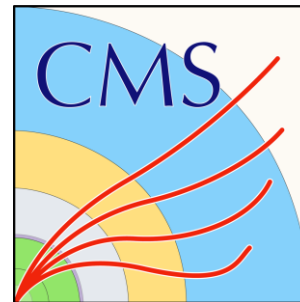
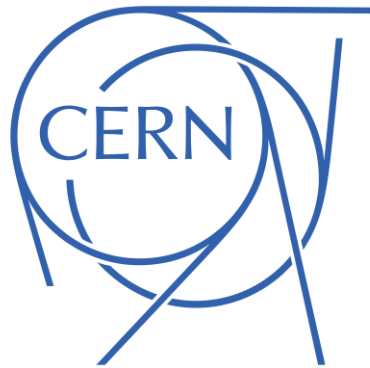


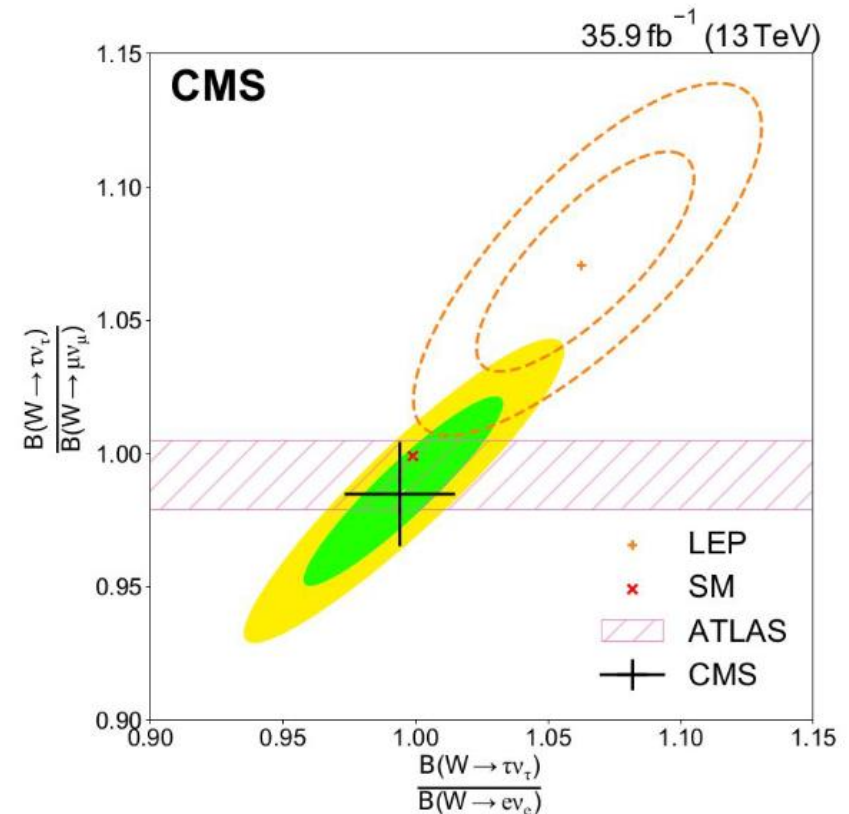
# LFU study in $t\bar{t}b\bar{b}$ decays in $pp$ collisions at the CMS detector with $\sqrt{s} = 13 \text{ TeV}$



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University of Latvia<sup>1</sup>, Riga Technical University<sup>2</sup>

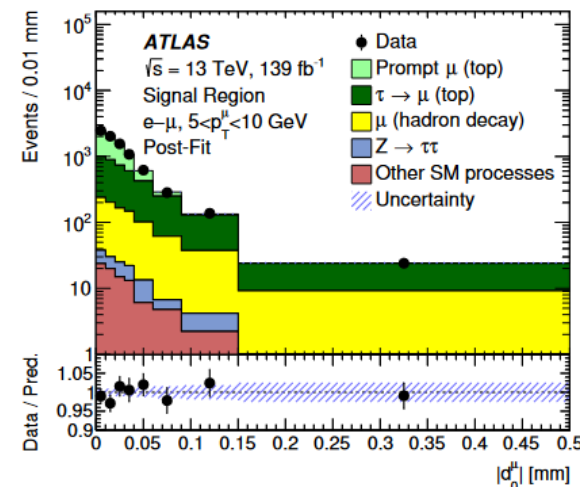
# Analysis motivation

- LFU measurements provide a simple way of testing one of the fundamental axioms of the SM.
- Earlier LEP measurements showed slight tension with the SM predictions [1].
- Later CMS and ATLAS measurements moved the results much closer to and in agreement with the the SM prediction [2][3].
- Measuring the LFU with increasing precision helps us to test the SM prediction with higher and higher confidence.

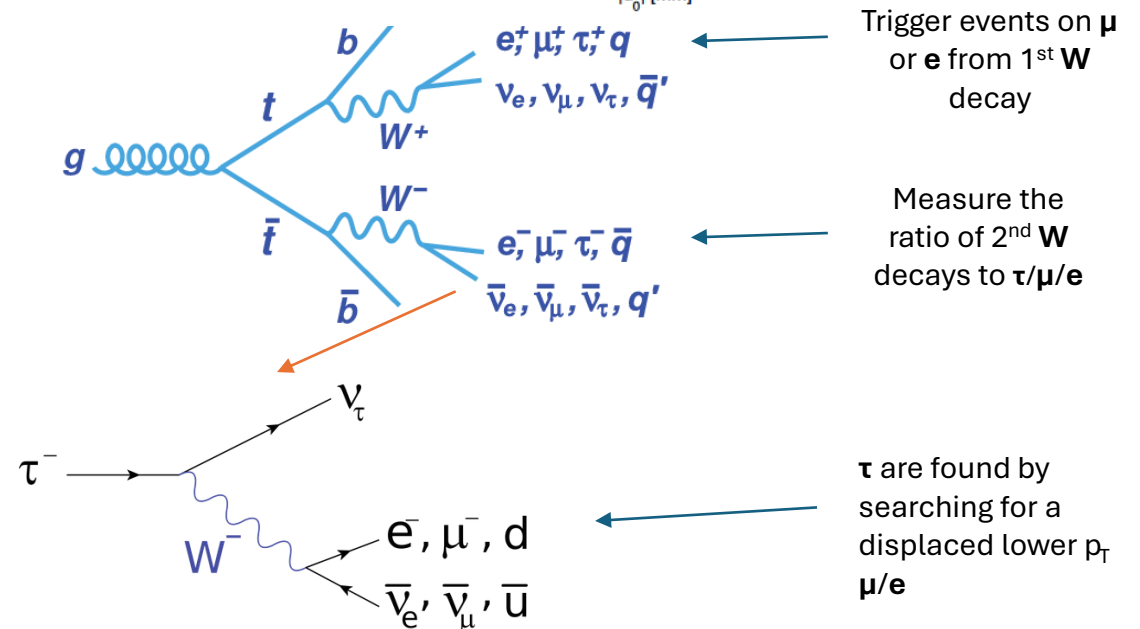


# Analysis approach

- Measuring the LFU  $R(\tau/\mu)$  and  $R(\tau/e)$  in the di-leptonic  $t\bar{t}$  decays.
- Measurement is done in the leptonic decay channels of the  $\tau$  lepton.
- Estimate the  $R(\tau/\mu)$  and  $R(\tau/e)$  using 2-D likelihood fit in lepton  $d_{xy}$  and  $p_T$  distributions to disentangle the prompt leptons (from  $W$ ) and non-prompt leptons (from  $\tau$  decay).
- Analysis is highly sensitive to lepton  $d_{xy}$ , so it needs correct treatment.
- Background contribution estimates are important for a correct prediction of the  $R(\tau/\mu)$  and  $R(\tau/e)$ .
- Result in  $R(\tau \rightarrow e|\mu / e)$  and  $R(\tau \rightarrow e|\mu / \mu)$  *triggered* either by single electron or muon from the other  $W$  boson decay. So 4 resulting channels –  $e\bar{e}, \mu\bar{\mu}, e\bar{\mu}$  and  $\mu\bar{e}$ .

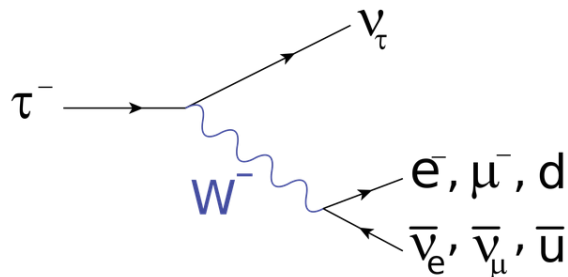


Result from a similar analysis done in ATLAS [\[link\]](#). Goal is to get such result both for  $R(\tau/\mu)$  and  $R(\tau/e)$ .

