

# Light QCD exotics at BESIII

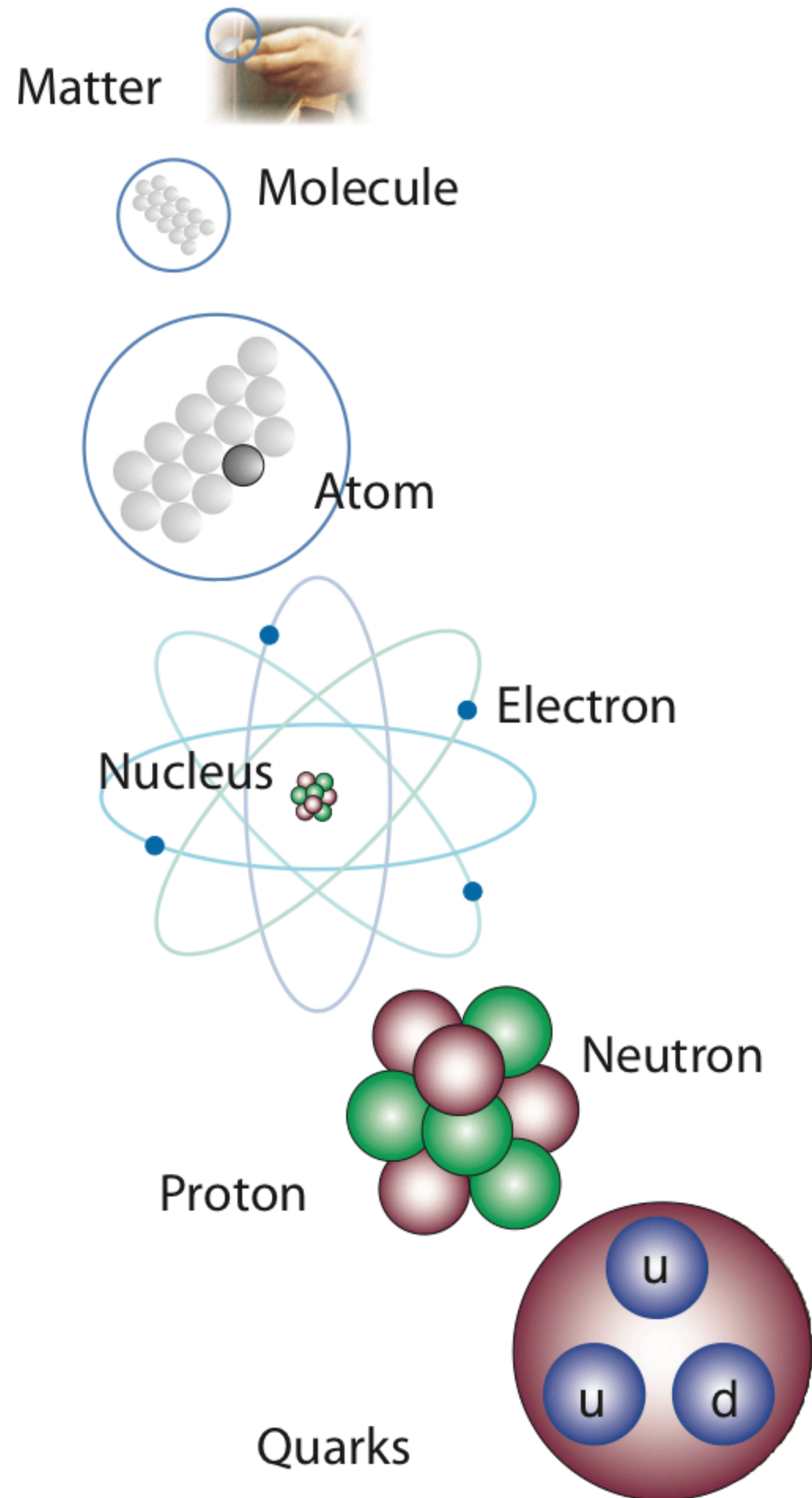
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**Yanping Huang**

(On behalf of the BESIII Collaboration)

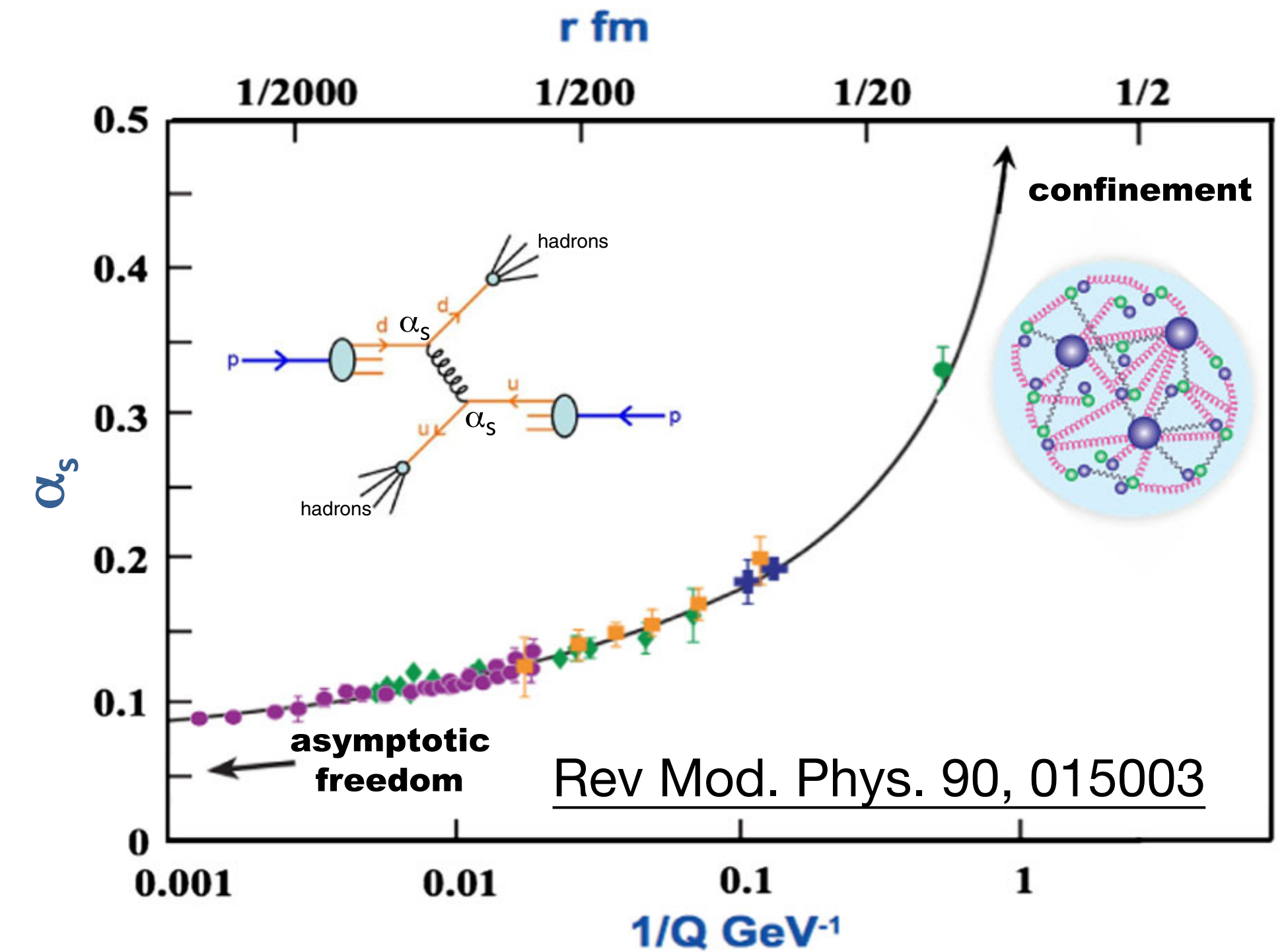
Institute of High Energy Physics, CAS

# Fundamental Structure of Matters



**Standard Model of Elementary Particles**

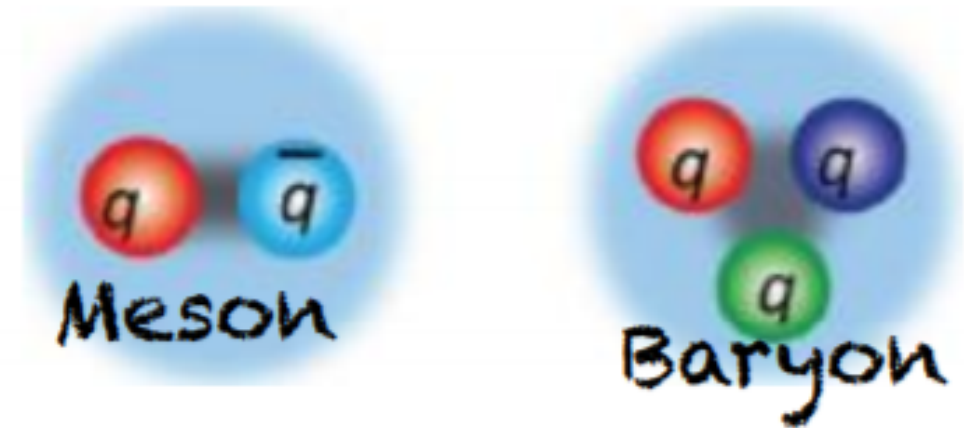
	three generations of matter (fermions)			interactions / force carriers (bosons)	
QUARKS	mass $\approx 2.2 \text{ MeV}/c^2$ charge $2/3$ spin $1/2$ <b>u</b> up	mass $\approx 1.28 \text{ GeV}/c^2$ charge $2/3$ spin $1/2$ <b>c</b> charm	mass $\approx 173.1 \text{ GeV}/c^2$ charge $2/3$ spin $1/2$ <b>t</b> top	mass $0$ charge $0$ spin $1$ <b>g</b> gluon	mass $\approx 125.11 \text{ GeV}/c^2$ charge $0$ spin $0$ <b>H</b> higgs
	mass $\approx 4.7 \text{ MeV}/c^2$ charge $-1/3$ spin $1/2$ <b>d</b> down	mass $\approx 95 \text{ MeV}/c^2$ charge $-1/3$ spin $1/2$ <b>s</b> strange	mass $\approx 4.18 \text{ GeV}/c^2$ charge $-1/3$ spin $1/2$ <b>b</b> bottom	mass $0$ charge $0$ spin $1$ <b><math>\gamma</math></b> photon	
	mass $\approx 0.511 \text{ MeV}/c^2$ charge $-1$ spin $1/2$ <b>e</b> electron	mass $\approx 105.66 \text{ MeV}/c^2$ charge $-1$ spin $1/2$ <b><math>\mu</math></b> muon	mass $\approx 1.7768 \text{ GeV}/c^2$ charge $-1$ spin $1/2$ <b><math>\tau</math></b> tau	mass $\approx 91.19 \text{ GeV}/c^2$ charge $0$ spin $1$ <b>Z</b> Z boson	
LEPTONS	mass $< 1.0 \text{ eV}/c^2$ charge $0$ spin $1/2$ <b><math>\nu_e</math></b> electron neutrino	mass $< 0.17 \text{ MeV}/c^2$ charge $0$ spin $1/2$ <b><math>\nu_\mu</math></b> muon neutrino	mass $< 18.2 \text{ MeV}/c^2$ charge $0$ spin $1/2$ <b><math>\nu_\tau</math></b> tau neutrino	mass $\approx 80.360 \text{ GeV}/c^2$ charge $\pm 1$ spin $1$ <b>W</b> W boson	GAUGE BOSONS VECTOR BOSONS



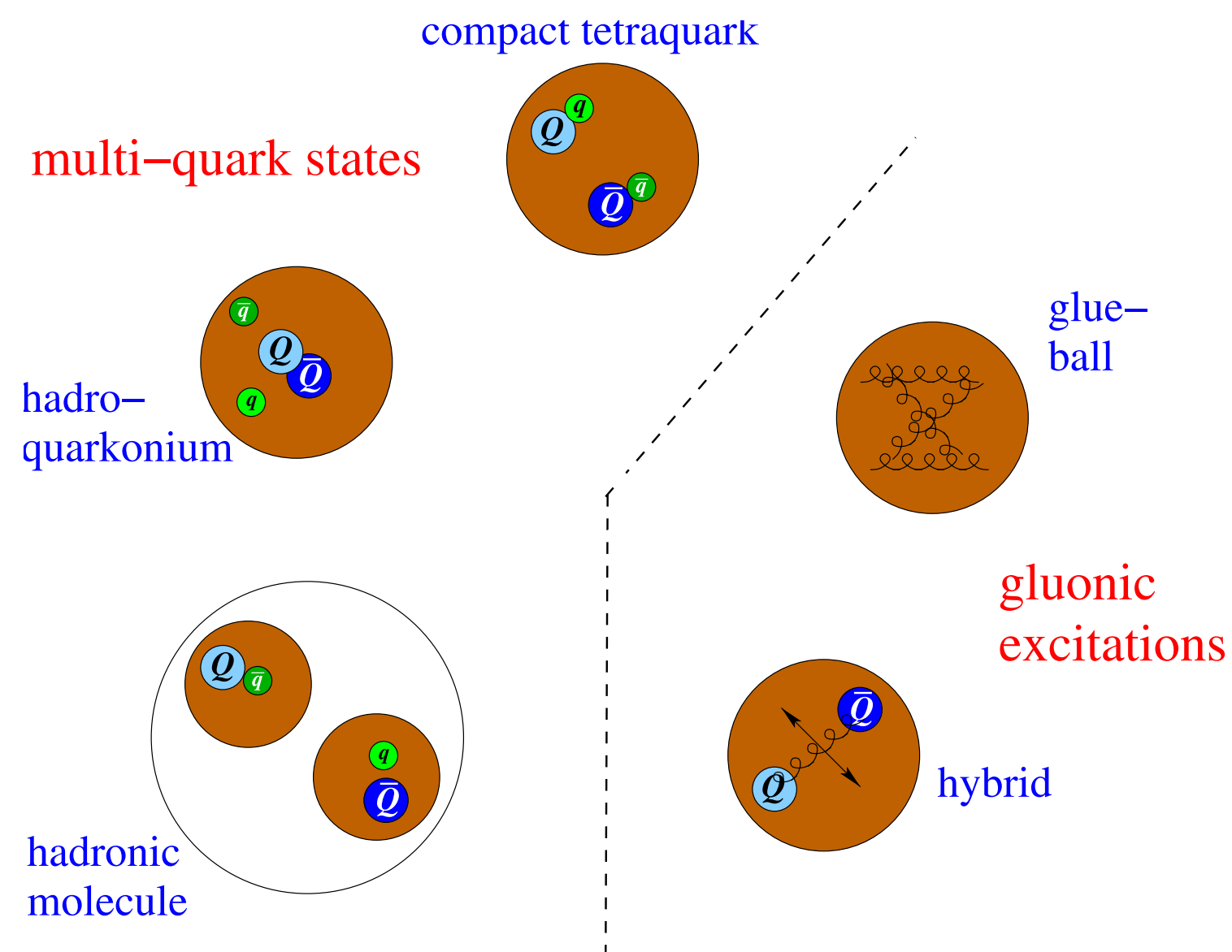
**Hadron spectroscopy can provide us clues for the understanding of fundamental structure via the hadron property study**

# Forms of hadrons

## Quark model



## New forms of hadrons



Physics report 873 (2020) 1-154

### ◆ Quark model (QM)

- ◆ Identify hadrons as compound objects consisting of quarks and antiquarks
- ◆ Dynamics description inside hadrons

### ◆ New form of hadrons:

- ◆ **Multi-quark:** quark number  $\geq 4$
- ◆ **Hybrid state:** the mixture of quark and gluon
- ◆ **Glueball:** composed of gluons

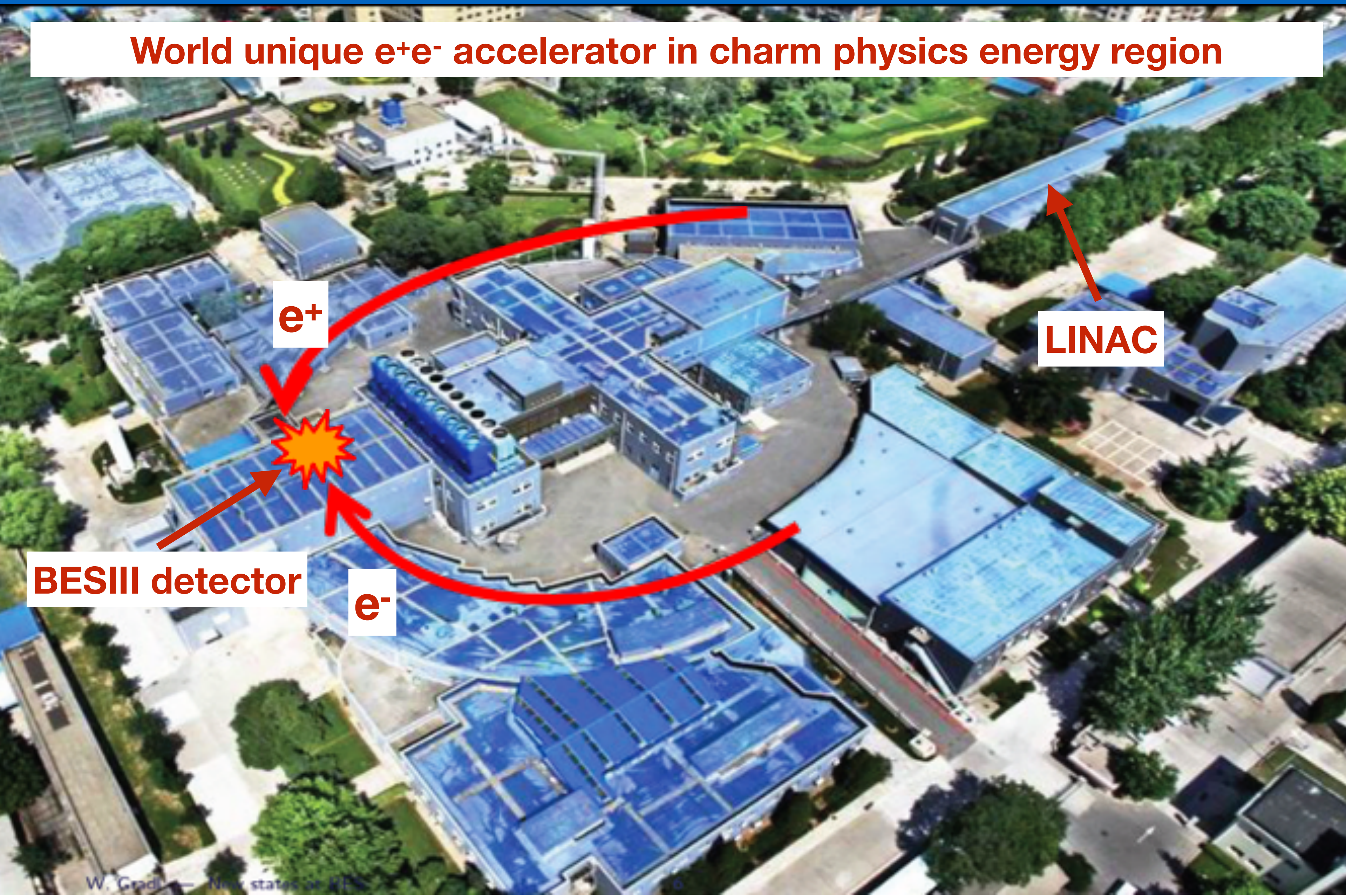
### ◆ Identification from QM: challenging

- ◆ **Exotic quantum states**
- ◆ **Crypto exotic with particular properties**

Many candidates, but no unambiguous hadrons with nonstandard structure have established

# Beijing Electron Positron Collider (BEPCII)

World unique  $e^+e^-$  accelerator in charm physics energy region



**2004: Construction**

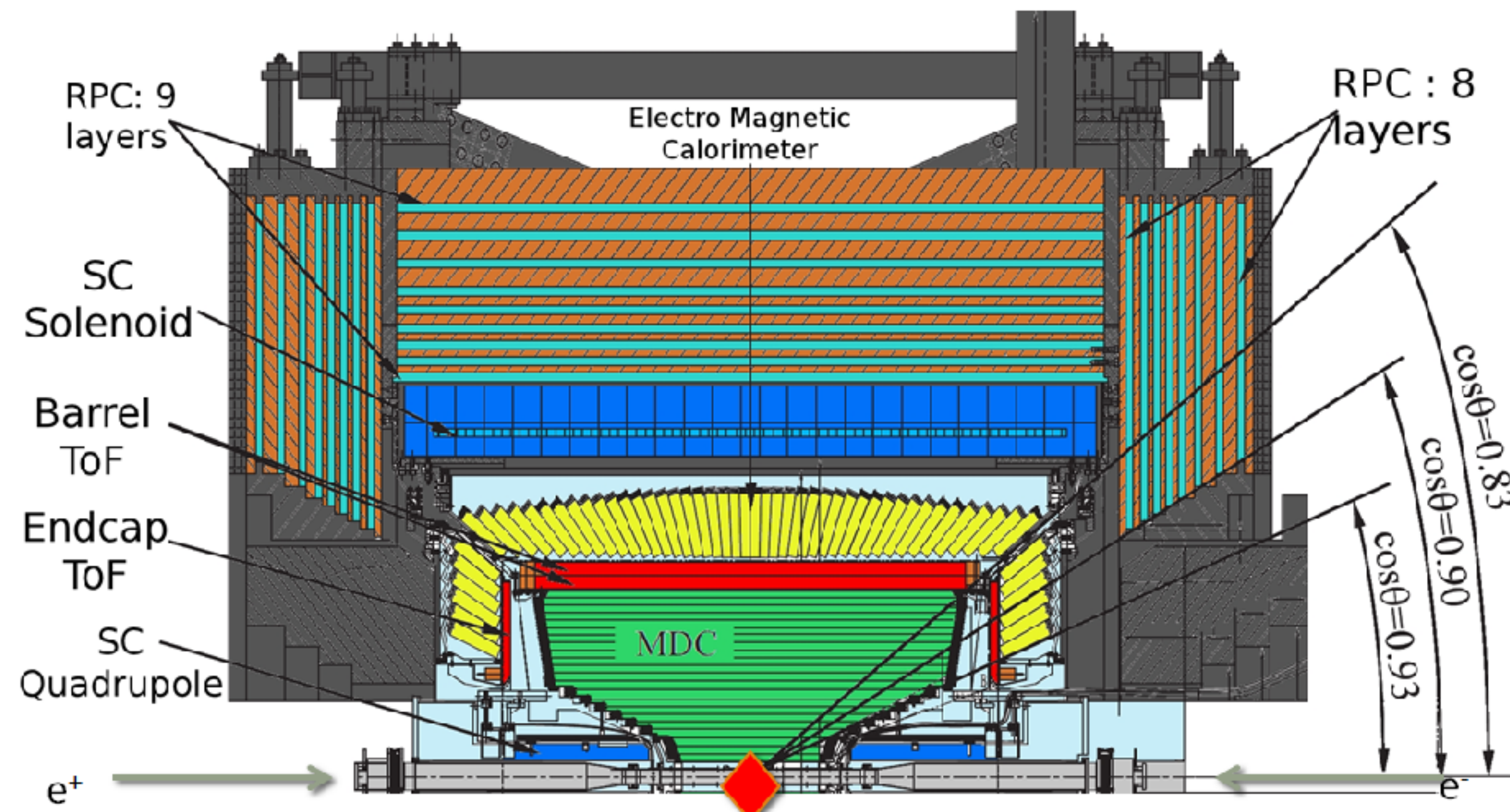
- Double rings
- Beam energy:  
1.0 - 2.3 (2.45) GeV
- Designed luminosity:  
 $1 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$

**2008: test run**

**2009-now: BESIII physics runs**

# BESIII detector

Designed for neutral and charged particle with excellent resolution, PID, and large coverage



Total weight 730 ton,  
~40,000 readout channel  
Data rate: 5kHz, 50Mb/s

- ◆ Magnet: 1T Superconducting
- ◆ MDC: small cell & He gas
  - $\sigma_{xy} = 130 \mu\text{m}$
  - $\sigma_p/p = 0.5\% @ 1\text{GeV}$
  - $dE/dx = 6\%$
- ◆ TOF: plastic scintillator/MRPC
  - $\sigma_T = 80 \text{ ps}$  Barrel
  - $\sigma_T = 110 (60) \text{ ps}$  Endcap
- ◆ EMC: CsI crystals
  - $\Delta E/E = 2.5\% @ 1\text{GeV}$  - Barrel
  - $\Delta E/E = 5\% @ 1\text{GeV}$  - Endcap
- ◆ Muon ID: 9 layer RPC

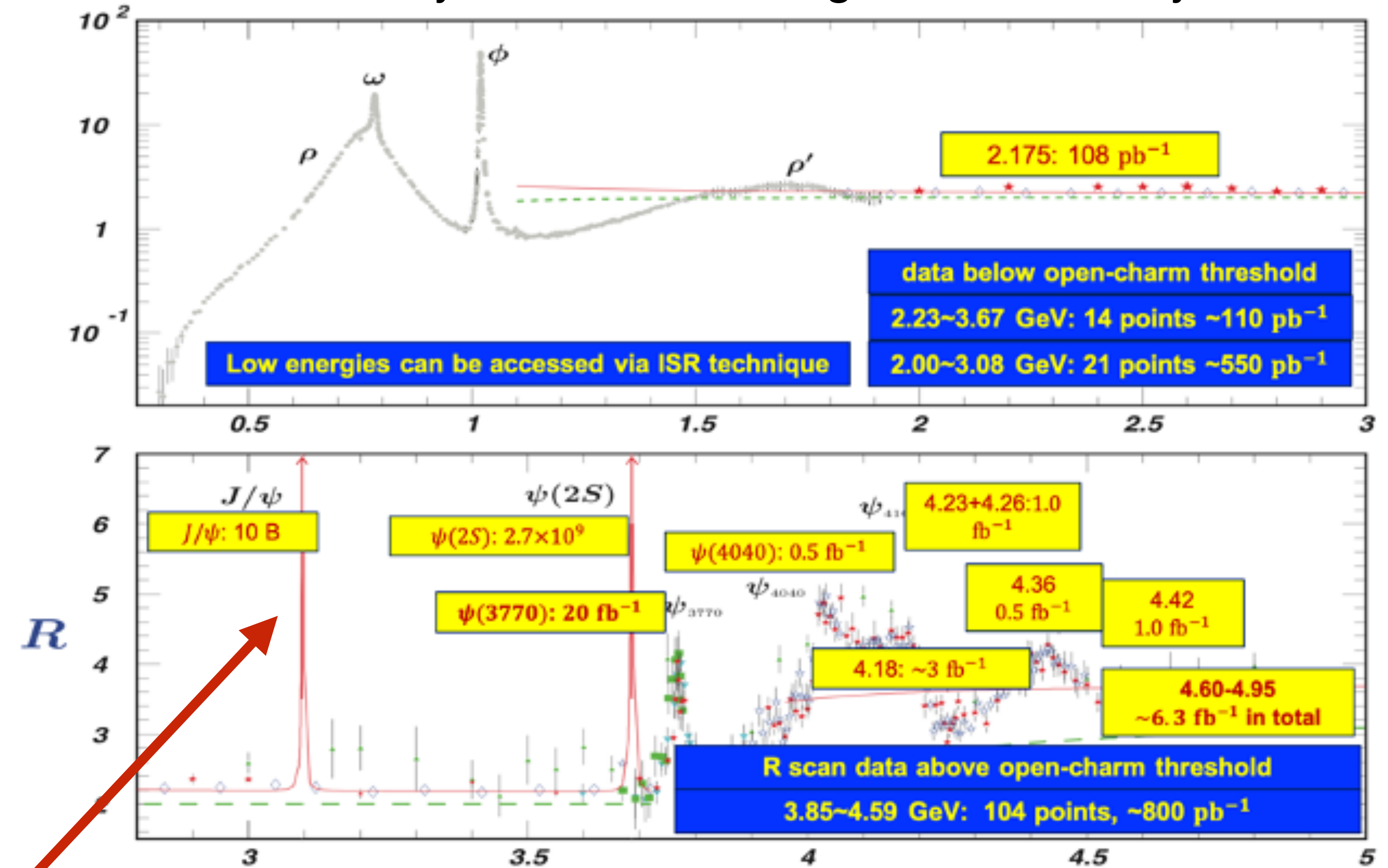
**Has been in full operation since 2008, all sub-detectors are in a very good status!**

