Flavor in the SMEFT and EW precision observables
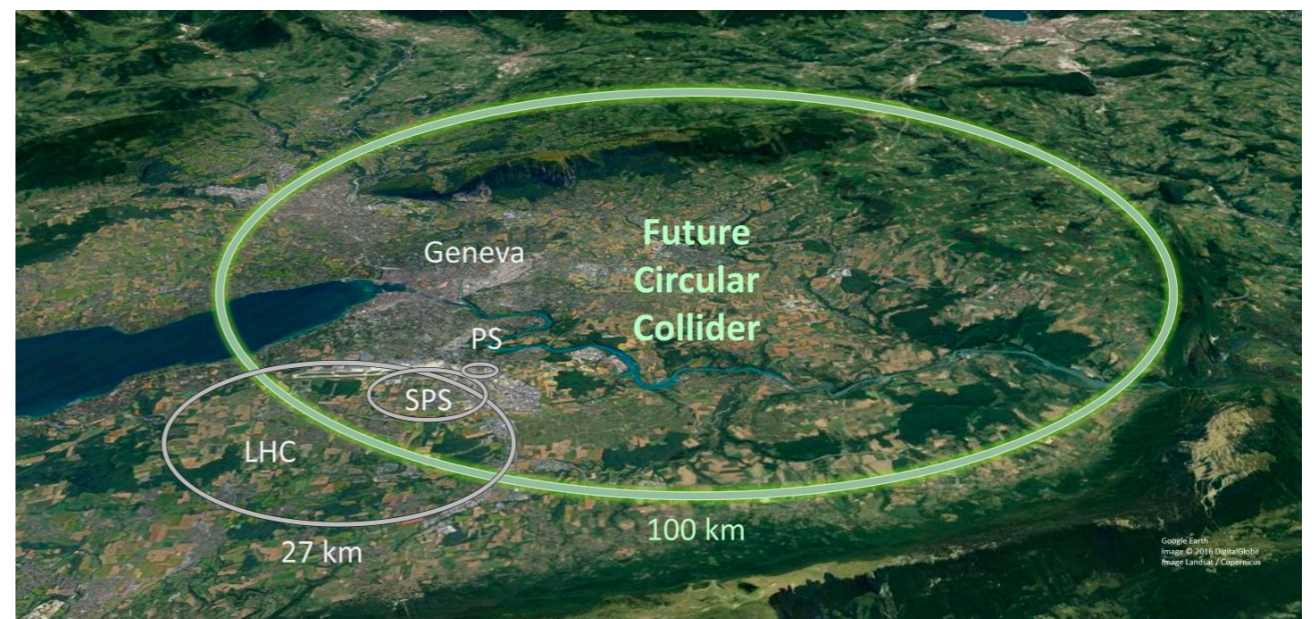
Ben A. Stefanek

GENT Fellow, IFIC Valencia
Flavor and Origin of Matter Group
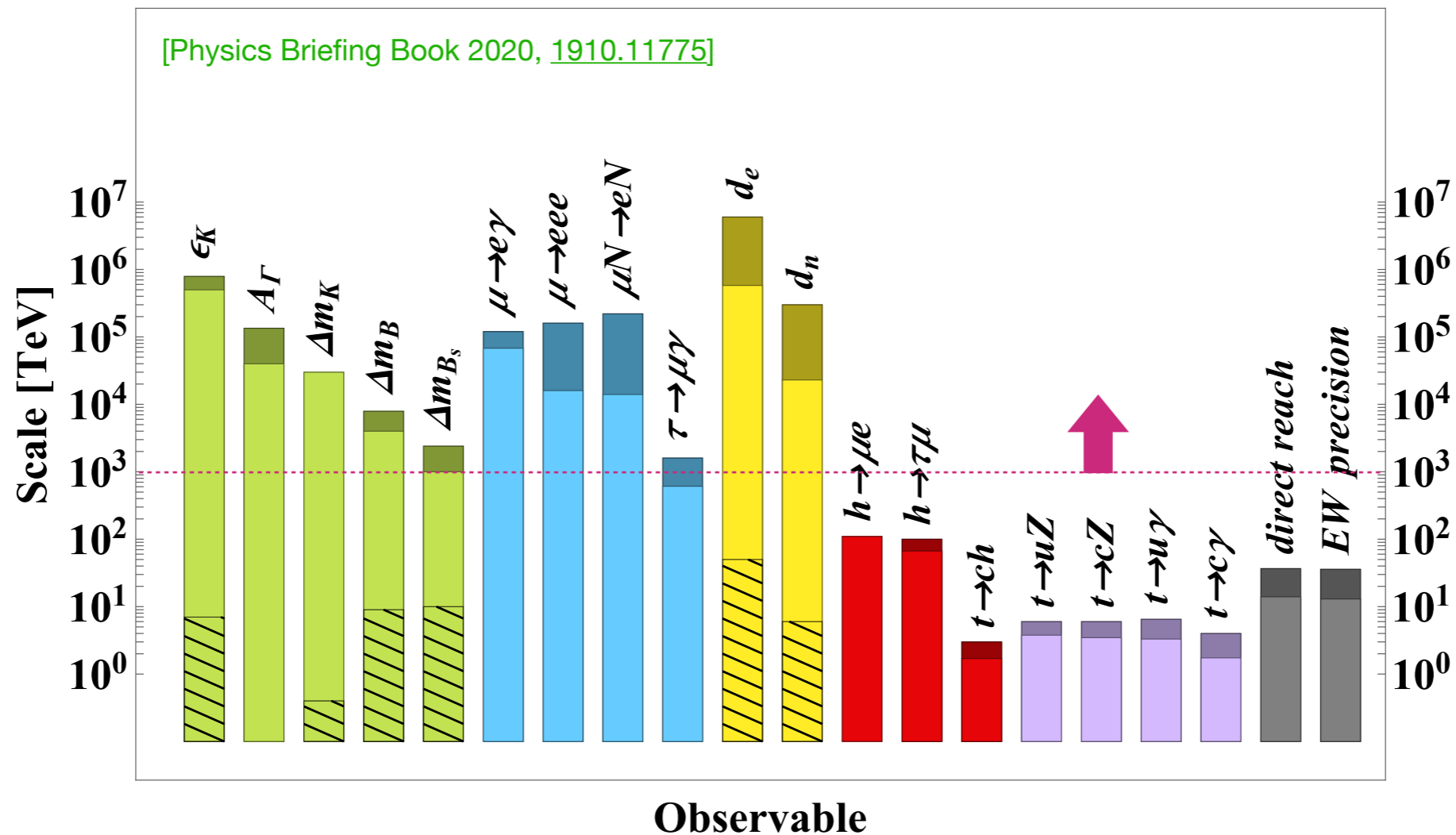
LHCb Implications 2024
October 25th, 2024

[Based on: BAS, 2407.09593,
Allwicher, Cornella, Isidori, BAS, 2311.00020
Allwicher, Isidori, Lizana, Selimovic, BAS, 2302.11584]

What do we know about the structure of new physics?

[Physics Briefing Book 2020, 1910.11775]

- No clear deviations in **flavor data** that test the accidental symmetries of the SM. What does this tell us about the flavor structure of NP? There are two limiting cases:

  1. NP is very heavy, well above 1000 TeV. Then it's fine if the accidental symmetries of the SM are badly broken by NP.

  2. NP is close to the TeV scale. The accidental symmetries of the SM must also be very good symmetries of the NP.
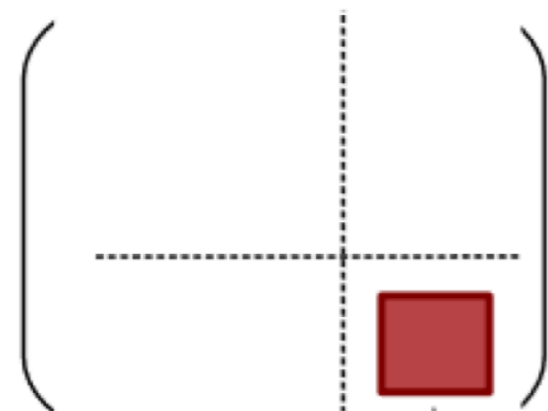
What do we know about the structure of new physics?

[Physics Briefing Book 2020, 1910.11775]
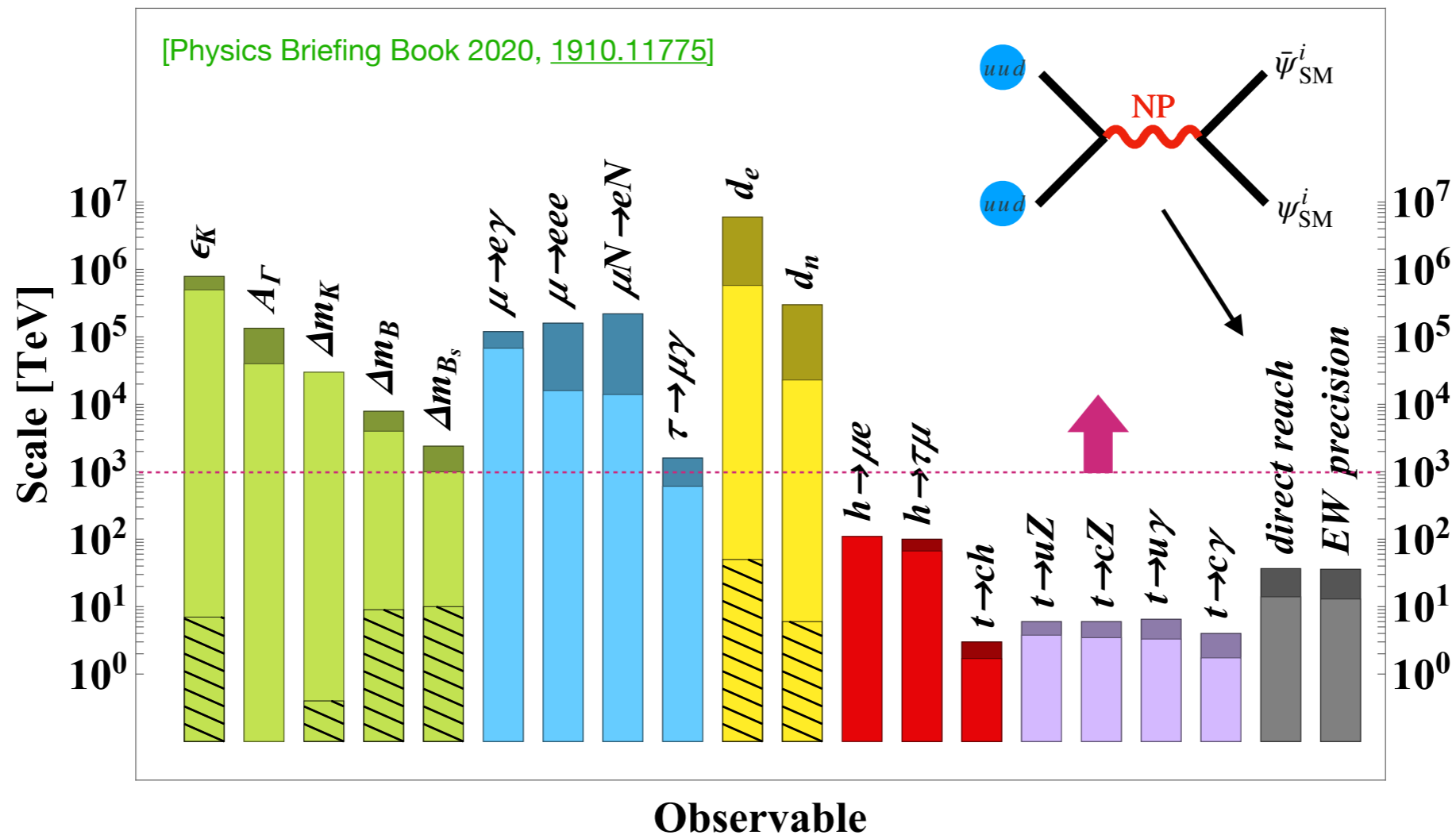
- No deviations in **flavor data** that test the accidental symmetries of the SM. Perhaps NP is very heavy, but there cannot be any large breaking of $U(2)^n$ at nearby energy scales.

- Similarly, **direct searches at the LHC** tell us that NP does not couple strongly to valence quarks at nearby energy scales.

- Interestingly, these two hints point toward a coherent hypothesis for the structure of NP.

The hypothesis of (dominantly) third-family NP

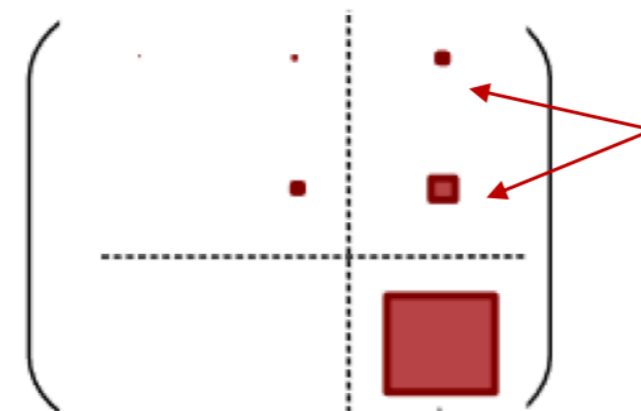- New physics is **NOT** flavor universal- there could be new flavor non-universal interactions as low as the TeV scale coupled dominantly to the third family. NP coupled to Higgs & top is what we need to address the EW hierarchy problem.

- These new interactions see flavor just like the SM Higgs. They could be connected to a low scale solution to the SM flavor puzzle. (see e.g. Davighi and BAS, arXiv: 2305.16280)

- NP dominantly coupled to the third family is described by an approximate $U(2)^n$ flavor symmetry, just like the SM Yukawa couplings.

$U(2)$-breaking effects
Barbieri et al, 1105.2296
Isidori, Straub, 1202.0464
Fuentes-Martin et al, 1909.02519

Exact $U(2)$ limit   Observed Yukawa

NP coupled only to 3rd family   Also small couplings to light families

[R. Barbieri, G. Isidori, J. Jones-Perez, P. Lodone, D. Straub, 1105.2296]   **4**

Hints of 3rd-family NP: Lessons from B-anomalies

High-p_T

Flavor (*B* physics)

$bb \to \tau\tau$
(PDF supp.)

q_L^3 l_L^3

q_L^3 l_L^3

$\sim V_{ts}$

$U(2)_q$

q_L^3 l_L^3

q_L^2 l_L^3
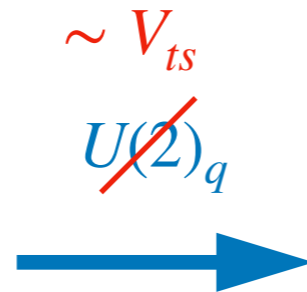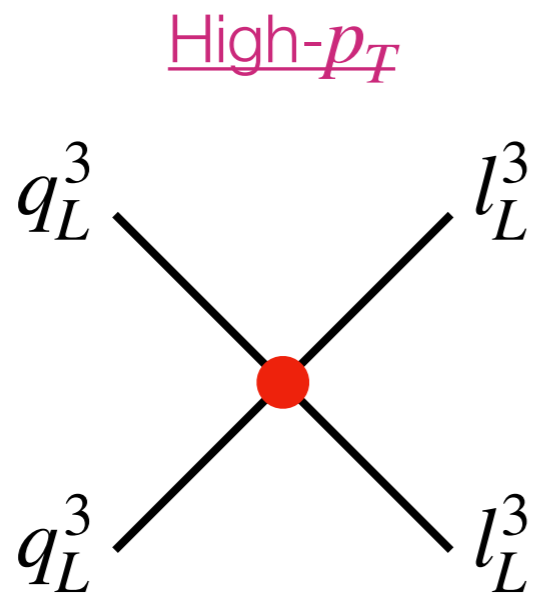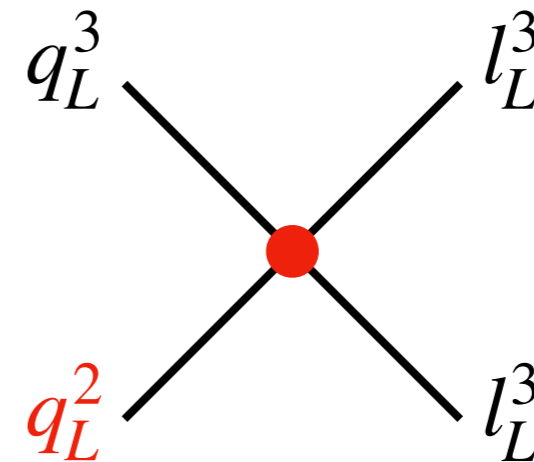
$bsll$
$bs\nu\nu$
$bc\tau\nu$

Hints of 3rd-family NP: Lessons from B-anomalies

High-p_T

Flavor (B physics)

q_L^3 l_L^3

$bb \to \tau\tau$
(PDF supp.)

q_L^3 l_L^3

$\sim V_{ts}$

$\cancel{U(2)_q}$

q_L^3 l_L^3

q_L^2 l_L^3

$bsll$
$bs\nu\nu$
$bc\tau\nu$

$\dfrac{y_t^2}{16\pi^2}$

H ---- y_t l_L^3

H ---- y_t l_L^3

Electroweak precision data

$$(H^\dagger D_\mu^I H)(\bar{l}_L^3 \gamma^\mu \tau^I l_L^3)$$

Modifies $Z\tau\tau, Z\nu\nu, W\tau\nu$ couplings!

