements:

- SM predictions for inclusive jet measurement rederived with up-to-date PDF set
- For all (CMS) measurements, derived theoretical uncertainties on SM predictions (PDF, factorization and renormalization scale uncertainties)
- PDF and luminosity uncertainties (partially) correlated between the input measurements
- SMEFT parameterizations derived up to $\mathcal{O}(c^2/\Lambda^4)$ in a consistent way for all input measurements
 - For the «direct» EFT measurement $t\bar{t}X$:
 - basis rotation from `dim6top` to SMEFT `topU31` as implemented in SMEFTsim3
 - added operators that were not considered in original analysis: $\mathcal{Q}_{H\Box}$ and 2-heavy-2-light-quark

Basis rotation

- Perform PCA to identify 42 linear combinations of Wilson coefficients that can be constrained simultaneously
- 22 «flat directions» ($\lambda < 0.04$) fixed to zero

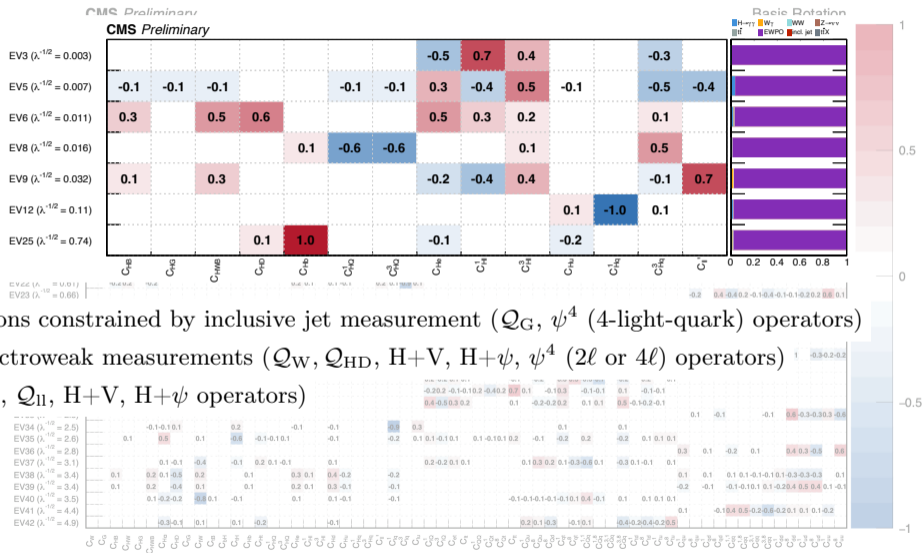


- 8 linear combinations constrained by inclusive jet measurement (Q_G, ψ^4 (4-light-quark) operators)

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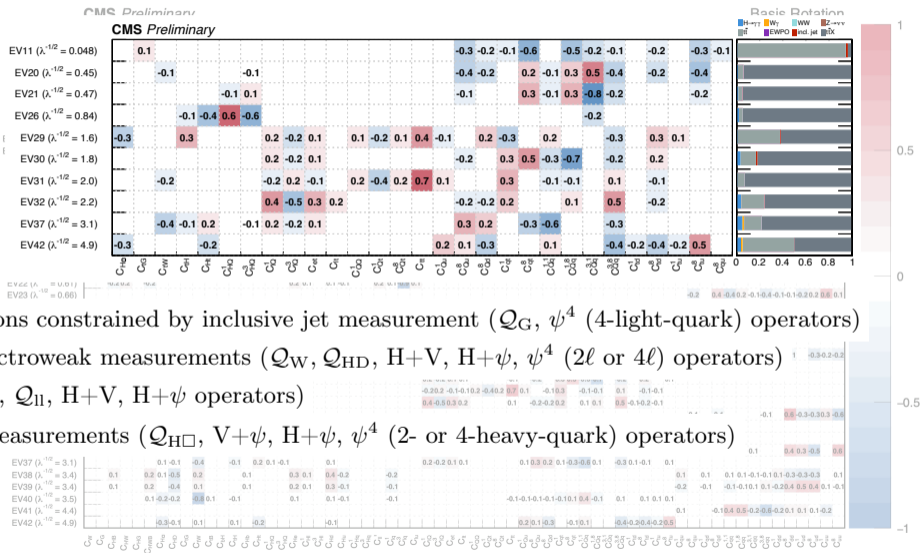
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- 8 by Higgs and electroweak measurements ($\mathcal{Q}_W, \mathcal{Q}_{HD}, H+V, H+\psi, \psi^4$ (2ℓ or 4ℓ) operators)
- 7 by EWPO ($\mathcal{Q}_{HD}, \mathcal{Q}_{II}, H+V, H+\psi$ operators)



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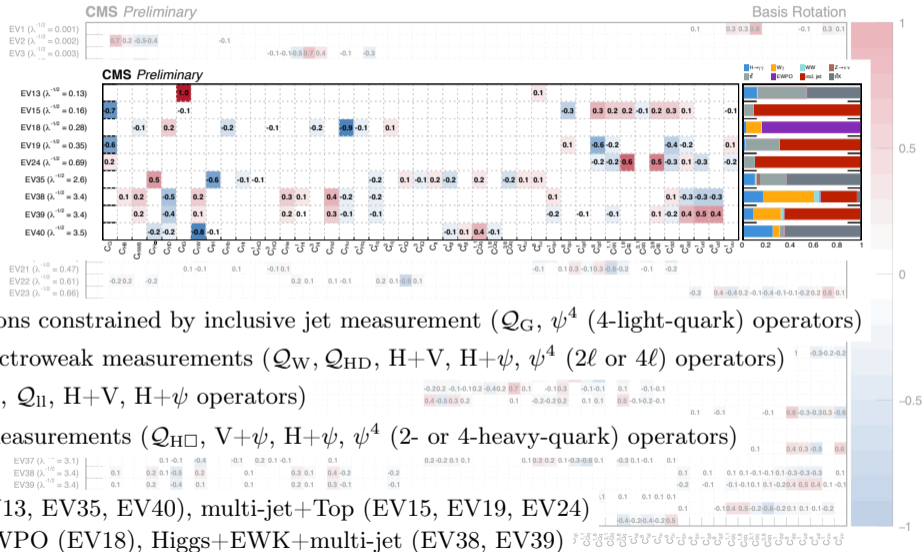
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- 10 by top quark measurements ($\mathcal{Q}_{H\Box}, V+\psi, H+\psi, \psi^4$ (2- or 4-heavy-quark) operators)