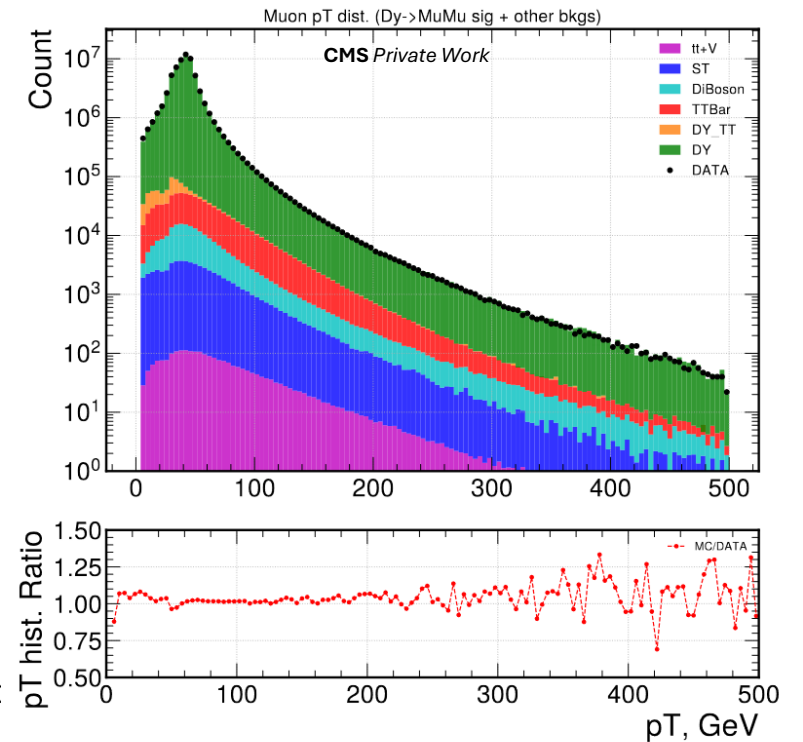
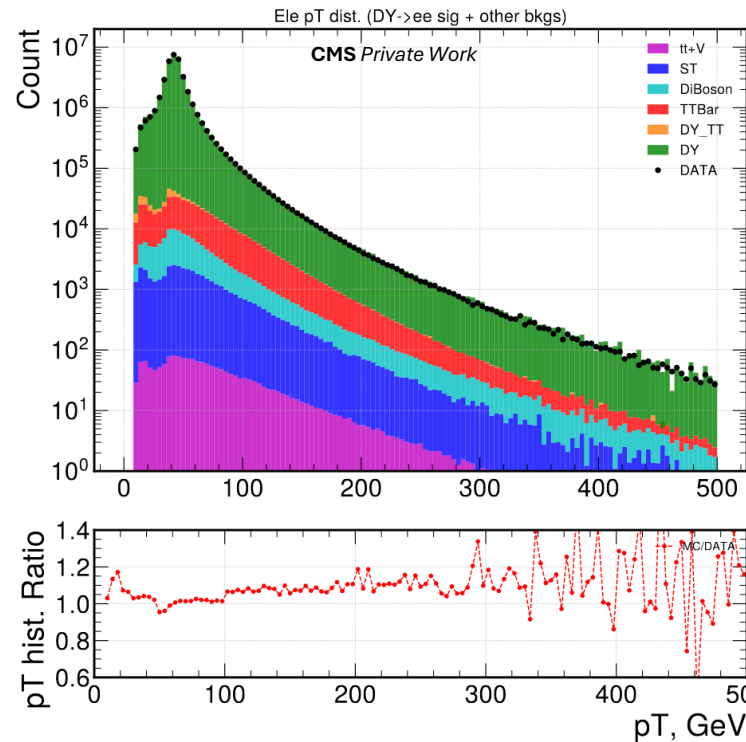


# Analysis activities

- Important aspect of this analysis is the fact that the identification of  $\tau$  lepton is done by searching for more displaced lower- $p_T$  lepton.
- This is a challenging aspect since in  $\tau$  leptonic decays two additional neutrinos are created.
- This puts a special interest of pushing the non-triggered lepton's  $p_T$  cut as low as possible to acquire more signal statistics.
- Usually, this means going below the object group's officially provided SFs  $p_T$  lower bounds and makes a need for manual SF calculation present.



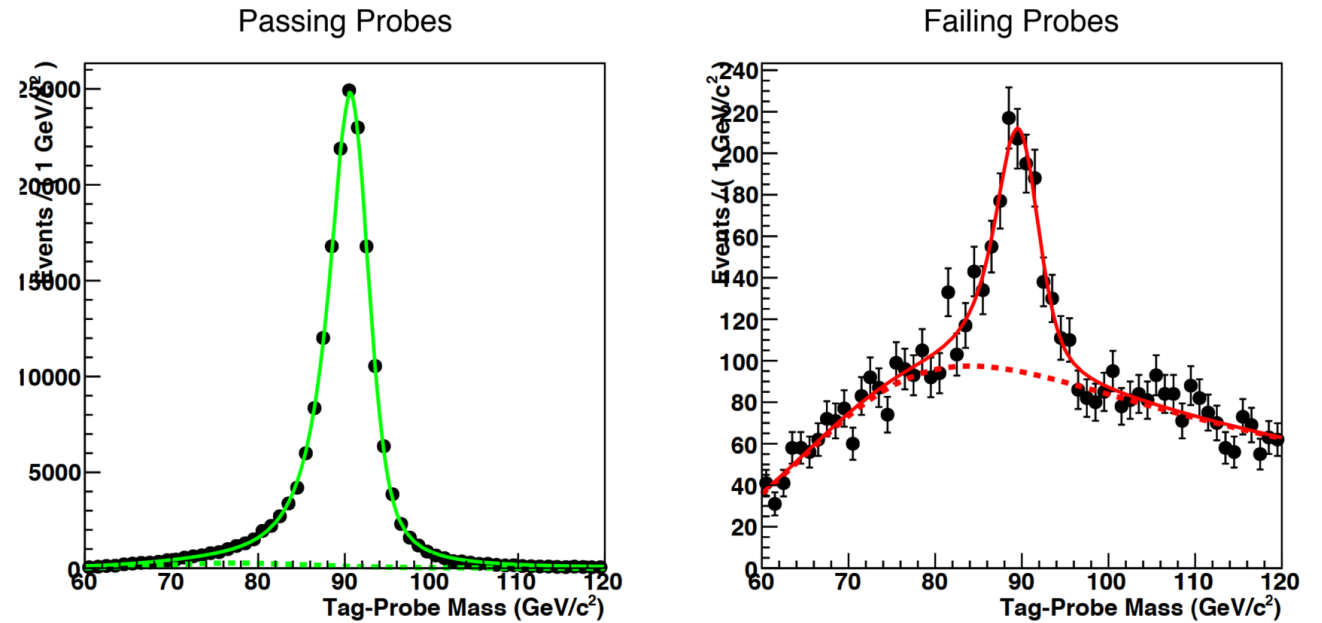
$\tau$  leptonic decay  
Feynman diagram



$p_T$  distributions of electrons (*left*) and muons (*right*) in di-leptonic decays triggered by a single lepton trigger. Leptons from  $\tau$  decay (*orange*) are at the low- $p_T$  part of the distribution.

# Analysis activities – Scale Factors (SFs), Tag&Probe (TnP) measurement

- Lepton SF measurements are done using Tag&Probe method.
- In this method a well know resonance is used (Z,J/ψ) and its leptonic decays are exploited.
- The pair of leptons is selected by requiring tight cuts on tag lepton and afterwards an efficiency is measured using probe lepton for a specific selection criteria. This is done both in DATA and MC.
- The efficiency is measured by counting how many probe leptons passed the selection criteria.
- Usually, the passing and failing probe count is acquired using fits, to get rid of any background contributions.
- In the end, the SF is calculated by dividing the acquired DATA and MC efficiencies.



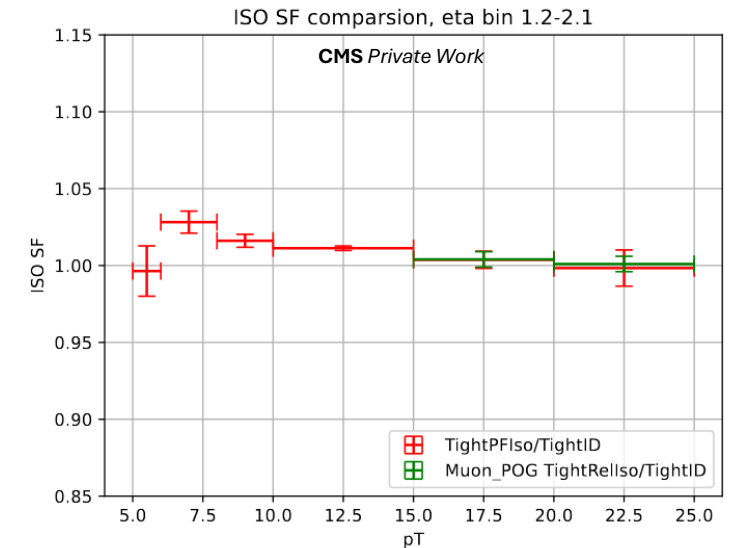
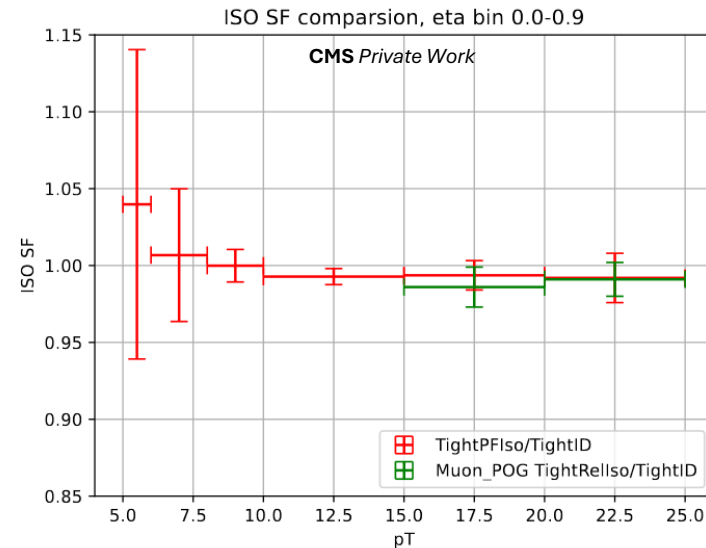
Example for passing and failing probe fits in Tag&Probe method.

