

Z' MODELS AT A MUON COLLIDER

Mass reach and model discrimination
arXiv:2402.18460 (EPJC 84, 568 (2024))

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Early Career Researchers & Muon Colliders, 28 Aug 2024

Motivation

- Despite success of SM, open questions remain: dark matter, matter-antimatter asymmetry, **unification beyond electroweak**
- Multitude of well-motivated UV-complete models for **SM gauge group extensions**
- Naturally come with **additional neutral gauge boson Z'**
- Study large set of models in terms of **effective Lagrangian** with different **axial** and **vector** couplings to SM fermions:

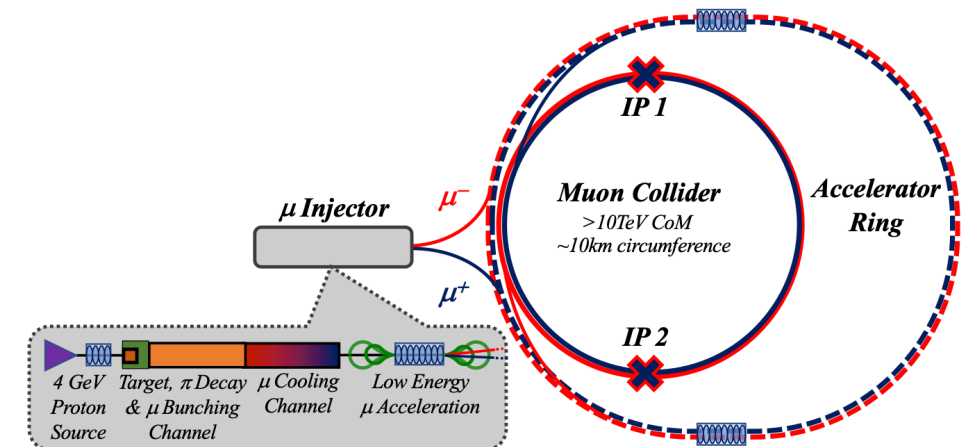
$$-\mathcal{L}_{NC} = eA_\mu J_A^\mu + g_Z Z_\mu J_Z^\mu + g_{Z'} Z'_\mu J_{Z'}^\mu$$

$$J_A^\mu = \sum_f \bar{f} \gamma^\mu q_f f, \quad J_Z^\mu = \sum_f \bar{f} \gamma^\mu (v_f^{SM} - \gamma_5 a_f^{SM}) f, \quad J_{Z'}^\mu = \sum_f \bar{f} \gamma^\mu (v_f - \gamma_5 a_f) f,$$

- Muon collider has a great potential to study this
- **Collider options we discuss:**

$$E_{CM} = \{3, 10\} \text{TeV}, \quad \mathcal{L}_{int} = 10 \text{ab}^{-1} (E/10 \text{TeV})^2$$

Model	$g_{Z'}$	$2v_l$	$2a_l$
SSM	$\frac{e}{s_W c_W}$	$2s_W^2 - \frac{1}{2}$	$-\frac{1}{2}$
E_6	$\frac{e}{c_W}$	$\frac{2 \cos \beta}{\sqrt{6}}$	$\frac{\cos \beta}{\sqrt{6}} + \frac{\sqrt{10} \sin \beta}{6}$
LR	$\frac{e}{c_W}$	$\frac{1}{\alpha} - \frac{\alpha}{2}$	$\frac{\alpha}{2}$
ALR	$\frac{e}{s_W c_W \sqrt{1-2s_W^2}}$	$\frac{5}{2} s_W^2 - 1$	$-\frac{1}{2} s_W^2$
LH	$\frac{e}{s_W}$	$-\frac{c}{4s}$	$-\frac{c}{4s}$
USLH	$\frac{e}{c_W \sqrt{3-4s_W^2}}$	$\frac{1}{2} - 2s_W^2$	$\frac{1}{2}$
$U(1)_X$	$\frac{e}{4c_W}$	-8	2



