Neutrino oscillation physics with neutrinos from accelerators

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For the T2K collaboration



Physics in Collisions Athens, October 22, 2024









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CINIS

_es **deux infinis**

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Outline

- Introduction
- T2K experiment
- T2K oscillation analysis and results
- T2K-NOvA combined fit
- T2K-SK combined fit
- Next generation long baseline experiments : HyperKamiokande
- Conclusions

On behalf of the T2K collaboration, and for some results of the T2K-NovA, T2K-SK and HyperKamiokande collaborations

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Extraordinary neutrinos



Credit :Symmetry

3

Extraordinary neutrinos

TeV

GeV

MeV

keV

eV

meV

neutrinos

- « Nonzero neutrino masses are not possible without the existence of new fundamental fields » (A. De Gouvea CERN Courier May 2024, see also PDG Neutrino Masses Mixing and Oscillations,)
- Neutrino masses are at least 6 orders of magnitude below the other fermions
- Large mixing angles

 $V_{CKM} = \begin{pmatrix} 1 & 0.2 & 0.001 \\ 0.2 & 1 & 0.01 \\ 0.001 & 0.01 & 1 \end{pmatrix} \qquad V_{PMNS} = \begin{pmatrix} 0.8 & 0.5 & 0.2 \\ 0.4 & 0.6 & 0.7 \\ 0.4 & 0.6 & 0.7 \end{pmatrix}$

 Neutrinos are a crucial link between particle physics and cosmology Marco Zito PIC 2024

The PMNS neutrino mixing matrix

$$\begin{pmatrix} \nu_{e} \\ \nu_{\mu} \\ \nu_{\tau} \\ \nu_{\tau} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \begin{pmatrix} \cos \theta_{13} & 0 & \sin \theta_{13} e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -\sin \theta_{13} e^{i\delta_{CP}} & 0 & \cos \theta_{13} \end{pmatrix} \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ -\sin \theta_{12} & \cos \theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_{1} \\ \nu_{2} \\ \nu_{3} \\ 0 & 0 & 1 \end{pmatrix}_{\text{Mass eigenstates}}$$
eigenstates
$$\begin{array}{c} \text{Atmospherics and LBL} \\ \theta_{23} \sim 45^{\circ} \\ |\Delta m_{23}^{2}| \sim 2.5 \ 10^{-3} \ \text{eV}^{2} \end{array} \quad \begin{array}{c} \text{Reactors} \\ \theta_{13} \sim 10^{\circ} \\ \text{LBL} & \theta_{13} \delta_{CP} \end{array} \quad \begin{array}{c} \text{Solar and reactors} \\ \theta_{12} \sim 35^{\circ} \\ \Delta m_{21}^{2} \sim 7.5 \ 10^{-5} \ \text{eV}^{2} \end{array}$$

- Long baseline (LBL) experiments are sensitive to 5 of the PMNS parameters :
- θ_{23} $|\Delta m^2_{32}|$ most precise measurements by LBL
- θ_{13} Precisely measured by reactor exp.
- $\delta_{_{CP}}$ (LBL only) and mass ordering (LBL, atm, JUNO)

What we measure in long baseline experiments :

 $v_{\mu} \rightarrow v_{\mu}$ disappearance

$$P(v_{\mu} \rightarrow v_{\mu}) \approx 1 - (\cos^{4}\theta_{13}\sin^{2}2\theta_{23} + \sin^{2}2\theta_{13}\sin^{2}\theta_{23}) \sin^{2}\frac{\Delta m^{2}_{31}L}{4E}$$

Leading term

- θ_{23} close to 45° : maximal disappearance
- Easy to observe, but difficult to determine $\theta_{_{23}}$ octant, relying mainly on the subleading term



What we measure in long baseline experiments :

