

# Particle Detectors

*Lecture at the African School for Fundamental Physics and Applications,  
July 2024  
Marrakesh, Morocco*

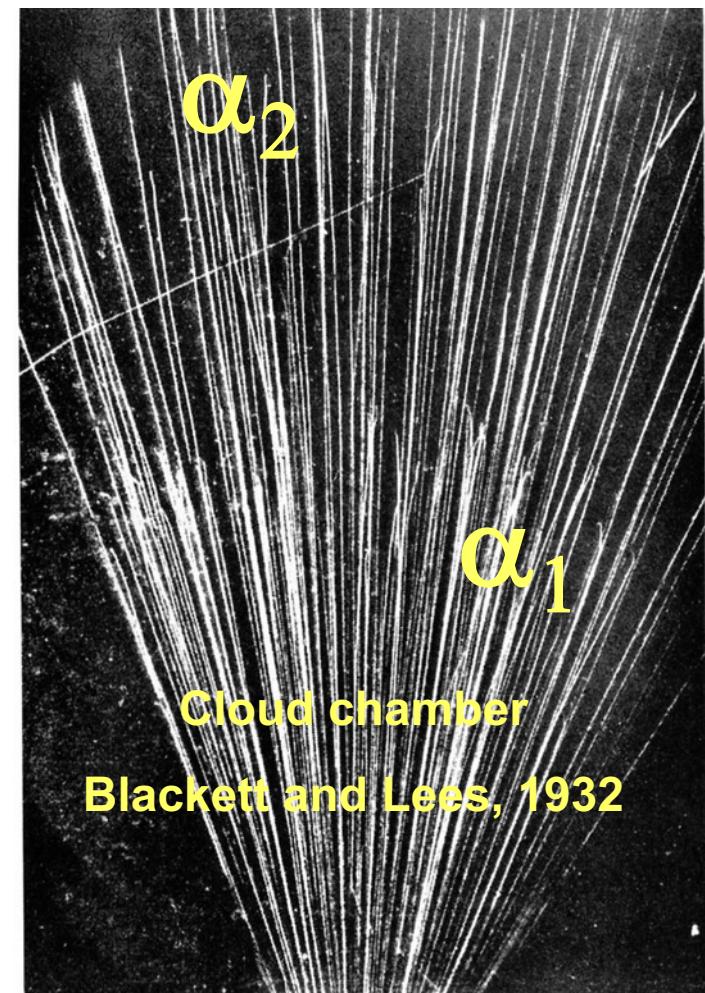
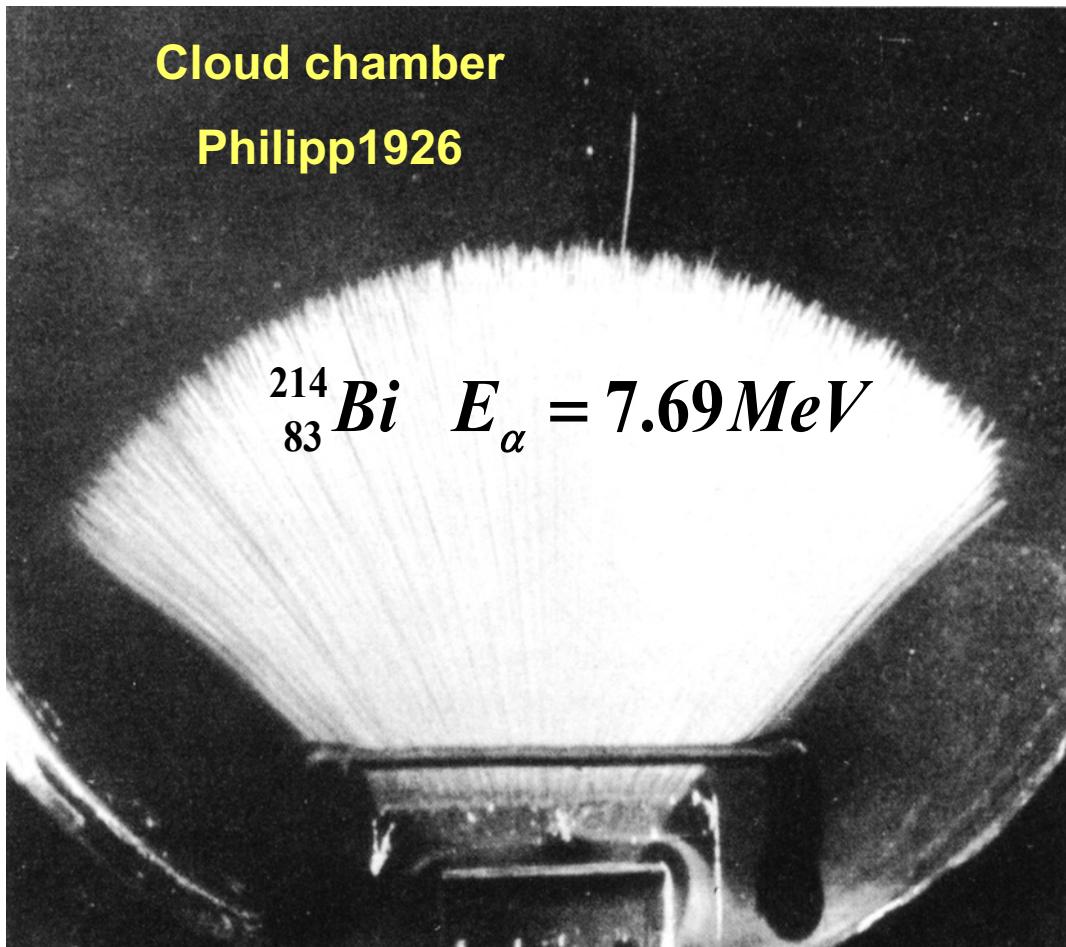
## Lecture I

*Interaction of radiation and particles with matter*

$$H^0 \rightarrow \mu^+ \mu^- \mu^+ \mu^-$$

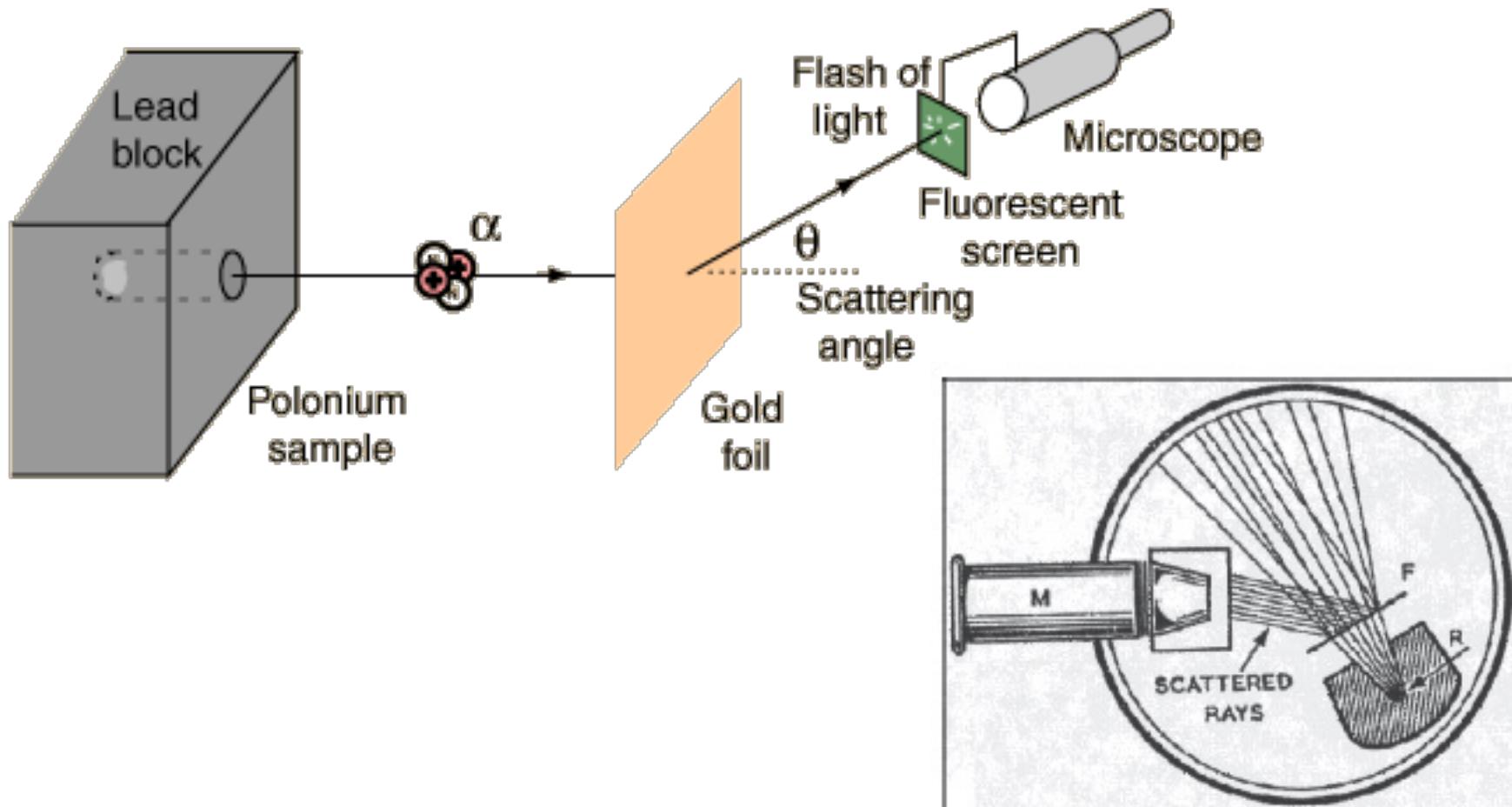
**CMS at the LHC**

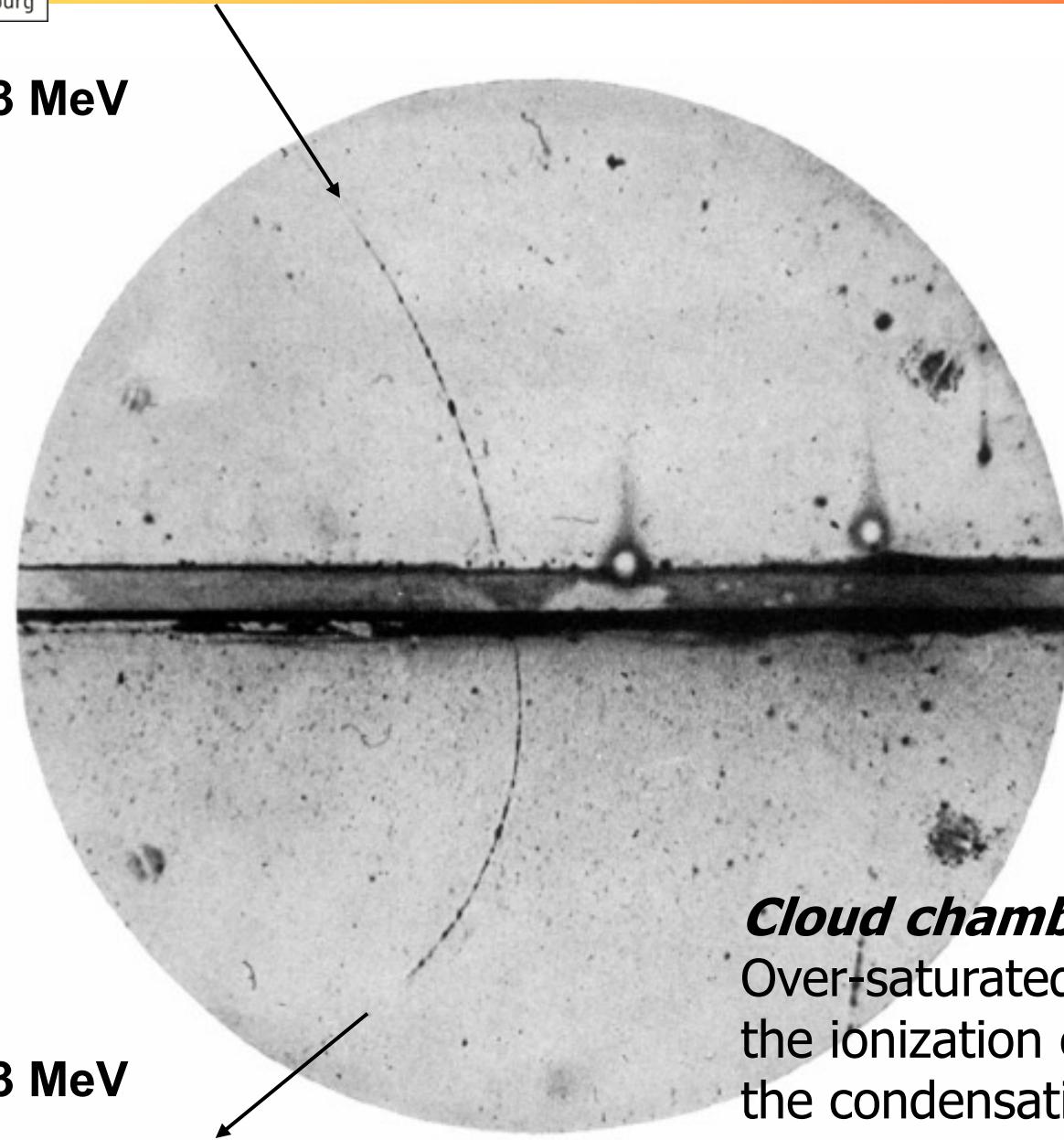
# Cloud Chamber



# Seeing particles: *Rutherford scattering*

## *Experiment by Hans Geiger and Ernest Marsden 1909*

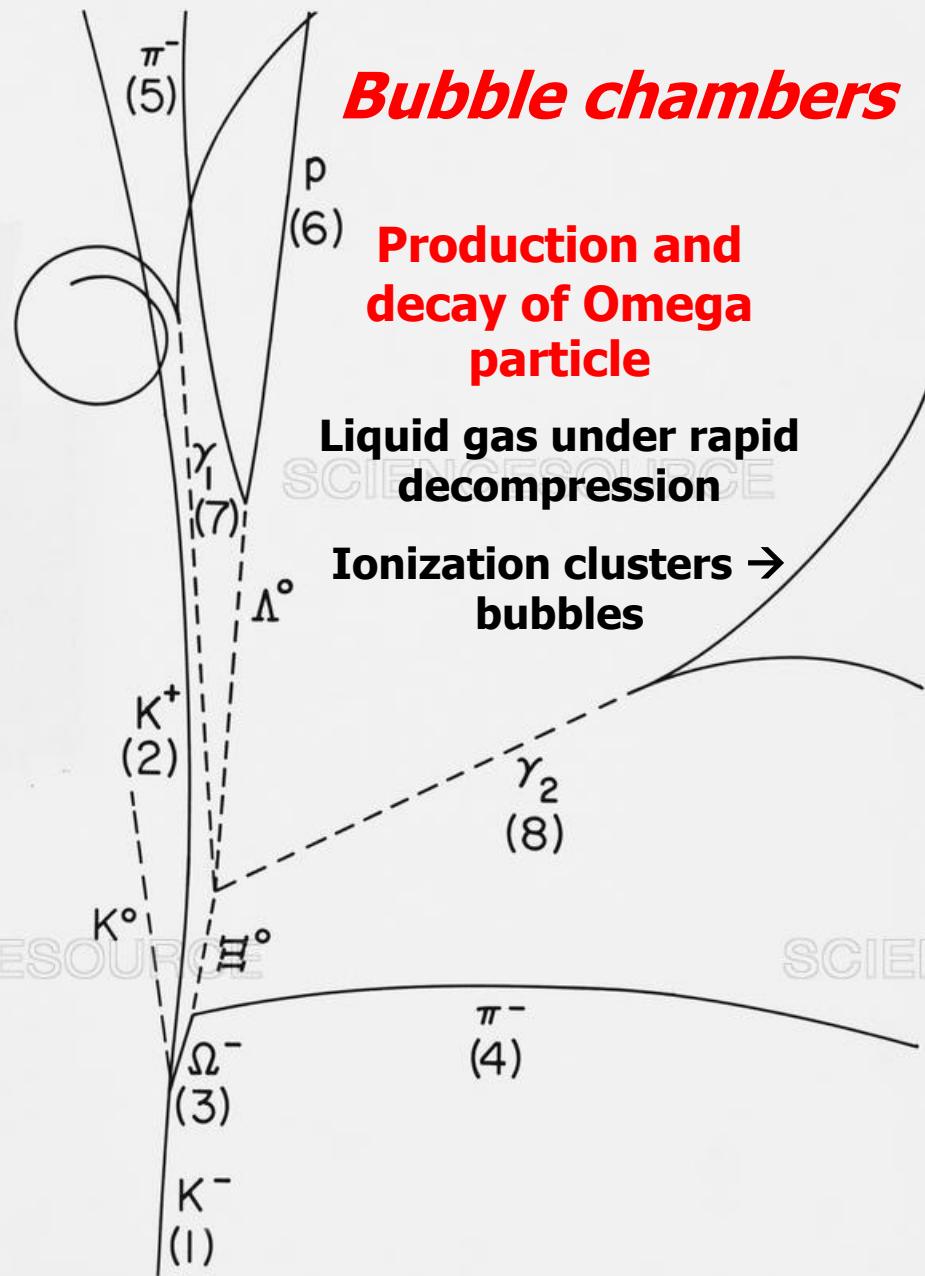
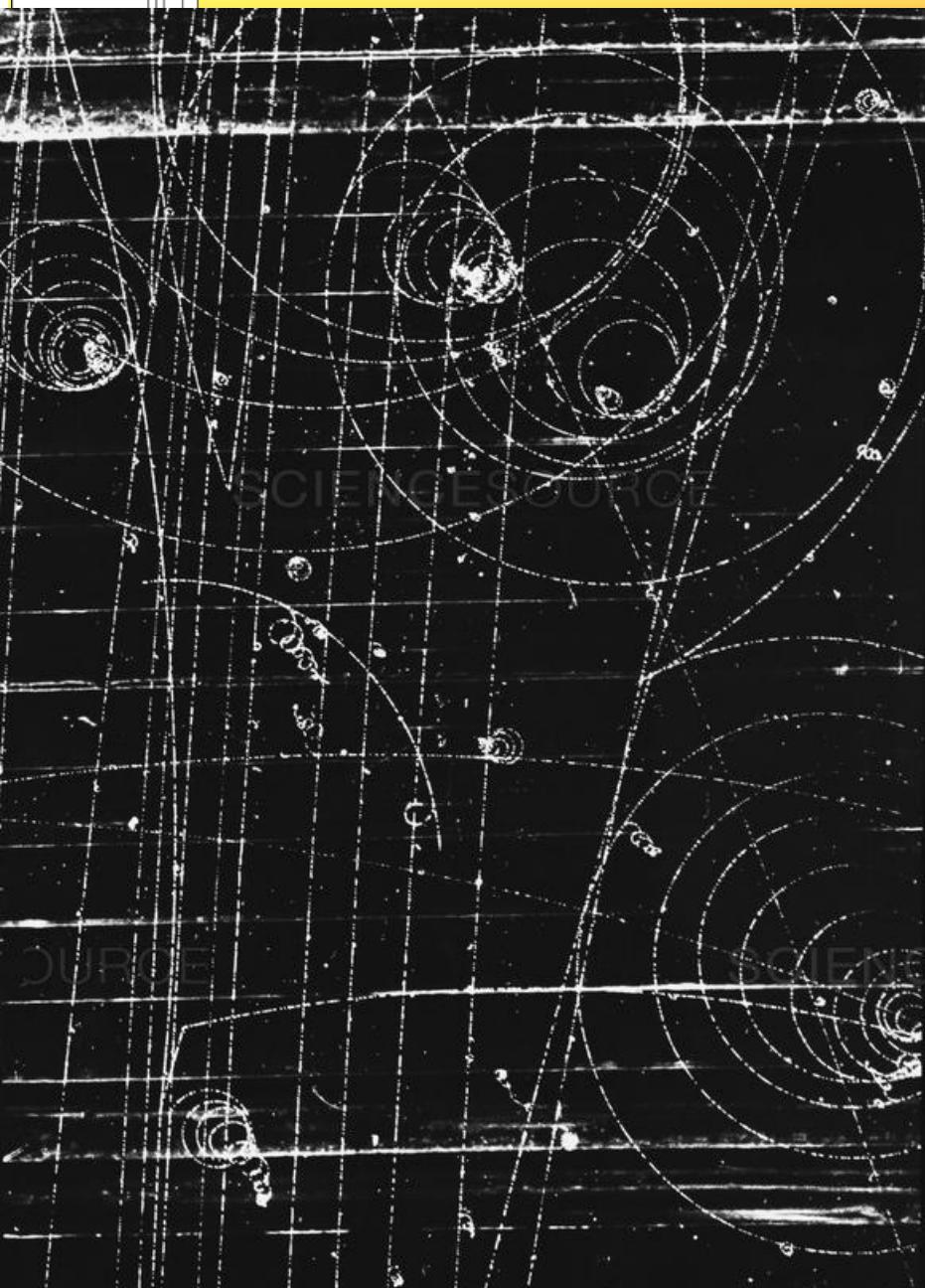




1932  
Discovery of  
the positron by  
C.D.Anderson

6 mm Pb

***Cloud chamber (C.T.R. Wilson)***  
Over-saturated vapour :  
the ionization clusters become  
the condensation nuclei



# Particle Detectors

*Lecture at the African School for Fundamental Physics  
Marrakesh, Morocco, July 2024*

Goal of these lectures:

to understand how nuclear and particle physics detectors work

## Lecture I

- Introduction
- Interaction of radiation and particles with matter

## Lecture II + III. Given by Sally Seidel

- The basics of detectors

## Lecture IV (tentative programme)

- High purity segmented Ge-detectors for Nuclear physics
- Recent developments of CMOS pixel detectors
- Fast detectors for time of flight measurements
- High granularity calorimeters
- Dark Matter detectors and other Exotics

# Particle Detectors

*Lecture at the African School for Fundamental Physics  
Nelson Mandela University in Gqeberha, 2022*

## *1st Lecture*

### **Introduction**

- The goal: measuring subatomic particles (E, p, charge,, mass, ....)
- Detection of particles, how do they interact with matter, what does the interaction depend on (E, p, charge,, mass, beta, gamma ....)

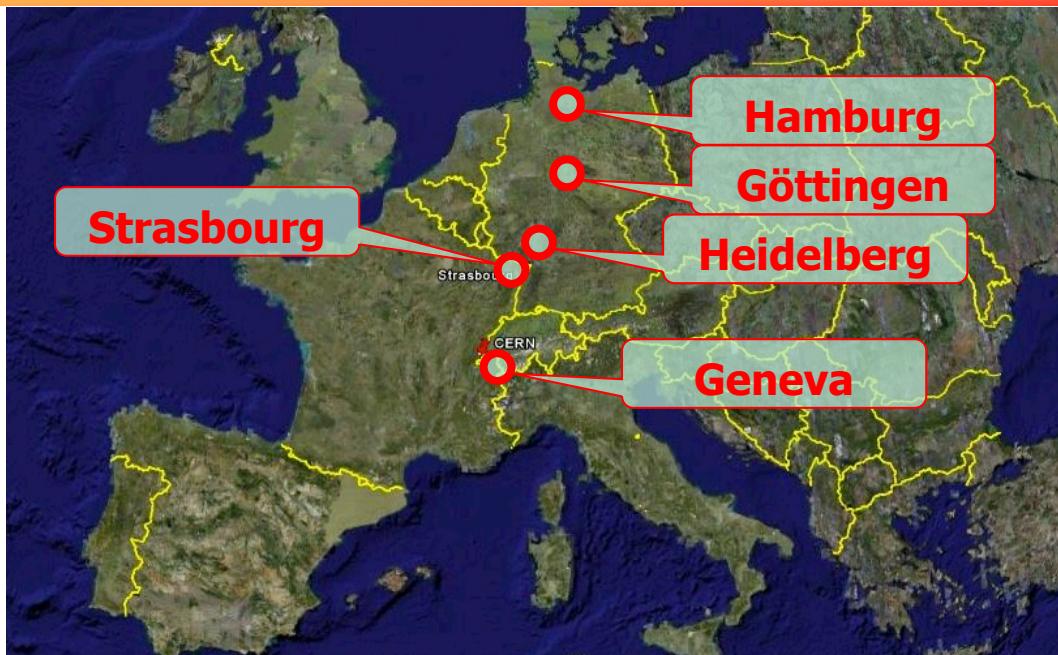
### **Interaction of particles and radiation with matter**

- Photons: PE, Compton, Pair creation
- Ionization/excitation, Bethe Bloch formula, range of particles, Bragg peak
- Electrons, Bremsstrahlung, critical energy, radiation length
- Electromagnetic showers of electrons and photons, (muons)
- Hadronic interactions → showers, interaction length, solid and atmospheric absorbers
- Multiple scattering
- Cerenkov, Transition radiation

### ***Exercises for the evening !!!!!***

# Who am I?

**Ulrich Goerlach**



- Born in Göttingen, Germany
- Physics (and Math) studies at the Universities Göttingen and Heidelberg
- Diploma (now Master) and PhD at the Max Planck Institute for Nuclear Physics in Heidelberg
- Post-doc (particle physics) at CERN, Geneva
- Researcher at University Heidelberg
- Researcher(staff) at CERN Geneva
- Researcher(staff) at DESY, Hamburg
- University Professor at the Unistra, (Université de Strasbourg)
- Professor émérité since 01/09/2022

# Bibliographie

## Text books :

- C. Grupen, Particle Detectors, Cambridge University Press, 1996, 2011
- G. Knoll, Radiation Detection and Measurement, 3rd ed. Wiley, 2000
- W. R. Leo, Techniques for Nuclear and Particle Physics Experiments, Springer, 1994
- K. Kleinknecht, Detectors for particle radiation , 2nd edition, Cambridge Univ. Press, 1998
- D. Green, The physics of Particle Detectors, Cambridge Univ. Press 2000, 2005
- S. Tavernier, Experimental Techniques in Nuclear and particle Physics, Springer 2010
- G. Lutz, Semiconductor Radiation Detectors, Springer, 1999
- W. Blum, L. Rolandi, Particle Detection with Drift Chambers, Springer, 1994
- R. Wigmans, Calorimetry, Oxford Science Publications, 2000

## Review Articles

- Experimental techniques in high energy physics, T. Ferbel (editor), World Scientific, 1991.
- Instrumentation in High Energy Physics, F. Sauli (editor), World Scientific, 1992.
- Many excellent articles can be found in Ann. Rev. Nucl. Part. Sci.
- ...
- . CERN-Summer student lectures and academic training...

