

# Dual Readout Method in Calorimetry

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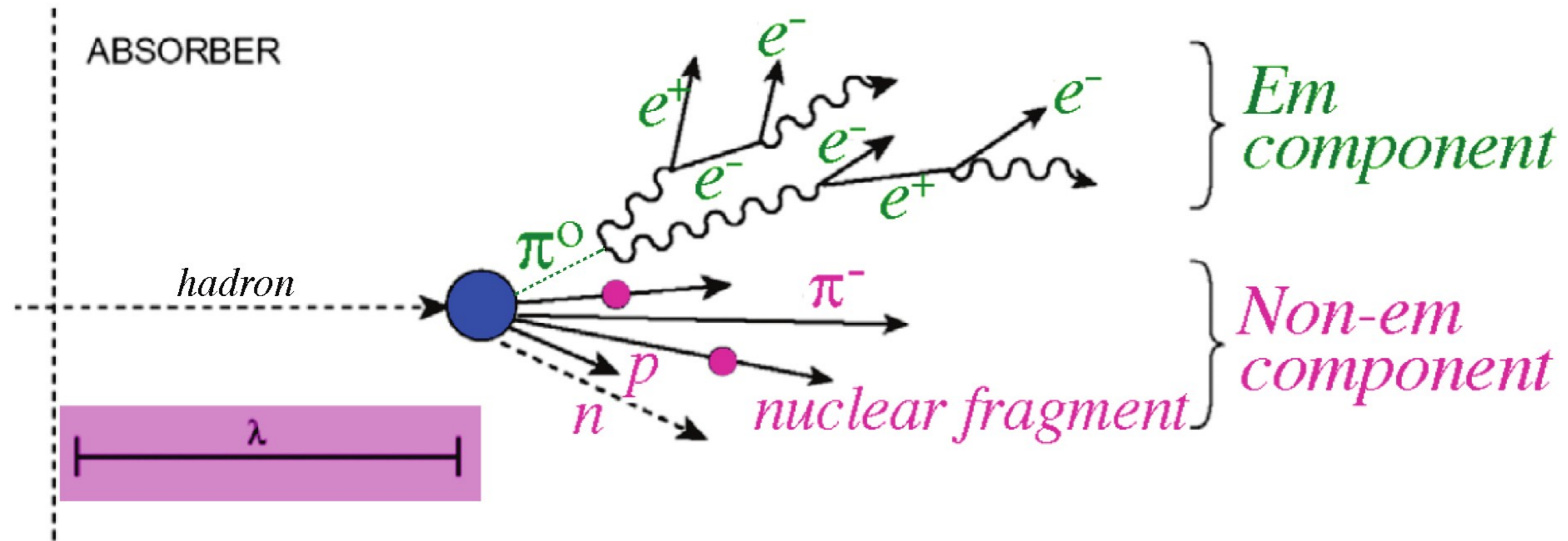
1. Hadron calorimetry issues
2. Dual-readout calorimetry
3. Few DREAM/RD52 results
4. Dual readout goes granular ( IDEA fibre calorimeter )
5. Exploit timing and DNNs
6. Crystal option (IDEA++) and pPFA
7. Next steps

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# 1. Hadron calorimetry issues

# hadron calorimetry

Due to  $\pi^0$  and  $\eta$  production, hadronic showers develop 2 main components:



hadronic component:  $p$ ,  $n$ ,  $\pi^\pm$ , nuclear fission, ... delayed photons, ...

shower typical size:  $\lambda_1 \sim 35 \text{ g/cm}^2 \cdot A^{1/3}$



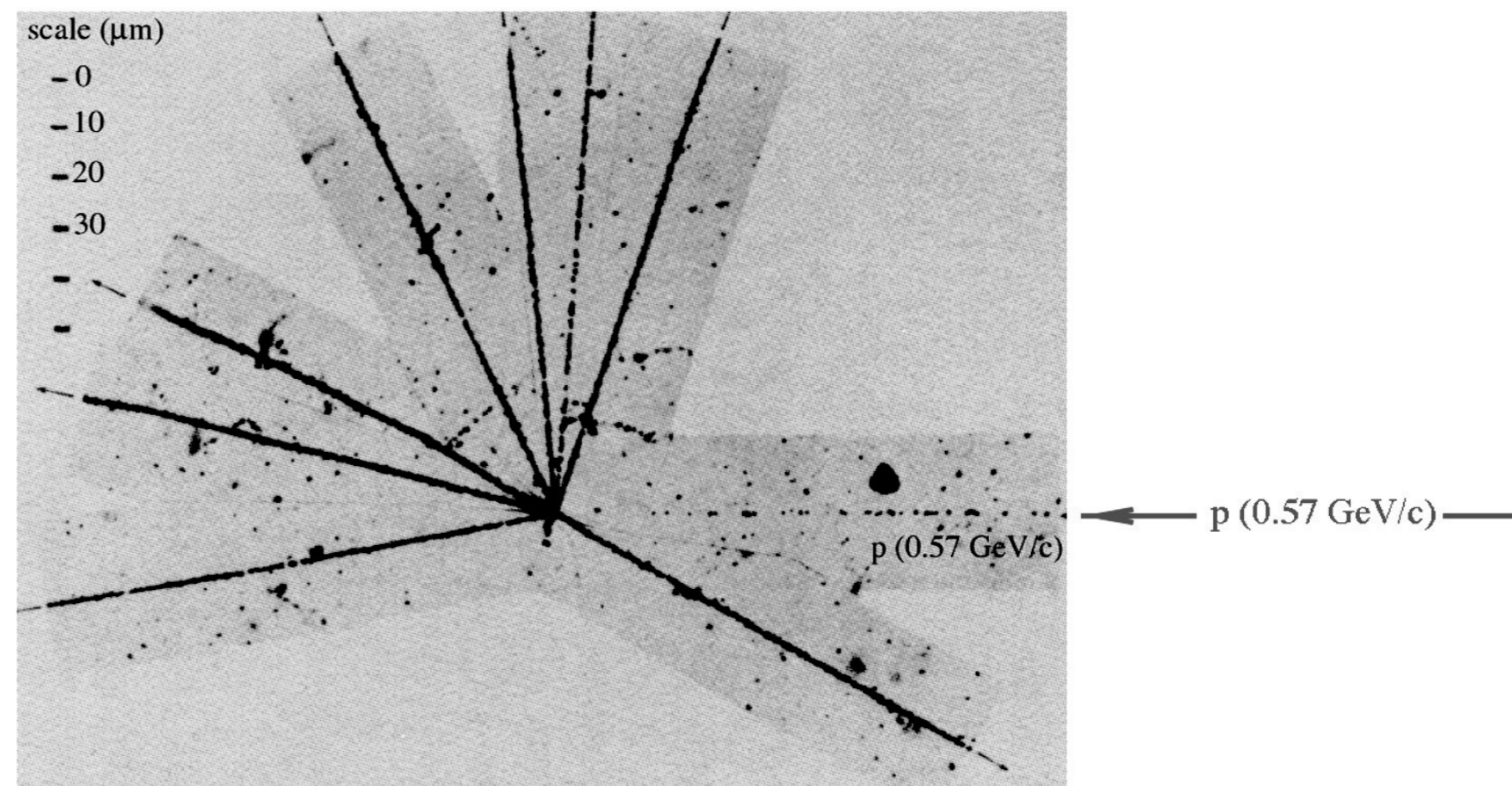
# hadronic showers

- **Electromagnetic (em) component**

- electrons, photons

- **Hadronic (non-em) component**

- charged mesons  $\pi^\pm$ ,  $K^\pm$  [ ~ 20% ]
- nuclear fragments, p [ ~ 25% ]
- neutrons, soft  $\gamma$ 's [ ~ 15% ]
- break-up of nuclei ("invisible") [ ~ 40% ]



average values ... issue: fluctuations!

Many components w/ large fluctuations in relative yield

1. Large non-gaussian fluctuations in em/non-em energy sharing
2. Increase of *em* component with energy
3. Large, non-gaussian fluctuations in "invisible" energy losses

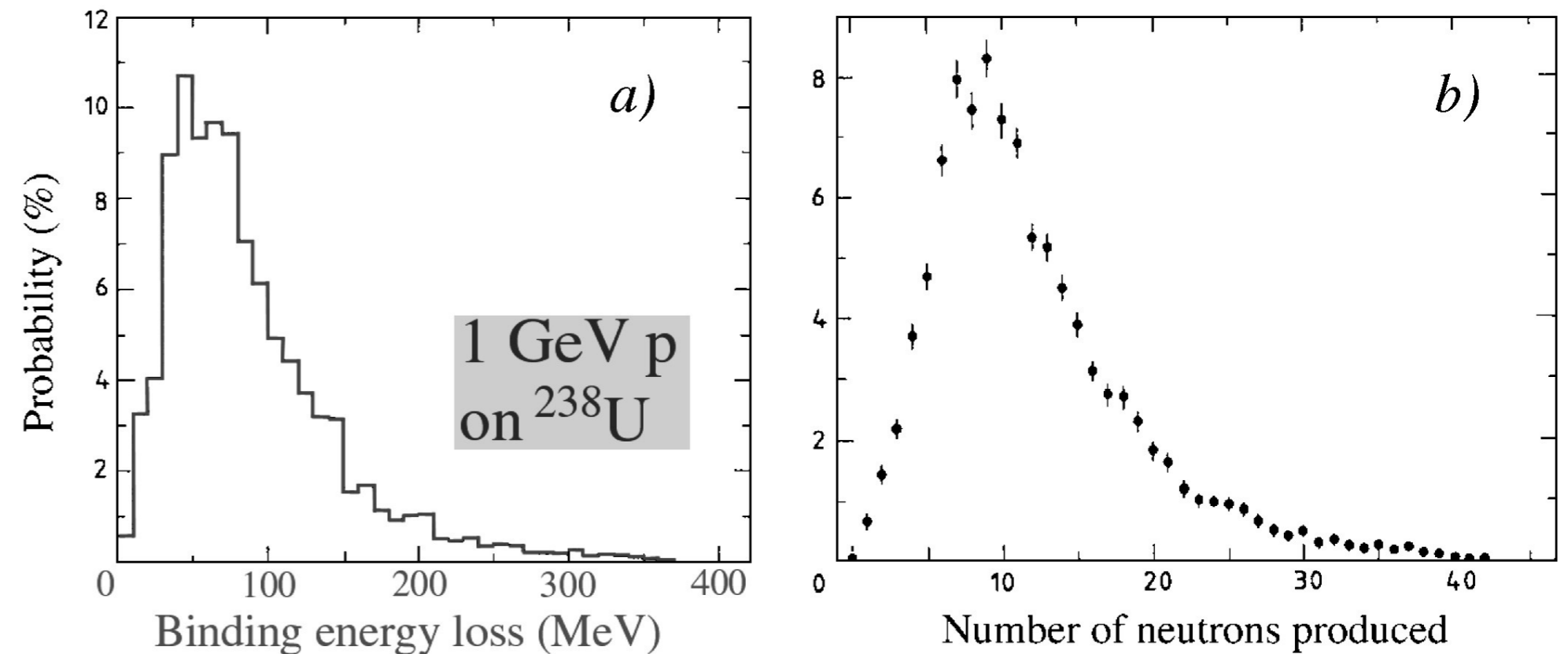
# invisible energy

- ◆ in nuclear reactions, energy lost (binding energy) to free protons and neutrons
- ◆ no measurable signal (invisible energy)
- ◆ on average about 30-40% of non-em shower energy

Large event-by-event fluctuations limit resolution

Correlation between invisible energy and kinetic energy carried by released nucleons

Evaporation nucleons: soft spectrum, mostly neutrons (2-3 MeV)



Wigmans, NIM A259, 389

# em fraction $f_{em}$

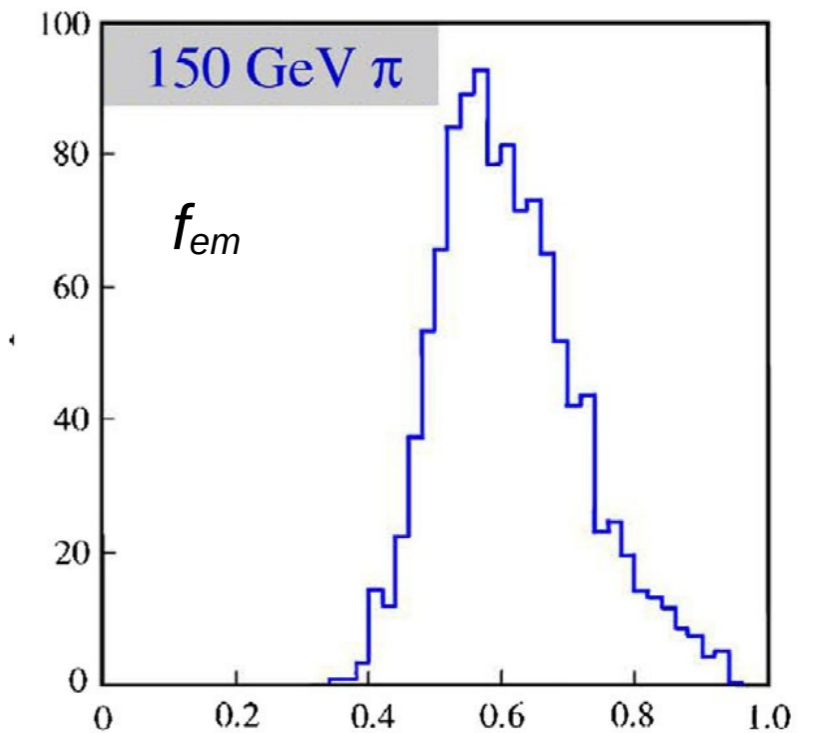
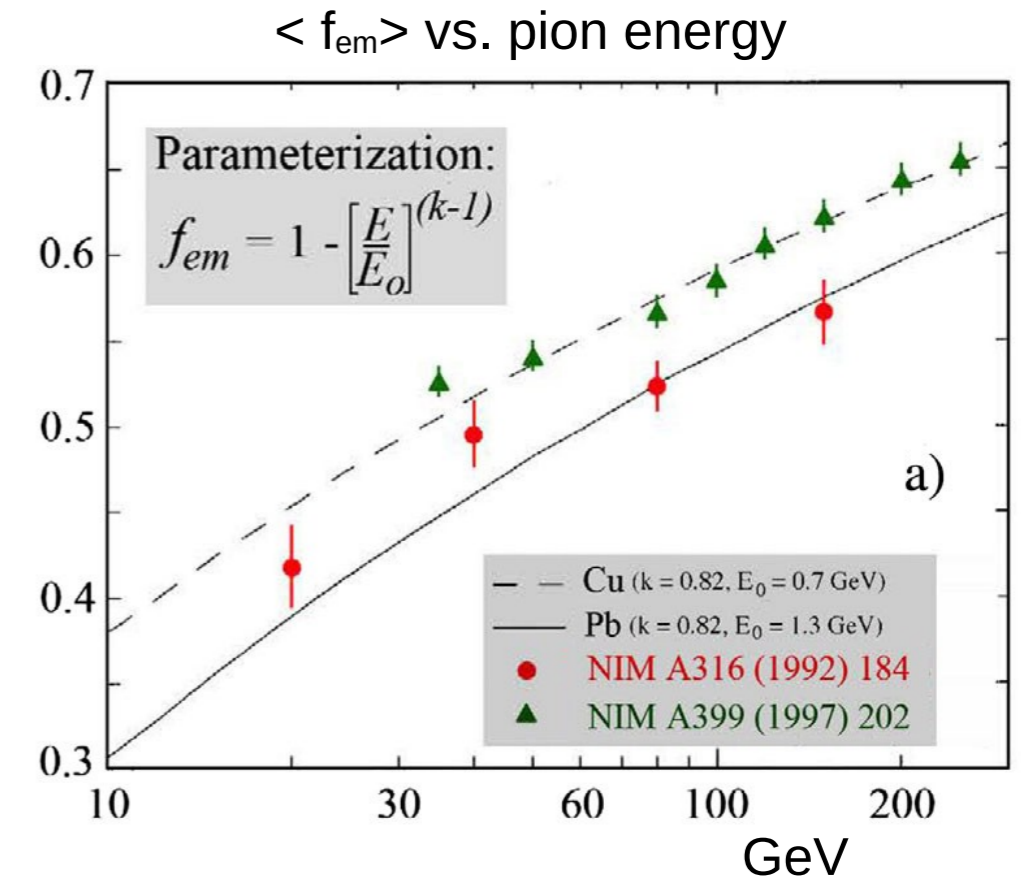
Shower energy fraction mainly carried by  $\pi^0$  (but also  $\eta$ ) mesons  
For shower initiated by charged pions:

$$\langle f_{em} \rangle = 1 - \left( \frac{E}{E_0} \right)^{(k-1)}$$

$E_0$ : average energy for single  $\pi^0$  production,  $k \approx 0.8 < \sim 1$

$\langle f_{em} \rangle$  large and energy dependent

fluctuations in  $f_{em}$  large and non-poissonian



DOI: 10.1103/RevModPhys.90.025002

# detector response

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Response:

detected signal per unit energy deposit

e.g. number of scintillating (or Cherenkov) p.e. / deposited GeV

Hadronic showers:

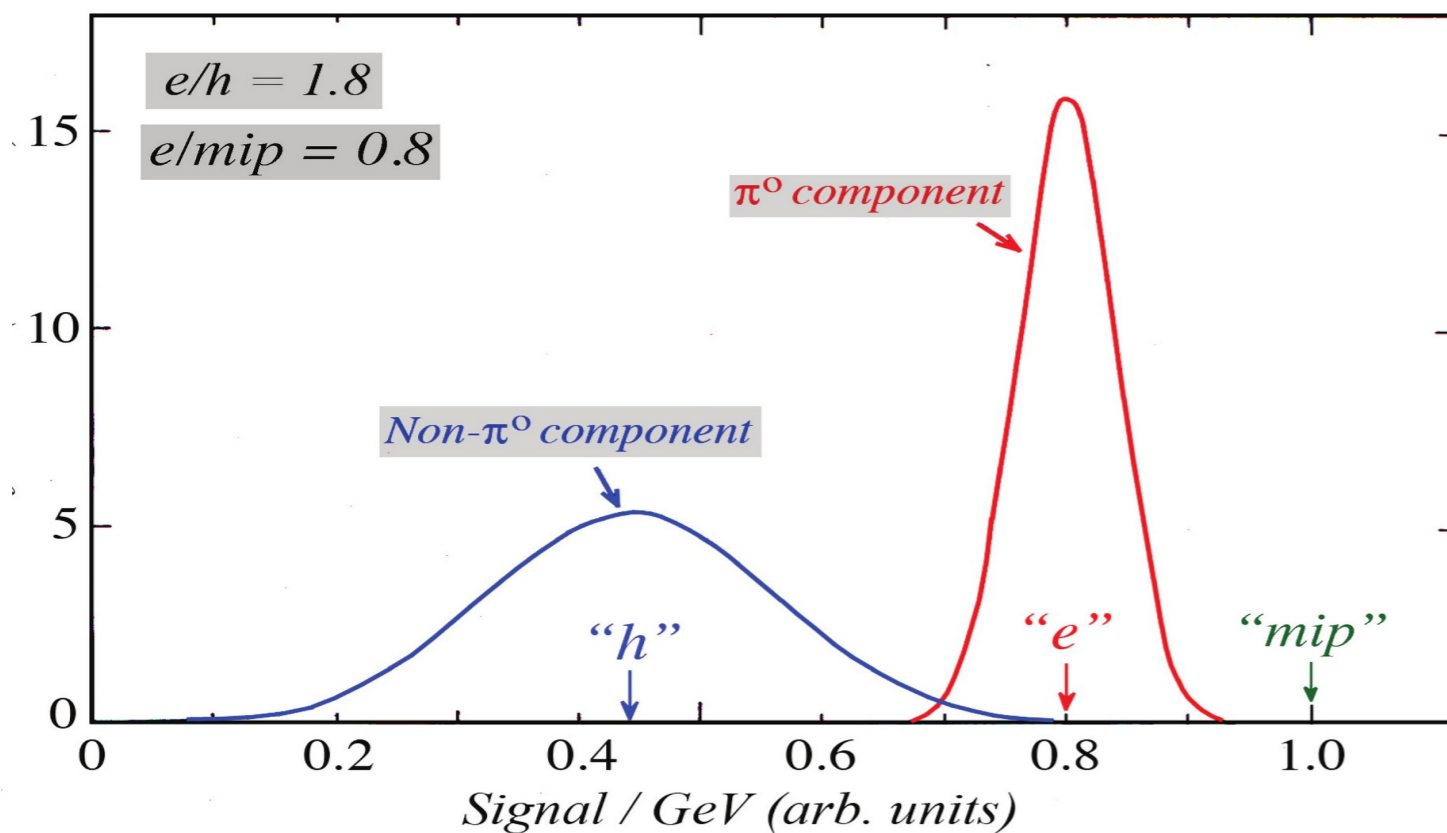
em component → response e

hadronic component → response h

what about relative ratio (e/h) ?



# detector response to hadronic showers



$e \neq h$

e.g. (left plot):

only  $1/1.8 \approx 56\%$  of non- $\pi^0$  energy accounted by signal

$e/h$  ratio: detector characteristic

typically,  $\sim 2$  for crystals, in range 1-1.8 for sampling calorimeters

Nevertheless:

- 1)  $e/\pi$  depends on energy ( $f_{em}$  depends on  $E$  and shower “age”)
- 2)  $\langle f_{em} \rangle$  different for  $\pi$ ,  $K$ ,  $p$   $\rightarrow$  response depends on particle type

# response to hadronic showers

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Response to protons ?

Average signal for protons:  $S_p = e \cdot \langle f_{em}(p) \rangle \cdot E + h \cdot (1 - \langle f_{em}(p) \rangle) \cdot E$

→ Response:  $R_p = S_p / E \equiv p, \quad \langle f_{em}(p) \rangle \equiv f_p = f_p(E)$

→  $p = e \cdot f_p + h \cdot (1 - f_p) = h \cdot (1 + f_p \cdot (e/h - 1))$

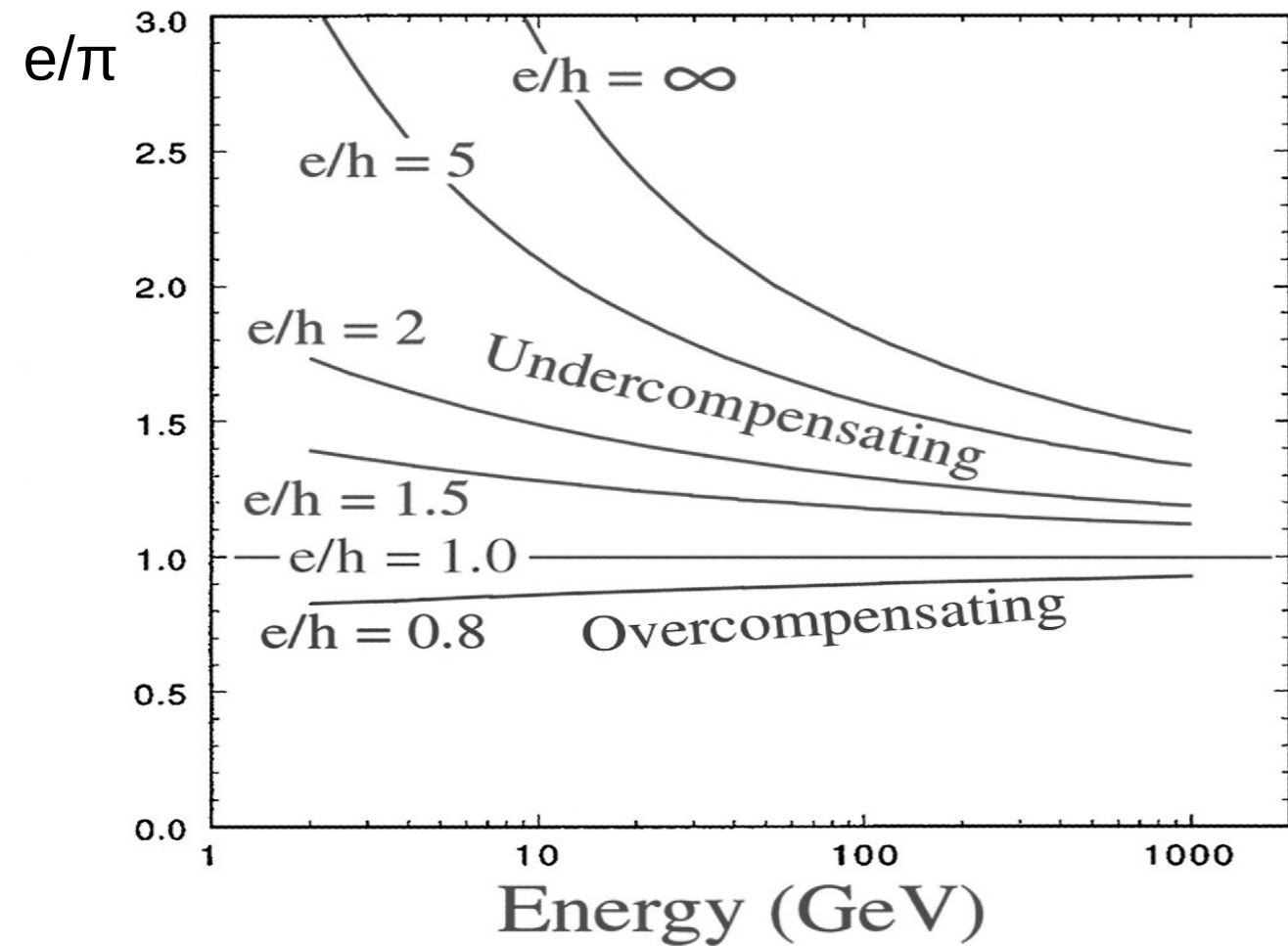
$e/p = e/h / (1 + f_p \cdot (e/h - 1)) \rightarrow$  do we have a problem ?

# e/π ratio

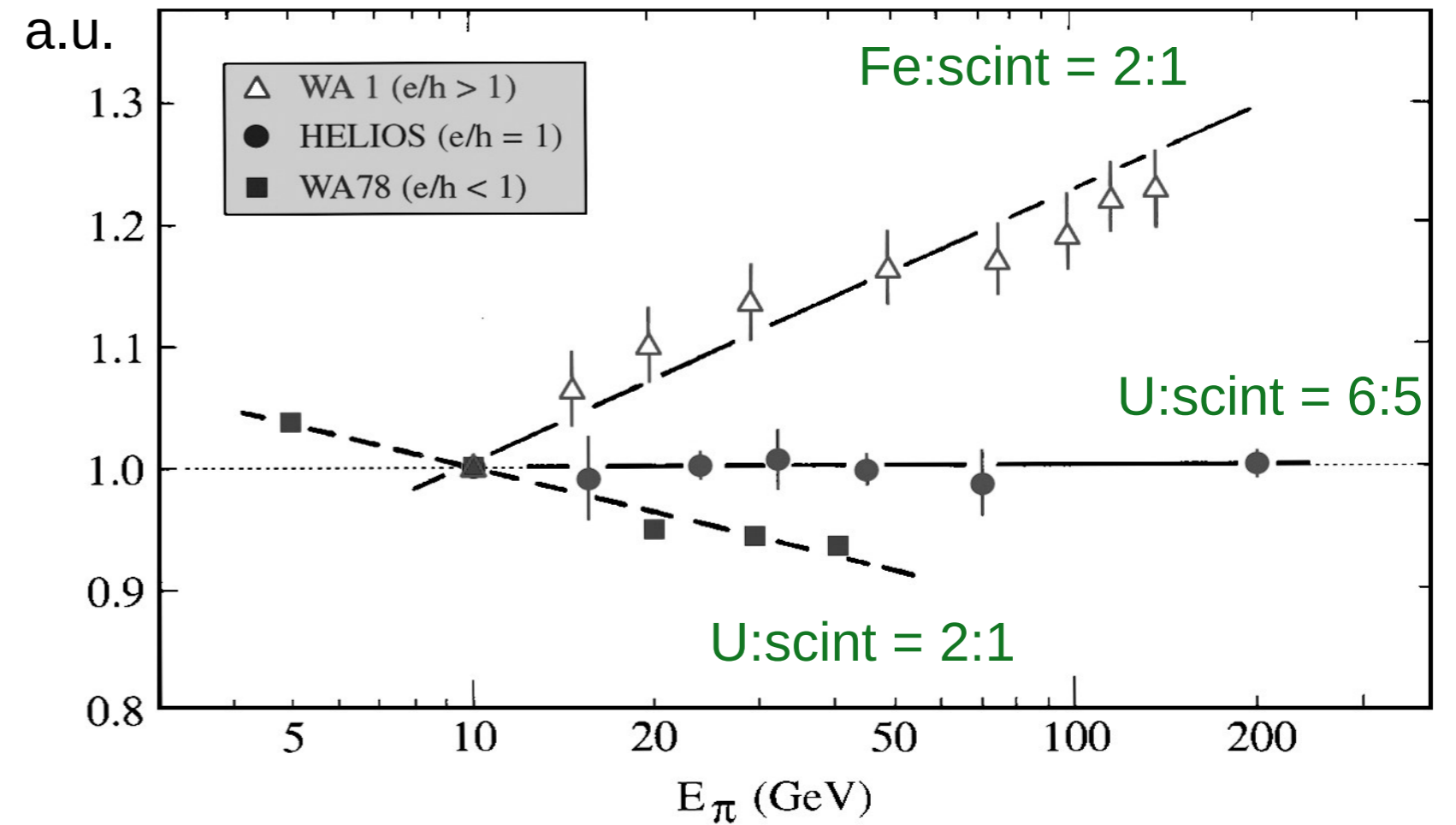
As well, calorimeter response to charged pions: π

$$e/\pi = e/h / ( 1 + f_{\pi} \cdot ( e/h - 1 ) ) \quad f_{\pi} \equiv \langle f_{em}(\pi) \rangle \neq f_p$$

e/π as function of E



Response to π as function of E



response to π as function of E

# compensation in hadron calorimetry

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$e/h = 1 \rightarrow$  compensating calorimeter

1) increase  $h \rightarrow$  boost hadron response

e.g. by adding hydrogen or Uranium, both acting as “neutron converters”

$\rightarrow$  large integration volume and time

2) decrease  $e \rightarrow$  decrease em sampling fraction or frequency  $\rightarrow$  spoil em performance

$\rightarrow$  tune active / passive material ratio



# e/mip ratio

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mip : minimum ionising particle → only ionisation

dE/dx (mip) :

lead ~ 12.6 MeV/cm → 7 MeV/X<sub>0</sub>

copper ~ 12.7 MeV/cm → 18 MeV/X<sub>0</sub>

( PMMA ~ 2.3 MeV/cm → 78 MeV/X<sub>0</sub> )

Moreover in high-Z absorbers :

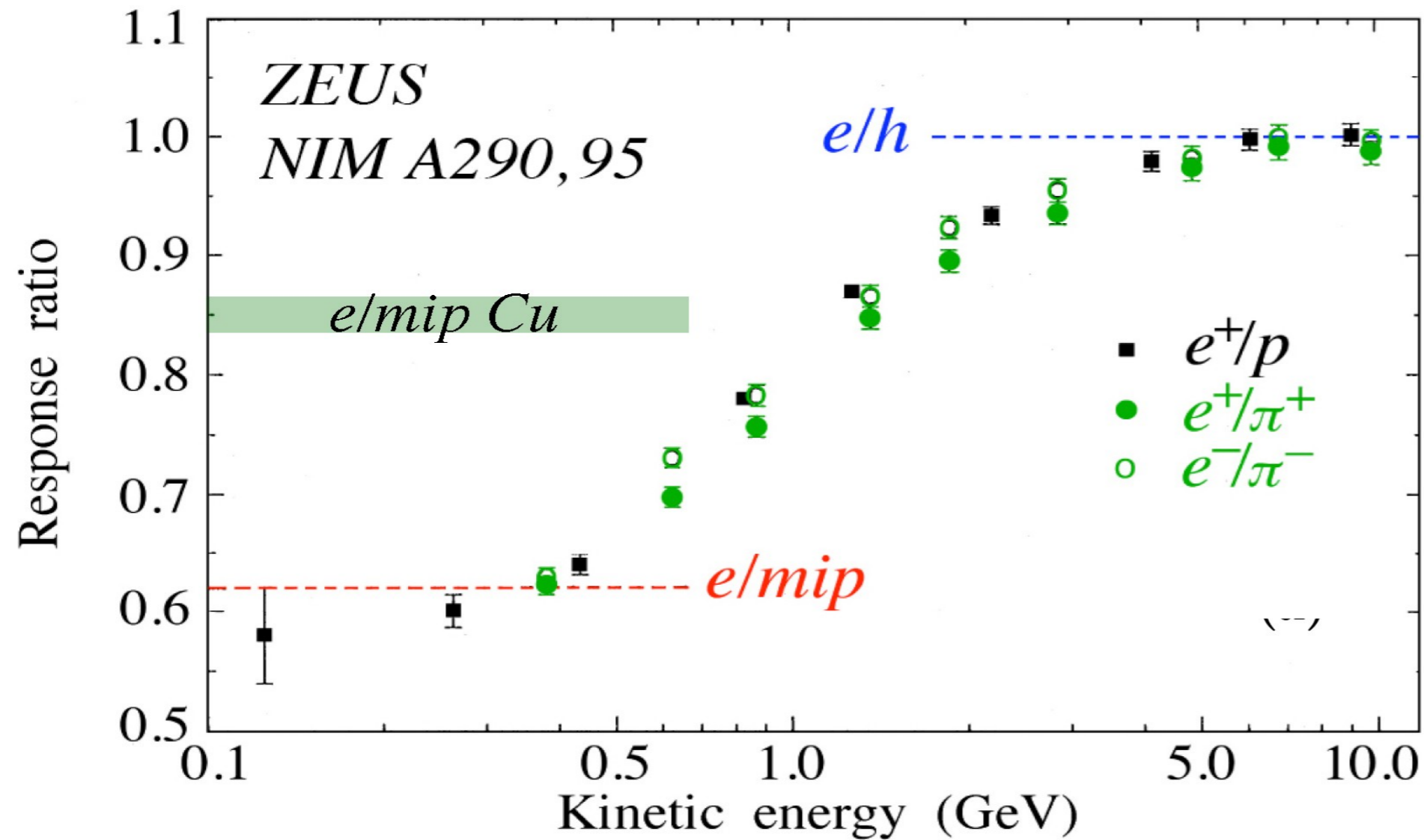
**Z<sup>5</sup> dependence of photoelectric effect** → most soft-γ interact in absorber

**photoelectrons have very short range** → contribute to signal only close to boundaries

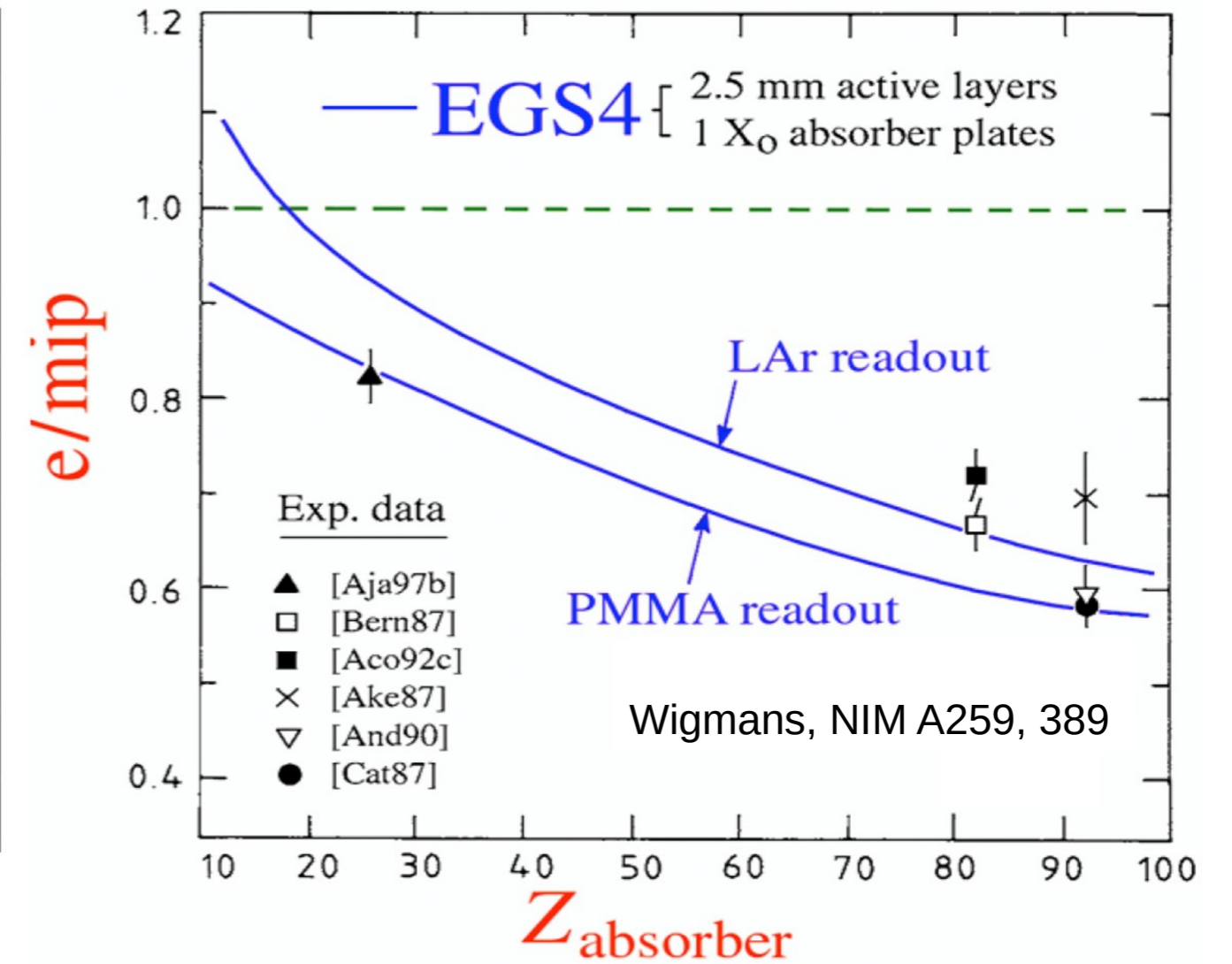
→ response to em showers suppressed wrt. mips

# e/mip ratio

Low-energy response ( compensating calorimeter! )



Non-linearity at low energy with high-Z absorbers (U, Pb)



Mitigated with low-Z absorbers (Cu)

Relevant for jet detection ... should we really care about ?