$v_{\mu} \rightarrow v_{e}$ appearance

 $P(v_{\mu} \rightarrow v_{e}) = 4c^{2}{}_{13}s^{2}{}_{13}s^{2}{}_{23}\sin^{2}\Delta_{31}$ "Atmospheric" term (leading) +8c^{2}{}_{13}s_{12}s_{13}s_{23}(c_{12}c_{23}\cos\delta - s_{12}s_{13}s_{23})S_{12}S_{13}S_{23}\cos\Delta_{32}\sin\Delta_{31}\sin\Delta_{21} CP conserving =8c^{2}{}_{13}c_{12}c_{23}s_{12}s_{13}s_{2}\sin\delta\sin\Delta_{32}\sin\Delta_{31}\sin\Delta_{21} CP violating term +4s^{2}{}_{12}c^{2}{}_{13}(c^{2}{}_{12}c^{2}{}_{23} + s^{2}{}_{12}s^{2}{}_{23}s^{2}{}_{13} - 2c_{12}c_{23}s_{12}s_{23}s_{13}\cos\delta)\sin^{2}\Delta_{21} "Solar" term NB in vacuum ! $c_{ij} = \cos\theta_{ij}s_{ij} = \sin\theta_{ij}$ $\Delta_{ij} = \Delta m^{2}{}_{ij}L/4E$

- θ_{13} relatively large (precisely measured by reactors exp.)
- CP violation effect : small modulation ~30 %
- Neutrino propagating in the Earth crust : « matter effect », mimicking a CP violation effect. Enhancement or suppression for neutrinos depending on the mass ordering.



Why accelerator-based experiments ?

- Allow to produce an (almost) pure v_{μ} neutrino beam, with tuned and controlled flux
- Allow to choose a beam of neutrinos or antineutrinos by reversing the polarity of the magnetic focussing system (CP measurement!)
- Precisely measure neutrino interactions at the near detectors. Precisely control other neutrino species, (anti)neutrinos with a magnetic spectrometer
- Control of the experimental conditions: precision measurements of parameters (ideally we would like to push precision to the % level like the CKM matrix)
- Underground observatory for other neutrinos : solar, atmospherics, SN etc

The Tokai to Kamioka (T2K) experiment



The T2K beamline



- 30 GeV/c proton beam from J-PARC main ring impinging on a graphite target
- p+C interactions copiously produce pions (and kaons)
- 90m decay volume followed by beam dump and muon monitors
- Off-axis beam (kinematics of pion two-body decay) allow to tune the energy by aiming the beam slightly off (2.5°)
- Charge selected and focused by three magnetic horns : either $\pi^+ \rightarrow \mu^+ \nu_{\mu}$ or $\pi^- \rightarrow \mu^- \overline{\nu_{\mu}}$





T2K beamline upgrade

- Replacement of the Main Ring Power Supply for higher repetition rate from 2.48 s to 1.36s
- Horns operated at 320 kA (instead of 250 kA) : 10 % increase in v flux
- A major upgrade preparing for HK period, 800 kW reached in 2024 (1.3 MW by 2027)



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NA61-SHINE

- Hadroproduction experiment at CERN SPS
- Precisely measures pion and kaon cross-section and spectra with a T2K replica target
- Allows to precisely control the neutrino flux (unprecedented 5 % level !)
- Will provide measurements also for NOvA, DUNE





Double differential cross-section Eur.Phys.J.C 79 (2019) 2, 100

ND280: Neutrino Mode, v

T2K Neutrino flux



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Super-Kamiokande



•50 kton Water Cherenkov detector operated since 1996

- •11146 20" PMTs inner detector, 1885 8" PMTs outer detector
- •Depth ~1000 m (2700 mwe)
- Particle identification capability e/µ
- •Added 0.03 % Gd in 2022 to improve the neutron tagging efficiency
- Reconstruction of the lepton momentum and angle
- Multi-ring fit allows to identify π° decays (suppresses the NC π° background)
- Identification of delayed Michel electrons



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Near detector complex at 280 m



The off-axis near detector ND280





ND280 upgrade in 2023



- Installed inside the UA1/NOMAD magnet (0.2 T) donated by CERN
- Active targets (FGD1 pure scintillator ; FGD2 includes also water layers)
- Three large TPCs with MicroMegas detectors : charge and momentum, PID based on dE/dx
- An electromagnetic calorimeter
- A major upgrade with novel detectors was installed in 2023-2024 including TOF all around it

