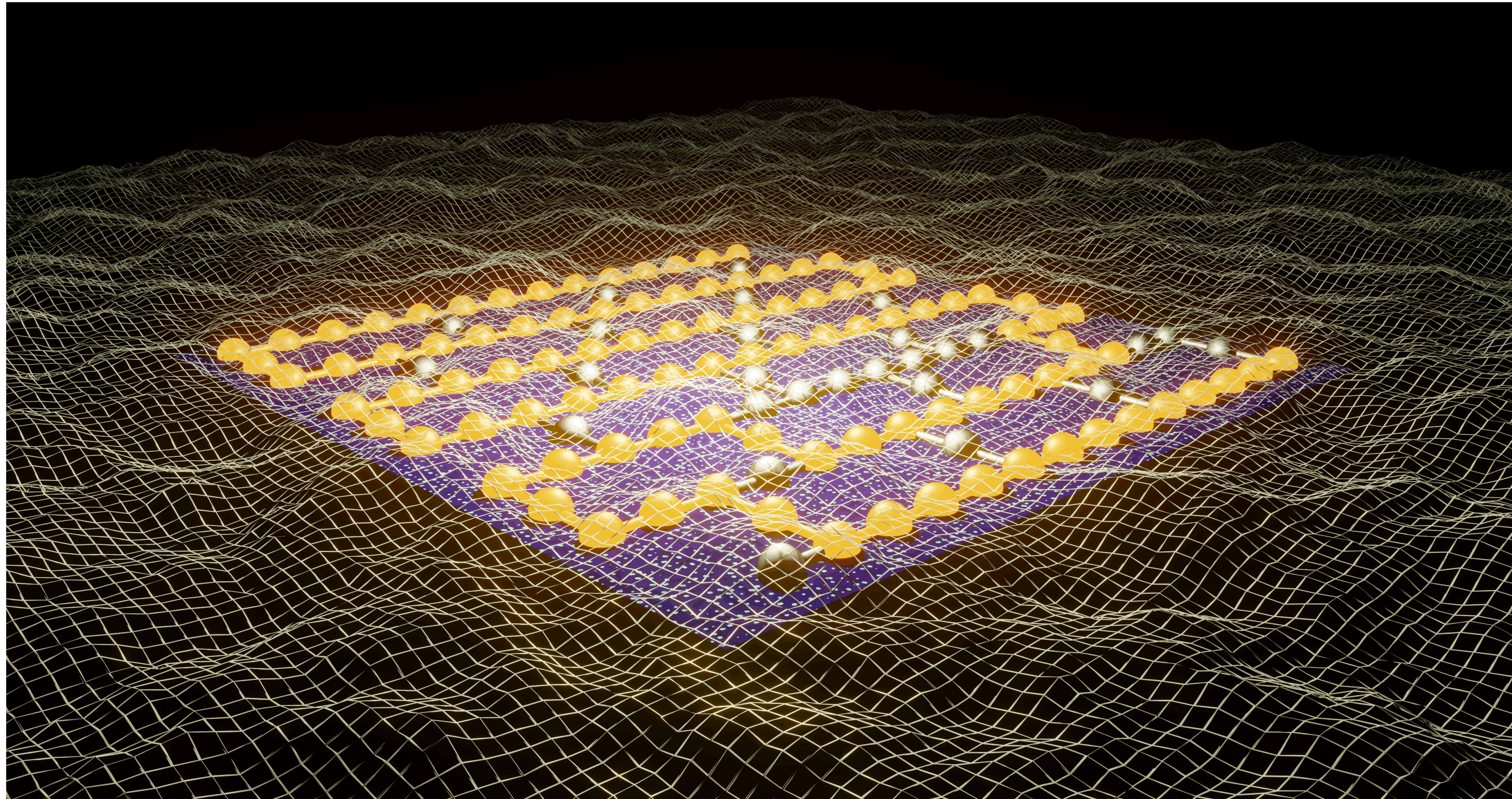


# Simulations of hadron dynamics on a quantum computer



NTG

Roland C. Farrell  
QTI-TH Forum 5/30/24



$u^b$

<sup>b</sup>  
UNIVERSITÄT  
BERN



I will discuss work done in collaboration with



Marc Illa



Anthony Ciavarella




Martin Savage

Details can be found in:

PRX QUANTUM 5, 020315 (2024)

**Scalable Circuits for Preparing Ground States on Digital Quantum Computers:  
The Schwinger Model Vacuum on 100 Qubits**

Roland C. Farrell<sup>\*,†</sup>, Marc Illa<sup>†</sup>, Anthony N. Ciavarella<sup>‡</sup>, and Martin J. Savage<sup>§</sup>  
*InQubator for Quantum Simulation (IQUS), Department of Physics, University of Washington, Seattle,  
Washington 98195, USA*

 (Received 8 September 2023; revised 12 December 2023; accepted 21 March 2024; published 18 April 2024)

**Quantum Simulations of Hadron Dynamics in the Schwinger Model using 112 Qubits**

Roland C. Farrell<sup>\*,†</sup>, Marc Illa<sup>†</sup>, Anthony N. Ciavarella<sup>‡</sup>, and Martin J. Savage<sup>§</sup>

<sup>†</sup>*InQubator for Quantum Simulation (IQUS), Department of Physics,  
University of Washington, Seattle, WA 98195, USA.*

<sup>‡</sup>*Physics Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA*  
(Dated: January 17, 2024)

*PRX Quantum 5, 020315*

*ArXiv: 2401.08044*

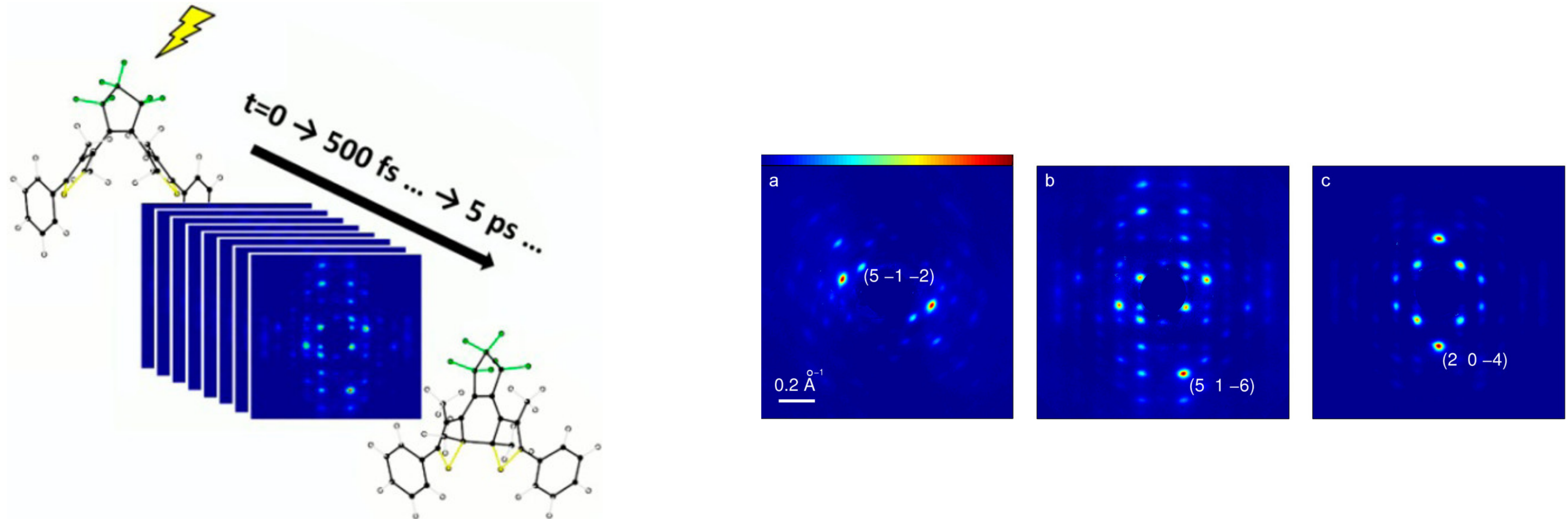


# Outline

- ① Motivation and background
- ② Mapping electrons and photons to qubits
- ③ Preparing hadrons on a quantum computer
- ④ Time evolving hadron on a quantum computer



# Probing reactions in real-time

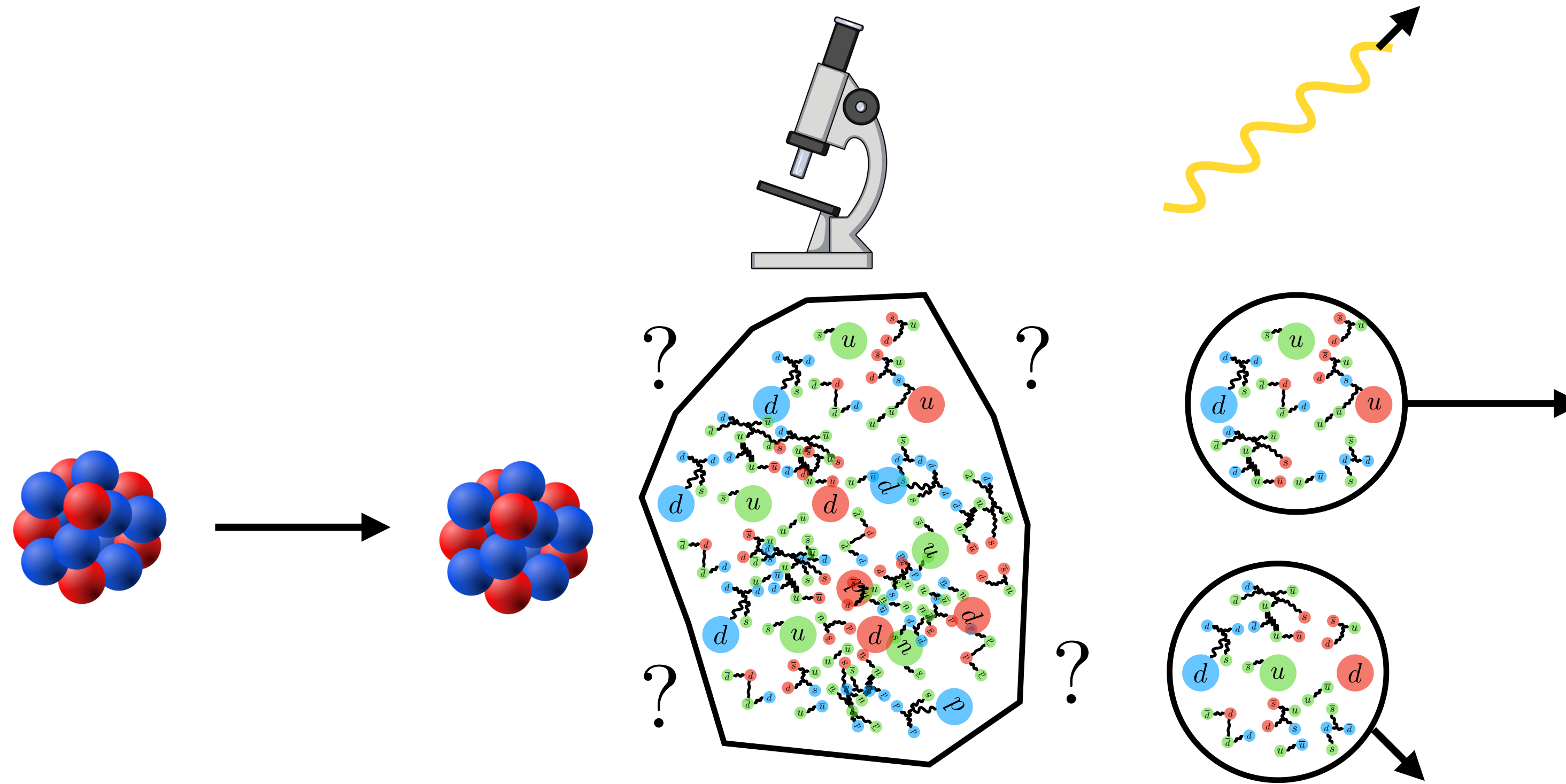


*J. Phys. Chem. B* 2013, 117, 49, 15894-15902

Femtosecond electron diffraction has revealed how molecules re-arrange



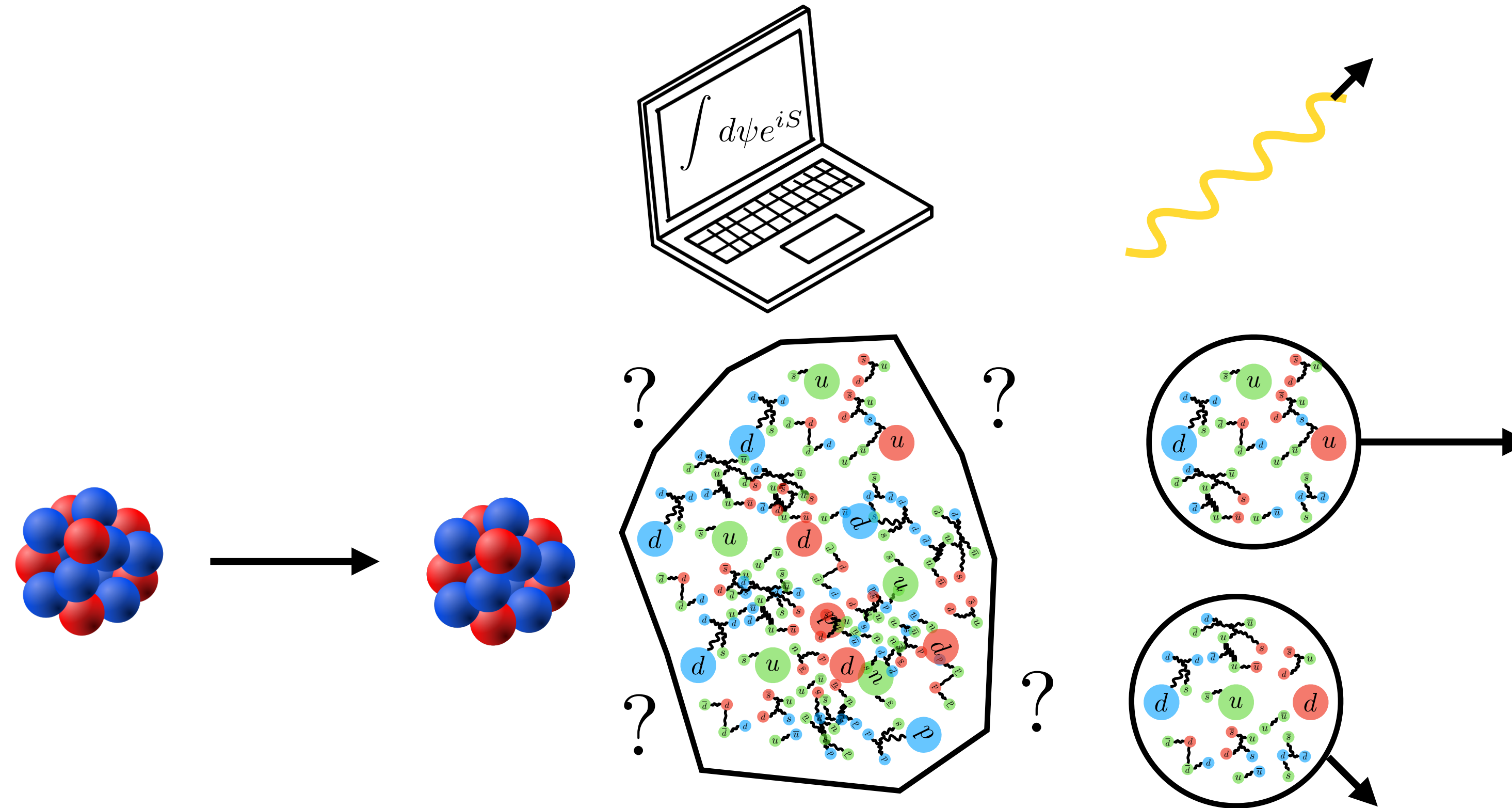
# Probing reactions in real-time



Hadronic processes are difficult to dissect experimentally



# Probing reactions in real-time



Accessible through simulations



# Lattice QCD on classical computers



$$Z_E = \int d\psi d\psi^\dagger dA_\mu e^{-S_E}$$



Lattice QCD has been very successful  
calculating static quantities



# Lattice QCD on classical computers



$$Z_E = \int d\psi d\psi^\dagger dA_\mu e^{-S_E}$$



Lattice QCD has been very successful  
calculating static quantities

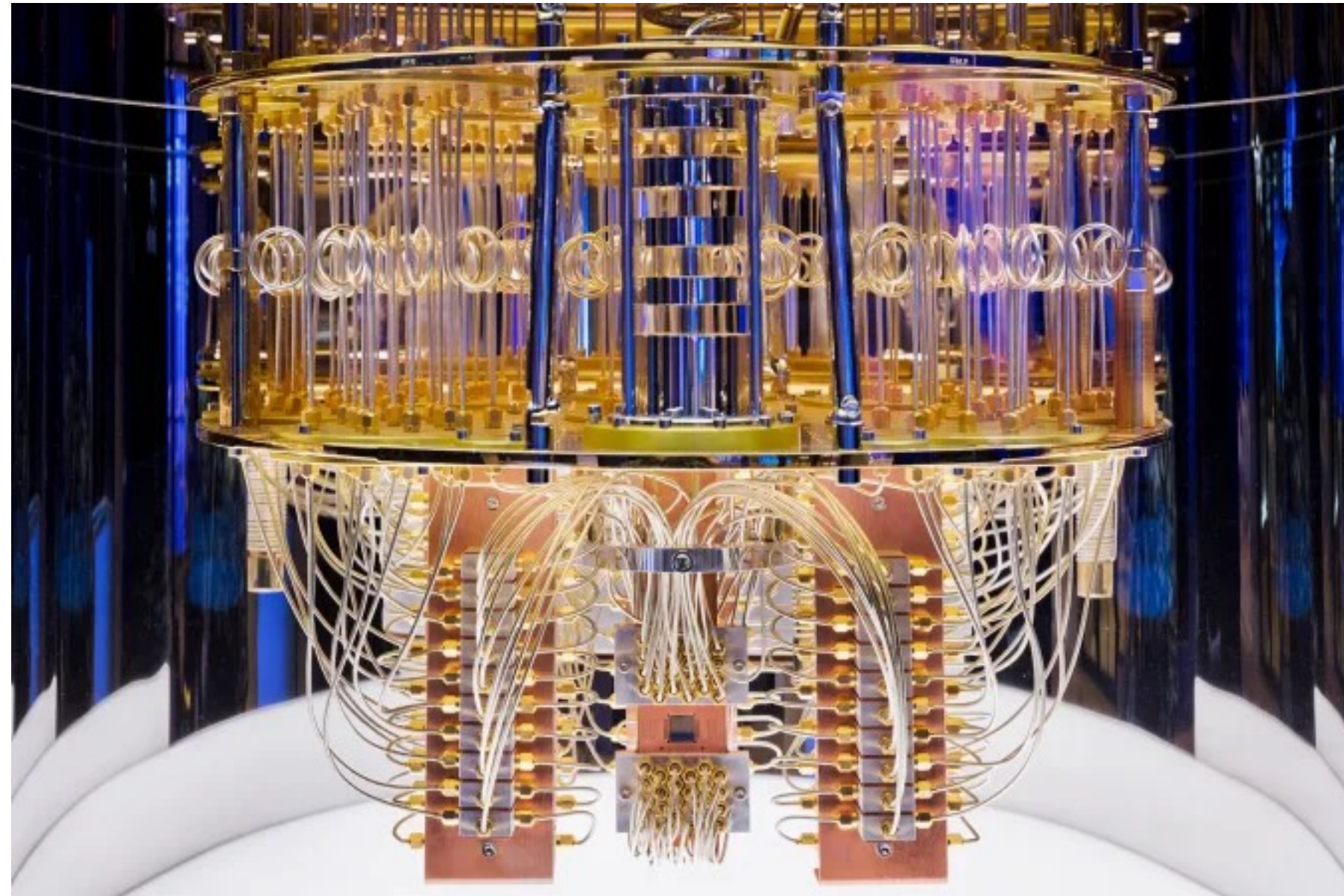
$$Z = \int d\psi d\psi^\dagger dA_\mu e^{iS}$$



Simulations in Minkowski space  
encounter the “sign problem”



# Lattice QCD on quantum computers



Quantum mechanics naturally evolves in Minkowski space

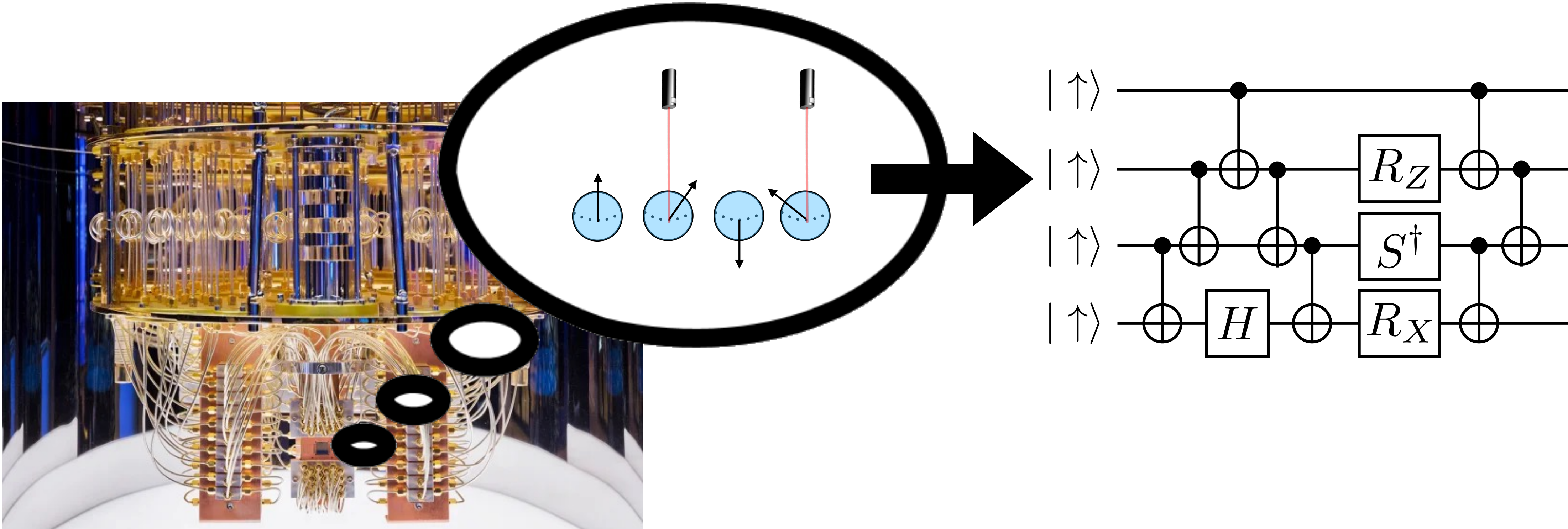
$$U(t) = e^{-i\hat{H}_{\text{QCD}}t}$$



Emulate QCD on a system of highly controllable qubits



A quantum computer is a highly controllable quantum system



More gates = more device errors



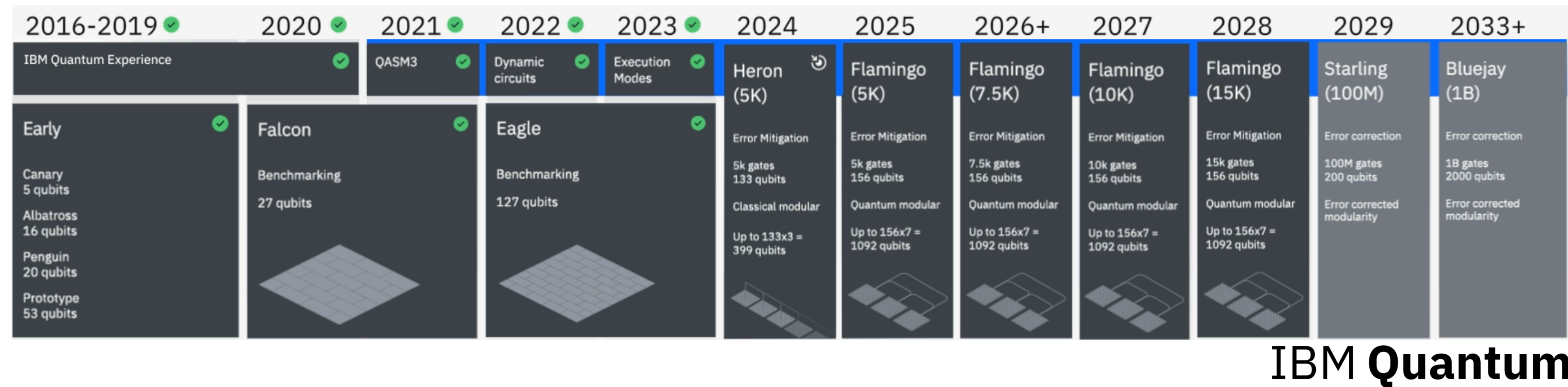
# Quantum computers are rapidly improving!