"On the Importance of Electroweak Corrections for B Anomalies"
[Feruglio, Paradisi, Pattori, 1705.00929]

6
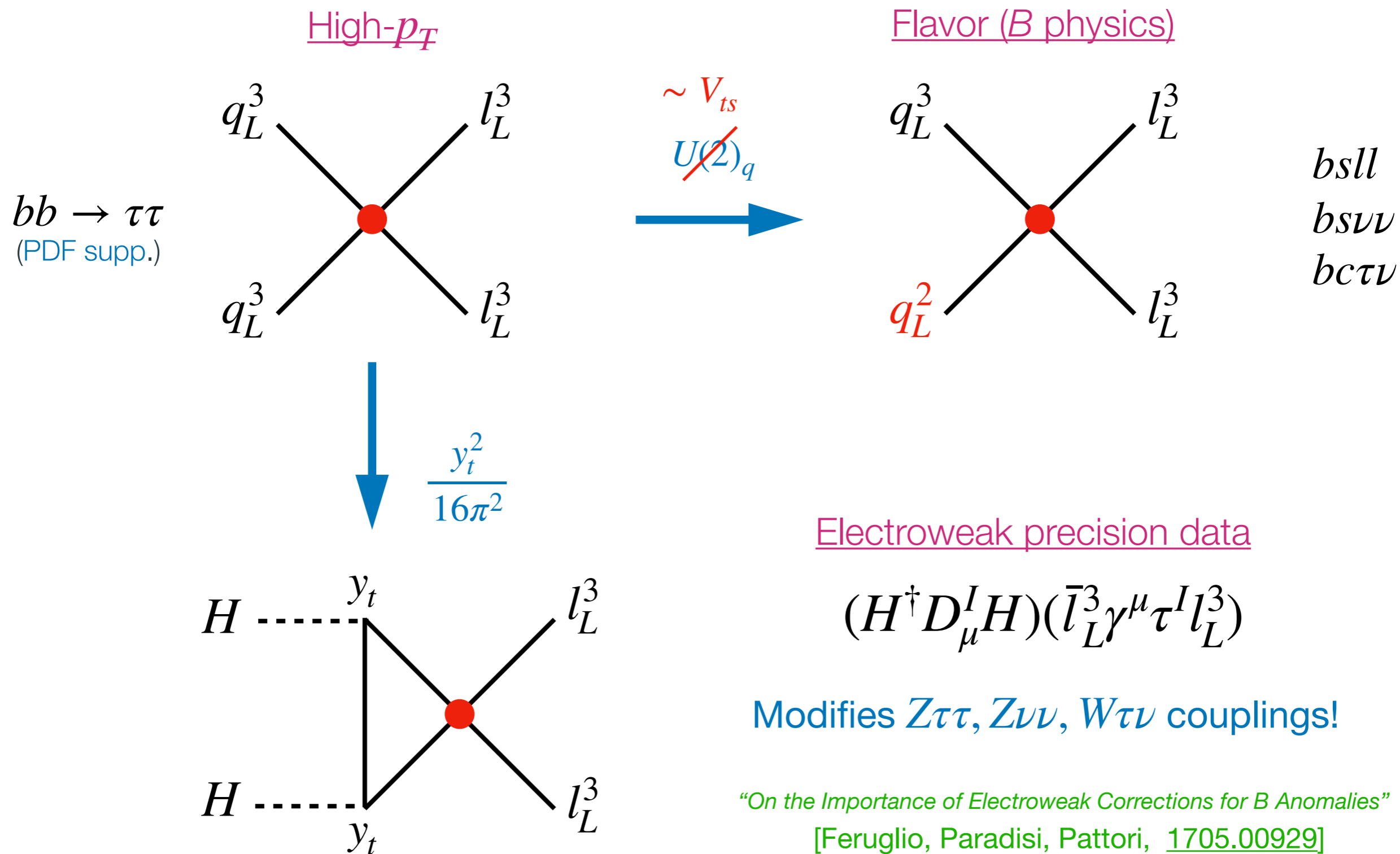
Combining data: NP must confront a triad of bounds

New physics

Flavor conserving

Flavor violating

EW Precision

Direct searches

Flavor Bounds

$U(2)$ can help
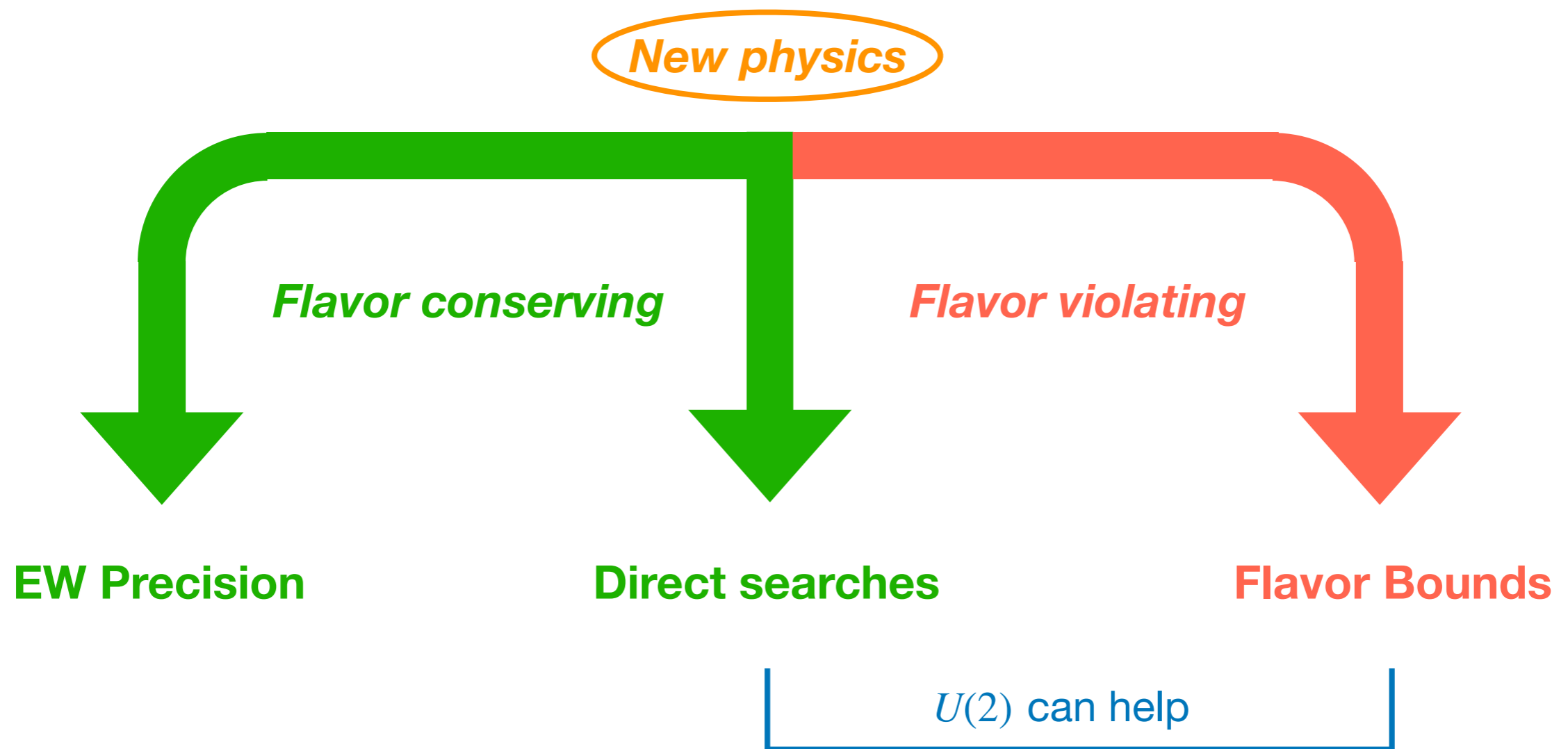
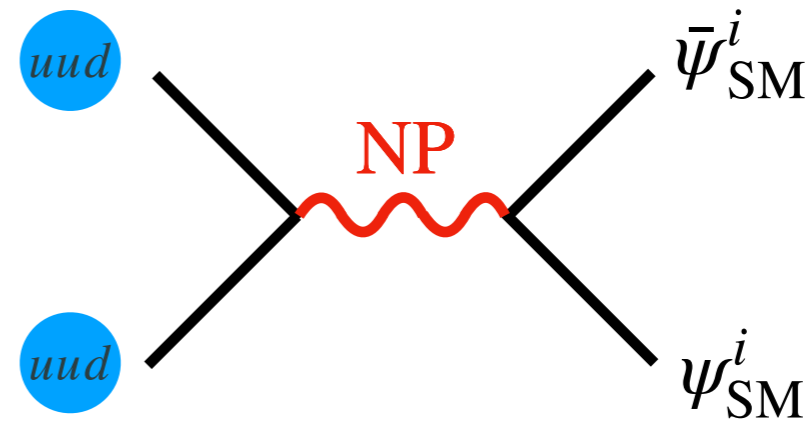- U(2) helps pass flavor + collider bounds, but is less effective against EWPT.

*A future EW precision machine is ideal to test the U(2) hypothesis!*

Tera-Z: Flavor-blind probes of flavor

- Searches at the LHC have the benefit of potentially *directly* producing NP states, but also an inherent flavor asymmetry in the production:

LHC: Strong bounds on flavor universal NP O(10 TeV), but NP coupled to the third family is much less constrained O(1 TeV).

- With a "tera-Z" program at FCC-ee, we can exploit the flavor blindness of the SM gauge interactions to *indirectly* probe NP coupled to any generation!

$10^{12} \, Z's$

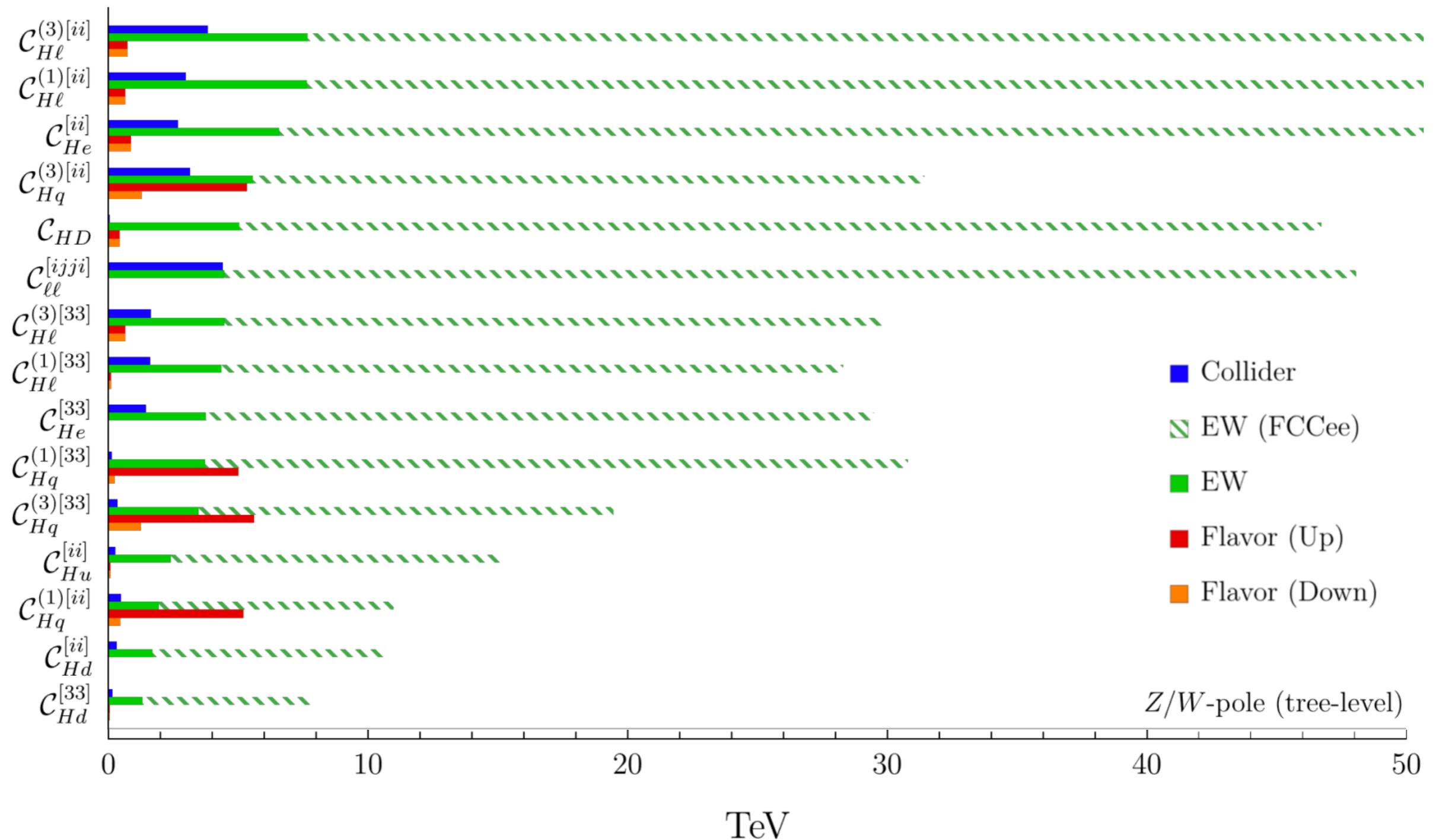$(H^\dagger D_\mu H)(\bar{\psi}^i_{\mathrm{SM}} \gamma^\mu \psi^i_{\mathrm{SM}})$
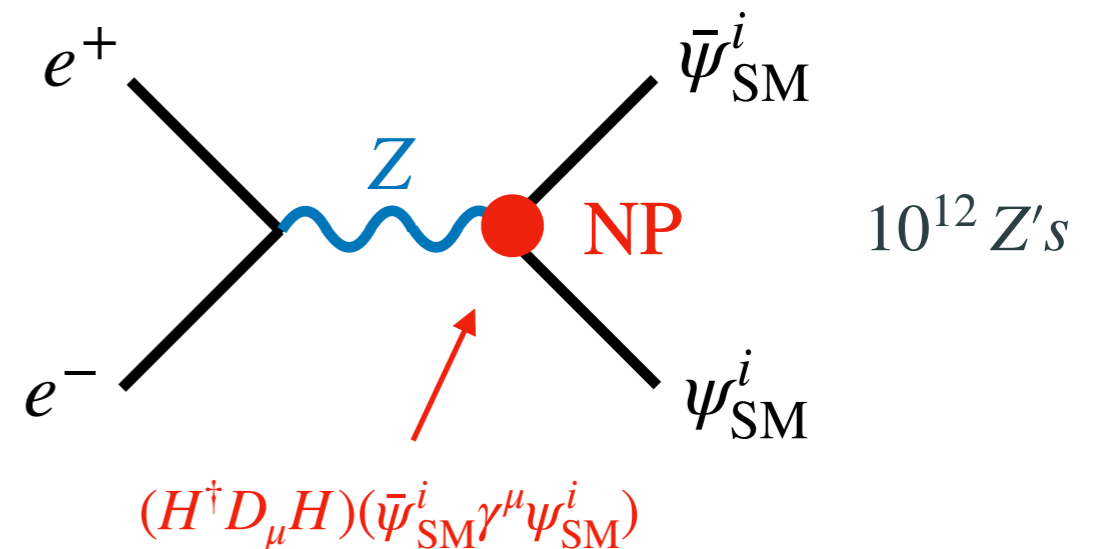
Tera-Z: Almost flavor democratic bounds. Non-universal NP scenarios such as 3rd family NP $(U(2)^n)$ will be extremely well probed.

Tera-Z @ leading order

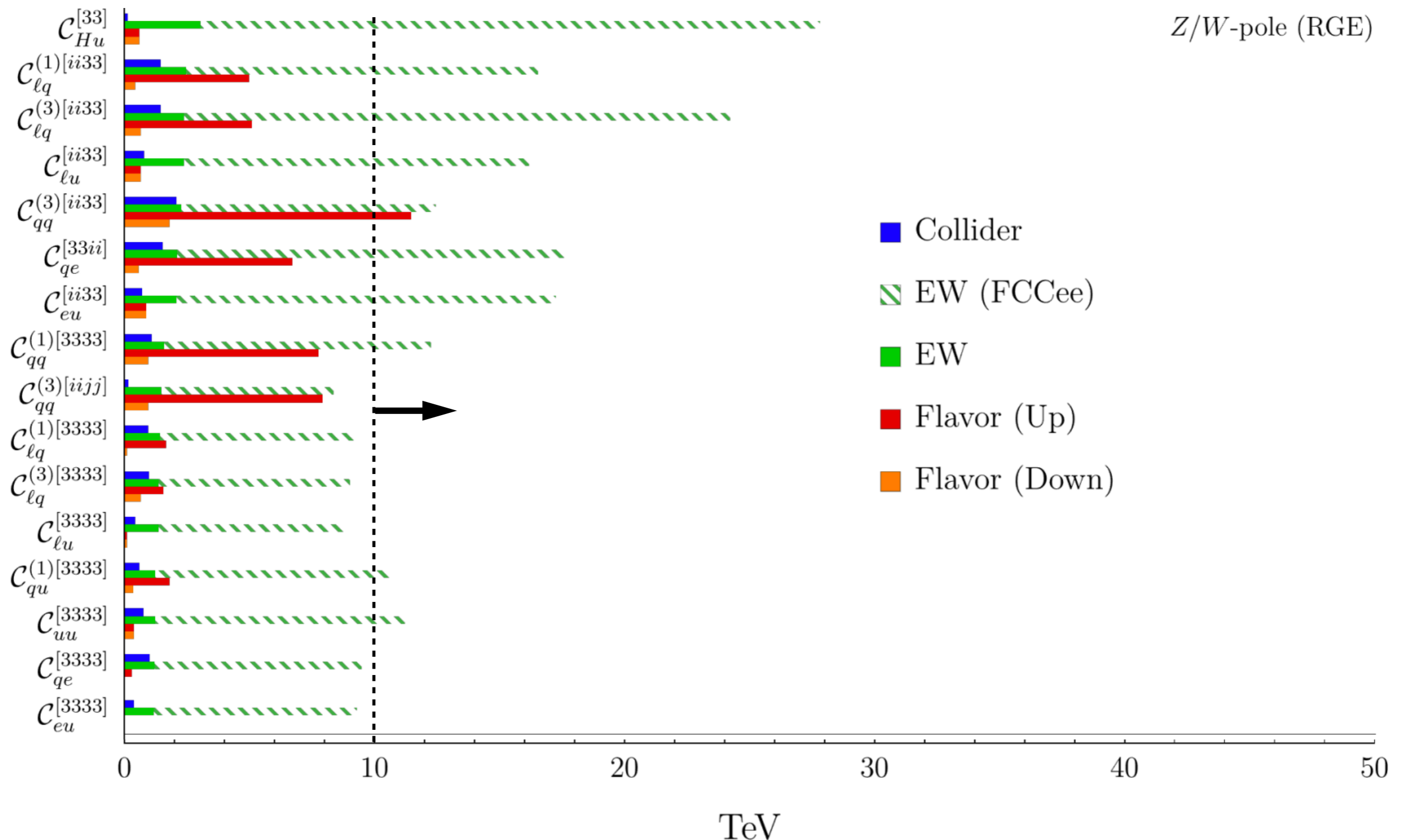[Allwicher, Cornella, Isidori, BAS, 2311.00020]

● Here are the Wilson coefficients entering the Z-pole at LO in the $U(2)^5$ limit.

