

# **Discovery of a Glueball-like particle X(2370)** (*a*) **BESIII**



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- (On behalf of the BESIII Collaboration)
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# The Standard Model



- - Gluons are the force carriers of the strong interactions
  - Gluon self-interaction: prediction of non-Abelian Gauge SU(3) QCD theory

The basic theory for strong interactions is quantum chromodynamics (QCD)











## Other forms of hadrons:

- Multi-quark: quark number >= 4
- Hybrid state: the mixture of quark and gluon
- + Glueball: composed of gluons (gg, ggg, gggg ....)



## Glueballs are unique particles formed by gluons (force carriers) due to non-Abelian gauge self-interactions of gluons

# **Forms of hadrons**







- Quenched lattice QCD is the non-perturbative method for this theory from the first principles.
- The predictions of masses and production rates of pure glueballs are expected to be reliable.
  - Lattice QCD predictions:
  - ◆ 0++ ground state: 1.5 1.7 GeV/c<sup>2</sup>
  - ◆ 2++ ground state: 2.3 2.4GeV/c<sup>2</sup>
    - **0-+ ground state:** 2.3 2.6GeV/c<sup>2</sup>





# **Glueball Search**

- $J/\psi$  radiative decays from electron-positron collision
  - positron collision
  - Glueball production in J/ψ radiative decays
  - Glueball decays
  - Many historical glueball candidates, but also some difficulties

Many experiments searched for glueballs over the past 4 decades, mostly in

+ The advantage for glueball searches via  $J/\psi$  radiative decays from electron-







**Gluon rich environment** 



- Isospin filter: final states dominated by I=0 processes
- Spin-parity filter: C parity must be +, so J<sup>pc</sup>=0<sup>-+</sup>, 0<sup>++</sup>, 1<sup>++</sup>, 2<sup>++</sup>, 2<sup>-+</sup>...
- Clean environment in electron-positron collision: very different from proton-antiproton collision
- Ideal place to search for glueballs

# J/\u03c6 radiative decays





## Glueball Production in J/\u03c6 radiative decays

## $\boldsymbol{\circledast}$ Rich production in $J/\psi$ radiative decays:

+ Glueball production rate in  $J/\psi$  radiative decays could be higher than normal hadrons









## Flavor symmetric decays

- No rigorous predictions on decay patterns and their branching ratios
- since both of them can only decay via gluons
  - $\bullet$  e.g. the 0<sup>-+</sup> glueball could have similar decays of  $\eta_c$
  - One of the favorite decay modes of  $\eta_c$  is  $\pi\pi\eta'$ , so  $J/\psi \rightarrow \gamma \pi\pi\eta'$  could be a good place to search for the 0<sup>-+</sup> glueball

# The glueball decays could have similar decays to the Charmonium families





## Historical Glueball Candidates — 0<sup>++</sup> scalar Glueball

- fo(1710): discovered by MarkII in 1980's as  $\theta_2(1720)$  and  $J^{pc} = 2^{++}$  from a simple fit to the angular distribution. Lots of studies at MarkII, DM2, BESI, BESII, BESII
  - + J<sup>pc</sup> was firstly changed to 0<sup>++</sup> on a full PWA of  $J/\psi \rightarrow \gamma KK @$  BESI
  - + The high production rate of  $J/\psi \rightarrow \gamma f_0(1710)$  and the suppression of  $f_0(1710) \rightarrow \eta \eta'$  strongly support its interpretation:
    - · A scalar glueball or large glueball content if it is a mixture of glueball and normal meson
  - + With PS subtracted,  $\Gamma(f_0(1710) \rightarrow \pi \pi: KK) = 1:2.43$ , which should be 1:1 for a pure glueball decays
  - Difficulty: What causes the flavor symmetric breaking needs to be understood from first principle of QCD (not just phenomenological understanding).
  - $B[J/\psi \to \gamma f_0(1710) \to \gamma \pi \pi] = (4.01 \pm 1.0) \times 10^{-4}$ • BESII: PLB 642 441 (2006)
  - $B[J/\psi \rightarrow \gamma f_0(1710) \rightarrow \gamma K_s^0 K_s^0] = (2.00^{+0.03+0.31}_{-0.02-0.10}) \times 10^{-4}$ • BESIII: PRD 98 072003 (2018)

