

# **Study of the QCD Phase Structure in High-Energy Nuclear Collisions**

**Nu Xu**

# Outline

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## 1) Introduction

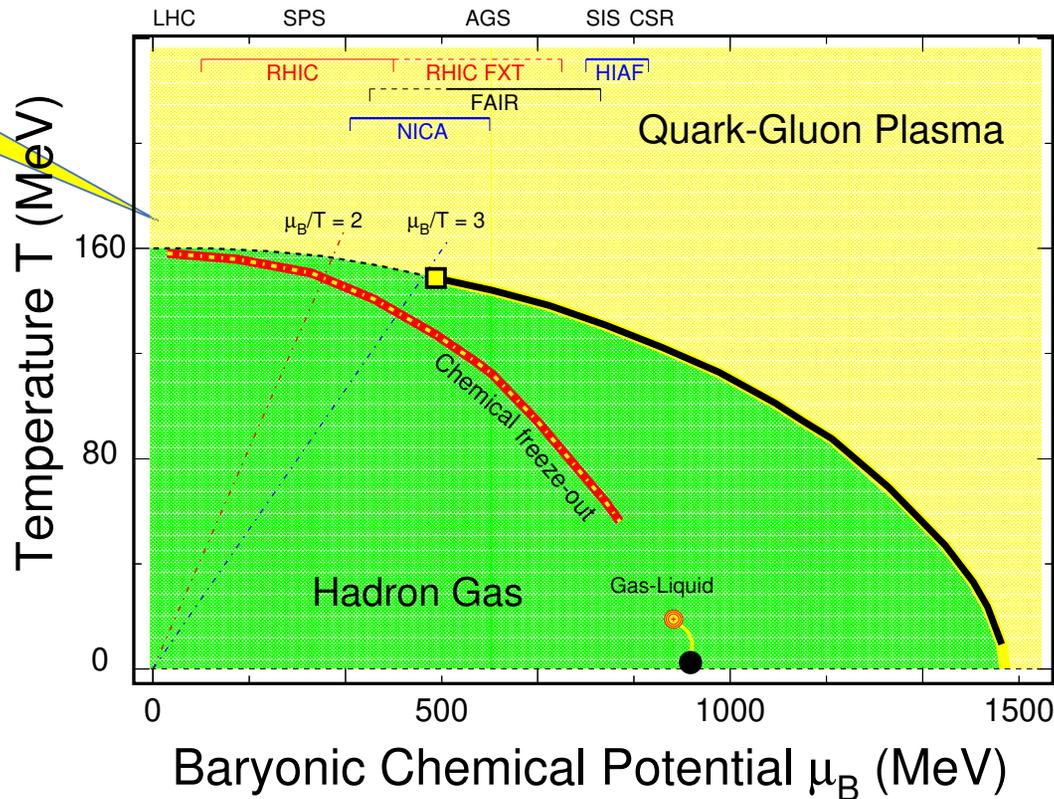
## 2) Selected Recent Results

- Collectivity and Baryon Correlation from FXT
- Criticality from BES-II (collider)

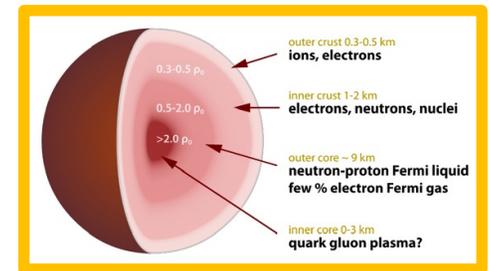
## 3) Summary

# Nuclear Collisions and QCD Phase Diagram

Early Universe

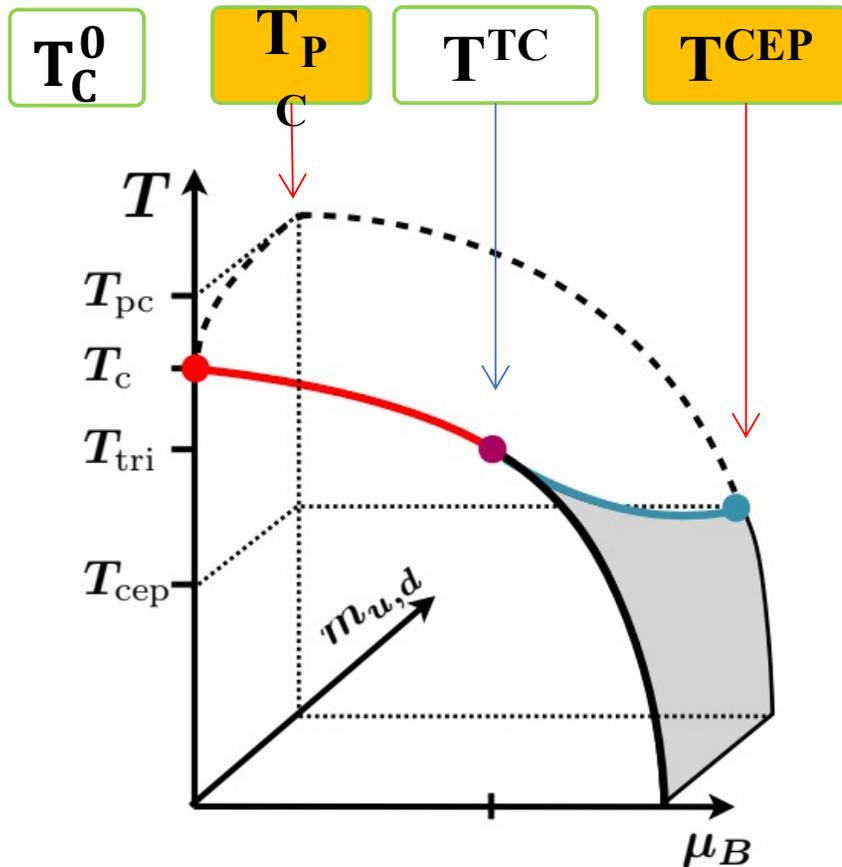


High baryon density:  
Inner structure of compact stars



- 1) RHIC BES: → search for 1<sup>st</sup>-order phase transition and **QCD critical point**;
- 2) Baryon interactions (e.g.  $N - N$ ,  $Y - N$ ) → inner structure of compact stars

# LGT Calculation: QCD Phase Structure



F. Karsch *et al.*, 2020

1) QCD transition temperature:

$$T_{PC} = 156.5 \pm 1.5 \text{ MeV}$$

2) Chiral crossover line

$$T_{PC}(\mu_B) = T_{PC}^0 \left[ 1 - \kappa_2 \left( \frac{\mu_B}{T_{PC}^0} \right)^2 - \kappa_4 \left( \frac{\mu_B}{T_{PC}^0} \right)^4 \right]$$

$$\kappa_2 = 0.012(4), \quad \kappa_4 = 0.00(4)$$

3) Chiral transition temperature:

$$T_C = 132_{-6}^{+3} \text{ MeV}$$

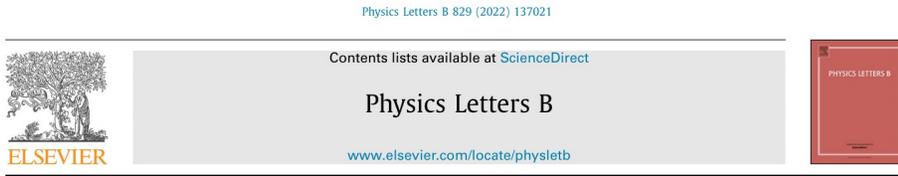
4) QCD critical end point:

$$T^{CEP} < T_C, \quad \mu_B^{CEP} \gtrsim 3T_C$$

HotQCD: Phys.Lett.**B795**, 15(2019);  
Phys. Rev. Lett. **123**, 062002(2019)