Tera-Z beyond leading order

[Allwicher, Cornella, Isidori, BAS, 2311.00020]

- At NLO, gain sensitivity to hundreds more operators, in some cases O(10 TeV):

[Allwicher, Cornella, Isidori, BAS, 2311.00020]

- At NLO, gain sensitivity to hundreds more operators, in some cases O(10 TeV):

$$[C_{Hl}^{(1,3)}]_{33}$$

$$[C_{lq}^{(1,3)}]_{3333}$$

Large RG effects due to y_t :

$$[C_{Hl}^{(1,3)}]_{33} \propto \frac{N_c y_t^2}{16\pi^2} [C_{lq}^{(1,3)}]_{3333} \log\left(\frac{m_Z^2}{\Lambda_{NP}^2}\right)$$
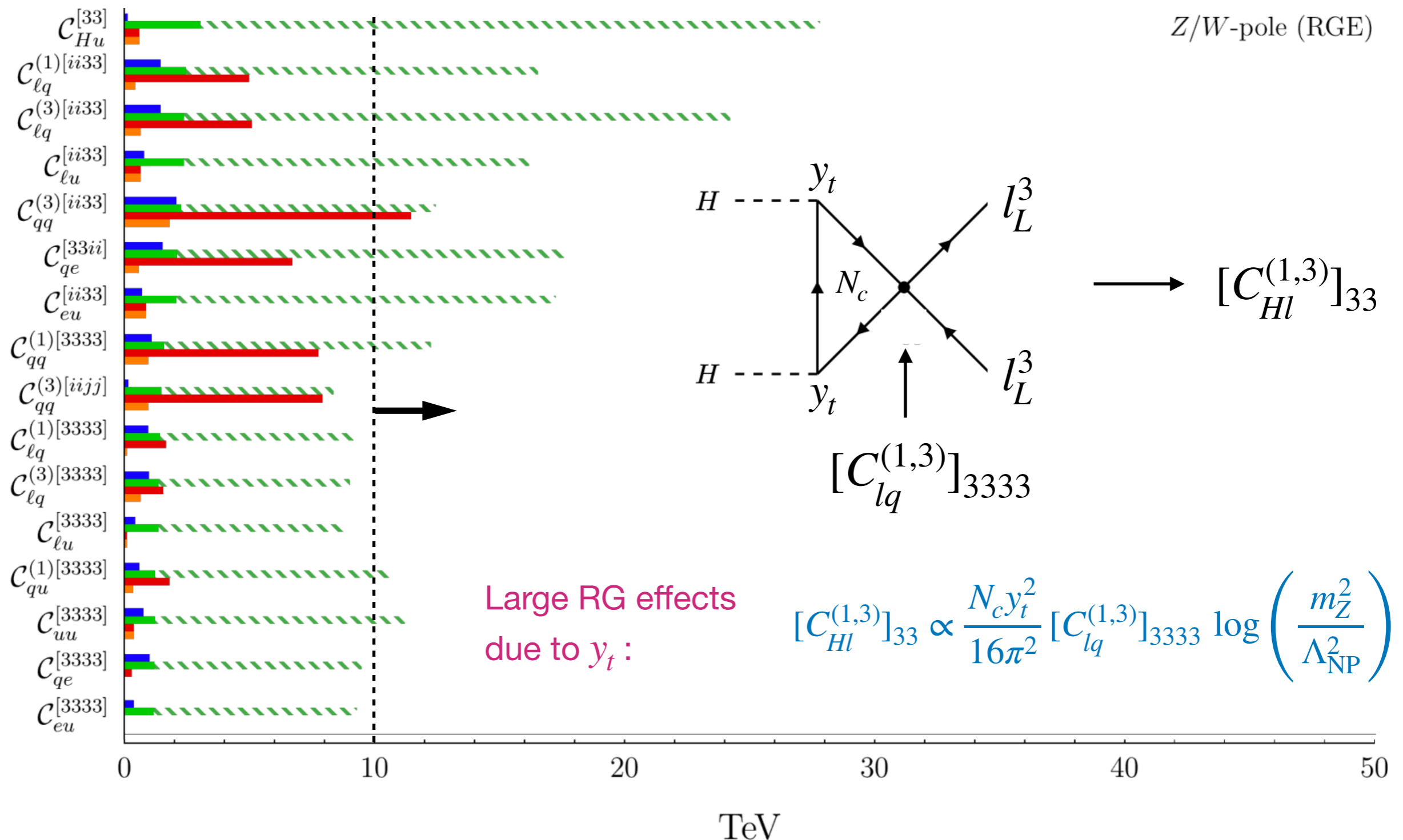
Tera-Z beyond leading order

[Allwicher, Cornella, Isidori, BAS, 2311.00020]

- *"On the Importance of Electroweak Corrections for 3rd-generation New Physics"*

Z/W-pole (RGE)

$$\longrightarrow \quad [C_{Hl}^{(1,3)}]_{33}$$

$$[C_{lq}^{(1,3)}]_{3333}$$

Large RG effects due to y_t :

$$[C_{Hl}^{(1,3)}]_{33} \propto \frac{N_c y_t^2}{16\pi^2} [C_{lq}^{(1,3)}]_{3333} \log\left(\frac{m_Z^2}{\Lambda_{\text{NP}}^2}\right)$$
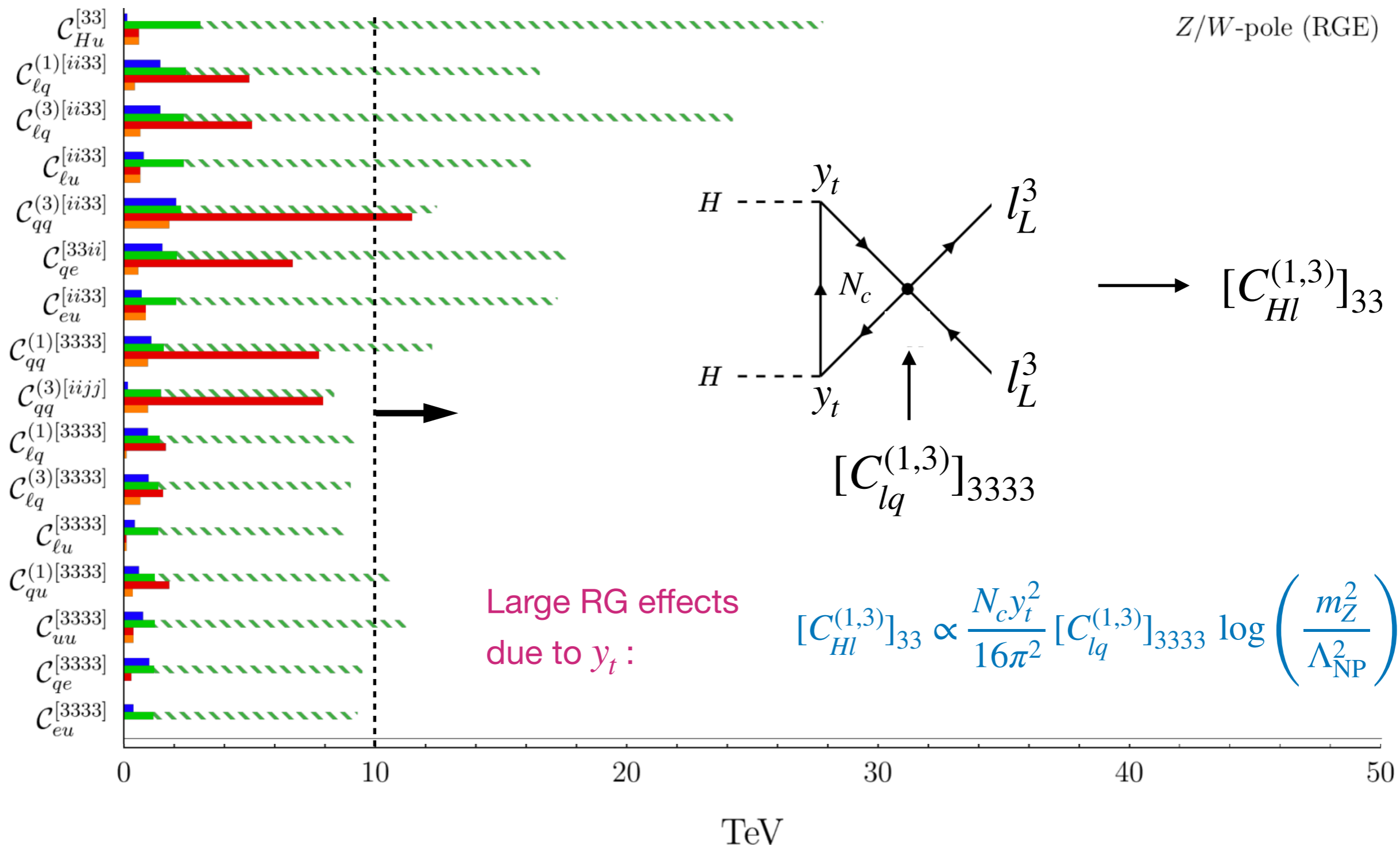
Example: Composite Higgs models

- Ok, so tera-Z is the ideal machine to indirectly search for NP at nearby energies protected by the accidental symmetries of the SM. But why do I care?

- Let's assume the EW hierarchy problem is solved because the Higgs arises as a composite state of some new strong dynamics described by one mass scale m_* and one coupling g_*.

- It is frequently claimed that such theories are good examples of "universal" theories, because the low-energy EFT simply features a strongly-interacting light Higgs (SILH). In this case, there is nothing to say about flavor.

- But that's not the full story, is it? We know the top Yukawa is O(1). This means that the left- or right-handed top (or both) must have a sizable degree of compositeness.

The top Yukawa is realized via partial compositeness

$$H \dashleftarrow g_* \qquad \begin{matrix} \varepsilon_L \quad q_L^3 \\ \\ \varepsilon_R \quad t_R \end{matrix} \qquad \Longrightarrow \quad y_t \simeq g_* \varepsilon_L \varepsilon_R$$
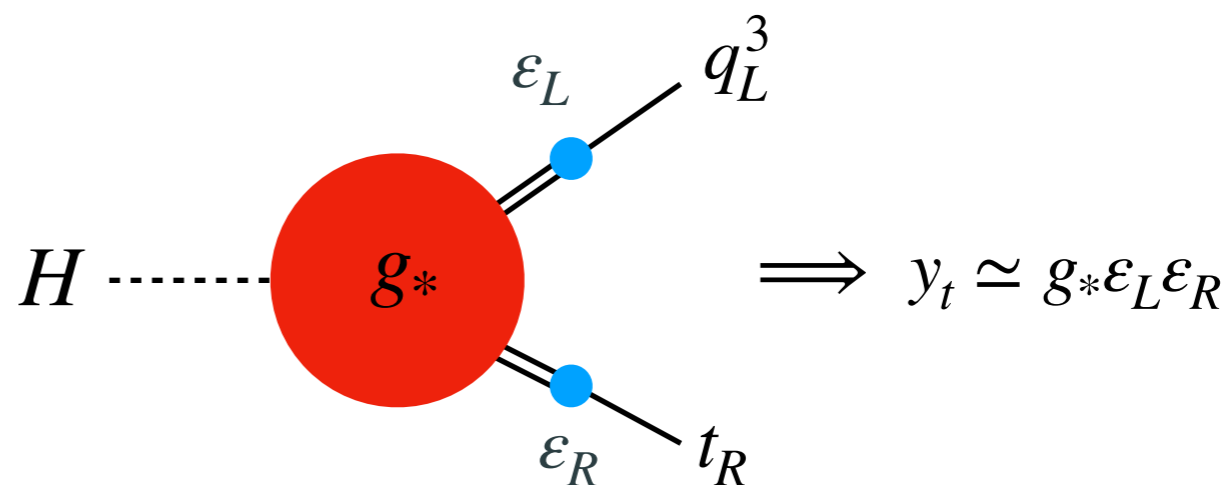
Non-universality of composite Higgs models

The top Yukawa is realized via partial compositeness

$$\implies y_t \simeq g_* \varepsilon_L \varepsilon_R$$
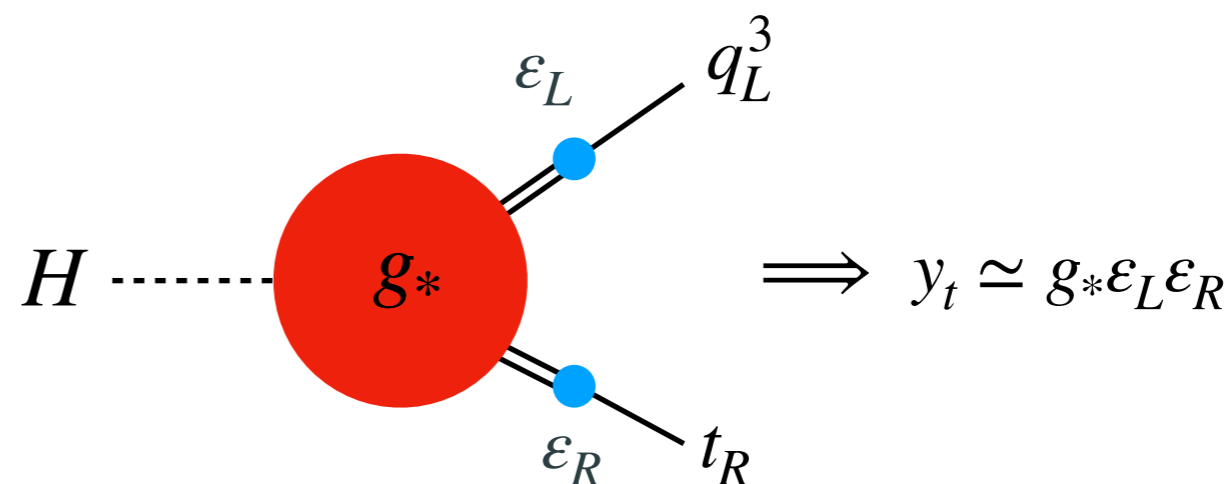
● Via these mixing parameters, the composite sector will unavoidably generate other large top+H operators, for example:
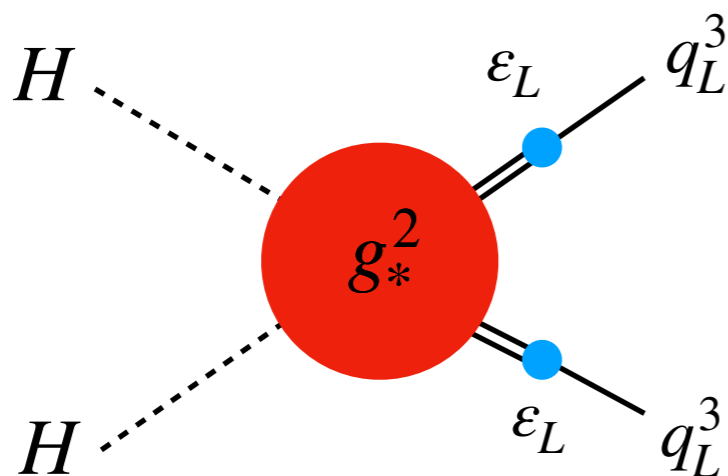
$$\mathcal{O}_{Hq}^{(1)} = (H^\dagger D_\mu H)(\bar{q}_L^3 \gamma^\mu q_L^3)$$
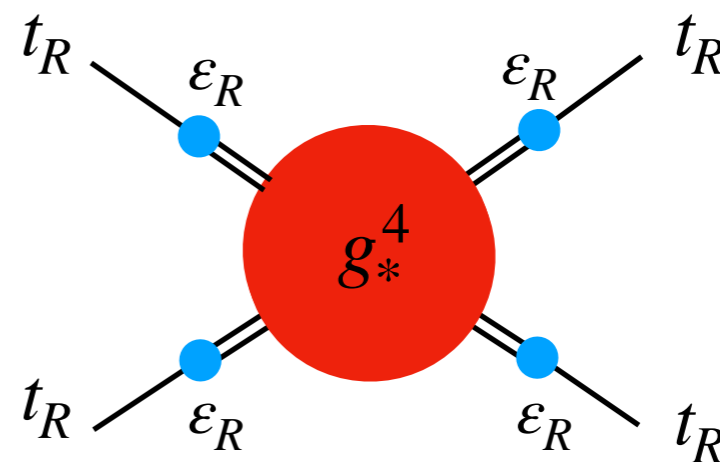
$$\mathcal{O}_{tt} = (\bar{t}_R \gamma_\mu t_R)(\bar{t}_R \gamma^\mu t_R)$$

