





#### Dark photon production in Higgs decays at FCC-ee Expression of interest

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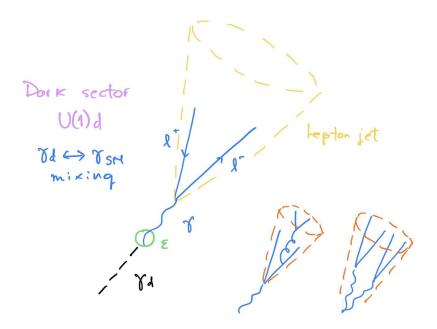
FCC LLP meeting

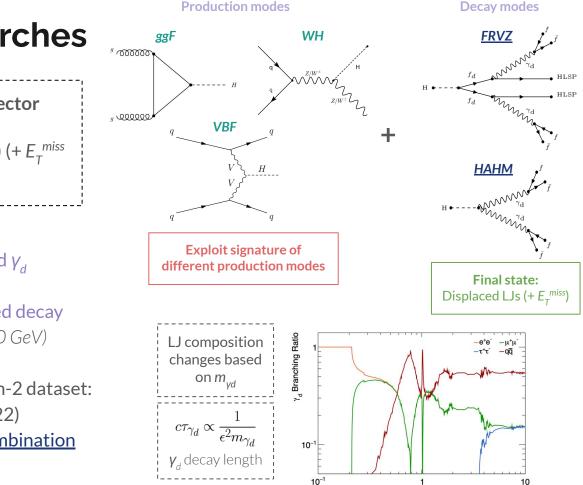
6 June 2024

### Dark sectors signatures

- Light dark sectors as general possibility in colliders (minimal extensions, DM candidates, various exotic signatures)
- At the LHC, **light dark particles** would be produced with large boosts, causing their decay products to form jet-like structures
- LJ-like signatures arise in models with a dark sector composed of unstable particles with MeV-GeV masses decaying to SM particles
- Studies in ATLAS:
  - Searches for **displaced LJ-like signatures** in Run-2 data
  - Different **Higgs production modes:** 
    - ggF+WH production
    - VBF production
  - Run-3 analysis ongoing

Lepton jet (LJ) = cluster of collimated light charged particles  $(e^+e^-, \mu^+\mu^-, qq')$ 





**Production modes** 

### **ATLAS Run-2 searches**

- $H \rightarrow 2\gamma_{d}$  (+ X) via **Higgs & vector** portals
- SM final states  $(\gamma_d \rightarrow \ell^+ \ell'/qq) (+ E_T^{miss})$ signature in FRVZ decay)

- Small coupling  $\varepsilon$ : long-lived  $\gamma_d$  $0 \quad 10^{-7} < \varepsilon < 10^{-5}$
- With  $m_{vd} << m_{H}$ : collimated decay  $\circ$  m<sub>vd</sub> ~ O(10 MeV)-O(10 GeV)
- Two searches using full Run-2 dataset:
  - ggF+WH search (2022) 0
  - VBF search & full combination Ο (2023)

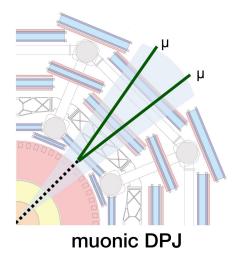
m, [GeV]

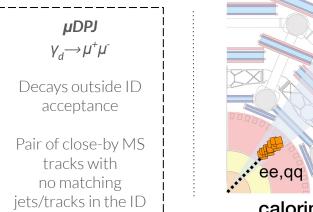
#### **Displaced LJ signatures**

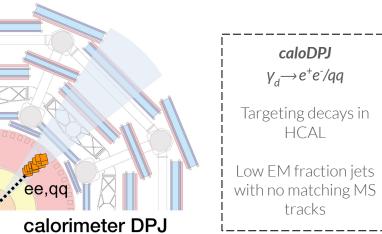
Custom reconstructed objects: Dark Photon Jets (DPJ)

Sensitive to  $\gamma_d$  decays after pixel detector

	Collisional	Non-collisional		
Backgrounds	Multi-jet (e.g.,	Cosmic rays	Beam-induced	
	QCD MJ, V+jets)	(µDPJ)	(caloDPJ)	



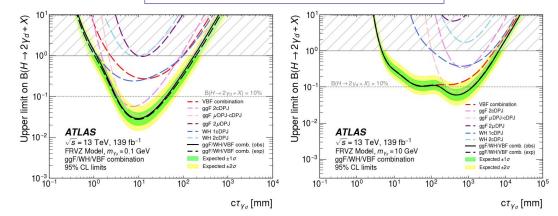


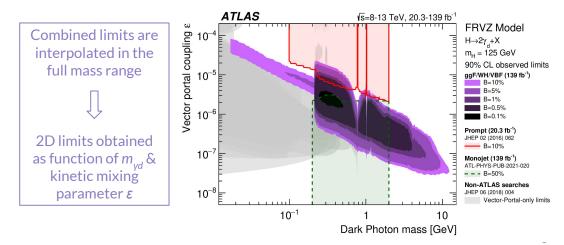


#### **Run-2** results

#### Combination with observed ggF/WH limits

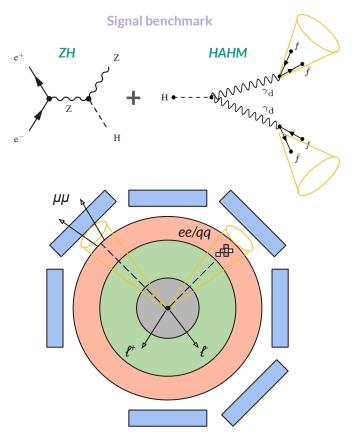
- Explored  $\gamma_d$  masses  $\in$  [0.017, 15] GeV
- Explored lifetimes translating in  $c\tau_{yd} \in [2, 1000] \text{ mm}$
- Interpretation of results:
  - Exotic Higgs decays to LLPs
  - Dark sector models (FRVZ, HAHM)
  - Caveat:
    - Full combination is FRVZ
    - Not commonly used compared to minimal models studied by other facilities