$$\epsilon_{DATA \text{ or } MC} = \frac{N_{pass}}{N_{pass} + N_{fail}}$$

$$Scale \ Factor = \frac{\epsilon_{DATA}}{\epsilon_{MC}}$$

# Analysis activities – SFs, low- $p_T$ results

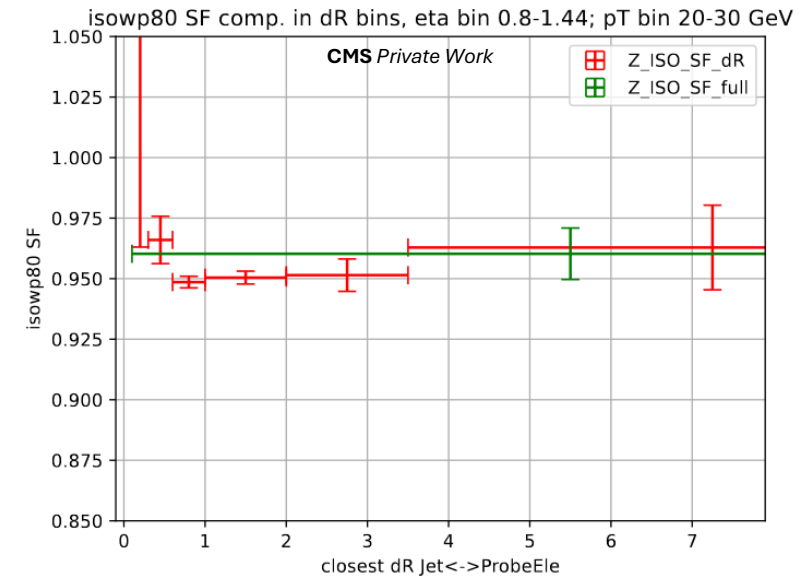
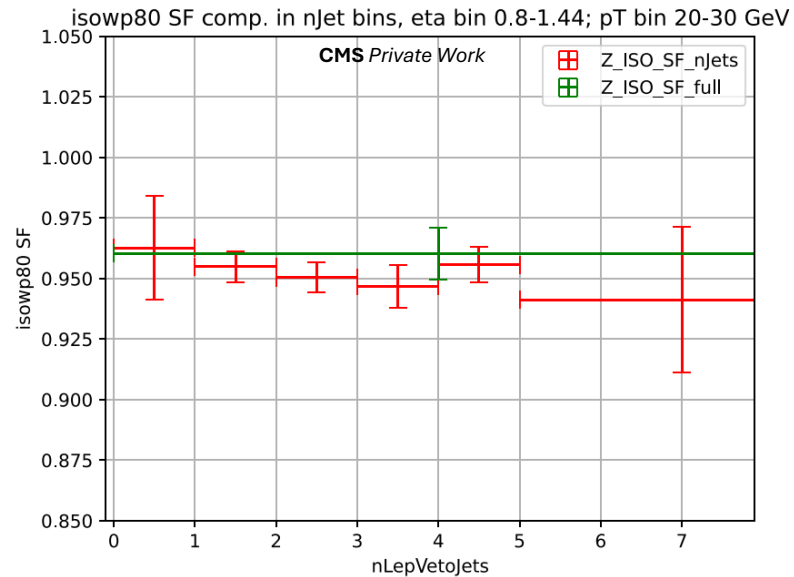
- Official muon reconstruction (RECO) and identification (ID) SFs, are provided without any systematical uncertainties below  $p_T$  of 15 GeV.
- A calculation was done to recalculate the SFs with full uncertainties included.
- There are no isolation (ISO) SFs provided below  $p_T$  of 15 GeV.
- A calculation was done on  $Z \rightarrow \mu\mu$  events with full uncertainties. (Needs Extra discussion with Muon Object group's convenors)
- Additional investigations using  $J/\psi$  resonance for low- $p_T$  SF calculation was done. Particularly, using the Bparking dataset.



Example of muon low- $p_T$  ISO SFs in one barrel and one endcap  $|\eta|$  bin.

# Analysis activities – ISO SFs, extra uncertainty

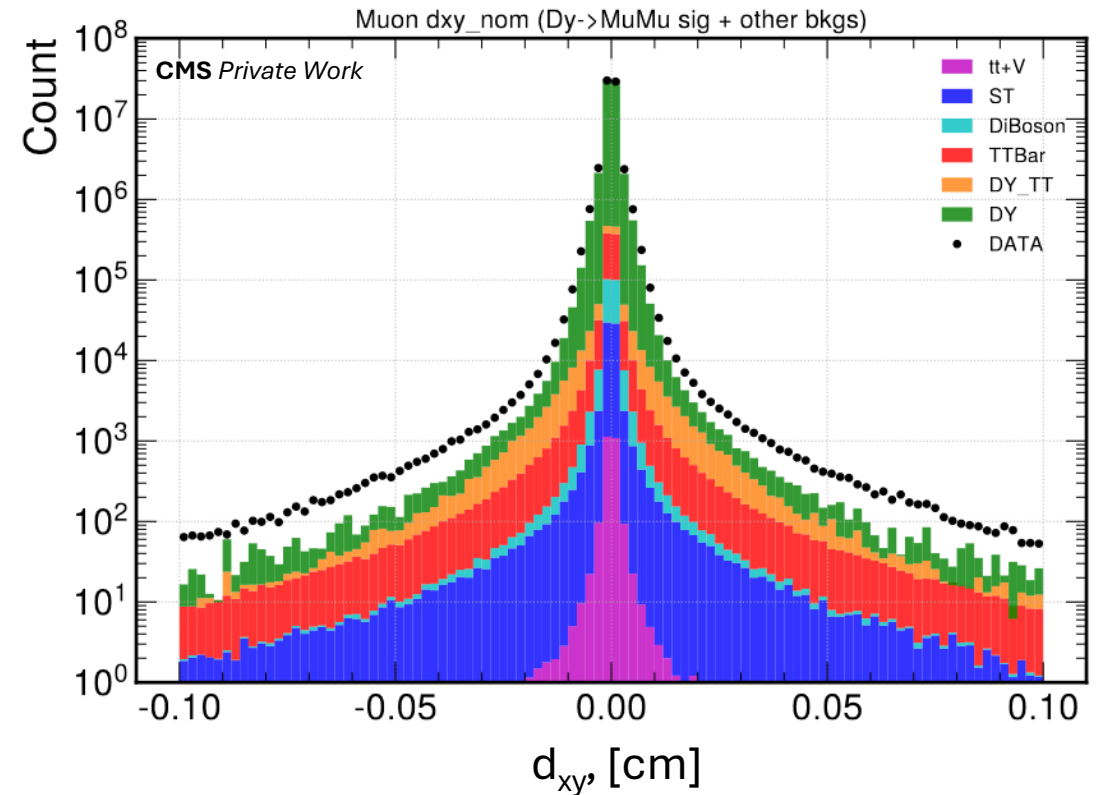
- All centrally provided SFs are calculated from Drell-Yan process resonances, which is a rather clean event topology.
- A general recommendation exists to add extra uncertainty to lepton ISO SFs when they are applied to  $t\bar{t}$  processes.
- This additional systematic uncertainty would limit the precision of the analysis.
- Additional studies of SFs dependence on  $n_{\text{Jets}}$  and  $dR$  to the closest jet were done to see if there is any clear dependence.
- Goal of these studies is to forgo the application of this extra uncertainty.
- Electron object group have agreed to drop this, now in discussion with the muon object group.



Example of electron ID+ISO SF trend in  $n_{\text{Jet}}$  (left) and  $dR$  (right) bins (in a particular  $p_T$  and  $|\eta|$  bin).

# Analysis activities – lepton $d_{xy}$ corrections, general problem

- $d_{xy}$  parameter is of paramount importance in this analysis.
- A quick look at the nominal  $d_{xy}$  distributions in DATA and MC, shows a clear discrepancy between the two distributions.
- This is due to some extrapolations used in MC and usage of a limited precision magnetic field map in the reconstruction process.
- Before any measurement can be done, the MC  $d_{xy}$  distributions must be corrected so that it would match the distribution observed in DATA.