Left-handed top operators

- Operators with q_L^3 typically have correlated signatures in EWPO and flavor.
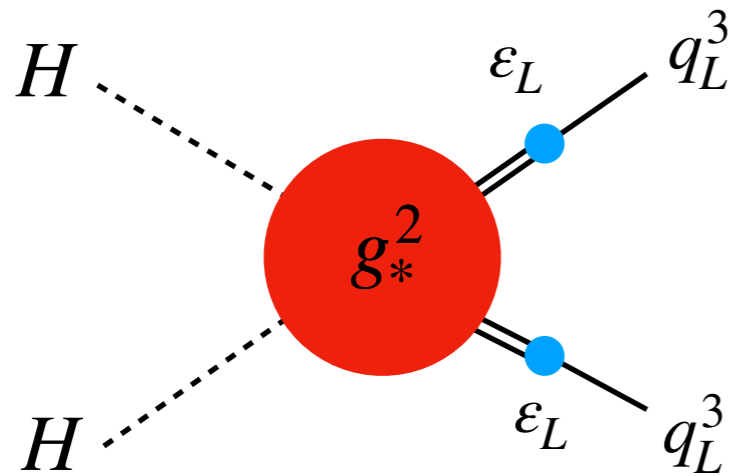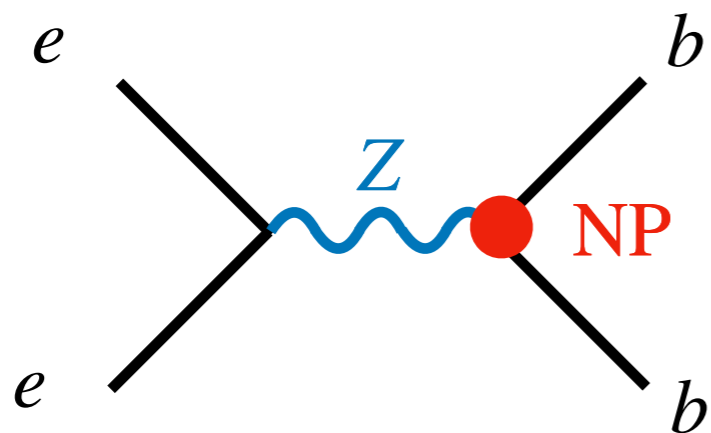
$$(H^\dagger D_\mu H)(\bar{q}_L^3 \gamma^\mu q_L^3)$$

EWPO: Zbb vertex corrections

Left-handed top operators

- Operators with q_L^3 typically have correlated signatures in EWPO and flavor.

$$(H^\dagger D_\mu H)(\bar{q}_L^3 \gamma^\mu q_L^3)$$

$\sim V_{ts}$

$\cancel{U(2)_q}$
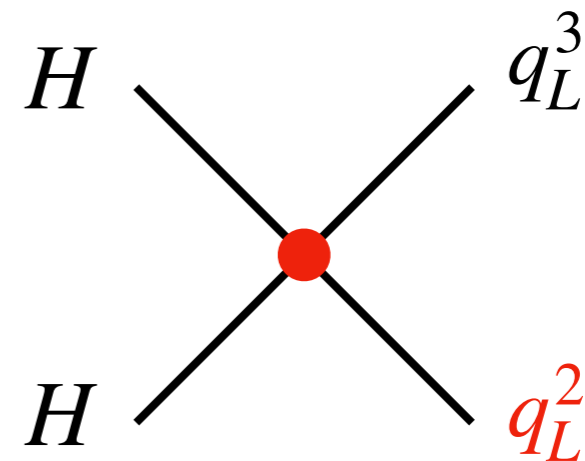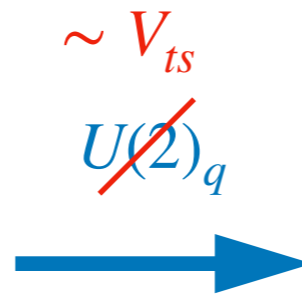
$$(H^\dagger D_\mu H)(\bar{q}_L^2 \gamma^\mu q_L^3)$$
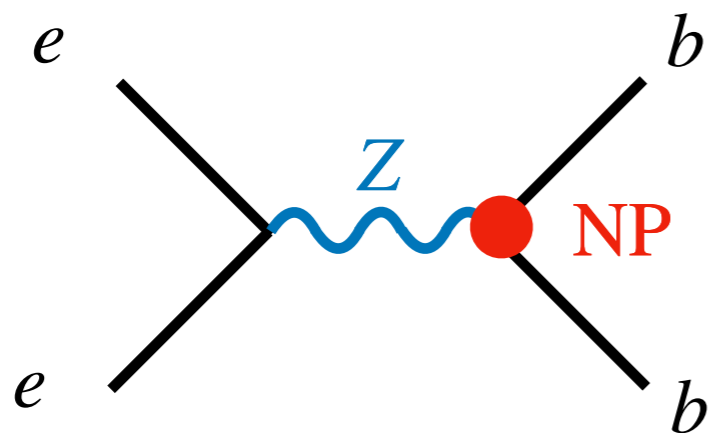
EWPO: Zbb vertex corrections
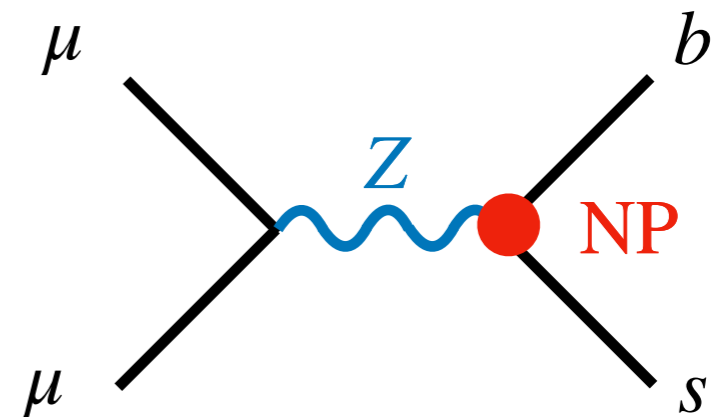
Flavor: $B_s \to \mu^+\mu^-$, ΔM_{B_s}

Right-handed top operators

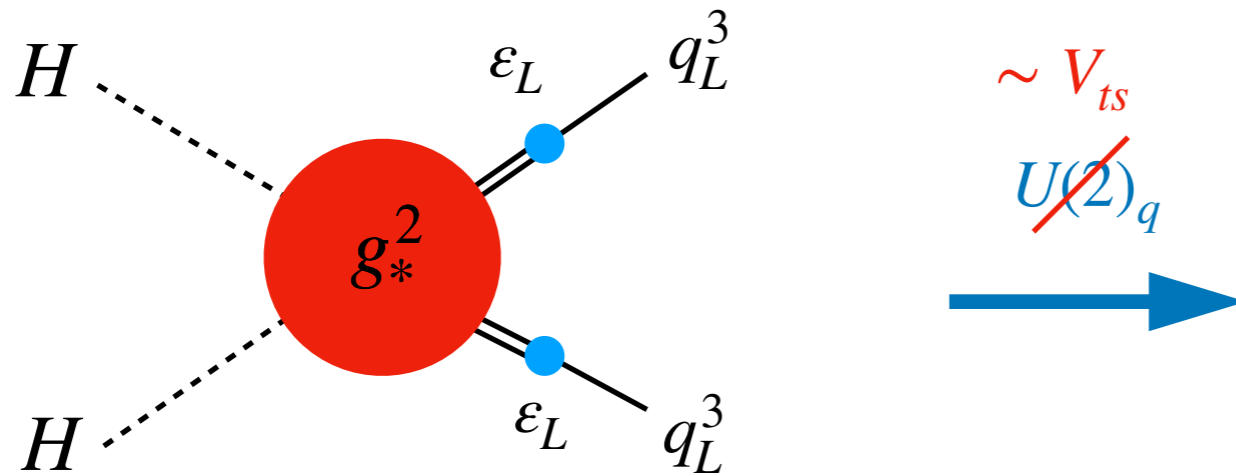- Operators with t_R not obviously constrained by flavor or EW precision tests...
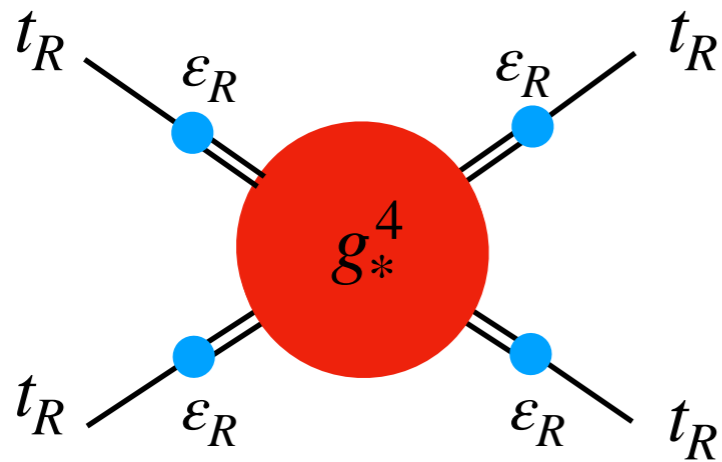
$$\mathcal{O}_{tt} = (\bar{t}_R \gamma_\mu t_R)(\bar{t}_R \gamma^\mu t_R)$$
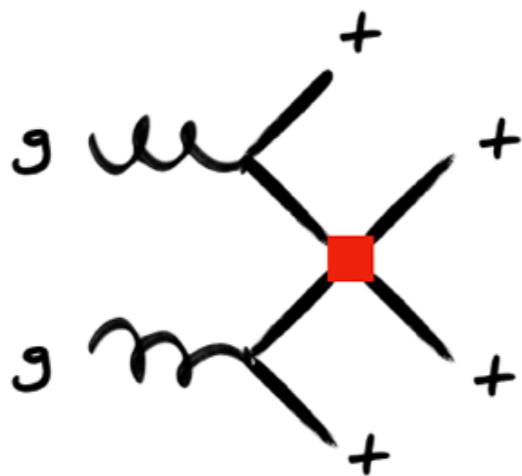
LHC: $pp \to t\bar{t}t\bar{t}$

Right-handed top operators

- Operators with t_R not obviously constrained by flavor or EW precision tests…
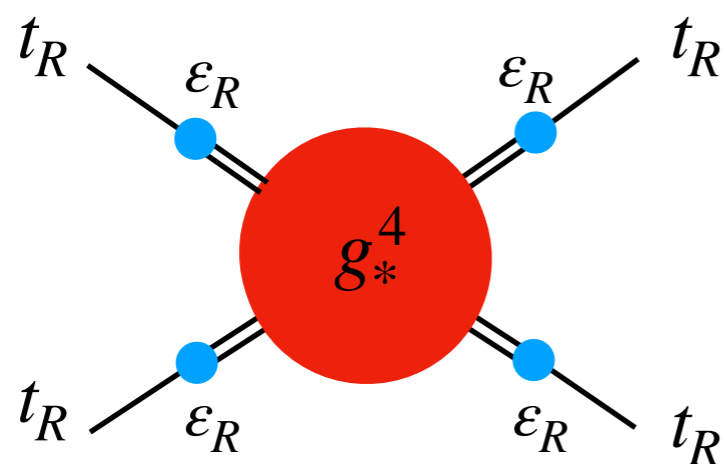
$$\frac{N_c^2 y_t^4}{(16\pi^2)^2}$$
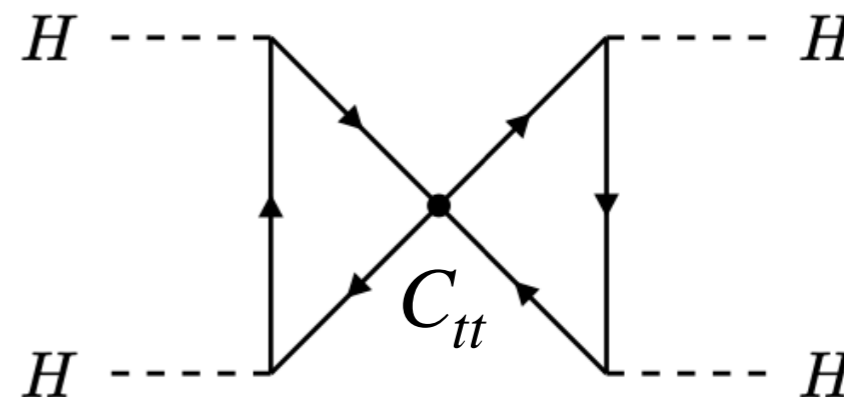
$$\mathcal{O}_{tt} = (\bar{t}_R \gamma_\mu t_R)(\bar{t}_R \gamma^\mu t_R)$$

$$\mathcal{O}_{HD} = |H^\dagger D_\mu H|^2$$
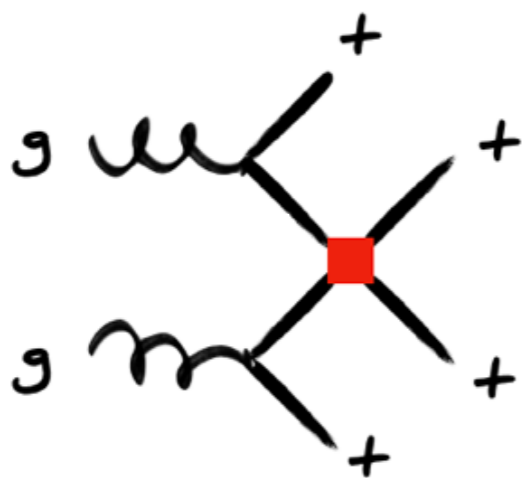
$$\frac{\delta m_W}{m_W} = -\frac{v^2}{4}\frac{C_{HD}}{(1 - t_W^2)}$$

LHC: $pp \rightarrow t\bar{t}t\bar{t}$

EWPO + LHC: T parameter / m_W

Beyond leading-log running of 4-top operators

- The dominant part of this 2-loop effect can be captured by integrating the full 1-loop RG equations, which resums higher loop effects of the form $(\alpha \log)^n$.
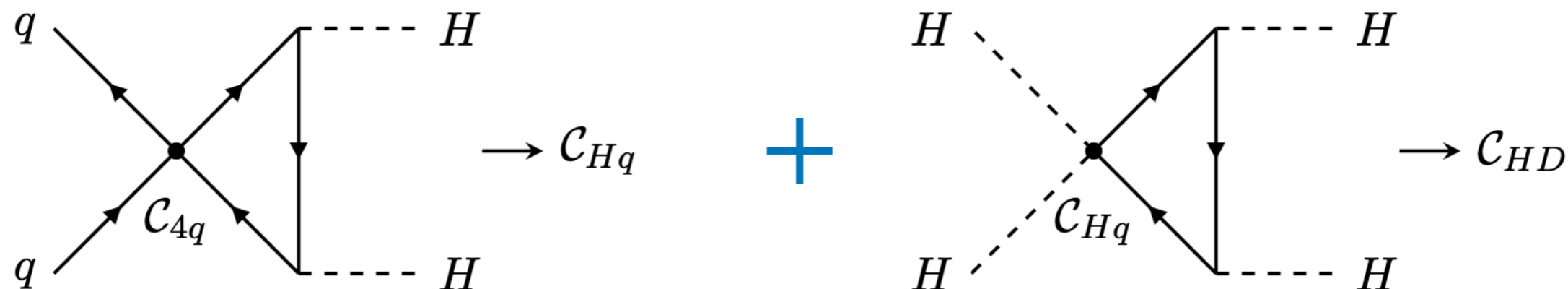
- The full 2-loop computation is now also available: [Haisch, Schnell, 2410.13304]

- This two-loop effect allows sensitivity to 4-top operators via measurements of m_W. An analytic formula for this $\alpha_t^2 \log^2$ contribution can be found if we neglect the running of the SM couplings:

$$[\mathcal{C}_{HD}]_{\mathrm{NLL}} = \frac{2N_c\, y_t^4}{(16\pi^2)^2} \left[(1 + 2N_c)\mathcal{C}_{qq}^{(1)} + 3\mathcal{C}_{qq}^{(3)} + 2(1 + N_c)\mathcal{C}_{tt} - 2N_c\mathcal{C}_{qt}^{(1)} \right] \log^2\left(\frac{\mu^2}{m_*^2} \right)$$

[BAS, 2407.09593]   [Allwicher, Isidori, Lizana, Selimovic, BAS, 2302.11584]