# Thermalization in Heavy-Ion Collisions

S. Gupta, **D. Mallick** *et al.* Phys. Lett. **B829**, (2022) 137021

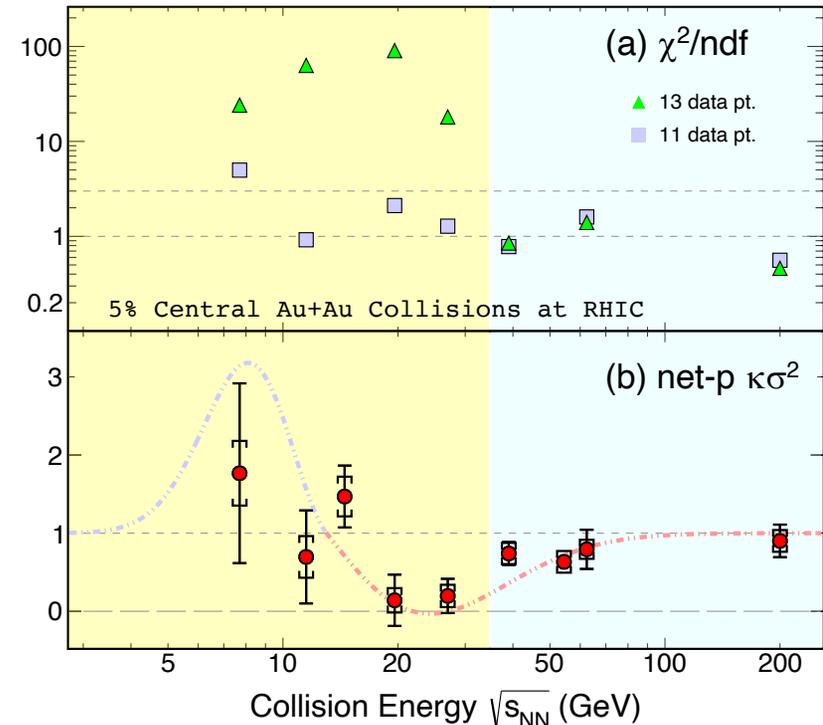
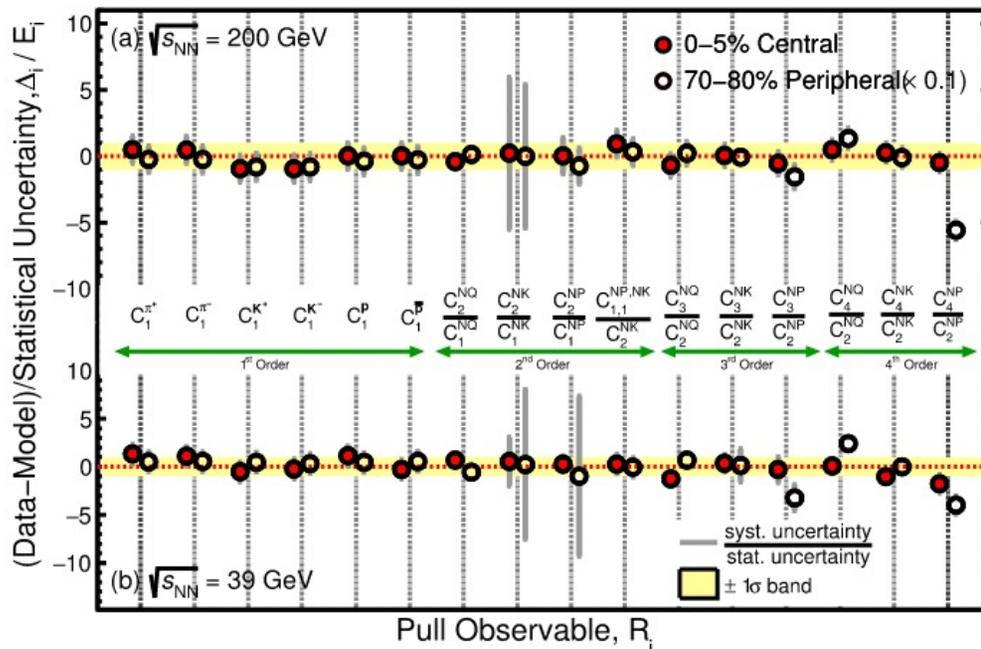


Limits of thermalization in relativistic heavy ion collisions

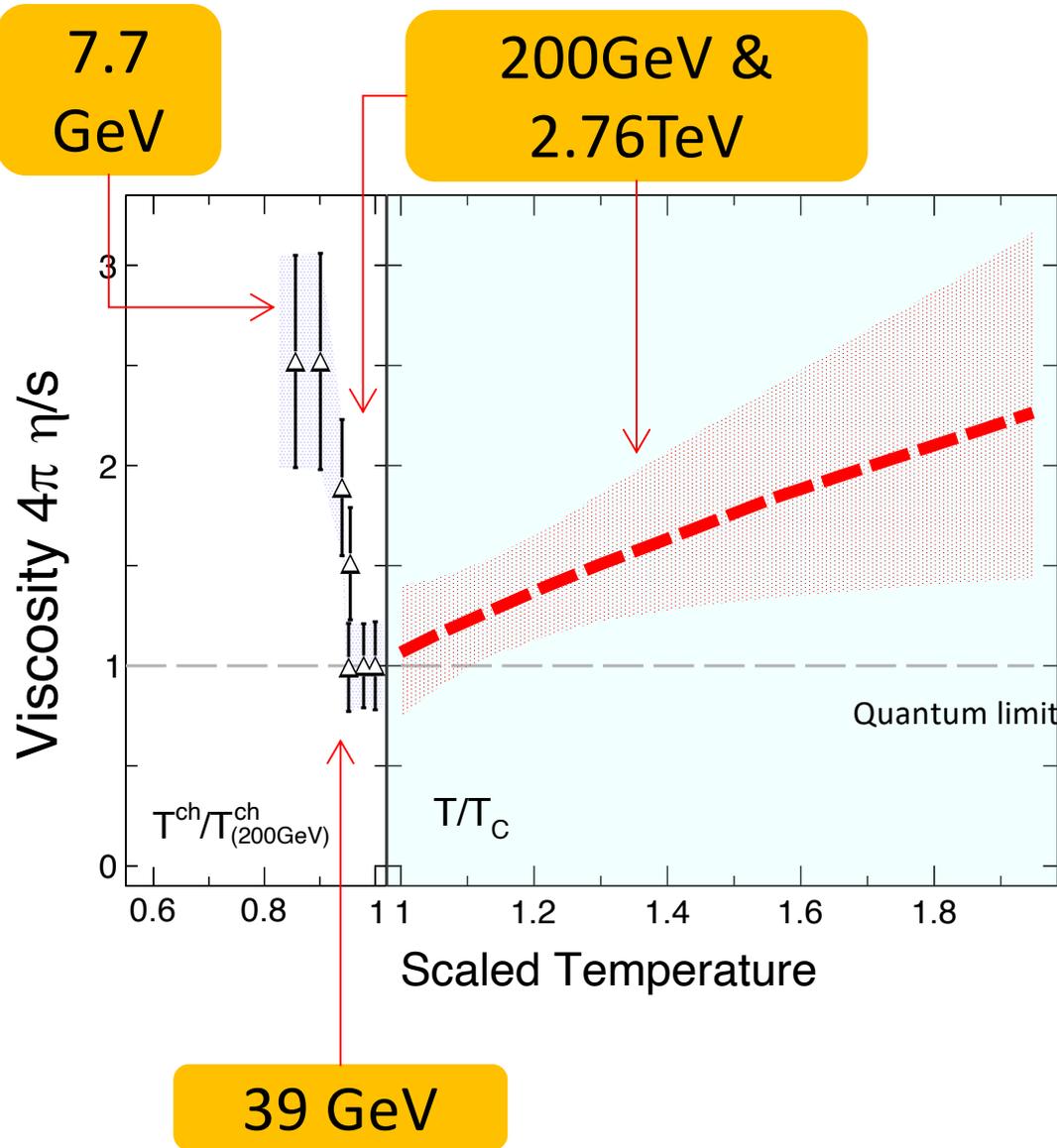
Sourendu Gupta<sup>a</sup>, Debasish Mallick<sup>b,c</sup>, Dipak Kumar Mishra<sup>d</sup>, Bedangadas Mohanty<sup>b,c,\*</sup>, Nu Xu<sup>e</sup>



- 1) Test of the thermal model with high moments data: 4<sup>TH</sup> order;
- 2) Below 39 GeV, **data is not consistent with equilibrium.**



