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Constraint on initial conditions from non-linear causality

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Based on arXiv:2412.02405[nucl-th]. (To appear in PRC)

Introduction

Discovery of perfect fluidity announced in 2005



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Contact: Karen McNulty Walsh, (631) 344-8350, or Peter Genzer, (631) 344-3174

RHIC Scientists Serve Up 'Perfect' Liquid

New state of matter more remarkable than predicted - raising many new questions

April 18, 2005

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Precision QGP

spin/magneto hydrodynamics, Bayesian analysis,

QGP fluids as thermal media

thermal photon/dilepton jet quenching, heavy quark(onium) Validation of QGP fluidity

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Today's talk!



Validation through causality

Linearized 2nd order hydro under static equilibrium background $(\Pi = 0, \pi^{\mu\nu} = 0, u^{\mu} = 0)$

causality √

As long as large relaxation time

W.A. Hiscock, L. Lindblom, Annals of Physics 151, 466 (1983).

2nd order dissipative hydrodynamics in nonlinear regime causality ?

F.S. Bemfica et al., Phys. Rev. Lett. 126, 222301 (2021).

→Validity of fluid picture and early thermalization/hydrodynamization?



Conditions for nonlinear causality Necessary conditions: $0 \le v_c^2 \le 1$ v_c : characteristic velocity (under specific situation) Sufficient conditions: $g(v_c^2 > 1) > 0$ $g(v_c^2 < 0) < 0$ $g(v_c^2)$: third-degree polynomial

F.S. Bemfica et al., Phys. Rev. Lett. 126, 222301 (2021). See also Appendix B in T. Hoshino and TH, arXiv:2412.02405[nucl-th]

 $F_i(e, p, \Pi, \pi^{\mu\nu}, \eta, \zeta, \cdots) \ge 0$ <u>Purpose</u>: Scrutinize validation of hydrodynamic description from nonlinear causality in 1D expansion

Model

Equation of motion in 1D expansion

Balance eq.+ BRSSS eq. with boost invariant solutions

R. Baier *et al.*, JHEP **04**, 100 (2008). J.D. Bjorken, Phys. Rev. D **27**, 140 (1983).

$$\tau \frac{d}{d\tau} e = -e - p(e) + \phi$$

$$\tau_{\pi} \frac{d}{d\tau} \phi = \frac{4\eta}{3\tau} - \phi - \frac{4\tau_{\pi}}{3\tau} \phi + \frac{\lambda}{2\eta^2} \phi^2$$

e: energy density *p*: pressure $\phi = \pi^{00} - \pi^{33}$: shear pressure η: shear viscosity $τ_π$: relaxation time λ: 2nd order transport coefficient

Equation of state and transport coefficient

EoS 1: Conformal EoS (default)

$$p(e) = \frac{1}{3}e$$



EoS 2: Lattice EoS (see backup)

A. Bazavov et al., Phys. Rev. D 90, 094503 (2014).

Transport coefficients (AdS/CFT)

P. Kovtun et al., Phys. Rev. Lett. 94, 111601 (2005): R. Baier et al., JHEP 04, 100 (2008).

$$\frac{\eta}{s} = \frac{1}{4\pi}, \quad \tau_{\pi}T = \frac{2 - \ln 2}{2\pi}, \quad \frac{\lambda T}{\eta} = \frac{1}{2\pi}$$

Behavior of solutions





<u>Hydrodynamization</u> Attractor solution

Local equilibrium ($\phi = 0$)

Acceleration of hydrodynamization due to ϕ^2 term in EoM

Results



Necessary conditions in 1D expansion

$$\eta \ge 0 \qquad \frac{\eta}{\tau_{\pi}} \ge 0 \qquad e+p-\frac{\eta}{\tau_{\pi}} \ge 0$$
$$e+p-\frac{\phi}{\tau_{\pi}} \ge 0$$
$$e+p+\phi-\frac{\eta}{\tau_{\pi}} \ge 0$$
$$\left(e+p-\frac{\phi}{2}\right)c_{s}^{2} + \frac{4}{3}\left(-\frac{\phi}{2}\right) + \frac{4\eta}{3\tau_{\pi}} \ge 0 \qquad \left(e+p-\frac{\phi}{2}\right)(1-c_{s}^{2}) + \frac{2}{3}\phi - \frac{4\eta}{3\tau_{\pi}} \ge 0$$
$$\left(e+p+\phi\right)c_{s}^{2} + \frac{4}{3}\phi + \frac{4\eta}{3\tau_{\pi}} \ge 0 \qquad \left(e+p+\phi\right)(1-c_{s}^{2}) - \frac{4}{3}\phi - \frac{4\eta}{3\tau_{\pi}} \ge 0$$