## **Acknowledgements**

- Many thanks to all my colleagues who have prepared lectures like this one in the past and from which I profited a lot!!!
- I tried to quote the authorship of the slides I took from theses lectures and I apologize for the cases in which I forgot or could not trace them anymore

# *Photons at low energy*

# Interaction of photons with matter

- **Photo-electric effect** Absorption of  $\gamma$ ; dominant for  $E_\gamma \leq 0.1\text{-}1 \text{ MeV}$
- **Compton effect** Diffusion  $\gamma \rightarrow \gamma'$  Dominant for  $0.1 \leq E_\gamma \leq 10 \text{ MeV}$
- **Creation of (e<sup>+</sup>e<sup>-</sup>)-pairs** Absorption de  $\gamma$   $E_\gamma \geq 1.022 \text{ MeV}$
- Nuclear photo-electric and photo-nuclear reaction are very rare!

Statistical processes governed by a cross section:

(reaction rate per unit of flux)  $\sigma_I$  (1 barn =  $10^{-24}\text{cm}^2$ ):

Intensity (number of  $\gamma$  behind an absorber of depth x, [x]=g/cm<sup>2</sup>)

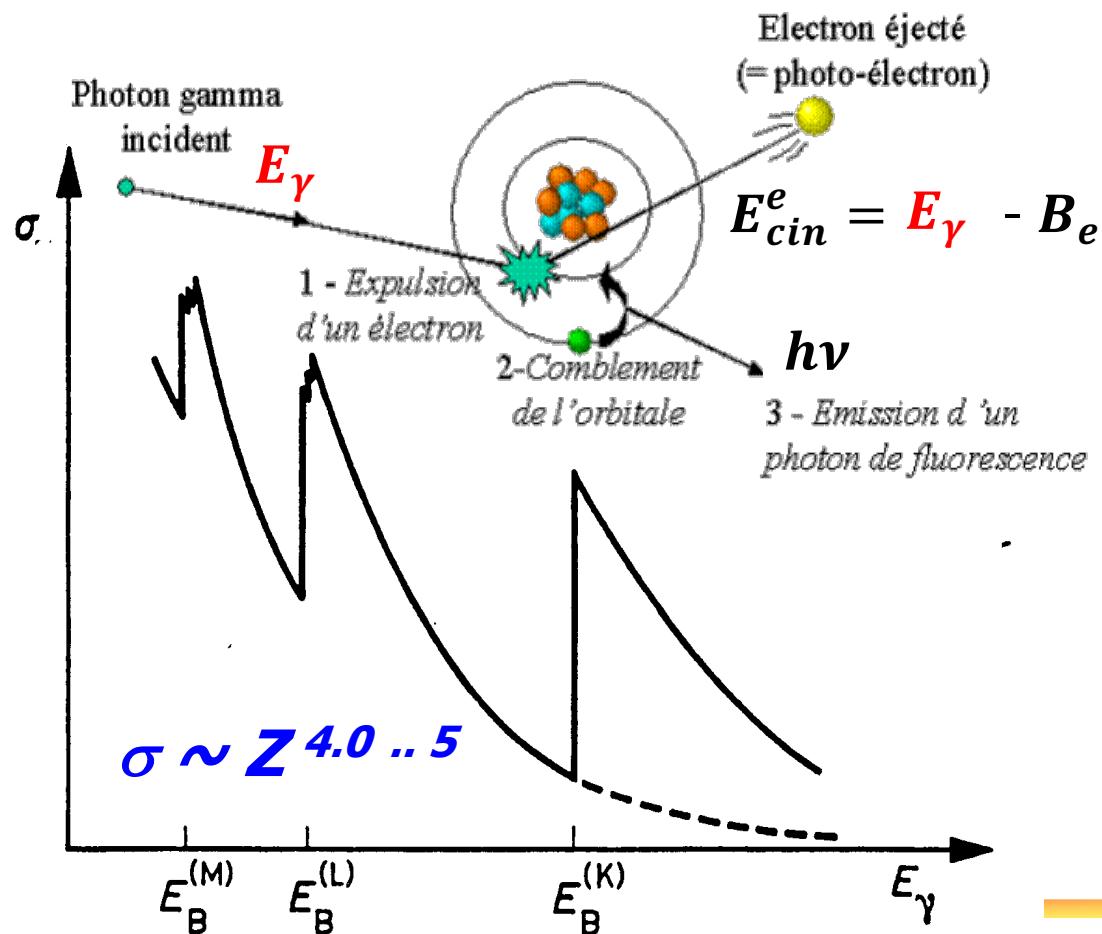
$$I = I_o \exp(-\mu x) \quad (dI = -I \mu dx)$$

$\mu$  = Attenuation or/and absorption coefficient;  $[\mu] = \text{cm}^2/\text{g}$

$\mu = N_A/A(g) \cdot \Sigma_i \sigma_i$ ;  $N_A$  Avogadros number, A=atomic weight in gramme

# Photo-electric effect

$$\sigma_{p.e.}^K \Big|_{atom} = \sqrt{\frac{32}{\left(\frac{E_\gamma}{m_e c^2}\right)^7}} \cdot Z^5 \alpha^4 \times \underbrace{\left(\frac{8}{3} \pi r_e^2\right)}_{r_e = \frac{e^2}{4\pi\epsilon_0 m_e c^2}} \times \text{corrections}$$

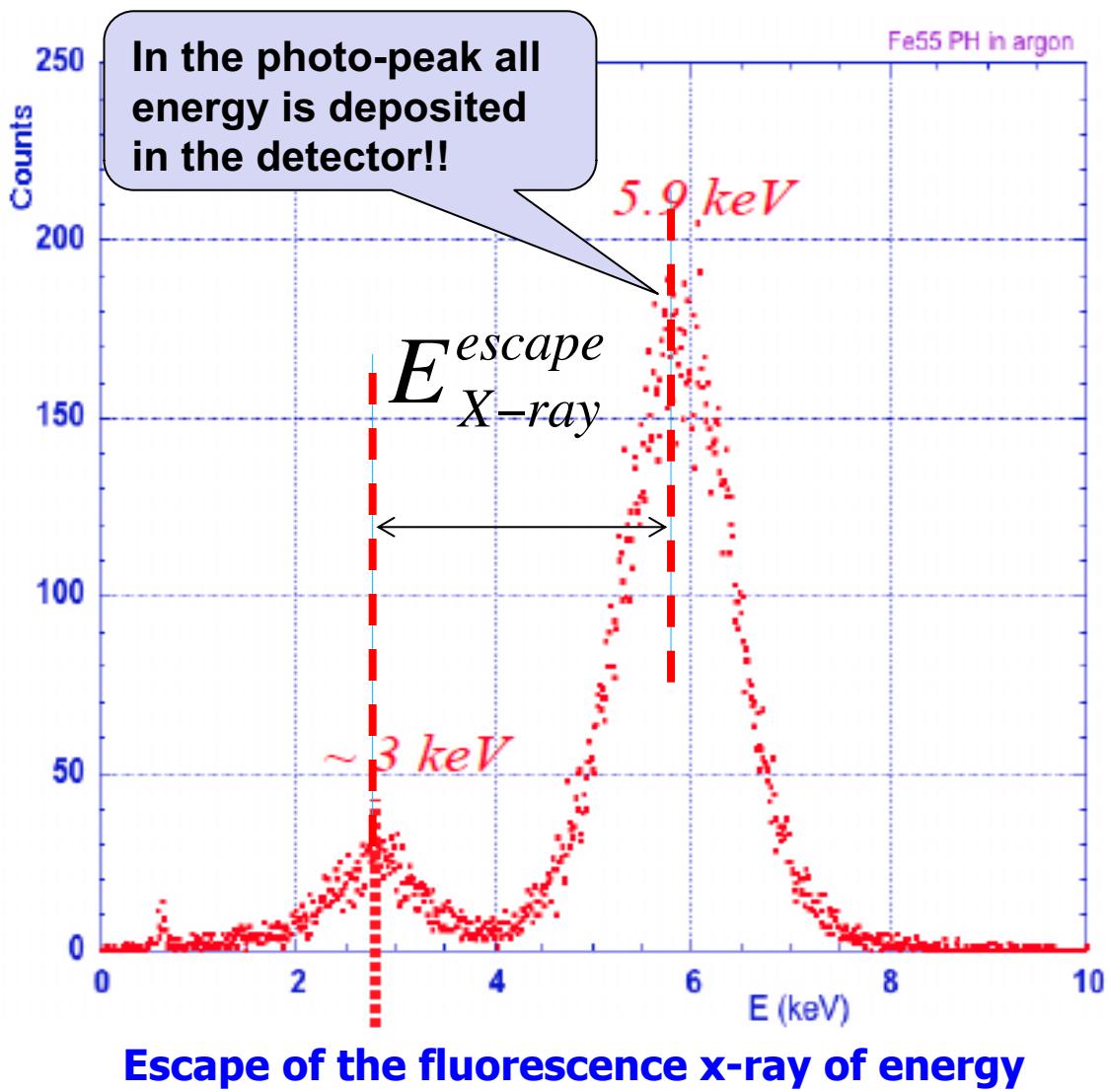


- At high  $Z$ , the hole in the K-shell is filled by an electron under the emission of a fluorescence x-ray of energy  $E_{h\nu} = E_K - E_{L,M,N}$

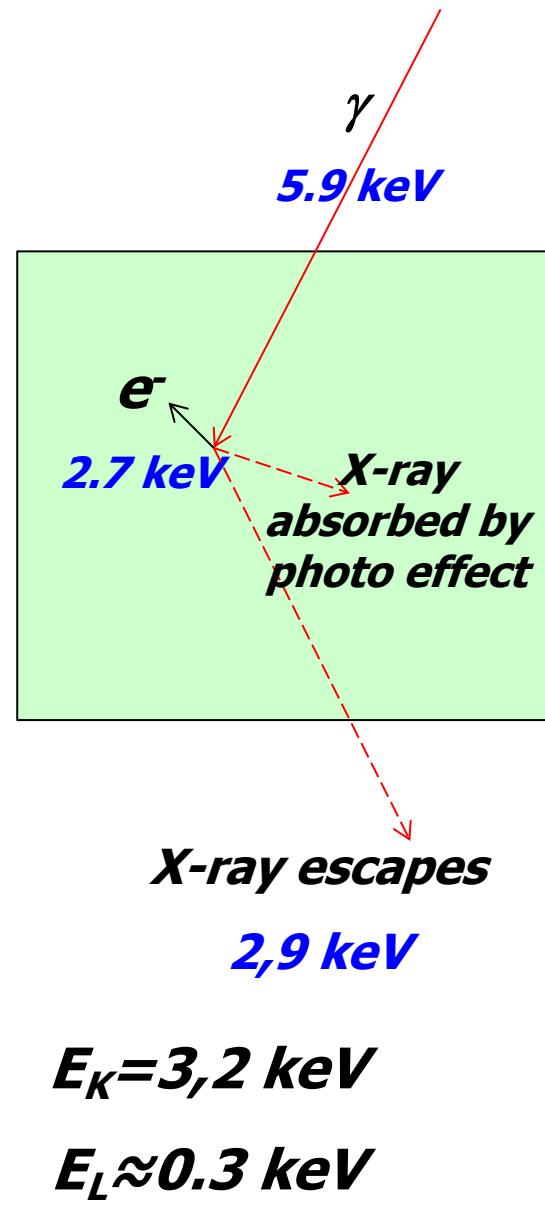
- At low  $Z$ , Auger electrons occur: electrons of higher shells (L) are ejected with energy

$$E_{Auger} = E_K - 2E_L$$

## X-RAY ABSORPTION SPECTRUM $^{55}\text{Fe}$ X-Rays (5.9 keV) in Argon:



$$E_X = E_K - E_{L,M,N} = 3.2 - 0.3 = 2.9 \text{ keV}$$



# Compton-effect

**Scattering of a gamma on a “free” electron**

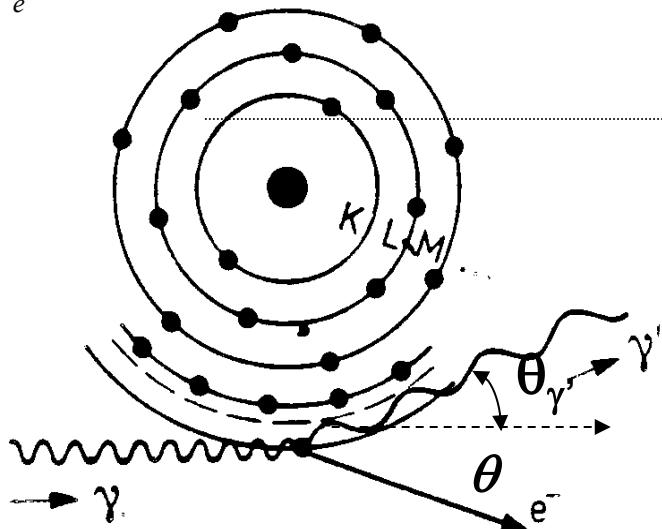
$$hv' = \frac{hv}{1 + \varepsilon(1 - \cos\theta_{\gamma'})};$$

$$\varepsilon = hv / m_e c^2$$

$$T_e = hv - hv'$$

$$\Delta\lambda = \lambda' - \lambda = \frac{\hbar c}{m_e c^2} (1 - \cos\theta_{\gamma'})$$

$$\lambda_c = \frac{\hbar c}{m_e c^2}$$
 Compton wave length of an electron

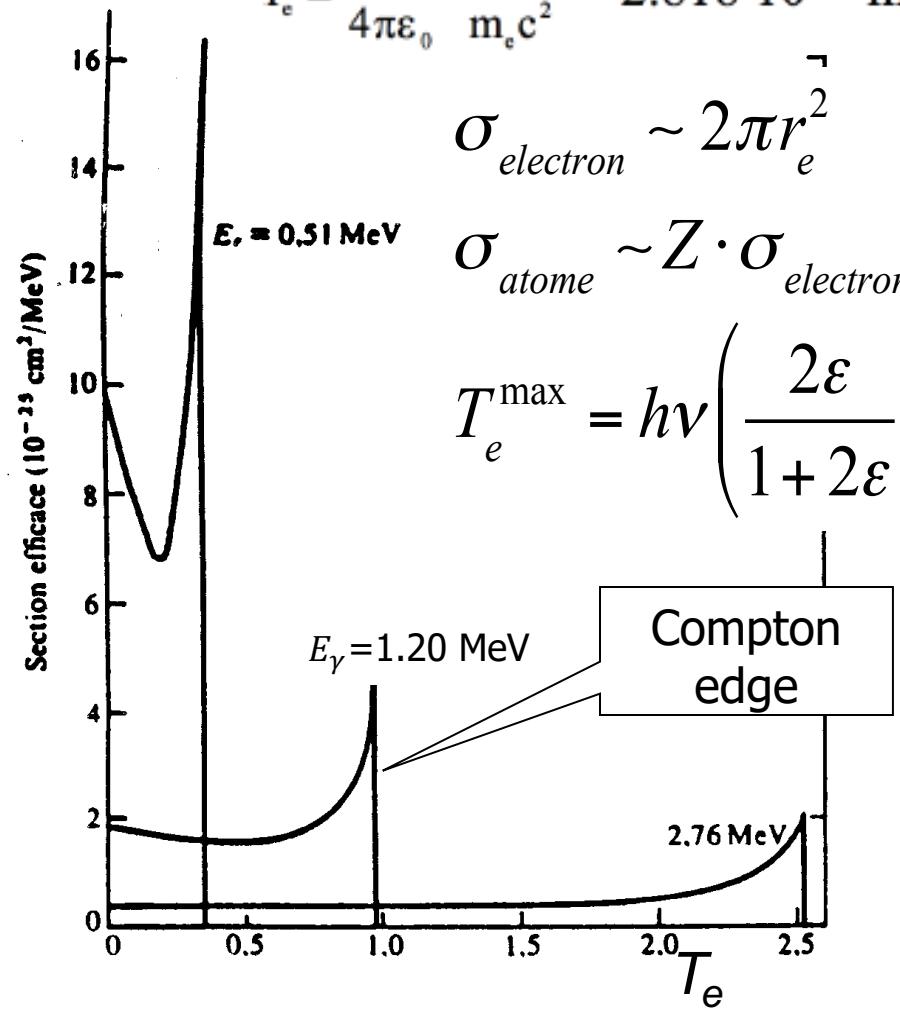


$$r_e = \frac{1}{4\pi\varepsilon_0} \cdot \frac{e^2}{m_e c^2} = 2.818 \cdot 10^{-15} \text{ m}$$

$$\sigma_{electron} \sim 2\pi r_e^2$$

$$\sigma_{atome} \sim Z \cdot \sigma_{electron}$$

$$T_e^{\max} = h\nu \left( \frac{2\varepsilon}{1 + 2\varepsilon} \right)$$



Compton  
edge

# Kinematics of Compton scattering exercise !!

*longitudinal momentum conservation:*

$$p_\gamma = \frac{h\nu}{c} = \frac{h\nu'}{c} \cos\theta_{\gamma'} + |\vec{p}_e| \cos\theta_{e'}$$

$$h\nu' = \frac{h\nu}{1 + \varepsilon(1 - \cos\theta_{\gamma'})};$$

$$\varepsilon = h\nu / m_e c^2$$

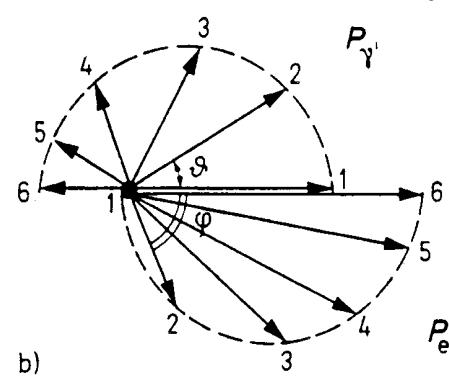
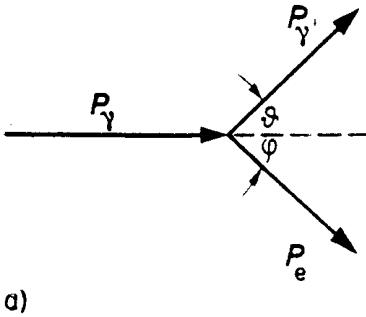
*transversal momentum conservation::*

$$0 = \frac{h\nu'}{c} \sin\theta_{\gamma'} - |\vec{p}_e| \sin\theta_{e'}$$

$$\Delta\lambda = \lambda' - \lambda = \frac{hc}{m_e c^2} (1 - \cos\theta_{\gamma'})$$

*Energy conservation:*  $T_e = h\nu - h\nu'$

$$\lambda_c = \frac{hc}{m_e c^2} \text{ longueur d'onde de Compton d'un électron}$$



a)

b)

## The Klein-Nishina formula

$$\frac{d\sigma}{d\omega} = Zr_0^2 \left( \frac{1}{1 + \alpha(1 - \cos\theta)} \right)^2 \left( \frac{1 + \cos^2\theta}{2} \right) \left( 1 + \frac{\alpha^2(1 - \cos\theta)^2}{(1 + \cos^2\theta)[1 + \alpha(1 - \cos\theta)]} \right)$$

$$h\nu' = \frac{h\nu_0}{1 + \alpha(1 - \cos\theta)} \quad \text{with} \quad \alpha = \frac{h\nu_0}{m_0 c^2}$$

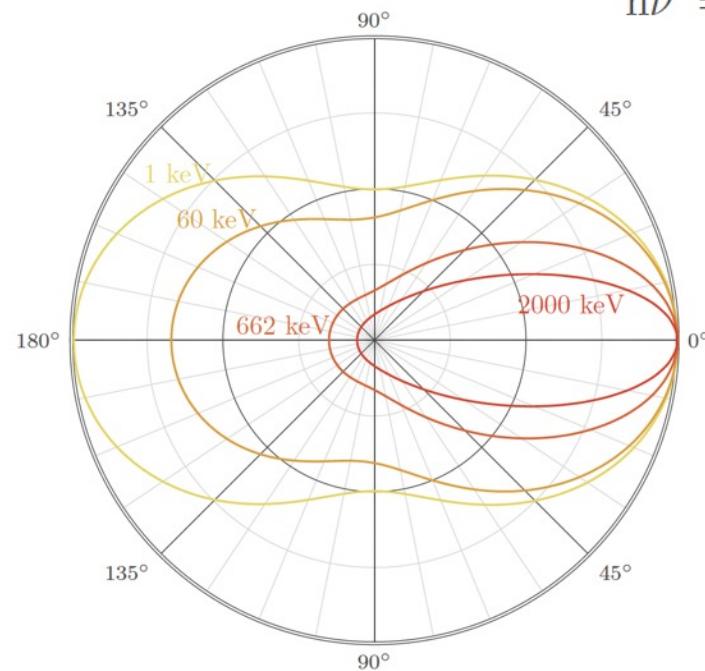
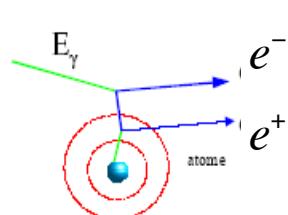


Figure 1.2: Probability of Compton scattering as a function of the scattering angle  $\theta$  for an incident  $\gamma$ -ray coming from the left. The different curves correspond to various initial energies.

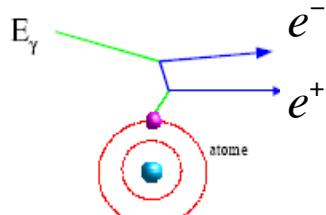
# Creation of electron positron pairs



In the field of a nucleus

$$E_\gamma \geq 2m_e + \frac{2m_e^2}{m_N}$$

$$m_N \gg m_e \Rightarrow E_\gamma \geq 2m_e$$

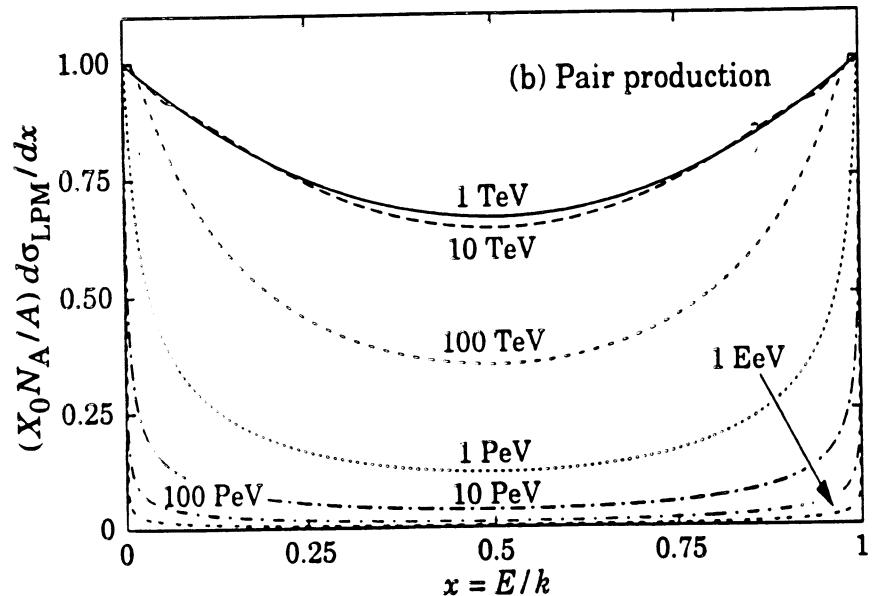
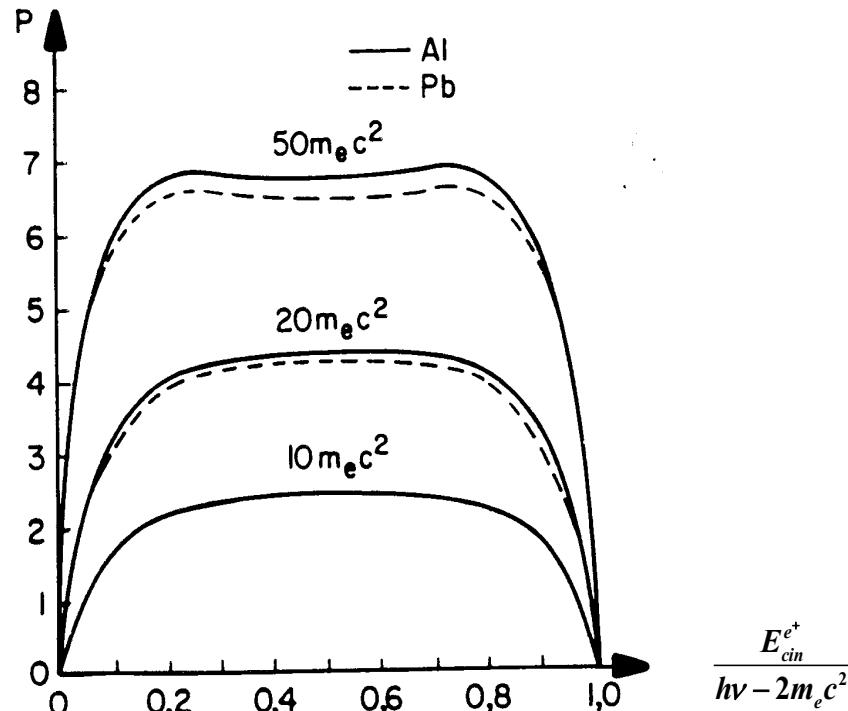


