

## NEWS SCIENCE &amp; ENVIRONMENT

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27 August 2011 Last updated at 06:41 GMT



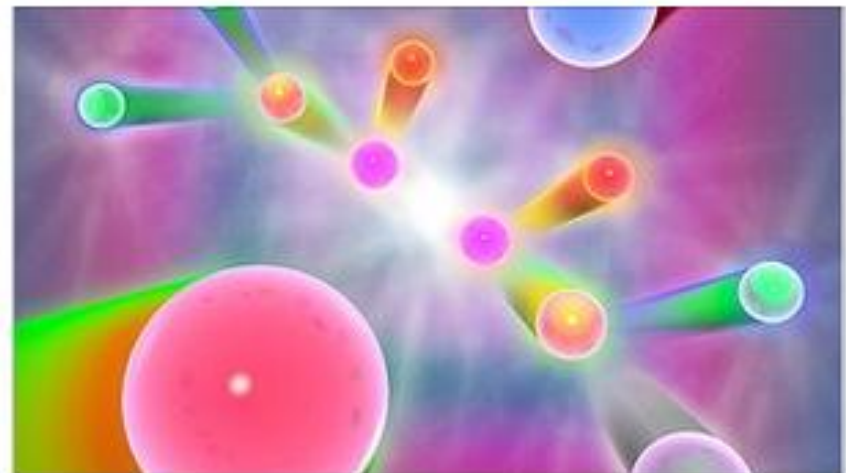
# LHC results put supersymmetry theory 'on the spot'

... nevertheless

## Overview of SUSY Global Fits

Results from the Large Hadron Collider (LHC) have all but killed the simplest version of an enticing theory of sub-atomic physics.

*John ELLIS,  
Kings College London  
& CERN, Geneva, Switzerland*



Supersymmetry predicts the existence of

# Outline

- Data
- Models
- Techniques
- Examples
- Perspectives

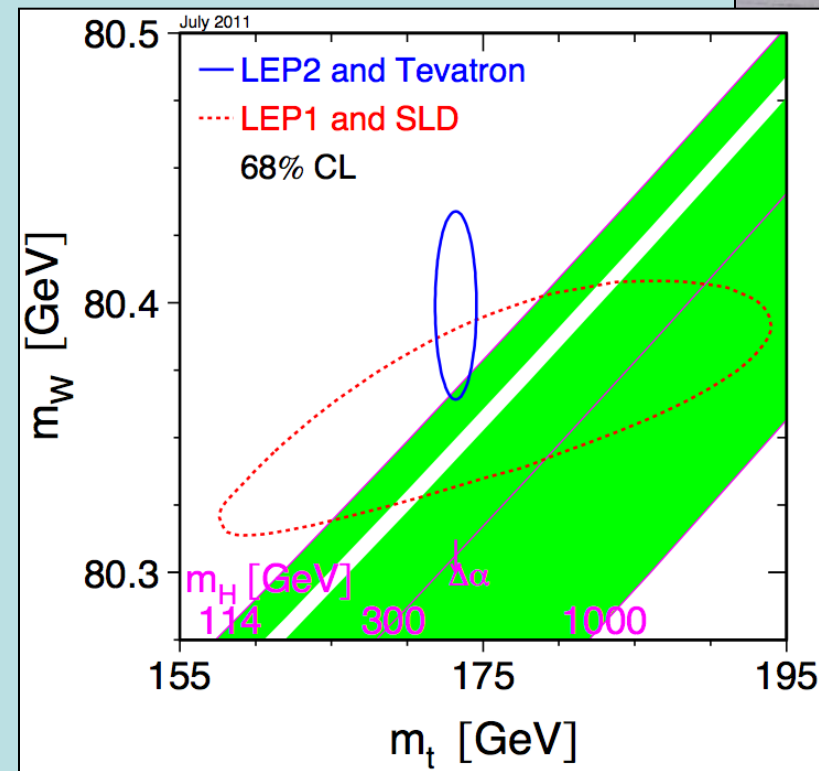
# Data

- **Electroweak precision observables**
- **Flavour physics observables**
- $g_\mu - 2$
- Higgs mass
- Dark matter
- **LHC**

Observable	Source Th./Ex.	Constraint
$m_t$ [GeV]	[39]	$173.2 \pm 0.90$
$\Delta\alpha_{\text{had}}^{(5)}(m_Z)$	[38]	$0.02749 \pm 0.00010$
$M_Z$ [GeV]	[40]	$91.1875 \pm 0.0021$
$\Gamma_Z$ [GeV]	[24] / [40]	$2.4952 \pm 0.0023 \pm 0.001_{\text{SUSY}}$
$\sigma_{\text{had}}^0$ [nb]	[24] / [40]	$41.540 \pm 0.037$
$R_t$	[24] / [40]	$20.767 \pm 0.025$
$A_{\text{fb}}(\ell)$	[24] / [40]	$0.01714 \pm 0.00095$
$A_\ell(P_\tau)$	[24] / [40]	$0.1465 \pm 0.0032$
$R_b$	[24] / [40]	$0.21629 \pm 0.00066$
$R_c$	[24] / [40]	$0.1721 \pm 0.0030$
$A_{\text{fb}}(b)$	[24] / [40]	$0.0992 \pm 0.0016$
$A_{\text{fb}}(c)$	[24] / [40]	$0.0707 \pm 0.0035$
$A_b$	[24] / [40]	$0.923 \pm 0.020$
$A_c$	[24] / [40]	$0.670 \pm 0.027$
$A_\ell(\text{SLD})$	[24] / [40]	$0.1513 \pm 0.0021$
$\sin^2 \theta_w^{\ell}(Q_{\text{fb}})$	[24] / [40]	$0.2324 \pm 0.0012$
$M_W$ [GeV]	[24] / [40]	$80.399 \pm 0.023 \pm 0.010_{\text{SUSY}}$
$\text{BR}_{b \rightarrow s\gamma}^{\text{EXP}} / \text{BR}_{b \rightarrow s\gamma}^{\text{SM}}$	[41] / [42]	$1.117 \pm 0.076_{\text{EXP}} \pm 0.082_{\text{SM}} \pm 0.050_{\text{SUSY}}$
$\text{BR}(B_s \rightarrow \mu^+ \mu^-)$	[27] / [37]	$( < 1.08 \pm 0.02_{\text{SUSY}} ) \times 10^{-8}$
$\text{BR}_{B \rightarrow \tau\nu}^{\text{EXP}} / \text{BR}_{B \rightarrow \tau\nu}^{\text{SM}}$	[27] / [42]	$1.43 \pm 0.43_{\text{EXP+TH}}$
$\text{BR}(B_d \rightarrow \mu^+ \mu^-)$	[27] / [42]	$< ( 4.6 \pm 0.01_{\text{SUSY}} ) \times 10^{-9}$
$\text{BR}_{B \rightarrow X_s \ell\ell}^{\text{EXP}} / \text{BR}_{B \rightarrow X_s \ell\ell}^{\text{SM}}$	[43] / [42]	$0.99 \pm 0.32$
$\text{BR}_{K \rightarrow \mu\nu}^{\text{EXP}} / \text{BR}_{K \rightarrow \mu\nu}^{\text{SM}}$	[27] / [44]	$1.008 \pm 0.014_{\text{EXP+TH}}$
$\text{BR}_{K \rightarrow \pi\nu\bar{\nu}}^{\text{EXP}} / \text{BR}_{K \rightarrow \pi\nu\bar{\nu}}^{\text{SM}}$	[45] / [46]	$< 4.5$
$\Delta M_{B_s}^{\text{EXP}} / \Delta M_{B_s}^{\text{SM}}$	[45] / [47, 48]	$0.97 \pm 0.01_{\text{EXP}} \pm 0.27_{\text{SM}}$
$(\Delta M_{B_s}^{\text{EXP}} / \Delta M_{B_s}^{\text{SM}}) / (\Delta M_{B_d}^{\text{EXP}} / \Delta M_{B_d}^{\text{SM}})$	[27] / [42, 47, 48]	$1.00 \pm 0.01_{\text{EXP}} \pm 0.13_{\text{SM}}$
$\Delta\epsilon_K^{\text{EXP}} / \Delta\epsilon_K^{\text{SM}}$	[45] / [47, 48]	$1.08 \pm 0.14_{\text{EXP+TH}}$
$a_\mu^{\text{EXP}} - a_\mu^{\text{SM}}$	[49] / [38, 50]	$( 30.2 \pm 8.8 \pm 2.0_{\text{SUSY}} ) \times 10^{-10}$
$M_h$ [GeV]	[26] / [51, 52]	$> 114.4 \pm 1.5_{\text{SUSY}}$
$\Omega_{\text{CDM}} h^2$	[29] / [53]	$0.1109 \pm 0.0056 \pm 0.012_{\text{SUSY}}$
$\sigma_p^{\text{SI}}$	[23]	$(m_{\tilde{\chi}^0}, \sigma_p^{\text{SI}})$ plane
jets + $\cancel{E}_T$	[16, 18]	$(m_0, m_{1/2})$ plane
$H/A, H^\pm$	[19]	$(M_A, \tan \beta)$ plane

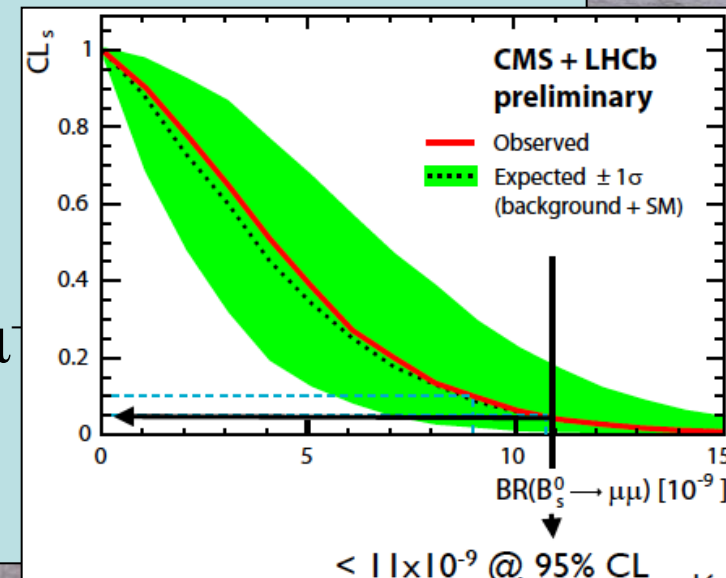
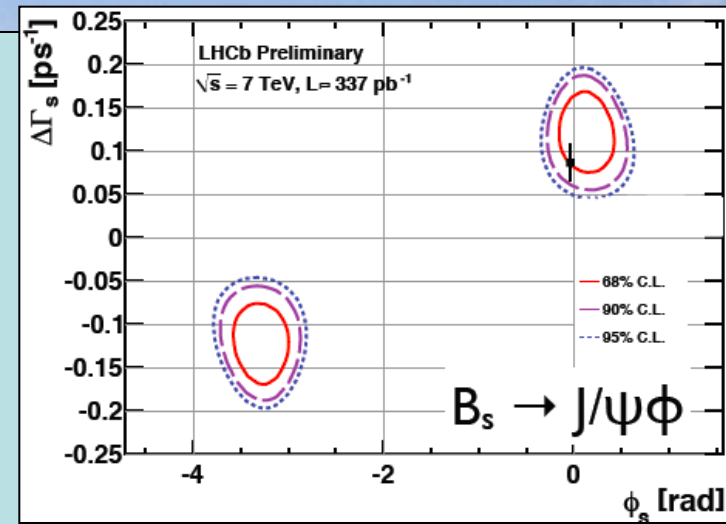
# Electroweak Precision Observables

- Inclusion essential for fair comparison with Standard Model
- Some observables may be significantly different
  - E.g.,  $m_W$ ,  $A_{fb}(b)$
  - Advantage for SUSY?
- Some may not be changed significantly
  - Should be counted against/for all models



# Flavour Physics Observables

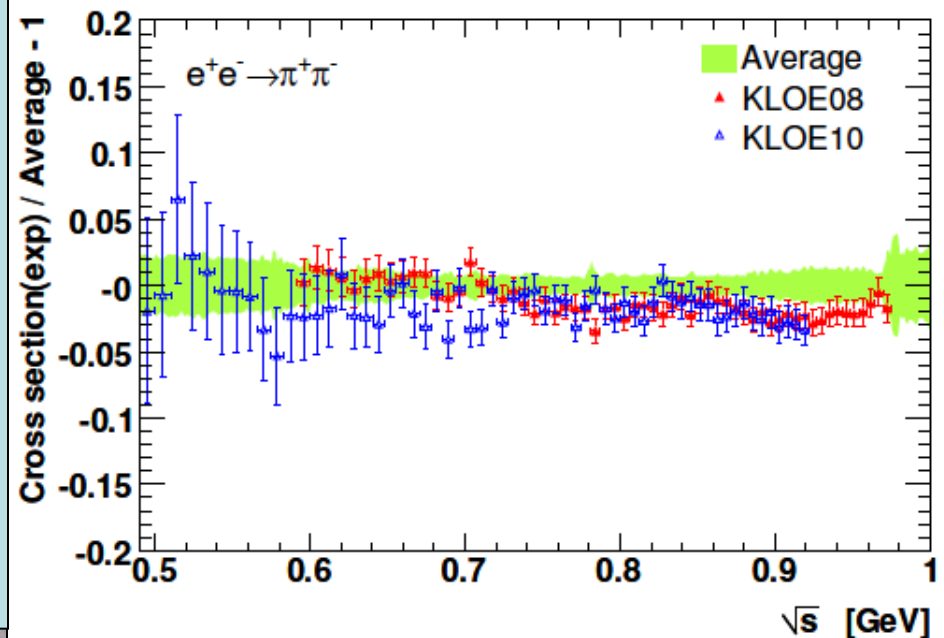
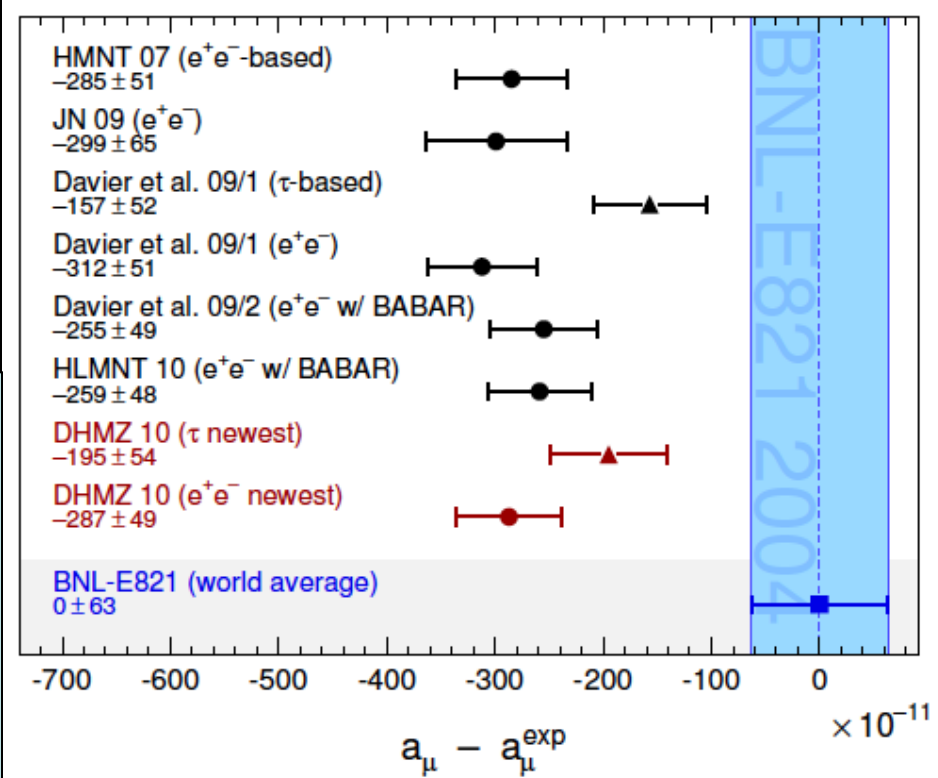
- Inclusion requires additional hypotheses
  - E.g., minimal flavour violation
- Many anomalies reported
  - E.g., top production asymmetry, dimuon asymmetry,  $B_s \rightarrow J/\psi \phi$
- Difficult to interpret within SUSY
- Significant progress with  $B_s \rightarrow \mu\mu$
- Valuable constraint on SUSY models