Setup

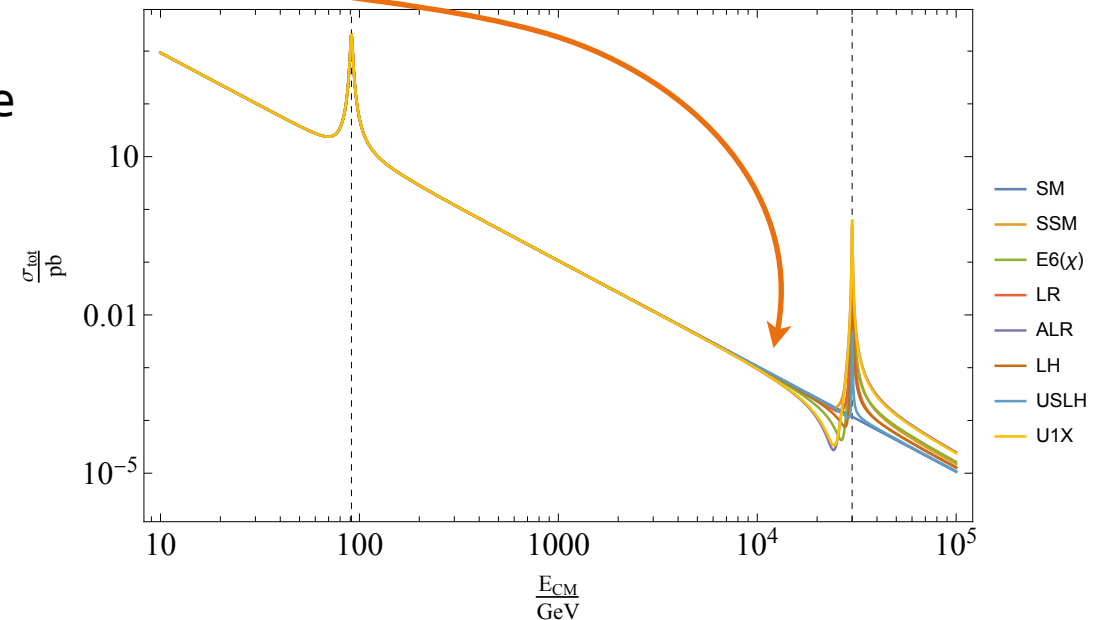
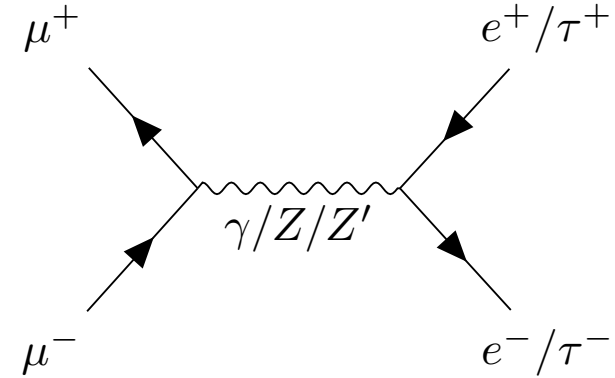
What do we study?

- Study **s-channel** lepton production at a muon collider
- Born approximation gives reliable results in **off-peak region**

⇒ **Particularly simple analysis**

- Discuss statistical significance in terms of χ^2 w.r.t. reference observables \hat{O}_i and uncertainties $\Delta\hat{O}_i$:

$$\chi^2(a_l, v_l, M_{Z'}) = \sum_{i=1}^{n_{ob}} \left[\frac{\hat{O}_i - O_i(a_l, v_l, M_{Z'})}{\Delta\hat{O}_i} \right]^2$$



Observables

Input for the χ^2

- Total cross-section σ_f

- Forward-backward asymmetry:

$$A_{FB}^f = \frac{\sigma_F^f - \sigma_B^f}{\sigma^f}$$

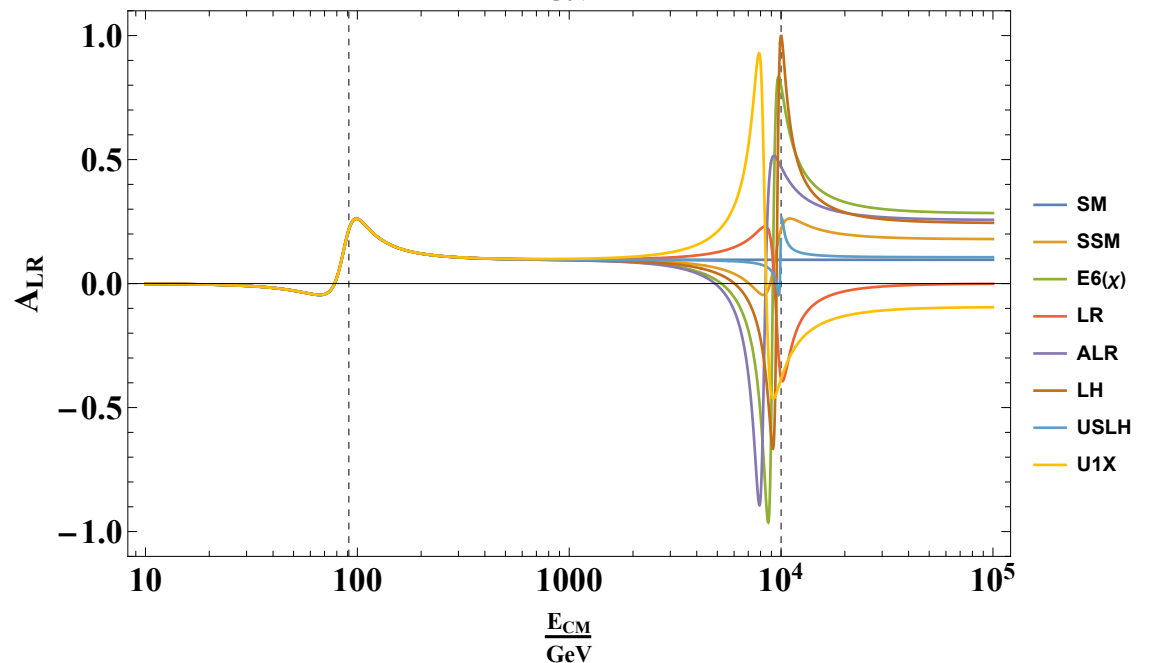
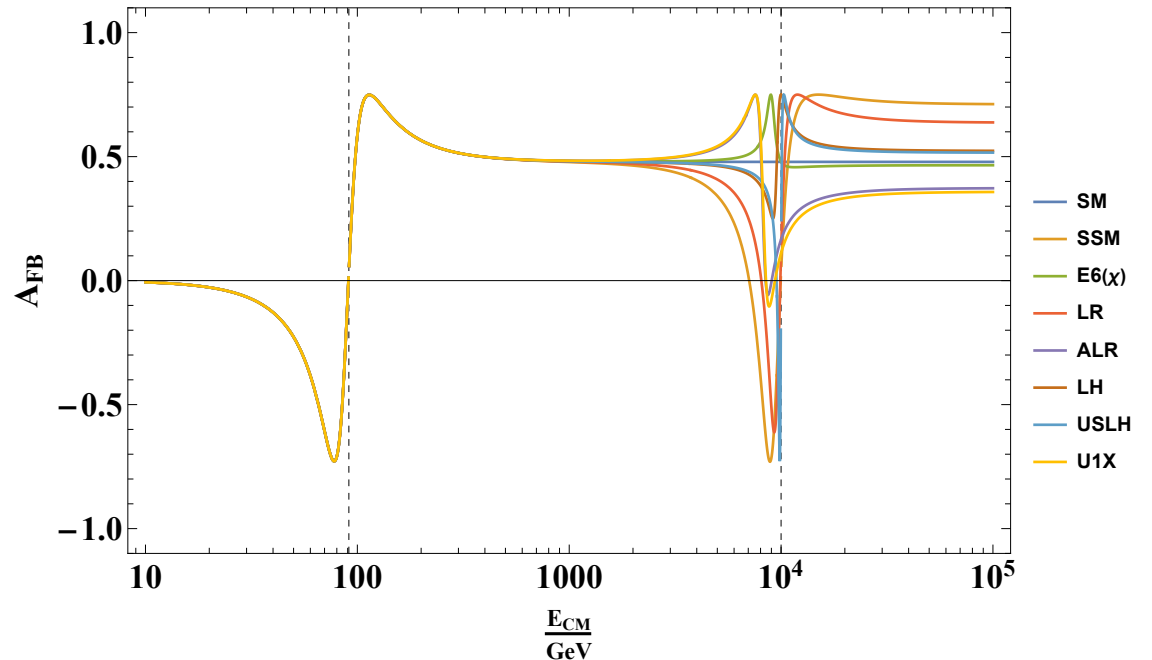
- Left-right asymmetry (initial state):

$$A_{LR}^f = \frac{\sigma_{LR}^f - \sigma_{RL}^f}{\sigma^f}$$

- Polarisation asymmetry (final state):

$$A_{pol} = \frac{\sigma_{lr}^f - \sigma_{rl}^f}{\sigma^f} \quad (= A_{LR} \text{ for massless fermions})$$

- Signal strengths can be significant even far off-peak
⇒ yields a high reach/discrimination power