# Equation of State for Strong Interaction



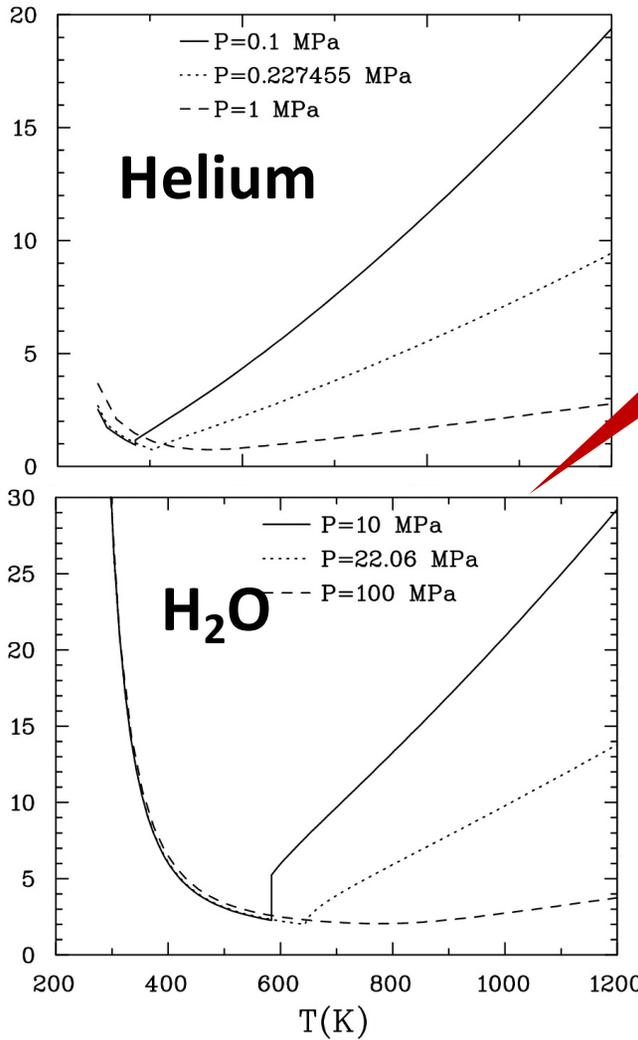
- 1) Left-plot: Energy dependence of  $\eta/s$  extracted from light-flavor hadron  $v_2$  and  $v_3$ . Right-plot: extracted from Bayesian fits to  $R_{AA}$  and  $v_2$  at 200 GeV collisions;
- 2) Both sides meet at the unity of the scaled temperature;
- 3) The values of  $\eta/s$  increase quickly below  $\sqrt{s_{NN}} = 39$  GeV  $\rightarrow$  QGP dominants in higher energies;

## 4) Evidence of the QCD transition!

- 1) L.P. Csernai, J.I. Kapusta, L.D. McLerran, PRL **97** (2006) 152303
- 2) X.Dong, Y.J. Lee & R.Rapp, ARNPS, **69** (2019) 417
- 3) J.E.Bernhard, J.S.Moreland & S. Bass, Nat. Phys. **15** (2015) 1113
- 4) I. Karpenko, P. Huovinen, H. Petersen, and M. Bleicher, Phys.Rev. **C91**, 064901 (2015).
- 5) G.Nijs, W.van der Schee, U. Gürsoy and R. Snellings, PRL **126**, (2021) 202301

# Strongly-Interacting Low-Viscosity Matter

Viscosity over Entropy Ratio  $\eta/s$

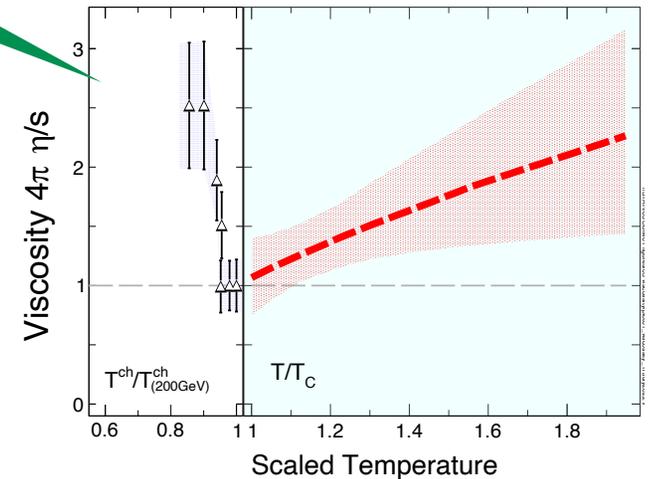
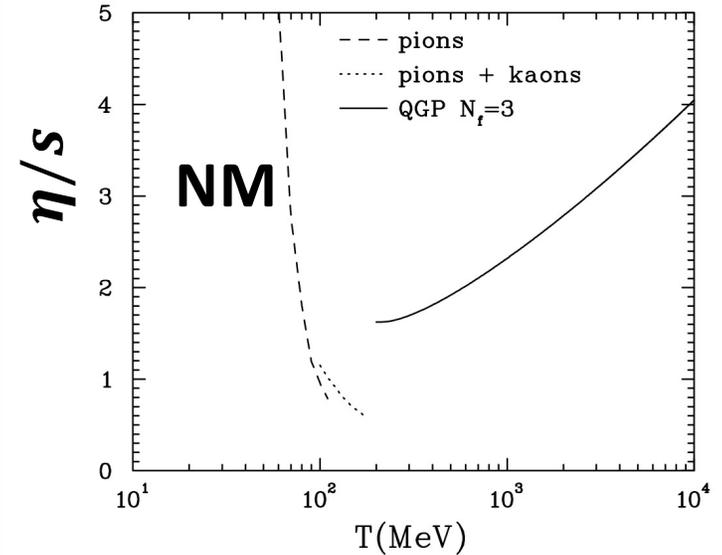


L.P. Csernai, J.I. Kapusta,  
L.D. McLerran, PRL **97** (2006)  
152303

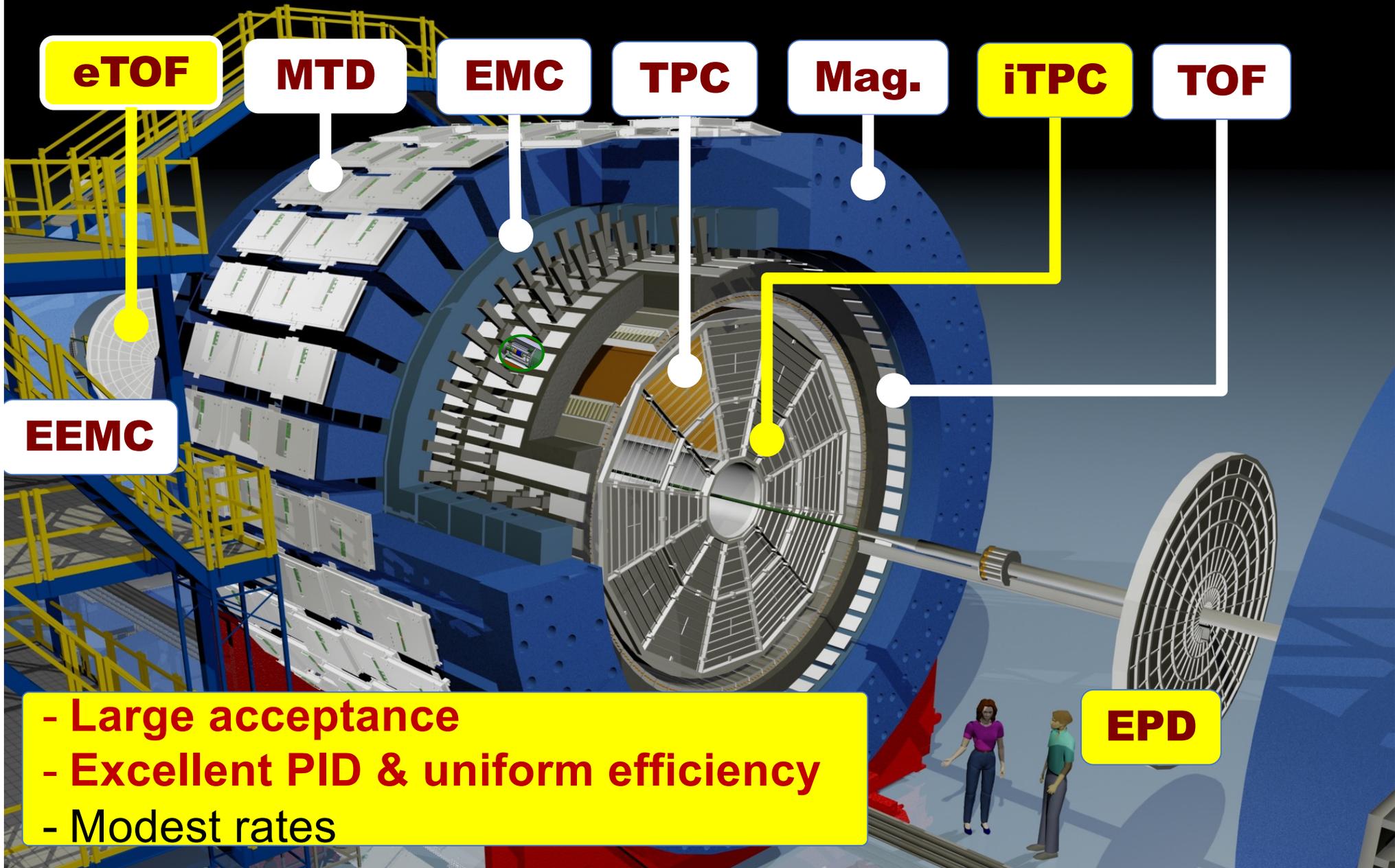
**EM interaction**  
 $\eta/s \sim 1$

**Strong Interaction**  
 $\eta/s \sim 0.1$

- QGP matter in  $\sqrt{s_{NN}} \geq 39$  GeV collisions!
- Universal behavior for the QCD phase transition!