# BESIII Data samples

Totally about 50fb<sup>-1</sup> integrated luminosity

Data sets collected so far include

- ◆ 10×10<sup>9</sup> J/ψ events
- ◆ 2.7×10<sup>9</sup> ψ(2S) events
- ◆ 20 fb<sup>-1</sup> ψ(3770)
- ◆ Scan data between 1.8 and 3.08 GeV, and above 3.74GeV
- ◆ Large datasets for XYZ studies:  
Scan with >500pb<sup>-1</sup> per energy point space 10-20MeV apart

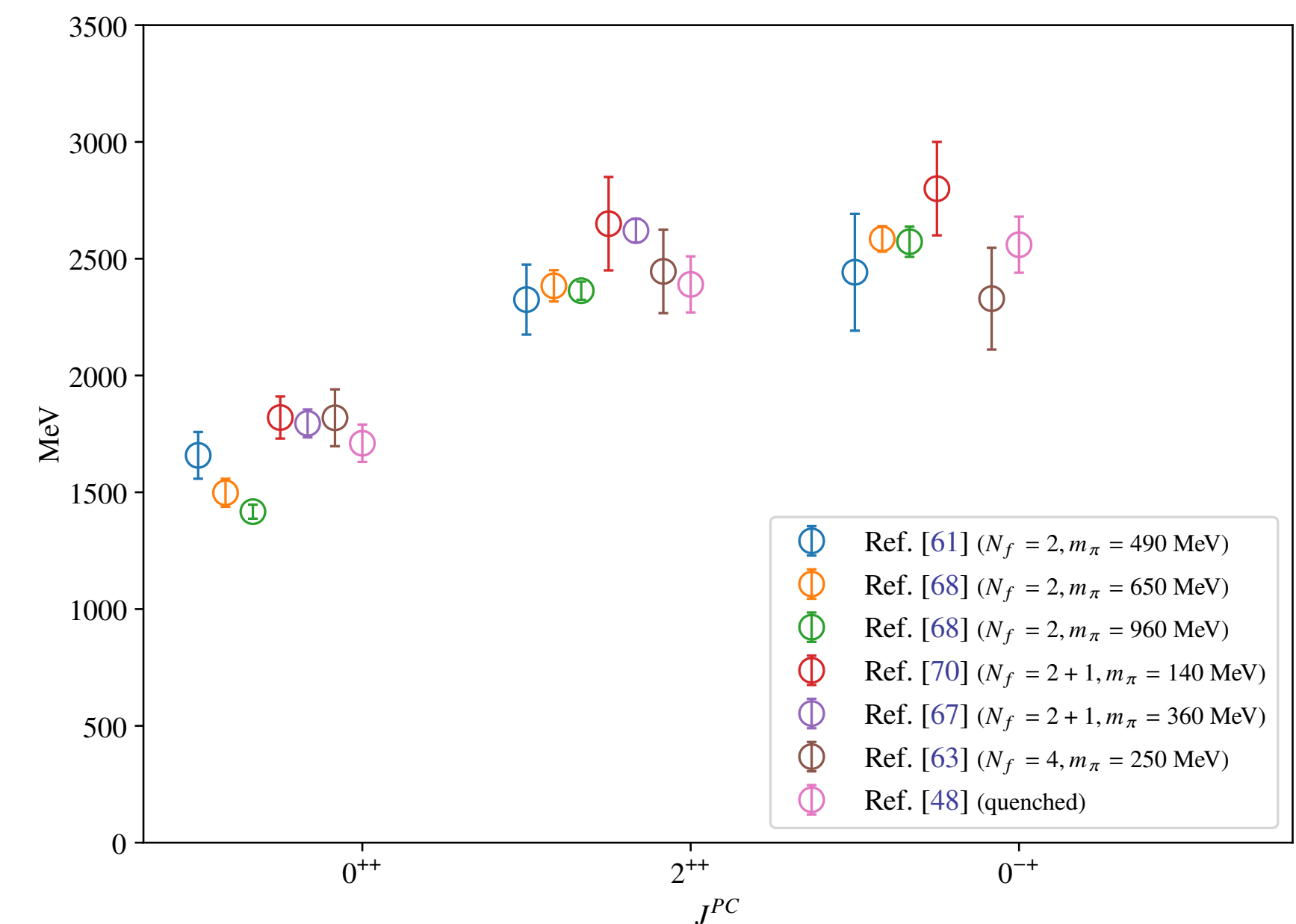


**World largest J/ψ data sample : ~10 billion**

# Glueballs

- ◆ The basic theory for strong interactions is quantum chromodynamics (QCD)
  - ◆ **Glueon self-interaction:** prediction of non-Abelian Gauge SU(3) QCD theory
  - ◆ **Glueballs are unique particles formed with force carriers via self-interactions**
  - ◆ **Glueballs to QCD is just as important as Higgs Boson to EW**

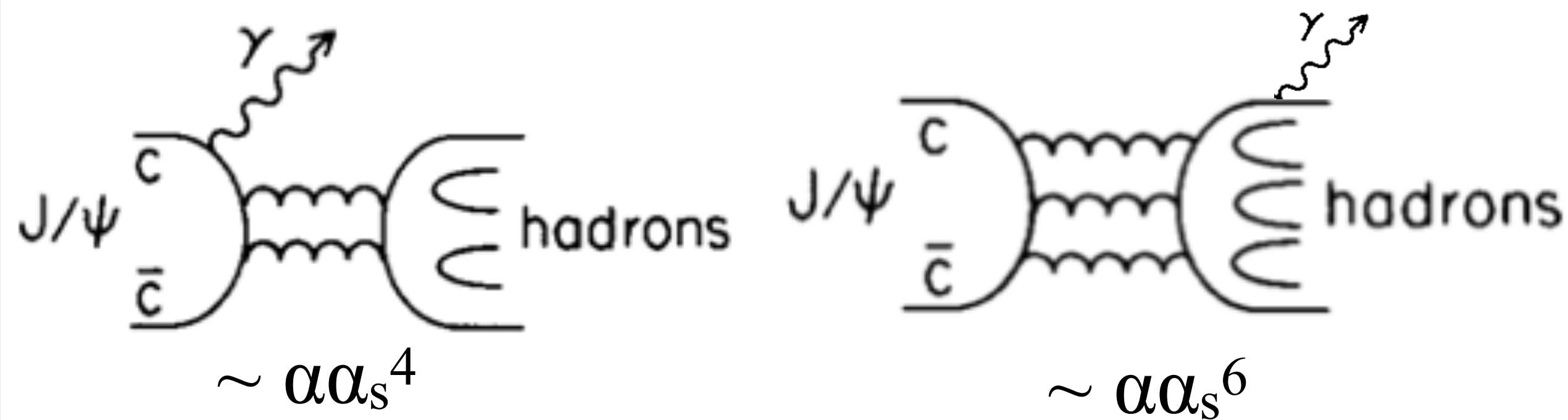
- ◆ **Lattice QCD** (LQCD) is a non-perturbative method from the first principles in theory.
- ◆ **Different lattice QCD groups** (including lattice simulations with dynamical quarks)
  - ◆ Predictions on **masses and production rates** of pure glueballs
  - ◆ Consistent results and expected to be reliable.
- ◆ Lattice QCD predictions on glueball masses:
  - ◆  **$0^{++}$  ground state:** 1.5 - 1.7 GeV/c<sup>2</sup>
  - ◆  **$2^{++}$  ground state:** 2.3 - 2.4 GeV/c<sup>2</sup>
  - ◆  **$0^{-+}$  ground state:** 2.3 - 2.6 GeV/c<sup>2</sup>



[arxiv:2305.04869](https://arxiv.org/abs/2305.04869)

# Glueball production in $J/\psi$ Radiative decay

## ◆ Gluon rich environment



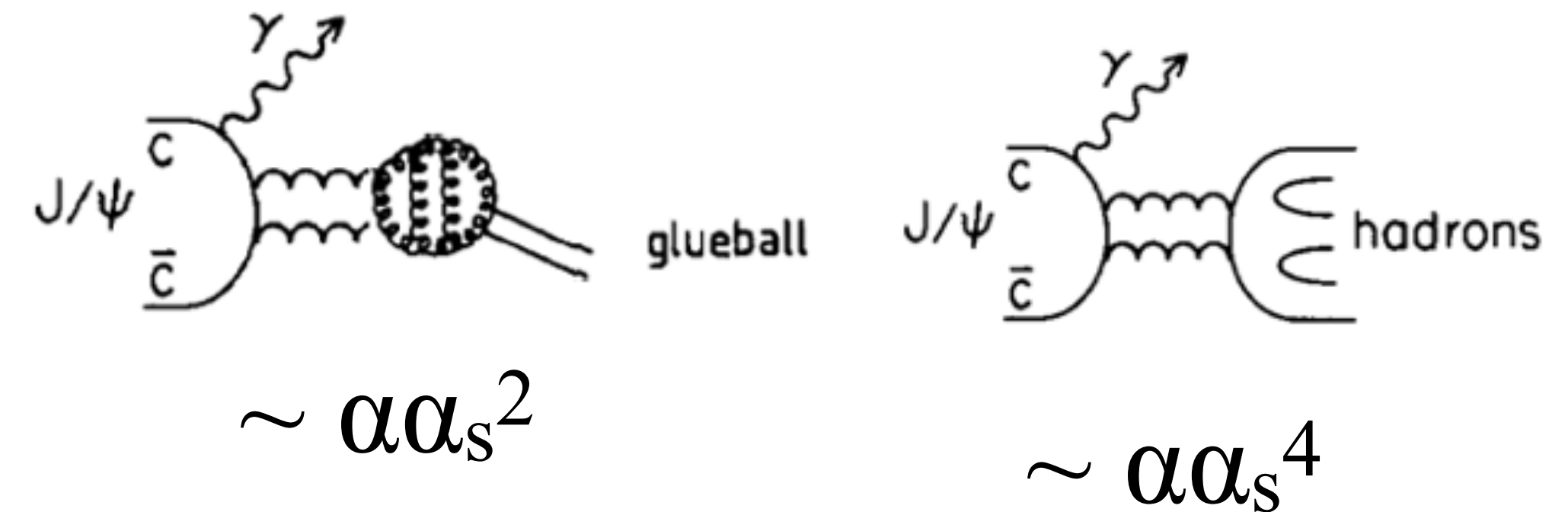
◆ **Isospin filter:** final states dominated by  $I=0$  processes

◆ **Spin-parity filter:** **C** parity must be +, so  $J^{PC}=0^{-+}, 0^{++}, 1^{++}, 2^{++}, 2^{-+} \dots$

◆ **Clean environment** in  $e^+e^-$  collision: very different from **p-p collision**

## ◆ Rich glueball production in $J/\psi$ radiative decays:

◆ **Glueball production rate** in  $J/\psi$  radiative decays could be **higher** than normal hadrons

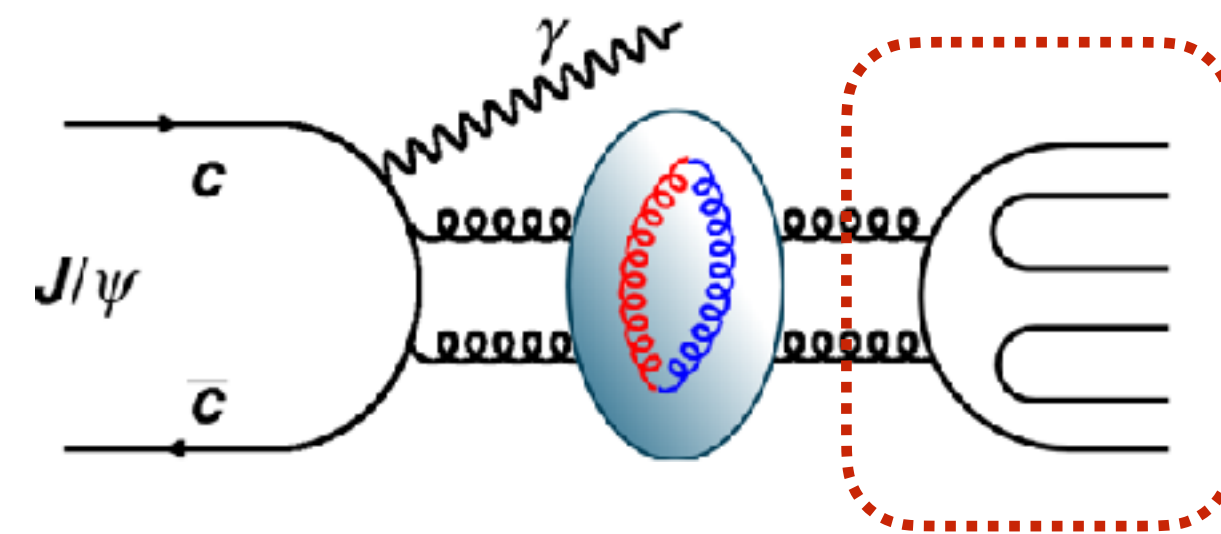
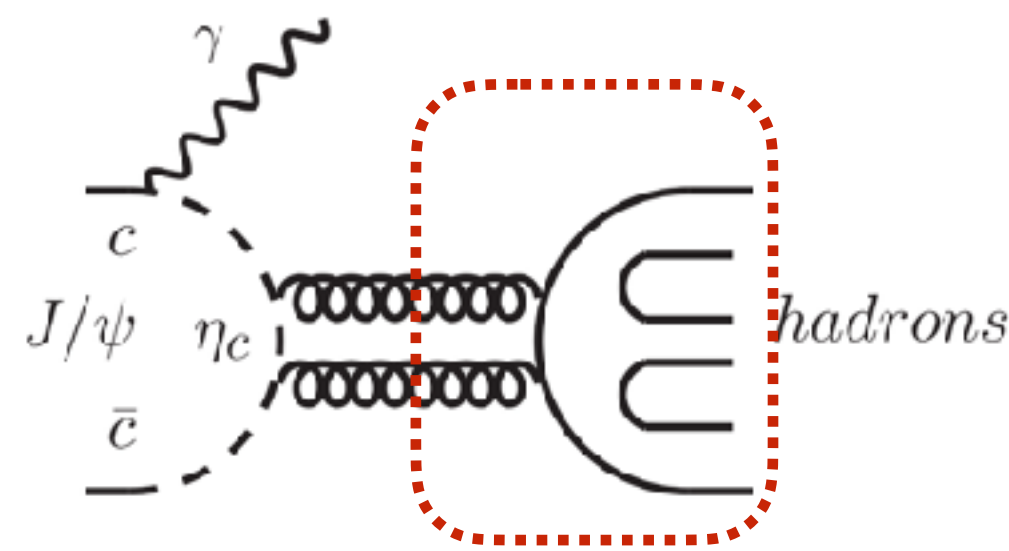


➡  **$J/\psi$  Radiative decay is an ideal place to search for glueballs**



# Glueball Decays

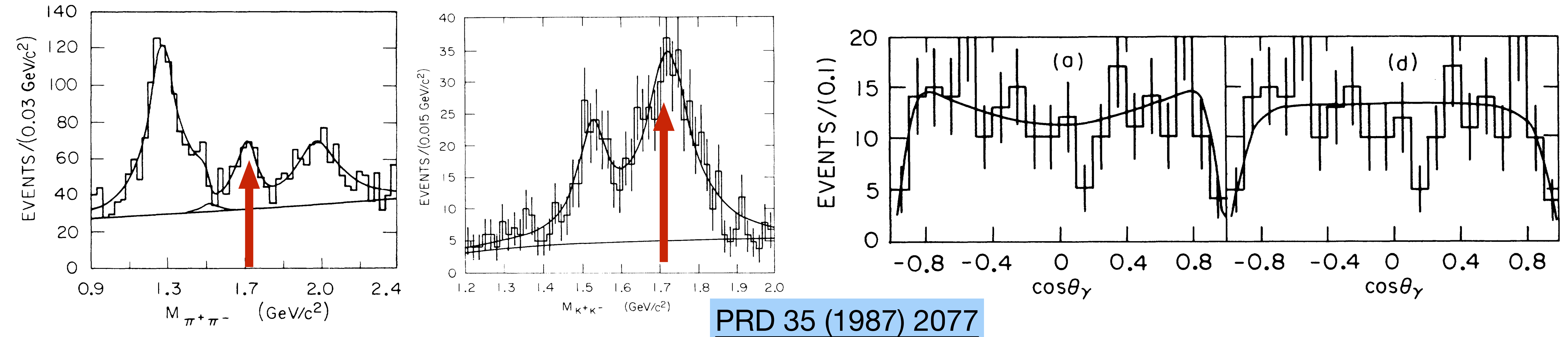
- ◆ **Flavor symmetric decays**
- ◆ **No rigorous predictions on decay patterns and their branching ratios**
- ◆ The glueball decays could be the analogy to **Charmonium decays** since they all decay via gluons (OZI suppression) [PLB 380 189(1996), Commu. Theor. Phys. 23.373 (1995)]
  - ◆ e.g. the  $0^{-+}$  glueball could have similar decays of  $\eta_c$



# Historical Glueball Candidates

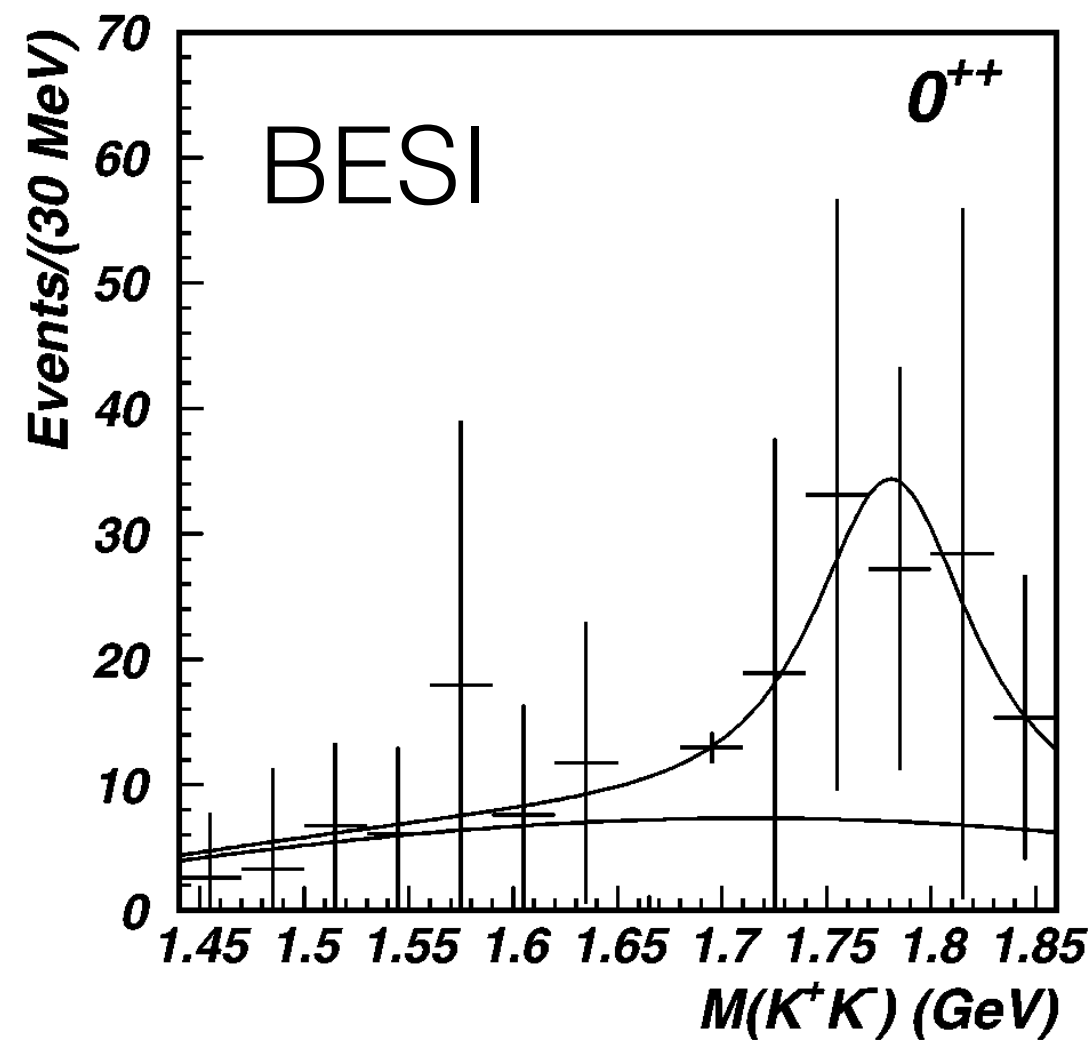
- ◆ **Many experiments searched for glueballs over the past 4 decades**
- ◆ **Many historical glueball candidates**, but with some **difficulties/controversies**.
  - ◆ **Scalar Glueball candidate ( $0^{++}$ ):**  $f_0(1500)$ ,  $f_0(1710)$
  - ◆ **Tensor Glueball candidate ( $2^{++}$ ):**  $f_2(2340)$
  - ◆ **Pseudoscalar Glueball candidate ( $0^{-+}$ ):**  $\eta(1405)$

# Historical Glueball Candidates — Scalar $f_0(1710)$

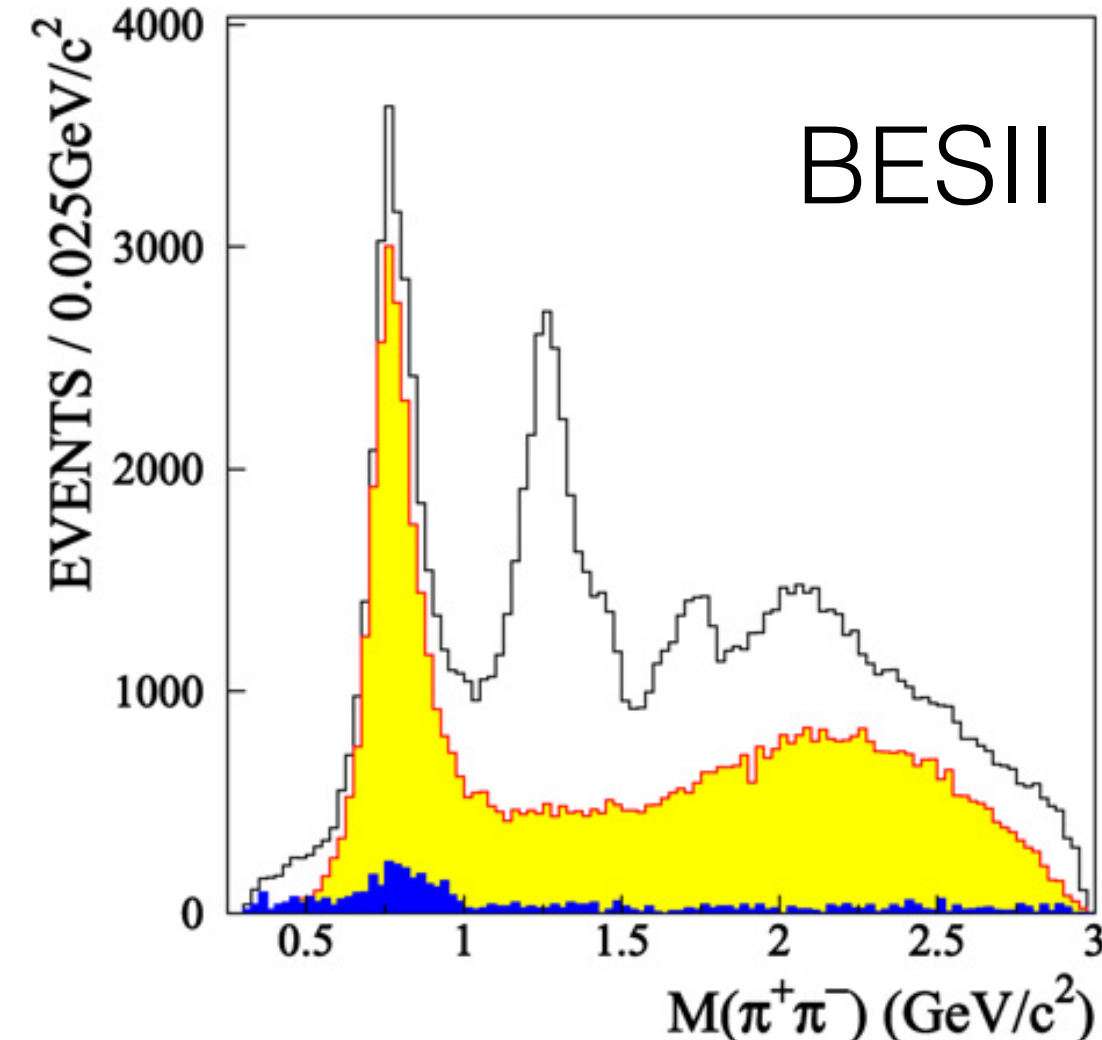


- ◆ The  $f_0(1710)$  was discovered in  $J/\psi \rightarrow \gamma\pi^+\pi^-$  and  $J/\psi \rightarrow \gamma K^+K^-$  by MarkIII in 1987 as  $\theta_2(1720)$
- ◆  $J^{PC} = 2^{++}$  from a simple fit to the angular distribution
- ◆ The significance of  $2^{++}$  state is  $\sim 3\sigma$  better than  $0^{++}$  assumption

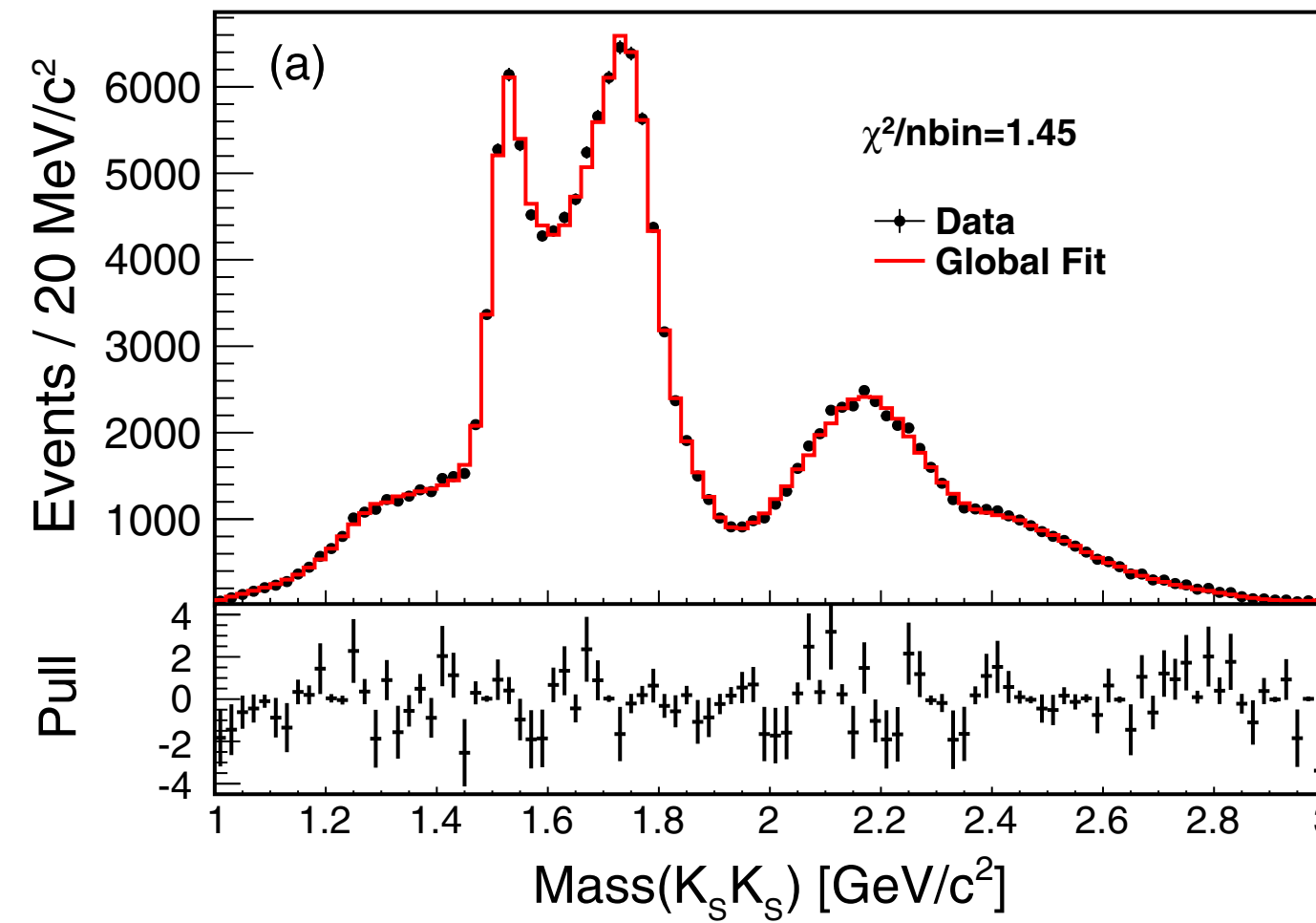
# Historical Glueball Candidates — Scalar $f_0(1710)$