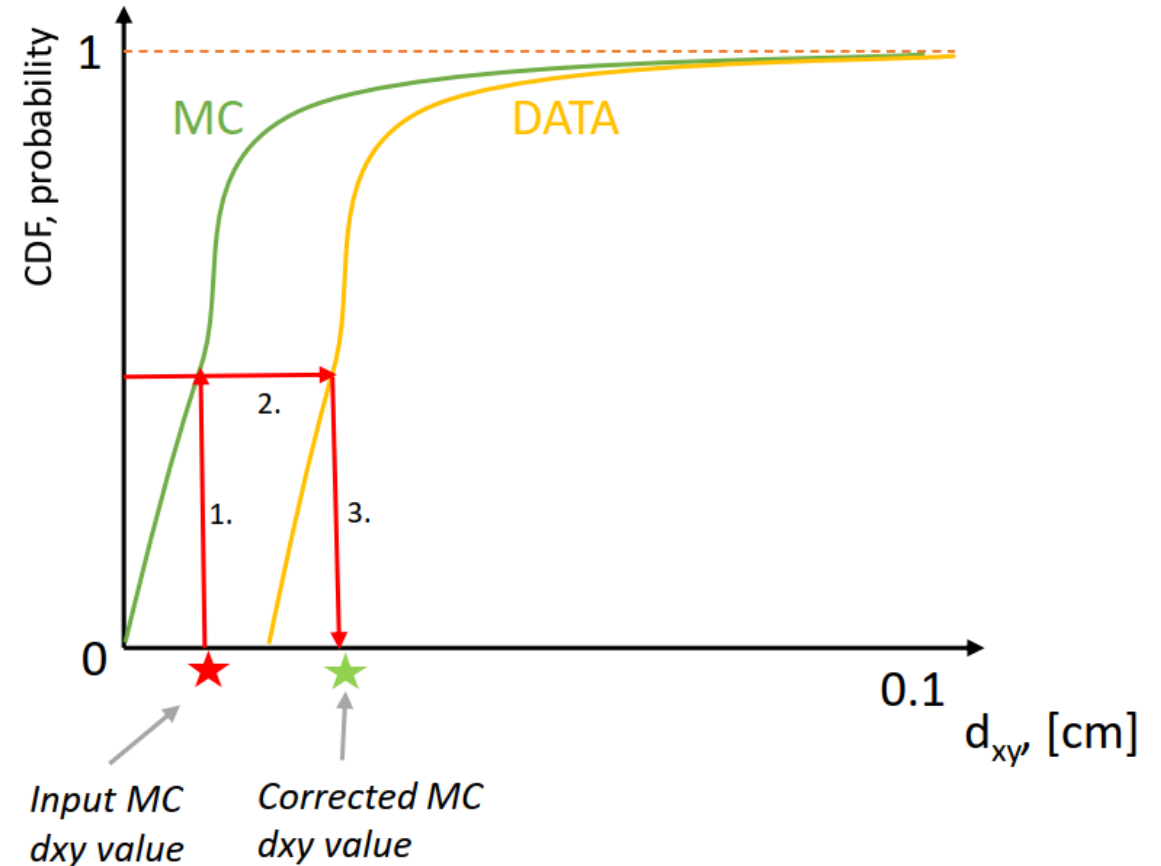


Nominal muon  $d_{xy}$  distribution for DATA and MC. A clear mismatch can be seen.



# Analysis activities – lepton $d_{xy}$ corrections, quantile corrections

- To correct the MC  $d_{xy}$  distributions a ‘*quantile correction*’ method is used.
- Method can be explained in a few steps:
  - Acquire the **cumulative distribution function** (CDF) of the DATA and MC distributions.
  - Calculate the amount of shift needed for MC  $d_{xy}$  values, so that the CDF of MC  $d_{xy}$  distribution would match the one from DATA.
  - The calculated shift of  $d_{xy}$  values for MC is the correction that needs to be applied to all the MC points.
- Such corrections are calculated in various  $p_T/\eta$  bins to account for detector geometry and kinematical effects.



Schematic view of the quantile corrections method (Differences between MC and DATA CDFs are exaggerated for illustrative purpose)

# Analysis activities – lepton $d_{xy}$ corrections, quantile corrections

How to calculate the CDF of the  $d_{xy}$  distribution?



- **Binned approach:**
  - *CDF calculation:*
    - Calculate the CDF from the histogram bins of the  $d_{xy}$  distribution.
  - *Limitations/problems:*
    - Needs a fine binning
    - Limited events in the tail region can make the CDF 'jumpy' (multiple  $d_{xy}$  value bins can have the same CDF value).
  - *Uncertainties:*
    - Use the Poissonian uncertainty for histogram bins as a statistical uncertainty and different bin count as a systematical uncertainty.

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- **Full fit approach:**

- *CDF calculation:*
  - Fit the whole  $d_{xy}$  distribution and calculate the CDF for the fitted function.
  - Improves the “smoothness” in the tail region.
- *Limitations/problems:*
  - Problematic to fit the peak and tails perfectly at the same time.
- *Uncertainties:*
  - The fit parameter uncertainties for a statistical uncertainty and different fit function for a systematical uncertainty.

# Analysis activities – lepton $d_{xy}$ corrections, quantile corrections

How to calculate the CDF of the  $d_{xy}$  distribution?

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• **Full fit approach:**

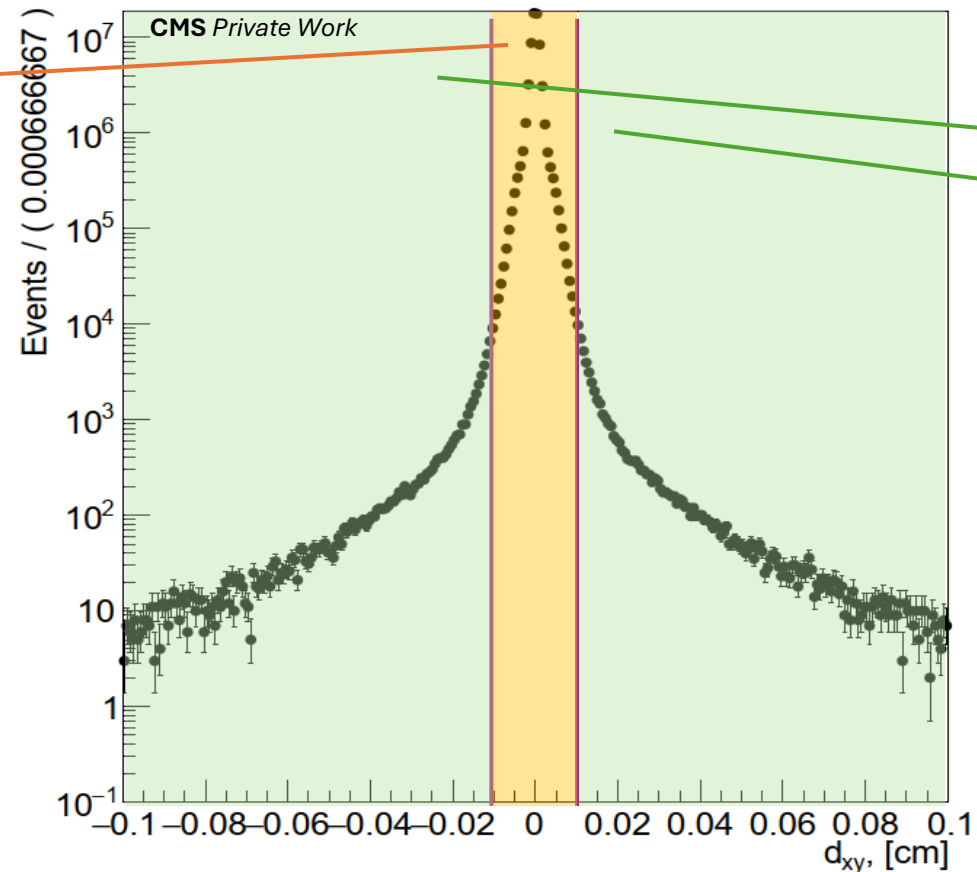
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- *Uncertainties:*
  - The fit parameter uncertainties for a statistical uncertainty and different fit function for a systematical uncertainty

• **Modified approach: (chosen way)**

- *CDF calculation:*
  - Use the binned approach at the center of the distribution.
  - Use fits in the tail part of the distribution.
  - Combine the results to from the CDF of the  $d_{xy}$  distribution.
  - Takes the best parts of each method.
- *Limitations/problems:*
  - Combination of the two methods.
- *Uncertainties:*
  - Combination of binned and pure fit method uncertainty estimation.

# $d_{xy}$ correction methodology – calculating correction

- Applying the modified method for CDF calculation to the lepton  $d_{xy}$  distribution  
dxy distrib. logY