ND280 Upgrade : Super Fine Grained Detector

- A novel detector to serve as active target for the neutrino interactions
- 2 million optically independent scintillator cubes (1cm³) read out by three orthogonal WLS fibers (60 000 channels, MPPC)
- ~ 40 p.e./MIP/fiber
- High granularity: proton threshold at 300 MeV/c, separation of electron/gamma, 3D-like tracking reconstruction. Reconstruction of neutrons
- Lowering the proton threshold will help modeling neutrino nucleus interactions



A candidate event of numu interaction with two protons exiting the nucleus







ND280 Upgrade :High Angle TPCs

- Two new TPCs equipped with resistive MicroMegas technology (charge spreading)
- Atmospheric pressure : $Ar CF_4$ (3%)- iC_4H_{10} (2%)
- Pad size ~1x1 cm², 200 μm space resolution
- dE/dx ~ 7 % for MIP, PID e/ μ



Run number : 16070 | SubRun number : 7 | Event number : 169035 | Spill : 2272 | Time : Thu 2023-12-21 02:30:36 JST | Partition : 61 | Trigger: Beam Spill



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 3D View
 Back
 Left Side
 Bottom
 Multiple Views

 Hide
 Multiple Views

 Hide
 Left Column

 Hide
 Right Side

Run number : 16070 | SubRun number : 2 | Event number : 57918 | Spill : 57538 | Time : Wed 2023-12-20 22:12:15 JST | Partition : 61 | Trigger: Beam Spill



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Neutrino-nucleus cross-section

- At T2K energies the Charged Current Quasi-Elastic (CCQE) scattering is dominant
- But significant 2p2h and resonant contribution (CCRES)
- A wrong model for the cross-section might bias the neutrino oscillation results
- Selection of relevant samples at the near detector : CC0pi, CC1pi, CCnpi, topologies related to CCQE, CCRES, DIS



T2K oscillation analysis



Near and Far detector data are fitted either sequentially or simultaneously depending on the analysis considered

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ND280 selections

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ND280 is a magnetized detector

- We select interactions on CH (FGD1) and CH/Water (FGD2)
- Precise measurement of p and θ
- We separate nu from antinu interactions on the basis of the charge of the lepton
- Separate samples based on the number of reconstructed pions, protons, photons. 22 samples used in the fit (about 120 k ev)





Super-Kamiokande selections













- 1 Ring mu-like or e-like in nu mode (CCQE enhanced)
- 2 Rings (mu-like) or additional decay el. (elike) (CC1pi enhanced)
- 1 Ring mu-like or e-like in antinu mode (CCQE enhanced)





Oscillation analysis results $:\theta_{23}$ and $|\Delta m^2_{32}|$

T2K

NOvA

MINOS+

IceCube

SuperK

RENO

RENO

Dava Bay

nGd

nGd

nH

2.2

SuperK+T2K

- Mature and precise measurements (2 % on $|\Delta m^2_{32}|$)
- θ_{23} Close to maximal disappearance
- Slight preference for upper octant





Oscillation analysis results : δ_{CP} and mass ordering

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Sample	$\delta_{CP}=-\pi/2$	$\delta_{CP}=0$	δ _{CP} =π/2	$\delta_{CP}=\pi$	Data
ν-mode 1Rμ	417.2	416.3	417.1	418.2	357
ν -mode MR	123.9	123.3	123.9	124.4	140
$\bar{\nu}$ -mode 1Rµ	146.6	146.3	146.6	147.0	137
ν -mode 1Re	113.2	95.5	78.3	96.0	102
$\bar{\nu}$ -mode 1Re+d.e.	10.0	8.8	7.2	8.4	15 🍃
$\bar{\nu}$ -mode 1Re	17.6	20.0	22.2	19.7	16



