



# Refinement of the Proposed Gamma-Ray Burst Time Delay Model

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## Introduction

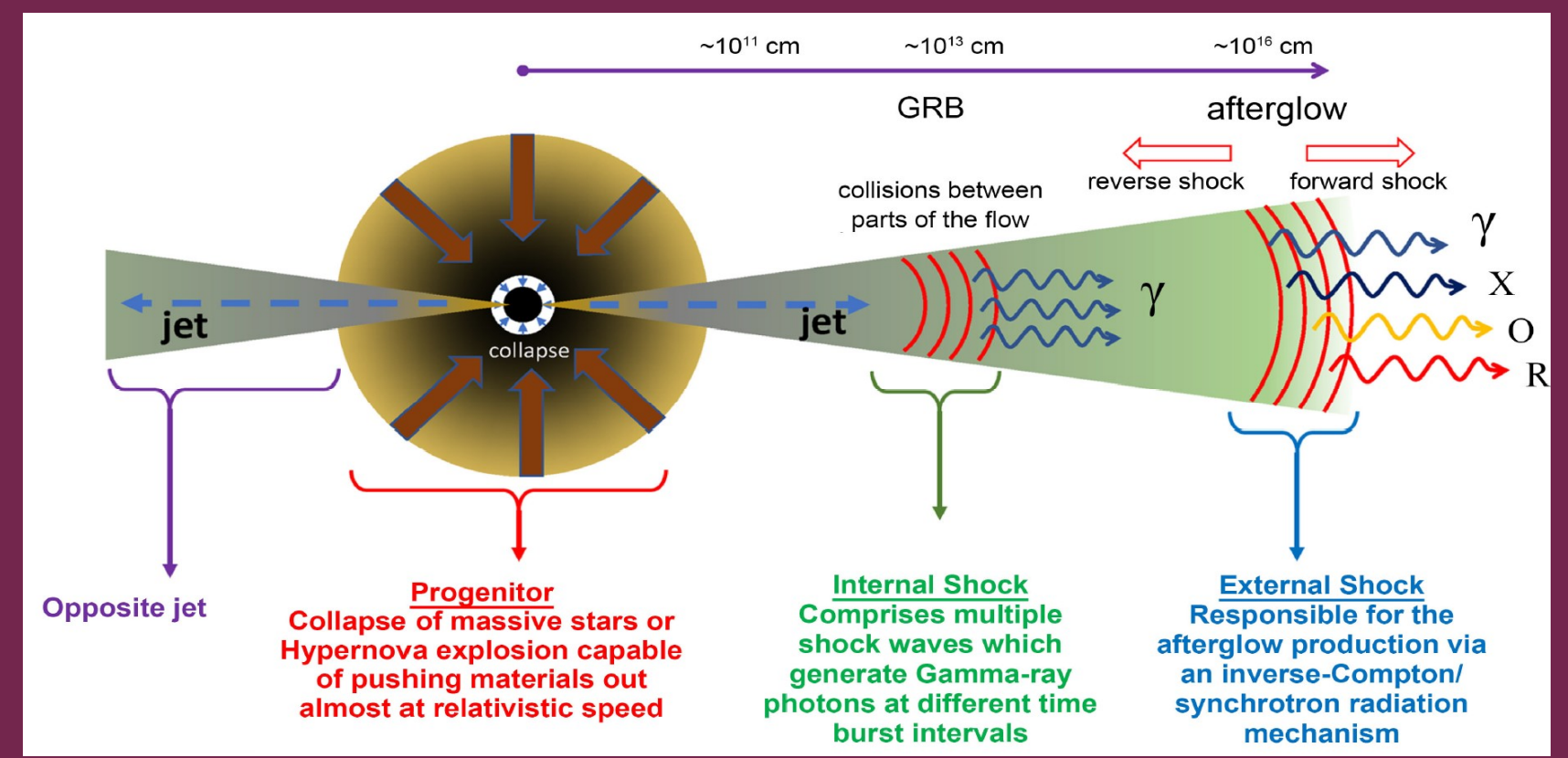


Figure 1: A modified cartoon depiction showing schematics of the fireball model and the basic components of the internal and external Shocks of GRB Jets

## Theoretical Framework

**FDSL Model:** 
$$\Delta t = \frac{Dv_*}{C} \left( \frac{1}{v_l} - \frac{1}{v_h} \right) \dots\dots\dots(1)$$

**Non-Simultaneous Emission Model:** 
$$\Delta t = \frac{Dv_*}{c_0} \left( \frac{1}{v_l} - \frac{1}{v_h} \right) + t_c \dots\dots\dots(2)$$