# STAR DETECTOR SYSTEM



**eTOF**

**MTD**

**EMC**

**TPC**

**Mag.**

**iTPC**

**TOF**

**EEMC**

**EPD**

- Large acceptance
- Excellent PID & uniform efficiency
- Modest rates

# Major Upgrades for BES-II



## iTPC:

- Improves  $dE/dx$
- Extends  $\eta$  coverage from 1.0 to 1.6
- Lowers  $p_T$  cut-in from 125 to 60 MeV/c
- Ready in 2019



## eTOF:

- Forward rapidity coverage
- PID at  $\eta = 0.9$  to 1.6
- **Borrowed from CBM-FAIR**
- Ready in 2019



## EPD:

- Improves trigger
- Better centrality & event plane measurements
- Ready in 2018

- 1) Enlarge rapidity acceptance
- 2) Improve particle identification
- 3) Enhance centrality/event plane resolution**

iTPC: <https://drupal.star.bnl.gov/STAR/starnotes/public/sn0619>

eTOF: STAR and CBM eTOF group, arXiv: 1609.05102

EPD: J. Adams, et al. NIM **A968**, 163970 (2020)



# STAR BES-I and BES-II Data Sets

## Au+Au Collisions at RHIC

Collider Runs						Fixed-Target Runs					
	$\sqrt{s_{NN}}$ (GeV)	#Events	$\mu_B$	$y_{beam}$	run		$\sqrt{s_{NN}}$ (GeV)	#Event s	$\mu_B$	$y_{beam}$	run
1	200	380 M	25 MeV	5.3	Run-10, 19	1	13.7 (100)	50 M	280 MeV	-2.69	Run-21
2	62.4	46 M	75 MeV		Run-10	2	11.5 (70)	50 M	320 MeV	-2.51	Run-21
3	54.4	1200 M	85 MeV		Run-17	3	9.2 (44.5)	50 M	370 MeV	-2.28	Run-21
4	39	80 M	112 MeV		Run-10	4	7.7 (31.2)	260 M	420 MeV	-2.1	Run-18, 19, 20
5	27	585 M / 220	156 MeV	3.36	Run-11, 18	5	7.2 (26.5)	470 M	440 MeV	-2.02	Run-18, 20
6	19.6	595 M / 270 M	206 MeV	3.1	Run-11, 19	6	6.2 (19.5)	120 M	490 MeV	1.87	Run-20
7	17.3	256 M / 116 M	230 MeV		Run-21	7	5.2 (13.5)	100 M	540 MeV	-1.68	Run-20
8	14.6	340 M / 145 M	262 MeV		Run-14, 19	8	4.5 (9.8)	110 M	500 MeV	1.52	Run-20
9	11.5	257 M / 110 M	316 MeV		Run-10, 20	9	3.9 (7.3)	120 M	633 MeV	-1.37	Run-20
10	9.2	160 M / 78 M	372 MeV		Run-10, 20	10	3.5 (5.75)	120 M	670 MeV	-1.2	Run-20
11	7.7	104 M / 45 M	420 MeV		Run-21	11	3.2 (4.59)	200 M	699 MeV	-1.13	Run-19
						12	3.0 (3.85)	260 + 2000 M	760 MeV	-1.05	Run-18, 21

Most precise data to map the QCD phase diagram

$$3 < \sqrt{s_{NN}} < 200 \text{ GeV}; \quad 760 > \mu_B > 25 \text{ MeV}$$

# Outline

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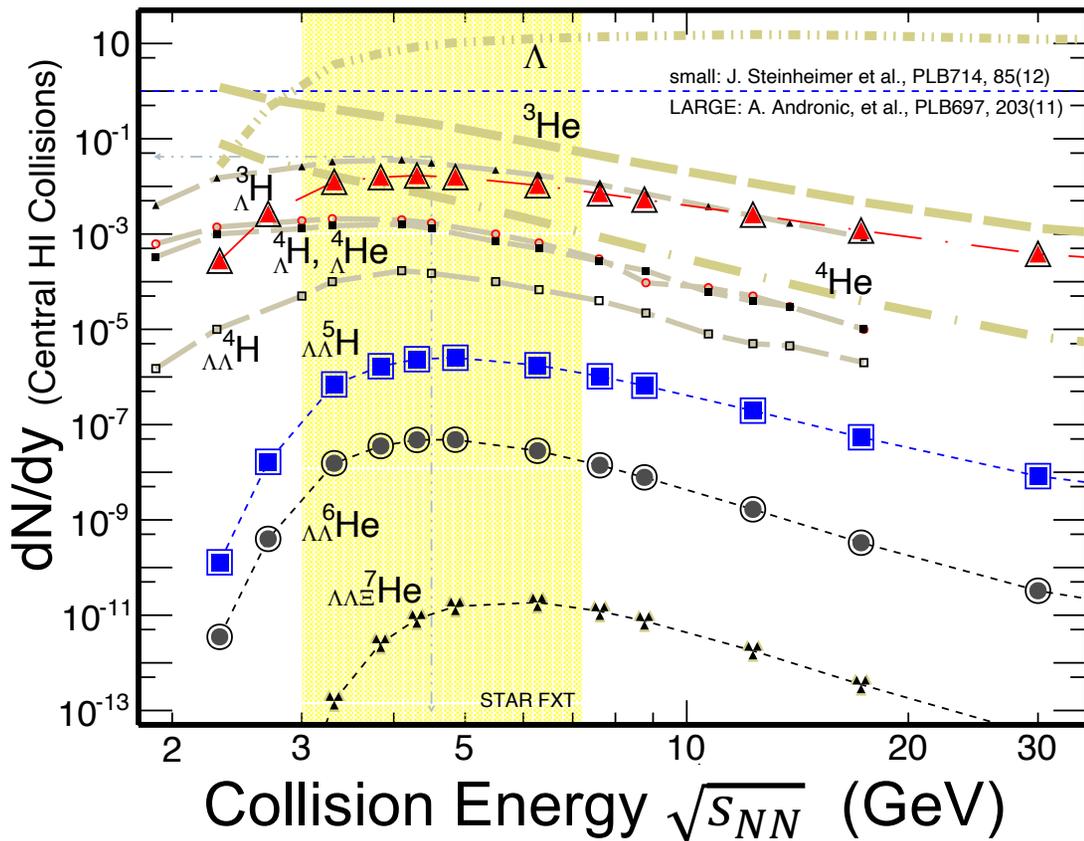
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- Collectivity and Baryon Correlation from FXT
- Criticality from BES-II (collider)