In the field of an electron

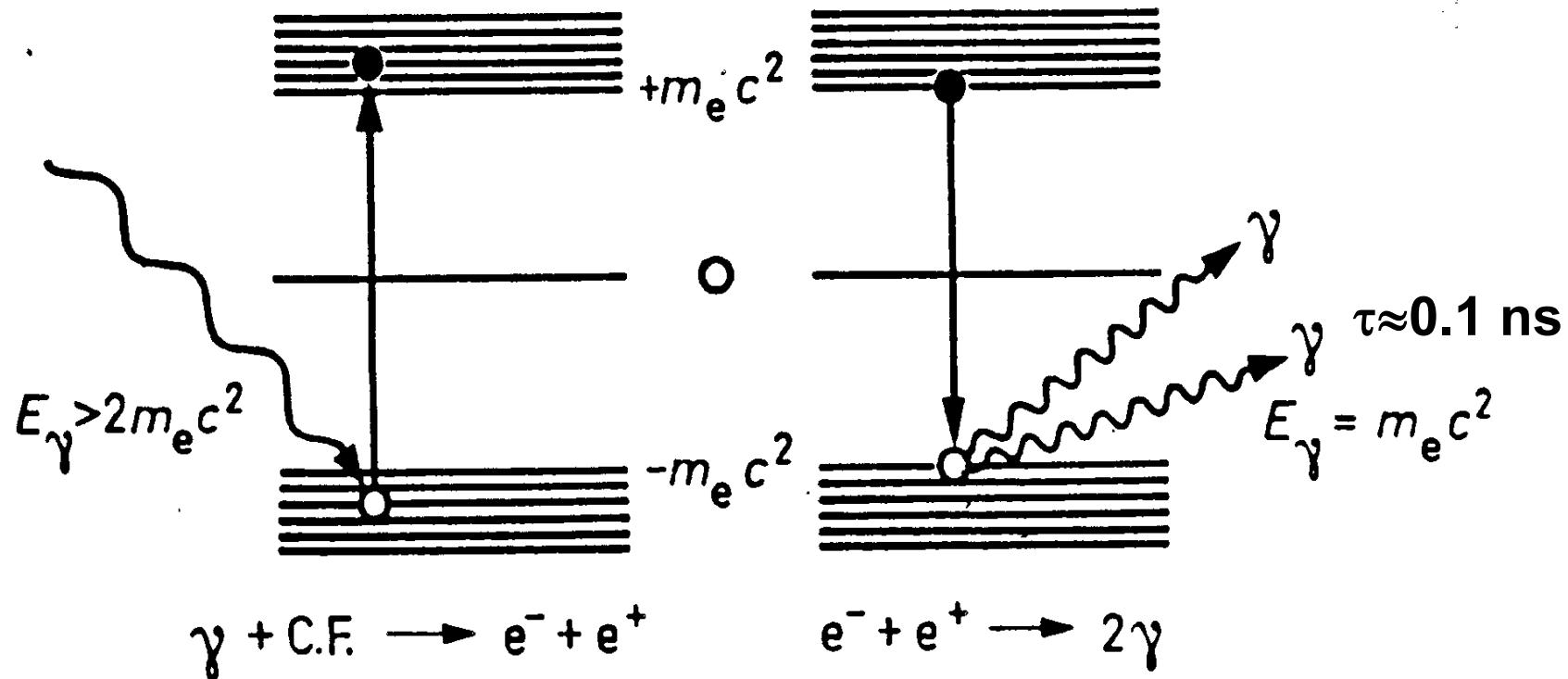
$$\sigma_{pair} \approx \frac{7}{9} \frac{A(g)}{N_A} \cdot \frac{1}{X_0} \sim Z(Z+1)$$

$$\mu_{pair} = \frac{N_A}{A} \sigma_{pair} \approx \frac{7}{9} \frac{1}{X_0} ; \lambda_{pair} = \frac{1}{\mu_{pair}} = \frac{9}{7} X_0$$

$X_0$  = radiation length



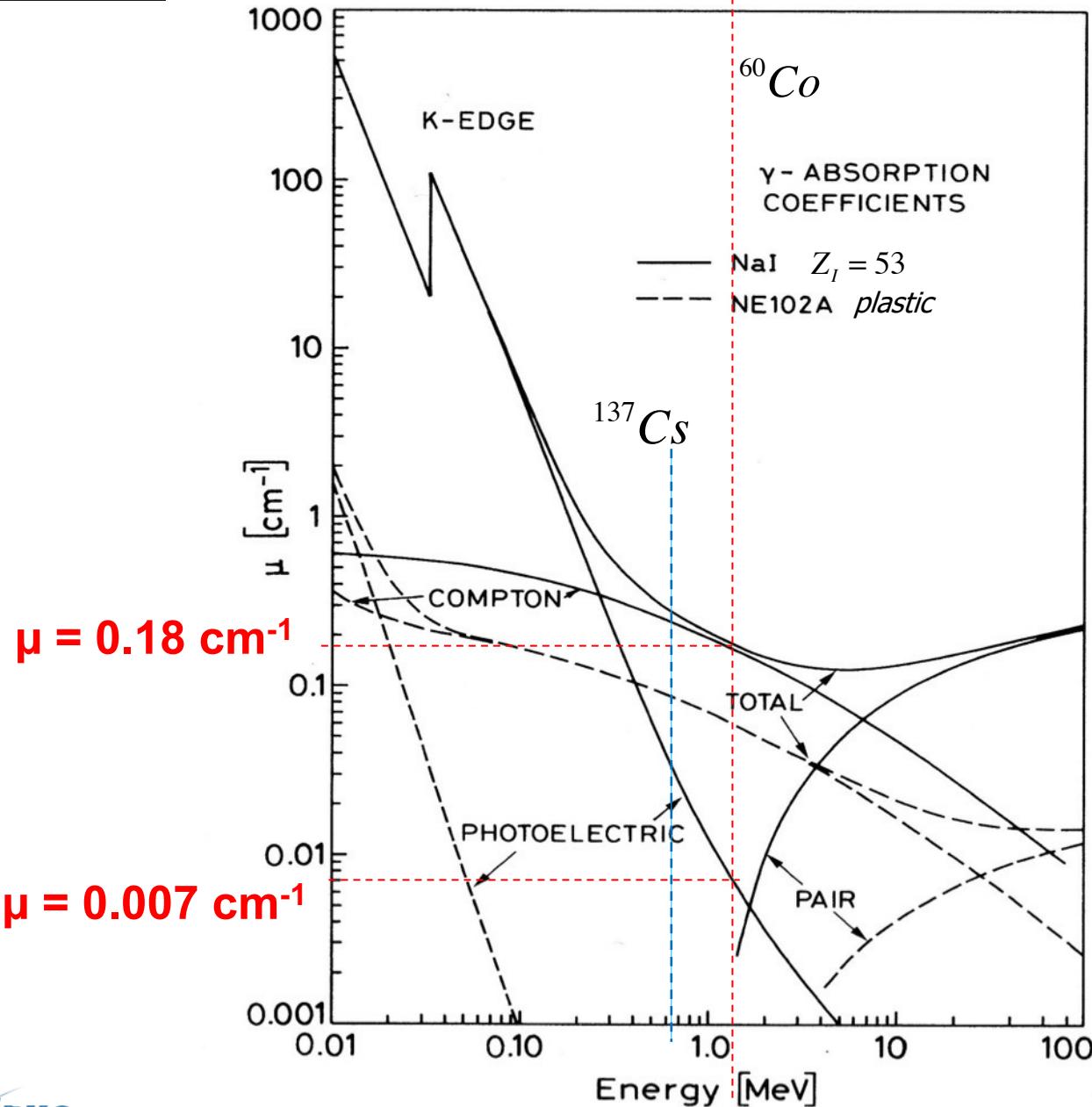
# Creation and annihilation of electron positron pairs



Only in the presence of a nucleus, cannot occur in free space !

!!!!  $\gamma \gg (e^+ e^-)$ : photon( $E_\gamma = h\nu, P_\gamma = h\nu/c$ );  $E_\gamma = E_{ee}$ !

$$\text{electron - pair : } E_{ee} = 2\gamma m_e c^2, P_{ee} = 2\gamma m_e v_e = \frac{h\nu}{c} \frac{\nu}{c} = \frac{h\nu}{c} \beta \neq P_\gamma$$



## Photo-electric effect

### Absorption of $\gamma$

## Compton scattering

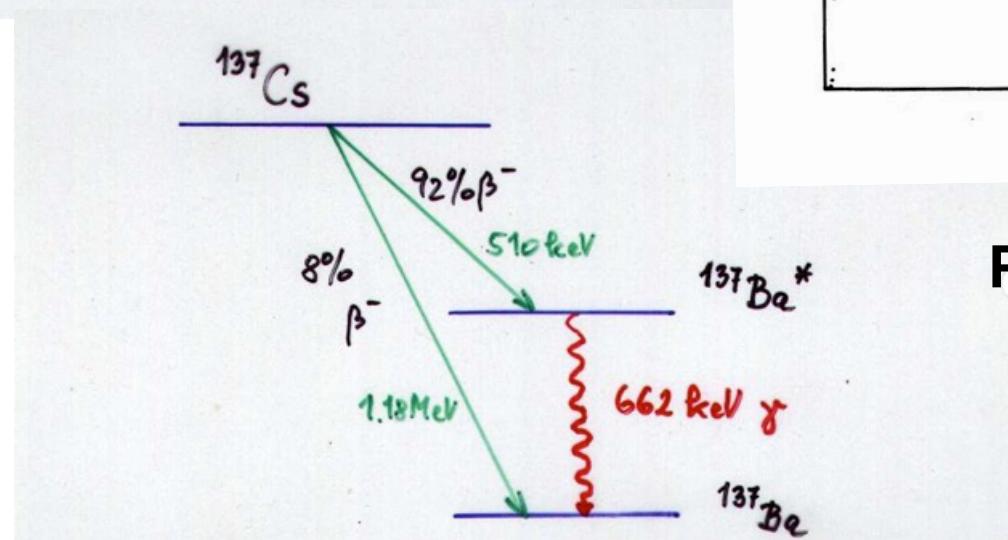
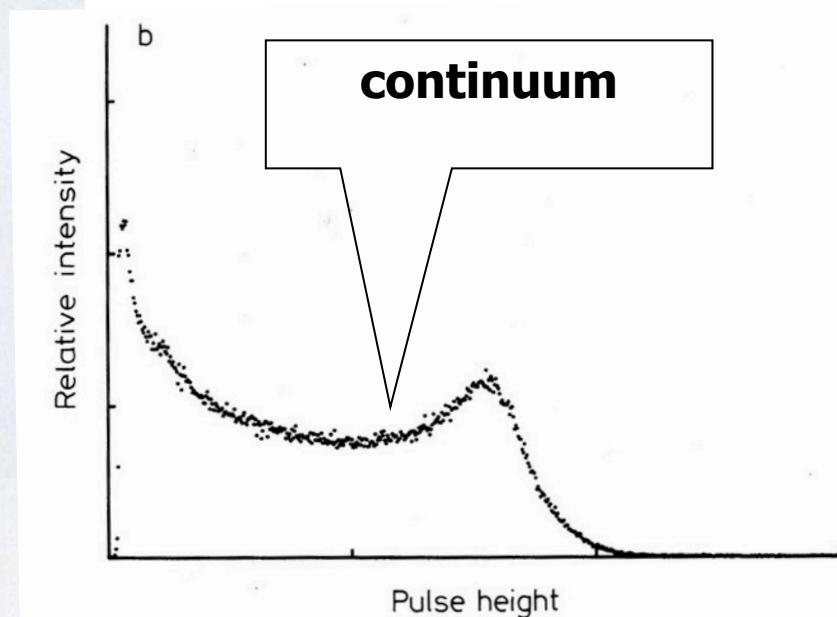
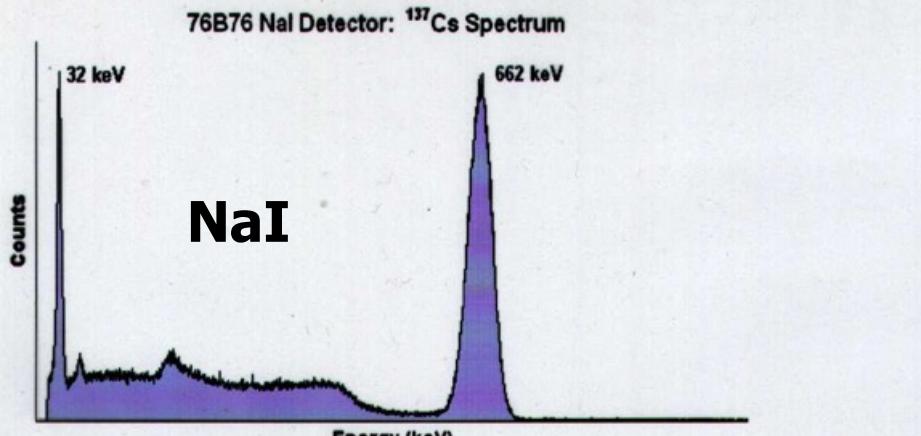
### scattering $\gamma \rightarrow \gamma'$

## Creation of $(e^+e^-)$ pairs

### Absorption of $\gamma$

# Response function of a Scintillator

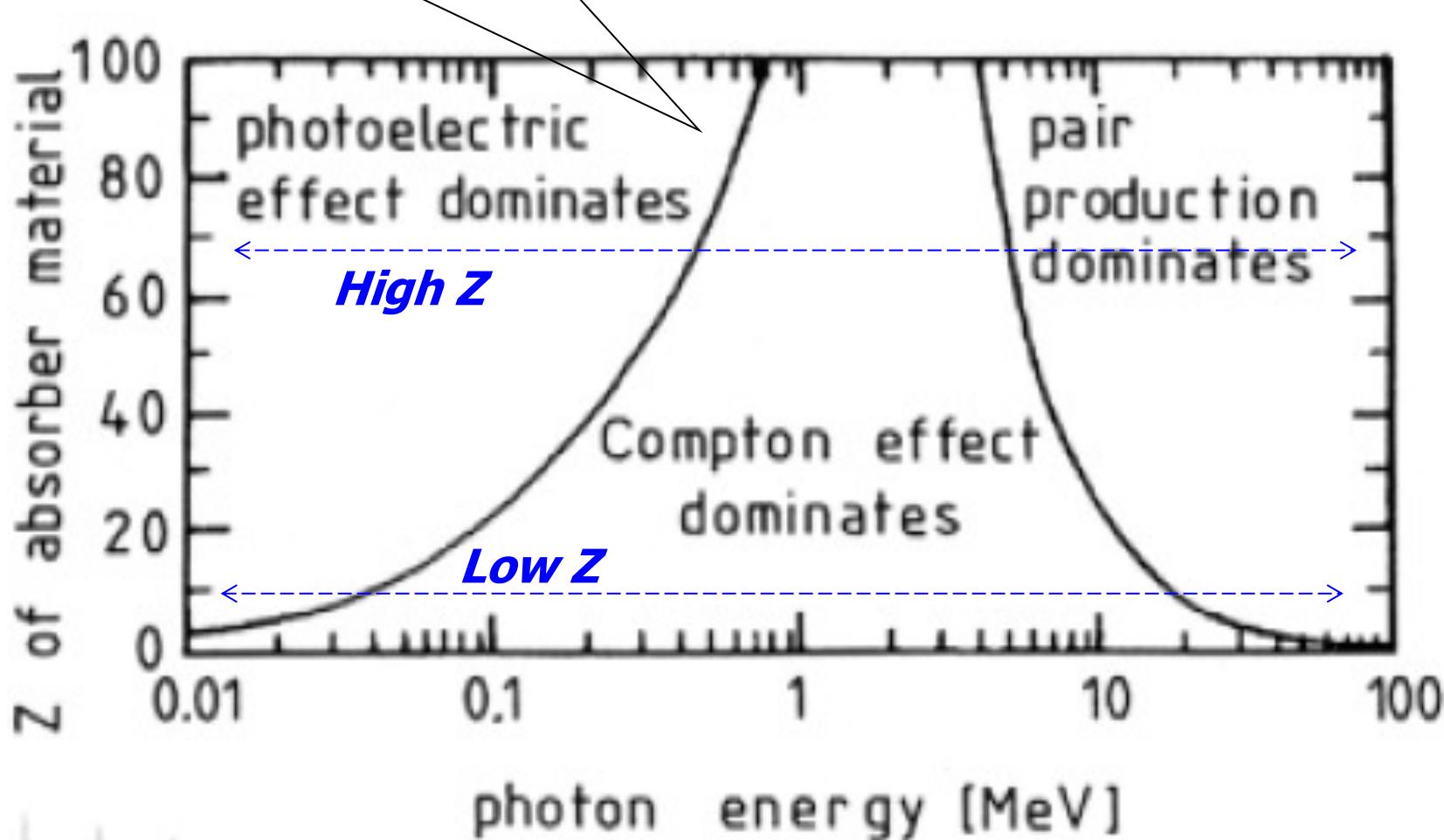
Two examples of how a scintillator responds to mono-energetic photons



Plastic Scintillator

Regions where one process is dominant, not exclusive !

## Interaction of photons with matter



# Attenuation length of photons

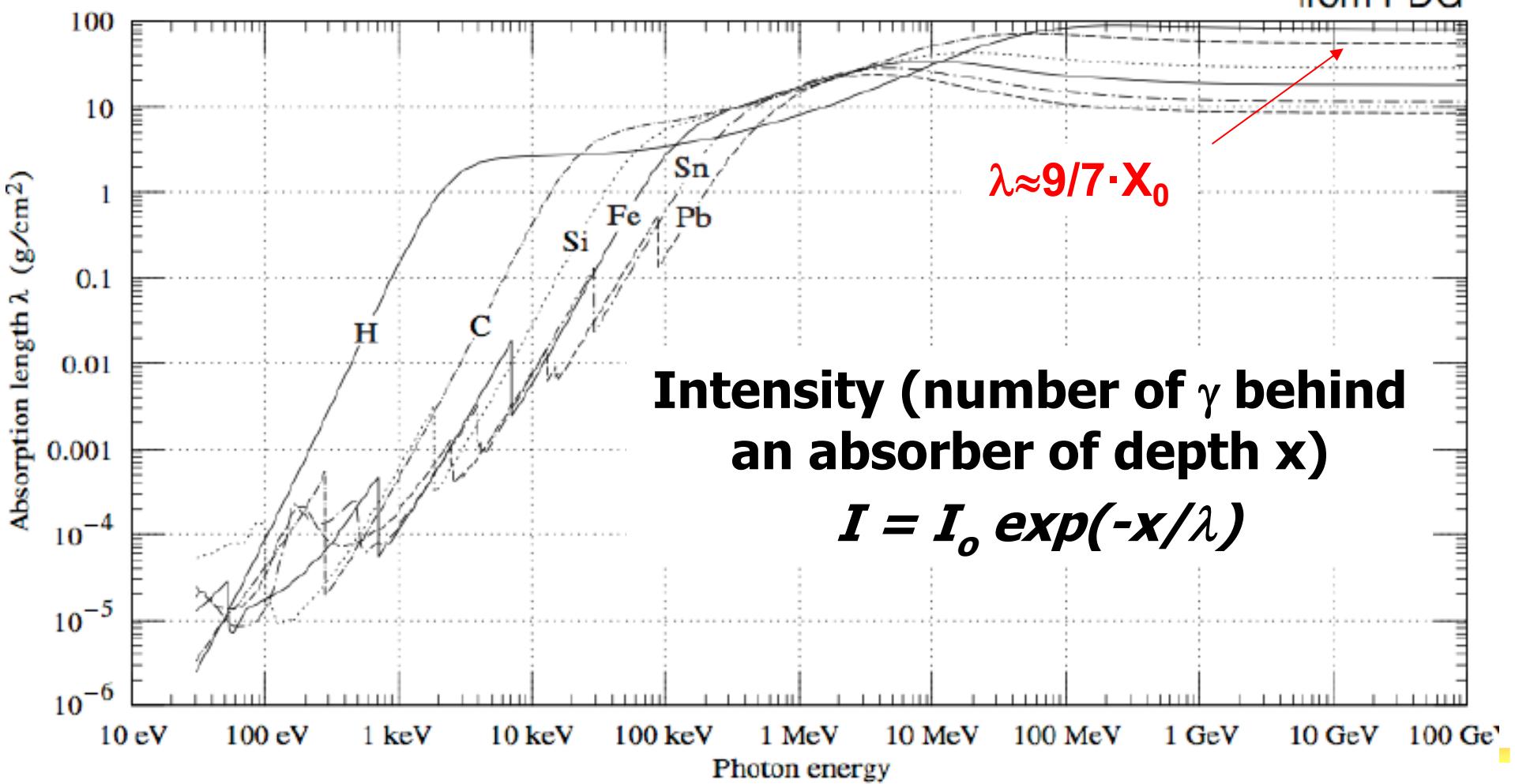
Mass absorption coefficient  $\lambda = 1/(\mu/\rho)$  [g.cm<sup>2</sup>] with  $\mu=N_A\sigma/A$

$$\sigma_{Ph} \propto \frac{Z^5}{E^{3.5}}$$

$$\sigma_{Compton} \propto \frac{\ln E}{E} \cdot Z$$

$$\sigma_{Pair} \propto Z^2$$

from PDG



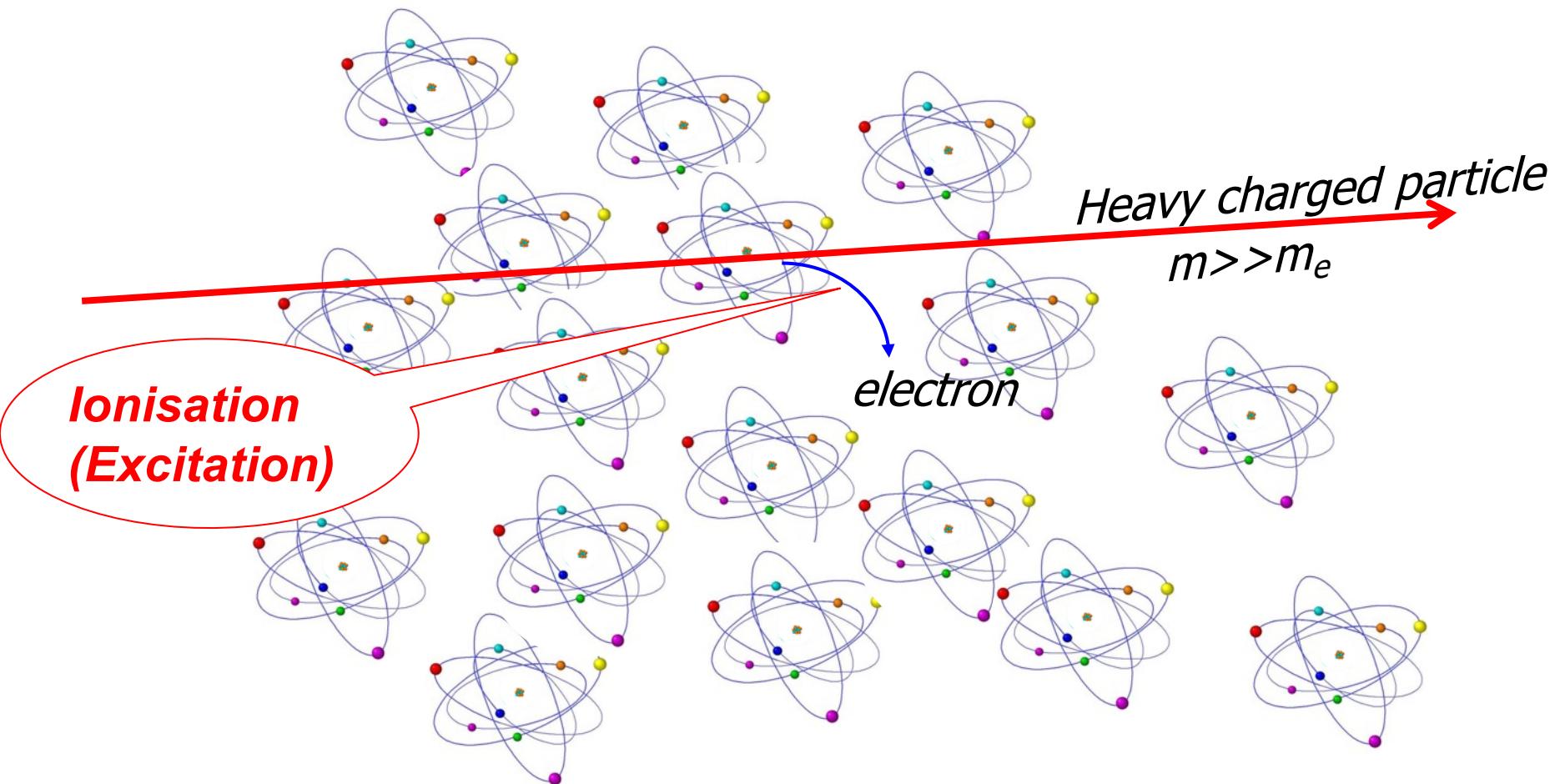
Intensity (number of  $\gamma$  behind  
an absorber of depth x)