## **A lot of studies from BES in** $J/\psi \rightarrow \gamma KK, \gamma \pi \pi, \gamma \eta \eta, \gamma \eta \eta'$

 $B[f_0(1500) \rightarrow \eta \eta']/B[f_0(1500) \rightarrow \pi \pi] = (1.66^{+0.42}_{-0.40}) \times 10^{-1}$  $B[f_0(1710) \to \eta \eta']/B[f_0(1710) \to \pi \pi] < (2.9^{+1.1}_{-0.9}) \times 10^{-3}$ • BESIII: PRD 106 072012 (2022)







## Historical Glueball Candidates — 0<sup>++</sup> scalar Glueball

- ♦ f<sub>0</sub>(1500): discovered by Crystal Barrel in 1990's as a unique 0++ candidate since  $f_0(1710)$  was  $f_2$  at that time.
  - Difficulty: compared with  $f_0(1710)$ , much lower production rate than  $f_0(1710)$ disfavors its interpretation as a scalar glueball
- Mixing between  $f_0(1500)/f_0(1710)$ , or even with  $f_0(1790)$ 
  - Difficulty: dynamic mixing mechanism needs to be understood from the first principle of QCD (not just phenomenological understanding).

BESIII:  

$$B(J/\psi \rightarrow \gamma f_0(1 + B(J/\psi \rightarrow \gamma f_0(1 + \gamma f_0(1 +$$

 $(1500)) \sim 0.29 \times 10^{-3}$  $(1710)) \sim 2.2 \times 10^{-3}$ 





## 

- First observed by MarkIII is J/ψ→ γKK in 1980's, then by BESI in 1990's in J/ψ → γKK, γππ, γppbar with very narrow mass peak.
- + It was a tensor glueball candidate due to good flavor symmetric decay property.
- Difficulty: it was not confirmed by BESII, nor BESIII with much higher statistics.



- ♦ f<sub>2</sub>(2340)

  - resonances. (PWA components)



+ Its large production rate in  $J/\psi \rightarrow \gamma (KK/\eta \eta / \eta' \eta' / \phi \phi)$  favors its interpretation as a tensor glueball. A Many wide f<sub>2</sub> mesons in the mass region of 2.3GeV of 2++ glueball mass from the LQCD predictions + Difficulty: no clear mass peak of these f<sub>2</sub> mesons due to large overlaps among various wide

 More PWA studies are needed to check the consistency among various decays modes. However, due to large overlaps again, no independent mass and width scan can be performed in PWA.

Resonance	M (MeV/ $c^2$ )	$\Gamma ({\rm MeV}/c^2)$	B.F. (×10 <sup>-</sup>
$\eta(2225)$	$2216^{+4+21}_{-5-11}$	$185^{+12+43}_{-14-17}$	$(2.40 \pm 0.10)$
$\eta(2100)$	$2050_{-24-26}^{+30+75}$	$250^{+36+181}_{-30-164}$	$(3.30 \pm 0.09)$
<i>X</i> (2500)	$2470^{+15+101}_{-19-23}$	$230^{+64+56}_{-35-33}$	$(0.17 \pm 0.02)$
$f_{s}(2100)$	2101	224	$(0.43 \pm 0.04)$
$f_2(2010)$	2011	202	$(0.35 \pm 0.05)$
$f_2(2300)$	2297	149	$(0.44 \pm 0.07)$
$f_2(2340)$	2339	319	$(1.91 \pm 0.14)$
0 <sup>-+</sup> PHSP			$(2.74 \pm 0.15)$









## ♦ ŋ(1405)

- + first discovered by MarkII in 1980's, named as  $\eta(1440)$  with complicated structures. Lots of studies at MarkII, MarkIII, DM2 and BES.
- + Believed as the first glueball candidate due to its large production rate in  $J/\psi$ radiative decays and lack of reliable LQCD predictions in 1980's
- No longer to be 0-+ glueball candidate due to its large different mass from LQCD prediction.