Slight preference for $\delta_{_{CP}} \sim -\pi/2$ but CP conserving value within 2σ

slight preference for normal ordering

NB this is not a simple counting analysis

NOVA

Vu

810 km

Long baseline neutrino experiments based on the Fermilab NUMi neutrino beam

E~2 GeV L=810 km

Similar liquid scintillator calorimeters at near (300 t) and far position (14kt) (Ash River, MN)

Near detector

Calorimetric neutrino energy reconstruction

Fermilab

See talk by Jianming Bian in the parallel session



Figures and plots courtesy Nova Collaboration

T2K-NovA : θ_{23} and $|\Delta m^2_{32}|$

- The NovA and T2K collaborations have worked very hard on a joint fit
- Full use of multidimensional likelihoods
- Thorough check of correlation between sources of syst. uncertainties
- A lot of checks on the neutrino interaction models used
- The joint fit p-value is greated than 5 %





consistency of the 3v model.

T2K-NovA : v appearance





T2K-NovA $\delta_{\rm CP}$



Inverted ordering : $\delta_{CP} \sim -\pi/2$ preferred. Normal ordering $\delta_{CP} \sim -\pi$ (but very weak constraint). The mass ordering preference is not statistically significant.

T2K-SK

- T2K has good sensitivity to δ_{CP} but mild sensitivity to mass ordering
- SK has good constraint on mass ordering but not on δ_{CP}
- Adding SK atmospheric sample allows to break the degeneracies between the CP violation parameter δ_{CP} and the mass ordering → boost sensitivity to CP
- Unified interaction model for T2K and SK low-energy samples, and detector systematics

Normal ordering is preferred, p-value for IO 0.08









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cess Tunn

187 kton 20 000 PMT

Hyper-Kamiokande

- 187 kt (8 times bigger than SuperKamiokande)
- Same baseline as T2K (295 km)
- Upgraded beam from J-PARC (1.3 MW)
- Instrumented with 20k PMTs and 800 mPMT
- Start operation end of 2027
- $v_{\mu} \rightarrow v_{e}$ samples larger than 1000 ev
- Mass ordering with atmospherics and beam
- Other topics : solar neutrinos, SN (70k events at 10kpc), SN relics, proton decay





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	$\sin^2 \theta_{23}$	Atmospheric neutrino	Atm + Beam
Mass	0.40	2.2 σ	→ 3.8 σ
ordering	0.60	4.9 σ -	→ 6.2 σ
θ_{23}	0.45	2.2 σ	→ 6.2 σ
octant	0.55	1.6 σ -	→ 3.6 σ

10 years with 1.3MW, normal mass ordering is assumed



Conclusions

- The present generation of long baseline experiments has contributed to establishing the 3-neutrinos oscillation paradigm (ν_e appearance, precision |Δm²₃₂|, θ₁₃ in agreement with reactors)
- It has established new methods for modelling neutrino-nucleus interactions, near detector fit etc
- It has unveiled tantalizing hints of (possible) CP violation effects, however these measurements are statistically limited
- A new generation of experiments HyperKamiokande and DUNE is in construction with complementary features. They will bring in precision to solve the remaining questions.

Acknowledgements

Thanks to Claudio Giganti, Shigetaka Moriyama, Jeremy Winscott, for providing slides and plots



This is a simplified two neutrino scenario

Neutrino oscillations





Neutrino masses and ordering

- Neutrinos have a tiny mass : m < 2 eV from measurement of the β spectrum (Katrin will push this limit to 0.2 eV)
- Since they oscillate, neutrino have masses
- Oscillations have measured two mass splitting: $|\Delta m^2_{atm}| = 2.4 \ 10^{-3} \ eV^2$ and $\Delta m^2_{sol} = 7.5 \ 10^{-5} \ eV^2$ and vacuum leading order measurements are not sensitive to the absolute mass scale



The lightest solution is: m3~0, m1~m2~50 meV

• The measurement of the sign of Δm^2_{atm} has implications for the theoretical understanding of the v mass mechanism, long baseline CP violation measurements, 0- v double beta decay, and cosmology ⁴²