$$I = I_o \exp(-x/\lambda)$$

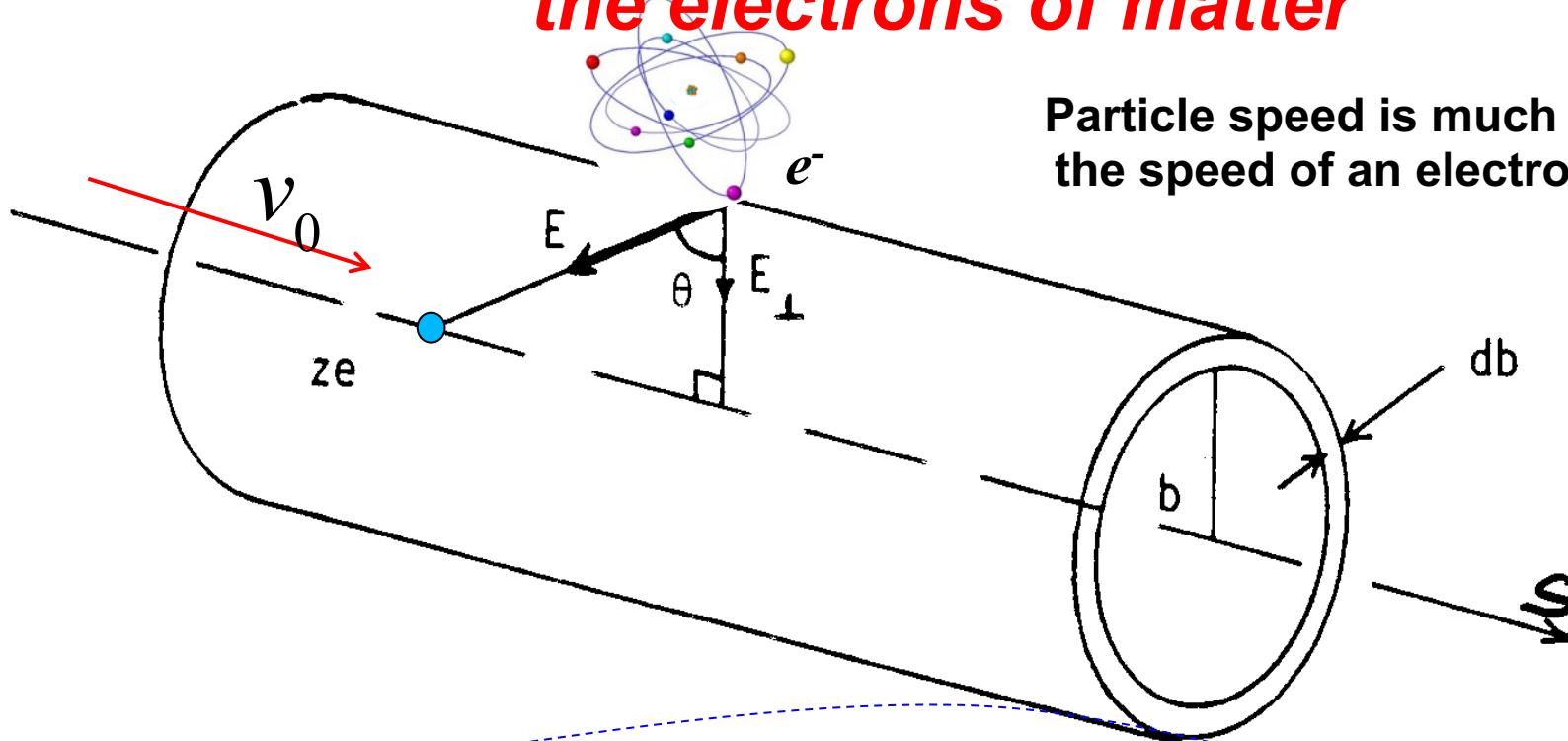
# *Questions ???*

# Charged « heavy particles »

## Coulomb interaction



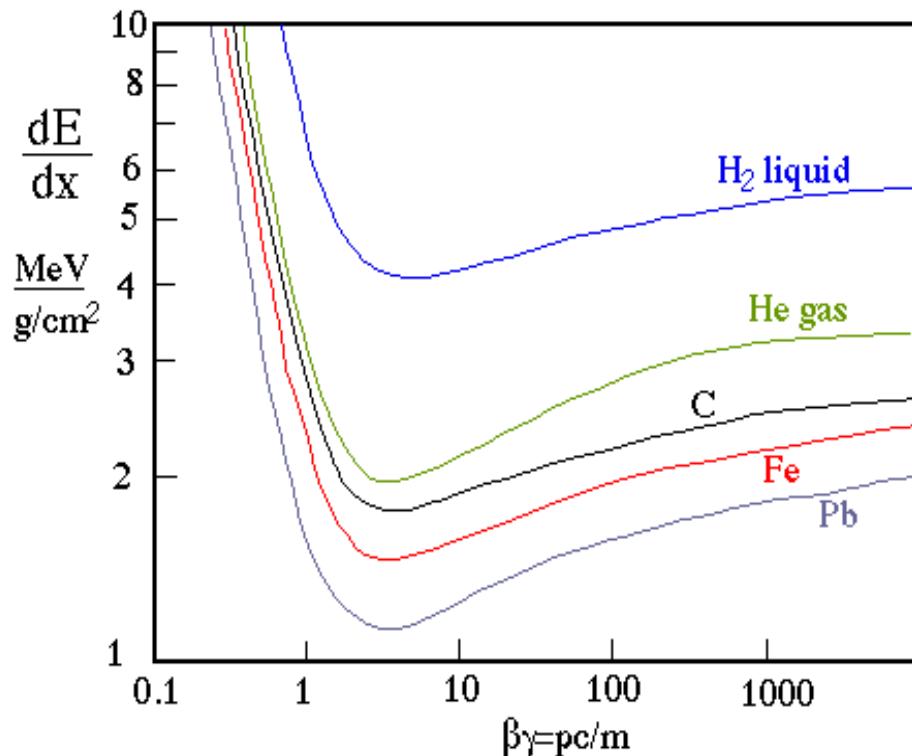
# Interaction of charged “heavy” particles with the electrons of matter



Particle speed is much larger than the speed of an electron bound to a nucleus

$$-\frac{dE}{ds} = -\int_0^\infty \frac{dE}{db} db = \frac{4\pi z^2 e^4 k^2}{m_e v_0^2} n_e \ln \frac{b_{\max}}{b_{\min}}$$
$$k = \frac{1}{4\pi\epsilon_0}$$

# Bethe – Bloch formula



$x = \text{surface density}$

$$-\frac{dE}{dx} = -\frac{1}{\rho} \frac{dE}{ds}$$

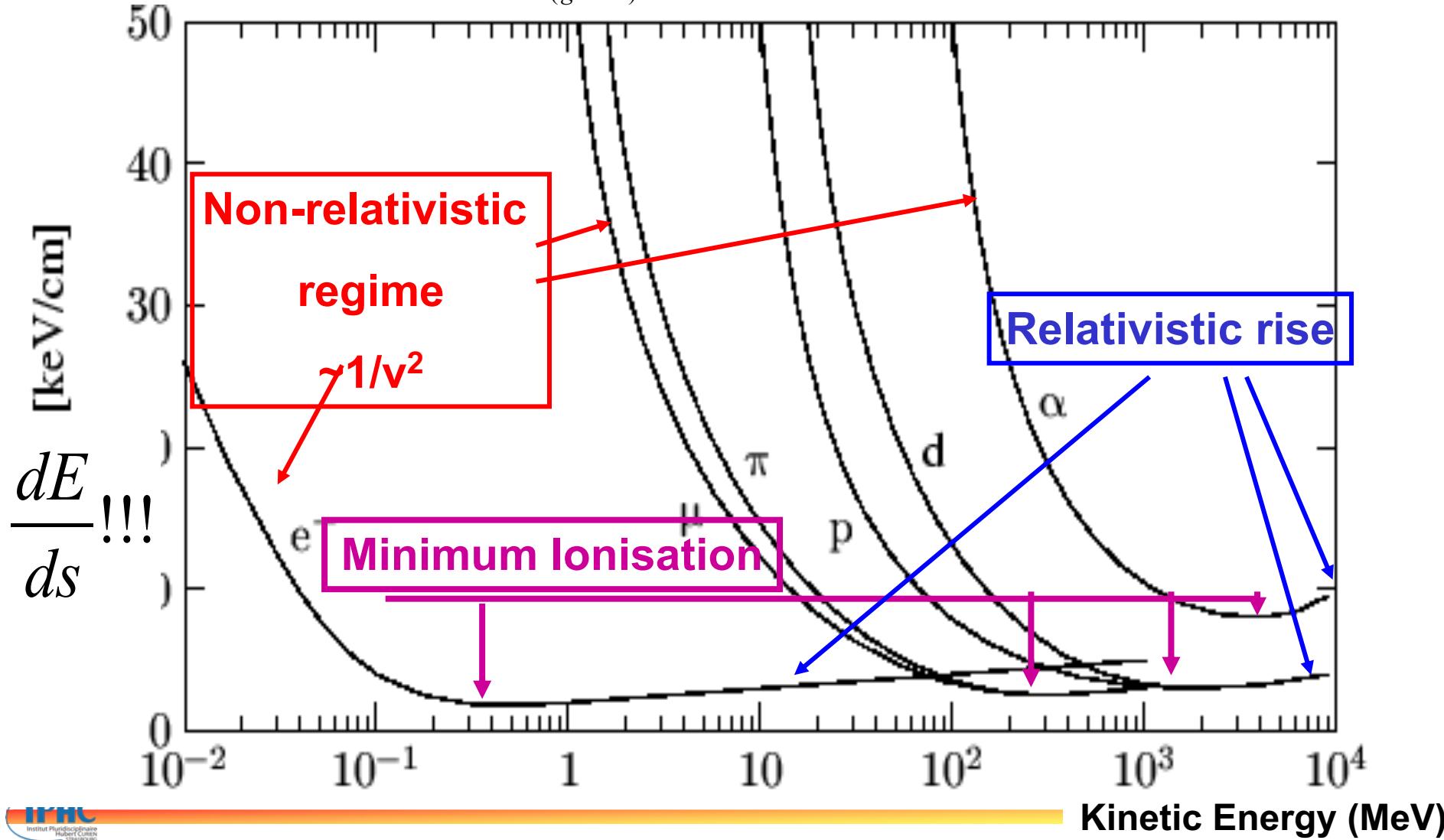
$$n_e = N_A \cdot \rho \cdot \frac{Z}{A}$$

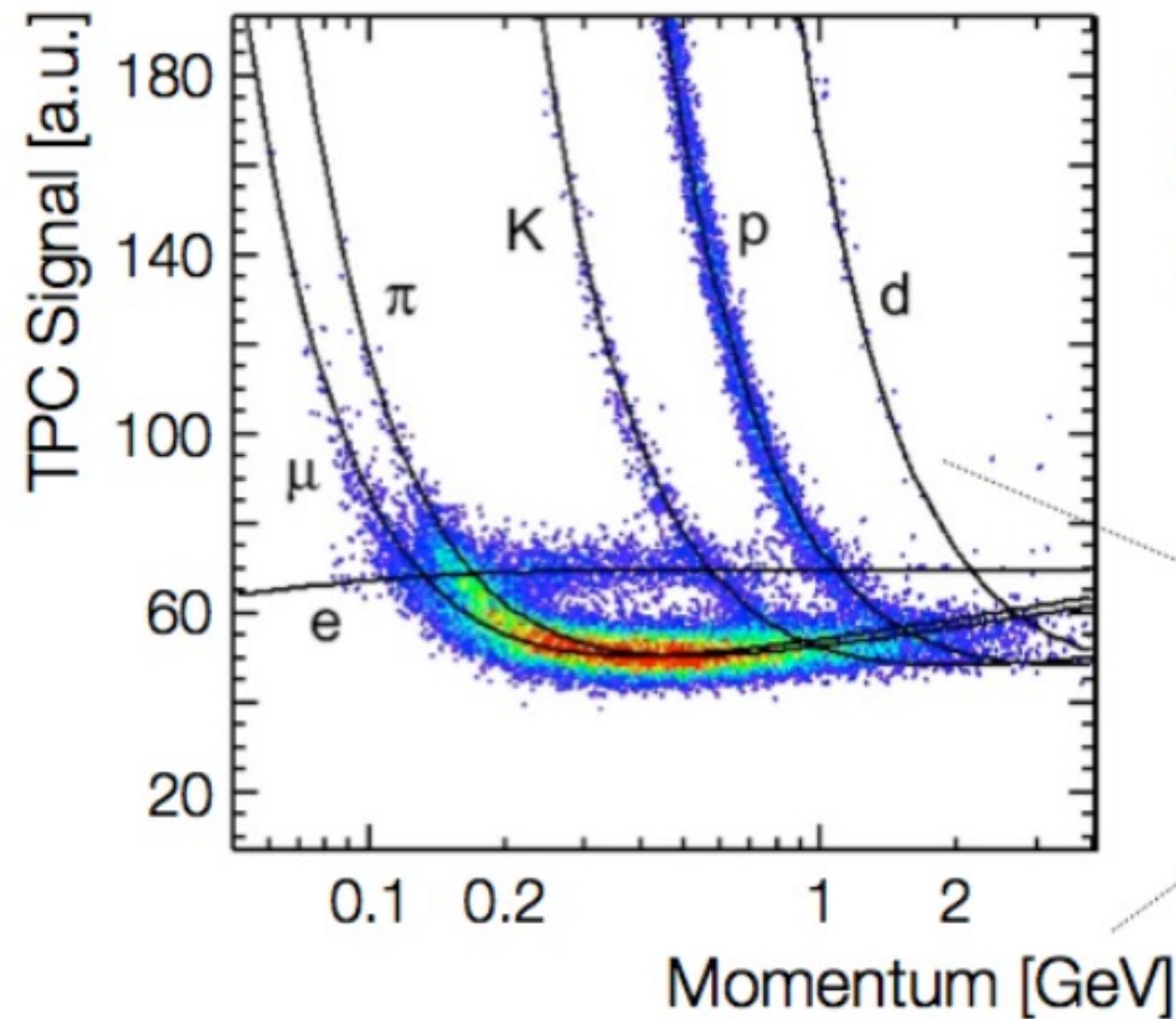
$$r_e = \frac{e^2}{4\pi\epsilon_0 m_e c^2} = \frac{\alpha \hbar c}{m_e c^2}$$

$$-\frac{1}{\rho} \frac{dE}{ds} = -\frac{dE}{dx} = \underbrace{4\pi N_A r_e^2 m_e c^2}_{0.3071 \text{ MeV}/(\text{g/cm}^2)} \frac{Z}{A} z^2 \frac{1}{\beta^2} \left[ \frac{1}{2} \ln \frac{2m_e c^2 \gamma^2 \beta^2 \cdot T_e^{\max}}{I^2} - \beta^2 \frac{\delta}{2} \frac{C}{Z} \right]$$

*Density- shell correction*

$$-\frac{1}{\rho} \frac{dE}{ds} = -\frac{dE}{dx} = \underbrace{4\pi N_A r_e^2 m_e c^2}_{0.3071 \text{ MeV}/(\text{g/cm}^2)} \frac{Z}{A} z^2 \frac{1}{\beta^2} \left[ \frac{1}{2} \ln \frac{2m_e c^2 \gamma^2 \beta^2 \cdot T_e^{\max}}{I^2} - \beta^2 - \frac{\delta}{2} - \frac{C}{Z} \right]$$





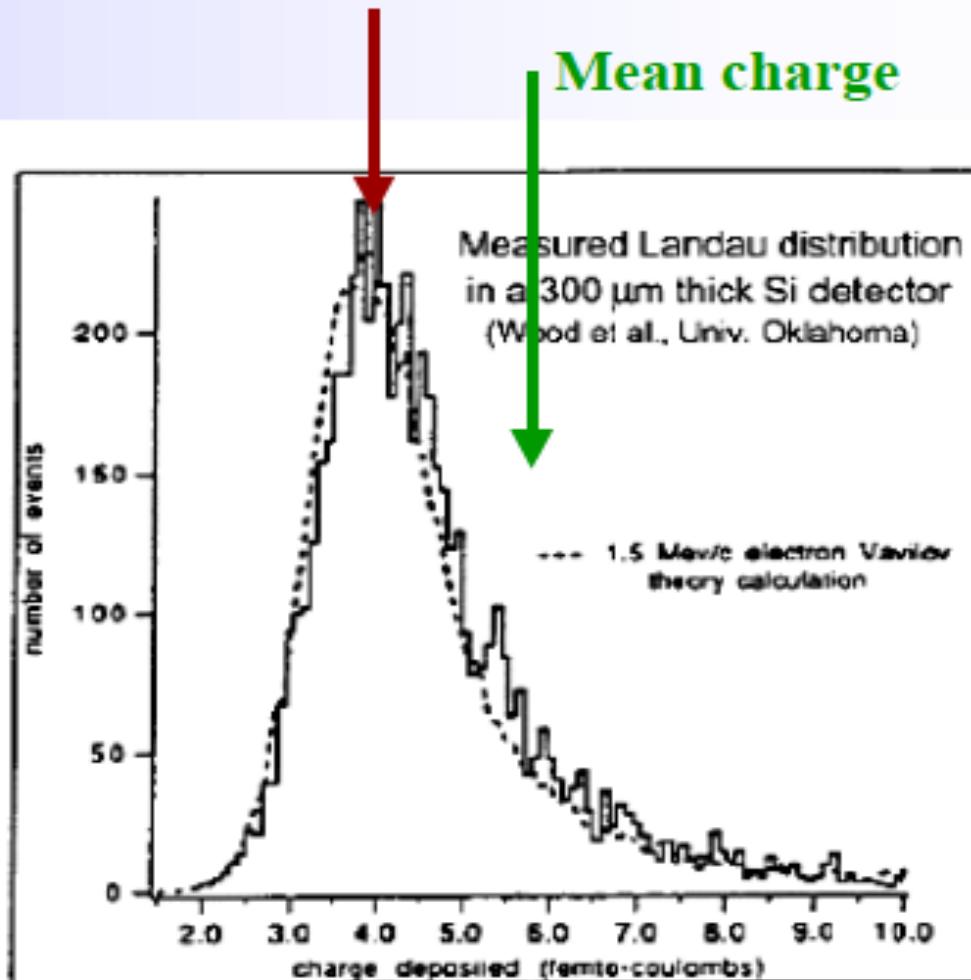
Measured  
energy loss  
[ALICE TPC, 2009]

Bethe-Bloch

Remember:  
 $dE/dx$  depends on  $\beta$ !

# Fluctuations of energy loss by charged particles

Most probable charge  $\approx 0.7 \times$  mean.

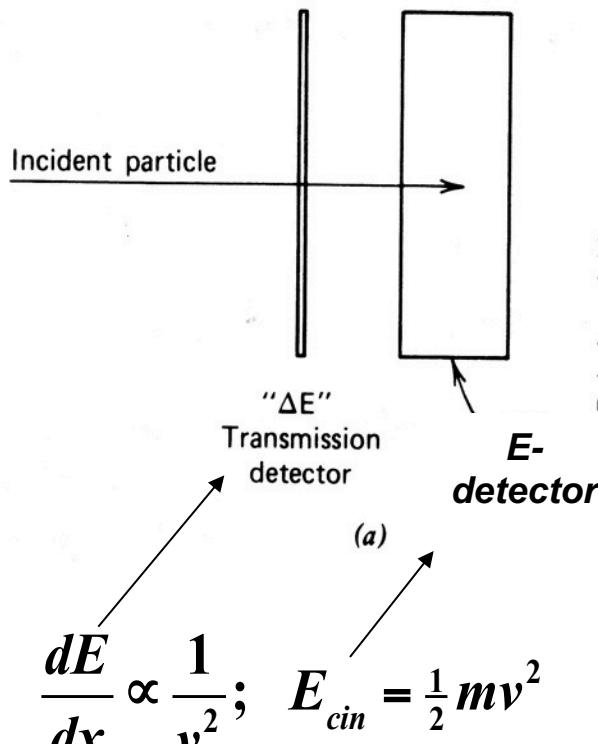


Mean / average energy loss is predicted by Bethe-Bloch formula

- Large fluctuations of energy loss, specially in thin layers
- Results from the stochastic nature of collisions.
- Large transfer of energy can occur in a single collision
- If the number of collisions becomes very large the distribution approaches a Gaussian (Central Limit Theorem).

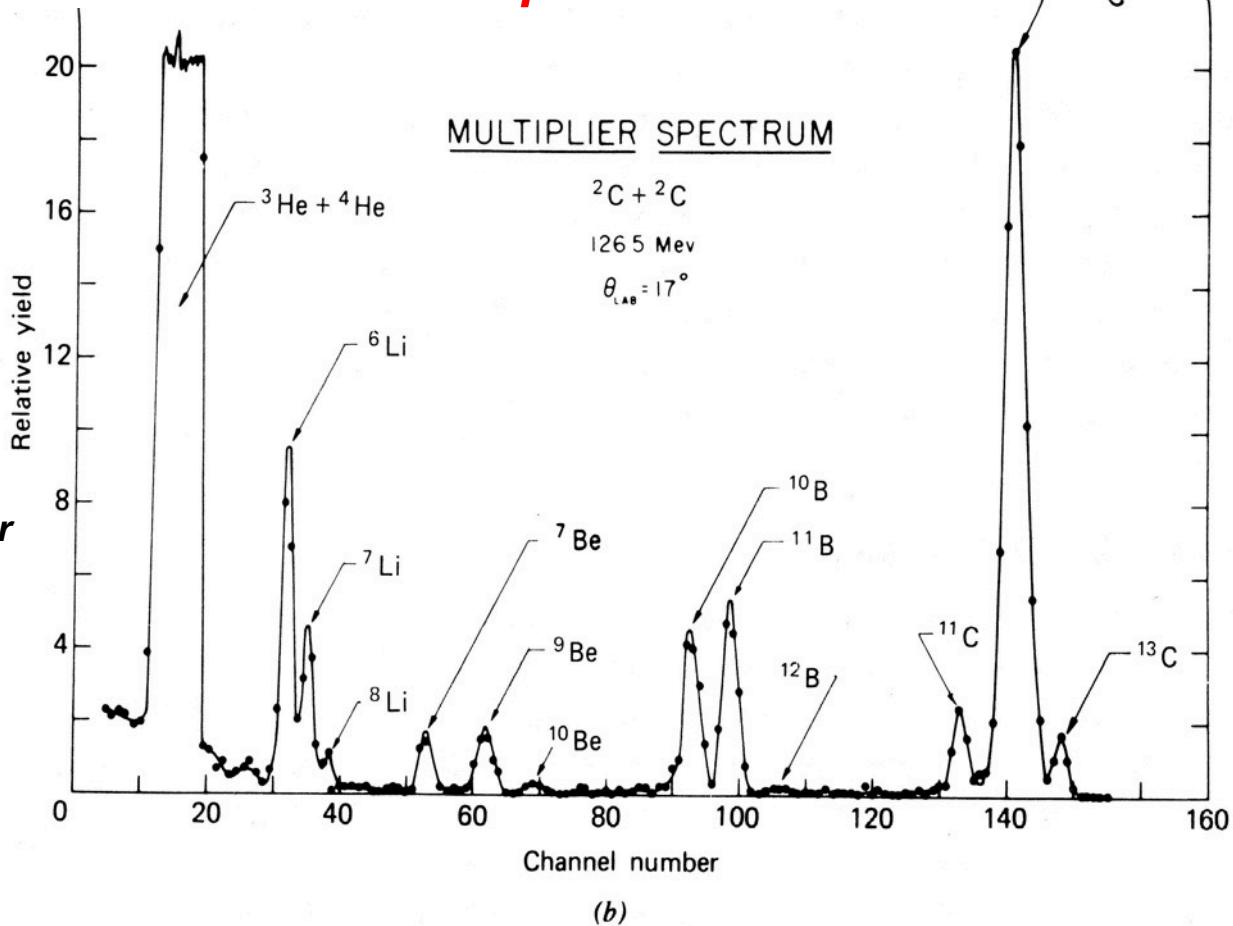
CMS silicon detector

# Identification of masses for non relativistic particles



⇒

$$\frac{dE}{dx} \times E_{cin} \propto m$$

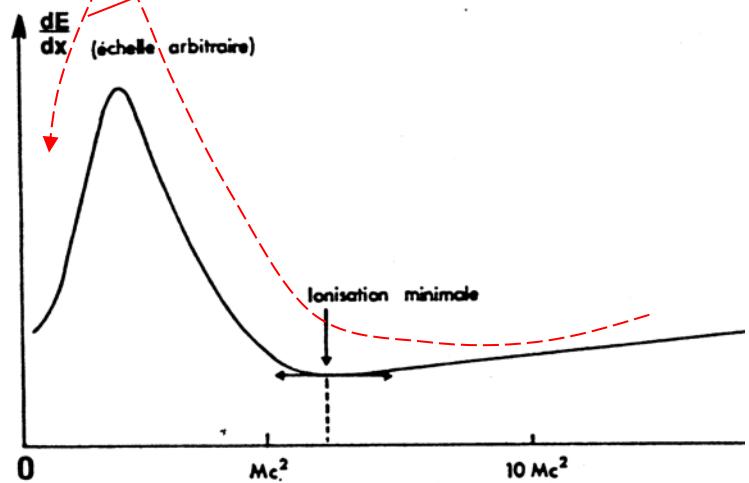


**Figure 11-16** (a) A particle identifier arrangement consisting of tandem  $\Delta E$  and  $E$  detectors operated in coincidence. (b) Experimental spectrum obtained for the  $\Delta E \cdot E$  signal product for a mixture of different ions. (From Bromley.<sup>90</sup>)