# what compensation does and does not

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- ◆ NO guarantee for high resolution

- ◆ fluctuations in  $f_{em}$  are canceled but others may be very large

- ◆ Has drawbacks

- ◆ high-Z absorber required → small e/mip → non linearity @ low energy

- ◆ low sampling fraction required → em resolution limited

- ◆ relies on neutrons → integration over large volume and time

- ◆ SPACAL: to get  $30\%/√E$  ~15 tonnes of lead and ~50 ns integration time

- 

- ◆ high-res em and high-res hadron calorimetry mutually exclusive:

- ◆ good jet energy resolution ⇒ compensation

- ⇒ small sampling fraction (~3%) ⇒ poor em resolution

- ◆ good em resolution ⇒ high sampling fraction (100% crystals, 20% LAr)

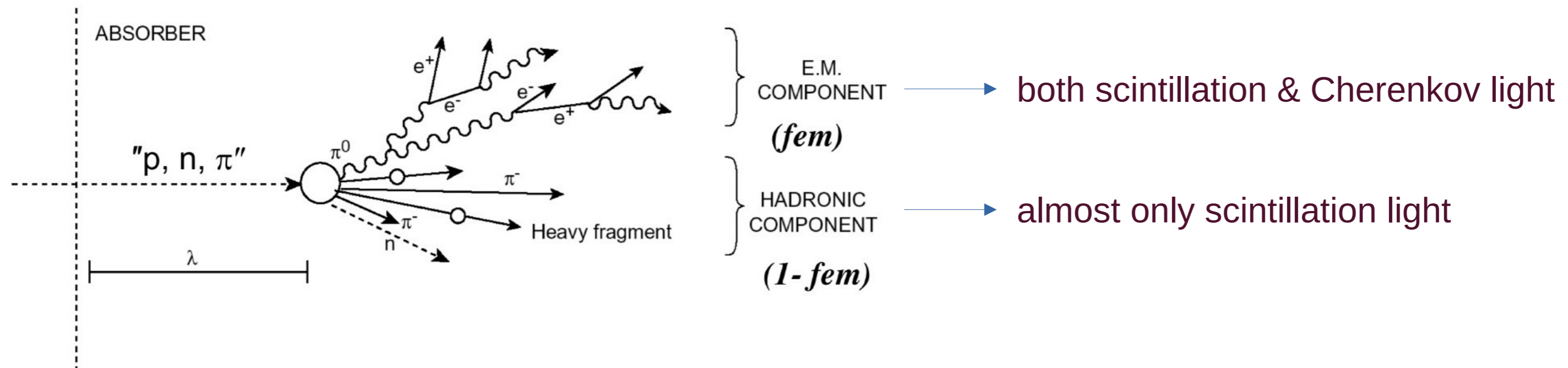
- ⇒ large non compensation ⇒ poor jet resolution

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## 2. Dual-readout calorimetry

# dual-readout calorimetry

Disentangle relativistic (i.e. electromagnetic) and non relativistic (i.e. nuclear) components of hadronic shower



→ get (compensate for)  $f_{em}$  event by event

# dual-readout algebra

$$S = E \times [ f_{em} + s \times (1 - f_{em}) ]$$

$$C = E \times [ f_{em} + c \times (1 - f_{em}) ]$$

$f_{em}$  = electromagnetic shower fraction

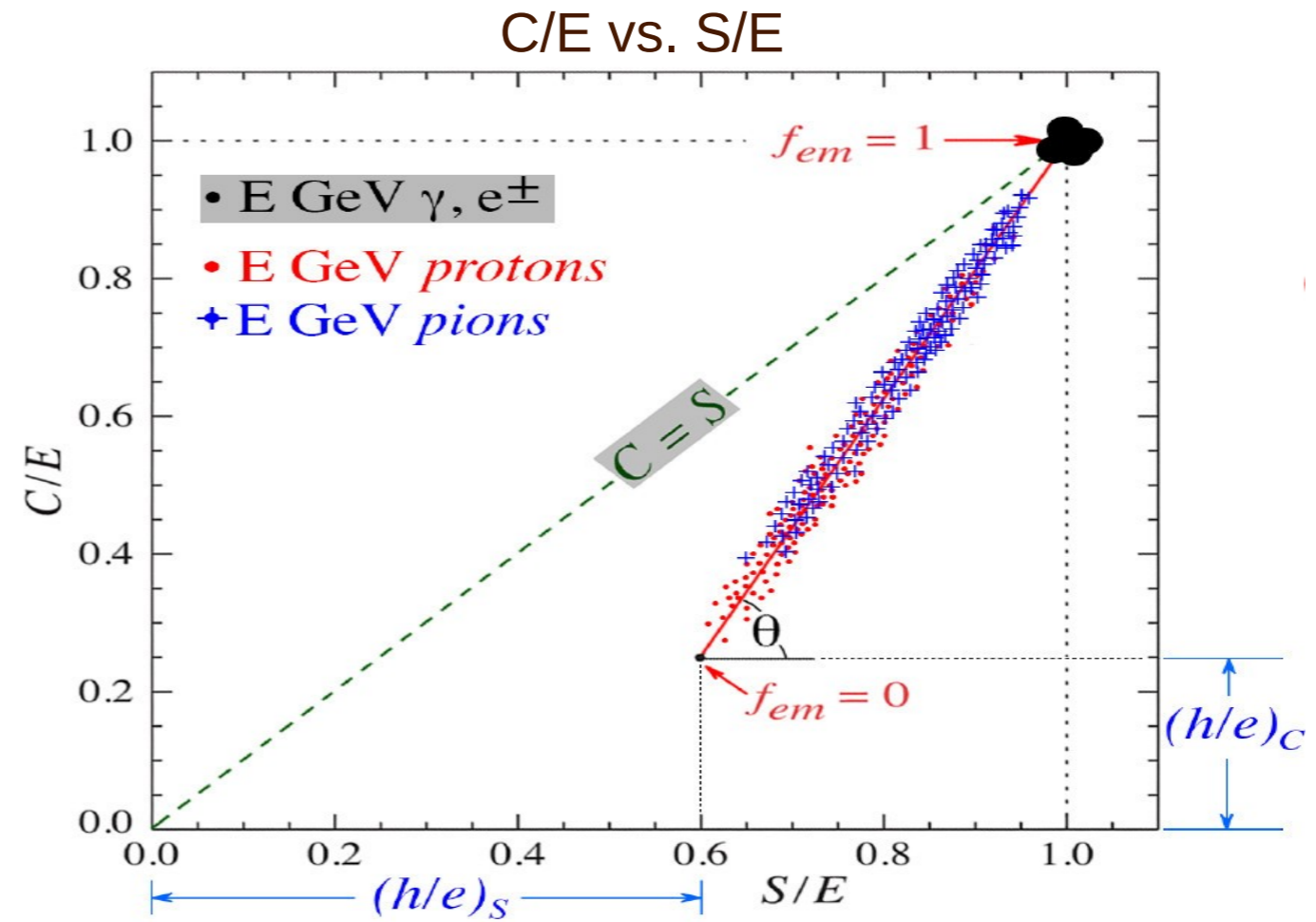
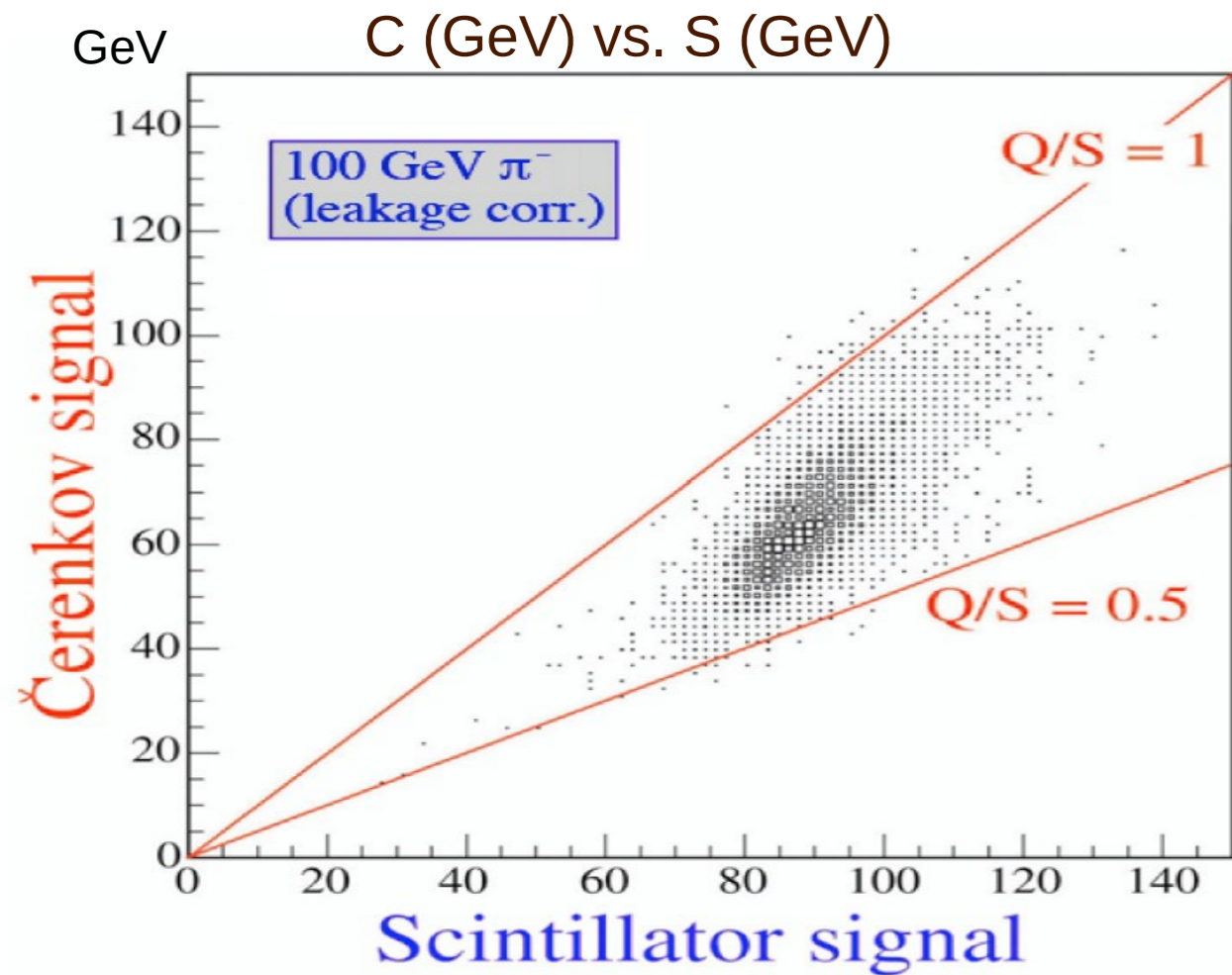
$s = (h/e)_s$  ,  $c = (h/e)_c$  : detector-specific constants

by solving the system, both  $E$  and  $f_{em}$  can be reconstructed

$E$  measured at em energy scale



# applying dual-readout formulae



Hadronic data points (S, C) located nearby straight lines

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$$E = \frac{S - \chi C}{1 - \chi}$$

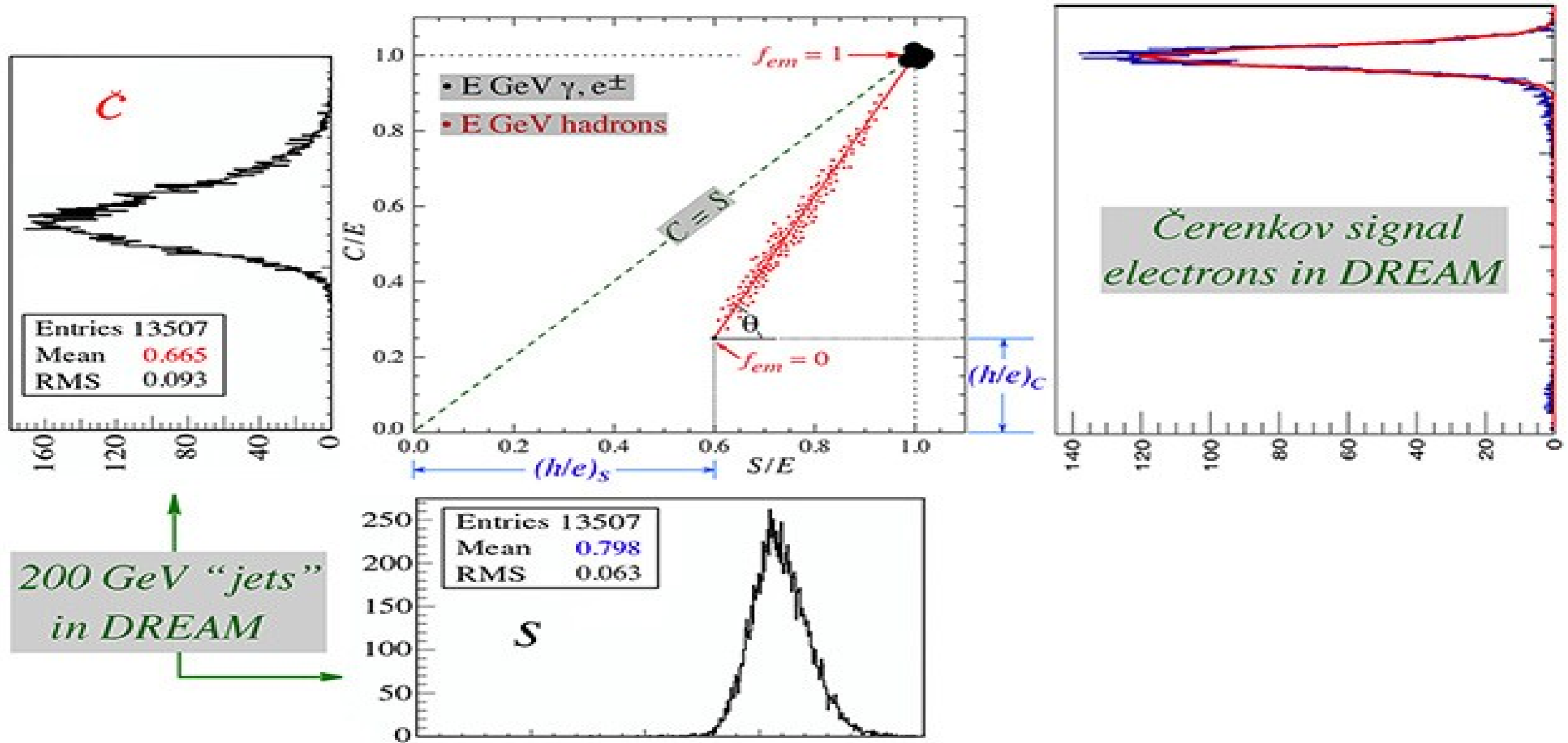
*is universally valid*

$$\cot \theta = \frac{1 - (h/e)_s}{1 - (h/e)_c} = \chi$$

$\theta, \chi$  independent of both:

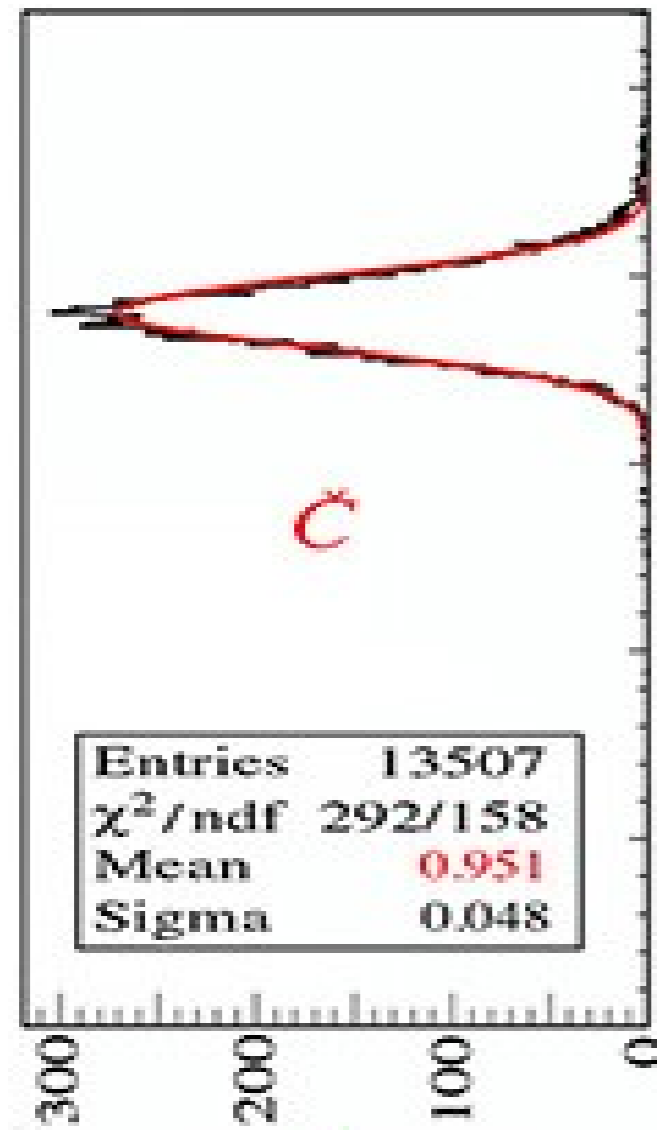
- i) energy (!)
- ii) type of hadron (!!)

# before dual-readout correction

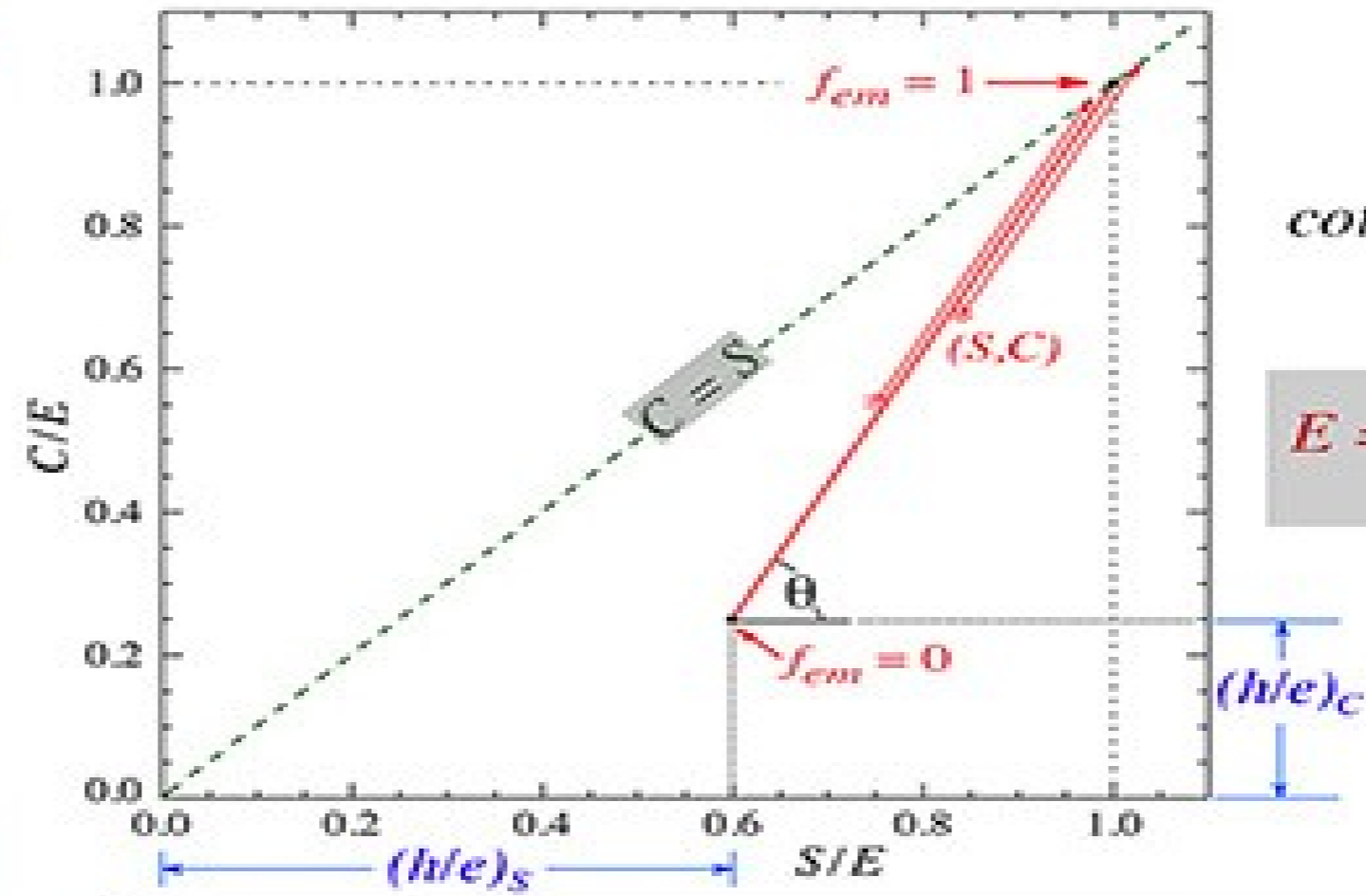




# after dual-readout correction

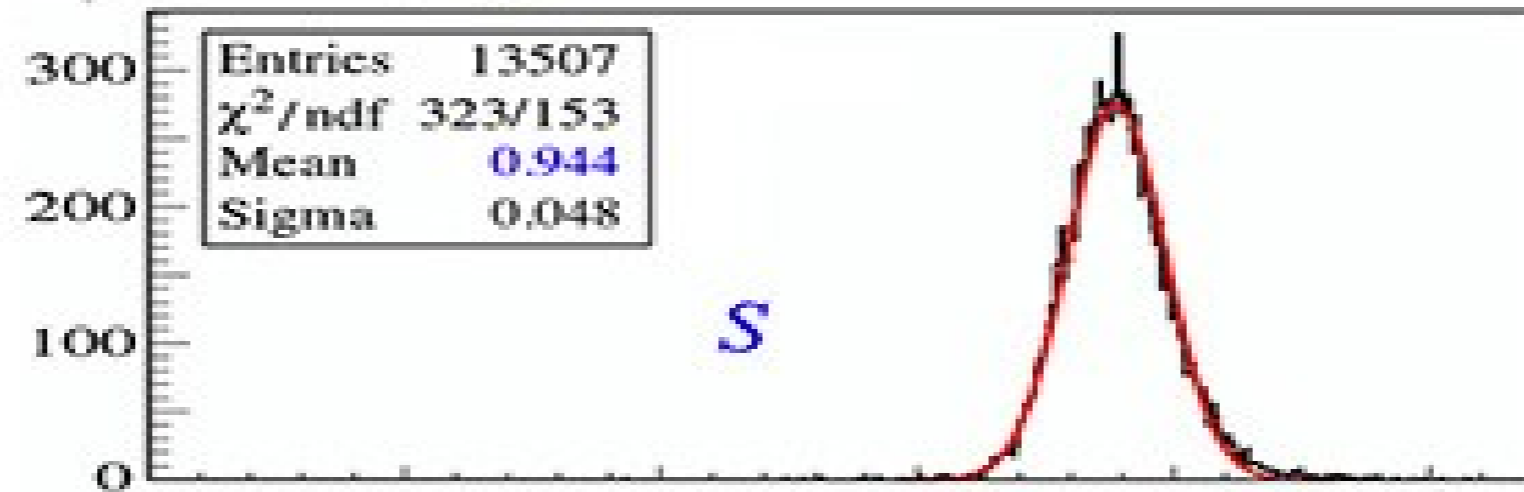


200 GeV "jets"  
in DREAM



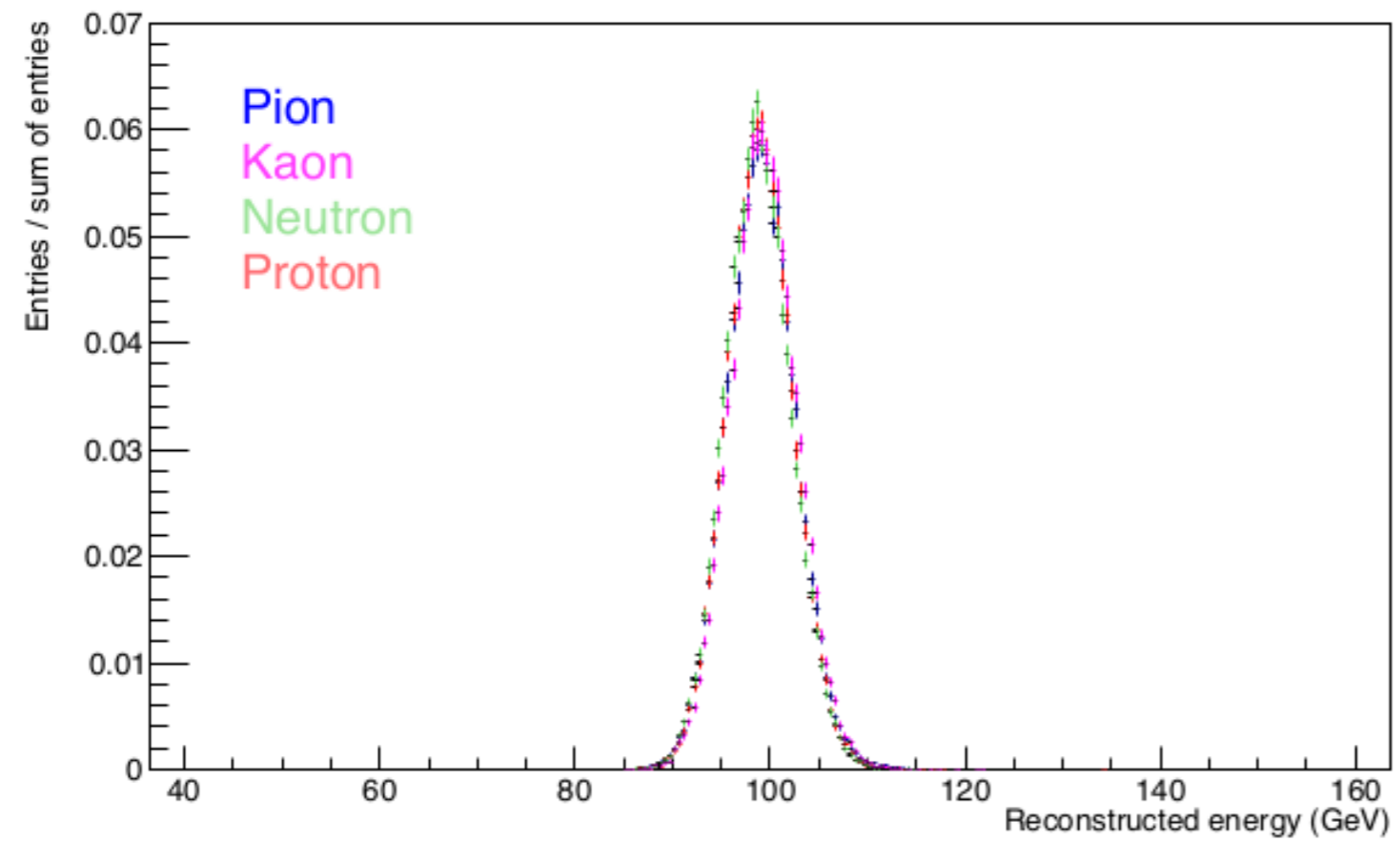
$$\cot \theta = \frac{1 - (h/e)_s}{1 - (h/e)_c} = \chi$$

$$E = \frac{S - \chi C}{1 - \chi}$$

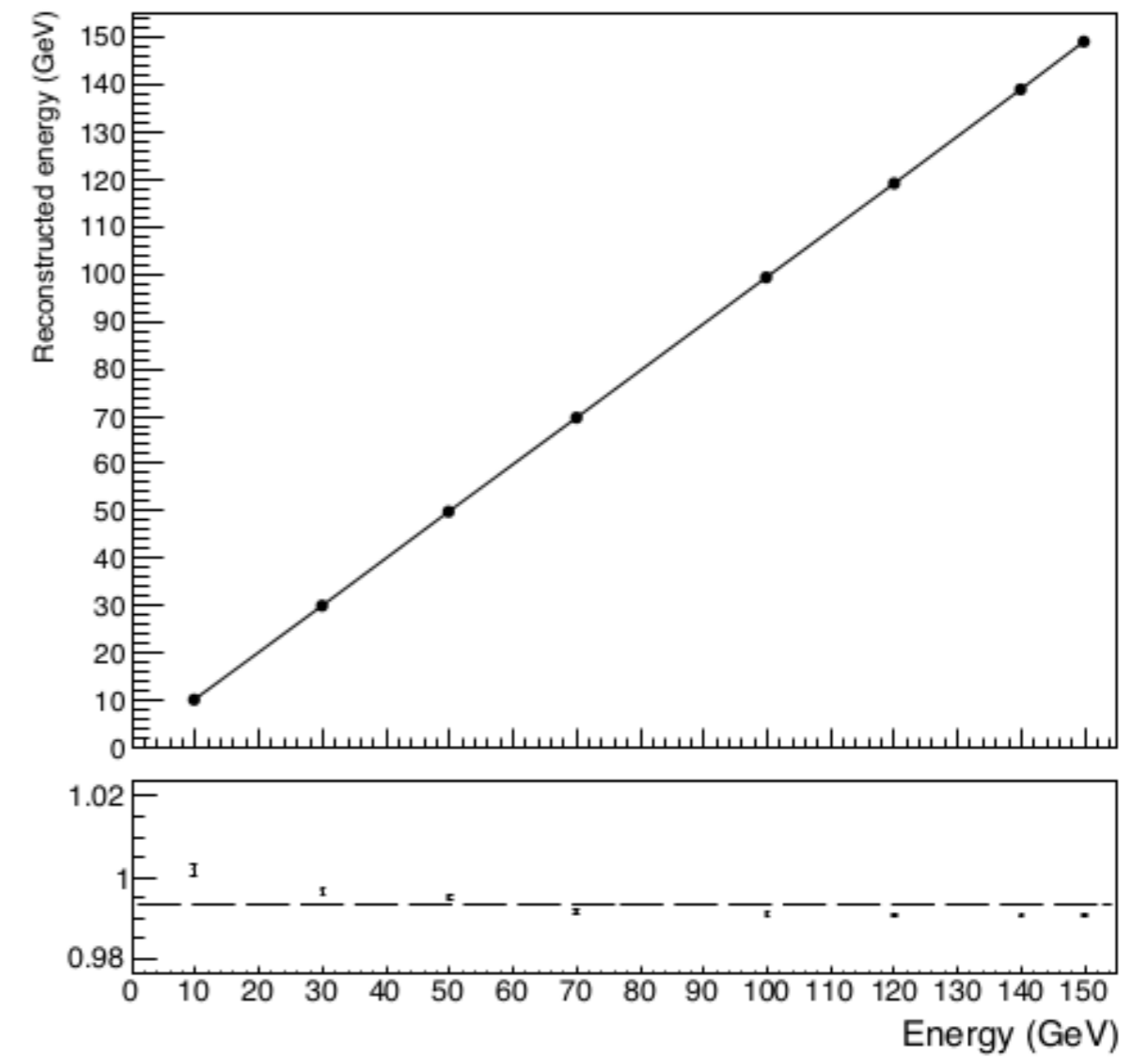


# Geant4 simulations

100 GeV hadrons



10-150 GeV  $\pi^-$



$$C/S = [ f_{em} + s \times (1 - f_{em}) ] / [ f_{em} + c \times (1 - f_{em}) ]$$

→ C/S depends only on  $f_{em}$  so that

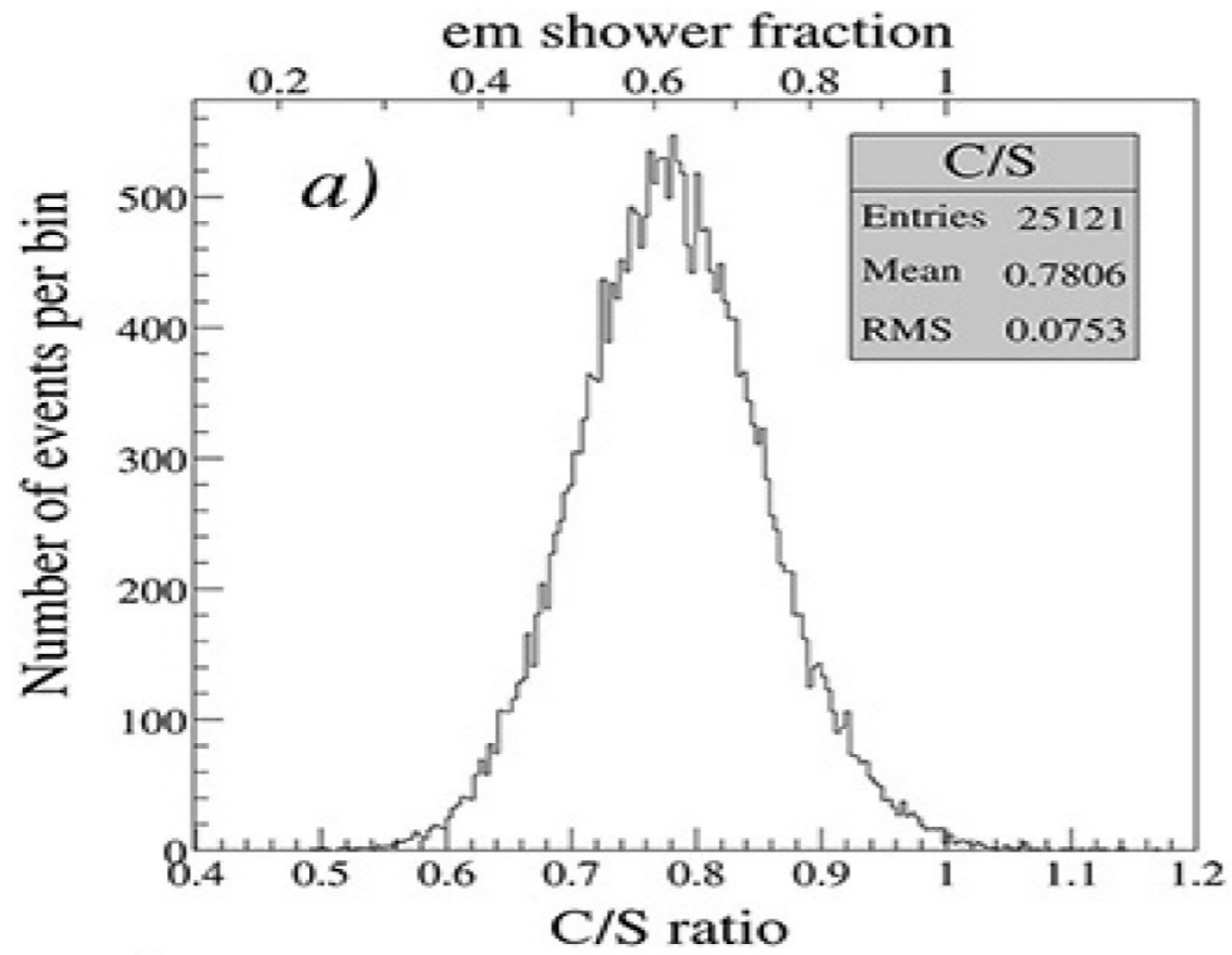
$$f = \frac{c - s(C/S)}{(C/S)(1 - s) - (1 - c)}$$

→  $f_{em}$  depends only on C/S → can use C/S to select  $f_{em}$  subsamples

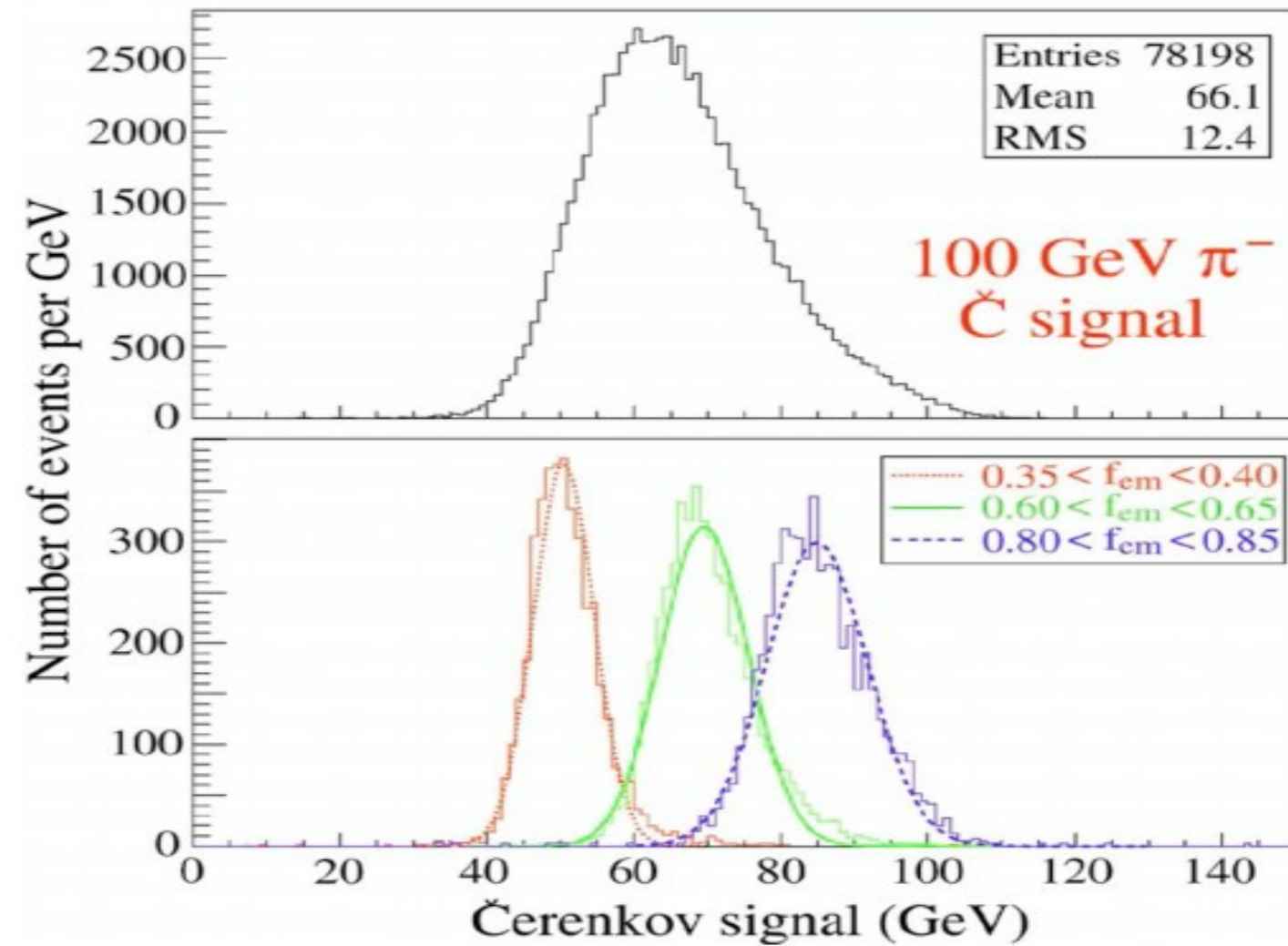
to get  $f_{em}$  absolute value, at least one of (h/e) factors needs to be known

[ or extracted e.g. by fitting  $\langle C/E \rangle$  as function of E ]

# $f_{em}$ fluctuations



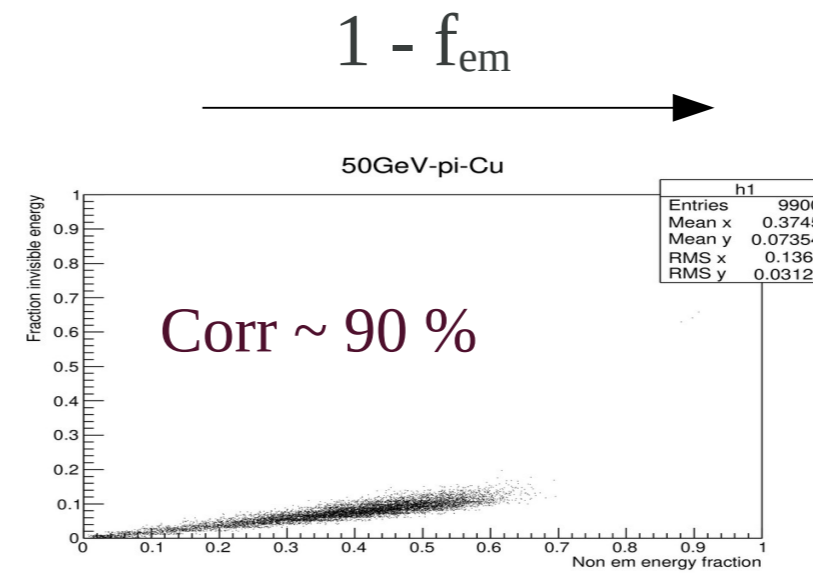
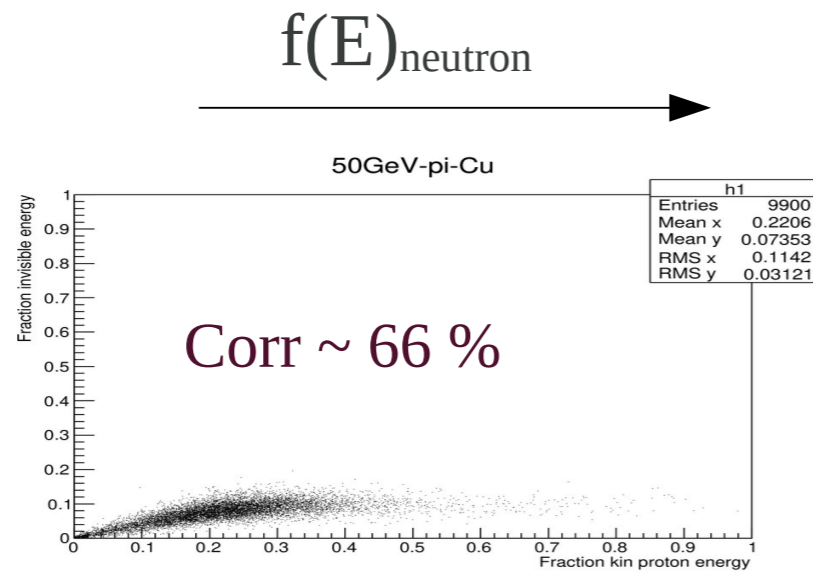
## DREAM: Effect of event selection based on $f_{em}$



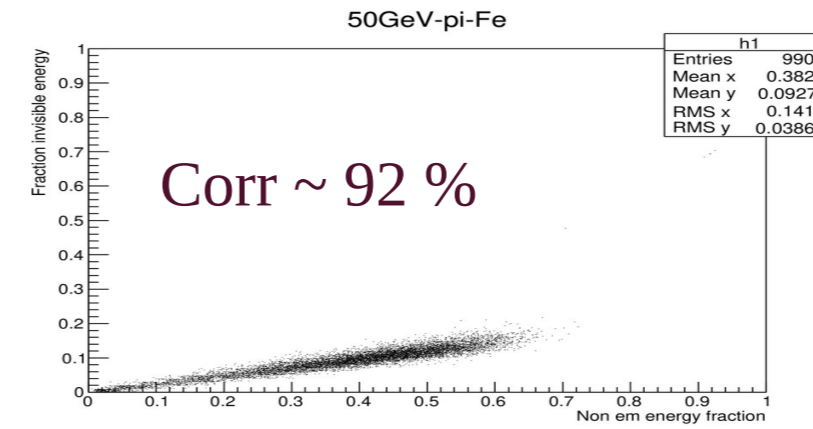
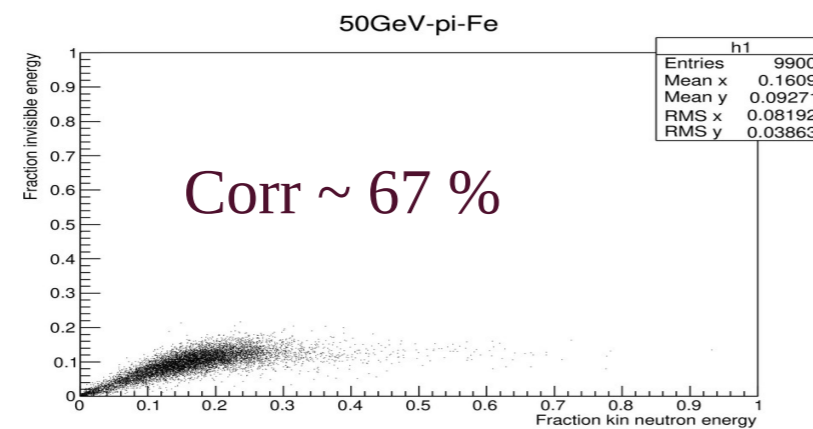
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# invisible energy fraction – Geant4 simulations

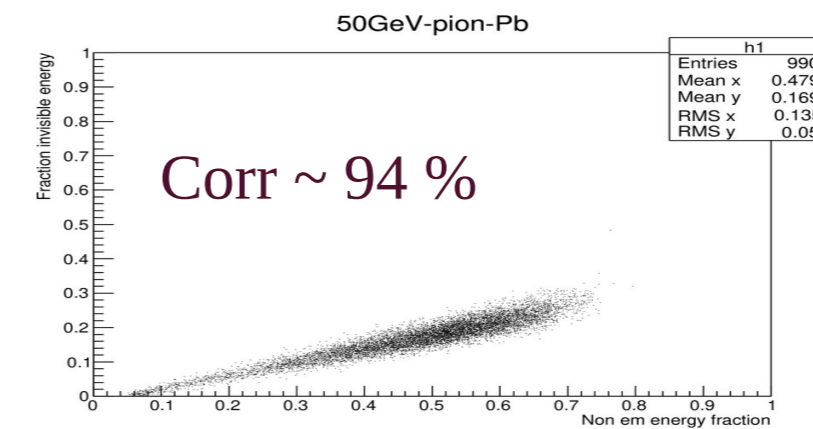
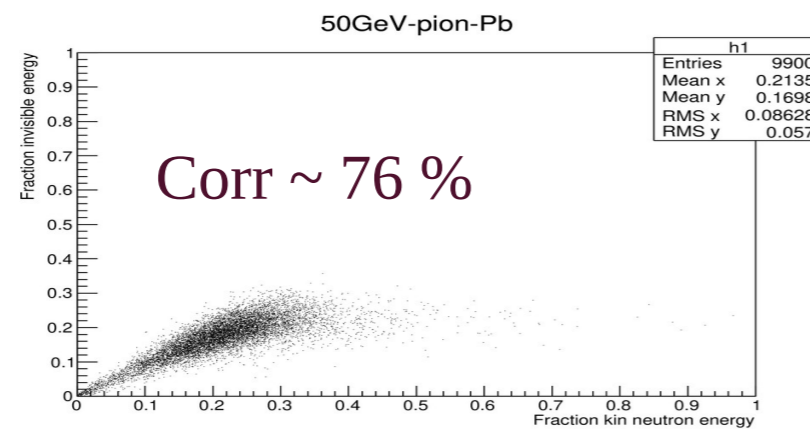
*Copper*



*Iron*



*Lead*



$f_{\text{inv}}$

# back to dual-readout formulae ...

$$E = \frac{S - \chi \cdot C}{1 - \chi}$$

measurable event by event, if  $\chi$  known

$$1 - f_{em} = \frac{1}{1 - \left(\frac{h}{e}\right)_c} \cdot \frac{S - C}{S - \chi \cdot C}$$

measurable if  $\chi$  known

(1-f<sub>em</sub>) can be reconstructed within (unknown) constant factor (>) O(1)

$$\chi = \frac{1 - \left(\frac{h}{e}\right)_s}{1 - \left(\frac{h}{e}\right)_c} = \frac{E - S}{E - C}$$

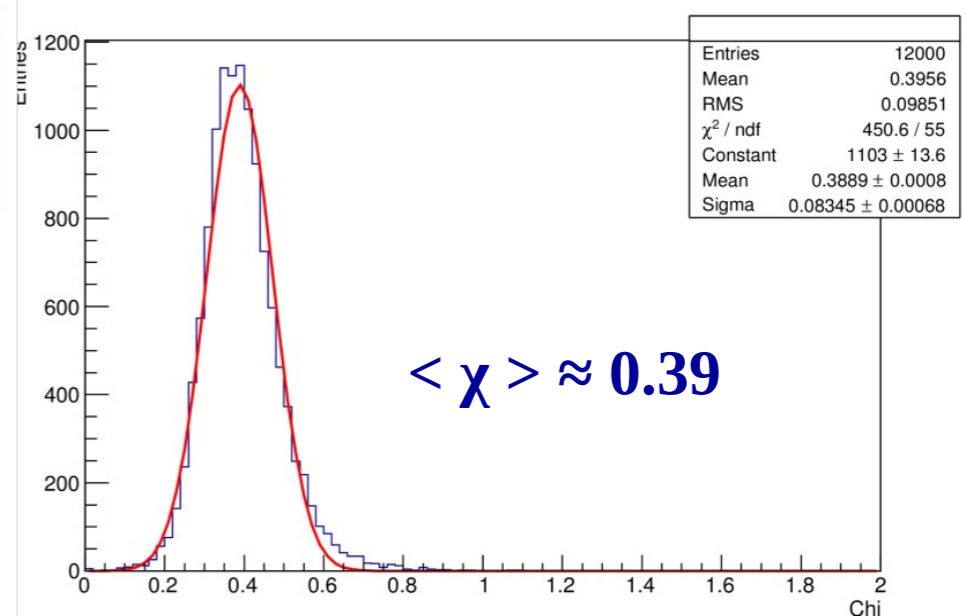
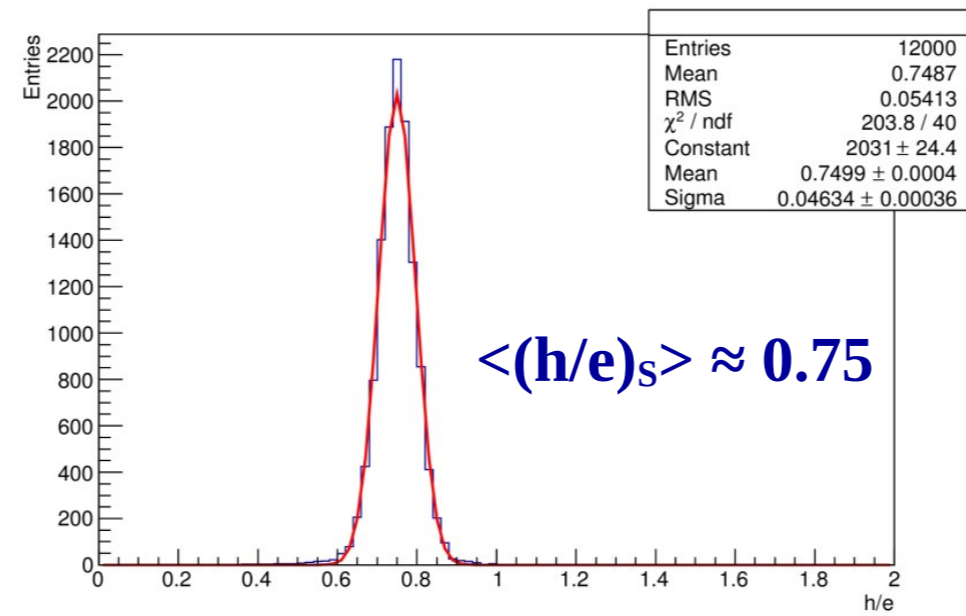
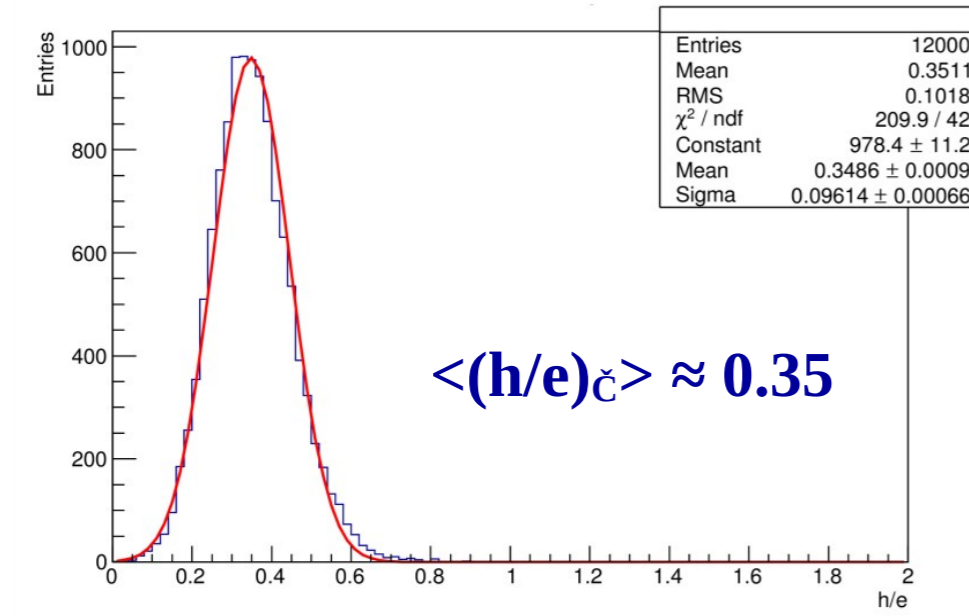
$$\text{if } \left(\frac{h}{e}\right)_s > \left(\frac{h}{e}\right)_c \Rightarrow \chi < 1$$