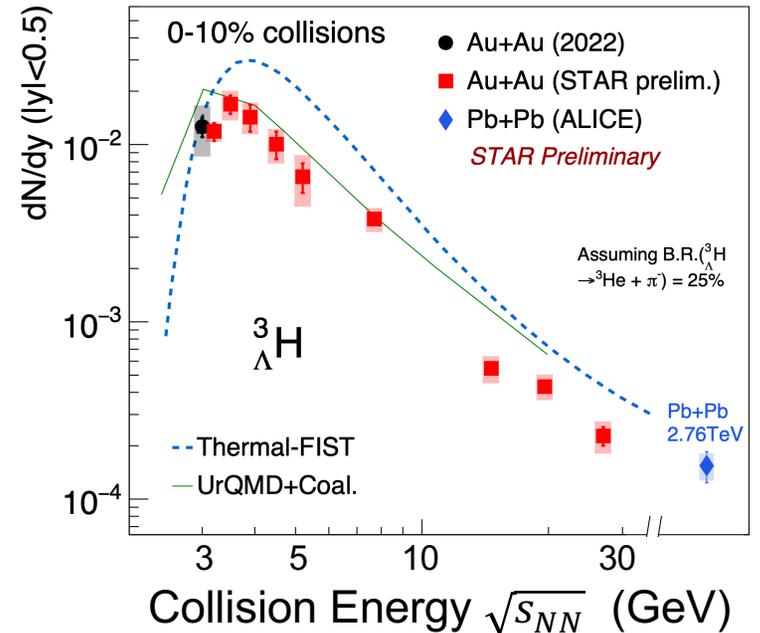
## 3) Summary

# STAR FXT Program and High Baryon Density Region

A. Andronic *et al.* PLB697, 203(2011);  
J. Steinheimer *et al.* PLB714, 85(2012)



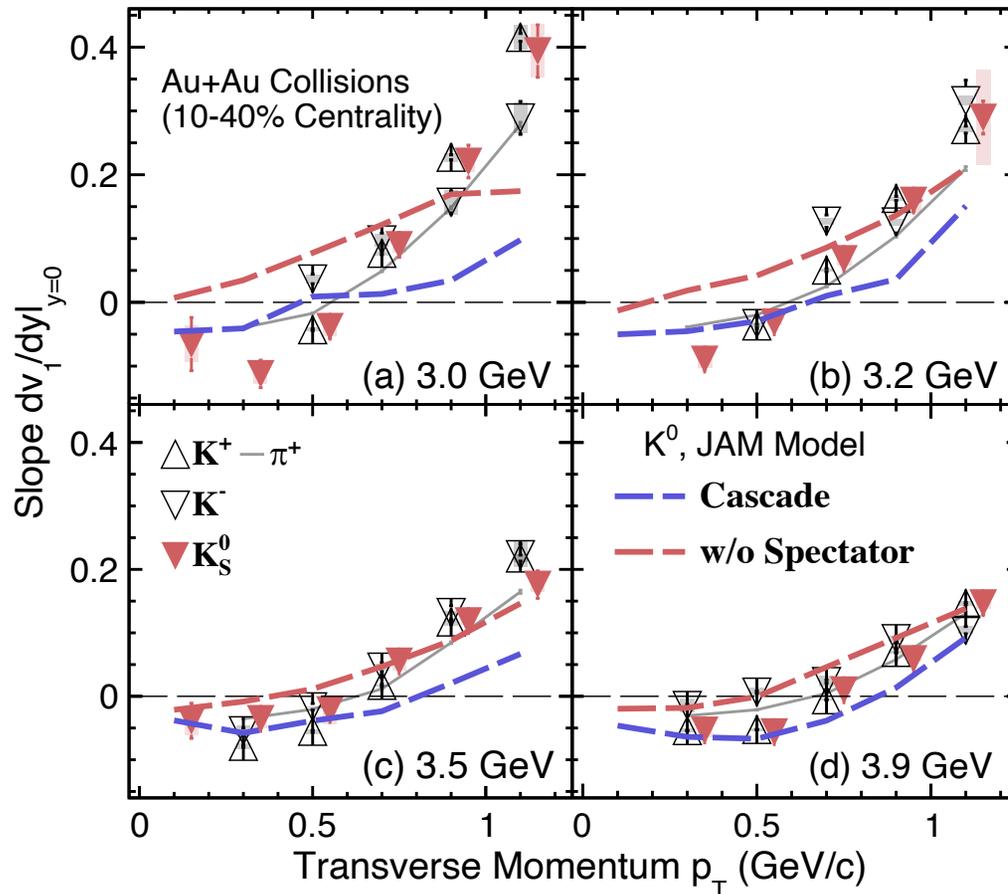
STAR: CPOD2024,  
SQM2024



- 1) Hypernucleus:  ${}^3_{\Lambda}H$  yields versus energy: peaks at 3.2 GeV;
- 2) For  $\sqrt{s_{NN}} < 10$  GeV, calculations from coalescence more consistent with data

# Kaon Anti-Flow at High Baryon Density Region

STAR: CPOD2024,  
SQM2024



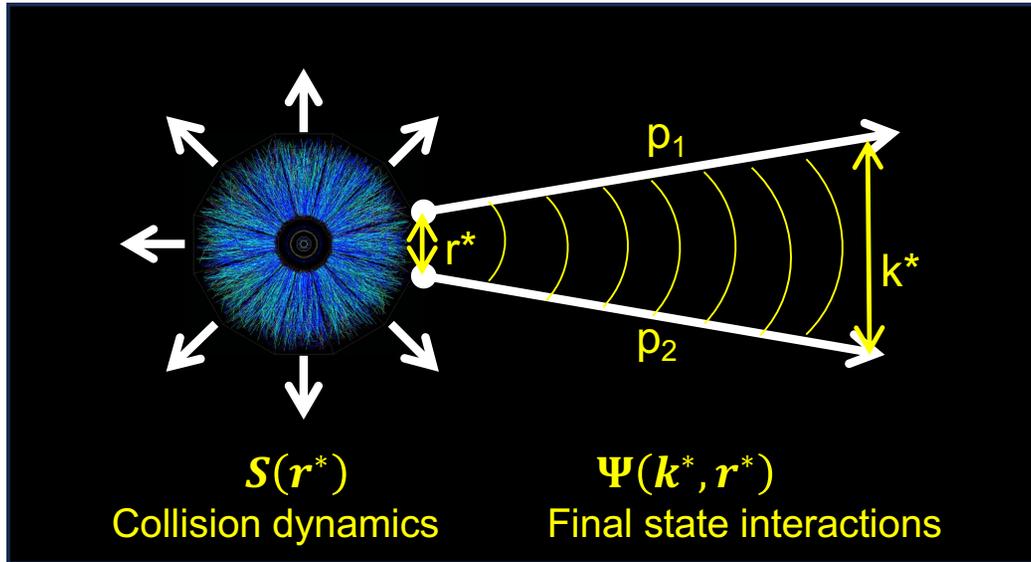
- 1) A systematic analysis of the  $p_T$  dependence of the neutral- and charged-Kaon  $v_1$  from Au+Au collisions at  $\sqrt{s_{NN}} = 3.0 - 3.9$  GeV;
- 2) At  $p_T < 0.6$  GeV, all mid-rapidity  $v_1$  slopes are negative. Kaon potential was proposed to explain the data, ref.[1,2];
- 3) JAM model calculations suggest that spectator shadowing, similar to the case of elliptical  $v_2$ , plays important role for the negative  $v_1$  slope parameter.

→ Spectator shadowing  
→ **No Kaon potential is needed**

References:

- (1) P. Chung *et al.* (E895), PRL **85**, 940(2000);
- (2) G.-Q. Li, C. M. Ko, and B.-A. Li, PRL **74**, 235 (1995) and S. Pal, C. M. Ko, Z.-W. Lin, and B. Zhang, PR **C62**, 061903(2000)

# Baryon Correlation Functions



## STAR:

- (1) Meson HBT:  $\pi - \pi$ ,  $K - K$ ;
- (2) **Baryon Correlations:**

$p - p$	reference	
$p - \Lambda$ , $p - \Xi^-$ , $p - \Omega$	$Y-N$	
$p - \phi$		
$\Lambda - \Lambda$	$Y-Y$	
$p - d$ , $d - d$	$N-N-N$	
$d - \Lambda$	$Y-N-N$	

Source

$$C_{the}(k^*) = \frac{1}{4\pi} \int d^3r^* S(r^*) |\Psi(r^*, k^*)|^2$$

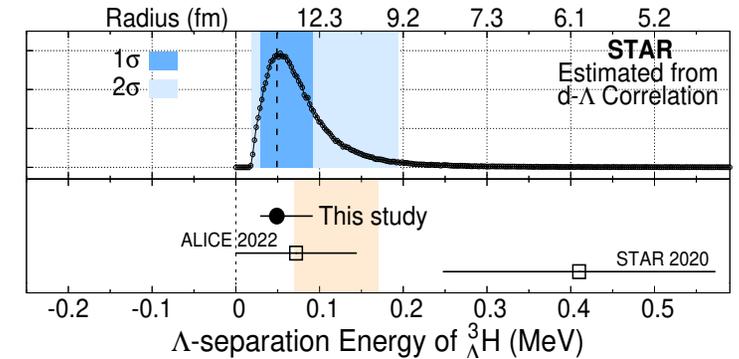
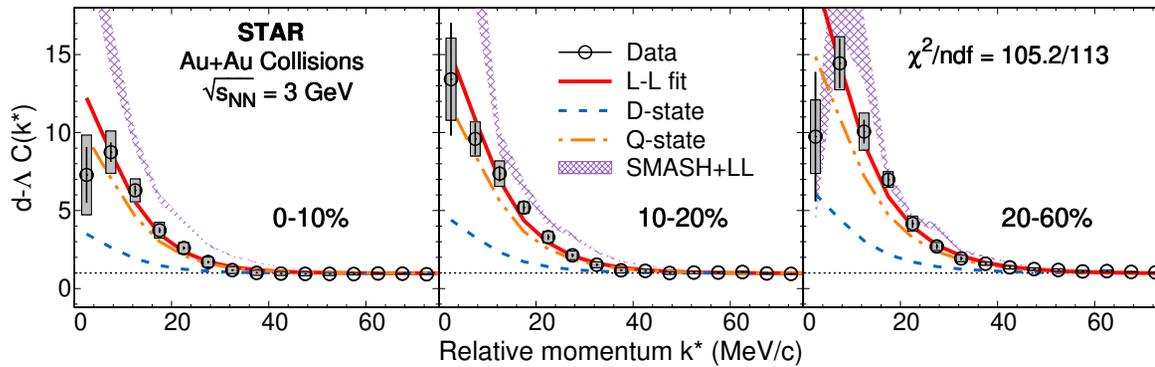
$$C_{exp}(k^*) = \lambda \frac{N_{same}(p_1, p_2)}{N(p_1)N(p_2)}$$