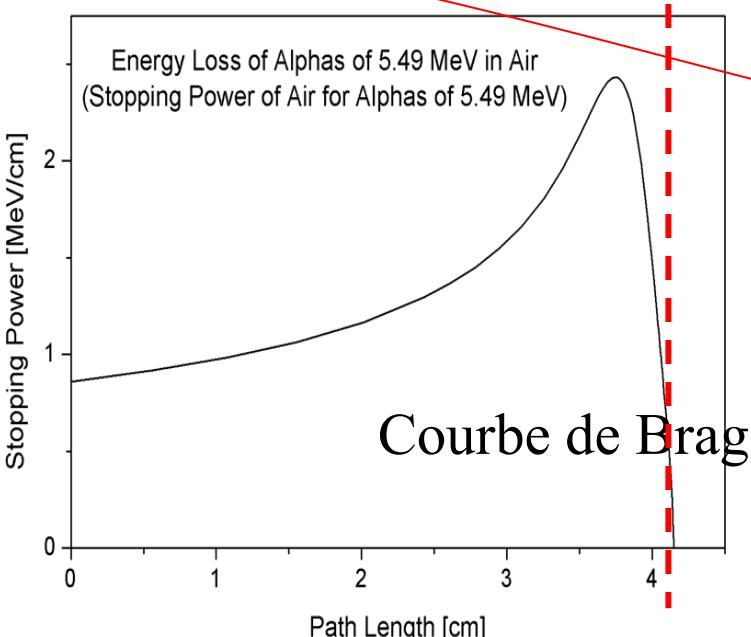
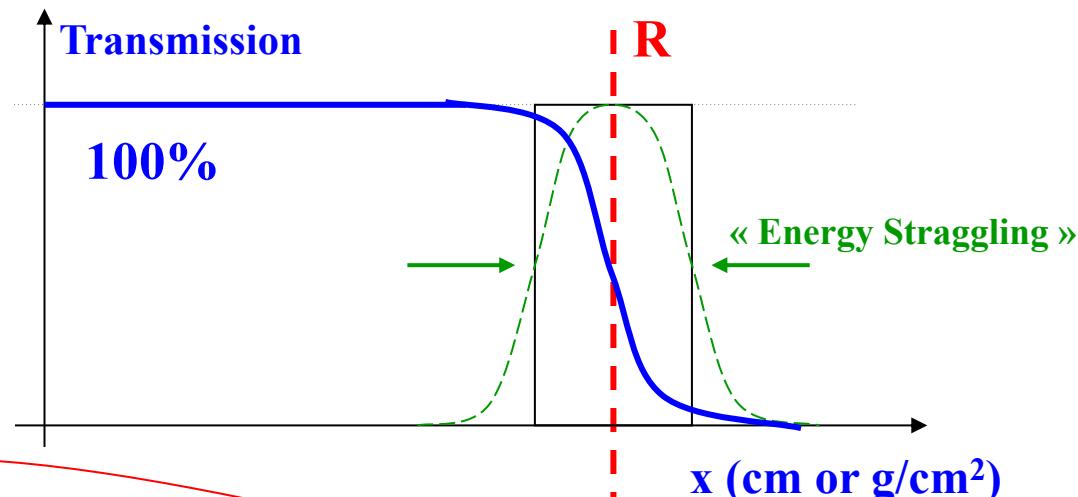
**Range of charged particles is a very well defined quantity**

$$\langle R \rangle = \int_{E_0}^0 \left( \frac{dE}{dx} \right)^{-1} dE$$

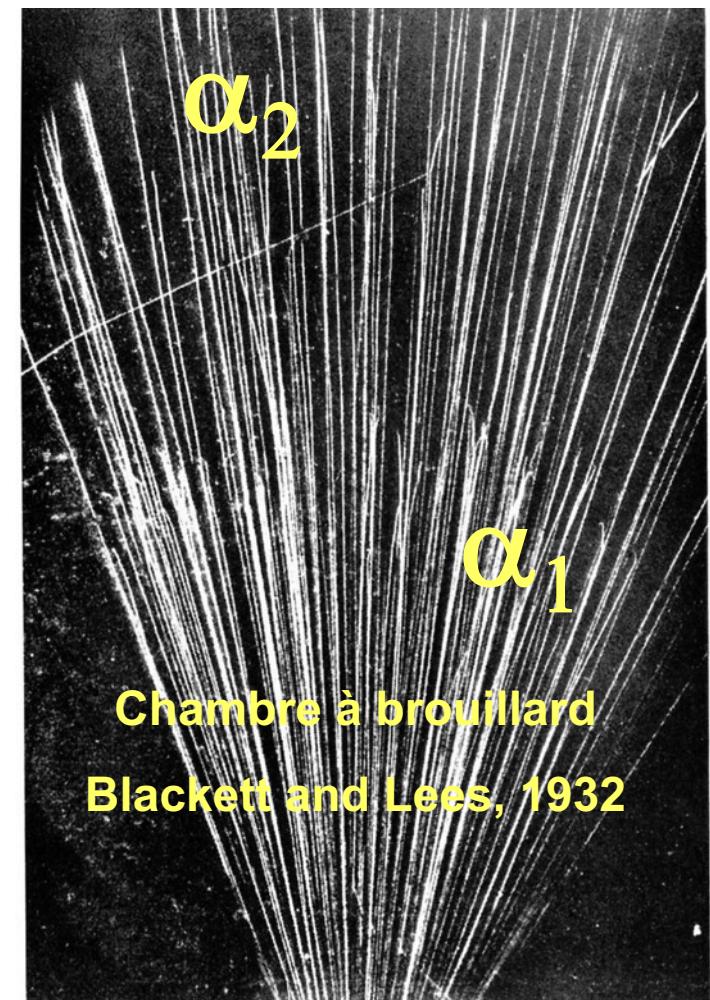
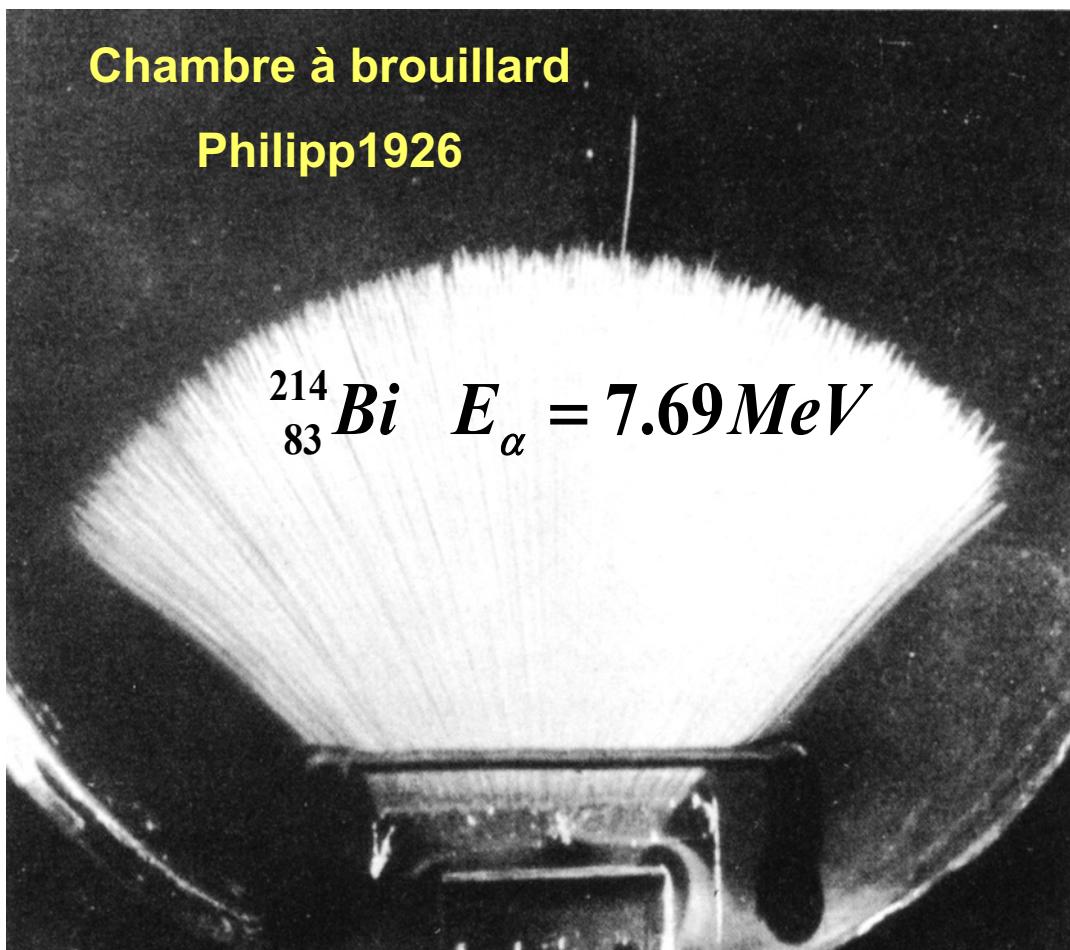
$$\frac{\langle R \rangle \rho}{Mc^2} \sim \frac{1}{z_0^2} \frac{A}{Z} f(\beta_0 \gamma_0)$$



**Range of heavy charged particle**



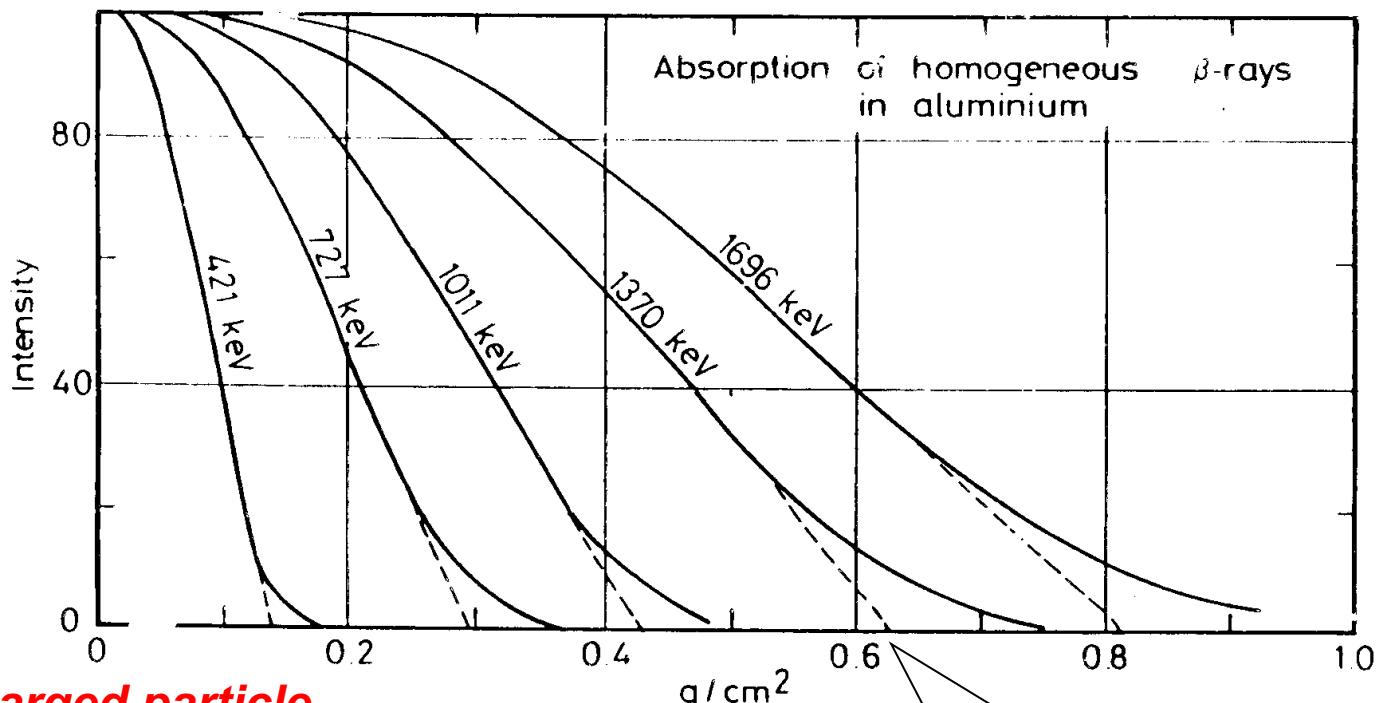
# Cloud Chamber



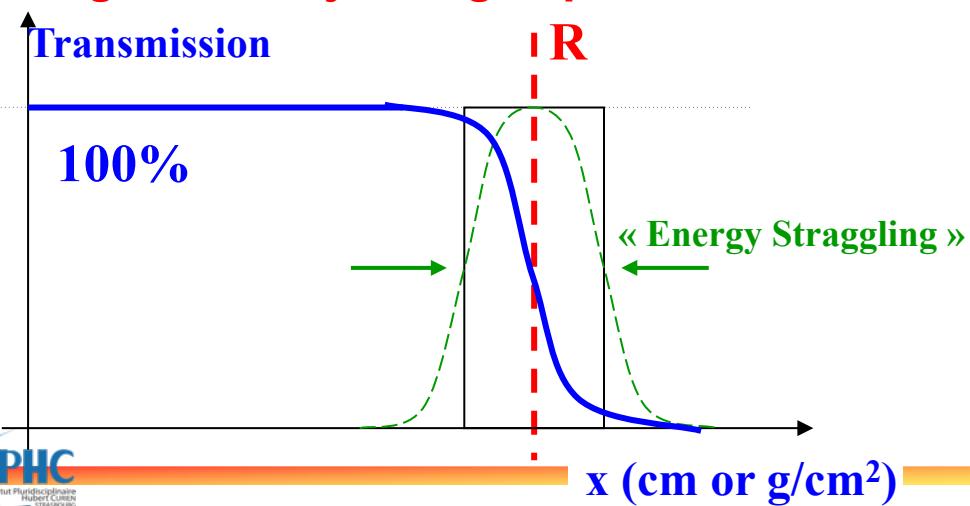
# Electrons

- Electron – electron collisions
- Identical particles / equal masses
- Higher energy transfer
- Larger directional changes
- Badly defined trajectory

# Low energy electrons



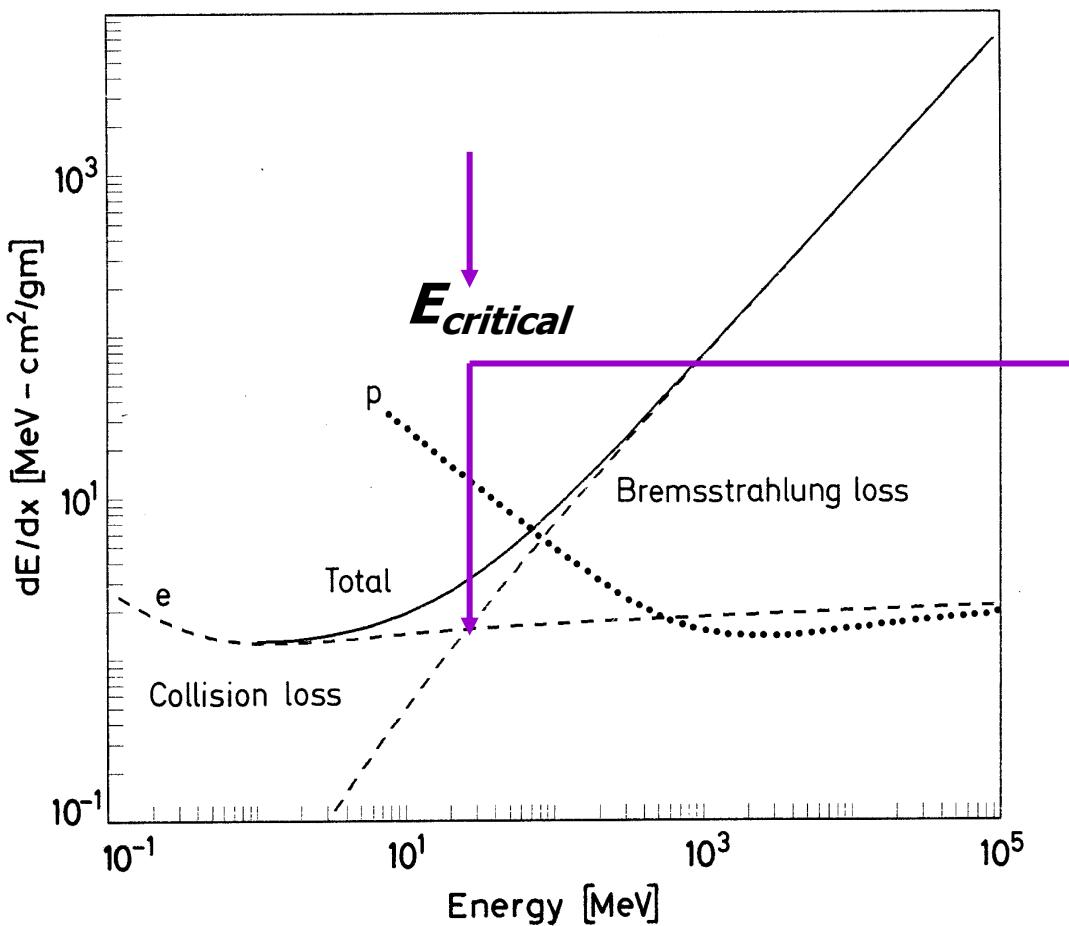
Range of heavy charged particle



**Definition of an effective range**

# High energy electrons: Bremsstrahlung

$$\frac{dE^{rad}}{dx} = -\frac{dE^{e^-}}{dx} = \frac{E^{e^-}}{X_0} \Rightarrow E^e(x) = E_0^e \exp(-x/X_0) \quad X_0 = \text{radiation length}$$



$$\frac{dE}{dx}^{rad} = 4\alpha N \frac{Z^2}{A} z^2 r^2 E \ln\left(\frac{183}{Z^{1/3}}\right)$$

$$r_e = \frac{e^2}{4\pi\epsilon_0 m_e c^2}$$

$$E_{critical} \sim \left(\frac{m_{particle}}{m_{electron}}\right)^2 \frac{1}{Z}$$

For muons the critical energy is about 200 GeV !

$$E_c = \frac{610 \text{ MeV}}{Z+1,24}$$

Liquids  
and solids

$$E_c = \frac{710 \text{ MeV}}{Z+0,92}$$

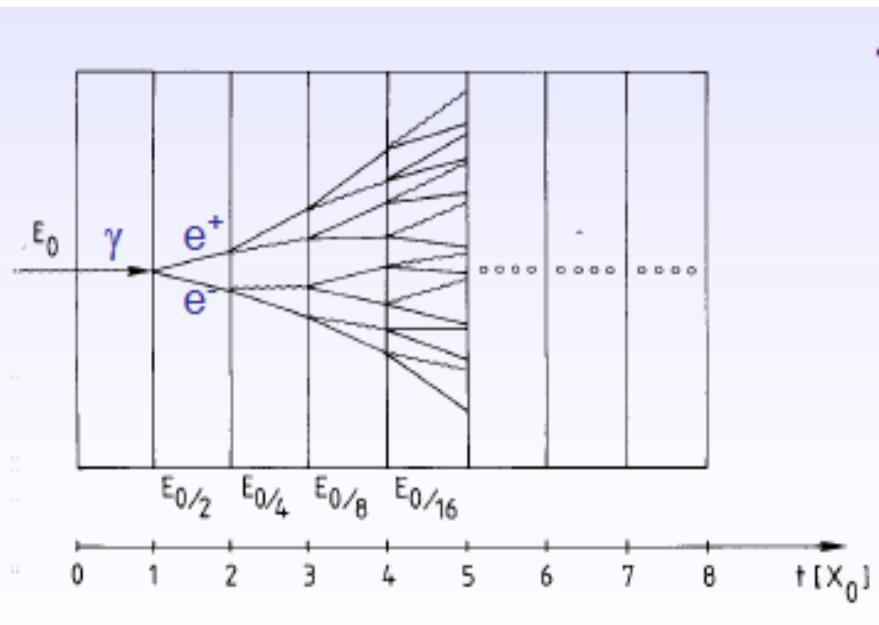
Gas

## Interaction of electrons:

### **radiation length and critical energy**

milieu	Z	A	$X_0$ (g/cm <sup>2</sup> )	$X_0$ (cm)	$E_C$ (MeV)
hydrogène	1	1.01	63	700000	350
hélium	2	4	94	530000	250
lithium	3	6.94	83	156	180
carbone	6	12.01	43	18.8	90
azote	7	14.01	38	30500	85
oxygène	8	16	34	24000	75
aluminium	13	26.98	24	8.9	40
silicium	14	28.09	22	9.4	39
fer	26	55.85	13.9	1.76	20.7
cuivre	29	63.55	12.9	1.43	18.8
argent	47	109.9	9.3	0.89	11.9
tungstène	74	183.9	6.8	0.35	8
plomb	82	207.2	6.4	0.56	7.4
air	7.3	14.4	37	30000	84
silice ( SiO <sub>2</sub> )	11.2	21.7	27	12	57
eau	7.5	14.2	36	36	83

# Electromagnetic shower



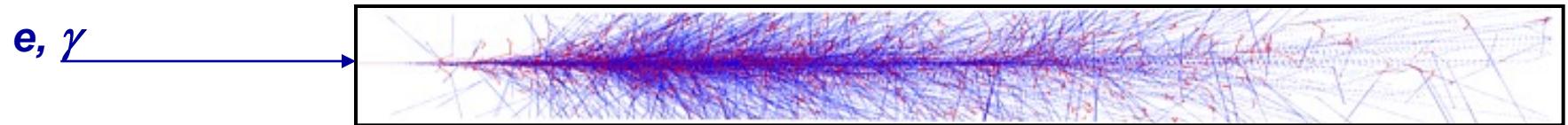
$$\bullet \quad N(t) = 2^t \quad E(t)/\text{particle} = E_0 \cdot 2^{-t}$$

Process continues until  $E(t) < E_c$

$$N^{total} = \sum_{t=0}^{t_{max}} 2^t = 2^{(t_{max}+1)} - 1 \approx 2 \cdot 2^{t_{max}} = 2 \frac{E_0}{E_c}$$

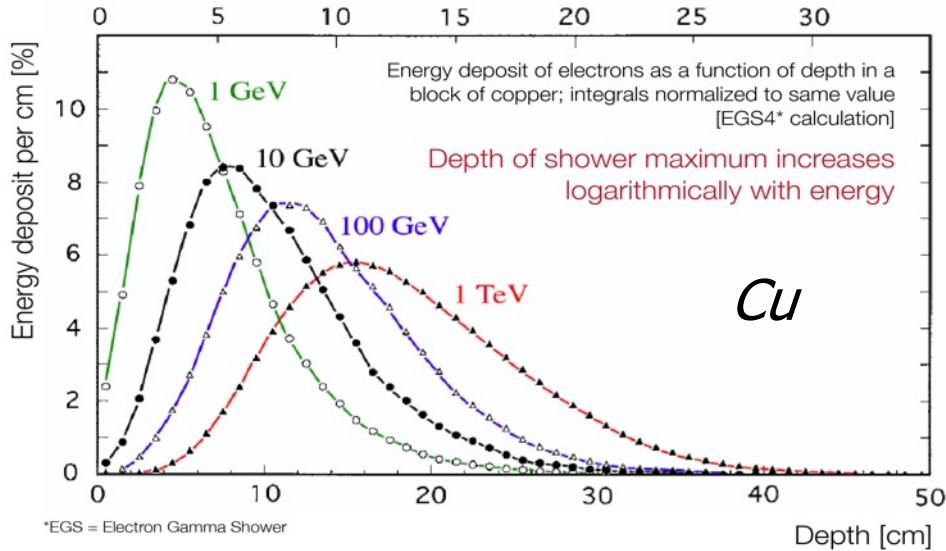
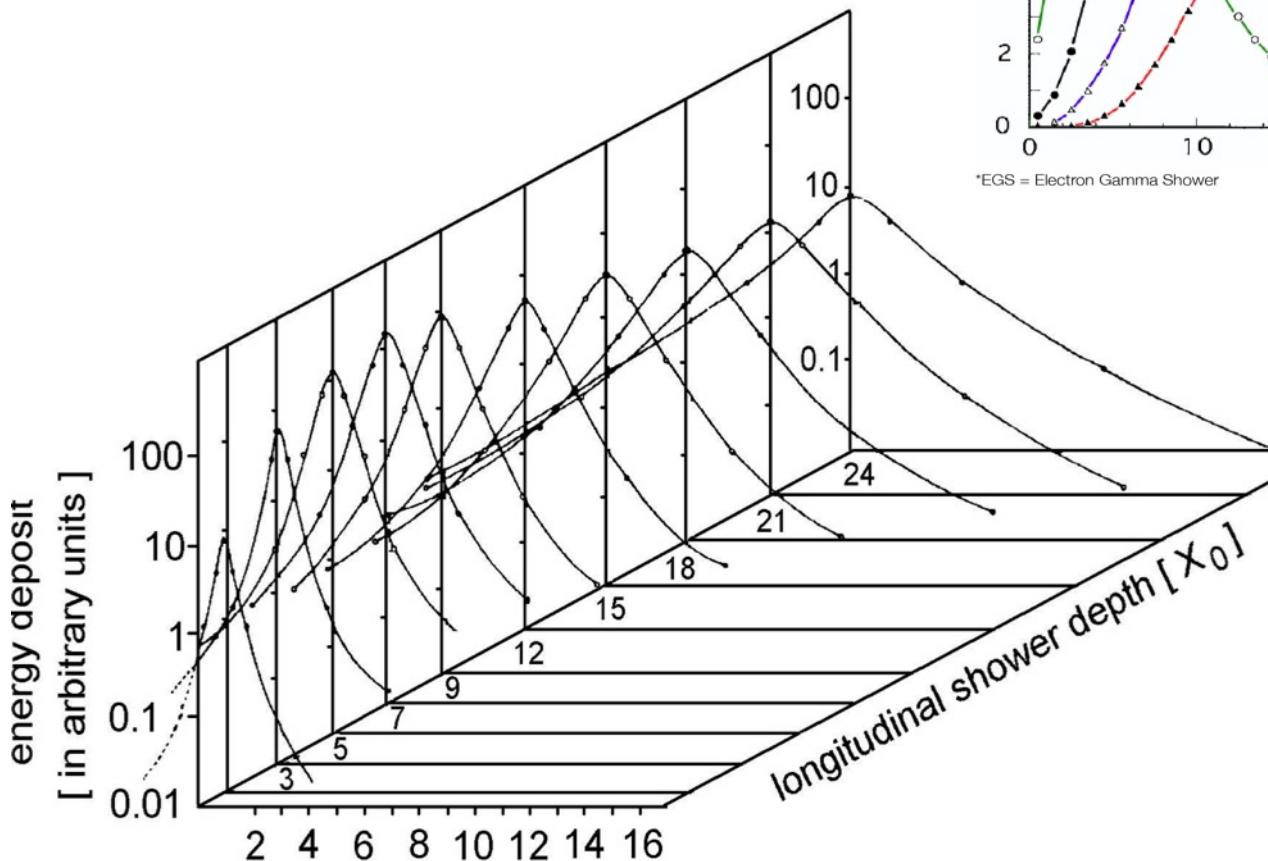
$$t_{max} = \frac{\ln E_0 / E_c}{\ln 2}$$