2016-2019	2020	2021	2022	2023	2024	2025	2026+	2027	2028	2029	2033+
IBM Quantum Experience	QASM3	Dynamic circuits	Execution Modes	Heron (5K)	Flamingo (5K)	Flamingo (7.5K)	Flamingo (10K)	Flamingo (15K)	Starling (100M)	Bluejay (1B)	
<b>Early</b> Canary 5 qubits Albatross 16 qubits Penguin 20 qubits Prototype 53 qubits	<b>Falcon</b> Benchmarking 27 qubits	<b>Eagle</b> Benchmarking 127 qubits	Error Mitigation 5k gates 133 qubits Classical modular Up to 133x3 = 399 qubits	Error Mitigation 5k gates 156 qubits Quantum modular Up to 156x7 = 1092 qubits	Error Mitigation 7.5k gates 156 qubits Quantum modular Up to 156x7 = 1092 qubits	Error Mitigation 10k gates 156 qubits Quantum modular Up to 156x7 = 1092 qubits	Error Mitigation 15k gates 156 qubits Quantum modular Up to 156x7 = 1092 qubits	Error correction 100M gates 200 qubits Error corrected modularity	Error correction 1B gates 2000 qubits Error corrected modularity		

**IBM Quantum**



# Quantum computers are rapidly improving!



Towards QCD, I will discuss work on the Schwinger model

- **QED in 1+1D: also a confining gauge theory with “hadrons”**

Atas et. al *Nat Commun* **12**, 6499 (2021)

Klco et. al *Phys. Rev. A* **98**, 032331

Surace et. al *Phys. Rev. X* **10**, 021041

Ciavarella et. al *Phys. Rev. D* **103**, 094501

Kokail et. al *Nature* **569**, 355–360 (2019)

Martinez et. al *Nature* **534**, 516–519 (2016)



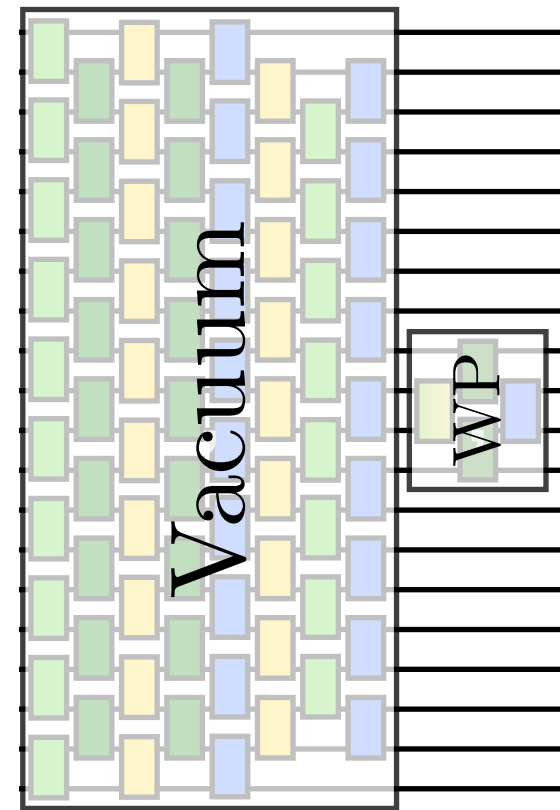
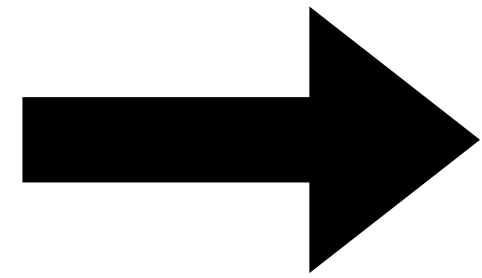
Goal: to simulate hadron dynamics on a quantum computer

## 0. Map the Hilbert space onto qubits



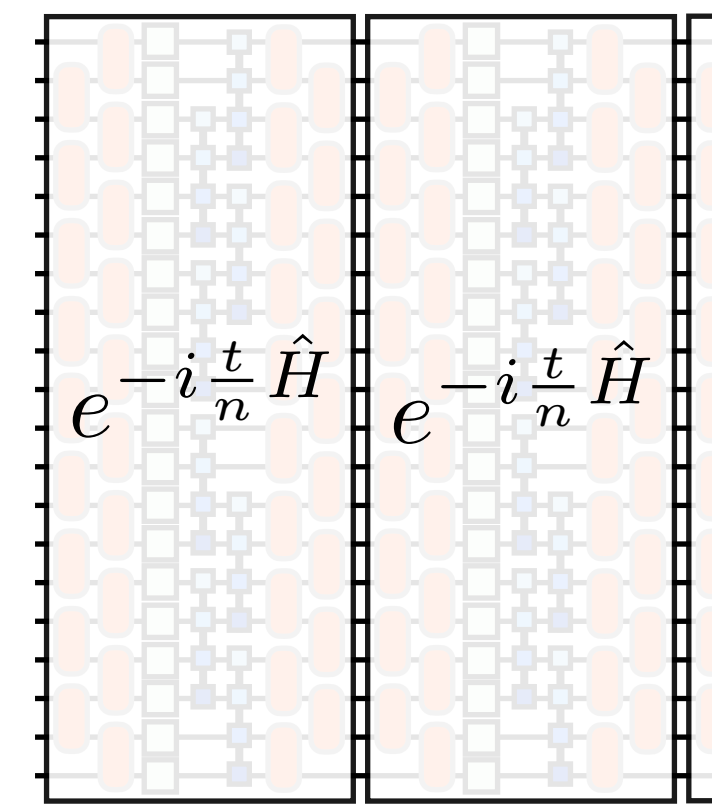
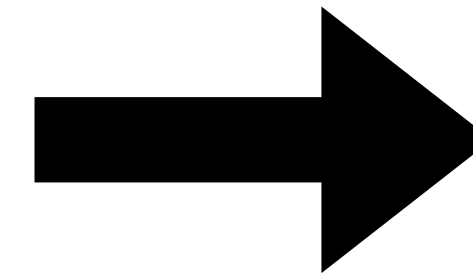
## 1. Prepare the initial state

$|\psi_{\text{WP}}\rangle$



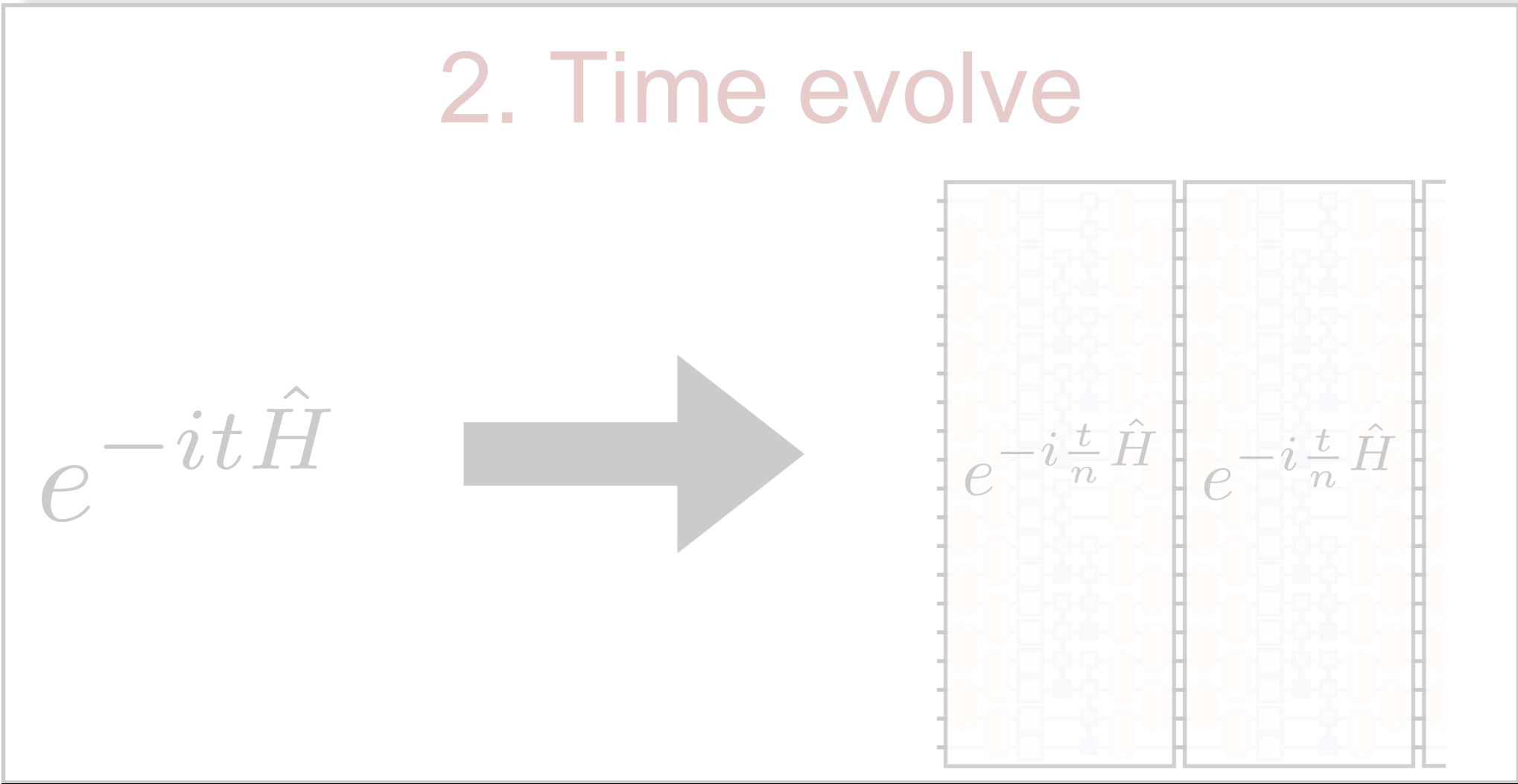
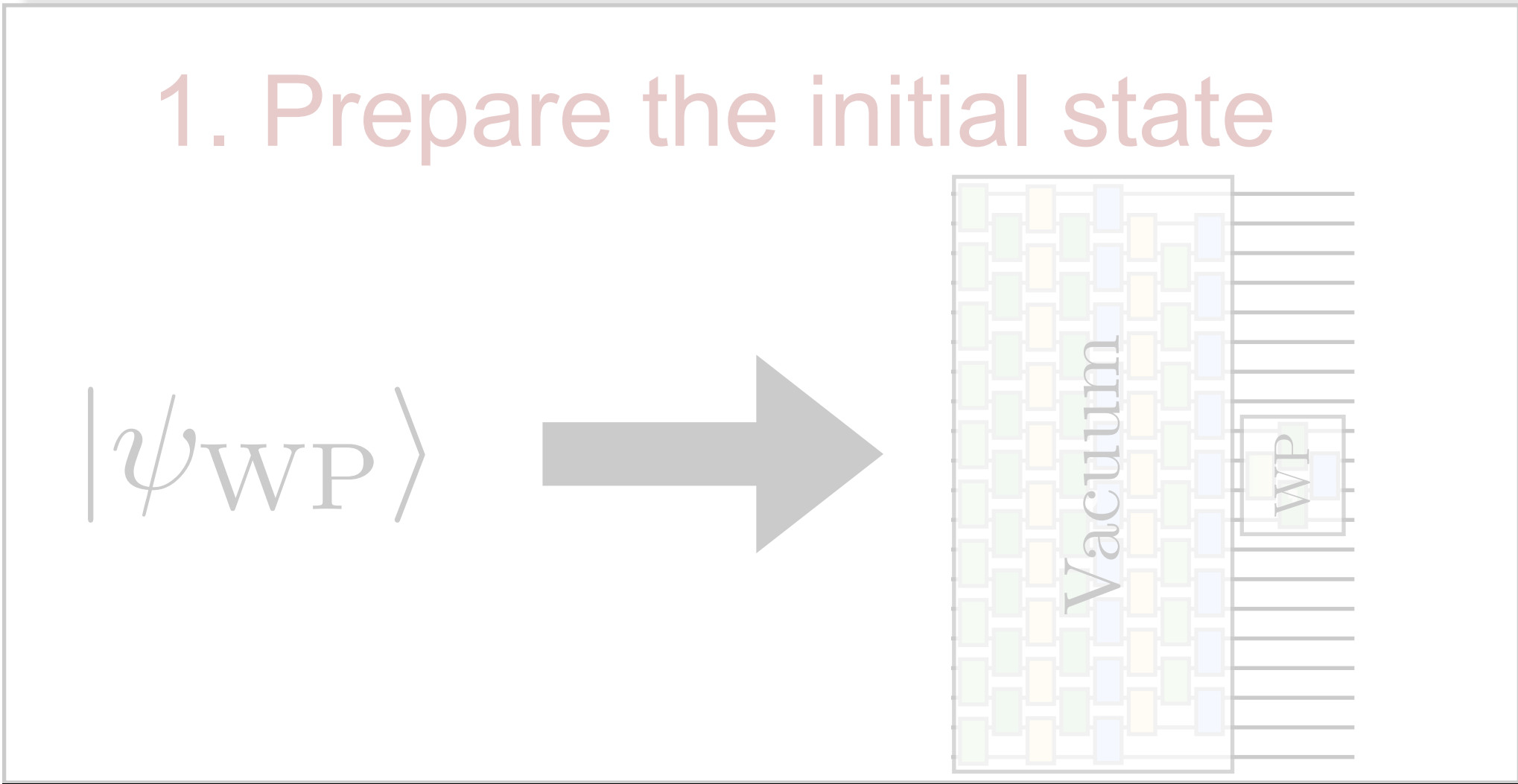
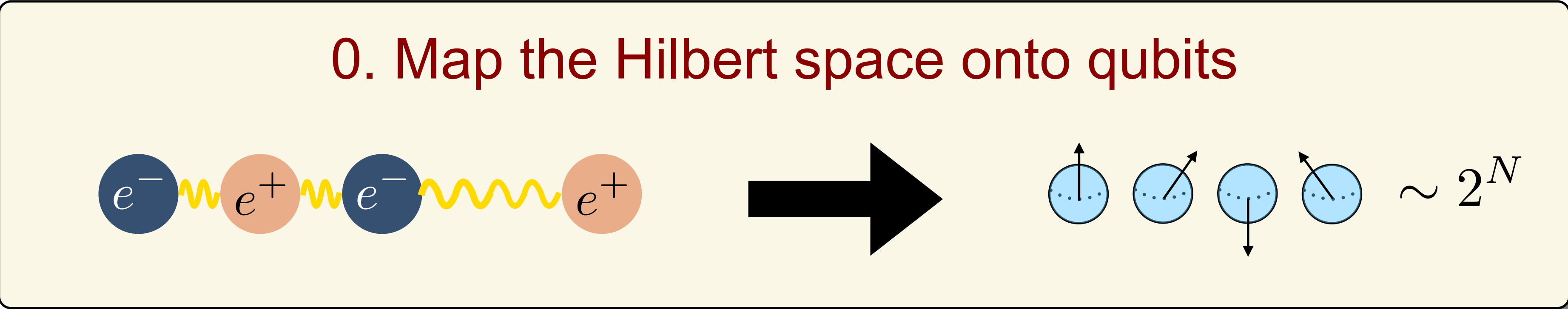
## 2. Time evolve

$e^{-it\hat{H}}$



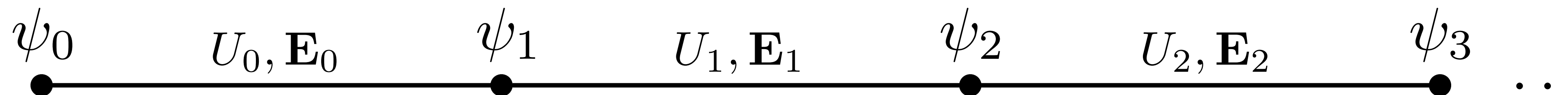


Goal: to simulate hadron dynamics on a quantum computer





# The Schwinger model on a staggered lattice

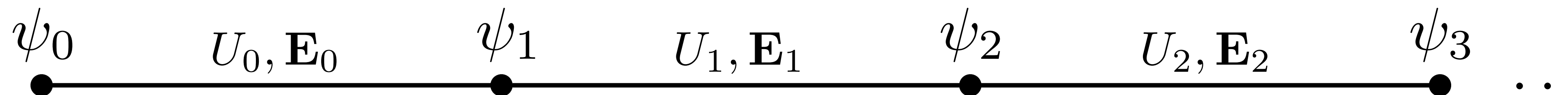


$$\hat{H}_{\text{KS}} = m \sum_{n=0}^{N-1} (-1)^n \psi_n^\dagger \psi_n + \frac{1}{2} \sum_{n=0}^{N-2} (\psi_n^\dagger U_n \psi_{n+1} + \text{h.c.}) + \frac{g^2}{2} \sum_{n=0}^{N-2} |\mathbf{E}_n|^2$$

Lattice of size  $N$  with electrons (positrons) on even (odd) numbered sites



# The Schwinger model on a staggered lattice



$$\hat{H}_{\text{KS}} = m \sum_{n=0}^{N-1} (-1)^n \psi_n^\dagger \psi_n + \frac{1}{2} \sum_{n=0}^{N-2} (\psi_n^\dagger U_n \psi_{n+1} + \text{h.c.}) + \frac{g^2}{2} \sum_{n=0}^{N-2} |\mathbf{E}_n|^2$$

Mass

Kinetic "hopping"

Electric

Lattice of size  $N$  with electrons (positrons) on even (odd) numbered sites



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$$\hat{H}_{\text{KS}} = m \sum_{n=0}^{N-1} (-1)^n \psi_n^\dagger \psi_n + \frac{1}{2} \sum_{n=0}^{N-2} (\psi_n^\dagger U_n \psi_{n+1} + \text{h.c.}) + \frac{g^2}{2} \sum_{n=0}^{N-2} |\mathbf{E}_n|^2$$

↑  
Mass

↑  
Kinetic “hopping”

↑  
Electric

In 1+1D the photon is not dynamical and can be removed



# The Schwinger model on a staggered lattice



$$\hat{H}_{\text{KS}} = m \sum_{n=0}^{N-1} (-1)^n \psi_n^\dagger \psi_n + \frac{1}{2} \sum_{n=0}^{N-2} (\psi_n^\dagger \psi_{n+1} + \text{h.c.}) + \frac{g^2}{2} \sum_{n=0}^{N-2} \left( \sum_{m \leq n} \hat{Q}_m \right)^2$$

No parallel transporter

Coulomb potential

A lattice of  $N$  interacting electrons and positrons



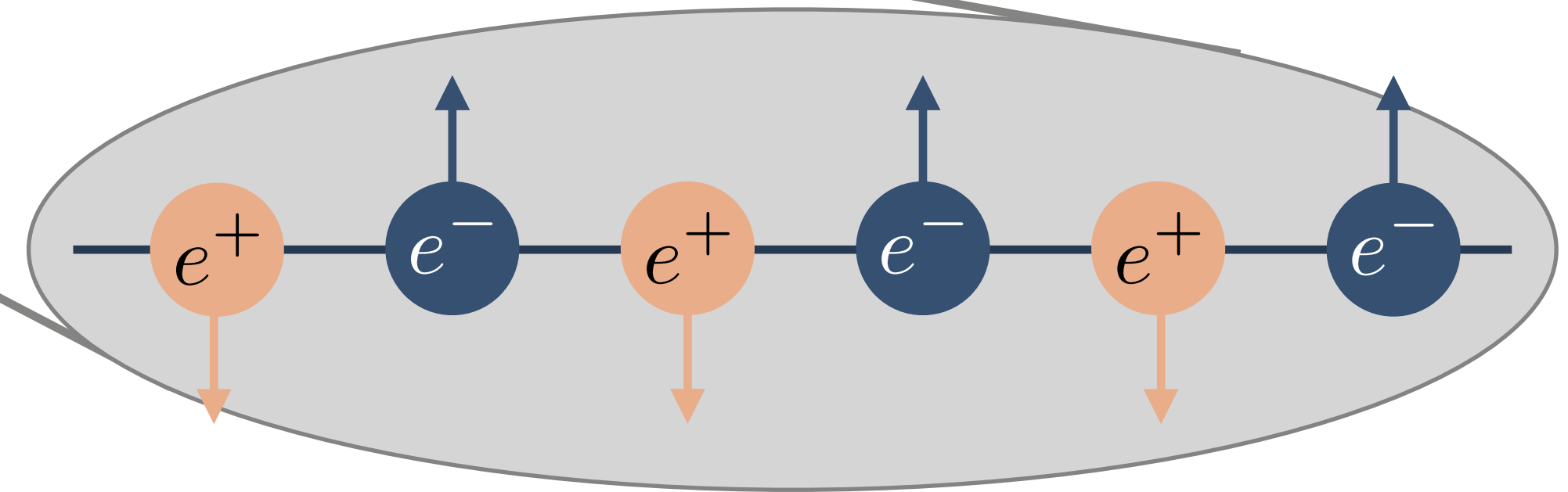
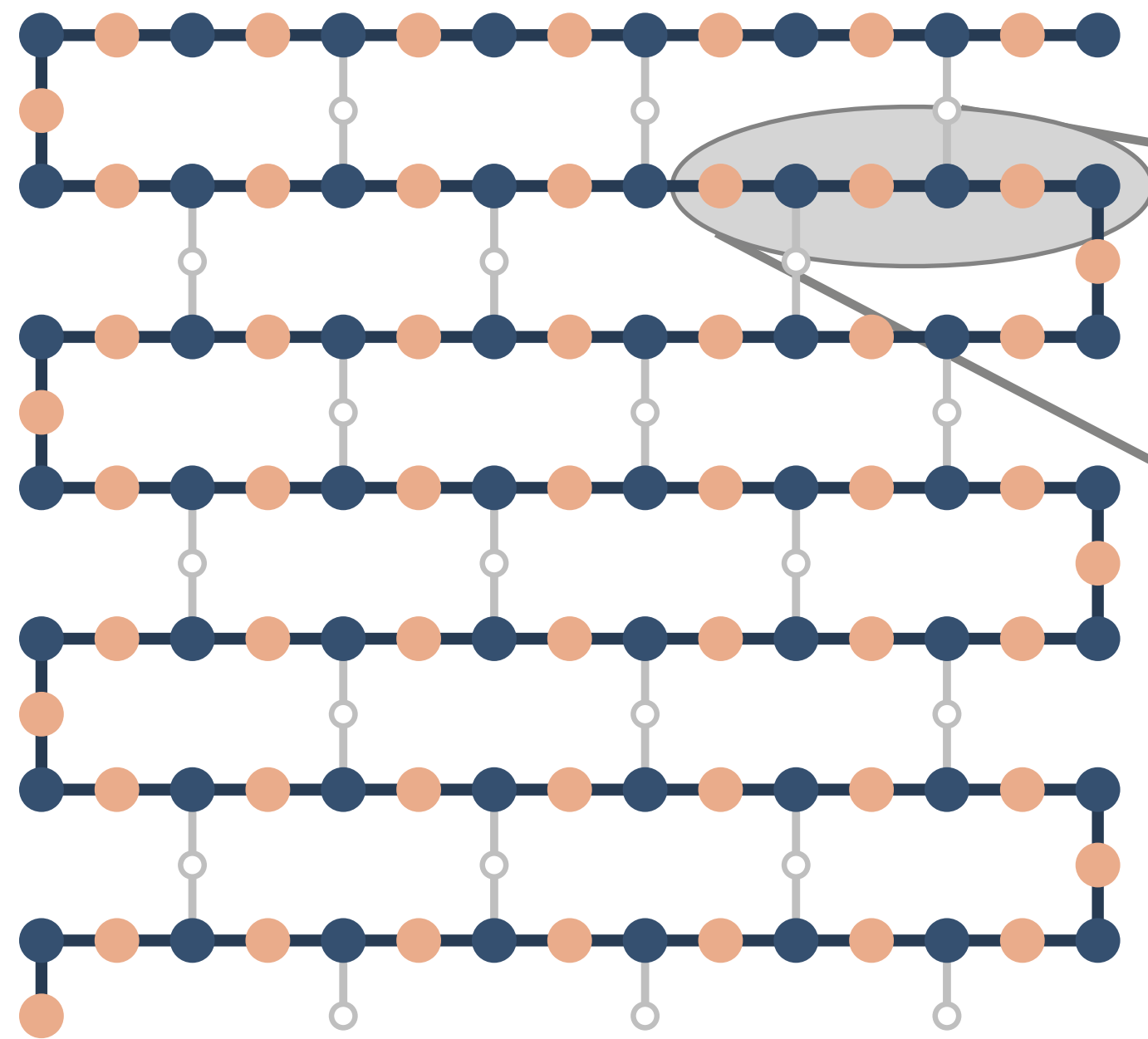
Mapping to qubits with the JW transformation  $\psi_n^\dagger = \prod_{i < n} (-\sigma_i^z) \sigma_n^+$

$$\hat{H} = \frac{m}{2} \sum_{n=0}^{N-1} (-1)^n \hat{Z}_n + \frac{1}{2} \sum_{n=0}^{N-2} (\hat{\sigma}_n^+ \hat{\sigma}_{n+1}^- + \text{h.c.}) + \frac{g^2}{2} \sum_{n=0}^{N-2} \left( \sum_{m \leq n} \hat{Q}_m \right)^2, \quad \hat{Q}_k = -\frac{1}{2} (\hat{Z}_k + (-1)^k)$$



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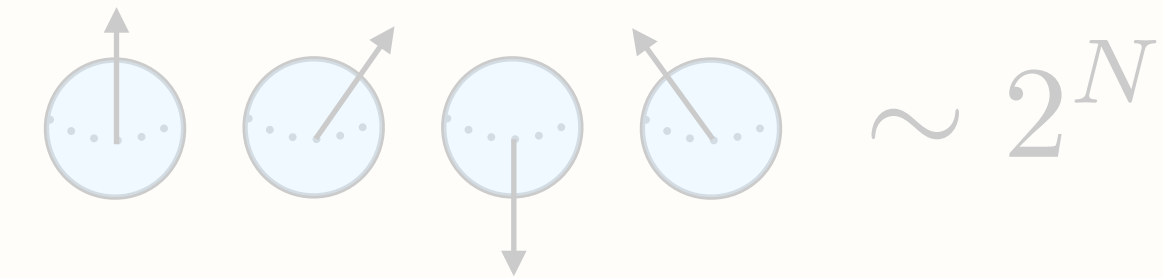
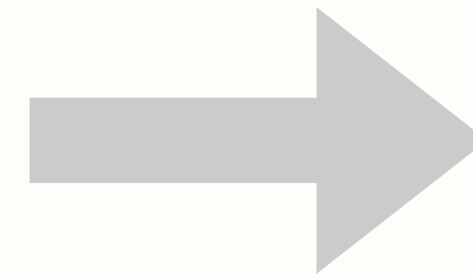
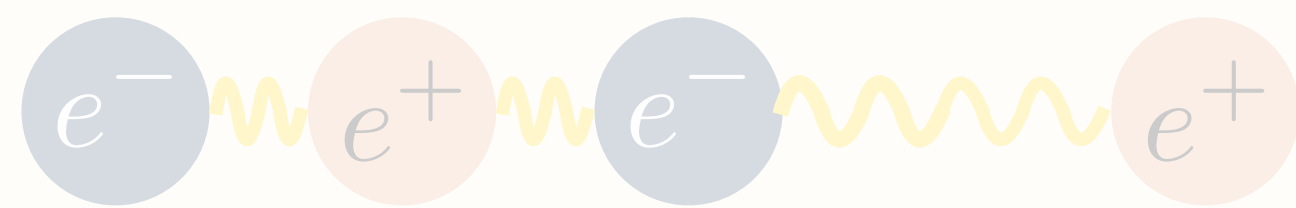


ibm\_torino



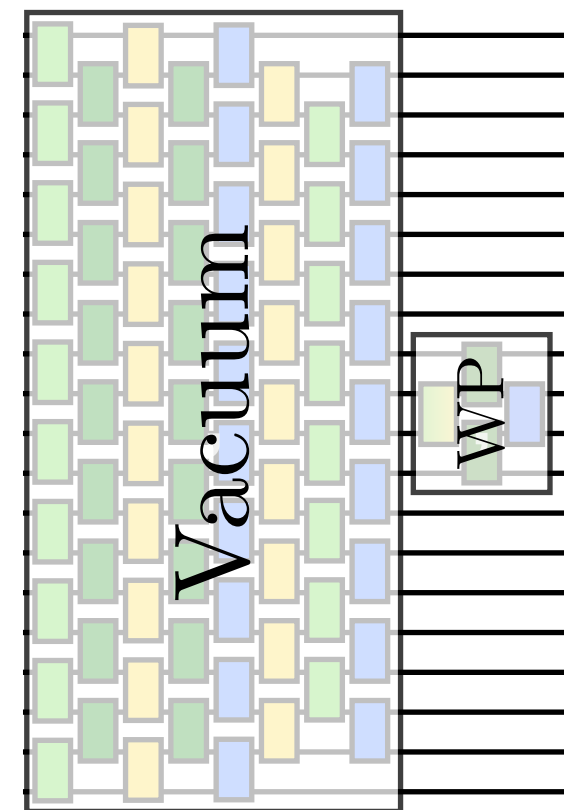
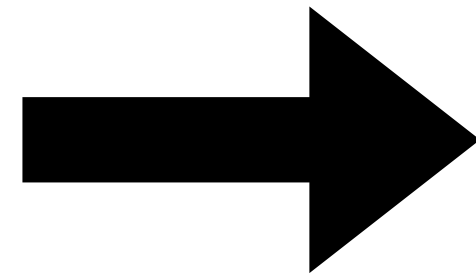
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## 0. Map the Hilbert space onto qubits



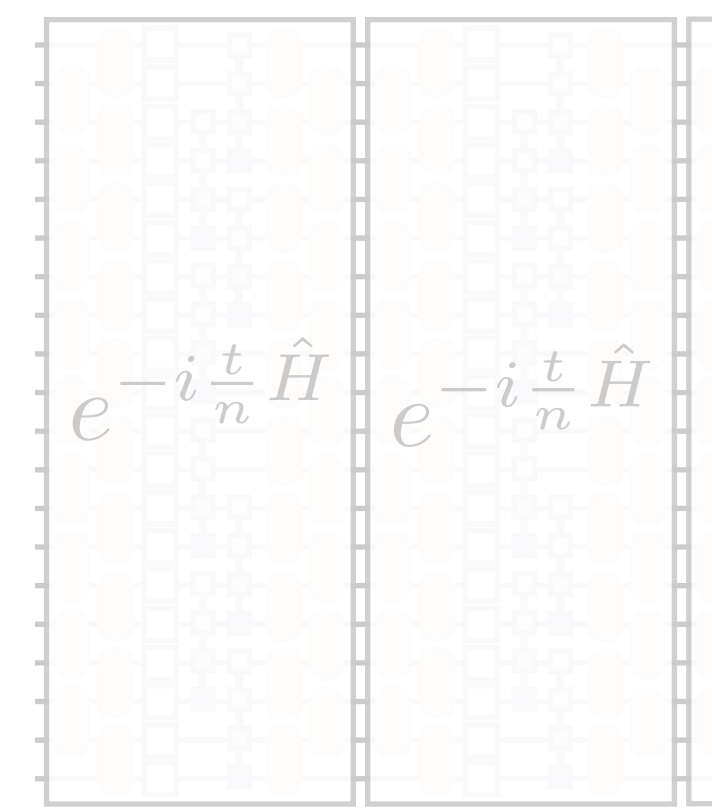
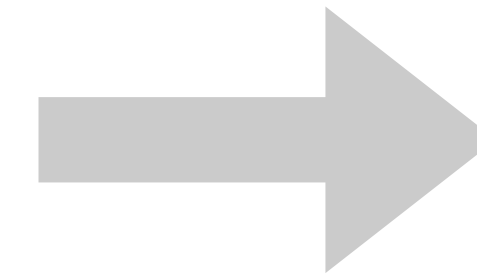
## 1. Prepare the initial state

$$|\psi_{\text{WP}}\rangle$$



## 2. Time evolve

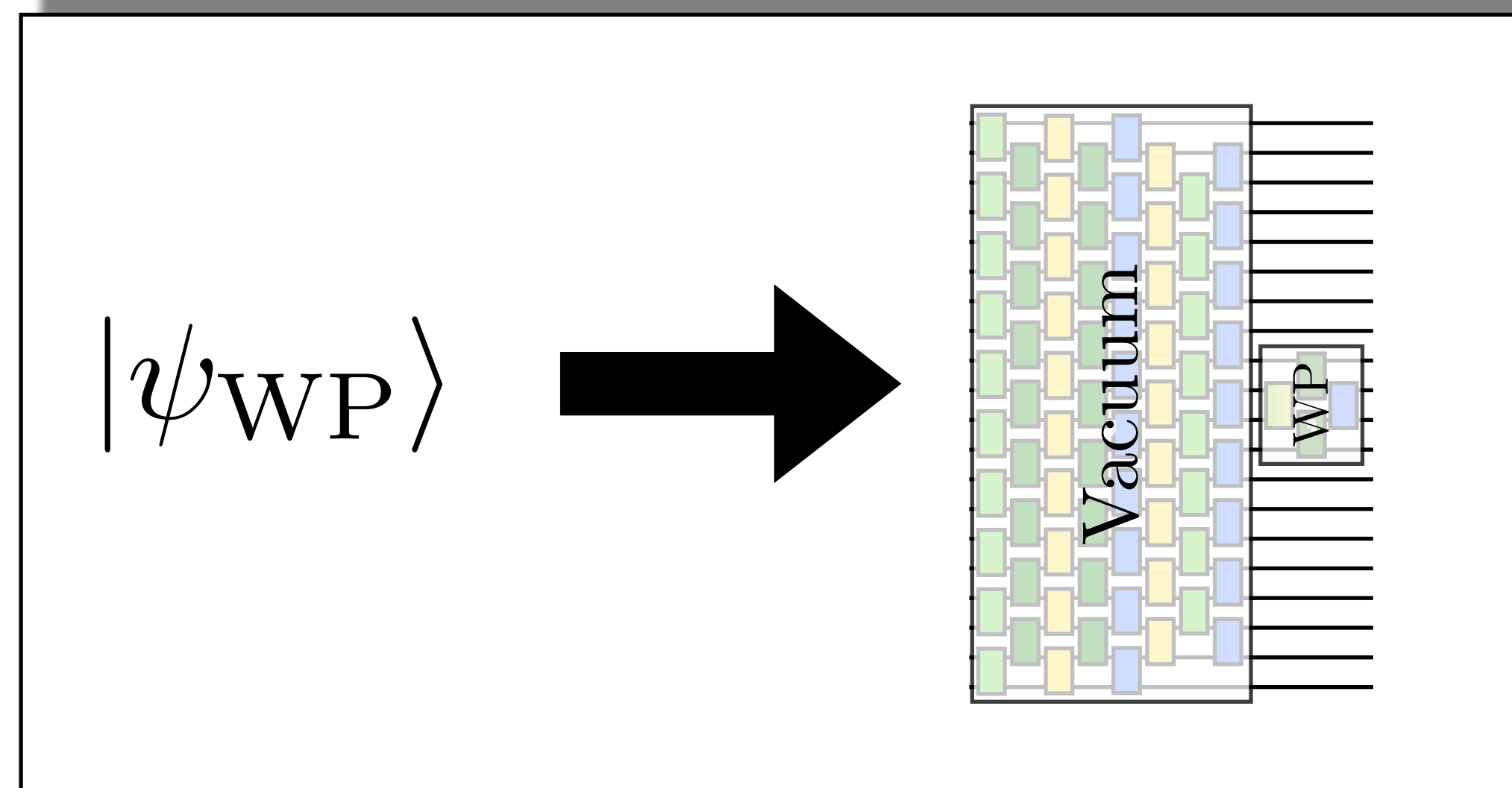
$$e^{-it\hat{H}}$$





Goal: prepare a hadron wavepacket

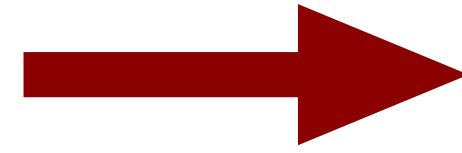
1. Prepare the interacting vacuum
2. Excite a hadron wave packet on top of the vacuum