$$k^* = \frac{1}{2} |p_1^* - p_2^*|$$

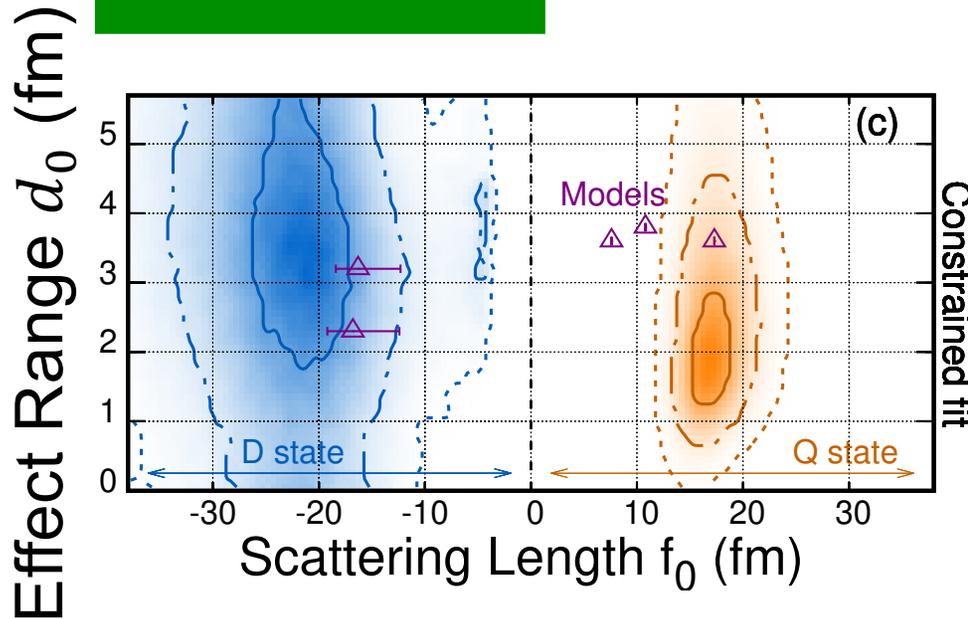
Final State Interactions:

- (1) Quantum statistics;
- (2) Coulomb;
- (3) Strong interaction

# $d - \Lambda$ Correlation Functions 3.0 GeV



STAR: CPOD2024



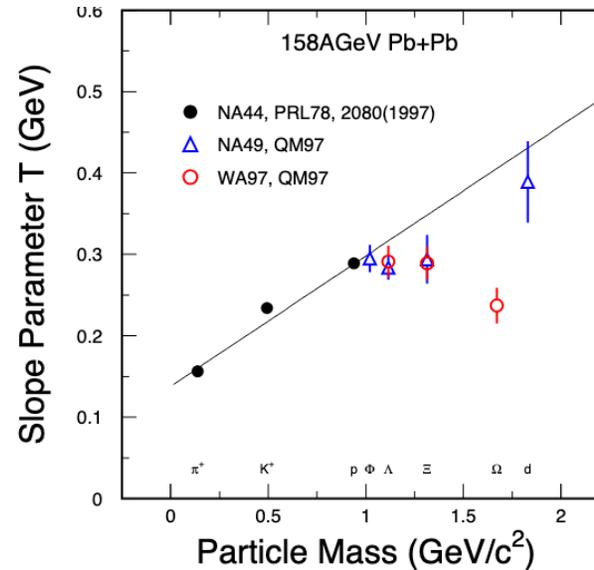
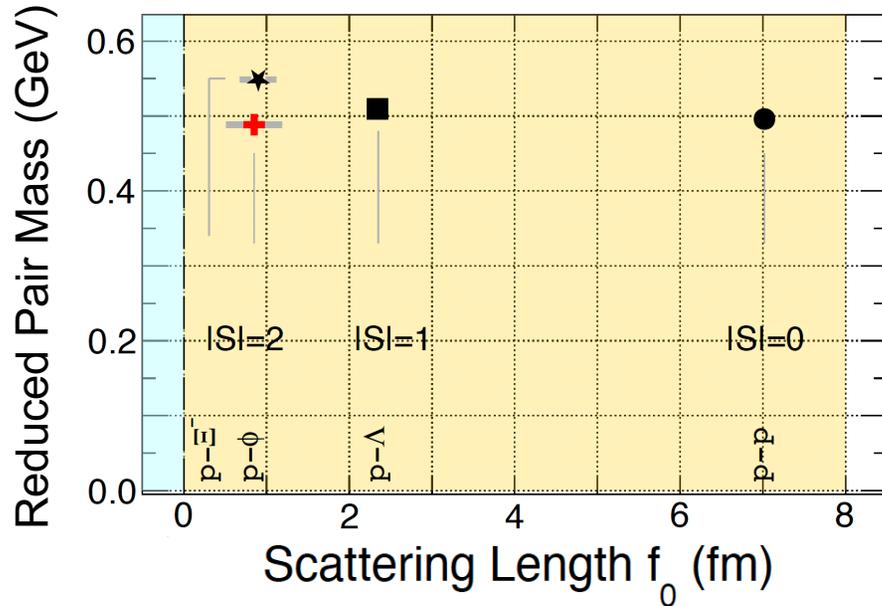
- 1) Centrality dependence of the  $d - \Lambda$  correlation functions from 3.0 GeV Au+Au collisions;
- 2) For the first time, spin dependent states,  $D$  and  $Q$ , identified experimentally!

→ **New window for studying 3-body interactions in the laboratory**

References:

- (1) J.M. Lattimer and M. Prakash, *Science* **304**, 536 (2004);
- (2) M. Kohno and H. Kamada, arXiv:2406.13899;
- (3) H. W. Hammer, *Nucl. Phys.* **A705**, 173 (2002)

# NY Correlations



H. van Hecke, H. Sorge  
 NX, Phys.Rev.Lett. **81**,  
 5764(1998). “Evidence of  
 early multi-strange hadron  
 freeze-out in high energy  
 nuclear collisions”

→ Rescatterings lead to  
 collectivity

→ Collectivity is reduced  
 as the strangeness  
 content is increased

## Hierarchy of strangeness content:

$$f_0(|s| = 0) > f_0(|s| = 1) > f_0(|s| = 2) > 0$$

- Interaction section is proportional to  $f_0^2$ , the observation implies that the strength of the interaction depends on strangeness;
- Important for understanding EOS of the medium in nuclear collisions and compact stars; In case of  $f_0 < 0$ , important for the search for di-baryons, such as  $p\Omega^-$ ;
- Understand the strangeness hierarchy in QCD calculations?