PbW<sub>0</sub> CMS,  $X_0=0.89$  cm



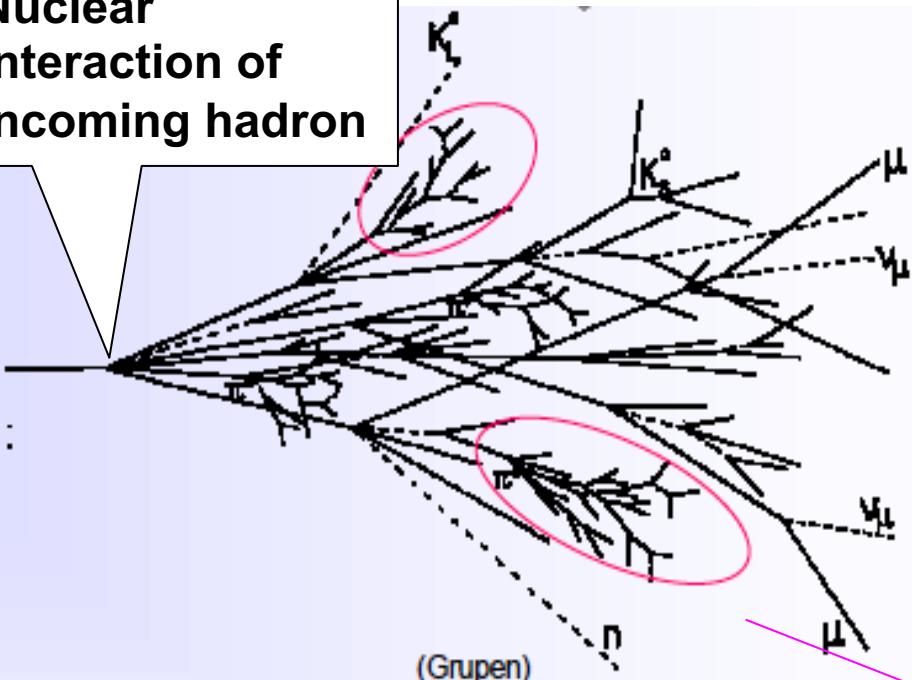
# 95% in a cylinder of $R_M$

$$R_M = \frac{21 \text{ MeV}}{E_c} X_0 \quad [\text{g/cm}^2]$$



$$t_{\max} = \ln \frac{E_0}{E_c} \frac{1}{\ln 2}$$

## Nuclear interaction of incoming hadron



hadronic

$$\downarrow N(x) = N_0 \exp(-x / \Lambda) ; \quad \frac{1}{\Lambda} = \sigma_{\text{int}} \cdot n_b$$

- charged hadrons  $p, \pi^\pm, K^\pm$
- nuclear fragments ....
- { • breaking up of nuclei (binding energy)
- neutrons, neutrinos, soft  $\gamma$ 's, muons

$\Lambda$  = nuclear interaction length

→ invisible energy → large energy fluctuations → limited energy resolution

# Hadronic showers

This is NOT(!)

a parton shower !!!

electromagnetic



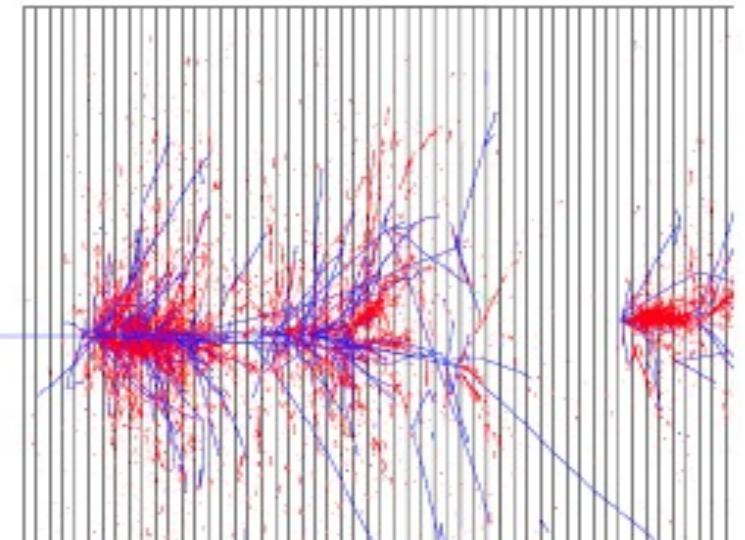
neutral pions  $\rightarrow 2\gamma$

$\rightarrow$  electromagnetic cascades

$$n(\pi^0) \approx \ln E(\text{GeV}) - 4.6$$

example  $E = 100 \text{ GeV}$ :  $n(\pi^0) \approx 18$

# Hadronic shower

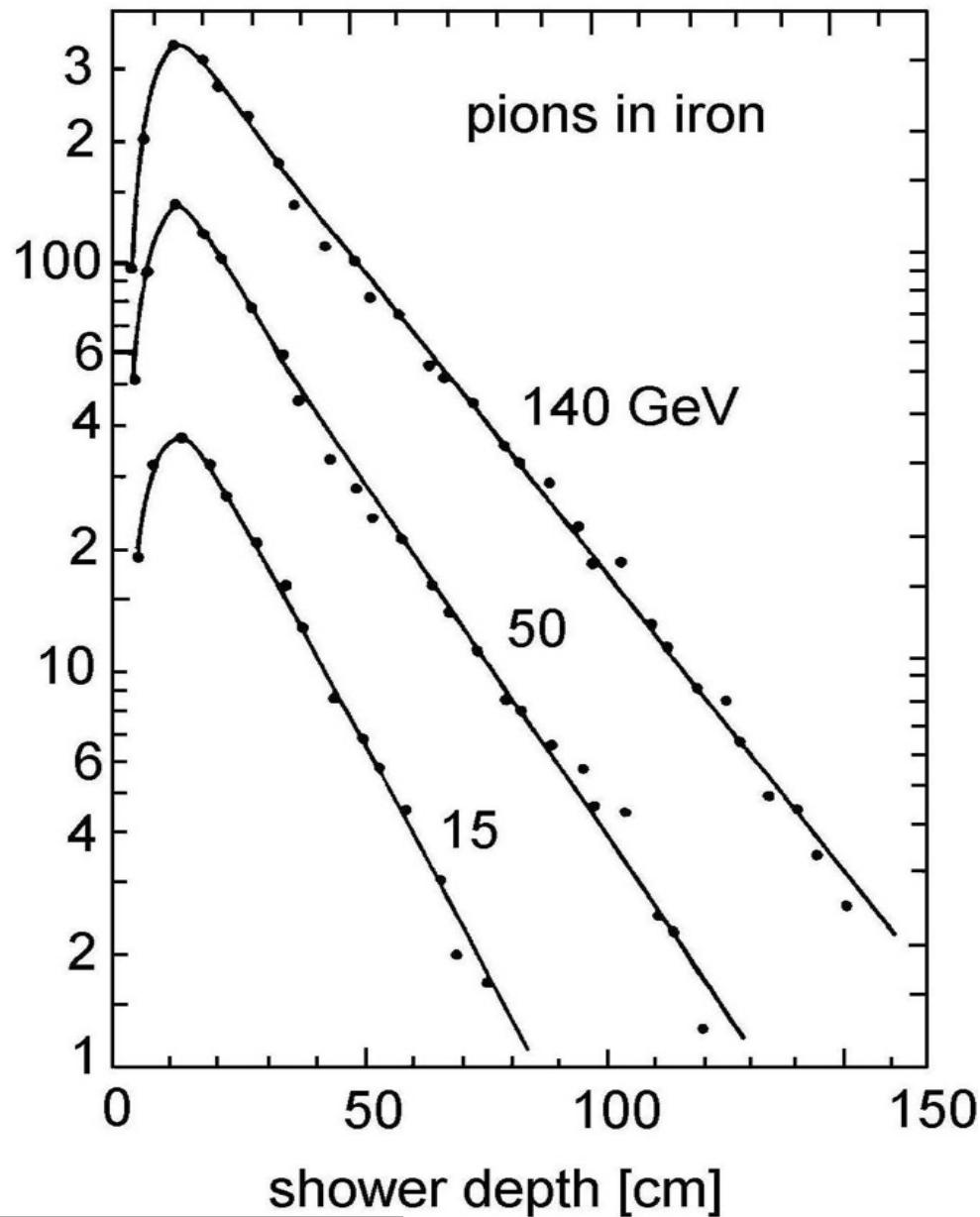


Same particle input

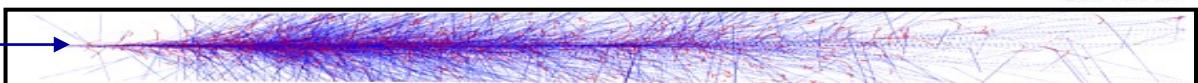
$$\Lambda \gg X_0$$

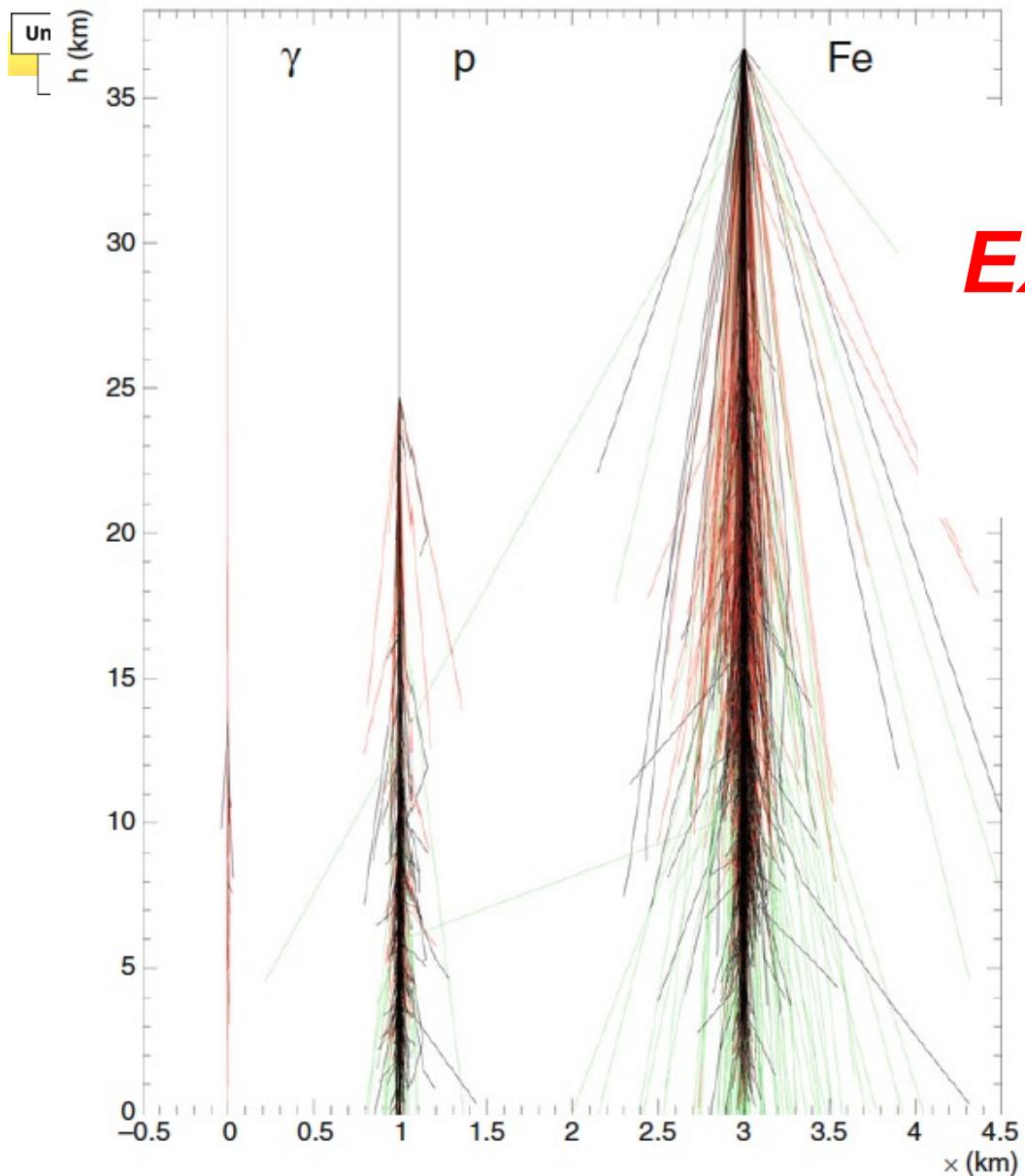
red - e.m. con  
blue - charged

number of shower particles



Comparison em shower:



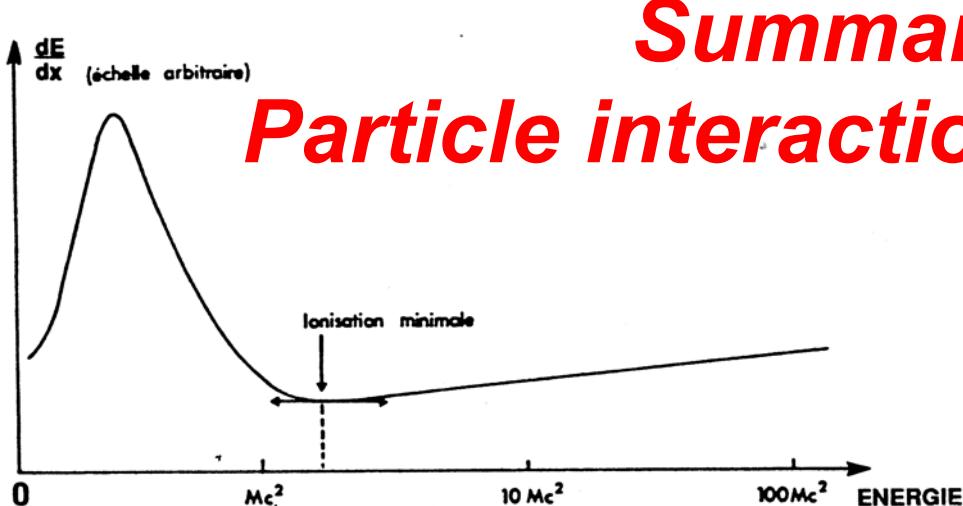


## Extensive Air shower $10^{14}$ eV

**The atmosphere as a big calorimeter**

**See lecture on  
astroparticles**

**Fig. 1.11** Side view of trajectories of particles of energy  $\geq 10$  GeV of a photon, a proton and an iron nucleus initiated shower having a total primary energy of  $10^5$  GeV each. The electromagnetic component is shown in red, hadrons are black and muons green. The widely spread particles in the lower region of the atmosphere in the hadron showers are mostly muons (courtesy of KASCADE)



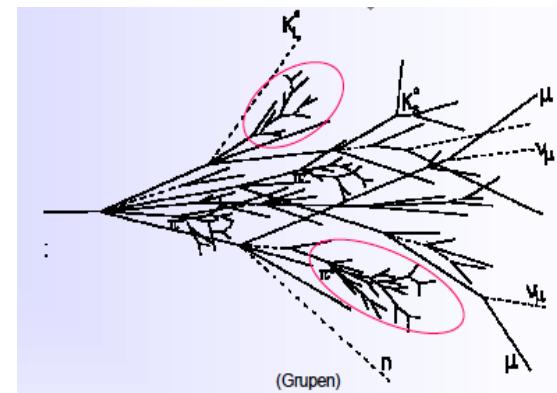
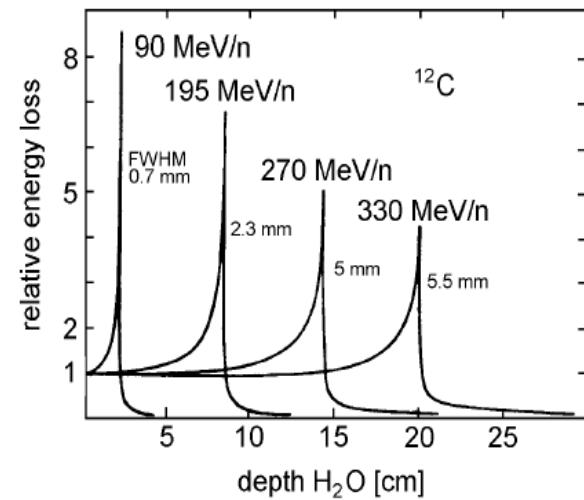
# Summary (I)

## Particle interaction with matter

### Heavy charged particles

- loose continuously kinetic energy along their path (**ionization**) with small fluctuations until they are stopped after a well defined distance; until that point their number remains constant and they travel on a straight line.
- At high energies also **hadronic interactions** may occur, leading to an hadronic shower :

$$N(x) = N_0 \exp(-x / \Lambda) ; \quad \frac{1}{\Lambda} = \sigma_{\text{int}} \cdot n_b$$



# Summary(II)

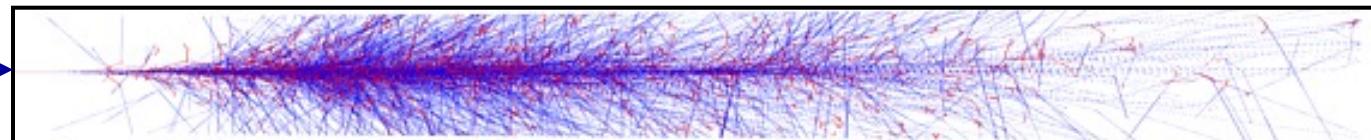
## Particle interaction with matter

### Electrons

- also loose their energy by **ionization** but with much larger fluctuations in the energy loss and deflections leading to a badly defined range in matter.
- At energies higher than a critical energy **Bremsstrahlung** is emitted. This process becomes rapidly dominant.
- Multiple pair creation and Bremsstrahlung will lead to **extended electromagnetic showers** characterized by the “radiation length  $X_0$ ”
- The **energy of the incoming electron (not the number !)** decreases exponentially with the path length.

$$E^e(x) = E_0^e \exp(-x / X_0)$$

e



# Summary (III)

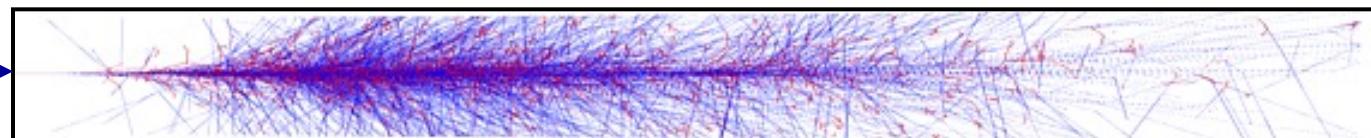
## Particle interaction with matter

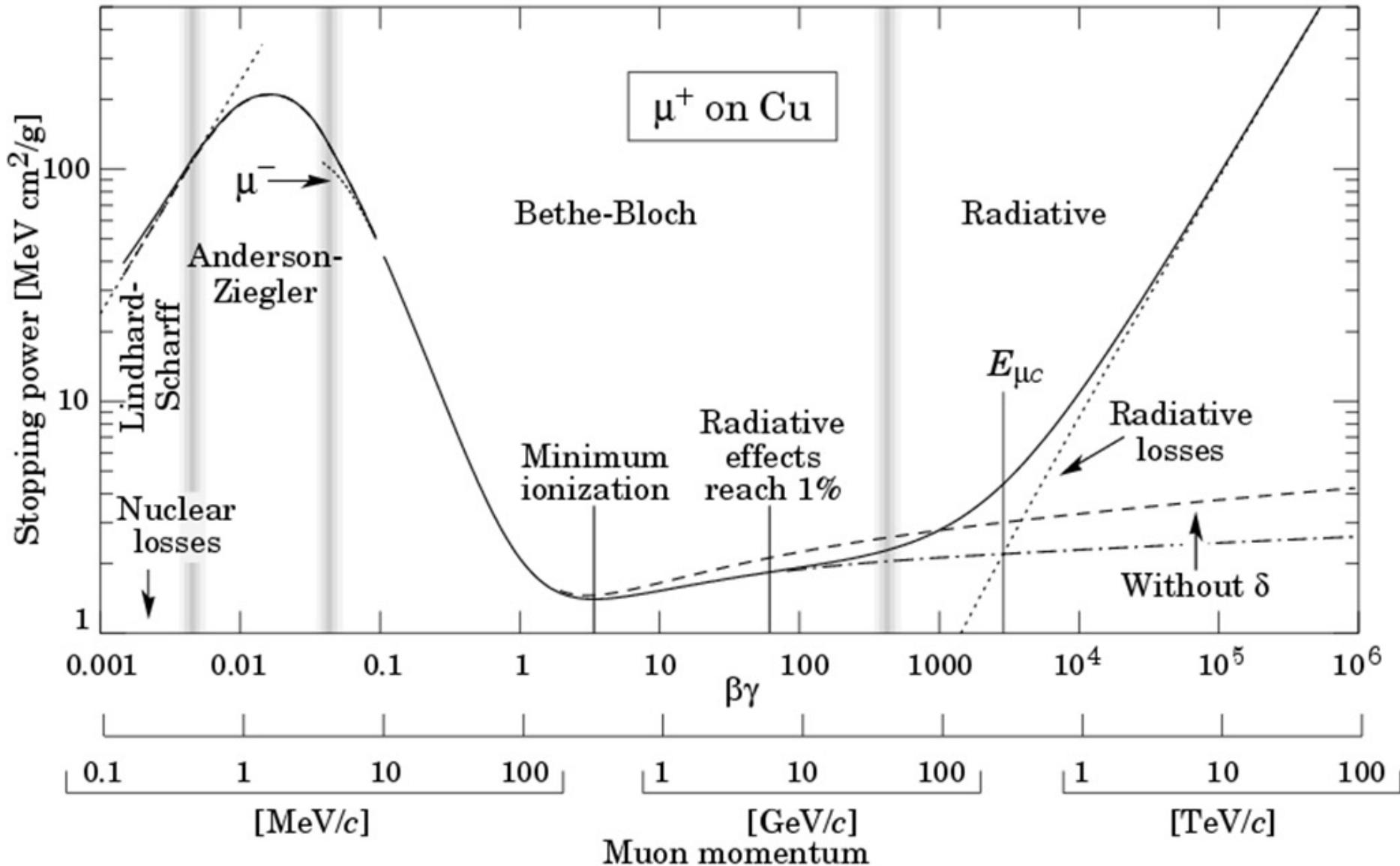
### Photons :

- At low energy (< 10 MeV) photons are absorbed by a single interaction (photoelectric, Compton effect or pair creation). The number of photons is attenuated exponentially, the energy of the remaining photons is not changed, however by the Compton effect lower energy photons are created.

$$N(x) = N_0 \exp(-x / \lambda) ; \quad \frac{1}{\mu} = \lambda_{\text{specific process}} = \text{attenuation length}; \quad x = \text{thickness}$$

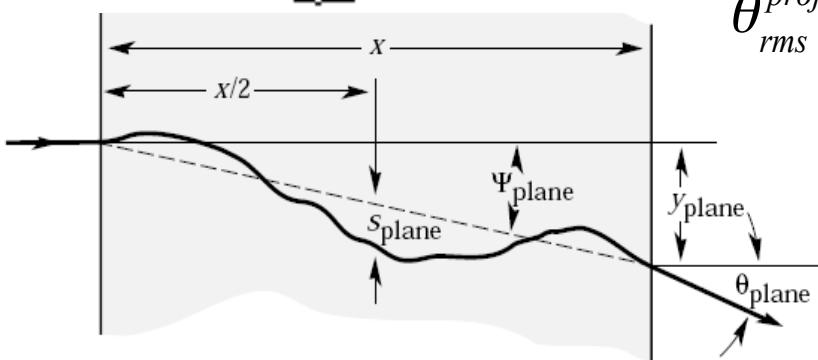
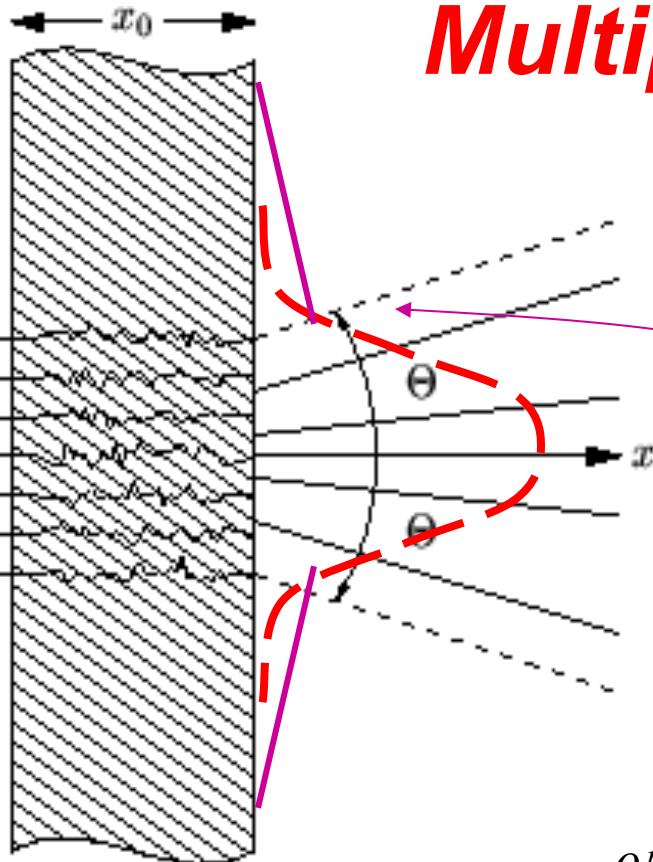
- At high energy ( $E >> 10$  MeV) successive pair creation followed by electron Bremsstrahlung will lead to extended **elm showers** characterized by the “radiation length  $X_0$ ”

 $\gamma$ 



# *Other processes*

- **Multiple scattering**
- **Cerenkov radiation**
- **Transition radiation**
- **Neutrons**
- **Neutrinos**
- **Direct dark matter detection**



# Multiple scattering

Scattering in the coulomb field of the nucleus (Rutherford)

Gaussian ( $\theta$ ) distribution for small angles  $\theta$ ,

Violent scatters can lead to large values of  $\theta$

$$\theta_{\text{rms}}^{\text{proj}} = \frac{13.6 \text{ MeV} / c}{p \cdot \beta} \sqrt{\frac{x}{X_0}} (1 + 0.038 \ln(x / X_0))$$

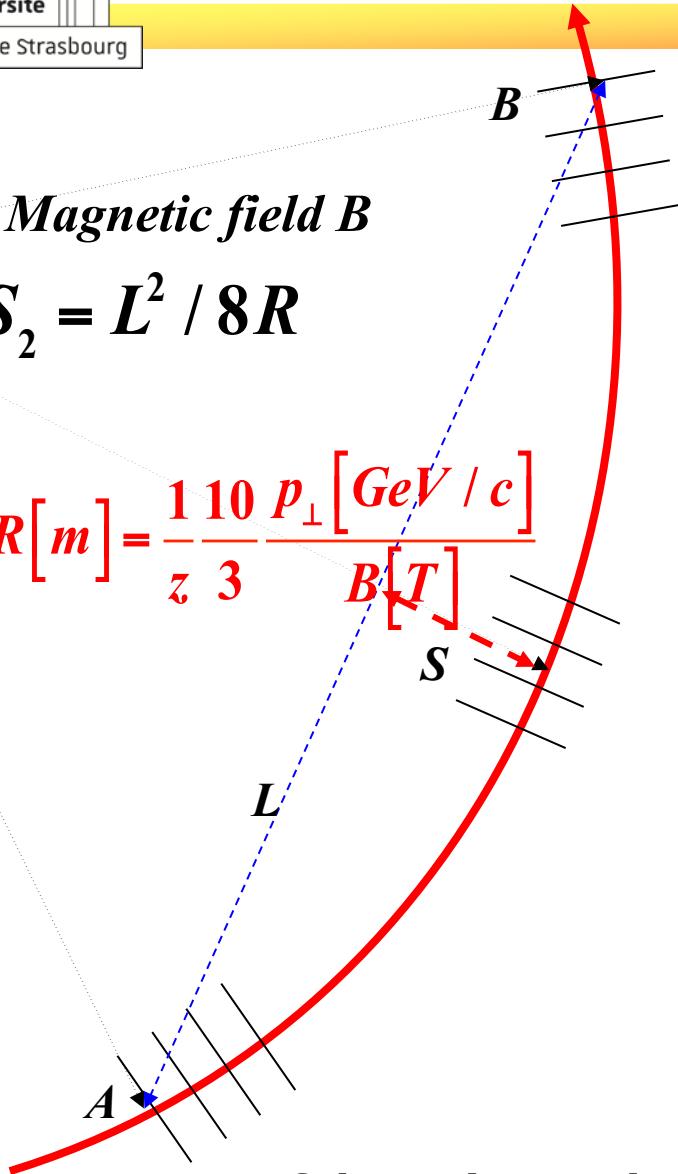
*z of charged particle*  
 $X_0$ =radiation length

Magnetic field  $B$

$$S_2 = L^2 / 8R$$

$$R[m] = \frac{1}{z} \frac{10}{3} \frac{p_{\perp}[GeV/c]}{B[T]}$$

$R$



If the trajectory is measured with  $N$  points:

$$\frac{dS}{S} = \frac{dp_{\perp}}{p_{\perp}} = \frac{80}{3 \cdot z} \frac{1}{BL^2} p_{\perp} dS$$

$$[B] = \text{Tesla}; [L] = \text{m}; [p_{\perp}] = \text{GeV}/c$$

$$\left| \frac{\sigma(p_T)}{p_T} \right|^{meas.} = \frac{\sigma(x) \cdot p_T}{0.3 \cdot BL^2} \sqrt{720/(N+4)} \quad (\text{for } N \geq \sim 10)$$

Exercise!!!