# Quo Vadis

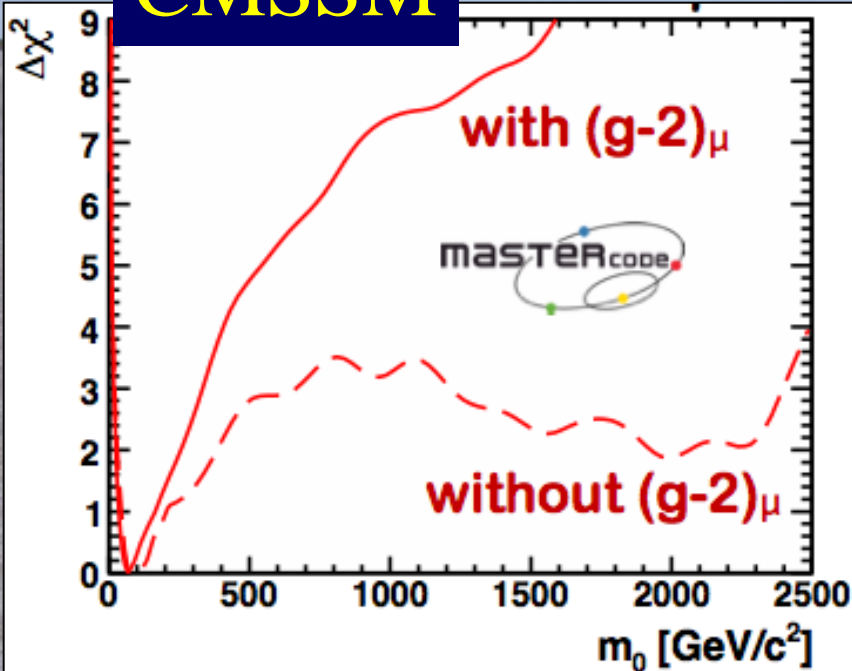
$$g_\mu - 2?$$

- Strong discrepancy between BNL experiment and  $e^+e^-$  data:
  - now  $\sim 3.6 \sigma$
- Better agreement between  $e^+e^-$  experiments
- Increased discrepancy between BNL experiment and  $\tau$  decay data
  - now  $\sim 2.4 \sigma$
- Convergence between  $e^+e^-$  experiments and  $\tau$  decay data
- **More credibility?**

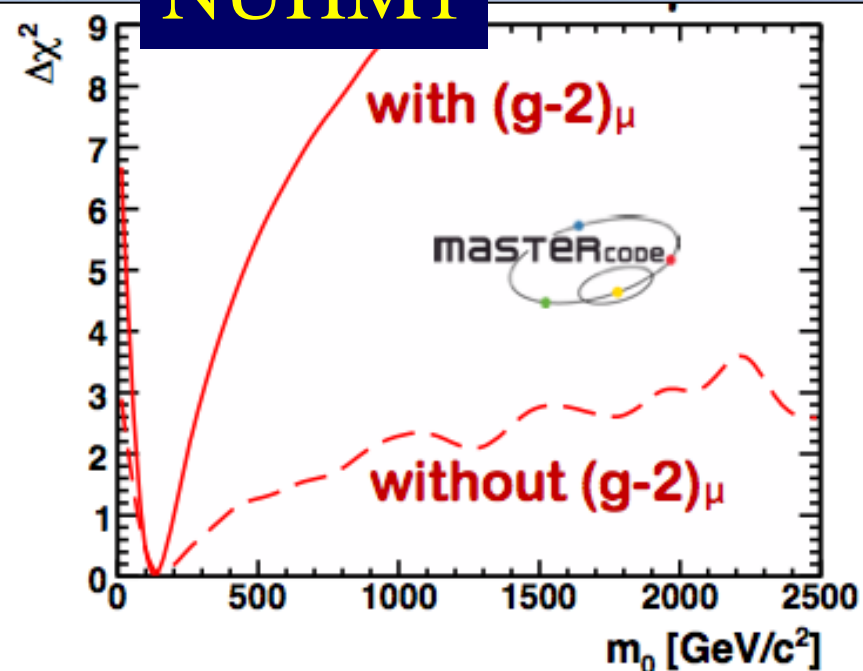


To  $g_\mu - 2$  or not to  $g_\mu - 2$  ?

CMSSM



NUHM1

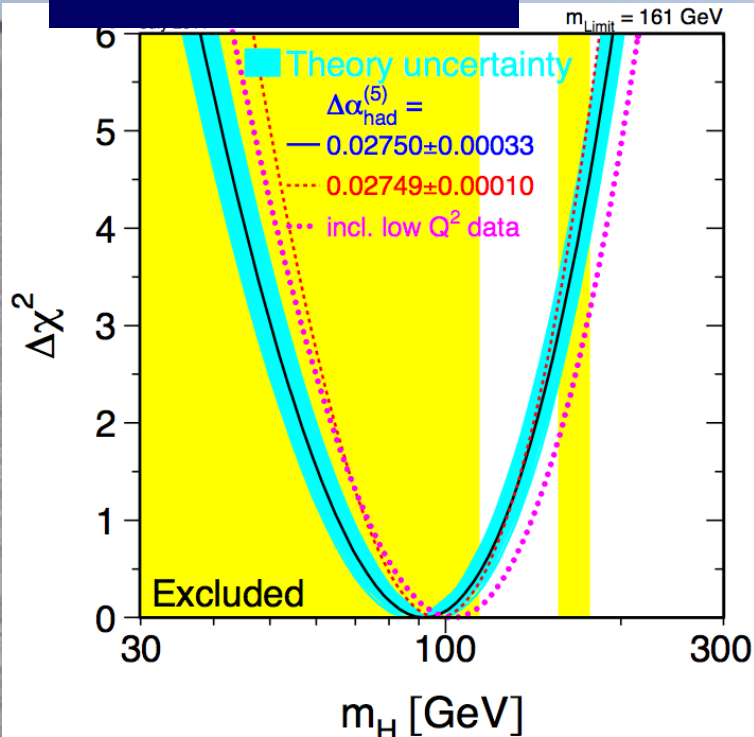


Pre-LHC fits:

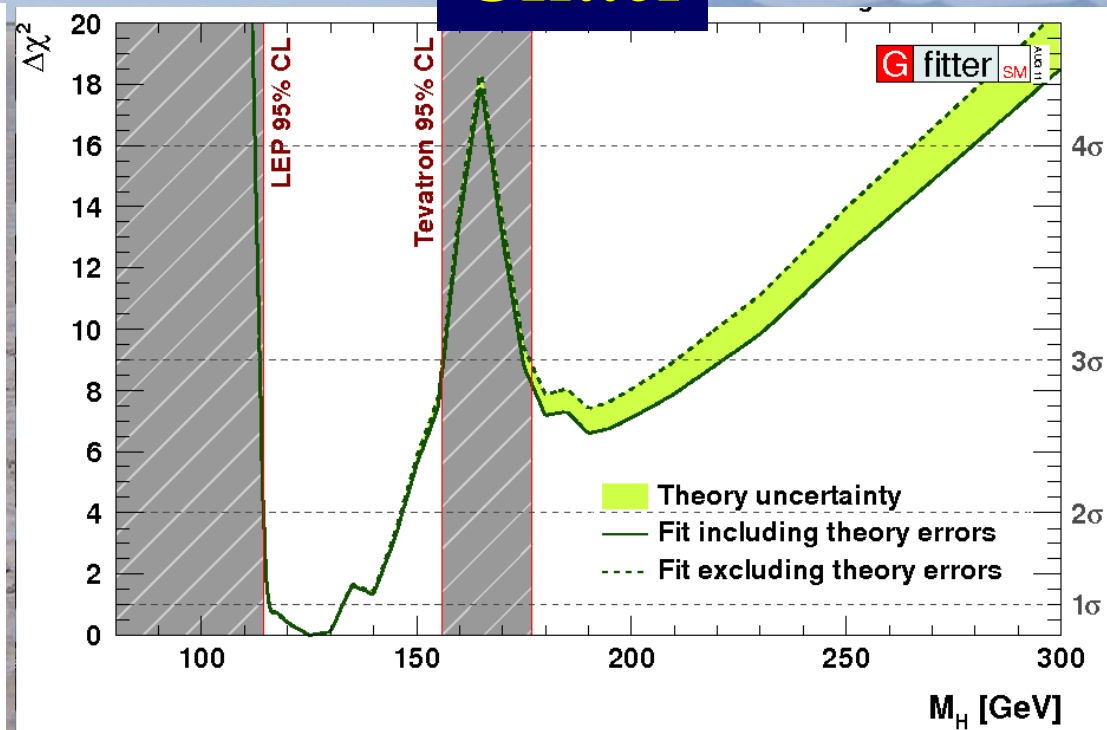
Mild preference for small masses even without  $g_\mu - 2$  ?

