

LHC longitudinal impedance measurement through Schottky spectra

Christophe Lannoy, Kacper Lasocha, Diogo Alves, Nicolas Mounet

Acknowledgements: Tatiana Pieloni, Ivan Karpov, Theodoros Argyropoulos

14th HL-LHC Collaboration Meeting, Genoa, 10th October 2024

Outline

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 - Transverse impedance effect
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Introduction: The Schottky Monitor

- The Schottky spectrum is based on the measurement of the beam fluctuations in the longitudinal and transverse planes.
- The Schottky spectrum is the **power spectral density** of the beam current in the longitudinal plane and the dipole moment in the transverse planes.
- Important **non-invasive** method for beam diagnostics (emittance, tune, chromaticity, bunch profile, ...).
- The Schottky monitor is one of the only instruments with the potential of measuring the LHC chromaticity in a non-invasive way.
- However, **impedance**, **non-linearities**, **and other collective effects** can strongly affect the Schottky spectrum, preventing the extraction of beam and machine parameters.

→ The distortion caused by impedance can also be used to estimate the impedance itself.



Details of the LHC Schottky system in M. Betz et al., NIM, vol. 874, pp 113-126, 2017



Longitudinal Schottky Spectrum (synchronous particle)





Longitudinal Schottky Spectrum



 au_i : Time difference between particle i and the synchronous particle



- 2. Writing the Fourier series of this periodic signal 3. Using the Jacobi Anger relation $e^{jz\sin\theta} = \sum_{p=-\infty}^{\infty} J_p(z)e^{jp\theta}$
- → The intensity signal can be written in the following form:

$$i_{i}(t) = qf_{0} \sum_{\substack{n \neq i = -\infty \\ \text{Summation} \\ \text{over harmonic } n}}^{\infty} \underbrace{J_{p}(n\omega_{0}\widehat{\tau_{i}})}_{\text{Amplitude}} e^{j\left[\underbrace{(n\omega_{0} + p\Omega_{s_{i}})}_{\text{Frequency}}t + \underbrace{p\varphi_{s_{i}}}_{\text{Phase}}\right]}_{\text{Summation over}}$$



Longitudinal Schottky Spectrum





Longitudinal Schottky Spectrum



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October 10th, 2024

Transverse Schottky spectrum



Experimental LHC spectra: Longitudinal Impedance Effects

- Longitudinal impedance significantly affects proton Schottky spectra.
- Spectra of bunches of different intensities (0.5e11 to 2e11 ppb) acquired at injection during MD block 1.





- Impedance can be source of instabilities and can cause intensity limitation.
 Important to have a good knowledge of the machine impedance.
- Current LHC longitudinal impedance model is a byproduct of the transverse impedance model.
 N. Mounet, PhD thesis, The LHC Transverse Coupled-Bunch Instability
- Could be inaccurate. Main source of longitudinal impedance not necessarily the same as for transverse impedance.
- Model re-evaluation is in progress (RF team, Michail Zampetakis, Ivan Karpov).

Can we extract information about the machine (longitudinal) impedance from the shift of the Schottky satellites?

- 1. Understand how impedance affects the dynamic of the particles (amplitude dependent tune shift).
- 2. How this new dynamic will be reflected in the Schottky spectrum.



Without impedance

Longitudinal equation of motion.



K: Elliptic integral of the first kind.

With impedance

Longitudinal equation of motion including forces coming from impedance:

$$\ddot{\phi} + \Omega_0^2 \sin \phi = \frac{\eta h \omega_0}{p_0} F_{Imp}(t)$$

$$\Omega_s(\hat{\phi}) = \Omega_0 \sqrt{S_1} \left(1 + \frac{3S_3}{8S_1} \hat{\phi}^2 \right)$$

With some approximations, a **relation between synchrotron frequency and oscillation amplitude** can be derived.

Where the S_n coefficients account for the effect of impedance and are defined from the bunch spectrum $\widehat{\lambda(\omega)}$ and the impedance function $Z(\omega)$.

Details in: C. Lannoy et al 2024, JINST 19 P03017



→ Impedance is responsible of an amplitudedependent synchrotron tune shift.



• The new relation between synchrotron frequency and amplitude can be inserted in the original theoretical expression of the Schottky spectrum:

Synchrotron frequency with impedance

 This last expression allows to extend theoretical frameworks such as the Monte Carlo approach or the matrix formalism (K. Lasocha and D. Alves).



 i_i

Benchmark of the theory against macro-particle simulation (PyHEADTAIL).





• Fitting of Schottky spectrum is not trivial as it **depends on many parameters**:

Longitudinal band

- RF voltage
- Long. bunch profile
- Long. impedance
- Intensity

Transverse bands

- All longitudinal parameters
- Betatron tune
- Chromaticity
- Transverse profile
- Transverse impedance
- Lattice non-linearities

...

→ The longitudinal band is easier to fit as it depends on less parameters.



• Fitting of Schottky spectrum is not trivial as it **depends on many parameters**:





Schottky spectra from MD 11723: Nominal Gaussian bunch, fit with $Im(Z_{||})/n = 70 \text{ m}\Omega$





Schottky spectra from MD 11723: Nominal Gaussian bunch, fit with $Im(Z_{||})/n = 135 \text{ m}\Omega$





Schottky spectra from MD 11786: Short q-Gaussian bunch



Short q-Gaussian bunch:

 $\sigma_{rms} = 0.67 \, ns$

•
$$q = 0.25$$

•
$$N = 4.8e10 \text{ ppb}$$

Fitting less obvious → Neither the full LHC impedance model nor a BB resonator can reproduce closely the measurement.

Better agreement might be obtained by fitting both shunt impedance and cutoff frequency (study ongoing).



- Overall, best fitting obtained with: $Im(Z_{||})/n = 135 \text{ m}\Omega$
- Increase of 70% compared with the current longitudinal impedance model: $Im(Z_{||})/n = 80 \text{ m}\Omega$

N. Mounet, PhD thesis, *The LHC Transverse Coupled-Bunch Instability* I. Karpov and L. Giacomel IWG talks, https://indico.cern.ch/event/1422663/

• Still preliminary result, impact of the cut-off frequency of the broadband model to be analysed.



Experimental LHC spectra: Transverse impedance effects

- Transverse impedance significantly affects proton Schottky spectra.
- Spectra of bunches of different intensities (0.1e11 to 2e11 ppb) acquired at injection during MD block 1.







Conclusion

Summary of the talk:

- Longitudinal impedance.
 - Shift of synchrotron satellites observed experimentally.
 - Theory available allowing fitting of impedance.
 - First measurements seem to indicate an increased impedance w.r.t. current model.
 - Further studies needed to analyse the impact of cut-off frequency.
- Transverse impedance.
 - Tune shift observed in experimental spectra.
 - Theory available for quadrupolar impedance and still to be developed for dipolar impedance.





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