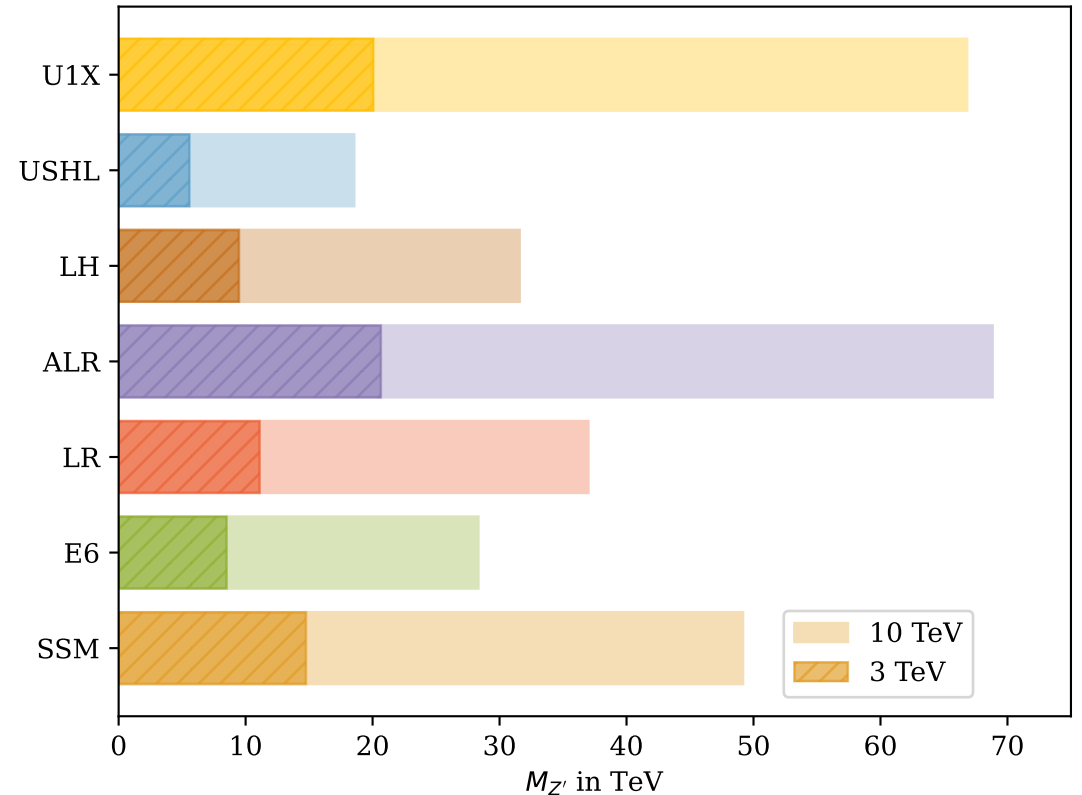


Results

Mass reach

$$\chi_{model}^2(M_{Z'}) = \sum_{i=1}^{n_{ob}} \left[\frac{\hat{O}_i - O_{i,model}(M_{Z'})}{\Delta \hat{O}_i} \right]^2$$

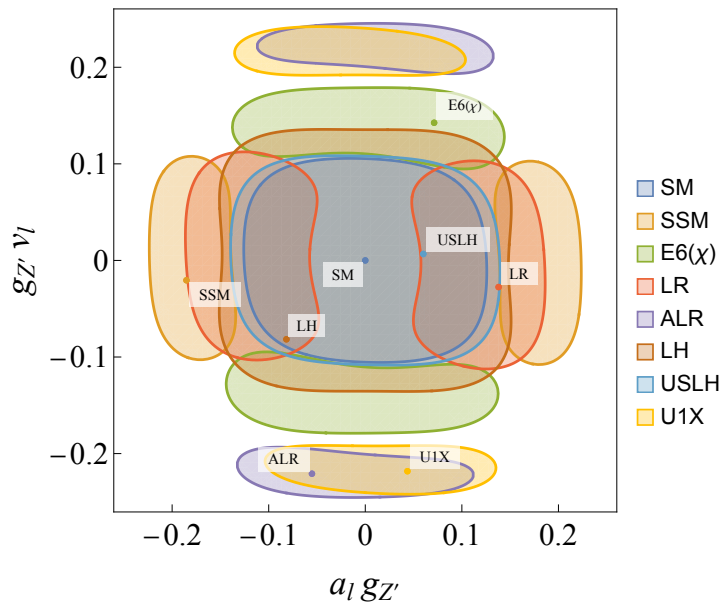
- Use $\chi_{model}^2(M_{Z'})$ for fixed couplings and vary $M_{Z'}$
- **We find limits up to $M_{Z'} \sim 70$ TeV**
(Note: current LHC limits up to ~ 5 TeV)
- Reach depends on magnitude of couplings
- Extension to hadronic observables **could push reach by up to $\sim 50\%$** , depending on the model
(see LEP-discussion [arXiv:hep-ph/9607306])