### What about a similar thing at FCC-ee?

- First look into dark photon production in Higgs decays at FCC-ee
- Good complementarity with ongoing FCC LLP searches:
  - Similarity with displaced signatures from ALPs
  - Additional exotic Higgs decay scenario
- Targeting FCC-ee ZH production & HAHM Higgs decay
  - $\circ \quad e^+e^- \longrightarrow Z(\ell^+\ell')H(2\gamma_d) @ \text{ecm } 240 \text{ GeV}$
- Experimental signature:
  - A reconstructed Z boson from  $l^+l^-$  pair
  - A displaced DPJ from each long-lived  $\gamma_d$



### Signal MC and future plans

- Signal simulated using MadGraph5 HAHM UFO model
  - 100k events per sample
  - MG5\_aMC v3.5.4 for LHE production
  - Pythia8 + Delphes using IDEA Delphes card
- Backgrounds:
  - Candidates: ZH, ZZ, Zqq, etc
  - Checking existing samples in winter2023 camp.
- Future plans:
  - Generator level studies (LHE level kinematics)
  - FCCAnalyses framework to study reco-level info
    - Explore low-level detector response; e.g.,
      - Calocluster and muon information (including timing)

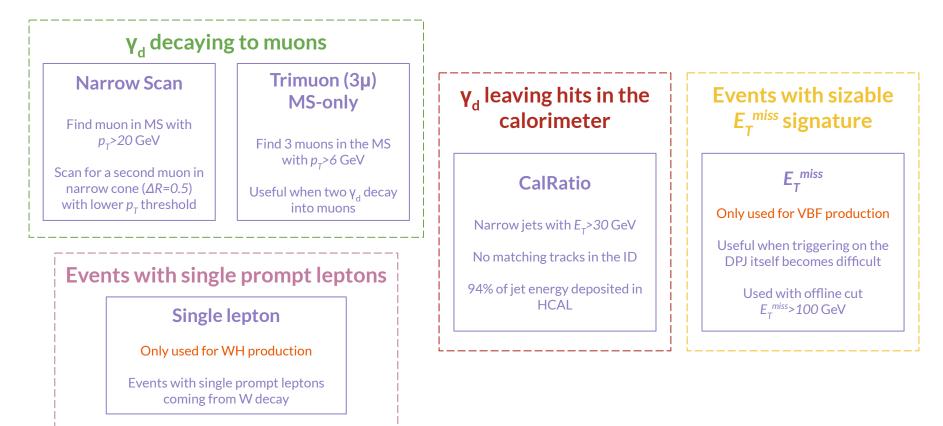
$m_{\gamma d} = 0.1  \text{GeV}$ $c \tau_{\gamma d} = 15  \text{mm}$	$m_{yd} = 2-6 \text{ GeV}$ $c\tau_{yd} = 100-1000$ mm
$BR(\gamma_d \rightarrow e^+e^-)=100\%$	Allow $\gamma_d \rightarrow \mu^+ \mu^-$ since $m_{vd} > 2m_{\mu}$
Useful for caloDPJ	since $m_{\gamma d} > 2m_{\mu}$
signatures	Useful for µDPJ signatures

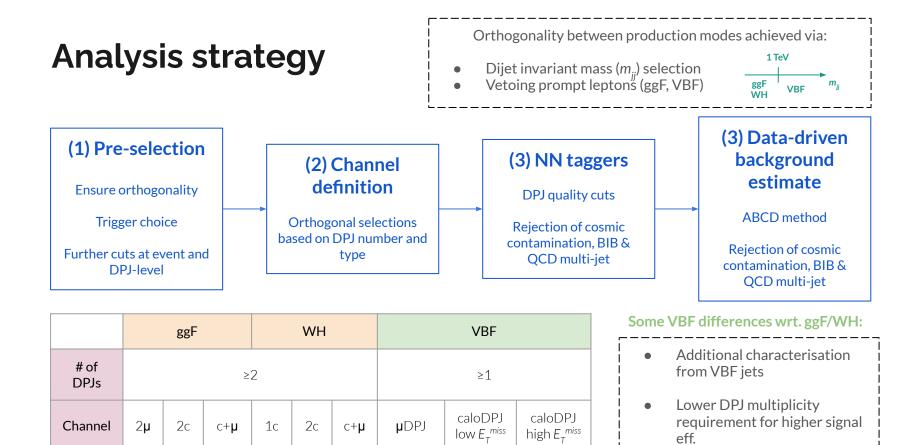
#### **Displaced DPJ considerations**

- µDPJ final states as "safe option" since easier to reconstruct (collimated muons in narrow cone or resolved dimuons with simple vertexing)
- Explore ATLAS-like NN taggers to distinguish displaced caloDPJs from prompt jets



