QCD and heavy flavor physics at colliders



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Outline

- Strong interactions and QCD
- Parton Distribution Functions
- Measuring jets at the LHC
- B-jet production
- Discrete symmetries and CP violation
- CKM matrix and unitarity triangle
- Meson-antimeson oscillations
- Exclusive final states

Strong interaction and QCD

Protons have equal positive charge, and would not be bound in nuclei without a strong, short-distance interaction.

Yukawa proposed that the exchange of

particles with masses around 100 MeV could

be responsible for these interactions.

Electron-proton Deep Inelastic Scattering has shown that (like Rutherford's experiment) cross-section has a very weak dependence on the momentum transfer.

Protons and neutrons are not elementary particles but made of smaller constituents (quarks, interacting through gluons)





QCD color charges

In the 70s, the current theory of strong interactions was formulated, based on gauge symmetries (like EW)

$$\mathcal{L}_{ ext{QCD}} = ar{\psi}_i \left(i \gamma^\mu (D_\mu)_{ij} - m \, \delta_{ij}
ight) \psi_j - rac{1}{4} G^a_{\mu
u} G^{\mu
u}_a$$

Quarks interact through gluons that carry a charge called "color".

Only 3-quark baryons of different colors,

or quark-antiquark mesons are stable.





Evidence for reality of color comes from the fact that quark production is 3 times larger than what it would be without it!

α_s , confinement, asymptotic freedom

A beautiful property of QCD is that it only depends on one parameter, the coupling α_s . Its strength depends on the momentum transfer, so strong at low momenta- large distances





Quarks are almost free inside the hadrons (asymptotic freedom), but as they are separated in high energy collisions the binding energy between them increases until it can produce a new quark-antiquark pair, creating new hadrons

Parton Distribution Functions

When we collide two protons, we really collide quarks and gluons (partons) within them. The crosssection is a convolution between the probability that the partons produce that final state, and the probability of having partons of that momentum fraction.

These probabilities are called Parton Distribution Functions, and are extracted from experimental data

Most of LHC collisions come from low-momentum gluon interactions

$$\begin{aligned} \sigma_{\mathbf{X}} &= \sum_{\mathbf{a},\mathbf{b}} \int_{0}^{1} d\mathbf{x}_{1} d\mathbf{x}_{2} \ \mathbf{f}_{\mathbf{a}}(\mathbf{x}_{1}, \mu_{\mathrm{F}}^{2}) \ \mathbf{f}_{\mathbf{b}}(\mathbf{x}_{2}, \mu_{\mathrm{F}}^{2}) \\ &\times \quad \hat{\sigma}_{\mathbf{a}\mathbf{b}\to\mathbf{X}} \left(\mathbf{x}_{1}, \mathbf{x}_{2}, \{\mathbf{p}_{i}^{\mu}\}; \alpha_{\mathrm{S}}(\mu_{\mathrm{R}}^{2}), \alpha(\mu_{\mathrm{R}}^{2}), \frac{\mathbf{Q}^{2}}{\mu_{\mathrm{R}}^{2}}, \frac{\mathbf{Q}^{2}}{\mu_{\mathrm{F}}^{2}} \right) \qquad \underbrace{\mathbf{p}_{\mathrm{B}}}_{\mathbf{f}_{\mathrm{b}}} \mathbf{x}_{2} \end{aligned}$$



Measuring PDFs and $\alpha_{\rm s}$

We cannot predict PDFs from first principles, but symmetry considerations lead to an empiric formula whose parameters are fit from data

 $f(x) = x^{(a_1-1)}(1-x)^{a_2}e^{a_3x}[1+e^{a_4}x]^{a_5}$

Data used range from ep Deep Inelastic Scattering (from HERA) to jet cross sections to angular distributions in W and Z production





Similarly, the coupling constant of the strong force is measured fitting data taken at different energy scales, from hadronic tau decays to Z boson momenta, and accounting for the "running" of the parameter vs momentum transfer Simultaneous fits of PDFs and α s are also performed





Jet production

Most common process at the LHC is production of low-energy hadrons (MinBias), and at higher energies they are reconstructed into jets using dedicated clustering algorithms





Jet pairs can be produced in qq, qg or gg interactions, and additional gluon radiation can produce multijet events



Jet reconstruction and measurements



p_t [GeV]

20

After hadronisation, particles are measured by tracker and calorimeter.