**Refined FDSL Model:** 
$$\frac{\Delta t}{D_{rel}} = \frac{D_* v_*}{c_0} \left( \frac{1}{v_l} - \frac{1}{v_h} \right) \dots\dots\dots(3)$$

**Conductance of the ISM:** 
$$\sigma = \frac{8\pi v_*}{\mu_0 c_0^2} = 8\pi \epsilon_0 v_* \dots\dots\dots(4)$$

**Distance Estimation:** 
$$S = \frac{Dv_*}{c_0} \dots\dots\dots(5)$$

## Key Findings

- Frequency equivalent:  $v_* \sim 1.500 \pm 0.009$  Hz.
- Distance Estimates:
  - GRB 030329 =  $69.40 \pm 0.10$  Mpc
  - GRB 980425 =  $40.00 \pm 0.00$  Mpc
  - GRB 000418 =  $58.40 \pm 0.40$  Mpc
  - GRB 021004 =  $86.00 \pm 1.00$  Mpc

## Discussions/Conclusion

- provide new insights into GRB jet dynamics and photon mass, reinforcing or challenging existing GRB models.
- The combined analysis of the four GRB sources strongly suggests that an independent distance measure to GRBs can be established because the graph of  $\Delta t / D_{rel}$  vs  $\Delta v^{-1}$  supports this position since from this graph we obtain an impressively linear correlation
- The fact that the data points of the four GRBs can be grouped into two subgroups suggests that these subgroups may very well be independent shock systems. This needs further investigation and will be subject of our next instalment which have also been published.
- The FDSL model provides a stronger theoretical framework for understanding photon time delays in GRBs.
- The results support and refine key GRB models, advancing knowledge of relativistic outflows.
- Moreover, these results lend support to two existing GRB models: the fireball model and the multiple shock wave model.
- **Future:** Explorae GRB archive involving large sample size of radio afterglow data.

## Time Delay Phenomenon

- (Albert et al., 2008; de Farias et al., 2021; Martínez & Errando, 2009; Zhang, 2019)

### Causes of Time delay

- Plasma Effect and Photon Mass Effect :  $\Delta t = K(v_h^{-2} - v_l^{-2})$
- FDSL Model:  $\Delta t = K(v_h^{-1} - v_l^{-1})$

## Specific Objectives

- To propose an alternative model based on a frequency-dependent speed of light (FDSL) in cosmic plasma (Eq. 1)
- To refine the previous GRB time delay by accounting for the non-simultaneous, systematic photon emission from the shock front (Eq. 2)
- Obtain a unified model for time delays across four different GRBs using a relative distance mechanism (Eq. 3)
- Estimate the frequency equivalence of the interstellar medium (ISM)'s conductance (Eq. 5)
- Obtain the Average distances to the four GRB samples (Eq. 5)

## Data Sample

- Zhang et al. (2016) used their GRB data to constraint the cosmological upper mass limit of the photon mass
- Chandra and Frail (2012) compiled 304 radio observations of GRB afterglows procured between January 1997 and January 2011.