# Important features of the vacuum

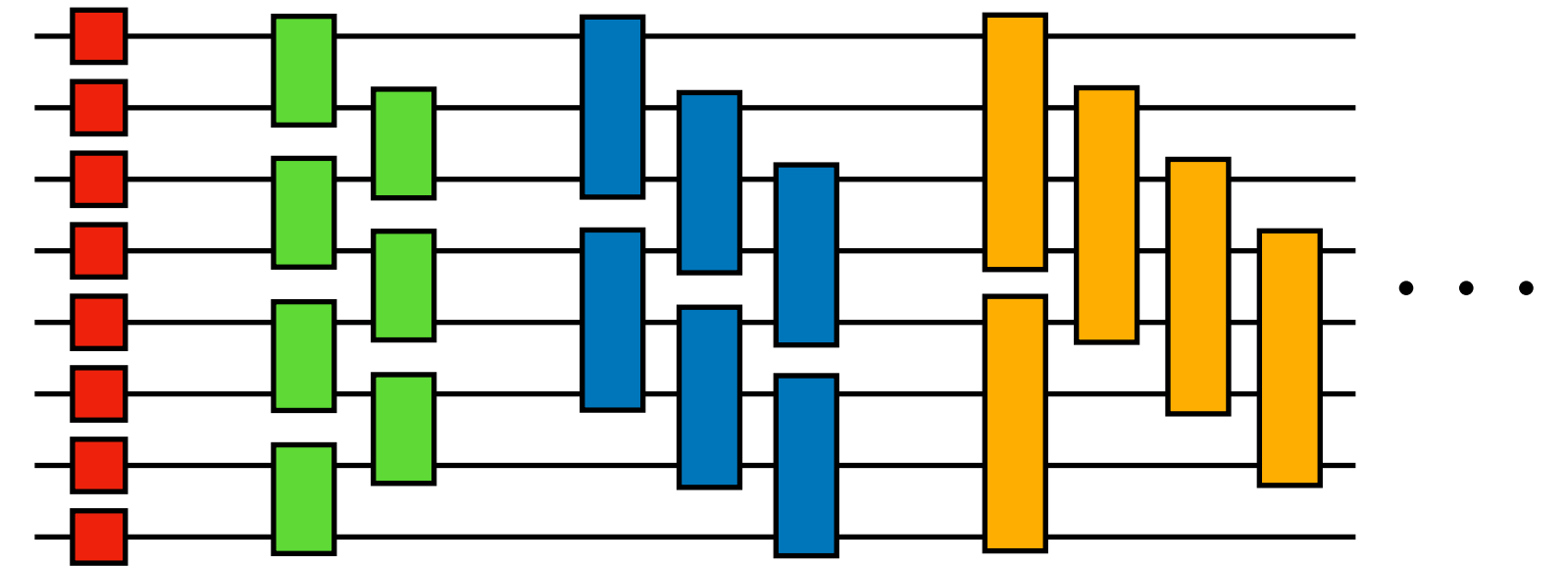
Translational and CP symmetry



Circuits are repeated across the lattice

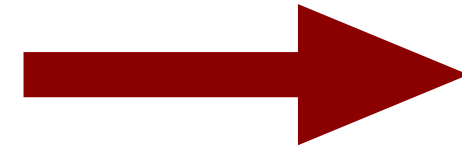
$$\langle \hat{Q}_n \rangle = (-1)^d \langle \hat{Q}_{n+d} \rangle$$

$$|\psi_{\text{vac}}\rangle_{N=8} =$$



# Important features of the vacuum

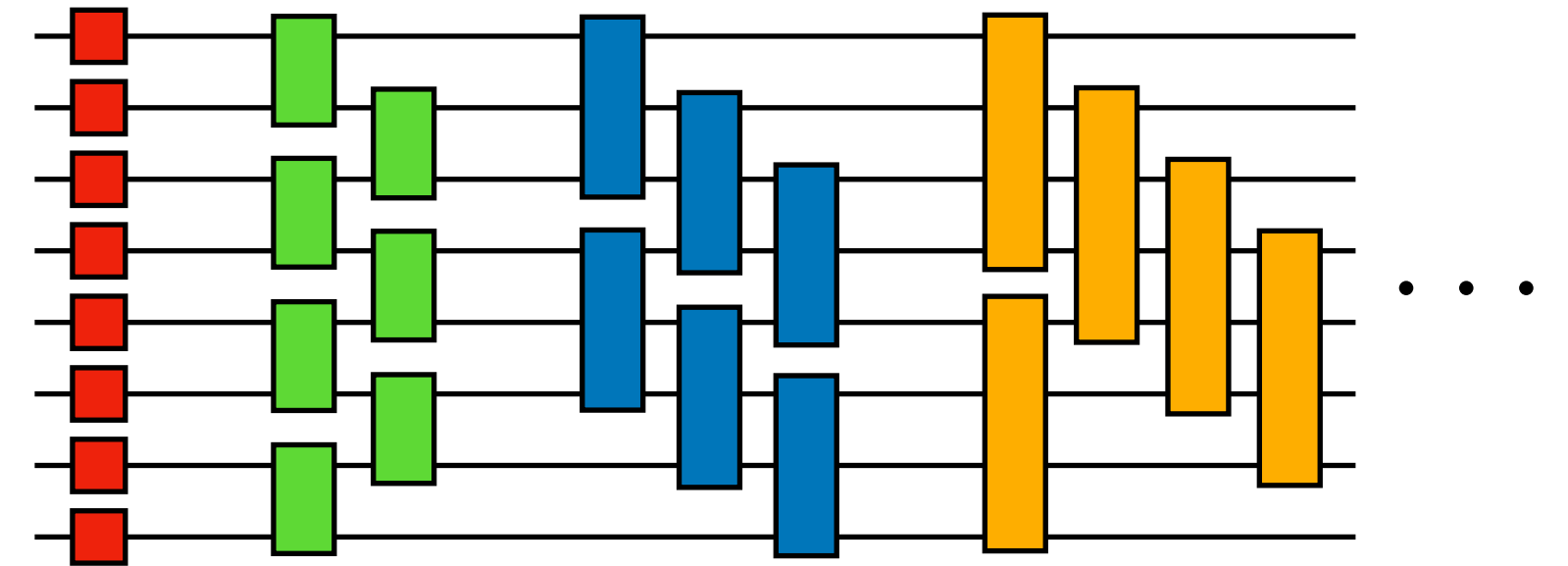
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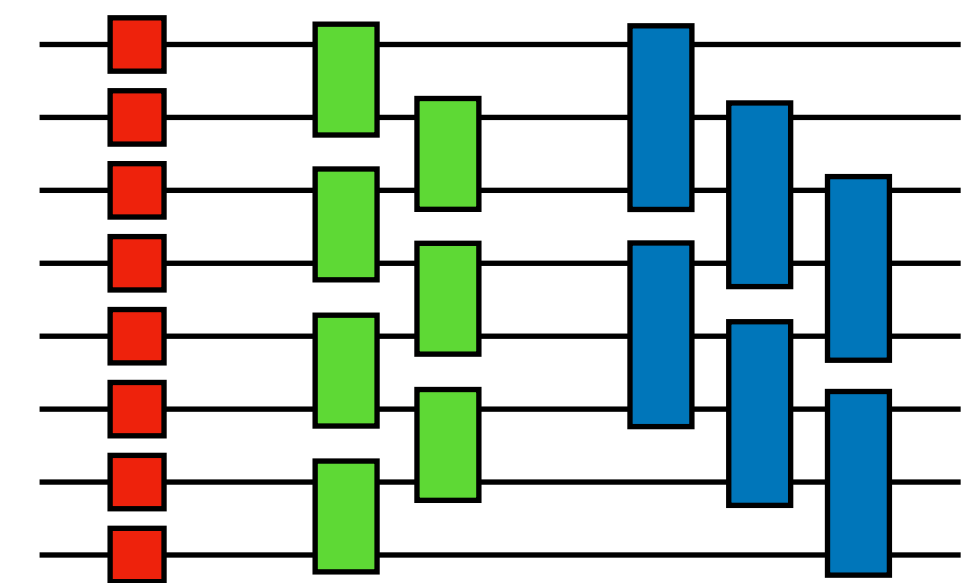
Spectrum is gapped



Circuits have structure over  $\sim m_{\text{hadron}}^{-1}$  sites

$$\langle \hat{Q}_n \hat{Q}_{n+d} \rangle_c \sim e^{-d m_{\text{hadron}}}$$

$$|\psi_{\text{vac}}\rangle_{N=8} \approx$$





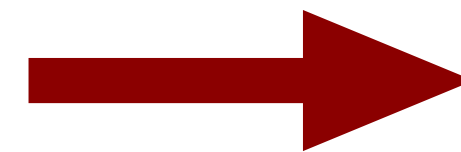
# Important features of the vacuum

Translational and CP symmetry



Circuits are repeated across the lattice

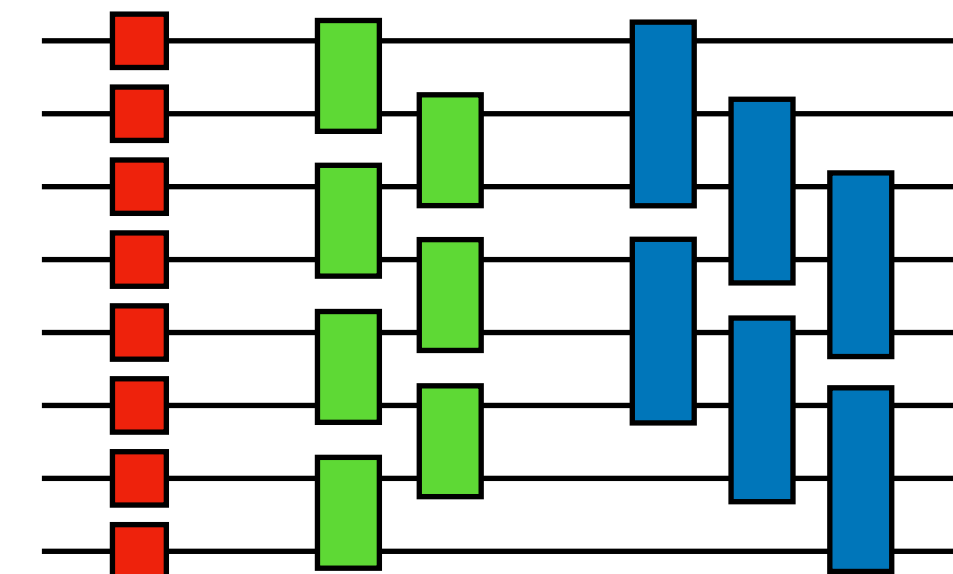
Spectrum is gapped



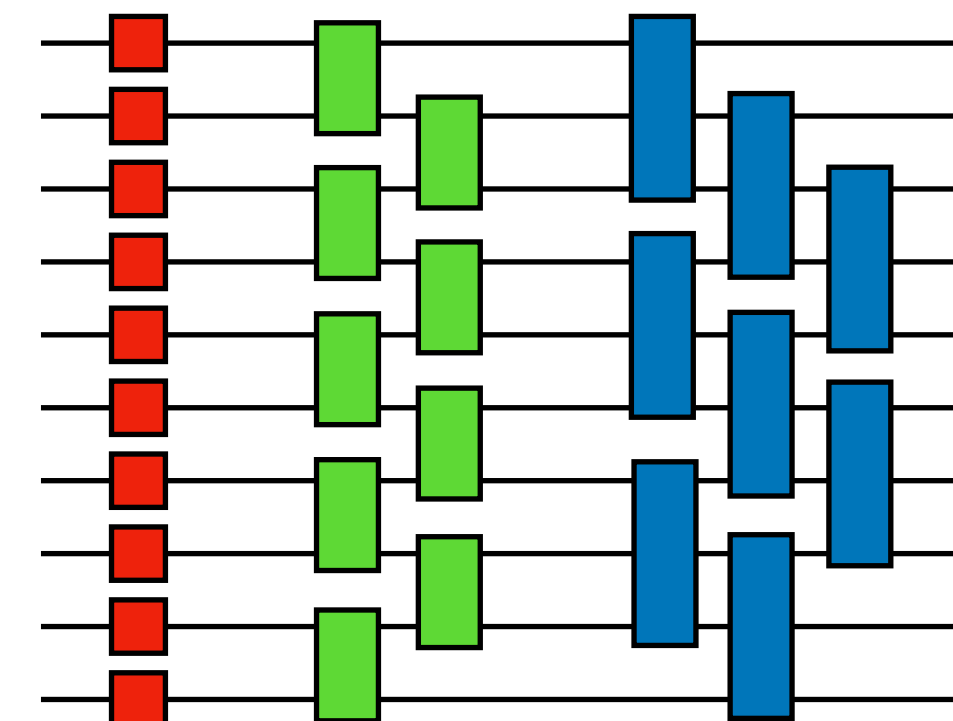
Circuits structure converges in  $N$

$$\langle \hat{Q}_n \hat{Q}_{n+d} \rangle_{N=8} = \langle \hat{Q}_n \hat{Q}_{n+d} \rangle_{N=10} + \mathcal{O}(e^{-Nm_{\text{hadron}}})$$

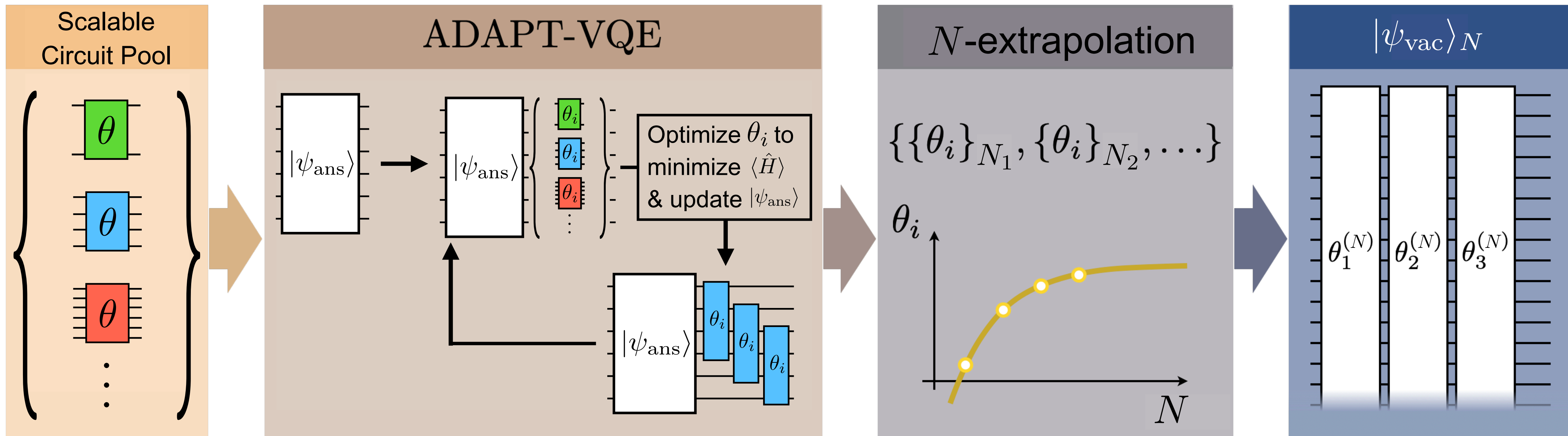
$$|\psi_{\text{vac}}\rangle_{N=8} \approx$$



$$|\psi_{\text{vac}}\rangle_{N=10} \approx$$



# The SC-ADAPT-VQE state preparation algorithm

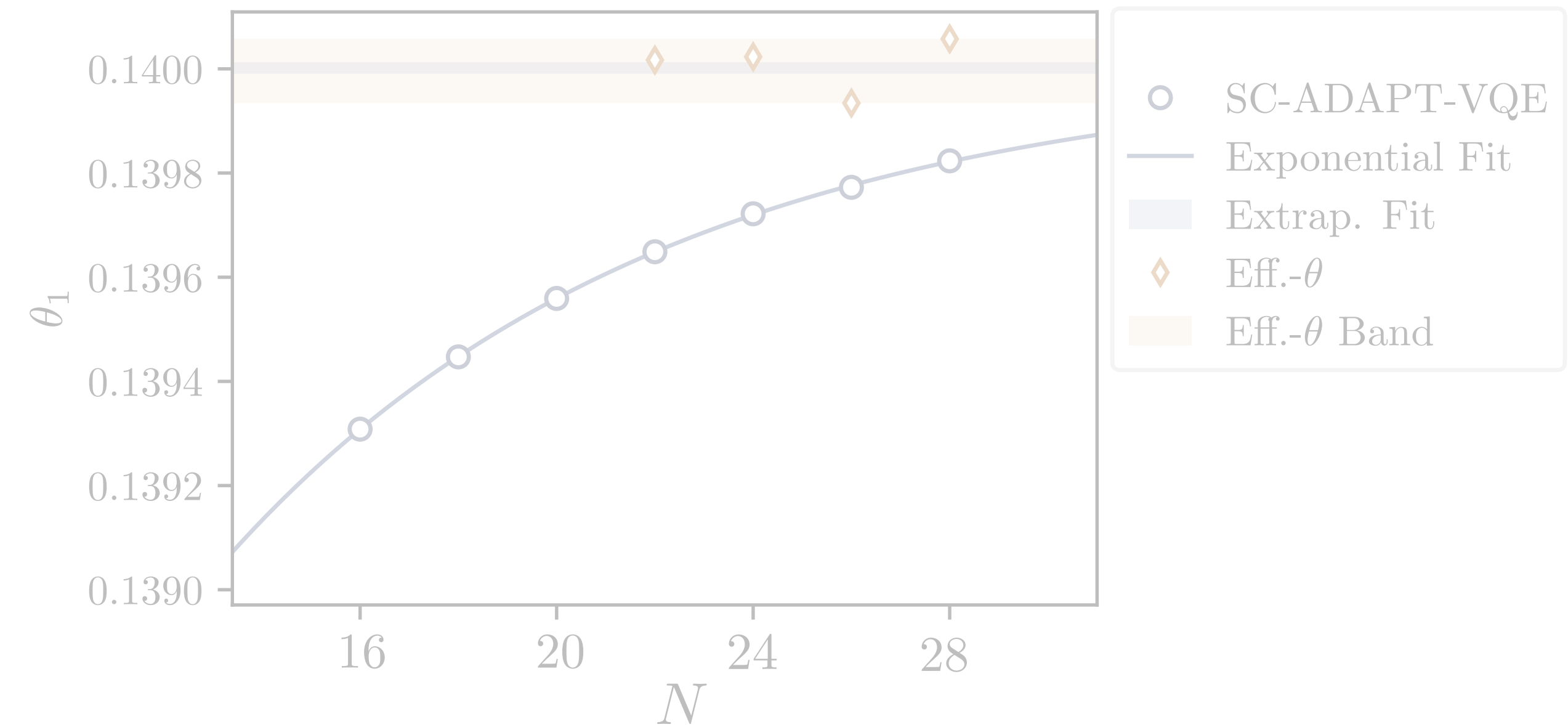
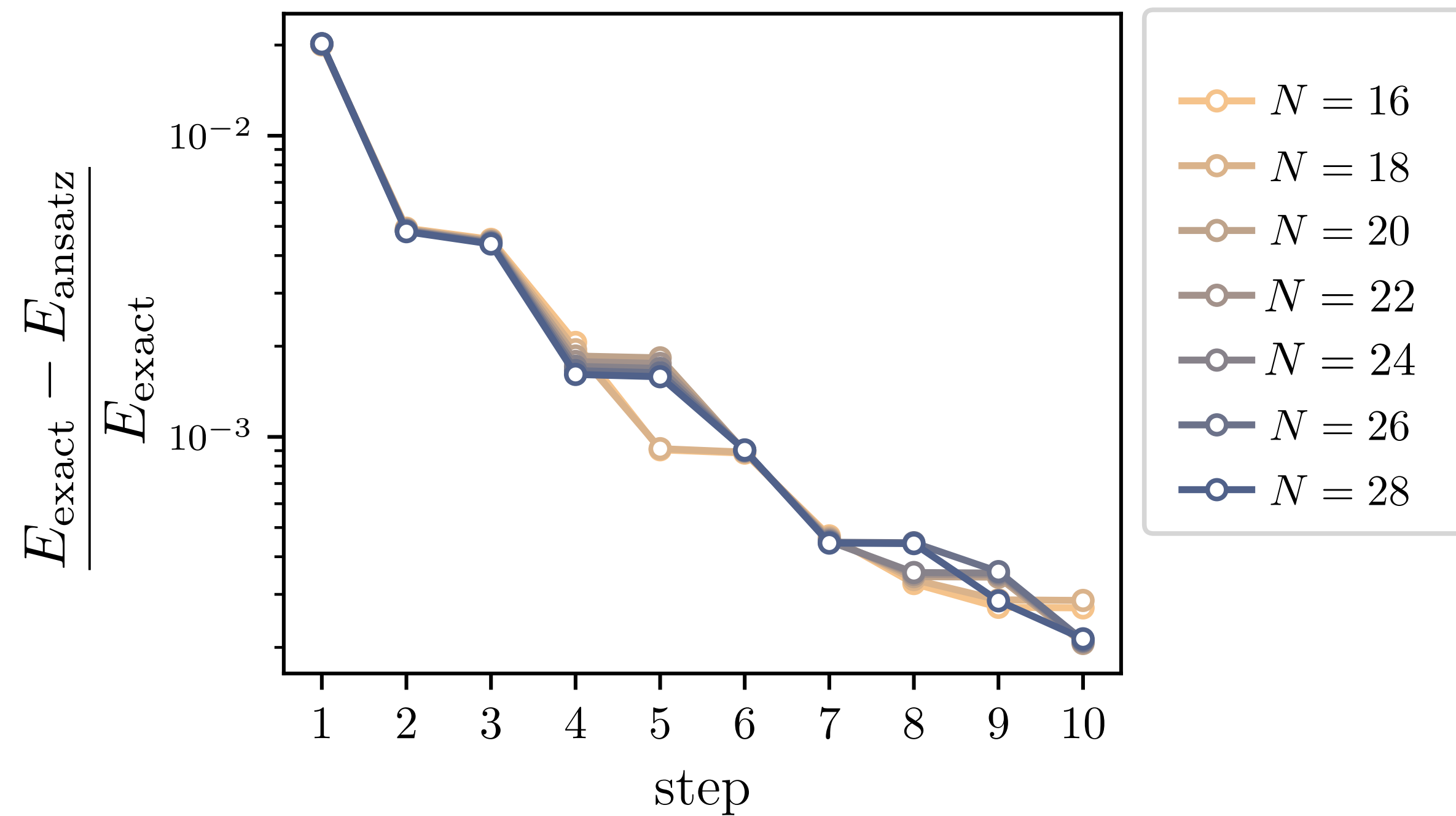


$\theta_i$  and  $\theta_i$  are found by variational minimizing  $E = \langle \hat{H} \rangle$  on classical computers.