The study of neutrino properties

Today : few % precision on most of the parameters

Oscillation		Bes	"1σ"	
parame	ter	(NO)	(IO)	error
∆m²	/10 ⁻³ eV ²	2.49	2.47	1.3 %
δm²	/10⁻⁵ eV²	7.34	7.34	2.2 %
$sin^2\theta_{13}$	/10 ⁻²	2.23	2.24	3.0 %
$sin^2\theta_{12}$	/ 10 -1	3.04	3.03	4.4 %
$\sin^2\theta_{aa}$		0.56	0.56	~5%

Lisi Granada 2019

пi

But there are still major unknowns : Dirac or Majorana, CP violation phase δ , mass ordering and θ_{23} octant, absolute mass

Neutrinos : next steps

- 1) Leptonic CP violation (PMNS parameter δ)
- 2) Mass ordering (normal or inverse)
- 3) Is $\theta_{23} = 45^{\circ}$?
- 4) Precision tests of PMNS (at %, as for CKM)
- 5) Are there new neutral states ? (steriles, HNL)

- a) What is the nature of neutrinos (Dirac or Majorana) ?
- b) What is the absolute mass value of neutrinos ?
- c) Discover and measure the cosmological neutrinos
- d) Exploration of the Universe with UHE neutrinos

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Combined CP and matter effects

See also Dr. Segarra talk

in today parallel session

Combined effect of CP and matter

The relative increase of matter effect versus CP effect is due to the fact that these experiments are tuned to the L/E of the first oscillation maximum. The increasing L and therefore E are such that Prob ($\underline{v}_{u} \rightarrow \underline{v}_{e}$) approaches the MSW resonance.

For T2K, CP modulation +-27%, Matter effect ~10%

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Neutrino oscillation in matter

- Neutrino forward scattering on electrons, equivalent to light refraction index, leads to an additional phase for <u>electron neutrinos</u> proportional to $G_{_F} N_{_e}$
- The sign of the potential and therefore the phase depends on neutrino vs antineutrino
- This can be parameterized (for a constant density) as an effective mixing angle exhibiting a MSW resonance (E_{res}~7 GeV for ρ=4.5 g/cm³) either for neutrinos (NO) or antineutrinos (IO).
- <u>Matter effects can either enhance or suppress $v_{\mu} \rightarrow v_{e}$ depending on the <u>ordering.</u> Effective mixing angle</u>

T2K-NOvA

Not conclusive : broad region in deltaCP allowed

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ND fit CC0pi parameters

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MEASUREMENT OF NEUTRINO AND ANTINEUTRINO ...

PHYSICAL REVIEW D 96, 092006 (2017)

TABLE XIV. Event reduction for the ν_e CC selection at the far detector. The numbers of expected MC events divided into five categories are shown after each selection criterion is applied. The MC expectation is based upon three-neutrino oscillations with the parameters as shown in Table XIII.

		$ u_{\mu} + ar{ u}_{\mu}$	$\nu_e + \bar{\nu}_e$	$\nu + \bar{\nu}$	$\bar{\nu}_{\mu} \rightarrow \bar{\nu}_{e}$	$\nu_{\mu} \rightarrow \nu_{e}$	
ν -beam mode	MC total	CC	CC	NC	CC	CC	Data
Interactions in FV	744.89	364.32	18.55	326.16	0.39	35.47	
FCFV	431.85	279.88	18.09	98.72	0.38	34.78	438
Single ring ^a	223.49	153.40	11.15	28.68	0.32	29.95	220
Electronlike ^b	66.94	6.46	11.06	19.53	0.31	29.57	70
$E_{\rm vis} > 100 {\rm ~MeV}^{\rm c}$	61.78	4.59	11.01	16.81	0.31	29.06	66
$N_{\rm Michel-e} = 0^{\rm d}$	50.60	0.97	8.97	14.24	0.31	26.11	51
$E_{\nu}^{\rm rec} < 1250 {\rm MeV}^{\rm e}$	40.71	0.25	4.26	10.85	0.22	25.14	46
Not π^0 -like ^f	28.55	0.09	3.68	1.35	0.18	23.25	32
$\bar{\nu}$ -beam mode							
Interactions in FV	312.38	164.04	9.00	132.75	4.30	2.29	
FCFV	180.48	123.24	8.75	42.05	4.20	2.24	170
Single ring	96.06	73.21	5.51	11.87	3.74	1.73	94
Electronlike	21.55	2.31	5.48	8.36	3.70	1.71	16
$E_{\rm vis} > 100 {\rm MeV}$	20.05	1.83	5.46	7.39	3.68	1.69	14
$N_{\text{Michel-e}} = 0$	16.40	0.33	4.71	6.24	3.66	1.46	12
$E_{\nu}^{\rm rec} < 1250 {\rm MeV}$	11.40	0.08	1.89	4.83	3.42	1.19	9
Not π^0 -like	6.28	0.02	1.58	0.60	3.04	1.05	4