# $m_H$ : Blue Band vs Green Band

## LEPEWWG



## Gfitter



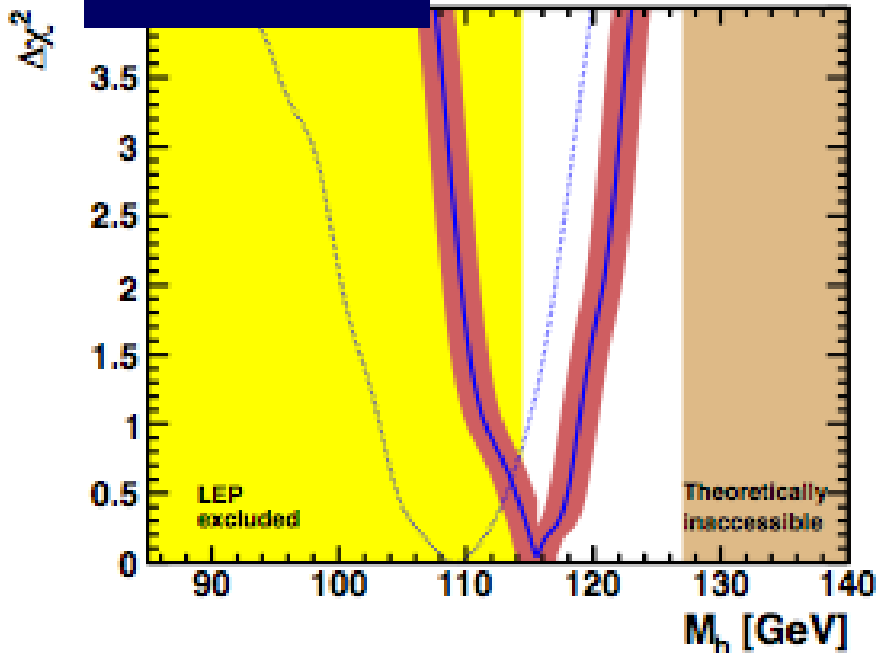
Precision data vs  
LEP, Tevatron

Combination  
with LHC

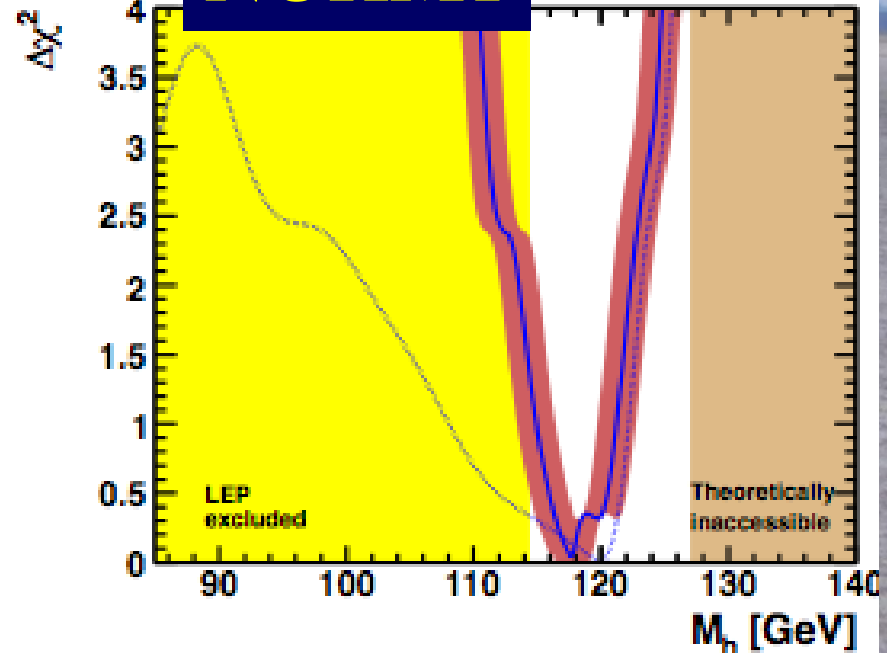


# $m_H$ : Blue Band vs Red Band

CMSSM



NUHM1



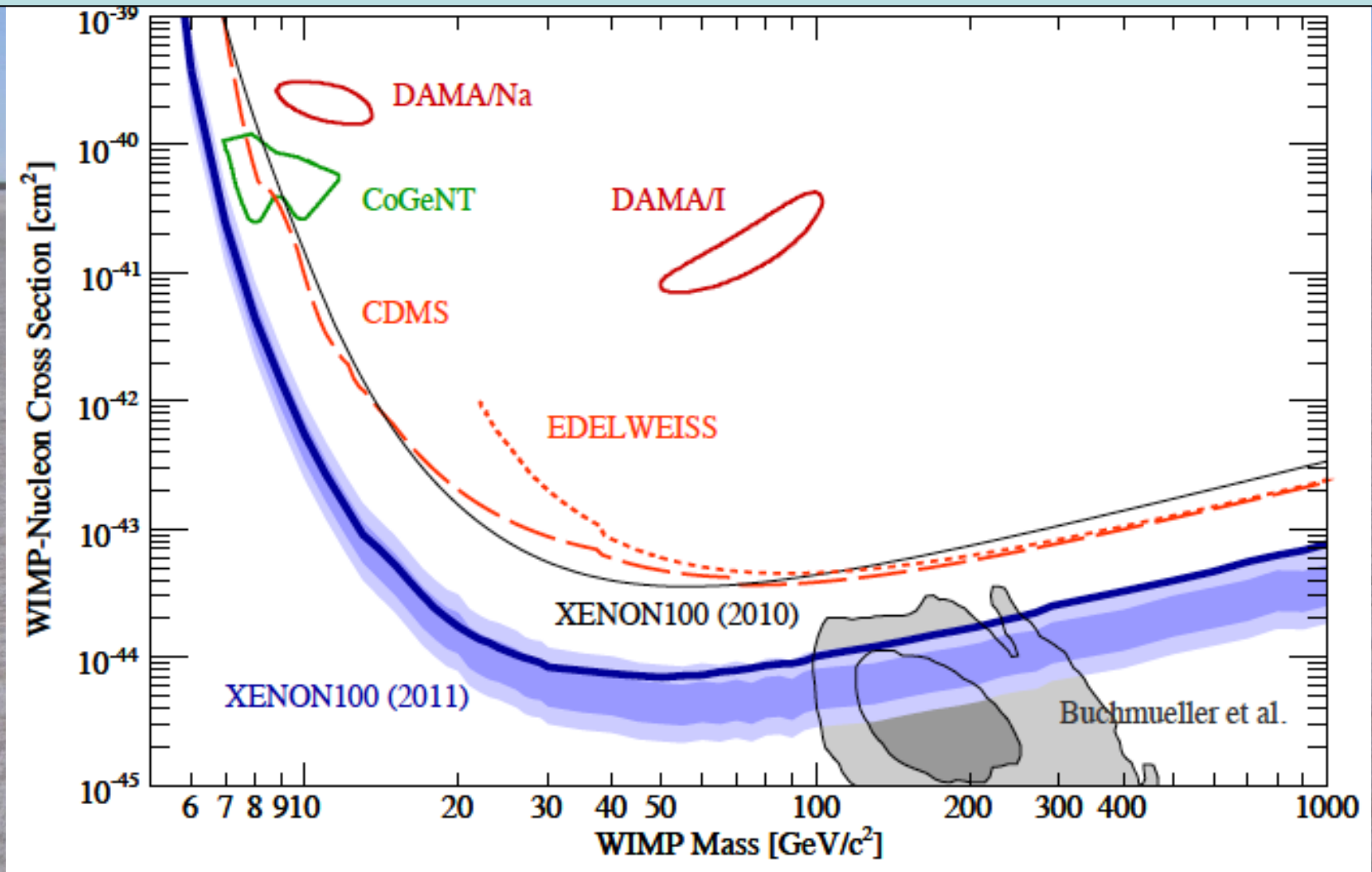
Dotted: pre-LHC fits ( $\Delta\chi^2 \sim 1$ )

Solid: post-2010-LHC fits (red band = TH error)

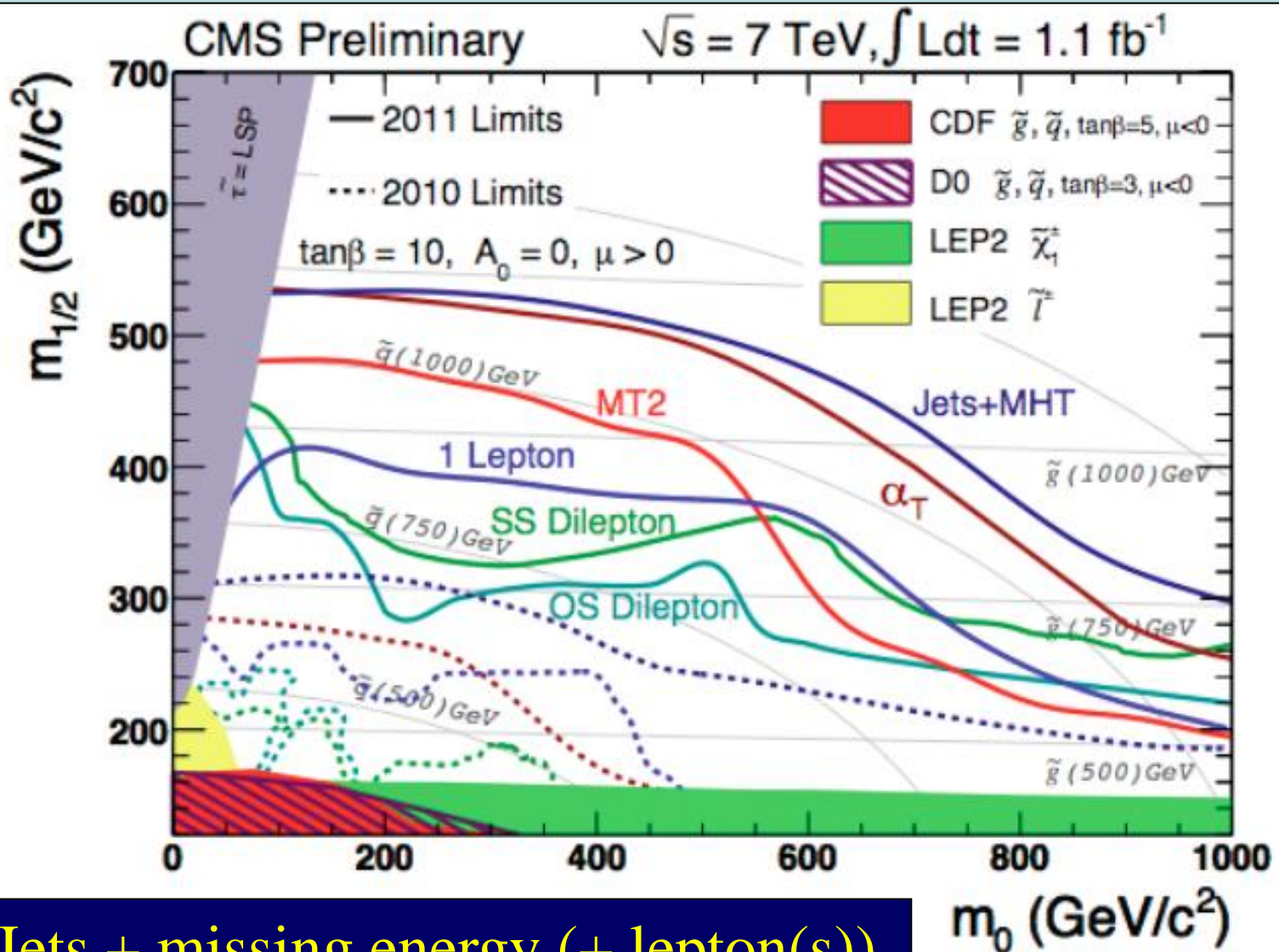
# Dark Matter Observables

- Cosmological cold dark matter density
  - $\Omega_{\text{CDM}} h^2 = 0.1109 \pm 0.0056$
- Reduces dimensionality of SUSY space by  $\sim 1$ 
  - Could be other sources of DM: little effect
- Upper limit on spin-independent scattering
- Other astrophysical constraints?
  - Annihilations inside Sun/Earth  $\rightarrow$  neutrinos?
  - Anomalies in cosmic-ray  $\gamma/e^+/e^-$  spectra?
- Not explicable in models discussed here

# XENON100 Experiment

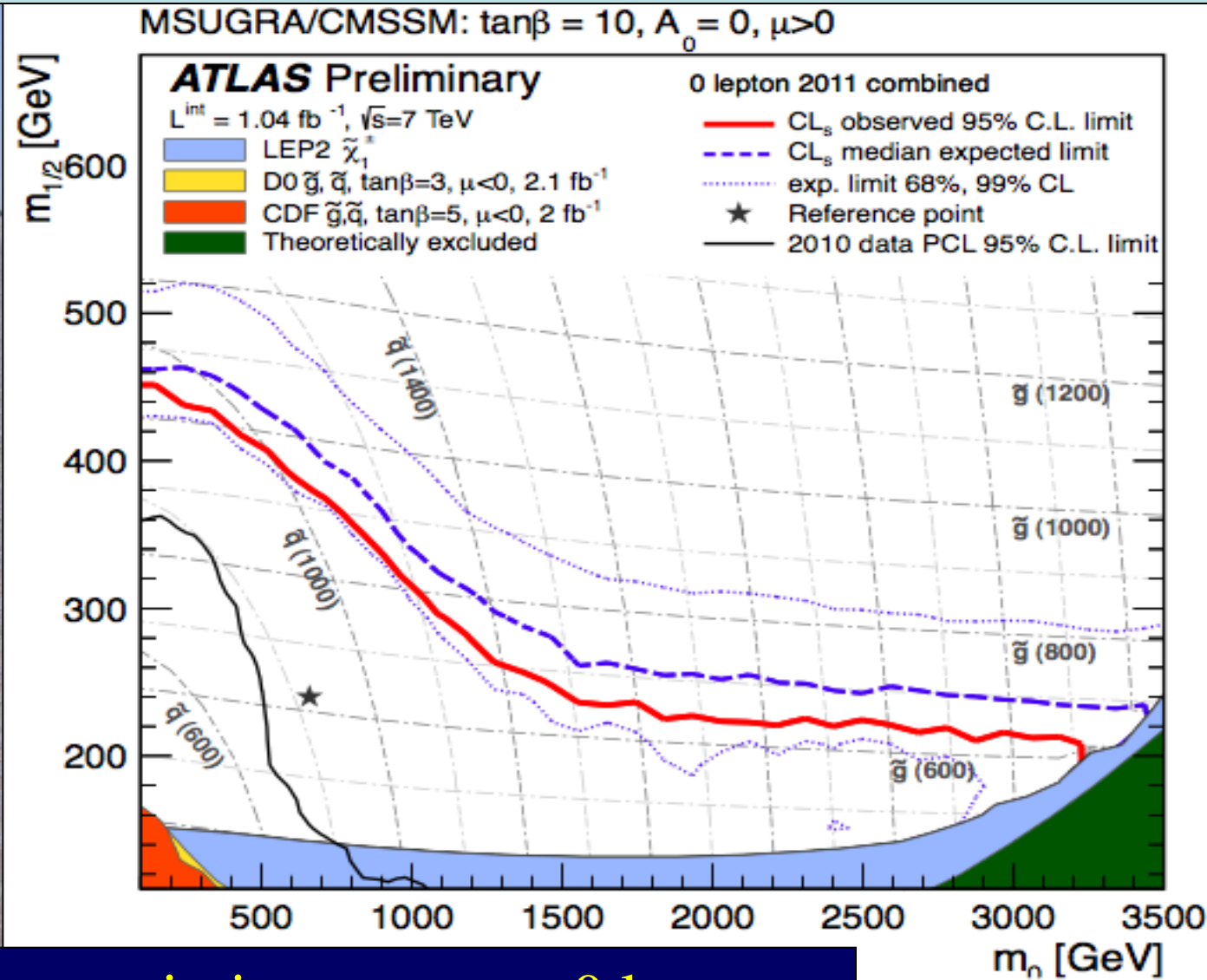


# Supersymmetry Searches in CMS



Jets + missing energy (+ lepton(s))

# Supersymmetry Searches in ATLAS



Jets + missing energy + 0 lepton

# Impact of LHC on the CMSSM

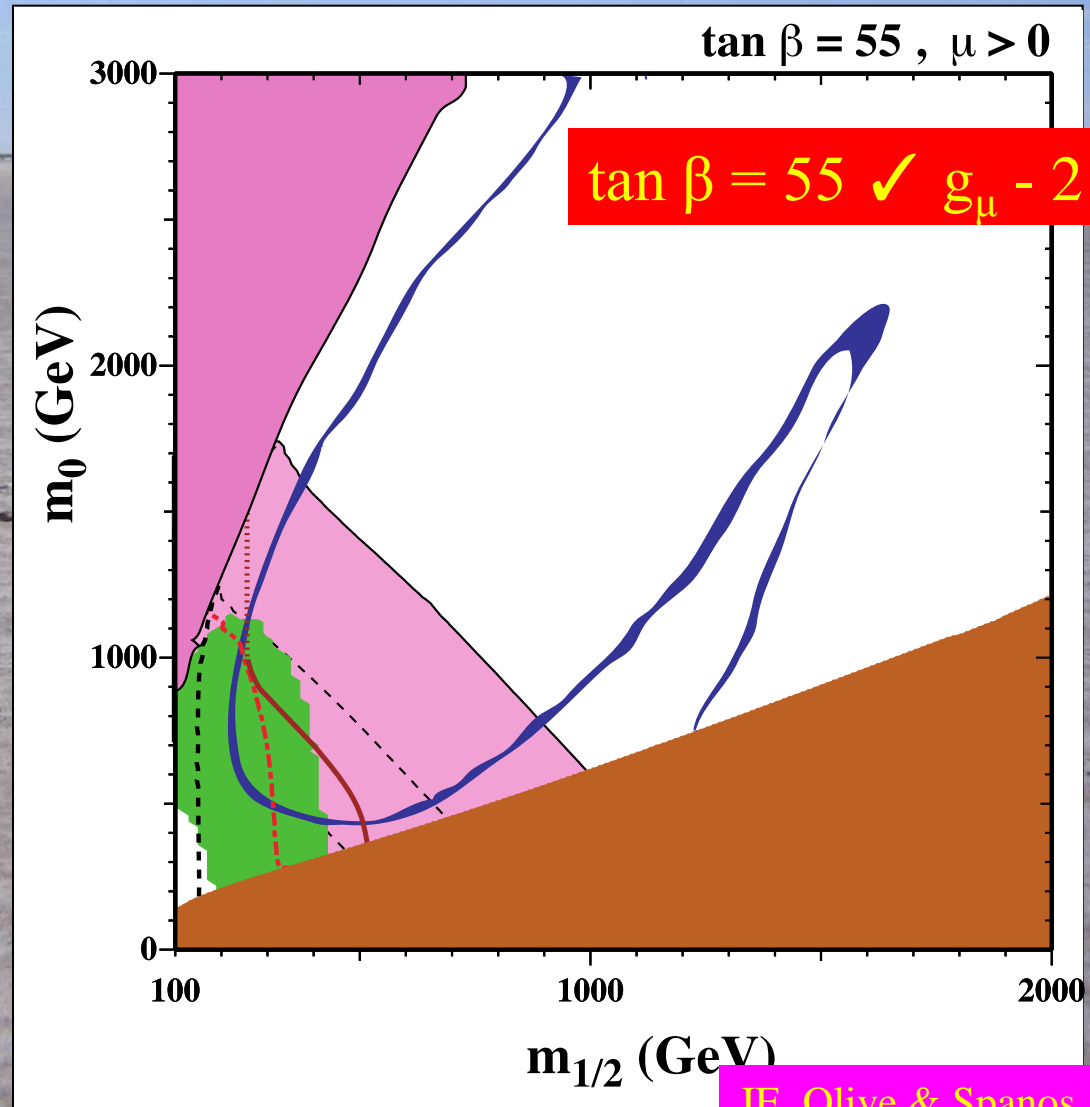
Assuming the lightest sparticle is a neutralino