A particle-flow algorithm combines tracking and calorimeter in an optimal way to produce particle candidates.

Particles are clustered using an iterative procedure merging those close in terms of metric



Inclusive jets: crosssection: each jet in the event in a given pT and y range



indices *i* and *j* run over all candidate jet constituents p = 1: k_t algorithm p = 0: Cambridge/Aachen algorithm p = -1: anti- k_t algorithm



Jet tagging

- Not all jets come from light quarks or gluons.
- B-quarks have a lifetime of a few ps and can travel a few mm before decaying, producing a secondary vertex.
- Energetic W bosons can decay into 2 nearby jets, reconstructed as a single jet with 2 prongs
- Energetic top quarks decay into a b and a W, with 3 prongs
- Looking at secondary vertices and at the jet internal structure can help distinguish these cases







B jet production at the LHC



4 main production mechanisms



q mm ~~~~~ g more (a) flavour creation (s-channel) (b) flavour creation (t-channel) q more g mon -g(d) flavour excitation (c) gluon splitting [pb/GeV] Data 2011 Stat. + Syst. **POWHEG+PYTHIA 6** →bb+X)/dm ATLAS √ s=7 TeV. 4.2 fb⁻¹



Use vertex mass and distance to distinguish bb, b, c and light quarks in jet

Invariant mass of two jets each identified as b



$g \rightarrow bb$ splitting with both b in a single jet



Study composition of jets by fitting separately each bin and compare to theory



Boosted $Z \rightarrow bb$ in a single jet

- To reduce BG, require production of a photon and a very energetic Z decaying into bb
- Being very energetic, the Z->bb is reconstructed as a single jet
- The jet must have:
 - a two-prong structure
 - two displaced vertices
- Z peak visible in the jet mass despite huge background



Boosted Higgs->bb



The Higgs coupling is proportional to the mass squared, so the largest decay probability is in 2 bquarks final states

This decay mode suffers from large BG from b quarks produced in normal strong interactions (see above)

To reduce BG, search for b-jets produced in association with a W or Z boson (associate production)

Since signal/BG ratio improves with Higgs pT, we only look at cases where the Higgs is **boosted**: its decay products are reconstructed in a single jet with a 2-prong sub-structure



Results for H->bb



Background estimated from data and subtracted. Then the various categories are combined in an optimised way.

First observation of the main decay mode of the Higgs boson!

- Events divided in 6 categories:
 - 0, 1 or two leptons
 - Medium- or high jet pT



Heavy Quark decays: Effective Theory

- Quantum ChromoDynamics has an intrinsic scale, $\Lambda_{QCD} \sim 200$ MeV, above which perturbative expansion can be applied, and below which (soft QCD) only empirical models can be used.
- For quark masses $m_Q >> \Lambda_{QCD}$ Perturbative expansions can be used, and calculations easier
- For states with two heavy quarks (J/ Ψ , Y), Non-Relativistic QCD is used.
- No time to describe HQET here; refer to e.g. A.V. Manohar and M.B. Wise, Heavy Quark Physics, Cambridge University Press (2000)

Symmetries in Physics

- An operator can be applied to a Lagrangian representing a physical system; if the Lagrangian is invariant under this transformation, the operator corresponds to a conserved quantity (Noether's theorem).
- Ex. invariance of Lagrangian under translation
 - $x \rightarrow x+a$ leads to momentum conservation
- If the Lagrangian is not conserved under an operator, thesymmetry is broken, and the physics will be different. In some cases, symmetry breaking is subtle and can be treated as a perturbation

Discrete symmetries

Three discrete symmetries can be applied to a Lagrangian:

- Parity
- Charge conjugation
- Time reversal

In classical physics, all these symmetries are conserved at microscopic level; macroscopically, the concept of entropy breaks T-symmetry.