^aThere is only one reconstructed Cherenkov ring.

^bThe ring is e-like.

^cThe visible energy, $E_{\rm vis}$, is greater than 100 MeV.

^dThere is no reconstructed Michel electron.

^eThe reconstructed energy, E_{ν}^{rec} , is less than 1.25 GeV. ^fThe event is not consistent with a π^0 hypothesis.

MEASUREMENT OF NEUTRINO AND ANTINEUTRINO ...

PHYSICAL REVIEW D 96, 092006 (2017)

TABLE XV.	Event reducti	ion for the ν_{μ}	CC selection at	the far detector.	The numbers	of expected MC events
divided into fo	our categories	are shown afte	r each selection	criterion is appli	ied. The MC ex	pectation is based upon
three-neutrino	oscillations w	with the param	eters as shown	in Table XIII.		

		$ u_{\mu}$	$ar{ u}_{\mu}$	$ u_{\mu} + ar{ u}_{\mu}$	$\nu_e + \bar{\nu}_e$	$\nu+\bar\nu$	
v-beam mode	MC total	CCQE	CCQE	CC nonQE	CC	NC	Data
Interactions in FV	744.89	100.17	6.45	257.70	54.41	326.16	
FCFV	431.85	78.75	4.85	196.28	53.25	98.72	438
Single ring ^a	223.49	73.49	4.70	75.21	41.41	28.68	220
Muonlike ^b	156.56	72.22	4.65	70.06	0.47	9.16	150
$p_{\mu} > 200 \text{ MeV}/c^{c}$	156.24	72.03	4.65	70.00	0.47	9.08	150
$N_{\text{Michel-e}} \leq 1^{d}$	137.76	71.28	4.63	52.61	0.46	8.78	135
$\bar{\nu}$ -beam mode							
Interactions in FV	312.38	20.04	30.77	113.23	15.59	132.75	
FCFV	180.48	15.04	24.95	83.26	15.19	42.05	170
Single ring	96.06	13.52	24.28	35.41	10.98	11.87	94
Muonlike	74.52	13.40	23.96	33.56	0.09	3.52	78
$p_{\mu} > 200 \text{ MeV}/c$	74.42	13.39	23.92	33.54	0.09	3.48	78
$N_{\text{Michel-e}} \leq 1$	68.26	13.18	23.85	27.79	0.09	3.35	66

^aThere is only one reconstructed Cherenkov ring. ^bThe ring is μ -like. ^cThe reconstructed momentum, p_{μ} , is greater than 200 MeV/c. ^dThere are less than two reconstructed Michel electrons.

MEASUREMENT OF NEUTRINO AND ANTINEUTRINO ...

PHYSICAL REVIEW D 96, 092006 (2017)

TABLE XVI. Event reduction for the ν_e CC1 π^+ selection at the far detector. The numbers of expected MC events divided into five categories are shown after each selection criterion is applied. The MC expectation is based on the parameters of Table XIII.