W boson mass

CMS *Preliminary*

m_W in MeV

LEP combination
Phys. Rep. 532 (2013) 119 — 80376 ± 33

D0
PRL 108 (2012) 151804 — 80375 ± 23

CDF
Science 376 (2022) 6589 — 80433.5 ± 9.4

LHCb
JHEP 01 (2022) 036 — 80354 ± 32

ATLAS
arxiv:2403.15085, subm. to EPJC — 80366.5 ± 15.9

CMS
This Work — 80360.2 ± 9.9

-·- EW fit

m_W (MeV)
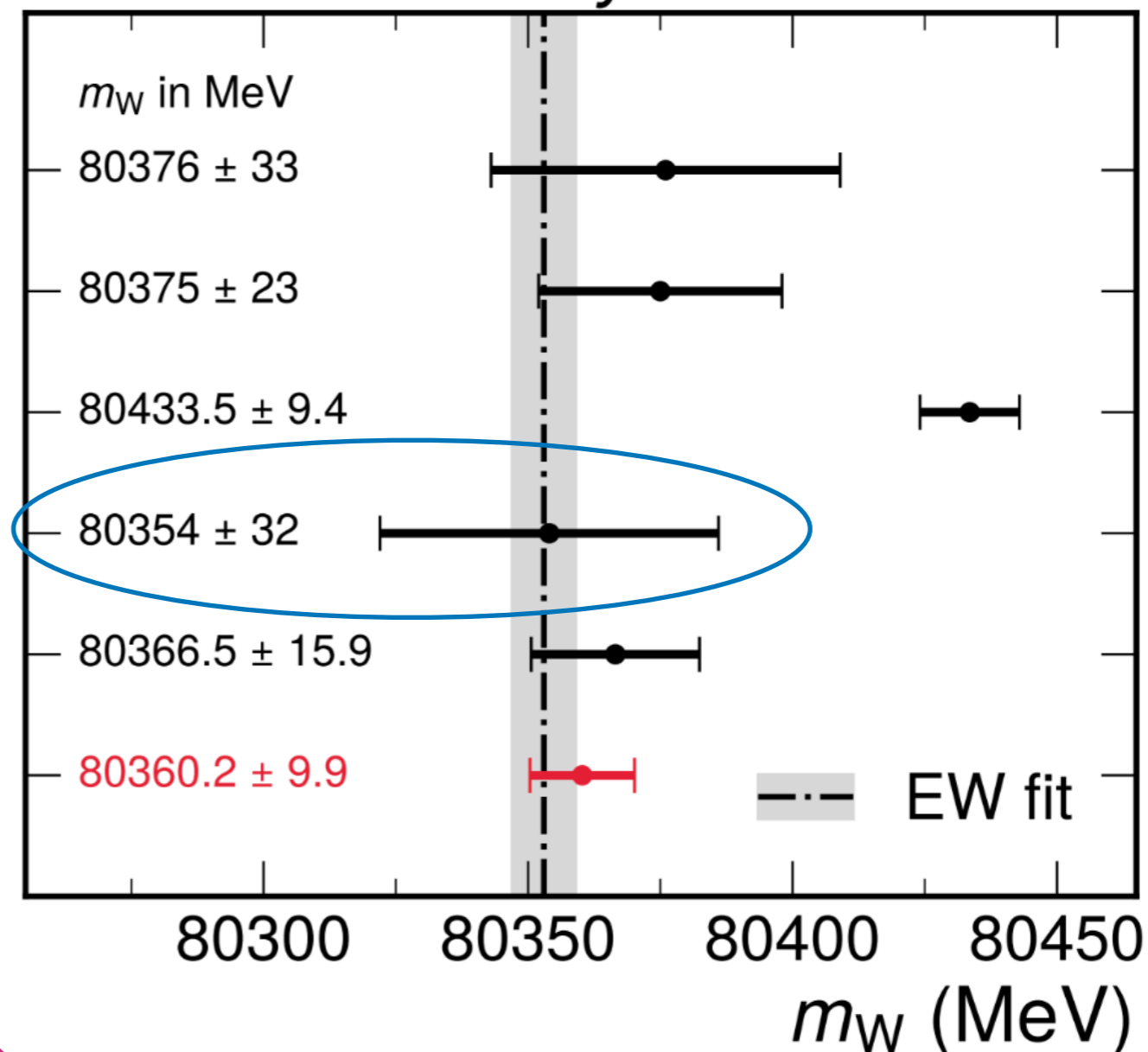
$$\frac{\delta m_W}{m_W} = -\frac{v^2}{4}\frac{C_{HD}}{(1-t_W^2)}$$

Best current bound on C_{tt}!

- LHCb already provides LEP-level sensitivity! And LHCb Upgrade II can reach a statistical precision on m_W of O(10 MeV). FCC-ee: precision of O(1 MeV).

[Physics case for an LHCb Upgrade II, 1808.08865]

Future summary plots

- Mixing-independent bound of $m_* \gtrsim 18$ TeV. Flavor and EW precision are complementary! FCC adds the most new info in the mixed + right comp. cases.

(a) Left compositeness

(b) Mixed compositeness

(c) Right compositeness

[BAS, 2407.09593]
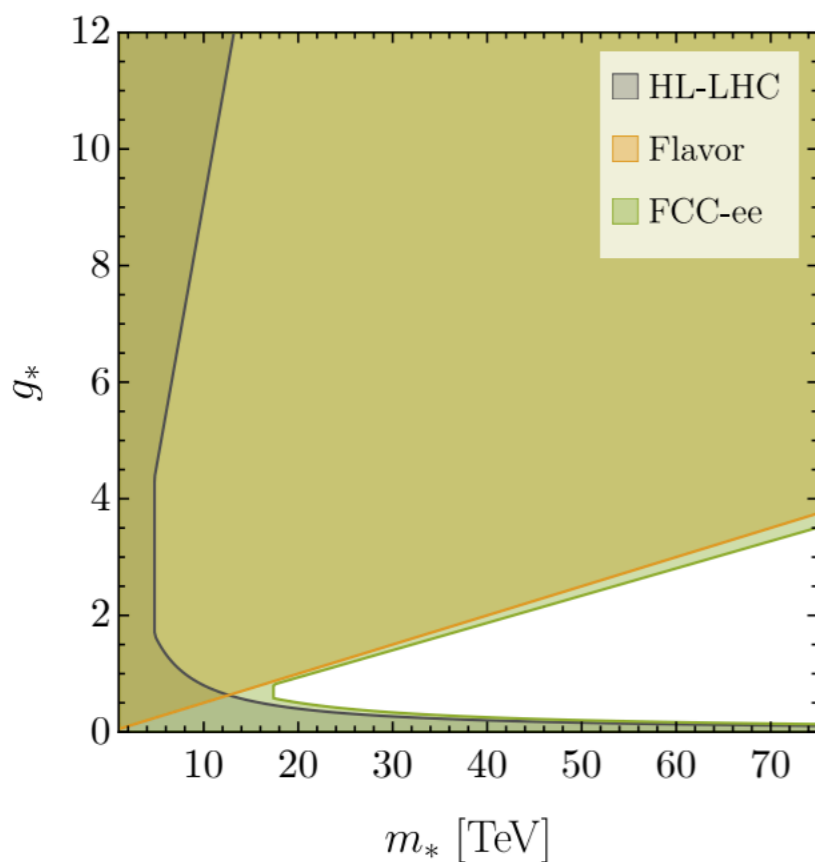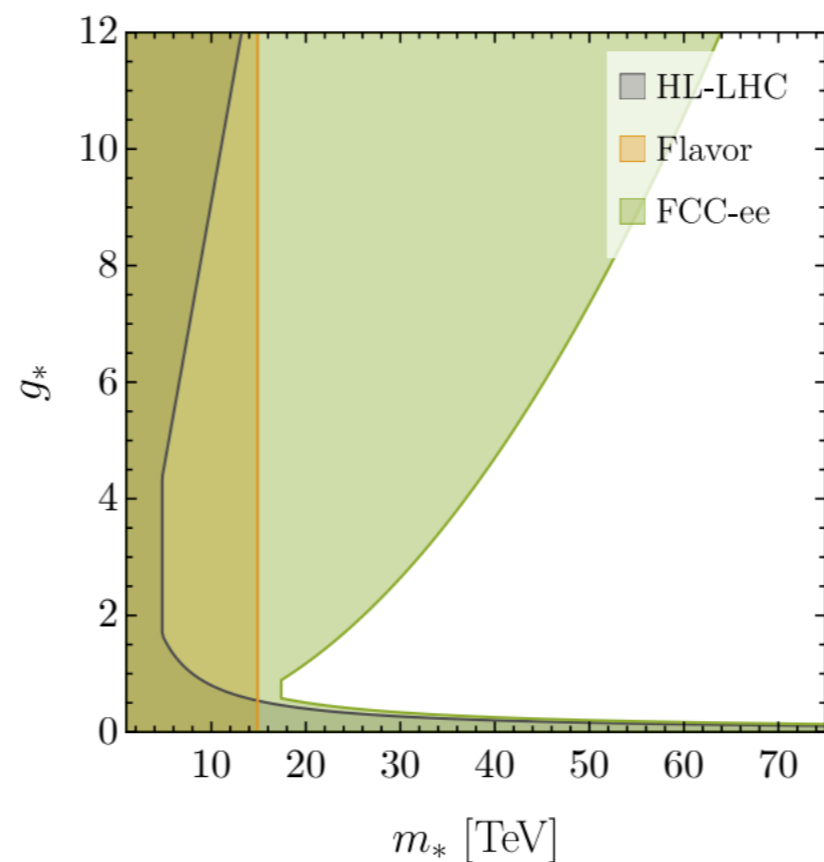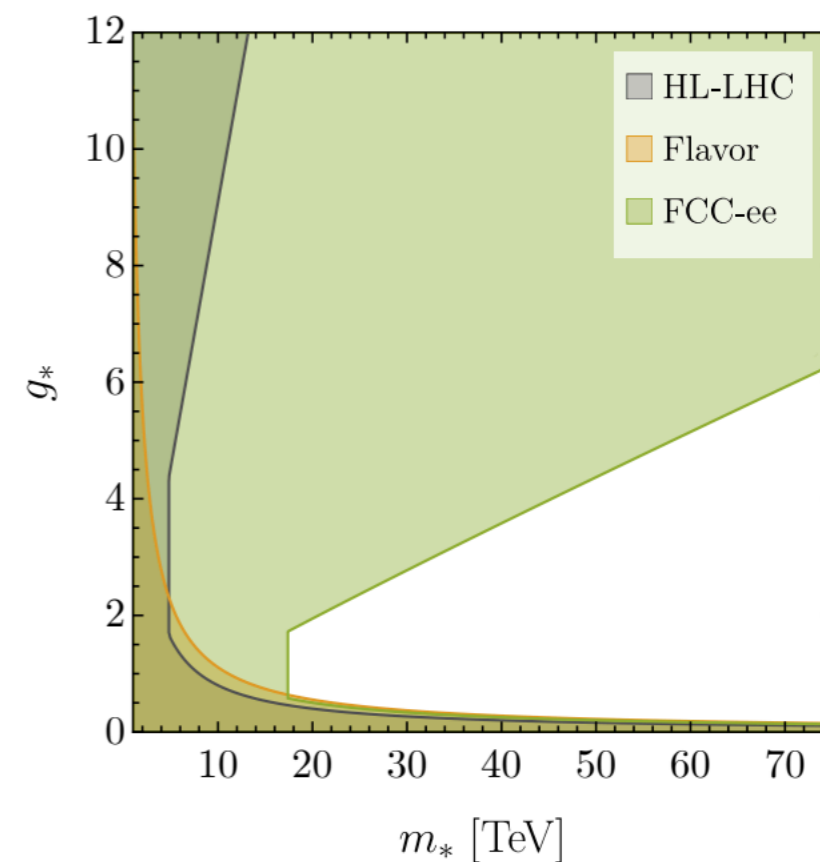
Conclusions

- We cannot have TeV-scale NP without some kind of flavor protection. Given the current direct search bounds from the LHC, flavor universal NP no longer seems very natural with bounds O(10) TeV.

- Instead, $U(2)$ flavor symmetries are very well-motivated since 1) NP can couple more to the third and less to the light families and 2) we expect NP solving the hierarchy problem (and/or flavor puzzle) to be mostly coupled to the Higgs and 3rd family. These features are exhibited in classic scenarios such as composite Higgs models.

- Third generation NP typically leads to correlated effects in flavor and EWPO. Non-universality implies flavor violations, so $b \to s$ transitions remain extremely interesting and motivated from the theory perspective. In particular, $B_s \to \mu^+\mu^-$, ΔM_{B_s}, and m_W are highly sensitive probes of new physics.

- Ultimately, FCC-ee is the way to go. High statistics at the Z-pole gives 1 and even 2 loop sensitivity to hundreds of SMEFT operators. We described such effects here, including a novel probe of 4-top operators via their two-loop contribution to the T parameter. This allows current EW precision data to set the best bound on these operators.

- Even with FCC, flavor data will provide a complementary probe. Flavor is undoubtedly the best place to make progress while we wait for the next-generation collider!

Backup

Constraints on 4-top operators from LHC data

- At the LHC, 3rd generation four-quark operators can be probed at tree level only in 4t, 4b, 2b2t production. Present measurements all have large uncertainties.

ATLAS		23.6 fb $(1 \pm 26\%)$
CMS		17 fb $(1 \pm 30\%)$
SM		12 fb $(1 \pm 20\%)$

σ_{4t} [fb]
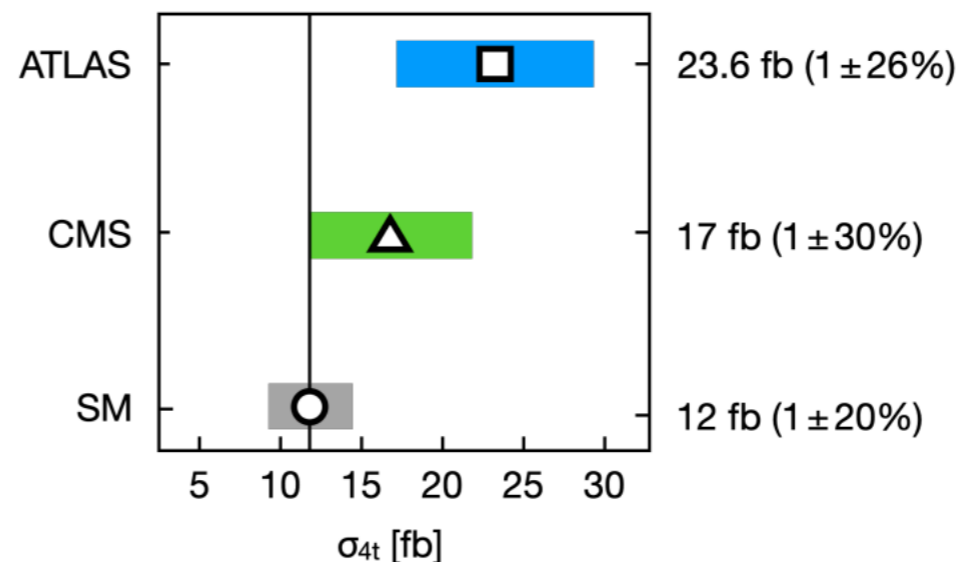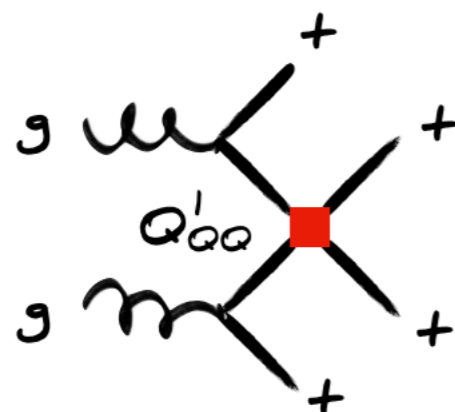
- Due to strong bottom PDF suppression, 3rd generation four-quark operators mainly contribute to 2-top production at 1-loop:
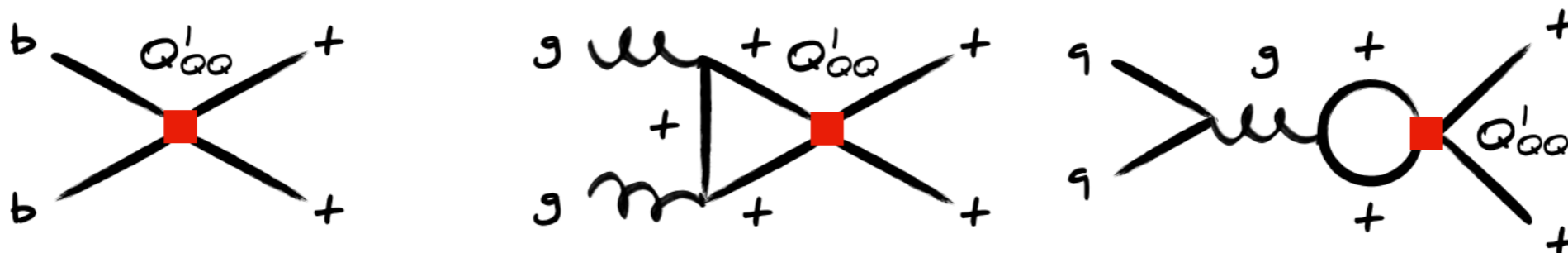
Constraints on 4-top operators: EWPD vs. LHC data

- Limits come from fits by theorists and depend on whether the fit is linear or also includes quadratic terms. 👁 See also Marcel + Jaco's talks

- Raises questions about stability of fit under d8 deformations & EFT applicability in general, since limits arise from configurations with momentum transfer of around 0.4 TeV (1.3 TeV) in 2t (4t) production.

- Depending on who you ask, bounds around 750–900 GeV for Ctt.