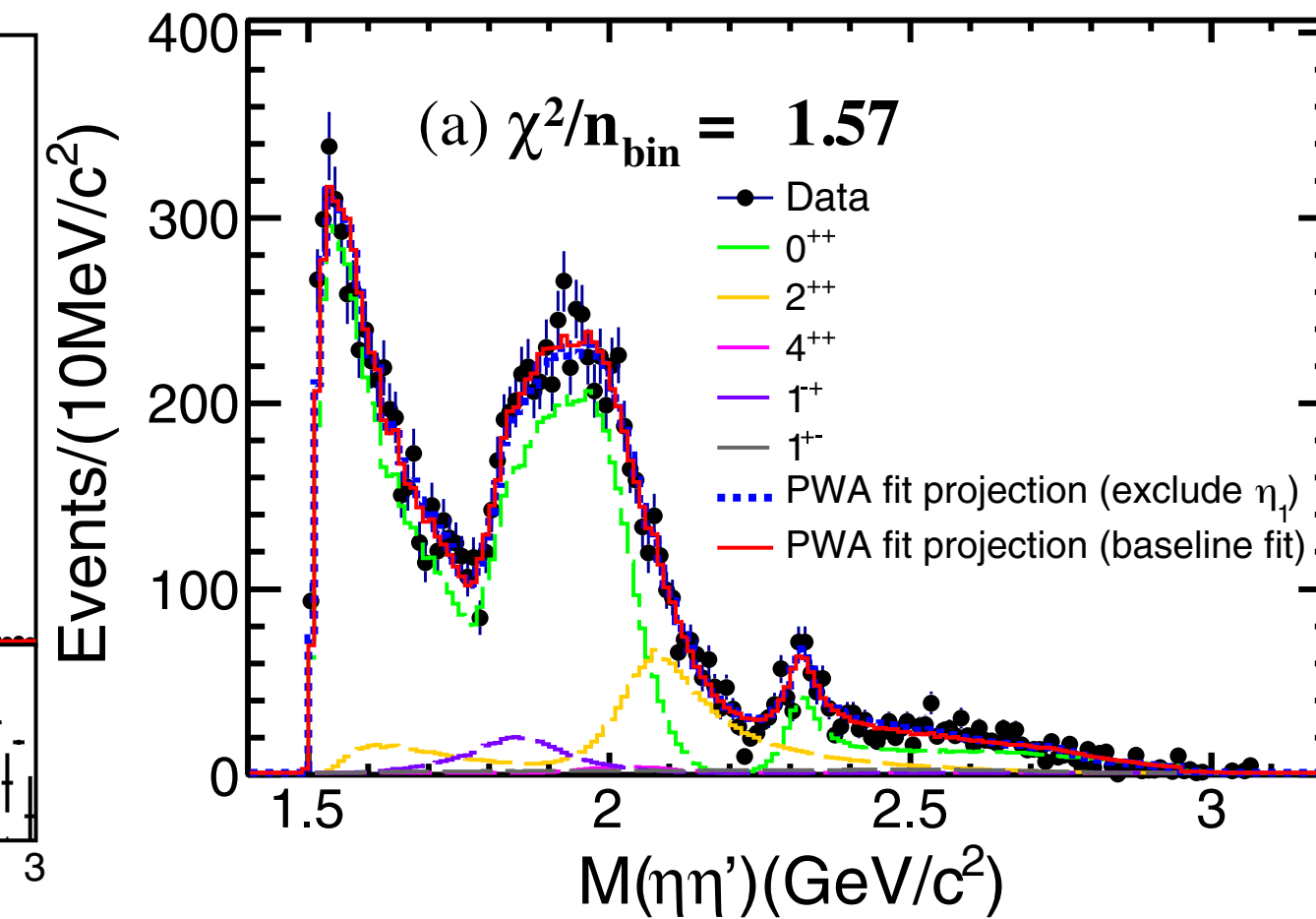
PRL 77(1996) 19



PLB 642 (2006) 441



PRD 98 (2018) 072003



PRD 106 (2022) 072012

◆ The  $f_0(1710)$  was firstly changed to be  $0^{++}$  from a full PWA of  $J/\psi \rightarrow \gamma KK$  @ BES I. Lots of studies at Mark II, DM2, BES I, BES II, BES III

◆ The  $f_0(1710)$  favors to be a scalar glueball or large glueball content: controversy of dynamic mixing mechanism

◆ High production rate of  $J/\psi \rightarrow \gamma f_0(1710)$

$$B[J/\psi \rightarrow \gamma f_0(1710) \rightarrow \gamma \pi \pi] = (4.0 \pm 1.0) \times 10^{-4}$$

BES II: PLB 642 (2006) 441

$$B[J/\psi \rightarrow \gamma f_0(1710) \rightarrow \gamma K_s^0 K_s^0] = (2.00^{+0.03}_{-0.02} \quad ^{+0.31}_{-0.10}) \times 10^{-4}$$

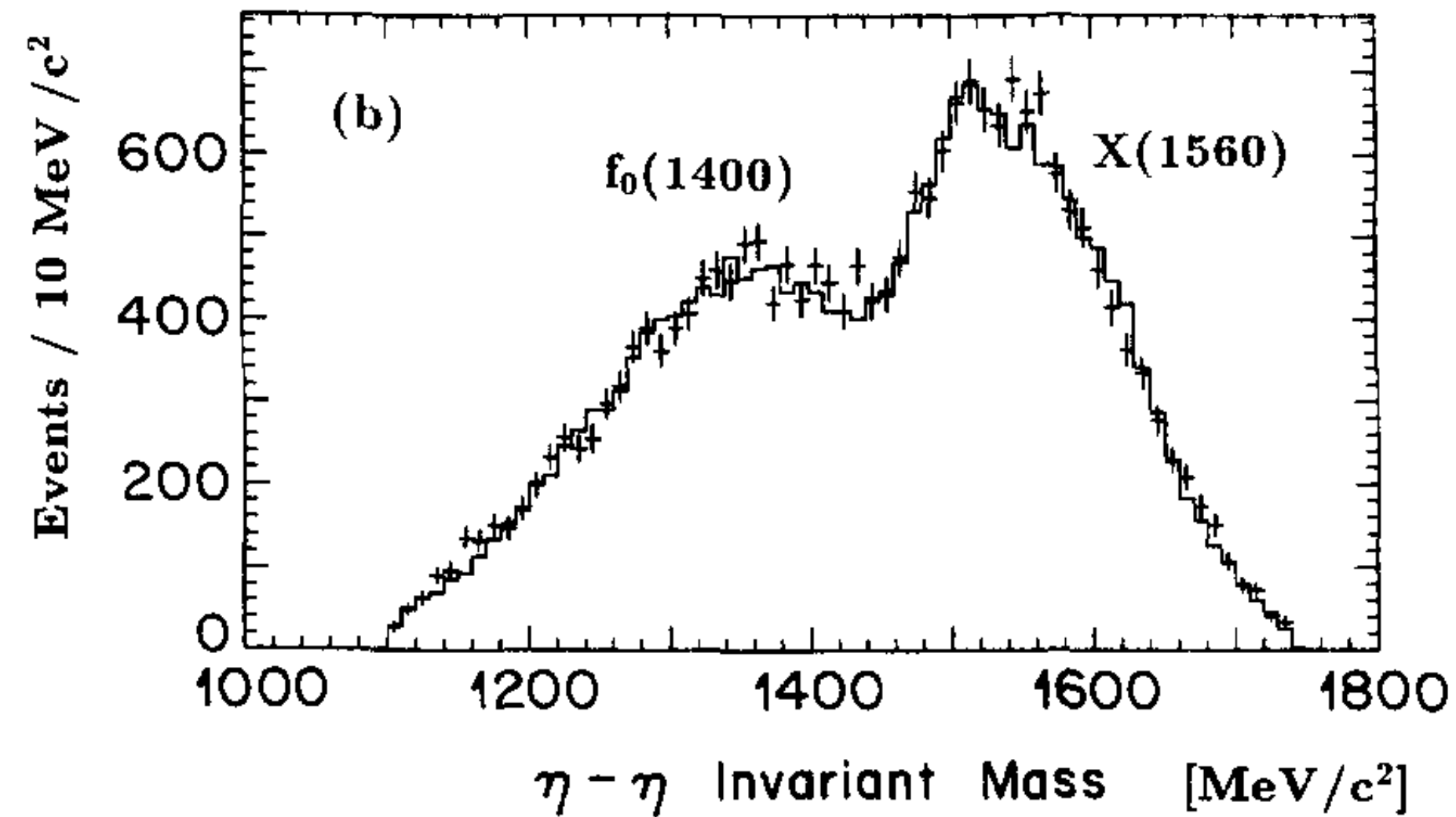
BES III: PRD 98 (2018) 072003

◆ Decay suppression in  $f_0(1710) \rightarrow \eta\eta'$

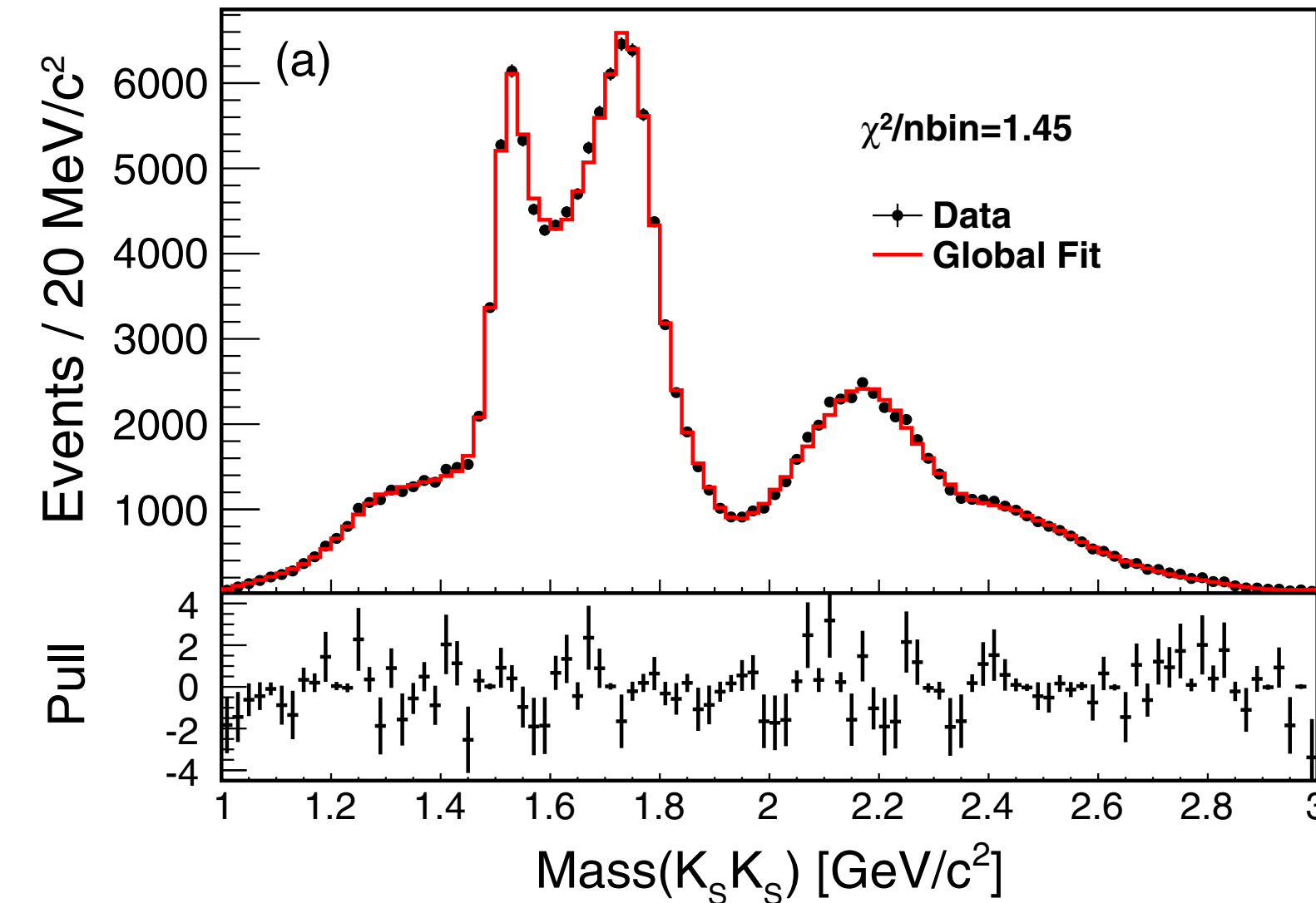
$$B[f_0(1710) \rightarrow \eta\eta'/f_0(1710) \rightarrow \pi\pi] < (2.9 \pm^{+1.1}_{-0.9}) \times 10^{-3}$$

BES III: PRD 106 072012(2022)

# Historical Glueball Candidates — Scalar $f_0(1500)$



PLB 291 (1992) 347



PRD 98 (2018) 072003

- ◆ The  $f_0(1500)$  was discovered by Crystal Barrel in 1992
- ◆ An unique  $0^{++}$  candidate since  $f_0(1710)$  was  $f_2$  at that time
- ◆ **Disfavors to its interpretation of a scalar glueball**

- ◆ **Lower production rate of  $J/\psi \rightarrow \gamma f_0(1500)$**

$$B[J/\psi \rightarrow \gamma f_0(1500) \rightarrow \gamma K_s^0 K_s^0] = (1.59^{+0.16}_{-0.16} \quad +0.18 \quad -0.56) \times 10^{-5}$$

$$B[J/\psi \rightarrow \gamma f_0(1710) \rightarrow \gamma K_s^0 K_s^0] = (2.00^{+0.03}_{-0.02} \quad +0.31 \quad -0.10) \times 10^{-4}$$

BESIII: PRD 98 (2018) 072003

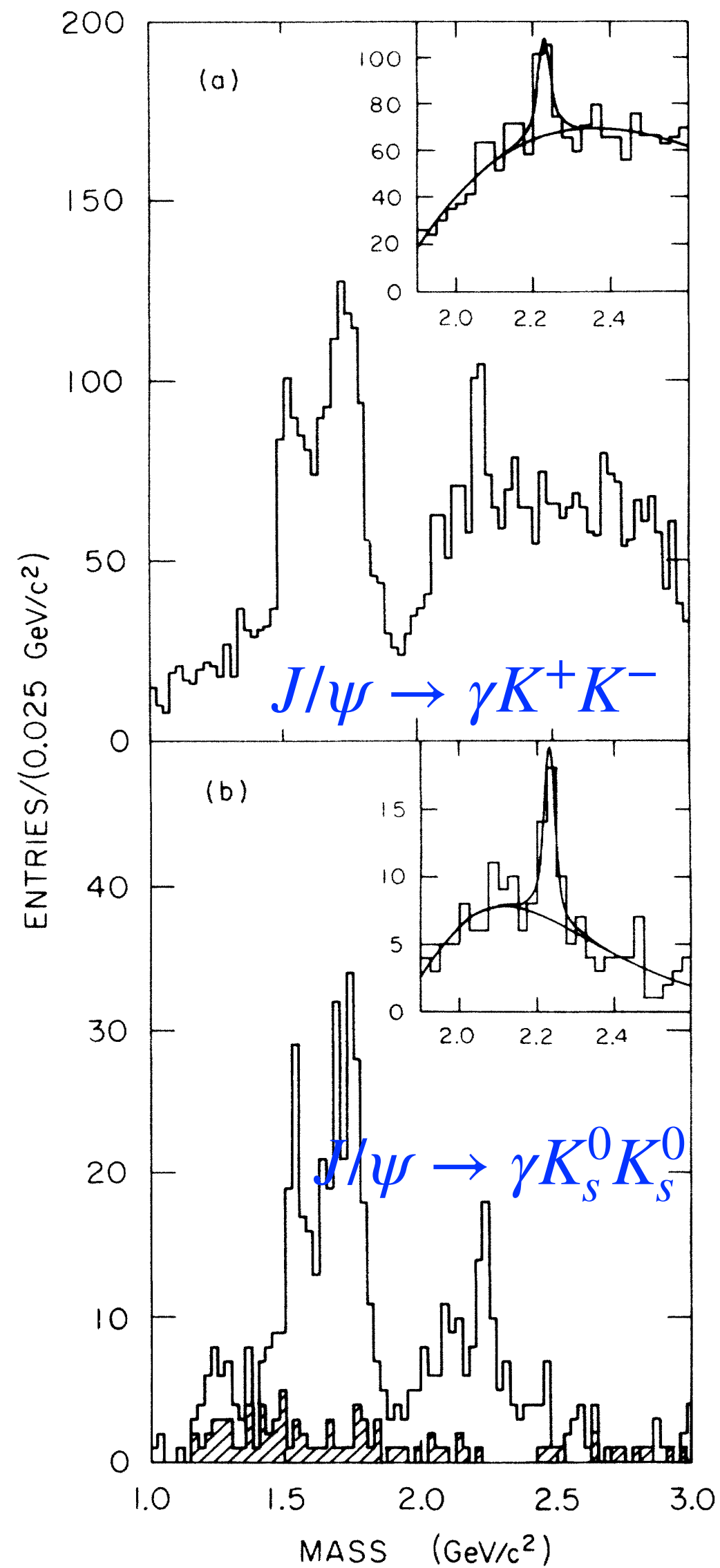
- ◆ **No strong suppression in  $f_0(1500) \rightarrow \eta\eta'$**

$$B[f_0(1500) \rightarrow \eta\eta'/f_0(1500) \rightarrow \pi\pi] = (1.66 \pm_{-0.40}^{+0.42}) \times 10^{-1}$$

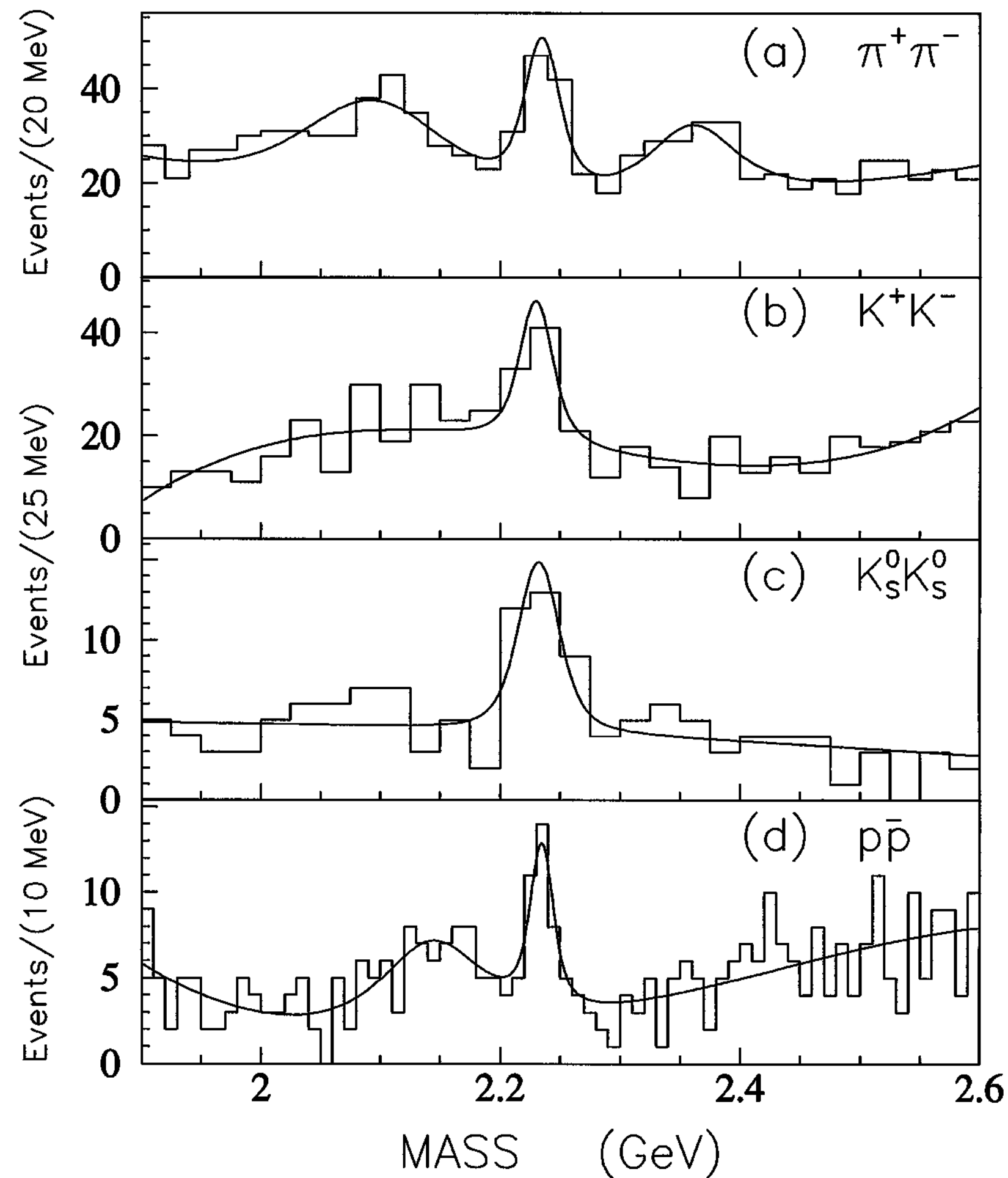
$$B[f_0(1710) \rightarrow \eta\eta'/f_0(1710) \rightarrow \pi\pi] < (2.9 \pm_{-0.9}^{+1.1}) \times 10^{-3}$$

BESIII: PRD 106 072012(2022)

# Historical Glueball Candidates — Tensor $\xi(2230)$



PRL 56 (1986) 107



PRL 76 (1996) 3502

- ◆ First observed by MarkIII is  $J/\psi \rightarrow \gamma KK$  in 1980's, then by BES I in 1990's in  $J/\psi \rightarrow \gamma KK, \gamma \pi \pi, \gamma p \bar{p}$  with very narrow mass peak.
- ◆ It was a tensor glueball candidate due to good flavor symmetric decay property.
- ◆ Difficulty: it was not confirmed by BES II, nor BES III with much higher statistics.

# Historical Glueball Candidates — Tensor $f_2(2340)$

$$\Gamma(J/\psi \rightarrow \gamma G_{2+}) = 1.01(22) \text{ keV}$$

$$\Gamma(J/\psi \rightarrow \gamma G_{2+})/\Gamma_{tot} = 1.1 \times 10^{-2}$$

CLQCD, *Phys. Rev. Lett.* 111, 091601 (2013)

◆ **Large production rate of  $f_2(2340)$  in  $J/\psi \rightarrow \gamma(KK/\eta\eta/\eta'\eta'/\phi\phi)$ :**  
substantially lower than the LQCD prediction for tensor glueball

$$\blacklozenge B(J/\psi \rightarrow \gamma f_2(2340) \rightarrow \gamma \eta\eta) = (3.8^{+0.62}_{-0.66} \text{ } ^{+2.37}_{-2.07}) \times 10^{-5} \text{ (PRD 87,2013,092009)}$$

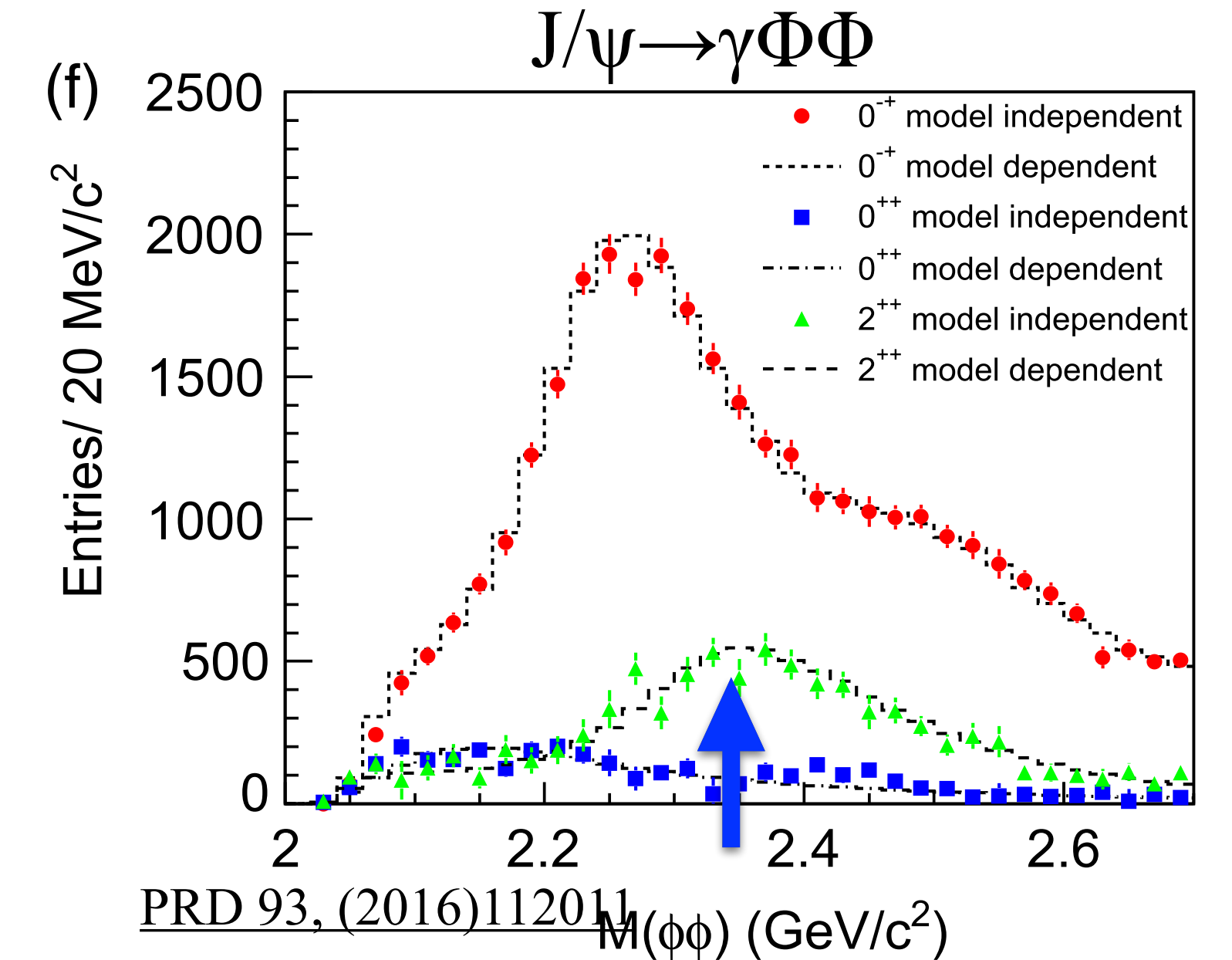
$$\blacklozenge B(J/\psi \rightarrow \gamma f_2(2340) \rightarrow \gamma \phi\phi) = (1.91 \pm 0.14^{+0.72}_{-0.73}) \times 10^{-4} \text{ (PRD 93,2016,112011)}$$

$$\blacklozenge B(J/\psi \rightarrow \gamma f_2(2340) \rightarrow \gamma K_s K_s) = (5.54^{+0.34}_{-0.40} \text{ } ^{+3.82}_{-1.49}) \times 10^{-5} \text{ (PRD 98,2018,072003)}$$

$$\blacklozenge B(J/\psi \rightarrow \gamma f_2(2340) \rightarrow \gamma \eta'\eta') = (8.67 \pm 0.70^{+0.16}_{-1.67}) \times 10^{-6} \text{ (PRD 105,2022,072002)}$$

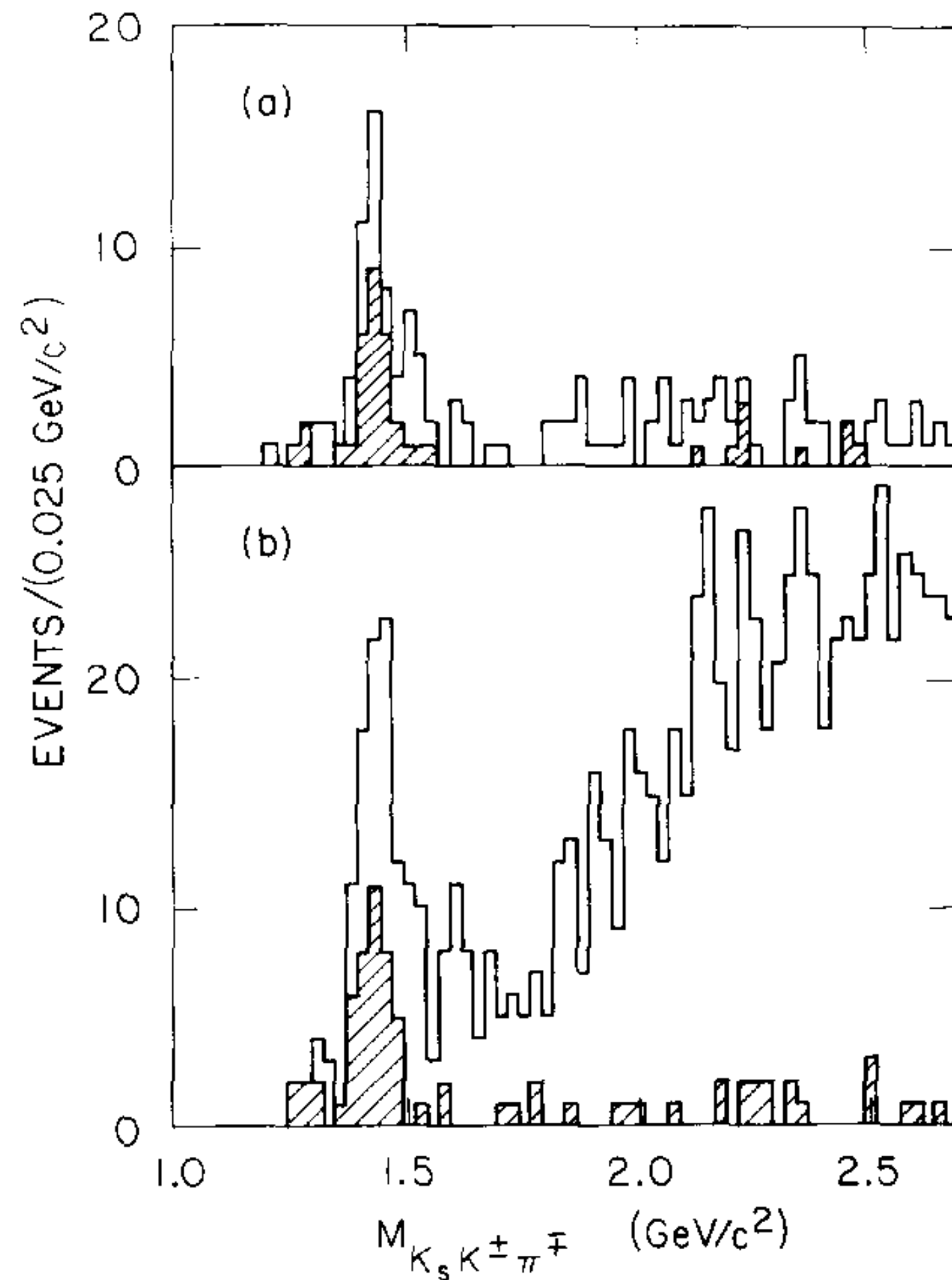
◆ **Difficulty: Many wide tensor mesons and large overlaps in the mass region of 2.3 GeV** ( $2^{++}$  glueball mass from the LQCD predictions)

◆ Studies are strongly model dependent.