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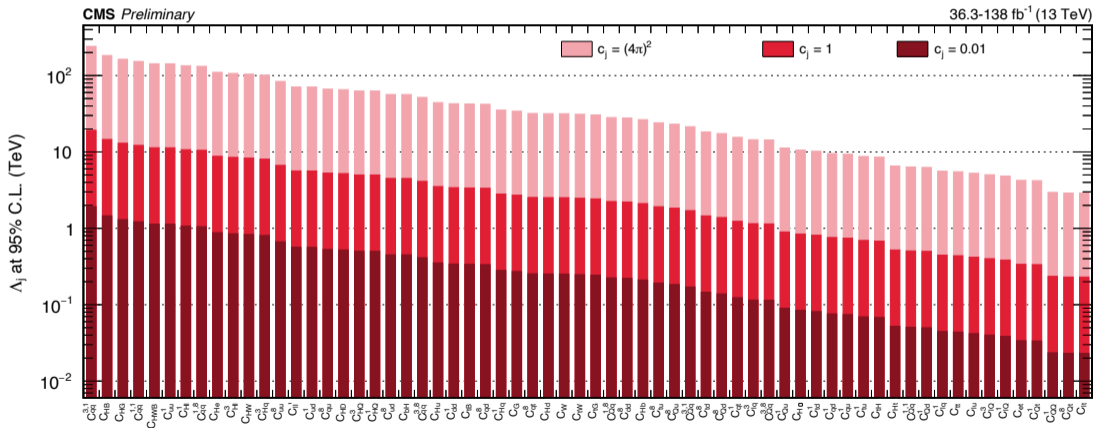
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- 10 by top quark measurements ($\mathcal{Q}_{H\Box}, V+\psi, H+\psi, \psi^4$ (2- or 4-heavy-quark) operators)
- 9 by a mixture
 - Higgs+Top (EV13, EV35, EV40), multi-jet+Top (EV15, EV19, EV24)
 - CMS EWK+EWPO (EV18), Higgs+EWK+multi-jet (EV38, EV39)

Individual constraints on Wilson coefficients

- Several Wilson coefficients receive significant constraints from multiple measurements, e.g.
 - Through combination of **$t\bar{t}$ cross section measurements and the $t\bar{t}X$ EFT analysis**, we obtain stronger constraints on the **2-heavy-2-light quark operators**
 - Combination of **$W\gamma$ and $H \rightarrow \gamma\gamma$** yields an improved constraint on c_W with respect to any single-analysis result (linear-only sensitivity $\sim 45\%$ higher than CMS $W\gamma$ result)
 - **2-(light)quark-2-lepton operators** constrained by combination of **EW vector boson** measurements
 - Interplay of Higgs- and Top-sectors ($c_{tG}, c_{tH}, c_{H\Box}$)
- Comparison of results with linear-only ($\mathcal{O}(c/\Lambda^2)$) and linear+quadratic parameterization ($\mathcal{O}(c^2/\Lambda^4)$) gives an indication of how much the inclusion of orders $1/\Lambda^4$ could change the sensitivity of the results

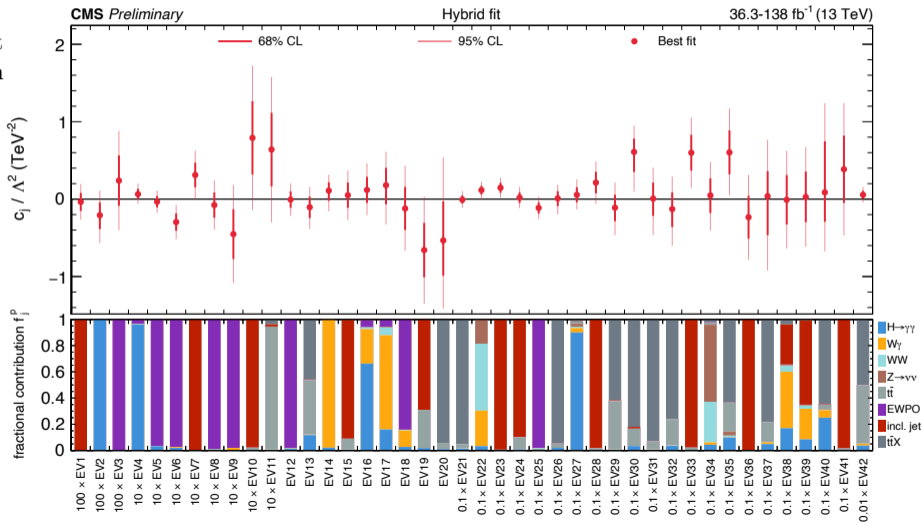
Lower limits on energy scales of new physics

- Translate constraints on c_j/Λ^2 into 95% CL lower limits on the scale of new physics Λ_j , by setting c_j to specific values (of 0.01, 1 and $(4\pi)^2$)



Constraints on linear combinations of Wilson coefficients

- Setting constraints on 42 linear combinations of Wilson coefficients (each varied simultaneously)
- Majority of POI receives significant contributions from multiple channels
- 8 linear combinations constrained by inclusive jet measurement
- 8 by Higgs and electroweak measurements
- 7 by EWPO
- 10 by top quark measurements
- 9 by a mixture



Constraints on linear combinations of Wilson coefficients

- Setting constraints on 42 linear combinations of Wilson coefficients (varied simultaneously)
- 95% confidence intervals range from around ± 10 to ± 0.002
- Majority of POI receives significant contributions from multiple channels
 - 8 linear combinations constrained by inclusive jet measurement
 - 8 by Higgs and electroweak measurements
 - 7 by EWPO
 - 10 by top quark measurements
 - 9 by a mixture
- The p-value for the compatibility with the SM is 1.7%
 - Deviation from SM is mostly driven by inclusive jet measurement
 - When excluding it from the combination, the p-value is found to be 26%

Summary

- Differential Higgs combination ($H \rightarrow \gamma\gamma, ZZ, WW, \tau\tau$) setting constraints on 28 CP-even and 3 CP-odd dimension-6 operators individually / 10 linear combinations simultaneously
 - no deviations from SM expectation observed
- Combination of measurements from Higgs, Top, Electroweak, and QCD sectors constraining 64 dimension-6 operators individually / 42 linear combination simultaneously
 - some deviation from SM (p-value 1.7%), mostly driven by multijet production
- Developments for future global combinations: Combine and (re-)interpret different types of measurements (differential cross sections and direct EFT measurements) in a consistent way