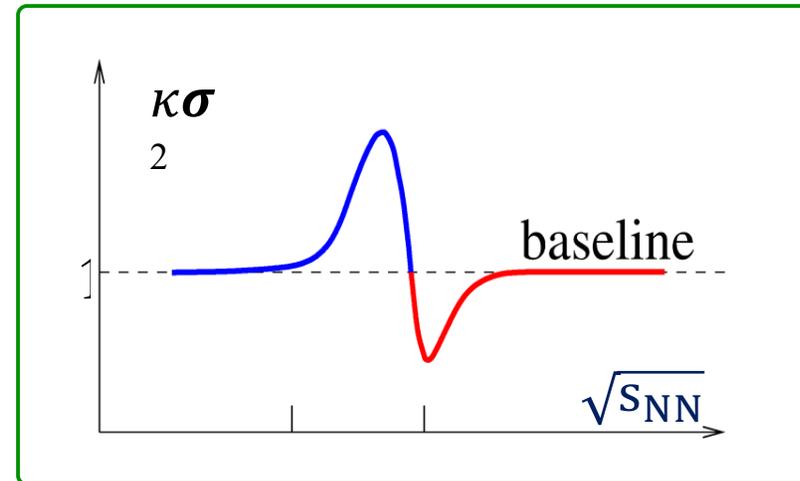
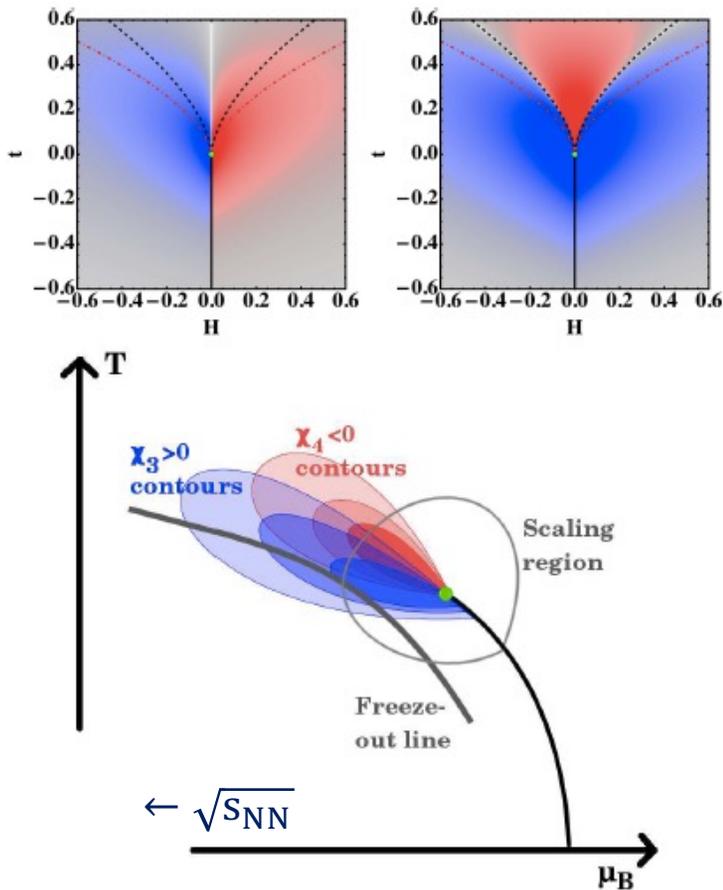
# High Moments from BES-II

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## **Precision Measurements of (Net-)Proton Number Fluctuations in Au+Au Collisions at RHIC (STAR Collaboration)**

A. Pamdav's talk

# Expectations for Models



- Characteristic “Oscillating pattern” is expected for the QCD critical point but the exact shape depends on the location of freeze-out with respect to the location of CP;
- Critical Region (CR)

- M. Stephanov, PRL**107**, 052301(2011) - V. Skokov, Quark Matter 2012

- J.W. Chen, J. Deng, H. Kohyama, Phys. Rev. **D93** (2016) 034037

# Conserved Quantities (B, Q, S)

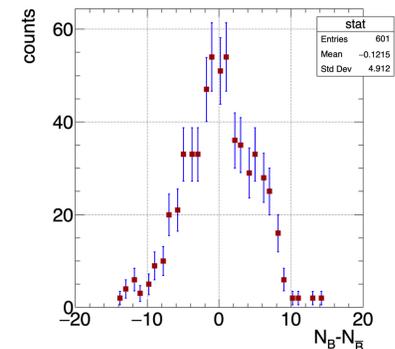
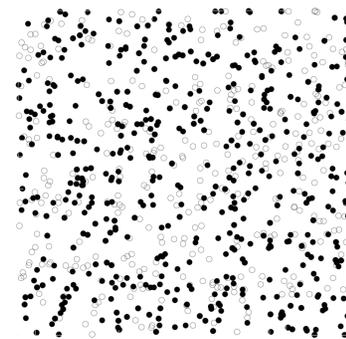
- 1) In strong interactions, baryons (B), charges (Q) and strangeness (S) are conserved;
- 2) Higher order moments/cumulants describe the shape of distributions and quantify fluctuations. They are sensitive to the correlation length  $\xi$ , phase structure;
- 3) Direct connection to theoretical calculations of susceptibilities.

Measured multiplicity N,	$\langle \delta N \rangle = N - \langle N \rangle$
mean: M = $\langle N \rangle$	= $C_1$
variance: $\sigma^2 = \langle (\delta N)^2 \rangle$	= $C_2$
skewness: S = $\langle (\delta N)^3 \rangle / \sigma^3$	= $C_3 / C_2^{3/2}$
kurtosis: $\kappa = \langle (\delta N)^4 \rangle / \sigma^3 - 3$	= $C_4 / C_2^2$

Moments, cumulants and susceptibilities:

2 <sup>nd</sup> order: $\sigma^2 / M \equiv C_2 / C_1 = \chi_2 / \chi_1$
3 <sup>rd</sup> order: $S \sigma \equiv C_3 / C_2 = \chi_3 / \chi_2$
4 <sup>th</sup> order: $\kappa \sigma^2 \equiv C_4 / C_2 = \chi_4 / \chi_2$

Animation: Anar Rustamov



INT 2008-2b : “The QCD Critical Point”

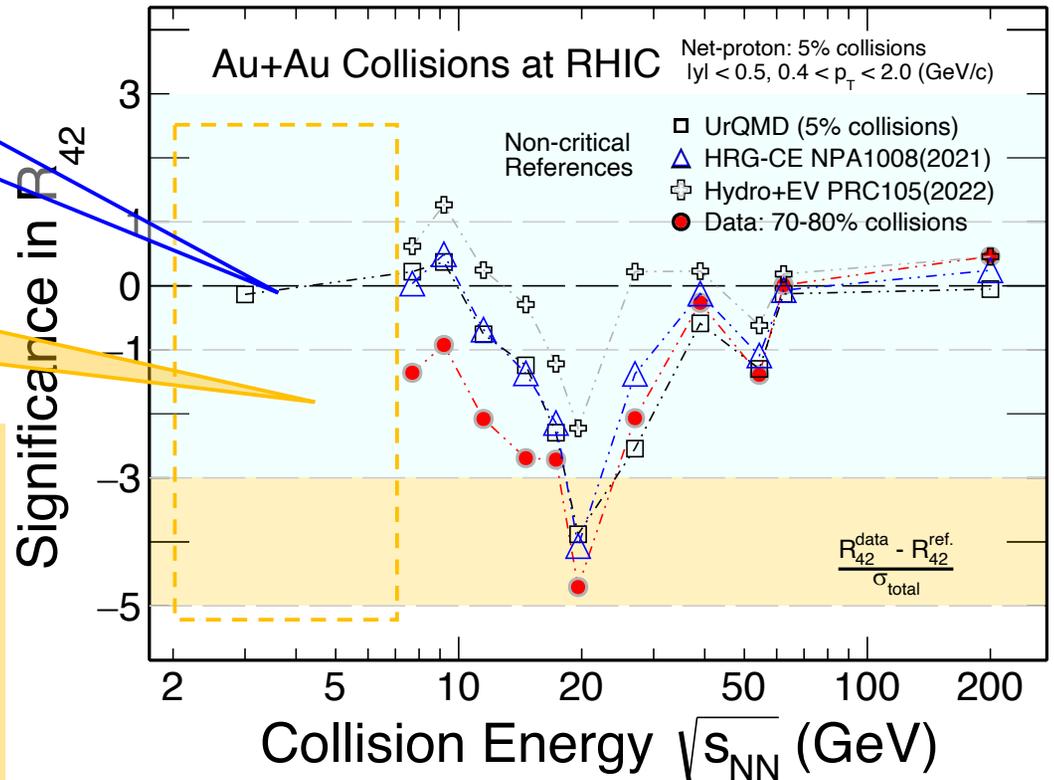
F. Gross *et al.* 2212.11107: “50 Years of QCD”

# Summary: Fluctuations

**STAR FXT**  
**HADES**  
**CBM**  
**(2028)**

\*Predictions on CP at 650 MeV  
~ 4 GeV

*“In summary, ... Dynamic model calculations including the criticality is needed in order to understand the results from BES-II. On the experiment side, data between  $\sqrt{s_{NN}} = 3.0$  and 8.0 GeV is needed in order to search for the signals of QCD critical point and the 1<sup>st</sup>-order phase boundary.”*



- 1) M. Hippert, et al., 2309.00579; X. An et al., NP **A1017** (2022) 122343;
- 2) W.J. Fu, et al., 2308.15508; F. Gao et al., PR **D104**, (2021) 054022

