

# Can high- $p_\perp$ theory and data constrain $\eta/s$ ?

Bithika Karmakar

Incubator for Scientific Excellence - Centre for Simulations of Superdense Fluids  
University of Wroclaw

Based on Phys.Rev.C 108 (2023) 4, 044907

Collaborators: Dusan Zigic, Igor Salom, Jussi Auvinen, Pasi Huovinen, Marko Djordjevic and  
Magdalena Djordjevic

# Outline

- Motivation
- $\eta/s$  of the medium : Soft-to-hard boundary
- High- $p_\perp$  energy loss: Generalized DREENA-A
- Phenomenological approach to constrain  $\eta/s$
- Theoretical approach to evaluate  $\eta/s$
- Summary

# Motivation

- Low- $p_\perp$  observables are used to explore the bulk properties of the QGP created in heavy-ion collisions.
- High- $p_\perp$  probes also become powerful tomography tools; Sensitive to global QGP features, e.g., different temperature profiles or initial conditions.
- QGP tomography: Jointly constraining QGP properties by low and high- $p_\perp$  physics.
- $\eta/s$  is well constrained by Bayesian analysis in low- $p_\perp$  sector in the temperature range  $T_c \lesssim T \lesssim 1.5T_c$  and weakly constrained at larger temperatures.
- High- $p_\perp$  data/theory can serve as complementary tool.

# $\eta/s$ of the medium : Soft-to-hard boundary

- QGP behaves as almost perfect fluid: Remarkably small  $\eta/s$ .
- QGP is expected to behave as weakly interacting gas: Weakly coupled
- Fluid dynamics predicts the  $\eta/s$  to be very low: Strongly coupled
- QGP may behave as perfect fluid near  $T_c$  (soft regime) and  $\eta/s$  may increase at high temperature (hard regime).
- Testing the soft-to-hard hypothesis is difficult: Anisotropy is weakly affected by the  $\eta/s$  at high temperature.

# High- $p_{\perp}$ energy loss : Generalized DREENA-A

- Dynamical Radiative and Elastic ENergy loss Approach
  - Based on finite temperature field theory (pQCD) and generalized HTL approach  
M. Djordjevic, PRC 74, 064907, (2006) ; PRC 80, 064909 (2009), M. Djordjevic and U. Heinz, PRL 101, 022302
  - Finite size dynamical QCD medium is considered
  - Takes into account both radiative and collisional energy losses
  - No fitting parameter in the theory

# High- $p_{\perp}$ energy loss : Generalized DREENA-A

- Optimized to incorporate any arbitrary event-by-event fluctuating temperature profile.  
D. Zivic, J. Auvinen, I. Salom, M. Djordjevic, P. Huovinen Phys.Rev.C 106 (2022) 4, 044909
- Constraints on early evolution.  
S. Stojku, J. Auvinen, M. Djordjevic, P. Huovinen, M. Djordjevic Phys.Rev.C 105 L021901 (2022)
- Map how the shape of the collision system is manifested in the high- $p_{\perp}$  data.  
S. Stojku, J. Auvinen, L. Zivkovic, P. Huovinen, M. Djordjevic Phys.Lett.B 835, 137501 (2022)
- Shape of the QGP droplet.  
BK, D. Zivic, P. Huovinen, M. Djordjevic, M. Djordjevic and J. Auvinen, Phys. Rev. C 110 (2024) 4, 044906
- DREENA-A is available on <http://github.com/DusanZivic/DREENA-A>

# Phenomenological approach

- Three different  $(\eta/s)(T)$  parametrizations have been considered.
- Parameters are adjusted to reproduce low- $p_{\perp}$  data.
- Temperature profile is generated for each case.
- High- $p_{\perp}$  predictions found using generalized DREENA-A.
- Compared with high- $p_{\perp}$  data.

# Modeling the bulk evolution

- Initial entropy profiles are generated using TRENTo model.
- $10^4$  events for Pb+Pb ( $\sqrt{s} = 5.02$  TeV) and Au+Au ( $\sqrt{s} = 200$  GeV) collisions.
- Initial free streaming is not preferred by high- $p_\perp$  data.

S. Stojku, J. Auvinen, M. Djordjevic, P. Huovinen and M. Djordjevic, Phys. Rev. C 105 (2022) 2, L021901

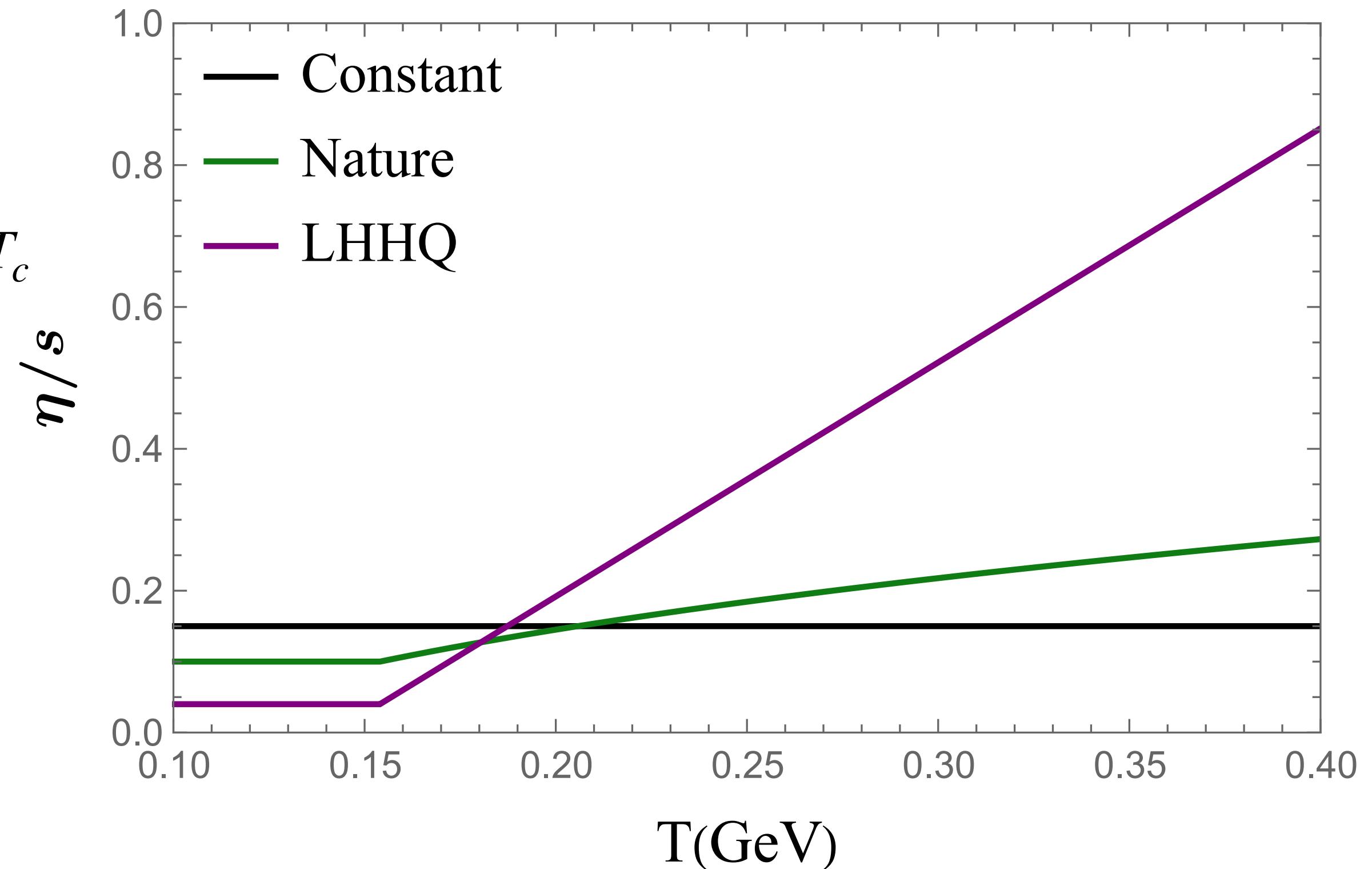
- Onset time for hydrodynamics:  $\tau_0 = 1fm$ .
- S. Stojku, J. Auvinen, M. Djordjevic, P. Huovinen and M. Djordjevic, Phys. Rev. C 105 (2022) 2, L021901
- (2+1)-dimensional fluid dynamical model (ViSHNew) + UrQMD