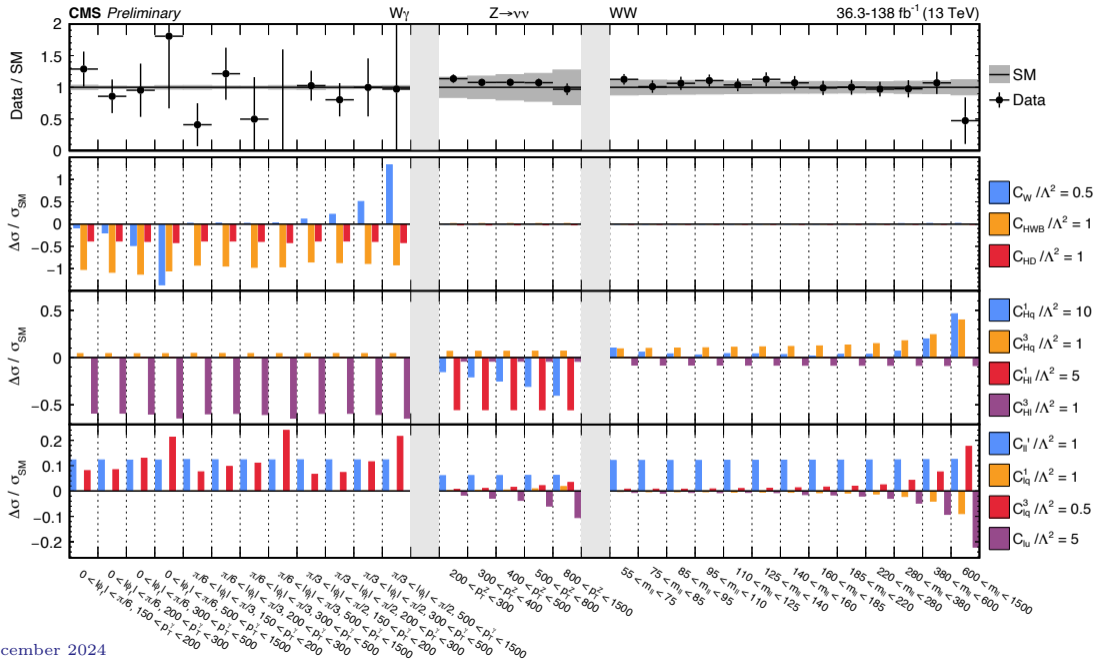
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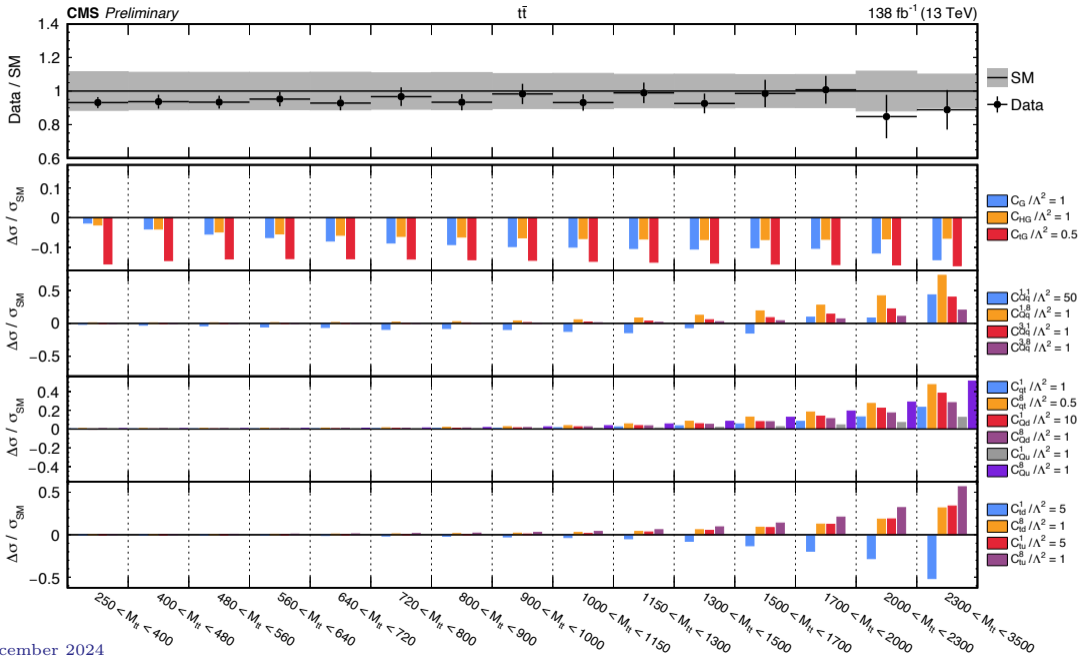
Linear combination	expected linear	observed linear	Wilson coefficient	expected linear	observed linear
EV1/ Λ^2	[-0.002, 0.002]	[-0.003, 0.002]	EV2/ Λ^2	[-0.003, 0.003]	[-0.006, 0.001]
EV3/ Λ^2	[-0.006, 0.006]	[-0.004, 0.009]	EV4/ Λ^2	[-0.012, 0.013]	[-0.006, 0.020]
EV5/ Λ^2	[-0.014, 0.014]	[-0.018, 0.011]	EV6/ Λ^2	[-0.022, 0.022]	[-0.052, -0.008]
EV7/ Λ^2	[-0.031, 0.031]	[-0.000, 0.062]	EV8/ Λ^2	[-0.032, 0.032]	[-0.040, 0.024]
EV9/ Λ^2	[-0.063, 0.063]	[-0.11, 0.018]	EV10/ Λ^2	[-0.093, 0.093]	[-0.014, 0.17]
EV11/ Λ^2	[-0.094, 0.094]	[-0.030, 0.16]	EV12/ Λ^2	[-0.21, 0.21]	[-0.22, 0.20]
EV13/ Λ^2	[-0.27, 0.25]	[-0.39, 0.16]	EV14/ Λ^2	[-0.29, 0.26]	[-0.16, 0.32]
EV15/ Λ^2	[-0.32, 0.32]	[-0.27, 0.37]	EV16/ Λ^2	[-0.32, 0.33]	[-0.21, 0.46]
EV17/ Λ^2	[-0.51, 0.44]	[-0.33, 0.61]	EV18/ Λ^2	[-0.55, 0.55]	[-0.67, 0.43]
EV19/ Λ^2	[-0.69, 0.69]	[-1.4, 0.033]	EV20/ Λ^2	[-0.78, 1.0]	[-1.4, 0.54]
EV21/ Λ^2	[-0.91, 0.99]	[-1.1, 1.0]	EV22/ Λ^2	[-1.3, 1.1]	[-0.015, 2.2]
EV23/ Λ^2	[-1.3, 1.3]	[0.18, 2.8]	EV24/ Λ^2	[-1.4, 1.4]	[-1.2, 1.6]
EV25/ Λ^2	[-1.5, 1.5]	[-2.6, 0.32]	EV26/ Λ^2	[-1.8, 1.5]	[-2.0, 1.8]
EV27/ Λ^2	[-1.8, 1.9]	[-1.3, 2.5]	EV28/ Λ^2	[-2.7, 2.7]	[-0.60, 4.9]
EV29/ Λ^2	[-3.4, 3.1]	[-4.7, 2.1]	EV30/ Λ^2	[-3.7, 3.3]	[0.97, 9.5]
EV31/ Λ^2	[-4.4, 3.7]	[-4.6, 4.0]	EV32/ Λ^2	[-4.6, 4.1]	[-6.0, 2.9]
EV33/ Λ^2	[-4.6, 4.6]	[1.4, 11]	EV34/ Λ^2	[-5.0, 4.7]	[-4.1, 4.8]
EV35/ Λ^2	[-5.0, 5.1]	[0.48, 12]	EV36/ Λ^2	[-5.5, 5.5]	[-7.8, 3.1]
EV37/ Λ^2	[-6.2, 6.3]	[-9.2, 7.7]	EV38/ Λ^2	[-6.2, 6.3]	[-6.4, 6.2]
EV39/ Λ^2	[-6.4, 6.5]	[-6.2, 6.7]	EV40/ Λ^2	[-7.6, 7.1]	[-6.8, 12]
EV41/ Λ^2	[-8.6, 8.6]	[-4.7, 12]	EV42/ Λ^2	[-9.5, 9.6]	[-4.2, 16]