Excluded because stau LSP

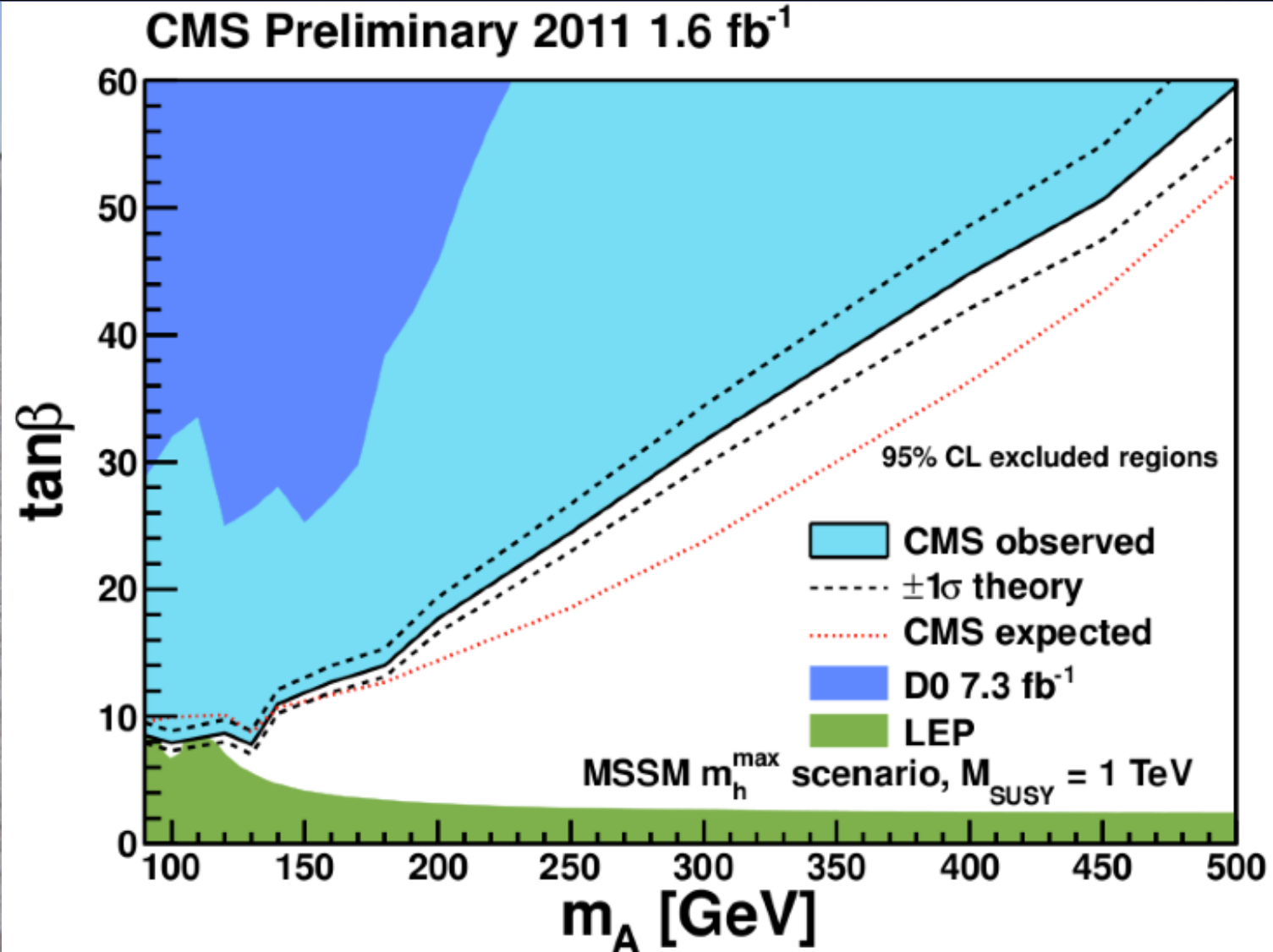
Excluded by  $b \rightarrow s$  gamma

WMAP constraint on CDM density

Preferred (?) by latest  $g - 2$



# Limits on Heavy MSSM Higgses



# Meta-Analyses: Cuts vs Likelihood

- Theorists seek to combine many constraints
- **Simply imposing 95% CL contours as cuts is inadequate**
  - Seek to construct global likelihood function
- **Want more information from experiments: several likelihood contours**
  - Can be used to check our simulations
- Otherwise, we will resort to unreliable estimates/guesses ☹



# Supersymmetric Models to Study

- Gravity-mediated:

- NUHM2

- as below,  $m_0 \neq m_{1/2}$

- NUHM1

- as below,  $c$

- CMSSM

- $m_0, m_{1/2}, \tan\beta$

- VCMSSM

- as above, &  $A_0$

- mSUGRA

- as above, &  $m_g$

- RPV CMSSM

Also studied  
in global fits

Most studied  
in global fits

Some  
Global  
fits

- Other SUSY  $\times$  models:

- Gauge-mediated

- Anomaly-mediated

- Mixed modulus-anomaly-mediated

- Phenomenological 19-

Less studied in global fits

- NMSSM

If model has  $N$  parameters,  
sample 100 values/parameter:  
 $10^{2N}$  points, e.g.,  $10^8$  in CMSSM

# MSSM: $> 100$ parameters

Minimal Flavour Violation: 13 parameters  
(+ 6 violating CP)

SU(5) unification: 7 parameters

NUHM2: 6 parameters

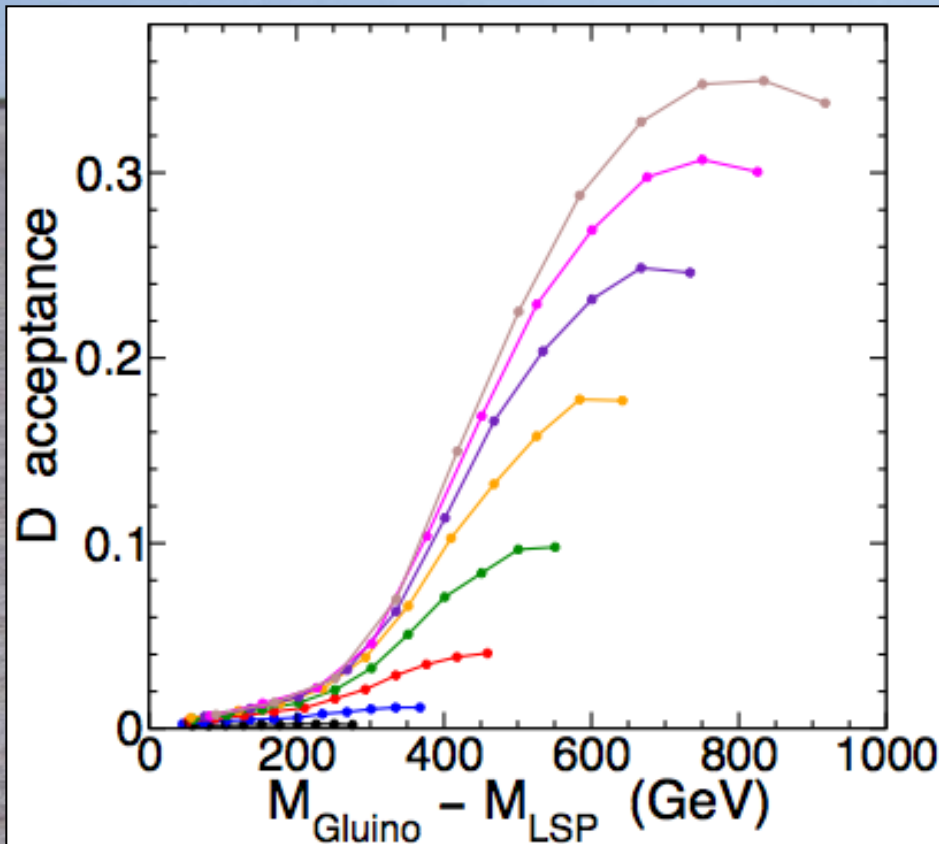
NUHM1 = SO(10): 5 parameters

CMSSM: 4 parameters

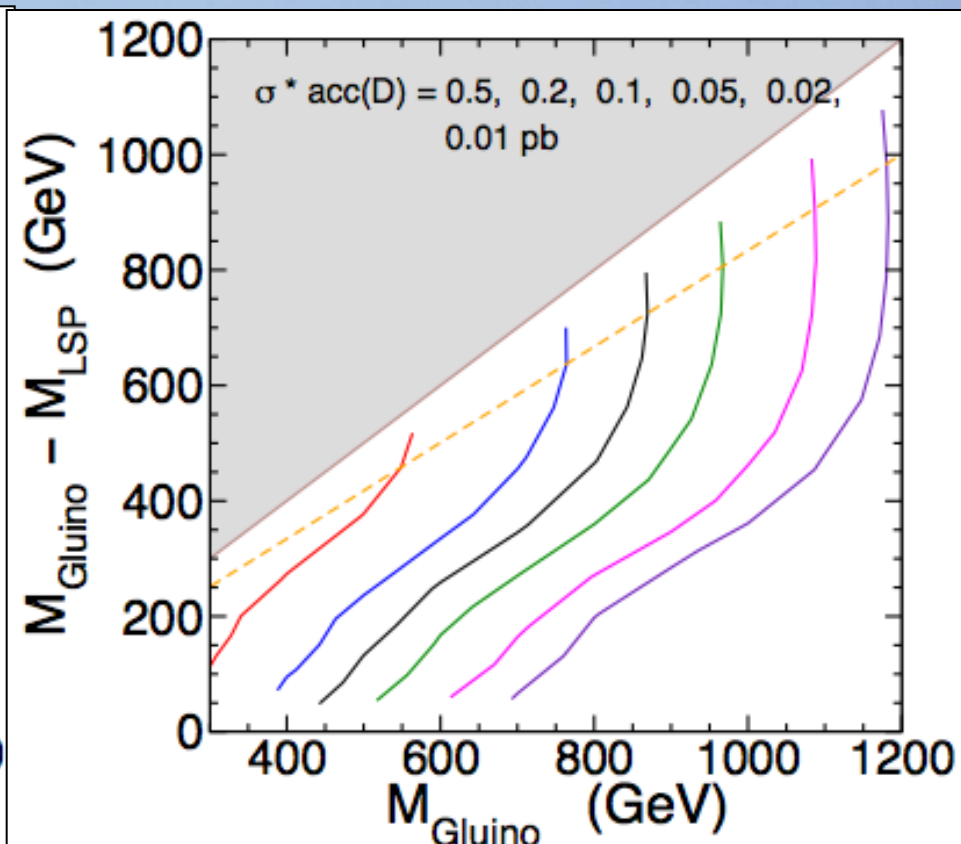
mSUGRA: 3 parameters

String?

# Current LHC Searches have Reduced Sensitivity to Compressed Spectra



Acceptance of typical ATLAS MET search



Exclusion by typical ATLAS MET search

# Bayesian vs Frequentist

- **Bayesian:** *“probability is a measure of the degree of belief about a proposition”*

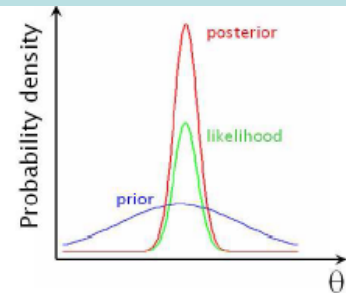
Bayes' theorem: posterior pdf

$$p(\theta, \psi | d) = \frac{p(d|\xi)\pi(\theta, \psi)}{p(d)}$$

$p(d|\xi) = \mathcal{L}$ : likelihood

$\pi(\theta, \psi)$ : prior pdf

$p(d)$ : evidence (normalization factor)



$$\text{posterior} = \frac{\text{likelihood} \times \text{prior}}{\text{normalization factor}}$$

- **Frequentist:** *“probability is the number of times the event occurs over the total number of trials, in the limit of an infinite series of equiprobable repetitions”*
- **Louis Lyons:** *“Bayesians address the question everyone is interested in by using assumptions no-one believes, while frequentists use impeccable logic to deal with an issue of no interest to anyone”*

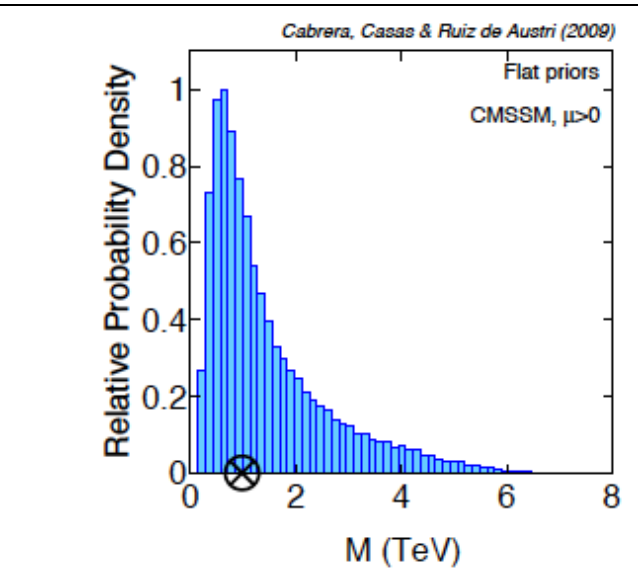
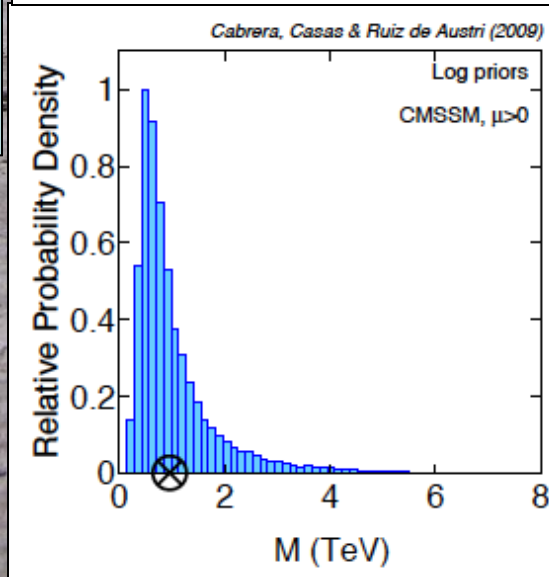
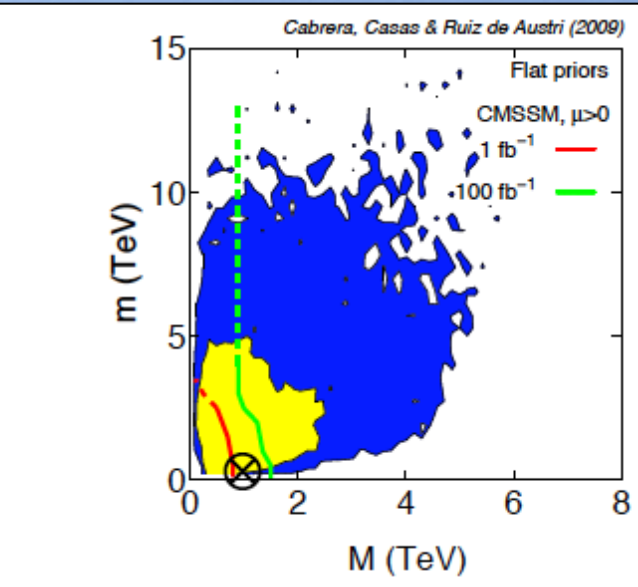
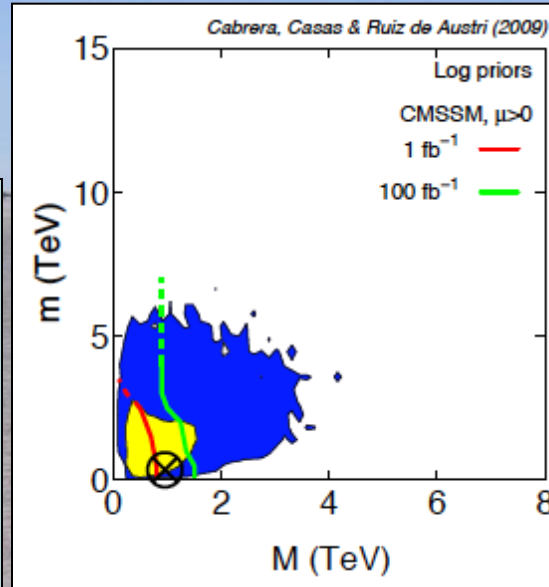
# Sensitivities to Bayesian Priors