# Temperature dependence of $\eta/s$

$$(\eta/s)(T) = \begin{cases} (\eta/s)_{\min}, & T < T_c, \\ (\eta/s)_{\min} + (\eta/s)_{\text{slope}}(T - T_c)\left(\frac{T}{T_c}\right)^{(\eta/s)_{\text{crv}}}, & T > T_c \end{cases}$$

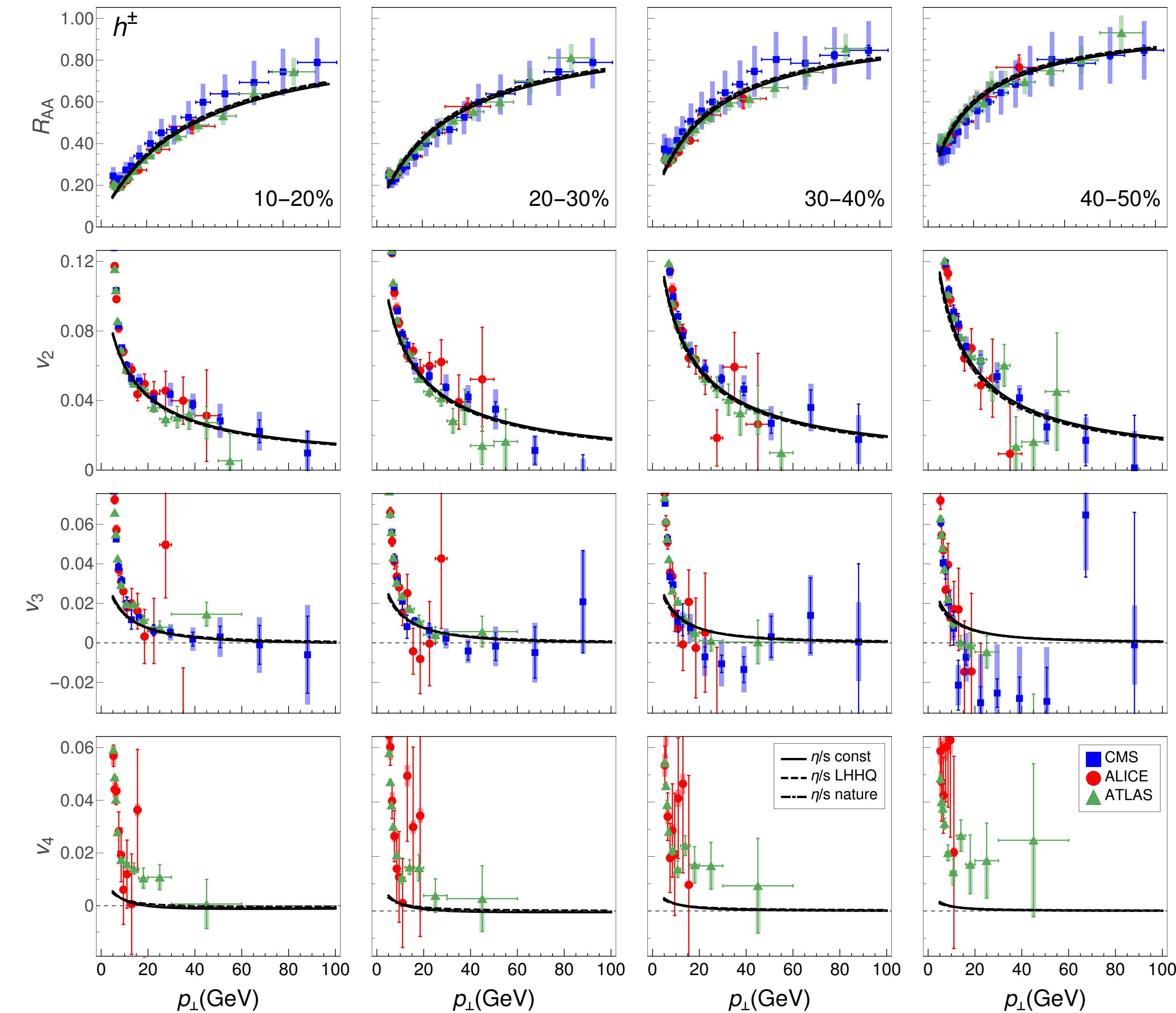
Nature: Nature Phys. 15, no. 11, 1113-1117 (2019)

LHHQ: Phys. Rev. Lett. 106, 212302 (2011)