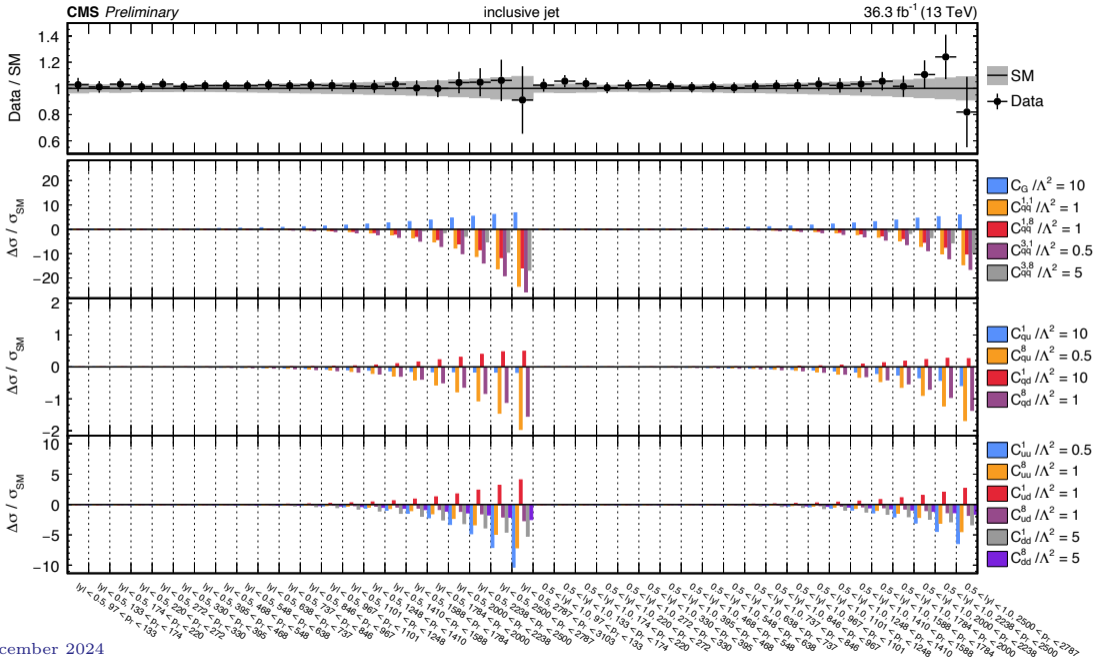
Wilson coefficient	expected linear	observed linear	expected linear+quadratic	observed linear+quadratic
$c_{qq}^{(3,1)}/\Lambda^2$	[-0.003, 0.003]	[-0.003, 0.002]	[-0.003, 0.003]	[-0.003, 0.003]
c_{HB}/Λ^2	[-0.005, 0.004]	[-0.009, 0.001]	[-0.005, 0.004]	[-0.008, 0.001]
c_{HG}/Λ^2	[-0.006, 0.006]	[-0.004, 0.008]	[-0.006, 0.006]	[-0.004, 0.008]
$c_{qq}^{(1,1)}/\Lambda^2$	[-0.007, 0.007]	[-0.008, 0.005]	[-0.005, 0.014]	[-0.007, 0.008]
$c_{uu}^{(1)}/\Lambda^2$	[-0.008, 0.008]	[-0.010, 0.005]	[-0.006, 0.012]	[-0.008, 0.007]
c_{HWB}/Λ^2	[-0.007, 0.008]	[-0.004, 0.012]	[-0.008, 0.008]	[-0.004, 0.011]
$c_{HI}^{(1)}/\Lambda^2$	[-0.009, 0.009]	[-0.006, 0.012]	[-0.009, 0.009]	[-0.006, 0.012]
$c_{qq}^{(1,8)}/\Lambda^2$	[-0.009, 0.009]	[-0.010, 0.008]	[-0.008, 0.010]	[-0.010, 0.009]
c_{He}/Λ^2	[-0.013, 0.013]	[-0.023, 0.003]	[-0.013, 0.013]	[-0.023, 0.003]
$c_{HI}^{(3)}/\Lambda^2$	[-0.014, 0.014]	[-0.015, 0.013]	[-0.014, 0.014]	[-0.015, 0.013]
c_{HW}/Λ^2	[-0.015, 0.013]	[-0.026, 0.003]	[-0.014, 0.014]	[-0.024, 0.003]
$c_{Hq}^{(3)}/\Lambda^2$	[-0.015, 0.015]	[-0.019, 0.012]	[-0.015, 0.015]	[-0.019, 0.012]
$c_{uu}^{(8)}/\Lambda^2$	[-0.022, 0.022]	[-0.029, 0.016]	[-0.019, 0.033]	[-0.024, 0.020]
c'_{ll}/Λ^2	[-0.031, 0.031]	[-0.027, 0.036]	[-0.031, 0.031]	[-0.027, 0.036]
$c_{ud}^{(1)}/\Lambda^2$	[-0.032, 0.032]	[-0.031, 0.032]	[-0.054, 0.022]	[-0.070, 0.021]
$c_{qu}^{(8)}/\Lambda^2$	[-0.036, 0.036]	[-0.054, 0.018]	[-0.031, 0.044]	[-0.045, 0.020]
c_{HD}/Λ^2	[-0.037, 0.037]	[-0.085, -0.011]	[-0.037, 0.037]	[-0.086, -0.012]
$c_{HQ}^{(3)}/\Lambda^2$	[-0.040, 0.040]	[-0.038, 0.042]	[-0.040, 0.040]	[-0.038, 0.042]
$c_{HQ}^{(1)}/\Lambda^2$	[-0.040, 0.040]	[-0.038, 0.042]	[-0.040, 0.040]	[-0.038, 0.042]
$\text{Re}(c_{bH})/\Lambda^2$	[-0.045, 0.050]	[-0.009, 0.090]	[-0.051, 0.046]	[-0.009, 0.077]
$c_{ud}^{(8)}/\Lambda^2$	[-0.049, 0.049]	[-0.052, 0.046]	[-0.041, 0.075]	[-0.045, 0.16]
$c_{qq}^{(3,8)}/\Lambda^2$	[-0.059, 0.059]	[-0.11, 0.012]	[-0.018, 0.025]	[-0.022, 0.025]