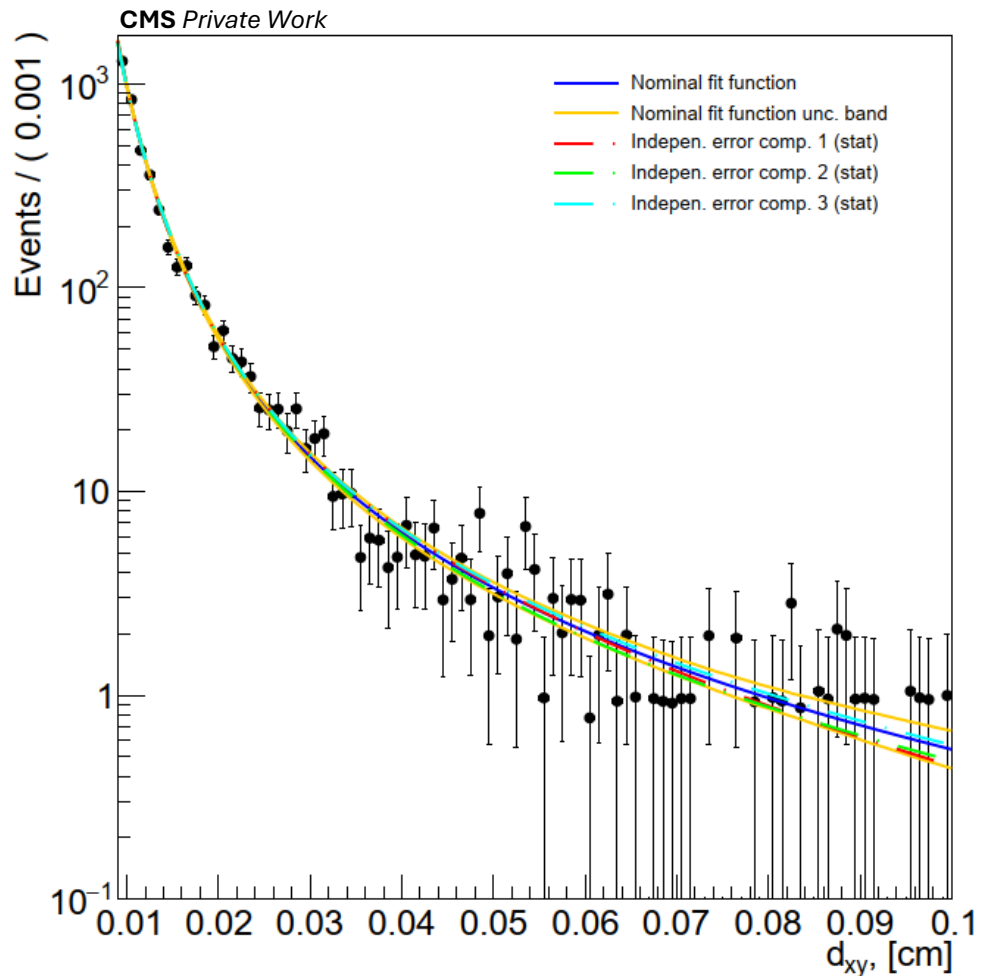


- In the central part of the distribution the binned approach is used for the CDF calculation.
- $\text{abs}(d_{xy}) [0.0-0.01] \text{ cm}$**
- Just count the event count in the histogram bins.
- For CDF calculations the absolute values and distributions of  $d_{xy}$  are used.

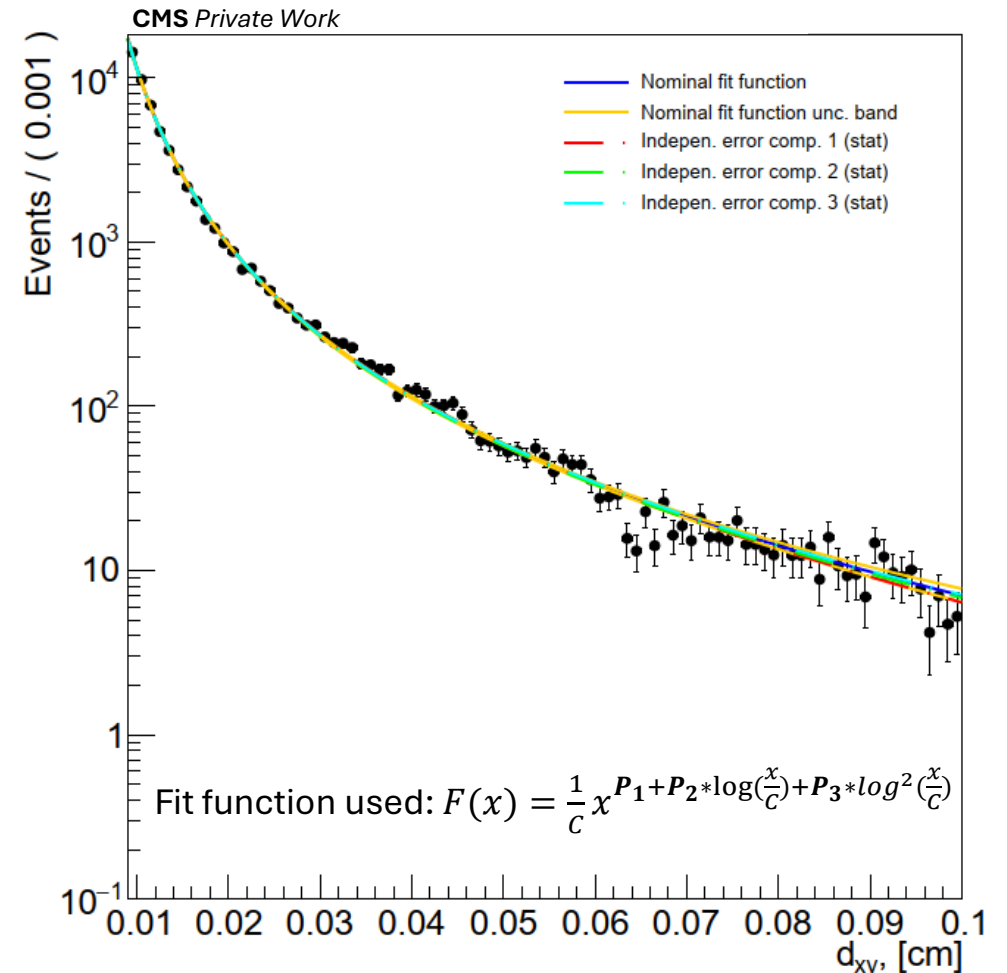
- In the tail part of the distribution the fit approach is used for the CDF calculation.
- $\text{abs}(d_{xy}) [0.01-0.1] \text{ cm}$**
- The event count is estimated from the fitted function.
- For CDF calculations the absolute values and distributions of  $d_{xy}$  are used.

# Analysis activities – lepton $d_{xy}$ corrections, MC fit example

- Example MC  $d_{xy}$  distribution tail fit for Muons:

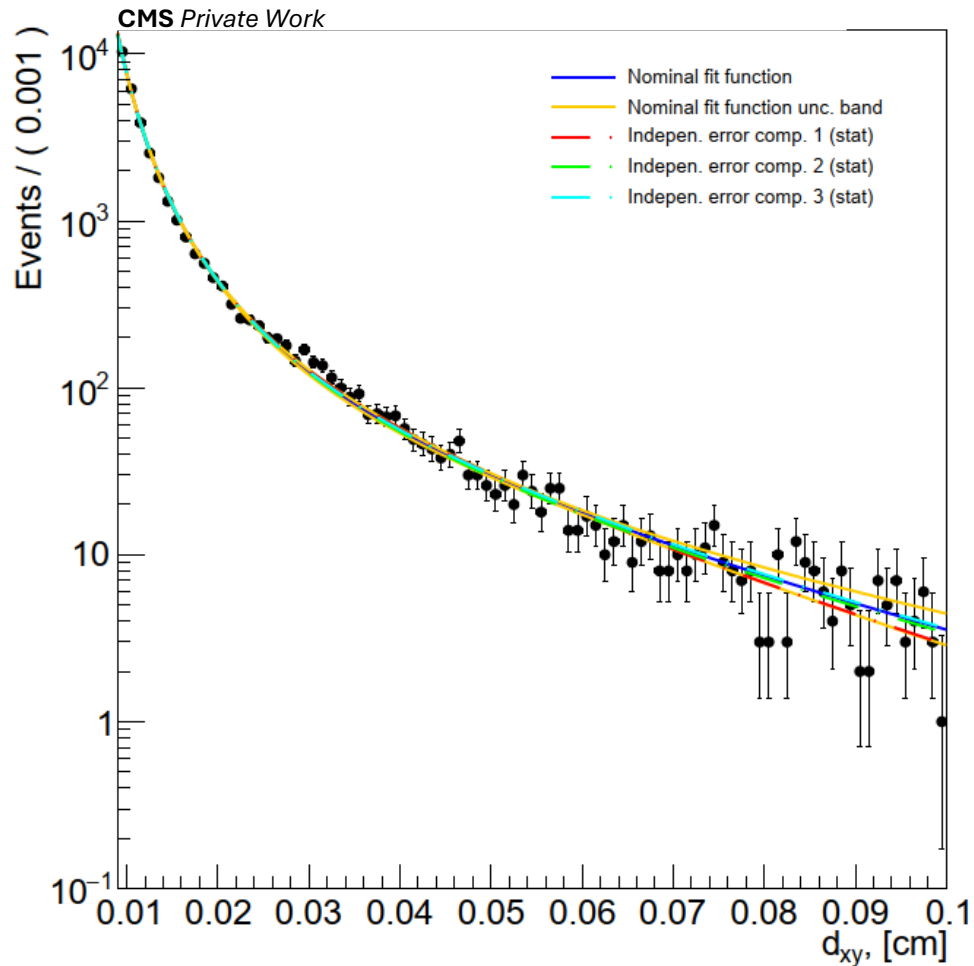


- Example MC  $d_{xy}$  distribution tail fit for Electrons:

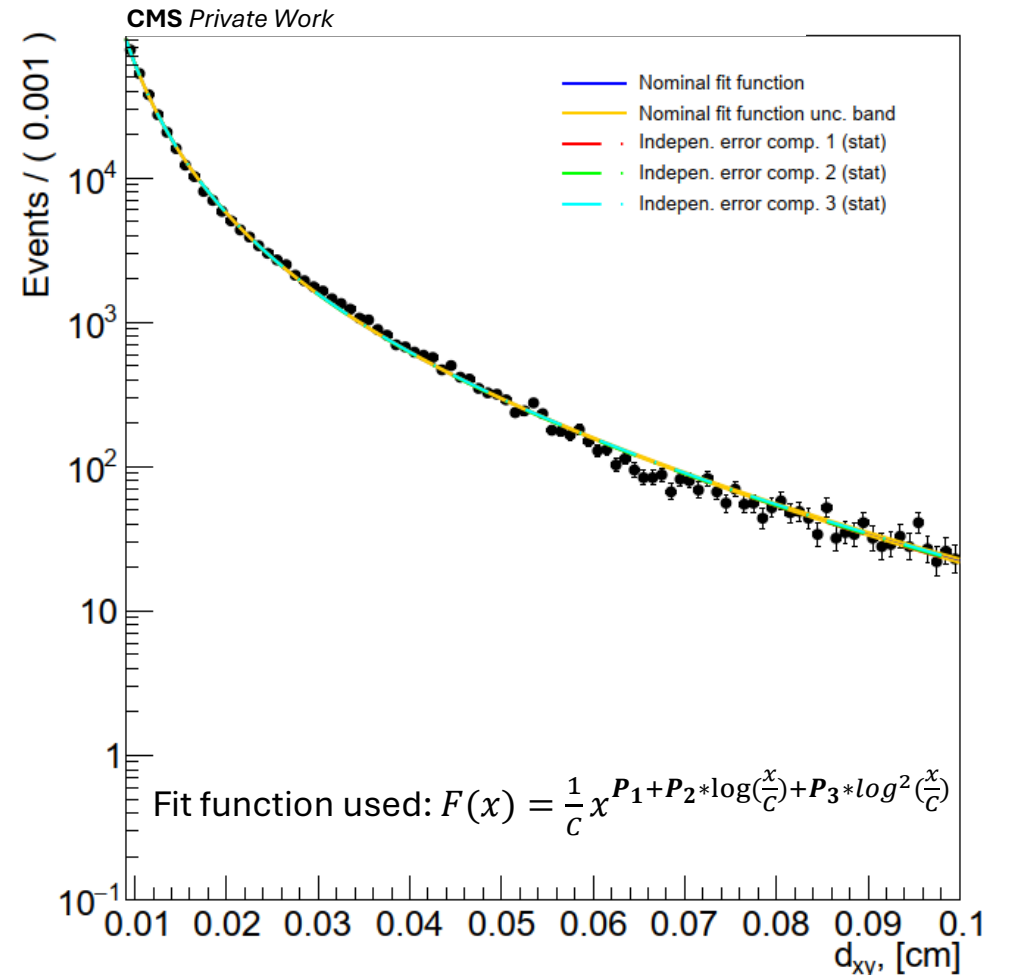


# Analysis activities – lepton $d_{xy}$ corrections, DATA fit example

- Example DATA  $d_{xy}$  distribution tail fit for Muons:



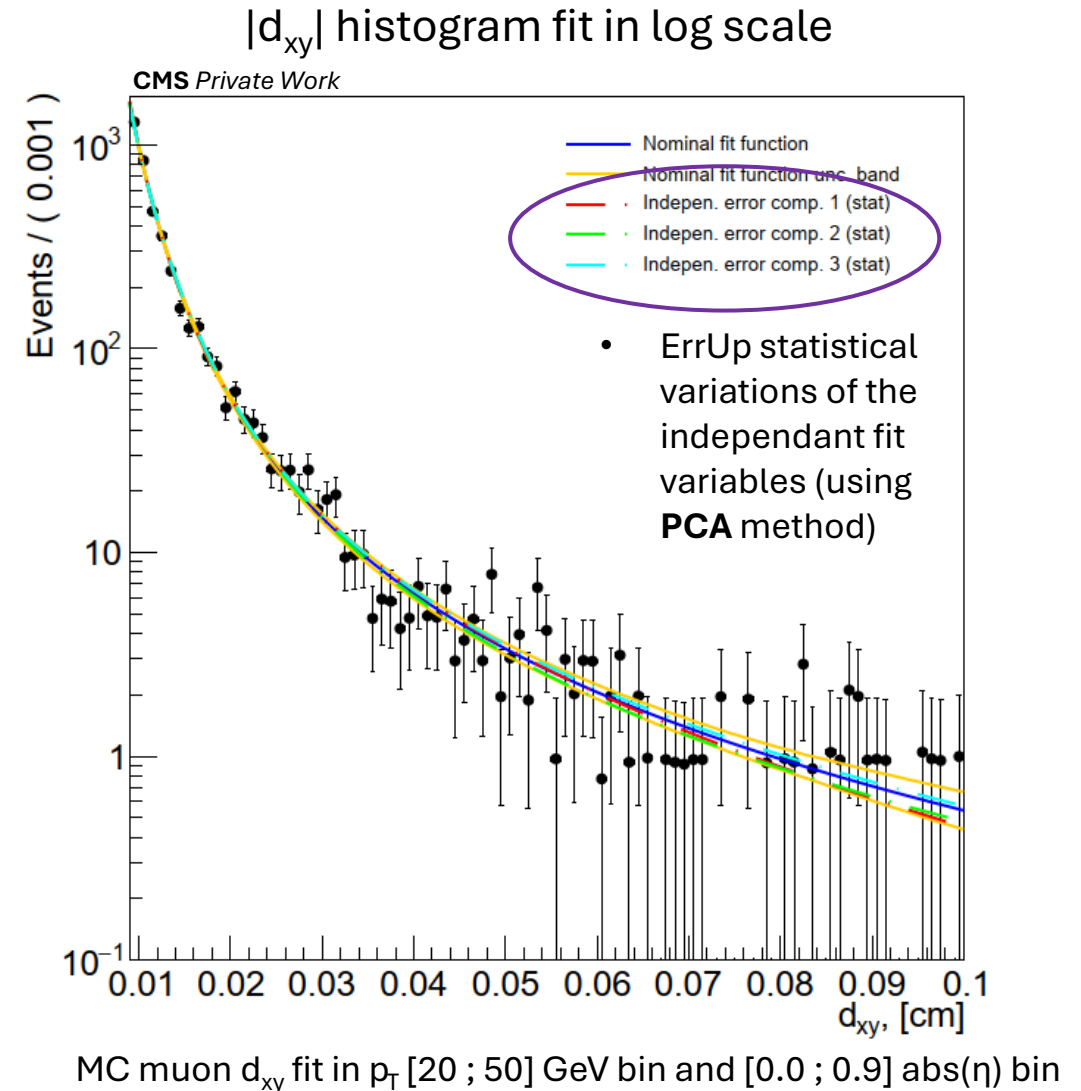
- Example DATA  $d_{xy}$  distribution tail fit for Electrons:



# $d_{xy}$ correction methodology – estimating the correction's uncertainty

Uncertainty estimation for the  $d_{xy}$  correction:

- Statistical uncertainty:
  - Histogram/binned method part:
    - Recalculate the CDF using binned values with errorUp/Dn added from Poissonian uncertainty.
    - The difference in the resulting correction from the recalculated CDF is the statistical uncertainty.
  - Fit part:
    - Using 'Principal Component Analysis' approach, find the independent variables as a linear combination of the fit variables used.
    - Recalculate the CDF for fit part using fit parameters+ErrUp/Dn from the independent variable uncertainties.
    - The difference in the resulting correction from the recalculated CDF is the statistical uncertainty.
    - Uncertainty gets calculate for each independent component and the resulting contributions get summed in quadrature. (As they are independent from each other)