Resonance	M (MeV/c <sup>2</sup> )	Γ (MeV/c <sup>2</sup> )	B.F. (×10 <sup>-4</sup> )	Sig.
$\eta(2225)$	2216 <sup>+4+21</sup> <sub>-5-11</sub>	185 <sup>+12+43</sup> <sub>-14-17</sub>	(2.40 ± 0.10 <sup>+2.47</sup> <sub>-0.18</sub> )	28σ
$\eta(2100)$	2050 <sup>+30+75</sup> <sub>-24-26</sub>	250 <sup>+36+181</sup> <sub>-30-164</sub>	(3.30 ± 0.09 <sup>+0.18</sup> <sub>-3.04</sub> )	22σ
$X(2500)$	2470 <sup>+15+101</sup> <sub>-19-23</sub>	230 <sup>+64+56</sup> <sub>-35-33</sub>	(0.17 ± 0.02 <sup>+0.02</sup> <sub>-0.08</sub> )	8.8σ
$f_0(2100)$	2101	224	(0.43 ± 0.04 <sup>+0.24</sup> <sub>-0.03</sub> )	24σ
$f_2(2010)$	2011	202	(0.35 ± 0.05 <sup>+0.28</sup> <sub>-0.15</sub> )	9.5σ
$f_2(2300)$	2297	149	(0.44 ± 0.07 <sup>+0.09</sup> <sub>-0.15</sub> )	6.4σ
$f_2(2340)$	2339	319	(1.91 ± 0.14 <sup>+0.72</sup> <sub>-0.73</sub> )	11σ
$\phi(1039)^{--}$ PHSP			(2.74 ± 0.15 <sup>+0.16</sup> <sub>-1.48</sub> )	6.8σ

# Historical Glueball Candidates — Pseudoscalar $\eta(1405)$

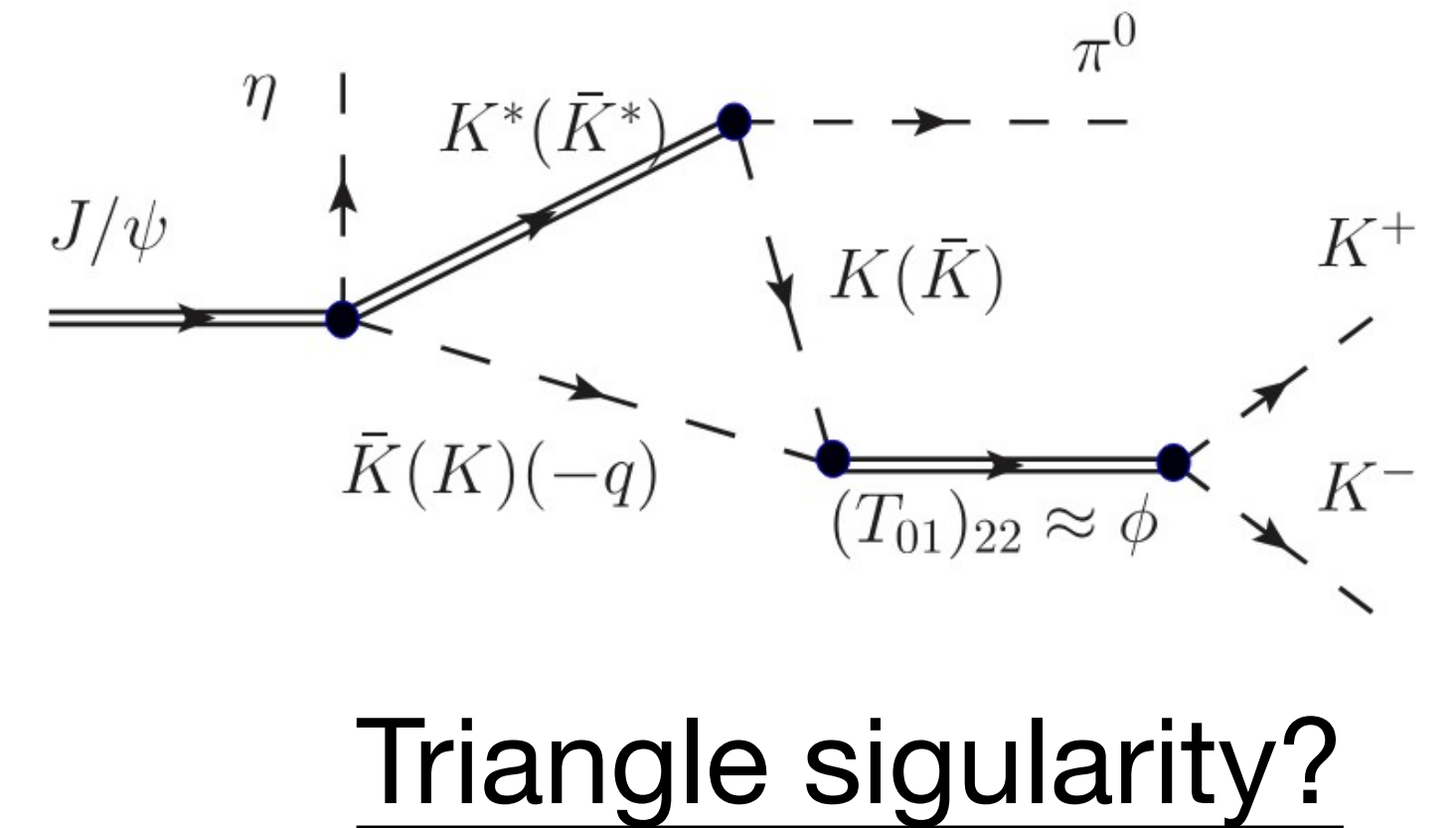
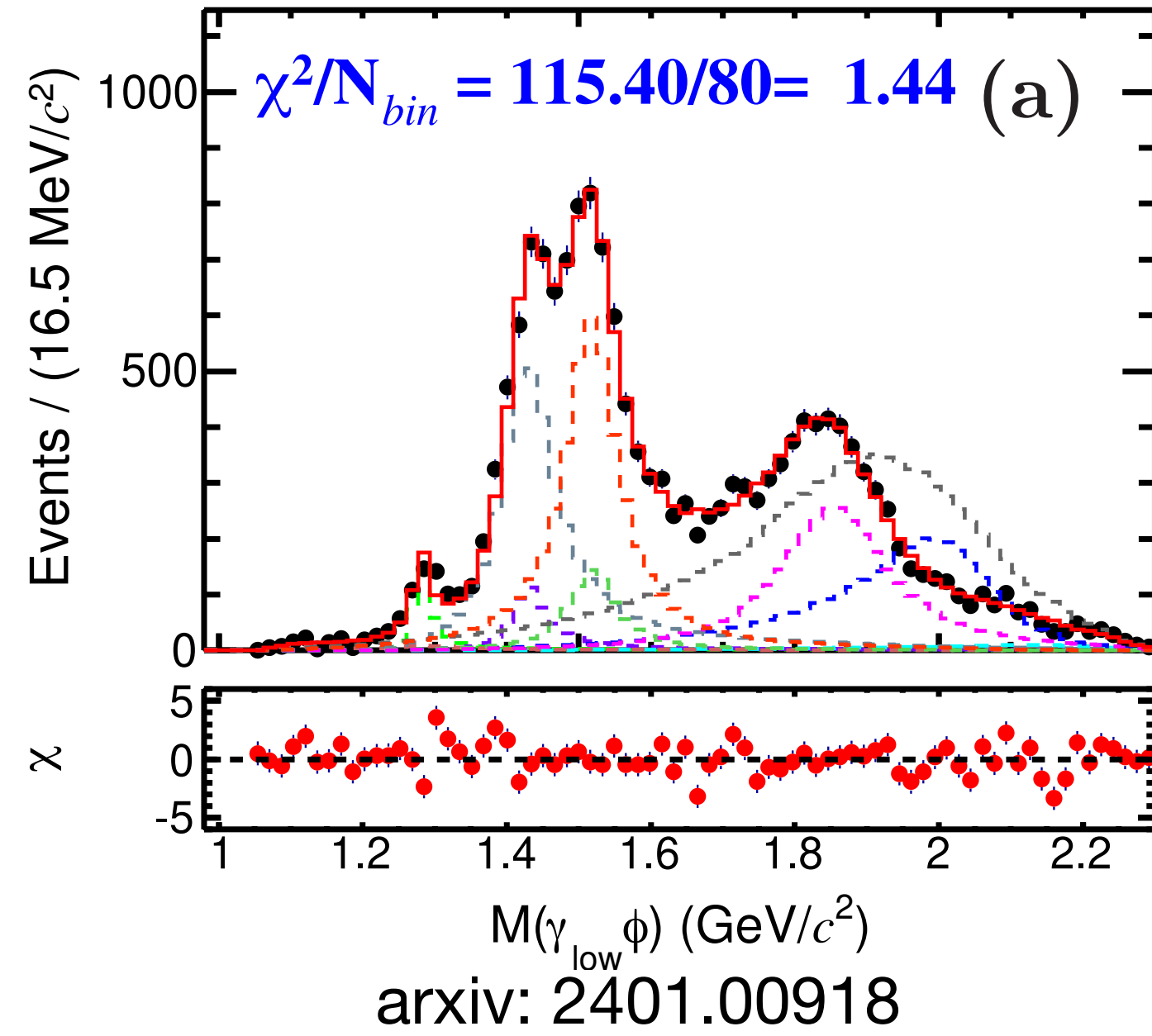
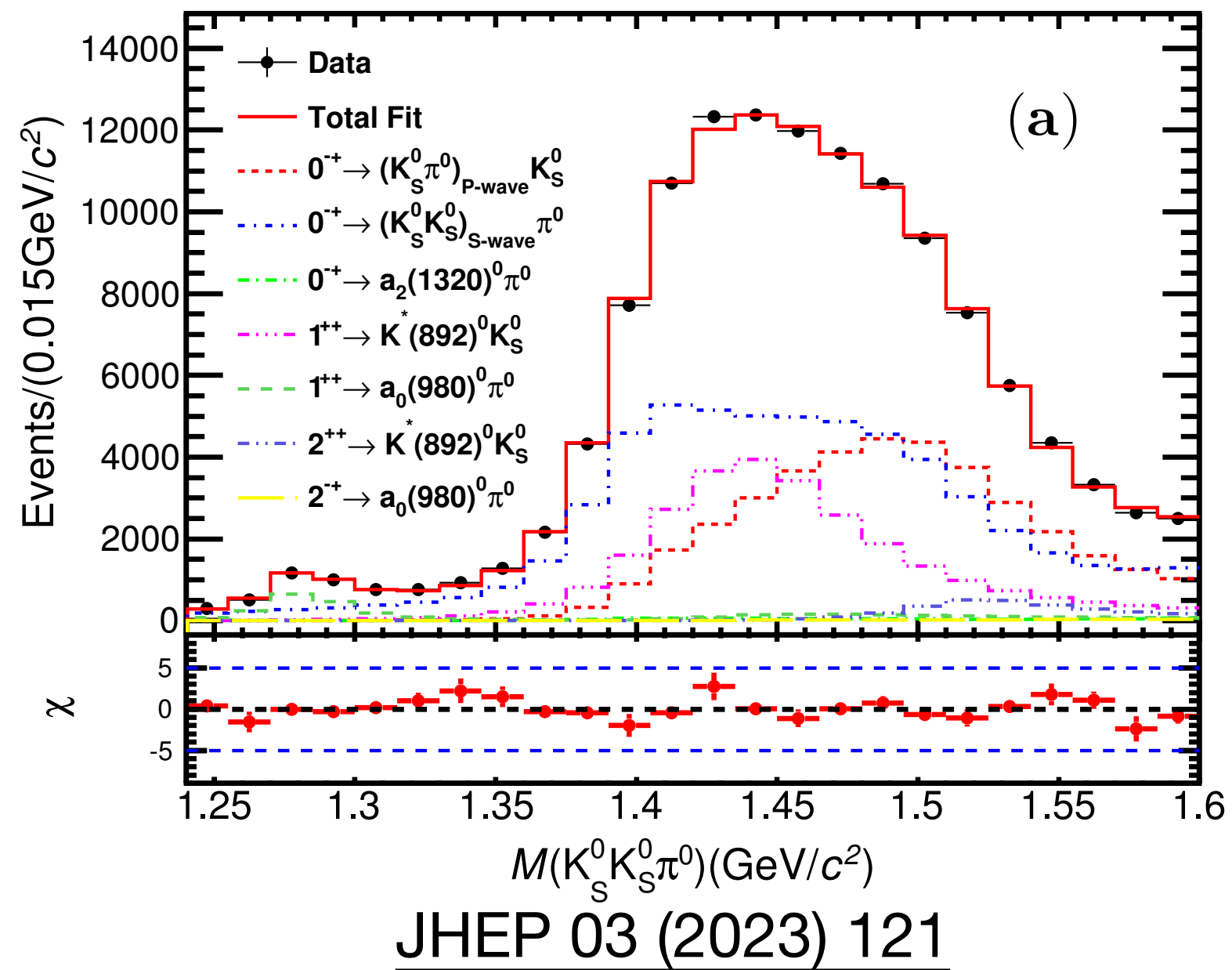


Phys. Lett. 97B (1980) 2

- ◆ First discovered by MarkII in 1980, named as  $\eta(1440)$  with complicated structures.
- ◆ Believed as the first glueball candidate due to its large production rate in  $J/\psi$  radiative decays
- ◆ Lots of studies at MarkII, MarkIII, DM2 and BES:
  - ◆ **No longer a  $0^{-+}$  glueball candidate due to its large different mass from latest LQCD prediction (Lack of reliable LQCD predictions in 1980's)**



# Shed new lights on $\eta(1405)/\eta(1475)$ puzzle

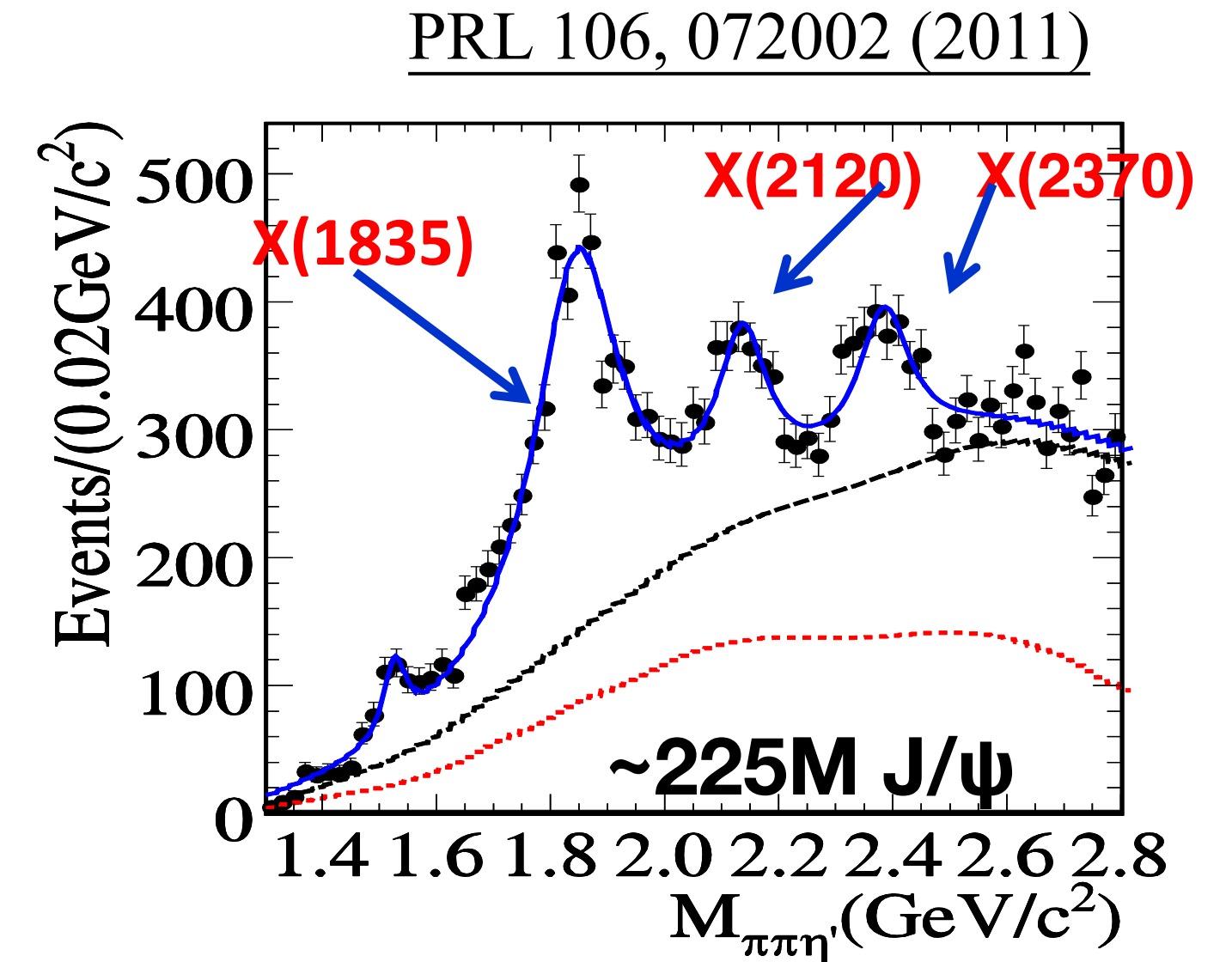


- ◆  $\eta(1295)$  and  $\eta(1475)$  are generally assigned to be the first radial excitation of the ground states of  $\eta$  and  $\eta'$
- ◆  $\eta(1405) - \eta(1475)$  puzzle :Whether or not the  $\eta(1405) - \eta(1475)$  are 1 or 2 states?
- ◆ PWA of  $J/\psi \rightarrow \gamma K_S K_S \pi^0$ : Two isoscalar states  $\eta(1405)$  and  $\eta(1475)$  around 1.4 GeV can well fit data
- ◆ PWA of  $J/\psi \rightarrow \gamma \gamma \Phi$ : observed  $\eta(1405)$  with  $18.9\sigma$ , while  $\eta(1475)$  can not be excluded ( $3.9\sigma$ )

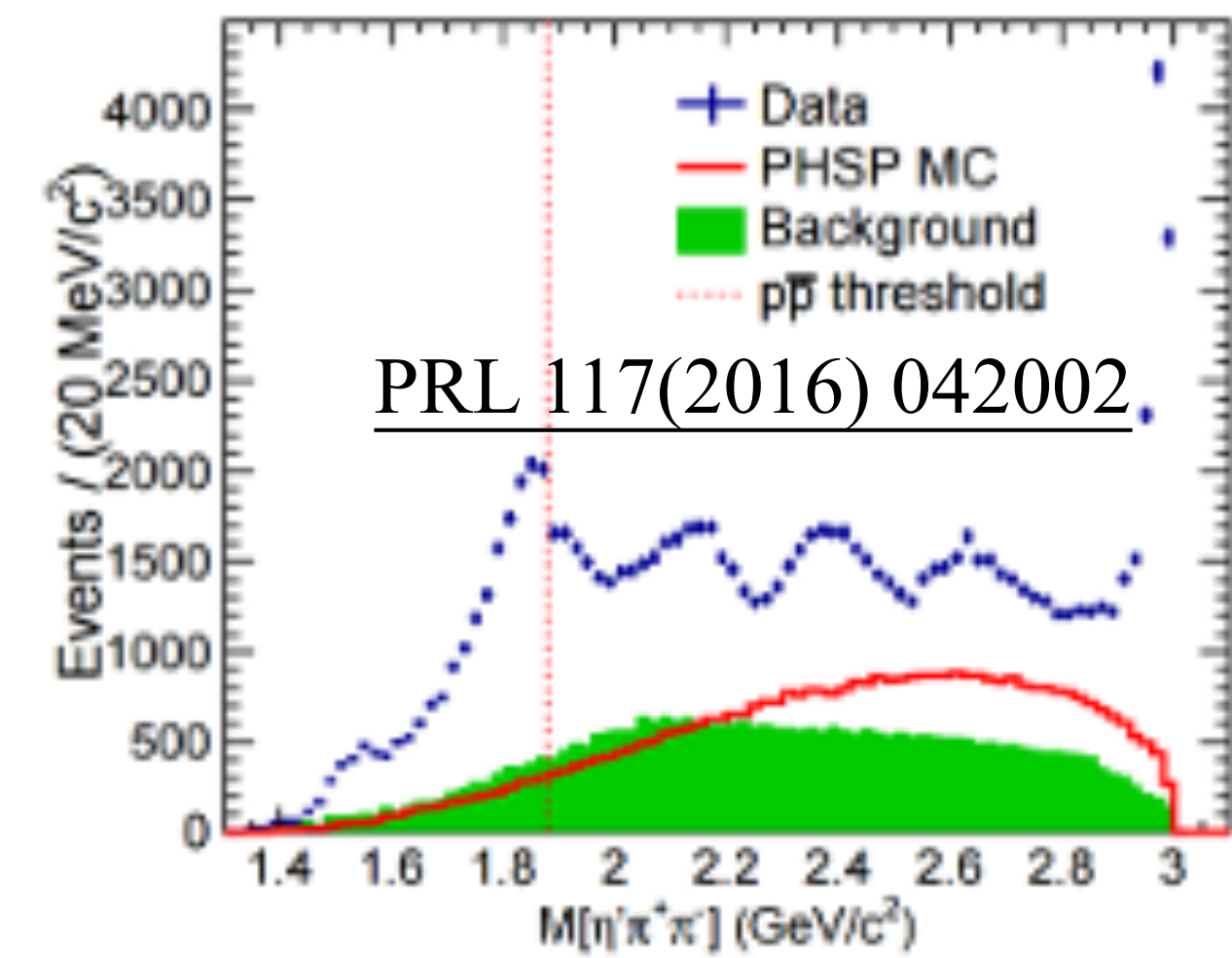
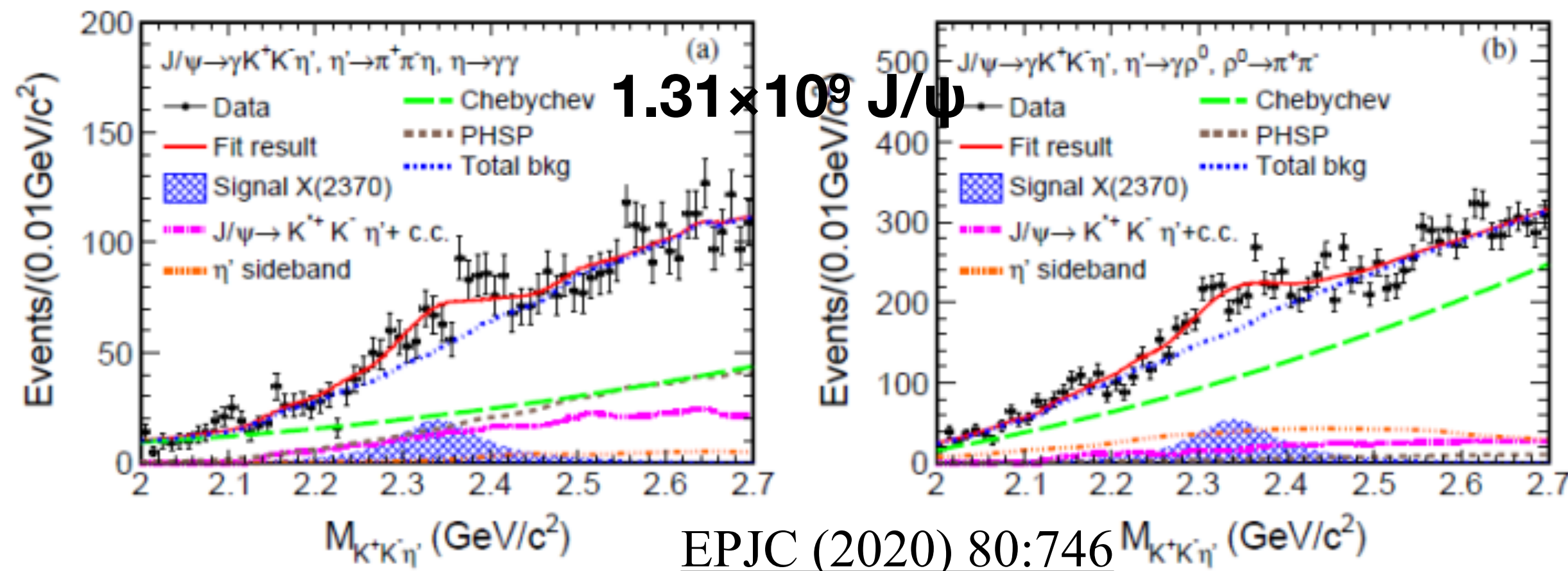
# X(2370)