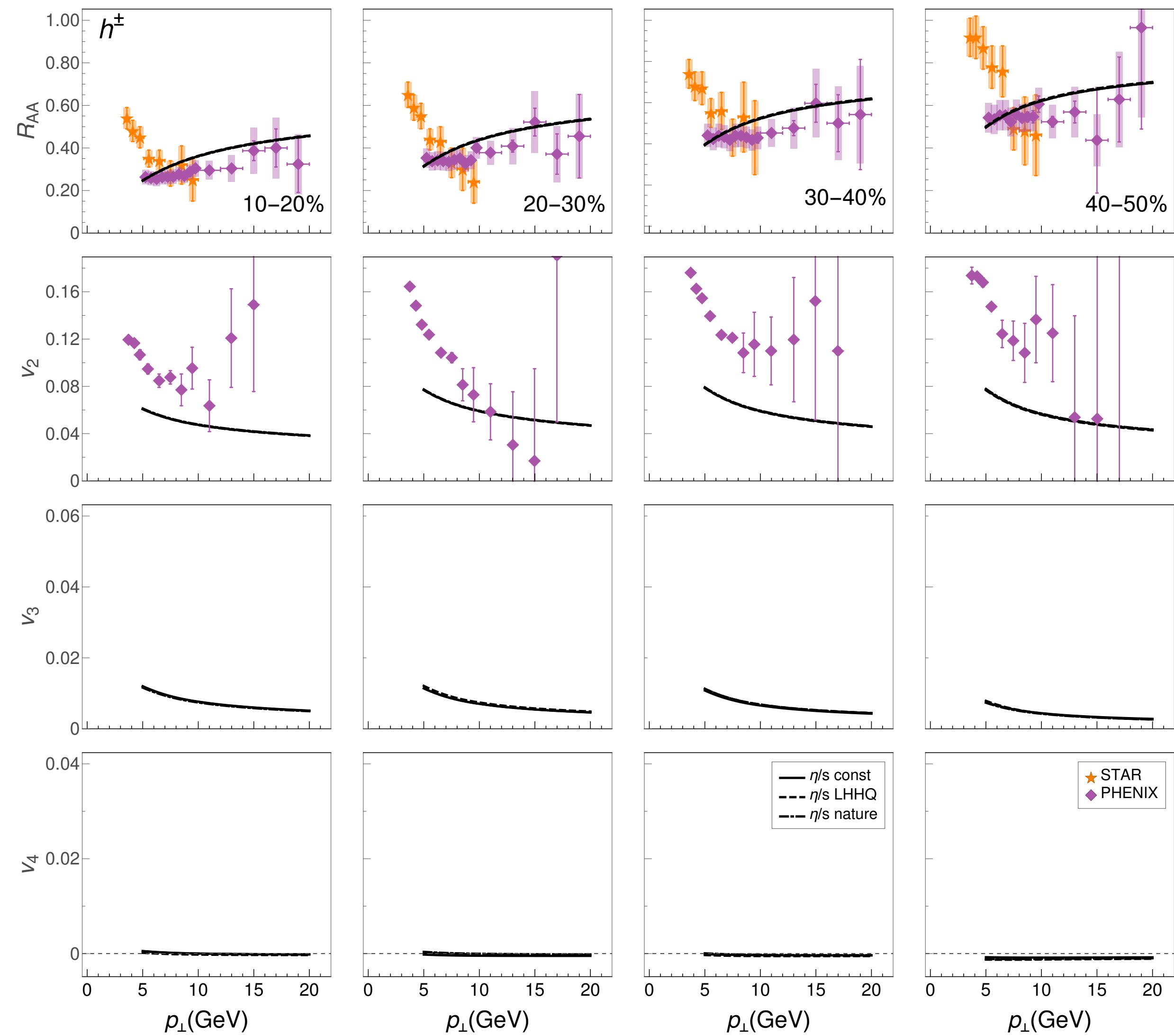
- Pion, kaon, proton multiplicities and  $v_2\{4\}$  are reproduced by varying the TRENTo normalization factor for three  $\eta/s$  parametrizations.