### **Trigger strategy**





NS/3µ/

 $E_{T}^{miss}$ 

Single lepton

 $E_{\tau}^{miss}$ 

Narrow Scan/3µ/

CalRatio

Trigger

•	$E_{\tau}^{miss}$ triggers for both DPJ
	signatures & no CalRatio

### **NN-based taggers for DPJ quality**

#### Cosmic-ray tagger (µDPJ)

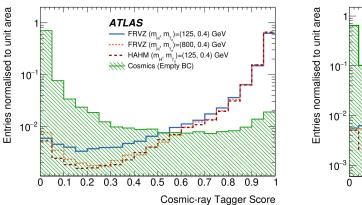
- Based on track parameters and RPC timing information
- Per-track tagging classifying **cosmic background against tracks originated by collision products**

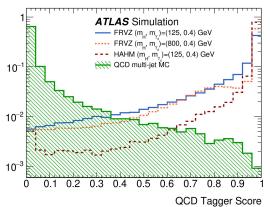
#### QCD tagger (cDPJ)

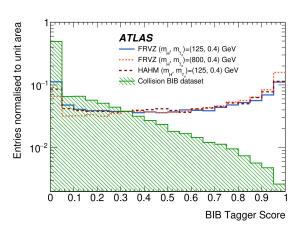
- 3D representations of jet energy built with calo-clusters
- Using energy deposit, *Φ* and *η* in each calorimeter sampling
- CNN trained to classify QCD MJ from signal-like jets

#### **BIB** tagger (cDPJ)

- Using same information than QCD tagger
- CNN trained to classify
   Beam-Induced Background jets
   from signal-like jets







#### Signal region definitions



$\mathrm{SR}^{\mathrm{ggF}}_{2\mu}$	$\mathrm{SR}_{\mathrm{2c}}^{\mathrm{ggF}}$	$SR_{c+\mu}^{ggr}$
2	0	1
0	2	1
yes	-	-
yes	-	yes
-	yes	-
-	< 2.5	-
-	< 0.4	-
$> \pi/5$	$> \pi/5$	$> \pi/5$
-	> 0.2	> 0.2
< 4.5	< 4.5	< 4.5
-	> 0.95	> 0.9
	$\frac{1}{0}$ yes $\frac{1}{2}$ $> \pi/5$	$\begin{array}{c ccc} 0 & 2 \\ \hline 0 & 2 \\ \hline \\ yes & - \\ yes \\ - & yes \\ - & 2.5 \\ - & < 2.5 \\ - & < 0.4 \\ > \pi/5 & > \pi/5 \\ - & > 0.2 \\ < 4.5 & < 4.5 \end{array}$

Requirement / Region	$SR_c^{WH}$	$SR_{2c}^{WH}$	$SR_{c+\mu}^{WH}$
Number of $\mu$ DPJs	0	0	1
Number of caloDPJs	1	2	1
Single-lepton trigger $(\mu, e)$	yes	yes	yes
$m_{\rm T}$ [GeV]	> 120	-	-
$ t_{caloDPJ} $ [ns]	< 4	< 4	< 4
Leading (far) caloDPJ width	< 0.08	< 0.10 (0.15)	< 0.1
caloDPJ $p_{\rm T}$ [GeV]	> 30	-	-
JVT	< 0.6	< 0.6	< 0.6
$\min(\Delta\phi)$	$< 3\pi/5$	$< 3\pi/10$	$< 7\pi/20$
min(QCD tagger)	> 0.99	> 0.91	> 0.9

#### VBF

Requirement / Region	$\mathrm{SR}_\mu$	$\mathrm{SR}^{\mathrm{L/H}}_{\mathrm{c}}$
Number of DPJs	$\geq 1$	$\geq 1$
Leading DPJ type	$\mu { m DPJ}$	caloDPJ
	$E_{\mathrm{T}}^{\mathrm{miss}}$	
Trigger	Tri-muon MS-only	$E_{\mathrm{T}}^{\mathrm{miss}}$
	Muon narrow-scan	
$p_{\rm T}({\rm jet}) \; [GeV]$	> 30	> 30
$N_{ m jet}$	$\geq 2$	$\geq 2$
$m_{ m jj} \; [GeV]$	$\geq 1000$	$\geq 1000$
$ \Delta \eta_{ m jj} $	> 3	> 3
$ \Delta \phi_{ m jj} $	< 2.5	< 2.5
$N_\ell$	0	0
$N_{b ext{-jet}}$	0	0
$C_{\rm DPJ}$	> 0.7	-
$\Delta \phi_{\min}$	-	> 0.4
$E_{\mathrm{T}}^{\mathrm{miss}} \left[ GeV \right]$	> 100	$SR_{c}^{L}$ : [100, 225]
T [Gev]	> 100	$SR_c^H: > 225$
—µDPJ charge—	0	-
caloDPJ tagger	-	> 0.9
$\sum_{\Delta R=0.5} p_{\rm T}  [{\rm GeV}]$	< 2	< 2

### Data-driven background estimation: ABCD method

#### • Estimate expected QCD multi-jet background in each SR

- Non-collisional backgrounds (CR, BIB) are suppressed before populating ABCD planes
- Validations performed in BC & DC subplanes
   + additional validation regions (backup)

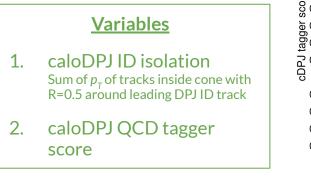
#### **Estimation using ABCD**

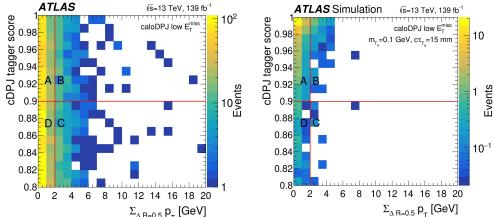
- Define plane using two uncorrelated variables
- Split plane in A, B, C & D regions:

• A = Signal-enriched

- B,C,D = Background-enriched
- Estimate  $N_A$  as:  $N_A = \frac{N_B \times N_D}{N_C}$

#### • e.g., ABCD planes for VBF low $E_T^{miss}$ channel:





### **Unblinded results:** anything new?

**Unblinding** Populate signal regions with real data and check if we have found something new!

-

- Before unblinding:
  - Estimate expected exclusion limits on observable of interest  $BR(H \rightarrow 2\gamma_d + X)$
- After unblinding:
  - No new physics found!
  - All predictions in good agreement with observations
  - Estimate observed exclusion limits on observable of interest BR( $H \rightarrow 2\gamma_d + X$ )

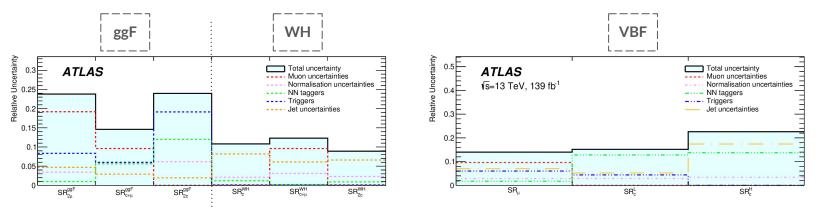
Selection	Search channel	CRB	CRC	CRD	SR expected	SR observed
	$2\mu$	55	61	389	$317 \pm 47$	269
ggF	$c+\mu$	169	471	301	$108 \pm 13$	110
	2c	97	1113	12146	$1055 \pm 82$	1045
	с	1850	3011	155	93 ± 12	103
WH	$c+\mu$	30	49	31	$19 \pm 8$	20
	2c	79	155	27	$14 \pm 5$	15

			VB	=	
Selection	CRB	CRC	CRD	SR expected	SR observed
$\mathrm{SR}_\mu$	44	22	21	$42\pm14$	41
$\mathrm{SR}_{\mathrm{c}}^{\mathrm{L}}$	224	256	1123	$983\pm95$	923
$\frac{\mathrm{SR}_{\mathrm{c}}^{\mathrm{L}}}{\mathrm{SR}_{\mathrm{c}}^{\mathrm{H}}}$	9	11	35	$29\pm14$	46

#### ggF & WH

### Systematic uncertainties

- ABCD method syst. uncertainty obtained by propagating the stat. uncertainty in the CRs
- **Experimental uncerts.** are evaluated from **data/MC differences** in the DPJ reconstruction and **NN taggers** 
  - **Muon uncertainties:** Reconstruction of close-by muon, evaluated using a tag-and-probe method on  $J/\Psi \rightarrow \mu\mu$  as function of  $\Delta R_{\mu\mu}$
  - Normalisation uncerts.: Luminosity and pile-up reweighting
  - **NN taggers:** Set of weights is extracted from  $Z \rightarrow \mu\mu$  or dijet samples and propagated to signal samples to cover MC/data differences
  - **Triggers:** Same close-by muon tag-and-probe approach is adapted to *trimuon* and *NarrowScan* triggers. *MET trigger* uncertainty obtained by propagating 100% of scale factors uncertainty
  - Jet energy resolution and energy scale are considered, plus additional jet energy scale uncert. for low EM fraction jets

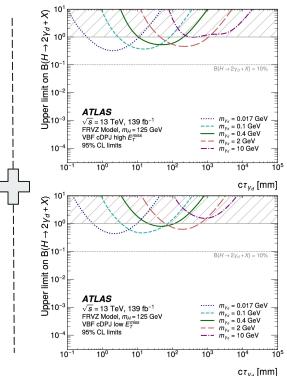


### **Upper limits on BR(H→2γ<sub>d</sub>+X):** e.g., VBF

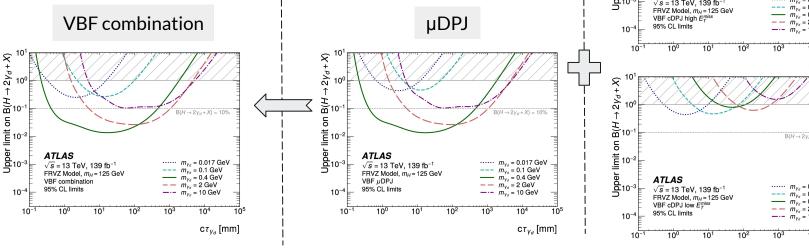
- Single ABCD limits for each channel and mass point
- Observed upper limits on  $BR(H \rightarrow 2\gamma_d + X)$  for each SR and overall VBF combination
- Limits available for ggF & WH allow for full combination!