◆ Discovered by BESIII in  $J/\psi \rightarrow \gamma\pi^+\pi^-\eta'$  in 2011

	$M(\text{MeV}/c^2)$	$\Gamma(\text{MeV}/c^2)$	Sig.
X(1835)	$1836.5 \pm 3.0^{+5.6}_{-2.1}$	$190.1 \pm 9.0^{+38}_{-36}$	$>20\sigma$
X(2120)	$2122.4 \pm 6.7^{+4.7}_{-2.7}$	$83 \pm 16^{+31}_{-11}$	$7.2\sigma$
X(2370)	$2376.3 \pm 8.7^{+3.2}_{-4.3}$	$83 \pm 17^{+44}_{-6}$	$6.4\sigma$

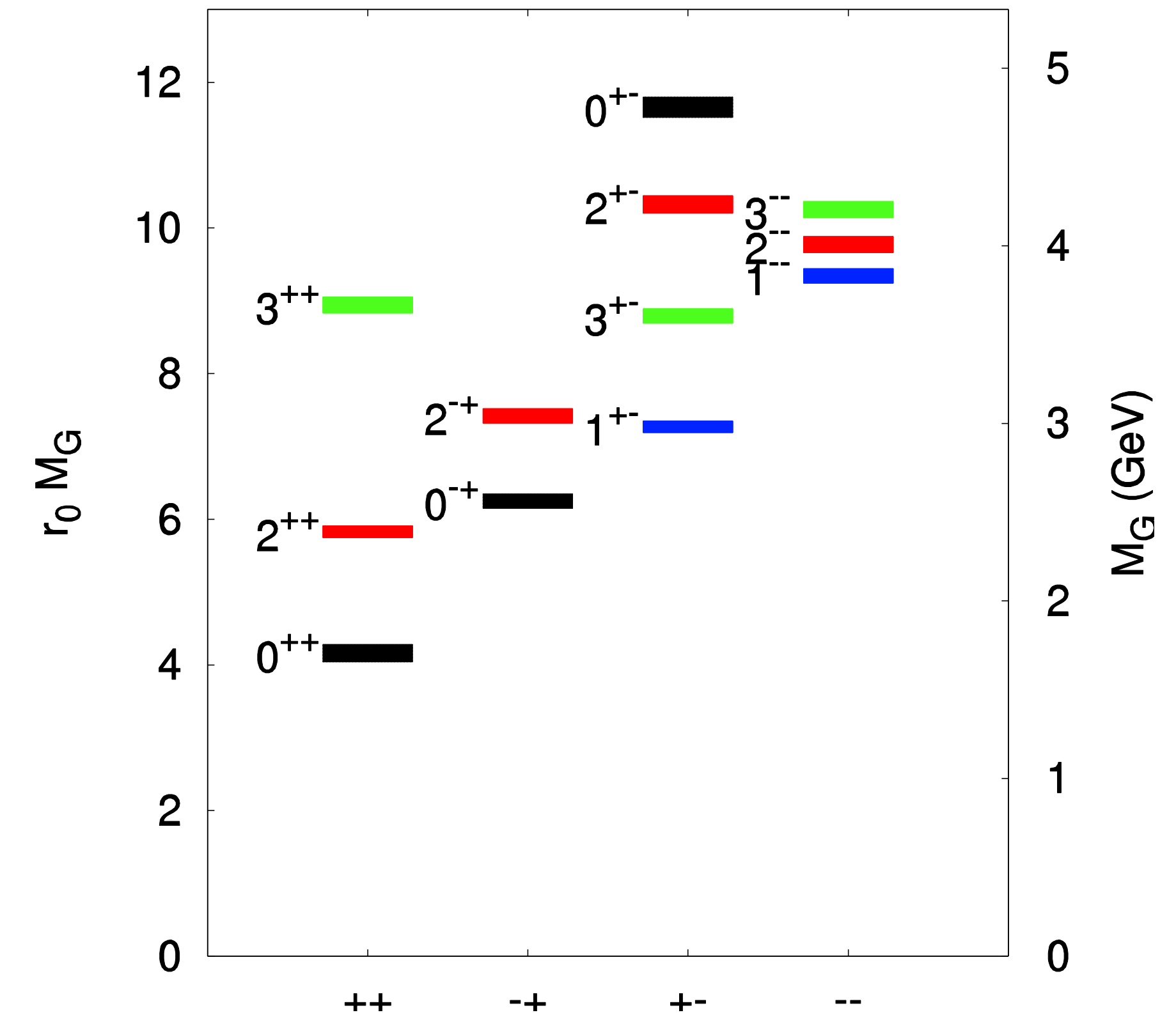


◆ Confirmed by BESIII in  $J/\psi \rightarrow \gamma\pi^+\pi^-\eta'$  and  $J/\psi \rightarrow \gamma K\bar{K}\eta'$  (new mode)

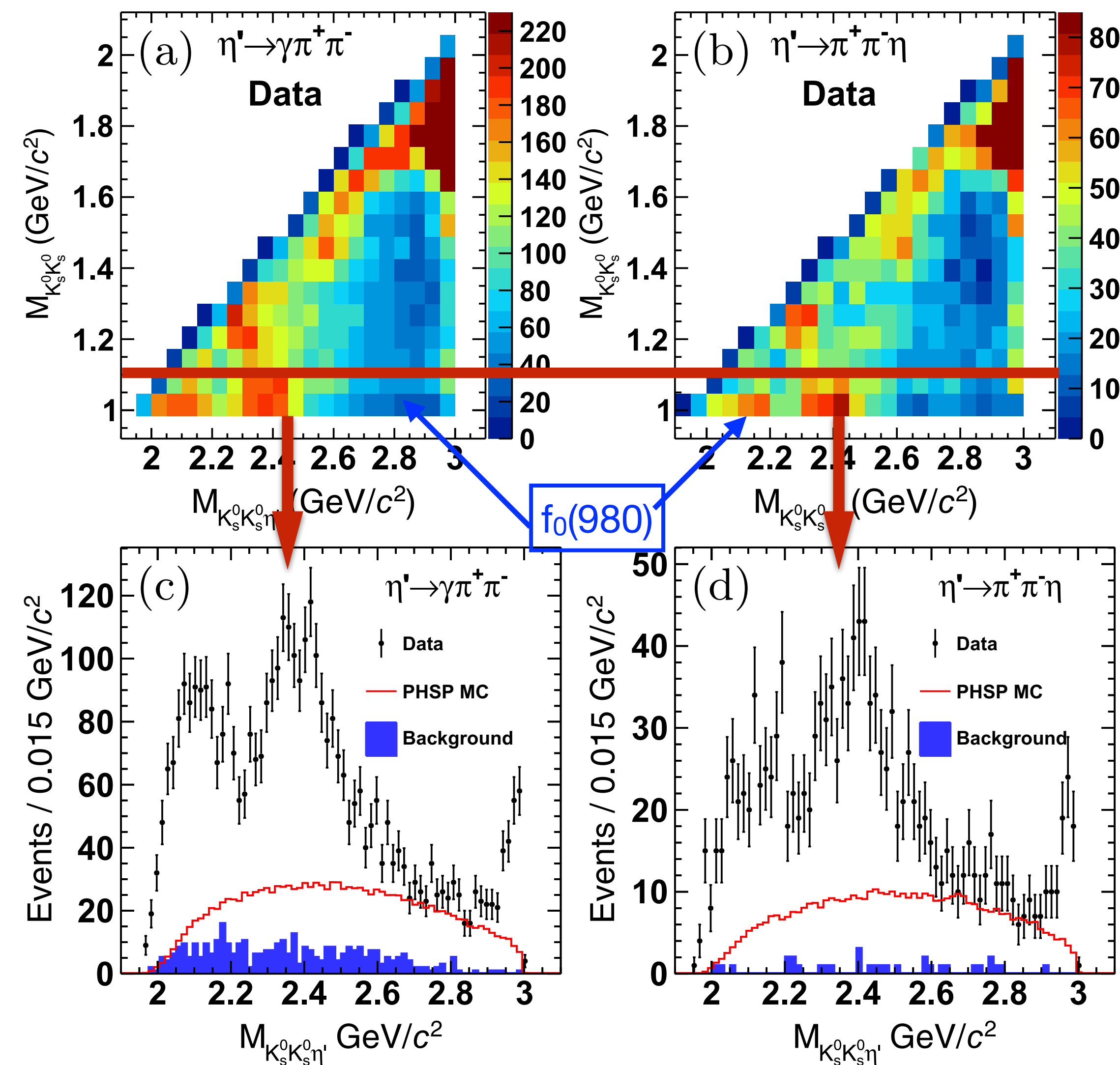


# X(2370) - good candidate of $0^{-+}$ glueball

- ◆ Its mass is consistent with LQCD prediction on the  $0^{-+}$  glueball
- ◆ Produced in the gluon-rich  $J/\psi$  radiative decays
- ◆ Observed in flavor symmetric decay modes of  $\pi^+\pi^-\eta'$  and  $K\bar{K}\eta'$  — favorite decay modes of  $0^{-+}$  glueball
- ◆ **Determination of its spin-parity is crucial**

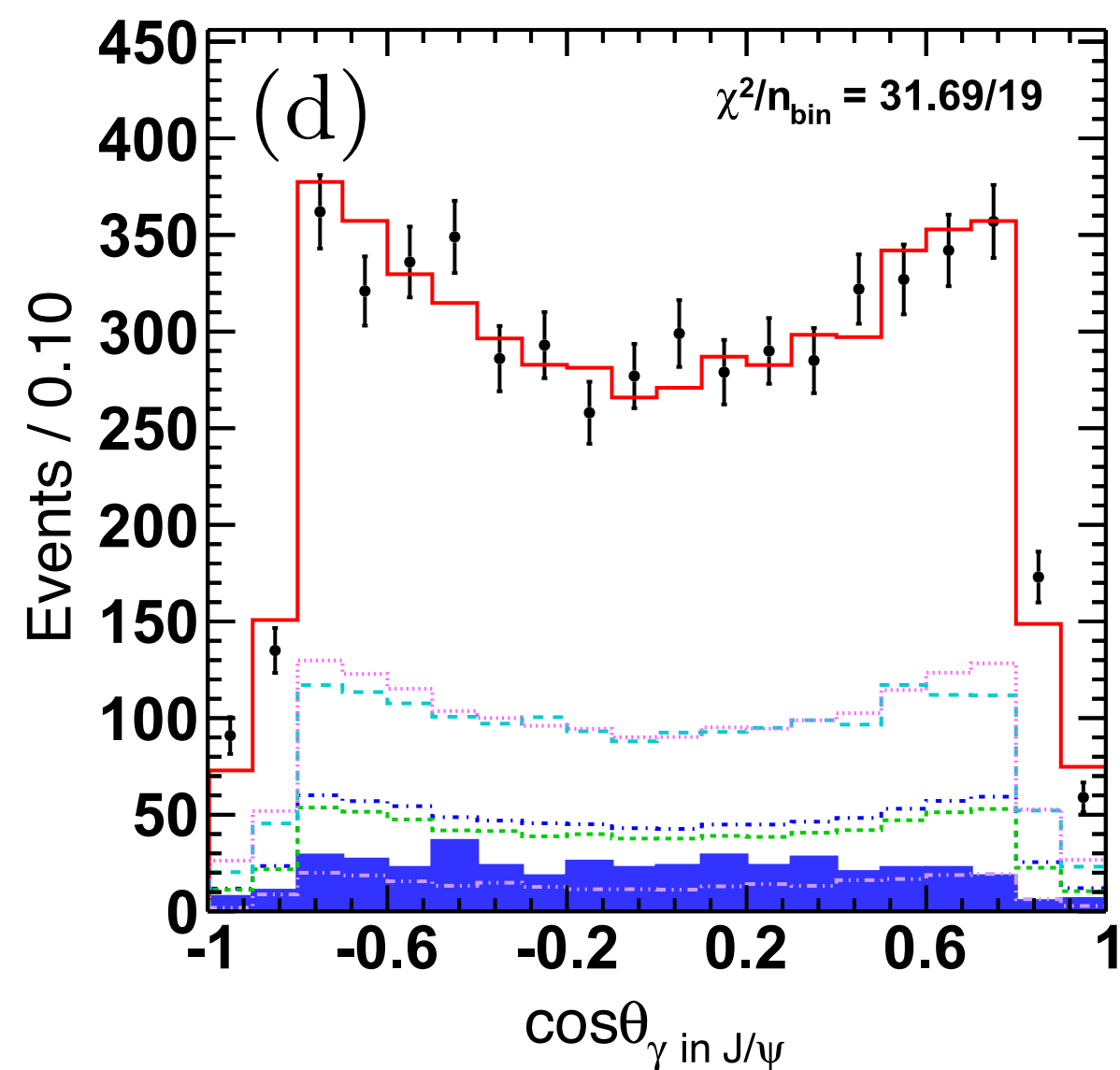
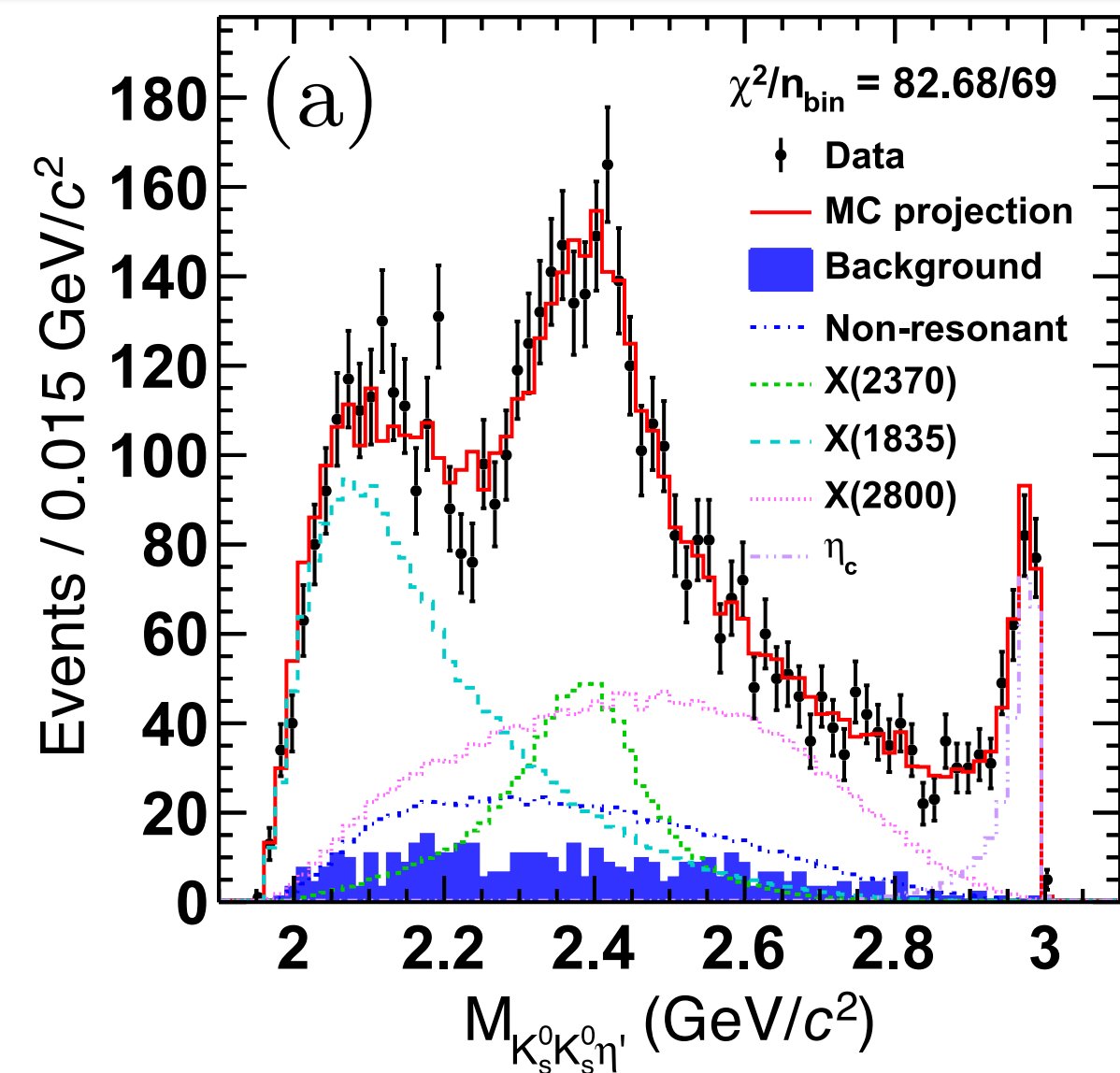


# Spin-Parity determination of the $X(2370)$ in $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta'$



- ◆ Analysis advantage of  $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta'$ :
  - ◆ Almost background free channel (exchange symmetry and C-parity conservation)
  - ◆ 10 billion  $J/\psi$  data
  - ◆ Very good BESIII detector performance
- ◆ Similar structures in  $\eta' \rightarrow \pi^+ \pi^- \eta$  /  $\gamma \pi^+ \pi^-$  modes:
  - ◆ Evident  $f_0(980)$  in  $K_s^0 K_s^0$  mass threshold
  - ◆ Clear signal of  $X(1835), X(2370), \eta_c$  with  $f_0(980)$  selection
- ◆ Best PWA fit can well describe the data:
  - ◆ **Spin-parity of the  $X(2370)$  is determined to be  $0^-$  with significance larger than  $9.8\sigma$  w.r.t. other  $J^{PC}$  assumptions**

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PRL 132 (2024) 181901

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  - ◆ Clear signal of  $X(1835), X(2370), \eta_c$  with  $f_0(980)$  selection
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  - ◆ **Spin-parity of the  $X(2370)$  is determined to be  $0^{-+}$  with significance larger than  $9.8\sigma$  w.r.t. other  $J^{PC}$  assumptions**

# Compared with LQCD prediction on Lightest $0^{-+}$ Glueball

## **X(2370) measurements:**

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**$J^{PC} = 0^{-+}$  with significance  $>9.8\sigma$**

**$M = 2395 \pm 11^{+26}_{-94}$  MeV**

**$\Gamma = 188^{+18}_{-17}{}^{+124}_{-33}$  MeV**

**$B(J/\psi \rightarrow \gamma X(2370))B(X(2370) \rightarrow f_0(980)\eta')$   
 $B(f_0(980) \rightarrow K^0_s K^0_s)$   
 $= (1.31 \pm 0.22^{+2.85}_{-0.84}) \times 10^{-5}$**

## **LQCD prediction on lightest pseudoscalar glueball:**

**$J^{PC} = 0^{-+}$**

**$M = 2395 \pm 14$  MeV**

**$B(J/\psi \rightarrow \gamma G_{0^{-+}}) = (2.31 \pm 0.80) \times 10^{-4}$**

PRD 100 (2019) 054511

- ◆ The measurements are in a good agreement with the predictions on **lightest pseudoscalar glueball**
- ◆ **The spin-parity of the X(2370) is determined to be  $0^{-+}$  for the first time**
- ◆ **Mass is in a good agreement with LQCD predictions**
- ◆ The estimation on  $B(J/\psi \rightarrow \gamma X(2370))$  and prediction on  $B(J/\psi \rightarrow \gamma G_{0^{-+}})$  are consistent within errors (assuming  $\sim 5\%$  decay rate,  $B(J/\psi \rightarrow \gamma X(2370)) = (10.7^{+22.8}_{-7}) \times 10^{-4}$ )

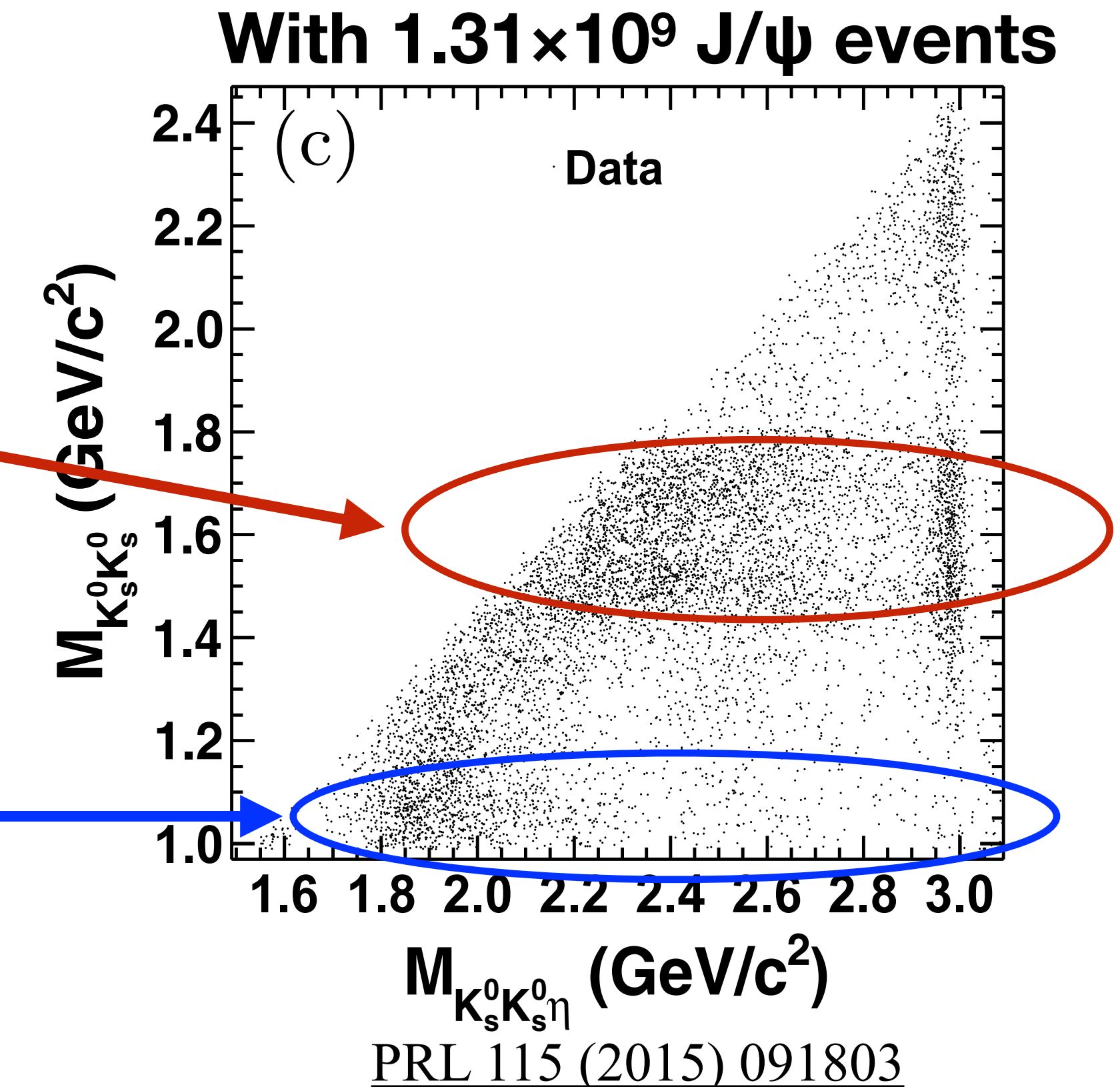
# X(2370) in $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta$

Observation and Spin-Parity Determination of the X(1835) in  $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta$