		$ u_{\mu} + ar{ u}_{\mu}$	$\nu_e + \bar{\nu}_e$	$\nu+\bar\nu$	$\bar{\nu}_{\mu} \rightarrow \bar{\nu}_{e}$	$\nu_{\mu} \rightarrow \nu_{e}$	
v-beam mode	MC total	CC	CC	NC	CC	CC	Data
Interactions in FV	744.89	364.32	18.55	326.16	0.39	35.47	
FCFV	431.85	279.88	18.09	98.72	0.38	34.78	438
(1) Single ring ^a	223.49	153.40	11.15	28.68	0.32	29.95	220
(2) Electronlikeb	66.94	6.46	11.06	19.53	0.31	29.57	70
(3) $E_{\rm vis} > 100 {\rm MeV^c}$	61.78	4.59	11.01	16.81	0.31	29.06	66
(4) $N_{\text{Michel},e} = 1^{\text{d}}$	9.36	2.42	1.87	2.14	0.01	2.92	14
(5) $E_{\nu}^{\rm rec} < 1250 {\rm MeV}^{\rm e}$	4.66	0.70	0.50	0.78	< 0.01	2.66	11
(6) Not π^0 -like ^f	3.14	0.29	0.39	0.15	< 0.01	2.31	5

^aThere is only one reconstructed Cherenkov ring. ^bThe ring is *e*-like.

^cThe visible energy, $E_{\rm vis}$, is greater than 100 MeV. ^dThere is one reconstructed Michel electron.

^eThe reconstructed energy, E_{ν}^{rec} , is less than 1.25 GeV. ^fThe event is not consistent with a π^0 hypothesis.

	ν_e CCQE-like	ν_{μ}	$\nu_e \text{ CC1} \pi^+$
Source of uncertainty	$\delta N/N$	$\delta N/N$	$\delta N/N$
Flux	3.7%	3.6%	3.6%
(w/ ND280 constraint)			
Cross section	5.1%	4.0%	4.9%
(w/ ND280 constraint)			
Flux+cross section			
(w/o ND280 constraint)	11.3%	10.8%	16.4%
(w/ ND280 constraint)	4.2%	2.9%	5.0%
FSI + SI + PN at SK	2.5%	1.5%	10.5%
SK detector	2.4%	3.9%	9.3%
All			
(w/o ND280 constraint)	12.7%	12.0%	21.9%
(w/ ND280 constraint)	5.5%	5.1%	14.8%

TABLE XIX. Effect of 1σ variation of the systematic uncertainties on the predicted event rates of the ν -mode samples.

Eur. Phys. J. C (2023) 83:782

Table 10 Uncertainties on the number of events in each FD sample broken down by source after (before)the fit to ND data. "FD + SI + PN" combines the uncertainties from the FD detector, secondary particle interactions (SI), and photo-nuclear (PN) effects. "Flux⊗Interaction" denotes the combined effect from the ND constrained flux and inter-

action parameters, and the unconstrained interaction parameters. The change in the "FD + SI + PN" uncertainties before and after the ND fit is an indirect effect due to the change of interaction mode fractions in the samples after the ND fit

Sample		Uncertainty so	ource (%)	Flux⊗Interaction (%)	Total (%)	
		Flux	Interaction	FD + SI + PN		
$1R\mu$	ν	2.9 (5.0)	3.1 (11.7)	2.1 (2.7)	2.2 (12.7)	3.0 (13.0)
	$\overline{\nu}$	2.8 (4.7)	3.0 (10.8)	1.9 (2.3)	3.4 (11.8)	4.0 (12.0)
1Re	ν	2.8 (4.8)	3.2 (12.6)	3.1 (3.2)	3.6 (13.5)	4.7 (13.8)
	$\overline{\nu}$	2.9 (4.7)	3.1 (11.1)	3.9 (4.2)	4.3 (12.1)	5.9 (12.7)
1Re1de	ν	2.8 (4.9)	4.2 (12.1)	13.4 (13.4)	5.0 (13.1)	14.3 (18.7)