Pre-LHC:

Logarithmic vs flat

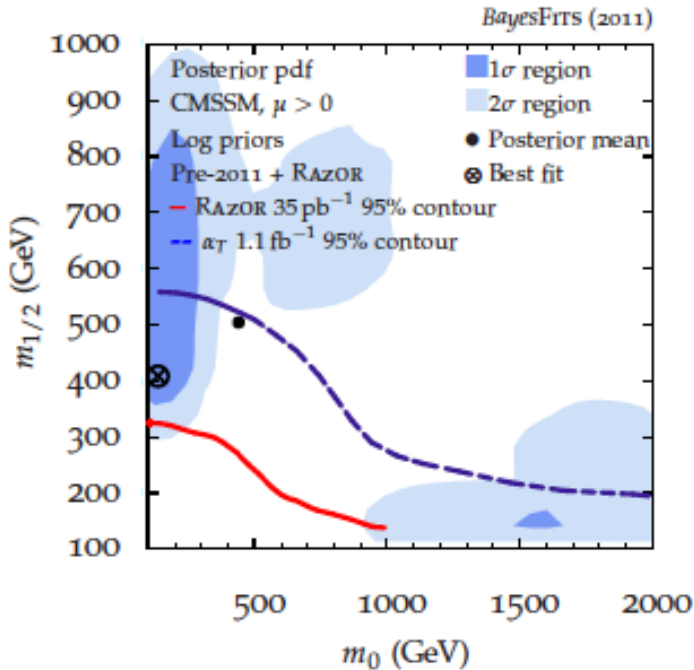
-  $(m_{1/2}, m_0)$  plane

- Probability density for  $m_{1/2}$

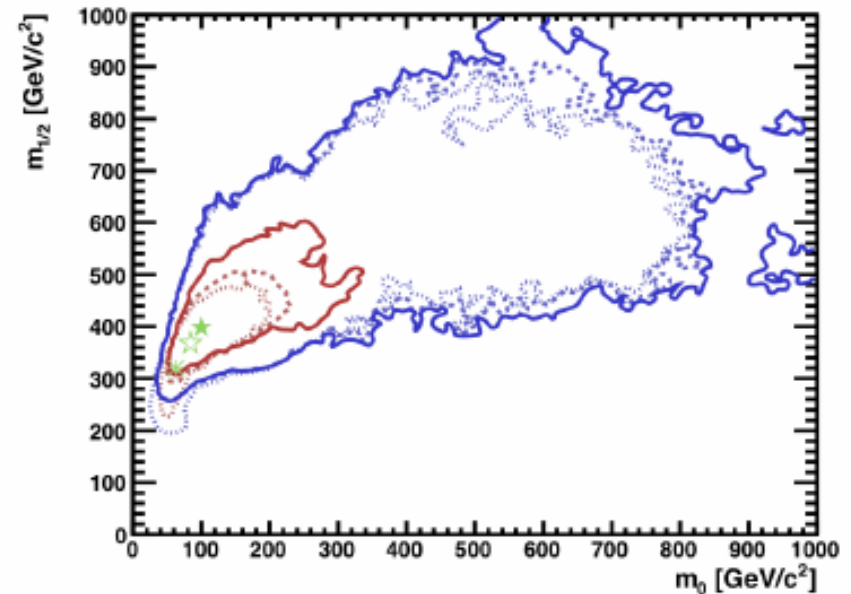


# To Focus-Point or not to Focus-Point?

## Bayesian pdf

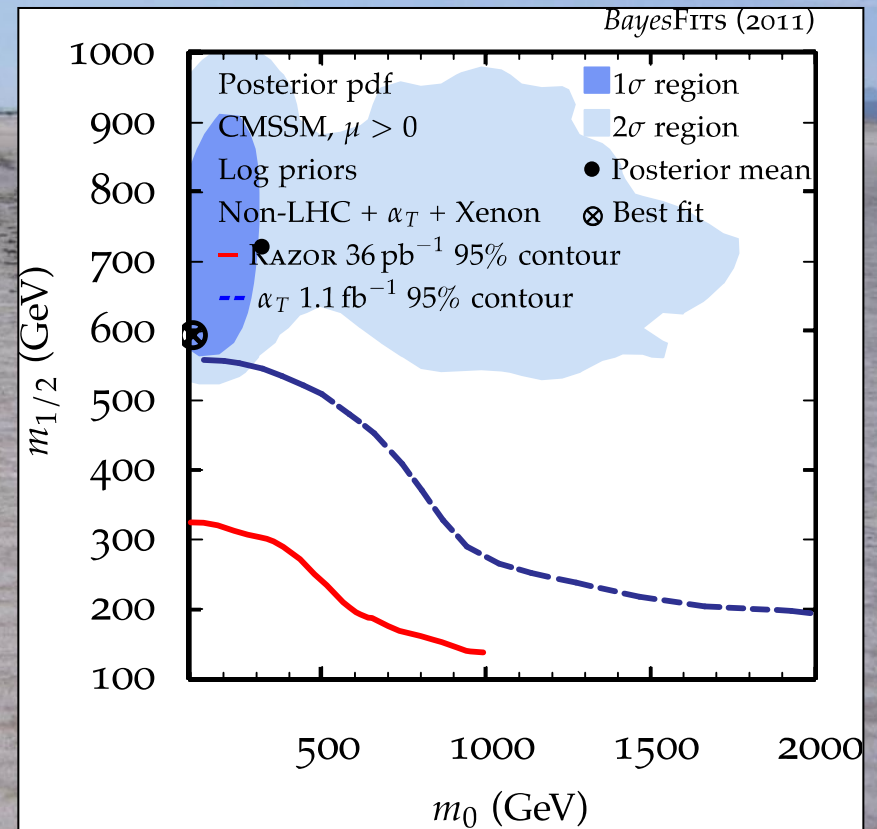
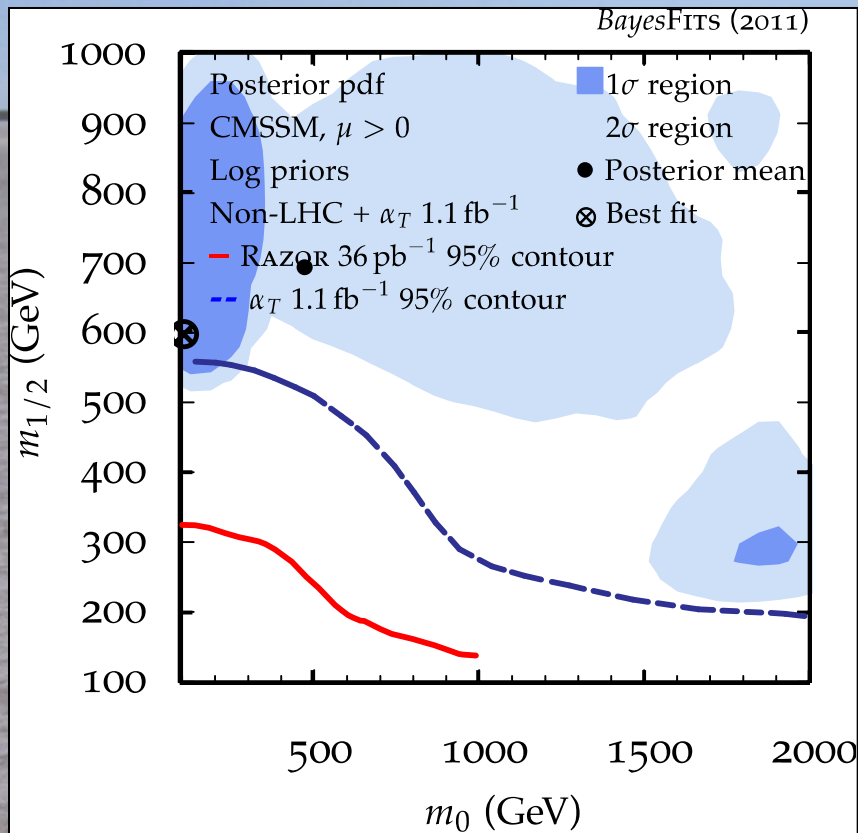


## MasterCode



- reasonable agreement in the  $m_{1/2} \gtrsim m_0$  region
- disagreement about large  $m_0$  region

# To Focus-Point or not to Focus-Point?

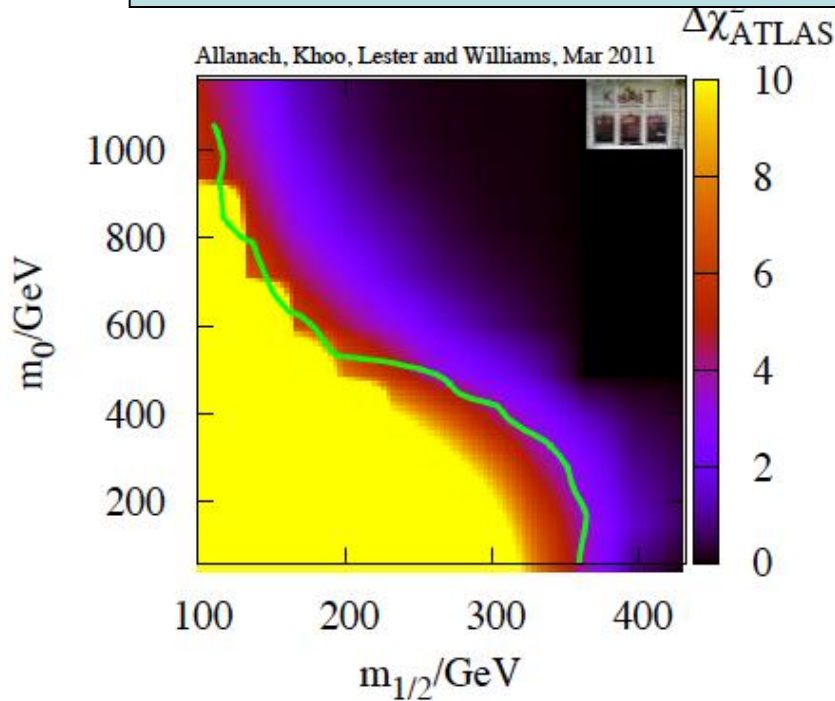


1/fb LHC data, no XENON100  
Focus-point remains

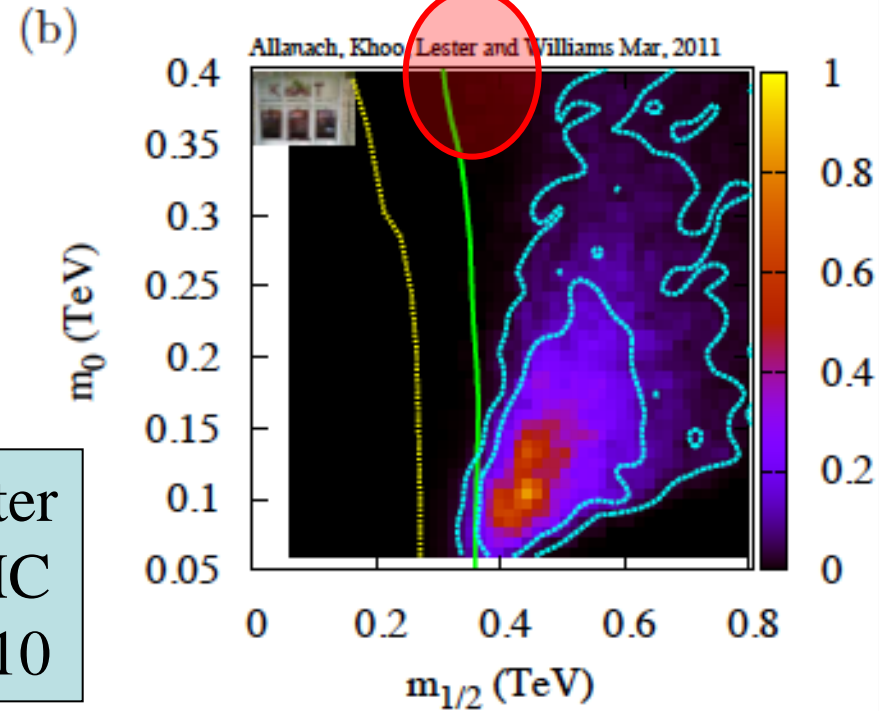
1/fb LHC data, with XENON100  
Focus-point disappears

# To Focus-Point or not to Focus-Point?

Another Bayesian analysis ...