$\chi$  measurable if E known

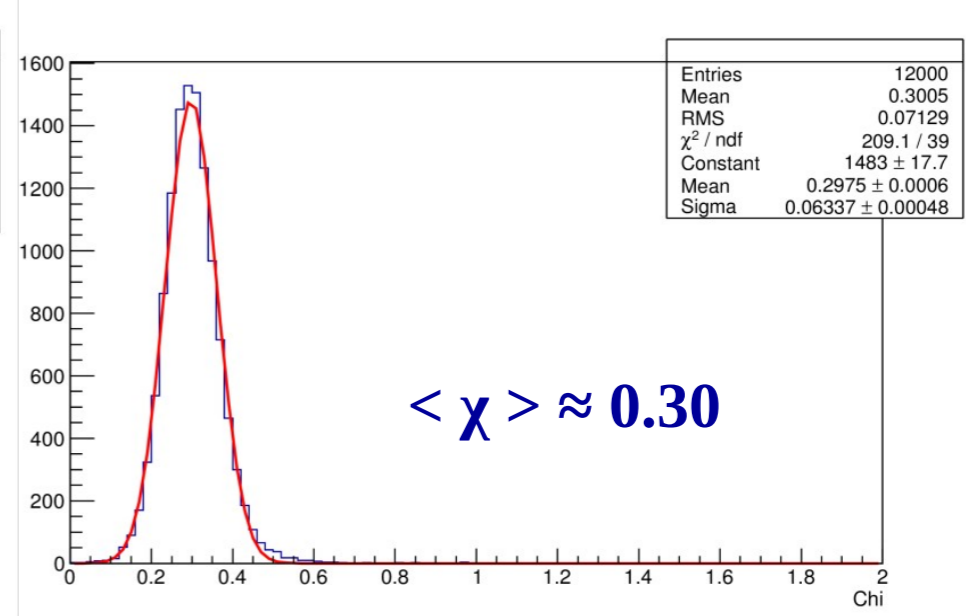
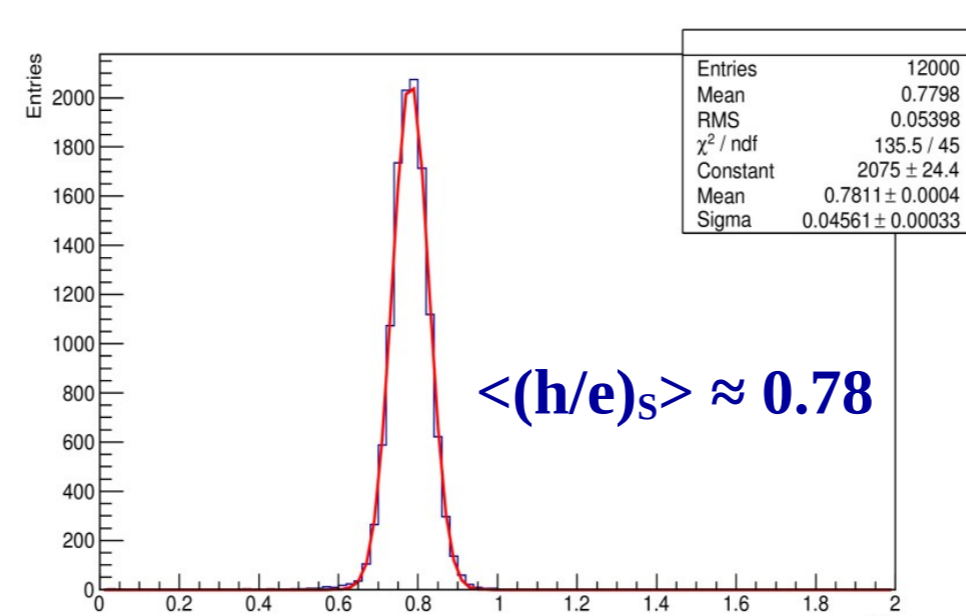
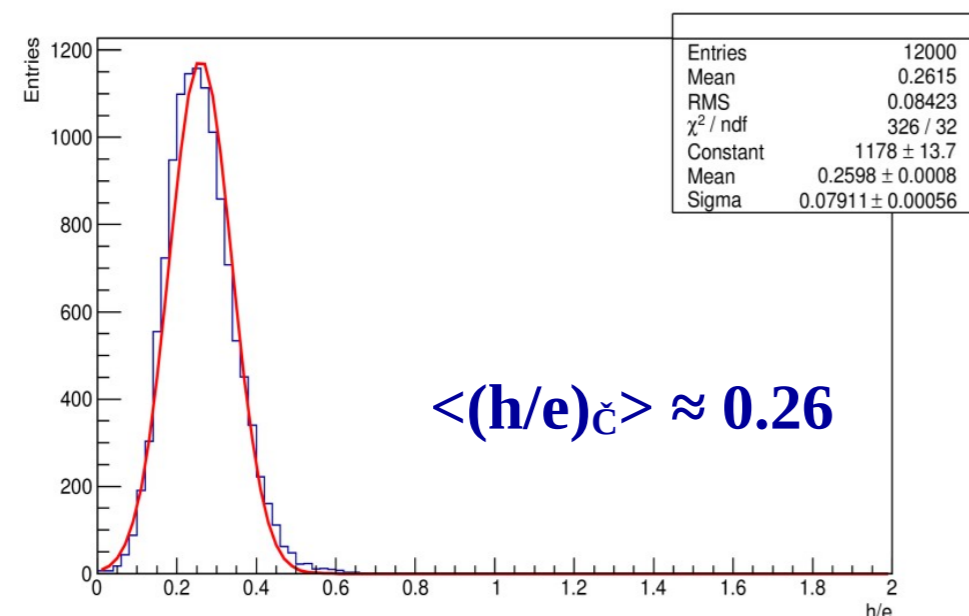
$\chi$  can be extracted from testbeam data



# Geant4 simulations – (h/e) and $\chi$ factors



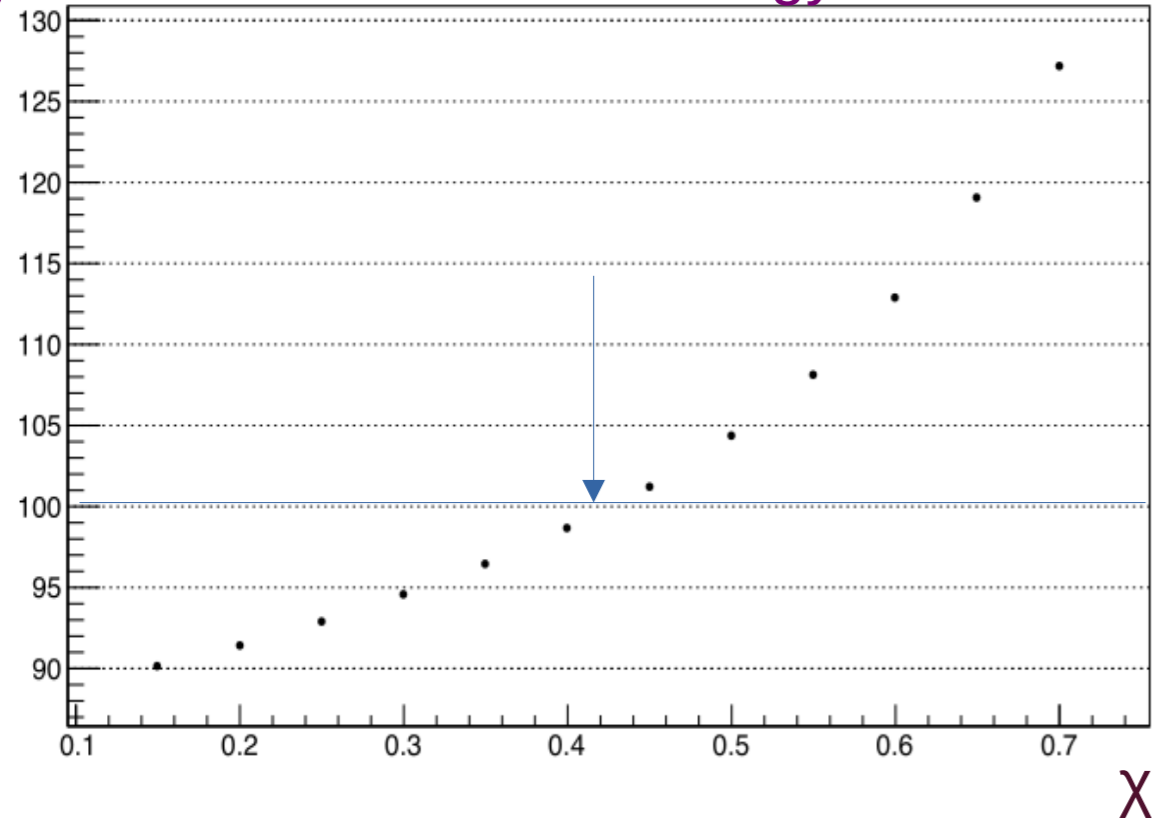
80 GeV protons in Copper  $\uparrow$  & Lead  $\downarrow$



# Geant4 simulations – $\chi$ scan

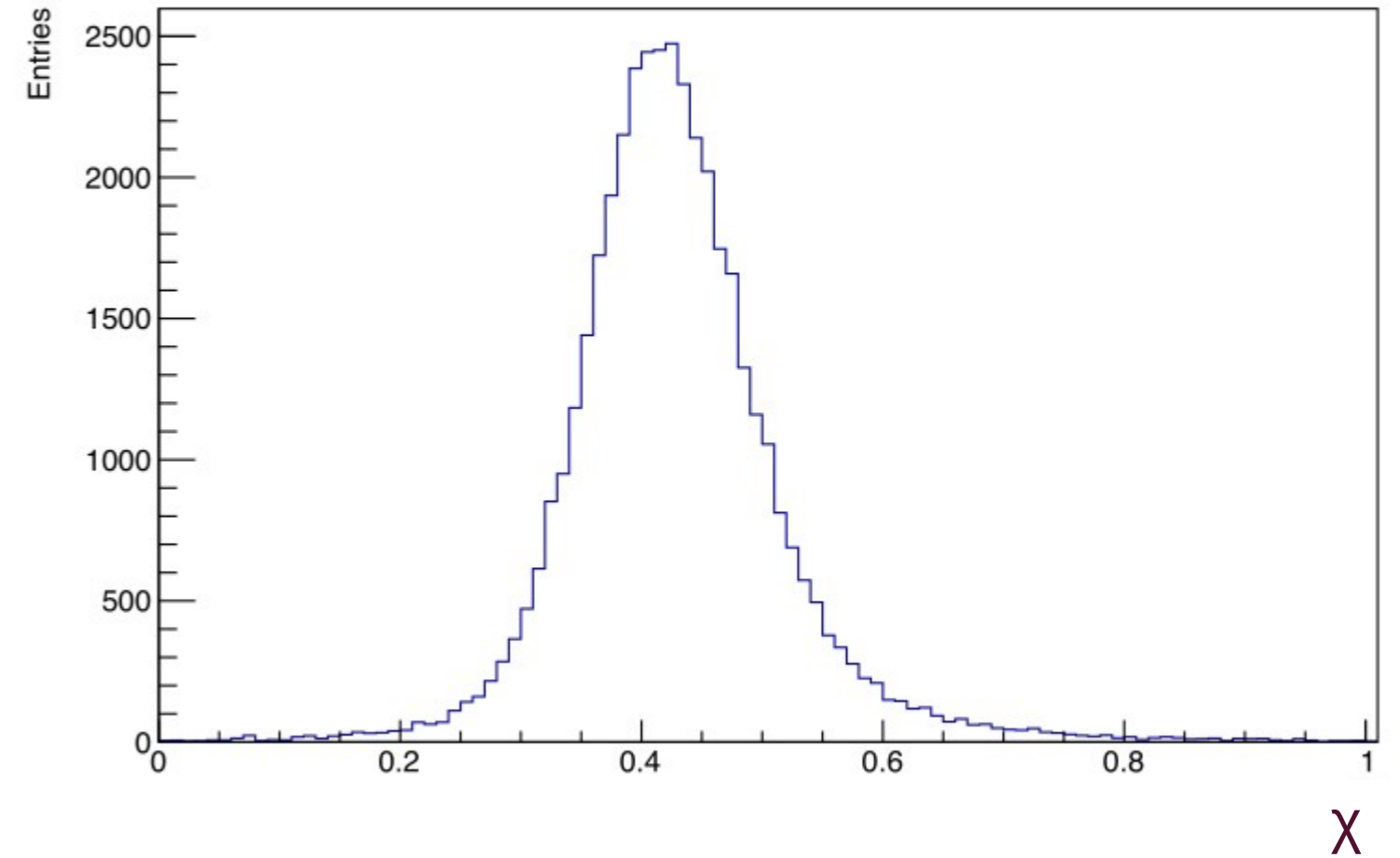
GeV

Reconstructed energy



100 GeV  $\pi^-$

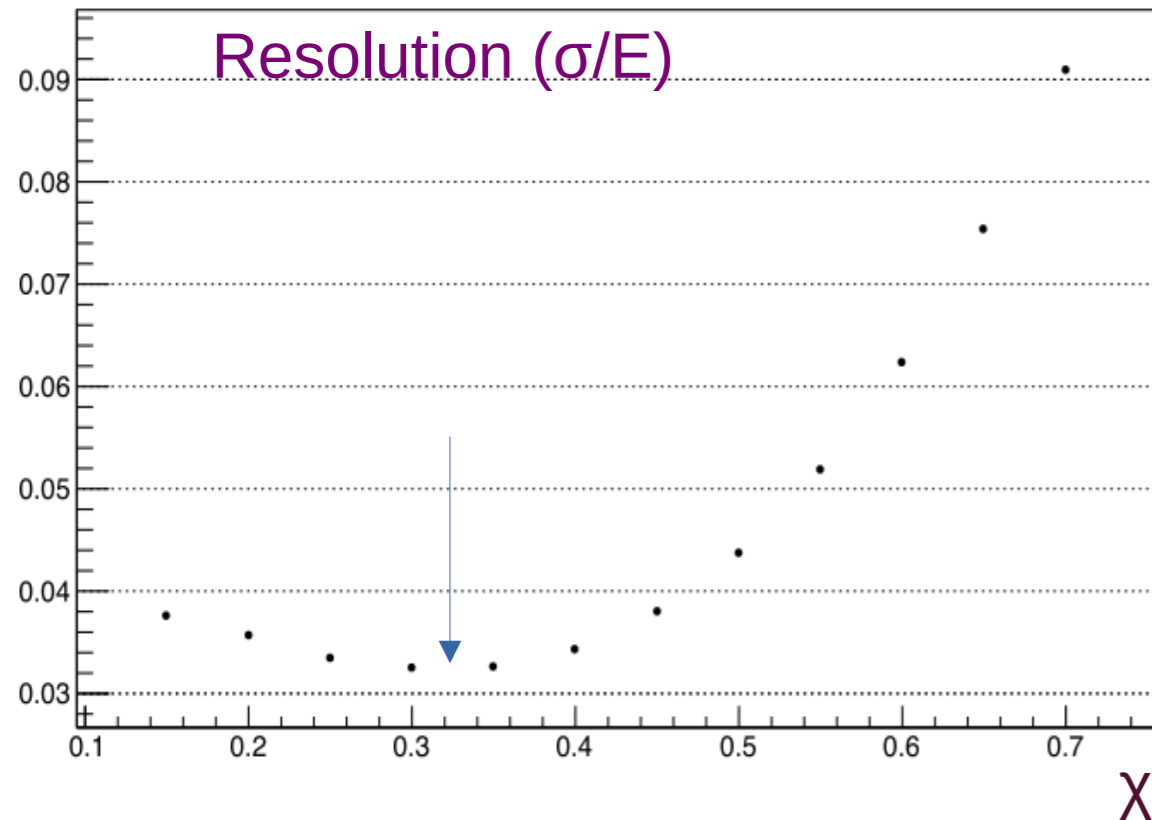
$\chi$  for optimal linearity



Can't optimise both !

Target should be linearity

Resolution ( $\sigma/E$ )



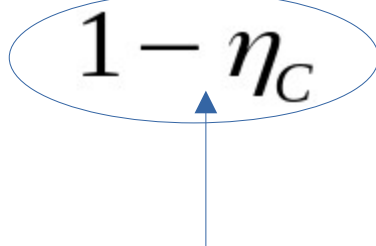


# $f_{em}$ (really $f_h$ ) estimation

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Independently for S and C signals, you can easily get:

$$\eta_x \equiv (h/e)_x$$

$$f_h \stackrel{\text{def}}{=} (1 - f_{em}) = \frac{1 - S/E}{1 - \eta_S} = \frac{1 - S/E}{\chi \cdot (1 - \eta_C)} = \frac{1 - C/E}{1 - \eta_C}$$


$f_h$  can be estimated event-by-event within scale factor  $\approx 1$   
(since  $\eta_C \ll 1$ )

# (h/e) estimation (?)

Up to few hundreds GeV,  $\langle f_h \rangle$  as function of  $E$ , should be fairly well described by:

$$\langle f_h(E) \rangle \approx (E/E_0)^{m-1} \quad \text{for } E > E_0$$

where mainly (?)  $m$  should depend on absorber,  $E_0$  on particle type

Two-parameter fit to:

$$1 - \langle C/E \rangle \approx (1 - \eta_C) \times (E/E_0)^{m-1} = \lambda \times E^{m-1}$$

$$\lambda \equiv (1 - \eta_C) \times E_0^{1-m}$$

Some more input/assumptions (?):

$$m \in [0.80, 0.87] \Rightarrow 1 - m \in [0.13, 0.20] \ll 1$$

$$E_0(\pi) \ [ \ E_0(p) \ ] \approx 1 \text{ GeV} \ [ \ 2.6 \text{ GeV} \ ]$$

with pion data, since  $E_0^{1-m}(\pi) \approx 1 \Rightarrow \lambda(\pi) \approx 1 - \eta_C$

then with proton [ kaon, ... ] data  $\Rightarrow E_0(p) \ [ \ E_0(K), \dots \ ]$

to be checked with M.C.  
and (hopefully) validated  
with some TB data ...

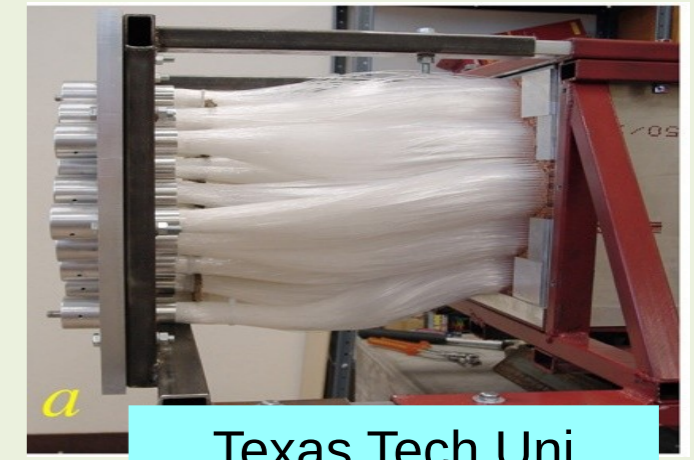
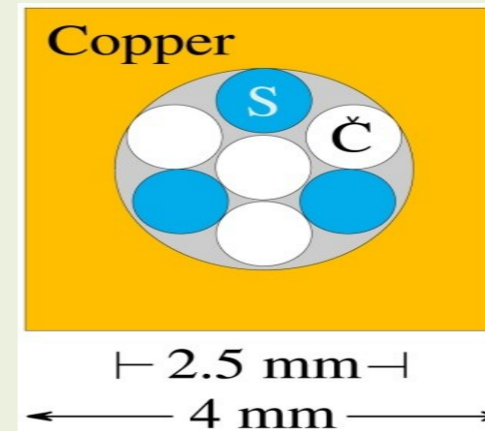
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## 3. Few DREAM/RD52 results

# DREAM/RD52 dual-readout spaghetti prototypes

2003  
DREAM

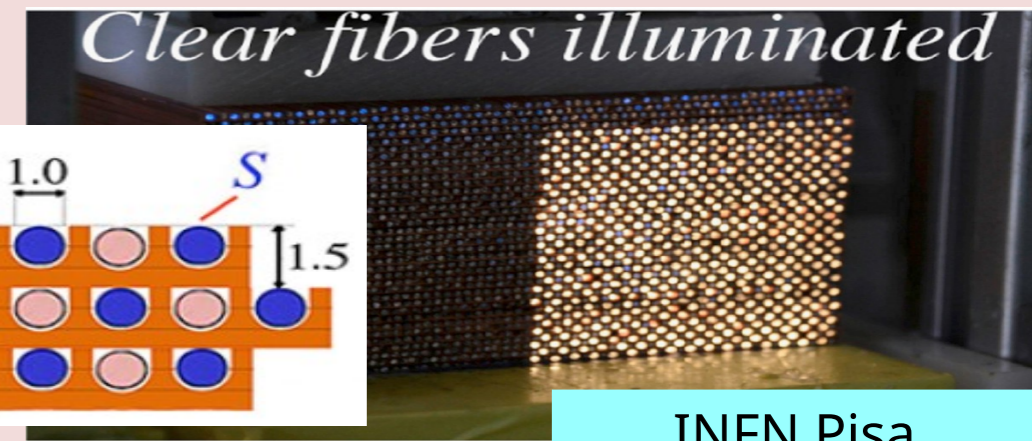
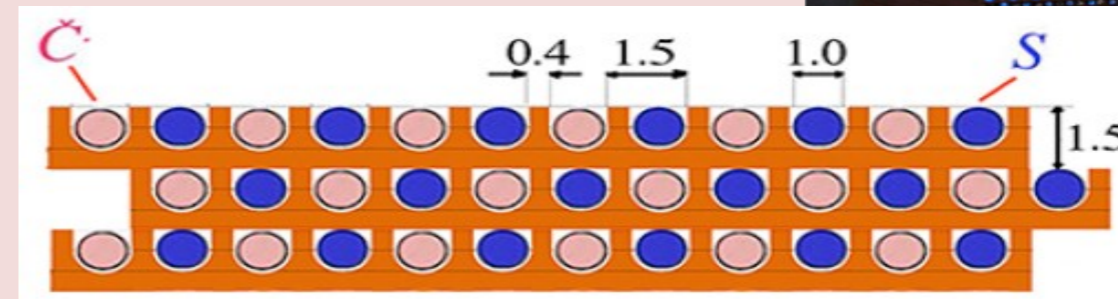
Cu: 19 towers, 2 PMT each  
2 m long, 16.2 cm radius  
Sampling fraction: 2%  
Depth:  $\sim 10 \lambda_{\text{int}}$



Texas Tech Uni

2012  
RD52

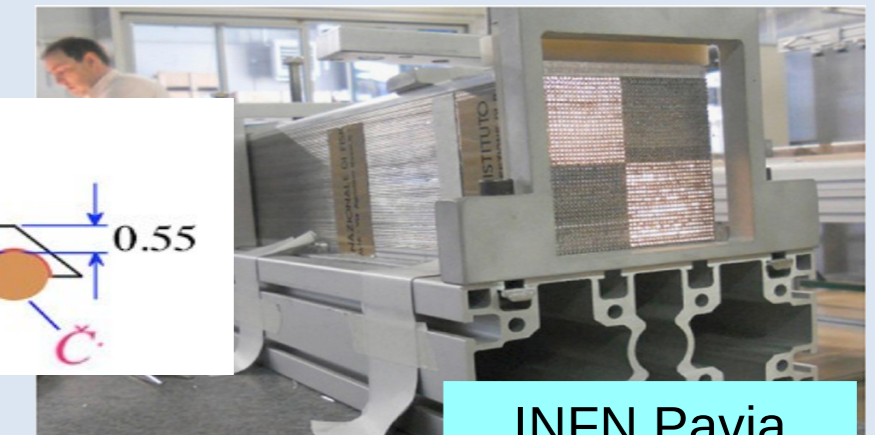
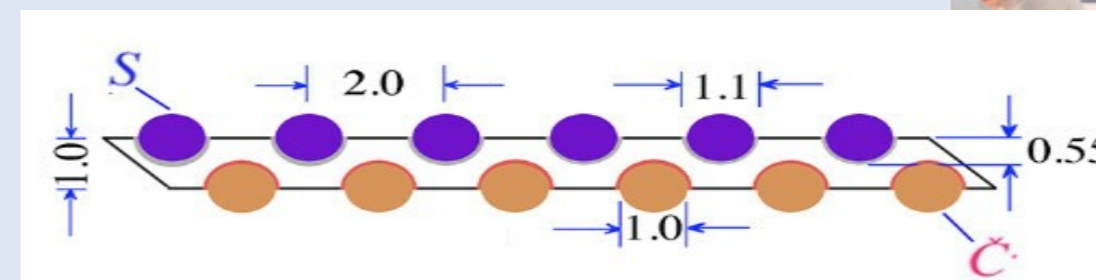
Cu, 2 modules  
Each module:  $9.2 \times 9.2 \times 250 \text{ cm}^3$   
Fibers: 1024 S + 1024 C, 8 PMT  
Sampling fraction:  $\sim 4.6\%$   
Depth:  $\sim 10 \lambda_{\text{int}}$



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2012  
RD52

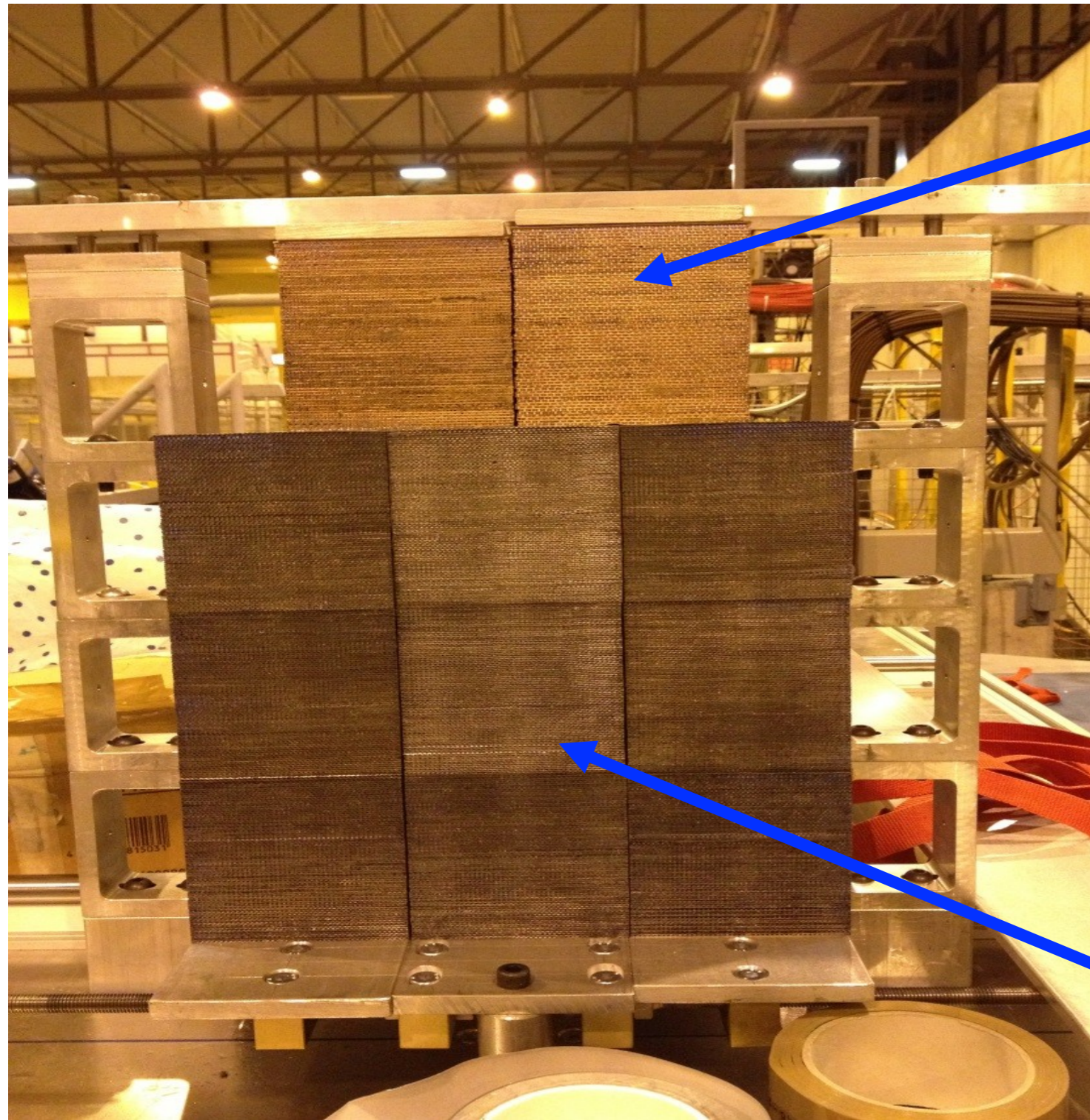
Pb, 9 modules  
Each module:  $9.2 \times 9.2 \times 250 \text{ cm}^3$   
Fibers: 1024 S + 1024 C, 8 PMT  
Sampling fraction:  $\sim 5.3\%$   
Depth:  $\sim 10 \lambda_{\text{int}}$



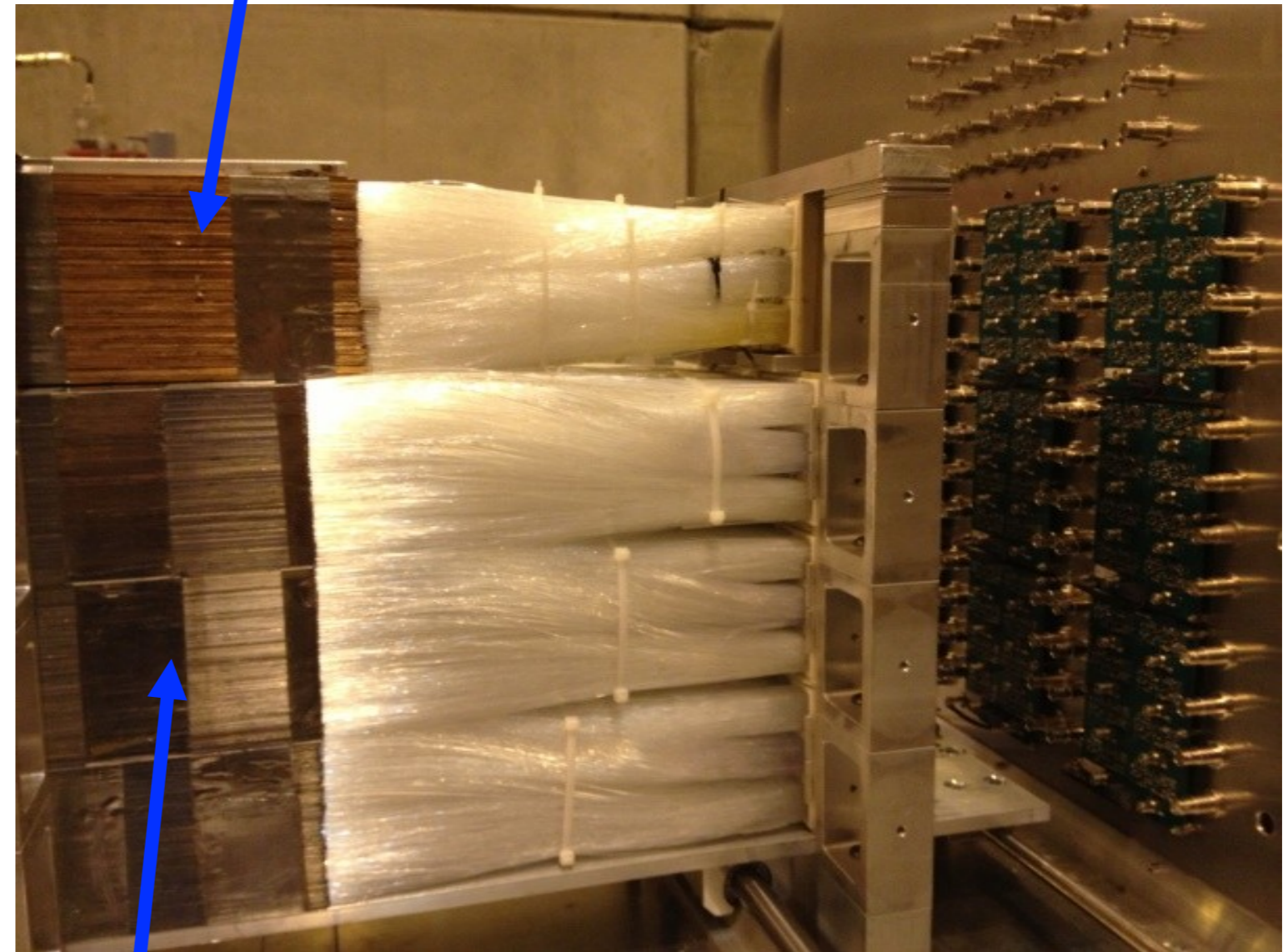
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# RD52 dual-readout spaghetti prototypes



2 Cu modules



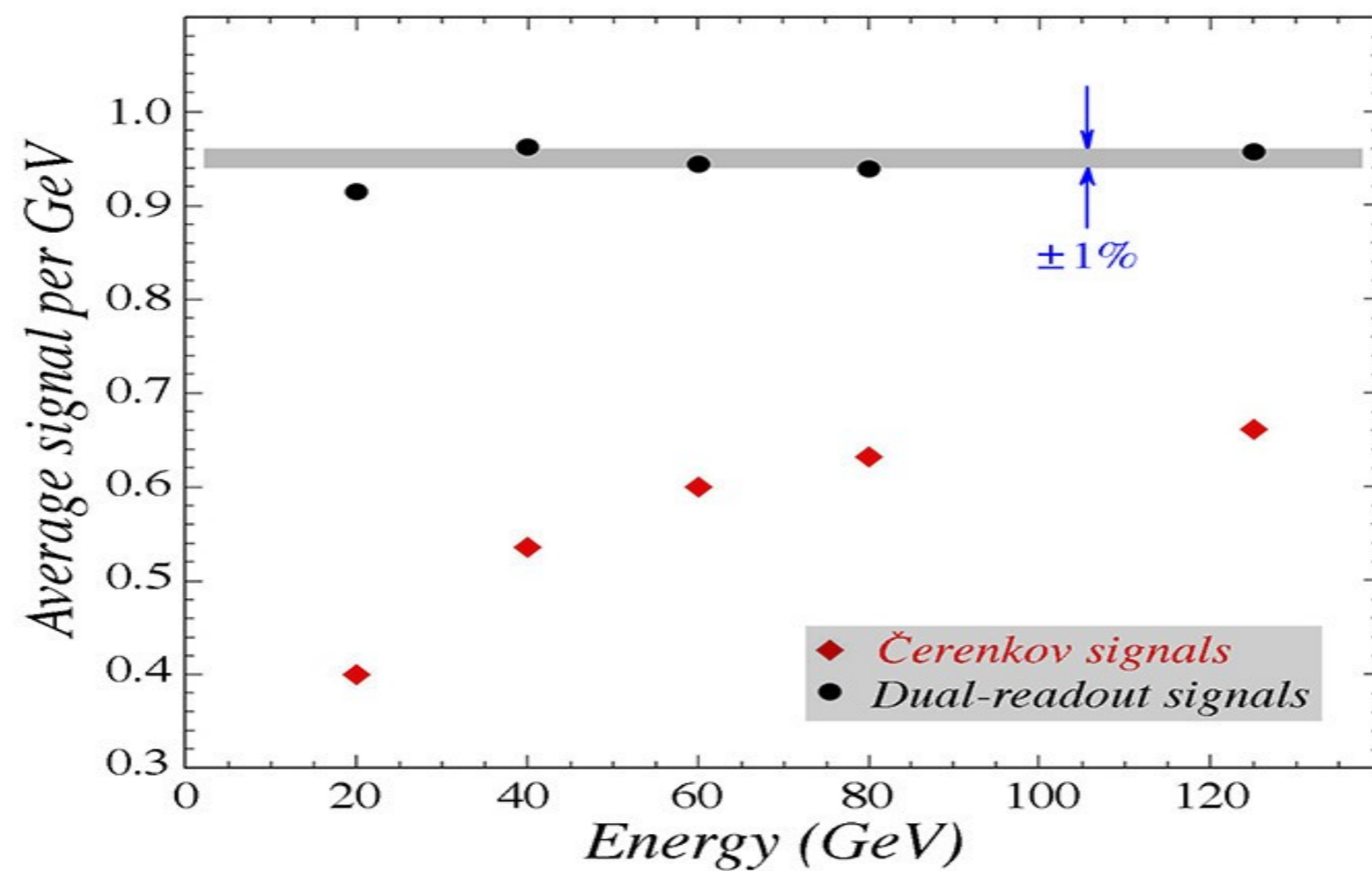
3x3 lead matrix



# dual-readout at work (1)

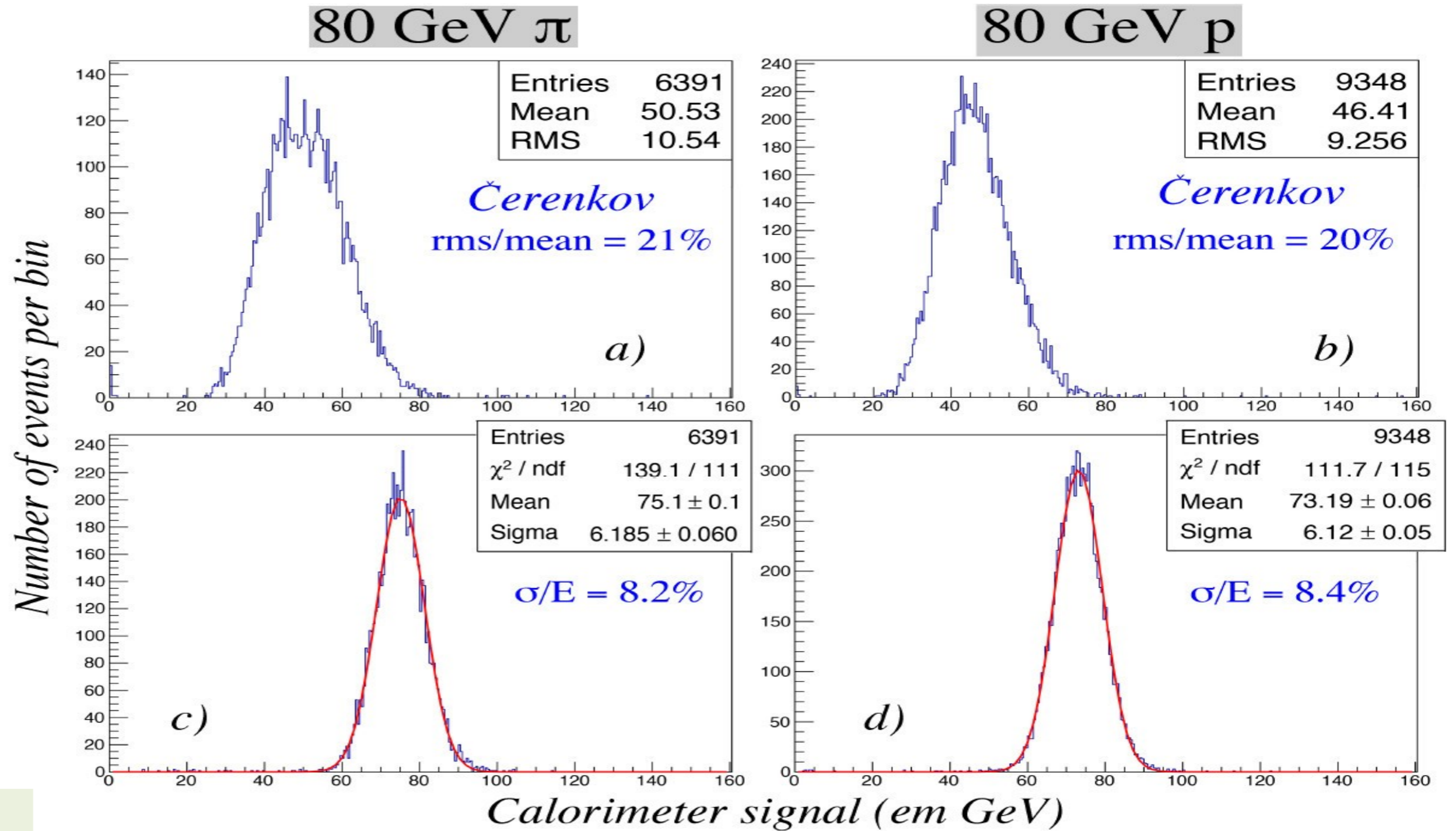
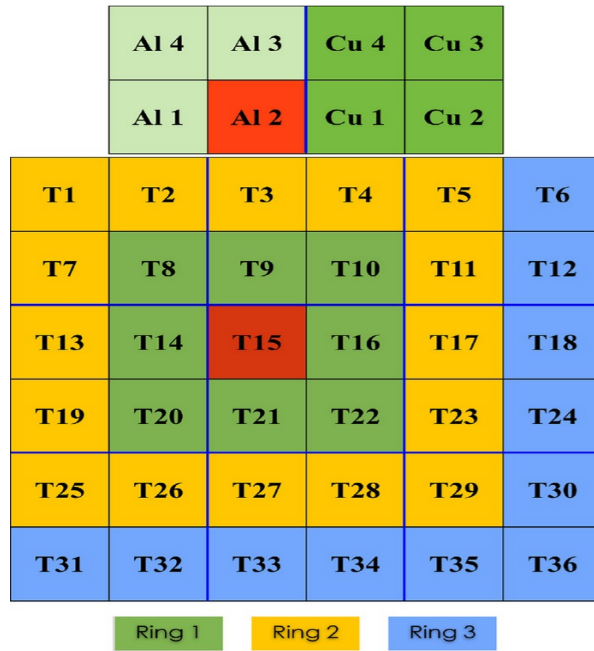
## *Effects of the dual-readout method*