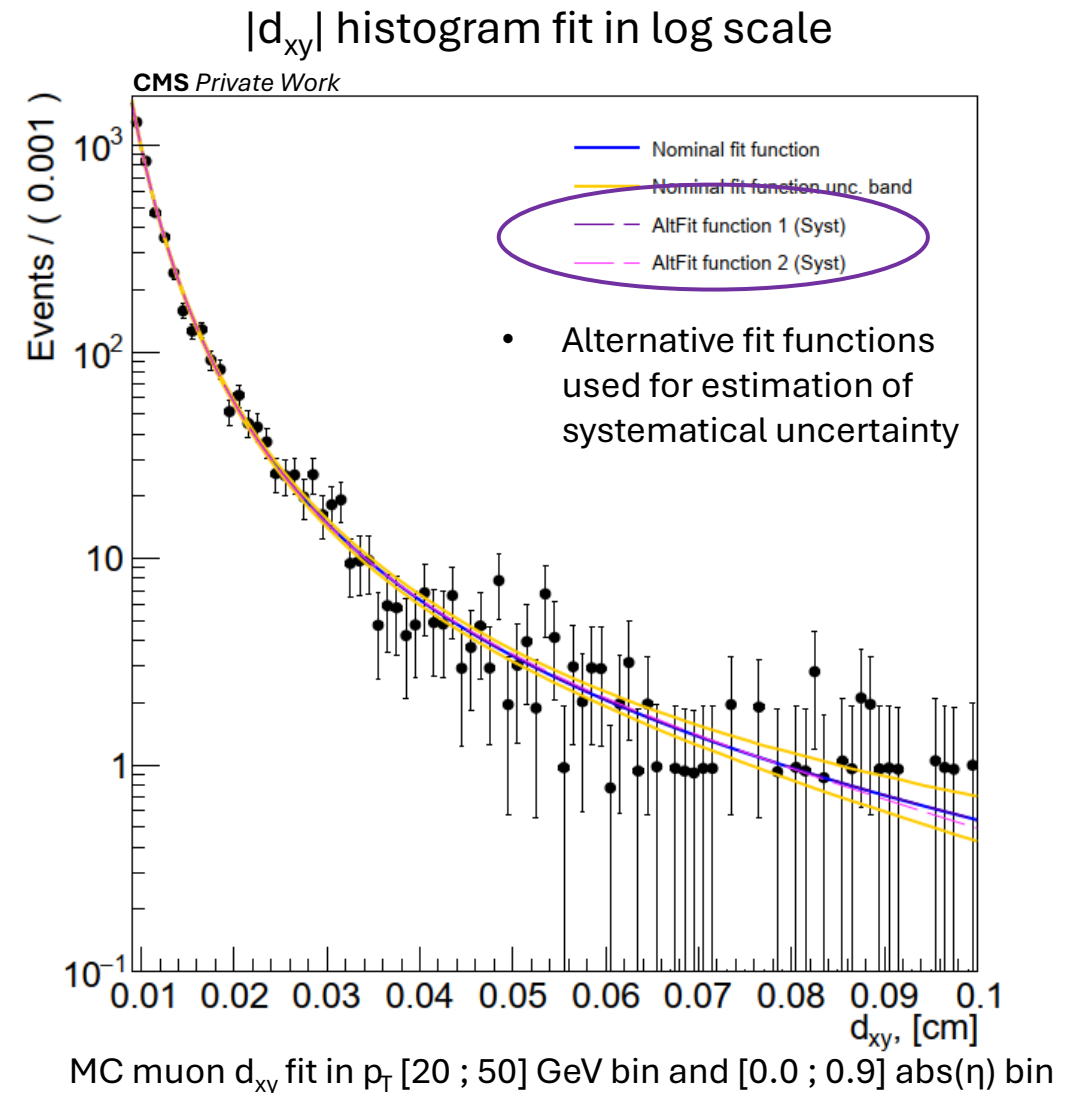




# $d_{xy}$ correction methodology – estimating the correction's uncertainty

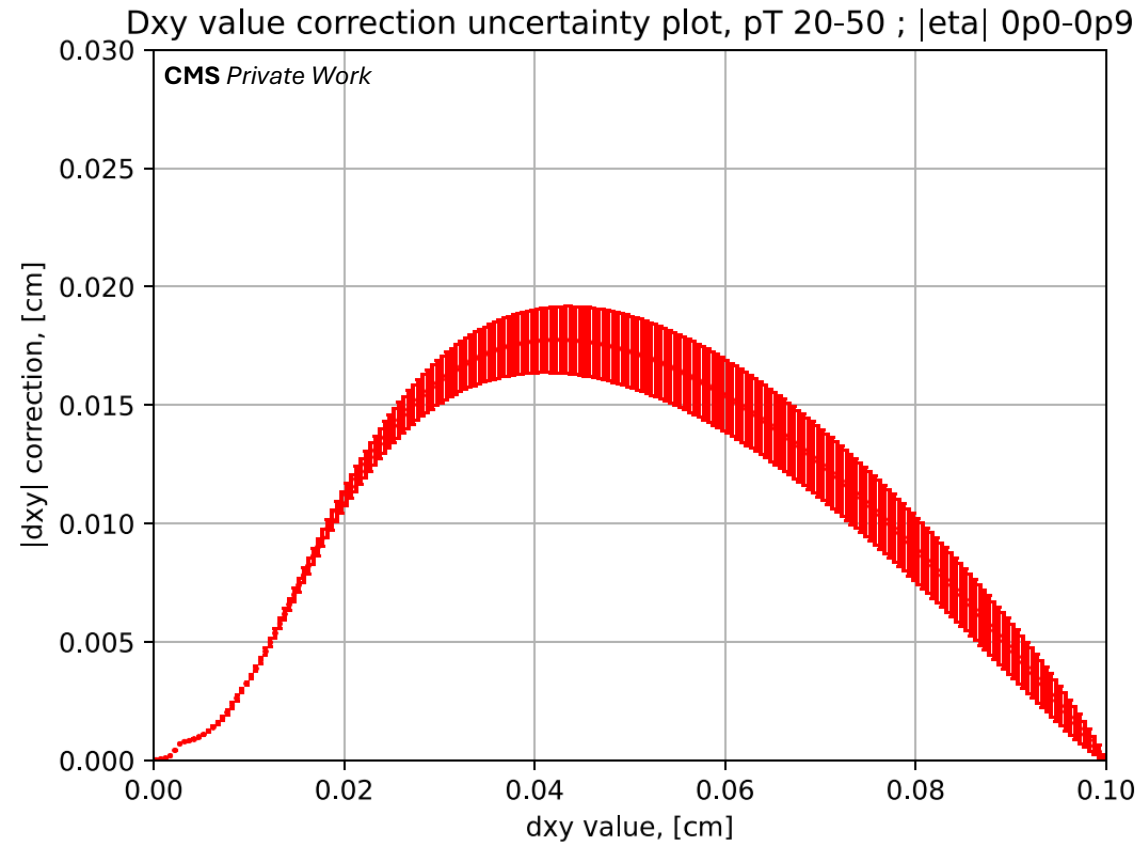
Uncertainty estimation for the  $d_{xy}$  correction:

- Systematical uncertainty:
  - Histogram/binned method part:
    - Potential check - Recalculate the CDF using different histogram bin count.
    - The difference in the resulting correction from the recalculated CDF is the systematical uncertainty.
  - Fit part:
    - Use a different fit function and recalculate the CDF.
    - The difference in the resulting correction from the recalculated CDF is the systematical uncertainty.
    - Potential check – change the bin count used in the histogram that gets fitted. Estimate additional systematical uncertainty from this change of binning.
- Total uncertainty:
  - Combine the statistical and systematical contributions in quadrature.