12

Sufficient conditions in 1D expansion $\phi > 0$ case

$$e + p - \frac{\phi}{2} - \frac{\eta}{\tau_{\pi}} \ge 0$$
 $\left(e + p - \frac{\phi}{2}\right)c_s^2 - \frac{2}{3}\phi + \frac{\eta}{3\tau_{\pi}} \ge 0$

$$\frac{4}{3}\left(\phi + \frac{\eta}{\tau_{\pi}}\right) + \left(\frac{1}{2} + c_{s}^{2}\right)\phi + \frac{3c_{s}^{2}\phi^{2}}{e + p - \frac{\phi}{2} - \frac{\eta}{\tau_{\pi}}} \le (e + p)(1 - c_{s}^{2})$$

$$\left(\frac{\eta}{\tau_{\pi}}\right)^{2} - 3c_{s}^{2}\phi^{2} \ge 0$$

$$\left(e + p - \frac{\phi}{2}\right)c_{s}^{2} + \frac{4}{3}\left(-\frac{\phi}{2} + \frac{\eta}{\tau_{\pi}}\right) \ge \frac{(e + p + \phi)^{2}\left(e + p - \frac{\phi}{2} + \frac{2\eta}{\tau_{\pi}}\right)}{3\left(e + p - \frac{\phi}{2}\right)^{2}}$$



Sufficient conditions in 1D expansion $\phi < 0$ case

$$e + p - \phi - \frac{\eta}{\tau_{\pi}} \ge 0$$
 $(e + p + \phi)c_s^2 + \frac{4}{3}\phi + \frac{\eta}{3\tau_{\pi}} \ge 0$

$$\frac{4}{3}\left(-\frac{\phi}{2}+\frac{\eta}{\tau_{\pi}}\right) - \left(1+\frac{1}{2}c_{s}^{2}\right)\phi + \frac{3c_{s}^{2}\phi^{2}}{e+p+\phi-\frac{\eta}{\tau_{\pi}}} \leq (e+p)(1-c_{s}^{2})$$

$$\left(\frac{\eta}{\tau_{\pi}}\right)^{2} - 3c_{s}^{2}\phi^{2} \geq 0$$

$$(e+p+\phi)c_{s}^{2} + \frac{4}{3}\left(\phi+\frac{\eta}{\tau_{\pi}}\right) \geq \frac{\left(e+p-\frac{\phi}{2}\right)\left(e+p+\phi+\frac{2\eta}{\tau_{\pi}}\right)}{3(e+p+\phi)}$$



Constraint on inverse Reynolds number



Necessary conditions $-0.47 \le \frac{\phi}{e+p} \le 0.23$

Sufficient conditions $-0.07 \le \frac{\phi}{e+p} \le 0.07$

Inverse Reynolds number $Re^{-1} \equiv \frac{|\phi|}{e+p}$ \leftarrow constrained from nonlinear causality 14



Dynamical violation of causality





→ Necessity of nonequilibrium description



Constraint on initial conditions



 ${}^{\exists}\tau_{0,\min} \approx 5.3\tau_{\pi 0}$

 $e_{0,\min} \sim 10 \text{ GeV/fm}^3$ ($\tau_0 = 0.8 \text{ fm}$)



 $\tau_{0,\min} \sim 1 \text{ fm}, e_{0,\max} \sim 5 \text{ GeV/fm}^{3}$

 $\tau_{0,\min} \sim 0.7 \text{ fm}, e_{0,\max} \sim 20 \text{ GeV/fm}^3$

nyan *et al*.

(CMS),

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Pocket formulae of minimum initial time



Summary



We scrutinized the initial conditions in 1D expansion from nonlinear causality.

- Nonlinear causality constrains the inverse Reynolds number
 - $Re^{-1} < 0.23$ From necessary conditions $Re^{-1} < 0.07$ From sufficient conditions
- Available regions of initial conditions from nonlinear causality
 - No hope for hydrodynamization
 → Need nonequilibrium description
 - Insufficient to start from local equilibrium at early time
 - Existence of minimum time and maximum energy density with a help of Bjorken energy density



Results with lattice EoS



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Causality violation in transverse plane



Red: Acausal **Blue**: Causal

time

Violations predominate in the early stage and/or the edge region.