- On the other hand, EWPD gives a robust 2-loop bound from T

$$\hat{T} = -\frac{v^2}{2} C_{HD} < 10^{-3} \implies C_{tt} \leq \frac{1}{(1.2 \text{ TeV})^2}$$

[Degrande et al., 2402.06528]

$pp \to t\bar{t}, \mathcal{O}(\Lambda^{-4})$
$pp \to t\bar{t}, \mathcal{O}(\Lambda^{-2})$
$pp \to t\bar{t}t\bar{t}, \mathcal{O}(\Lambda^{-4})$
$pp \to t\bar{t}t\bar{t}, \mathcal{O}(\Lambda^{-2})$

$c_{QQ}^1/\Lambda^2 \; [1/\text{TeV}^2]$

$c_{tt}^1/\Lambda^2 \; [1/\text{TeV}^2]$

[Credit to Uli Haisch, HEFT 2024, Precision tests of 3rd-generation four-quark SMEFT operators]
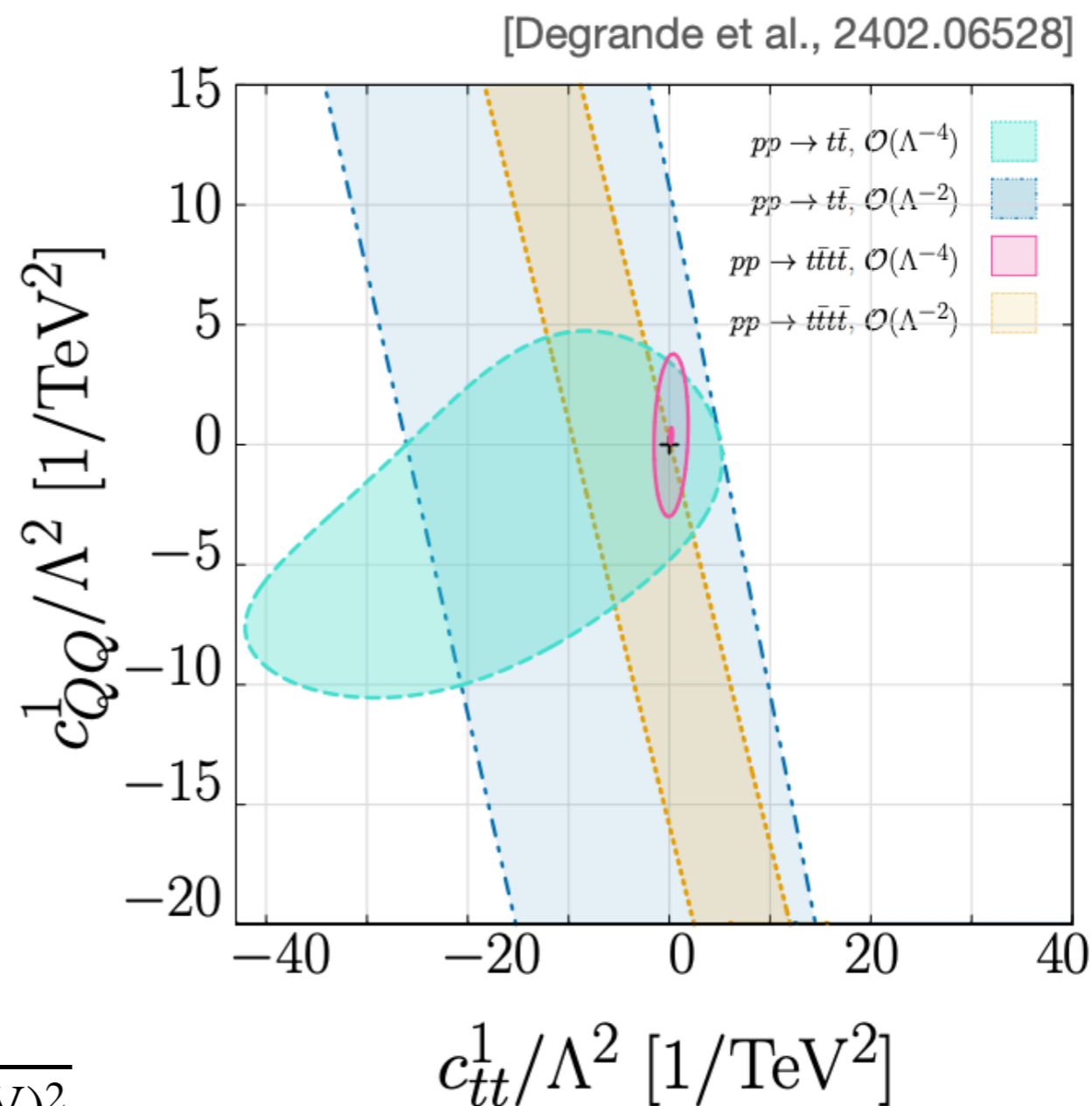
Partial compositeness: A few more details

- To say something more quantitative about composite Higgs in particular, we need to provide a bit more detail on the fermionic mixing

<p style="text-align:center;">Generates V_{ts}, V_{td}</p>

$$\mathcal{L}_{\mathrm{mix}} = \lambda_L \bar{q}_L^3 \mathcal{O}_L + \lambda_R \bar{t}_R \mathcal{O}_R + \lambda_q^i \bar{q}_L^i \mathcal{O}_q + \mathcal{L}_{\mathrm{light}}$$

<p style="text-align:center;">Generates y_t</p>

Light family masses+mixings

- This theory respects a $U(2)_q \times U(2)_u \times U(3)_d \times U(3)_l \times U(3)_e$ flavor symmetry without the coupling λ_q^i. This coupling breaks $U(2)_q$ and will control flavor violation in the theory. For example, B-meson mixing behaves as: $(\bar{q}_L^i \lambda_q^i \gamma_\mu q_L^3)^2$

Results: Right compositeness

- Right compositeness has $\epsilon_L = y_t/g_*$, $\epsilon_R = 1$.   Flavor constraints: $C_{B_s} \propto \dfrac{g_*^2}{m_*^2} \epsilon_L^4$
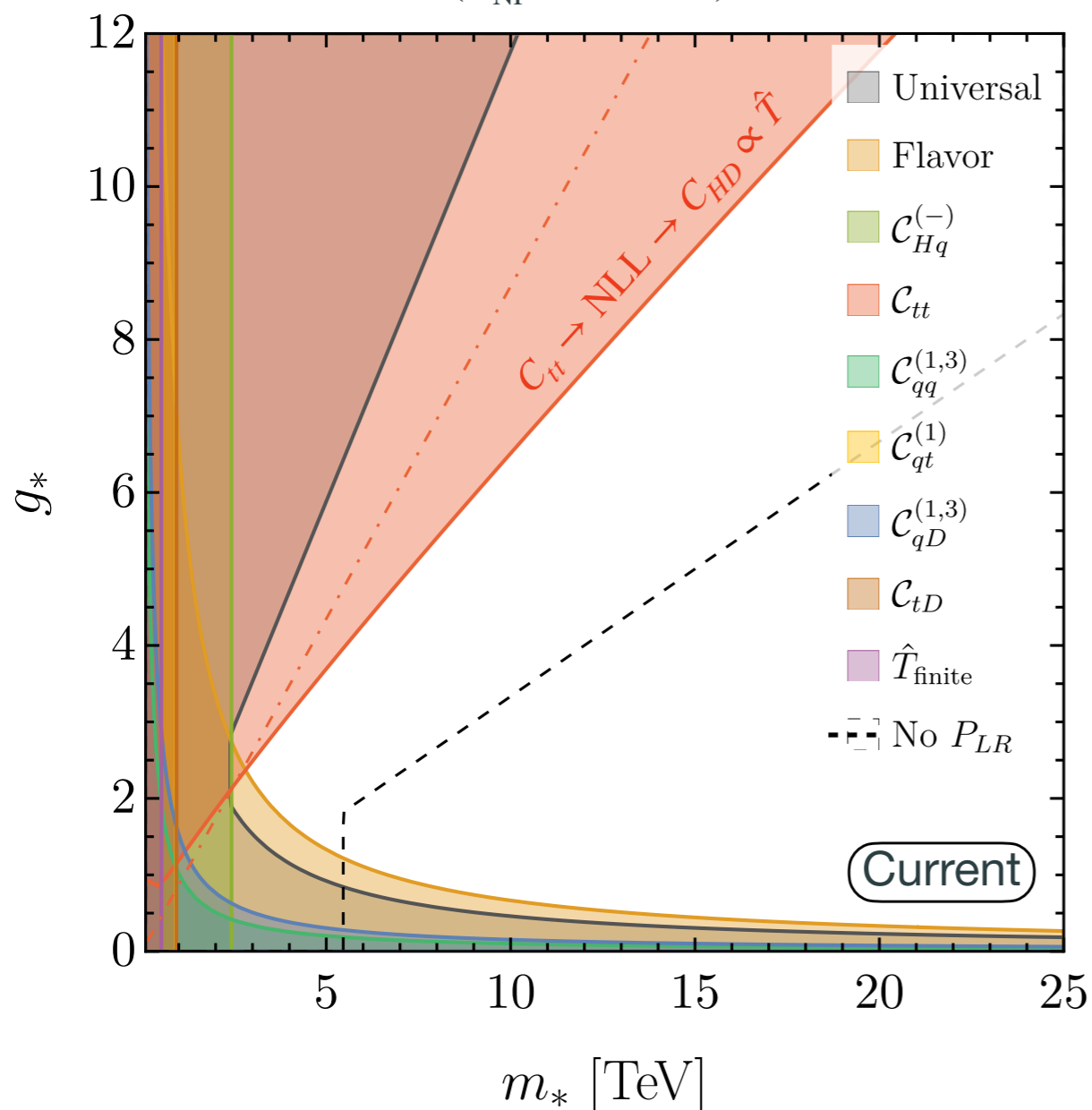
$(\Lambda_{\rm NP} = 2.5~{\rm TeV})$ $(\Lambda_{\rm NP} = 25~{\rm TeV})$
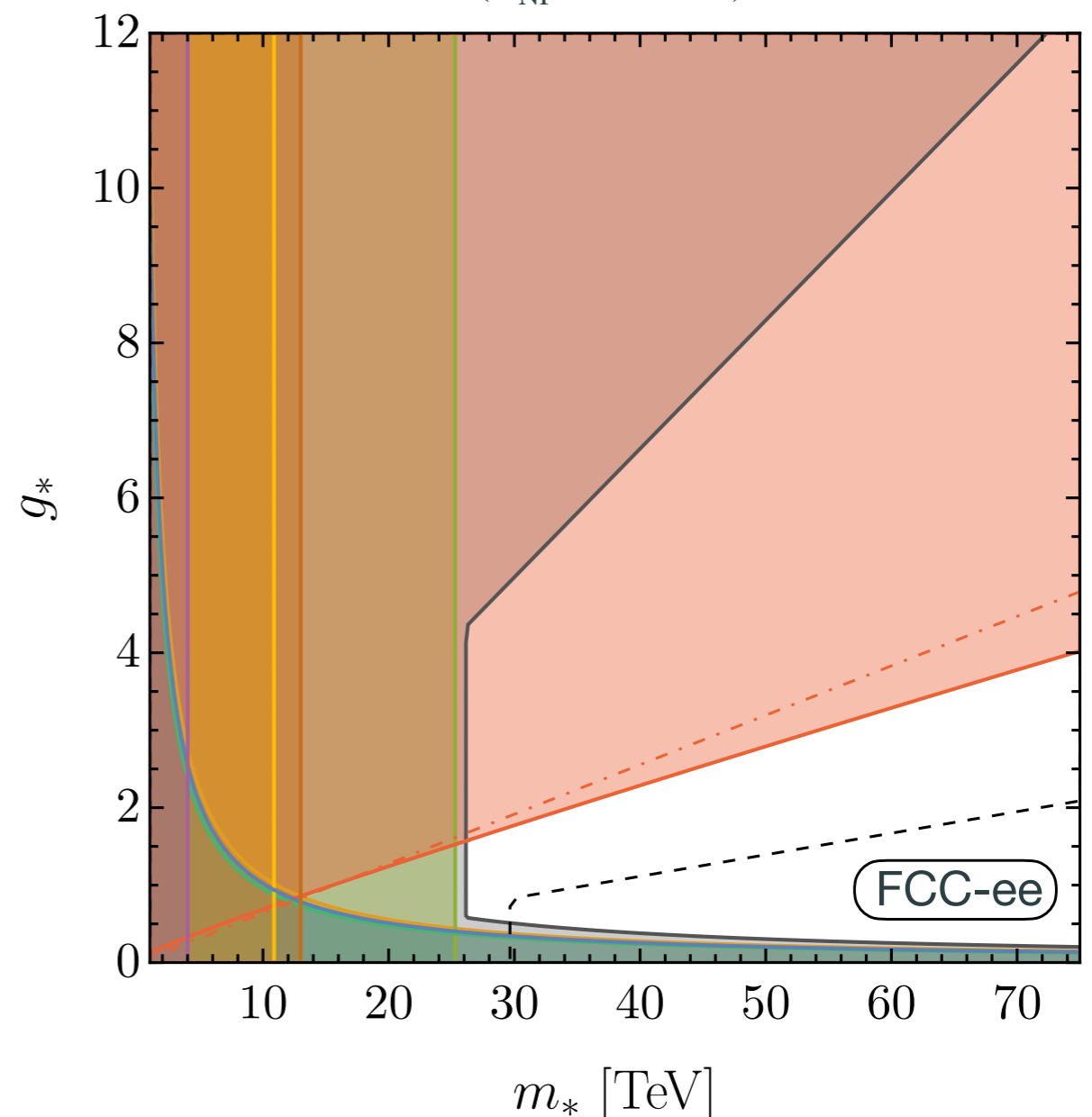
[BAS, 2407.09593]

Universal operators in composite Higgs models

● Now let's have a look at the operators we can write only involving the Higgs (and gauge fields of course). We work here in the SILH basis:

Flavor universal bosonic operators	
$\mathcal{O}_H = \frac{1}{2}\partial_\mu(H^\dagger H)\partial^\mu(H^\dagger H)$	$\mathcal{O}_T = \frac{1}{2}(H^\dagger \overleftrightarrow{D}_\mu H)(H^\dagger \overleftrightarrow{D}^\mu H)$
$\mathcal{O}_W = i\frac{g_2}{2}(H^\dagger \overleftrightarrow{D}^I_\mu H)D_\nu W^{I\,\mu\nu}$	$\mathcal{O}_B = i\frac{g_1}{2}(H^\dagger \overleftrightarrow{D}_\mu H)\partial_\nu B^{\mu\nu}$
$\mathcal{O}_{2W} = -\frac{g_2^2}{2}(D^\mu W^I_{\mu\nu})(D_\rho W^{I\rho\nu})$	$\mathcal{O}_{2B} = -\frac{g_1^2}{2}(\partial^\mu B_{\mu\nu})(\partial_\rho B^{\rho\nu})$

$\mathcal{O}_H$: Higgs coupling modifications $\mathcal{O}_T$: Peskin-Takeuchi T parameter

$\mathcal{O}_{W+B}$: Peskin-Takeuchi S parameter $\mathcal{O}_{2W,2B}$: $W + Y$ parameters
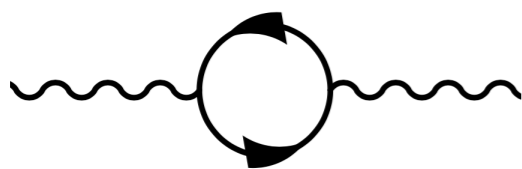
Recall: $\Pi_{VV}(p^2) = \Pi_{VV}(0) + p^2\Pi'_{VV}(0) + p^4\Pi''_{VV}(0) + \dots$

$\downarrow$ $\downarrow$ $\downarrow$

T S W, Y

[BAS, 2407.09593]

Single operator bounds including (resummed) RGE

Model-building tricks

Custodial symmetry in the strong sector

$C_T = 0$ (LO)

A custodial symmetry for Zbb

$C_{Hq}^{(1)} + C_{Hq}^{(3)} = 0$

$C_{Ht} = 0$ (LO)

[Agashe, Contino, Da Rold, Pomarol, hep-ph/0605341]

Wilson Coef.	[Obs]$_{\text{bound}}$	Λ_{bound} [TeV]	Wilson Coef.	[Obs]$_{\text{bound}}$	Λ_{bound} [TeV]
$\mathcal{C}_T$	A_b^{FB}	8.17	$\mathcal{C}_T$	m_W	74.24
$\mathcal{C}_{Hq}^{(1)}$	R_τ	3.98	$\mathcal{C}_{Hq}^{(1)}$	m_W	39.82
$\mathcal{C}_{Hq}^{(3)}$	R_b	3.94	$\mathcal{C}_{Hq}^{(3)}$	R_μ	24.81
$\mathcal{C}_{Ht}$	A_b^{FB}	3.00	$\mathcal{C}_{Ht}$	m_W	35.92
$\mathcal{C}_{Hq}^{(-)}$	A_b^{FB}	2.98	$\mathcal{C}_{Hq}^{(-)}$	m_W	33.97
$\mathcal{C}_B$	A_b^{FB}	2.48	$\mathcal{C}_B$	A_e	26.15
$\mathcal{C}_W$	A_b^{FB}	2.41	$\mathcal{C}_W$	A_e	24.67
$\mathcal{C}_{qD}^{(3)}$	R_τ	1.87	$\mathcal{C}_{qD}^{(3)}$	R_μ	12.24
$\mathcal{C}_{tW}$	A_b^{FB}	1.86	$\mathcal{C}_{tW}$	A_e	26.19
$\mathcal{C}_{qq}^{(1)}$	R_τ	1.53	$\mathcal{C}_{qq}^{(1)}$	m_W	17.22
$\mathcal{C}_{2W}$	A_b^{FB}	1.51	$\mathcal{C}_{2W}$	A_e	15.17
$\mathcal{C}_{tB}$	A_b^{FB}	1.44	$\mathcal{C}_{tB}$	A_e	20.24
$\mathcal{C}_{qq}^{(3)}$	R_b	1.30	$\mathcal{C}_{qq}^{(3)}$	m_W	10.25
$\mathcal{C}_{tt}$	A_b^{FB}	1.15	$\mathcal{C}_{tt}$	m_W	15.66
$\mathcal{C}_{qt}^{(1)}$	R_τ	1.14	$\mathcal{C}_{qt}^{(1)}$	m_W	14.61
$\mathcal{C}_{qD}^{(1)}$	A_b^{FB}	1.12	$\mathcal{C}_{qD}^{(1)}$	A_e	13.71
$\mathcal{C}_{tD}$	A_b^{FB}	0.94	$\mathcal{C}_{tD}$	A_e	13.00
$\mathcal{C}_{2B}$	A_b^{FB}	0.78	$\mathcal{C}_{2B}$	A_e	8.59
$\mathcal{C}_H$	A_b^{FB}	0.47	$\mathcal{C}_H$	m_W	6.03
$\mathcal{C}_{tG}$	A_b^{FB}	0.46	$\mathcal{C}_{tG}$	A_e	7.91
$\mathcal{C}_{tH}$	$H \to \mu\mu$	0.17	$\mathcal{C}_{tH}$	$H \to \tau\tau$	0.94
$\mathcal{C}_{qt}^{(8)}$	R_τ	0.11	$\mathcal{C}_{qt}^{(8)}$	m_W	1.61