Things are more complicated in quantum mechanics

Partity: P

- Reflection through a mirror, followed by a rotation of π around an axis defined by the mirror plane.
 - Space is isotropic, so we care if physics is invariant under a mirror reflection.
- \mathcal{P} is violated in weak interactions:

 $[\mathcal{P}, \mathcal{H}_w] \neq 0$

- Vectors change sign under a *P* transformation, pseudovectors or axial-vectors do not.
- \mathcal{P} is a unitary operator: $\mathcal{P}^2=1$.

T. D. Lee & G. C. Wick Phys. Rev. **148** p1385 (1966) showed that there is no operator \mathcal{P} that adequately represents the parity operator in QM.



Charge Conjugation: C

 $e^- \rightarrow e^+$

 $\gamma \rightarrow \gamma$

- Change a quantum field φ into φ[†], where φ[†] has opposite U(1) charges:
 - baryon number, electric charge, lepton number, flavour quantum numbers like strangeness & beauty etc.
- Change particle into antiparticle.
 - the choice of particle and antiparticle is just a convention.



$$[\mathcal{C}, \mathcal{H}_{w}] \neq 0$$

♦ C is a unitary operator: $C^{2}=1$.

Combining Charge and Parity: CP

The fundamental point is that CP symmetry is broken in any theory that has complex coupling constants in the Lagrangian which cannot be removed by any choice of phase redefinition of the fields in the theory.

Weak interactions are left-right asymmetric.

- It is not sufficient to consider C and P violation separately in order to distinguish between matter and antimatter.
- i.e. if helicity is negative (left) or positive (right).
- $\blacksquare CP$ is a unitary operator: $CP^2 = 1$

Time Reversal: T

Not to be confused with the classical consideration of the entropy of a macroscopic system.

'Flips the arrow of time'

- Reverse all time dependent quantities of a particle (momentum/spin).
- Complex scalars (couplings) transform to their complex conjugate.
- It is believe that weak decays violate T, but EM interactions do not.

 $\Box T$ is an anti-unitary operator: $T^2 = -1$.



Combining all symmetries: CPT

- All locally invariant Quantum Field Theories conserve CPT.¹
- CPT is anti-unitary: $CPT^2 = -1$.
- CPT can be violated by non-local theories like quantum gravity. These are hard to construct.
 - see work by Mavromatos, Ellis, Kostelecky etc. for more detail.
- $\textcircled{\sc onserved}$, a particle and its antiparticle will have
 - ◎ The same mass and lifetime .
 - Symmetric electric charges.
 - Opposite magnetic dipole moments (or gyromagnetic ratio for point-like leptons).

Applying CP to physical states

 $CP \mid u \rangle = \mid \overline{u} \rangle$

The u quark has $J^P = \frac{1}{2^+}$, so the \mathcal{P} operator acting on u has an eigenvalue of +1. The \mathcal{C} operator changes particle to antiparticle.

$$CP \mid \pi^0 \rangle = - \mid \pi^0 \rangle$$

The π^0 has $J^{PC} = 0^{-+}$, so the minus sign comes from the parity operator acting on the π^0 meson. The *C* operator changes particle to antiparticle. A π^0 is its own antiparticle.

$$CP \mid \pi^{\pm} \rangle = - \mid \pi^{\mp} \rangle$$

The π^{\pm} has $J^{P} = 0^{-}$, so the minus sign comes from the parity operator acting on the π meson. The *C* operator changes the particle to antiparticle. Flavour interactions in the SM: the CKM matrix

 In the SM Lagrangian, charged-current interactions, mediated by the W boson, allow interactions between U-like and D-like quarks

$$\mathcal{L}_{ ext{CC}} = -rac{g}{\sqrt{2}} \left(ar{ ilde{U}}_L \gamma^\mu W^+_\mu V ilde{D}_L + ar{ ilde{D}}_L \gamma^\mu W^-_\mu V^\dagger ilde{U}_L
ight).$$

• Where V is a non-diagonal mixing matrix

$$V = \left(\begin{array}{cccc} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{array} \right)$$

How many parameters in the matrix?

in general, an $n \times n$ unitary matrix has n^2 real and independent parameters:

- a n × n matrix would have 2n² parameters
- the unitary condition imposes n normalization constraints
- n(n 1) conditions from the orthogonality between each pair of columns:

thus $2n^2 - n - n(n - 1) = n^2$.