## Reconstruction of transverse momentum in a magnetic field

- Movement of a charge  $z$  in a uniform magnetic field
- Momentum resolution  $dp/p$
- Spatial resolution of the sagitta  $dS/S$

# Resolution and multiple scattering

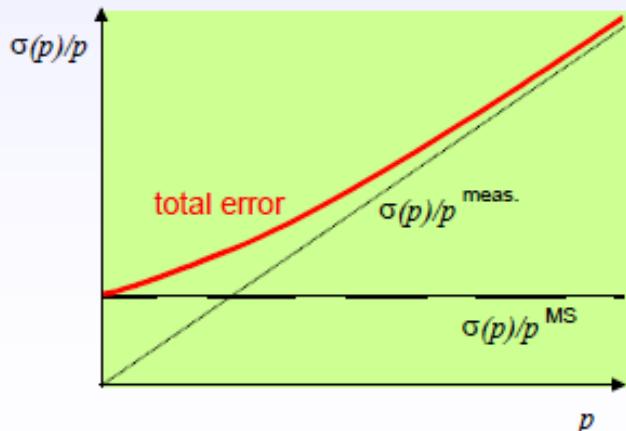
$$\left| \frac{\sigma(p_T)}{p_T} \right|^{meas.} = \frac{\sigma(x) \cdot p_T}{0.3 \cdot BL^2} \sqrt{720/(N+4)} \quad (\text{for } N \geq \sim 10)$$

$$\left. \begin{array}{l} \frac{\sigma(p)}{p_T} \propto \sigma(x) \cdot p_T \\ \sigma(x) \Big|^{MS} \propto \theta_0 \propto \frac{1}{p} \end{array} \right\} \quad \left. \frac{\sigma(p)}{p_T} \right|^{MS}$$

= constant, i.e. independent of  $p$  !

More precisely:

$$\left. \frac{\sigma(p)}{p_T} \right|^{MS} = 0.045 \frac{1}{B \sqrt{LX_0}}$$



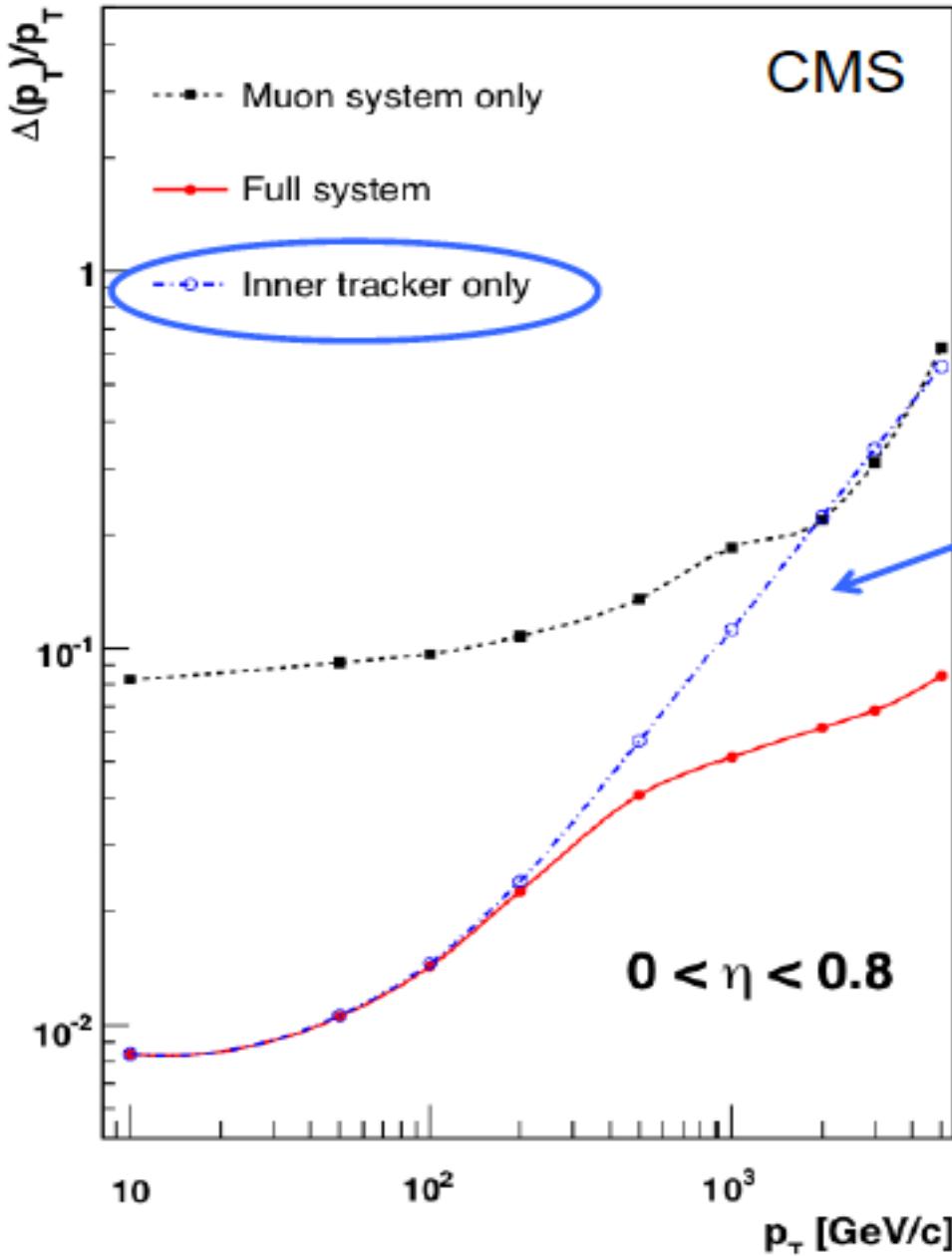
Example:

$$p_t = 1 \text{ GeV/c}, L = 1 \text{ m}, B = 1 \text{ T}, N = 10$$

$$\sigma(x) = 200 \text{ } \mu\text{m}: \quad \left| \frac{\sigma(p_T)}{p_T} \right|^{meas.} \approx 0.5\%$$

Assume detector ( $L = 1\text{m}$ ) to be filled with 1 atm. Argon gas ( $X_0 = 110\text{m}$ ),

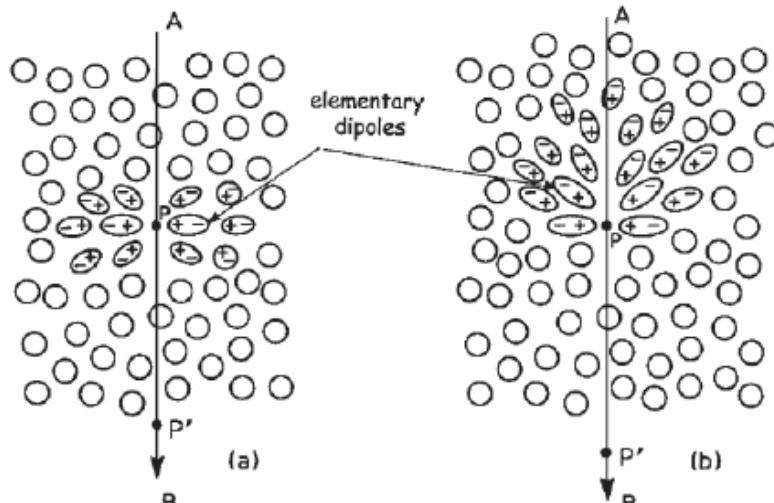
$$\left. \frac{\sigma(p)}{p_T} \right|^{MS} \approx 0.5\%$$



$$\frac{dp_\perp}{p_\perp} = \alpha \times p_\perp dS$$

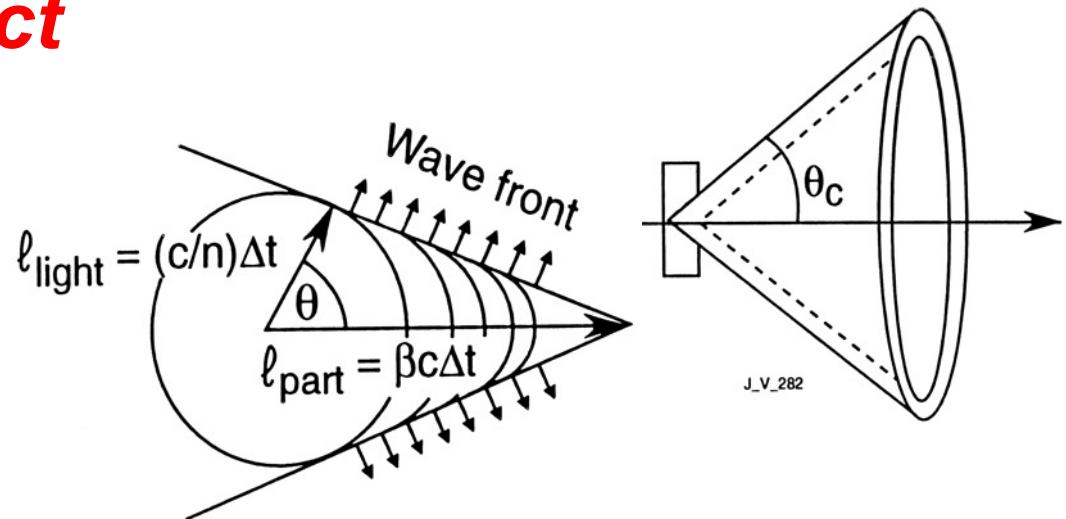
+ ( Multiple scattering constant )

# Cerenkov effect



$$v_p/c < c/n(\lambda)$$

$$v_p/c > c/n(\lambda)$$



$$\nu = \beta c > c / n$$

$$\cos \theta_c = \frac{c \cdot \Delta t / n}{\beta c \cdot \Delta t} = \frac{1}{\beta n}$$

$$\Rightarrow \beta > \frac{1}{n}; \cos \theta_c^{\max} = \frac{1}{n}$$

$$\lambda_{\text{photons}} \approx 200 - 700 \text{ nm}$$

$$\frac{d^2 N_{hv}}{dE_{hv} dx} \approx 370 \sin^2 \theta_c \text{ eV}^{-1} \text{ cm}^{-1}$$

# Exercise

## Blue light in a reactor

1. What produces the light?
2. Water  $n=1.333$ . calculate the minimal energy of an electron to produce Cerenkov light



# Transition radiation

- Elm. radiation is emitted when a charged particle traverses a discontinuity of refractive index, e.g. the boundary between vacuum and a dielectric layer.

- Radiated energy  $W$  / boundary:

$$W = \frac{1}{3} \alpha \hbar \omega_{pl} \gamma \approx \gamma !!$$

- Plasma frequency

$$\omega_{pl} = \sqrt{\frac{N_e e^2}{\epsilon_0 m_e}} ; \left\{ \begin{array}{l} \text{plasma} \\ \text{frequency} \end{array} \right\}$$

$$\hbar \omega_{pl} \approx 20 - 30 \text{ eV}$$

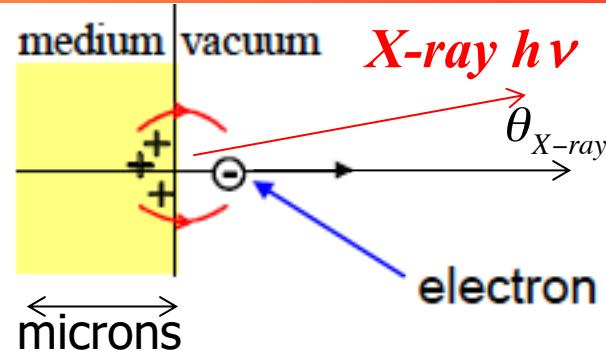
- Energy of emitted photons (X-rays)  $h\nu = \hbar \omega \approx \frac{1}{4} \hbar \omega_{pl} \gamma \rightarrow \text{keV range}$

Proportionally to rel. gamma factor!

- Number of emitted photons:

$$N_{ph} \approx \frac{W}{\hbar \omega} \sim \alpha \approx \frac{1}{137}; \Rightarrow \text{many layers}$$

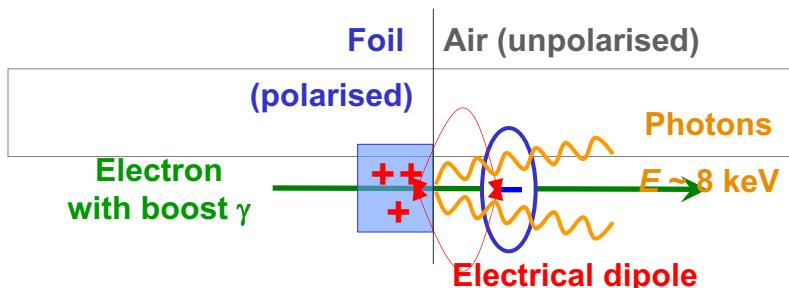
$$\theta_{X-ray} \sim 1/\gamma$$



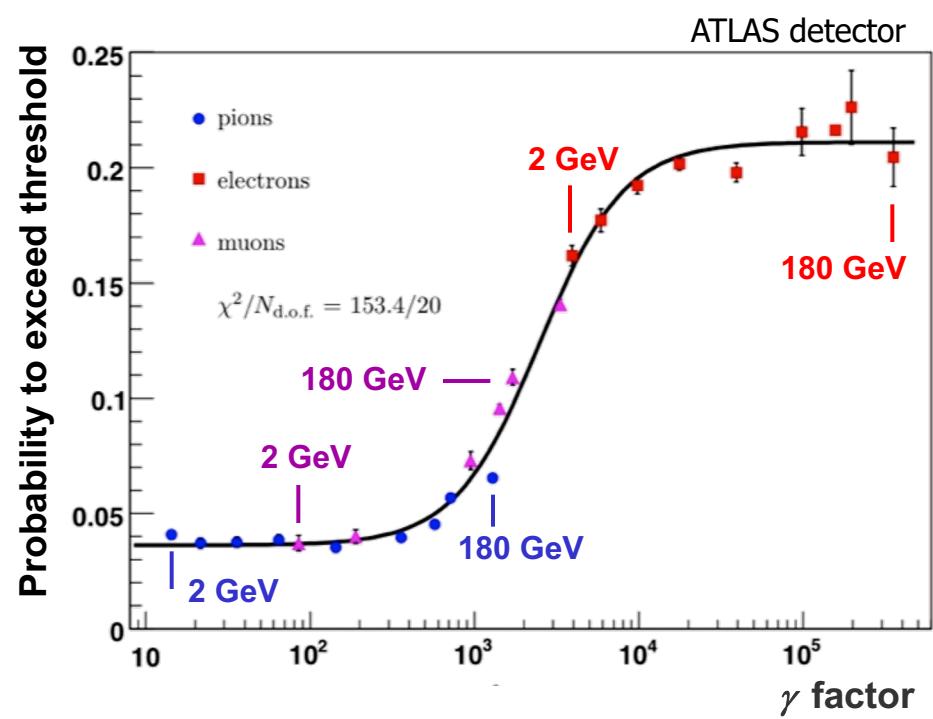
# Transition radiation

- Effect can be explained by re-arrangement of electric field
- A charged particle approaching a boundary creates a electric dipole with its mirror charge
- The time-dependent dipole field causes the emission of electromagnetic radiation

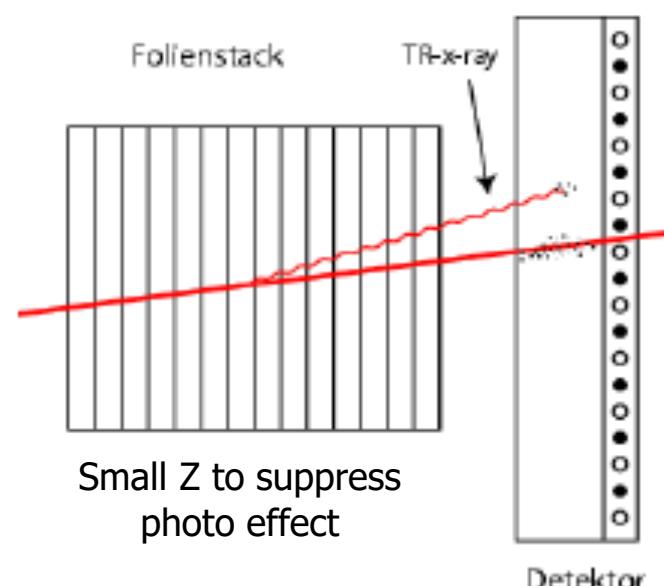
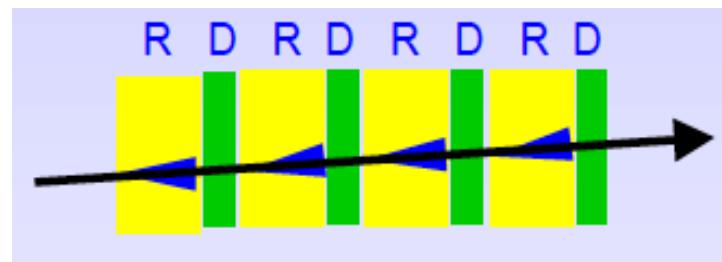
**Photon radiation when charged ultra-relativistic particles traverse the boundary of two different dielectric media (foil & air)**



→ Significant radiation for  $\gamma > 1000$   
and  $> 100$  boundaries

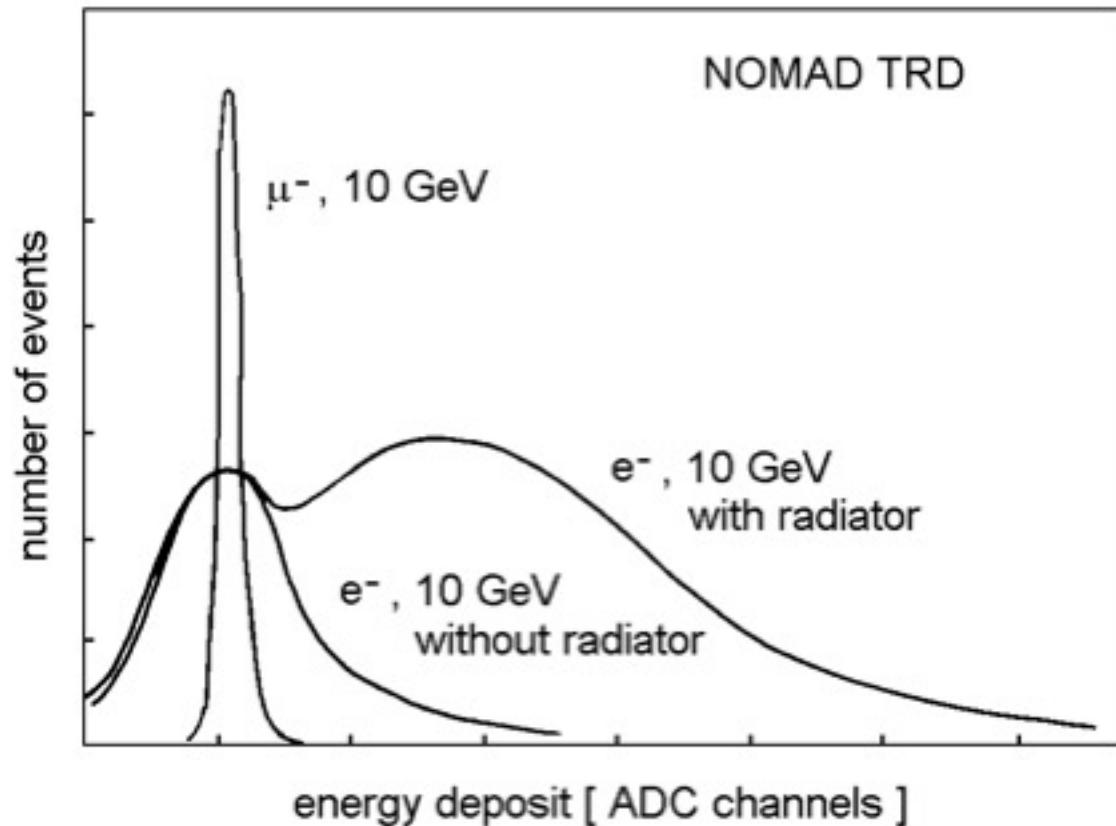


# Transition Radiation Detectors



$$W = \frac{1}{3} \alpha \hbar \omega_{pl} \gamma \approx \gamma !!$$

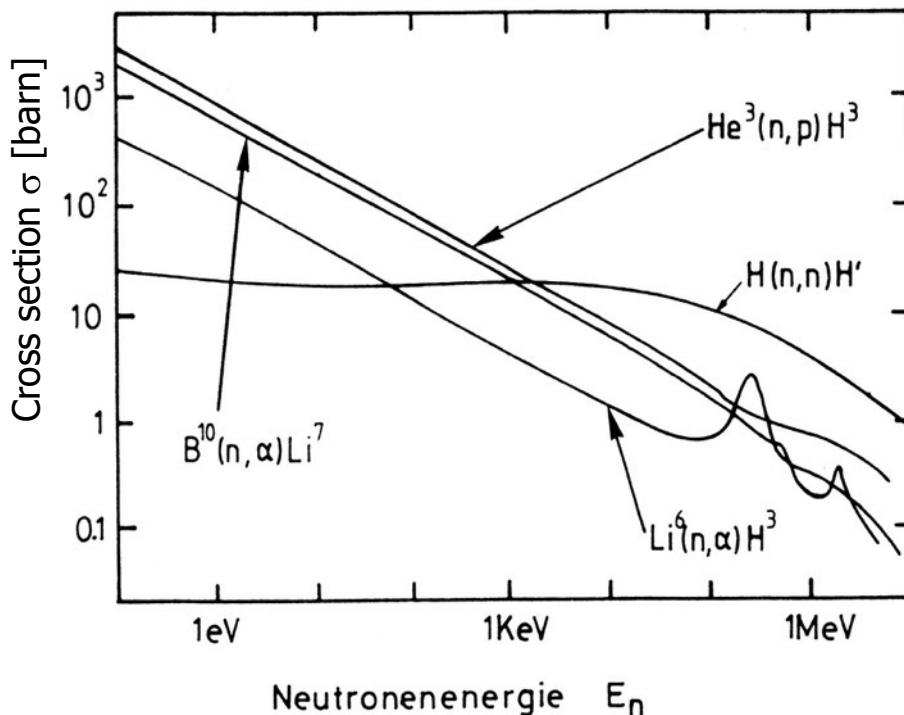
$$\hbar \omega \approx \frac{1}{4} \hbar \omega_{pl} \gamma \rightarrow \text{keV range}$$



$$N_{ph} \approx \frac{W}{\hbar \omega} \sim \alpha \approx \frac{1}{137}; \Rightarrow \text{many layers}$$

$$\theta_{x-ray} \sim 1/\gamma$$

# Neutrons

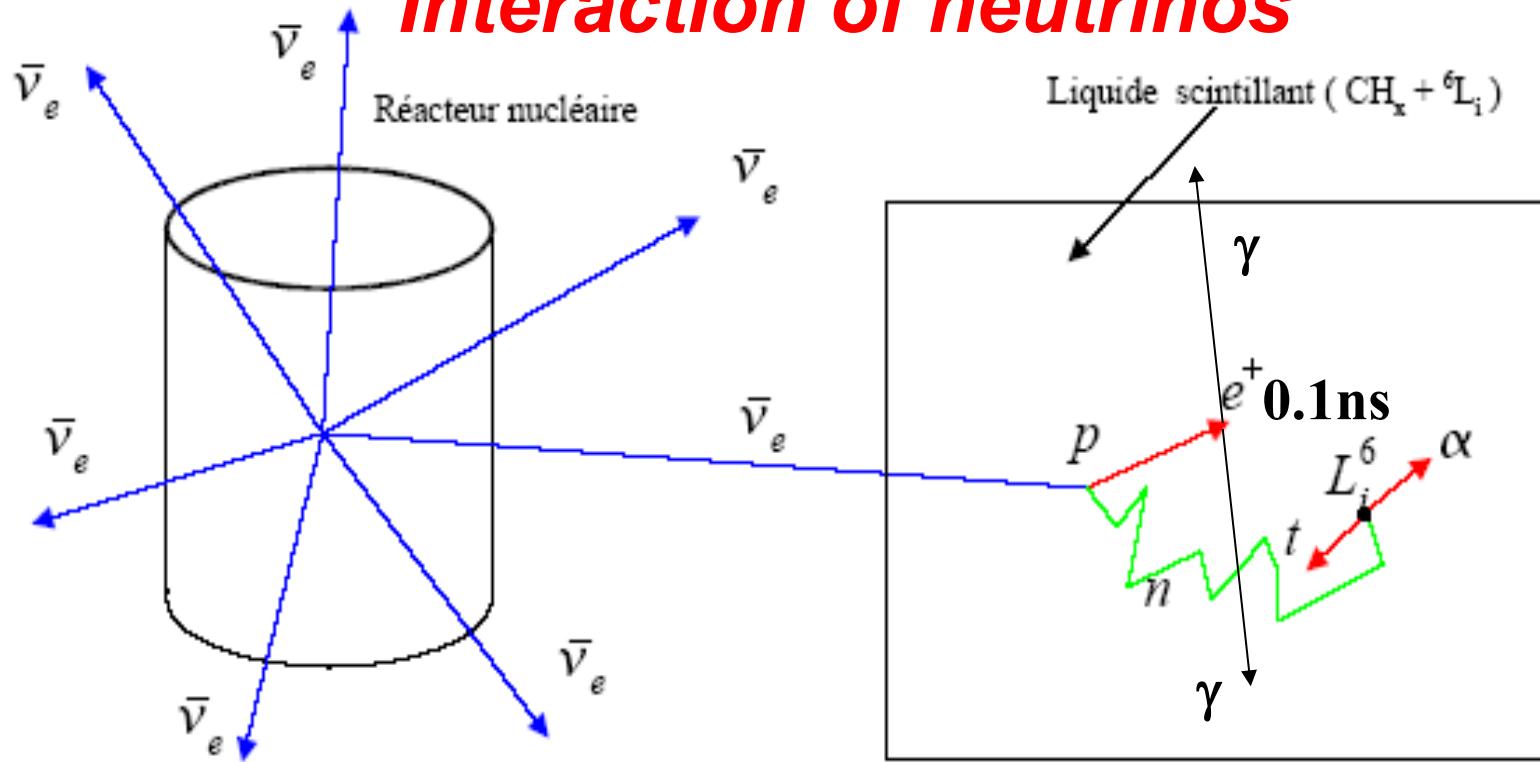


$$N = N_0 \exp(-x / \lambda);$$

$$\lambda^{-1} = N\sigma_{tot}$$

- Elastic scattering off a nucleus  $E_{\text{neutron}} \approx \text{MeV}$
- Inelastic scattering  $E_{\text{neutron}} > \text{MeV}$
- Radiative capture  $\sigma \sim 1 / \text{velocity}$
- Nuclear reactions, fission

# Interaction of neutrinos



**Reines & Cowan**  
**1959**

$$\epsilon_{\nu} \sim 0$$

La réaction de détection est :  $\bar{\nu}_e + p \rightarrow n + e^+$ , qui est rapidement (100  $\mu s$ ) suivie de la capture du neutron sur un noyau de  $L_i^6$  selon la réaction :  $n_{th} + L_i^6 \rightarrow \alpha + t + 4,8 MeV$ . Les particules chargées produisent des impulsions de scintillation en coïncidence. La signature de détection d'un neutrino correspond à l'enregistrement de deux impulsions lumineuses induites par le positon et la paire  $\alpha - t$ .