(a) Current bounds $(\Lambda_{\text{NP}} = 2.5 \text{ TeV})$

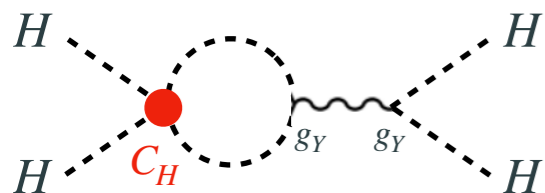(b) FCC-ee projection $(\Lambda_{\text{NP}} = 25 \text{ TeV})$

Single operator bounds including (resummed) RGE

Symmetry protected

S parameter

NLO/RG non-universal effects

NLO/RG universal effects

Wilson Coef.	$[\text{Obs}]_{\text{bound}}$	Λ_{bound} [TeV]		Wilson Coef.	$[\text{Obs}]_{\text{bound}}$	Λ_{bound} [TeV]
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$\mathcal{C}_{tH}$	$H \to \mu\mu$	0.17		$\mathcal{C}_{tH}$	$H \to \tau\tau$	0.94
$\mathcal{C}_{qt}^{(8)}$	R_τ	0.11		$\mathcal{C}_{qt}^{(8)}$	m_W	1.61

(a) Current bounds $(\Lambda_{\text{NP}} = 2.5 \text{ TeV})$

(b) FCC-ee projection $(\Lambda_{\text{NP}} = 25 \text{ TeV})$

[BAS, 2407.09593]

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Intrinsic non-universality of composite Higgs models

- What's missing with this picture? Even if you play all of the model-building tricks, its true at LO only! The most dangerous operators are generated via RGE as we run from m_* to the EW scale.

- Phenomenologically, the most important effects are $\propto N_c y_t^2 \log(m_Z^2/m_*^2)$:
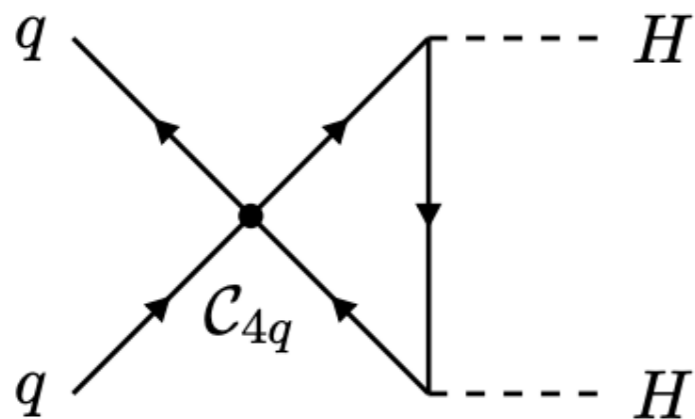
*4-top operators running
into EW vertex corrections.*
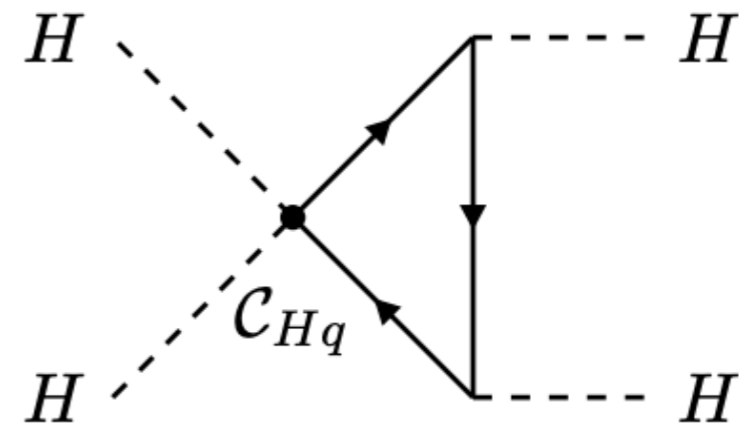
*EW vertex corrections running
into the T parameter*.*

$$\mathcal{O}_{qq}^{(1,3)}, \mathcal{O}_{qt}^{(1)}, \mathcal{O}_{tt} \rightarrow \mathcal{O}_{Hq}^{(1,3)}, \mathcal{O}_{Ht}$$

$$\mathcal{O}_{Hq}^{(1)}, \mathcal{O}_{Ht} \rightarrow \mathcal{O}_{HD}$$

Required custodial violation is coming from the SM!

The full 2-loop contribution to the T parameter

- While the double-log contribution is expected to dominate, in general the full 2-loop contribution of 4-top operators to the T parameter takes the form of a second-order logarithmic polynomial. E.g. for Ctt, we have:

$$[\mathcal{C}_{HD}]_{\text{2-loop}} = \frac{N_c(N_c+1)}{4\pi^2} \alpha_t^2 \left[\underbrace{\log^2(\mu^2/m_*^2)}_{\text{1-loop RGE}} + \underbrace{c_1 \log(\mu^2/m_*^2)}_{\text{2-loop RGE}} + \underbrace{c_2}_{\text{finite}} \right] \mathcal{C}_{tt}.$$

- The O(1) constants c1+c2 cannot be obtained from the 1-loop RG equations. In particular, c1 corresponds to the 2-loop anomalous dimension. To get all contributions, we need to do a 2-loop computation:
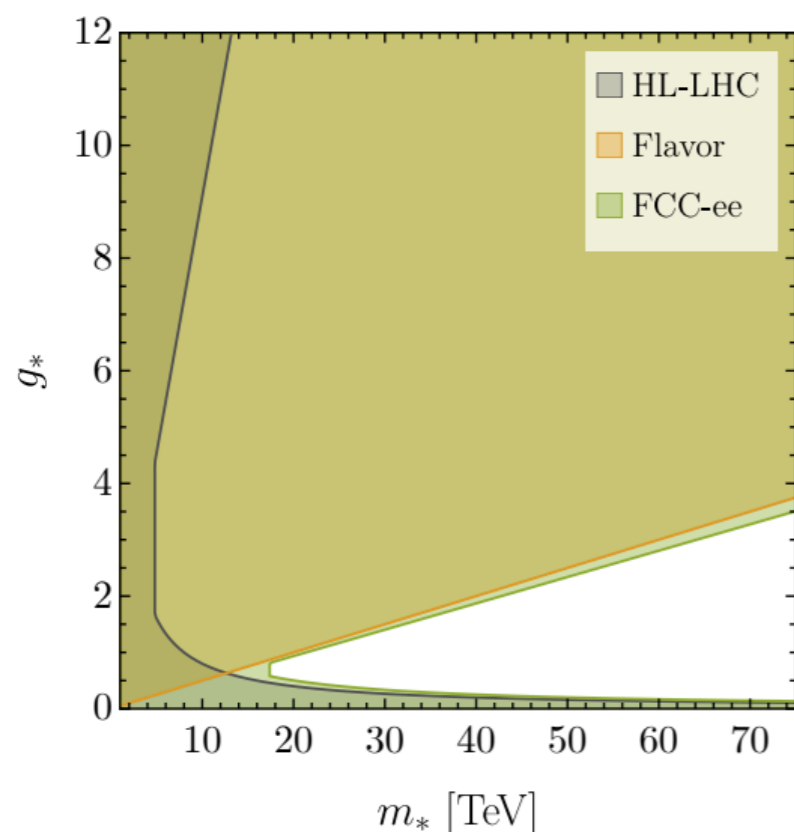

$\Longrightarrow$
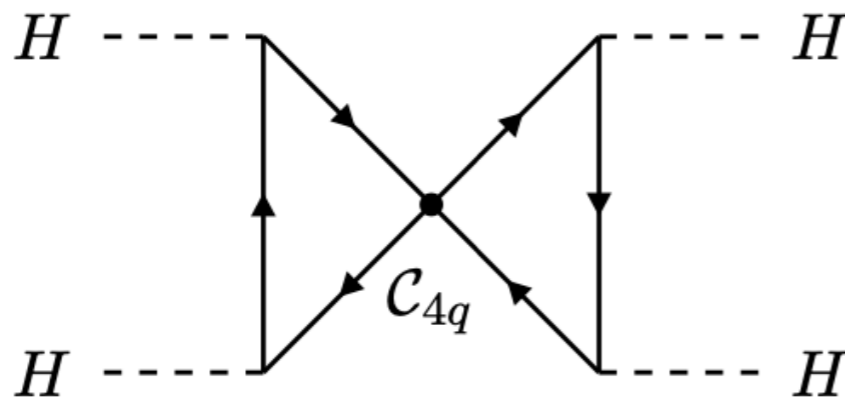
U. Haisch and L. Schnell, Precision tests of third-generation four-quark operators: matching SMEFT to LEFT, to appear soon

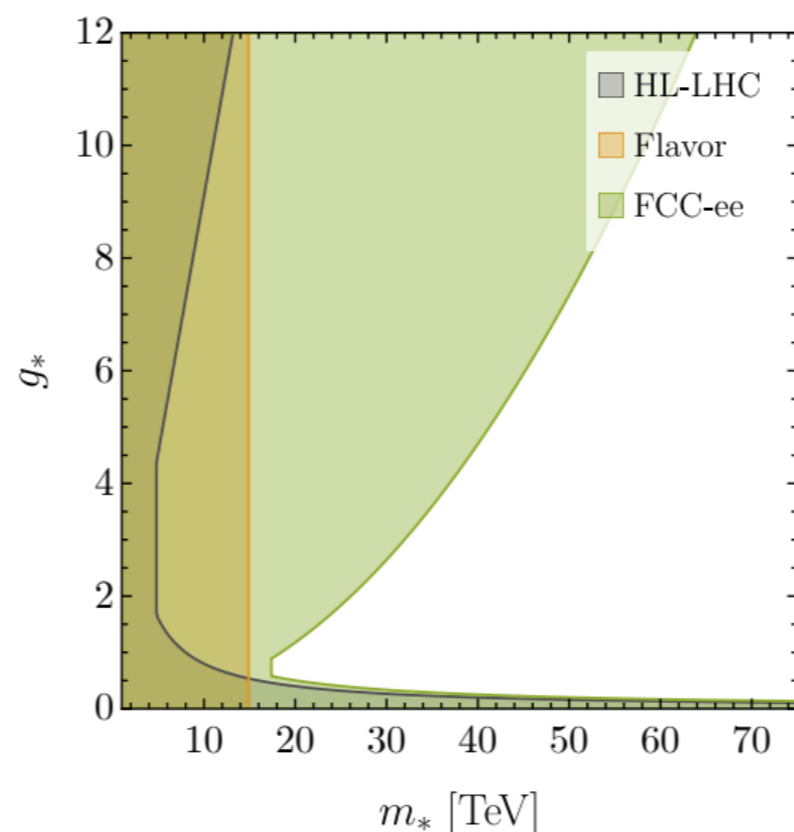$$c_1 = -1/2 \text{ and } c_2 = 0^*$$

[BAS, 2407.09593]

$^*\overline{\text{MS}}$ *for WCs, OSS for SM params*
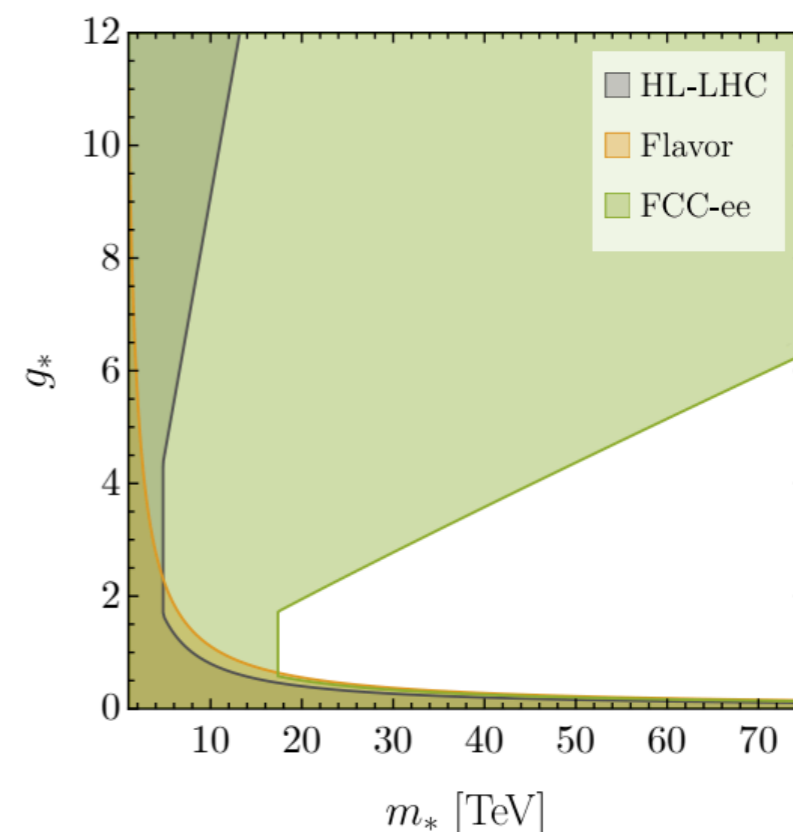
Future summary plots (with theory uncertainty)

- Flavor non-universal RG effects give the best bound for $g_* \gtrsim 1$, while universal effects are only better for $g_* < 1$. Interestingly: $\langle H \rangle \sim f = m_*/g_*$

(a) Left compositeness   (b) Mixed compositeness   (c) Right compositeness

Assuming:
$$[\Delta m_W]_{\text{Th}} \simeq 1 \text{ MeV},$$
$$[\Delta A_\ell]_{\text{Th}} \simeq 5 \times 10^{-5}$$

These absolute theoretical uncertainties are about a factor of 3 (2) larger than the projected absolute experimental error in the case of mW (Ae).

[BAS, 2407.09593]

Matching to composite Higgs model parameters

- The full UV Lagrangian can be written schematically as

$$\mathcal{L}_{\mathrm{UV}} = \mathcal{L}_{\mathrm{SM}'} + \mathcal{L}_{\mathrm{strong}} + g A_\mu^{\mathrm{SM}} J_{\mathrm{strong}}^\mu + \mathcal{L}_{\mathrm{mix}}(\psi, \mathcal{O}_\psi)$$

- After integrating out all heavy composite states, the low energy theory has the form

$$\mathcal{L}_{\mathrm{EFT}} = \mathcal{L}_{\mathrm{SM}'} + \frac{m_*^4}{g_*^2} \widehat{\mathcal{L}}_{\mathrm{EFT}} \left(\frac{g_* H}{m_*}, \frac{D_\mu}{m_*}, \frac{g F_{\mu\nu}}{m_*^2}, \frac{\lambda_L \bar{q}_L^3}{m_*^{3/2}}, \frac{\lambda_R \bar{t}_R}{m_*^{3/2}}, \frac{\lambda_q^i \bar{q}_L^i}{m_*^{3/2}}, \frac{g_*^2}{16\pi^2}, \frac{g}{16\pi^2} \right)$$