# Results



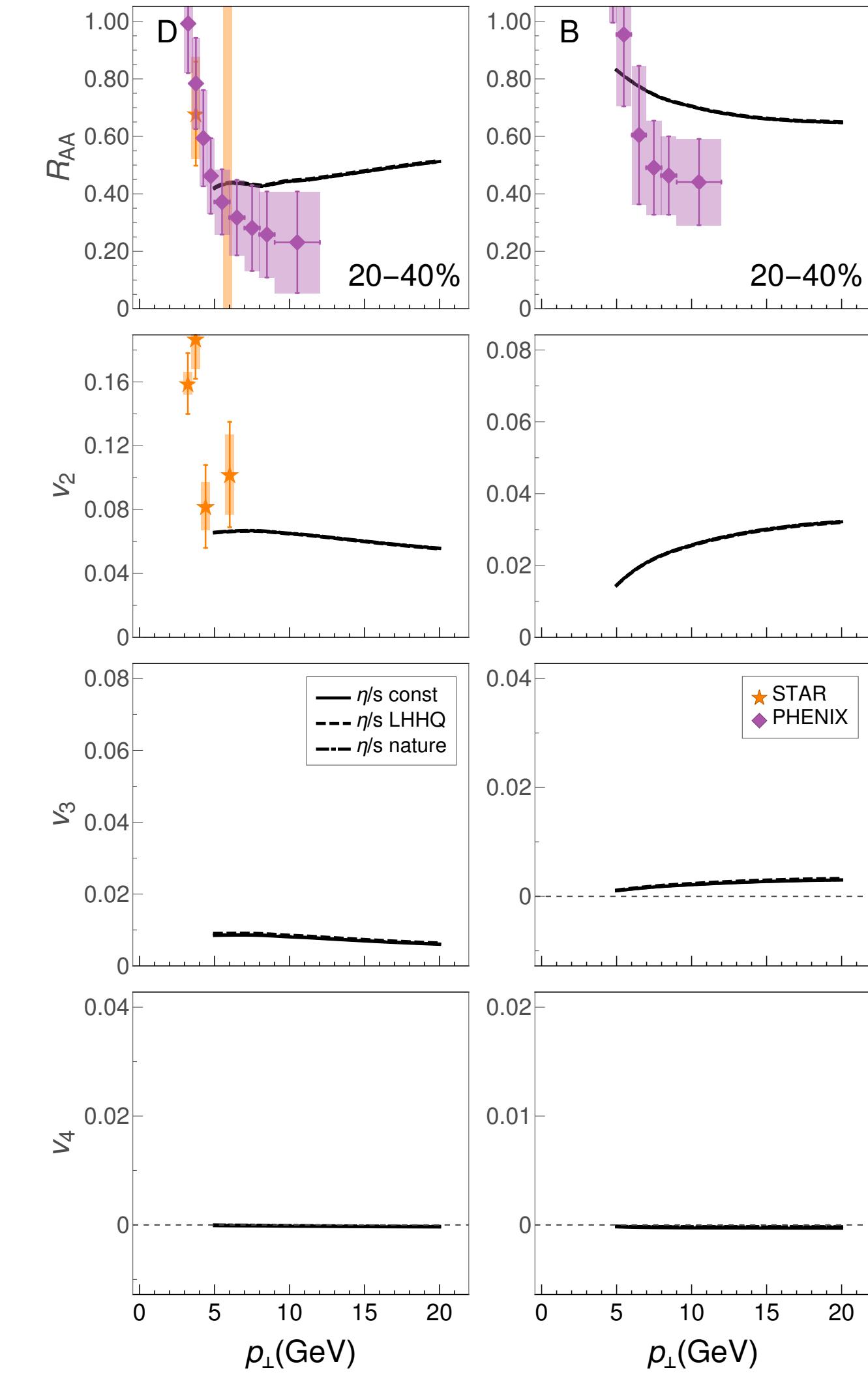
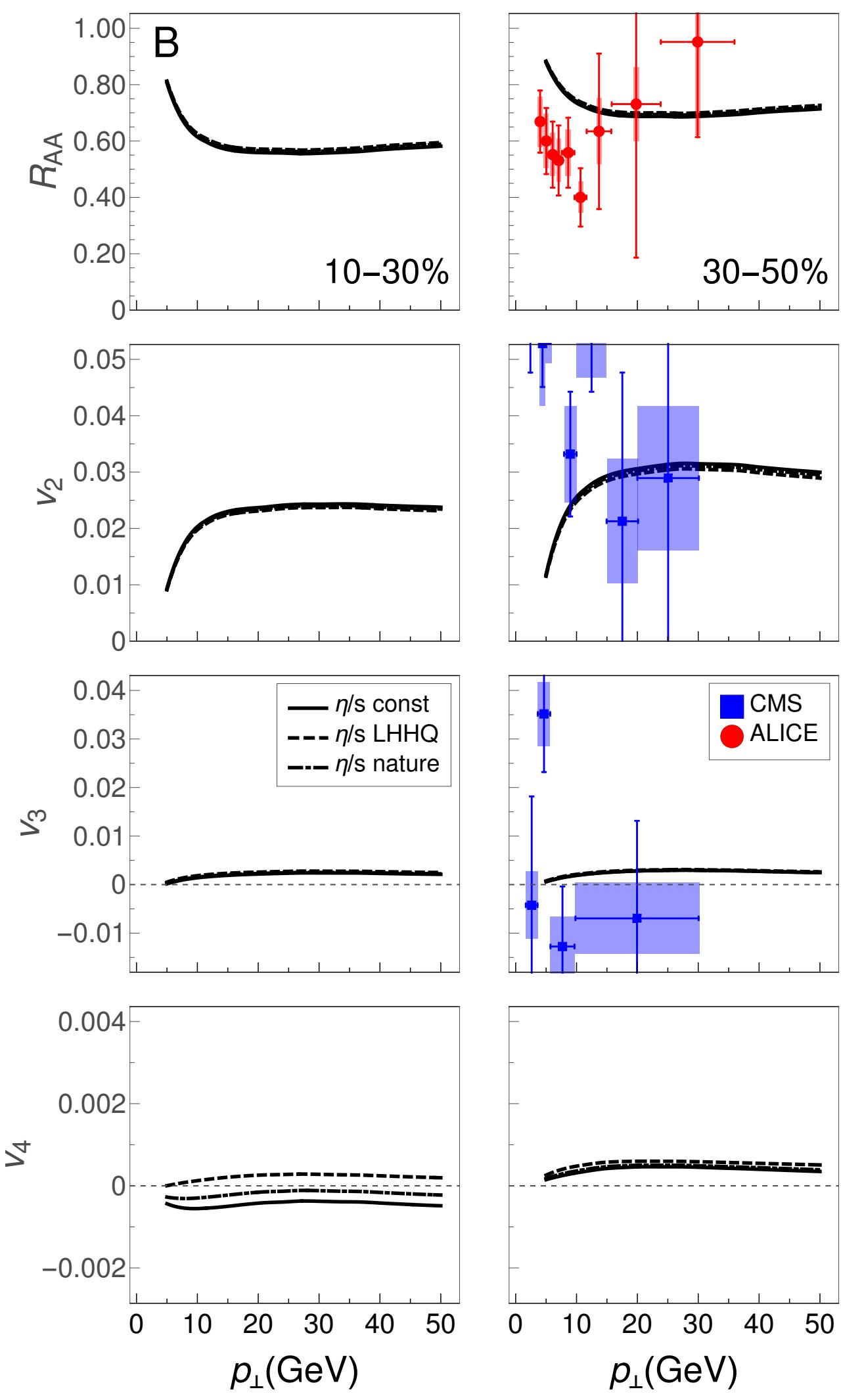
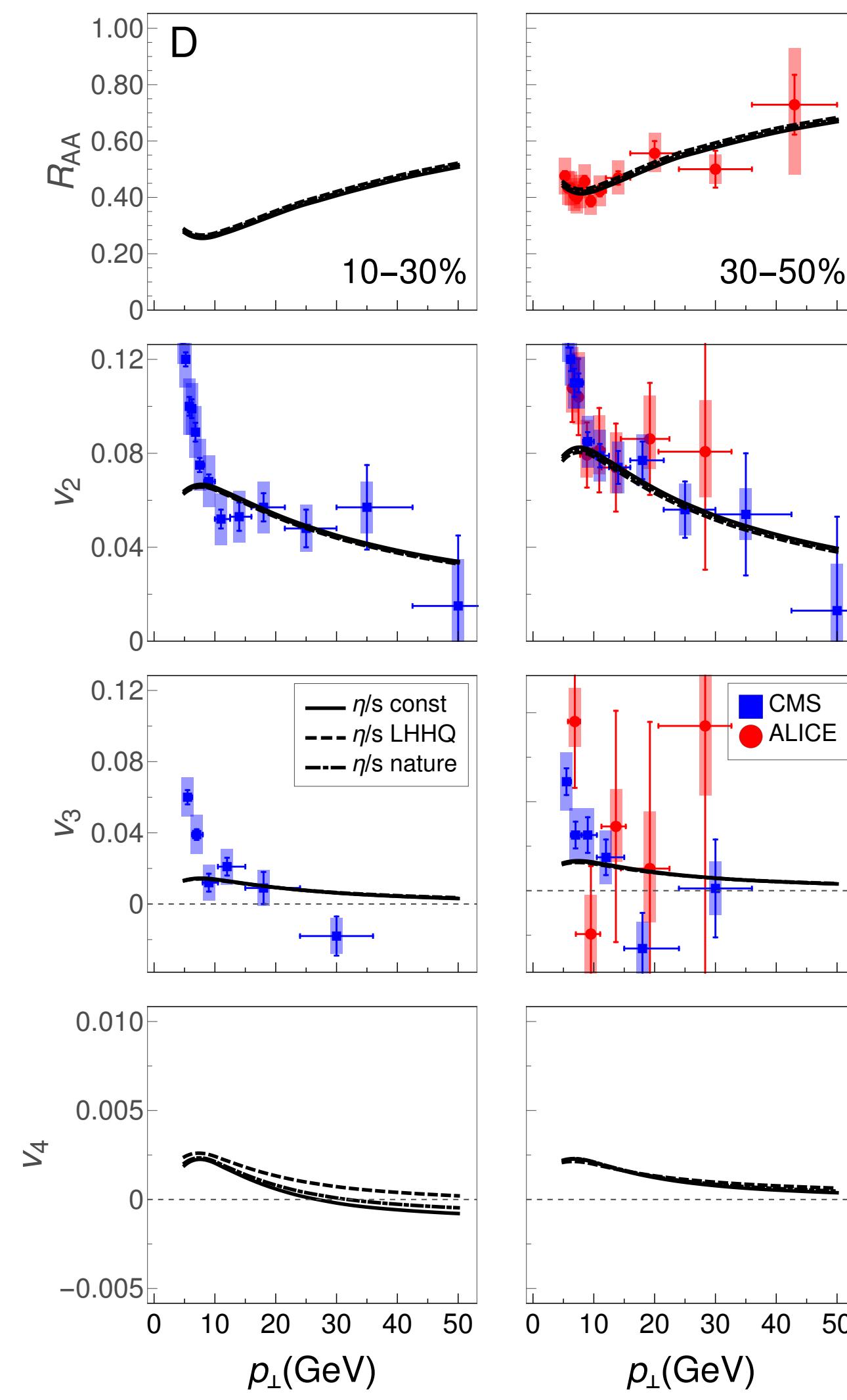
$\text{Pb} + \text{Pb}$  ( $\sqrt{s} = 5.02 \text{ TeV}$ )

# Results



Au + Au ( $\sqrt{s} = 200 \text{ GeV}$ )

# Results



Pb + Pb ( $\sqrt{s} = 5.02 \text{TeV}$ )

Au + Au ( $\sqrt{s} = 200 \text{GeV}$ )