Circuits are systematically scaled and executed on a quantum computer

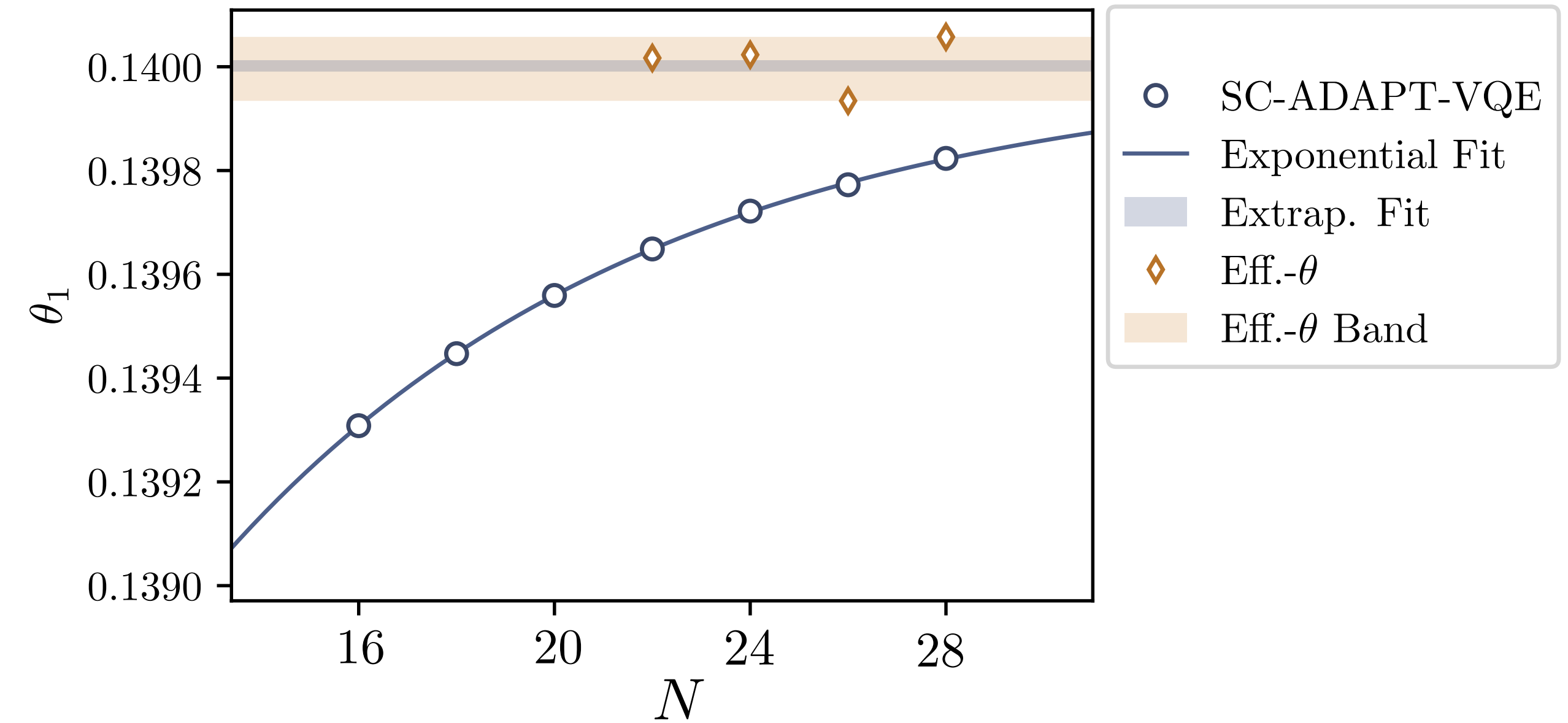
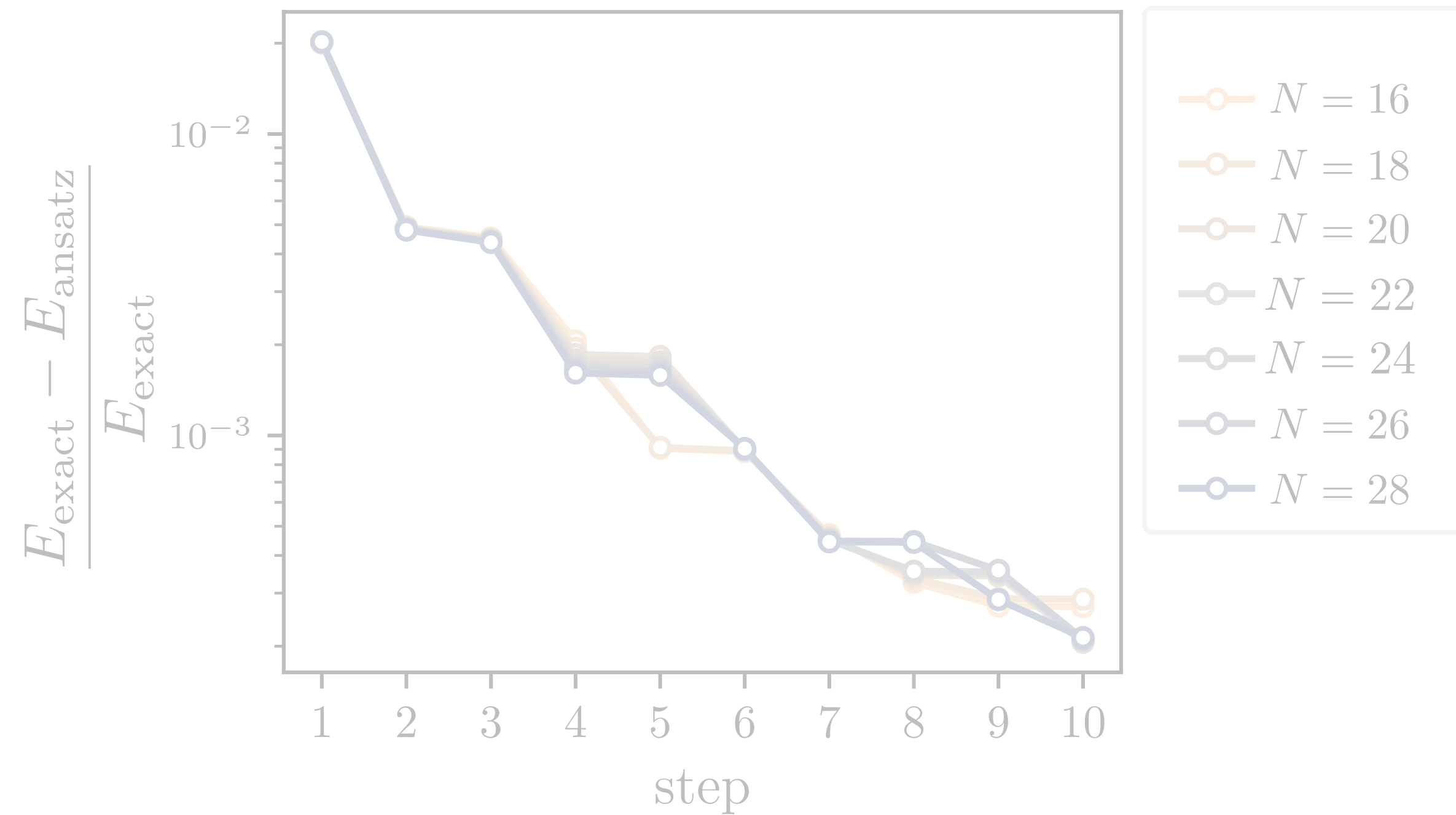


# Vacuum preparation circuits found for $N \leq 28$ using classical computers



Energy converges exponentially as larger correlations are added

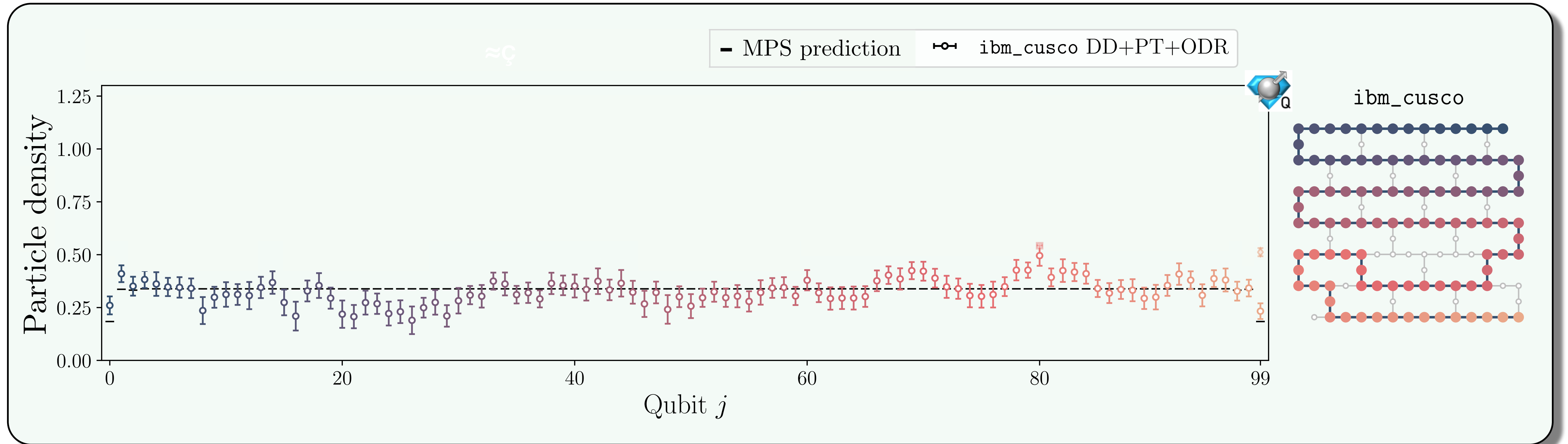
# Vacuum preparation circuits found for $N \leq 28$ using classical computers



Vacuum preparation circuit structure converges exponentially in  $N$



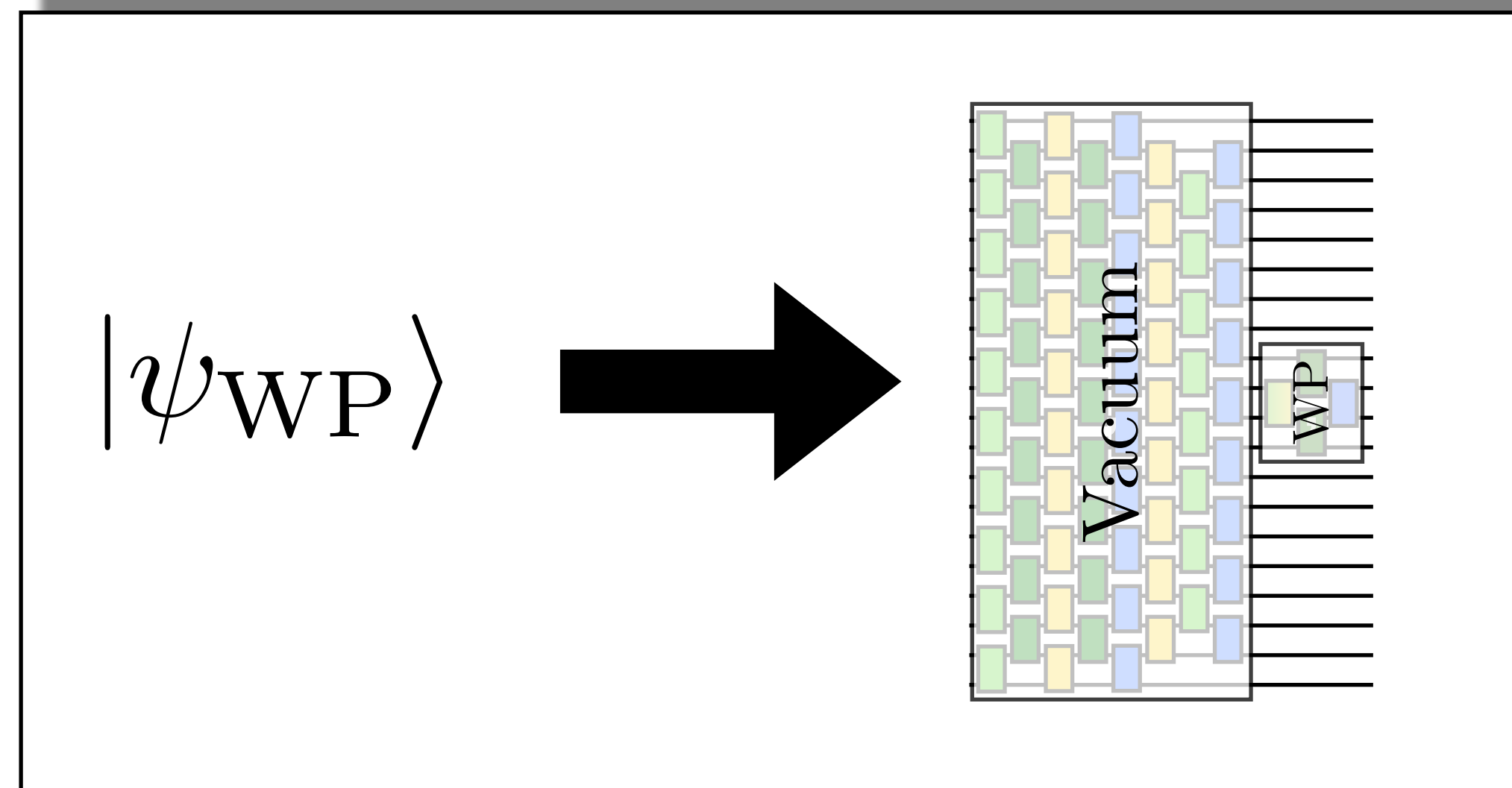
# Results from IBM's quantum computer



Vacuum preparation circuits were scaled to  $N = 100$  and run on `ibm_cusco`

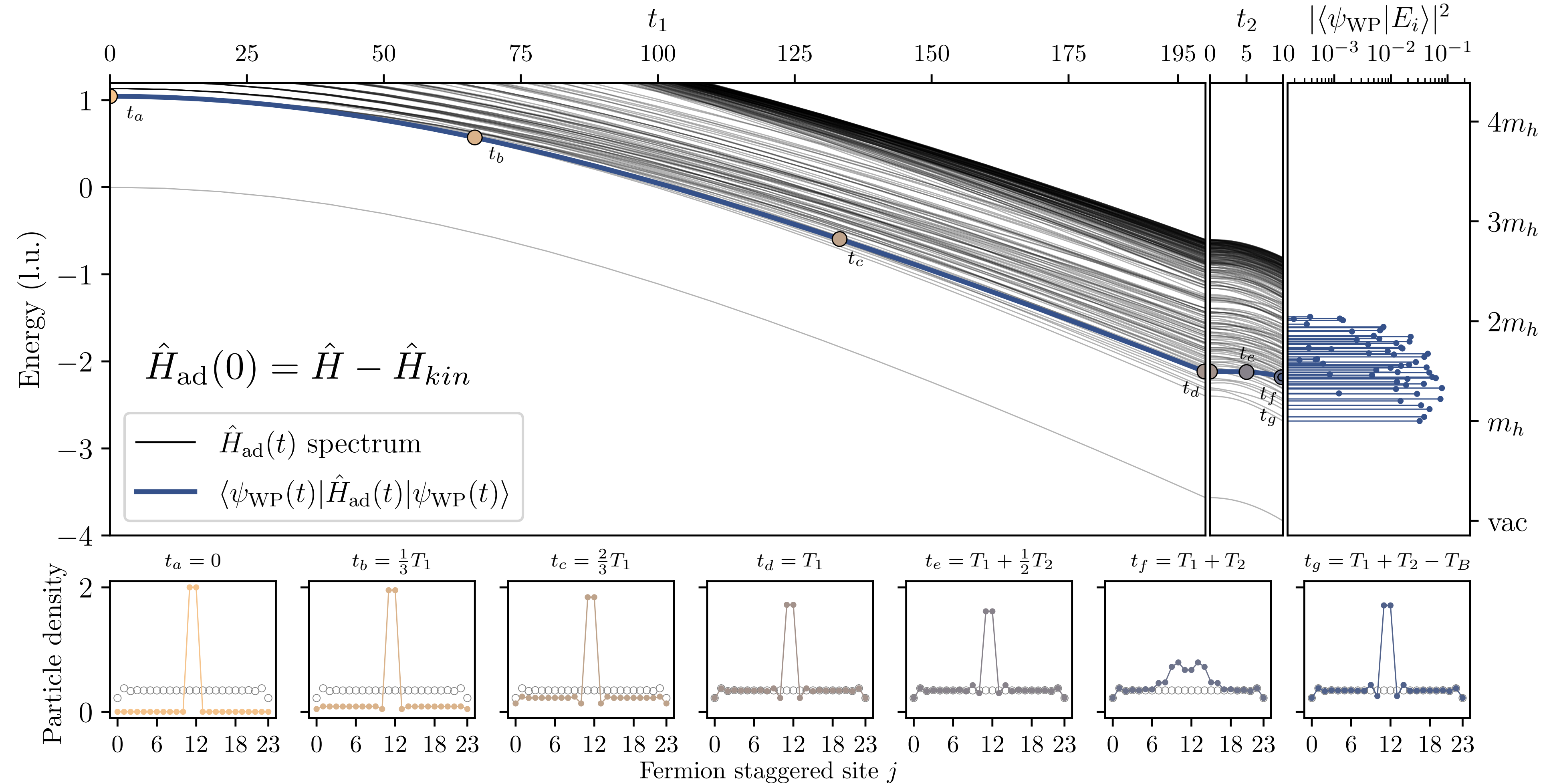
Goal: prepare a hadron wavepacket

1. Prepare the interacting vacuum ✓
2. Excite a hadron wave packet on top of the vacuum



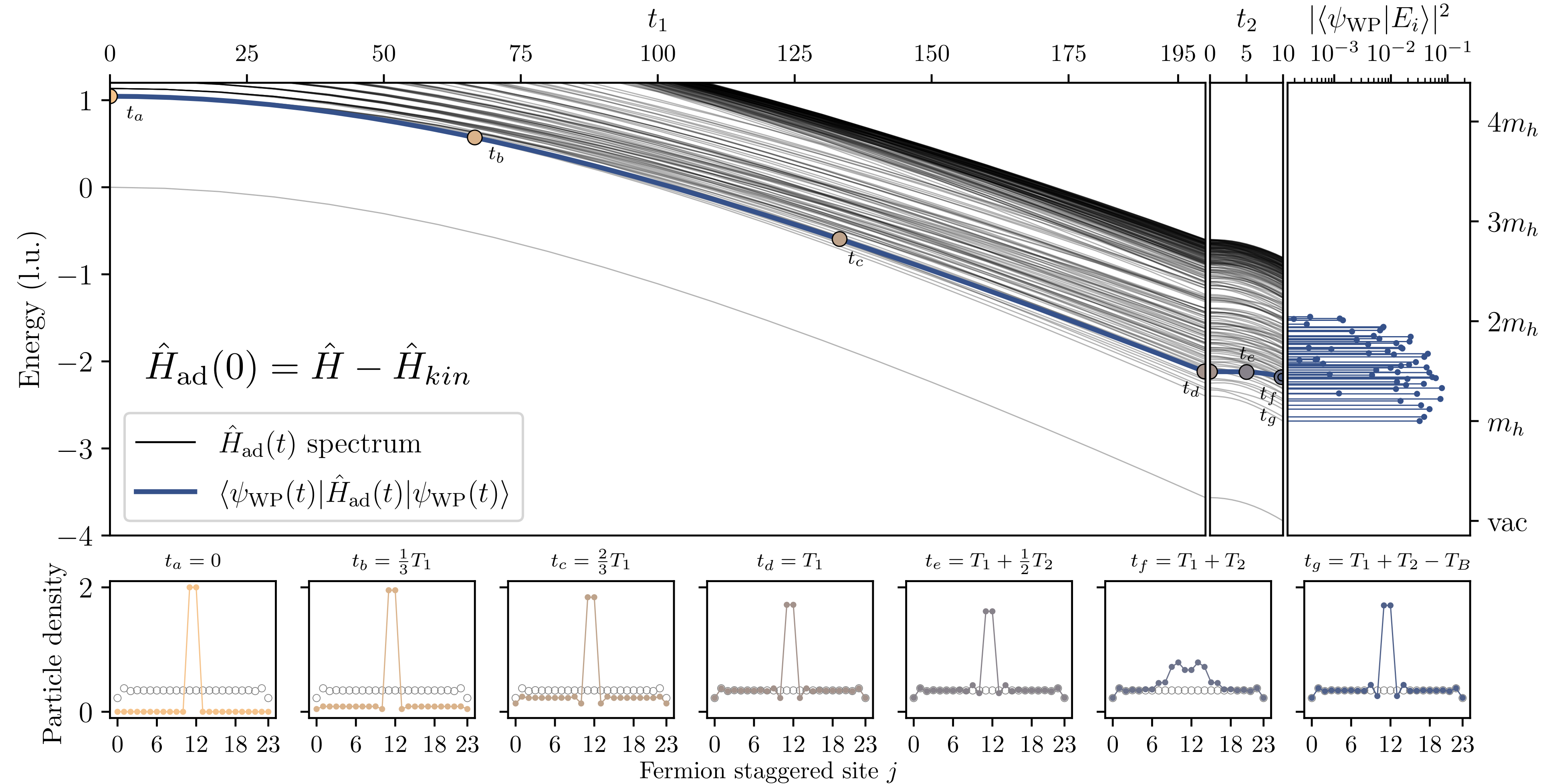


# Adiabatic state preparation



A hadronic wave packet can be prepared by adiabatically turning on  $\hat{H}_{kin}$

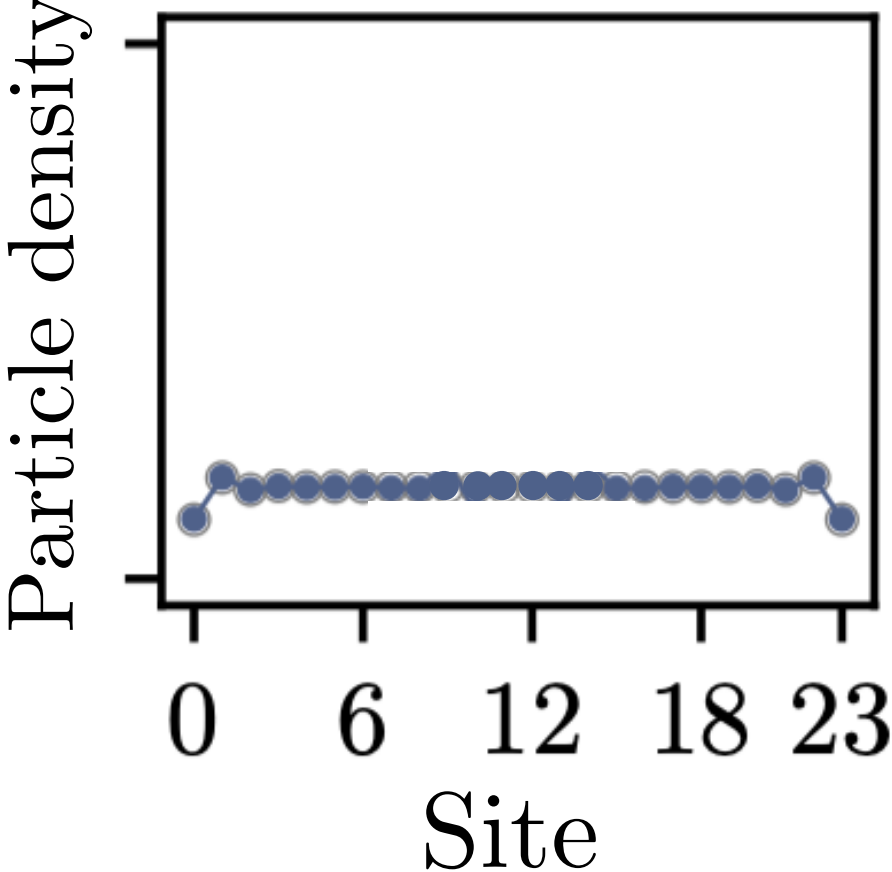
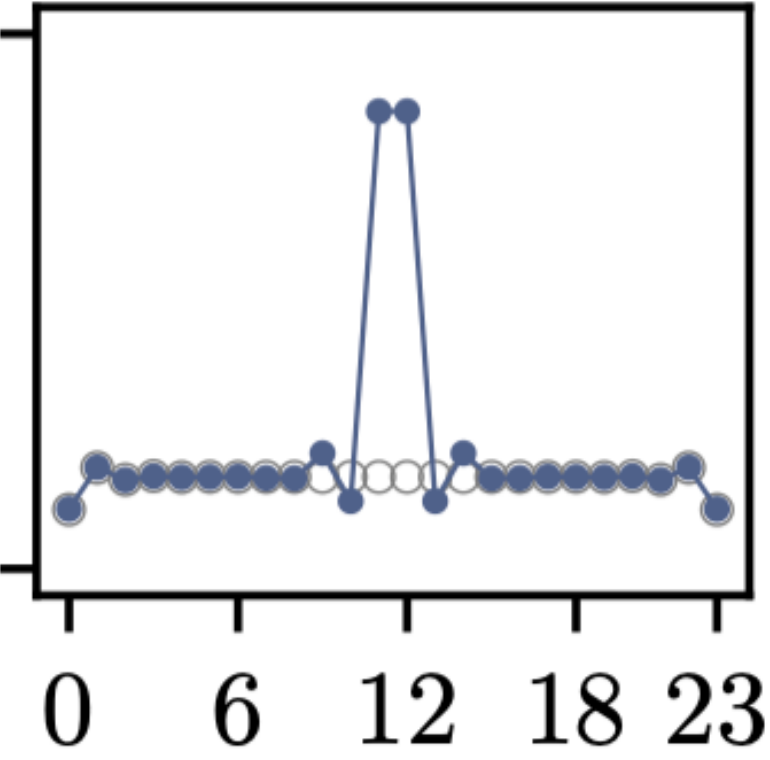
# Adiabatic state preparation



Adiabatic preparation circuits require too many gates: use SC-ADAPT-VQE

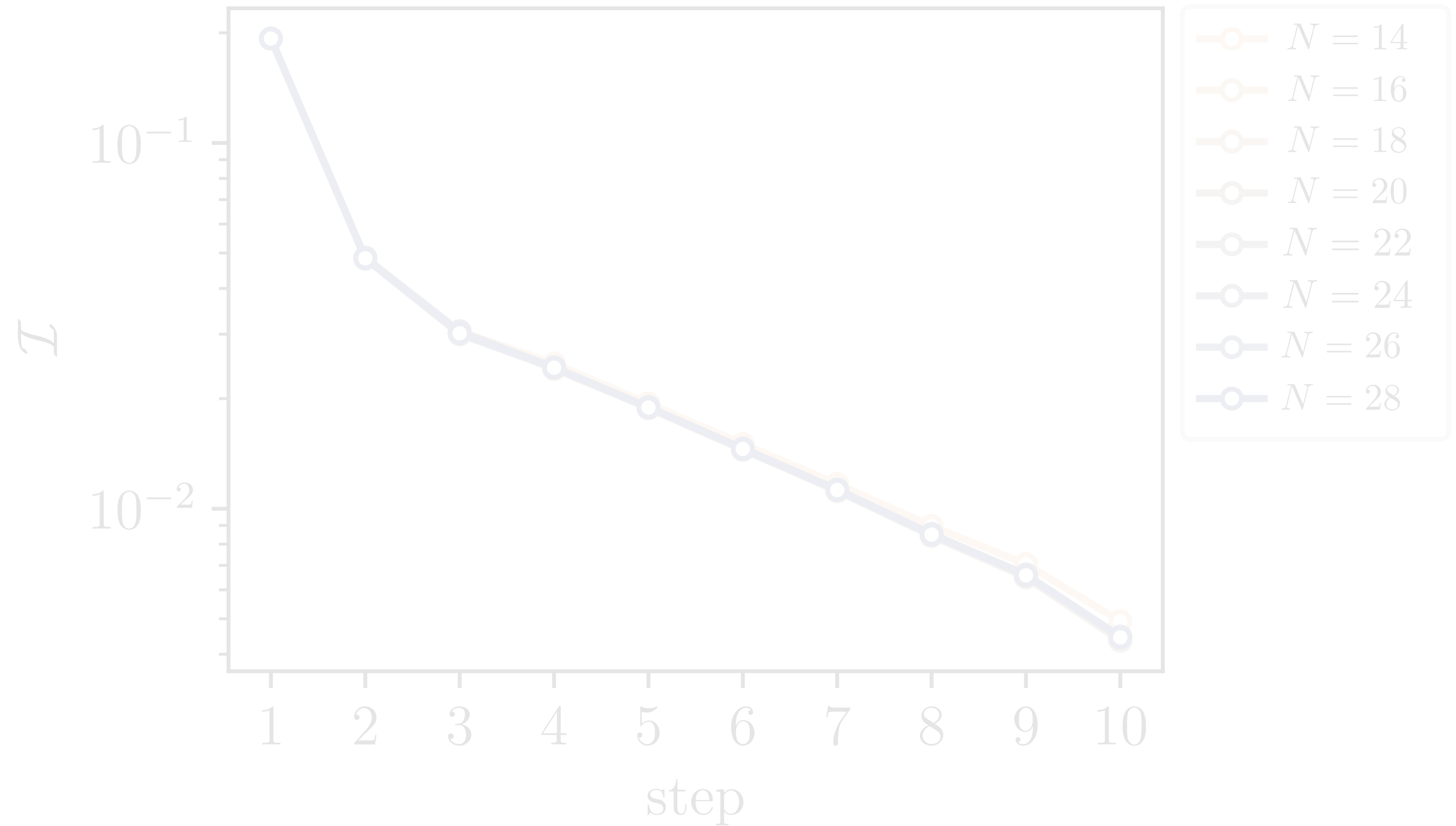
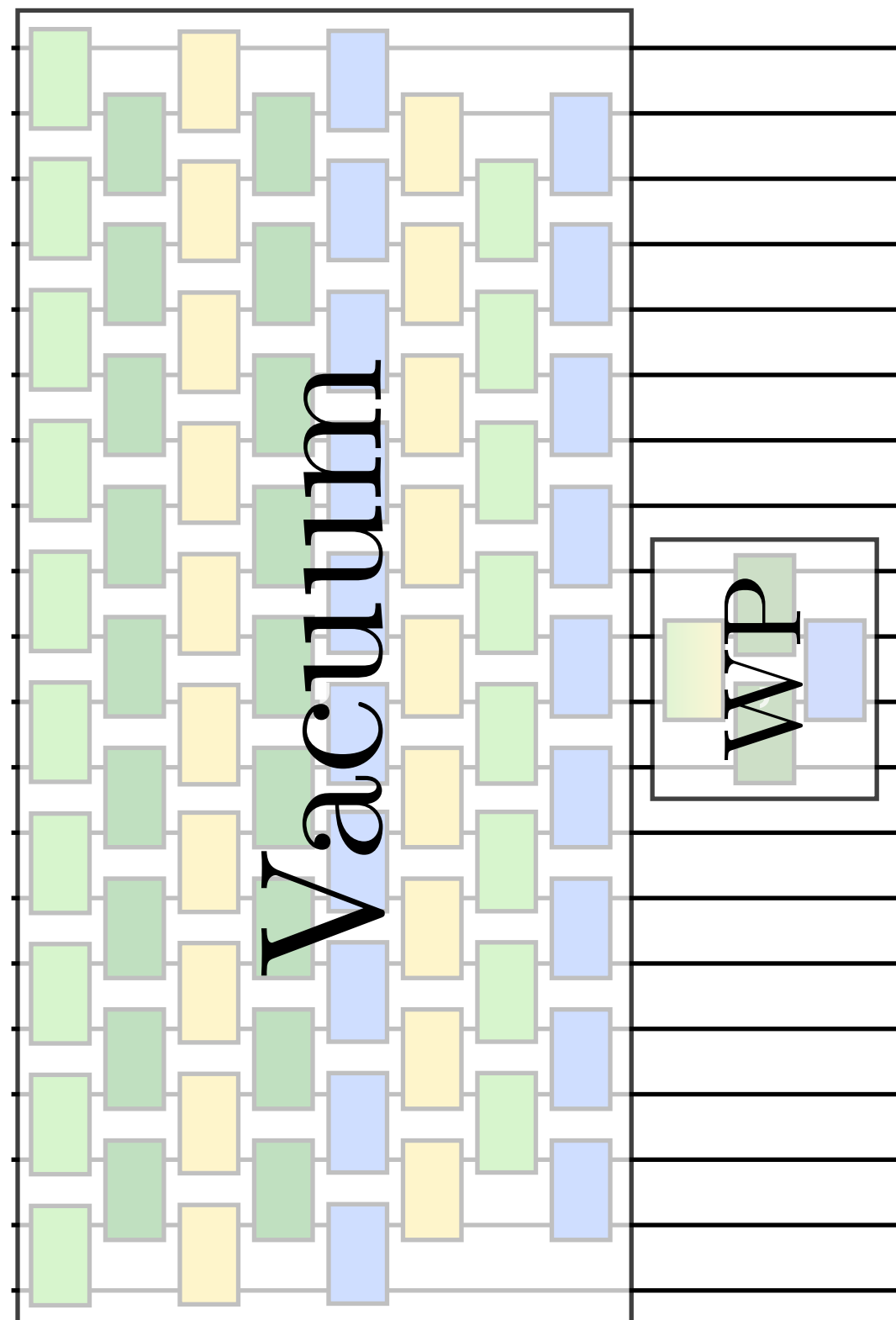