### Signal linearity



NIM A 866 (2017) 76

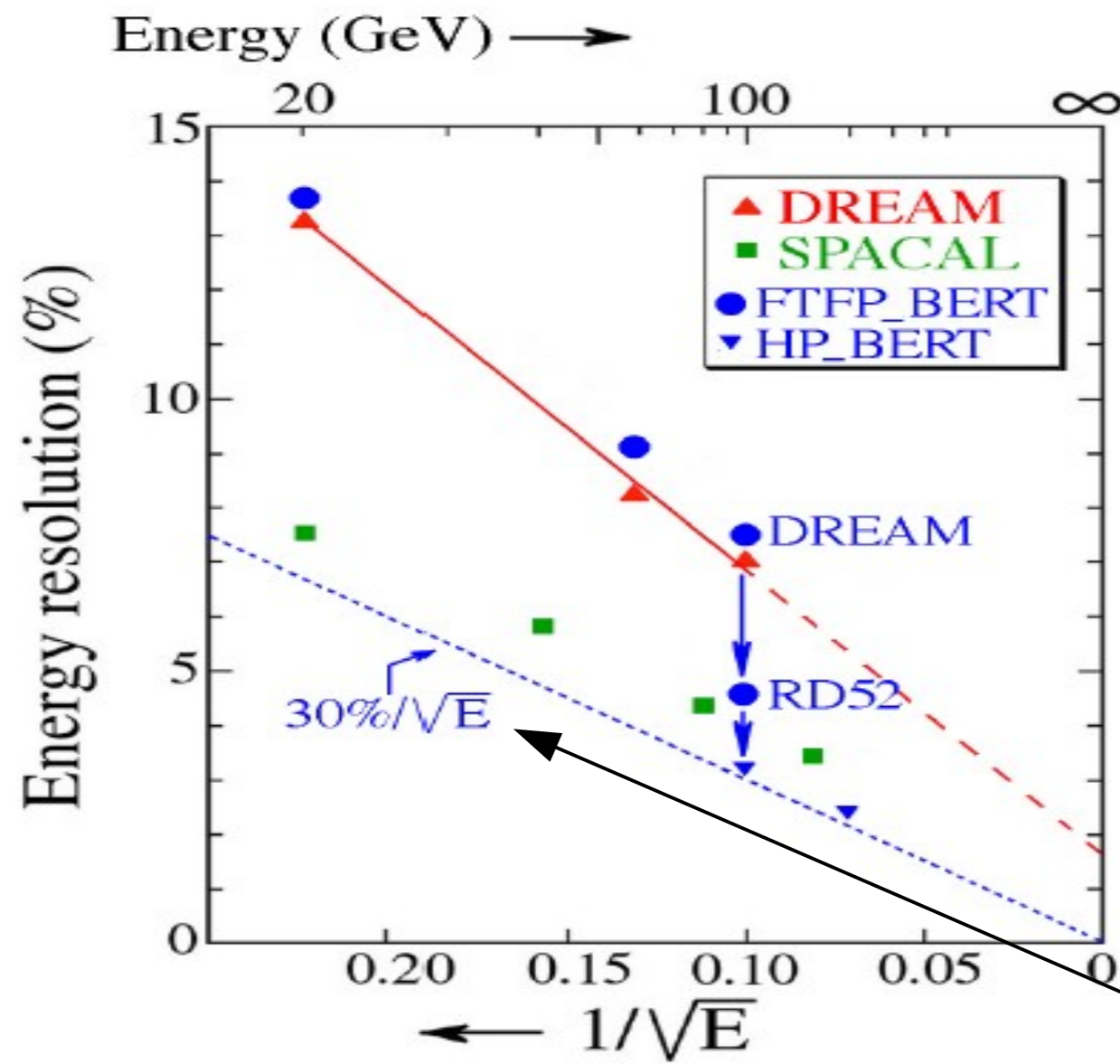
# dual-readout at work (2)



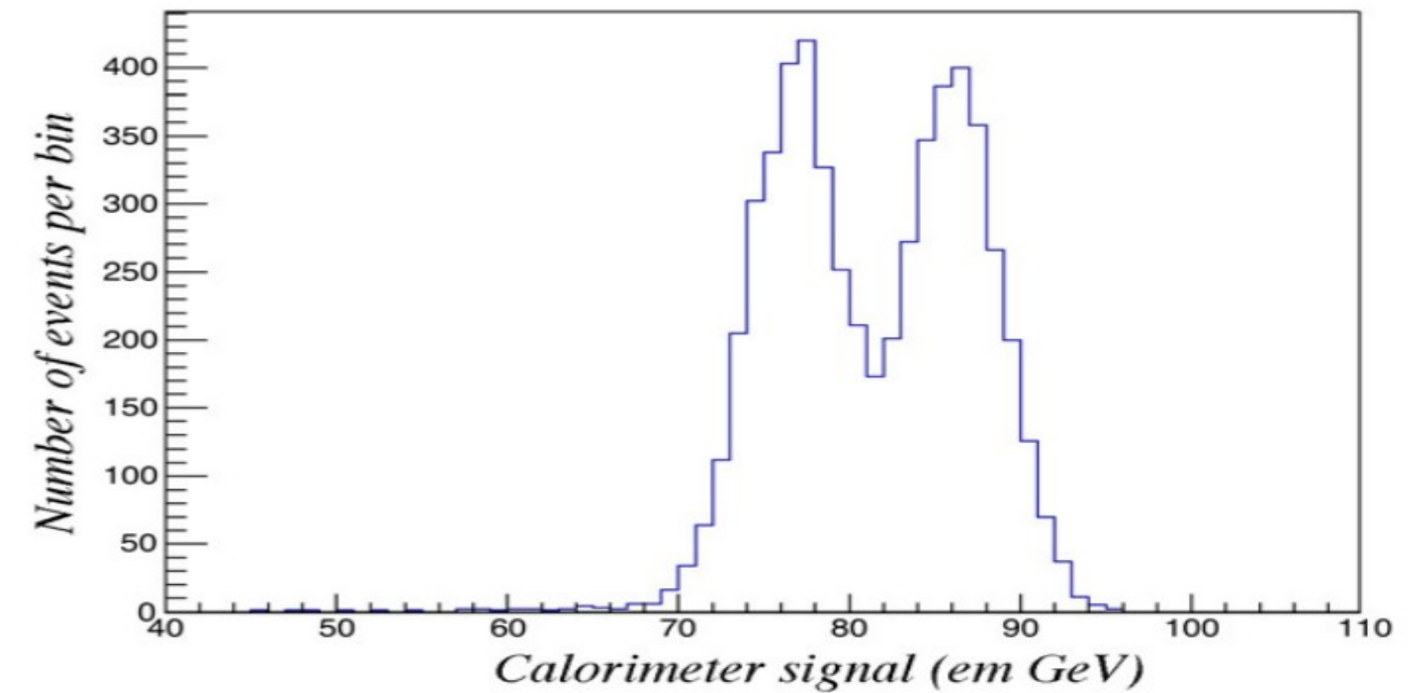
NIM A 866 (2017) 76

# RD52 expected hadronic performance

## Hadronic Resolution



## W/Z separation



Geant4 simulations

NIM A 824 (2016) 721



# particle ID (electron/hadron discrimination)

RD52 lead calorimeter

(60 GeV)  $e^-$  vs.  $\pi^-$

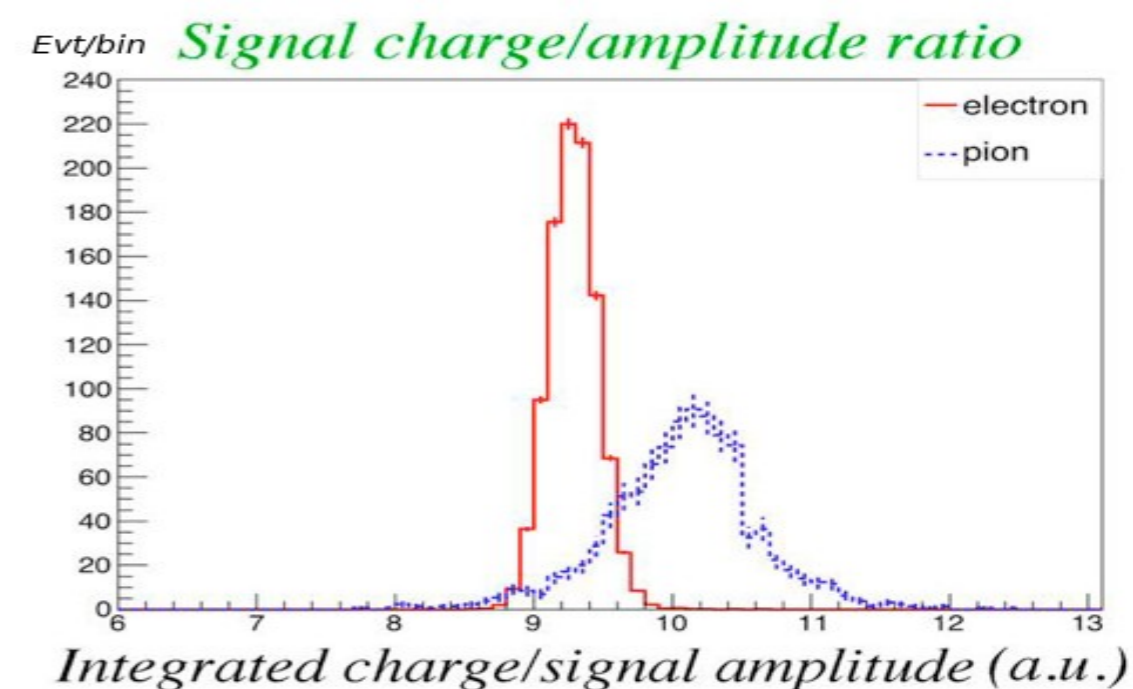
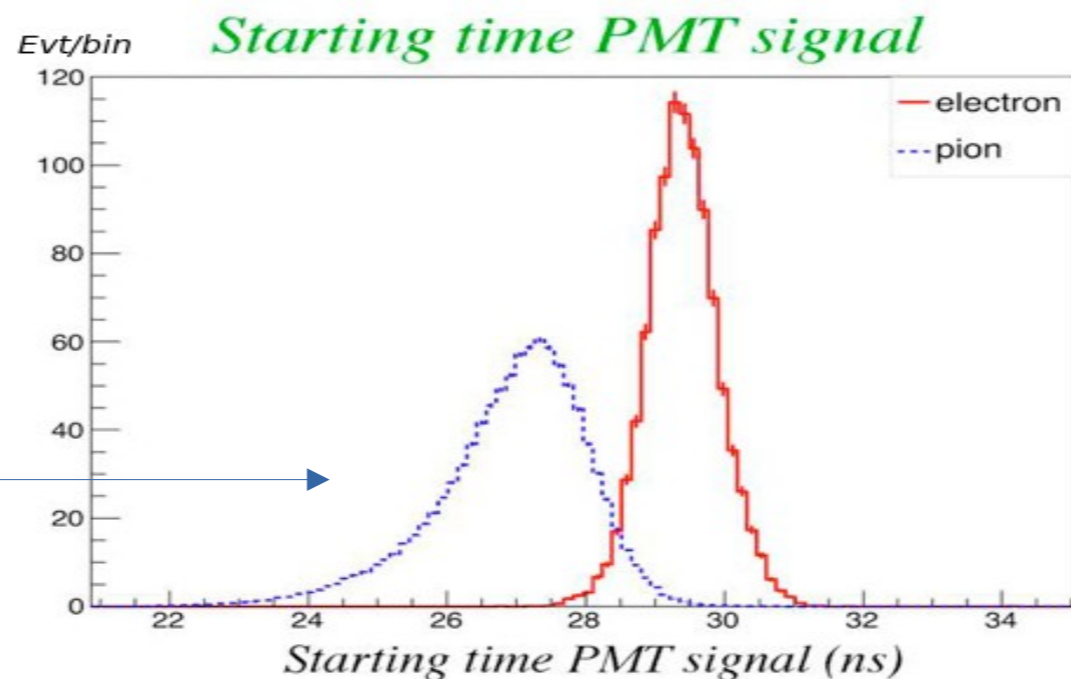
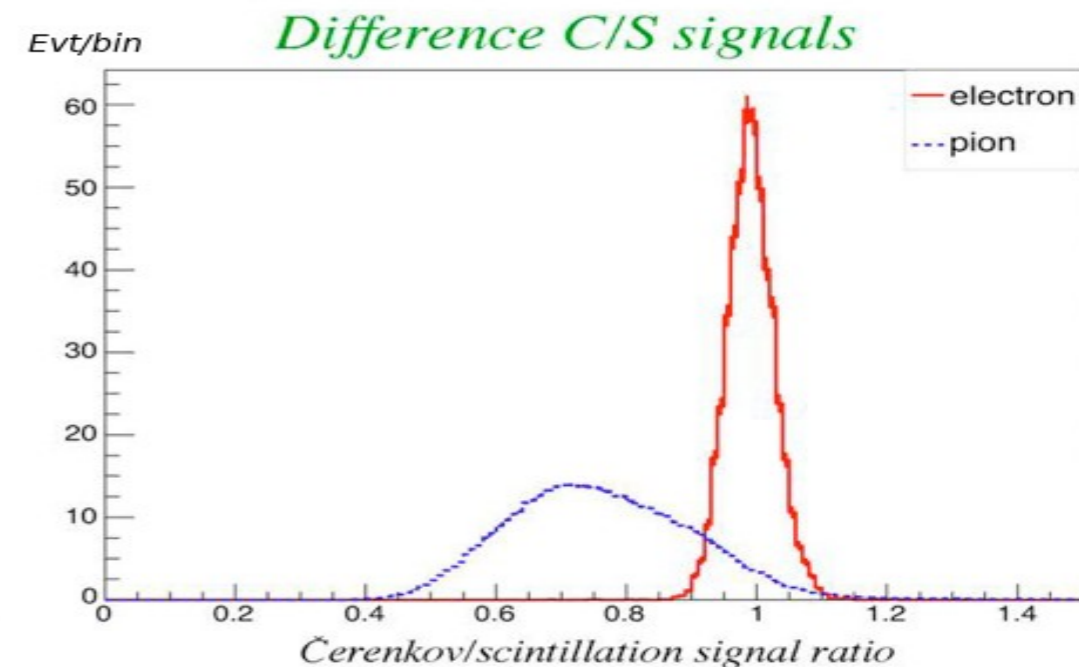
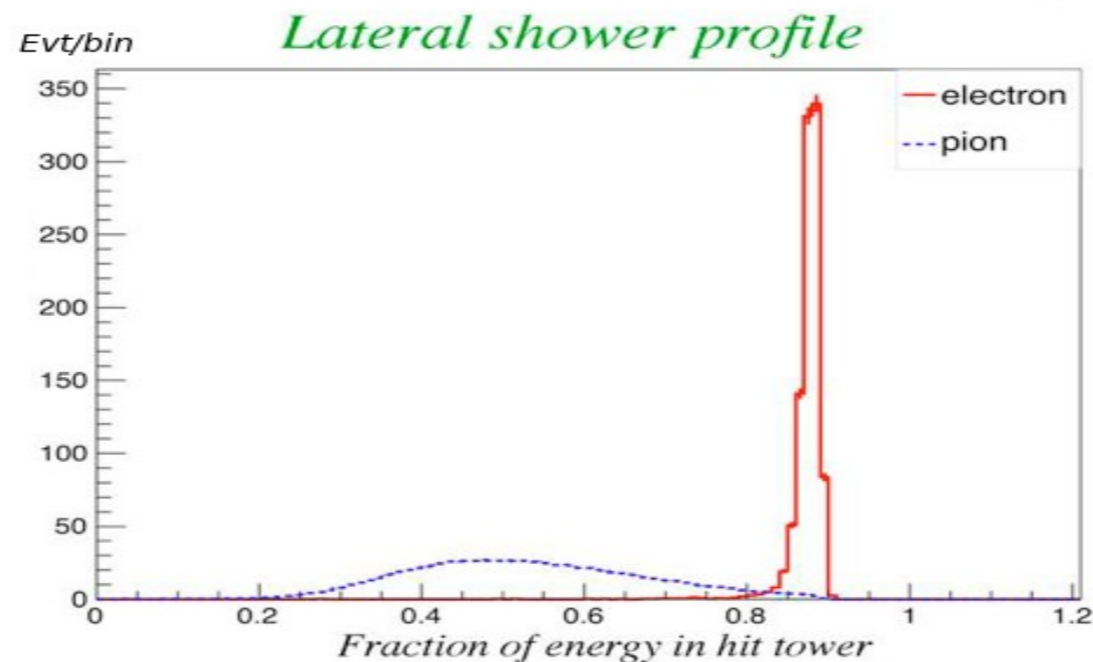
$\epsilon(e^-) > 99\%$

$R(\pi^-) \sim 500$

NIM A 735 (2014) 120

time-of-arrival distribution  
measured w/ TDC

*Methods to distinguish  $e/\pi$  in longitudinally unsegmented calorimeter*



*Combination of cuts:  $>99\%$  electron efficiency,  $<0.2\%$  pion mis-ID*

---

## 4. Dual readout goes granular ( IDEA fibre calorimeter )

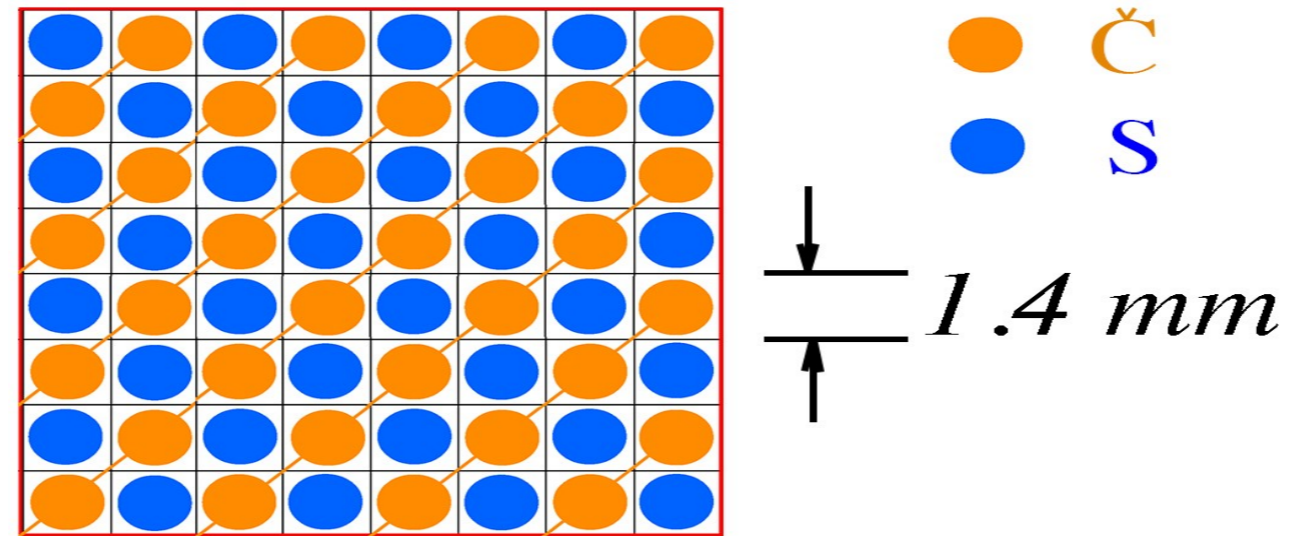
# RD52 SiPM module

Brass module, dimensions: ~ 112 cm long, 12 x 12 mm<sup>2</sup>

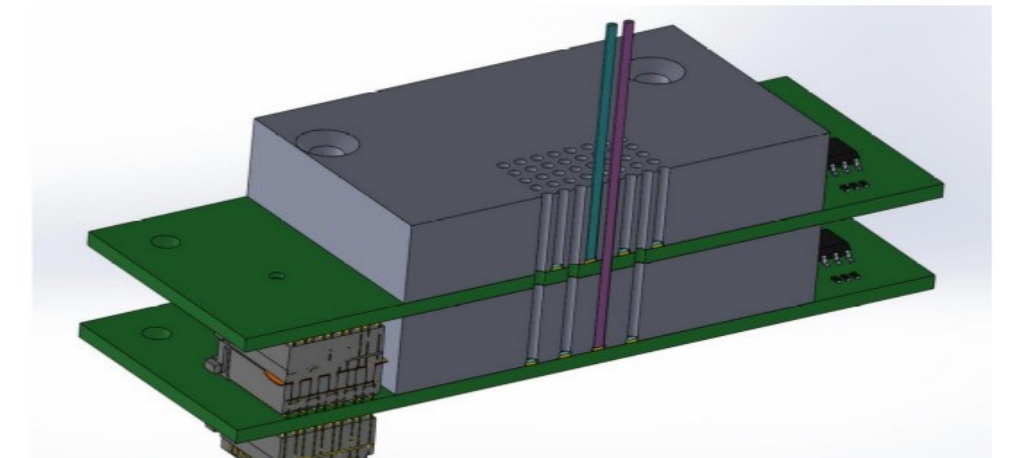
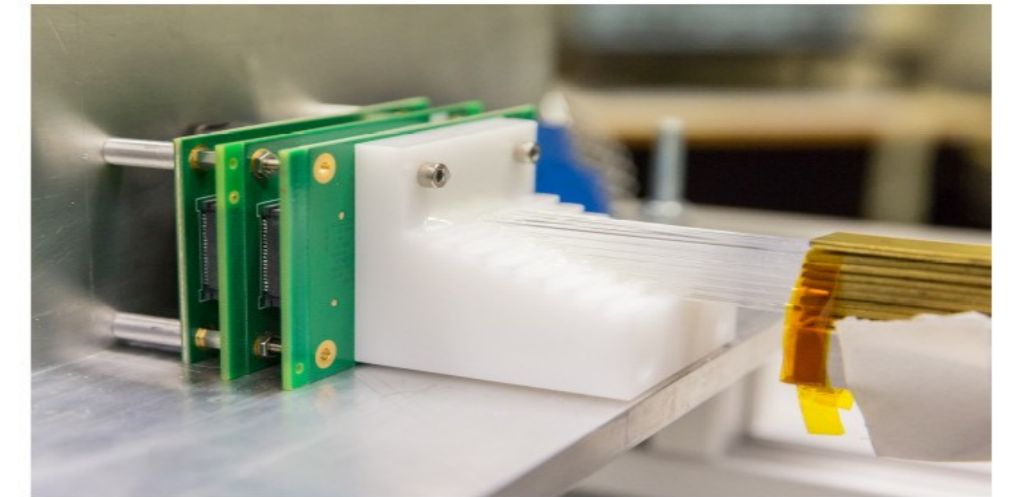
32 (S) + 32 (Č) fibres  
 $X_0 \sim 29$  mm  
 $R_M \sim 31$  mm

$\sim (0.4 R_M)^2 \times 39 X_0$

shower cont.  $\sim 45\%$   
 $f_{\text{sampl}} \sim 5-6\%$

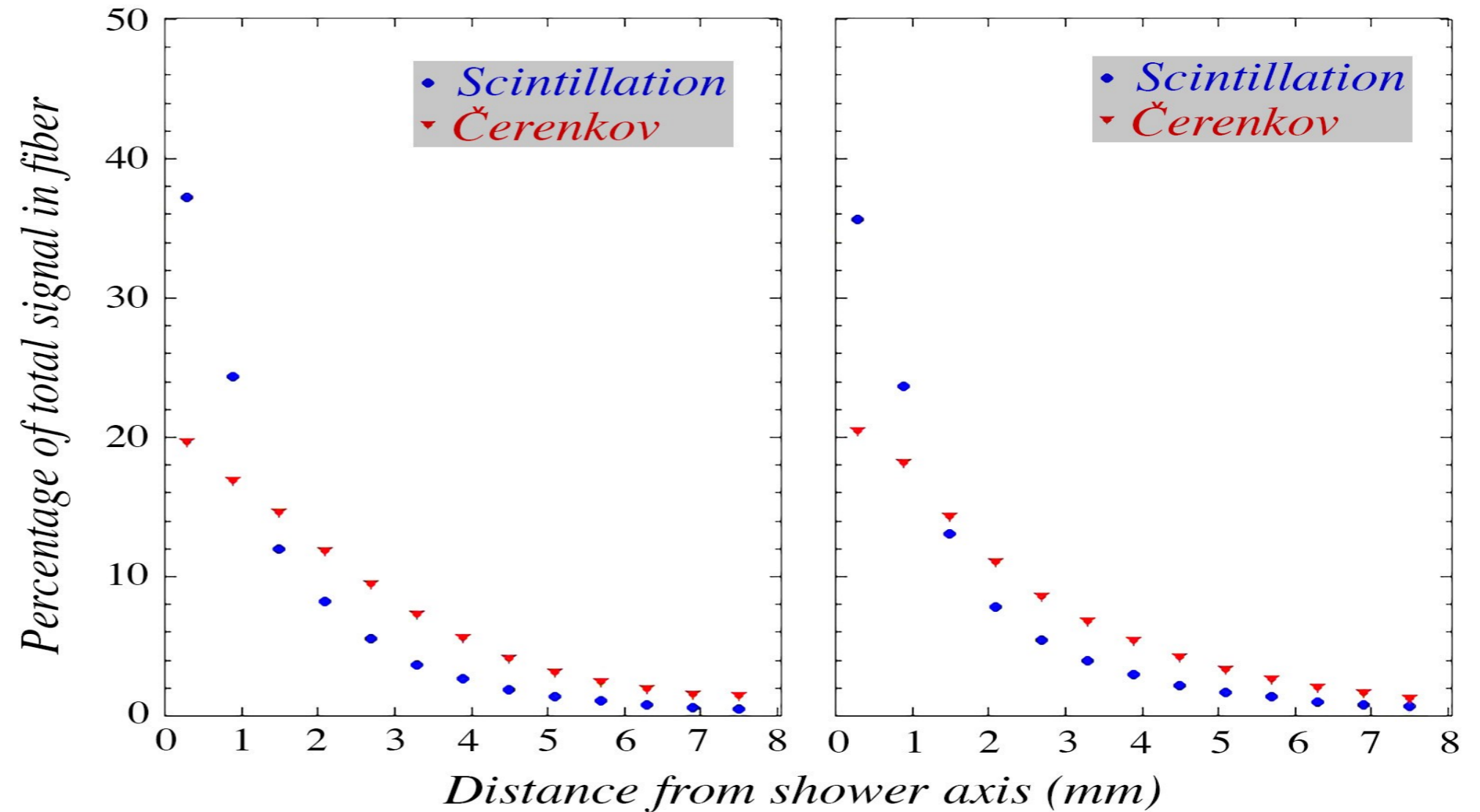


Light sensors (SiPM)



# lateral shower profile w/ SiPMs

10 / 40 GeV  $e^-$   
 $\theta, \Phi = 0^\circ$



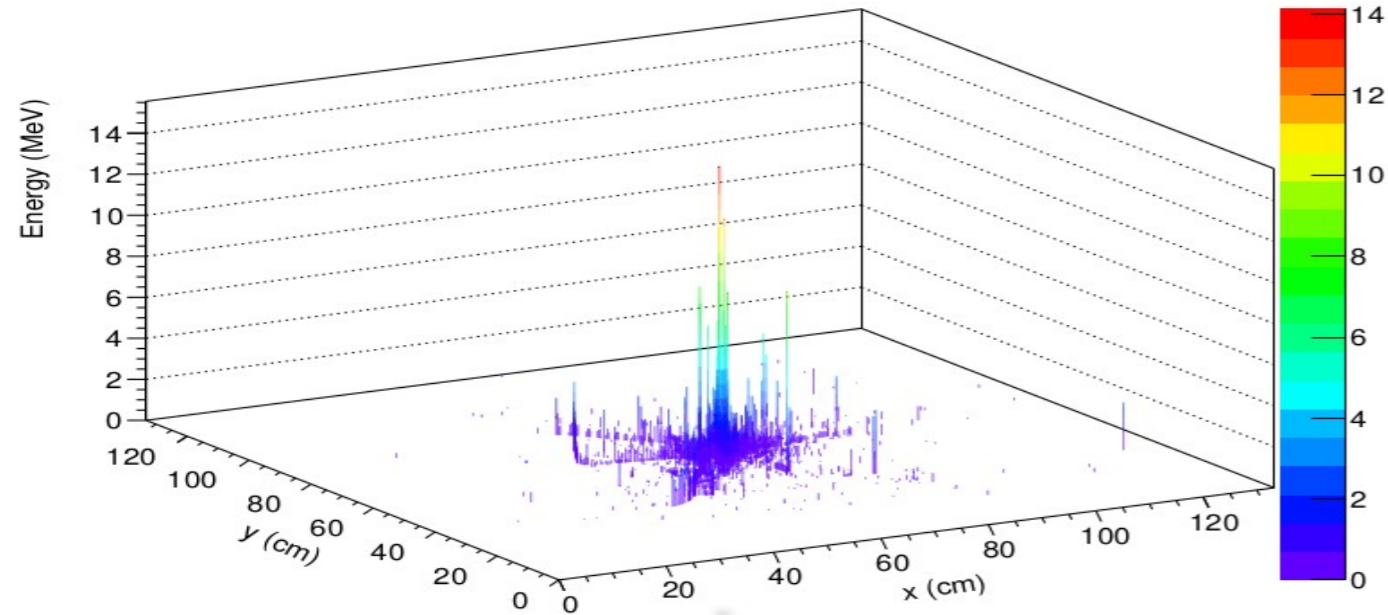
em shower very narrow:

- ~10% (~50%) within ~1 (~10) mm from shower axis
- fibre readout can easily provide (powerful) input to PFA



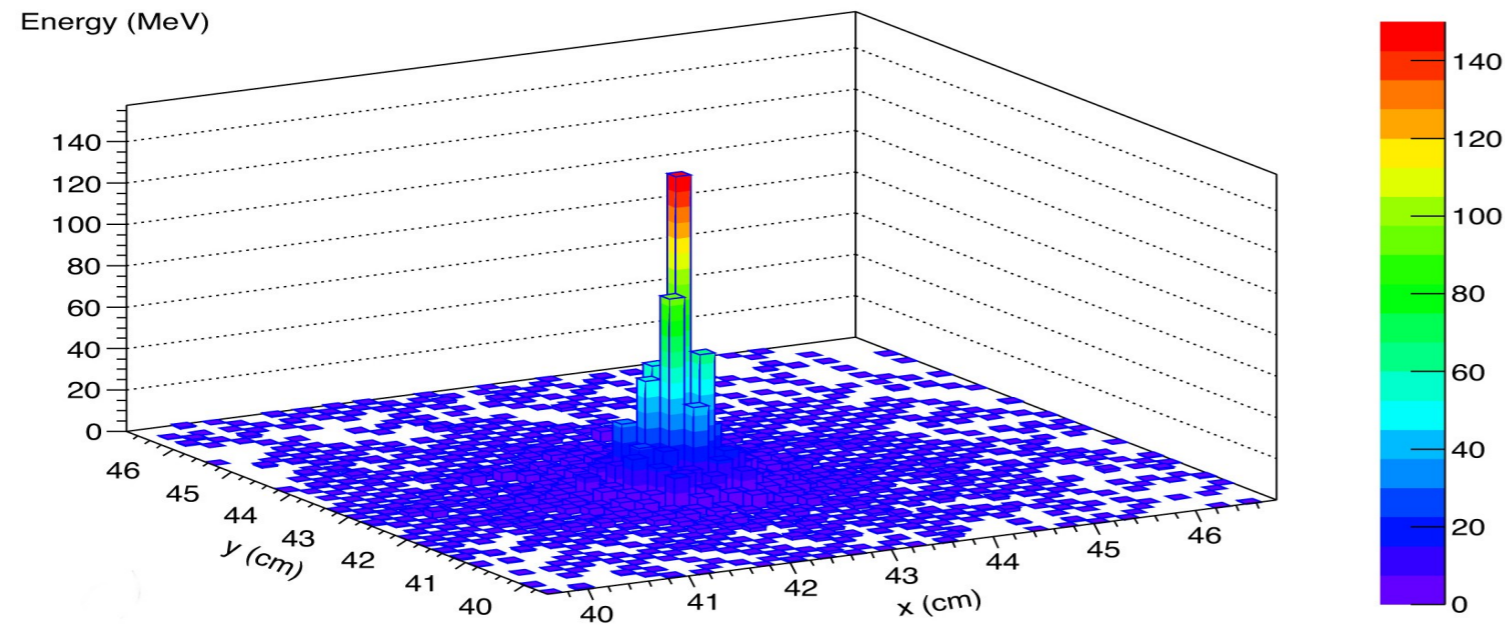
# 2D fibre imaging

## 80 GeV $\pi^-$

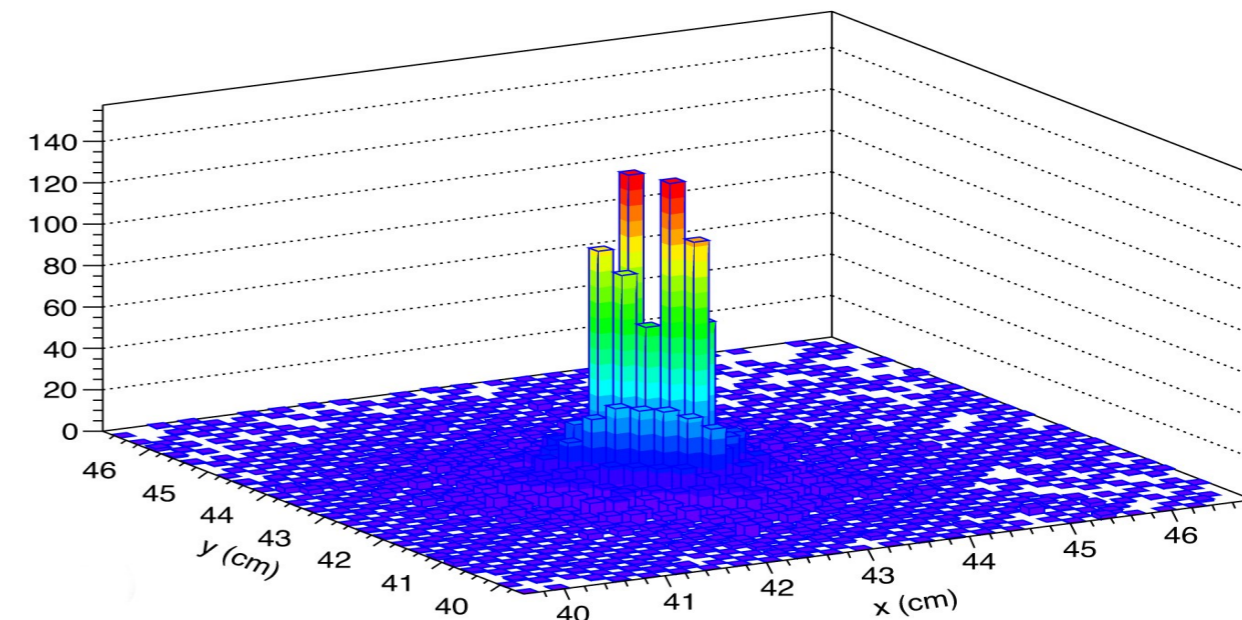


## Geant4 single-particle simulations

## 50 GeV $e^-$



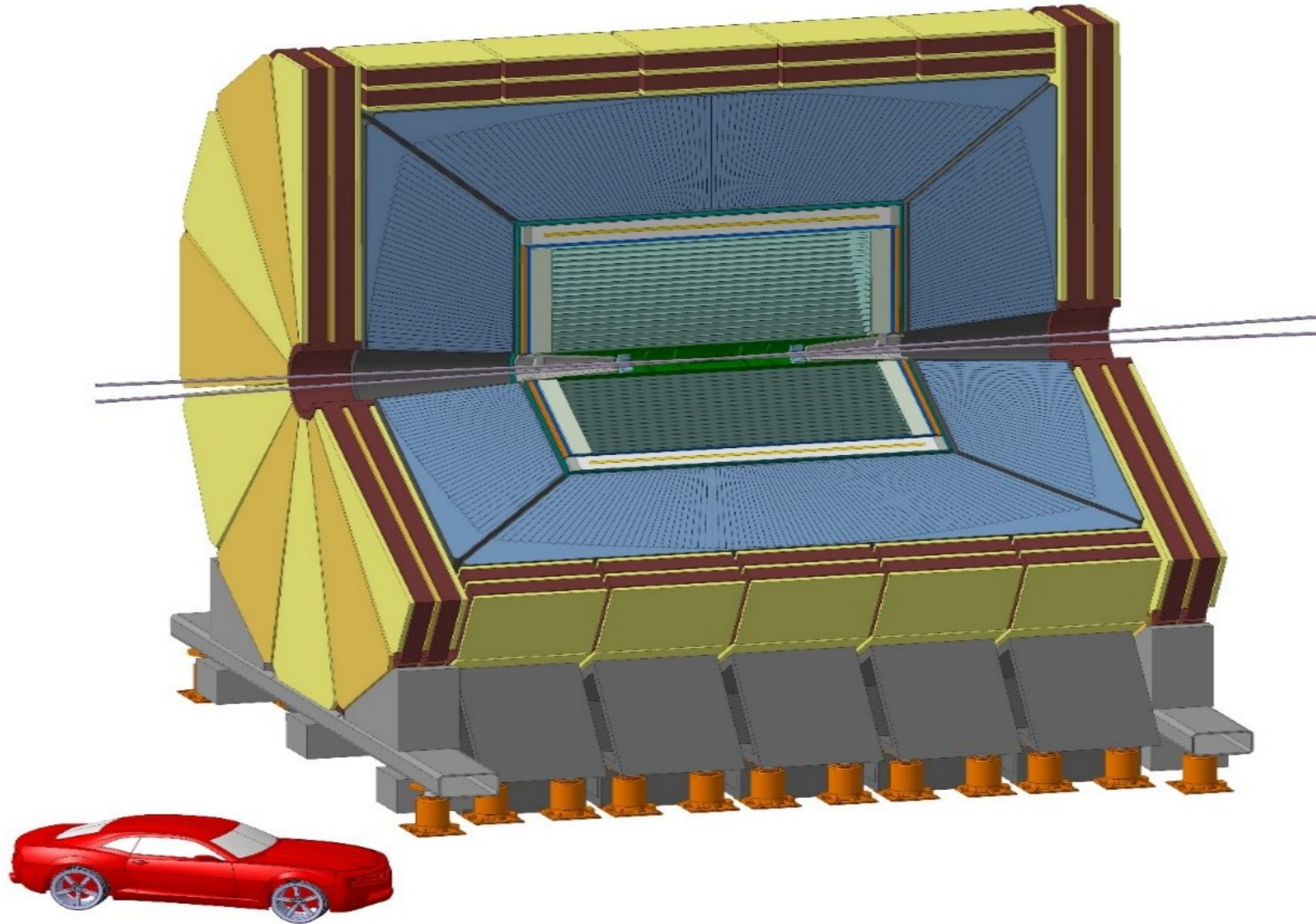
## 100 GeV $\pi^0$





# IDEA: Innovative Detector for e<sup>+</sup>e<sup>-</sup> Accelerators

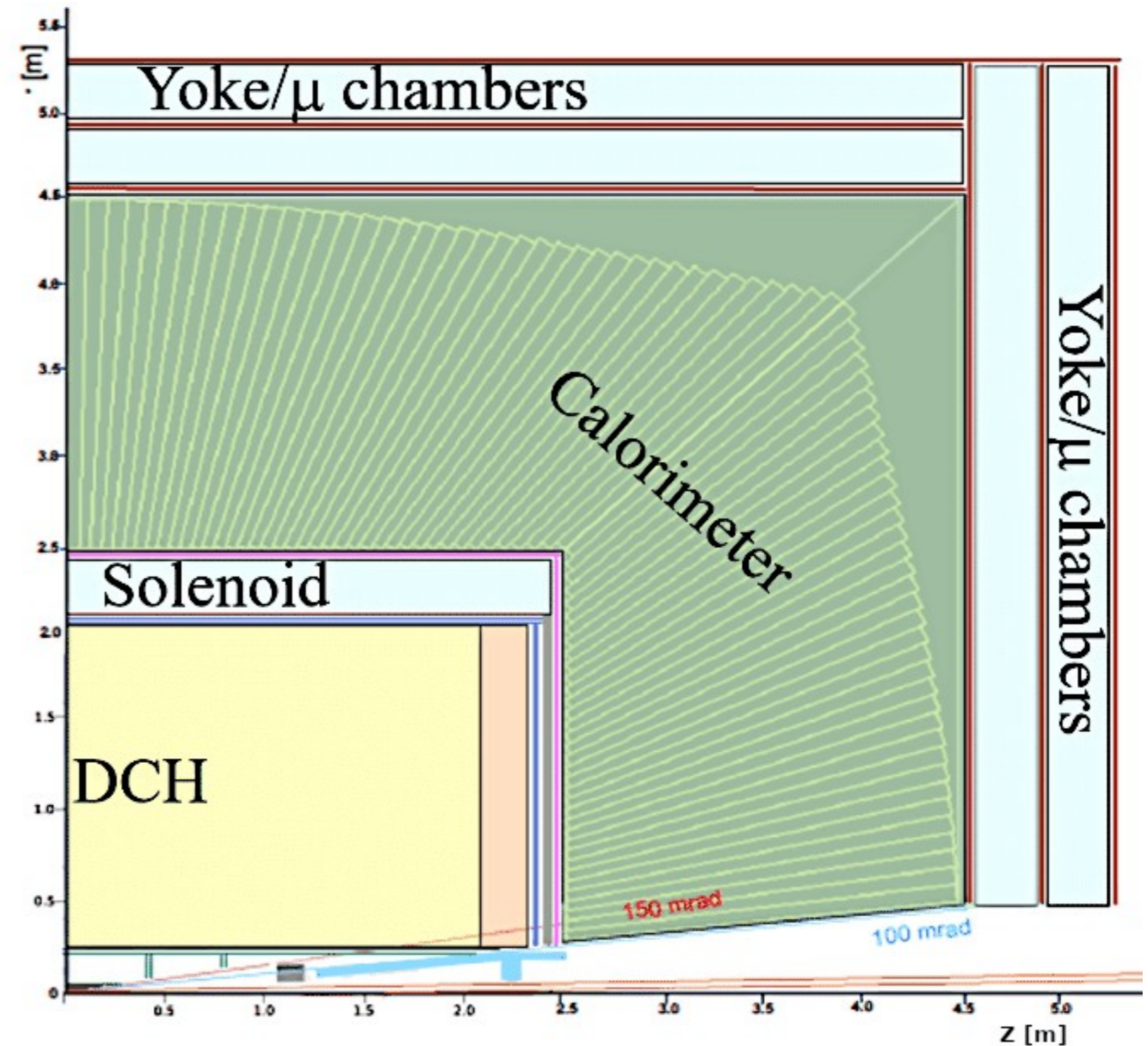
---





# IDEA baseline concept

- ◆ Muon chambers
  - ◆  $\mu$ -RWELL in return yoke
- ◆ Dual-readout calorimetry 2 m /  $7 \lambda_{\text{int}}$ 
  - ◆  $\mu$ -RWELL preshower
- ◆ Thin superconducting solenoid
  - ◆ 2 T, 30 cm,  $\sim 0.7 X_0$ ,  $0.16 \lambda_{\text{int}}$  @  $90^\circ$
- ◆ Highly transparent for tracking
  - ◆ Si pixel vertex detector
  - ◆ Drift Chamber
  - ◆ Si wrappers (strips)
- ◆ Beam pipe:  $r \sim 1.5$  cm