# Theoretical approach :

## Jet transport coefficient from dynamical energy loss formalism

- Jet transport coefficient ( $\hat{q}$ )  $\equiv$  Squared average transverse momentum exchange between the medium and the fast parton per unit length
- Interaction between the parton and medium is characterized by the HTL resummed elastic collision rate:

$$\frac{d\Gamma_{el}}{d^2q} = \frac{C_A}{\pi} T \alpha(ET) \frac{\mu_E^2 - \mu_M^2}{(q^2 + \mu_E^2)(q^2 + \mu_M^2)}$$

- In fluid rest frame:

$$\hat{q} = \int_0^{\sqrt{6ET}} d^2q q^2 \cdot \frac{d\Gamma_{el}}{d^2q} = C_A T \frac{4\pi}{(11 - \frac{2}{3}n_f)} \frac{\left( \mu_E^2 \ln \left[ \frac{6ET + \mu_E^2}{\mu E^2} \right] - \mu_M^2 \ln \left[ \frac{6ET + \mu_M^2}{\mu_M^2} \right] \right)}{\ln(\frac{ET}{\Lambda^2})}$$

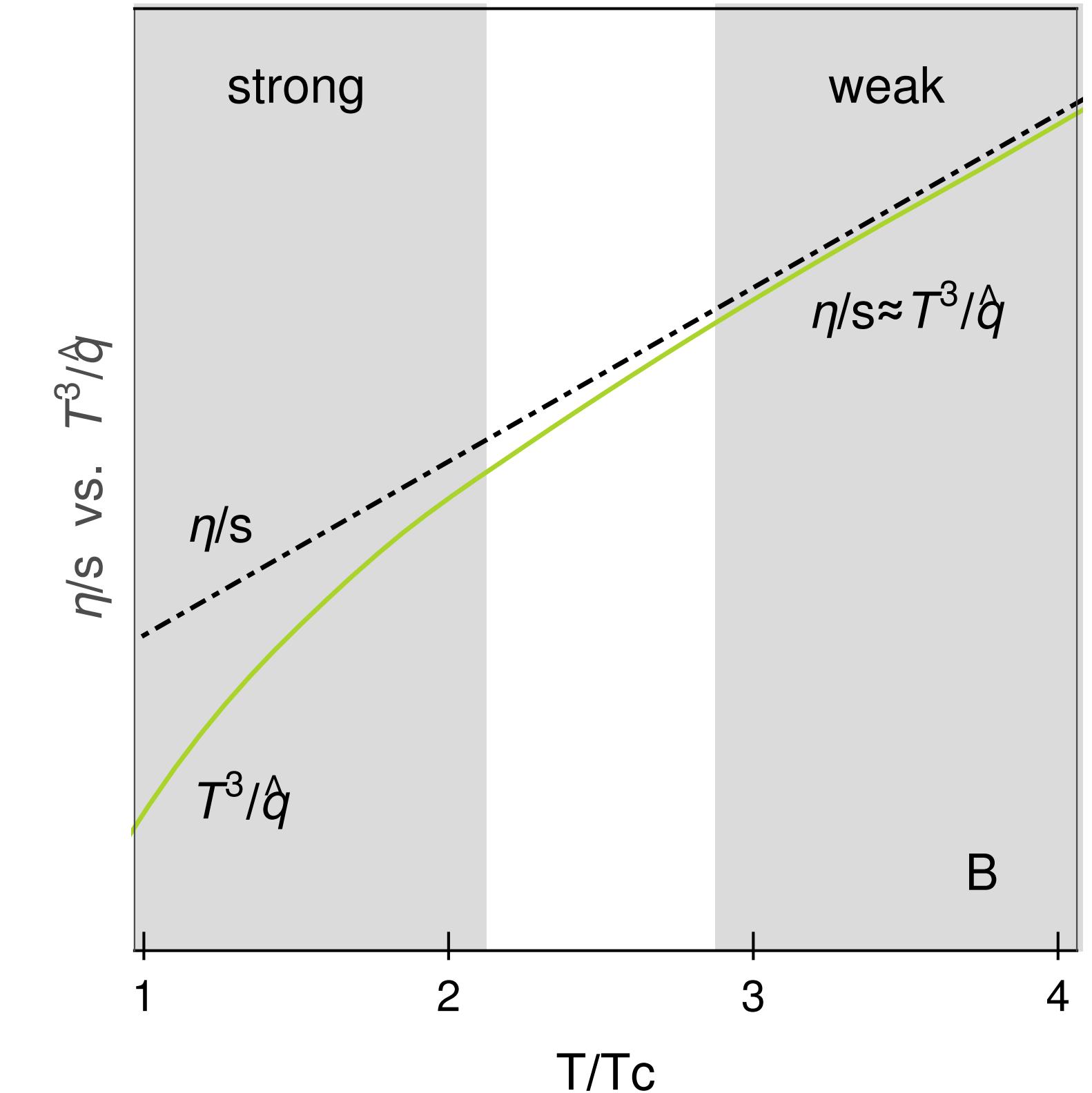
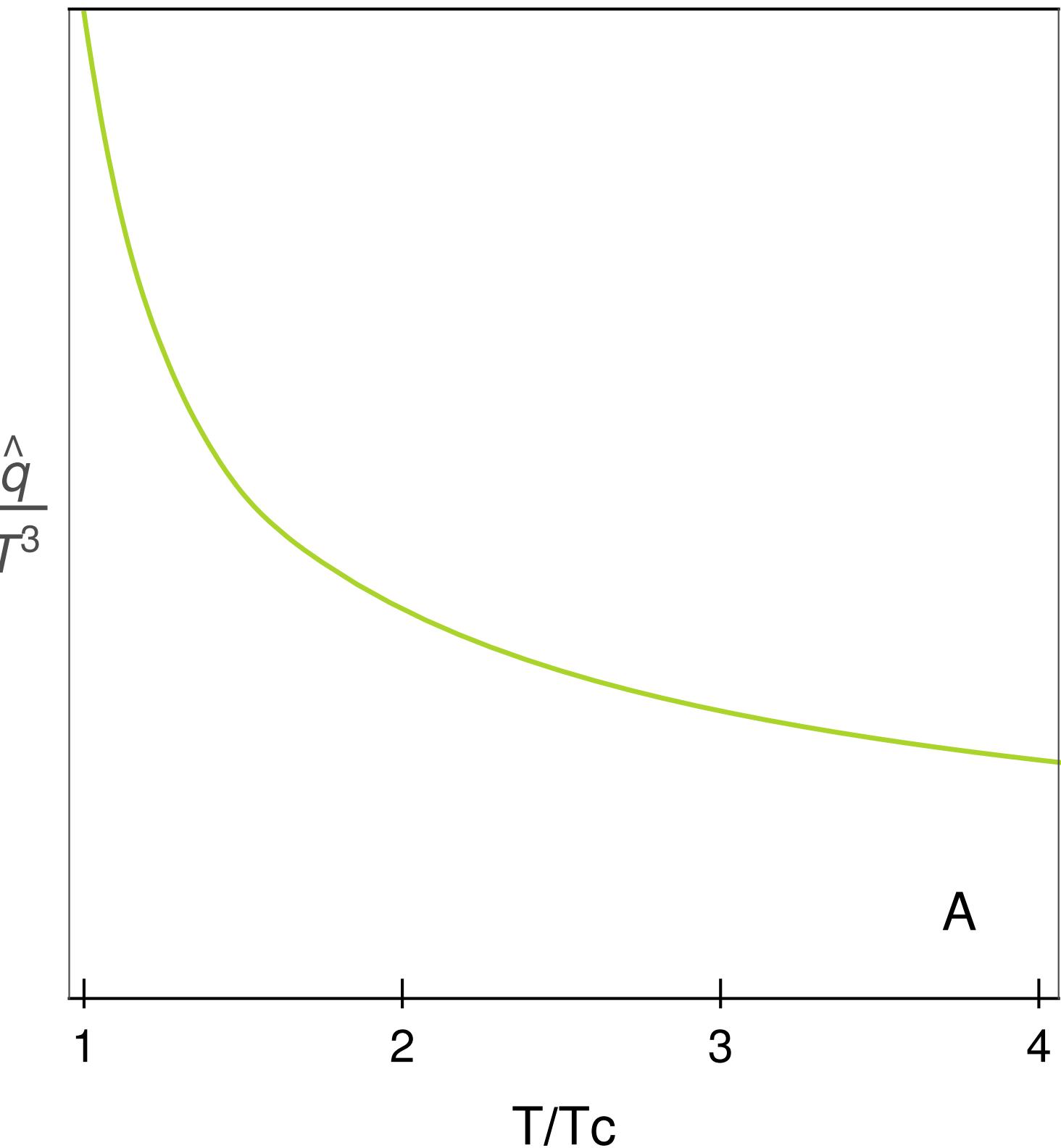
- In weakly coupled limit:

$$\eta/s \approx 1.25 T^3 / \hat{q}$$

Phys. Rev. Lett. 99 192301 (2007), Phys. Rev. D 104, L071501 (2021)

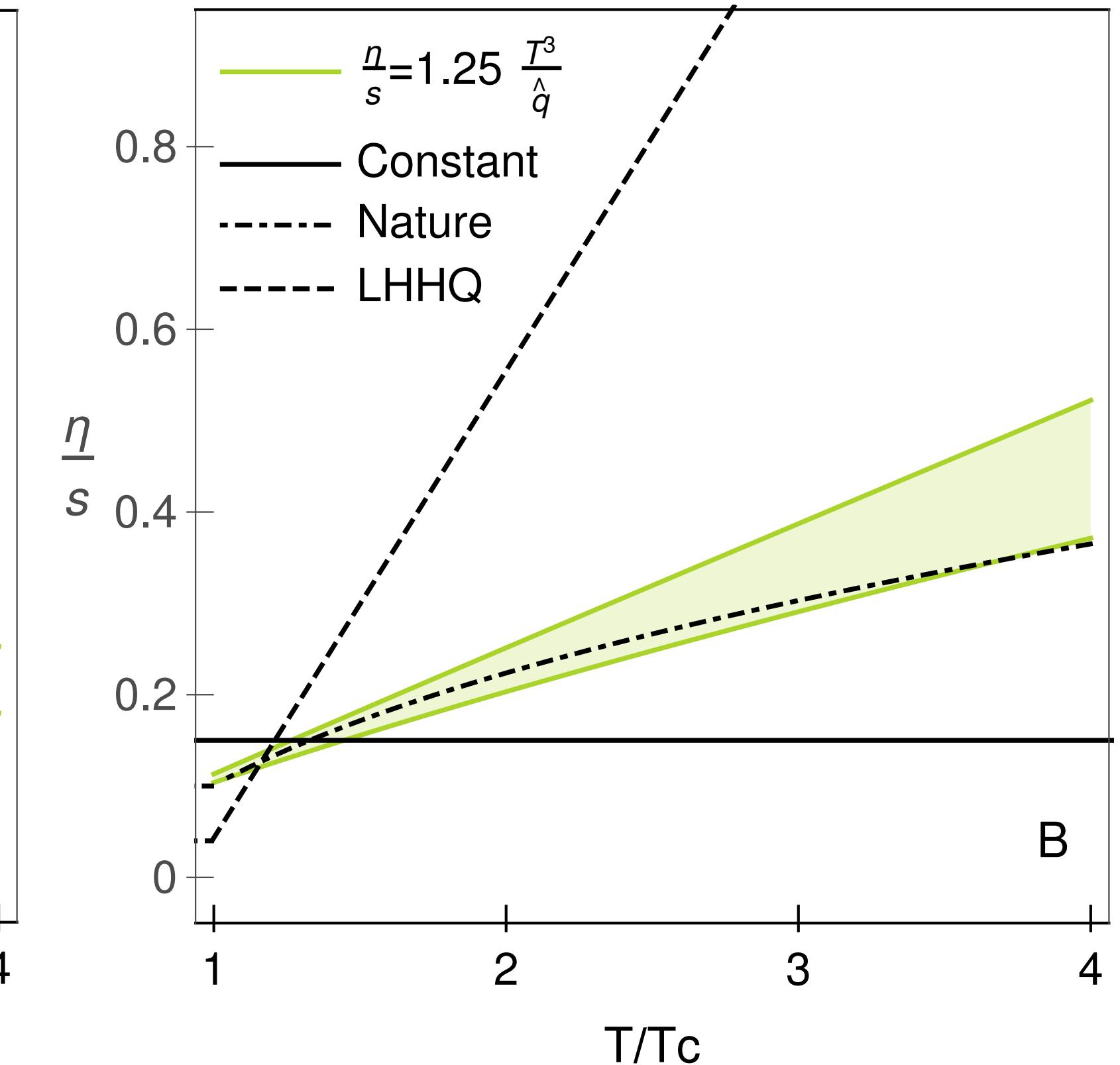
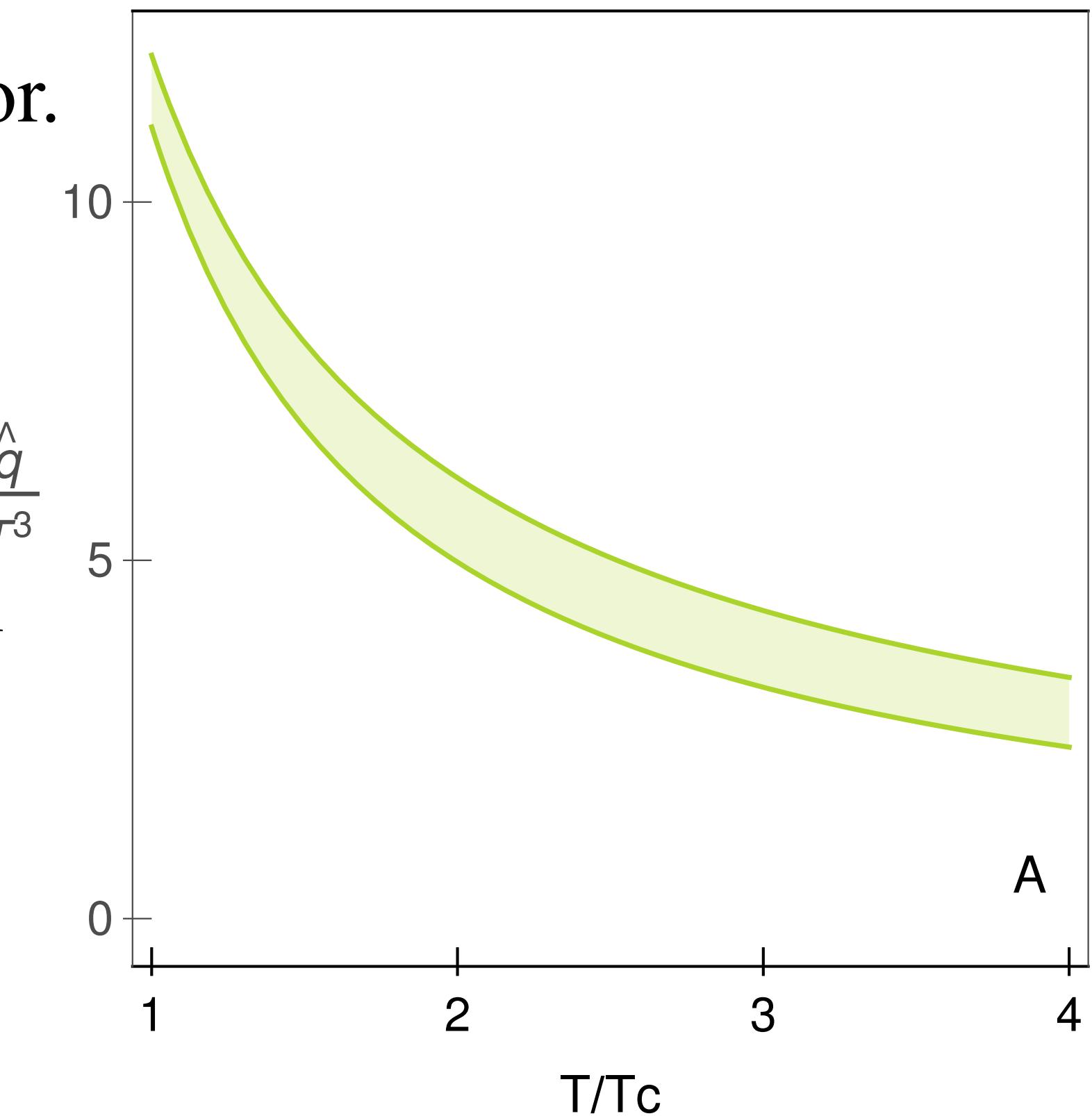
# $\eta/s$ from jet transport coefficient