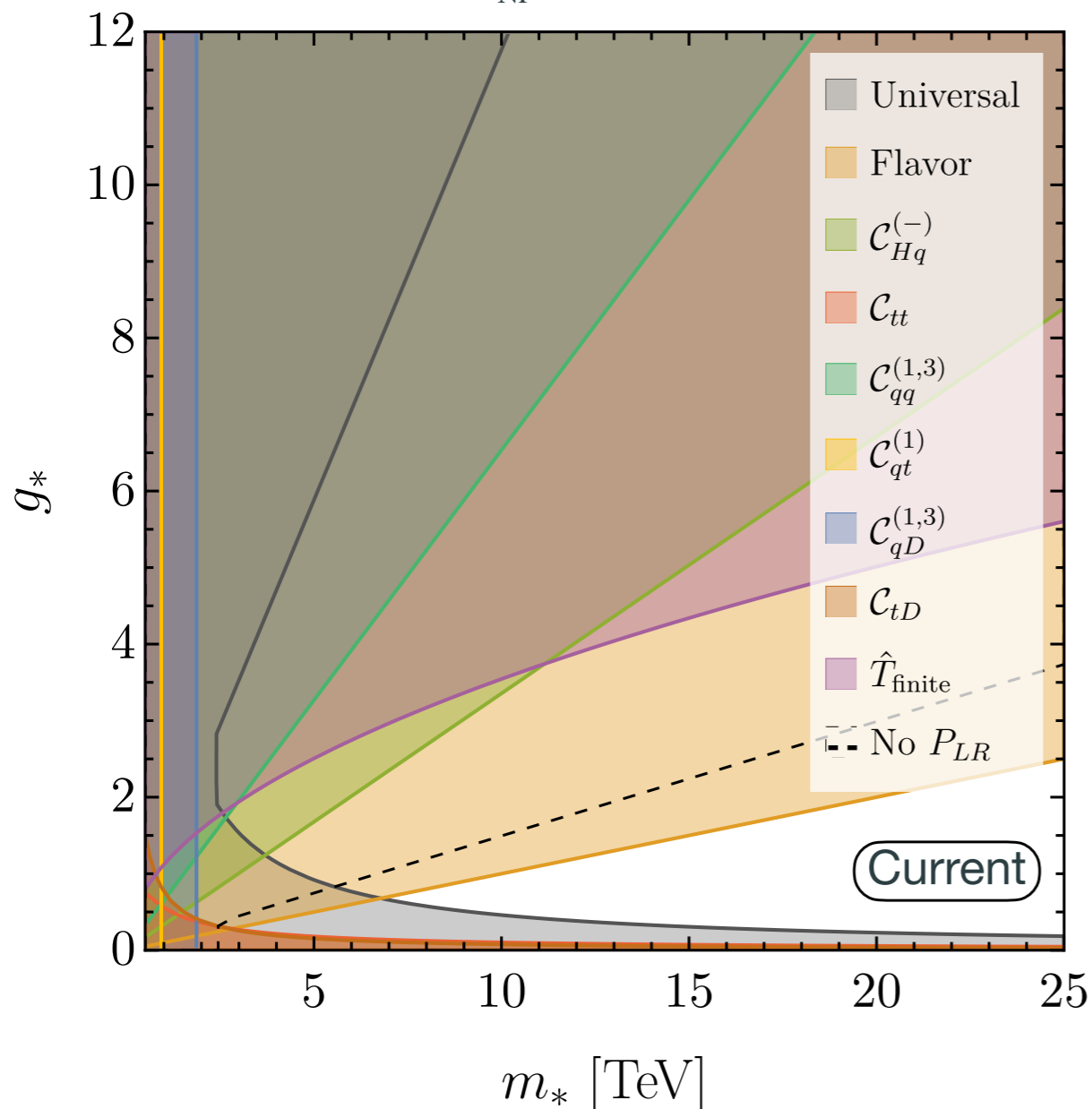- Let us write the WCs in terms of composite Higgs model parameters :

$$C_{Hq}^{(1)} (H^\dagger D_\mu H)(\bar{q}_L^3 \gamma_\mu q_L^3) \implies C_{Hq}^{(1)} \sim \frac{m_*^4}{g_*^2} \frac{g_*^2}{m_*^3} \frac{\lambda_L^2}{m_*^3} = \frac{\lambda_L^2}{m_*^2} = \frac{g_*^2}{m_*^2} \epsilon_L^2$$

$$C_{tt} (\bar{t}_R \gamma_\mu t_R)(\bar{t}_R \gamma_\mu t_R) \implies C_{tt} \sim \frac{m_*^4}{g_*^2} \frac{\lambda_R^4}{m_*^6} = \frac{\lambda_R^4}{g_*^2 m_*^2} = \frac{g_*^2}{m_*^2} \epsilon_R^4$$

[G. F. Giudice, C. Grojean, A. Pomarol, R. Rattazzi, hep-ph/0703164]

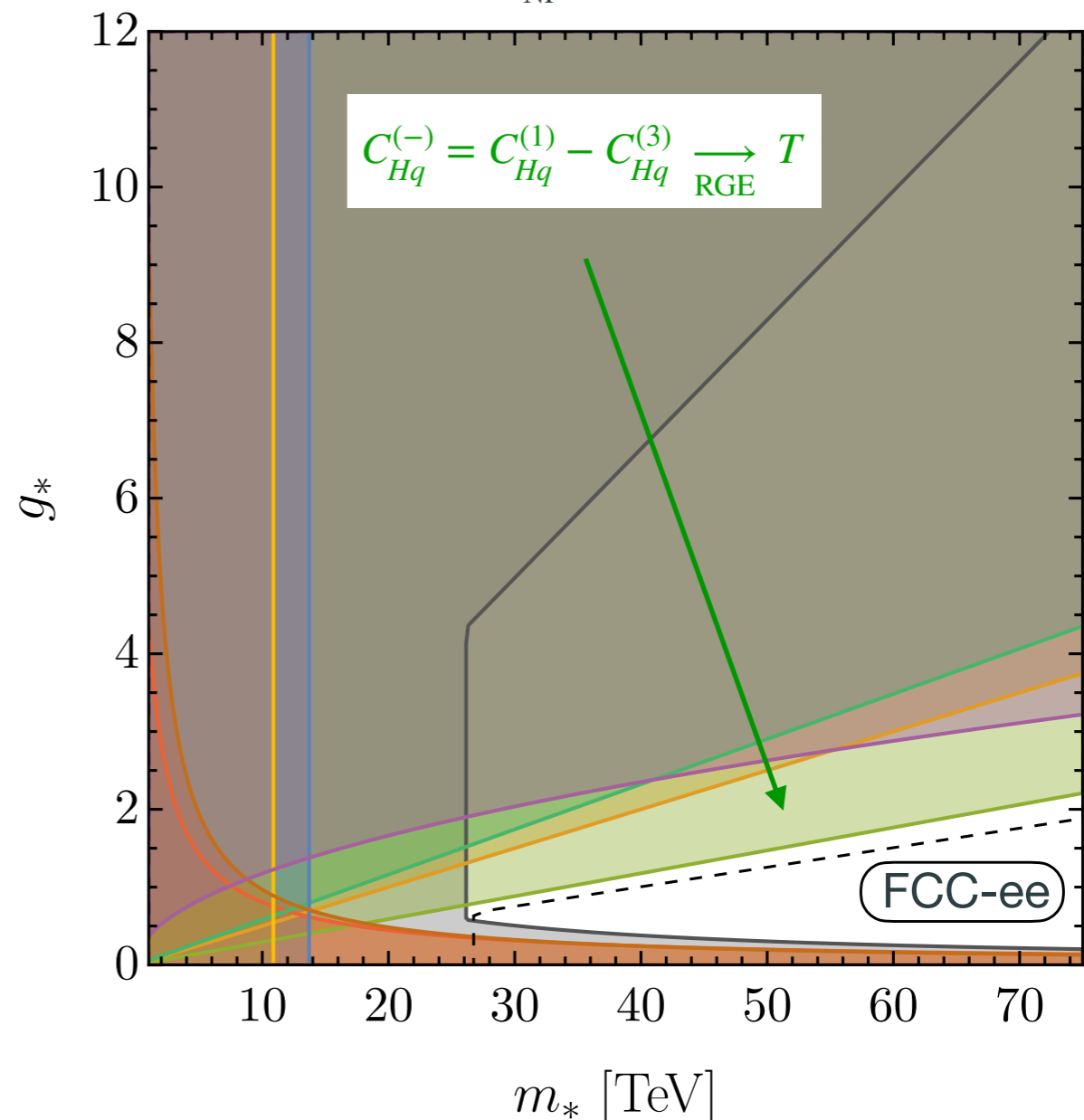$$(\lambda_{L,R} = g_* \, \epsilon_{L,R})$$

Left compositeness

- Left compositeness has $\epsilon_L = 1$, $\epsilon_R = y_t/g_*$.   Flavor constraints: $C_{B_s} \propto \dfrac{g_*^2}{m_*^2} \epsilon_L^4$

$(\Lambda_{NP} = 2.5 \text{ TeV})$ $(\Lambda_{NP} = 25 \text{ TeV})$

Legend:
- Universal
- Flavor
- $\mathcal{C}_{Hq}^{(-)}$
- $\mathcal{C}_{tt}$
- $\mathcal{C}_{qq}^{(1,3)}$
- $\mathcal{C}_{qt}^{(1)}$
- $\mathcal{C}_{qD}^{(1,3)}$
- $\mathcal{C}_{tD}$
- $\hat{T}_{\text{finite}}$
- No P_{LR}

$C_{Hq}^{(-)} = C_{Hq}^{(1)} - C_{Hq}^{(3)} \xrightarrow[\text{RGE}]{} T$

Current   FCC-ee

[BAS, 2407.09593]

Mixed compositeness

- Mixed compositeness has $\epsilon_L = \epsilon_R = \sqrt{y_t/g_*}$.　　Flavor constraints: $C_{B_s} \propto \dfrac{g_*^2}{m_*^2}\epsilon_L^4$
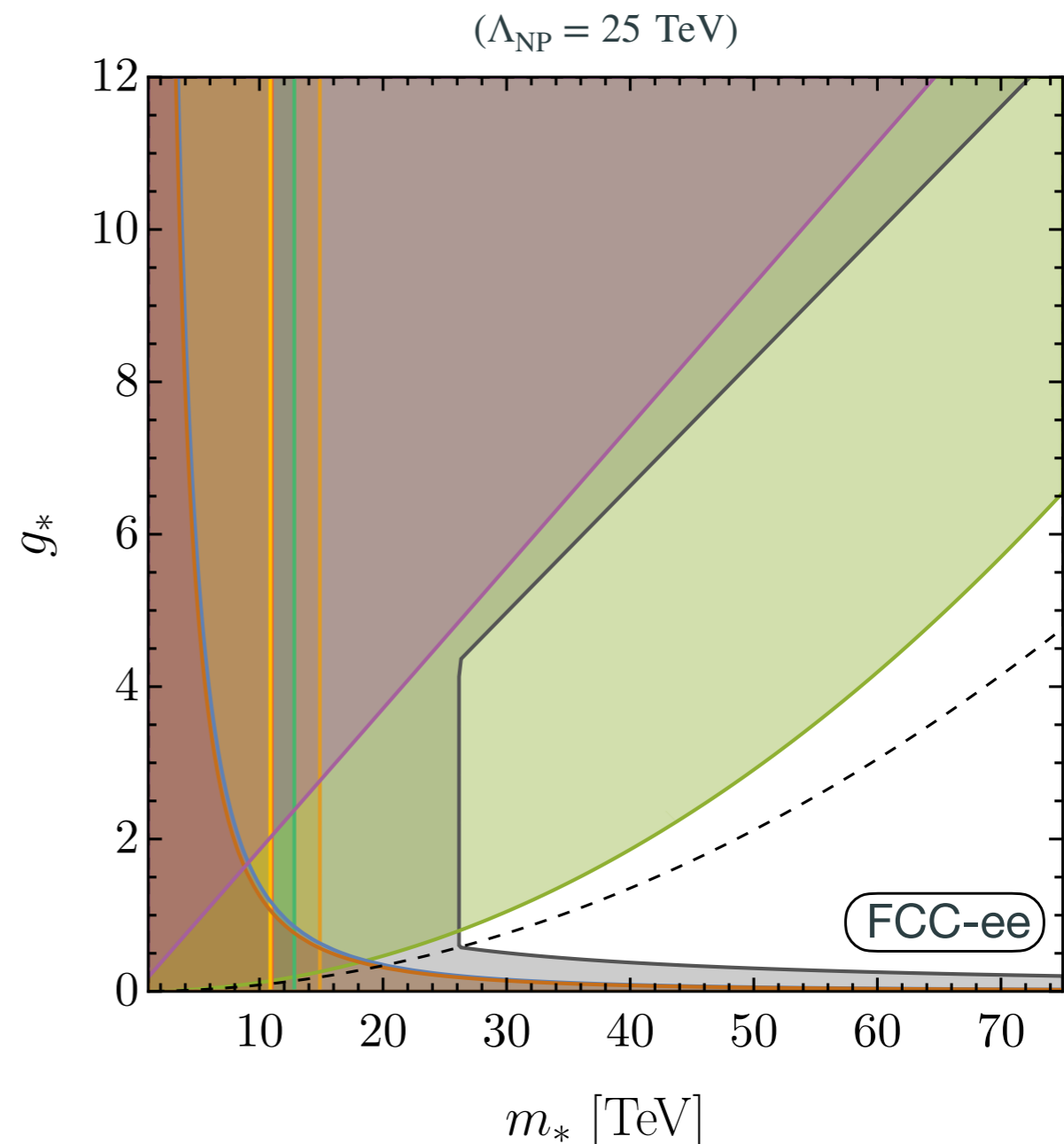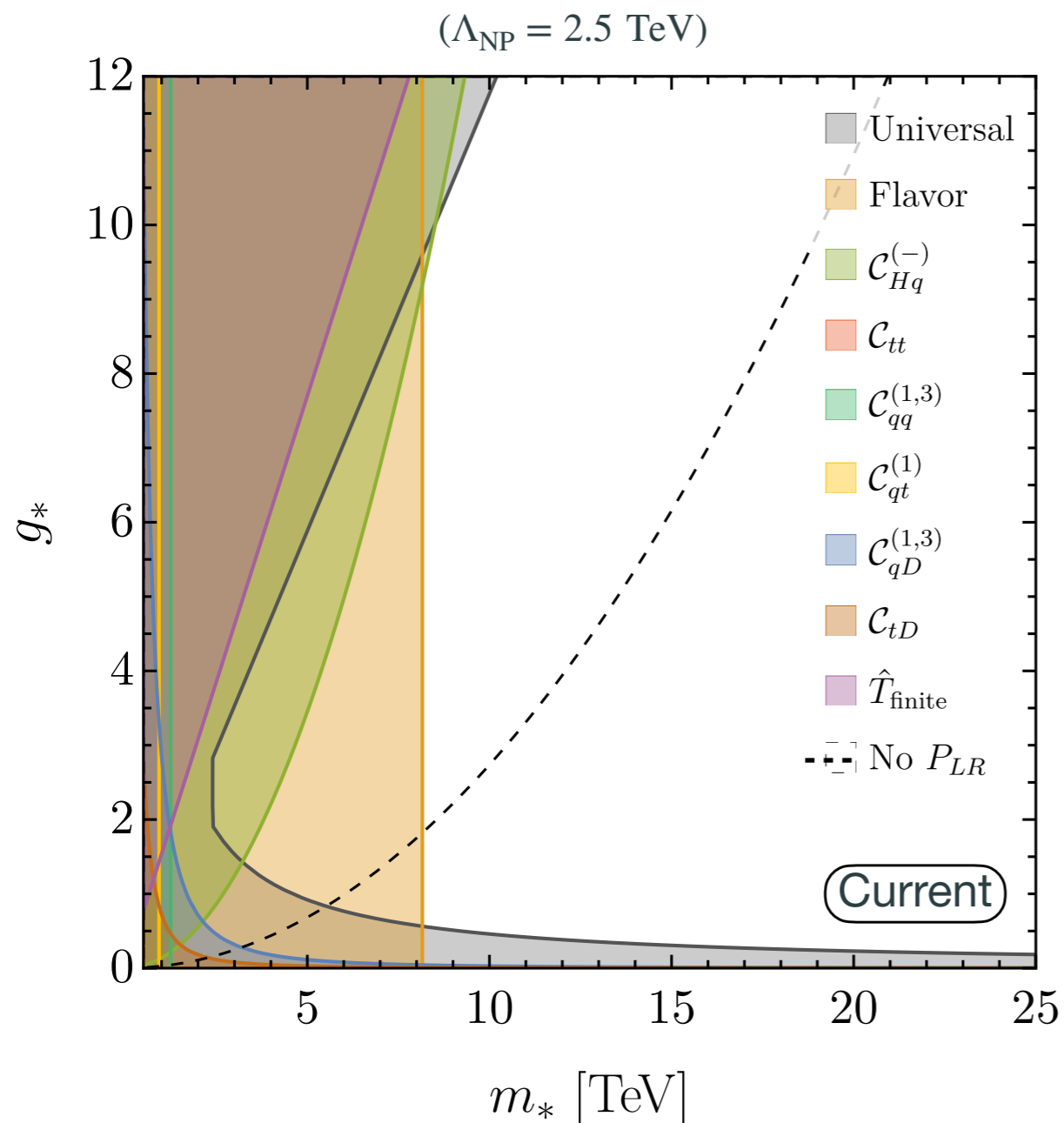

$(\Lambda_{\mathrm{NP}} = 2.5~\mathrm{TeV})$　　　　　　　$(\Lambda_{\mathrm{NP}} = 25~\mathrm{TeV})$

Legend:
- Universal
- Flavor
- $\mathcal{C}_{Hq}^{(-)}$
- $\mathcal{C}_{tt}$
- $\mathcal{C}_{qq}^{(1,3)}$
- $\mathcal{C}_{qt}^{(1)}$
- $\mathcal{C}_{qD}^{(1,3)}$
- $\mathcal{C}_{tD}$
- $\hat{T}_{\mathrm{finite}}$
- No P_{LR}

Current　　　FCC-ee

[BAS, 2407.09593]

What does a consistent SMEFT analysis look like?

- We are facing a mass gap. That means we should integrate out any heavy NP states at $\Lambda_{\mathrm{NP}} \gtrsim 1$ TeV and run down to the scale of the experiment to compare with data. For scale dependence to cancel (at leading log), we also need to compute observables at NLO in the SMEFT.

- The full 1-loop RG equations are known for the d6 SMEFT, and automated tools exist. 2-loop running is "coming soon". No excuse anymore to neglect running, but many global SMEFT fits still do.

- The EFT framework is the only viable way to resum large logarithms via the RG equations. Already the mass gap can be up to 3 orders of magnitude…

- Perhaps the most important point of this talk:

$$\dot{C}_i = \gamma_{ij} C_j \implies C_i(\mu_{\mathrm{EW}}) \neq C_i(\Lambda_{\mathrm{NP}})$$

E

Λ_{NP} — New physics

10^3 GeV — LHC data

SMEFT

10^2 GeV — EWPD

LEFT

$\sim$ GeV — Flavor data

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