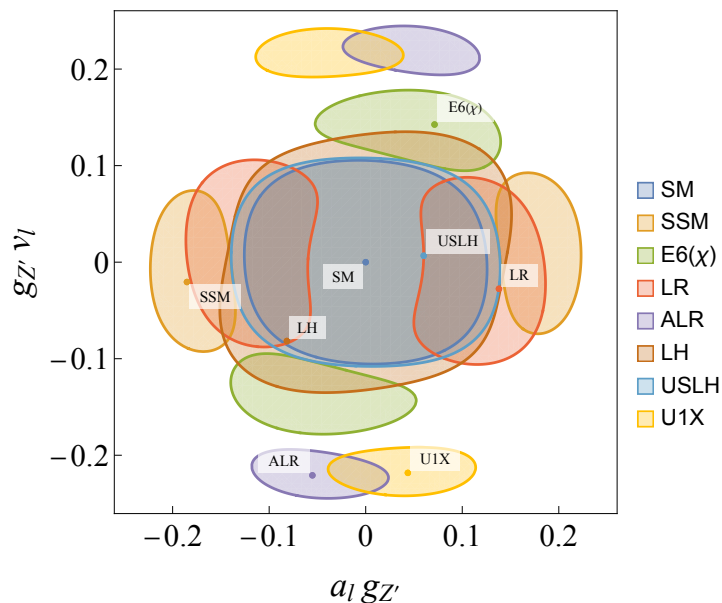
Results

Resolving power

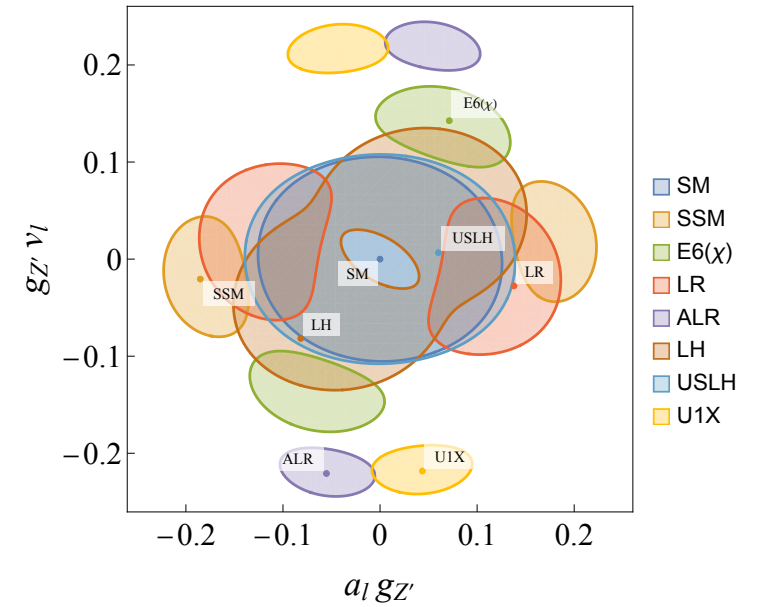
- Use $\chi_{M_{Z'}}^2(a_l, v_l)$ for fixed mass and vary couplings w.r.t. reference models:
$$\chi_{M_{Z'}}^2(a_l, v_l) = \sum_{i=1}^{n_{ob}} \left[\frac{\hat{O}_i - O_{i,M_{Z'}}(a_l, v_l)}{\Delta \hat{O}_i} \right]^2$$
- Test influence of **polarized beams** or final state **polarization measurement**
- Setup: $\mathcal{L}_{int} = 10 \text{ ab}^{-1}$, $E_{CM} = 10 \text{ TeV}$, $M_{Z'} = 30 \text{ TeV}$



$$P_{eff} = 0\%, \Delta_{sys}(A_{Pol}) = 5\%$$



$$P_{eff} = 30\%, \Delta_{sys}(A_{Pol}) = 5\%$$



$$P_{eff} = 0\%, \Delta_{sys}(A_{Pol}) = 1\%$$

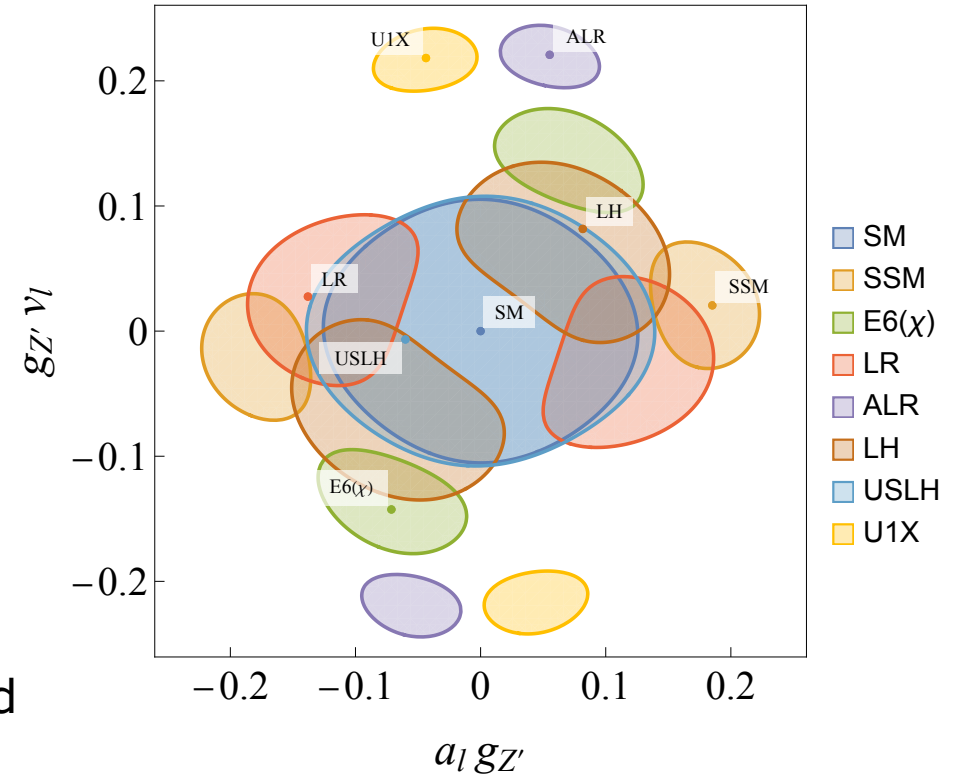
- Similar yields for either using **polarized beams** or **low error on polarization measurement**

Conclusion

What could we find at a muon collider?