- $\hat{q}$  quantifies the parton coupling strength in the medium
- $\hat{q}/T^3$  must rise rapidly near  $T_c$  from above.
- Our formalism valid in weakly coupled regime.
- $T^3/\hat{q}$  and  $\eta/s$  should agree in the weak coupling regime.
- Soft-to-hard boundary



# $\eta/s$ from jet transport coefficient

- $\hat{q}/T^3$  shows expected behavior.
- Enhanced quenching near  $T_c$ .
- $\eta/s$  is surprisingly close to the constraints from Bayesian analysis.

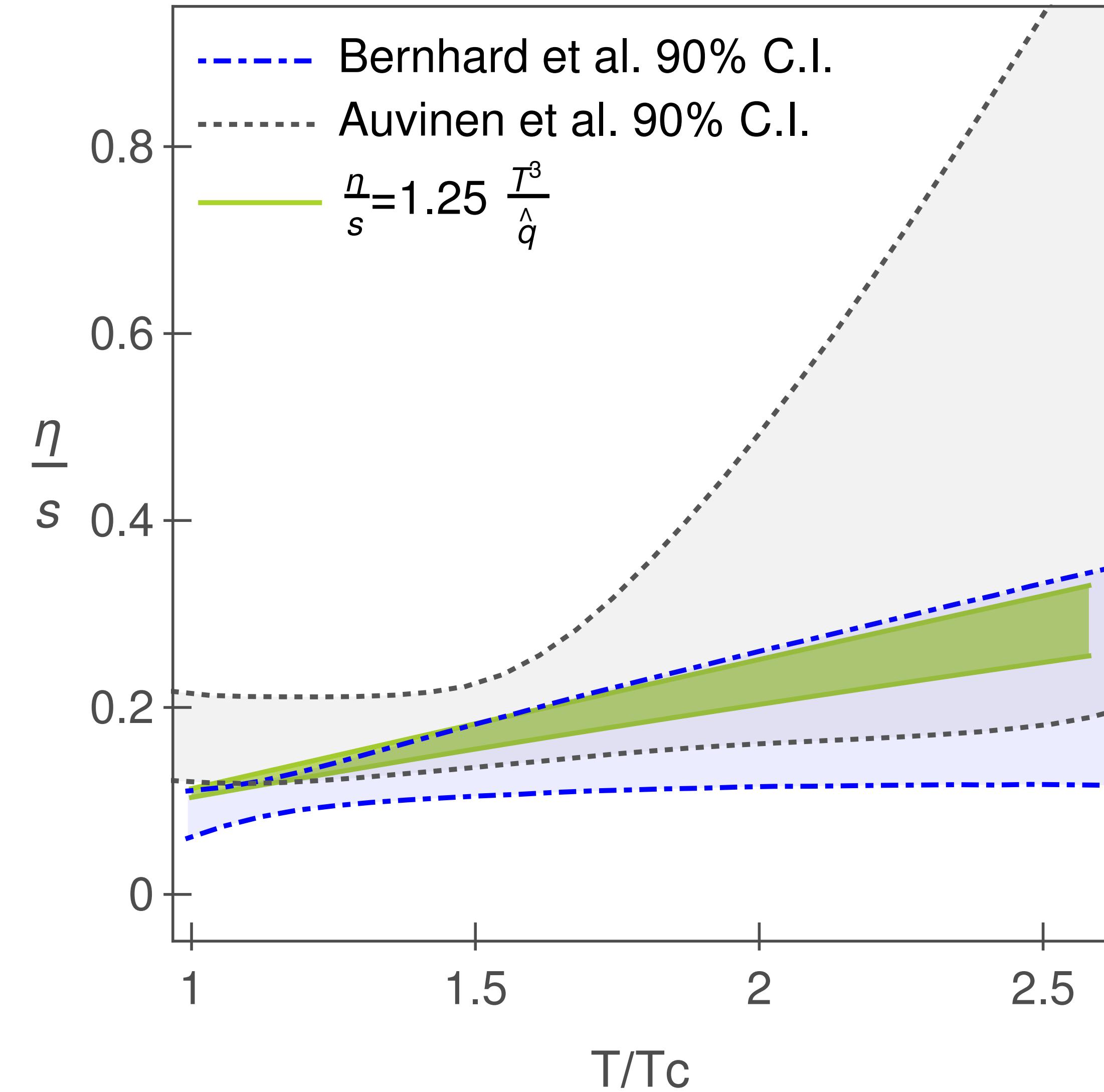


# $\eta/s$ from jet transport coefficient

- Uncertainty due to initial jet energy is very small
- Surprisingly close to the parametrization inspired by the Bayesian analysis.
- Does not drop significantly below the inferred  $\eta/s$  values near  $T_c$ .
- No soft-to-hard boundary.

Blue → Nature Phys. 15, no. 11, 1113-1117 (2019)

Black → Phys. Rev. C 102, 044911 (2020)



# Summary

- We use generalized DREENA-A to compute high- $p_\perp$  energy loss.
- In the phenomenological approach:
  - Three different  $(\eta/s)(T)$  parametrizations have been considered.
  - The predictions from the generalized DREENA-A for three  $\eta/s$  scenarios lead to plots that are almost indistinguishable.
- In the theoretical approach:
  - Jet transport coefficient and jet quenching strength are calculated from the dynamical energy loss formalism.
  - $\eta/s$  shows surprisingly good agreement all the way to  $T_c$  with constraints extracted from existing Bayesian analyses. Provides much smaller uncertainties at high temperatures.
  - No guidance on locating soft-to-hard boundary.