Limits on single *ct* are extrapolated via lifetime reweighting to other cr values (backup)

caloDPJ

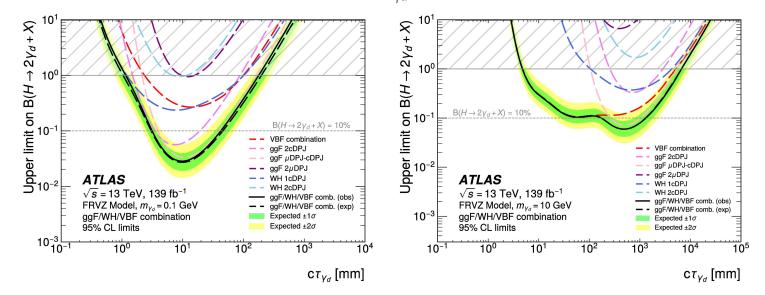


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### Combined limits on BR(H→2γ<sub>d</sub>+X): ggF+WH+VBF

- Limits on  $BR(H \rightarrow 2\gamma_d + X)$  combining all ggF/WH/VBF SRs per  $\gamma_d$  mass point
- Combination of observed limits obtained for  $m_{vd} \in [0.017, 15]$  GeV



- Higher sensitivity obtained from ggF channels
- VBF offers competitive sensitivity at low and high  $c\tau_{vd}$ , particularly at high  $m_{vd}$  values

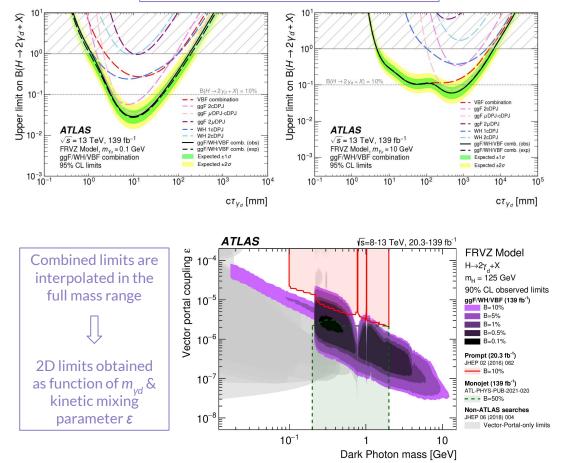
### **Displaced LJs VBF**

- First ATLAS search using VBF production
- Analysis performed for combination with previous ggF/WH iteration

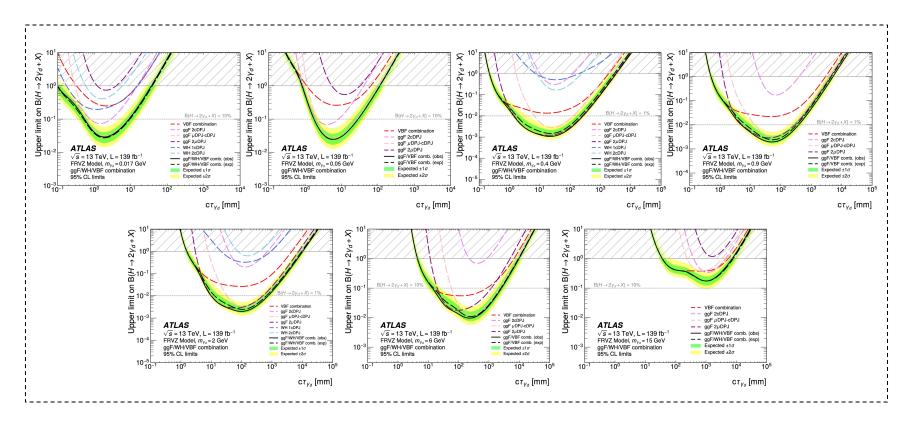
1	Event selection	<ul> <li>VBF jets cuts, triggers, etc.</li> <li>Per-DPJ object selection µDPJ/caloDPJ signal regions</li> </ul>
2	Background estim. & signal efficiency extrapol.	<ul> <li>Data-driven background estimate per SR (ABCD)</li> <li>Signal acceptance x efficient extrapol. as function of cr<sub>yd</sub></li> </ul>
3	Exclusion limits on $B(H \rightarrow 2\gamma_d + X)$	<ul> <li>Expected &amp; observed ULs on B(H→2γ<sub>d</sub>+X) from VBF</li> <li>Full combination with ggF/WH limits</li> </ul>

- Combination renders strongest limits
- up-to-date for displaced LJs searches in ATLAS
- Analysis presented in EPS-HEP 2023
- Paper submitted to EPJC on Nov/2023
- Inclusive production study for Run-3 is on the way!

#### Combination with observed ggF/WH limits

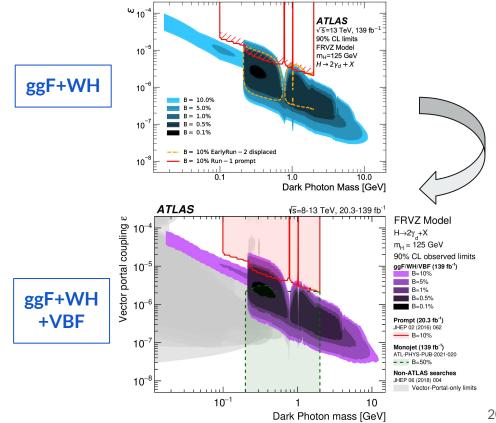


#### BR(H→2γ<sub>d</sub>+X) combined limits: ggF+W/H+VBF



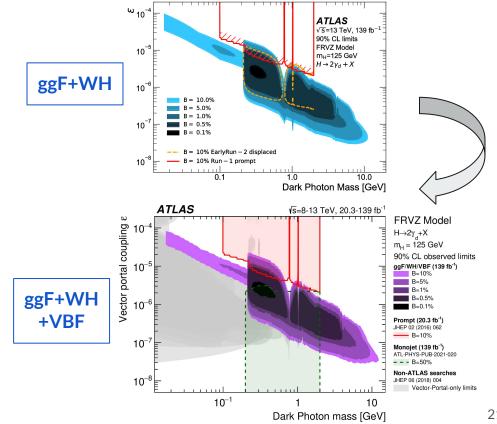
#### **FRVZ vector portal interpretation:** ( $\epsilon$ , $m_{vd}$ ) limits