- Large variety of well-motivated **Z' models** in the literature
- **Muon collider** as a powerful tool for finding and resolving them
- **Significant reach** of muon colliders to find Z' bosons of up to ~ 70 TeV
- **Strong resolving power** between Z' models for masses up to ~ 30 TeV
- Accurate **polarization measurement or polarized beams** can yield significant increase in model discrimination

Thank you!



Contact

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Muon Collider

"At this stage, building upon significant prior work, **no insurmountable technological issues were identified**. Therefore a development path can address the major challenges and deliver a **3 TeV muon collider by 2045**".

◆ Pros:

- Clean collision environment due to their point-like nature
- Bremsstrahlung significantly reduced compared to electron colliders due to their high mass

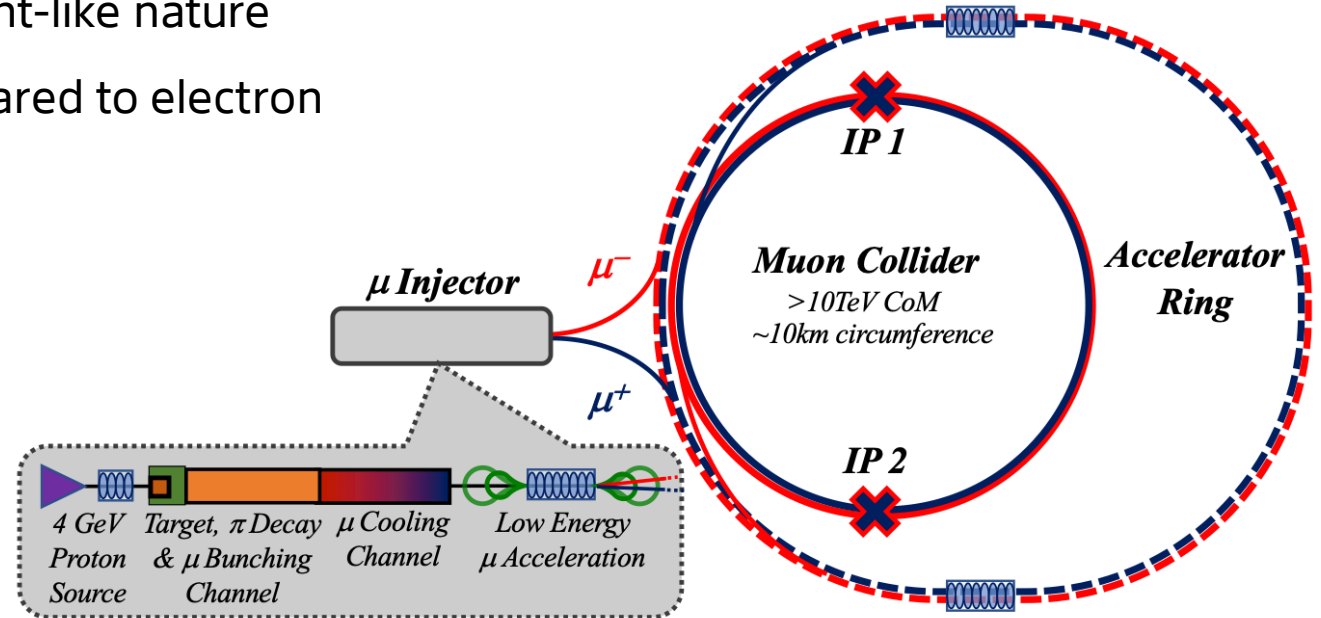
$$\Rightarrow \text{Energy loss per turn: } \frac{\Delta E_\mu}{\Delta E_e} \simeq 10^{-10}$$

◆ Cons:

- Short lifetime of muons
($\tau_0 = 2.2 \mu\text{s}$, $\tau(7 \text{ TeV}) \simeq 150 \text{ ms}$)
- Beam induced background
- High neutrino flux

Options we discuss:

$$E_{CM} = \{3, 10\} \text{ TeV}, \quad L_{int} = 10 \text{ ab}^{-1} (E/10 \text{ TeV})^2$$



Challenging, but not impossible!