# IDEA dual-readout calorimetry group

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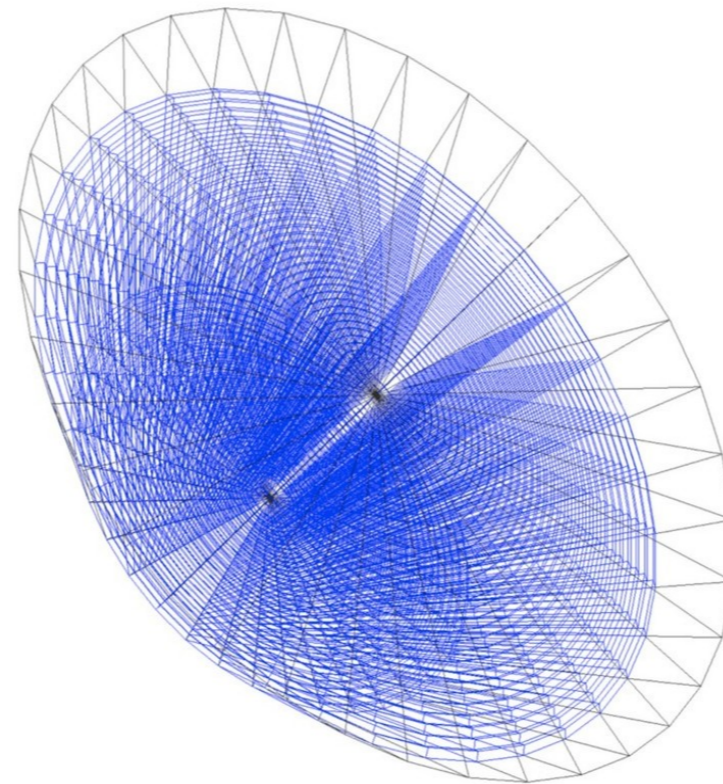
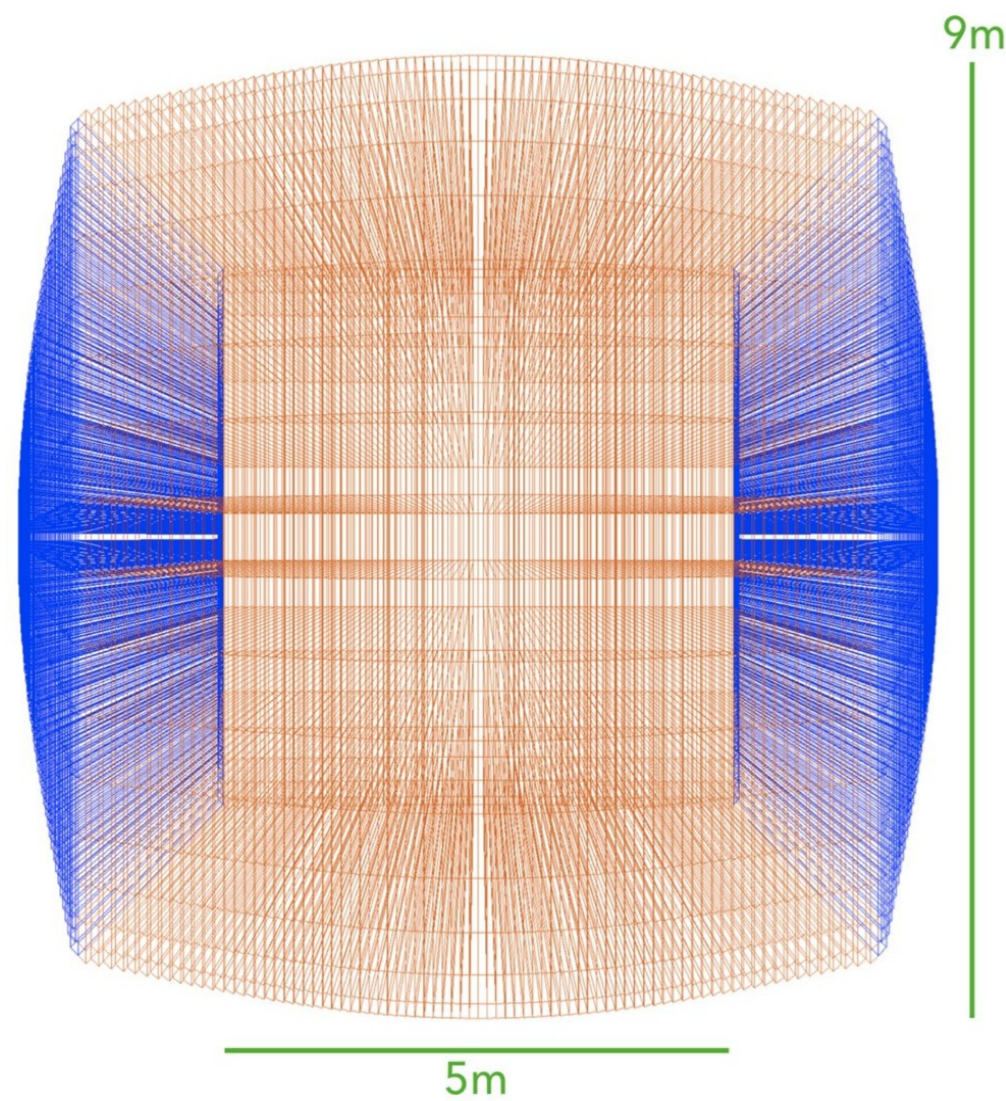
Three main activity pillars:

1. Europa: INFN, Sussex University → mainly (but not only) fibre-sampling calorimetry
2. Korea → projective fibre-sampling calorimetry
3. U.S. (Calvision project) → mainly (but not only) crystal em calorimetry

keywords: dual readout, high granularity & timing



# IDEA all-fibre DR calorimeter option

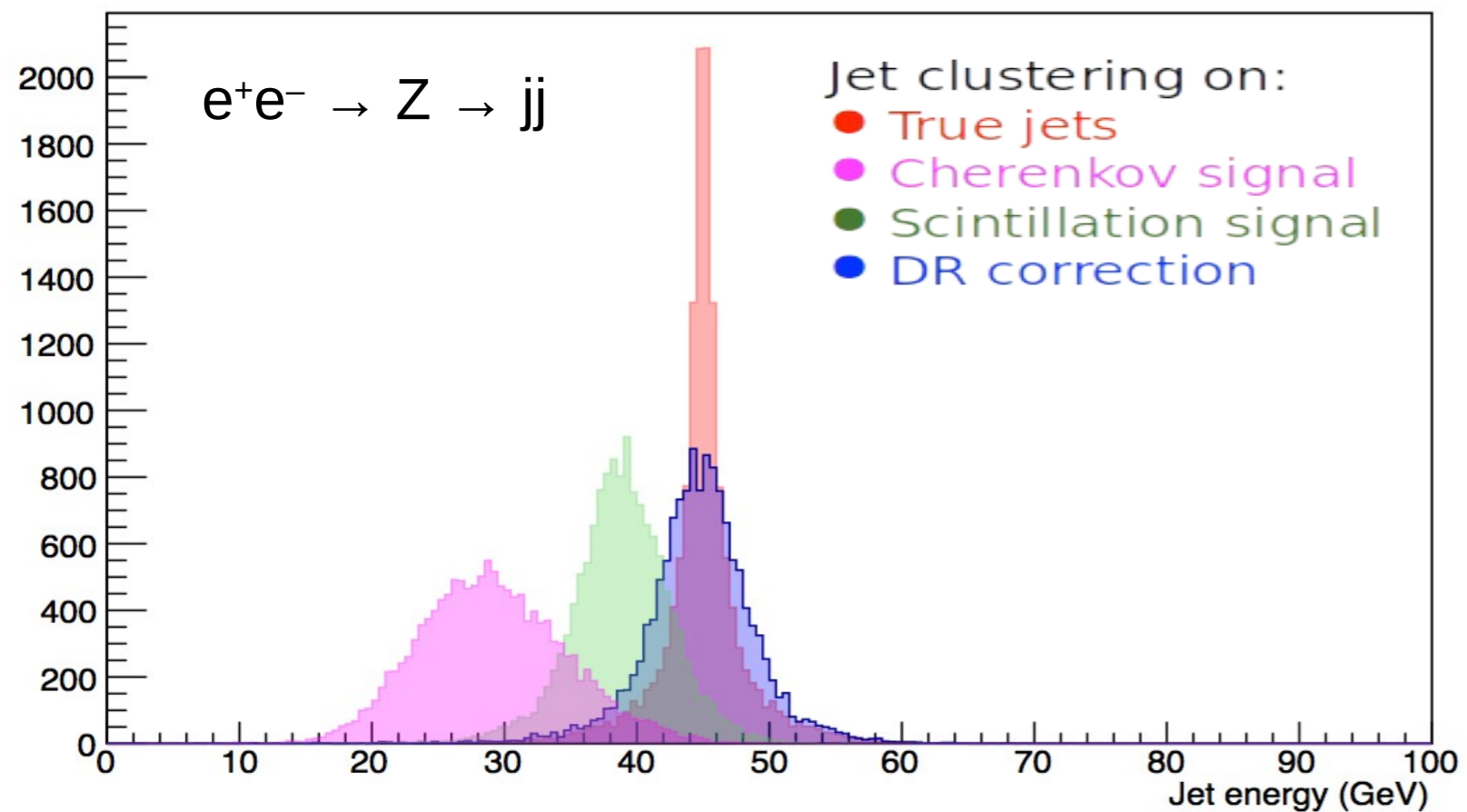


- ◆ DR fibre calorimeter
  - ◆ O(100 M) fibres
    - ◆ 1 mm  $\varnothing$ , 1.5 mm pitch
  - ◆ copper absorber
  - ◆ 75 projective towers  $\times$  36 slices
    - ◆  $\Delta\vartheta = 1.125^\circ$ ,  $\Delta\phi = 10.0^\circ$
    - ◆  $\vartheta$  coverage:  $|\vartheta| > 100$  mrad
- ◆ G4 simulation available
  - ◆ tuned to RD52 TB data

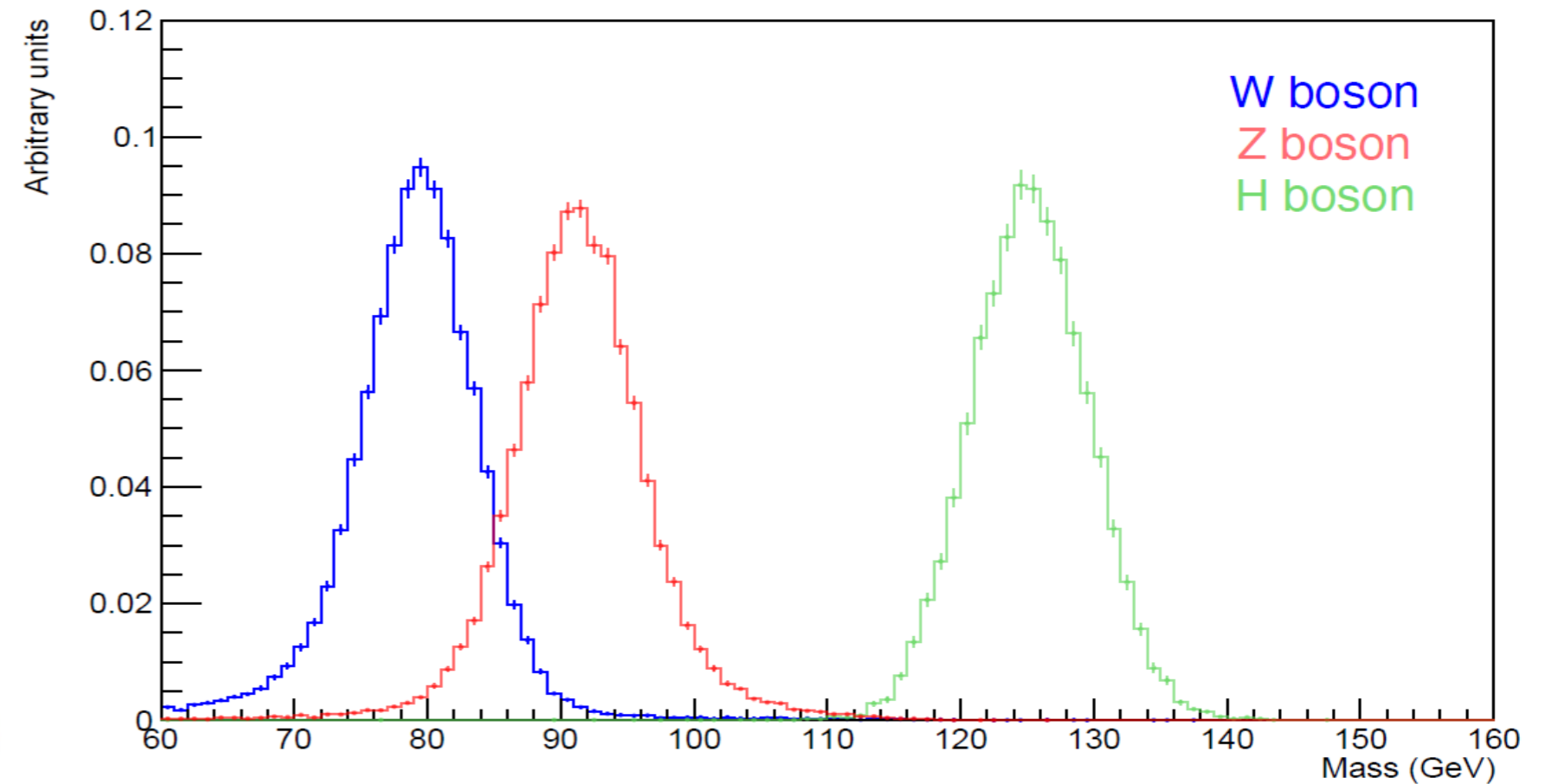
# Geant4 simulations

- ◆ Gaussian resolution
- ◆ Adequate separation of W / Z / H

Single jet resolution @ 45 GeV



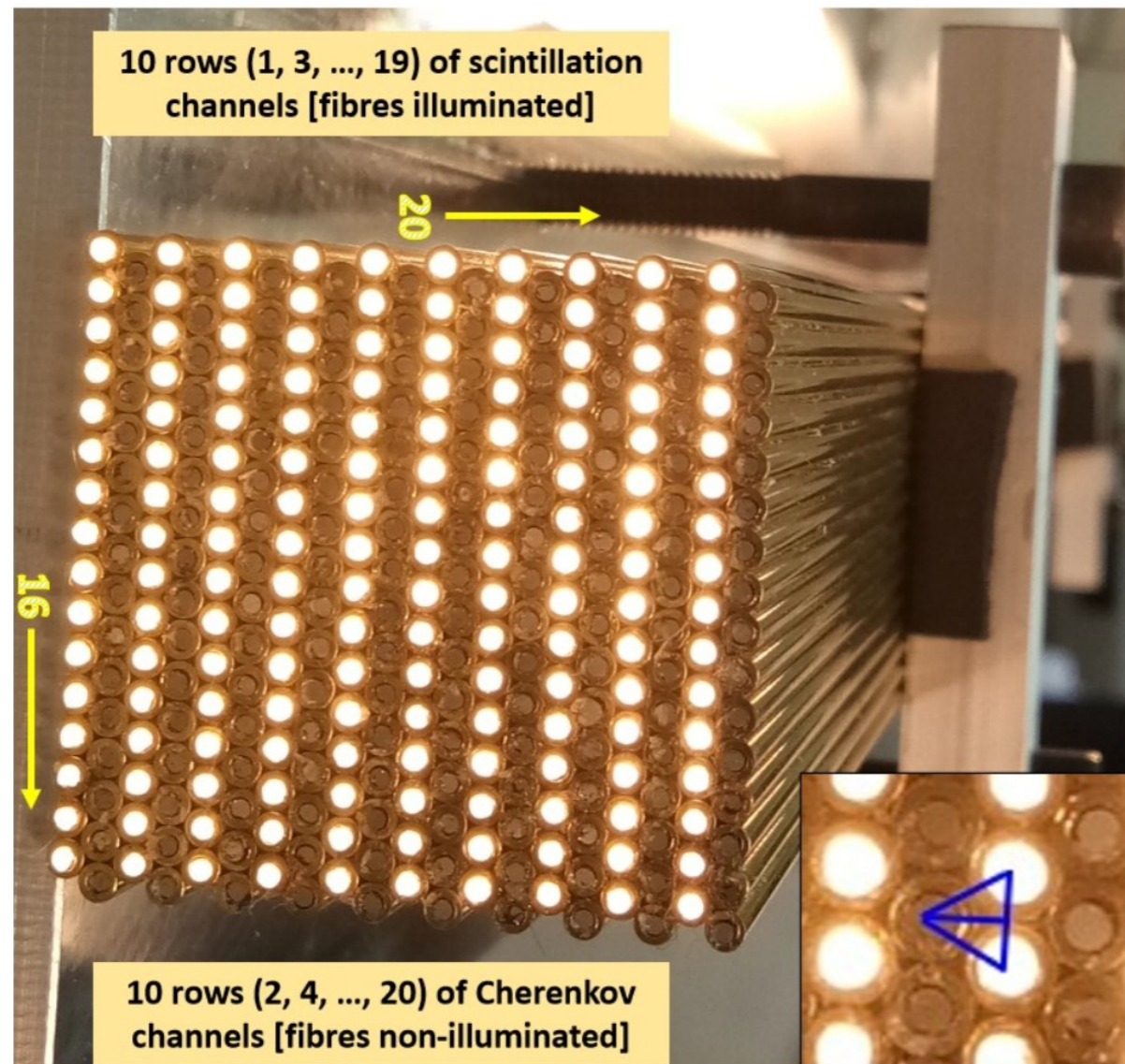
W/Z/H  $\rightarrow$  jj invariant mass



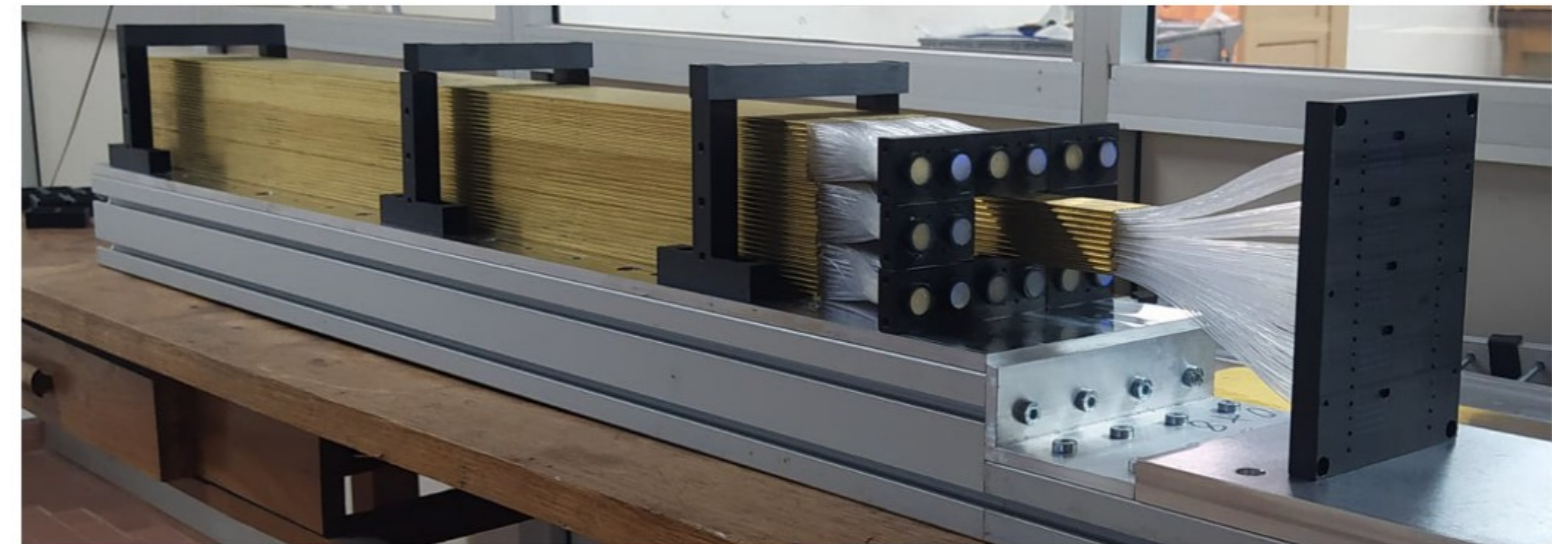


# IDEA 2020 em-size bucatini prototype (EU)

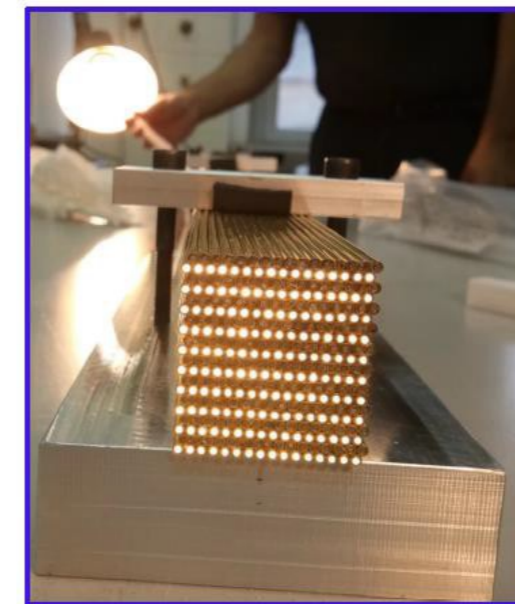
Nine  $\sim 3.5 \times 3.3$  cm<sup>2</sup> towers made of capillary brass tubes



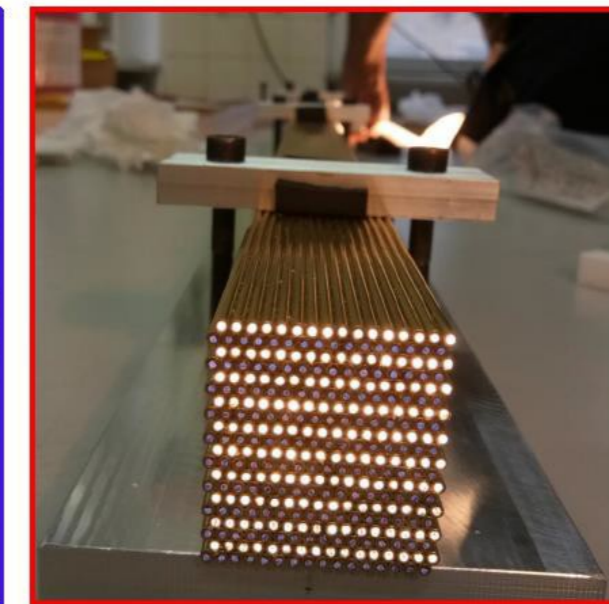
Central tower (360 fibres) w/ highly granular SiPM readout



Eight (surrounding) towers read out with PMTs



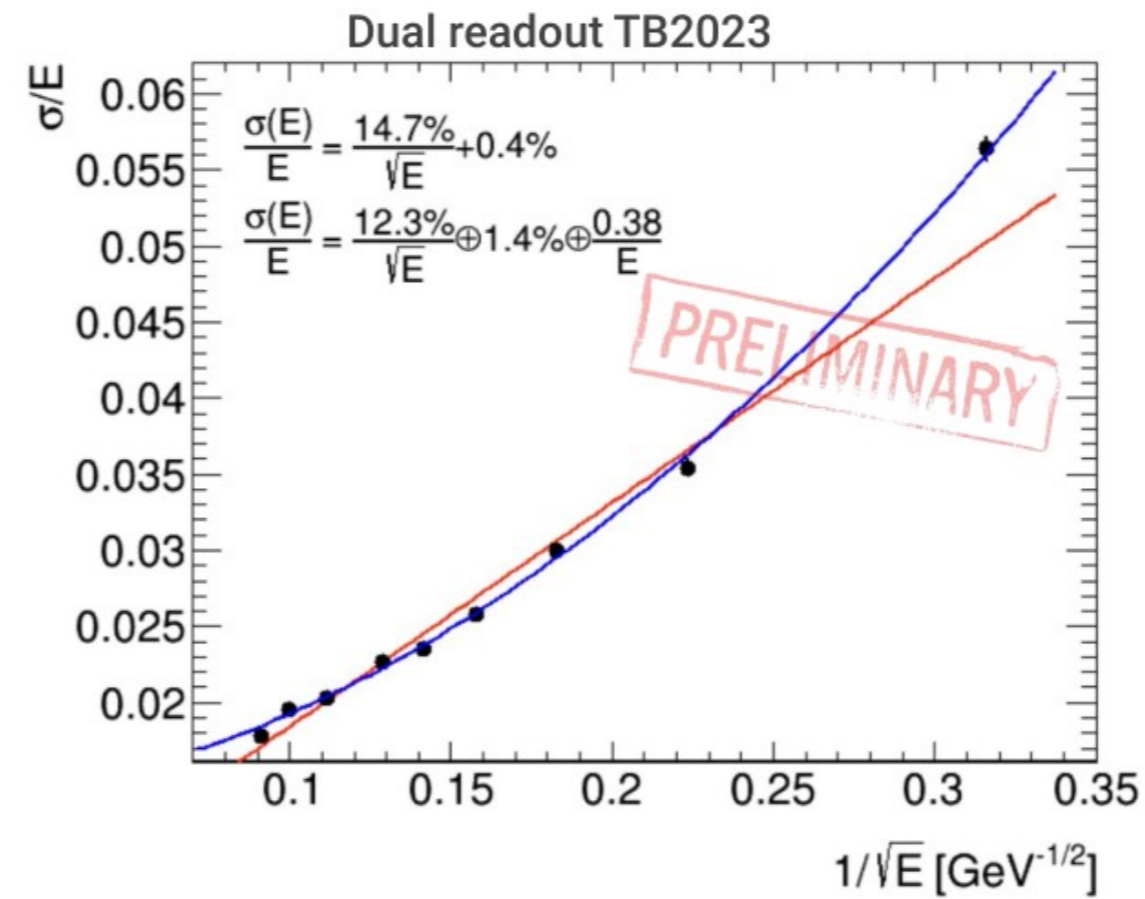
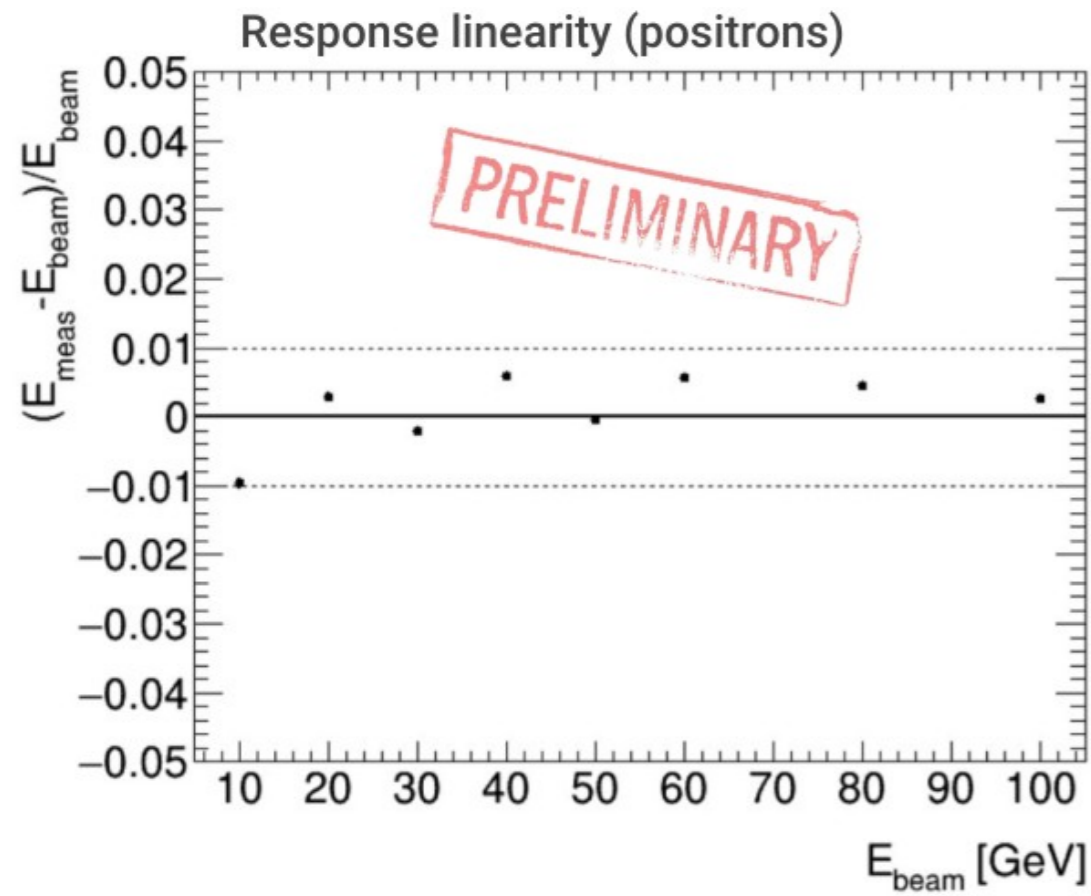
Scintillation fibers



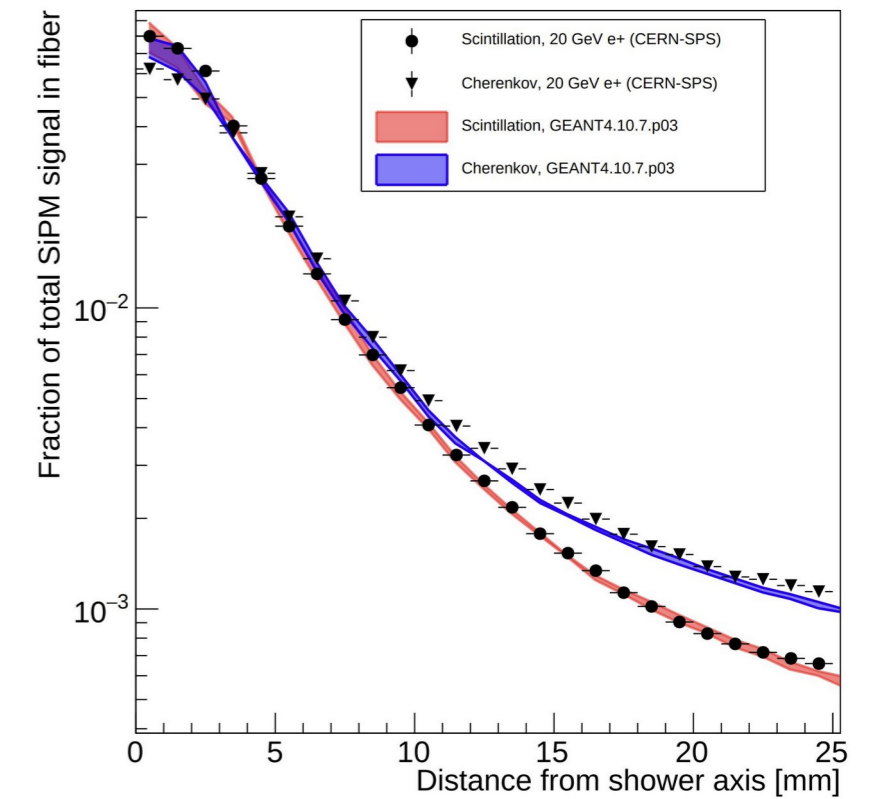
Cherenkov fibers



# Few testbeam results



### Lateral shower profile (2021 TB)



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## 5. Exploiting timing and DNNs

# $\tau$ -decay tagging w/ DNNs

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Testbeam module (brass absorber): dimensions:  $133.2 \times 133.2 \times 250 \text{ cm}^3$

Reduced granularity ( $1.2 \times 1.2 \text{ cm}^2$ , 32 S & 32 C fibres):  $111 \times 111$  modules

Simulation of both detector and SiPM response

Feature extraction: E(Q), Pk, ToP, ToA, ToT

→ each event represented by  $111 \times 111 \times 5 \times 2$  tensor

# NN implementation

Two DNN architecture variants studied:

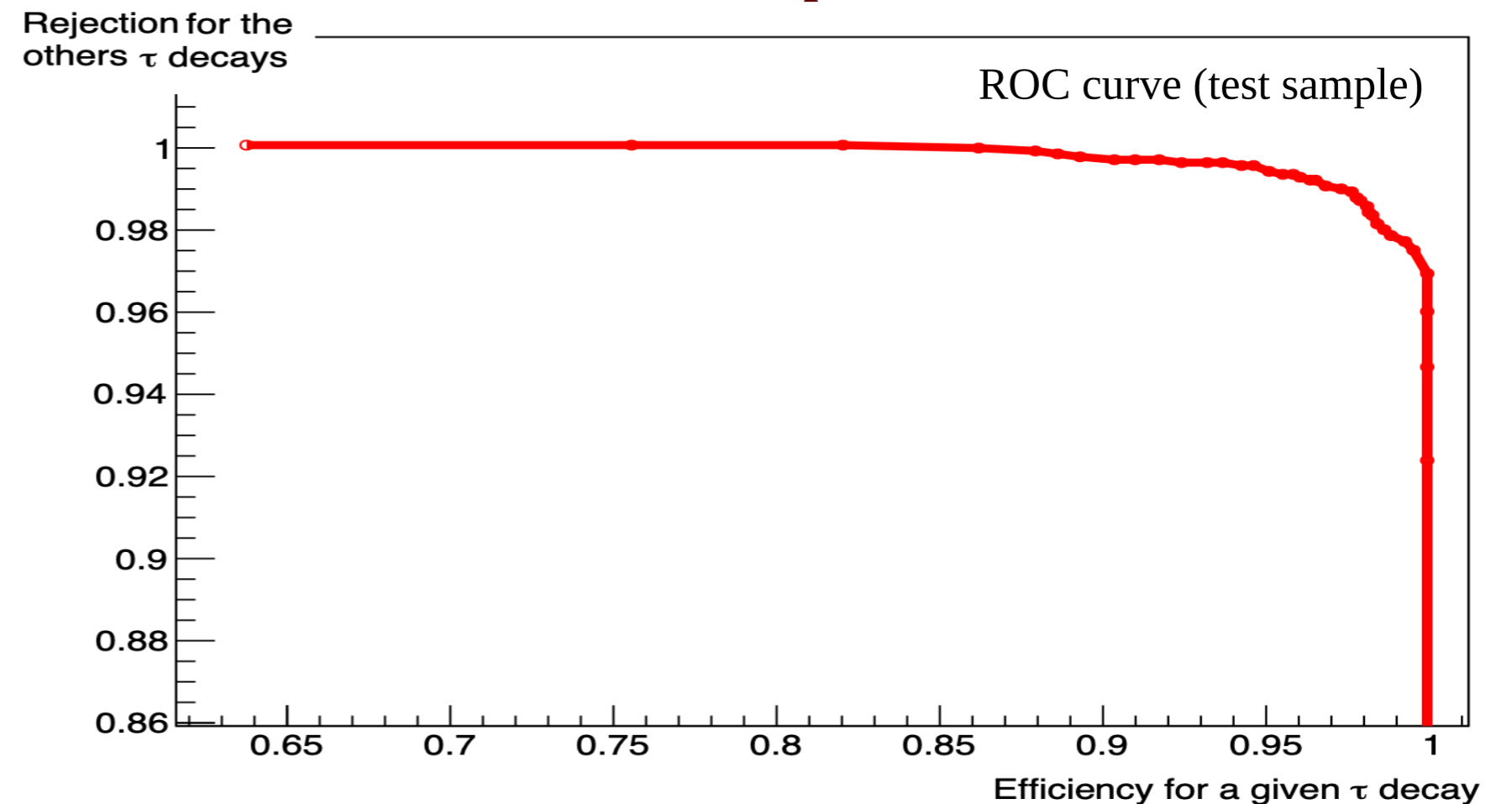
- VGG-11 like (VGG = Visual Geometry Group, Oxford Un.)
- Dynamic Graph CNN (DGCNN)

6 event classes (covering  $\sim 90\%$  of  $\tau$  decays)

Training set: 6 BR  $\times$  2000 evts

$\tau \rightarrow \pi\pi^0\nu$
$\tau \rightarrow \mu\nu\nu$
$\tau \rightarrow e\nu\nu$
$\tau \rightarrow \pi\nu$
$\tau \rightarrow \pi\pi\pi\nu$
$\tau \rightarrow \pi\pi^0\pi^0\nu$

VGG example

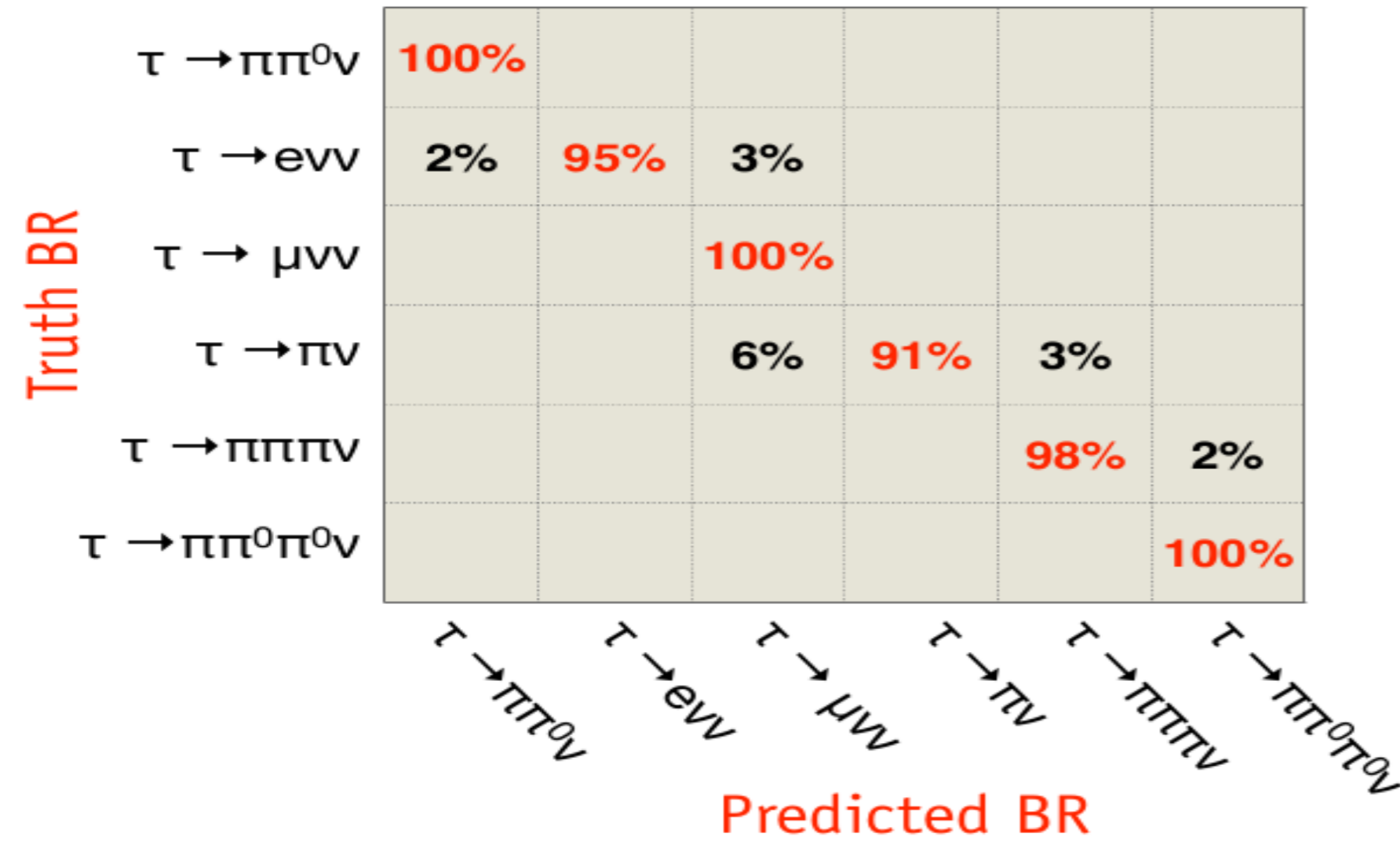




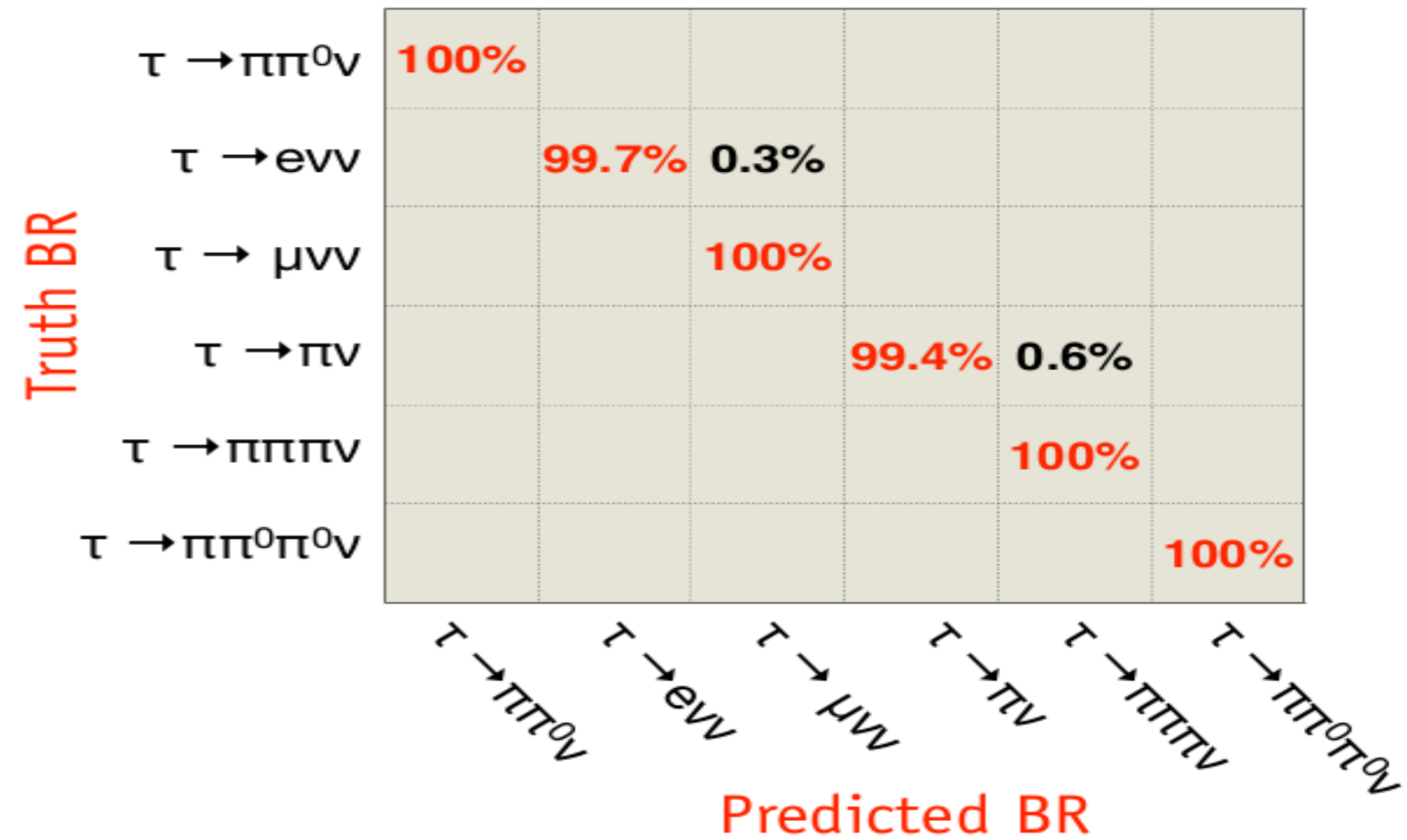
# NN performance

## Confusion matrix on test set

VGG-11  
average accuracy: 97.3%



DGCNN  
average accuracy: 99.9%



# DNN w/ IDEA layout (but no time info)

No SiPM response simulation

→ information: fibre signal output (# p.e.)