- 2D limits obtained as a function of  $m_{vd}$ & kinetic mixing parameter  $\varepsilon$
- For each generated  $(m_{vd}, c\tau_{vd})$  pair, the analysis efficiency is extrapolated to the 2D plane:
  - Along *ɛ* using the lifetime reweighting curves
  - Along  $m_{vd}$  according to  $\gamma_d$  branching ratio
- Combination renders **strongest limits** up-to-date for displaced LJ searches in ATLAS



#### **FRVZ vector portal interpretation:** ( $\epsilon$ , m<sub>vd</sub>) limits

- For each generated  $(m_{vd}, c\tau_{vd})$  pair, the analysis efficiency is extrapolated to the 2D plane:
  - Along **ɛ** using the lifetime reweighting curves
  - Along  $m_{vd}$  according to  $\gamma_d$  branching ratio
- 2D limits are obtained doing a simultaneous fit of the available ggF/WH/VBF analysis **channels** in a  $(m_{vd}, c\mathbf{r}_{vd})$  grid
- The final limit is obtained by running a linear interpolation between the results from each simultaneous fit



### Status and current work

#### Run-2

- No new physics for now!
- Observed limits obtained for all mass points in each signal region
- Full ggF+WH+VBF combined limits on  $BR(H \rightarrow 2\gamma_d + X)$  at 95% CL
- $[\varepsilon, m_{yd}]$  limits for full combination  $\rightarrow$  Strongest ATLAS exclusion for displaced LJ searches!

#### **Run-3: Preliminary studies**

- Inclusive production analysis is ongoing!
- Several opportunities for improvement:

# Explore HAHM signals

Study additional signal benchmark with low  $E_T^{miss}$  signature

#### Improved trigger strategy

Exploring NS+VBF for µDPJ signatures

CalRatio+VBF for caloDPJ signatures

#### Implement updated taggers

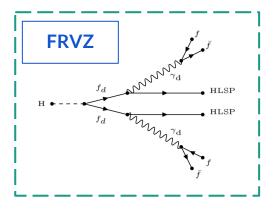
NN taggers trained in newest release for performance improval

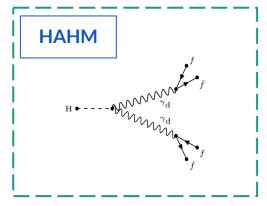
## Optimised SR definitions

Explore further observables for background rejection/prediction

### Run-3: Trigger studies for VBF

- Three signatures crucially related to trigger selections:
  - Production mode (VBF jets)
  - Displaced reconstruction (LLPs)
  - Missing transverse energy
- VBF & LLP: Low trigger efficiency on their own
- **Run-2 VBF:**  $E_T^{miss}$  trigger forces offline cut that reduces sensitivity to models with low intrinsic  $E_T^{miss}$  (e.g., HAHM)
- Run-3 wishlist:
  - **µDPJ:** VBF + NarrowScan MS-only
  - Inclusive NS ready for stable beam this year
  - caloDPJ: VBF + CalRatio
  - Studying low  $m_{ii}$  L1 threshold
  - CalRatio development ongoing





# **VBF** analysis

#### VBF analysis strategy (2) Per-DPJ type selection Inclusive DPJ selection: (1) Pre-selection $\mu$ DPJ channel $\rightarrow$ Leading DPJ is $\mu$ DPJ caloDPJ channel $\rightarrow$ Leading DPJ is caloDPJ VBF jets selection: At least two jets with $p_{\tau}$ >30 GeV (3) NN tagger cuts $m_{ii} > 1 \text{ TeV} |\Delta \eta_{ii}| > 3 |\Delta \Phi_{ii}| < 2.5$ Taggers implemented in ggF/WH Trigger: public analysis: $\mu$ DPJ channel $\rightarrow$ NarrowScan || Trimuon || $E_{\tau}^{miss}$ $\mu$ DPJ channel $\rightarrow$ Reject cosmic ray muons caloDPJ channel $\rightarrow E_{\tau}^{miss}$ caloDPJ channel $\rightarrow$ Reject QCD & BIB jets Lepton veto (orthogonal to WH) *b*-jet veto (targeting *t*-quark decays) **Data-driven** (4) background estimate Further channel-specific cuts: **Reduce background** 0 ABCD method to estimate multijet **Trigger-related** Ο background in signal regions **DPJ** quality cuts Ο

#### **VBF - Trigger strategy**

Chain	Triggering on	Final state	Name	Year
Narrow Scan	Long-lived particles	рDРJ	HLT_mu20_msonly_mu6noL1_msonly_nscan05 HLT_mu20_msonly_mu10noL1_msonly_nscan05_noComb HLT_mu20_msonly_mu15noL1_msonly_nscan05_noComb HLT_mu20_msonly_iloosems_mu6noL1_msonly_nscan05_L1MU20_J40 HLT_mu20_msonly_iloosems_mu6noL1_msonly_nscan05_L1MU20_XE30 HLT_mu6_dRI1_mu20_msonly_iloosems_mu6noL1_dRI1_msonly	2015 2016 2016 2017/18 2017/18 2017/18
Trimuon	MS-only muons		HLT_3mu6_msonly	2015 2016 2017 2018
MET	E <sub>T</sub> <sup>miss</sup>	µDPJ & caloDPJ	HLT_xe70 HLT_xe90_mht_L1XE50 HLT_xe110_mht_L1XE50 HLT_xe110_pufit_L1XE55 HLT_xe110_pufit_xe70_L1XE50	2015 2016 2016 2017 2018