Detailed modelling of experimental likelihood

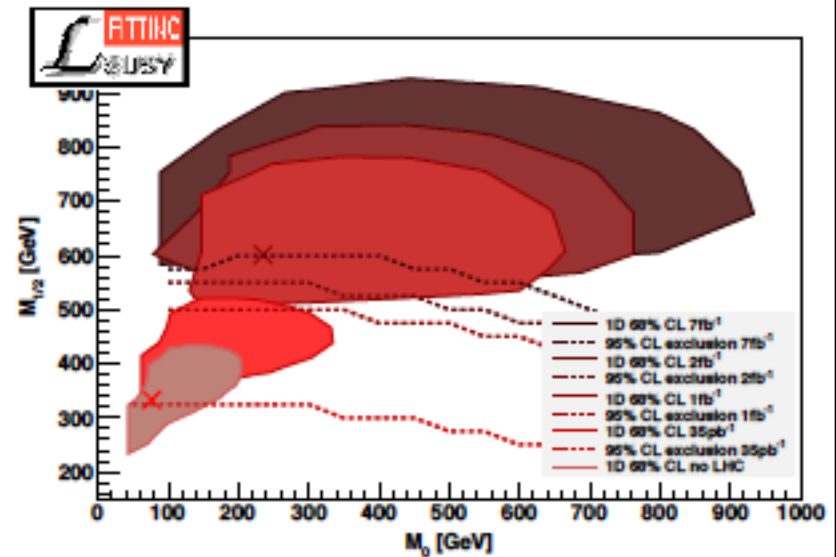
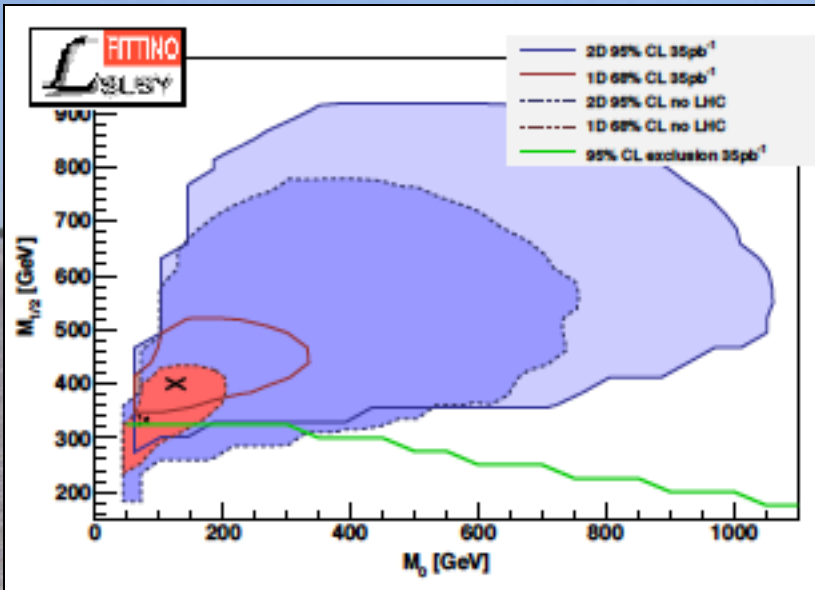


After LHC 2010

... no sign of the fixed-point region

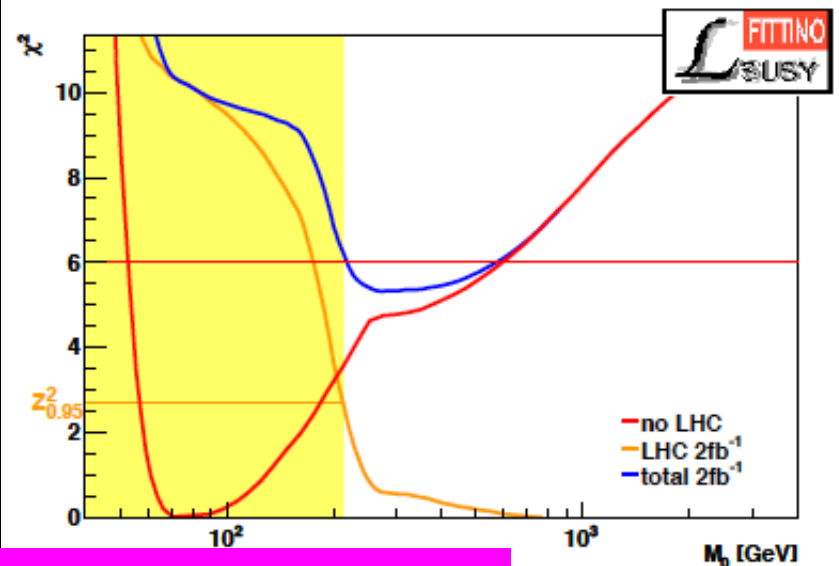


# Pre-LHC vs Post-LHC



Uses MasterCode package

- LHC will push out in the  $(m_{1/2}, m_0)$  plane if no SUSY
- Illustration of possible pre/post-LHC tension  $m_{1/2}$

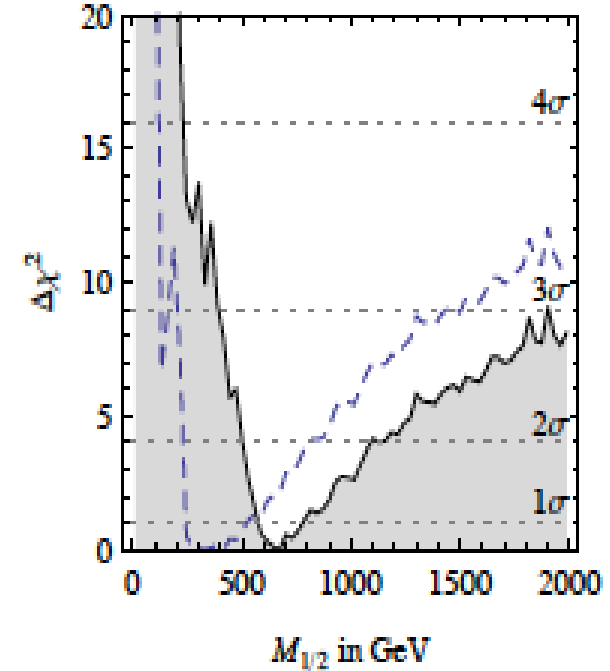
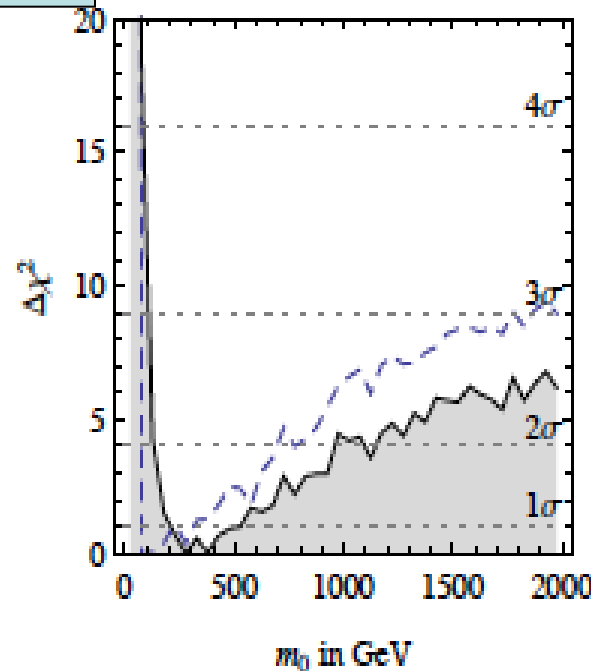
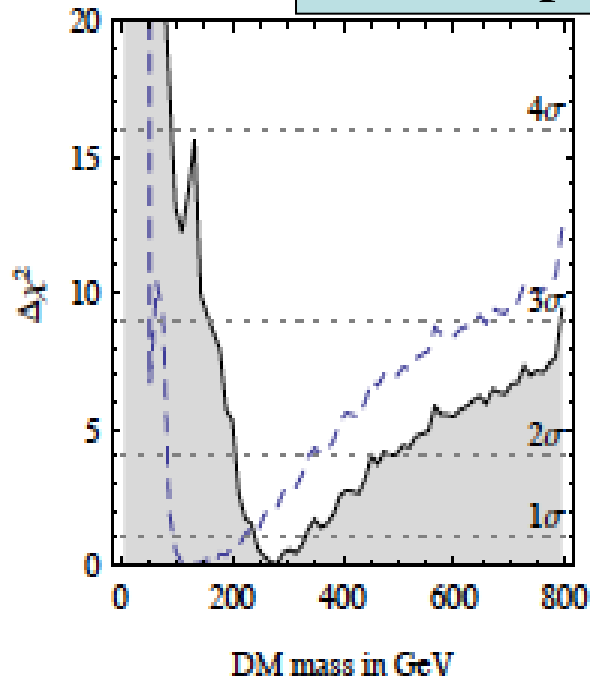


# Including XENON100

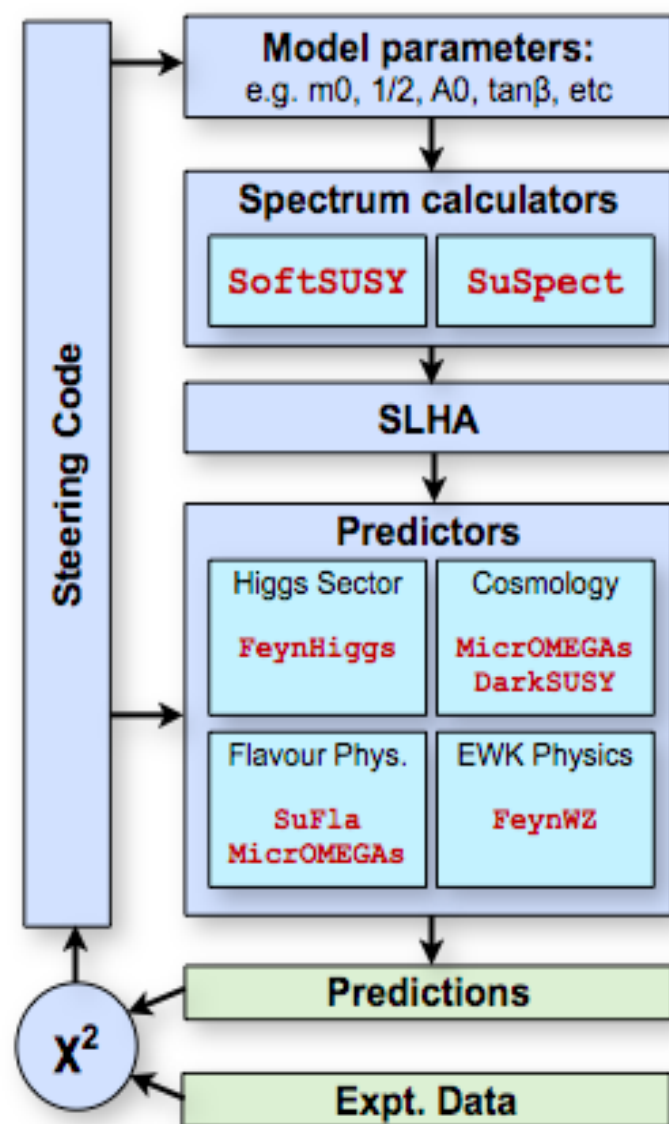
quantity	experiment	Standard Model
$\alpha_3(M_Z)$ [45]	$0.1184 \pm 0.0007$	parameter
$m_t$ [46]	$173.1 \pm 0.9$	parameter
$m_b$ [47]	$4.19 \pm 0.12$	parameter
$\Omega_{\text{DM}} h^2$ [48]	$0.112 \pm 0.0056$	0
$\delta g_\mu$ [49]	$(2.8 \pm 0.8) 10^{-9}$	0
$\text{BR}(B_d \rightarrow X_s \gamma)$ [50]	$(3.50 \pm 0.17) 10^{-4}$	$(3.15 \pm 0.23) 10^{-4}$
$\text{BR}(B_s \rightarrow \mu^+ \mu^-)$ [19]	$(0.9 \pm 0.6) 10^{-8}$	$(0.33 \pm 0.03) 10^{-8}$
$\text{BR}(B_u \rightarrow \tau \bar{\nu})/\text{SM}$ [51]	$1.25 \pm 0.40$	1

200,000 points

*The data we fit, together with LHC and XENON100 bounds.*



- **Combines diverse set of tools**
  - different codes : all state-of-the-art
    - Electroweak Precision (**FeynWZ**)
    - Flavour (**SuFla**, **micrOMEGAs**)
    - Cold Dark Matter (**DarkSUSY**, **micrOMEGAs**)
    - Other low energy (**FeynHiggs**)
    - Higgs (**FeynHiggs**)
  - different precisions (one-loop, two-loop, etc)
  - different languages (Fortran, C++, English, German, Italian, etc)
  - different people (theorists, experimentalists)
- **Compatibility is crucial! Ensured by**
  - close collaboration of tools authors
  - standard interfaces



# Constructing the $\chi^2$

$$\chi^2 = \sum_i^N \frac{(C_i - P_i)^2}{\sigma(C_i)^2 + \sigma(P_i)^2} + \sum_i^M \frac{(f_{SM_i}^{obs} - f_{SM_i}^{fit})^2}{\sigma(f_{SM_i})^2}$$
$$+ \chi^2(b \rightarrow s\gamma) \quad + \chi^2(g_\mu - 2) \quad + \chi^2(\Omega h^2) \quad + \chi^2(m_h)$$
$$+ \chi^2(\text{BR}(B_s \rightarrow \mu\mu)) + \chi^2(\text{LHC}) \quad + \chi^2(\text{XENON100})$$

**Recent Experimental Data!**

- **Fit Methods (globally over all model parameters!)**

- **Markov Chain Monte Carlo (MCMC)**

- Actually used as a mere sampling method (sampling density not used)
- success and failure of the steps defined by the  $\chi^2$

- $\chi^2$  fit: **Minuit** minimisation

- used for “scans” or in conjunction with MCMCs to get overall best minimum

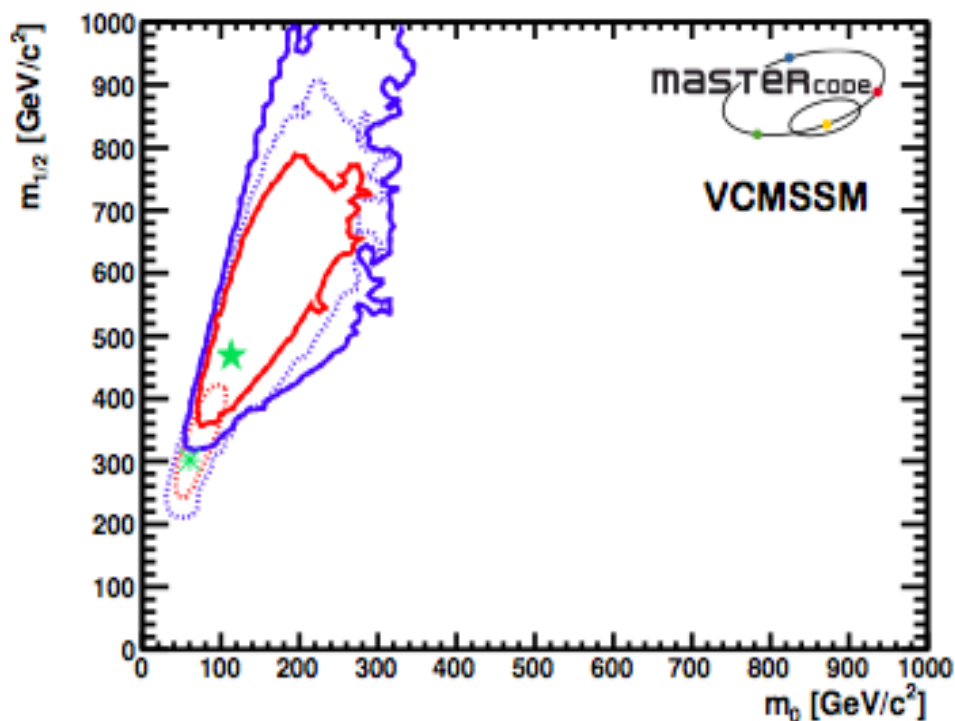
- **Afterburners**

- $\chi^2$  terms additive  $\rightarrow$  effects therefore also additive

- **Study effect of “interesting” ( $g-2$ ,  $b \rightarrow s\gamma$ ,  $\Omega h^2$ , etc) observables!**