# SC-ADAPT-VQE for preparing hadron wave packets

	Vacuum	Wave packet
Variationally minimize	$E = \langle \psi_{\text{ansatz}}   \hat{H}   \psi_{\text{ansatz}} \rangle$	$\mathcal{I} = 1 -  \langle \psi_{\text{ansatz}}   \psi_{\text{WP}} \rangle ^2$
Scalability	<p>Translational symmetry</p>  <p>Particle density</p> <p>Site</p>	<p>Localized</p>  <p>0 6 12 18 23</p>

Localized circuits maximize overlap with the adiabatically prepared wave packet

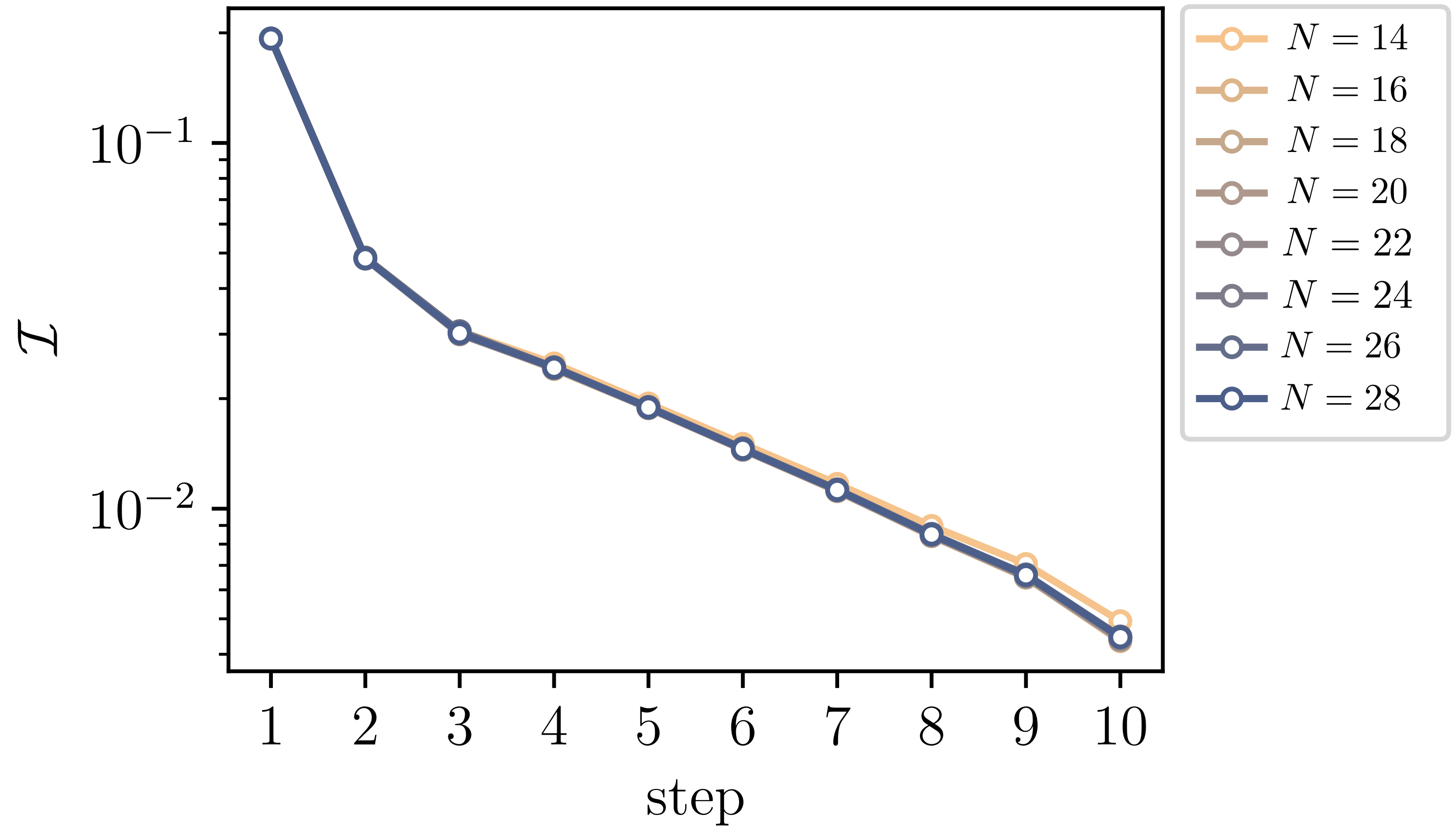
# SC-ADAPT-VQE for preparing hadron wave packets



SC-ADAPT-VQE wave packet is built on top of the vacuum



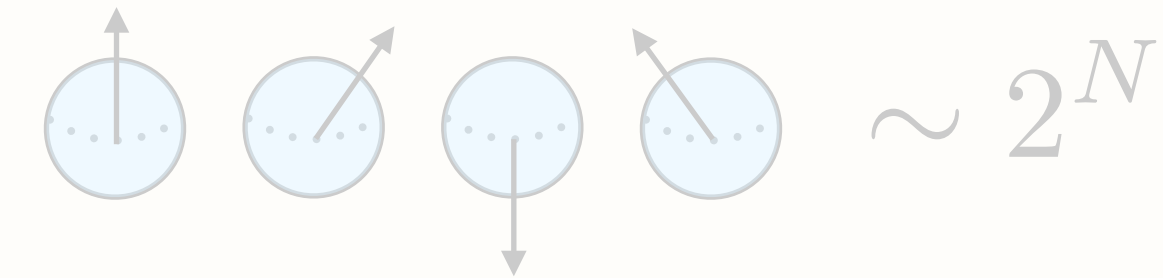
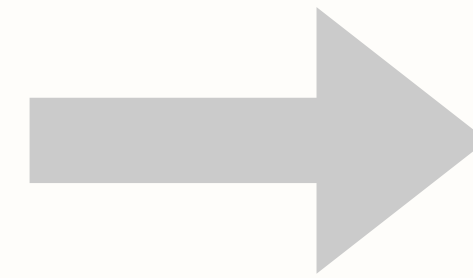
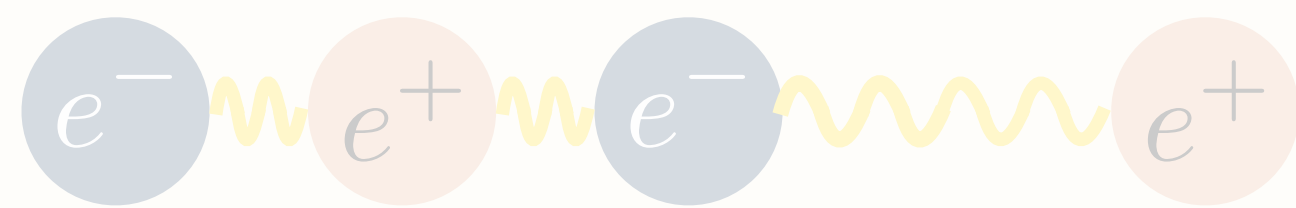
# SC-ADAPT-VQE for preparing hadron wave packets



**Infidelity decreases exponentially as larger correlations are added**

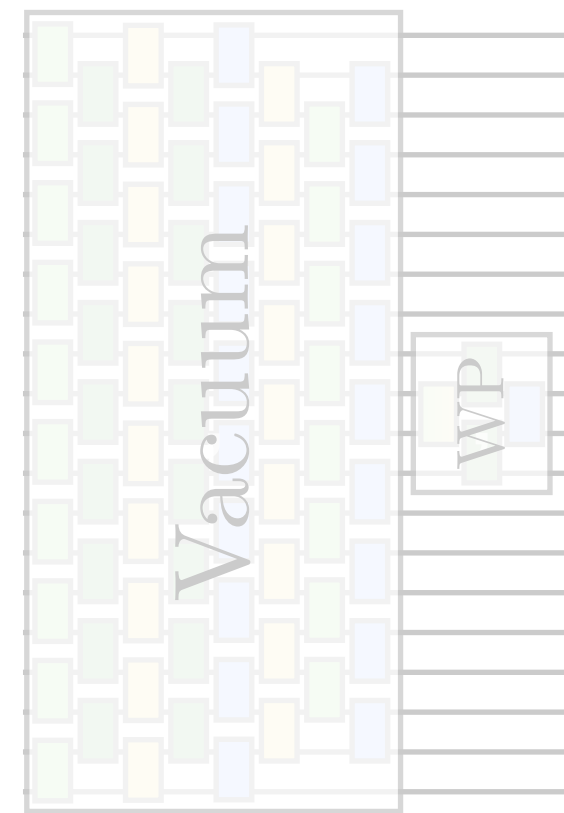
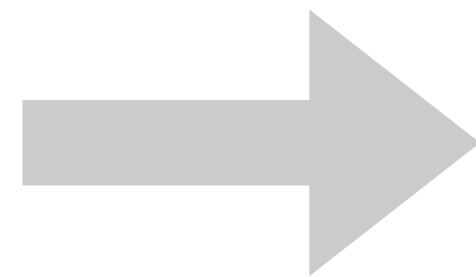
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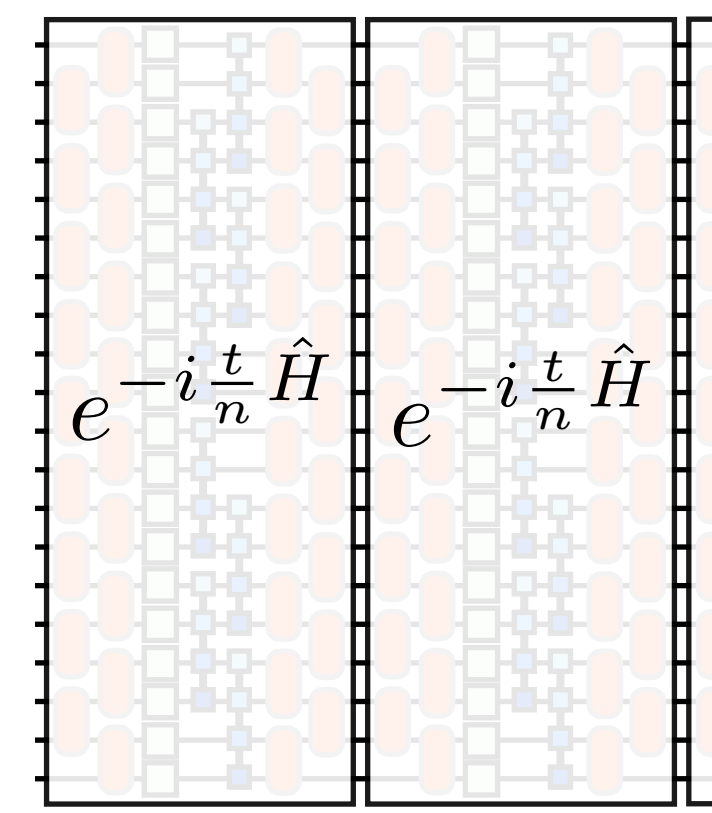
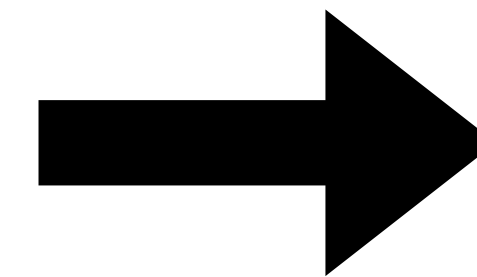
## 1. Prepare the initial state

$$|\psi_{\text{WP}}\rangle$$



## 2. Time evolve

$$e^{-it\hat{H}}$$



# Trotterized time evolution

$$\hat{H} = \underbrace{\frac{m}{2} \sum_{n=0}^{N-1} (-1)^n \hat{Z}_n}_{\hat{H}_m} + \underbrace{\frac{1}{2} \sum_{n=0}^{N-2} (\hat{\sigma}_n^+ \hat{\sigma}_{n+1}^- + \text{h.c.})}_{\hat{H}_{kin}} + \underbrace{\frac{g^2}{2} \sum_{n=0}^{N-2} \left( \sum_{m \leq n} \hat{Q}_m \right)^2}_{\hat{H}_{el}}$$



# Trotterized time evolution

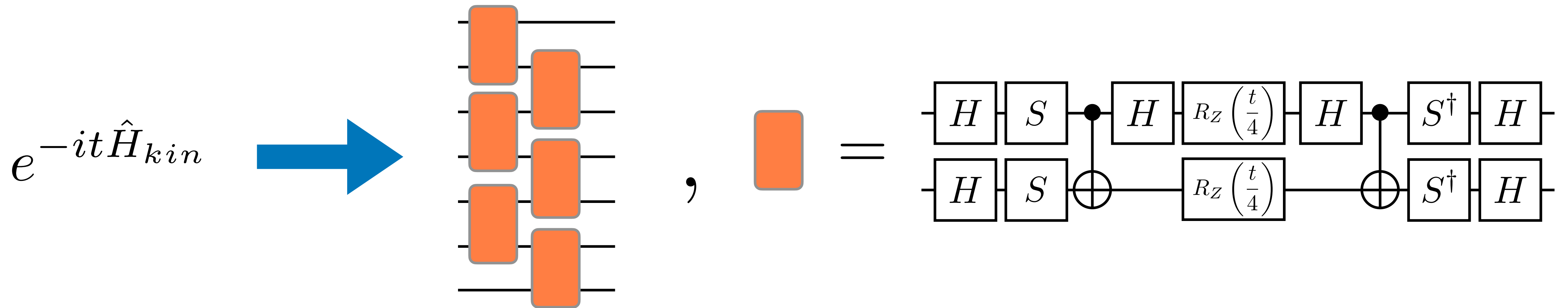
$$\hat{H} = \underbrace{\frac{m}{2} \sum_{n=0}^{N-1} (-1)^n \hat{Z}_n}_{\hat{H}_m} + \underbrace{\frac{1}{2} \sum_{n=0}^{N-2} (\hat{\sigma}_n^+ \hat{\sigma}_{n+1}^- + \text{h.c.})}_{\hat{H}_{kin}} + \underbrace{\frac{g^2}{2} \sum_{n=0}^{N-2} \left( \sum_{m \leq n} \hat{Q}_m \right)^2}_{\hat{H}_{el}}$$

$$e^{-it\hat{H}_m} = \prod_{n=0}^{N-1} e^{-it \frac{m}{2} (-1)^n \hat{Z}_n} \quad \rightarrow \quad \begin{array}{c} \text{---} R_Z(mt) \text{---} \\ \text{---} R_Z(-mt) \text{---} \\ \text{---} R_Z(mt) \text{---} \\ \text{---} R_Z(-mt) \text{---} \end{array}$$

$e^{-it\hat{H}_m}$  requires only single-qubit gates

# Trotterized time evolution

$$\hat{H} = \underbrace{\frac{m}{2} \sum_{n=0}^{N-1} (-1)^n \hat{Z}_n}_{\hat{H}_m} + \underbrace{\frac{1}{2} \sum_{n=0}^{N-2} (\hat{\sigma}_n^+ \hat{\sigma}_{n+1}^- + \text{h.c.})}_{\hat{H}_{kin}} + \underbrace{\frac{g^2}{2} \sum_{n=0}^{N-2} \left( \sum_{m \leq n} \hat{Q}_m \right)^2}_{\hat{H}_{el}}$$



$e^{-it\hat{H}_{kin}}$  requires  $N - 2$  two-qubit gates

## Trotterized time evolution

$$\hat{H} = \underbrace{\frac{m}{2} \sum_{n=0}^{N-1} (-1)^n \hat{Z}_n}_{\hat{H}_m} + \underbrace{\frac{1}{2} \sum_{n=0}^{N-2} (\hat{\sigma}_n^+ \hat{\sigma}_{n+1}^- + \text{h.c.})}_{\hat{H}_{kin}} + \underbrace{\frac{g^2}{2} \sum_{n=0}^{N-2} \left[ \sum_{m \leq n} (\hat{Z}_m + (-1)^m \hat{I}) \right]^2}_{\hat{H}_{el}}$$

$\hat{H}_{el}$  has  $\hat{Z}\hat{Z}$  between all pairs of qubits:  $\mathcal{O}(N^2)$  two-qubit gates

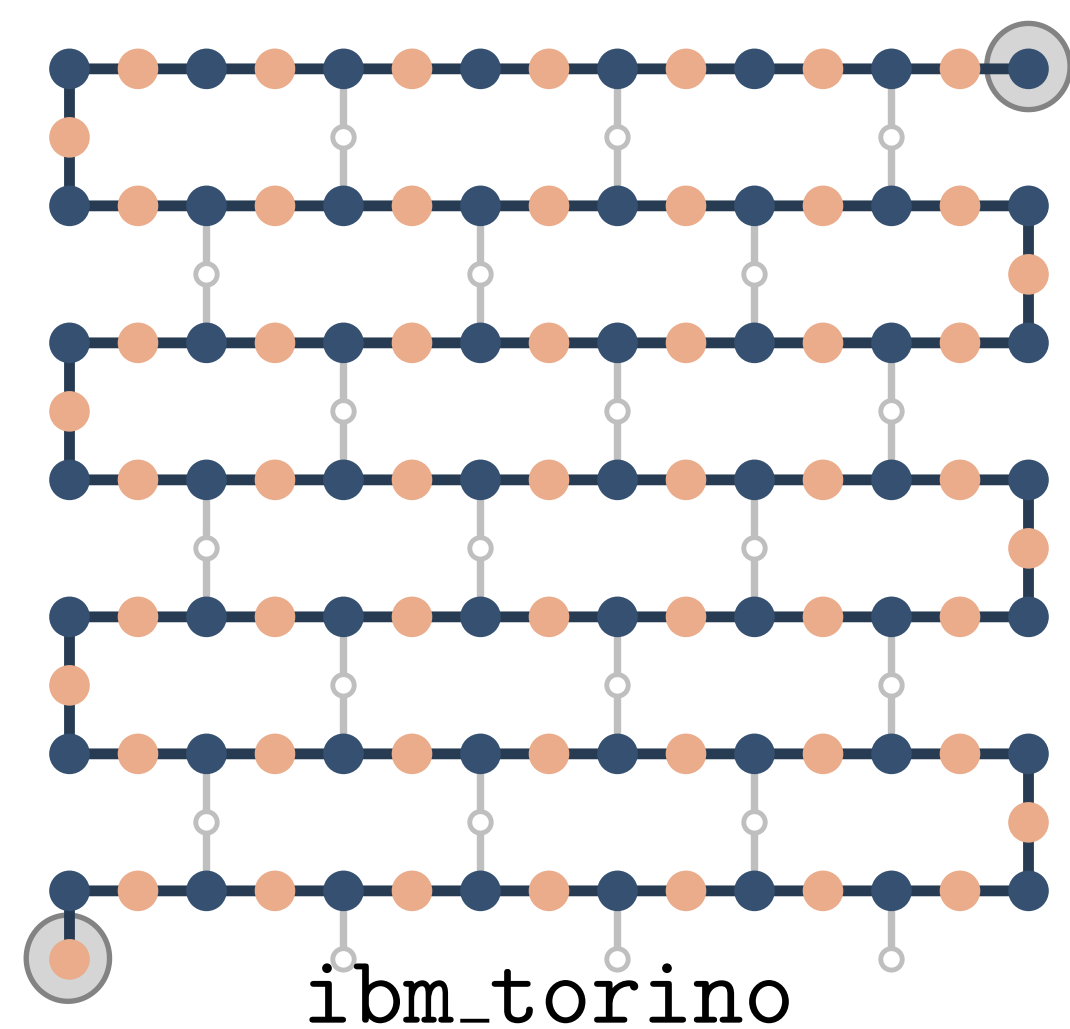




# Trotterized time evolution

$$\hat{H} = \underbrace{\frac{m}{2} \sum_{n=0}^{N-1} (-1)^n \hat{Z}_n}_{\hat{H}_m} + \underbrace{\frac{1}{2} \sum_{n=0}^{N-2} (\hat{\sigma}_n^+ \hat{\sigma}_{n+1}^- + \text{h.c.})}_{\hat{H}_{kin}} + \underbrace{\frac{g^2}{2} \sum_{n=0}^{N-2} \left[ \sum_{m \leq n} (\hat{Z}_m + (-1)^m \hat{I}) \right]^2}_{\hat{H}_{el}}$$

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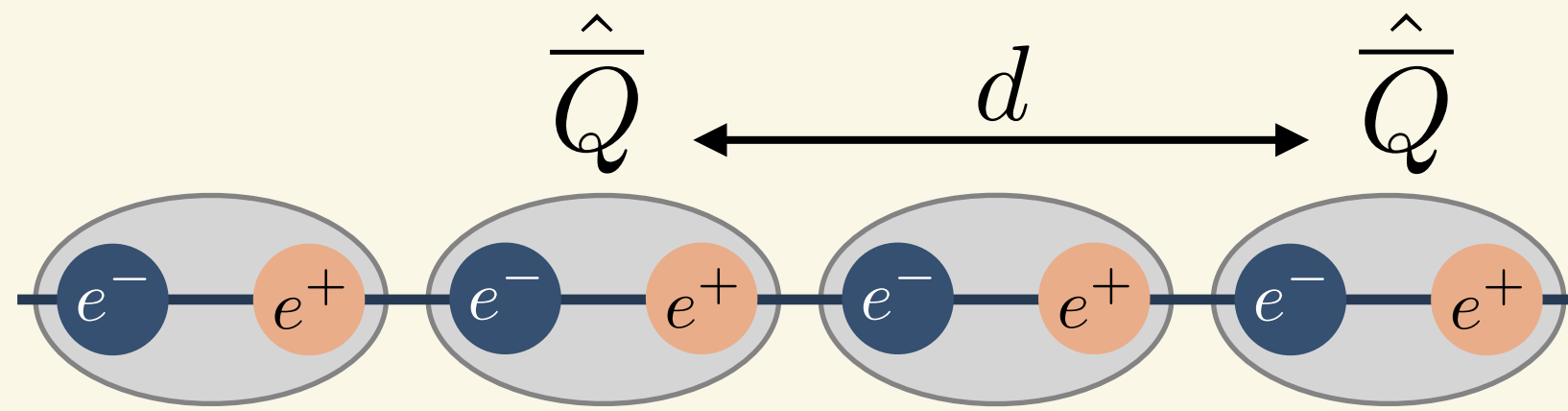


Overhead for long-range gates:

$\mathcal{O}(N^2)$  circuit depth

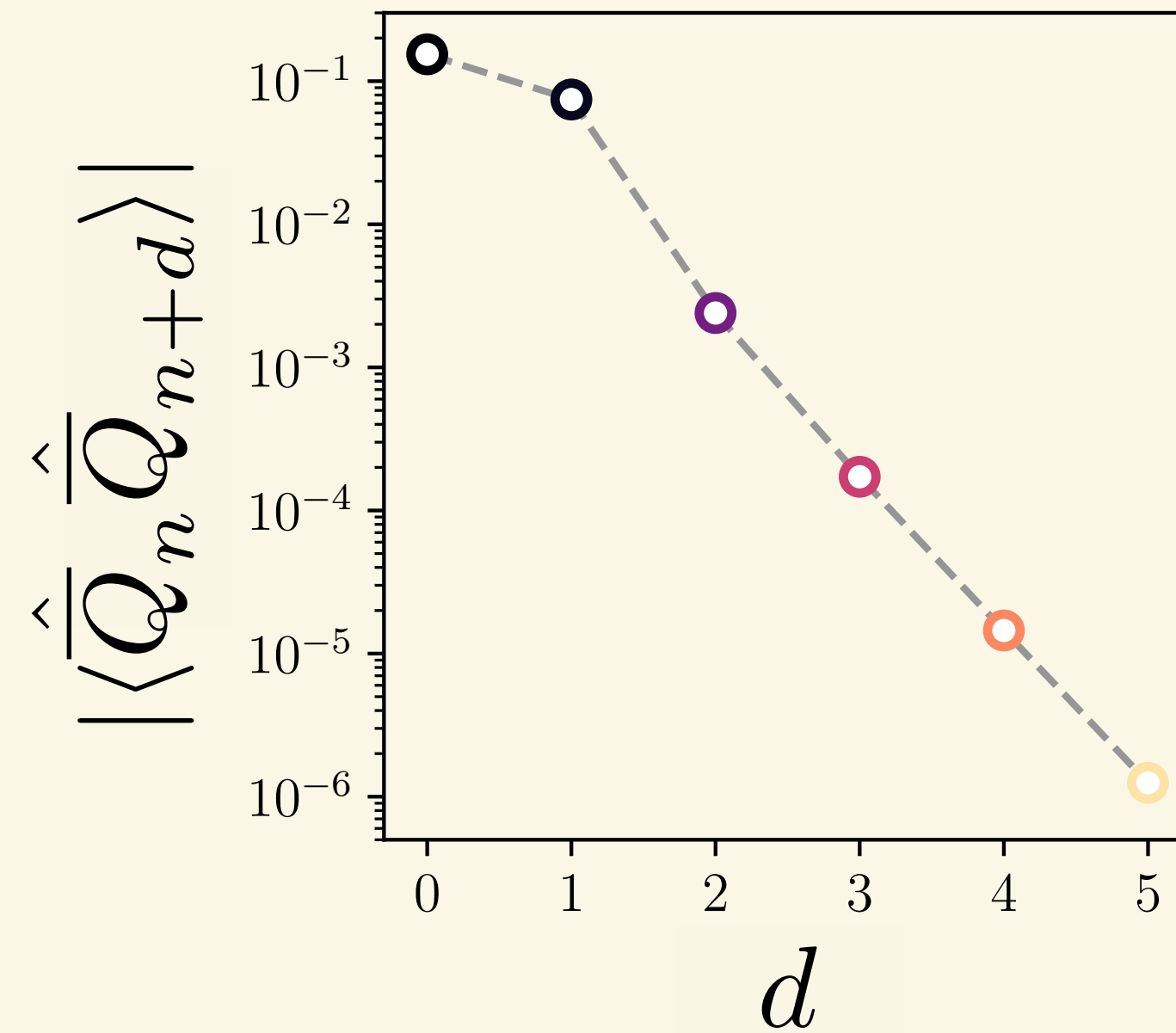
# Effective electric interaction

Confinement screens charges; interaction effectively short-ranged



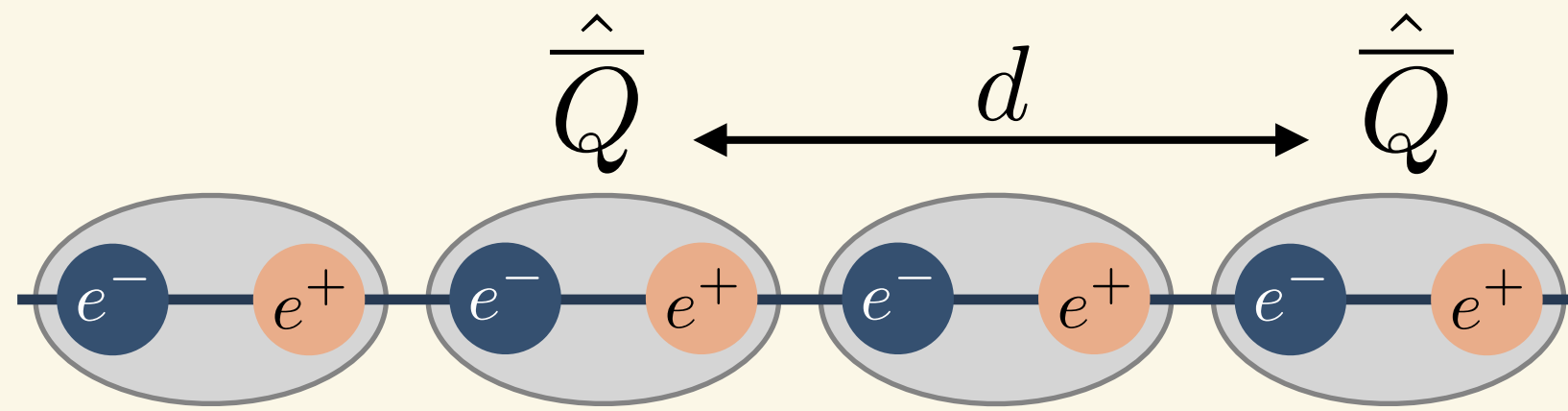
$$\hat{Q}_n = \hat{Q}_{2n} + \hat{Q}_{2n+1}$$

$$\hat{\delta}_n = \hat{Q}_{2n} - \hat{Q}_{2n+1}$$



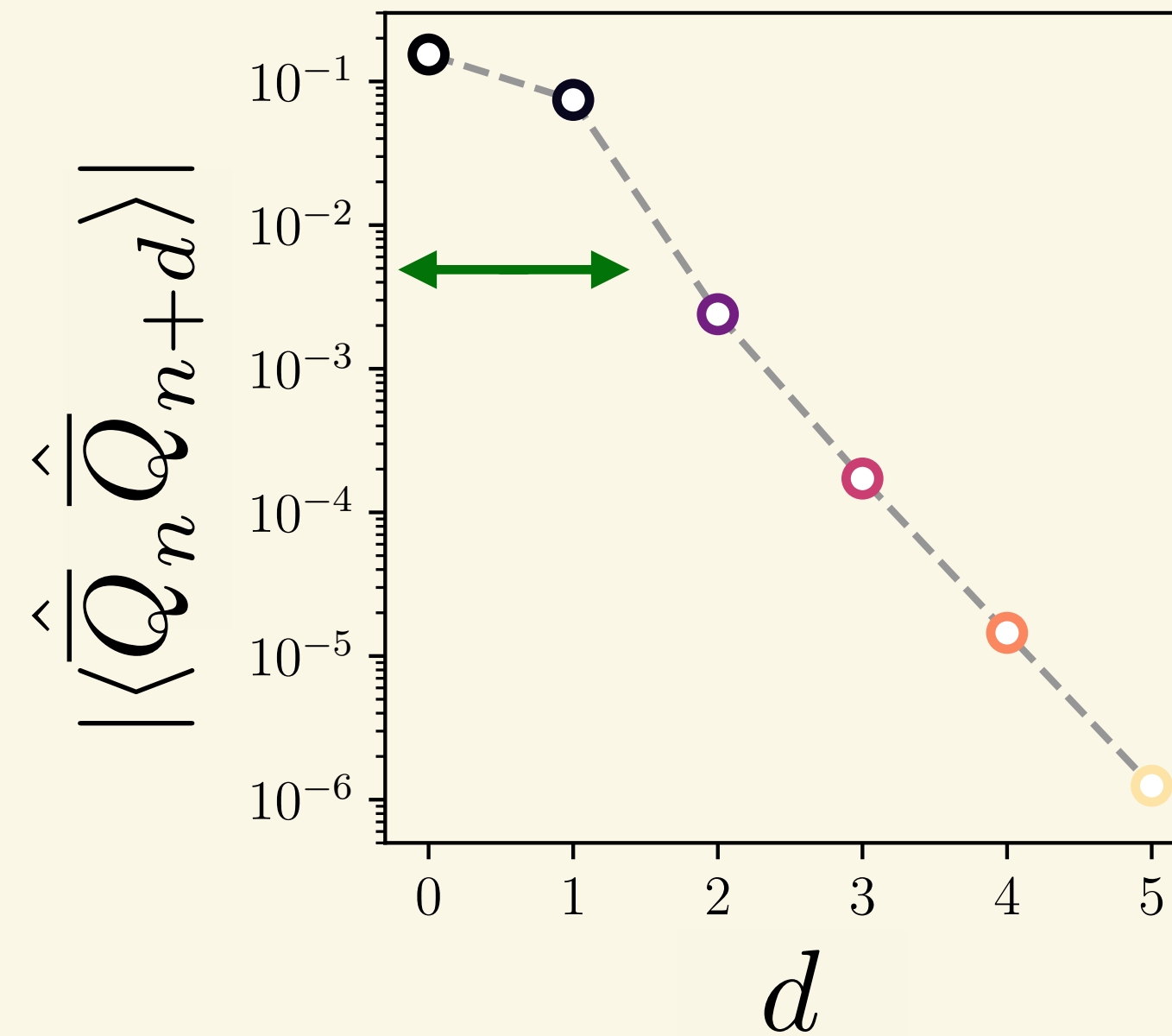
# Effective electric interaction

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$$\hat{Q}_n = \hat{Q}_{2n} + \hat{Q}_{2n+1}$$

$$\hat{\delta}_n = \hat{Q}_{2n} - \hat{Q}_{2n+1}$$



Truncate interactions beyond the confinement length  $\sim m_{\text{hadron}}^{-1}$