[arXiv:2303.08533]

Asymmetries

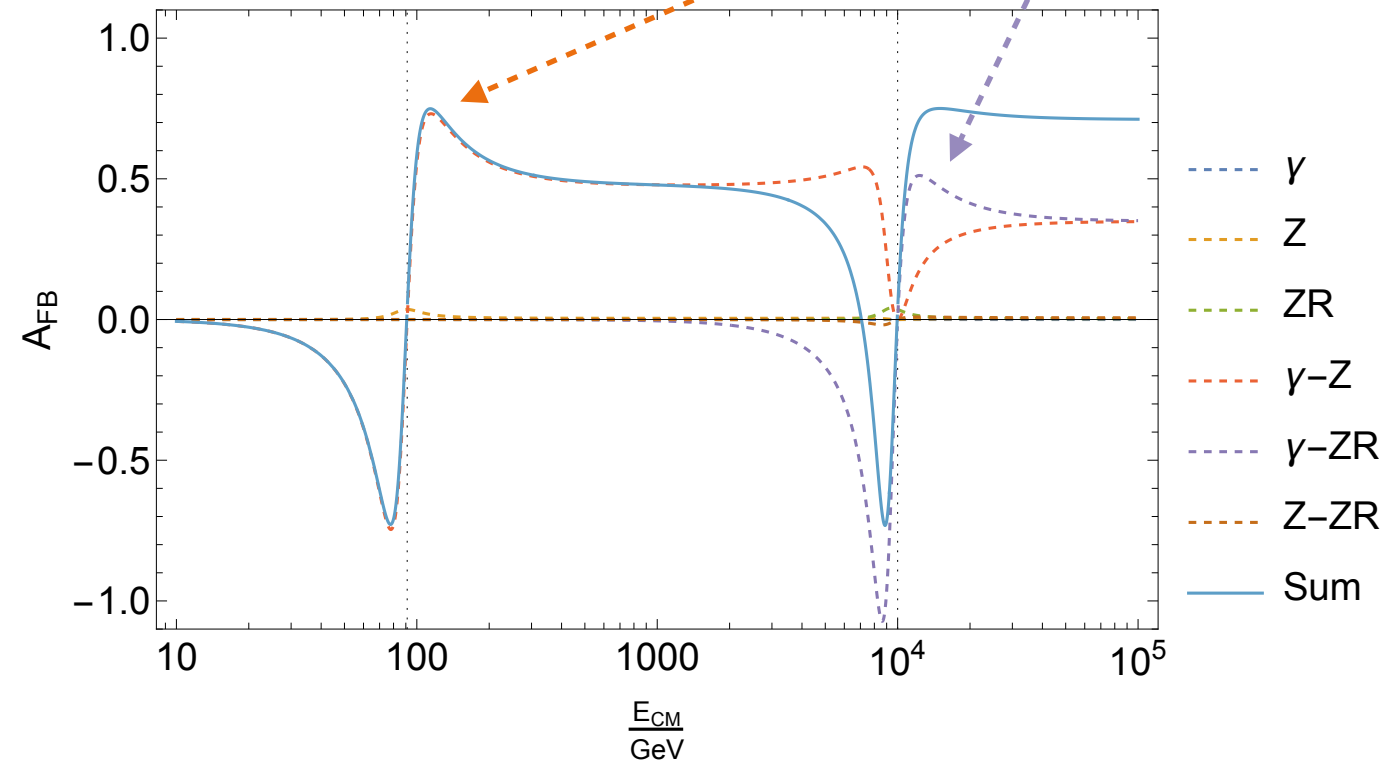
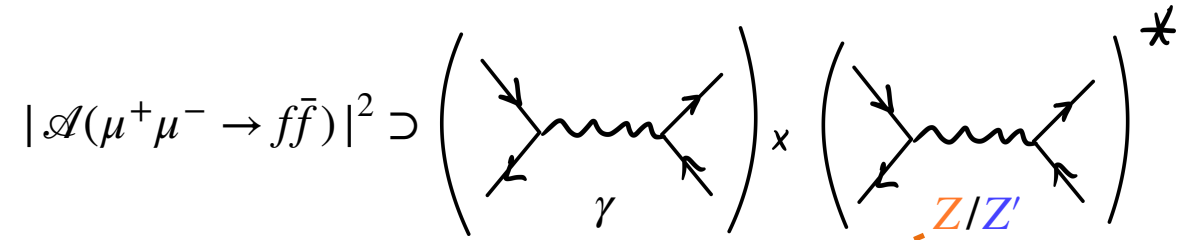
How do they work?