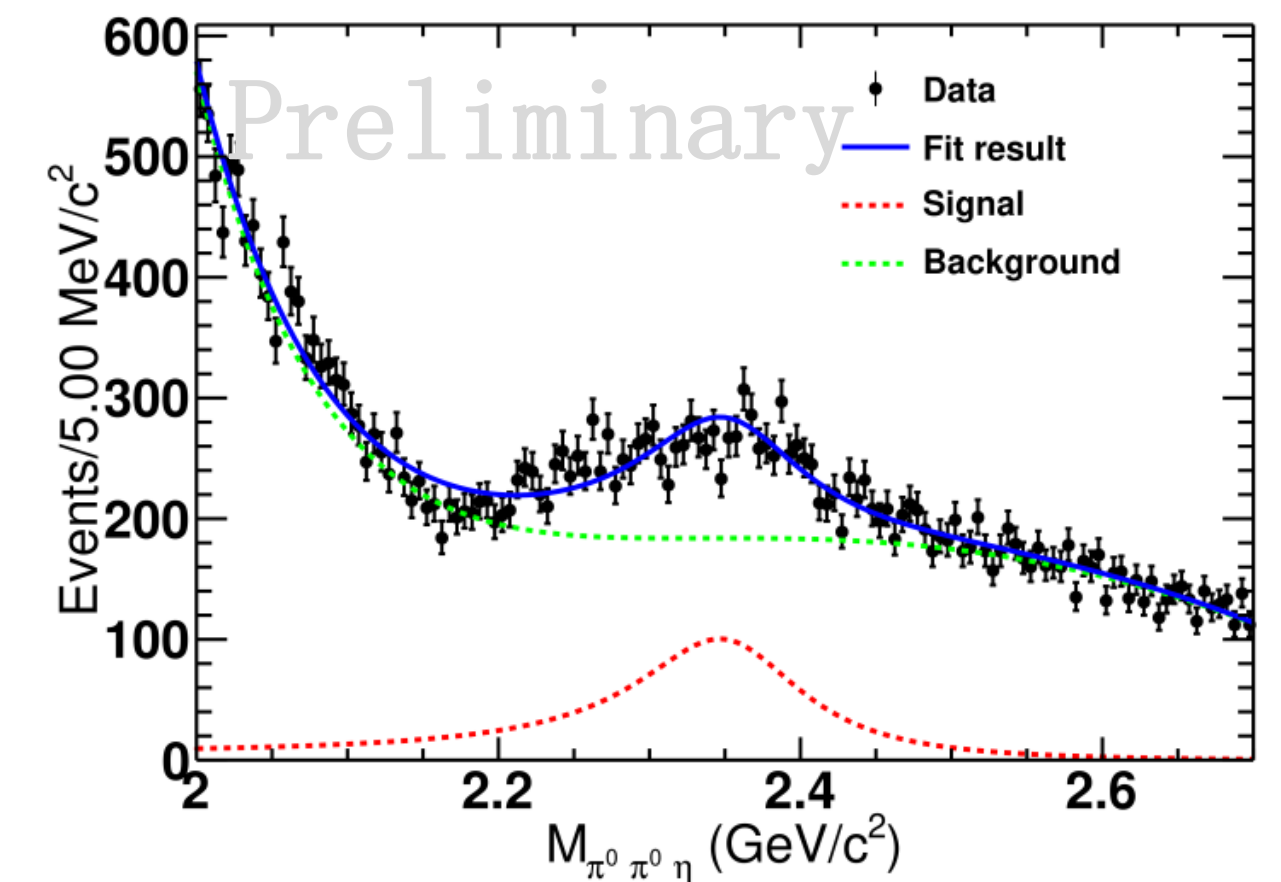
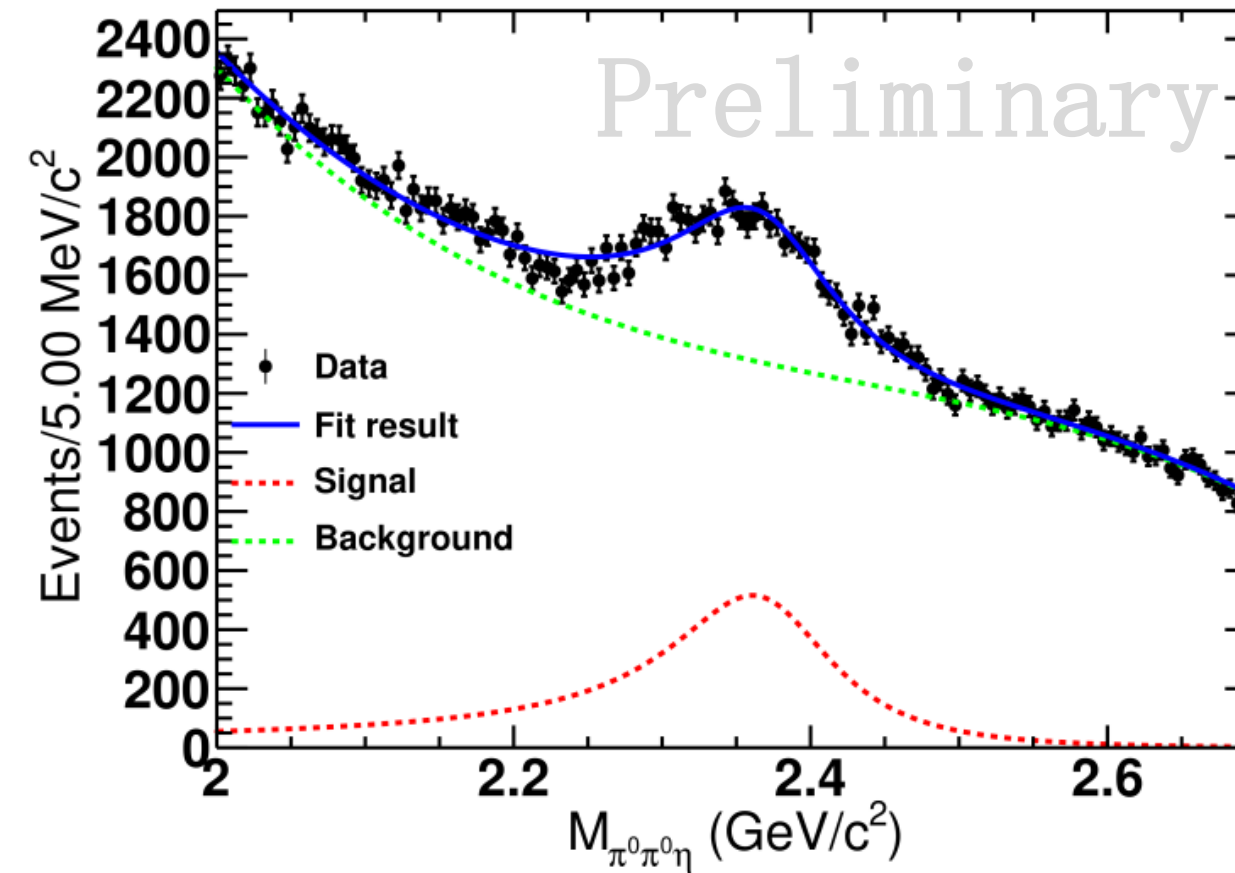
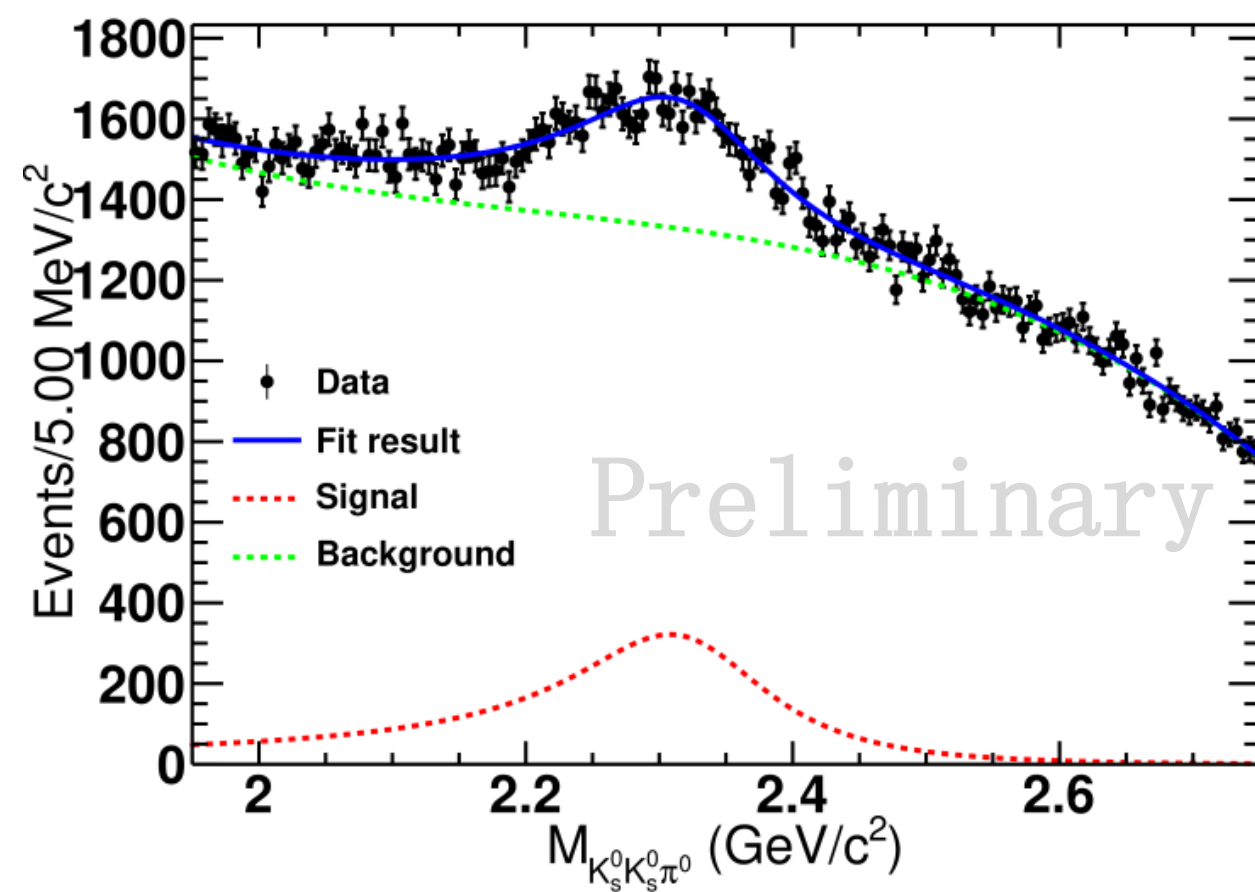
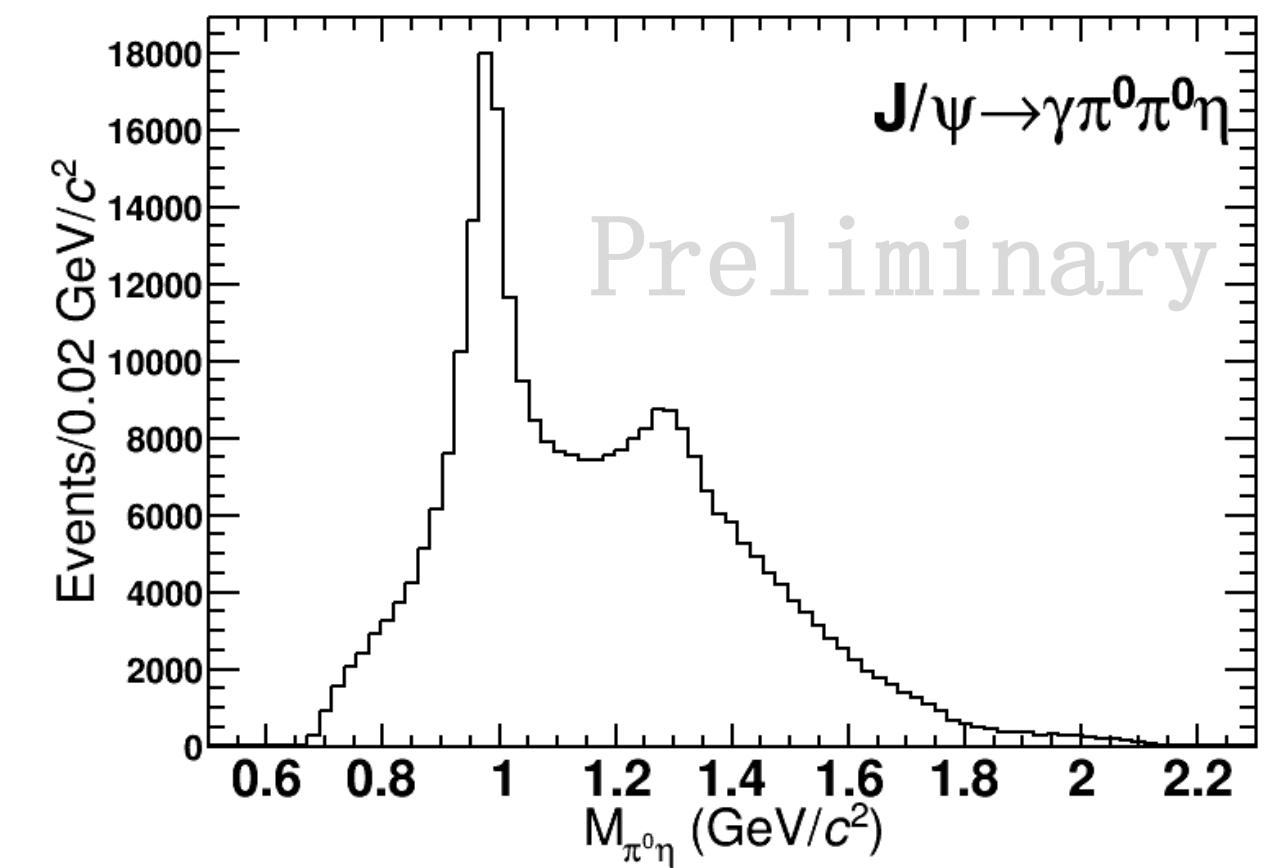
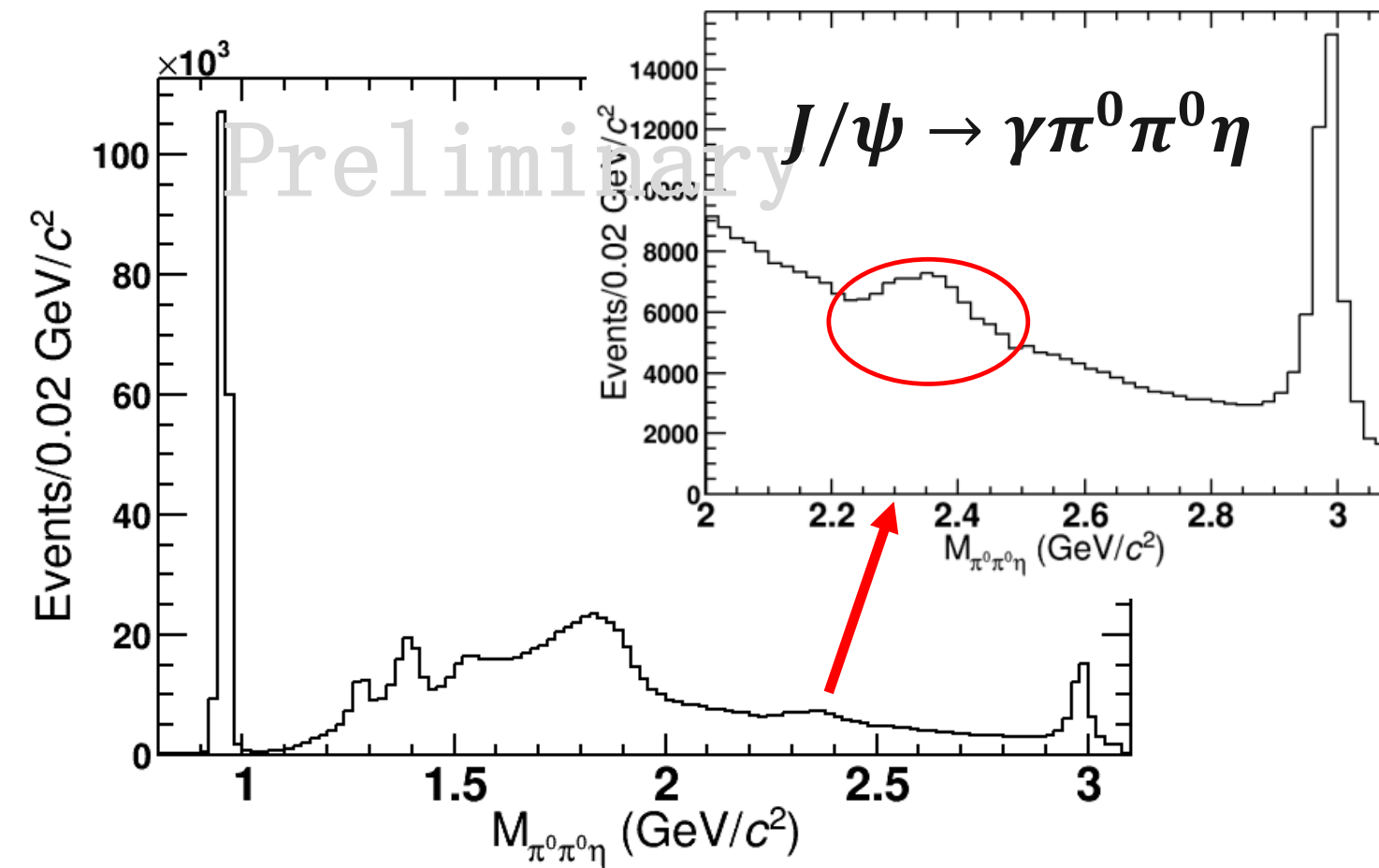
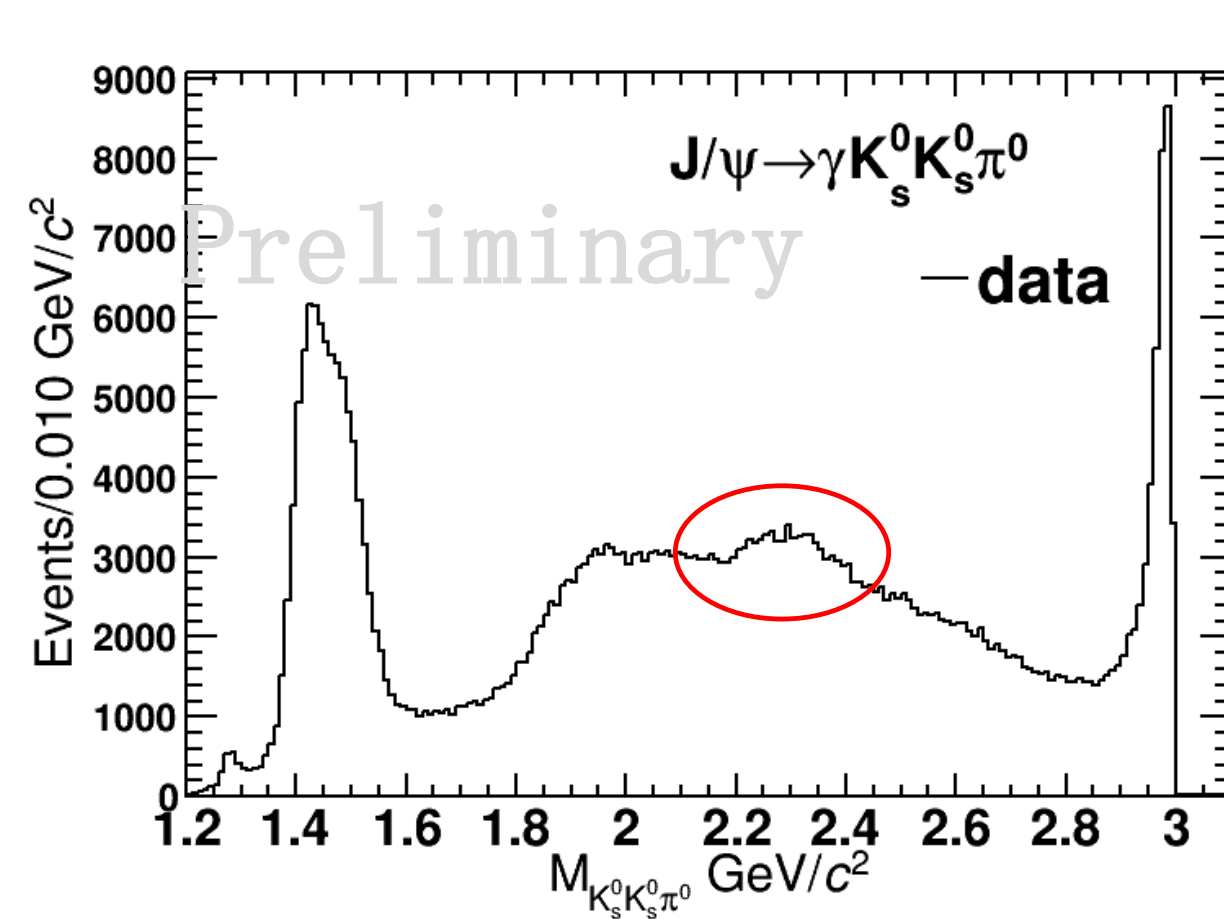
Qualitatively, we can clearly observe: similar decay patterns of the X(2370) and  $\eta_c$  if phase space allows

In the upper KK mass band of 1.5-1.7 GeV range, clear signals of both X(2370) and  $\eta_c$

In the lower KK mass band of  $f_0(980)$ , no X(2370), nor  $\eta_c$



# Observation of new decay modes of the X(2370)



First observation of  $X(2370) \rightarrow K_s^0 K_s^0 \pi^0$ ,  $X(2370) \rightarrow \pi^0 \pi^0 \eta$  and  $X(2370) \rightarrow a(980) \eta$  with significances  $\gg 5\sigma$  and accompanied with  $\eta_c$



# Observation of the X(2370) in the 5 golden decay modes

5 major  $\eta_c$  decay modes (from PDG)  
— 5 “Golden” modes in  $0^{-+}$  glueball traditional searches

Decays involving hadronic resonances

$\Gamma_1$	$\eta'(958)\pi\pi$	( 1.87 ± 0.26 ) %
$\Gamma_2$	$\eta'(958)K\bar{K}$	( 1.61 ± 0.25 ) %

Decays into stable hadrons

$\Gamma_{34}$	$K\bar{K}\pi$	( 7.0 ± 0.4 ) %
$\Gamma_{35}$	$K\bar{K}\eta$	( 1.32 ± 0.15 ) %
$\Gamma_{36}$	$\eta\pi^+\pi^-$	( 1.7 ± 0.5 ) %

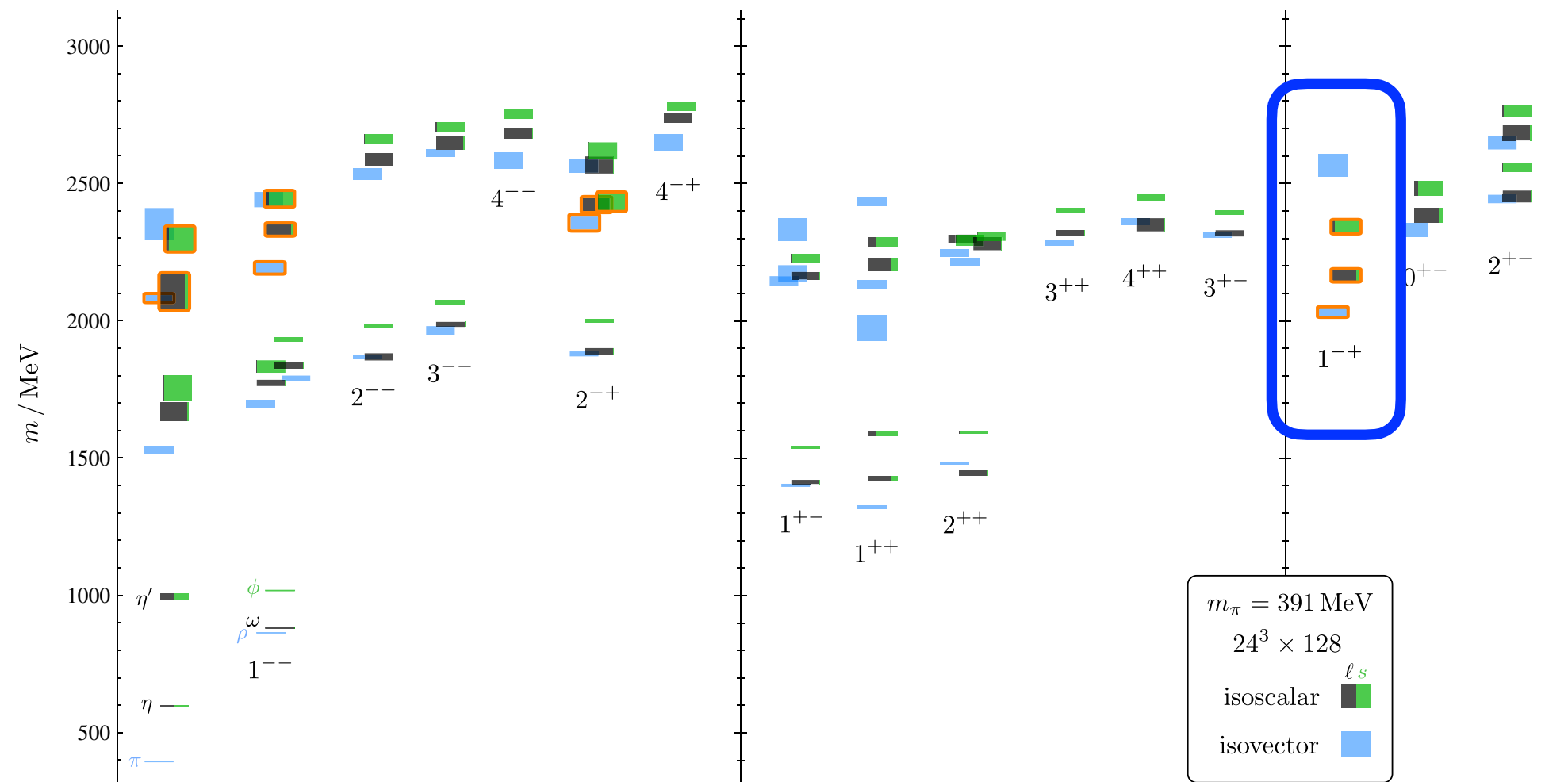
◆ The  $0^{-+}$  glueball decays could be the analogy to  $\eta_c$  decays

- Decay modes of X(2370)  $\rightarrow \pi\pi\eta', K\bar{K}\eta', K\bar{K}\pi, \pi\pi\eta, K\bar{K}\eta, a(980)\pi$  observed, consistent with  $0^{-+}$  glueball

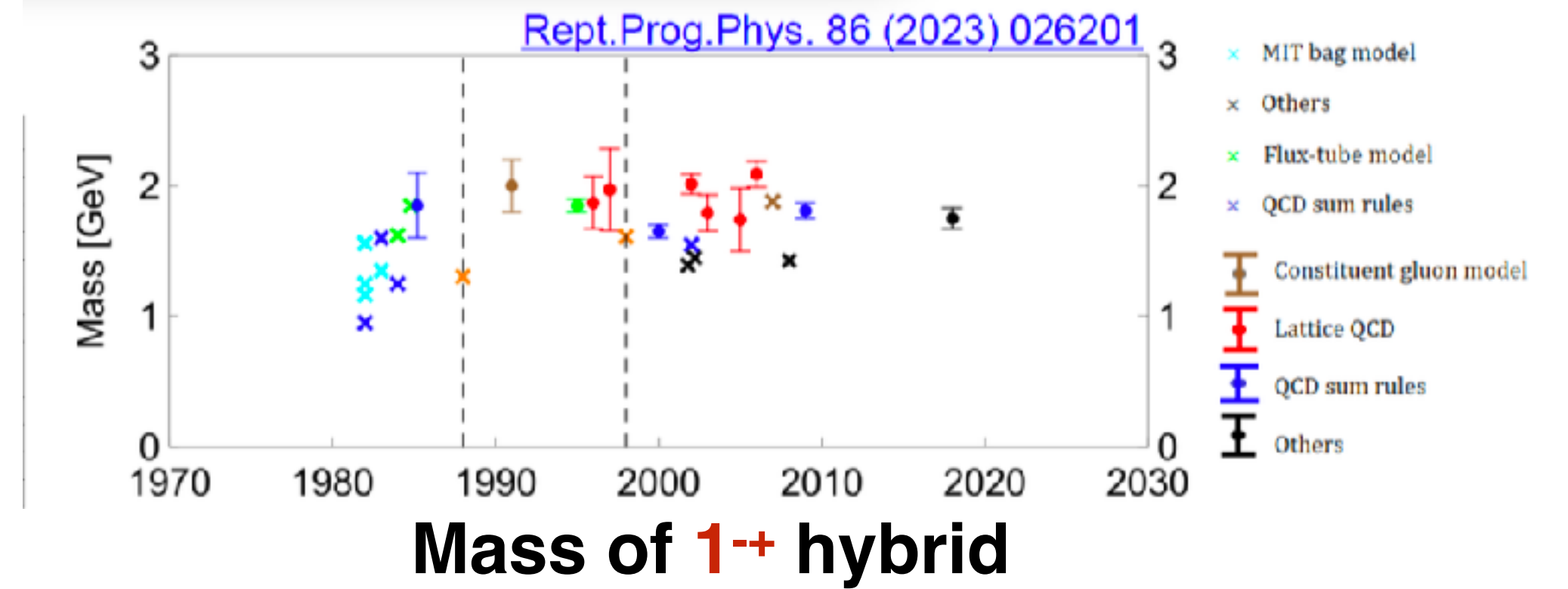
**Such high similarity between the X(2370) and  $\eta_c$  decay modes strongly supports the glueball interpretation of the X(2370)**

# Exotic $1^{-+}$ state

$J^{PC}$	$q\bar{q}$
$0^{++}$	yes
$0^{+-}$	-
$0^{-+}$	yes
$0^{--}$	-
$1^{++}$	yes
$1^{+-}$	yes
$1^{-+}$	-
$1^{--}$	yes
$2^{++}$	yes
$2^{+-}$	-
$2^{-+}$	yes
$2^{--}$	yes
$3^{++}$	yes
$3^{+-}$	yes
$3^{-+}$	-
$3^{--}$	yes

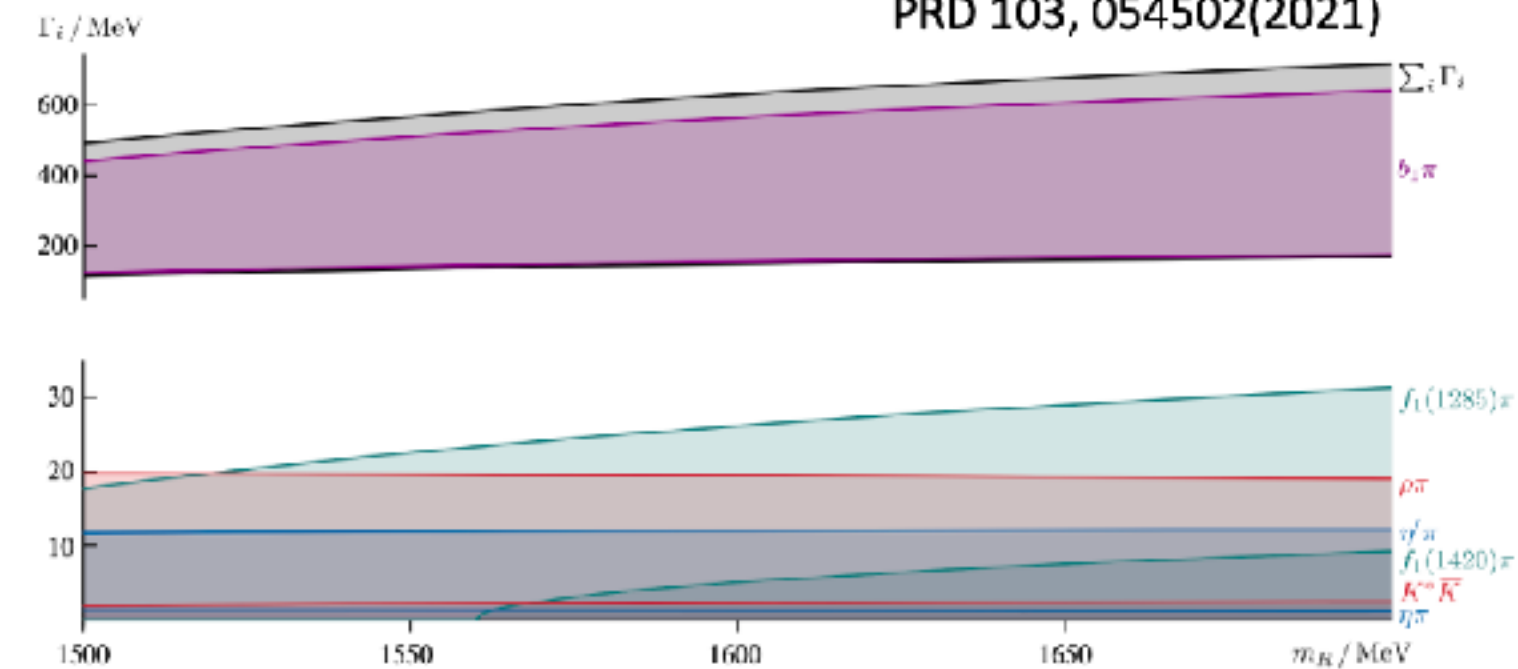


[PRD 88 094505\(2013\)](#)