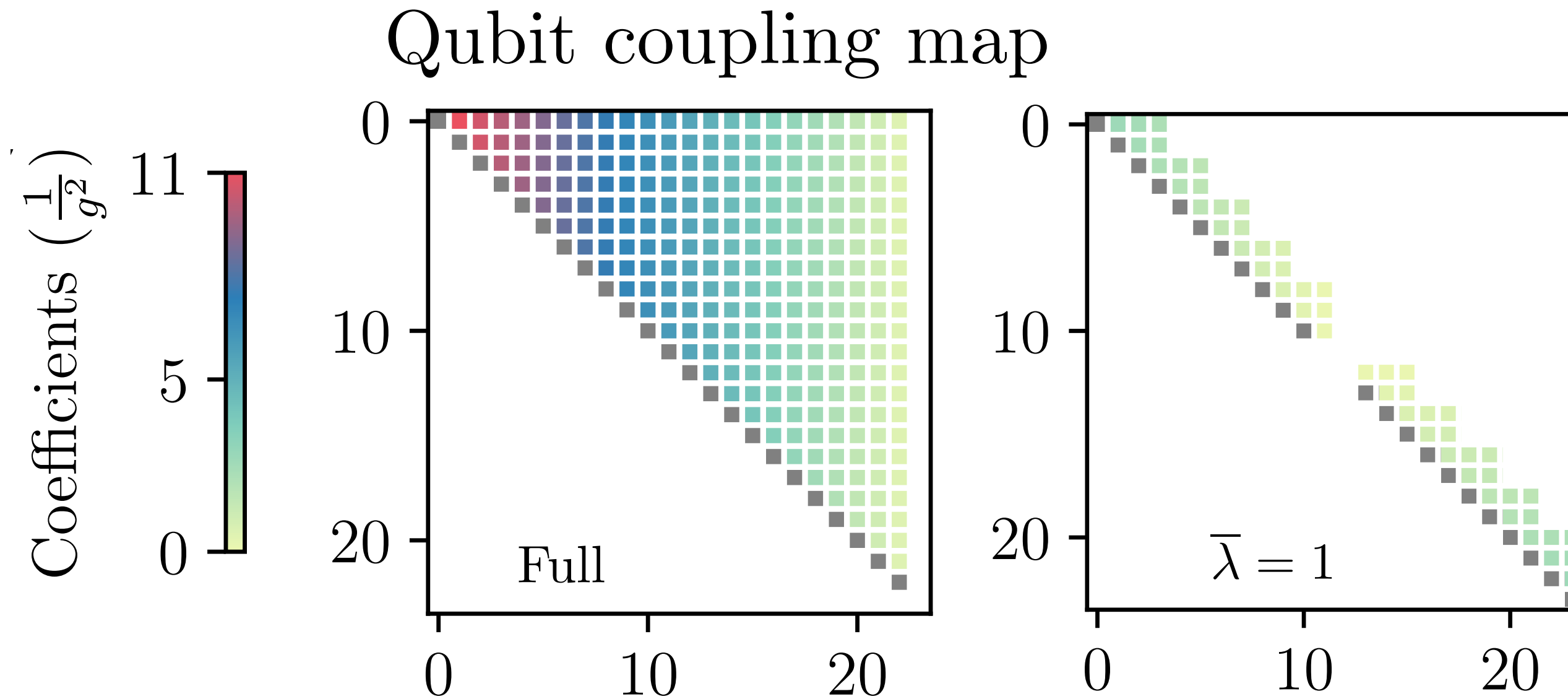


## Truncating the interaction beyond $\bar{\lambda}$ spatial sites

$$\hat{H}_{el}(\bar{\lambda}) = \frac{g^2}{2} \left\{ \sum_{n=0}^{\frac{N}{4}-1} \left[ \left( \frac{N}{2} - \frac{5}{4} - 2n \right) \hat{Q}_n^2 + \frac{1}{2} \hat{Q}_n \hat{\delta}_n + \frac{1}{4} \hat{\delta}_n^2 + \left( \frac{3}{4} + 2n \right) \hat{Q}_{\frac{N}{4}+n}^2 - \frac{1}{2} \hat{Q}_{\frac{N}{4}+n} \hat{\delta}_{\frac{N}{4}+n} + \frac{1}{4} \hat{\delta}_{\frac{N}{4}+n}^2 \right] \right. \\ \left. + 2 \sum_{n=0}^{\frac{N}{4}-2} \sum_{m=n+1}^{\min(\frac{N}{4}-1, n+\bar{\lambda})} \left[ \left( \frac{N}{2} - 1 - 2m \right) \hat{Q}_n \hat{Q}_m + \frac{1}{2} \hat{Q}_n \hat{\delta}_m + (1 + 2n) \hat{Q}_{\frac{N}{4}+n} \hat{Q}_{\frac{N}{4}+m} - \frac{1}{2} \hat{Q}_{\frac{N}{4}+m} \hat{\delta}_{\frac{N}{4}+n} \right] \right\}$$

# Truncating the interaction beyond $\bar{\lambda}$ spatial sites

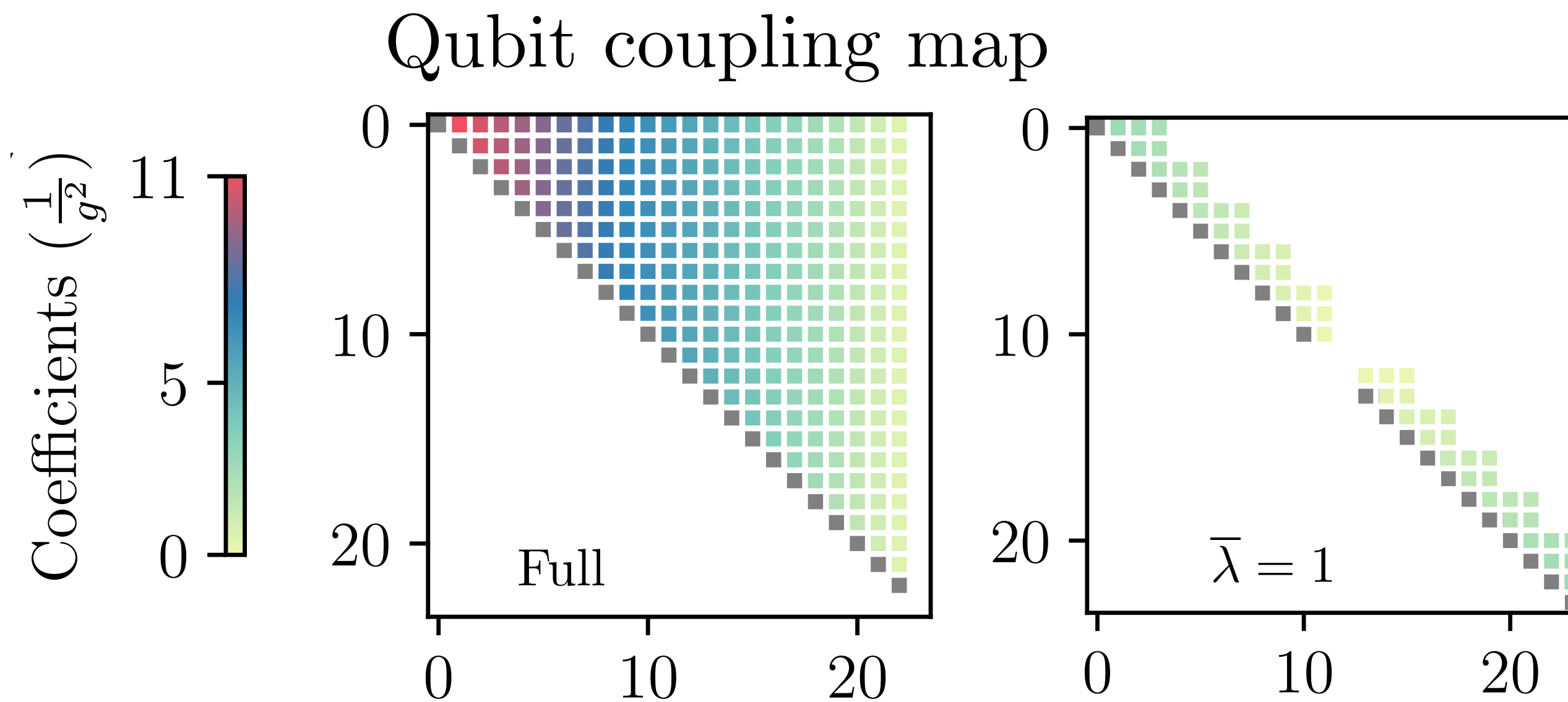
$$\hat{H}_{el}(\bar{\lambda}) = \frac{g^2}{2} \left\{ \sum_{n=0}^{\frac{N}{4}-1} \left[ \left( \frac{N}{2} - \frac{5}{4} - 2n \right) \hat{Q}_n^2 + \frac{1}{2} \hat{Q}_n \hat{\delta}_n + \frac{1}{4} \hat{\delta}_n^2 + \left( \frac{3}{4} + 2n \right) \hat{Q}_{\frac{N}{4}+n}^2 - \frac{1}{2} \hat{Q}_{\frac{N}{4}+n} \hat{\delta}_{\frac{N}{4}+n} + \frac{1}{4} \hat{\delta}_{\frac{N}{4}+n}^2 \right] \right. \\ \left. + 2 \sum_{n=0}^{\frac{N}{4}-2} \sum_{m=n+1}^{\min(\frac{N}{4}-1, n+\bar{\lambda})} \left[ \left( \frac{N}{2} - 1 - 2m \right) \hat{Q}_n \hat{Q}_m + \frac{1}{2} \hat{Q}_n \hat{\delta}_m + (1 + 2n) \hat{Q}_{\frac{N}{4}+n} \hat{Q}_{\frac{N}{4}+m} - \frac{1}{2} \hat{Q}_{\frac{N}{4}+m} \hat{\delta}_{\frac{N}{4}+n} \right] \right\}$$



$e^{-it\hat{H}_{el}(\bar{\lambda})}$  requires  $\mathcal{O}(\bar{\lambda}N)$  two-qubit gates

# Truncating the interaction beyond $\bar{\lambda}$ spatial sites

$$\hat{H}_{el}(\bar{\lambda}) = \frac{g^2}{2} \left\{ \sum_{n=0}^{\frac{N}{4}-1} \left[ \left( \frac{N}{2} - \frac{5}{4} - 2n \right) \hat{Q}_n^2 + \frac{1}{2} \hat{Q}_n \hat{\delta}_n + \frac{1}{4} \hat{\delta}_n^2 + \left( \frac{3}{4} + 2n \right) \hat{Q}_{\frac{N}{4}+n}^2 - \frac{1}{2} \hat{Q}_{\frac{N}{4}+n} \hat{\delta}_{\frac{N}{4}+n} + \frac{1}{4} \hat{\delta}_{\frac{N}{4}+n}^2 \right] \right. \\ \left. + 2 \sum_{n=0}^{\frac{N}{4}-2} \sum_{m=n+1}^{\min(\frac{N}{4}-1, n+\bar{\lambda})} \left[ \left( \frac{N}{2} - 1 - 2m \right) \hat{Q}_n \hat{Q}_m + \frac{1}{2} \hat{Q}_n \hat{\delta}_m + (1 + 2n) \hat{Q}_{\frac{N}{4}+n} \hat{Q}_{\frac{N}{4}+m} - \frac{1}{2} \hat{Q}_{\frac{N}{4}+m} \hat{\delta}_{\frac{N}{4}+n} \right] \right\}$$

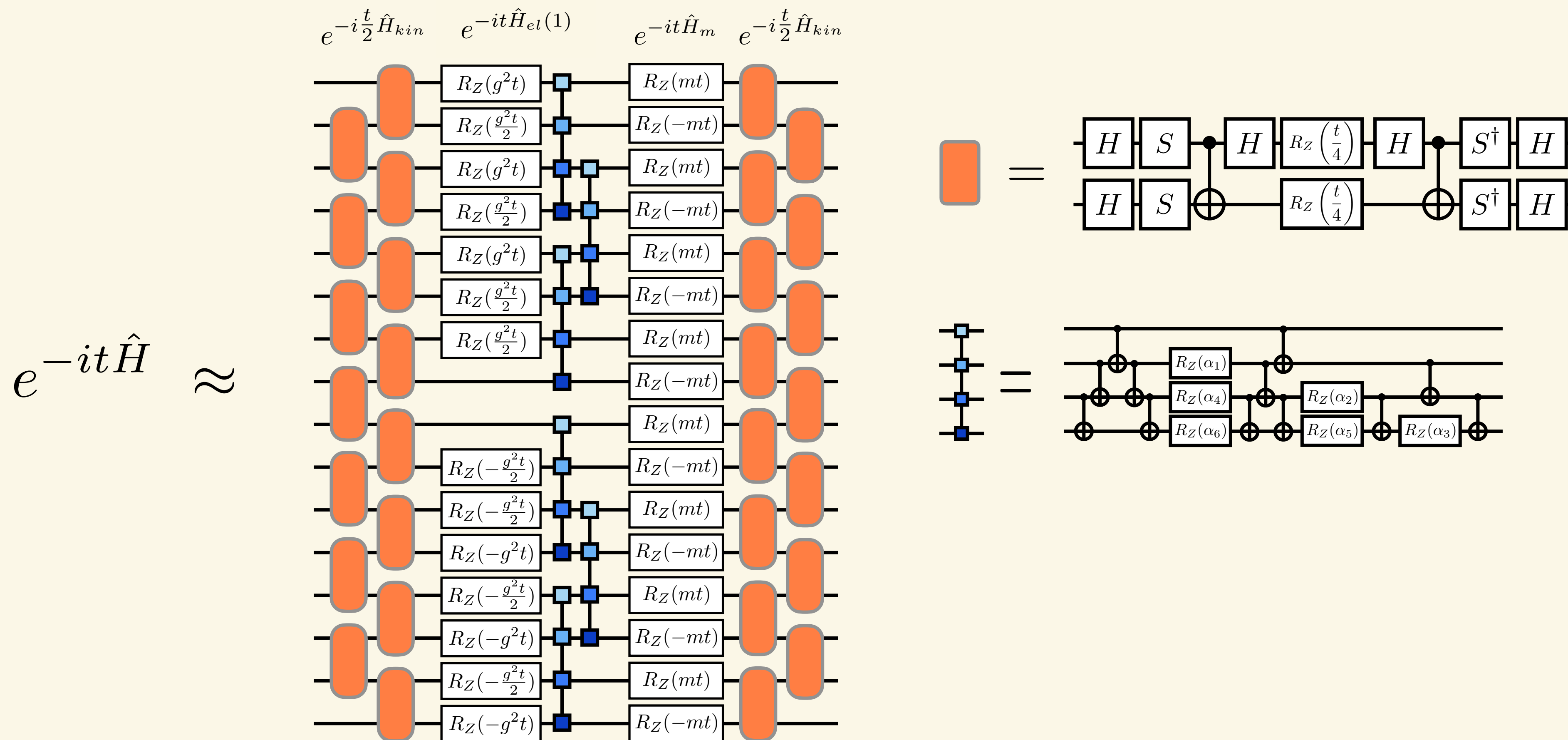


$\bar{\lambda} = 1$  will be used

$e^{-it\hat{H}_{el}(\bar{\lambda})}$  requires  $\mathcal{O}(\bar{\lambda}N)$  two-qubit gates

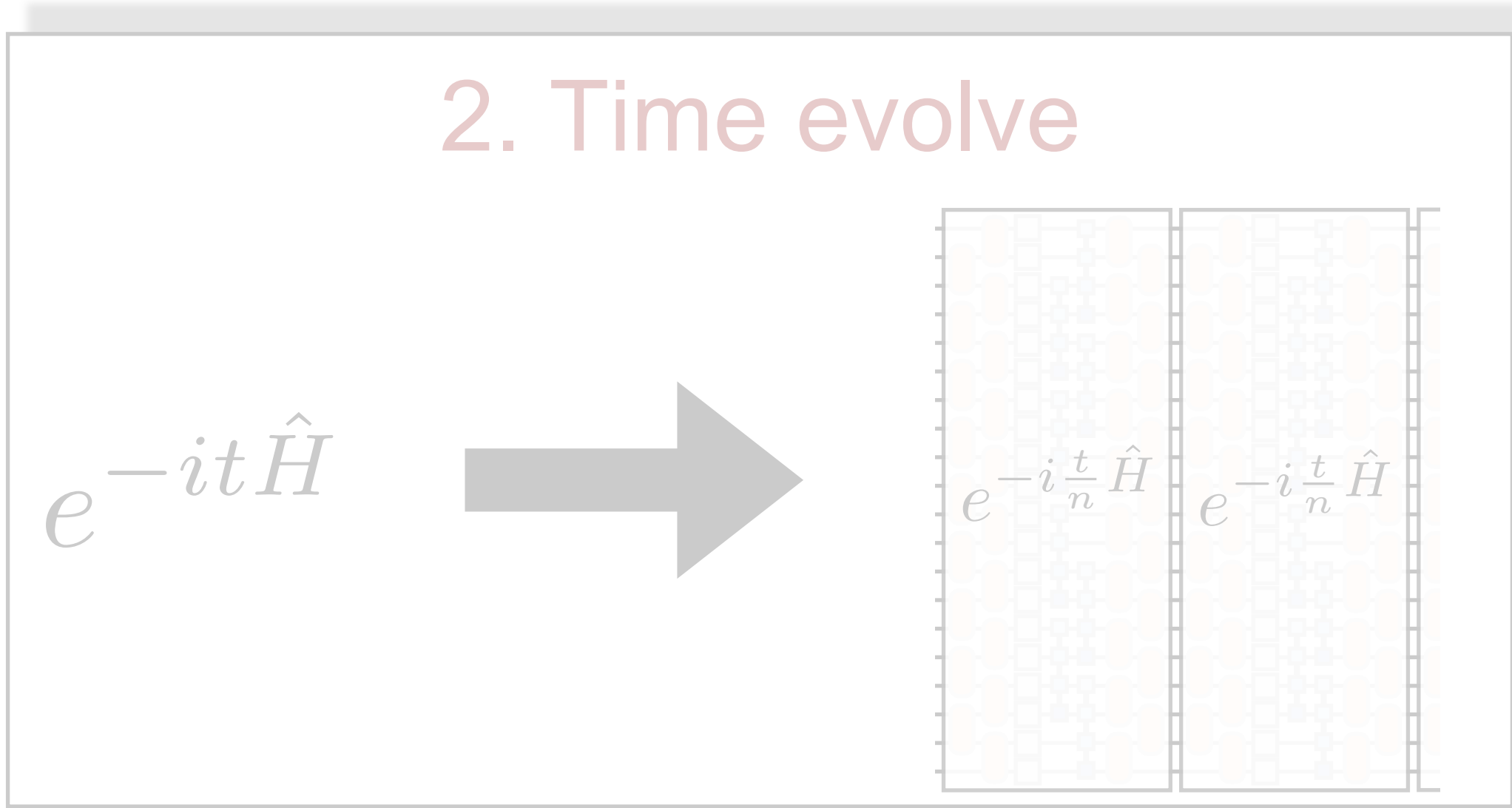
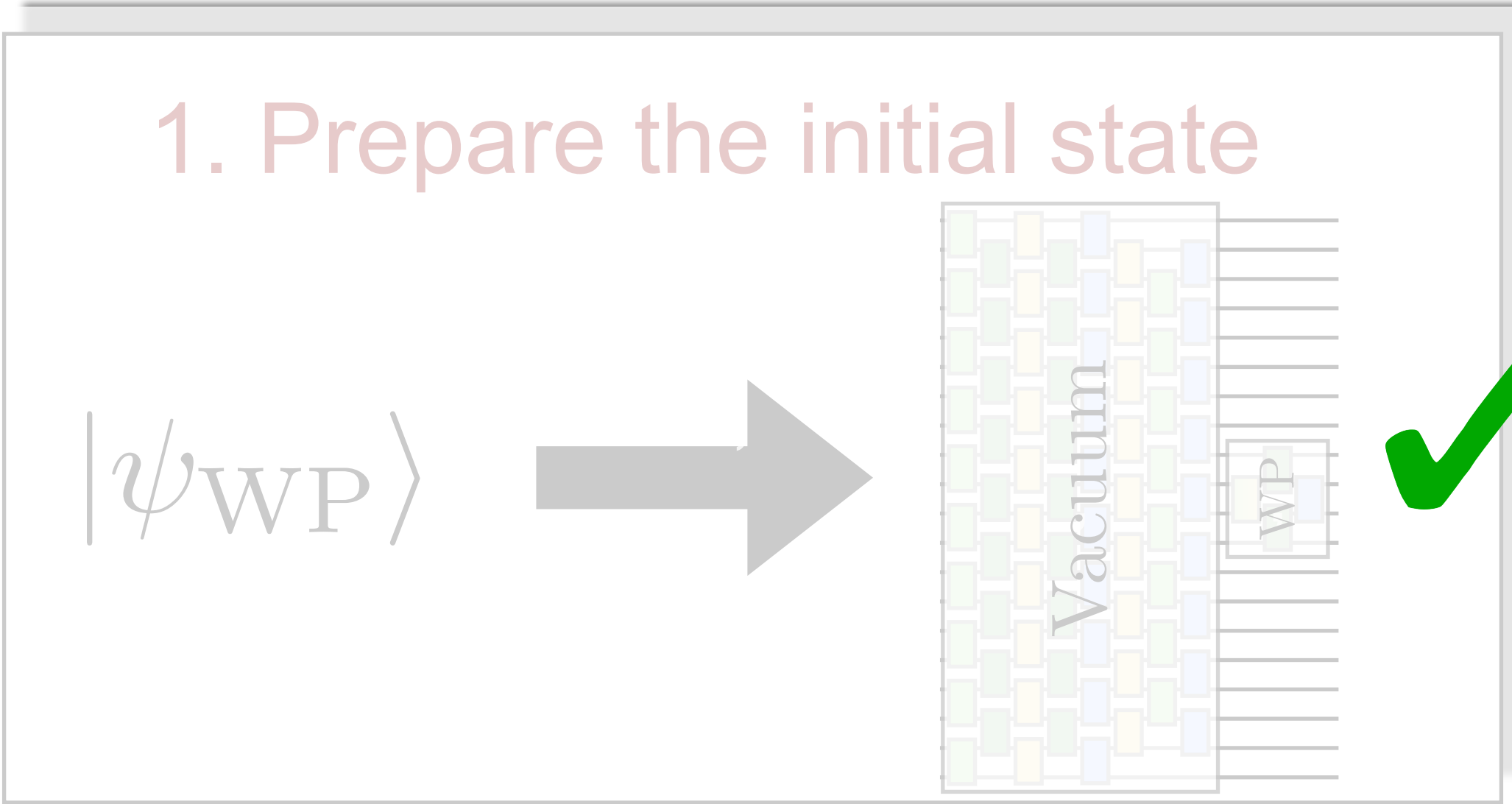
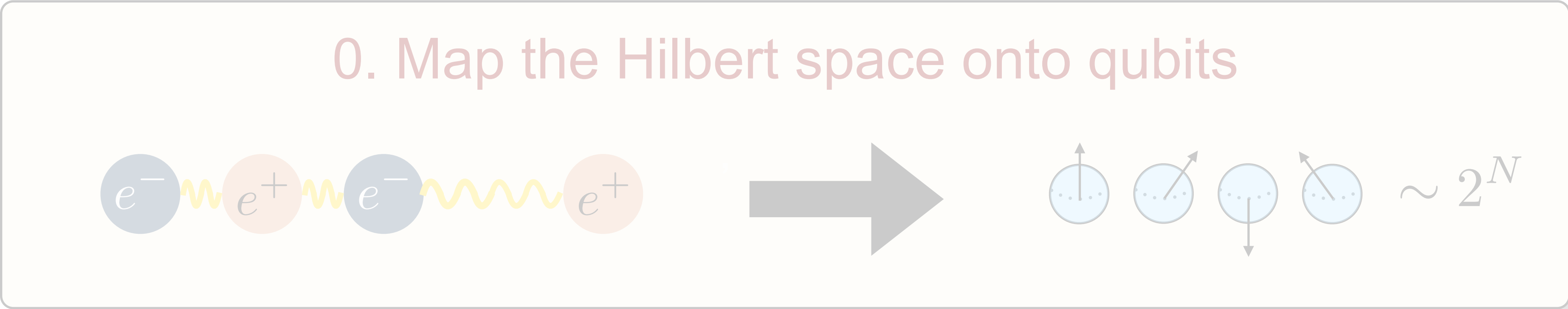