To demonstrate this in a much simpler system, e.g., boostinvariant system

C. Plumberg et al., Phys. Rev. C 105, L061901 (2022).

Characteristic velocity Hydro eqs. as quasi-linear PDE $A^{\alpha}(\Psi)\nabla_{\alpha}\Psi = F(\Psi)$ $\Psi = (e, u^{\mu}, \Pi, \pi^{0\mu}, \pi^{1\mu}, \pi^{2\mu}, \pi^{3\mu})^{\mathrm{T}}$

Characteristic eqs. det $(A^{\alpha}\xi_{\alpha}) = 0, \ \xi^{\alpha} = \nabla^{\alpha}\Phi(x)$

Normal vector of characteristic surface \rightarrow (Light-like or) space-like vector $\xi^{\alpha} = bu^{\alpha} + a^{\alpha}, \quad \xi \cdot \xi = b^2 + a \cdot a \leq 0$

Characteristic velocity $0 \le k(=-b^2/a \cdot a) \le 1, \quad 0 \le k = v_c^2 \le 1$

W.A. Hiscock and T.S. Olson, Phys. Lett. A 141, 125 (1989); F.S. Bemfica *et al.*, Phys. Rev. Lett. 126, 222301 (2021).



= const.

X

Is hydrodynamic description valid after all?



M.P. Heller and M. Spaliński, Phys. Rev. Lett. 115, 072501 (2015).

Hydrodynamic attractor solution
→ Is fluid dynamics far from equilibrium justified?
→ Are (almost) any initial conditions acceptable?

Purpose

Scrutiny of validation of hydrodynamic description from nonlinear causality



Conformal fluids in Bjorken expansion Balance eq. (Landau frame) and EoS

$$\partial_{\mu}T^{\mu\nu} = 0, \quad T^{\mu\nu} = eu^{\mu}u^{\nu} - P(g^{\mu\nu} - u^{\mu}u^{\nu}) + \pi^{\mu\nu}, \qquad P = e/3$$

Constitutive eq. (BRSSS eq. with relevant terms in Bjorken expansion

$$\tau_{\pi} D \pi^{\langle \mu \nu \rangle} + \pi^{\mu \nu} = 2 \eta \nabla^{\langle \mu} u^{\nu \rangle} - \frac{4}{3} \tau_{\pi} \theta \pi^{\mu \nu} + \frac{\lambda_{1}}{\eta^{2}} \pi^{\langle \mu}{}_{\rho} \pi^{\nu \rangle \rho}$$

 $\frac{d}{d\tau}e = -\frac{4}{3\tau}e + \frac{1}{\tau}\phi,$

R. Baier et al., JHEP 0804, 100 (2008).

Boost invariant flow
$$u^{\mu} = (\cosh \eta_s, 0, 0, \sinh \eta_s)$$

J.D. Bjorken, Phys. Rev. D 27, 140 (1983).

$$\left(1+\tau_{\pi}\frac{d}{d\tau}\right)\phi = -\frac{4\tau_{\pi}}{3\tau}\phi + \frac{4\eta}{3\tau}, \quad \phi = \pi^{00} - \pi^{33}$$
$$\Rightarrow P_{L} = \frac{e}{3} - \phi$$

*Ignore ϕ^2 term for the moment by putting $\lambda_1 = 0$ 25

Variable transformation "Conformal time": $w = \tau T$ "Equilibrium measure": $f = \frac{3}{2}\tau \frac{1}{w} \frac{dw}{d\tau}$

$$C_{\tau\pi}wf\frac{df}{dw} + 4C_{\tau\pi}f^2 + \left(\frac{2}{3}w - \frac{32}{9}C_{\tau\pi}\right)f - C_{\eta} + 4C_{\tau\pi} - \frac{3}{2}w = 0$$

Transport coefficients: $\eta = C_{\eta}s$, $\tau_{\pi} = \frac{C_{\tau\pi}}{T}$
MP Heller and M Spaliński Phys. Rev. Lett. **115**. 072501 (2015)

Note 1: In ideal hydrodynamics, $w \propto \tau^{2/3}$ from $T \propto \tau^{-1/3}$ Note 2: Different normalization employed for f



Attractor and repulsive line





Square of characteristic velocity



Acausality of the first order relativistic dissipative equations

The "first" order theories (a.la. Eckart/Landau-Lifshitz) \rightarrow Entropy current with the first order terms in dissipative currents ($s^{\mu} = s_0 u^{\mu} + q^{\mu}/T$)

Dispersion relation against linear perturbation

E.g.) Transverse mode ($\mathbf{k} \perp \mathbf{v}$): $\omega = -i \frac{\eta}{e+P} k^2$

Diffusive \rightarrow Infinite characteristic speed \rightarrow Acausal!