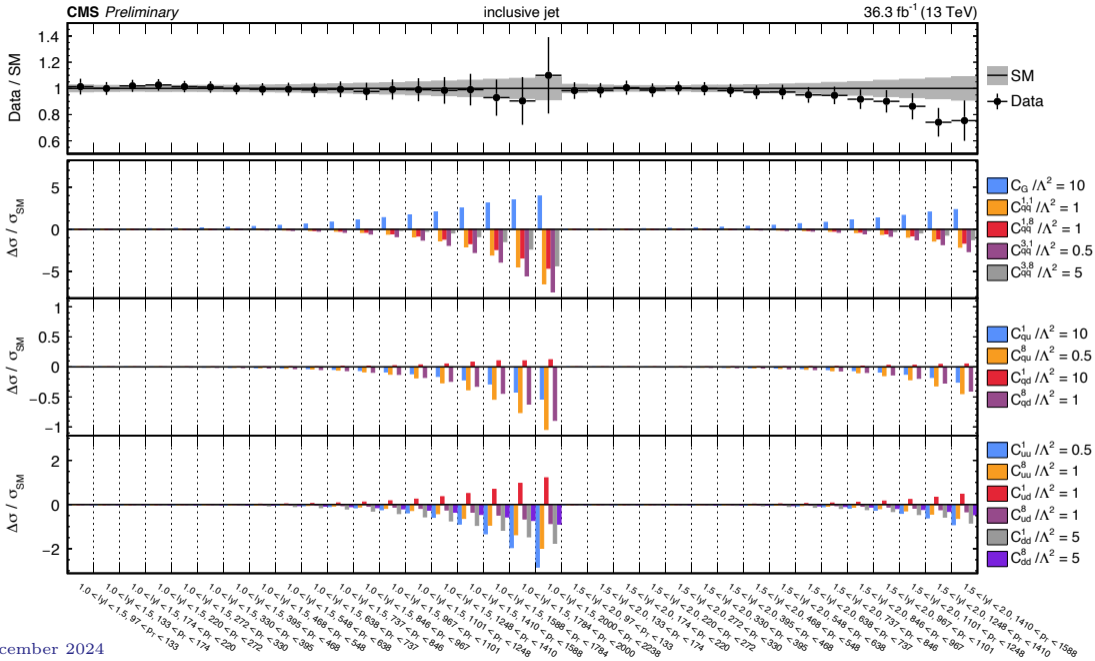
\dot{c}_{Hu} / Λ^2	$[-0.081, 0.080]$	$[-0.095, 0.066]$	$[-0.081, 0.080]$	$[-0.095, 0.065]$
$\text{Re}(c_{tB}) / \Lambda^2$	$[-0.089, 0.080]$	$[-0.16, 0.016]$	$[-0.085, 0.084]$	$[-0.15, 0.016]$
$c_{dd}^{(1)} / \Lambda^2$	$[-0.086, 0.086]$	$[-0.057, 0.12]$	$[-0.038, 0.056]$	$[-0.031, 0.065]$
$c_{qd}^{(8)} / \Lambda^2$	$[-0.089, 0.089]$	$[-0.11, 0.073]$	$[-0.066, 0.14]$	$[-0.080, 0.17]$
$c_{Hq}^{(1)} / \Lambda^2$	$[-0.13, 0.13]$	$[-0.15, 0.11]$	$[-0.13, 0.12]$	$[-0.14, 0.10]$
c_G / Λ^2	$[-0.14, 0.14]$	$[-0.14, 0.13]$	$[-0.017, 0.015]$	$[-0.016, 0.014]$
$c_{qt}^{(8)} / \Lambda^2$	$[-0.15, 0.15]$	$[-0.23, 0.076]$	$[-0.30, 0.12]$	$[-0.26, 0.066]$
$\text{Re}(c_{tW}) / \Lambda^2$	$[-0.17, 0.15]$	$[-0.30, 0.031]$	$[-0.16, 0.16]$	$[-0.26, 0.034]$
c_{Hd} / Λ^2	$[-0.16, 0.16]$	$[-0.14, 0.17]$	$[-0.15, 0.16]$	$[-0.14, 0.17]$
c_W / Λ^2	$[-0.16, 0.15]$	$[-0.30, 0.015]$	$[-0.061, 0.061]$	$[-0.065, 0.037]$
$\text{Re}(c_{tG}) / \Lambda^2$	$[-0.17, 0.16]$	$[-0.27, 0.070]$	$[-0.15, 0.18]$	$[-0.19, 0.074]$
$c_{Qq}^{(1,8)} / \Lambda^2$	$[-0.20, 0.20]$	$[-0.31, 0.084]$	$[-0.35, 0.14]$	$[-0.29, 0.075]$
$c_{dd}^{(8)} / \Lambda^2$	$[-0.20, 0.20]$	$[-0.14, 0.26]$	$[-0.10, 0.16]$	$[-0.081, 0.18]$
c_{Hb} / Λ^2	$[-0.22, 0.22]$	$[-0.33, 0.12]$	$[-0.22, 0.24]$	$[-0.31, 0.13]$
$c_{tu}^{(8)} / \Lambda^2$	$[-0.27, 0.27]$	$[-0.39, 0.15]$	$[-0.40, 0.18]$	$[-0.34, 0.11]$
$c_{Qu}^{(8)} / \Lambda^2$	$[-0.30, 0.30]$	$[-0.44, 0.15]$	$[-0.42, 0.19]$	$[-0.34, 0.12]$
$c_{Qq}^{(3,1)} / \Lambda^2$	$[-0.35, 0.35]$	$[-0.54, 0.15]$	$[-0.10, 0.084]$	$[-0.062, 0.049]$
$c_{td}^{(8)} / \Lambda^2$	$[-0.47, 0.47]$	$[-0.67, 0.28]$	$[-0.51, 0.26]$	$[-0.41, 0.18]$
$c_{Qd}^{(8)} / \Lambda^2$	$[-0.52, 0.52]$	$[-0.76, 0.28]$	$[-0.53, 0.28]$	$[-0.42, 0.19]$
$c_{qt}^{(1)} / \Lambda^2$	$[-0.65, 0.65]$	$[-0.99, 0.32]$	$[-0.10, 0.090]$	$[-0.078, 0.066]$
$c_{Qq}^{(3,8)} / \Lambda^2$	$[-0.76, 0.76]$	$[-1.1, 0.42]$	$[-0.24, 0.20]$	$[-0.14, 0.12]$