# Trotterized time evolution

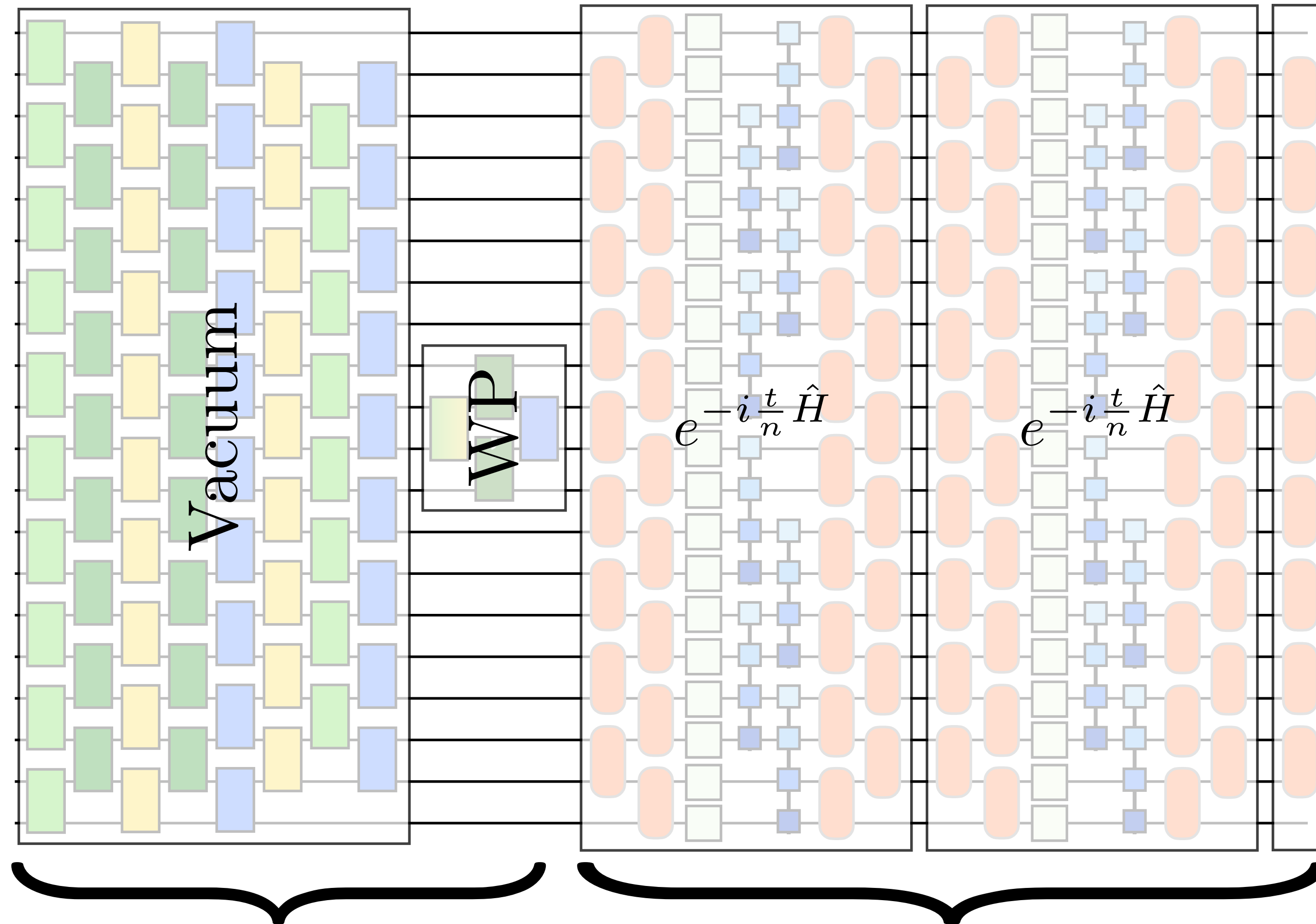


One second order Trotter step with the  $\bar{\lambda} = 1$  truncated electric interaction

# Goal: to simulate hadron dynamics on a quantum computer



# Quantum circuits for simulating hadron dynamics



Hadron wave packet prepared  
with SC-ADAPT-VQE

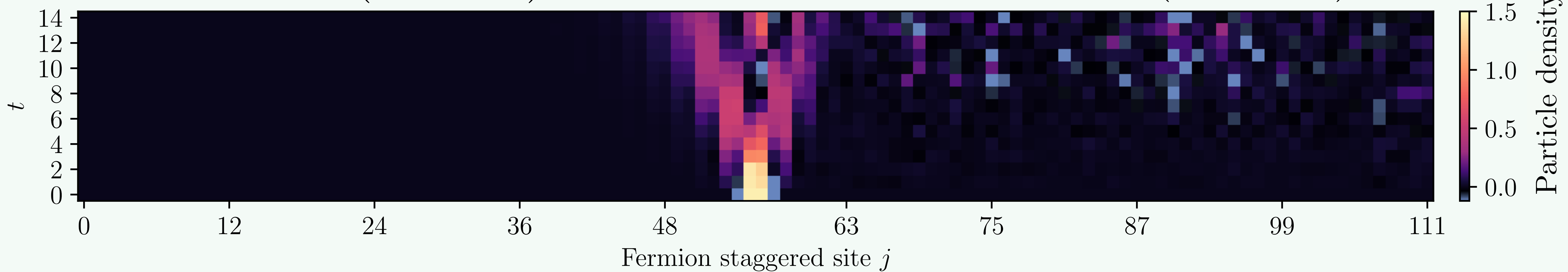
Trotterized time evolution with  
 $\bar{\lambda} = 1$  truncated interaction



# Results from IBM's quantum computer

MPS (classical)

ibm\_torino (quantum)

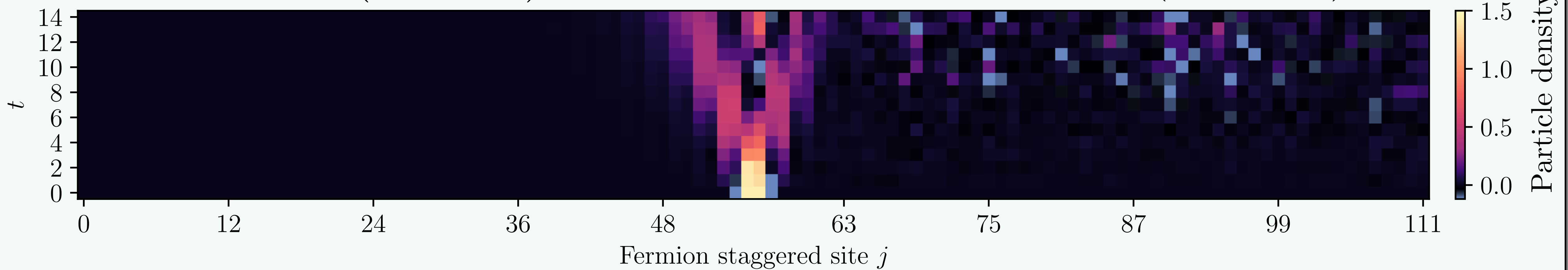


- Reflection symmetric in the absence of device errors
- Hadron propagation clearly identified

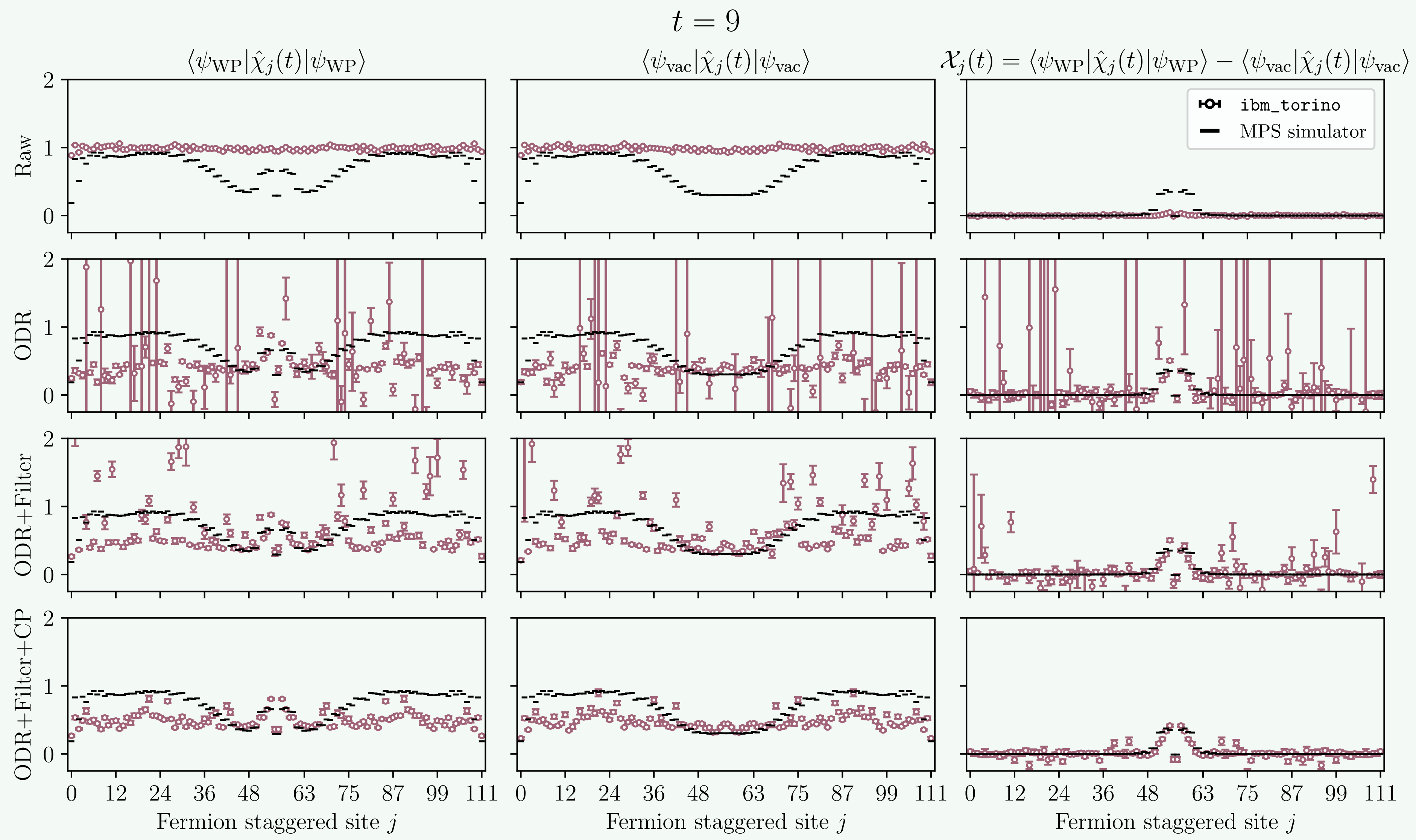
# Results from IBM's quantum computer

MPS (classical)

ibm\_torino (quantum)

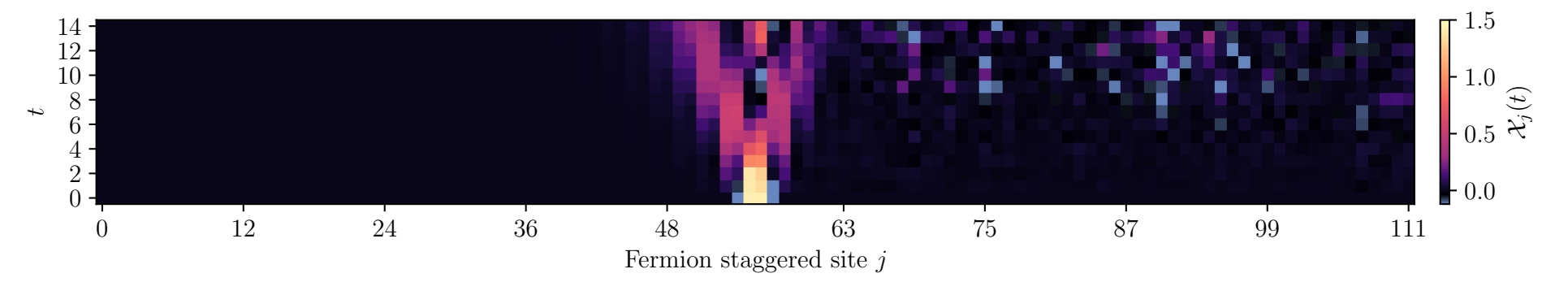
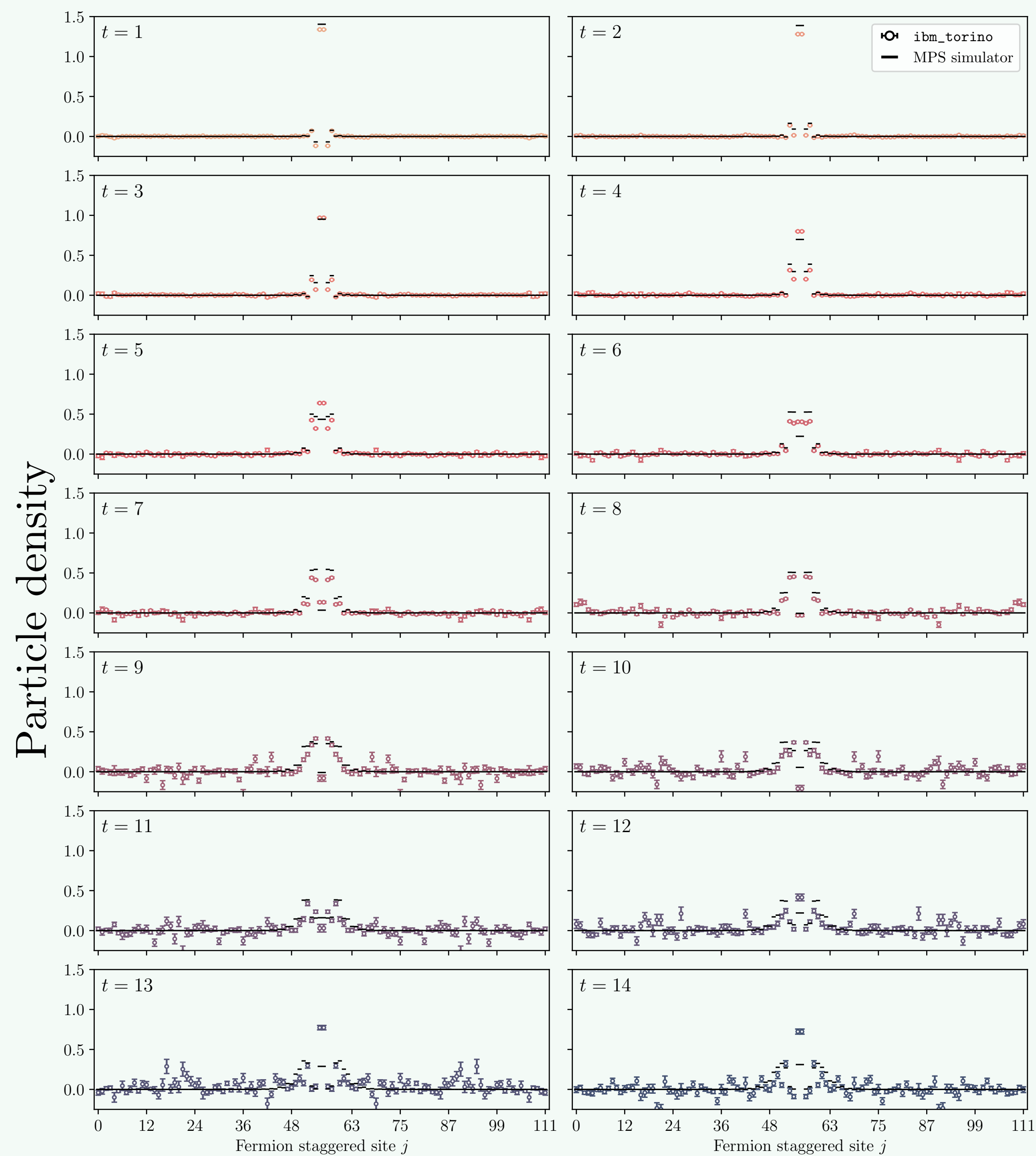


$t$	$N_T$	# of CNOTs (per $t$ )	CNOT depth (per $t$ )	Executed CNOTs ( $\times 10^9$ )	Total # of shots ( $\times 10^6$ )
1 & 2	2	2,746	70	$4 \times 2 \times 10.5$	$4 \times 2 \times 3.8$
3 & 4	4	4,598	120	$4 \times 2 \times 17.7$	$4 \times 2 \times 3.8$
5 & 6	6	6,450	170	$4 \times 2 \times 24.8$	$4 \times 2 \times 3.8$
7 & 8	8	8,302	220	$4 \times 2 \times 31.9$	$4 \times 2 \times 3.8$
9 & 10	10	10,154	270	$4 \times 2 \times 13.0$	$4 \times 2 \times 1.3$
11 & 12	12	12,006	320	$4 \times 2 \times 15.4$	$4 \times 2 \times 1.3$
13 & 14	14	13,858	370	$4 \times 2 \times 17.7$	$4 \times 2 \times 1.3$
<b>Totals</b>				$1.05 \times 10^{12}$	$1.54 \times 10^8$



Error mitigation essential to extract a signal!

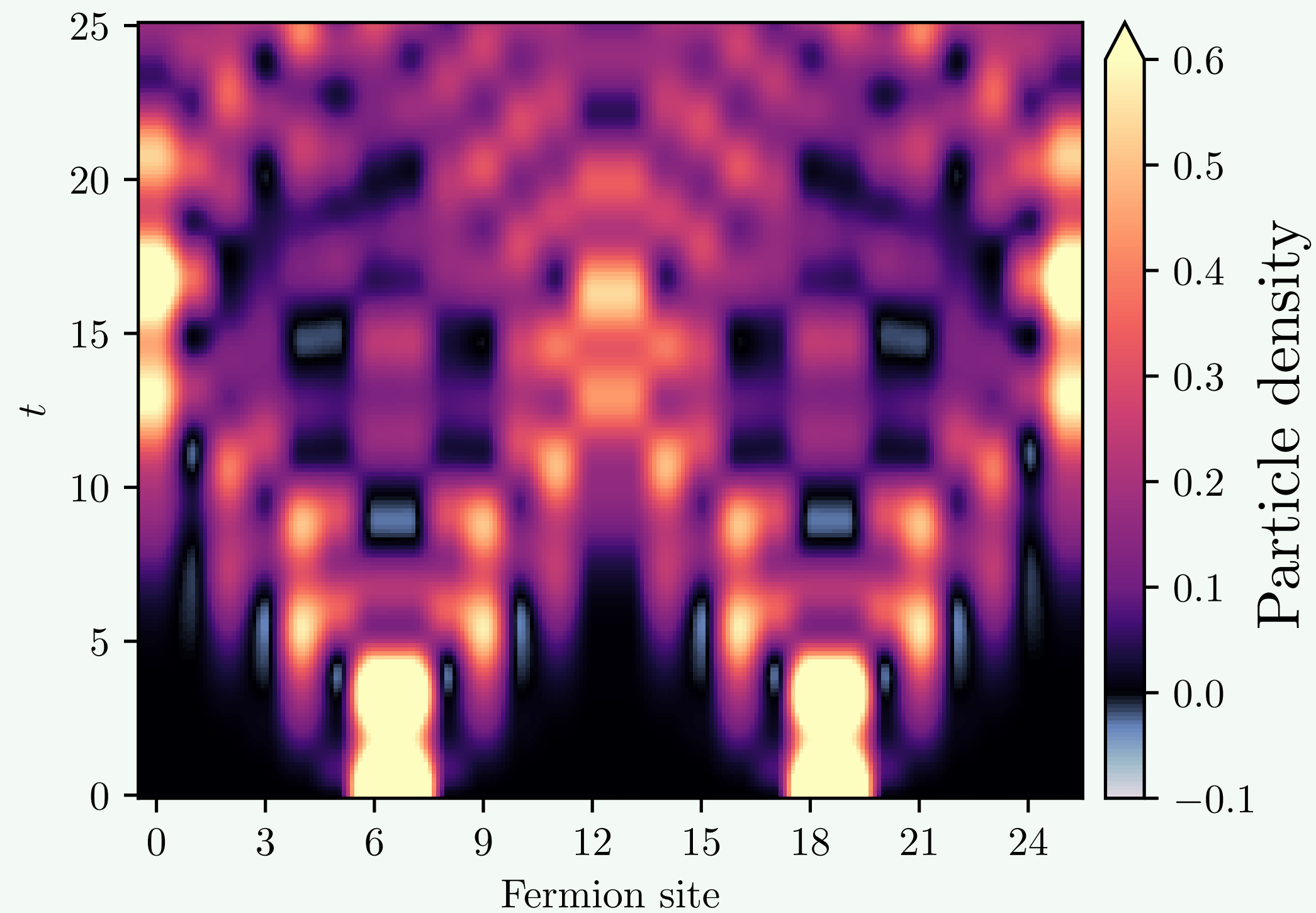




- Qualitative agreement with MPS
- Systematic error around the wave packet

# Looking toward the (immediate) future

## Hadron collisions

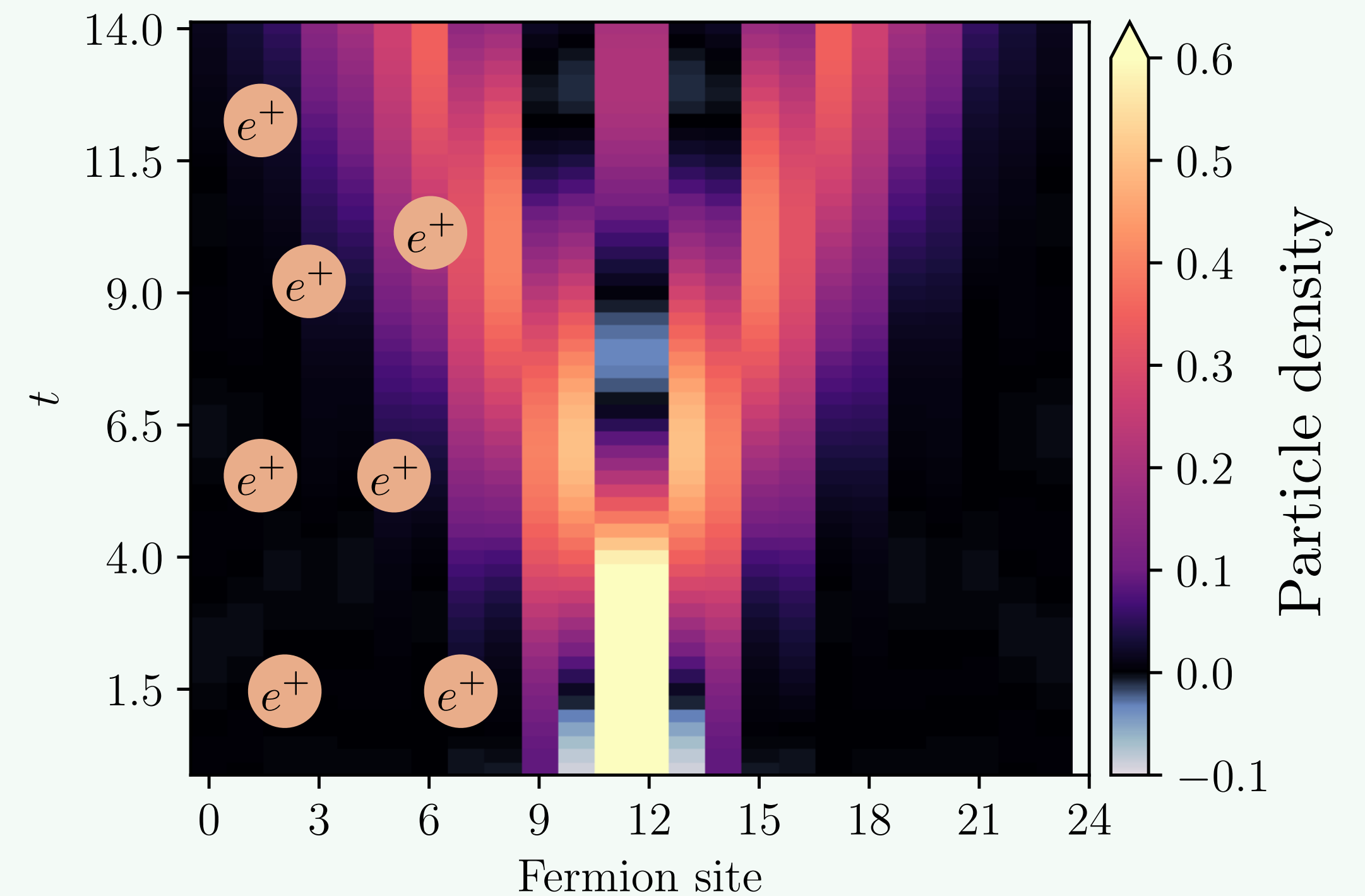


### Real-time scattering in the lattice Schwinger model

Irene Papaefstathiou,<sup>1,2</sup> Johannes Knolle,<sup>3,2,4</sup> and Mari Carmen Bañuls<sup>1,2</sup>

[arxiv.org/abs/2402.18429](https://arxiv.org/abs/2402.18429)

## In-medium effects



### Steps Toward Quantum Simulations of Hadronization and Energy-Loss in Dense Matter

Roland C. Farrell<sup>1,2,\*</sup> Marc Illa<sup>1,†</sup> and Martin J. Savage<sup>1,‡</sup>

[arxiv.org/abs/2405.06620](https://arxiv.org/abs/2405.06620)

# Summary

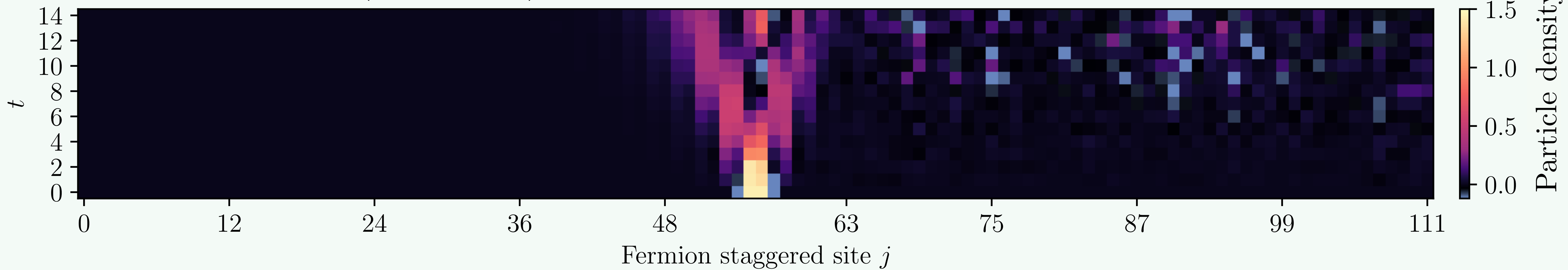
- Quantum simulations of fundamental physics are promising candidates for a “quantum advantage”
- Informed by symmetries and hierarchies in length scales, we developed efficient quantum simulation protocols for the Schwinger model
- Prepared a hadron wave packet and time evolved it on `ibm_torino`
- One of the most complex digital quantum simulations ever performed: up to 13,858 two-qubit gates over 112 qubits. 154 million measurements
- Error mitigation essential to extracting a signal



# Thanks for listening!

MPS (classical)

ibm\_torino (quantum)



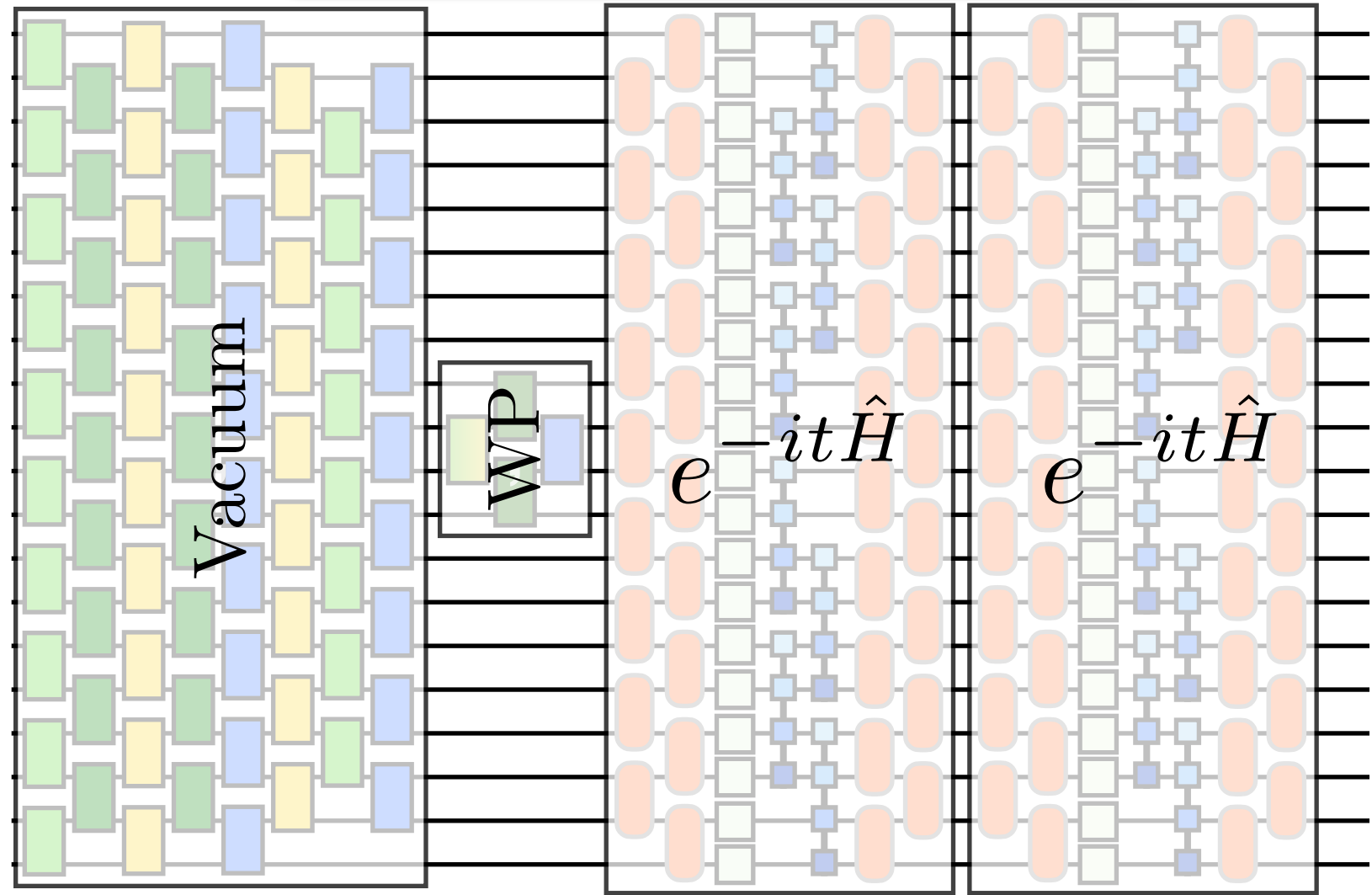
**IQuS** InQubator for Quantum Simulation  
UW Nuclear Theory Group