# Conclusions

- All particle detectors in nuclear, particle and astroparticle physics are based on the physics of the interaction of particles and radiation with matter
- The interactions produce free electrical charges (ionization, excitations of the medium) or sometime light (Cerenkov)
- These products of the interactions can be used to derive (electronic) signals to indicate the presence of an invisible particle
- We will see in the next lectures, how we can do this

# Some recommended exercises

- 1 Look at the classical derivation of the the Bethe-Bloch formula
  - 2 Kinematics of Compton scattering and (e+e-)-pair creation
  - 3 Cerenkov threshold for electrons in water
  - 4 Find the decay scheme of the  $^{55}\text{Fe}$  source: where do the 5.9 keV gammas come from?
  - 5 Estimate the nuclear interaction length in Iron  
(Fe, A=56;  $\rho=7.8 \text{ g/cm}^3$ )
- 
- 1 The number of particles in a em shower is proportional to the Energy. If we can measure the number of particles in a shower, how will the energy resolution scale with energy ?
  - 2 Movement of a charged particle in a magnetic field. If the curvature is measured, how well can we measure the momentum of the charged particle ?







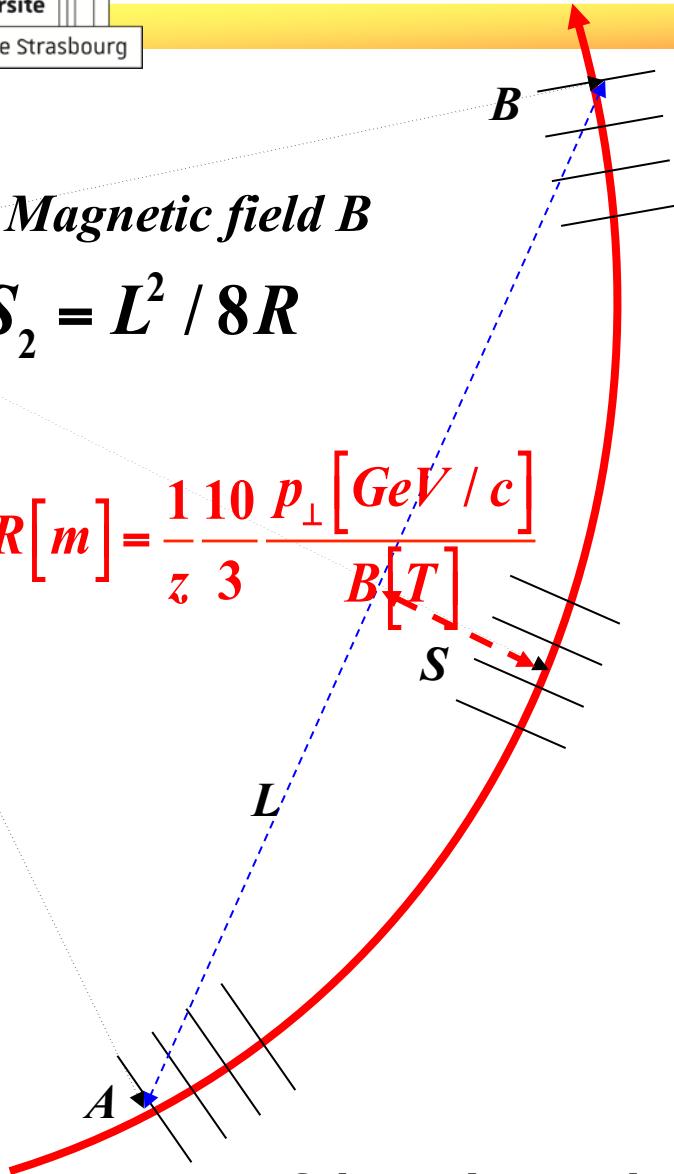


Magnetic field  $B$

$$S_2 = L^2 / 8R$$

$$R[m] = \frac{1}{z} \frac{10}{3} \frac{p_{\perp}[GeV/c]}{B[T]}$$

$R$



If the trajectory is measured with  $N$  points:

$$\frac{dS}{S} = \frac{dp_{\perp}}{p_{\perp}} = \frac{80}{3 \cdot z} \frac{1}{BL^2} p_{\perp} dS$$

$$[B] = \text{Tesla}; [L] = \text{m}; [p_{\perp}] = \text{GeV}/c$$

$$\left| \frac{\sigma(p_T)}{p_T} \right|^{meas.} = \frac{\sigma(x) \cdot p_T}{0.3 \cdot BL^2} \sqrt{720/(N+4)} \quad (\text{for } N \geq \sim 10)$$

Exercise!!!

## Reconstruction of transverse momentum in a magnetic field

- Movement of a charge  $z$  in a uniform magnetic field
- Momentum resolution  $dp/p$
- Spatial resolution of the sagitta  $dS/S$

$$R^2 = \left(L/2\right)^2 + (R-S)^2$$

$$0 = S^2 - 2RS + L^2/4$$

$$S_{1,2} = R \left( 1 \pm \sqrt{1 - \left( L/2R \right)^2} \right)$$

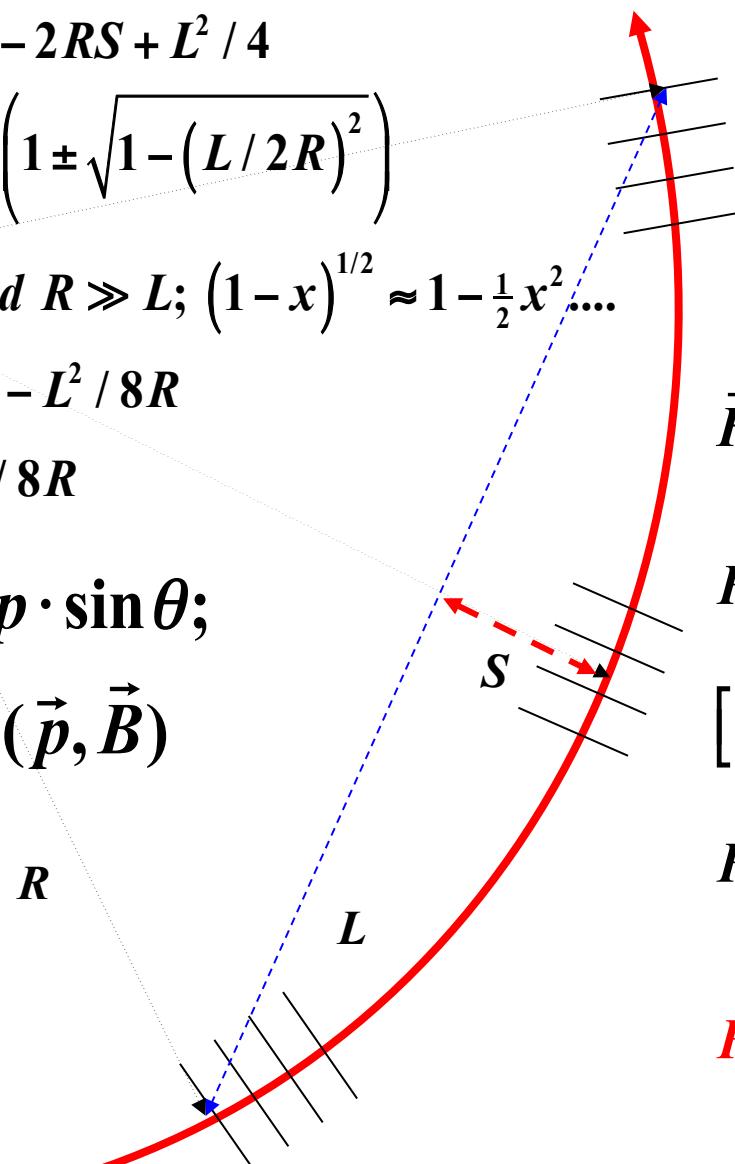
$$p_\perp \text{ grand } R \gg L; (1-x)^{1/2} \approx 1 - \frac{1}{2}x^2 \dots$$

$$S_1 = 2R - L^2/8R$$

$$S_2 = L^2/8R$$

$$p_\perp = p \cdot \sin \theta;$$

$$\theta = \alpha(\vec{p}, \vec{B})$$



## Momentum reconstruction in a uniform magnetic field

$$\vec{F} = q \cdot (\vec{v} \times \vec{B}) = m \vec{a}_R = m \frac{\vec{v}^2}{R}; \vec{v} \perp \vec{B}$$

$$R = \frac{m}{q} \frac{v}{B} = \frac{p_\perp}{q \cdot B}$$

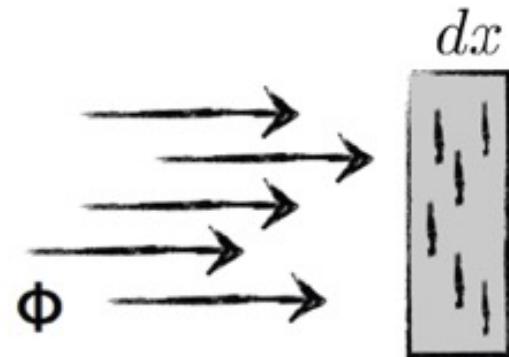
$$[p_\perp] = GeV/c; [q] = e \cdot z; [B] = T_{esla} = Vs/m^2$$

$$R = \frac{1}{z \cdot e} \frac{10^9 eV}{c} \frac{1}{Vs/m^2}; c = 3 \cdot 10^8 m/s$$

$$R[m] = \frac{1}{z} \frac{10}{3} \frac{p_\perp [GeV/c]}{B[T]}$$

# INTERACTION CROSS-SECTION

Flux  $\Phi = \frac{1}{S} \frac{dN_i}{dt}$  [L<sup>-2</sup>t<sup>-1</sup>]



Reactions per unit of time  $\frac{dN_{\text{reac}}}{dt} = \Phi \underbrace{\sigma N_{\text{target}} dx}_{\substack{[\text{L}^{-2}\text{t}^{-1}] [\text{?}] [\text{L}^{-1}] [\text{L}]}}$  [t<sup>-1</sup>] area obscured by target particle

Reaction rate per target particle  $W_{if} = \Phi \sigma$  [t<sup>-1</sup>]

Cross section per target particle  $\sigma = \frac{W_{if}}{\Phi}$  [L<sup>2</sup>] = reaction rate per unit of flux

1 b = 10<sup>-28</sup> m<sup>2</sup> (roughly the area of a nucleus with A = 100)

# CROSS-SECTION: ORDER OF MAGNITUDE

Standard

cross section unit:

$$[\sigma] = \text{mb}$$

$$\text{with } 1 \text{ mb} = 10^{-27} \text{ cm}^2$$

or in

natural units:

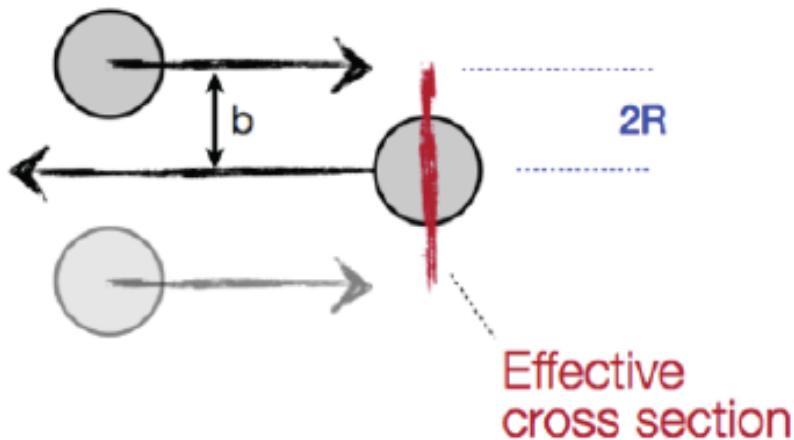
$$[\sigma] = \text{GeV}^{-2}$$

$$\text{with } 1 \text{ GeV}^{-2} = 0.389 \text{ mb}$$

$$1 \text{ mb} = 2.57 \text{ GeV}^{-2}$$

---

Estimating the  
proton-proton cross section:



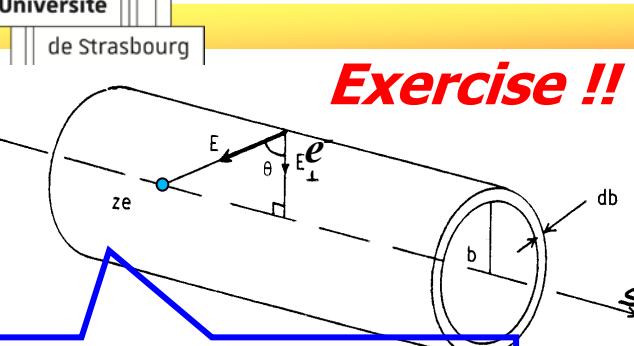
using:  $\hbar c = 0.1973 \text{ GeV fm}$   
 $(\hbar c)^2 = 0.389 \text{ GeV}^2 \text{ mb}$

Proton radius:  $R = 0.8 \text{ fm}$

Strong interactions happens up to  $b = 2R$

$$\begin{aligned}\sigma &= \pi(2R)^2 = \pi \cdot 1.6^2 \text{ fm}^2 \\ &= \pi \cdot 1.6^2 \cdot 10^{-26} \text{ cm}^2 \\ &= \pi \cdot 1.6^2 \cdot 10 \text{ mb} \\ &= 80 \text{ mb}\end{aligned}$$

## Exercise !!



**Cylinder of surface  $A$  and volume  $V$**

**Classical calculation by Bohr:**

**Momentum transfer  $\Delta p$  to the electron;**

**Energy loss of particle = - energy transfer to electron  $\Delta E$ ;**

$n_e$  = electron density

$$\Delta p_e = \int_{-\infty}^{\infty} F dt = e \int_{-\infty}^{\infty} \mathcal{E}_{\perp} dt = \frac{e}{v_0} \int_{-\infty}^{\infty} \mathcal{E}_{\perp} ds; \quad \mathcal{E}_{\perp} = \text{electric field}$$

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$$GAUSS: \iiint_V \operatorname{div} \vec{\mathcal{E}} dx dy dz = \oint_A \vec{\mathcal{E}} da; \quad \vec{\psi} = \text{vector field}$$

$$\iint_A \mathcal{E}_{\perp} da = \iiint_V \operatorname{div} \vec{\mathcal{E}} dx dy dz = \frac{1}{\epsilon_0} \iiint_V \rho dx dy dz = \frac{ze}{\epsilon_0}; \quad \operatorname{div} \vec{\mathcal{E}} = \frac{\rho}{\epsilon_0}$$

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$$da = 2\pi b ds; \quad 2\pi b \int_{-\infty}^{\infty} \mathcal{E}_{\perp} ds = \frac{ze}{\epsilon_0}$$

$$\Delta p_e = \frac{2}{4\pi\epsilon_0} \frac{ze^2}{bv_0} = 2k \frac{ze^2}{bv_0}; \quad k = \frac{1}{4\pi\epsilon_0}$$

$$\Delta E = -\Delta E_e = -\frac{(\Delta p_e)^2}{2m_e} = -2 \frac{z^2 e^4}{b^2 m_e} \left( \frac{k}{v_0} \right)^2$$

$$-dE(b) = \Delta E(b) n_e dV = 4\pi n_e \frac{z^2 e^4}{m_e} \left( \frac{k}{v_0} \right)^2 \frac{db}{b} ds; \quad (dV = 2\pi b db)$$

$$-\frac{dE}{ds} = -\int_0^{\infty} \frac{dE}{db} db = 4\pi n_e \frac{z^2 e^4}{m_e} \left( \frac{k}{v_0} \right)^2 \ln \left( \frac{b_{\max}}{b_{\min}} \right)$$

## ***Classical calculation by Bohr, $b_{min}$ and $b_{max}$***

**$b_{min}$**  : Maximal energy transfer to electron

$$T_e^{\max} = 2m_e v_0^2 \gamma^2 = 2 \frac{z^2 e^4}{b_{\min}^2 m_e} \left( \frac{k}{v_0} \right)^2$$

$$b_{\min} = \frac{z \cdot e^2 k^2}{\gamma m_e v_0^2}; \quad \gamma = \frac{1}{\sqrt{1 - \beta^2}}; \quad \beta = \frac{v_0}{c}; \quad v_0 = \text{particle speed!}$$

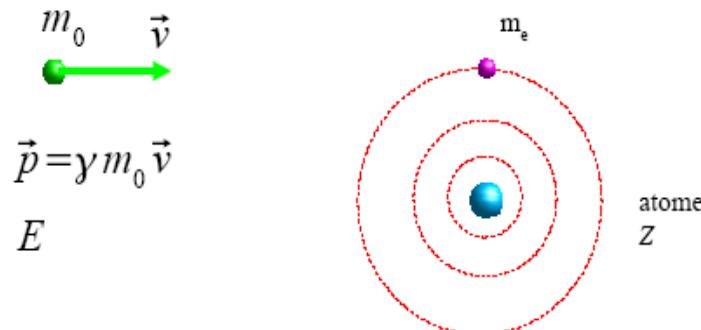
**$b_{max}$**  : interaction time  $\cong$  Orbit time  $\bar{T}$

$$\frac{b_{\max}}{\gamma v_0} \ll \bar{T}$$

$$b_{\max} = \gamma v_0 \bar{T}$$

$$-\frac{dE}{ds} = - \int_0^\infty \frac{dE}{db} db = \frac{4\pi z^2 e^4 k^2}{m_e v_0^2} n_e \ln \frac{\gamma^2 m_e v_0^3 \bar{T}}{z^2 e^2 k^2}$$

# Maximal energy transfer of charged “heavy” particles to the electrons of matter



$$v \gg v_e \simeq Z a c$$

$$E_{CM} = \left( m_0^2 c^4 + m_e^2 c^4 + 2 m_e c^2 E \right)^{\frac{1}{2}}$$

$$p_e^{CM} = p \frac{m_e c^2}{E_{CM}}$$

$$E_e^{CM} = (E + m_e c^2) \frac{m_e c^2}{E_{CM}}$$

$$\gamma^{CM} = \frac{E + m_e c^2}{E_{CM}}; \quad \beta^{CM} = \frac{pc}{E + m_e c^2}$$

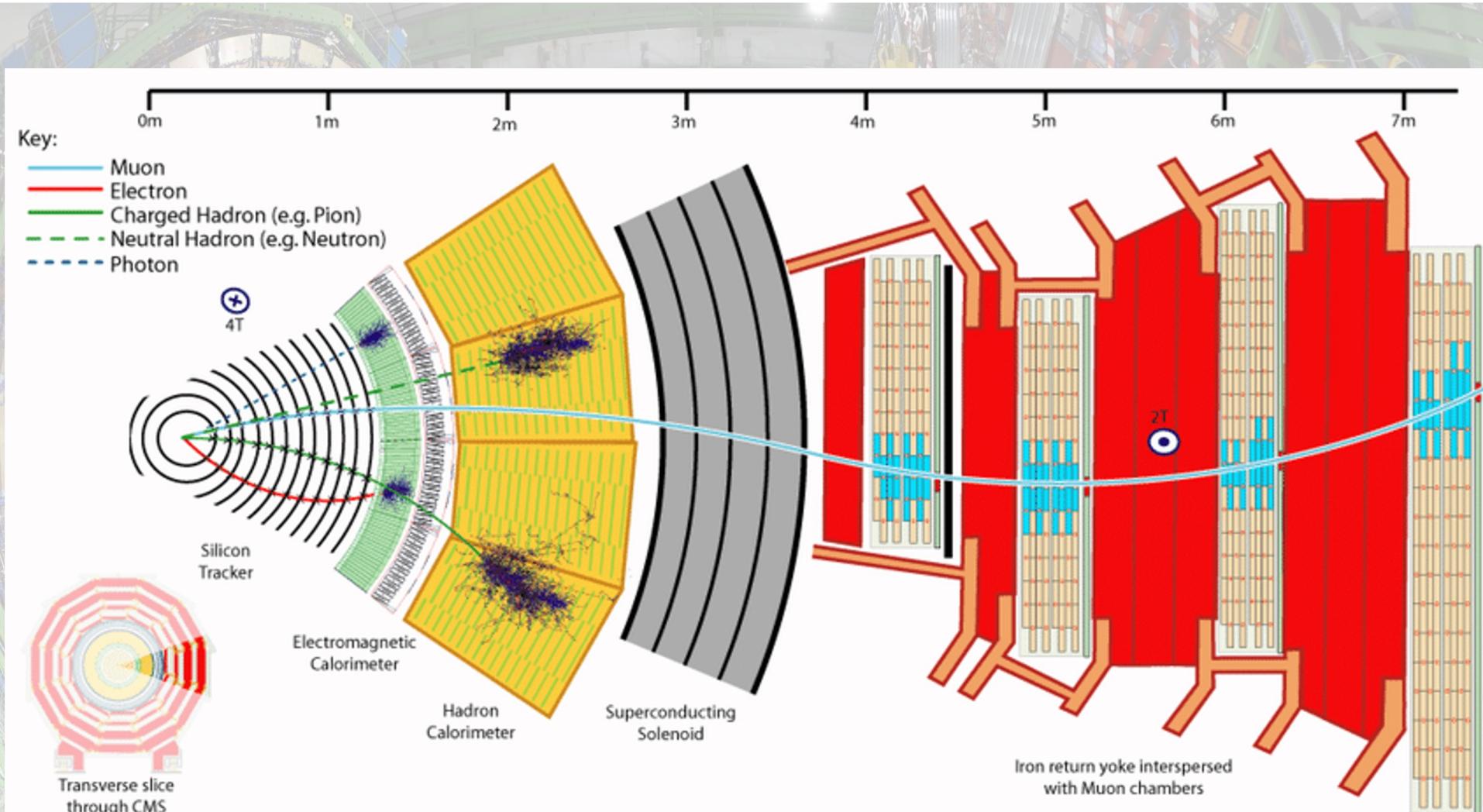
$$T_e^{\max} = E_e^{\max} - m_e c^2 = \frac{2 m_e^2 c^2 \beta^2 \gamma^2}{\left( E_{CM} / m_0 c^2 \right)^2}$$

$$m_0 \gg m_e; \quad 2 \gamma m_e / m_0 \ll 1$$

$$T_e^{\max} = 2 m_e c^2 \beta^2 \gamma^2$$

$$m_0 = m_e$$

$$T_e^{\max} = \frac{E^2 - m_e^2 c^4}{m_e c^2 + E} = E - m_e c^2 = T_e = T_0$$



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