$c_{lq}^{(3)}/\Lambda^2$	$[-0.81, 0.97]$	$[-1.5, -0.034]$	$[-0.32, 0.26]$	$[-0.26, 0.16]$
$c_{Qu}^{(1)}/\Lambda^2$	$[-1.2, 1.2]$	$[-1.9, 0.62]$	$[-0.14, 0.13]$	$[-0.10, 0.093]$
$c_{H\Box}/\Lambda^2$	$[-1.3, 1.4]$	$[-0.085, 2.7]$	$[-1.3, 1.3]$	$[-0.086, 2.5]$
$c_{td}^{(1)}/\Lambda^2$	$[-1.5, 1.5]$	$[-0.89, 2.1]$	$[-0.15, 0.17]$	$[-0.11, 0.13]$
$c_{qd}^{(1)}/\Lambda^2$	$[-1.7, 1.7]$	$[-1.8, 1.7]$	$[-0.060, 0.059]$	$[-0.069, 0.067]$
$c_{qu}^{(1)}/\Lambda^2$	$[-1.8, 1.8]$	$[-2.9, 0.72]$	$[-0.040, 0.040]$	$[-0.048, 0.047]$
$c_{tu}^{(1)}/\Lambda^2$	$[-2.1, 2.1]$	$[-3.0, 1.1]$	$[-0.12, 0.11]$	$[-0.091, 0.086]$
$\text{Re}(c_{tH})/\Lambda^2$	$[-2.2, 2.0]$	$[-3.8, 0.56]$	$[-2.2, 2.0]$	$[-3.8, 0.54]$
$c_{Qq}^{(1,1)}/\Lambda^2$	$[-3.9, 3.0]$	$[-3.8, 4.0]$	$[-0.10, 0.10]$	$[-0.075, 0.075]$
c_{Ht}/Λ^2	$[-3.1, 4.0]$	$[-3.8, 3.6]$	$[-3.8, 3.4]$	$[-4.9, 3.1]$
$c_{Qd}^{(1)}/\Lambda^2$	$[-4.0, 4.0]$	$[-6.1, 1.9]$	$[-0.18, 0.17]$	$[-0.14, 0.13]$
c_{tt}/Λ^2	$[-5.4, 3.9]$	$[-7.8, 2.7]$	$[-1.0, 1.1]$	$[-1.3, 1.4]$
$c_{lq}^{(1)}/\Lambda^2$	$[-4.8, 4.6]$	$[-5.3, 4.8]$	$[-0.54, 0.56]$	$[-0.36, 0.36]$
$c_{lQ}^{(3)}/\Lambda^2$	$[-5.6, 6.7]$	$[-6.9, 5.6]$	$[-2.1, 1.7]$	$[-2.0, 1.6]$
$c_{lQ}^{(1)}/\Lambda^2$	$[-7.2, 5.9]$	$[-6.3, 7.2]$	$[-1.9, 2.3]$	$[-1.8, 2.3]$
c_{lu}/Λ^2	$[-7.0, 6.2]$	$[0.76, 12]$	$[-0.60, 0.65]$	$[-0.37, 0.44]$
$c_{Qt}^{(1)}/\Lambda^2$	$[-6.6, 9.1]$	$[-4.5, 13]$	$[-1.9, 1.7]$	$[-2.4, 2.2]$
c_{et}/Λ^2	$[-9.5, 7.9]$	$[-7.7, 9.8]$	$[-2.0, 2.4]$	$[-1.9, 2.4]$
$c_{QQ}^{(1)}/\Lambda^2$	$[-18, 13]$	$[-28, 8.4]$	$[-3.9, 4.6]$	$[-5.2, 5.8]$
$c_{Qt}^{(8)}/\Lambda^2$	$[-19, 14]$	$[-29, 8.4]$	$[-3.4, 4.0]$	$[-4.4, 4.9]$
c_{lt}/Λ^2	$[-20, 17]$	$[-19, 19]$	$[-2.1, 2.2]$	$[-2.0, 2.2]$

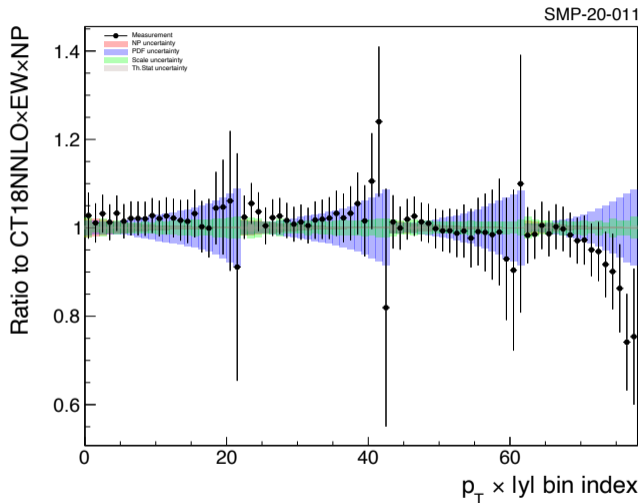








Modifications to input analyses: Inclusive jets predictions



- Rederived both nominal NNLO QCD predictions and uncertainties with CT18 NNLO PDF set
- PDF uncertainties: 28 eigenvector variations, symmetrized and taken as fully correlated between bins
- Renormalization and factorization scale: correlated between p_T bins of a given $|y|$ bin
- Theory statistical: obtained from fastNLO, treated as uncorrelated between bins
- Electroweak corrections and uncertainties from non-perturbative effects taken from HEPData

Electroweak precision observables from LEP & SLC

The measurement of eight pseudo-observables measured at LEP and SLC [35, 36] is incorporated in the interpretation presented here. These observables are the Z boson total width, Γ_Z ; the hadronic pole cross section, σ_{had}^0 , defined as

$$\sigma_{\text{had}}^0 = \frac{12\pi}{m_Z^2} \frac{\Gamma_{ee}\Gamma_{\text{had}}}{\Gamma_Z^2}, \quad (2)$$

where Γ_{ee} is the partial decay width of the Z boson to an electron-positron pair and $\Gamma_{\text{had}} = \Gamma_{uu} + \Gamma_{dd} + \Gamma_{cc} + \Gamma_{ss} + \Gamma_{bb}$ is the hadronic Z boson decay width; three ratios of partial decay widths, R_ℓ, R_c, R_b , defined as

$$R_\ell = \frac{\Gamma_{\text{had}}}{\Gamma_{\ell\ell}}, \quad R_{c,b} = \frac{\Gamma_{cc,bb}}{\Gamma_{\text{had}}}; \quad (3)$$

and three forward-backward asymmetries, $A_{FB}^{0,\ell}, A_{FB}^{0,c}, A_{FB}^{0,b}$, defined as

$$A_{FB} = \frac{N_F - N_B}{N_F + N_B}. \quad (4)$$

In this expression, N_F (N_B) is the number of events where the charged lepton, c quark, or b quark is produced in the direction of the electron beam (anti-electron beam). SMEFT corrections on these pseudo-observables were evaluated analytically in Ref. [36].