## Results

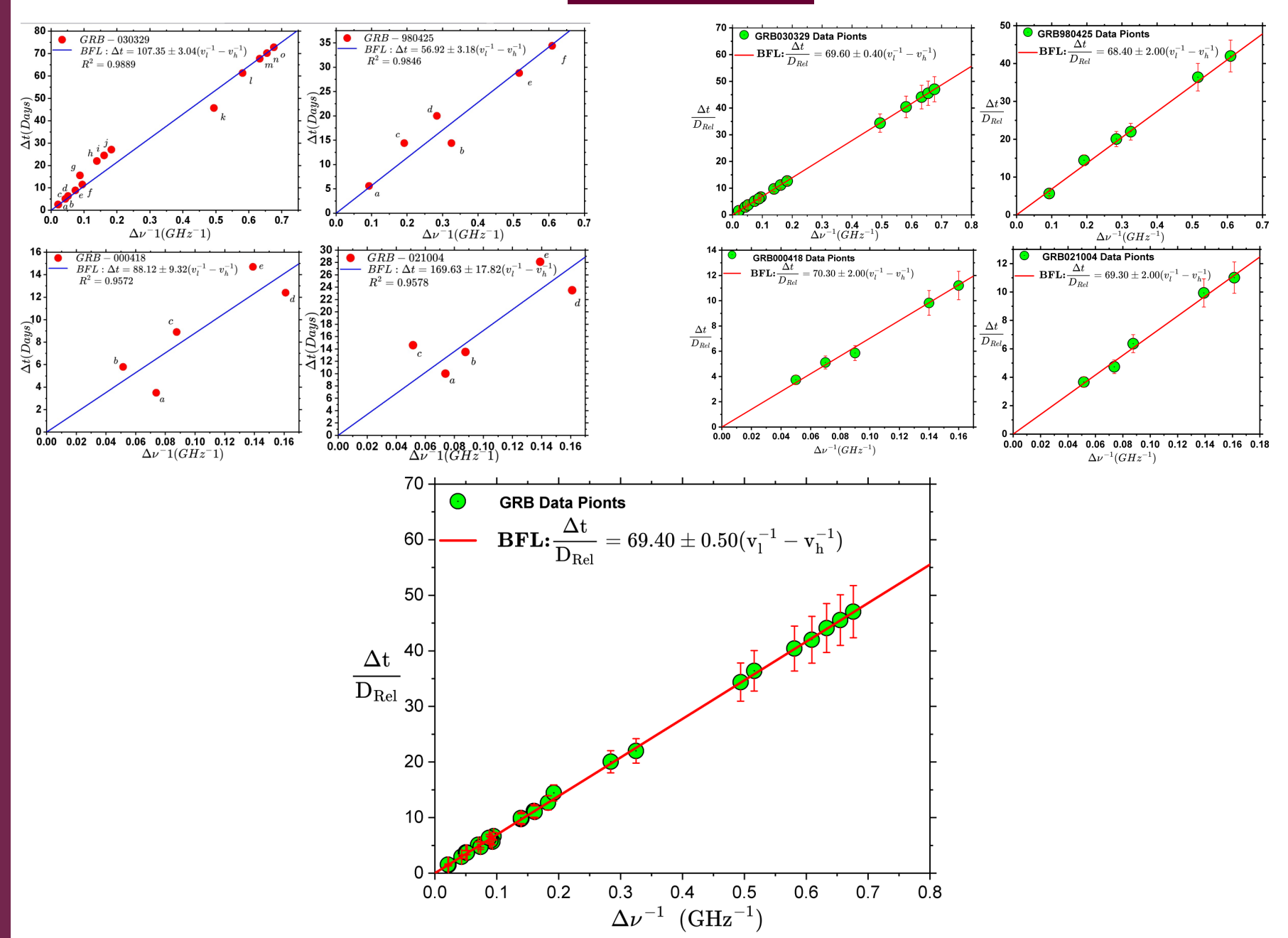


Figure 2: Final plot for GRB 030329, 980425, 000418, 021004 before and after after time delay and the relative distance correction used. Fitting passes through the origin (0, 0) naturally after the corrections were made indicating strong support for our model.

Source	Host Galaxy Redshift	Relative Distance	$D_c$ (Mpc)	$D_{avg}$ (Mpc)	$D_* v_* / c_0$ ( $10^{15}$ )	$R^2$
GRB030329	$0.1683 \pm 0.0001$	$1.7360 \pm 0.0030$	838.9000	$69.4000 \pm 0.1000$	$10.0000 \pm 0.1000$	1.0000
GRB980425	$0.0087 \pm 0.0000$	$1.0000 \pm 0.0000$	40.0000	$40.0000 \pm 0.0000$	$6.0000 \pm 2.0000$	0.9985
GRB000418	$1.1181 \pm 0.0001$	$1.4600 \pm 0.0100$	7804.0000	$58.4000 \pm 0.4000$	$9.0000 \pm 0.9000$	0.9932
GRB021004	$2.3304 \pm 0.0005$	$2.1500 \pm 0.0300$	19188.0000	$86.0000 \pm 1.0000$	$13.0000 \pm 3.0000$	0.9916
$v_* = 1.507 \pm 0.009$						

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## References

- Nyambuya, G. G., Marusenga, S., Abbey, G. F., Simpemba, P., & Simfukwe, J. (2023). Correlation in Gamma-Ray Burst Time Delays between Pairs of Radio Photons. Available at SSRN 43713(3), 195–216. <https://doi.org/10.4236/ijaa.2023.133012>
- Abbey, G. , Simfukwe, J. , Simpemba, P. , Phiri, S. , Srivastava, A. and Nyambuya, G. (2024). Refinement of the Proposed Gamma-Ray Burst Time Delay Model. International Journal of Astronomy and Astrophysics, 14, 120-147. <https://doi.org/10.4236/ijaa.2024.142008>