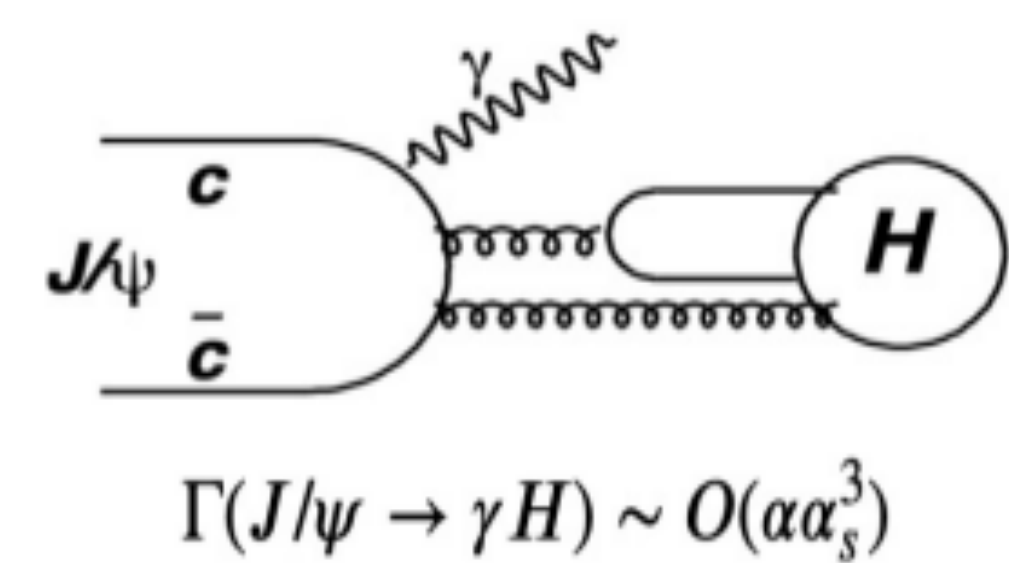
Mass of  $1^{-+}$  hybrid

PRD 103, 054502(2021)



Width of  $1^{-+}$  hybrid

- ◆ **Spin-exotic state of  $1^{-+}$  :** forbidden in conventional quark model
- ◆ Exotic state  $1^{-+}$  provide an unique way for hybrid search:
- ◆ LQCD predicts the **lightest nonet of  $1^{-+}$  hybrids:** 1.7 - 2.1GeV
- ◆ **Can be produced in the gluon-rich charmonium decays**



# Spin-exotic mesons

◆ Over 3 decades, experimental evidence for 3 candidates with  $1^-+$  state:

◆ All  $1^-+$  iso-vectors

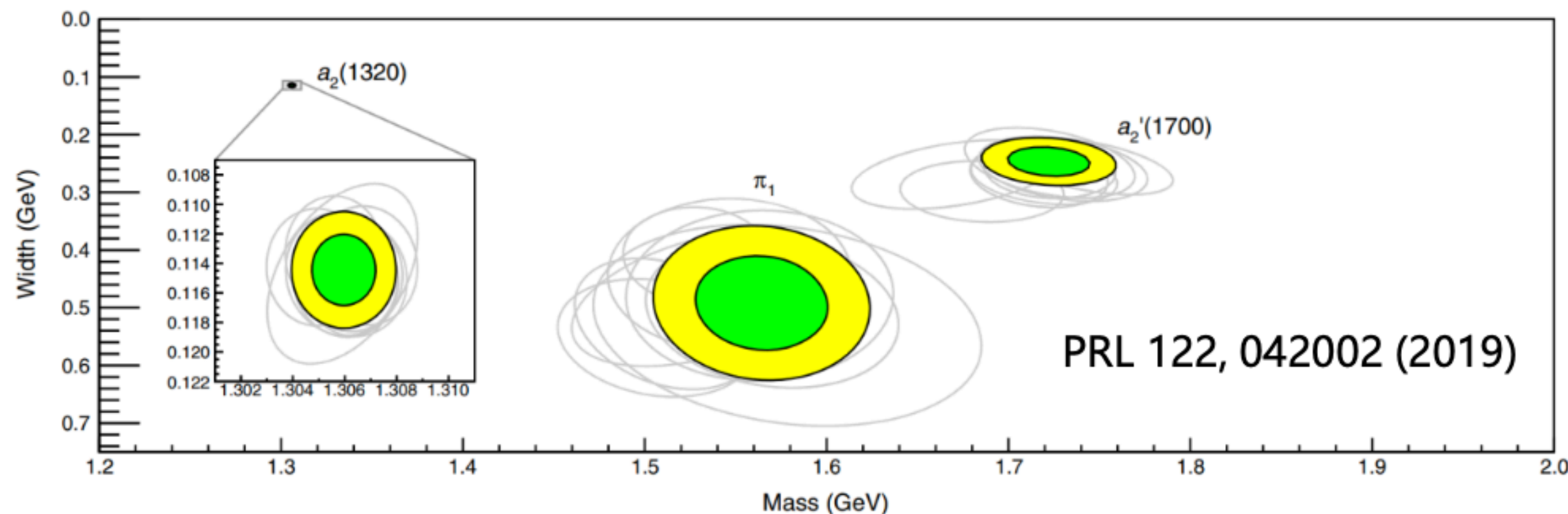
◆  $\pi_1(1400)$  : seen in  $\eta\pi$

◆  $\pi_1(1600)$  : seen in  $\rho\pi, \eta'\pi, b_1\pi, f_1\pi$

◆  $\pi_1(2015)$ : seen in  $b_1\pi$  and  $f_1\pi$

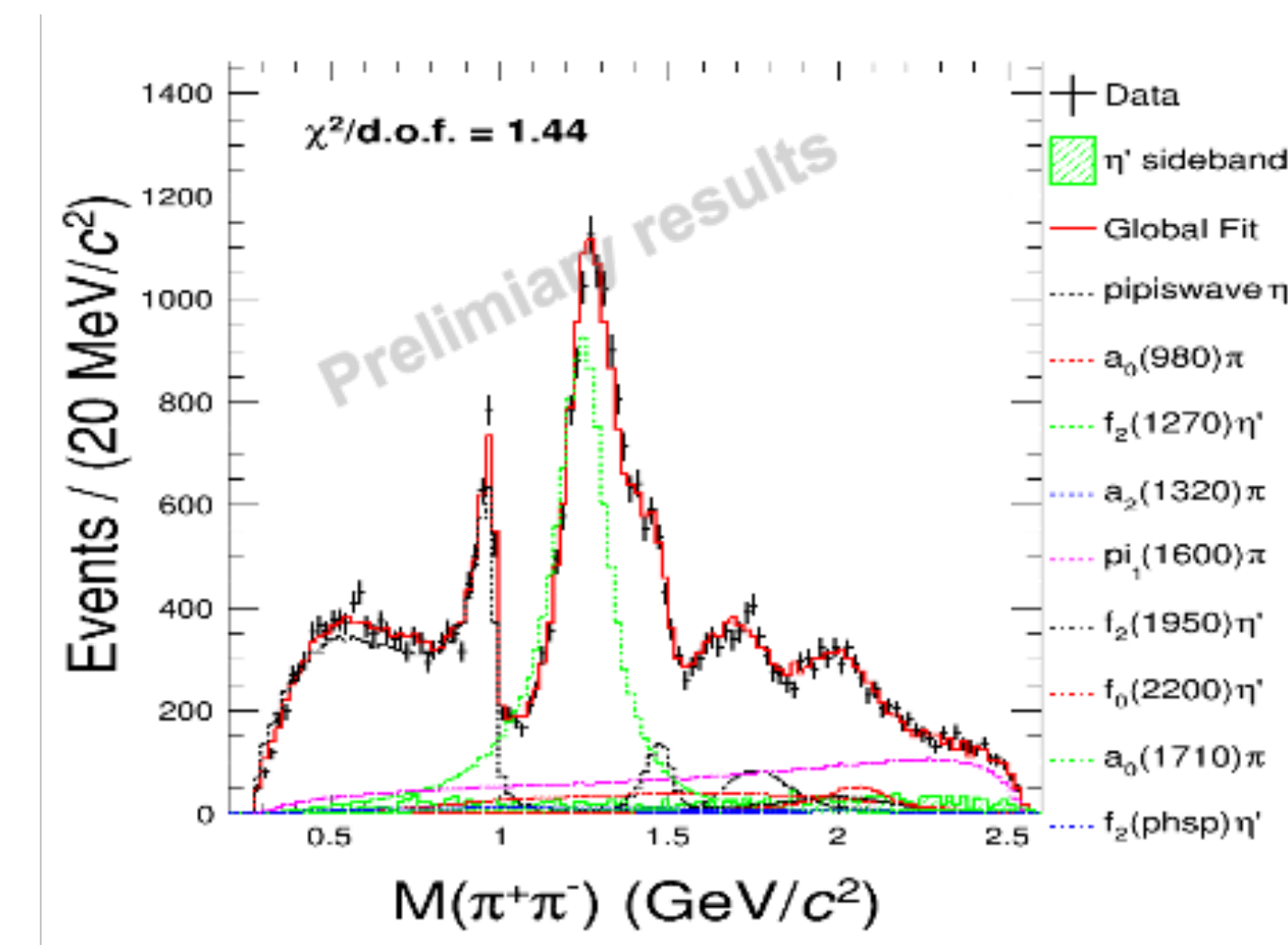
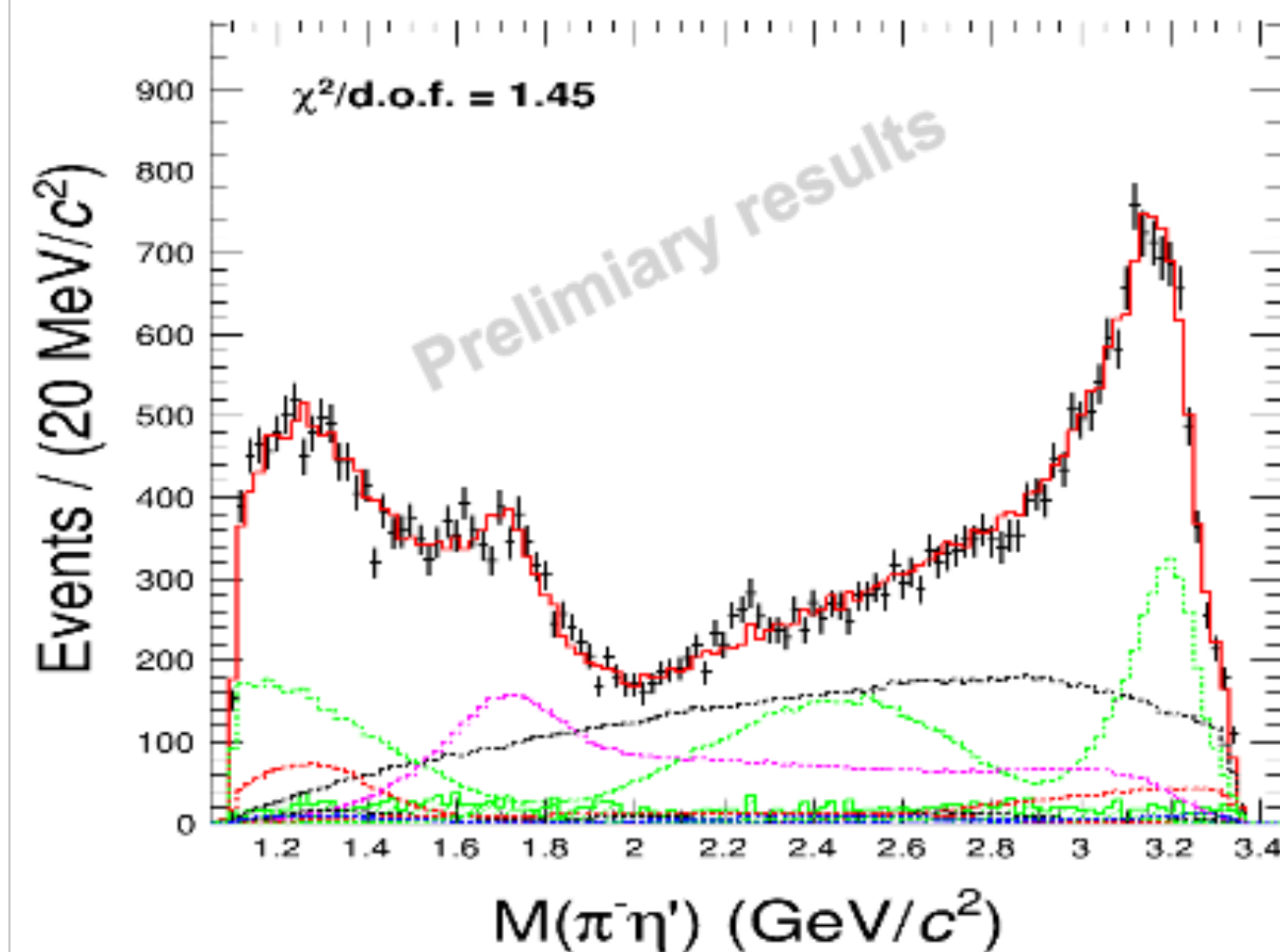
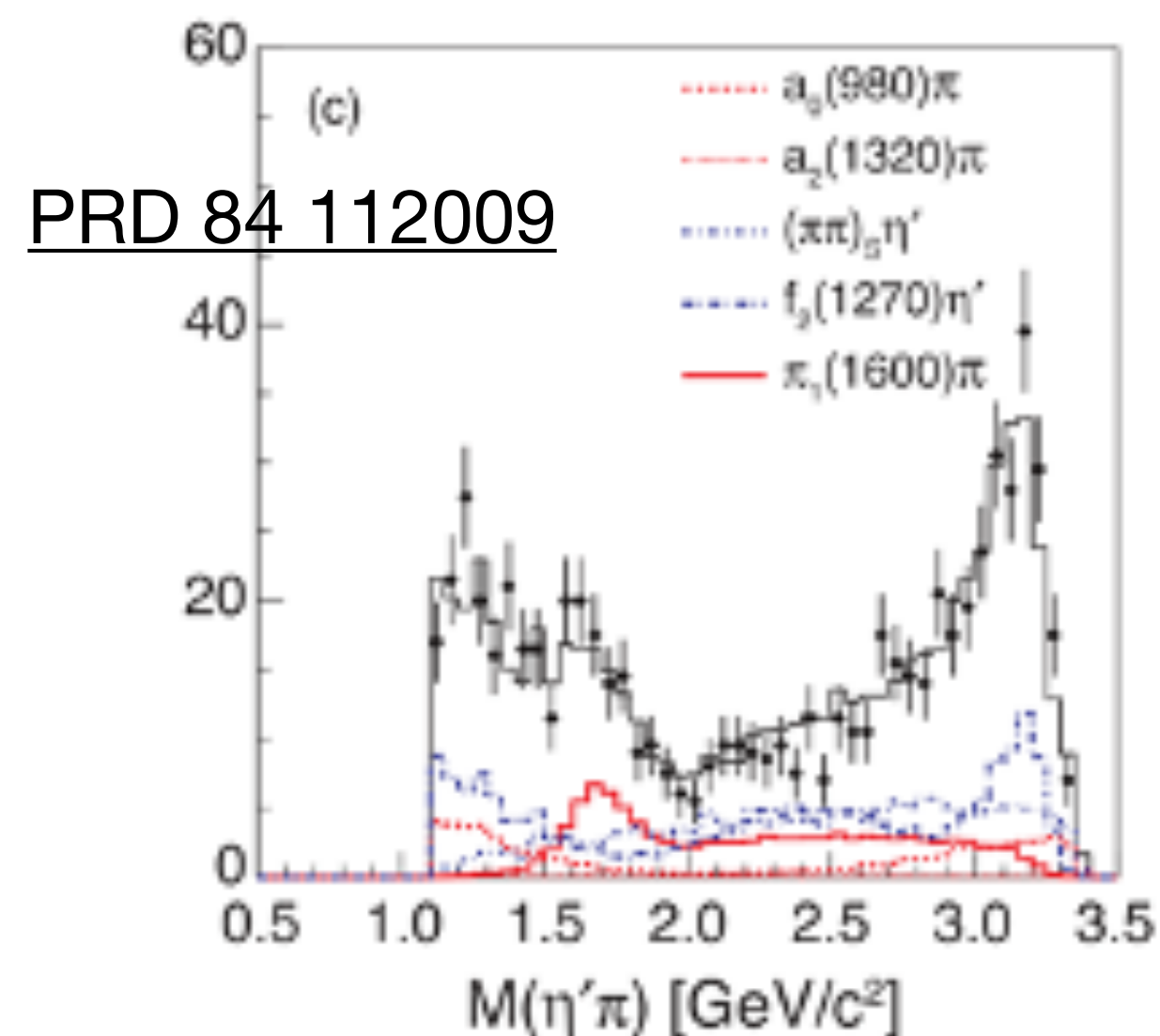
◆ Some claims are controversial

◆  $\pi_1(1400)$  and  $\pi_1(1600)$  can be one pole



	Decay mode	Reaction	Experiment
$\pi_1(1400)$	$\eta\pi$	$\pi^-p \rightarrow \pi^-\eta p$ $\pi^-p \rightarrow \pi^0\eta n$ $\pi^-p \rightarrow \pi^-\eta p$ $\pi^-p \rightarrow \pi^0\eta n$ $\bar{p}n \rightarrow \pi^-\pi^0\eta$ $\bar{p}p \rightarrow \pi^0\pi^0\eta$	GAMS KEK E852 E852 CBAR CBAR
	$\rho\pi$	$\bar{p}p \rightarrow 2\pi^+2\pi^-$	Obelix
$\pi_1(1600)$	$\eta'\pi$	$\pi^-Be \rightarrow \eta'\pi^-\pi^0Be$ $\pi^-p \rightarrow \pi^-\eta'p$	VES E852
	$b_1\pi$	$\pi^-Be \rightarrow \omega\pi^-\pi^0Be$ $\bar{p}p \rightarrow \omega\pi^+\pi^-\pi^0$ $\pi^-p \rightarrow \omega\pi^-\pi^0p$	VES CBAR E852
	$\rho\pi$	$\pi^-Pb \rightarrow \pi^+\pi^-\pi^-X$ $\pi^-p \rightarrow \pi^+\pi^-\pi^-p$	COMPASS E852
	$f_1\pi$	$\pi^-p \rightarrow \rho\eta\pi^+\pi^-\pi^-$ $\pi^-A \rightarrow \eta\pi^+\pi^-\pi^-A$	E852 VES
$\pi_1(2015)$	$f_1\pi$	$\pi^-p \rightarrow \omega\pi^-\pi^0p$	E852
	$b_1\pi$	$\pi^-p \rightarrow \rho\eta\pi^+\pi^-\pi^-$	

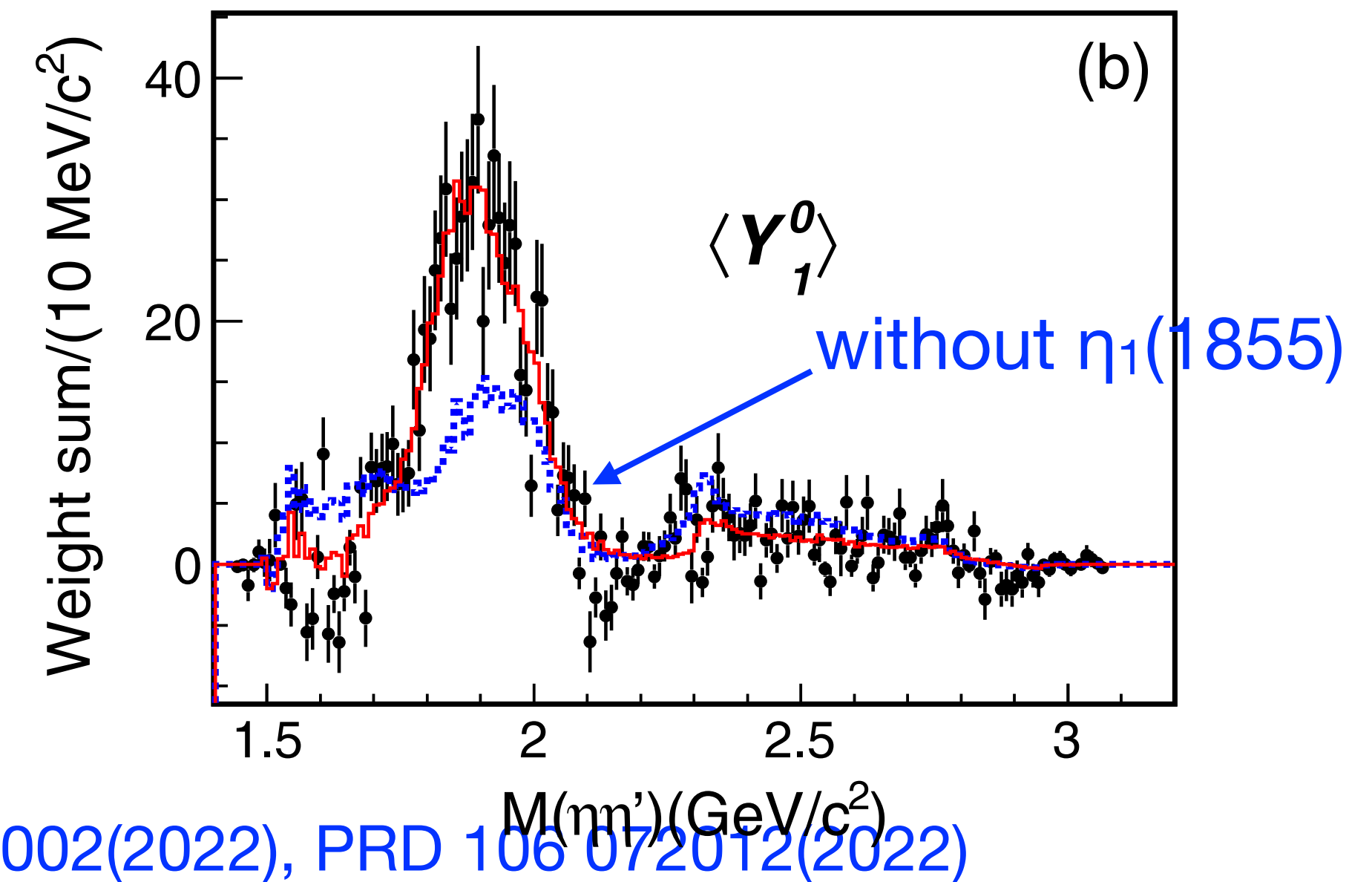
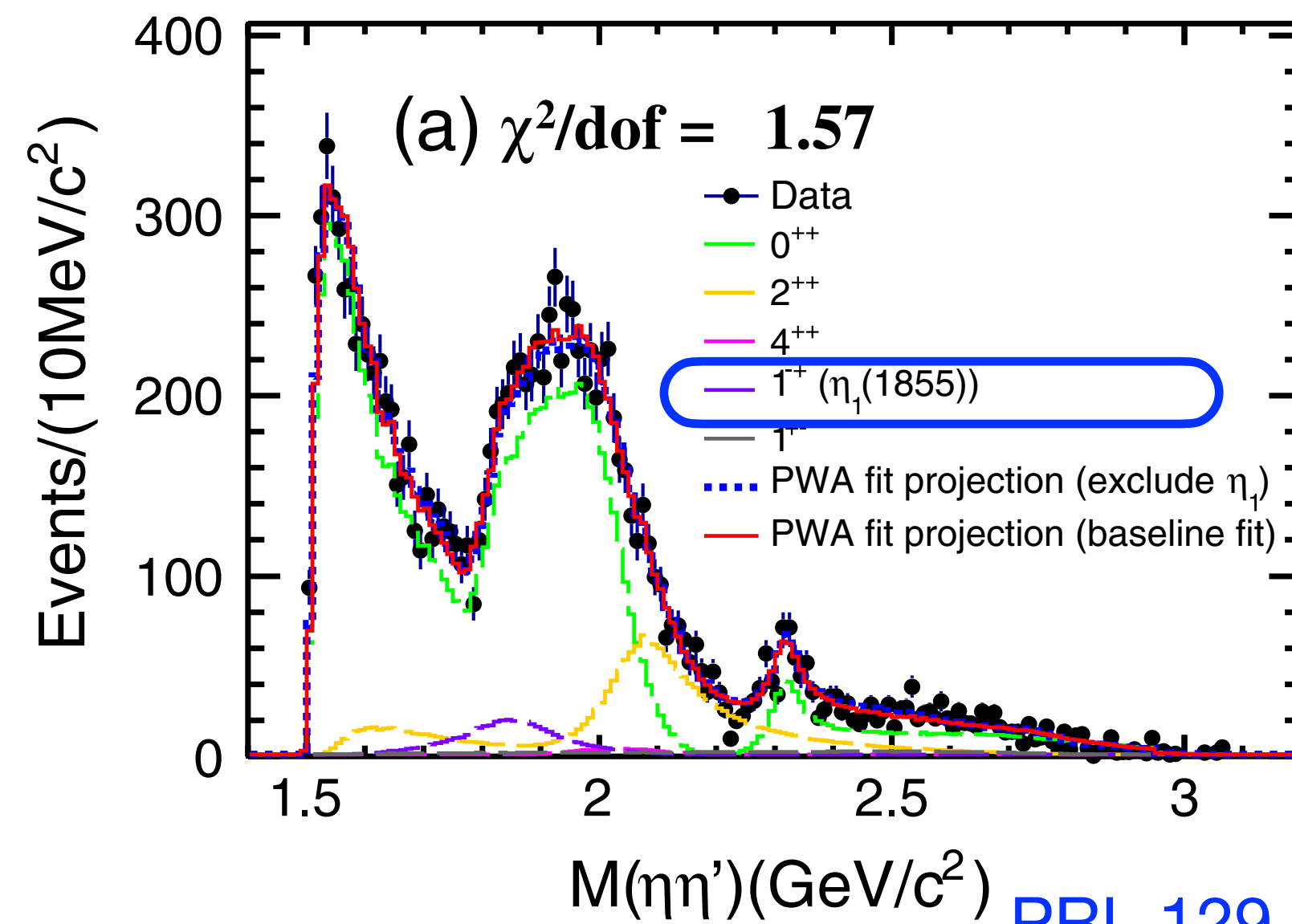
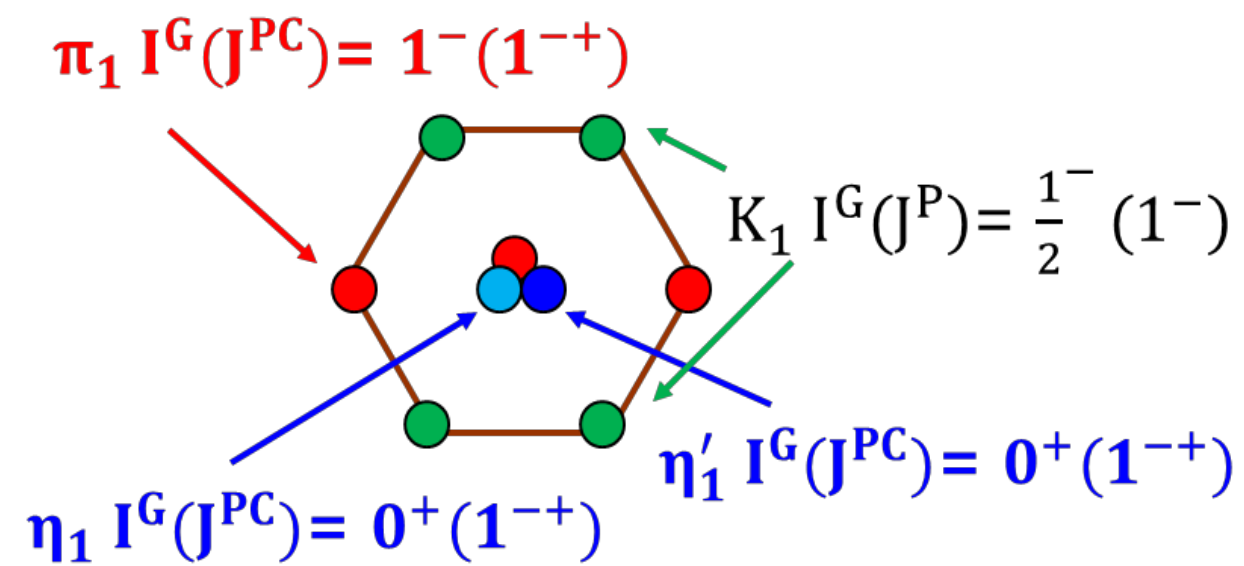
# Observation of Exotic $1^-+$ Isovector state $\pi(1600)$