In the CKM matrix, not all of these parameters have a physical meaning:

given n quark generations, 2n - 1 phases can be absorbed by the freedom to select the phases of the quark fields

▷ Each u, c or t phase allows for multiplying a row of the CKM matrix by a phase, while each d, s or b phase allows for multiplying a column by a phase.

thus: $n^2 - (2n - 1) = (n - 1)^2$.

Among the n² real independent parameters of a generic unitary matrix:

► $\frac{1}{2}$ n(n - 1) of these parameters can be associated to real rotation angles, so the number of independent phases in the CKM matrix case is:

 $n^2 - \frac{1}{2}n(n-1) - (2n-1) = \frac{1}{2}(n-1)(n-2)$

n(families)	Total indep. params. $(n-1)^2$	Real rot. angles $\frac{1}{2}n(n-1)$	Complex phase factors $\frac{1}{2}(n-1)(n-2)$
2	1	1	0
3	4	3	1
4	9	6	3

The matrix in terms of angles

• There are many ways of writing the matrix as a function of 4 parameters, but the most common (from PDG) uses 4 angles:

$$V = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

- Where $c_{ij} = cosq_{ij}$, $s_{ij} = sinq_{ij}$, with all angles real
- The only complex part of the matrix comes from the e^{id} terms, and that is responsible for CP violation!
- Indeed, the CP swapping on the Lagrangian gives a different result if the matrix has one or more complex terms

Approximate parametrisation

• Experimentally, mixing is larger for nearby generations, 1 >> q_{12} >> q_{23} >> q_{13} . Wolfenstein expanded in I = sin q_{12}

$$V = \begin{pmatrix} 1 - \lambda^2/2 & +\lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & +A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

- Diagonal terms ~1, V_{12} , V_{21} ~ I, V_{23} , V_{32} ~ I², V_{13} , V_{31} ~ I³
- At second order, use r = r (1 $l^2/2$), $\eta = \eta (1 l^2/2)$
- Now the complex component is only in $V_{\rm 13}$ and $V_{\rm 31}$ (third family!)

The CKM triangle

 The Wolfenstein parametrisation is graphycally represented as a triangle with base at (0,0) and (1,0) and apex at (r,η).



Measuring triangle angles



Measuring triangle sides



Current constraints on triangle (from www.pdg.org)



Several ways to independently measure sides and angles

All point to a coherent picture: CP violation well understood in the SM

$ V_{ m CKM} = egin{pmatrix} 0.97435 \pm 0.00016 \ 0.22486 \pm 0.00067 \ 0.00857^{+0.00020}_{-0.00018} \end{cases}$	$\begin{array}{c} 0.22500 \pm 0.00067 \\ 0.97349 \pm 0.00016 \\ 0.04110 \substack{+0.00083 \\ -0.00072} \end{array}$	$ \left. \begin{array}{c} 0.00369 \pm 0.00011 \\ 0.04182 \substack{+0.00085 \\ -0.00074 \\ 0.999118 \substack{+0.00031 \\ -0.000036 \end{array}} \end{array} \right) $
$\sin \theta_{12} = 0.22500 \pm 0.00$ $\sin \theta_{23} = 0.04182^{+0.0008}_{-0.0007}$	$\begin{array}{l} 0067,\qquad \sin\theta_{13}=0\\ 5\\ 4,\qquad \qquad \delta=1 \end{array}$	0.00369 ± 0.00011 , 1.144 ± 0.027 .
$\lambda = 0.22500 \pm 0.0$	$0067, \qquad A = 0.82$	$6^{+0.018}_{-0.015}$,