# Outline

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## 1) Introduction

## 2) Selected Recent Results

- Collectivity and Baryon Correlation from FXT
- Criticality from BES-II (collider)

## 3) Summary and Outlook

# Summary

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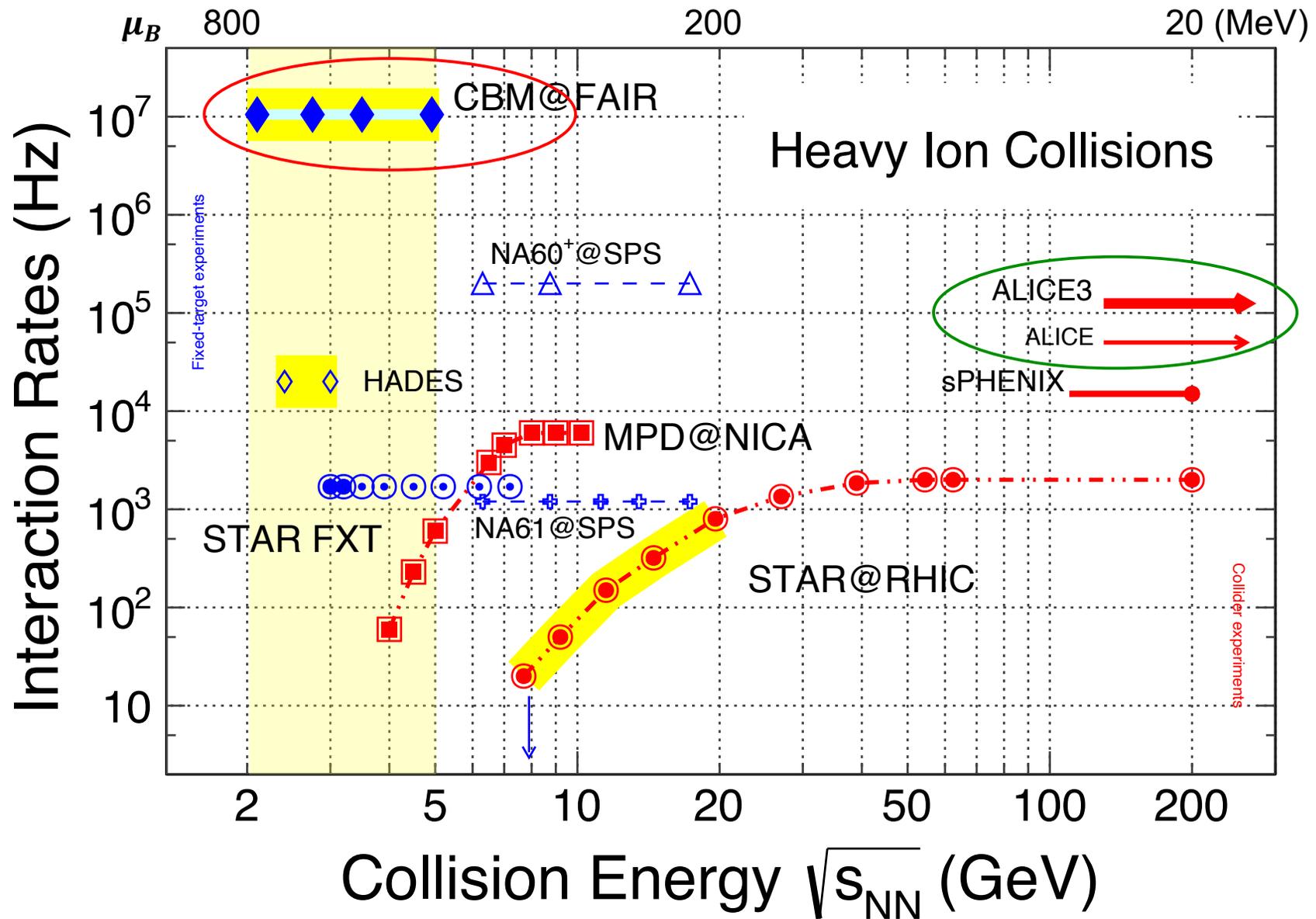
## 1) Rich physics at large $\mu_B$ region:

- Strangeness and EOS;
- Hypernuclei production;
- Baryon correlations;
- ...

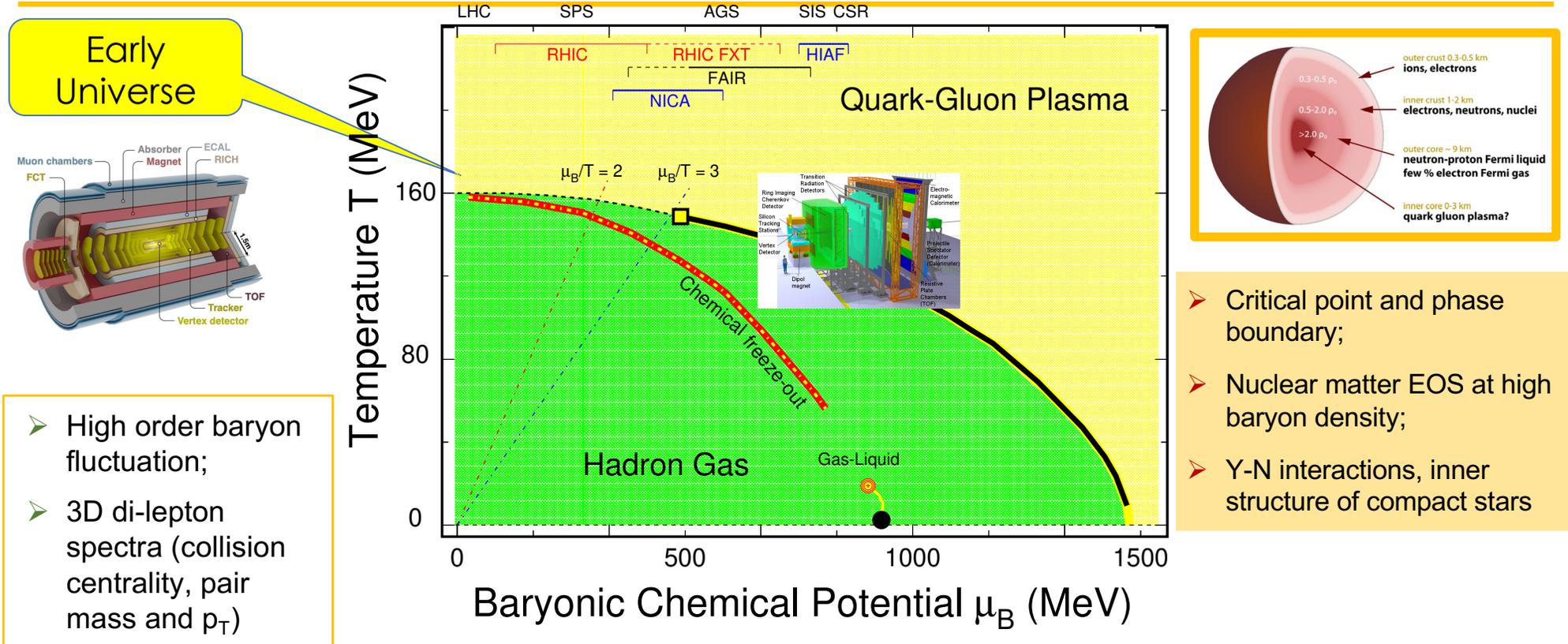
## 2) QCD critical point:

- BES-II data offered high statistics, better acceptance, centrality resolution and systematic;
- Will do (i)  $p_T$  and rapidity scan; (ii)  $C_5$ , and  $C_6$  analysis; (iii) complete the FXT data ( $\sqrt{s_{NN}} = 3 - 3.9$  GeV)

# Future High Rates Experiments



# Nuclear Collisions and QCD Phase Diagram



- 1) Property of QGP, smooth crossover transition at  $\mu_B = 0$ ;
- 2) Search for 1<sup>st</sup>-order phase transition and **QCD critical point**;
- 3) Baryon interactions (e.g.  $N - N$ ,  $Y - N$ )  $\rightarrow$  inner structure of compact stars

# Many Thanks to Organizers!

## Acknowledgements:

P. Braun-Munzinger, X. Dong, S. Esumi, F. Karsch, V. Koch, XF. Luo, B. Mohanty, **A. Pandav**, A. Rustamov, K. Redlich, M. Stephanov, J. Stachel, J. Stroth, V. Vovchenko, **Y. Zhang**

// BLUE: Theory // RED: Exp. //

# Thank you for your attention!