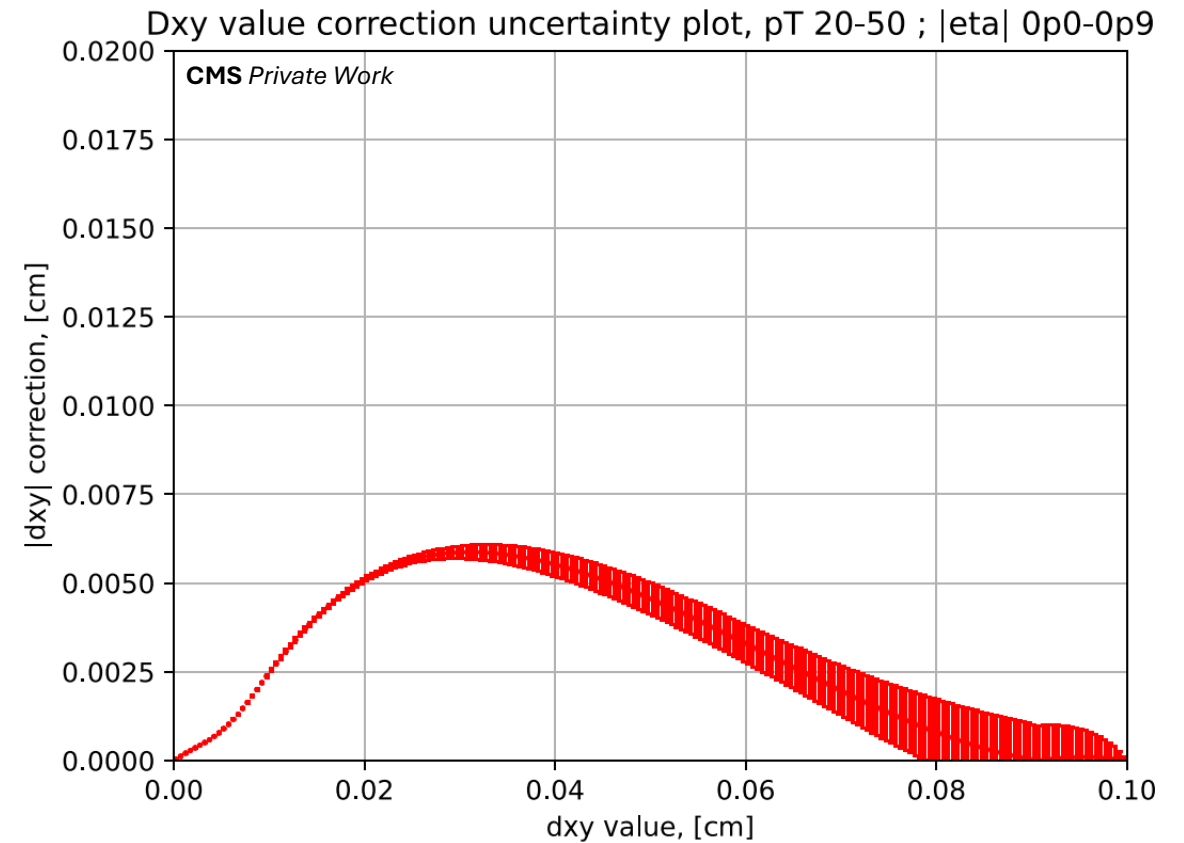


# $d_{xy}$ correction methodology – estimating the correction's uncertainty

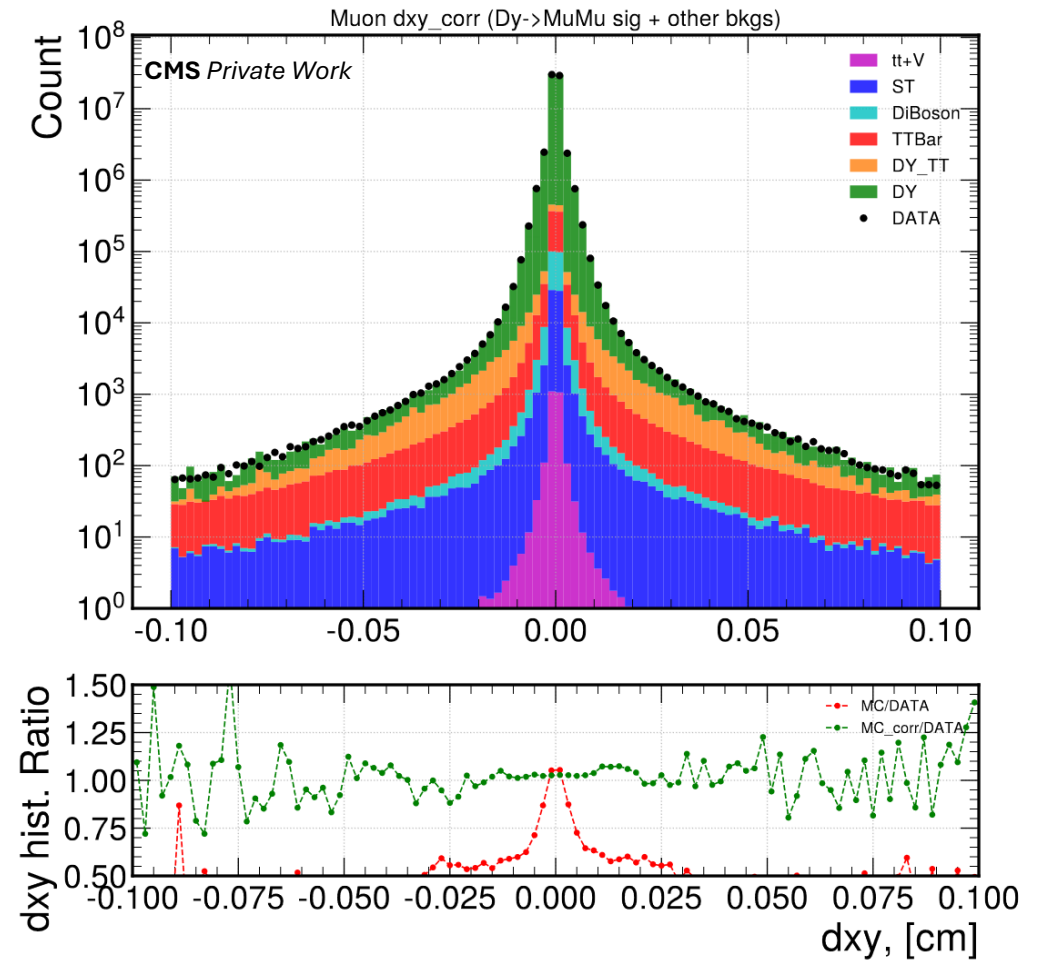
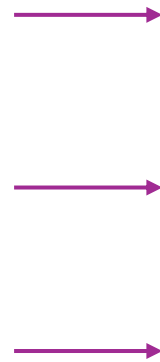
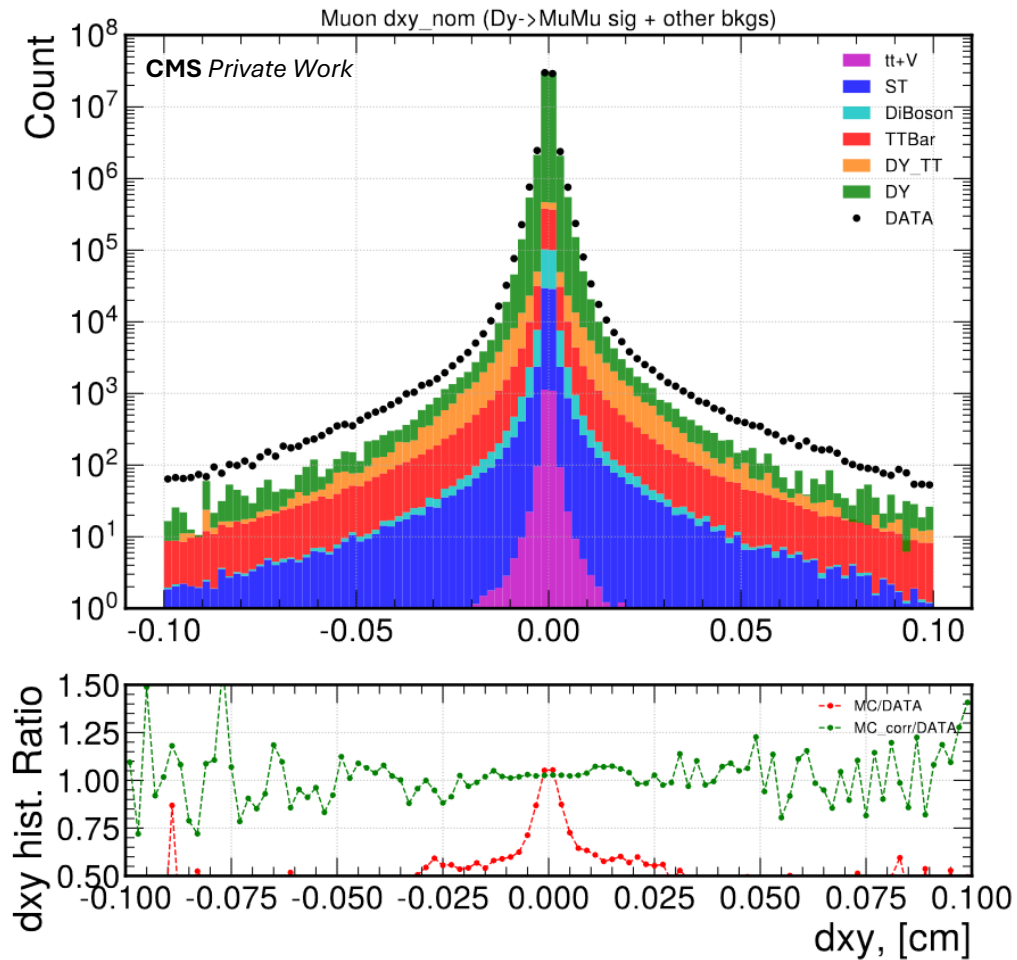
- Example  $d_{xy}$  correction uncertainties for Muons:



- Example  $d_{xy}$  correction uncertainties for Electrons:

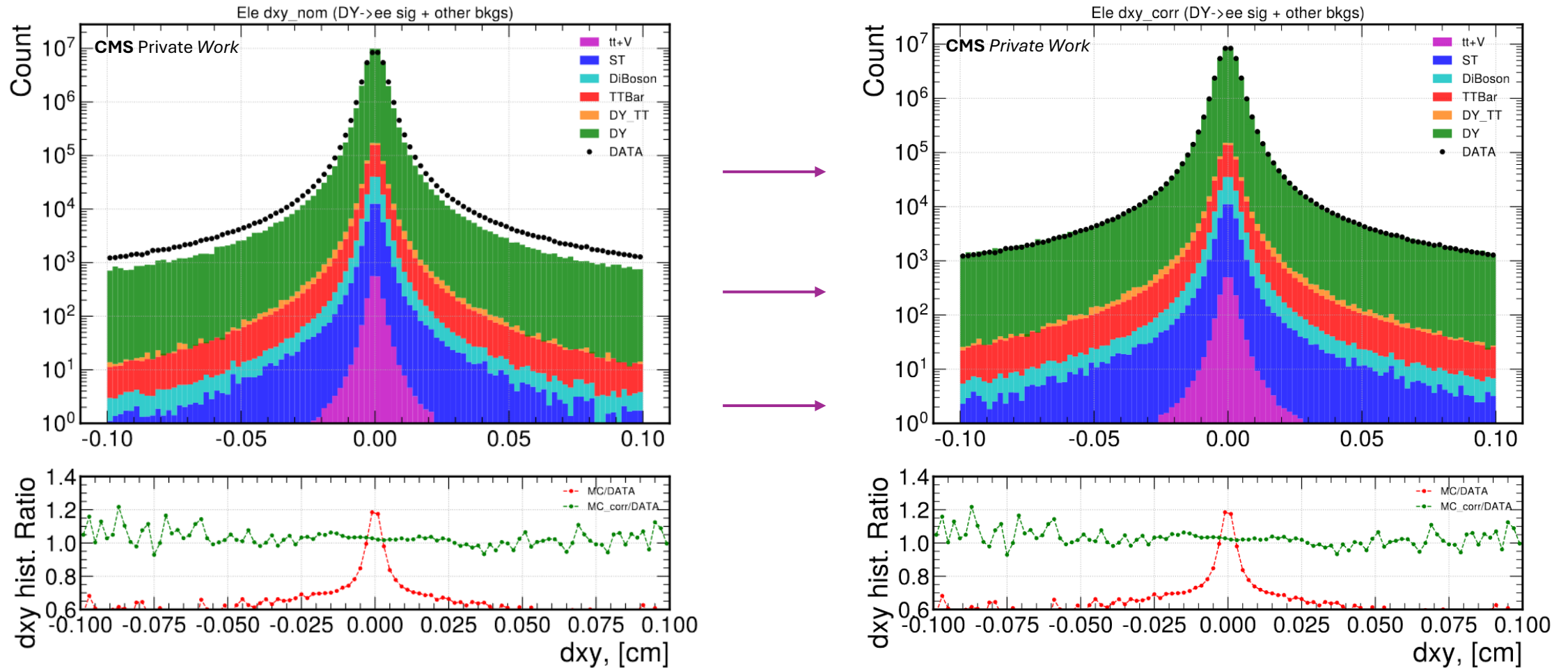


# Analysis activities – lepton $d_{xy}$ corrections, muon results



Muon  $d_{xy}$  MC distribution before (left) and after (right) the application of the correction.

# Analysis activities – lepton $d_{xy}$ corrections, electron results



Electron  $d_{xy}$  MC distribution before (left) and after (right) the application of the correction.

# Outlook and future tasks

- Additional control region checks for the  $d_{xy}$  corrections.
- Add the missing corrections in the analysis:
  - Rochester corrections
  - Jet energy/resolution corrections
- Estimate the QCD background using data-driven methods (ABCD method).
- Setup the 'combine' tool for the final fit and ratio extraction from the  $d_{xy}$  and  $p_T$  distributions
  - Include all the uncertainty sources

Thank You for Your attention!  
Questions, comments and suggestions are welcome!