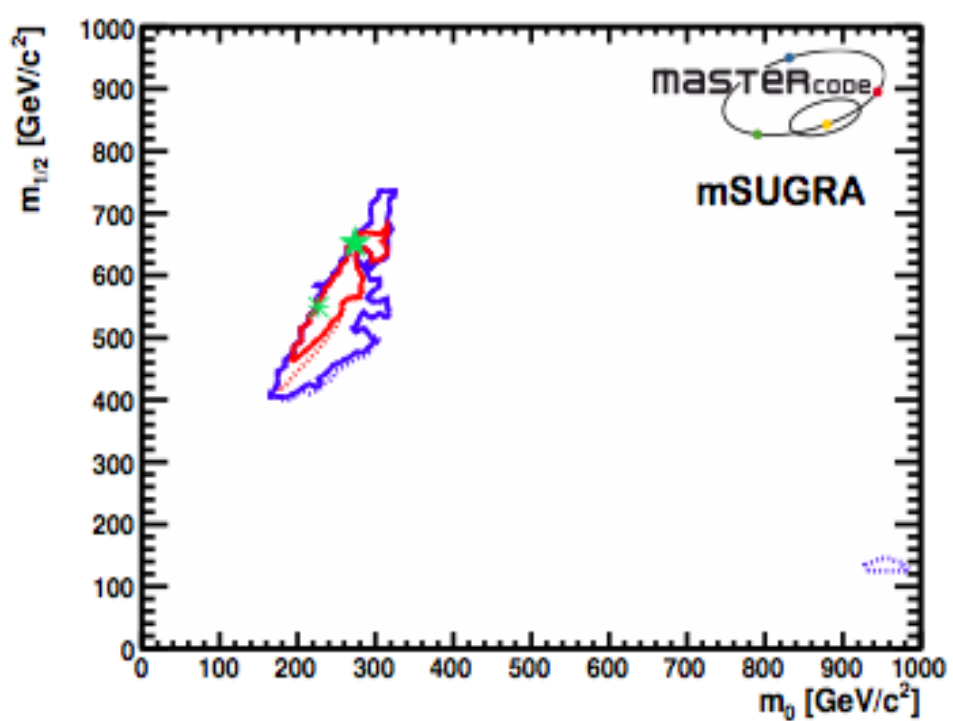
- sample space without “interesting” terms  $\rightarrow$  larger, more general sampling
- a posteriori add “interesting” terms after general sampling
- Only need to sample multi-d space once! Enormous cost savings to due RGEs

2010 ATLAS + CMS with 36 pb<sup>-1</sup> of LHC Data



**VCMSSM**

60 million points sampled



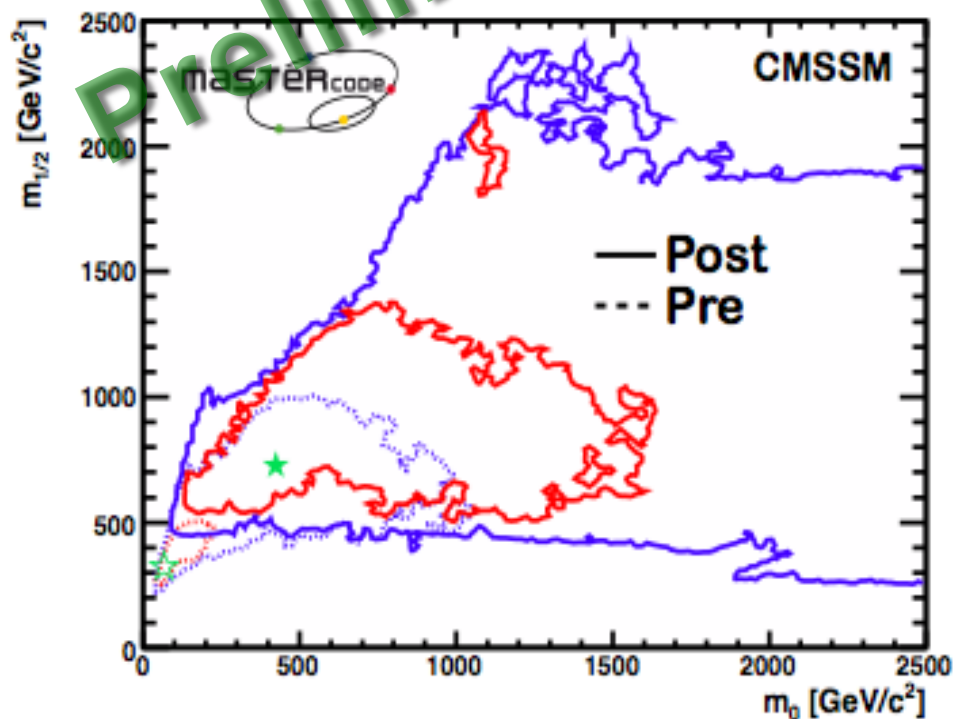
**mSUGRA**

60 million points sampled

	Model	Min $\chi^2$	Prob	$m_{1/2}$	$m_0$	$A_0$	$\tan \beta$
	VCMSSM	22.5	31%	300	60	30	9
	post-LHC/XENON100	27.1	13%	390	90	70	11
	mSUGRA	29.4	6.1%	550	230	430	28
	post-LHC/XENON100	30.9	5.7%	550	230	430	28

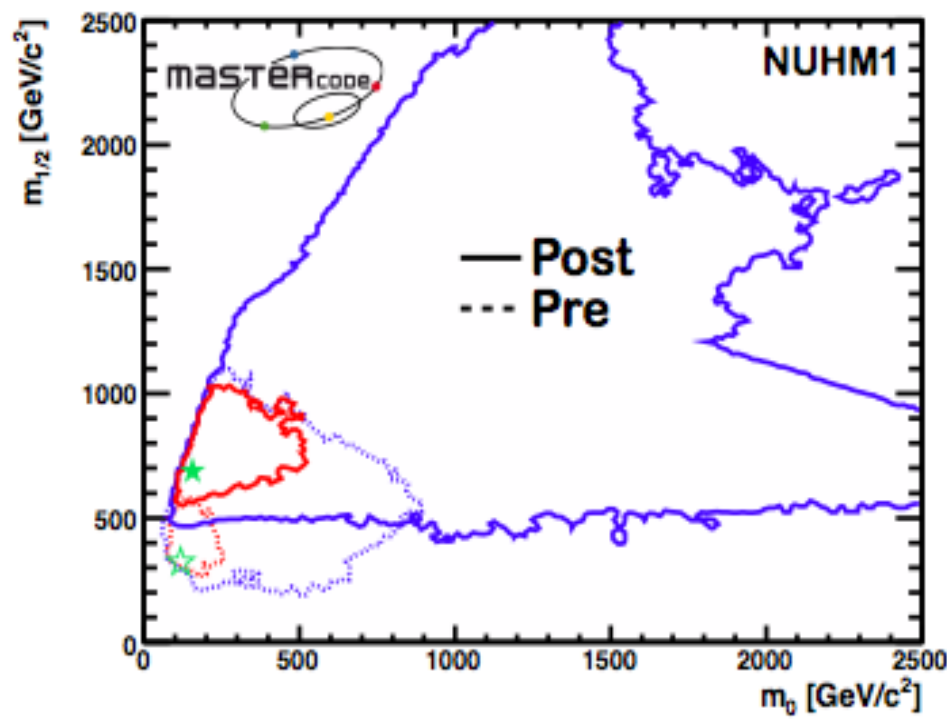
# Post-LHC, Post-XENON100

2014 ATLAS + CMS with  $1 \text{ fb}^{-1}$  of LHC Data



CMSSM

60 million points sampled



NUHM1

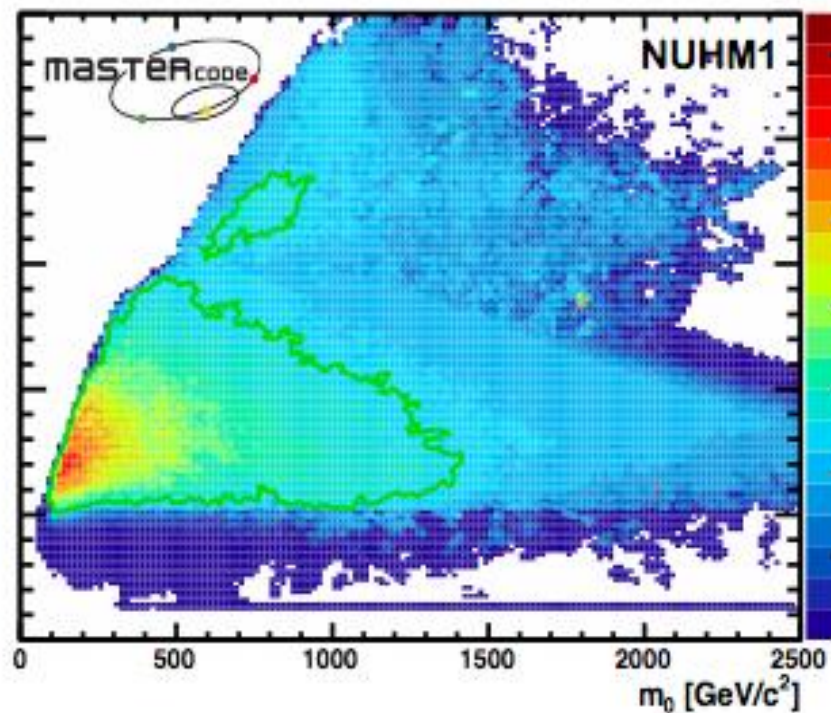
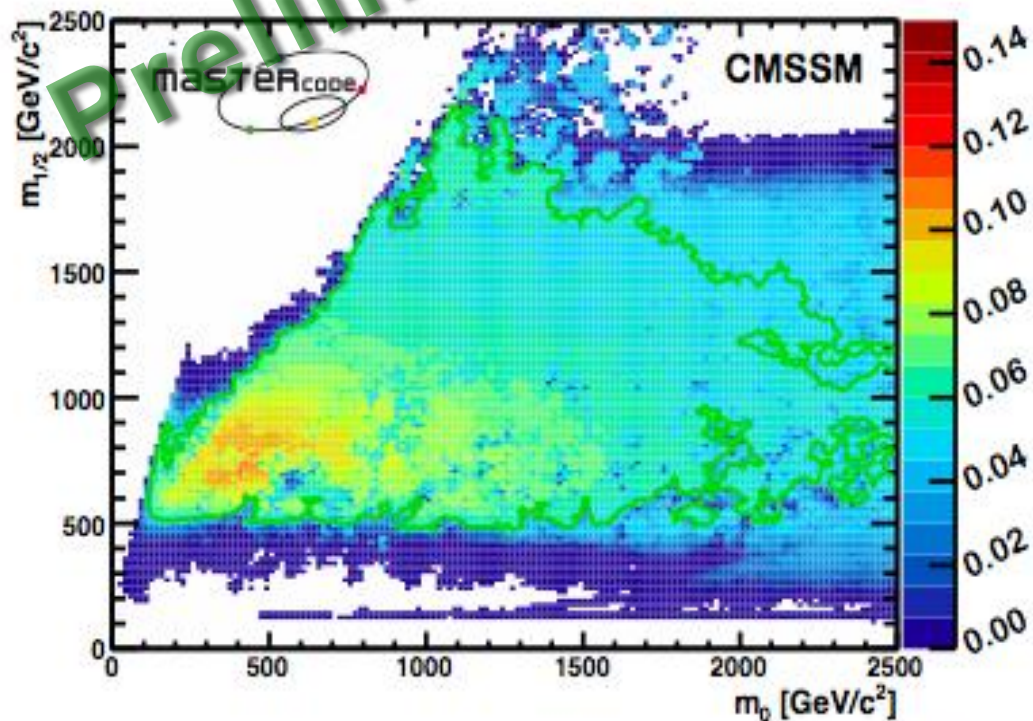
70 million points sampled

Red and blue curves represent  $\Delta\chi^2$  from global minimum, located at ★

Preferred region "opens up" at cost of worsening global  $\chi^2$  value!

# Post-LHC, Post-XENON100

2011 ATLAS + CMS with  $1 \text{ fb}^{-1}$  of LHC Data

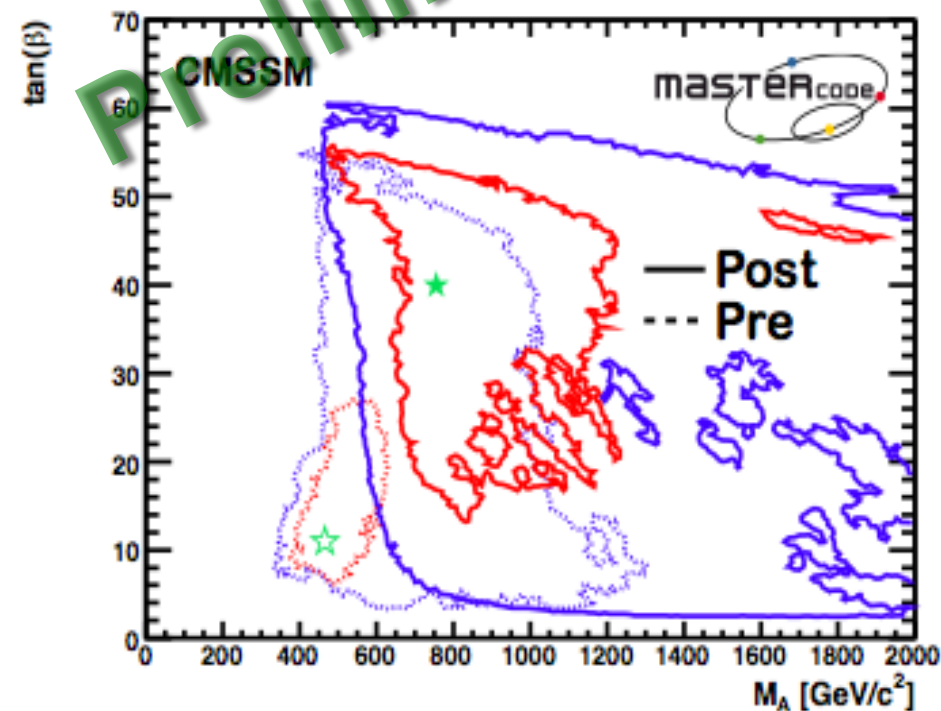


	Model	Min $\chi^2$	Prob	$m_{1/2}$	$m_0$	$A_0$	$\tan \beta$
post-LHC/XENON100	CMSSM	22.5	26%	310	60	-60	10
	NUHM1	20.5	25%	310	60	-60	10
post-LHC/XENON100	CMSSM	29.3	11%	730	420	-1100	40
	NUHM1	27.3	13%	690	160	-880	33