## Historical Difficulties in Glueball Searches

### Theoretically:

- + No prediction on the decay branch ratios so far (even the order)
- + Very rare prediction on the glueball production rate  $\Gamma(J/\psi \rightarrow \gamma G)$
- + Mix with qqbar mesons or even with 4q, qqg, mesons? Mixing dynamics?

### Experimentally:

- Data sample was not big enough
- No good way modeling background in many cases.
- + Interference among mesons makes the analysis more complicated:
  - PWA is a must, but it is complicated and takes a quite long time.



## **Beijing Electron Positron Collider (BEPCII)**

## World unique e+e- accelerator in charm physics energy region



e

### **BESIII detector**



## **2004: Construction**

- Double rings
- Beam energy:
  - 1.0 2.3 (2.45)GeV
- Designed luminosity:
  - 1×10<sup>33</sup> cm<sup>-2</sup> s<sup>-1</sup>

2008: test run

2009-now: BESIII physics runs





# **BESII detector**

### **Designed for neutral and charged particle with excellent resolution, PID, and large coverage**



Total weight 730 ton, ~40,000 readout channel Data rate: 5kHz, 50Mb/s



### Has been in full operation since 2008, all sub-detectors are in very good status!





# **BESIII Collaboration**

### Political Map of the World, November 2011



SALADAR ULLAR.

~600 members (more than 130 from outside of China) From 89 institutions in 17 countries Presed Real Print Print

### Europe (17/115)

Germany (6): Bochum University, GSI Darmstodt, Helmholtz Institute Mainz, Johannes Gutenberg University of Mainz, Universitaet Giessen, University of Münster Italy (3): Ferrara University, INFN, University of Torino Netherlands (1):KVI/University of Croningen Russia (2): Budker Institute of Nuclear Physics, Dubna JINR Sweden (1):Uppsala University Turkey (1):Turkish Accelerator Center Particle Factory Group UK (2): University of Manchester, University of Cotord Poland (1)National Centre for Nuclear Research

### Asia (6/10)

Pakistan (2): COMSATS Institute of Information Technology University of the Punjab, University of Lahore Mongolia (1): Institute of Physics and Technology Korea (1): Chung-Ang University India (1): Indian Institute of Technology madras Thailand (1): Suranaree University of Technology

### China (60/367)

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nstitute of High Energy Physics (146), other units(221): Beijing Institute of Petro-chemical Technology, Beihang University, China Center of Advanced Science and Technology, Fudan University, Guangxi Normal University, Guangxi University, Hangzhou Normal University, Henan Normal University, 10111 STLATT Henan University of Science and Technology. ICEAN. Huazhong Normal University, Huangshan College, Hunan University, ----Hunan Normal University, Henan University of Technology Institute of modern physics, Jilin University, Lanzhou University, Liaoning Normal University, Liaoning University, Nanjing Normal University, Nanjing University, Nankai University, North China Electric Power University, Peking University, Qufu normal university, Shanxi University, Shanxi Normal University, Sichuan University, Shandong Normal University, Shandong University, Shanghai Jiaotong University, Soochow University, South China Normal University, Southeast University, Sun Yat-sen University, Tsinghua University, University of Chinese Academy of Sciences, University of Jinan, University of Antarotica Science and Technology of China, University of Science and Technology Liaoning,

University of South China, Wuhan University, Xinyang Normal University, Zhejiang University, Zhengzhou University, YunNan University , China University of Geosciences



# BESII Data samples



### Totally about 50fb<sup>-1</sup> integrated luminosity

## World largest J/ $\psi$ data sample : ~10 billion



# Observation of the X(2370) in 2011





## $J/\psi \rightarrow \gamma \pi^+\pi^-\eta^2$ With ~225M J/ $\psi$ events

	M(MeV/c <sup>2</sup> )	Γ(MeV/c <sup>2</sup> )	S
X(1835)	1836.5±3.0+5.6-2.1	190.1±9.0+38-36	>'_
X(2120)	2122.4±6.7 <sup>+4.7</sup> -2.7	83±16 <sup>+31</sup> -11	7
X(2370)	2376.3±8.7+3.2-4.3	83±17+44-6	6