### VBF - Scale factors estimation for $E_{\tau}^{miss}$ trigger

- In order to trigger on  $E_T^{miss}$  below the efficiency plateau, scale factors (SFs) are estimated for each data period by studying the data/MC ratio in  $Z \rightarrow \mu\mu$  events
- All events required to pass:
  - VBF selection:  $N_{iets}(p_T > 30 \text{ GeV}) > 1, |\Delta \eta_{ii}| > 3, m_{ii} > 1 \text{ TeV}$
  - Standard ATLAS  $Z \rightarrow \mu\mu$  selection
  - Lowest unprescaled single lepton trigger
- Events in numerator also required to pass lowest unprescaled  $E_{\tau}^{miss}$  trigger
- Per data period:
  - Turn-on curves plotted as a function of proxy offline  $E_{T}^{miss}$ 
    - $= E_T^{miss} + p_T^{\mu\mu}$
  - Data/MC ratio fitted with error function to obtain final

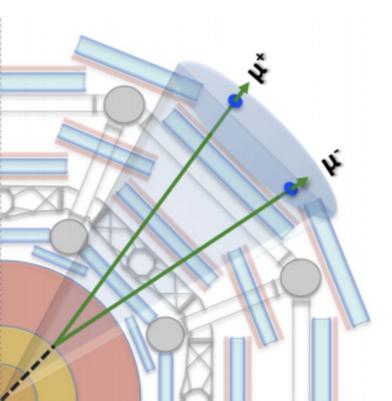
SFs	
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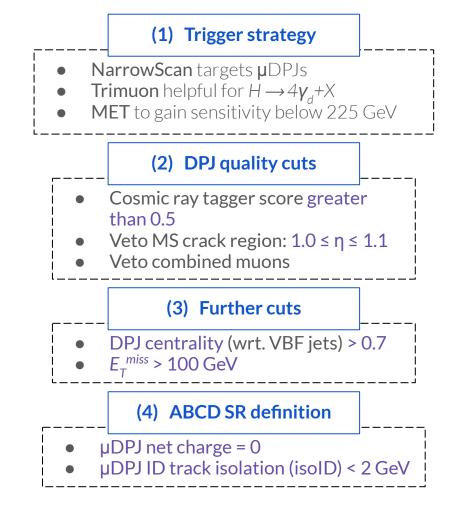
Trigger type	Lowest Unprescaled Chain	Year
E <sub>T</sub> <sup>miss</sup>	HLT_xe70 HLT_xe90_mht_L1XE50 HLT_xe110_mht_L1XE50 HLT_xe110_pufit_L1XE55 HLT_xe110_pufit_xe70_L1XE 50	2015 2016 2016 2017 2018
Single Muon	HLT_mu20_iloose_L1MU15 HLT_mu26_ivarmedium	2015 2016-201 8

#### $Z \rightarrow \mu \mu$ MC vs. Run 2 Data

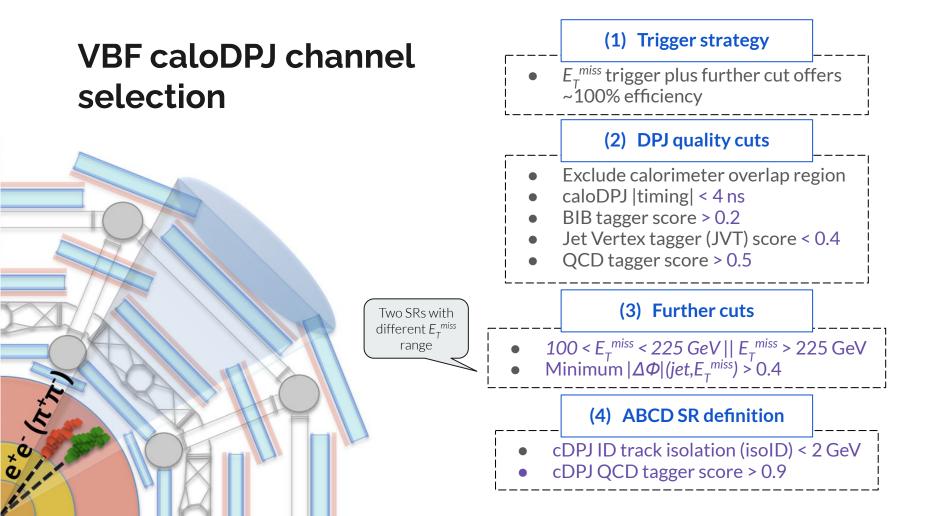
# VBF µDPJ channel

# VBF µDPJ channel selection

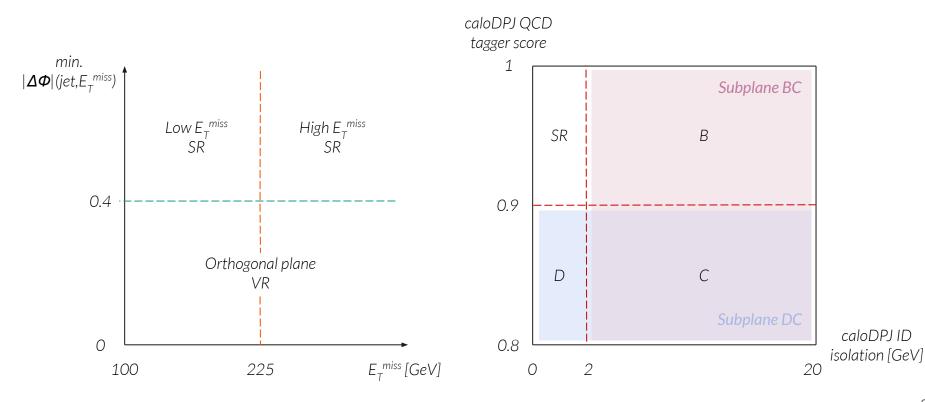




# VBF caloDPJ channel



#### VBF caloDPJ channel breakdown



#### VBF caloDPJ channel breakdown

#### Subplanes VR

VBF jets cuts &  $|\Delta \Phi_{ij}| < 2.5$ Lepton & *b*-jet vetos  $E_T^{miss}$  trigger  $E_T^{miss} > 100 \text{ GeV}$  $\Delta \Phi$ (jet. $E_T^{miss}$ ) > 0.4