3-class classification:

$\tau_{lep}$ ,  $\tau_{had}$ , QCD jet

8-class classification:

$\tau_0$ ,  $\tau_1$ ,  $\tau_2$ ,  $\tau_3$ ,  $\tau_4$ ,  $\tau_5$ ,  $\tau_6$ , QCD jet

[  $\tau$  from  $Z \rightarrow \tau\tau$  decays ]

3-class label	8-class label	
0	0	$\tau \rightarrow \mu\nu\nu$
0	1	$\tau \rightarrow e\nu\nu$
1	2	$\tau \rightarrow \pi\nu$
1	3	$\tau \rightarrow \pi\pi^0\nu$
1	4	$\tau \rightarrow \pi\pi^0\pi^0\nu$
1	5	$\tau \rightarrow \pi\pi\pi\nu$
1	6	$\tau \rightarrow \pi\pi\pi^0\nu$
2	7	$Z \rightarrow qq$ jets

# DGCNN w/ geometrical information only

DGCNN optimised but w/o #pe as input feature  
B field and material in

Truth BR	$\tau \rightarrow e\nu\nu$	90.36	4.07	2.21	0.03	0.00	0.00	3.34	0.00
	$\tau \rightarrow \pi\nu$	2.57	86.24	5.39	0.25	3.59	0.17	1.57	0.22
	$\tau \rightarrow \pi\pi^0\nu$	2.10	18.92	72.67	2.76	1.97	1.01	0.27	0.30
	$\tau \rightarrow \pi\pi^0\pi^0\nu$	0.74	3.54	58.43	33.04	0.84	2.81	0.05	0.54
	$\tau \rightarrow \pi\pi\pi\nu$	0.11	9.88	6.22	0.46	75.32	6.49	0.00	1.52
	$\tau \rightarrow \pi\pi\pi\pi^0\nu$	0.11	1.49	9.30	2.90	38.28	43.75	0.05	4.12
	$\tau \rightarrow \mu\nu\nu$	2.50	0.70	0.17	0.00	0.03	0.00	96.60	0.00
	$Z \rightarrow qq \text{ jets}$	0.08	0.33	0.63	0.94	2.92	3.09	0.08	91.92
		$\tau \rightarrow e\nu\nu$	$\tau \rightarrow \pi\nu$	$\tau \rightarrow \pi\pi^0\nu$	$\tau \rightarrow \pi\pi^0\pi^0\nu$	$\tau \rightarrow \pi\pi\pi\nu$	$\tau \rightarrow \pi\pi\pi\pi^0\nu$	$\tau \rightarrow \mu\nu\nu$	$Z \rightarrow qq \text{ jets}$
		Predicted BR							

input: fibre coordinates only  
avg accuracy: 73.7%

Truth BR	$\tau \rightarrow e\nu\nu$	96.95	0.79	0.62	0.03	0.00	0.00	1.58	0.03
	$\tau \rightarrow \pi\nu$	3.09	89.03	3.48	0.41	2.02	0.39	1.44	0.14
	$\tau \rightarrow \pi\pi^0\nu$	1.77	4.83	80.45	9.25	1.61	1.67	0.16	0.25
	$\tau \rightarrow \pi\pi^0\pi^0\nu$	0.30	0.38	10.43	84.55	0.16	3.87	0.05	0.25
	$\tau \rightarrow \pi\pi\pi\nu$	0.16	3.52	1.38	0.35	84.82	8.79	0.03	0.95
	$\tau \rightarrow \pi\pi\pi\pi^0\nu$	0.11	0.24	1.98	2.60	10.19	82.60	0.08	2.20
	$\tau \rightarrow \mu\nu\nu$	2.53	0.48	0.11	0.00	0.03	0.00	96.82	0.03
	$Z \rightarrow qq \text{ jets}$	0.08	0.25	0.19	1.05	2.54	4.08	0.06	91.75
		$\tau \rightarrow e\nu\nu$	$\tau \rightarrow \pi\nu$	$\tau \rightarrow \pi\pi^0\nu$	$\tau \rightarrow \pi\pi^0\pi^0\nu$	$\tau \rightarrow \pi\pi\pi\nu$	$\tau \rightarrow \pi\pi\pi\pi^0\nu$	$\tau \rightarrow \mu\nu\nu$	$Z \rightarrow qq \text{ jets}$
		Predicted BR							

input: fibre coordinates + type  
avg accuracy: 88.3% (w/ #p.e. 90.8%)

# longitudinal segmentation w/ timing (U.S.)

Dual-readout fibre calorimeter → signal sampled at 20 GHz

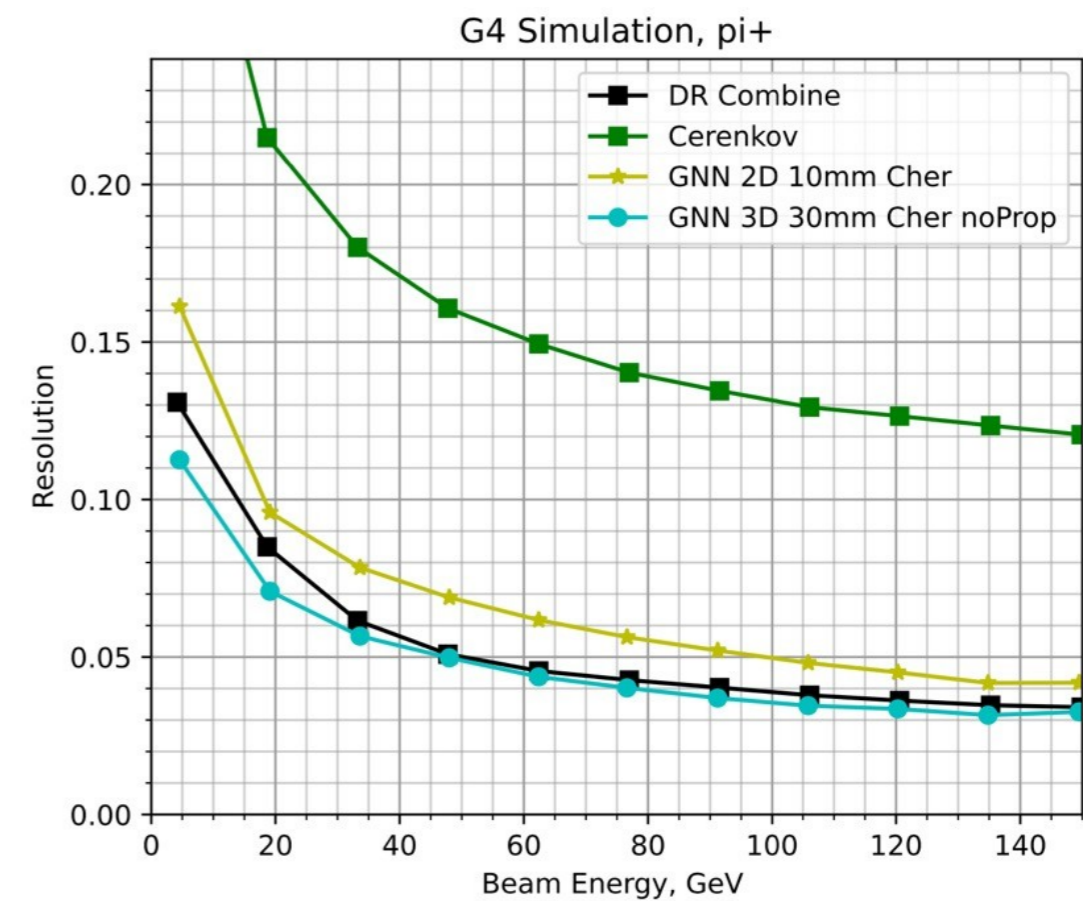
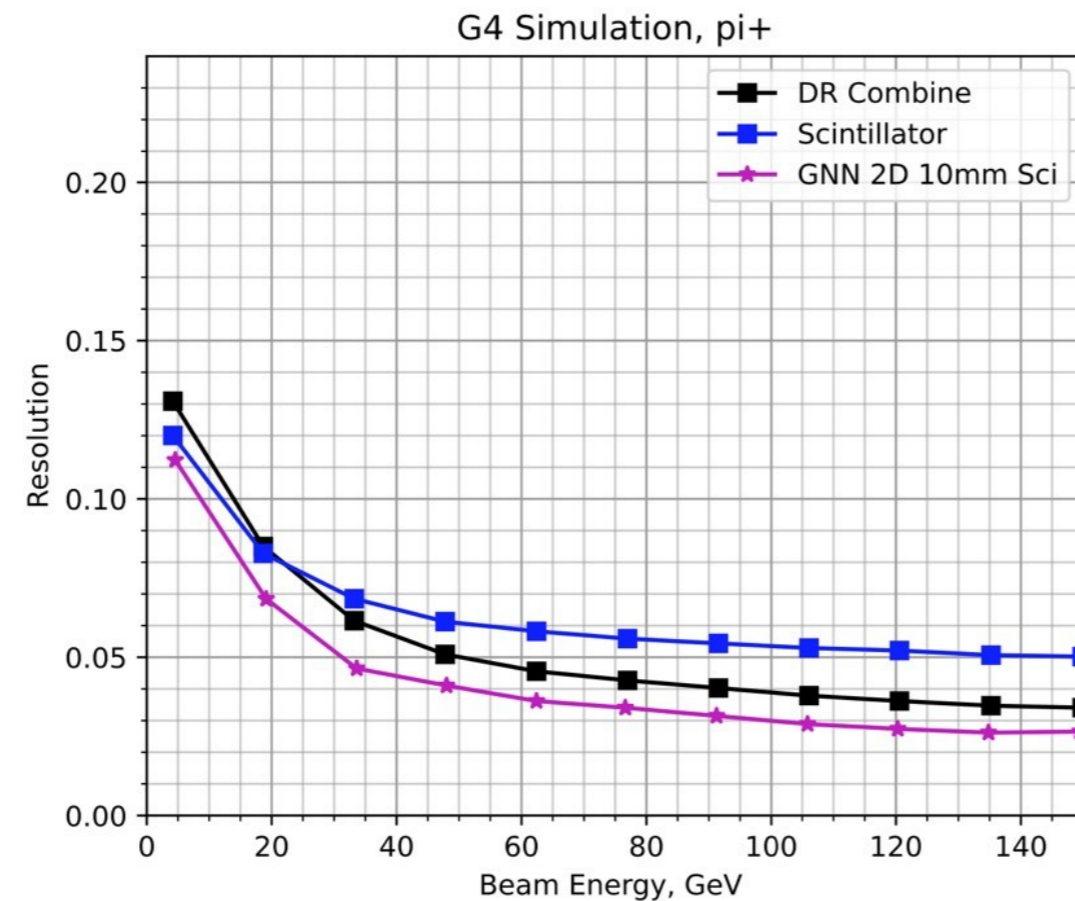
Cu absorber (2 m deep)

Preliminary results  
No optimisation

Fibre axis aligned w/ beam direction: 1 mm  $\Phi$  fibres, 1.5 mm spacing

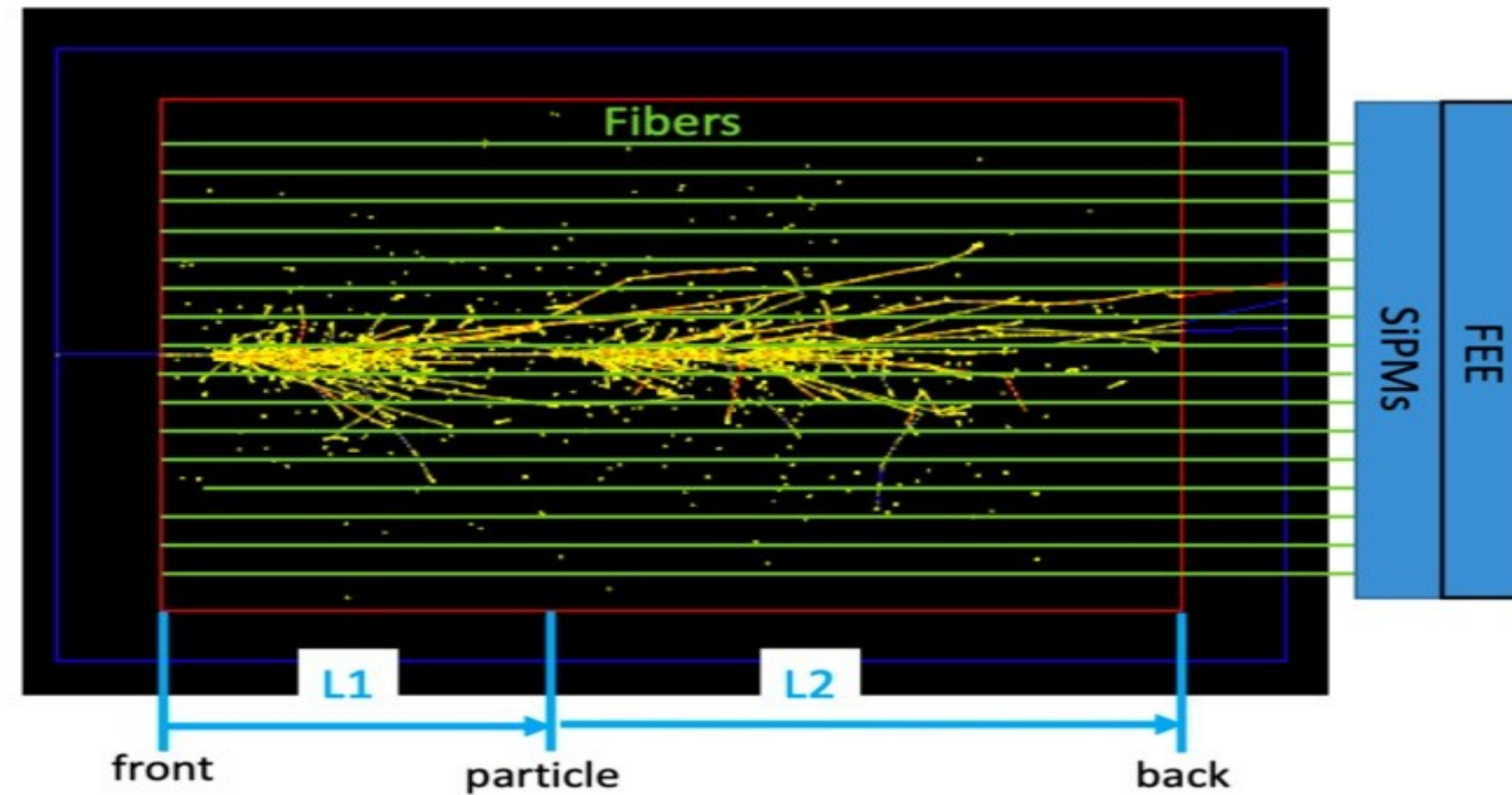
Transverse segmentation: 1×1 cm<sup>2</sup> for 2D analysis, 3×3 cm<sup>2</sup> for 3D analysis

## 3D imaging fibre DR calorimeter coupled to Graph DNN





# longitudinal segmentation w/ timing (U.S.)



**Table 1.** The energy resolution of the 3D GNN reconstruction with various timing resolutions for longitudinal segmentation.

Timing Resolution $\Delta(t), \text{ps}$	Position Resolution $\Delta(z), \text{cm}$	Energy Resolution $\sigma/E, \%$	@ 100 GeV
0	0.0	3.6	
100	5.0	3.9	
150	7.5	4.0	
200	10.0	4.2	

only Cherenkov fibres

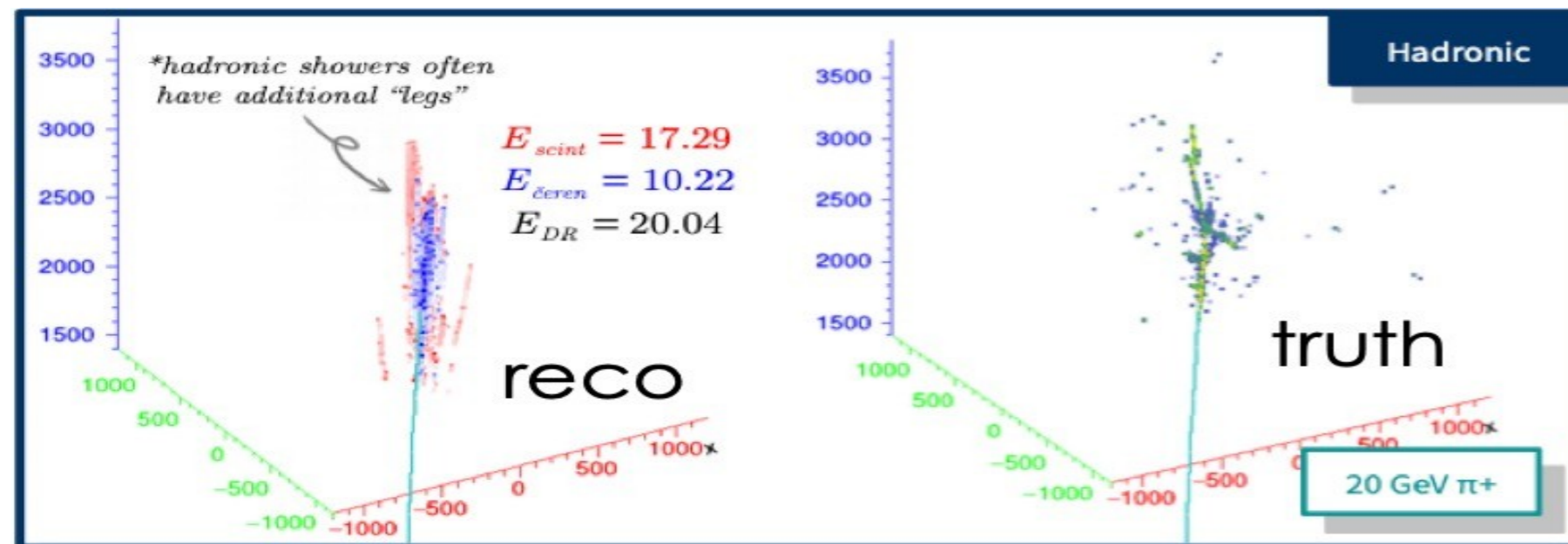
# longitudinal segmentation w/ timing (Korea)

Full SiPM signal sampled at 10 GHz

FFT used to mitigate exponential tail

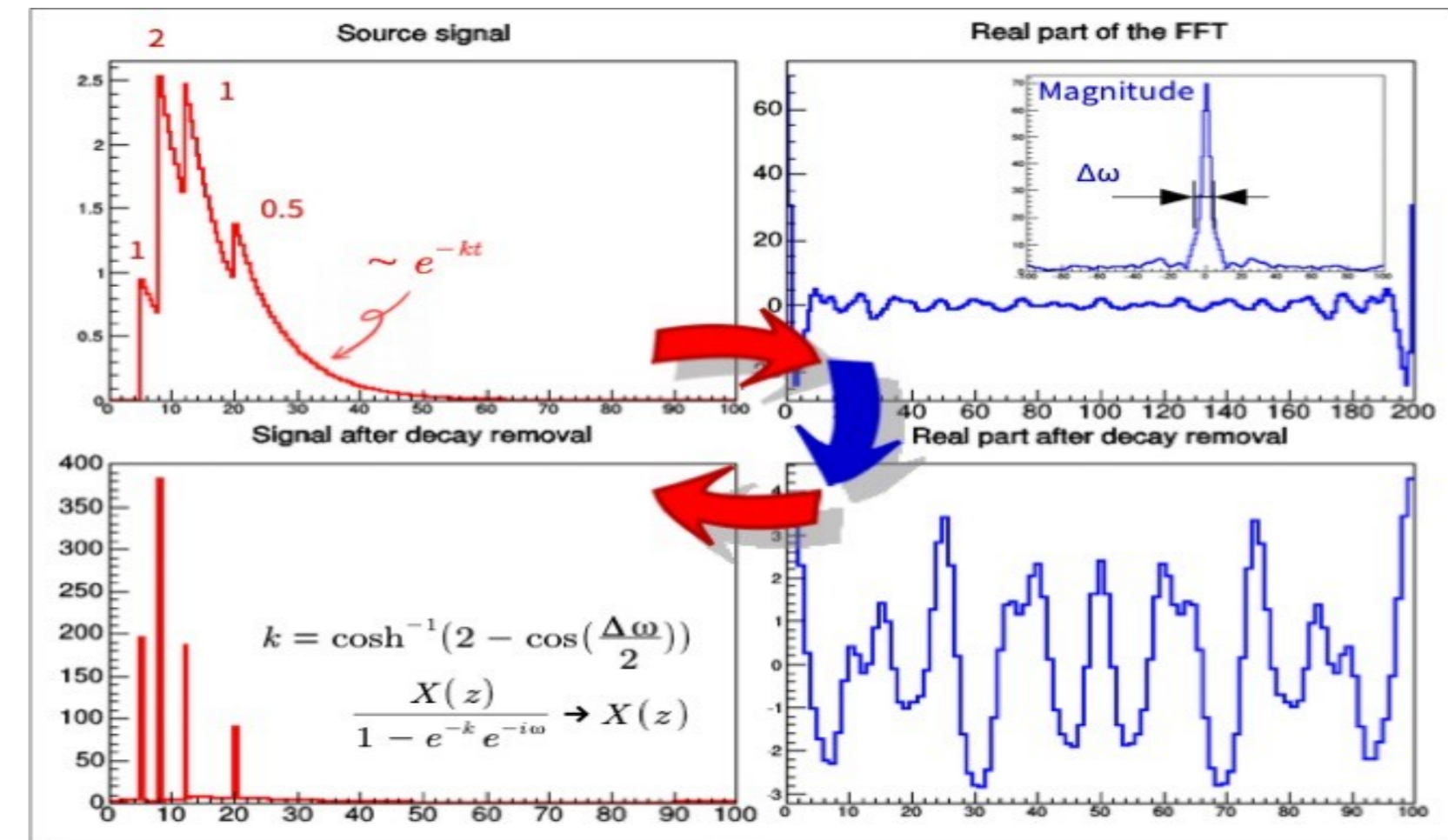
Unlocks full longitudinal information about energy deposit

Combined with DR information allows in-shower cluster identification



Time domain

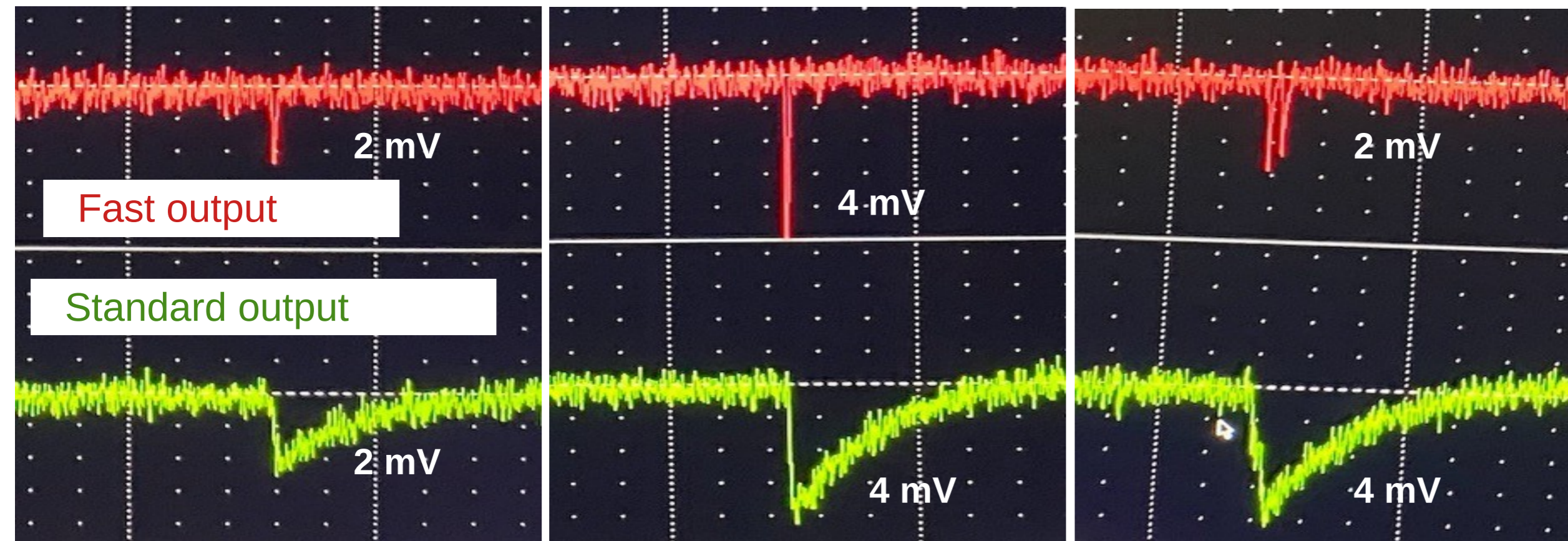
Frequency domain





# waveform digitisation (U.S.)

Results with SensL (MicroFC-30020SMT):  
SiPM with both fast and standard outputs



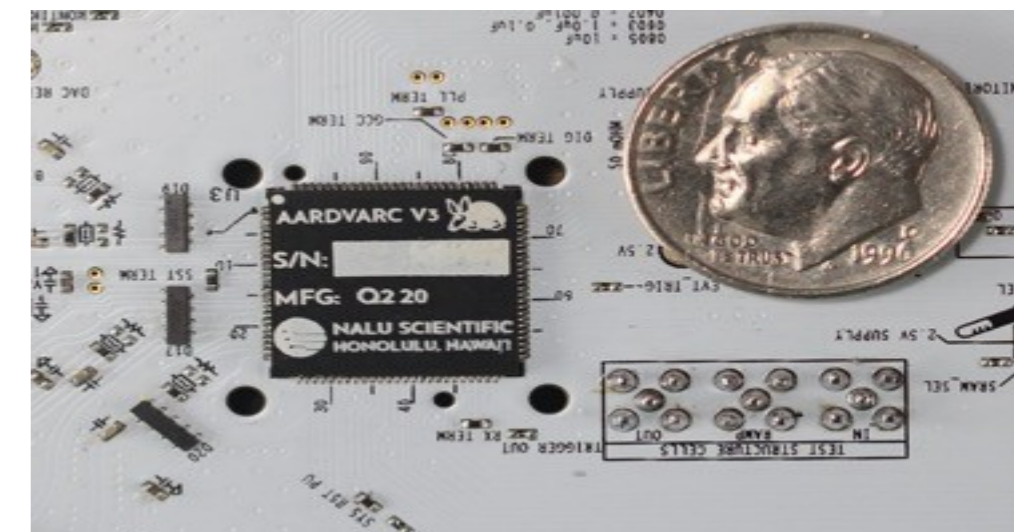
One-photon event

Two-photon event  
(simultaneous)

Two-photon event  
(5 ns apart)

NALU Scientific  
AARDVARC v3

- Sampling rate 10-14 GS/s
- 12 bits ADC
- 4-8 ps timing resolution
- 32 k sampling buffer
- 2 GHz bandwidth
- System-on-Chip (CPU)



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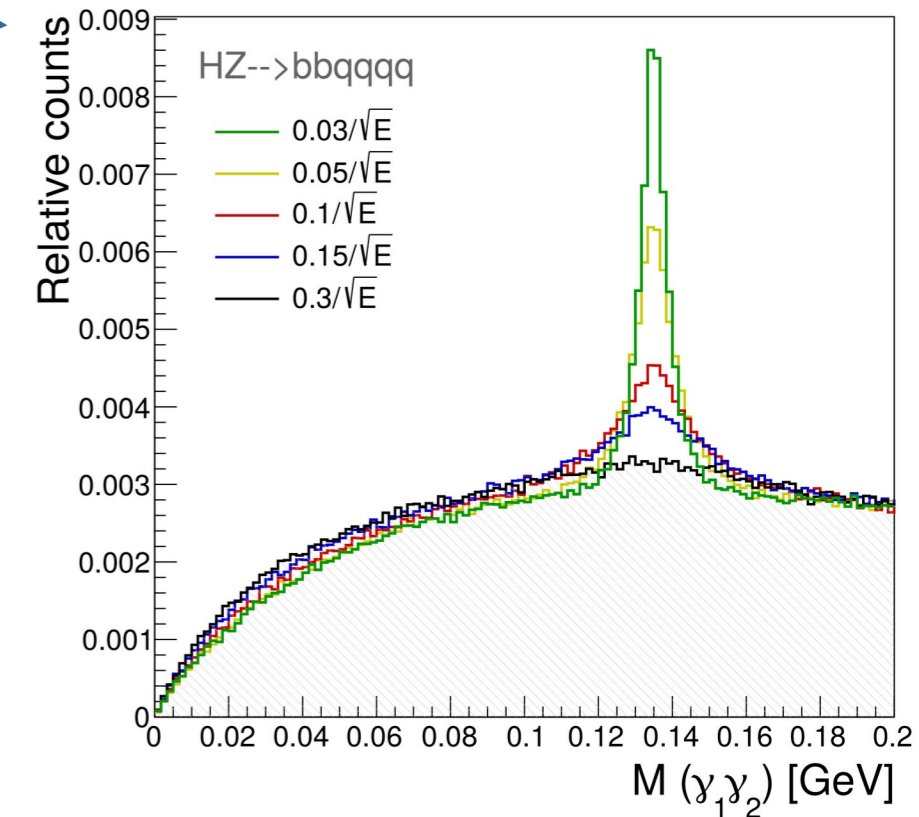
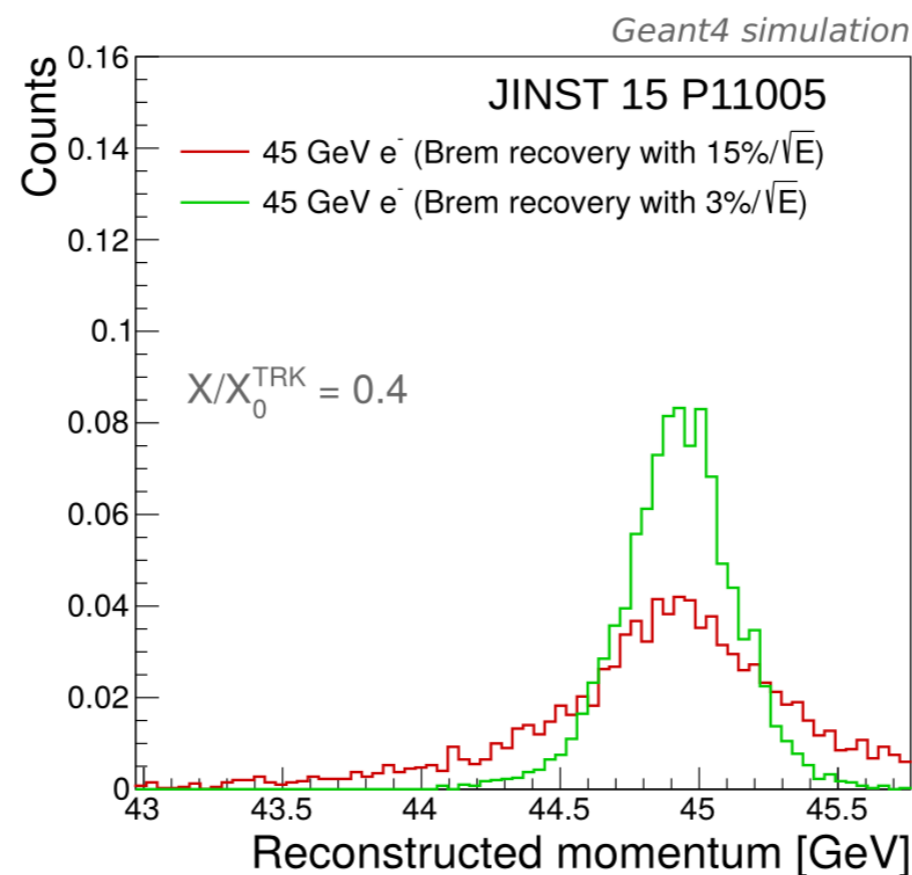
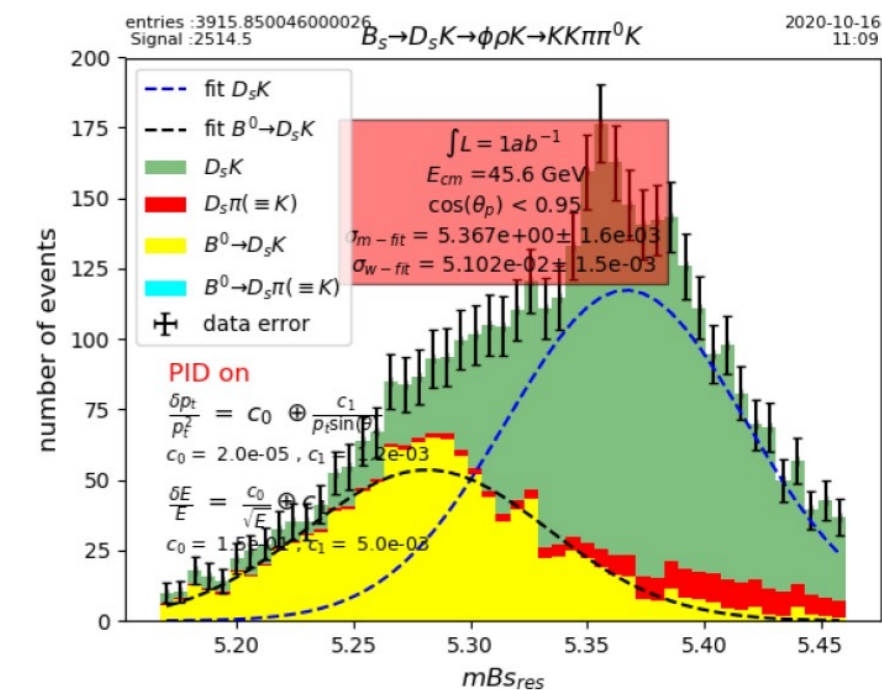
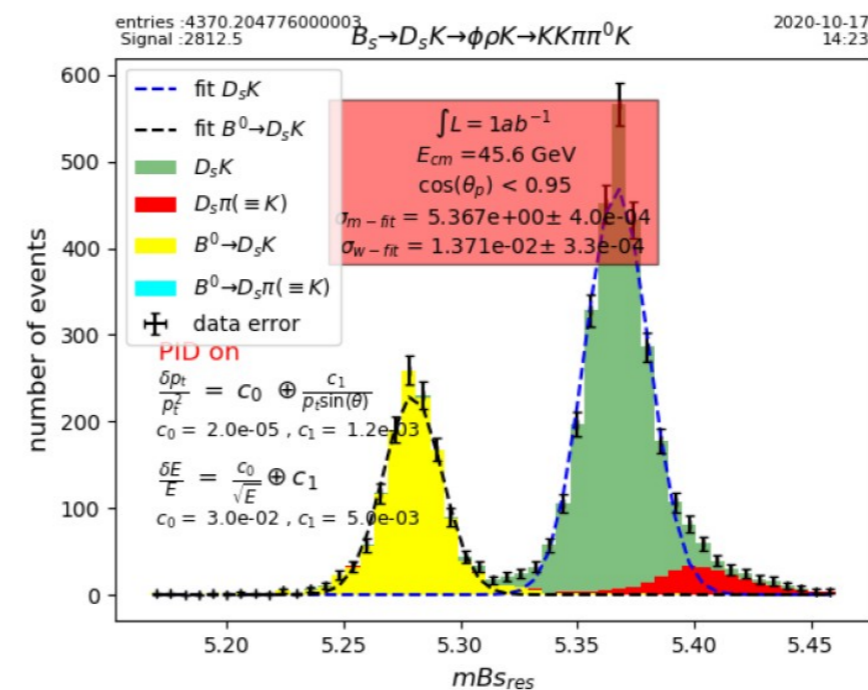
## 6. Crystal option (IDEA++) and pPFA



# high EM energy resolution @ FCC-ee

3%/√E EM energy resolution → improve event reconstruction and **expand landscape for physics studies @ e<sup>+</sup>e<sup>-</sup> colliders**

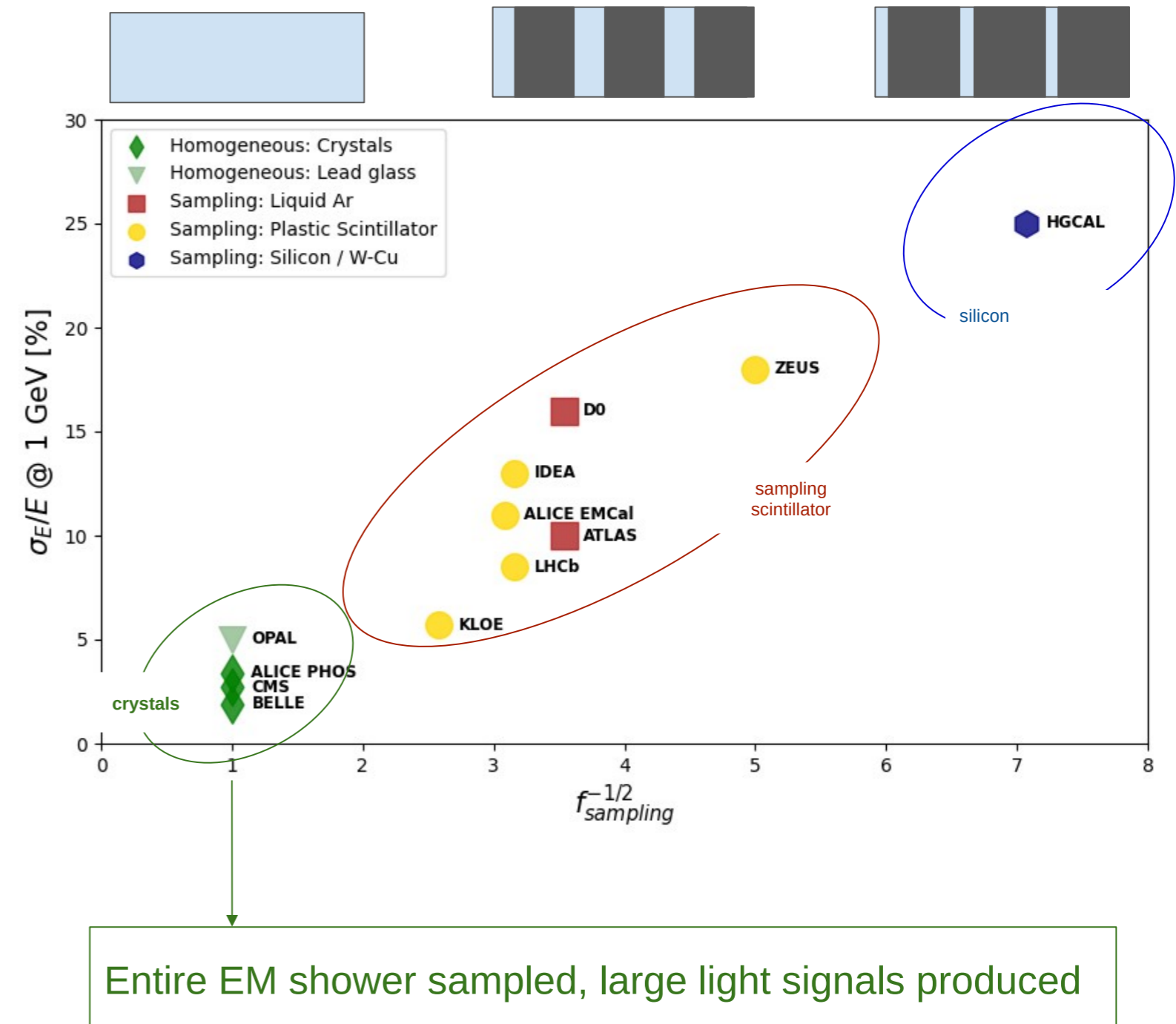
- CP violation studies with B<sub>s</sub> decay to final states with low energy photons
- Clustering of π<sup>0</sup>'s photons to improve performance of jet clustering algorithms
- Improve resolution of recoil-mass signal from Z → ee decays (recovering brems photons)



# homogeneous crystal calorimetry

- Long history in pushing frontier of high EM resolution
- Only way to get  $1-3\%/\sqrt{E}$  energy resolution for photons (and thus  $\pi^0$ 's)
- No stringent requirements on radiation tolerance and pileup @ future  $e^+e^-$  Higgs factorier → can exploit best possible precision of event reconstruction

A sample of existing and future calorimeters



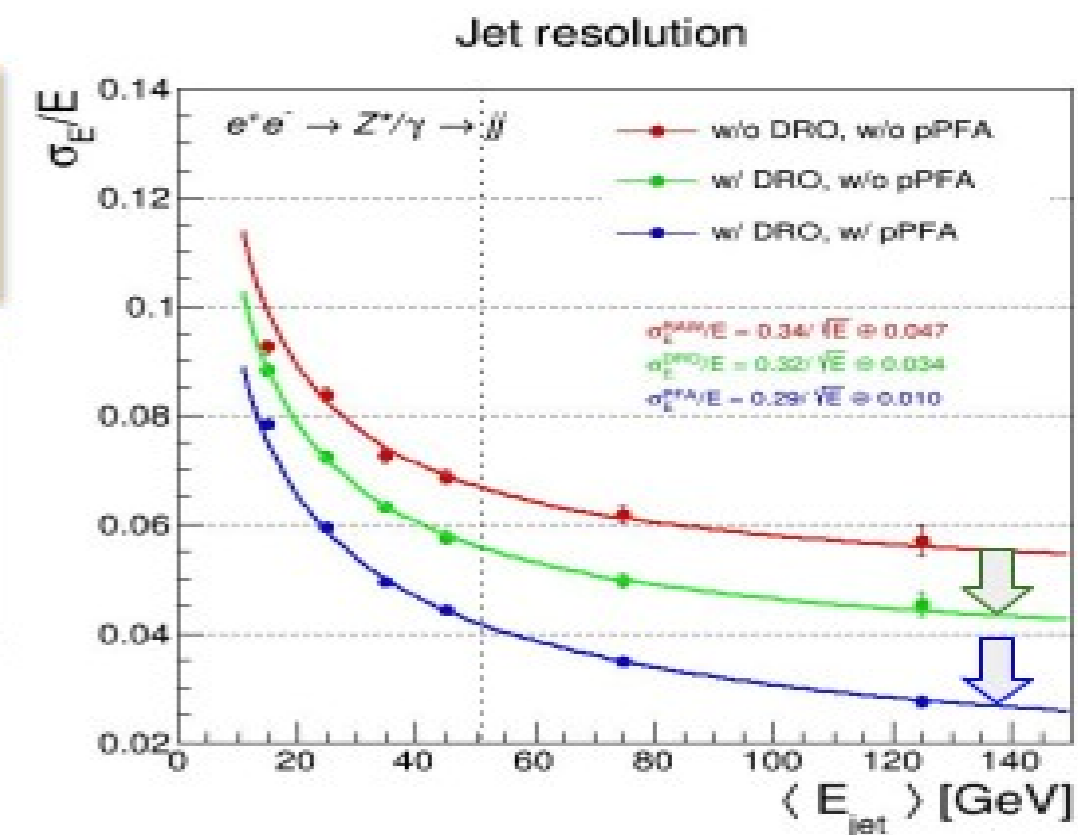
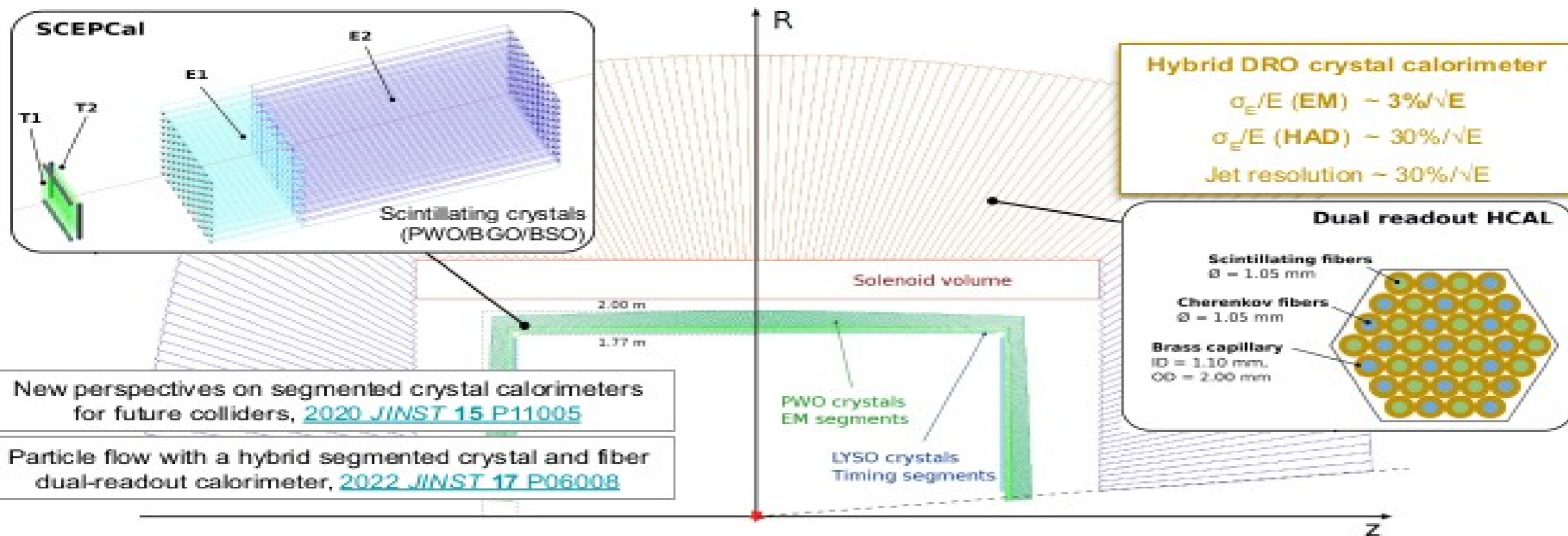
# dual-readout crystal option (IDEA++)

## Segmented Crystal EM Precision Calorimeter

ongoing joint efforts within US Calvision, IDEA and Crystal Clear collaborations

proof-of-concept with lab measurements and prototypes (PWO, BGO, BSO, ... with SiPM readout)