## $\odot$ Discovery of X(2370) in J/ $\psi \rightarrow \gamma \pi^+ \pi^- \eta^2$ with the statistic significance of 6.4 $\sigma$

- Mass, production and decay property are consistent with the LQCD prediction









## Confirmation of the X(2370) in $J/\psi \rightarrow \gamma KK\eta^2$



## Observation: X(2370) new decay mode of KKŋ'

- **Combination with 1.31 \times 10^9 \text{ J/}\psi events** 
  - $J/\psi \rightarrow \gamma K^+ K^- \eta'$  and  $J/\psi \rightarrow \gamma K_s K_s \eta'$
  - η'  $\rightarrow \gamma \pi \pi$  and η' $\rightarrow \pi \pi \eta$
- **\odot** Confirmation of the X(2370) with 8.3 $\sigma$ 
  - M = 2341.6±6.5(stat.)±5.7(syst.) MeV
  - $\Gamma = 117 \pm 10$ (stat.) $\pm 8$ (syst.) MeV
  - $Br(J/\psi \rightarrow \gamma X(2370) \rightarrow \gamma K^+K^-\eta') = (1.79 \pm 0.23 \pm 0.65) \times 10^{-5}$
  - $Br(J/\psi \rightarrow \gamma X(2370) \rightarrow \gamma KsKs\eta') = (1.18 \pm 0.32 \pm 0.39) \times 10^{-5}$





- Its mass is consistent with LQCD prediction on the 0<sup>-+</sup> glueball
- Observed in flavor symmetric decay modes of  $\pi^+\pi^-\eta'$  and KK $\eta'$  — favorite decay modes of 0<sup>-+</sup> glueball

We need to know its spin-parity

# X(2370) - good candidate of 0<sup>-+</sup> glueball





5

4

3

2

1



### Theoretically:

### + Guidance from $\eta_c$ decays

- Now we have prediction on glueball production rate from LQCD:  $B(J/\psi \rightarrow \gamma G_{0-+}) = 2.31 \pm 0.80 \times 10^{-4}$

### Experimentally:

- + World largest  $J/\psi$  data sample : ~10 billion
- Physics channels with few background
- GPU technique helps to speed up PWA [J.Phys.Conf. Ser. 219, 042031]

+ Luckily, for the X(2370), there is **no other 0**<sup>-+</sup> **resonance nearby** (in ~200MeV range) in  $J/\psi$  radiative decays

It takes a long time in PWA for the complicated interference and comprehensive test of different combinations





## Spin-Parity determination of the X(2370) in $J/\psi \rightarrow \gamma K^0_s K^0_s \eta^2$



- parity conservation.
- $\sim 10B \ clean \ J/\psi \ events$
- good reconstruction for  $K_{s}^{0}/\eta'$

## Almost no background: possible dominant background processes of J/ $\psi \rightarrow \pi^0 K_s^0 K_s^0 \eta'$ and $J/\psi \rightarrow K_s^0 K_s^0 \eta'$ are forbidden by exchange symmetry and C-

## High-precision efficiency and resolution of charged particles and photons:





### Signal selection:

- At least 3 charged pairs + 3 photons
- Constraint kinematic fit with energy-momentum conservation
- $K_{0s}$  reconstruction:  $|M_{\pi\pi} m_{Ks}| < 9 \text{ MeV/c}^2$
- +  $\eta$ ' reconstruction:  $|M_{\pi\pi\eta} m_{\eta'}| < 10 \text{ MeV/c}^2$

### **Background veto:**





# Selection for $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta^2$ , $\eta^2 \rightarrow \pi^+ \pi^- \eta$



Clean K<sup>0</sup><sub>s</sub> and η' Signal



### Signal selection:

- At least 3 charged pairs + 2 photons
- Constraint kinematic fit with energy-momentum conservation
- $K_{0s}$  reconstruction:  $|M_{\pi\pi} m_{Ks}| < 9 \text{ MeV/c}^2$
- +  $\eta$ ' reconstruction:  $|M_{\pi\pi\eta} m_{\eta'}| < 15 \text{ MeV/c}^2$