SMEFT parameterization (details on event generation)

$$\sigma_{p,\text{SMEFT}}^i = \sigma_{p,\text{SM}}^i \left(1 + \sum_j A_{p,j}^i \frac{c_j}{\Lambda^2} + \sum_{j,k} B_{p,jk}^i \frac{c_j c_k}{\Lambda^4} \right)$$

- $A_{p,j}^i \frac{c_j}{\Lambda^2}$: *linear terms* or *interference terms*, from interference of SM and BSM
- $B_{p,jk}^i \frac{c_j c_k}{\Lambda^4}$: *quadratic terms* or *cross terms* (when $j \neq k$)
- Constants $A_{p,j}^i$, $B_{p,jk}^i$ are computed by generating events at LO with MADGRAPH5_AMC@NLO + PYTHIA 8.3. SMEFT effects are modelled using SMEFTsim3 (and SMEFT@NLO for loop-induced processes $gg \rightarrow H$ and $gg \rightarrow ZH$)
- Phase space selections for each kinematic bin are reproduced using RIVET 3.1.9
- NNPDF 3.1 is used when computing the parameterizations
- All parameterizations use $\{m_W, m_Z, G_F\}$ input scheme and topU31 flavour symmetry

SMEFT operators (1/2)

X^3		
$\mathcal{Q}_G = f^{abc} G_\mu^{av} G_\nu^{bp} G_\rho^{c\mu}$	$\mathcal{Q}_W = \epsilon^{ijk} W_\mu^{iv} W_\nu^{jp} W_\rho^{k\mu}$	
$H^4 D^2$		
$\mathcal{Q}_{H\Box} = (H^\dagger H)\Box(H^\dagger H)$	$\mathcal{Q}_{HD} = (D^\mu H^\dagger H)(H^\dagger D_\mu H)$	
$X^2 H^2$		
$\mathcal{Q}_{HG} = H^\dagger H G_{\mu\nu}^a G^{a\mu\nu}$ $\mathcal{Q}_{HWB} = H^\dagger H W_{\mu\nu}^i B^{\mu\nu}$	$\mathcal{Q}_{HW} = H^\dagger H W_{\mu\nu}^i W^{i\mu\nu}$	$\mathcal{Q}_{HB} = H^\dagger H B_{\mu\nu} B^{\mu\nu}$
$\psi^2 H^3$		
$\mathcal{Q}_{tH} = (H^\dagger H)(\bar{Q}\tilde{H}t)$	$\mathcal{Q}_{bH} = (H^\dagger H)(\bar{Q}Hb)$	
$\psi^2 XH$		
$\mathcal{Q}_{tW} = (\bar{Q}\sigma^{\mu\nu}t)\sigma^i \tilde{H}W_{\mu\nu}^i$	$\mathcal{Q}_{tB} = (\bar{Q}\sigma^{\mu\nu}t)\tilde{H}B_{\mu\nu}$	$\mathcal{Q}_{tG} = (\bar{Q}\sigma^{\mu\nu}T^a t)\tilde{H}G_{\mu\nu}^a$
$\psi^2 H^2 D$		
$\mathcal{Q}_{Hl}^{(1)} = (H^\dagger i\overleftrightarrow{D}_\mu H)(\bar{l}_p \gamma^\mu l_r)$	$\mathcal{Q}_{Hl}^{(3)} = (H^\dagger i\overleftrightarrow{D}_\mu^i H)(\bar{l}_p \sigma^i \gamma^\mu l_r)$	$\mathcal{Q}_{He} = (H^\dagger i\overleftrightarrow{D}_\mu H)(\bar{e}_p \gamma^\mu e_r)$
$\mathcal{Q}_{Hq}^{(1)} = (H^\dagger i\overleftrightarrow{D}_\mu H)(\bar{q} \gamma^\mu q)$	$\mathcal{Q}_{Hq}^{(3)} = (H^\dagger i\overleftrightarrow{D}_\mu^i H)(\bar{q} \sigma^i \gamma^\mu q)$	$\mathcal{Q}_{Hu} = (H^\dagger i\overleftrightarrow{D}_\mu H)(\bar{u} \gamma^\mu u)$
$\mathcal{Q}_{Hd} = (H^\dagger i\overleftrightarrow{D}_\mu H)(\bar{d} \gamma^\mu d)$	$\mathcal{Q}_{HQ}^{(1)} = (H^\dagger i\overleftrightarrow{D}_\mu H)(\bar{Q} \gamma^\mu Q)$	$\mathcal{Q}_{HQ}^{(3)} = (H^\dagger i\overleftrightarrow{D}_\mu^i H)(\bar{Q} \sigma^i \gamma^\mu Q)$
$\mathcal{Q}_{Ht} = (H^\dagger i\overleftrightarrow{D}_\mu H)(\bar{t} \gamma^\mu t)$	$\mathcal{Q}_{Hb} = (H^\dagger i\overleftrightarrow{D}_\mu H)(\bar{b} \gamma^\mu b)$	

SMEFT operators (2/2)

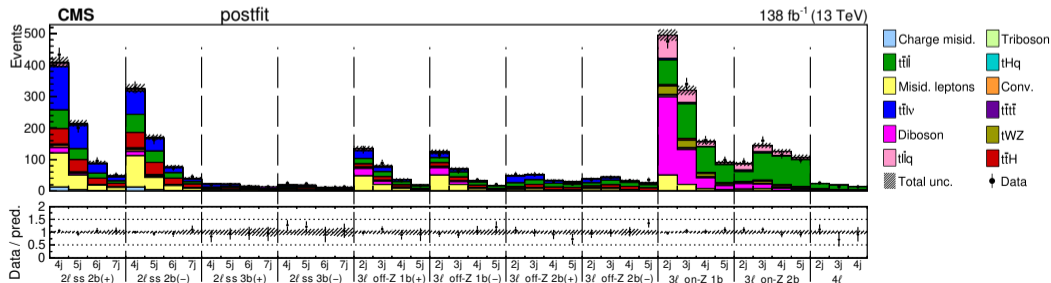
$\psi^4, (\bar{L}L)(\bar{L}L)$		
$\mathcal{Q}_{lq}^{(1)} = (\bar{l}_p \gamma_\mu l_r)(\bar{q} \gamma^\mu q)$	$\mathcal{Q}_{lq}^{(3)} = (\bar{l}_p \sigma^i \gamma_\mu l_r)(\bar{q} \sigma^i \gamma^\mu q)$	$\mathcal{Q}_{lQ}^{(1)} = (\bar{l}_p \gamma_\mu l_r)(\bar{Q} \gamma^\mu Q)$
$\mathcal{Q}_{lQ}^{(3)} = (\bar{l}_p \sigma^i \gamma_\mu l_r)(\bar{Q} \sigma^i \gamma^\mu Q)$	$\mathcal{Q}_{QQ}^{(1)} = (\bar{Q} \gamma_\mu Q)(\bar{Q} \gamma^\mu Q)$	$\mathcal{Q}_{ll} = (\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$
$\mathcal{Q}_{qq}^{(1,1)} = (\bar{q} \gamma_\mu q)(\bar{q} \gamma^\mu q)$	$\mathcal{Q}_{qq}^{(1,8)} = (\bar{q} T^a \gamma_\mu q)(\bar{q} T^a \gamma^\mu q)$	$\mathcal{Q}_{qq}^{(3,1)} = (\bar{q} \sigma^i \gamma_\mu q)(\bar{q} \sigma^i \gamma^\mu q)$
$\mathcal{Q}_{qq}^{(3,8)} = (\bar{q} \sigma^i T^a \gamma_\mu q)(\bar{q} \sigma^i T^a \gamma^\mu q)$	$\mathcal{Q}_{Qq}^{(1,1)} = (\bar{Q} \gamma_\mu Q)(\bar{q} \gamma^\mu q)$	$\mathcal{Q}_{Qq}^{(1,8)} = (\bar{Q} T^a \gamma_\mu Q)(\bar{q} T^a \gamma^\mu q)$
$\mathcal{Q}_{Qq}^{(3,1)} = (\bar{Q} \sigma^i \gamma_\mu Q)(\bar{q} \sigma^i \gamma^\mu q)$	$\mathcal{Q}_{Qq}^{(3,8)} = (\bar{Q} \sigma^i T^a \gamma_\mu Q)(\bar{q} \sigma^i T^a \gamma^\mu q)$	