Causality in non-linear regime?

Causality of second order hydrodynamics under static equilibrium background in linear perturbation $\Pi = 0, \qquad \pi^{\mu\nu} = 0, \qquad u^{\mu} = 0$ bulk pressure shear stress four velocity See, e.g., W.A. Hiscock, L. Lindblom, Annals of Physics 151, 466 (1983). \rightarrow Effects of transport coefficients in modern second order constitutive eqs. ?

$$\delta_{\pi\pi}\pi^{\mu\nu}\theta, \qquad \tau_{\pi\pi}\pi^{\langle\mu}{}_{\alpha}\sigma^{\nu\rangle\alpha}, \qquad \lambda_{\pi\Pi}\Pi\sigma^{\mu\nu}$$

→ Need to go beyond linear regime to capture full nonlinearity of relativistic dissipative hydrodynamic equation



Conditions for non-linear causality

Quasi-linear PDE $A^{\alpha}(\Psi)\nabla_{\alpha}\Psi = F$

Characteristic eqs. det $(A^{\alpha}\xi_{\alpha}) = 0, \ \xi^{\alpha} = \nabla^{\alpha}\Phi(x)$

The system is causal if* <u>Condition 1</u>: The roots of characteristic equations $\xi^0 = \xi^0(\xi^i)$ are real. <u>Condition 2</u>: The normal vector ξ^{α} of a characteristic surface is space-like (or light-like) so that the surface $\Phi(x) = \text{const.}$ is time-like.



 $|\xi^{\alpha} = bu^{\alpha} + a^{\alpha}, \quad \xi \cdot \xi = b^2 + a \cdot a \le 0, \quad 0 \le k(=-b^2/a \cdot a) \le 1$



*There exists a mathematically rigorous definition of causality.

F.S. Bemfica *et al.*, Phys. Rev. Lett. **126**, 222301 (2021). 31

Derivation of equilibrium measure in conformal + boost invariant flow





Necessary conditions in DNMR

$$\begin{aligned} (2\eta + \lambda_{\pi\Pi}) - \frac{1}{2} \tau_{\pi\pi} |\Lambda_1| &\geq 0 \\\\ & \frac{1}{2\tau_{\pi}} (2\eta + \lambda_{\pi\Pi}\Pi) + \frac{\tau_{\pi\pi}}{4\tau_{\pi}} (\Lambda_a + \Lambda_a) \geq 0 \\\\ & e + P_s + \Pi - \frac{1}{2\tau_{\pi}} (2\eta + \lambda_{\pi\Pi}\Pi) - \frac{\tau_{\pi\pi}}{4\tau_{\pi}} \Lambda_3 \geq 0 \\\\ & e + P_s + \Pi + \Lambda_a - \frac{1}{2\tau_{\pi}} (2\eta + \lambda_{\pi\Pi}\Pi) - \frac{\tau_{\pi\pi}}{4\tau_{\pi}} (\Lambda_d + \Lambda_a) \\\\ & \frac{1}{2\tau_{\pi}} (2\eta + \lambda_{\pi\Pi}\Pi) + \frac{\tau_{\pi\pi}}{2\tau_{\pi}} \Lambda_d + \frac{1}{6\tau_{\pi}} [2\eta + \lambda_{\pi\Pi}\Pi + (6\delta_{\pi\pi} - \tau_{\pi\pi})\Lambda_d] + \frac{\zeta + \delta_{\Pi\Pi}\Pi + \lambda_{\Pi\pi}\Lambda_d}{\tau_{\pi}} + (e + P_s + \Pi + \Lambda_d)c_s^2 \geq 0 \\\\ & e + P_s + \Pi + \Lambda_d - \frac{1}{2\tau_{\pi}} (2\eta + \lambda_{\pi\Pi}\Pi) - \frac{\tau_{\pi\pi}}{2\tau_{\pi}} \Lambda_d - \frac{1}{6\tau_{\pi}} [2\eta + \lambda_{\pi\Pi}\Pi + (6\delta_{\pi\pi} - \tau_{\pi\pi})\Lambda_d] - \frac{\zeta + \delta_{\Pi\Pi}\Pi + \lambda_{\Pi\pi}\Lambda_d}{\tau_{\pi}} - (e + P_s + \Pi + \Lambda_d)c_s^2 \geq 0 \end{aligned}$$

F.S. Bemfica *et al.*, Phys. Rev. Lett. **126**, 222301 (2021).