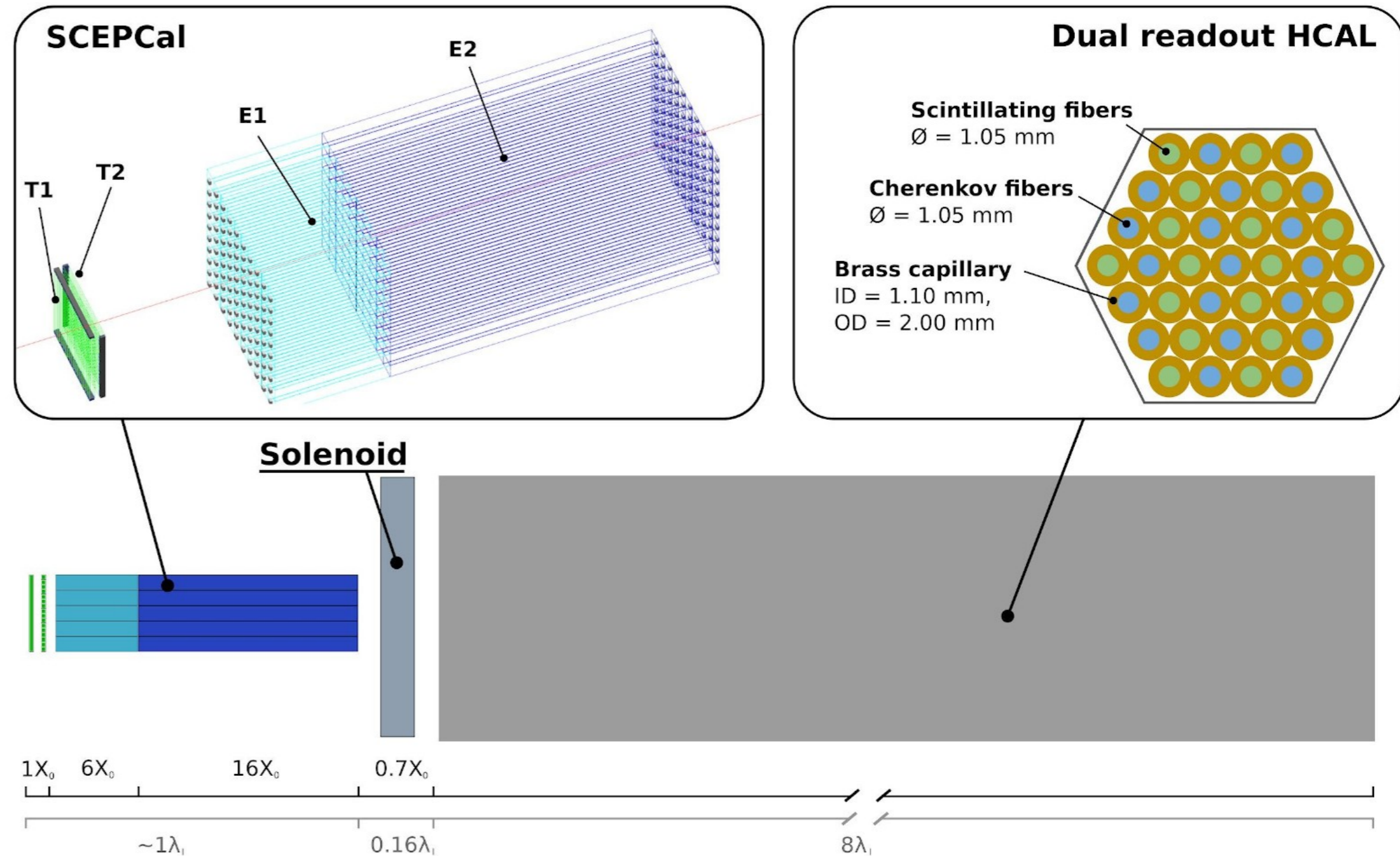
ongoing simulation effort in DD4HEP and FCC software + DR-pPFA developments





# dual-readout crystal option (IDEA++)

- ◆ **ECAL** ~20 cm  $\text{PbWO}_4$ 
  - ◆ 2 layers: 6+16  $X_0$
  - ◆ DR with filters
  - ◆  $\sigma_{\text{EM}} \approx 3\% / \sqrt{E}$
- ◆ **timing layer**
  - ◆ LYSO:Ce crystals
  - ◆  $\sigma_t \sim 20$  ps
- ◆ **HCAL layer**
  - ◆  $\sigma_{\text{HAD}}/E \sim 26\% / \sqrt{E}$

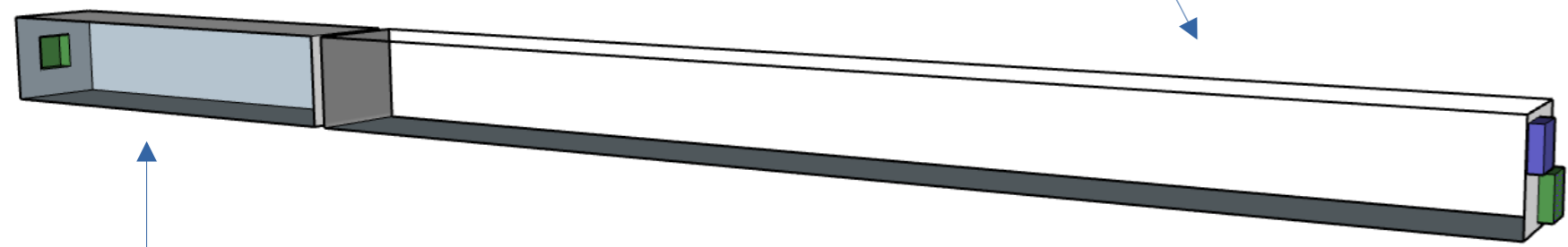




# dual-readout in crystals

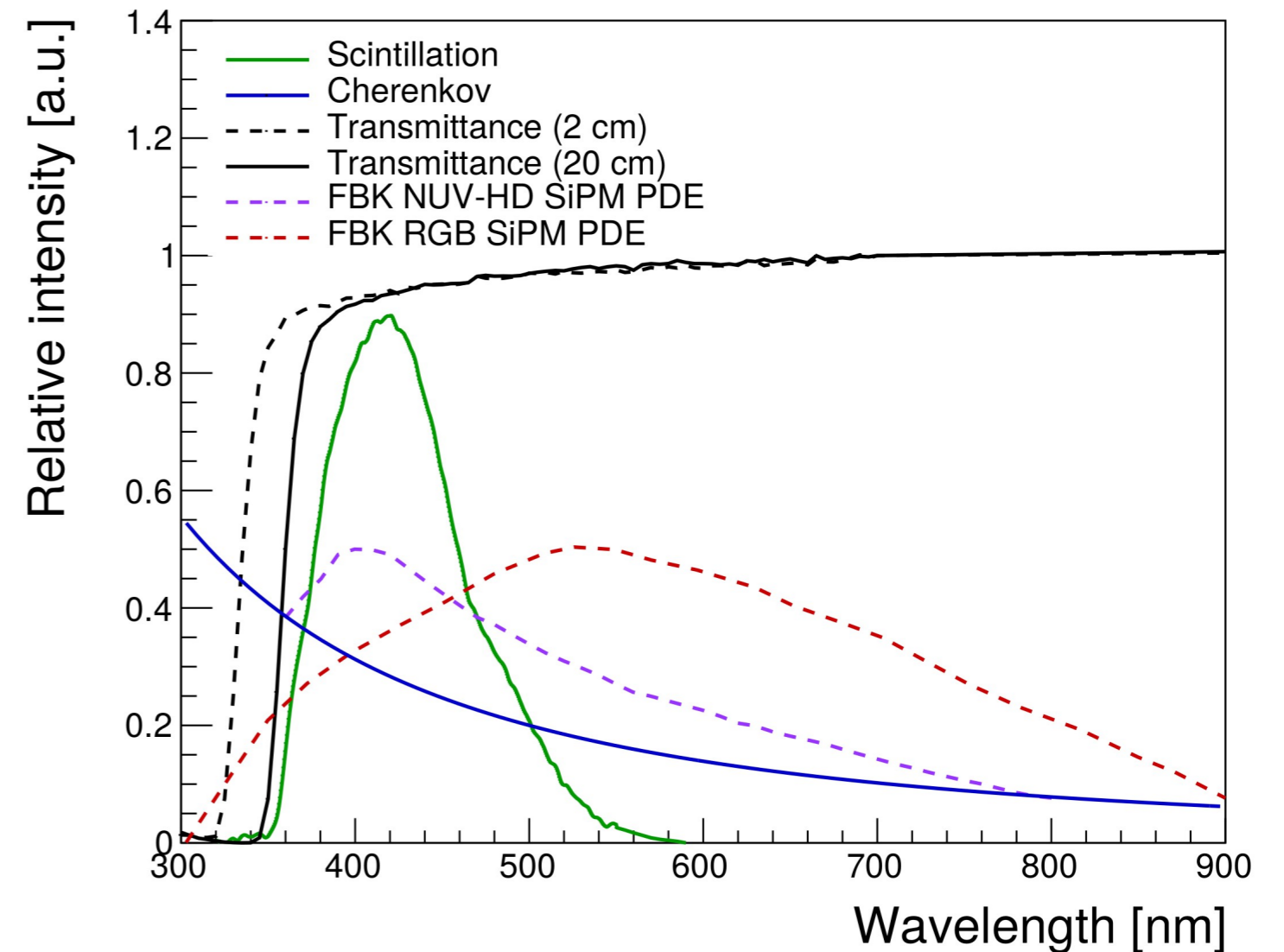
- Simultaneous readout of scintillation and Cherenkov light from same active element with dedicated SiPMs and wavelength filters

Rear crystal ECAL segment: two  $4 \times 4 \text{ mm}^2$  SiPMs with optical filters optimised for scintillation and Cherenkov detection



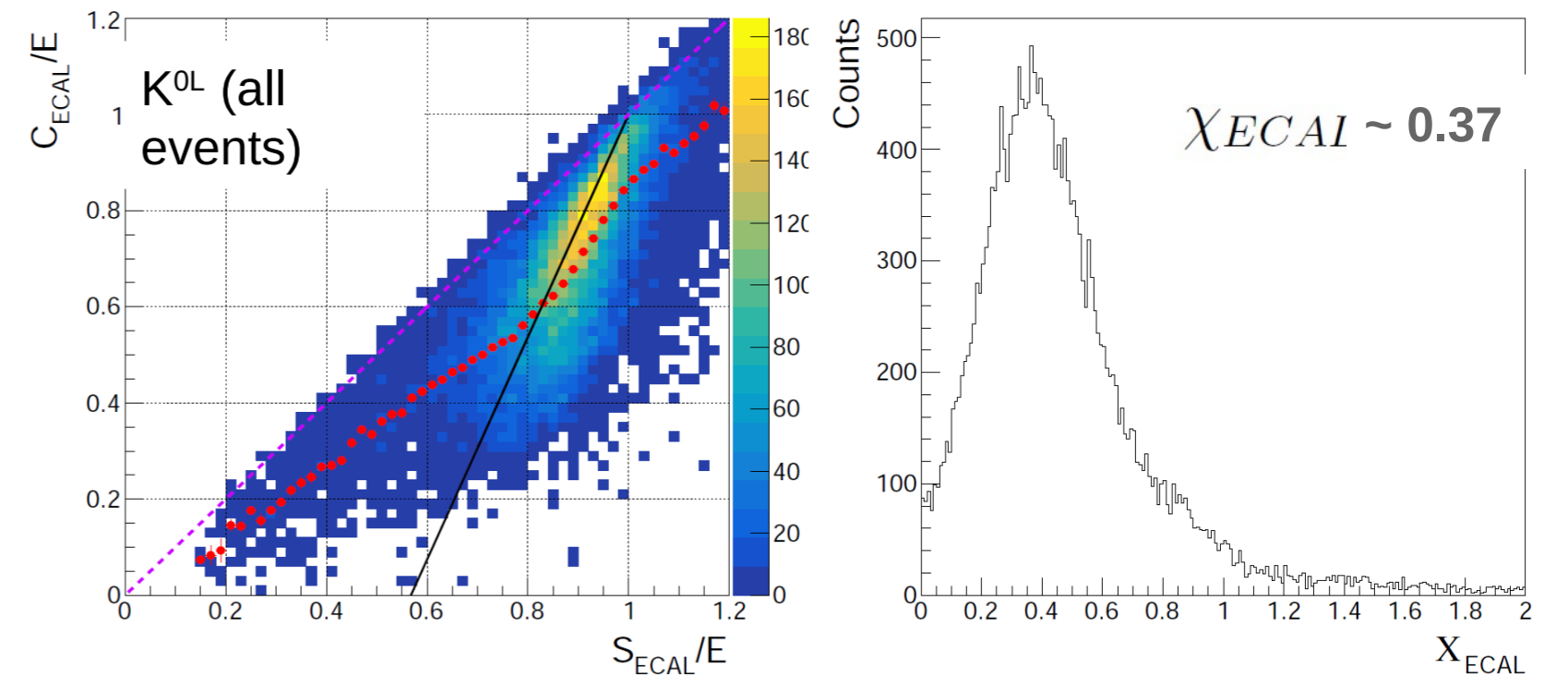
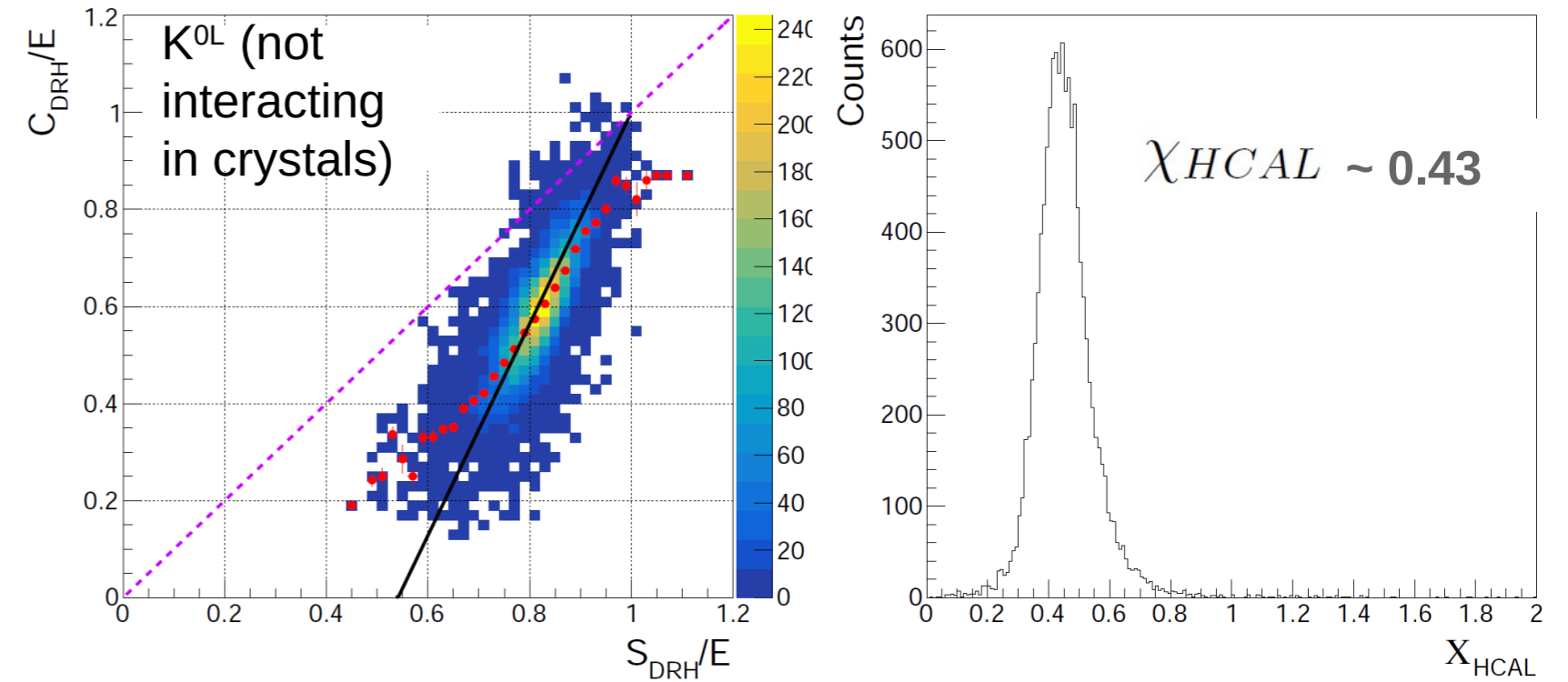
Front crystal ECAL segment: single  $5 \times 5 \text{ mm}^2$  SiPM per crystal optimised for scintillation light detection

PWO



# dual-readout method in hybrid system

1. Independently evaluate  $\chi$ -factors for crystal and fibre sections
2. Independently apply DRO correction on energy deposits for crystal and fibre sections
3. Add up corrected energy from both sections



$$\chi_{HCAL} = \frac{1 - (h/e)_s^{HCAL}}{1 - (h/e)_c^{HCAL}}$$

$$\chi_{ECAL} = \frac{1 - (h/e)_s^{ECAL}}{1 - (h/e)_c^{ECAL}}$$

$$E_{HCAL} = \frac{S_{HCAL} - \chi_{HCAL} C_{HCAL}}{1 - \chi_{HCAL}}$$

$$E_{ECAL} = \frac{S_{ECAL} - \chi_{ECAL} C_{ECAL}}{1 - \chi_{ECAL}}$$

$$E_{total} = E_{HCAL} + E_{ECAL}$$

# light yields (assumptions)

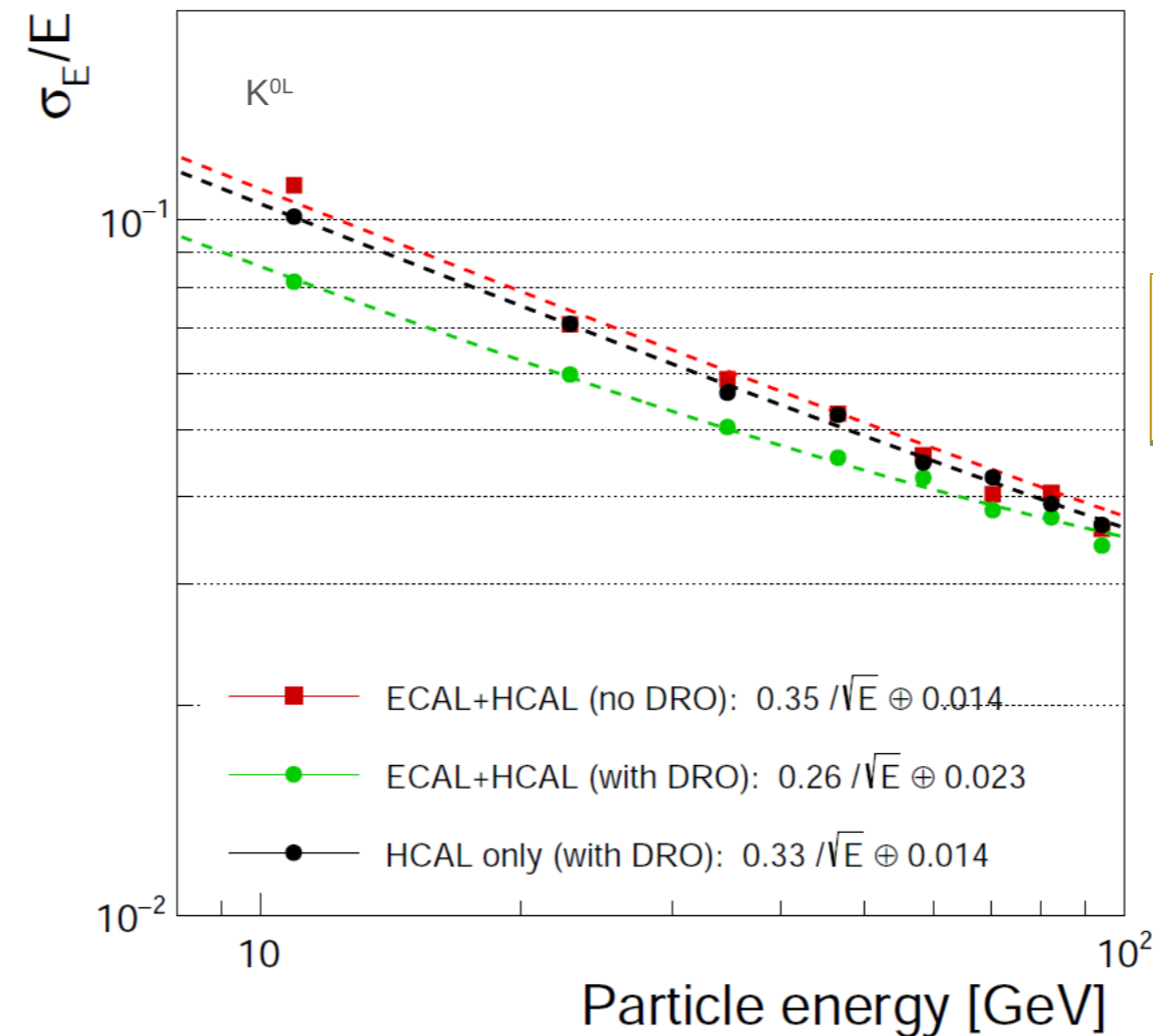
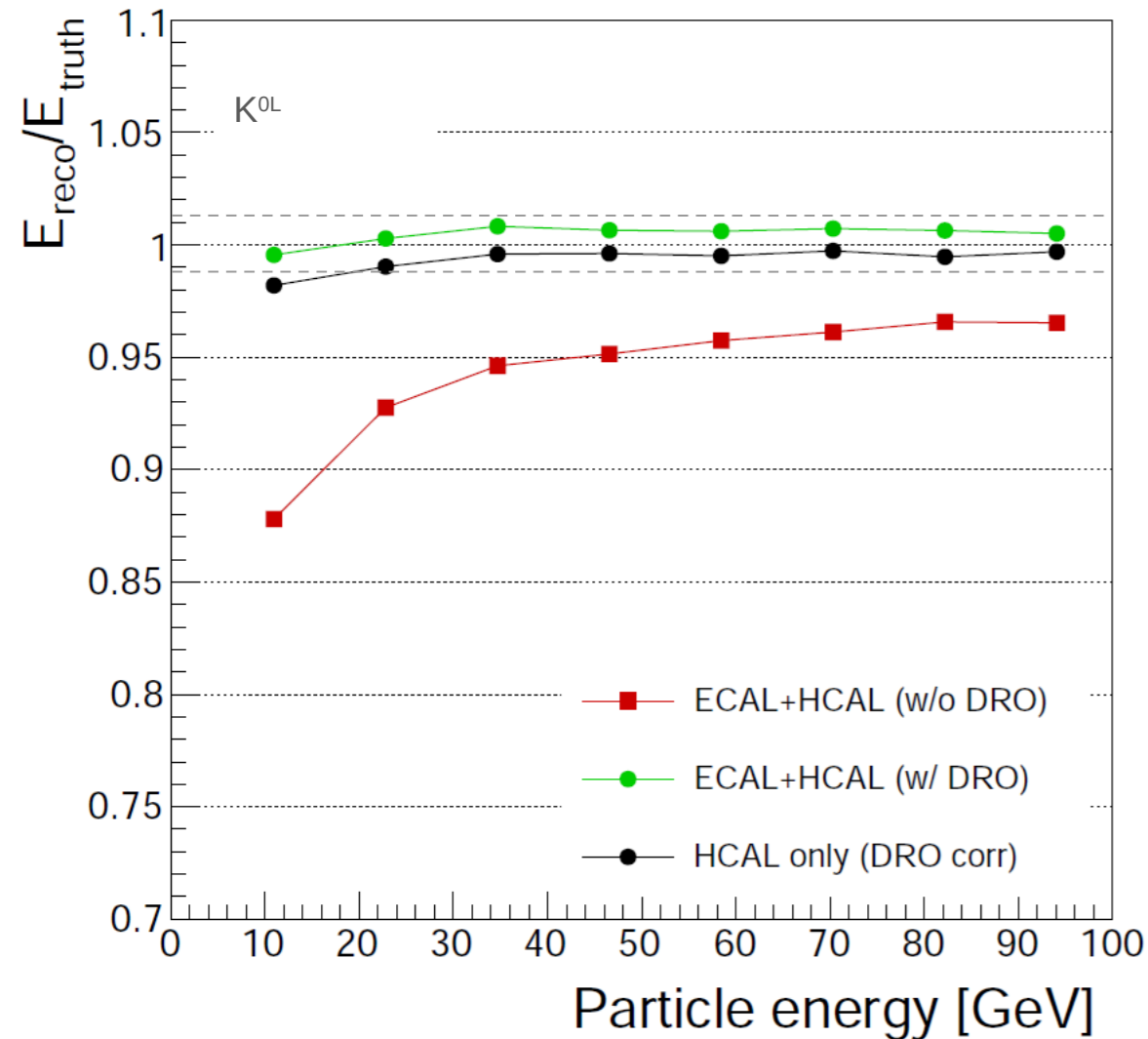
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- ECAL (crystal section): 2000 (scintillation) and 160 (Cherenkov) p.e./GeV
- HCAL (fibre section): 400 (S) and 100 (C ) p.e./GeV

# Energy resolution for neutral hadrons

- **Dual-readout method confirms applicability to hybrid calorimeter system**

- Response linearity to hadrons restored within  $\pm 1\%$
- Hadron energy resolution comparable to fibre-only IDEEA calorimeter



$$\sigma_E/E_{\text{HAD}} \sim 27\%/\sqrt{E} \oplus 2\%$$



# DR-oriented PF approach (DR-pPFA)

- Different optimisation of PF algorithm required for coarsely segmented calorimeter
- Q: Could better energy linearity and resolution offset coarser longitudinal segmentation?

	High granularity Si/W ECAL and scintillator based HCAL	Fiber-based dual-readout calorimeter	Hybrid crystal and dual-readout calorimeter	
N. of longitudinal layers	> 40	1	5	Moderate longitudinal segmentation (helpful to identify and measure $\pi^0$ jet component)
ECAL cell cross-section	25–100 mm <sup>2</sup>	2–144 mm <sup>2</sup>	100 mm <sup>2</sup>	
HCAL cell cross-section	100–900 mm <sup>2</sup>		400–2500 mm <sup>2</sup>	
EM energy resolution	15 – 25%/ $\sqrt{E}$	10 – 15%/ $\sqrt{E}$	$\approx 3\%/\sqrt{E}$	Highest energy resolution and linearity
HAD energy resolution	45 – 55%/ $\sqrt{E}$	25 – 30%/ $\sqrt{E}$	$\approx 25 – 30\%/\sqrt{E}$	

Highest longitudinal segmentation

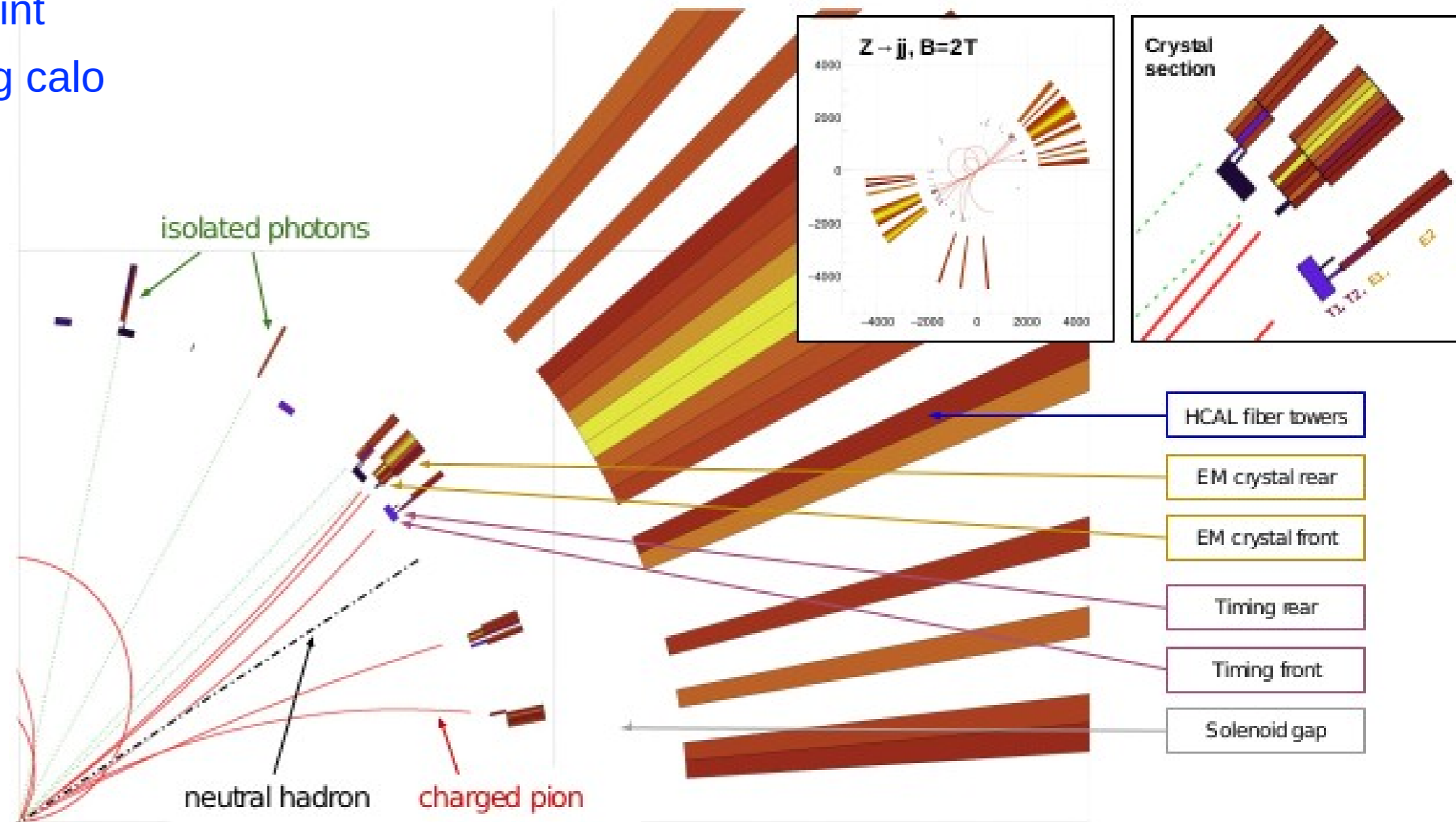
Highest transverse segmentation: full potential  
(e.g. using neural networks) yet to be explored

# jet reconstruction → IDEA++ DR-pPFA

<https://doi.org/10.1088/1748-0221/17/06/P06008>

Geant4 simulation of  $Z \rightarrow jj$  events:

- magnetic field ON but NO tracker
- Gaussian smearings of MC tracks according to expected IDEA tracker performance
- for each track, extrapolate impact point
- remove and store tracks not reaching calo



# jet reconstruction → IDEA++ DR-pPFA

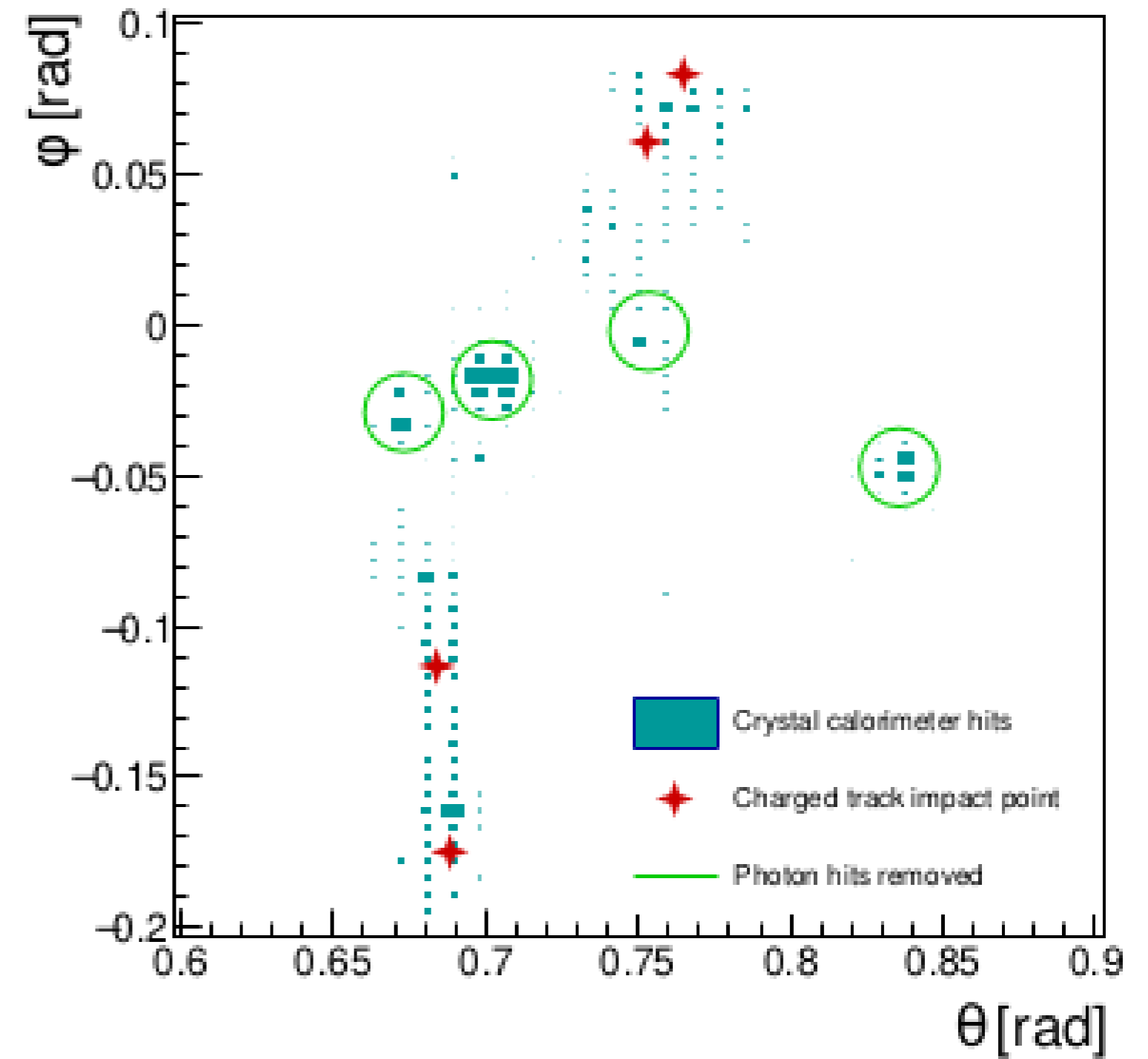
<https://doi.org/10.1088/1748-0221/17/06/P06008>

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- for each track, extrapolate impact point
- remove and store tracks not reaching calo
- identify EM neutral clusters (photons) by cluster radius

$$R_{\text{transverse}} = \frac{E_{\text{seed}}}{\sum_i E_{\text{hit},i} (\Delta R_i < 0.013)}$$

- remove and store photons ( $R < 0.9$ )



# jet reconstruction → IDEA++ DR-pPFA

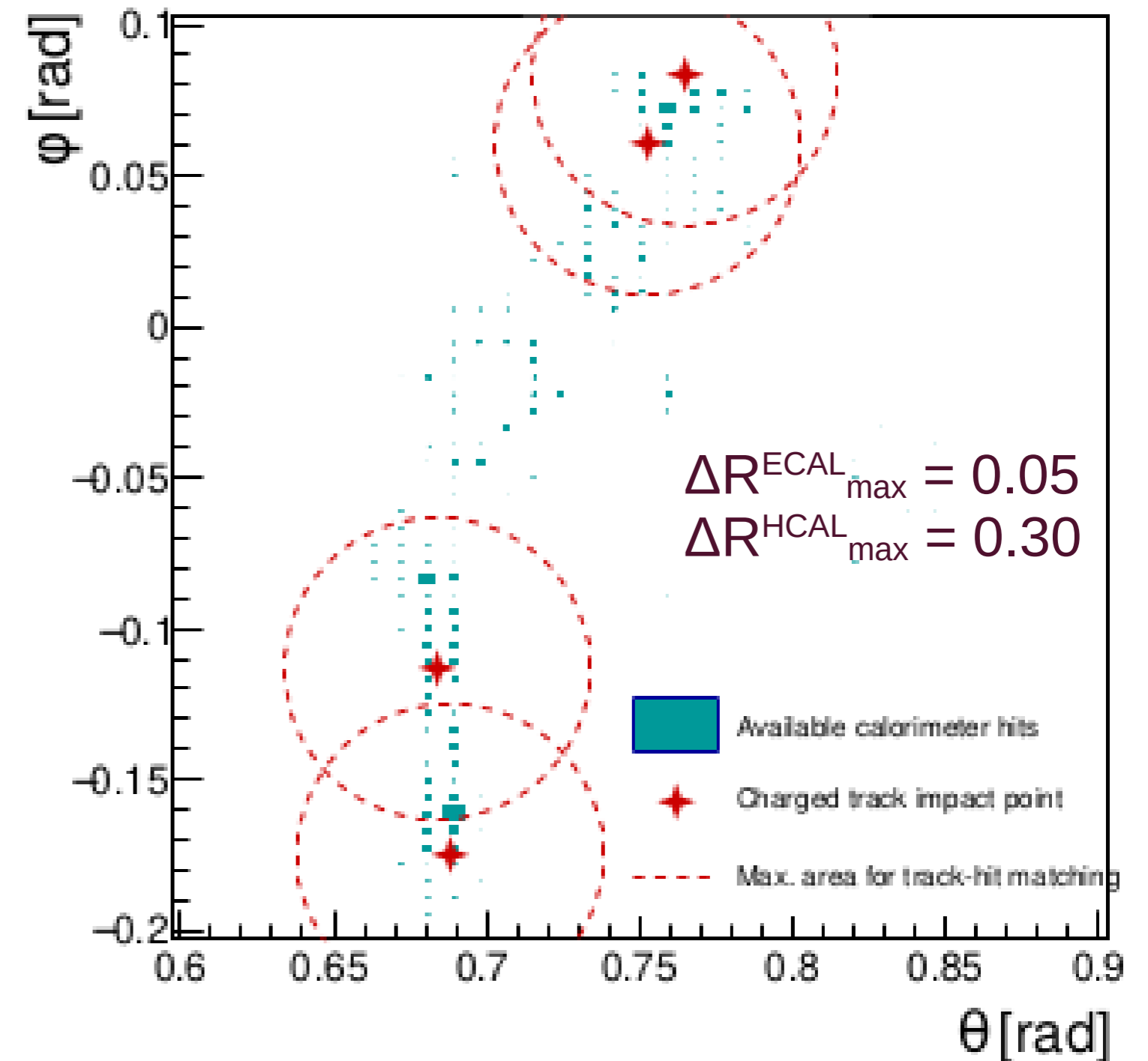
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- for each track, rank calo hits by distance





# jet reconstruction → IDEA++ DR-pPFA

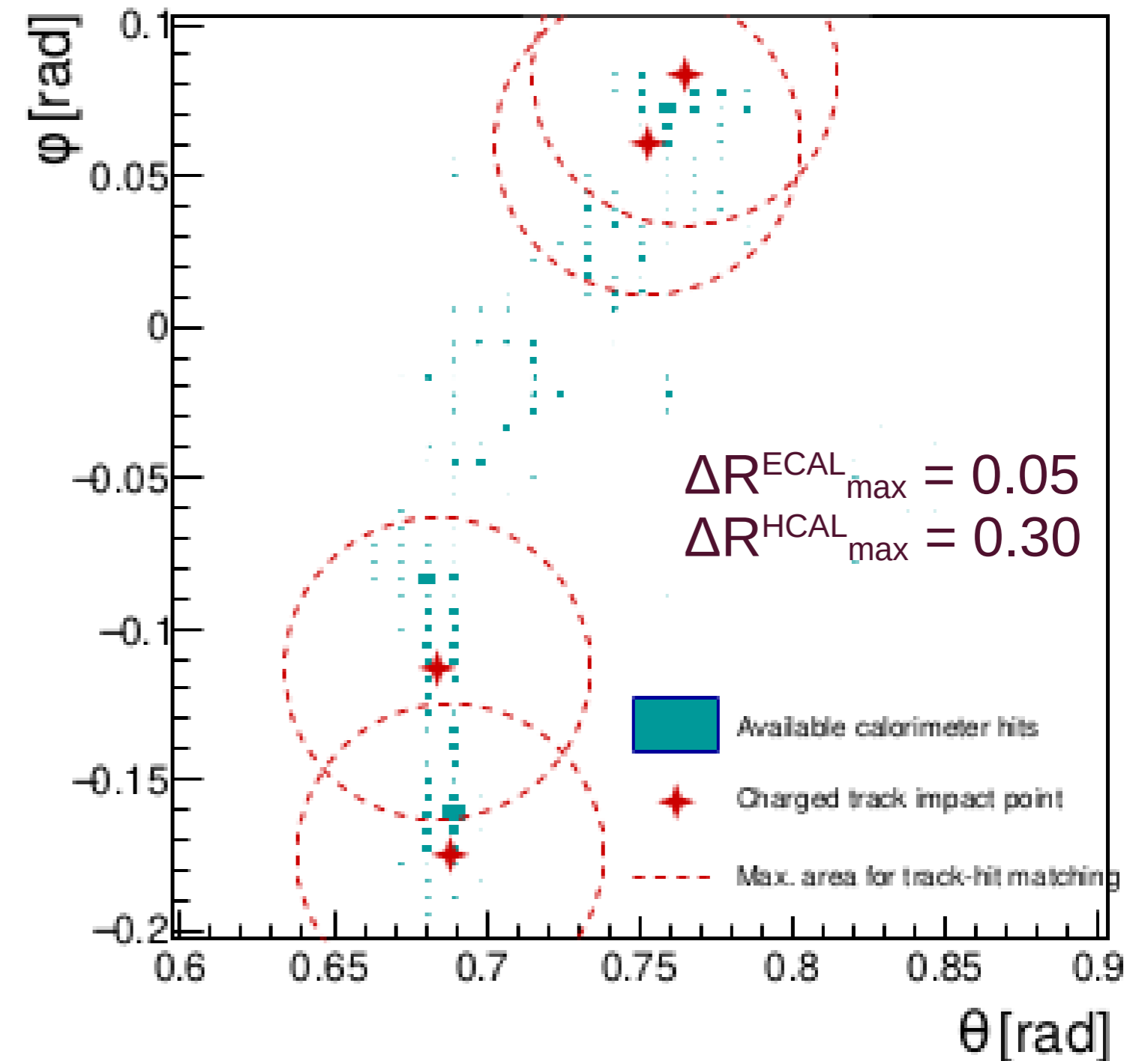
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- for each track, rank calo hits by distance
- collect hits in cone(s)



# jet reconstruction → IDEA++ DR-pPFA

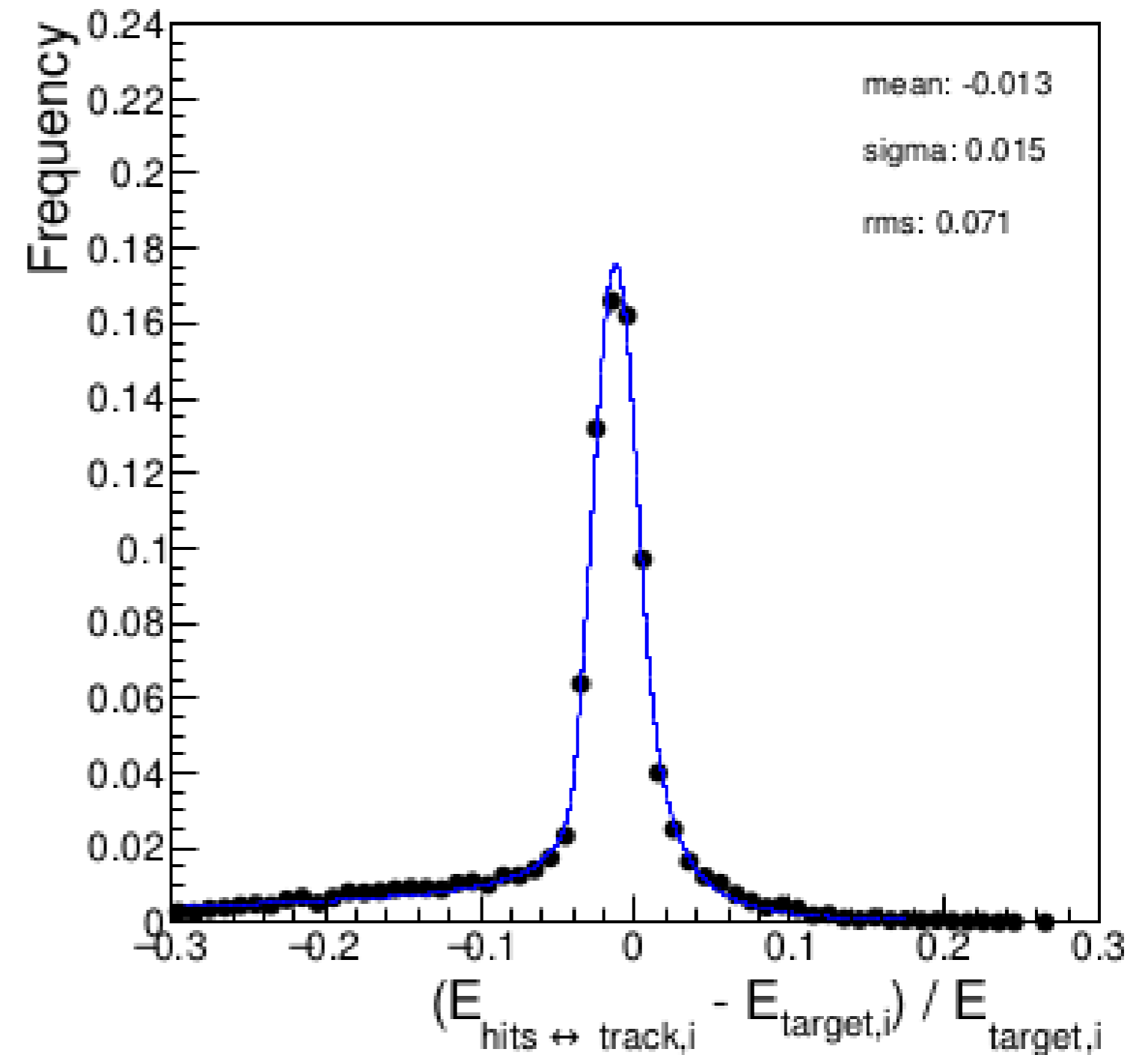
Geant4 simulation of  $Z \rightarrow jj$  events:

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- collect hits in cone(s)
- compare with  $E_{\text{target}}(\text{track})$

<https://doi.org/10.1088/1748-0221/17/06/P06008>



# jet reconstruction → IDEA++ DR-pPFA

Geant4 simulation of  $Z \rightarrow jj$  events:

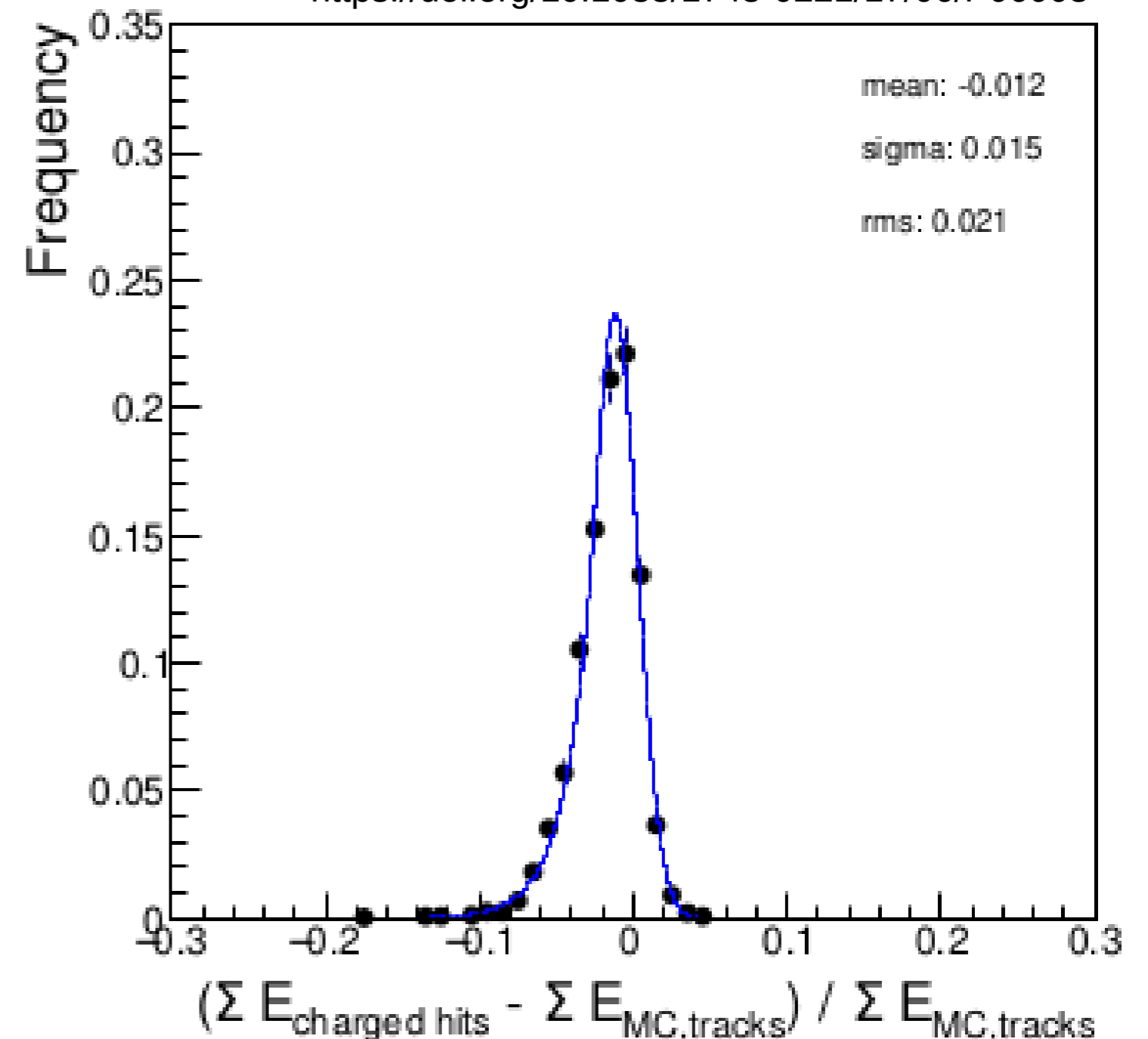
- magnetic field ON but NO tracker
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- identify EM neutral clusters (photons) by cluster radius

$$R_{\text{transverse}} = \frac{E_{\text{seed}}}{\sum_i E_{\text{hit},i} (\Delta R_i < 0.013)}$$

- remove and store photons ( $R < 0.9$ )
- for each track, rank calo hits by distance
- collect hits in cone(s)
- compare with  $E_{\text{target}}(\text{track})$
- if “good” agreement remove hits and replace them with track

*Please note: dual-readout is used to correct energy of clustered calorimeter hits and improve track-hit matching*

<https://doi.org/10.1088/1748-0221/17/06/P06008>



# jet clustering

<https://doi.org/10.1088/1748-0221/17/06/P06008>

- Jet clustering algorithm\* fed with collection of
  - all photon hits
  - tracks of
    - charged particles not reaching calorimeter
    - tracks swapped with calorimeter hits in previous step
  - All other calorimeter hits (both ECAL and HCAL) not been swapped out
- As result, 4-momentum vectors are clustered into two jets
- Jet energy (“non-swapped hadron” component) is corrected with DRO\*\*

$$E_{jet} = C_{PFA} \cdot \left[ \sum E_{hits,\gamma} + \sum E_{tracks} + \sum E_{hits,left\over,DRO} \right]$$

\*FASTJET package: generalized  $k_T$  algorithm with  $R=2\pi$  and number of jets fixed to 2

\*\*dual-readout used here to correct energy of calorimeter hits with no match to tracks (e.g. neutral hadrons)



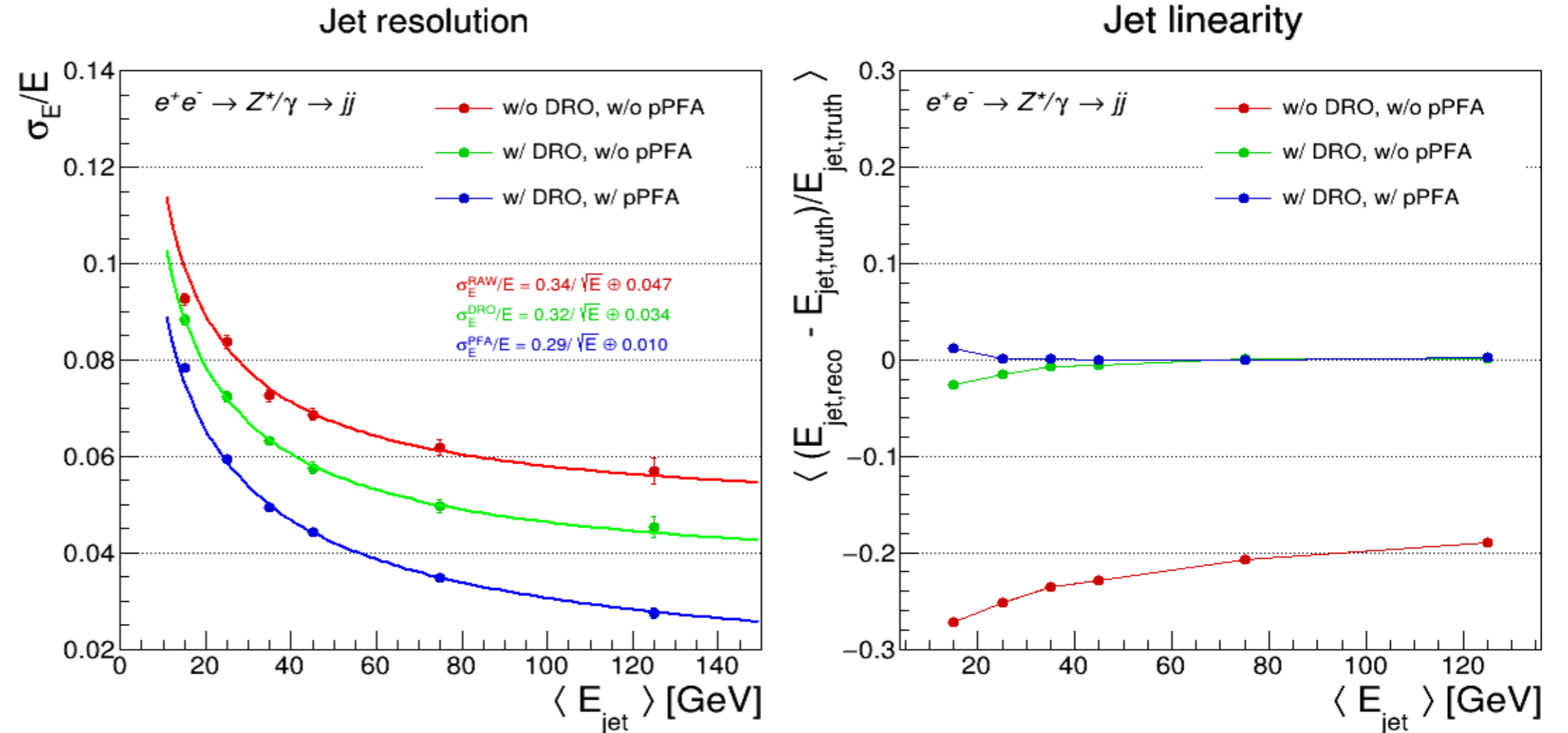
# jet energy resolution w/ and w/o DR-pPFA

<https://doi.org/10.1088/1748-0221/17/06/P06008>

Resolution and linearity as a function of jet energy in off-shell  $e^+e^- \rightarrow Z^* \rightarrow jj$  events (at different centre-of-mass energies):

*More details in: 2022 JINST 17 P06008*

- crystals + IDEEA w/o DRO
- crystals + IDEEA w/ DRO
- crystals + IDEEA w/ DRO + pPFA

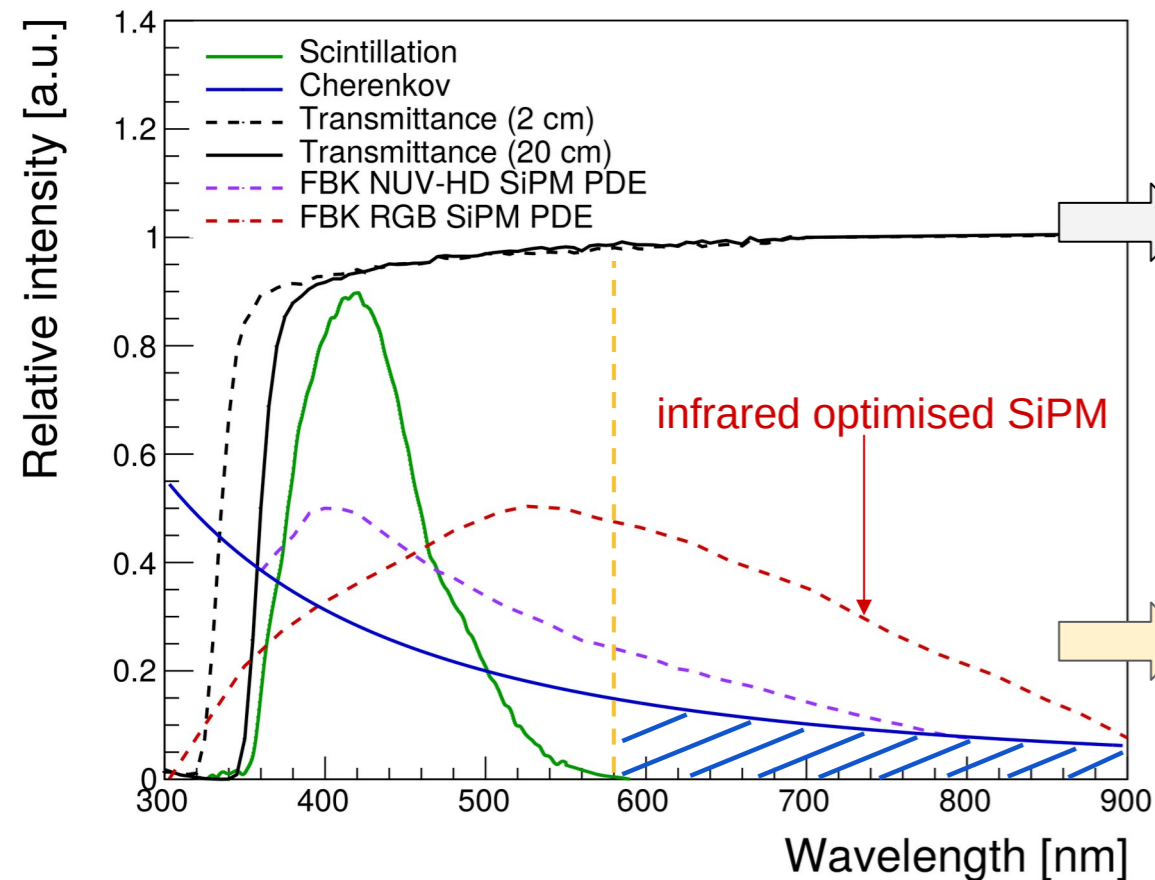


**Sensible improvement in jet energy resolution using dual-readout information combined with PF approach → 3-4% for energies above 50 GeV**

# dual-readout challenge w/ crystals

- Light yield and purity of S and C signals - likely - key discriminant between crystal options
- Different strategies exploitable for different scintillators

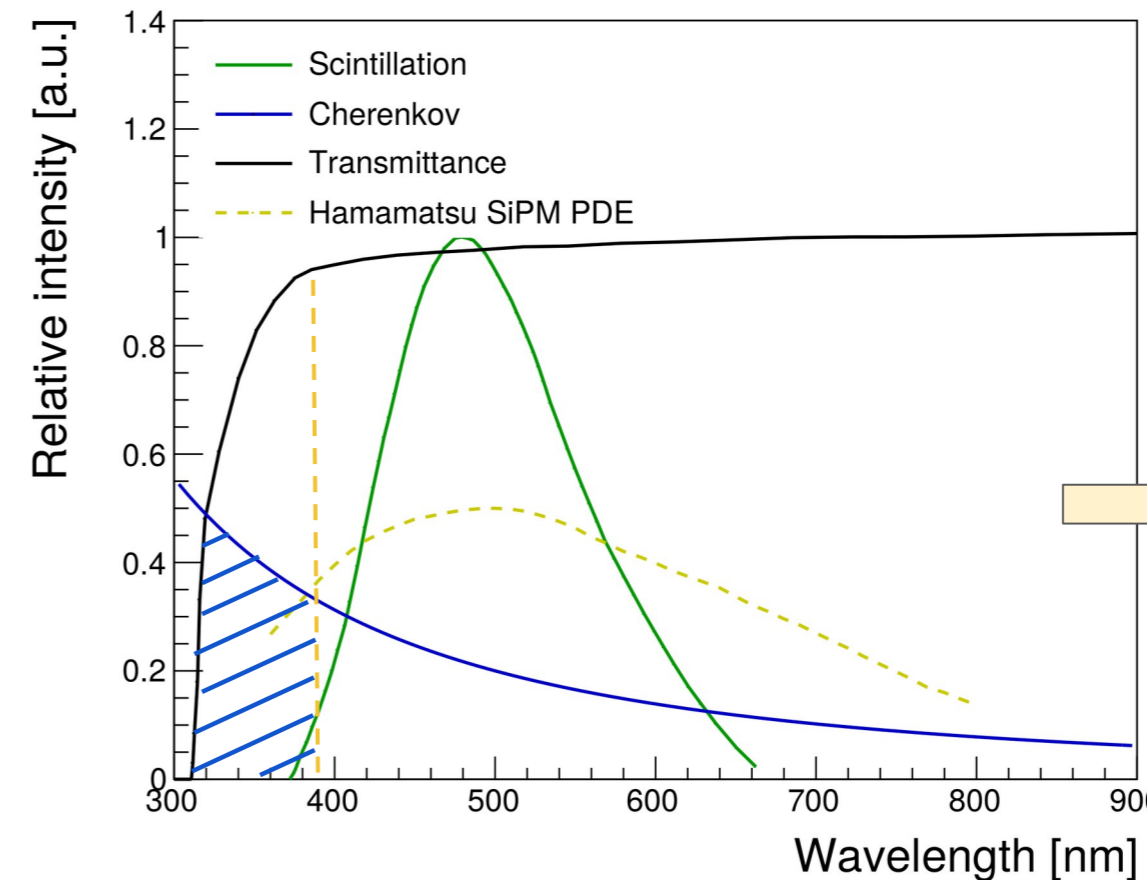
## PWO



Estimated:  
>2000 pe/GeV for  
scintillation photons  
>100 pe/GeV for  
Cherenkov photons

Cherenkov photons  
above scintillation peak  
much less affected by  
self-absorption

## BGO / BSO



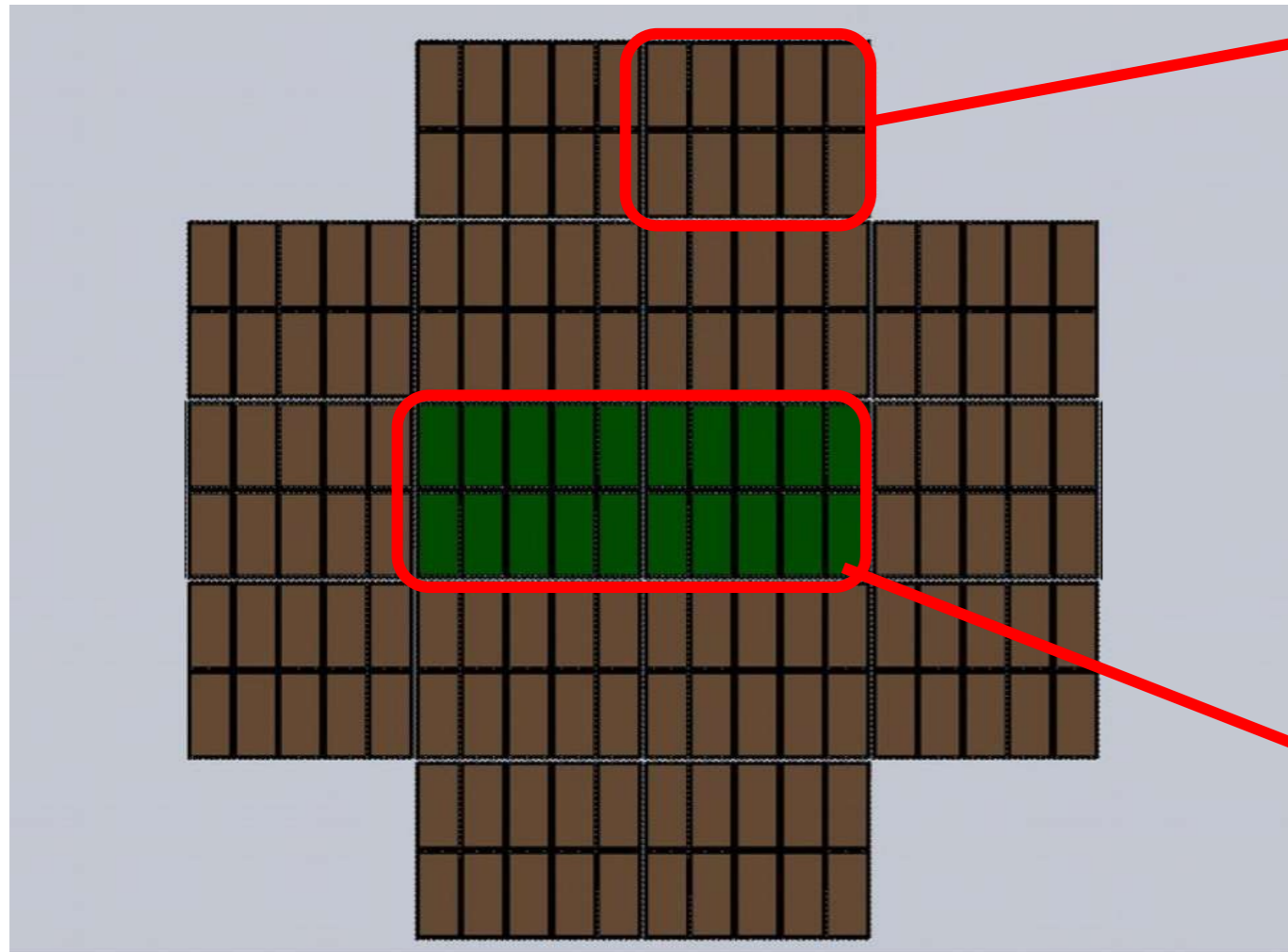
Larger Stokes shift, i.e.  
wider range of  
transparency for  
'Cherenkov UV'  
photons

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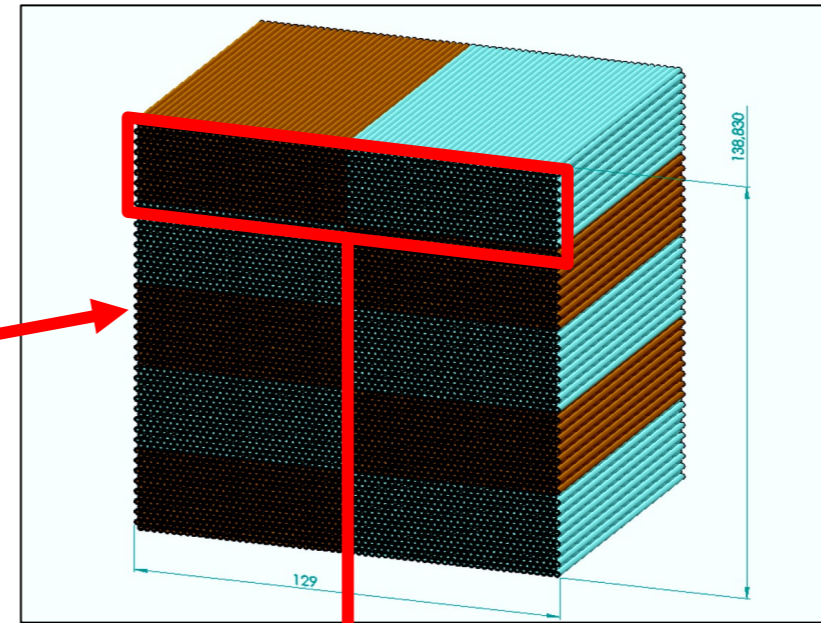
# Hadronic-containment prototype

# HiDRa – Highly granular Dual Readout demonstrator

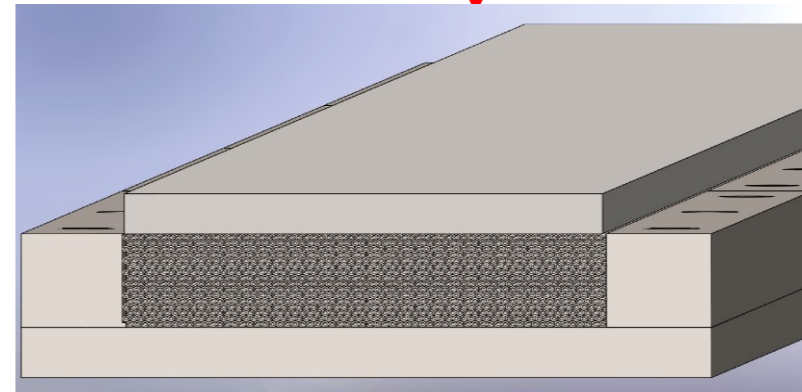
Hadronic-size prototype:  
16 modules w/ highly granular core



~ 65 × 65 × 250 cm<sup>3</sup>



1 Module: 5 MMs  
~ 13 × 13 cm<sup>2</sup>  
5120 fibres



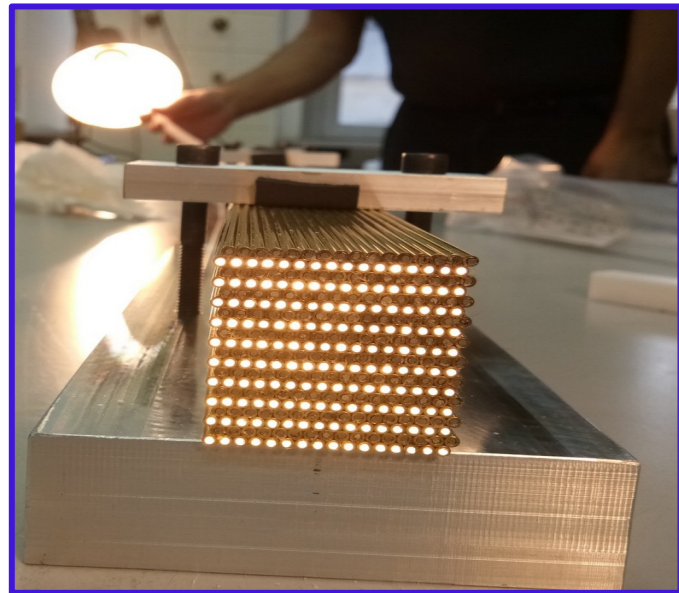
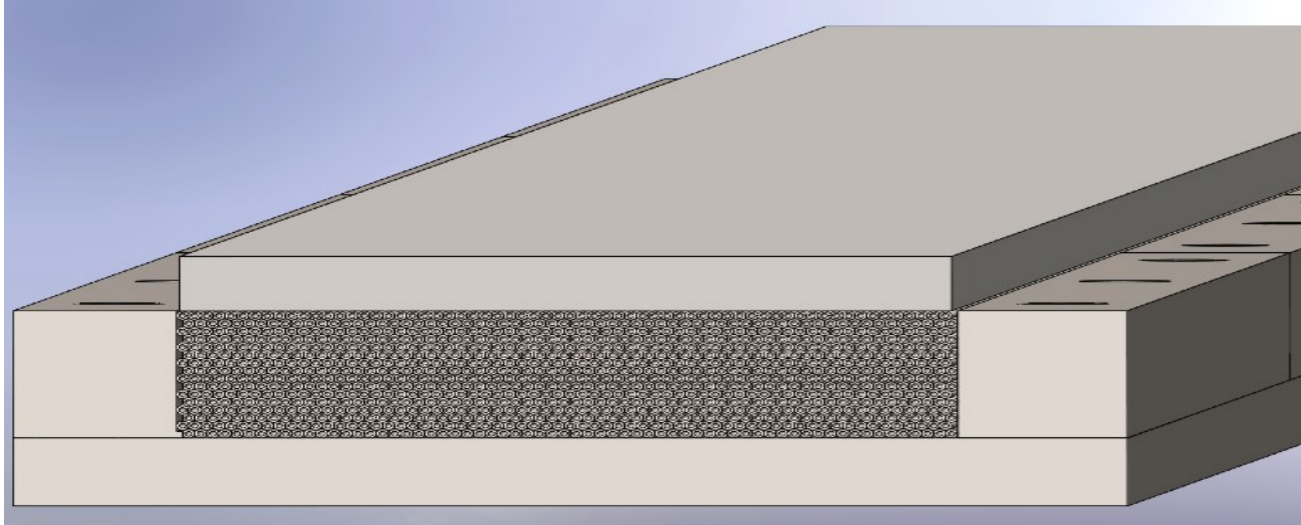
1 MiniModule:  
64 × 16 = 1024 fibres in total  
512 S + 512 C

highly granular core:  
10240 fibres to be read out with SiPMs

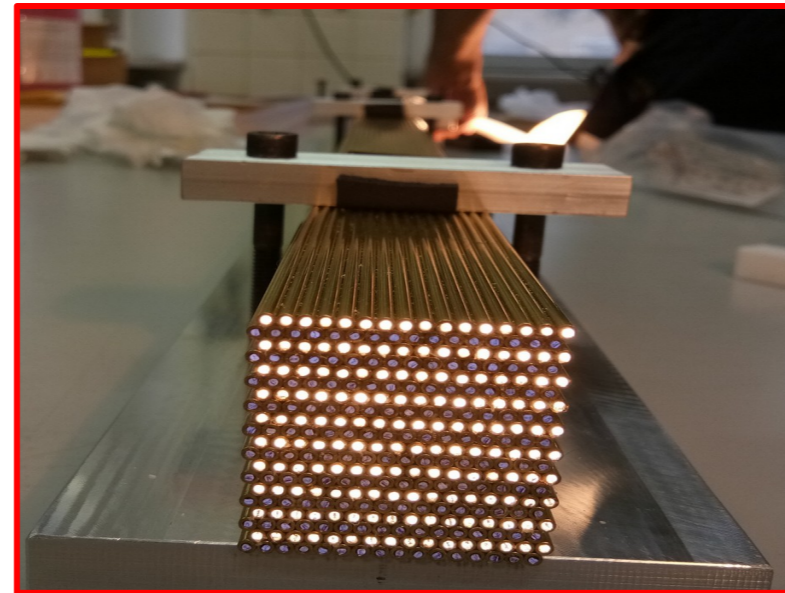


# Work in progress

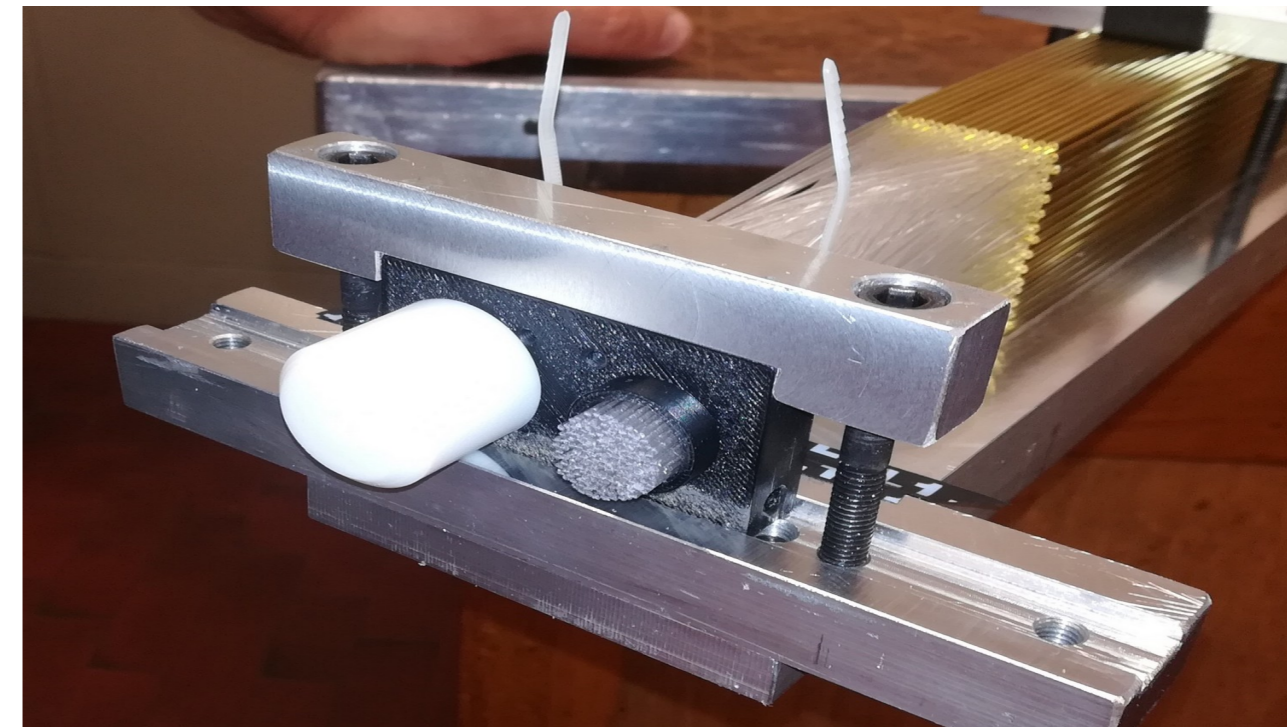
- Stainless steel capillary tubes w/ 2 mm diameter
- C and S fibres positioned per row
- Fibre separation at calorimeter rear end
- Fibre grouping for PMT coupling



scintillating fibres



Cherenkov fibres



Fibre disposal and grouping (pictures from 2020 brass prototype)

# SiPMs for HiDRa

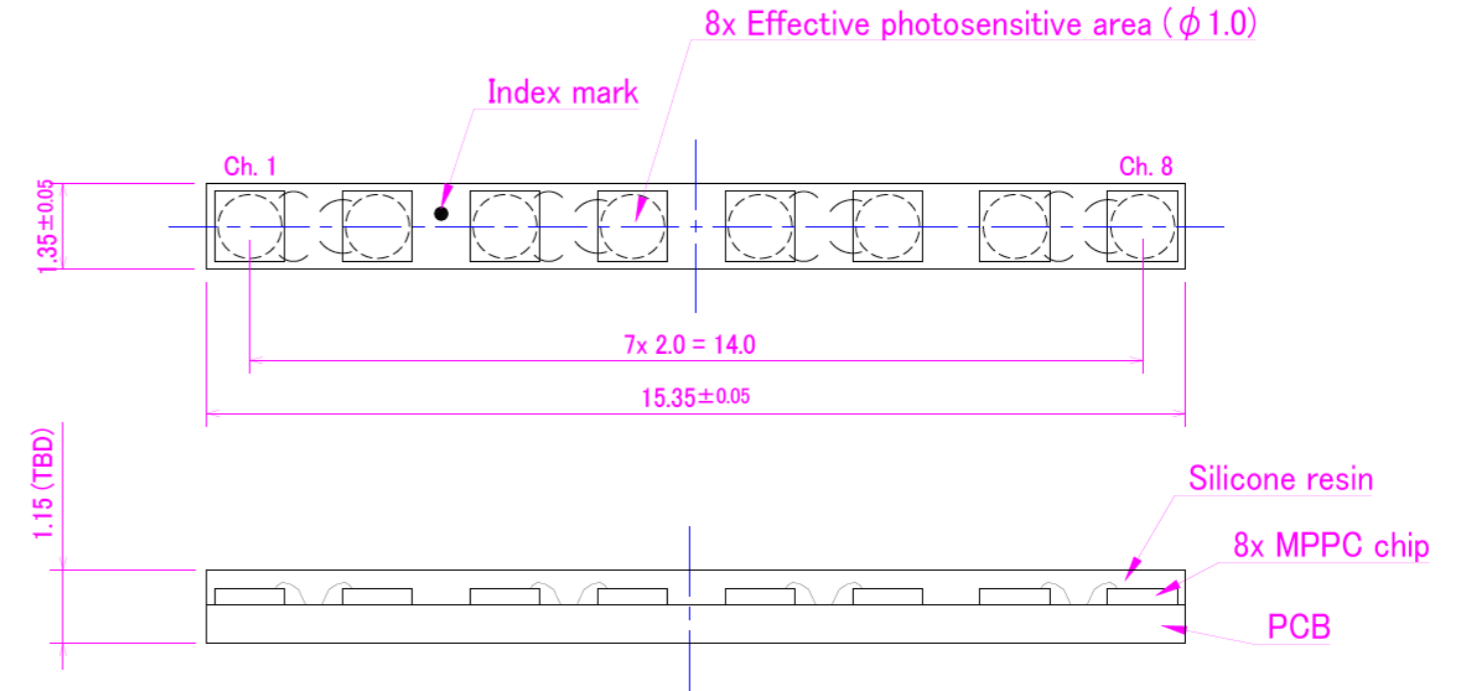
New solution by Hamamatsu:

boards with 8 “in-line” SiPMs

dimension  $1 \times 1 \text{ mm}^2$

10 or 15  $\mu\text{m}$  cell size

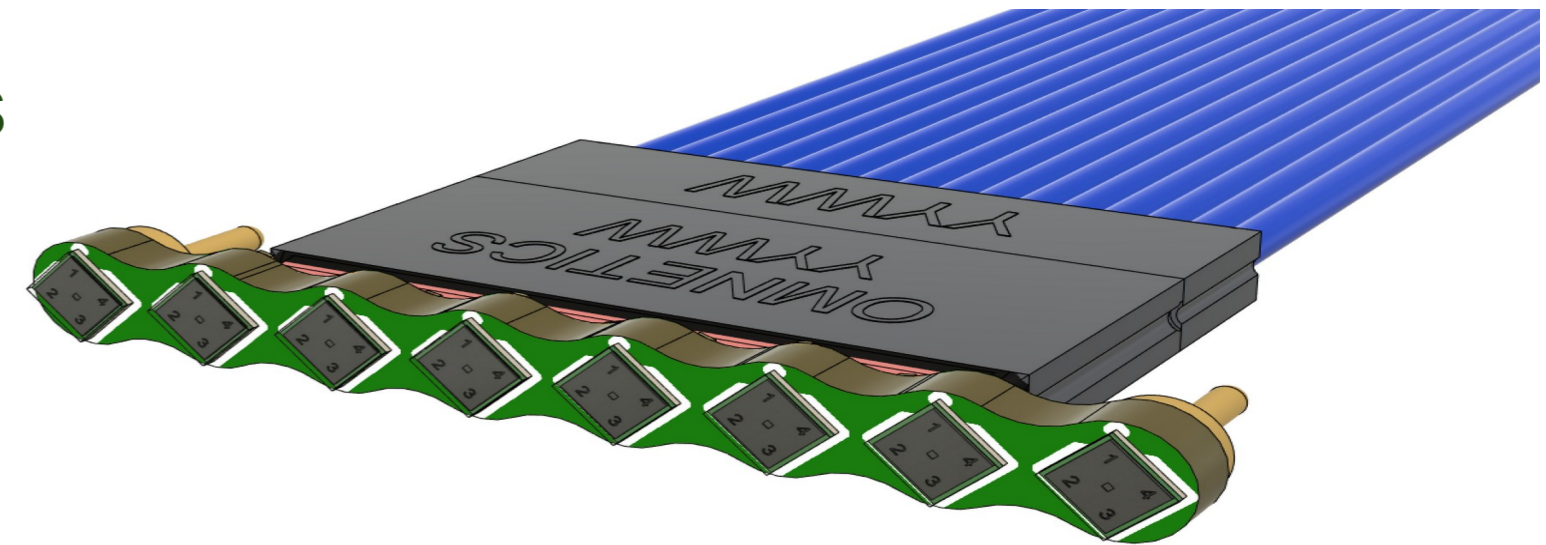
SiPMs selected such that  $\Delta V_{\text{bd}} < 100 \text{ mV}$



Our present best fit:

a) use 10  $\mu\text{m}$  cell-size SiPMs for scintillating fibres

b) use 15  $\mu\text{m}$  cell-size SiPMs for clear fibres

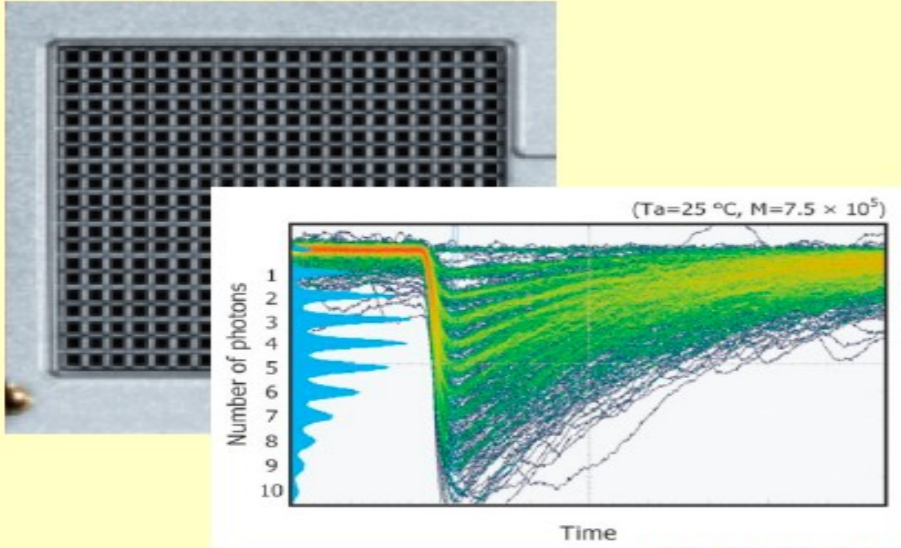


Testing 10 boards per cell-size type



# Alternative photosensors

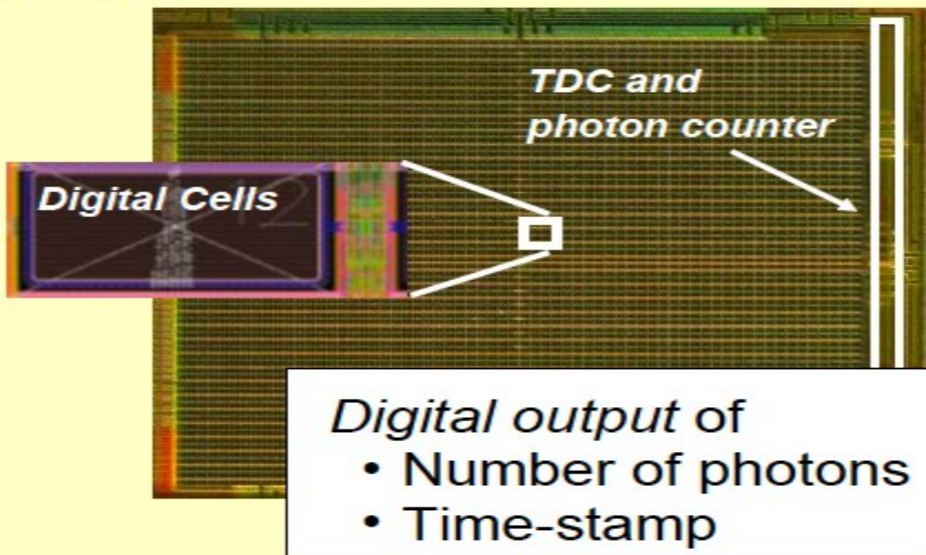
## Analog SiPM



The image shows a physical Analog SiPM sensor on the left, which is a square chip with a grid of small diodes. On the right is a graph showing the signal output. The y-axis is labeled 'Number of photons' and ranges from 1 to 10. The x-axis is labeled 'Time'. The graph shows a series of pulses that increase in amplitude over time, indicating the detection of multiple photons. The conditions for the measurement are given as  $(T_a=25\text{ }^\circ\text{C}, M=7.5 \times 10^5)$ . The source is cited as [www.hamamatsu.com](http://www.hamamatsu.com).

- Cells connected to common readout
- Analog sum of charge pulses
- Analog output signal

## Digital SiPM



The image shows a physical Digital SiPM sensor on the left, which is a square chip with a grid of small diodes. On the right is a graph showing the digital output. The y-axis is labeled 'Number of photons' and ranges from 1 to 10. The x-axis is labeled 'Time'. The graph shows a series of pulses that increase in amplitude over time, indicating the detection of multiple photons. The conditions for the measurement are given as  $(T_a=25\text{ }^\circ\text{C}, M=7.5 \times 10^5)$ . The source is cited as [www.hamamatsu.com](http://www.hamamatsu.com).

*Digital Cells*

*TDC and photon counter*

*Digital output of*

- Number of photons
- Time-stamp

- Each diode is a digital switch
- Digital sum of detected photons
- Digital data output

**digital SiPMs (dSiPMs)**

**no need for analogue-signal post-processing**

- SPAD array in CMOS:
  - complex functions embedded in single substrate (e.g. SPAD masking, counting, TDCs)
  - front-end electronics optimised to preserve signal integrity ( $\rightarrow$  timing)
  - simplified assembly of large area detectors
  - R&D costs relatively low for design over standard process

# Conclusions

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Growing interest for dual-readout calorimetry

(other activities ongoing on dual- and also triple-readout calorimeters)

IDEA fibre calorimeter: dual-readout + single-fibre light sensors (SiPM) + timing

→ highly granular 3D information

Dual-readout crystal option → may boost em performance without spoiling hadronic one

Highly granular 3D information

→ powerful input for deep-learning algorithms and/or PFA

→ highly performing final-state identification capabilities

Many R&D activities ongoing exploiting all directions → including different readout options (both charge-integrator and waveform sampling ASICs)

Hadronic-scale demonstrators under construction



# Targets

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Demonstrate (assess) physics performance for both single hadrons and jets (and electrons)

Validate Geant4 shower modeling

Assess scalable solutions concerning construction and signal readout/handling

Exploit DNN architectures for physics analysis

Assess performance in relevant benchmark physics channels

→ **Fully exploit dual-readout potential for physics programme at FCC-ee**

# Further lectures

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R.L. Workman et al. (Particle Data Group), Prog. Theor. Exp. Phys. 2022, 083C01 (2022)

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