# Extreme QCD 2025

- **Dates:** July 2 – 4, 2025
- **Venue:** University of Wroclaw,  
Wroclaw, Poland
- **Student support:** fee, travel,  
accommodation
- **Web:** INDICO  
INSPIRE



XQCD 2025

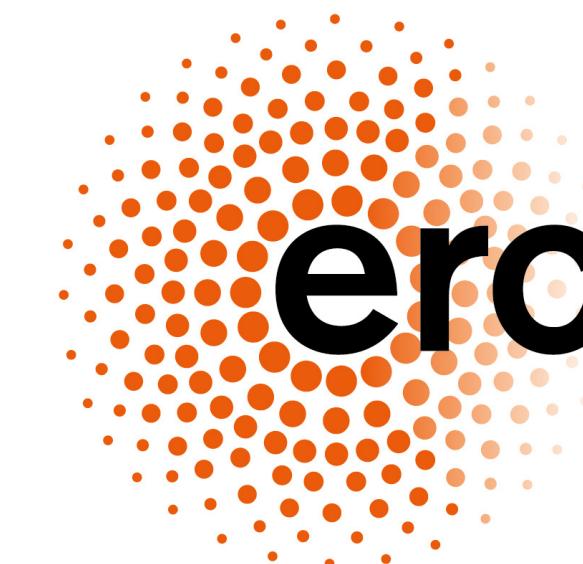


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*Thank you for your attention*



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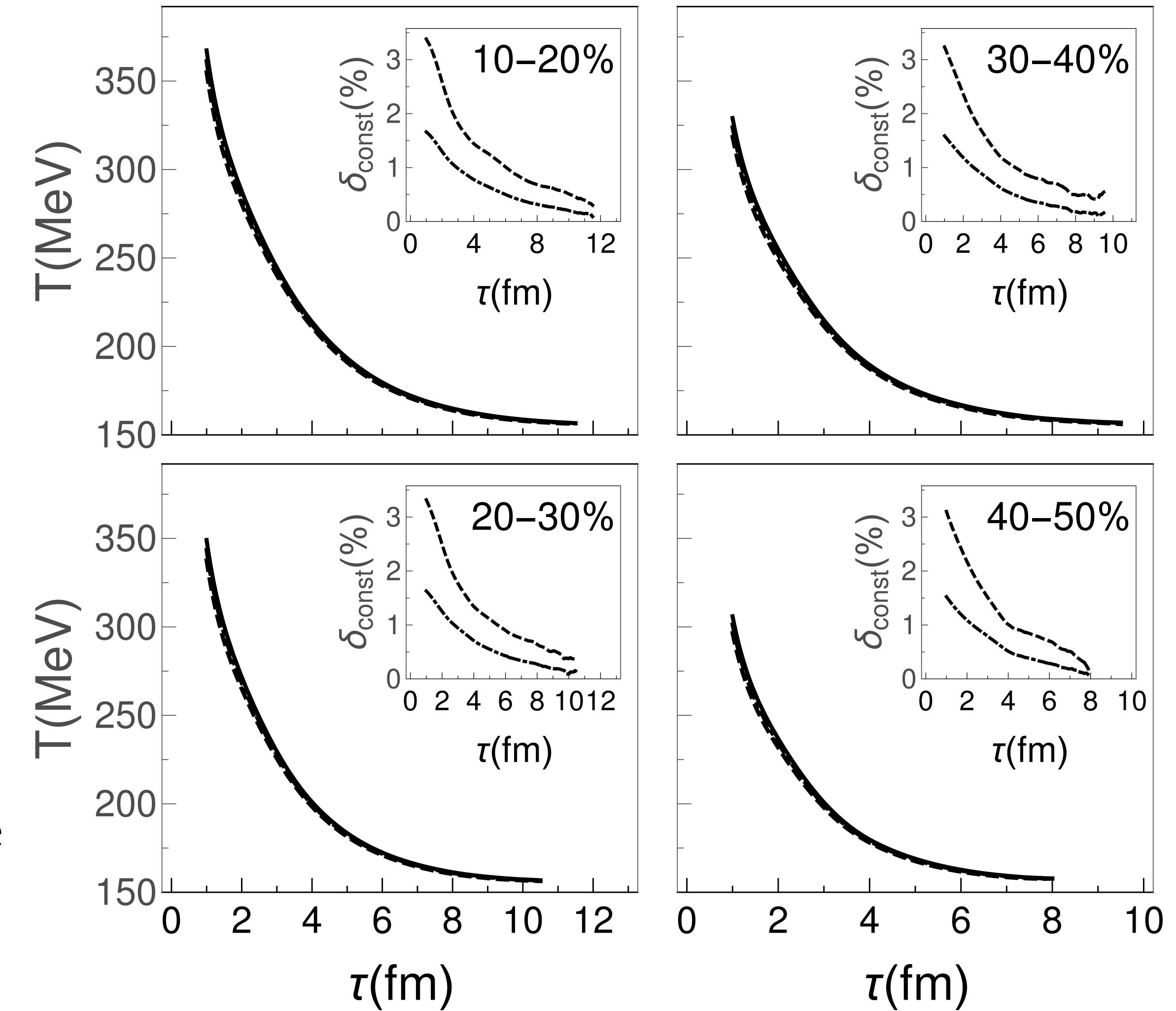
European Research Council

Established by the European Commission

# Average jet perceived temperature

BK, D. Zivic, I. Salom, J. Auvinen, P. Huovinen, M. Djordjevic and M. Djordjevic arXiv:2305.11318

- Pb + Pb  $\sqrt{s} = 5.02$  TeV
- Full = LHHQ; DotDashed = Nature,  
Dashed = Constant
- Inset: Dotdashed = Nature,  
Dashed = LHHQ
- Temperature difference during evolution  
is very small.
- Insufficient to lead to observable difference  
in the results.



- Mass of light quark  $M = \mu_E/6$
- Mass of charm and bottom quark 1.2 GeV and 4.75 GeV
- Gluon mass  $m_g = \mu_E/\sqrt{2}$
- $\mu_M/\mu_E = 0.6$
- $\Lambda_{QCD} = 0.2 GeV$ 
  - Constant  $\eta/s$  (0.15 for Pb+Pb and 0.12 for Au+Au collision)
  - Nature:  $(\eta/s)_{min} = 0.1, (\eta/s)_{slope} = 1.11, (\eta/s)_{crv} = -0.48$
  - LHHQ:  $(\eta/s)_{min} = 0.04, (\eta/s)_{slope} = 3.30, (\eta/s)_{crv} = 0$
- Bulk viscosity parametrized as  $(\zeta/s)(T) = \frac{(\zeta/s)_{max}}{1 + \left(\frac{T - T_0}{(\zeta/s)_{width}}\right)^2}$  with  $(\zeta/s)_{max} = 0.03$ ,  $(\zeta/s)_{width} = 0.022$  and  $T_0 = 0.183 GeV$ .