Sufficient conditions in DNMR

 $\tau_{\pi\pi} \leq 6\delta_{\pi\pi}$ $(e + P_s + \Pi - |\Lambda_1|) - \frac{1}{2\tau_-}(2\eta + \lambda_{\pi\Pi}\Pi) - \frac{\tau_{\pi\pi}}{2\tau_-}\Lambda_3 \ge 0$ $(2\eta + \lambda_{\pi\Pi}\Pi) - \tau_{\pi\pi}|\Lambda_1| > 0$ $\frac{\lambda_{\Pi\pi}}{\tau_{\Pi}} + c_s^2 - \frac{\tau_{\pi\pi}}{12\tau} \ge 0$ $1 \ge \frac{\frac{12\delta_{\pi\pi} - \tau_{\pi\pi}}{12\tau_{\pi}} \left(\frac{\lambda_{\Pi\pi}}{\tau_{\Pi}} + c_{s}^{2} - \frac{\tau_{\pi\pi}}{12\tau_{\pi}}\right) (\Lambda_{3} + |\Lambda_{1}|)^{2}}{\left[\frac{1}{2\tau} (2\eta + \lambda_{\pi\Pi}\Pi) - \frac{\tau_{\pi\pi}}{2\tau} |\Lambda_{1}|\right]^{2}}$ $\frac{1}{6\tau} \frac{[2\eta + \lambda_{\pi\Pi}\Pi + (\tau_{\pi\pi} - 6\delta_{\pi\pi})|\Lambda_1|] + \frac{\zeta + \delta_{\Pi\Pi}\Pi - \lambda_{\Pi\pi}|\Lambda_1|}{\tau_{\Pi}} + (e + P_s + \Pi - |\Lambda_1|)c_s^2 \ge 0$ $\frac{1}{3\tau_{\pi}}[4\eta + 2\lambda_{\pi\Pi}\Pi + (3\delta_{\pi\pi})\Lambda_{3}] + \frac{\zeta + \delta_{\Pi\Pi}\Pi + \lambda_{\Pi\pi}\Lambda_{3}}{\tau_{\pi}} + |\Lambda_{1}| + \Lambda_{3}c_{s}^{2} + \frac{\frac{12\delta_{\pi\pi} - \tau_{\pi\pi}}{12\tau_{\pi}}\left(\frac{\lambda_{\Pi\pi}}{\tau_{\Pi}} + c_{s}^{2} - \frac{\tau_{\pi\pi}}{12\tau_{\pi}}\right)(\Lambda_{3} + |\Lambda_{1}|)^{2}}{e + P_{s} + \Pi - |\Lambda_{1}| - \frac{1}{2\tau_{\pi}}(2\eta + \lambda_{\pi\Pi}\Pi) - \frac{\tau_{\pi\pi}}{2\tau_{\pi}}\Lambda_{3}} \le (e + P_{s} + \Pi)(1 - c_{s}^{2})$ $\frac{1}{3\tau_{\pi}} [4\eta + 2\lambda_{\pi\Pi}\Pi - (3\delta_{\pi\pi} + \tau_{\pi\pi}|\Lambda_{1}|)] + \frac{\zeta + \delta_{\Pi\Pi}\Pi - \lambda_{\Pi\pi}|\Lambda_{1}|}{\tau_{\Pi}} + (e + P_{s} + \Pi - |\Lambda_{1}|)c_{s}^{2} \ge \frac{(e + P_{s} + \Pi + \Lambda_{2})(e + P_{s} + \Pi + \Lambda_{3})}{3(e + P_{s} + \Pi - |\Lambda_{1}|)} \begin{cases} 1 + \frac{2\left[\frac{1}{2\tau_{\pi}}(2\eta + \lambda_{\pi\Pi}\Pi) + \frac{\tau_{\pi\pi}}{2\tau_{\pi}}\Lambda_{3}\right]}{e + P_{s} + \Pi - |\Lambda_{1}|} \end{cases}$ F.S. Bemfica et al., Phys. Rev. Lett. 126, 222301 (2021). 34