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ECFA meeting on e+e- to ZH angular measurements, 17.6.2024

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Can BSM physics induce larger CPV Higgs couplings?

- CP violation in Higgs couplings introduced via dimension-six operators:
 - Gauge boson interactions: $\Phi^{\dagger} \Phi W_{\mu\nu} \widetilde{W}^{\mu\nu}$, $\Phi^{\dagger} \Phi B_{\mu\nu} \widetilde{B}^{\mu\nu}$, $\Phi^{\dagger} \Phi W_{\mu\nu} \widetilde{B}^{\mu\nu}$, $\Phi^{\dagger} \Phi G_{\mu\nu} \widetilde{G}^{\mu\nu}$
 - Fermion interactions: $\Phi^{\dagger} \Phi(Qu \tilde{\Phi}), \Phi^{\dagger} \Phi(Qd \Phi), \Phi^{\dagger} \Phi(Qe \Phi)$ with complex Wilson coefficients

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Rewrite:
$$\mathcal{L}_{\text{yuk}} = -\sum_{f=u,d,c,s,t,b,e,\mu,\tau} \frac{y_f^{\text{SM}}}{\sqrt{2}} \bar{f} \left(c_f + i\gamma_5 \tilde{c}_f \right) fH,$$

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- All of them are independent (apart from RGE mixing)!
- Also independent from non-CPV Higgs coupling modifications.

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CPV in HVV via CPV in Hff I

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- consider CPV top-Yukawa coupling: $\mathcal{L}_{top} = \frac{y_t^{SM}}{\sqrt{2}} \bar{t} (c_t + i\gamma_5 \tilde{c}_t) tH$
- This coupling will directly affect $\bar{t}tH$ but also induce Higgs–gluon interaction:

$$\mathcal{L}_{Hgg} = -\frac{1}{4\nu} H \left(-\frac{g_s^2}{12\pi^2} c_g G^a_{\mu\nu} G^{a,\mu\nu} + \frac{g_s^2}{8\pi^2} \tilde{c}_g G^a_{\mu\nu} \; \tilde{G}^{a,\mu\nu} \right)$$

with $c_g = c_t$ and $\tilde{c}_g = \tilde{c}_t$ in heavy-top limit.

CPV in HVV via CPV in Hff II

[HB et al., 2309.03146]



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Naïve estimate for weak gauge-boson couplings:

- CPV in *HVV* couplings suppressed by $\frac{g^2}{16\pi^2}$ with respect to *Hff* couplings.
- *HWW*: suppression by ~ 0.003
- *HZZ*: suppression by ~ 0.001

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 - Interplay with direct searches for BSM particles.
 - CPV couplings of BSM particles can provide additional CP sources.

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Perform Higgs CP measurements without assuming that other Higgs couplings are at their SM values!

- Intricate interplay between $h_{\rm 125}$ measurements, direct searches, flavor constraints, EWPOs, EDM .

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Collider measurements are important since they allow to disentangle different couplings/particles!





Interplay with direct searches

[Biekötter et al., 2403.02425]



All points allowed by EDM measurements.

Left: points allowed without considering direct searches.

Right: points allowed with considering direct searches.

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Impact of LHC measurements

[Biekötter et al., 2403.02425]



Left: points allowed without LHC $H \rightarrow \tau \tau$ CP measurement.

Right: points allowed with LHC $H \rightarrow \tau\tau$ CP measurement [CMS, 2110.04836].

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Thanks for your attention!

Appendix



Fermions



- How can we constrain CP-violating couplings at the LHC?
 - Direct constraints: CP-odd observables.
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General amplitude structure for CP measurements:

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Higgs CP has become a testing ground for new analysis ideas/methods!

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Complementarity with EDM constraints

- Several EDMs are sensitive to CP violation in the Higgs sector via 2L Bar-Zee diagrams.
- Bounds strongly depend on assumptions about
 - first-generation Yukawa coupling,
 - absence of other CP-violating BSM physics.
- Significant increase in precision expected within the next years! (see e.g. [Snowmass report, 2203.08103])
- Evaluation of NLO corrections will become necessary. (see e.g. [Brod et al., 2306.12478])