 $ar{
ho} = 0.159 \pm 0.010\,, \qquad \qquad ar{\eta} = 0.348 \pm 0.010\,.$

Full reconstruction of B mesons

- The "clean" way: e+e- collisions a the Y(4S) peak, followed by decay into B⁺B⁻ or B⁰B⁰ (Babar, BELLE)
- The "dirty" way: proton collisions followed by b-tagging and invariar mass of final state combinations (LHCb, ATLAS, CMS)
 - Advantages: large rates, can produce Bs, Bc etc.
 - Disadvantages: large BG



Oscillations of neutral mesons in QM

• We have flavour eigenstates M^0 and \overline{M}^0 :

 ${\scriptstyle \odot}$ $M^{\scriptscriptstyle 0}$ can be $K^{\scriptscriptstyle 0}$ (sd), $D^{\scriptscriptstyle 0}$ (cu), $B_{\scriptscriptstyle d}{\scriptstyle^{\scriptscriptstyle 0}}$ (bd) or $B_{\scriptscriptstyle s}{\scriptstyle^{\scriptscriptstyle 0}}$ (bs)

- If we consider only strong or electromagnetic interactions only, these flavour eigenstates would correspond to the physical ones
- However due to the weak interaction, the physical eigenstates are different from the flavour ones. This means that they can mix into each other:

via short-distance or long-distance processes

 $\ensuremath{\textcircled{\bullet}}$ and then the flavour superposition decays

$$\mathbf{M} = \mathbf{p} \, \mathbf{M}^0 \pm \mathbf{q} \, \overline{\mathbf{M}}^0$$



Schroedinger equation for oscillation

• We have flavour eigenstates M^0 and \overline{M}^0 :

 ${\scriptstyle \circledcirc}$ $M^{\scriptscriptstyle 0}$ can be $K^{\scriptscriptstyle 0}$ (sd), $D^{\scriptscriptstyle 0}$ (cu), $B_{\scriptscriptstyle d}{}^{\scriptscriptstyle 0}$ (bd) or $B_{\scriptscriptstyle s}{}^{\scriptscriptstyle 0}$ (bs)

 $\begin{array}{ll} \mbox{flavour states} & \neq & \mbox{H}_{\rm eff} \mbox{ eigenstates:} \\ \mbox{(defined flavour)} & & \mbox{(defined } m_{\rm 1,2} \mbox{ and } \Gamma_{\rm 1,2}) \end{array}$

Time-dependent Schrödinger eqn. describes the evolution of the system:

$$i\frac{\partial}{\partial t}\left(\frac{M^{0}}{M^{0}}\right) = H\left(\frac{M^{0}}{M^{0}}\right) = \left(M - \frac{i}{2}\Gamma\right)\left(\frac{M^{0}}{M^{0}}\right)$$

 \odot H is the hamiltonian; M and Γ are 2x2 hermitian matrices ($a_{ij} = \overline{a_{ji}}$)

 $M = \frac{1}{2} (H+H^{\dagger})$ and $\Gamma = i(H-H^{\dagger})$

• CPT theorem: $M_{11} = M_{22}$ and $\Gamma_{11} = \Gamma_{22}$ • particle and antiparticle have equal masses and lifetimes

Solutions for physical states

 $M_{S,L}$ (or $M_{L,H}$) = p $M^0 \pm q \overline{M}^0$

label can be either S,L (short-, long-lived) or L,H (light, heavy) depending on values of $\Delta m \& \Delta \Gamma$ (labels 1,2 usually reserved for CP eigenstates)

p & q complex coefficients that satisfy $|p|^2 + |q|^2 = 1$

• CP conserved if physical states = CP eigenstates (|q/p| = 1)