### **Background veto:**

•  $\pi^0/\eta$  veto:  $|M_{\gamma\gamma} - m_{\pi 0}| > 20 \text{MeV/c}^2$ ,  $|M_{\gamma\gamma} - m_{\eta}| > 30 \text{MeV/c}^2$ 



Selection for  $J/\psi \rightarrow \gamma K^0_s K^0_s \eta^2$ ,  $\eta^2 \rightarrow \gamma \pi^+ \pi^-$ 



Clean K<sup>0</sup><sub>s</sub> and η' Signal



- ♦ Negligible mis-combination for K<sup>0</sup><sub>s</sub> reconstruction ( <0.1%)</p>
- No background from  $J/\psi \rightarrow \pi^0 K^0_{s} K^0_{s} \eta'$ : further validation directly from data
- Little background from non- $\eta$ ' processes: estimated directly from  $\eta$ ' mass sideband region:
  - No peaking background
  - + Non- $\eta$ ' background fraction: 1.8% for  $\eta' \rightarrow \pi^+\pi^-\eta$  6.8% for  $\eta' \rightarrow \gamma\pi^+\pi^-$



## The process with almost no background is good for the PWA







# Mass spectrum after final selection



### Similar structures in $\eta' \rightarrow \pi^+\pi^-\eta / \gamma\pi^+\pi^-$ modes:

- Evident f<sub>0</sub>(980) in K<sup>0</sup><sub>s</sub>K<sup>0</sup><sub>s</sub> mass threshold
- + A clear connection between the f<sub>0</sub>(980) and X(2370)

### • $f_0(980)$ selection with M(K<sup>0</sup><sub>s</sub>K<sup>0</sup><sub>s</sub>) <1.1GeV/c<sup>2</sup>

- + Clear signal of the X(2370) and  $\eta_c$
- Reduce PWA complexities from additional intermediate processes





# Partial wave analysis

It is necessary to perform partial wave analysis: To determine quantum numbers and interferences Amplitude construction with covariant tensor formalism [EPJA 16 (2003) 537 ] Parametrization with quasi-sequential two-body decays (only spin J(X)<3 states ): + J/ $\psi$ →γX, X→Yη': Y represent K<sup>0</sup><sub>s</sub>K<sup>0</sup><sub>s</sub> + J/ψ→γX, X→ZK<sup>0</sup><sub>s</sub>: Z represent K<sup>0</sup><sub>s</sub> η'  $\bullet$  An un-binned maximum likelihood fit on the combination of  $\eta' \rightarrow \pi^+\pi^-\eta / \gamma\pi^+\pi^-$  modes: + Non- $\eta$ ' background subtraction with the NLL values of events from  $\eta$ ' sideband region  $S = (-\ln \mathcal{L})_{data} - (-\ln \mathcal{L})_{bg} = -\left(\sum_{i=1}^{N_{data}}\right)$ 

$$\left(\ln\frac{\omega(\xi_i)}{\sigma}\right) + f_{norm} \cdot \left(\sum_{i=1}^{N_{sideband}} \ln\frac{\omega(\xi_i)}{\sigma}\right)$$





# PWA Fit



- Best fit can well describe the data including resonances (>5σ):
   X(1835), X(2370), X(2800), η<sub>c</sub>
  - Spin-parity of the X(2370) is determined to be 0<sup>-+</sup> with significance larger than 9.8σ w.r.t. other J<sup>pc</sup> assumptions
  - X(2800): a broad structure for the effective contributions from possible high mass resonances and the tail of  $\eta_c$  lineshape



cay mode	Mass ( $MeV/c^2$ )	Width ( $MeV/c^2$ )	Significan
$\dot{\eta}_{0}(980)\eta'$	2395 <sup>+11</sup> <sub>-11</sub>	$188^{+18}_{-17}$	14.9 <i>o</i>
$\dot{\mu}_{0}(980)\eta'$	1844	192	$22.0\sigma$
$\dot{\mu}_{0}(980)\eta'$	2799 <sup>+52</sup> <sub>-48</sub>	$660^{+180}_{-116}$	16.4 <i>σ</i>
$\dot{\mu}_{0}(980)\eta'$	2983.9	32.0	> 20.00
$(S_S^0 K_S^0)_{S-wave}$			$9.0\sigma$
${}^{0}_{S}K^{0}_{S})_{D-wave}$			16.3 <i>σ</i>