With  $1 \text{ fb}^{-1}$ : CMSSM and NUHM1 still above 10% CL  
 VCMSSM and mSUGRA now less than 5% CL

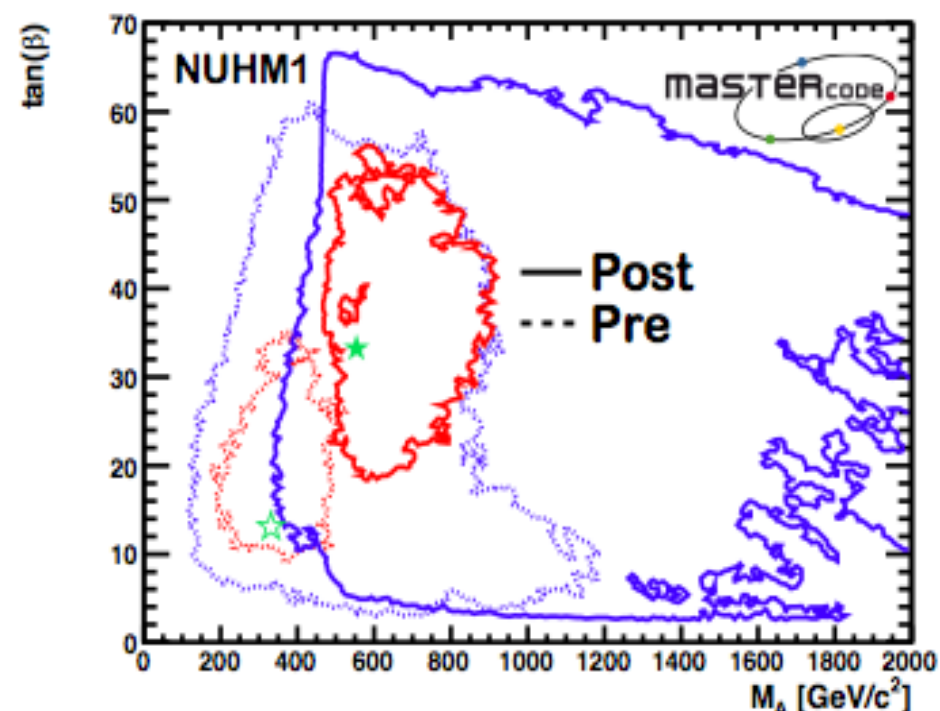
# Post-LHC, Post-XENON100

2011 ATLAS + CMS with 1 fb<sup>-1</sup> of LHC Data



CMSSM

60 million points sampled



NUHM1

70 million points sampled

Red and blue curves represent  $\Delta\chi^2$  from global minimum, located at  $\star$

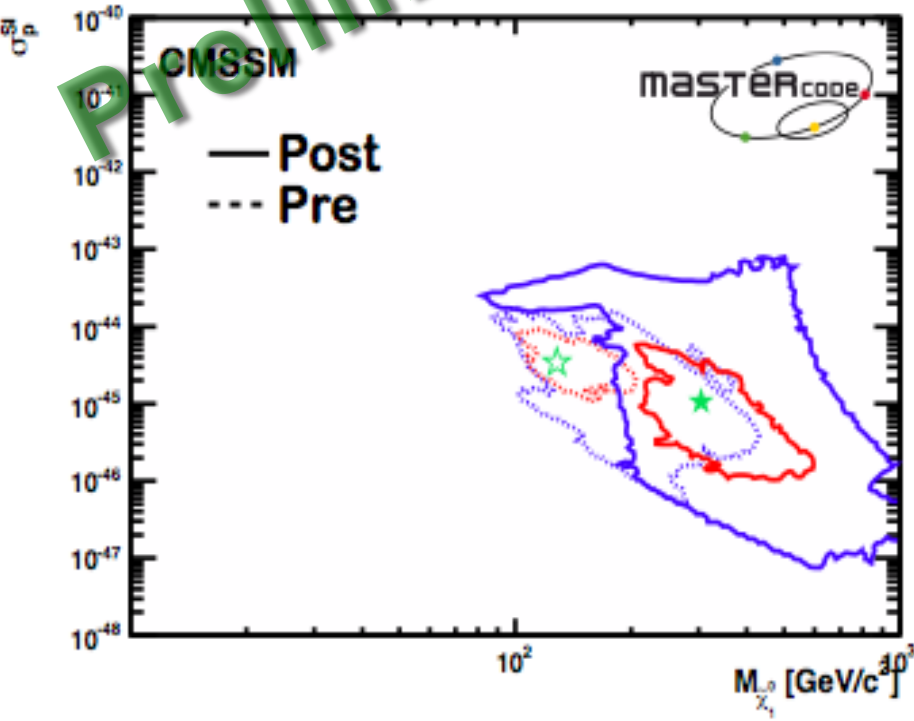
Preferred region "opens up" at cost of worsening global  $\chi^2$  value!



# Post-LHC, Post-XENON100

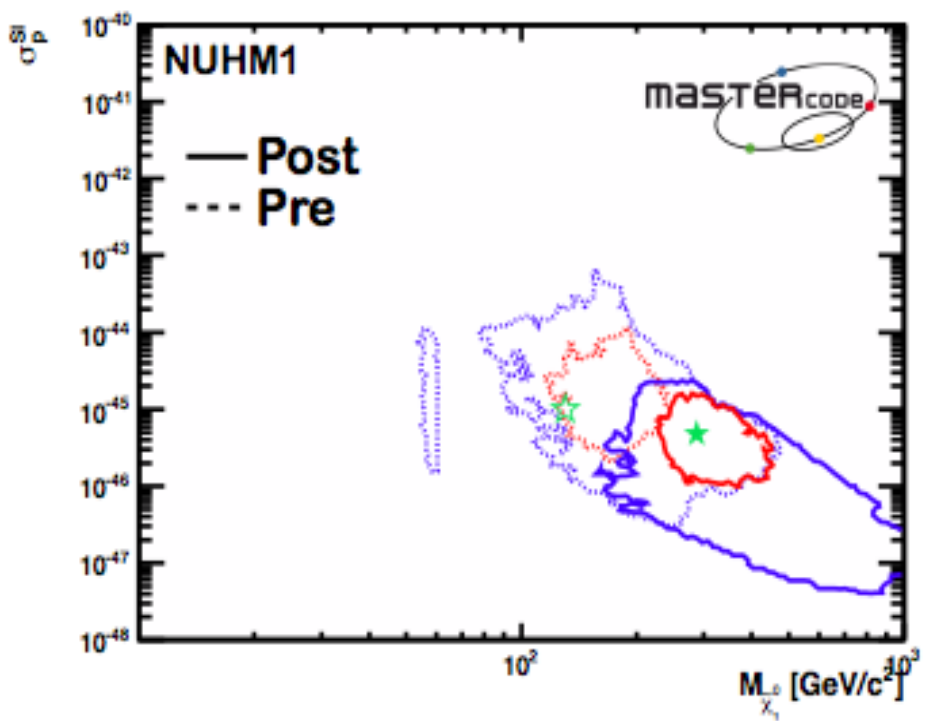
2014 ATLAS + CMS with 1 fb<sup>-1</sup> of LHC Data

Preliminary



CMSSM

60 million points sampled



NUHM1

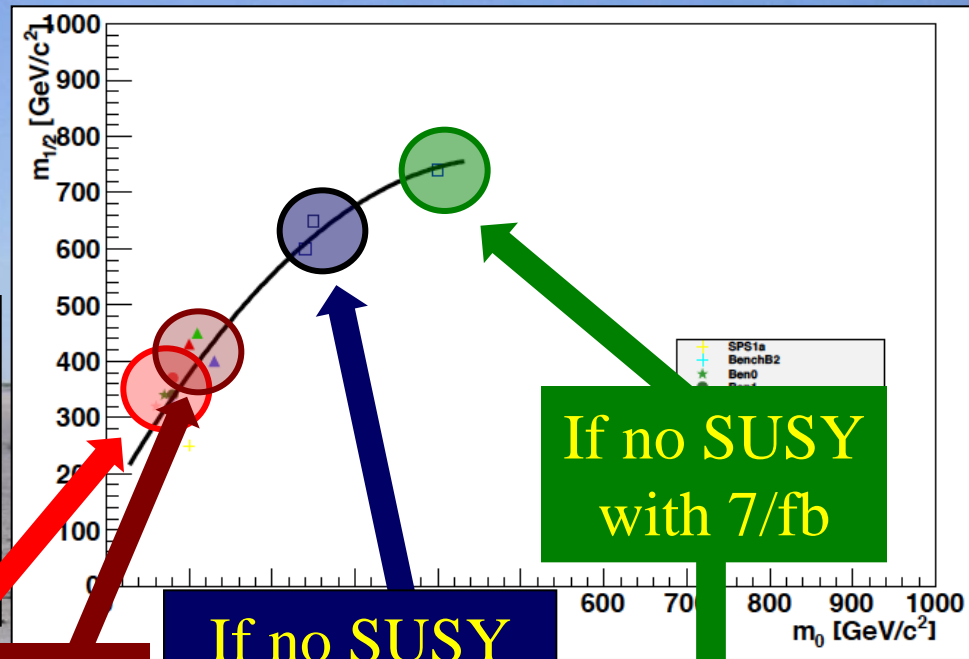
70 million points sampled

Red and blue curves represent  $\Delta\chi^2$  from global minimum, located at ★

Preferred region "opens up" at cost of worsening global  $\chi^2$  value!

# Trajectory of CMSSM Fits

How have best-fit CMSSM points evolved?  
 How would they evolve if SUSY is not discovered in 2011/2?



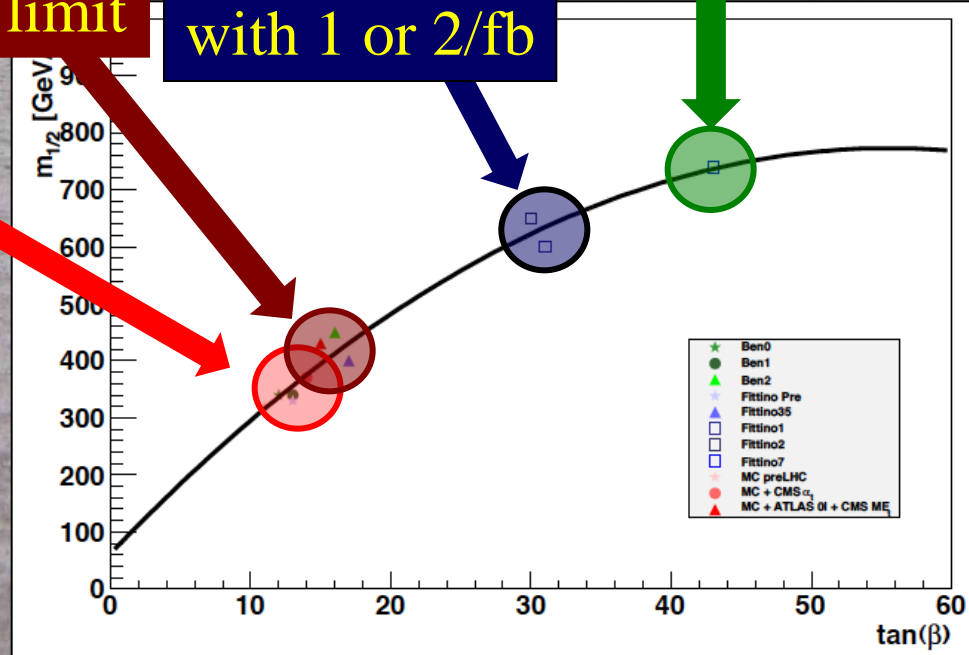
**Current limit**

**If no SUSY with 1 or 2/fb**

**If no SUSY with 7/fb**

**Pre-LHC**

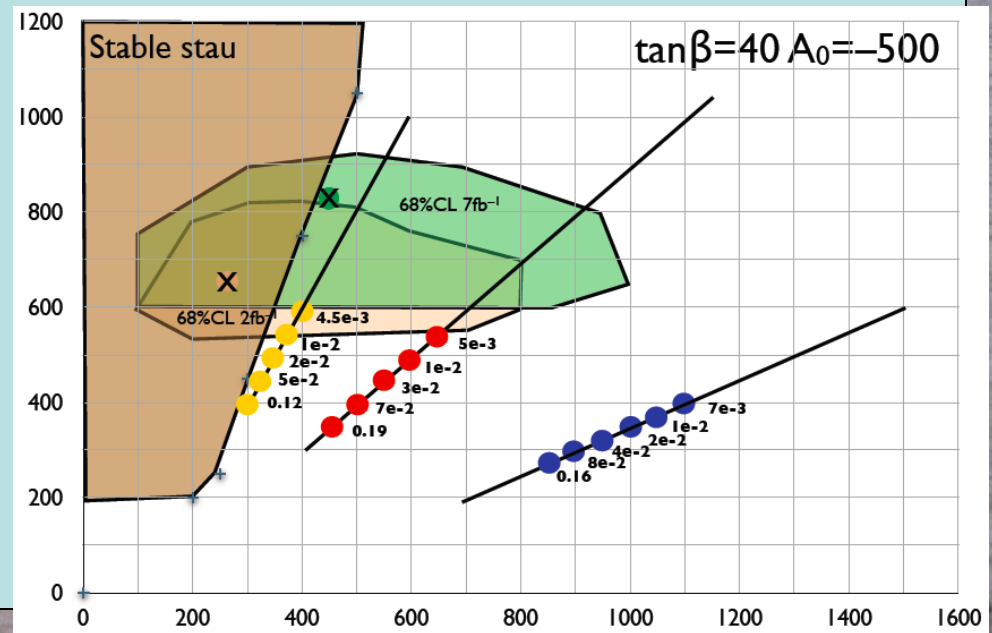
- Old benchmarks
- ★ Pre-LHC fits
- ◆ After LHC 2010
- After LHC 2011/2?



# Sustainable Benchmarks

- Many models:
  - CMSSM, NUHM1, RPV-CMSSM, mGMSB, mAMSB, MM-AMSB and pMSSM
- Benchmark planes, lines & points, e.g., CMSSM
  - Varied signatures
  - Similar along lines
  - **Move to next point if/as needed**

AbdusSalam, Allanach, Dreiner, Ellis, Heinemeyer, Krämer, Mangano, Olive, Rogerson, Roszkowski, Weiglein



# Summary & Perspectives

- LHC data putting pressure on popular models
- Theorists want to combine various constraints
  - Seek to construct global likelihood function
  - Tension between LHC and  $g_\mu - 2$
  - Mitigated at larger  $\tan \beta$
- **Need more information than 95% CL**
- **Desirable to improve TH-EXP dialogue**
- Need to extend studies to other models
  - Compressed spectra, RPV, ...