- Can study amplitude **interference effects** in angular distributions or **asymmetries**

- **Forward-backward asymmetry:**

$$A_{FB}^f = \frac{\sigma_F^f(0 \leq \theta < \frac{\pi}{2}) - \sigma_B^f(\frac{\pi}{2} \leq \theta < \pi)}{\sigma_{tot}^f}$$

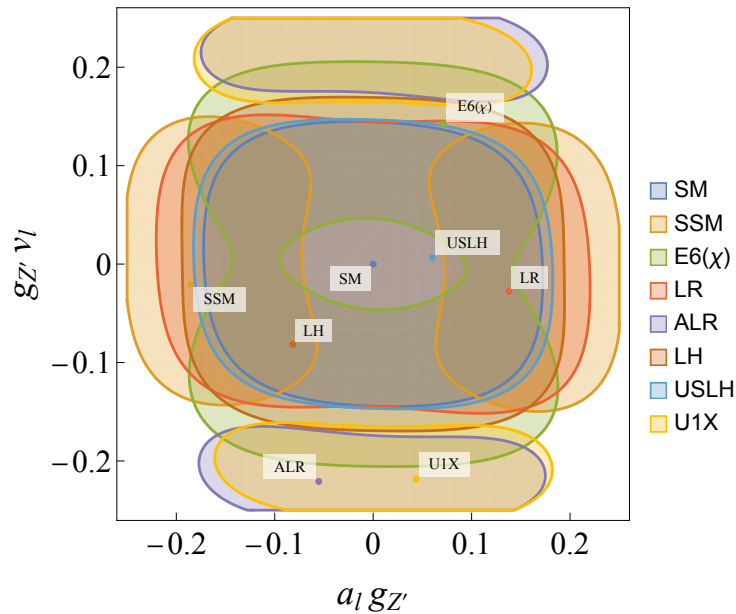
- γ -Z and γ -Z' interference are the main drivers of forward backward asymmetry



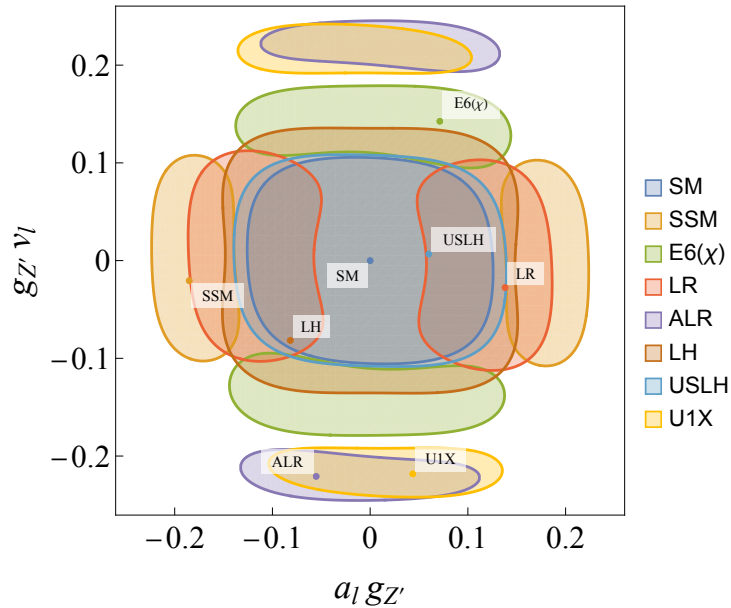
Results

Model discrimination

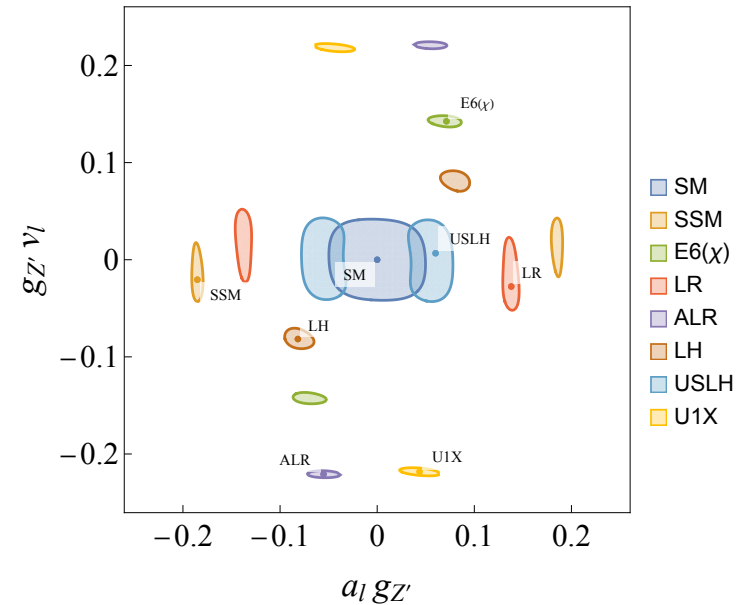
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$$\chi_{M_{Z'}}^2(a_l, v_l) = \sum_{i=1}^{n_{ob}} \left[\frac{\hat{O}_i - O_{i,M_{Z'}}(a_l, v_l)}{\Delta \hat{O}_i} \right]^2$$
- **Resolution power** for $L_{int} = 10 \text{ ab}^{-1}$, $E_{CM} = 10 \text{ TeV}$, $P_{eff} = 0 \%$ for three different Z' masses



$M_{Z'} = 40 \text{ TeV}$



$M_{Z'} = 30 \text{ TeV}$



$M_{Z'} = 15 \text{ TeV}$

- **Significant resolution even without polarization**