### • Additional decay modes: significance $<3\sigma$ and impact is ignored

 $K_2^*(1430)K_{s^0}, K_0^*(1680)K_{s^0}, (K_{s^0}K_{s^0})_s\eta', (K_{s^0}K_{s^0})_D\eta', (K_{s^0}\eta')_PK_{s^0}, (K_{s^0}\eta')_DK_{s^0}$ 

### Additional resonance checks: significance <5σ</p>

- + No evidence of the X(2120) in the  $K_sK_s$  mass threshold region for  $J/\psi \rightarrow \gamma K_sK_s\eta'$  only
- + The significance of X(2600)→ $f_0(980)$ η' is 4.2σ
- + Impact from the X(2120) and X(2600) is taken into account as systematic uncertainty
- The X(2800) with a mass of 2799 MeV and width of 660 MeV:
  - Used to described effective contributions from high mass region
  - + Strongly reply on the description of  $\eta_c$  lineshape: different variations are included into the systematic uncertainty
  - + Statistical uncertainties of the X(2800) mass and width are included in the systematic uncertainties on the X(2370) measurements

# **PWA Validations**

+ J<sup>pc</sup> and decay modes for each components:  $f_0(1500)\eta'$ ,  $f_2(1270)\eta'$ ,  $K^*(1410)K_s^0$ ,  $K_0^*(1430)K_s^0$ ,  $K_0^*(1430)$ 











- The measurements are in a agreement with the predictions on lightest pseudoscalar glueball
  - The spin-parity of the X(2370) is determined to be 0<sup>-+</sup> for the first time
  - Mass is in a good agreement with LQCD predictions
  - (assuming ~5% decay rate,  $B(J/\psi \rightarrow \gamma X(2370)) = 10.7^{+22.8}\gamma \times 10^{-4}$ )

# Final results

+ The estimation on B(J/ $\psi \rightarrow \gamma X(2370)$ ) and prediction on B(J/ $\psi \rightarrow \gamma G_{0-+}$ ) are consistent within errors



- Qualitatively, we can clearly observe:
  - In the upper M<sub>KK</sub> mass band of 1.5-1.7GeV range, clear signals of both X(2370) and  $\eta_c$
  - In the lower M<sub>KK</sub> mass band of f<sub>0</sub>(980), no **X(2370), nor** η<sub>c</sub>.
- Such high similarity between X(2370) and  $\eta_c$ decay modes also strongly supports the glueball interpretation of the X(2370).

Study in  $J/\psi \rightarrow \gamma K^0_s K^0_s \eta$ 

Observation and Spin-Parity Determination of the X(1835) in  $J/\psi \rightarrow \gamma K_S^0 K_S^0 \eta$ 







- Glueballs are important predictions from LQCD:
  - gluons
- The X(2370) is the first particle that matches the theoretical expectations for a glueball
  - + Spin-parity quantum numbers are determined to be  $J^{pc} = 0^{-+}$
  - A Measurements and predictions on mass and production rate are consistent within errors
  - + production and decay properties: the X(2370) is observed in  $J//\psi$  radiative decay and flavor symmetric decay modes (favorite decay modes of 0<sup>-+</sup> glueball)
  - Glueball-like particle, X(2370) is discovered by BESIII

Many thanks to the efficient work: The BESIII detector maintenance and offline software teams, computing center The BEPCII accelerator operation team which provide stable detector operation

+ Unique particles formed by gluons (force carriers) due to non-Abelian Gauge self-interactions of









## More decay modes of the X(2370) will be studied at BESIII

- Including KKπ, ππη
- like particle
- Improve the measurements on the mass, width, branching ratio and production rates of the X(2370)
  - Need to have better ways to understand and control the interferences in PWA.