- ◆ CLEO-c results: evidence of an exotic P-wave  $\eta'\pi$  amplitude with  $4\sigma$  and but no significant phase motion
- ◆ PWA in  $\psi' \rightarrow \gamma\chi_{c1}(\chi_{c1} \rightarrow \pi^+\pi^-\eta')$  with higher  $\psi'$  data sample @ BESIII:
  - ✦ **First observation of Exotic  $1^-+$  Isovector state  $\pi(1600)$  with a significance  $>10\sigma$  better than other  $J^{PC}$  assumption**
  - ✦ **The significance of phase motion is also greater than  $10\sigma$**

# Observation of An Exotic $1^-$ Isoscalar $\eta_1(1855)$

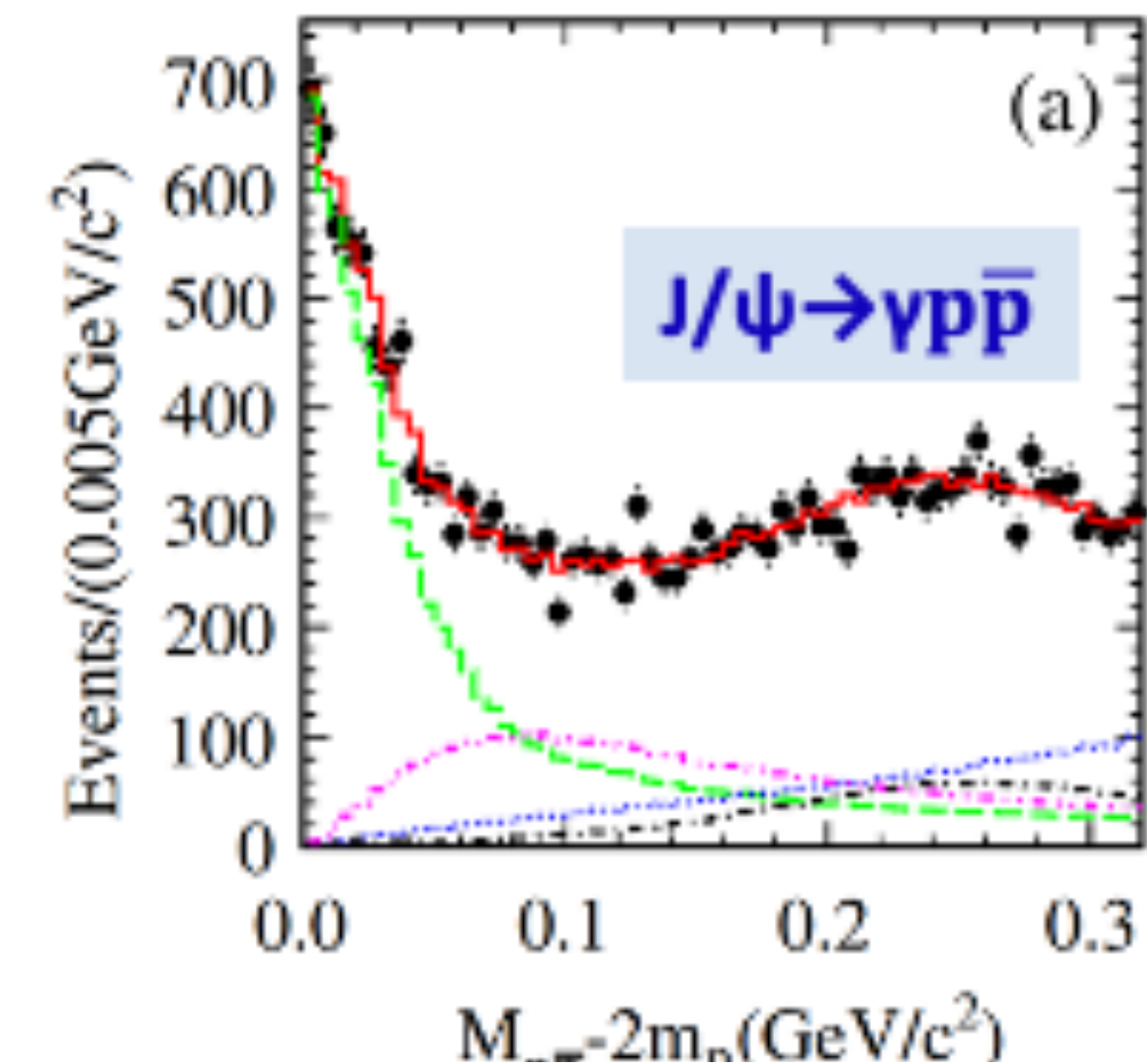
Isoscalar ( $1^-$ ) is critical to establish the nonet hybrid multiplet: partners for the Isovector ( $1^-$ )



[PRL 129 192002\(2022\)](#), [PRD 106 072012\(2022\)](#)

- ◆  $J/\psi \rightarrow \gamma \eta \eta'$  is a good channel for  $\eta_1(1^-)$  search
- ◆ **Observation of an isoscalar  $1^-$   $\eta_1(1855)$  in  $J/\psi \rightarrow \gamma \eta \eta'$  ( $>19\sigma$ )**
  - ◆ PWA: quasi two-body decay amplitudes in the sequential decay processes with covariant tensor formalism
  - ◆  $M = 1855 \pm 9^{+6}_{-1}$  MeV,  $\Gamma = 188 \pm 18^{+3}_{-8}$  MeV,  $B(J/\psi \rightarrow \gamma \eta_1(1855) \rightarrow \gamma \eta \eta') = (2.70 \pm 0.41^{+0.16}_{-0.35}) \times 10^{-6}$
- ◆ **Mass consistent with hybrid on LQCD, and more interpretations (KK Molecule/Tetraquark)**

# Observation of $X(p\bar{p})$ and $X(1835)$

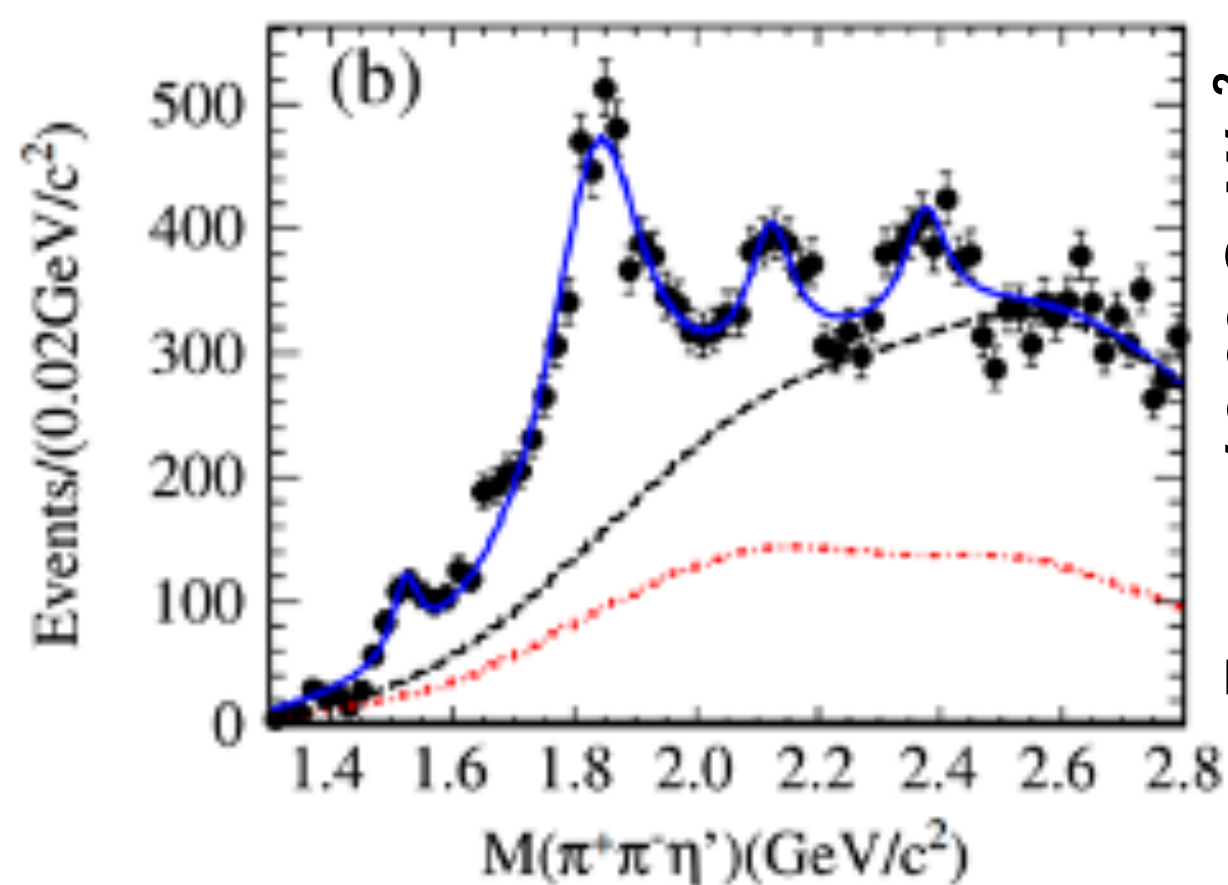


[PRL 108 \(2012\)112003](#)

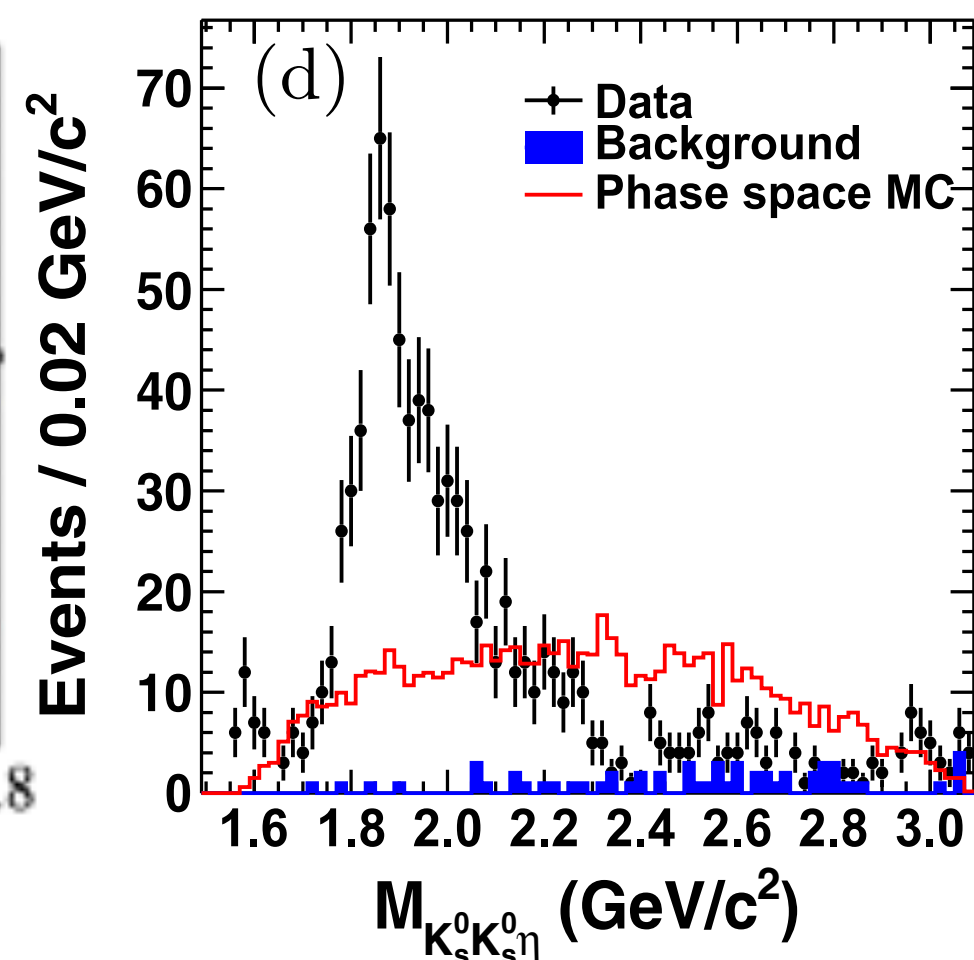
◆  $p\bar{p}$  mass threshold enhancement  $X(p\bar{p})$  :

- ◆ Discovered in  $J/\psi \rightarrow \gamma p\bar{p}$  by BESII in 2003 and confirmed by BESIII and CLEO-c
- ◆ Further determination of Spin-parity to be  $0^{-+}$
- ◆ No similar threshold structure in other channels  $\rightarrow$  It can not be pure FSI effect

$$M = 1832^{+19}_{-5} + {}^{+18}_{-17} \pm 19 \text{ MeV}/c^2, \quad \Gamma = 13 \pm 19 \text{ MeV}/c^2 (< 76 \text{ MeV}/c^2 @ 90\% \text{ C.L.})$$



[PRL 106 \(2011\)072002](#)



[PRL 115 091803](#)

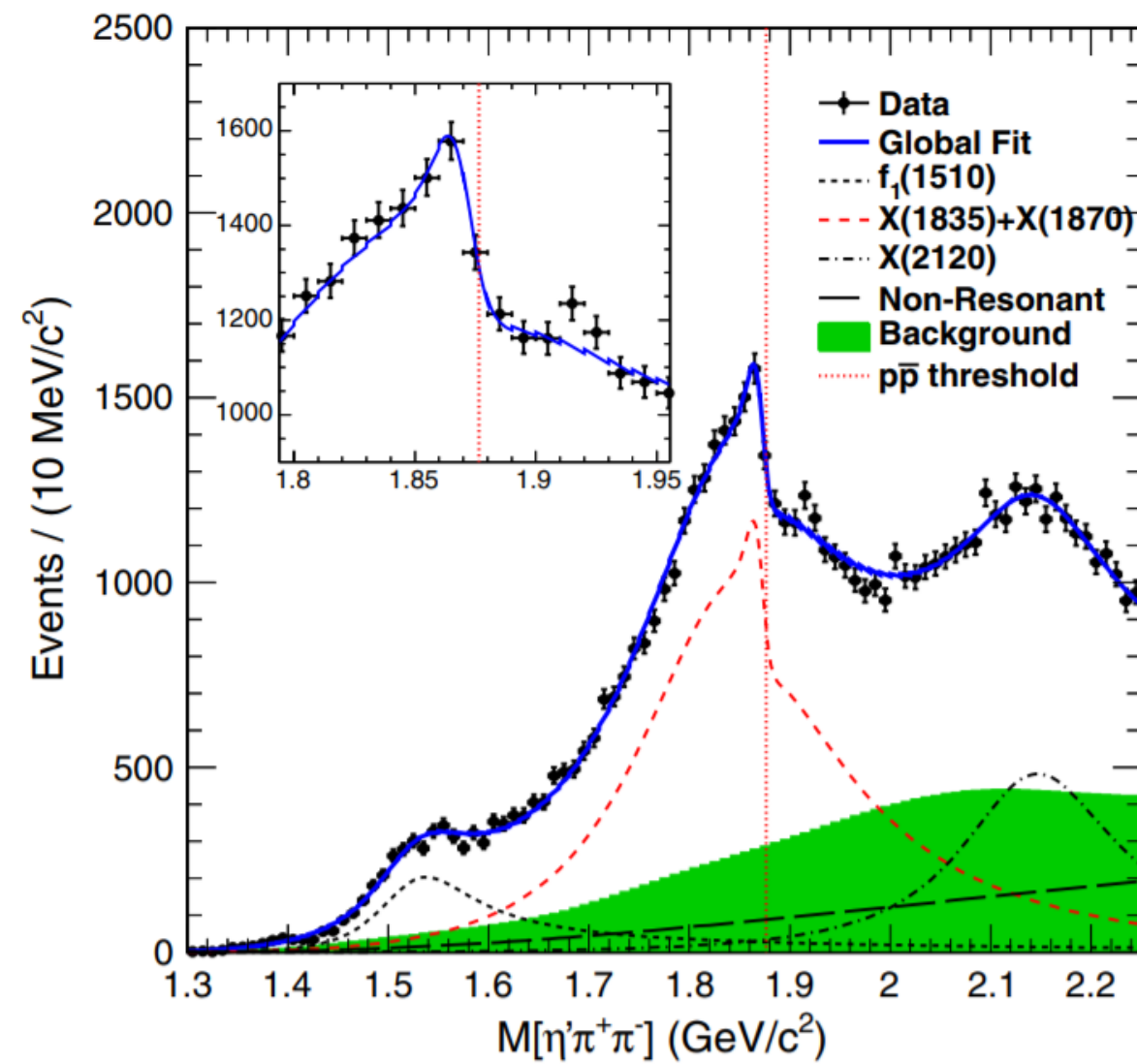
◆  $X(1835)$  :

- ◆ Discovered by BESII and confirmed by BESIII in  $J/\psi \rightarrow \gamma \pi \pi \eta'$
- ◆ Determination of Spin-parity to be  $0^{-+}$  in  $J/\psi \rightarrow \gamma K_s K_s \eta$

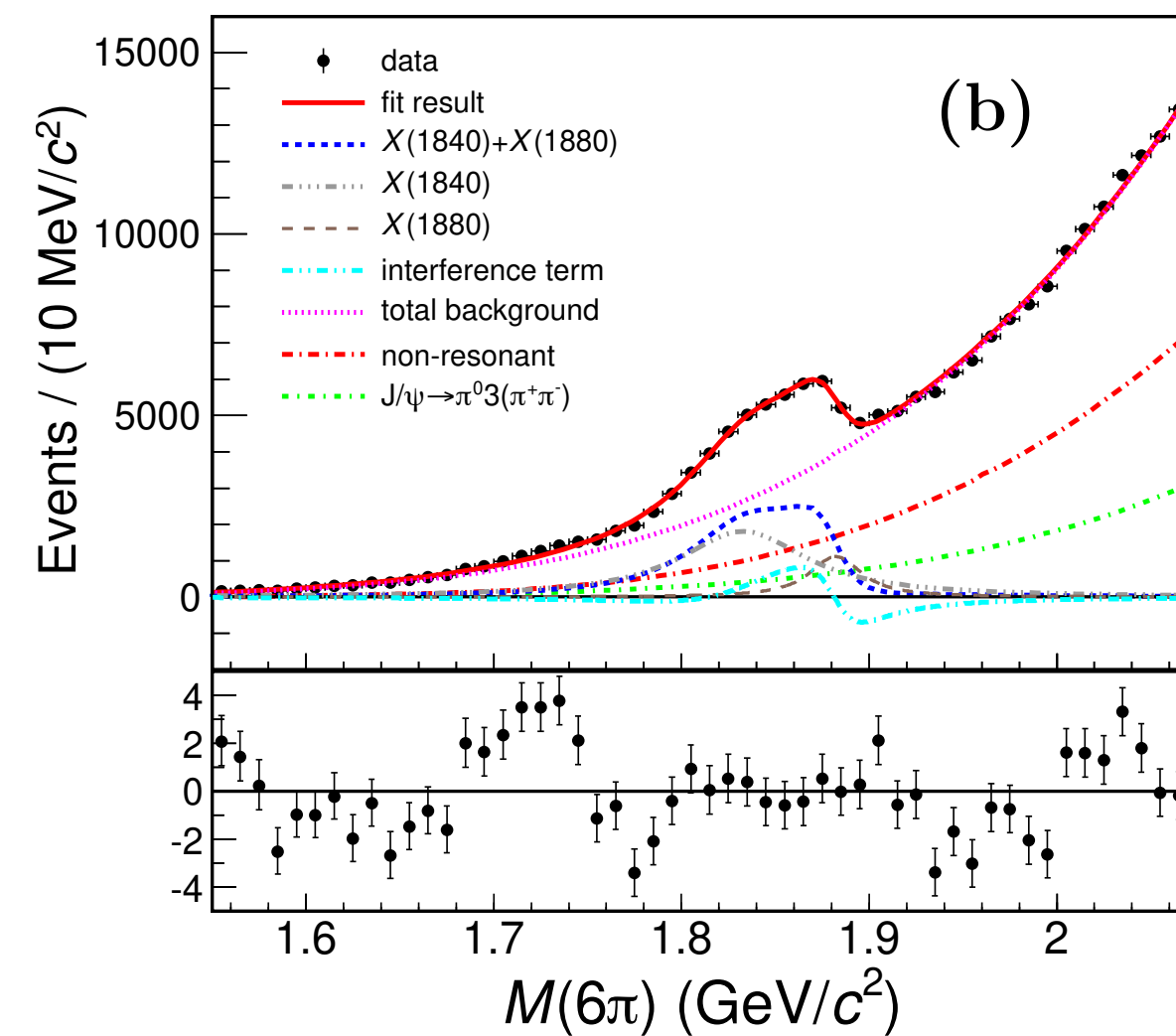
$$M = 1844 \pm 9^{+16}_{-25} \text{ MeV}/c^2$$

$$\Gamma = 192^{+20}_{-17} + {}^{+62}_{-43} \text{ MeV}/c^2$$

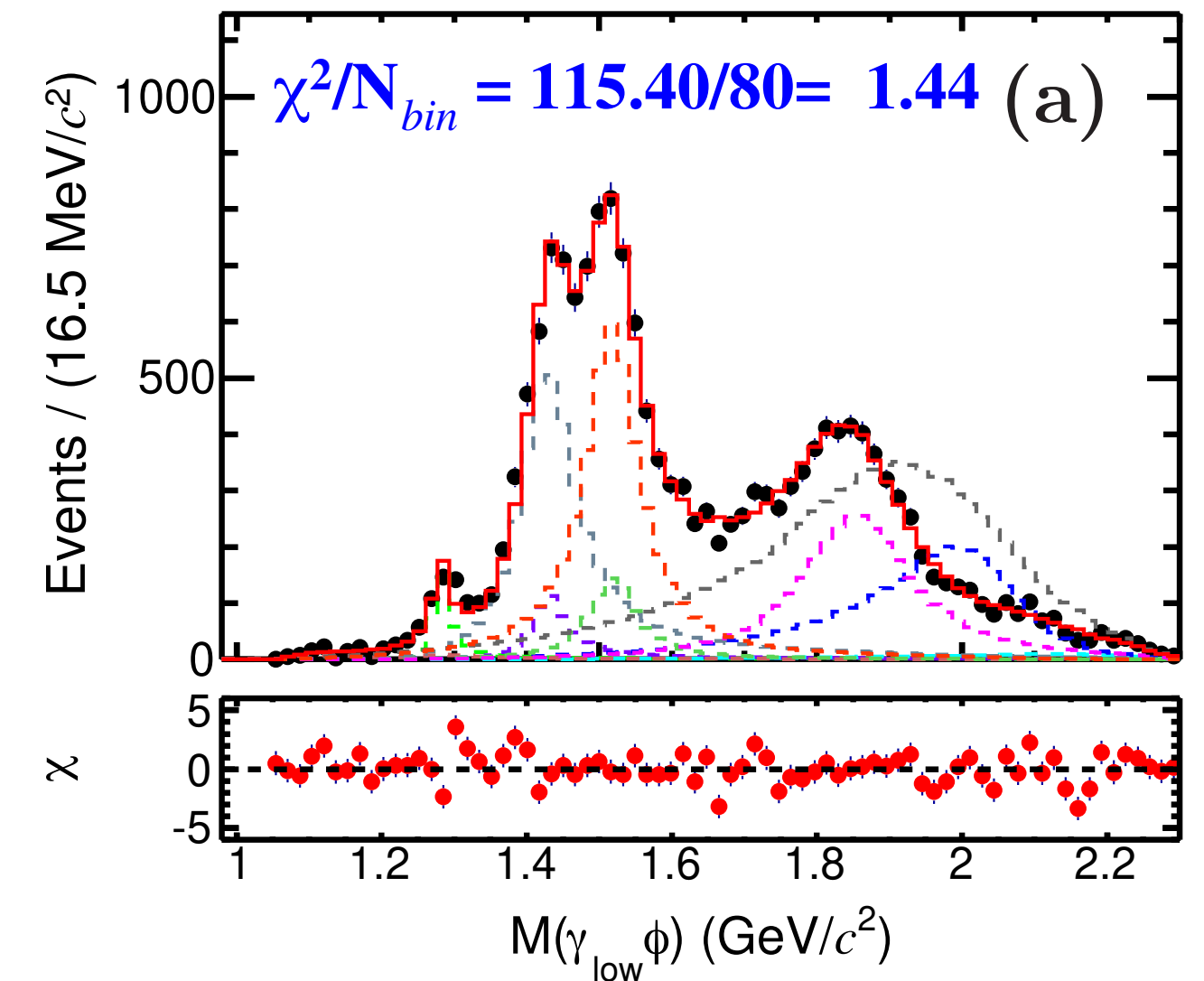
# Direct link between the $X(p\bar{p})$ and $X(1835)$



[PRL 117, 042002](#)



[PRL 132 \(2024\) 151901](#)



[arxiv:2401.00918](#)

- ◆ **Anomalous  $\pi\pi\eta'$  line shape near  $M_{p\bar{p}}$  threshold: first establish the direct link between the  $X(1835)$  and  $X(p\bar{p})$** 
  - ◆ Two models (Flatte formula/2-resonance) can fit data well: **interpretations of  $p\bar{p}$  mass threshold as a molecule state or a bound state**
- ◆ **Anomalous shape observed in  $J/\psi \rightarrow \gamma 3(\pi\pi)$  near  $M_{p\bar{p}}$  threshold**
  - ◆ **Two structures of  $X(1840)$  and  $X(1880)$  give a good description on data: interpretation of a bound state**
- ◆ **Mass and width of the  $X(1835)$  in  $J/\psi \rightarrow \gamma\gamma\phi$  are consistent with those in  $J/\psi \rightarrow \gamma K_s K_s \eta$ :**
  - ◆  **$X(1835)$  contains a sizable  $s\bar{s}$  component**

# Summary

- ◆ A set of interesting and important results from the light hadron spectroscopy achieved:
  - ◆ **Discovery of a glueball-like particle: X(2370)**
  - ◆ Strong correlation between the X(1835) and  $M_{p\bar{p}}$  threshold enhancement. A molecule state or a bound state?
  - ◆ Observation of An Exotic  $1^{-+}$  Isoscalar state  $\eta_1(1855)$  and Isovector state  $\pi(1600)$
  - ◆ ...
- ◆ With the more data, the more extensive and intensive investigation are ongoing, looking forward to new results in the near future.







# Interpretation

	X(2370)	$\eta_c$	Interpretation on the X(2370)
$f_0(980)\eta'$	✓	✓	Disfavors $q\bar{q}$ meson with pure $u\bar{u}/d\bar{d}$ component
$f_0(980)\eta$	Suppressed	Suppressed	Disfavors $q\bar{q}$ meson with pure $s\bar{s}$ component
$f_0(1500)\eta$	✓	✓	Disfavors $q\bar{q}$ meson with pure $s\bar{s}$ component

◆ **The X(2370) decay properties observed:** **disfavor the interpretation of  $q\bar{q}$  meson**

- ◆ Observed decay modes ( $\eta_c$  dominant decays) and suppressed decay modes are consistent between the X(2370) and  $\eta_c$
- ◆ **A good agreement with the glueball interpretation**

◆ **The X(2370) production properties observed:**

- ◆ richly produced in  $J/\psi$  radiative decays as the glueball expectation

◆ **Mass, spin-parity:** consistent with  $0^{-+}$  glueball prediction

In the mass region larger than 2GeV, the only particle X(2370) for the  $0^{-+}$  glueball candidate in  $J/\psi$  radiative decays and five golden decay modes ( $\pi\pi\eta'$ ,  $K\bar{K}\eta'$ ,  $K\bar{K}\pi$ ,  $\pi\pi\eta$ ,  $K\bar{K}\eta$ )