$\psi^4, (\bar{R}R)(\bar{R}R)$		
$\mathcal{Q}_{et} = (\bar{e}_p \gamma_\mu e_r)(\bar{t} \gamma^\mu t)$	$\mathcal{Q}_{tt} = (\bar{t} \gamma_\mu t)(\bar{t} \gamma^\mu t)$	$\mathcal{Q}_{uu}^{(1)} = (\bar{u} \gamma_\mu u)(\bar{u} \gamma^\mu u)$
$\mathcal{Q}_{uu}^{(8)} = (\bar{u} T^a \gamma_\mu u)(\bar{u} T^a \gamma^\mu u)$	$\mathcal{Q}_{tu}^{(1)} = (\bar{t} \gamma_\mu t)(\bar{u} \gamma^\mu u)$	$\mathcal{Q}_{tu}^{(8)} = (\bar{t} T^a \gamma_\mu t)(\bar{u} T^a \gamma^\mu u)$
$\mathcal{Q}_{dd}^{(1)} = (\bar{d} \gamma_\mu d)(\bar{d} \gamma^\mu d)$	$\mathcal{Q}_{dd}^{(8)} = (\bar{d} T^a \gamma_\mu d)(\bar{d} T^a \gamma^\mu d)$	$\mathcal{Q}_{ud}^{(1)} = (\bar{u} \gamma_\mu u)(\bar{d} \gamma^\mu d)$
$\mathcal{Q}_{ud}^{(8)} = (\bar{u} T^a \gamma_\mu u)(\bar{d} T^a \gamma^\mu d)$	$\mathcal{Q}_{td}^{(1)} = (\bar{t} \gamma_\mu t)(\bar{d} \gamma^\mu d)$	$\mathcal{Q}_{td}^{(8)} = (\bar{t} T^a \gamma_\mu t)(\bar{d} T^a \gamma^\mu d)$

$\psi^4, (\bar{L}L)(\bar{R}R)$		
$\mathcal{Q}_{lu} = (\bar{l}_p \gamma_\mu l_r)(\bar{u} \gamma^\mu u)$	$\mathcal{Q}_{lt} = (\bar{l}_p \gamma_\mu l_r)(\bar{t} \gamma^\mu t)$	$\mathcal{Q}_{qu}^{(1)} = (\bar{q} \gamma_\mu q)(\bar{u} \gamma^\mu u)$
$\mathcal{Q}_{qu}^{(8)} = (\bar{q} T^a \gamma_\mu q)(\bar{u} T^a \gamma^\mu u)$	$\mathcal{Q}_{Qu}^{(1)} = (\bar{Q} \gamma_\mu Q)(\bar{u} \gamma^\mu u)$	$\mathcal{Q}_{Qu}^{(8)} = (\bar{Q} T^a \gamma_\mu Q)(\bar{u} T^a \gamma^\mu u)$
$\mathcal{Q}_{qt}^{(1)} = (\bar{q} \gamma_\mu q)(\bar{t} \gamma^\mu t)$	$\mathcal{Q}_{qt}^{(8)} = (\bar{q} T^a \gamma_\mu q)(\bar{t} T^a \gamma^\mu t)$	$\mathcal{Q}_{Qt}^{(1)} = (\bar{Q} \gamma_\mu Q)(\bar{t} \gamma^\mu t)$
$\mathcal{Q}_{Qt}^{(8)} = (\bar{Q} T^a \gamma_\mu Q)(\bar{t} T^a \gamma^\mu t)$	$\mathcal{Q}_{qd}^{(1)} = (\bar{q} \gamma_\mu q)(\bar{d} \gamma^\mu d)$	$\mathcal{Q}_{qd}^{(8)} = (\bar{q} T^a \gamma_\mu q)(\bar{d} T^a \gamma^\mu d)$
$\mathcal{Q}_{Qd}^{(1)} = (\bar{Q} \gamma_\mu Q)(\bar{d} \gamma^\mu d)$	$\mathcal{Q}_{Qd}^{(8)} = (\bar{Q} T^a \gamma_\mu Q)(\bar{d} T^a \gamma^\mu d)$	

Input Measurements: CMS-TOP-22-006, $t\bar{t}$ EFT

- CMS-TOP-22-006 (JHEP 12 (2023) 068):
 - EFT in associated top quark production ($t\bar{t}H$, $t\bar{t}W$, $t\bar{t}Z$, tZq , tHq , and $t\bar{t}t\bar{t}$ processes)
- Each process can be studied individually, but they are irreducible backgrounds to each other
- Event selection based on number of leptons, jets, and b-tagged jets
 - 43 categories, binning in a kinematical variable within each category
- Total predicted event yield in each observable bin parameterized as a quadratic function of 26 WCs
 - Detector-level predictions accounting for all relevant EFT effects on each of the signal processes simultaneously



Input Measurements: CMS-TOP-22-006, $t\bar{t}X$ EFT

- Original analysis sets constraints on 26 Wilson coefficients in the dim6_{top} basis
- In the combination we use topU31 SMEFT basis as implemented in SMEFTsim3, and consider additional operators that may affect the $t\bar{t}X$ processes
- To include $t\bar{t}X$ analysis in the combination in a consistent way, we therefore had to
 - rotate from dim6_{top} to SMEFT topU31
 - study the effect of missing operators on $t\bar{t}X$ processes
- $\mathcal{Q}_{H\Box}$ uniformly scales all SM Higgs boson couplings
 - added to $t\bar{t}X$ analysis as **rescaling** of $t\bar{t}H$ and tHq signals
- **2-heavy-2-light quark operators** enhance $t\bar{t}Z$ and $t\bar{t}H$ production rates (effect on shape and normalization)
 - added to $t\bar{t}X$ analysis by **reweighting the signal samples** using standalone reweighting modules produced by MadGraph («post-mortem reweighting»)
- Effect of other operators found to be negligible