+ To check their similarities with  $\eta_c$ , and to understand the decay pattern of this glueball-

Looking forward to more reliable LQCD studies on the glueball properties







Exps.	MDC Wire reso.	MDC dE/dx Reso.	EMC Energy reso.		Exps. CDFII	TOF time reso. 100 ps	
CLEO	110 µm	5%	2.2-2.4 %		Belle		
Babar	125 µm	7%	2.67 %			$\frac{50  \mathrm{ps}}{(\mathrm{Barral})}$	
Belle	130 µm	5.6%	2.2 %			BESIII	98 ps (Endcap)
BESIII	115 µm	<5% (Bhabha)	2.3%			60 ps(Endcap, MRPC)	

**MUC:** Eff. ~ 96%

Noise:  $< 0.04 \text{ Hz/cm}^2(\text{Barrel}), < 0.1 \text{ Hz/cm}^2(\text{Endcap})$ 









$$\Gamma(J/\psi \to \gamma G_{0^{-+}}) = 0.0215(74) \text{ keV}$$
  
Br $(J/\psi \to \gamma G_{0^{-+}}) = 2.31(80) \times 10^{-4}.$  (32)

We introduce an effective coupling  $g_X$  to describe the interaction between the pseudoscalar X and the gluonic intermediate states in the processes  $J/\psi \rightarrow \gamma X$ , as defined in Eq. (30). It is interesting to see that all the  $g_X$ 's are comparable for the pseudoscalar glueball and the nonflavored  $q\bar{q}$  pseudoscalars ( $\eta$  states). We tentatively attribute the large production rates of the  $\eta$  states to the QCD  $U_A(1)$  anomaly which is totally a nonperturbative effect. Even though this study is performed in the quenched approximation and the uncertainty in the presence of

dynamical quarks is not controlled, we hope our result can provide useful theoretical information for experiments to unravel the properties of the possible pseudoscalar glueball.

# LQCD prediction

By applying the variational method to a large operator set, we obtain an optimal operator which couples predominantly to the ground state pseudoscalar glueball G. In this work,  $m_G$  is determined to be 2.395(14) GeV, and the onshell form factor of  $J/\psi \rightarrow \gamma G$  is derived as  $\hat{V}(0) =$ 0.0246(43), in the continuum limit, from which we obtain the following partial decay width and the production rate











![](_page_39_Figure_1.jpeg)

![](_page_39_Figure_2.jpeg)

![](_page_39_Picture_3.jpeg)

### Sources

Event selection Background estimation  $f_0(980)$  parametrization X(1835) parametrization  $\eta_c$  parametrization Breit-Wigner formula Broad  $0^{-+}$  structure Additional resonances Total

$\Delta M$	$\Delta\Gamma$	
$(MeV/c^2)$	(MeV)	$\Delta B/B(\%)$
• • •	• • •	$\pm 4.8$
+2	$+4 \\ -4$	+3.7 -5.1
-6	+7	$\pm 5.3$
$+15 \\ -12$	+24 -11	$+20.2 \\ -8.3$
-13	-8	-14.5
-1	+6	-8.3
-88	$+111 \\ -21$	$+211.8 \\ -56.5$
$+22 \\ -25$	+48 -21	$+41.9 \\ -20.8$
$+26 \\ -94$	$+124 \\ -33$	$+217.0 \\ -63.7$

component	$X(2370) \rightarrow f_0(980)\eta'$	$X(1835) \rightarrow f_0(980)\eta'$	$X(2800) \rightarrow f_0(980)\eta'$	$\eta_c \rightarrow f_0(980)\eta'$	$PHSP \rightarrow \eta'(K^0_S K^0_S)_{S-wave}$	$PHSP \rightarrow \eta'(K^0_S K^0_S)_{D-wave}$
$X(2370) \rightarrow f_0(980)\eta'$	1.00	1.12	1.15	0.08	-1.23	0.02
$X(1835) \rightarrow f_0(980)\eta'$		1.00	0.32	-0.07	-1.41	0.01
$X(2800) \rightarrow f_0(980)\eta'$			1.00	0.33	-1.18	0.02
$\eta_c \to f_0(980)\eta'$				1.00	0.11	0.00
$PHSP \to \eta'(K^0_S K^0_S)_{S-wave}$					1.00	-0.02
$PHSP \to \eta'(K^0_S K^0_S)_{D-wave}$						1.00

![](_page_41_Picture_1.jpeg)

![](_page_42_Picture_1.jpeg)