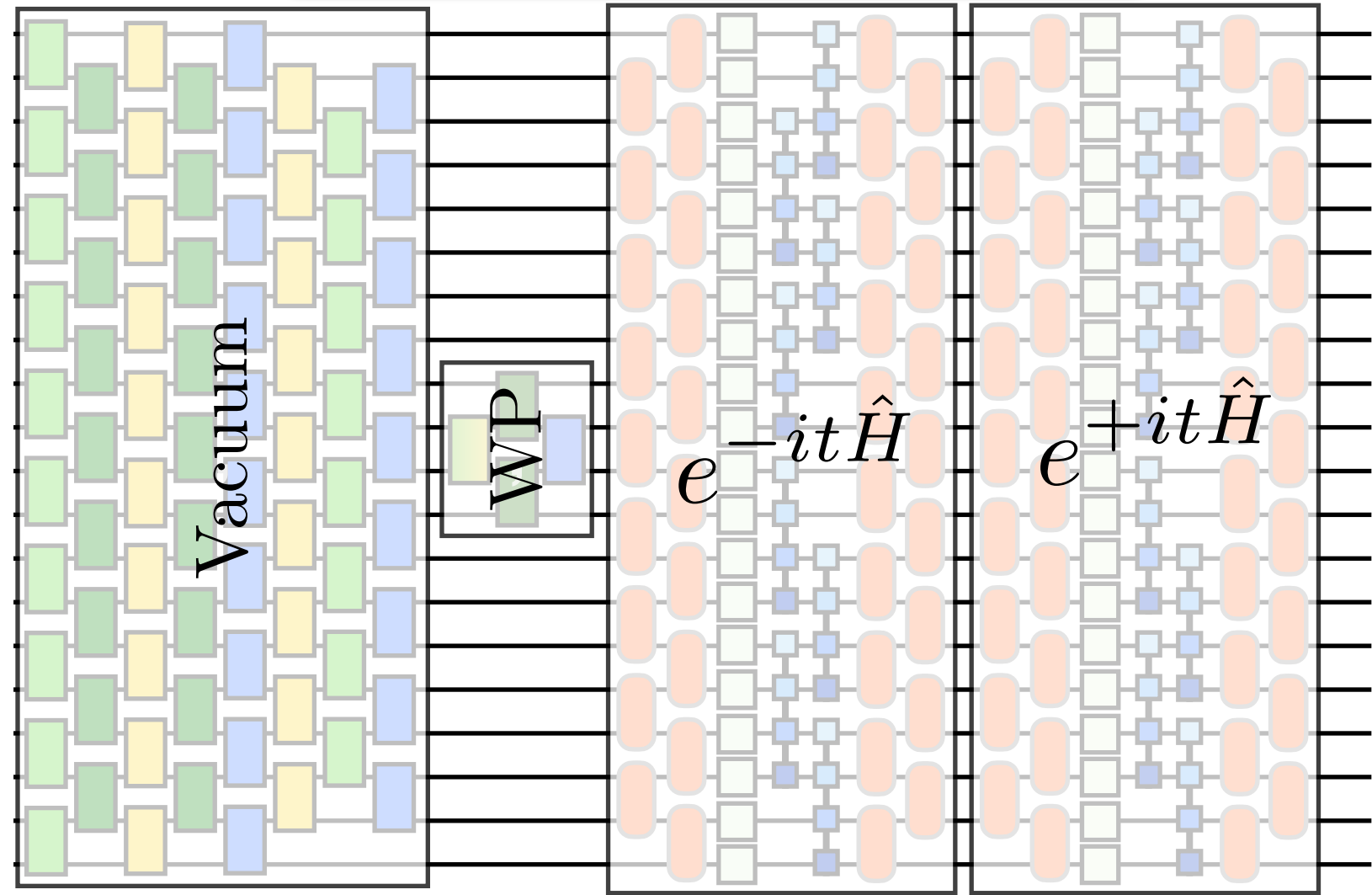
IBM Quantum



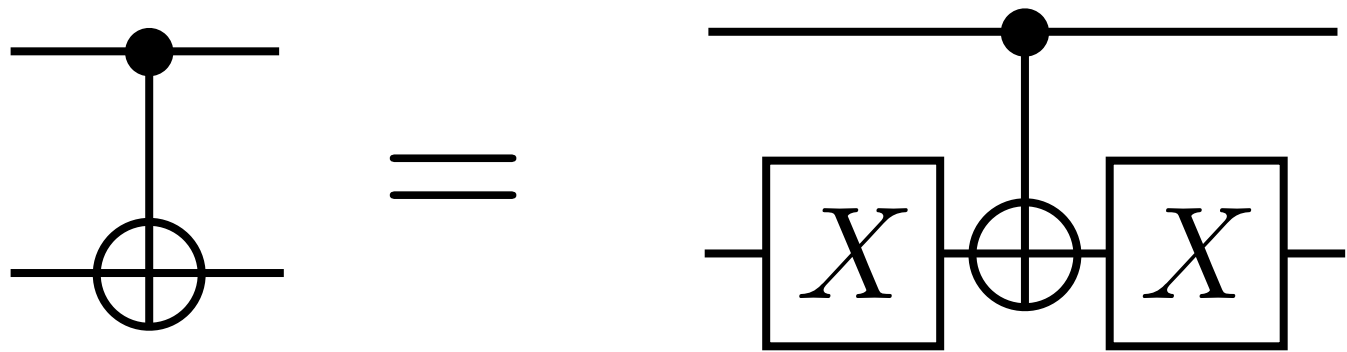
# Physics circuit



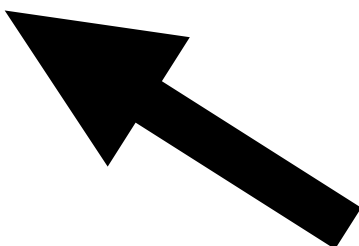
# Mitigation circuit



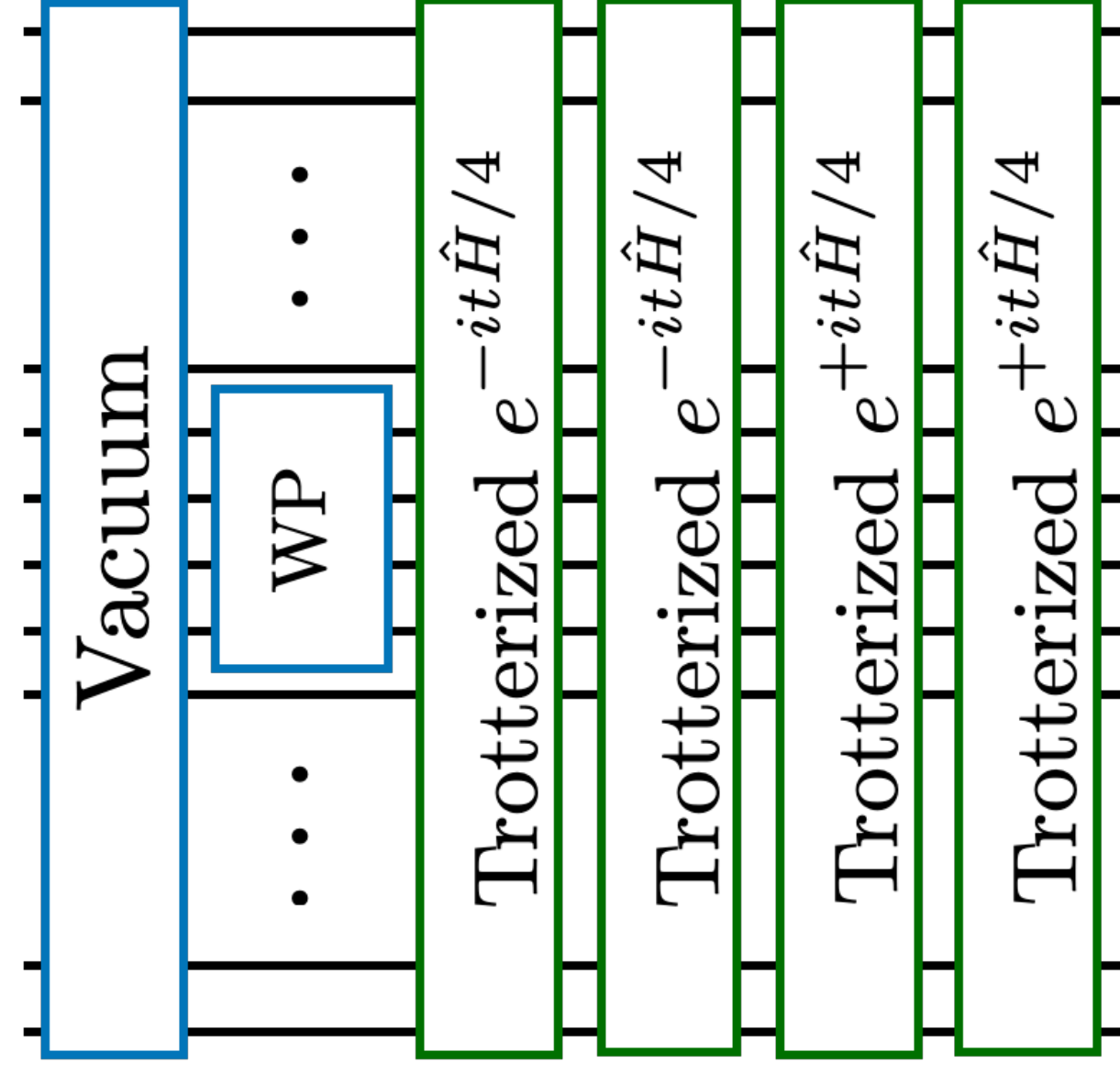
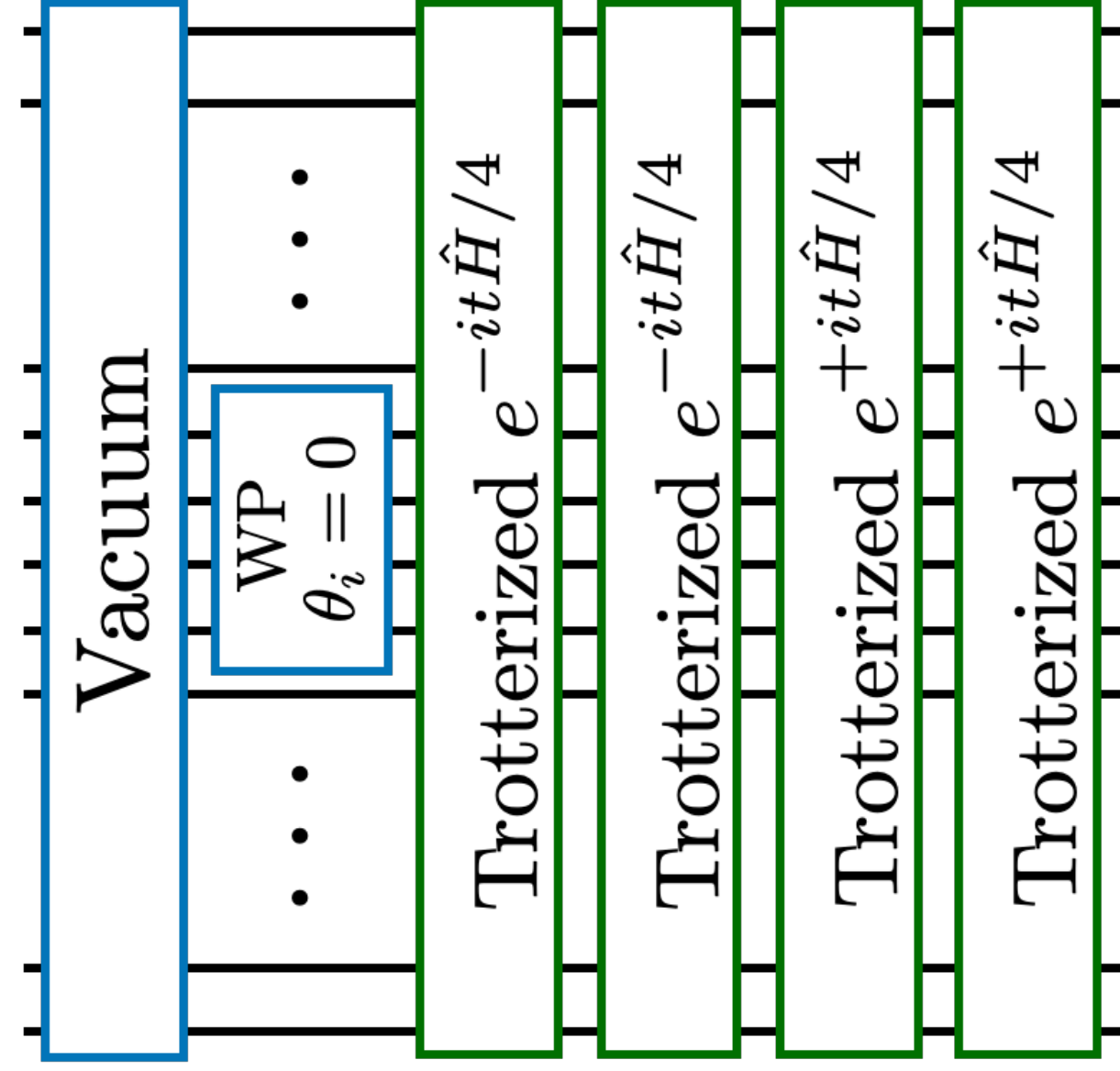
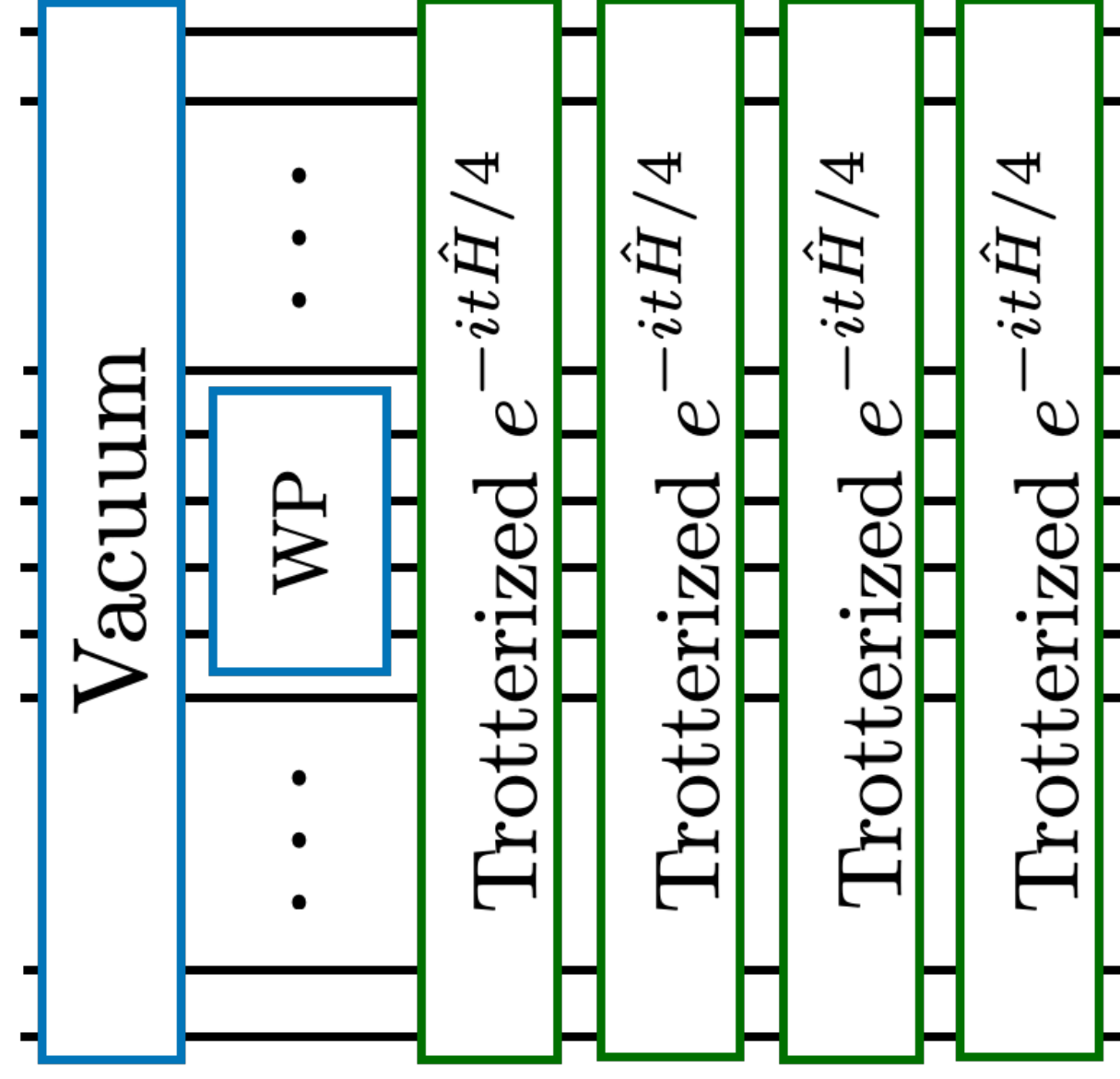
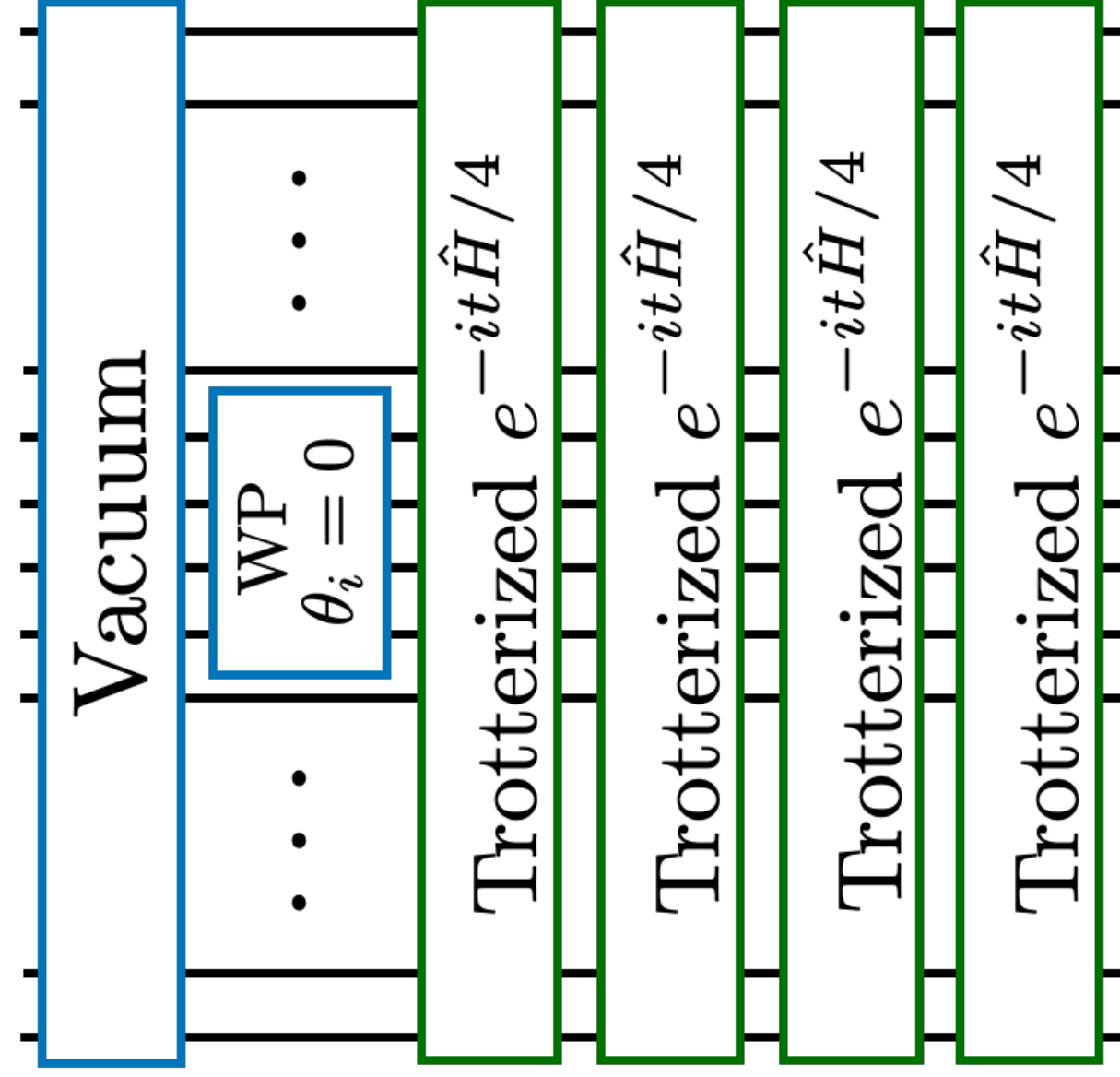
## Pauli twirling



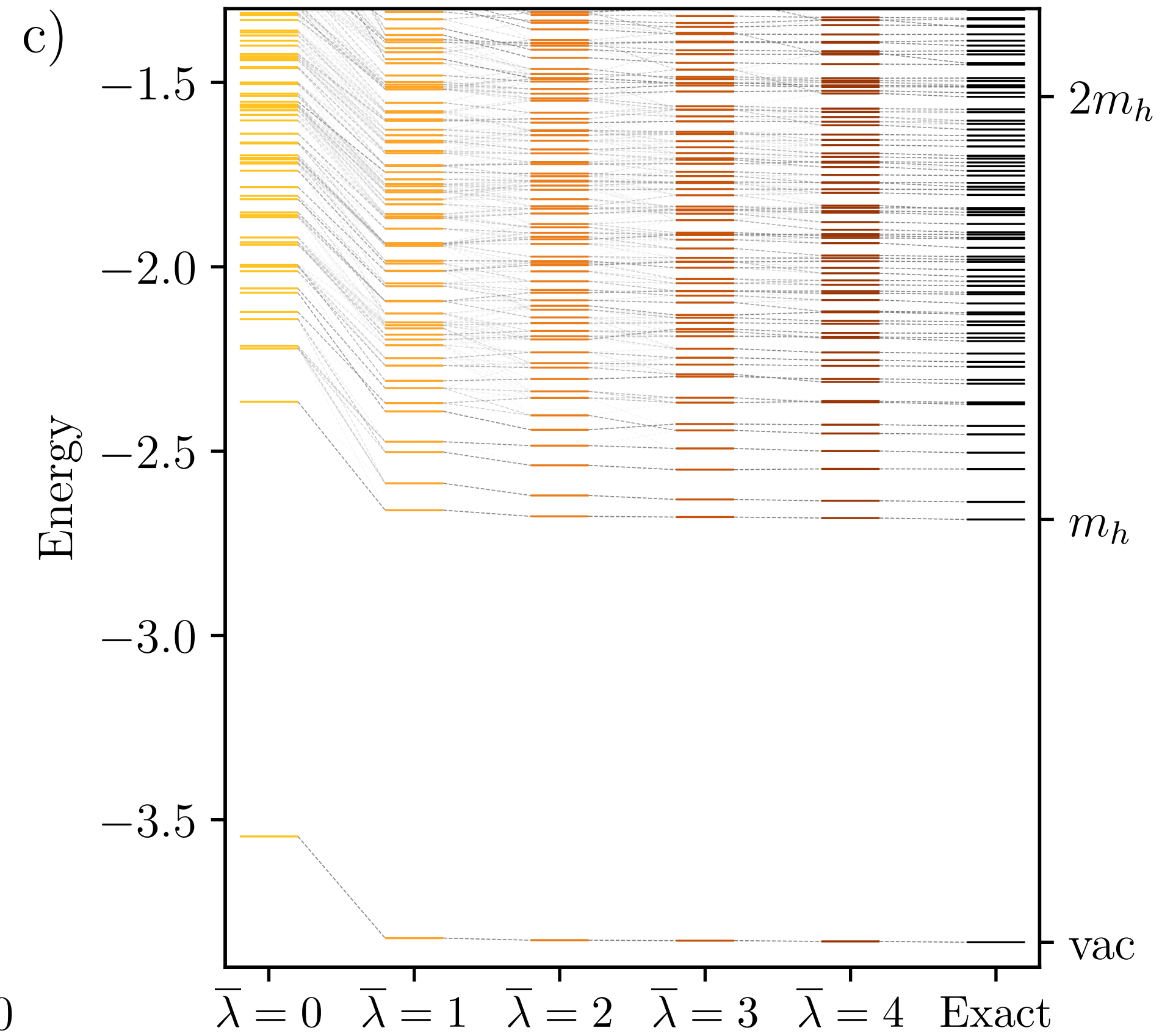
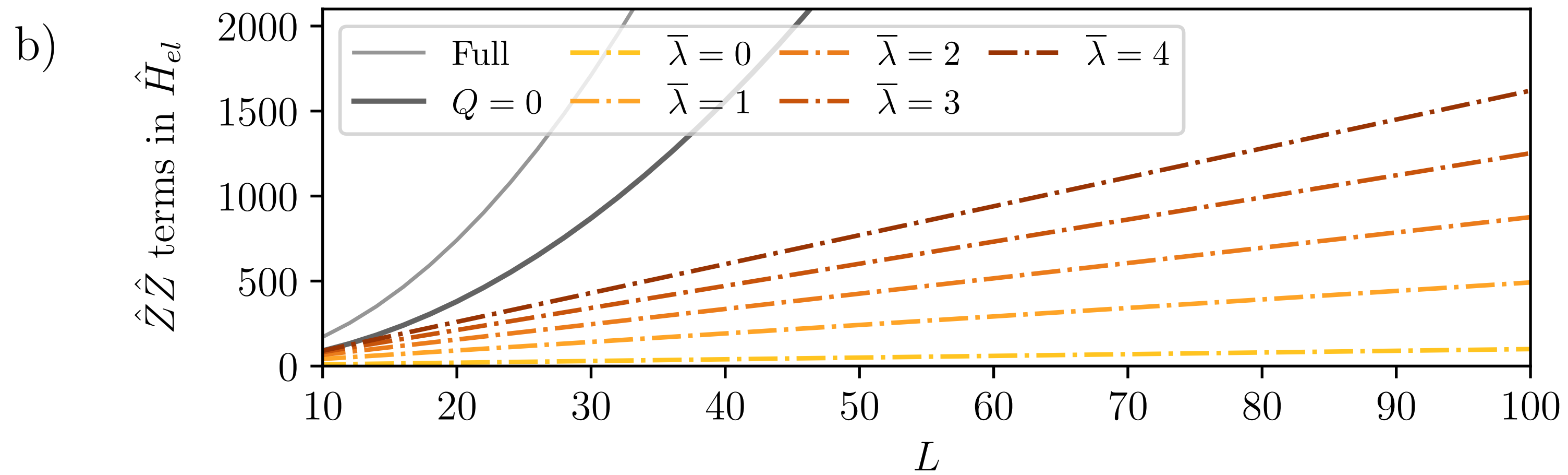
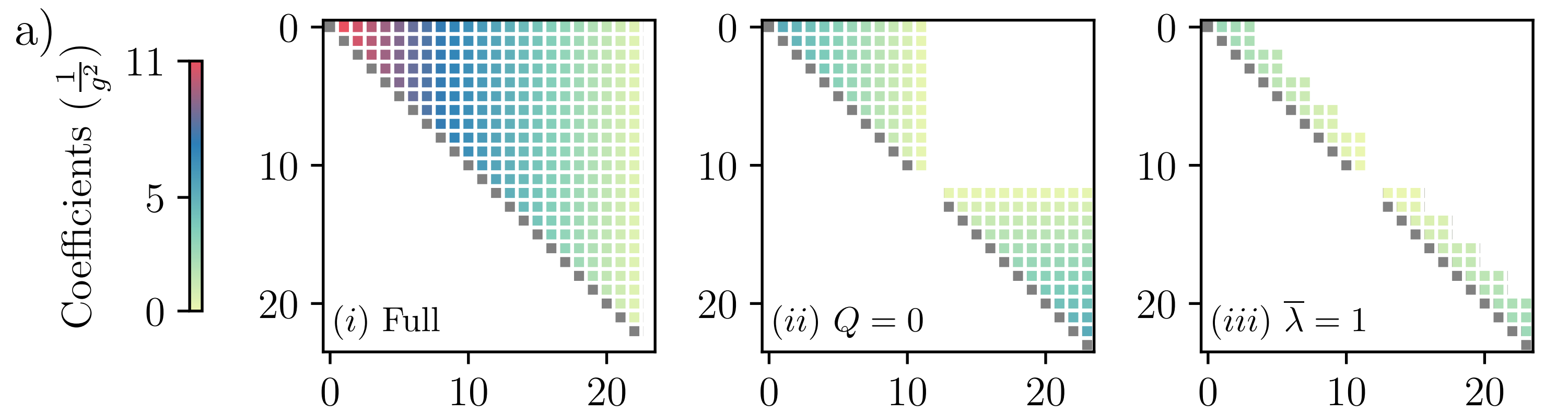
$$\frac{\langle \hat{Z} \rangle_{\text{measured}}}{\langle \hat{Z} \rangle_{\text{expected}} \Big|_{\text{physics}}} = \frac{\langle \hat{Z} \rangle_{\text{measured}}}{\langle \hat{Z} \rangle_{\text{expected}} \Big|_{\text{mitigation}}}$$



Solve for  $\langle \hat{Z} \rangle_{\text{expected}}$







# Effective electric interaction

Quantify errors on  $N = 24$  system that can be done exactly