 \odot Eigenvalues (μ) and mass (Δm) and lifetime ($\Delta \Gamma$) differences can be derived with this formalism:

$$\begin{split} \mu_{L,H} &= m_{L,H} - i/2 \Gamma_{L,H} = (M_{11} - i/2 \Gamma_{11}) \pm (q/p) (M_{12} - i/2 \Gamma_{12}) \\ \Delta m &= m_{H} - m_{L} \text{ and } \Delta \Gamma = \Gamma_{H} - \Gamma_{L} \\ (\Delta m)^{2} - \frac{1}{4} (\Delta \Gamma)^{2} &= 4 (|M_{12}|^{2} + \frac{1}{4} |\Gamma_{12}|^{2}) \\ \Delta m \Delta \Gamma &= 4 \mathcal{R} e (M_{12} \Gamma_{12}^{*}) \\ (q/p)^{2} &= (M_{12}^{*} - i/2 \Gamma_{12}^{*})/(M_{12} - i/2 \Gamma_{12}) \end{split}$$

other useful definitions: $x \equiv \Delta m/\Gamma$ $y \equiv \Delta \Gamma/2\Gamma$

Oscillation probability

• Bd and Bs oscillations formally identical, frequency very different





Oscillations in e⁺e⁻ collisions



Bd oscillations





$$\frac{d\Gamma(B^0 \to f)/d\Delta t - d\Gamma(B \to f)/d\Delta t}{d\Gamma(B^0 \to f)/d\Delta t + d\Gamma(\overline{B}^0 \to f)/d\Delta t} =$$

 $=(1-2w)\cos(x\Delta t)\otimes R(\Delta t)$



 $\Delta m_{d} = (0.507 \pm 0.005) \text{ ps}^{-1}$ $x = \Delta m_{d} \cdot \tau_{Bd} = 0.774 \pm 0.008$

Bs oscillations

At the Tevatron on the B_s:

 amplitude method, instead of extracting directly ∆m_s
 (à la LEP)

$$\frac{1}{|A_f|^2} \frac{d\Gamma(P^0(\overline{P}^0) \to f)}{d\Delta t} = [1 \pm A(1 - 2w)\cos(x\Delta t)]e^{-\Delta t}$$

- ► fit A at different values of ∆m_s; if A=1
 - \Rightarrow oscillations at this Δm_{s} value

Very precise determination from the Tevatron:

$$\Delta m_s = (17.77 \pm 0.10 \pm 0.07) \text{ ps}^{-1}$$

x= $\Delta m_s \cdot \tau_{Bs} = 25.5 \pm 0.6$



ATLAS and CMS: production of heavy quark-antiquark systems



Prompt-non prompt quarkonia

Also, to measure prompt and non-prompt yields simultaneously and disentangle the two contributions both CMS & ATLAS exploit a 2D mass and pseudo-proper time fit.



Observations of bottomium systems



Mesons with beauty and charm: Bc

B⁺ (**B**⁻) is the b-quark meson with the largest production rate composed of $u\bar{b}(\bar{u}b)$. **B**_c⁺ (**B**_c⁻) meson is a ground state of $\bar{b}c(b\bar{c})$ system and contains **two** heavy quarks of **different flavours** and its production **is then much rarer** $[\bar{b}b + \bar{c}c]$. **CMS** has reported the *inclusive* and *differential* ($y \& p_T$) $\sigma \cdot B$

 $B_c^{\pm} \rightarrow J/\psi (\rightarrow \mu \mu) \pi^{\pm} \qquad B^{\pm} \rightarrow J/\psi (\rightarrow \mu \mu) K^{\pm}$

Theoretical prediction uncertainties up to 40%: renormalization, factorization scales and the m_b dependencies.

Results from 4.77 fb⁻¹ Run I pp collisions @ 7 TeV : event selection based on displaced dimuon triggers.



Conclusions

- Proton collisions are really collisions between quarks and gluons, so Parton Distribution Functions fundamental to interpret the results
- Strong interactions are everywhere at the LHC, and jets are produced either alone on in association with many other objects
- Using secondary vertices and/or jet substructure it is possible to measure jets from b-quarks, t-quarks or bosons (even Higgs)
- Heavy quarks a fundamental "laboratory" due to large mass (perturbative calculations) and long lifetime
- CP-violating effects particularly relevant in third family
- Dedicated experiments (and accelerators!) built to extensively study quark mixing, all coherent with SM picture