Leading DPJ is caloDPJ caloDPJ gapRatio >0.9 caloDPJ BIBtagger score >0.2 caloDPJ |timing| <4 ns caloDPJ JVT score <0.4 caloDPJ QCD tagger score >0.5

BC caloDPJ ID isolation  $\rightarrow$  [2, 20] GeV caloDPJ OCD tagger score  $\rightarrow$  [0.8.1]

**DC** caloDPJ ID isolation  $\rightarrow$  [0, 20] GeV caloDPJ QCD tagger score  $\rightarrow$  [0.8,0.9]

#### Low MET SR

Orthogonal plane VR

Lepton & *b*-jet vetos

 $E_{T}^{miss}$  > 100 GeV  $\Delta \Phi$ (jet, $E_{T}^{miss}$ ) < 0.4

caloDPJ QCD tagger score >0.5

caloDPJ QCD tagger score  $\rightarrow$  [0.8,1]

VBF jets cuts &  $|\Delta \Phi_{ij}| < 2.5$ Lepton & *b*-jet vetos  $E_T^{miss}$  trigger  $E_T^{miss} \rightarrow [100, 225] \text{ GeV}$  $\Delta \Phi(\text{jet}, E_T^{miss}) > 0.4$ 

Leading DPJ is caloDPJ caloDPJ gapRatio >0.9 caloDPJ BIBtagger score >0.2 caloDPJ |timing| <4 ns caloDPJ JVT score <0.4 caloDPJ QCD tagger score >0.5

caloDPJ ID isolation  $\rightarrow$  [0, 2] GeV caloDPJ QCD tagger score  $\rightarrow$  [0.9,1]

#### High MET SR

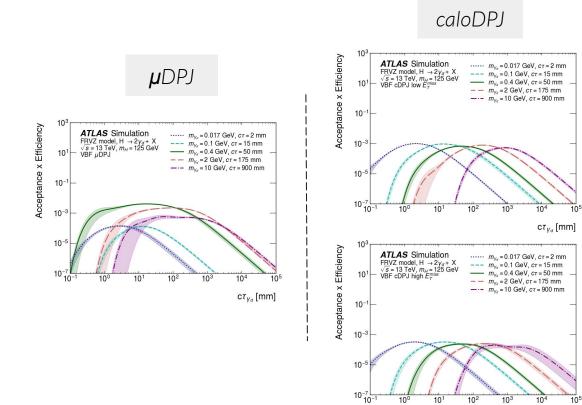
VBF jets cuts &  $|\Delta \Phi_{jj}| < 2.5$ Lepton & *b*-jet vetos  $E_T^{miss}$  trigger  $E_T^{miss} > 225$  GeV  $\Delta \Phi$ (jet, $E_T^{miss}$ ) > 0.4

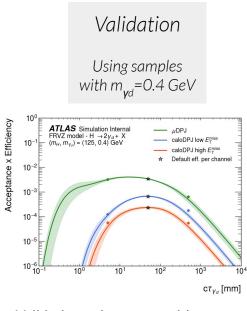
Leading DPJ is caloDPJ caloDPJ gapRatio >0.9 caloDPJ BIBtagger score >0.2 caloDPJ |timing| <4 ns caloDPJ JVT score <0.4 caloDPJ QCD tagger score >0.5

caloDPJ ID isolation  $\rightarrow$  [0, 2] GeV caloDPJ QCD tagger score  $\rightarrow$  [0.9,1]

# More on VBF analysis

### **VBF - Lifetime reweighting**





 Validation points agree with extrapolated curve for m<sub>vd</sub> = 0.4 GeV within uncertainty

 $c\tau_{V_d}$  [mm]

- Disagreement in cDPJ low  $E_{\tau}^{miss}$
- Extra syst. uncert. considered in low  $E_T^{miss}$  SR for  $c\tau > 50 mm$  to take into account non-closure

### **FRVZ vector portal interpretation:** ( $\epsilon$ , $m_{vd}$ ) limits

- 1. For each generated  $(m_{\gamma d'} c \tau_{\gamma d})$  pair, the analysis efficiency is extrapolated to the 2D plane:
  - a. Along cT ( $\epsilon$ ) using the lifetime reweighting curves
  - b. Along  $m_{vd}$  according to  $\gamma_d$  branching ratio
- 2. 2D limits are obtained doing a simultaneous fit of the available ggF/WH/VBF analysis channels in a  $100 \times 100$  grid in  $(m_{vd}, c\tau_{vd})$ 
  - a. Contaminations from  $\gamma_d \rightarrow e^+e^-$  in the µDPJ channels are not considered here
  - b. This step runs for each generated mass point
- The final limit is obtained by running a linear interpolation between the results that are obtained in step (2)
- "Wobbly" contour due to low resolution used when running the fit framework. This was done with about 13K fits!

