



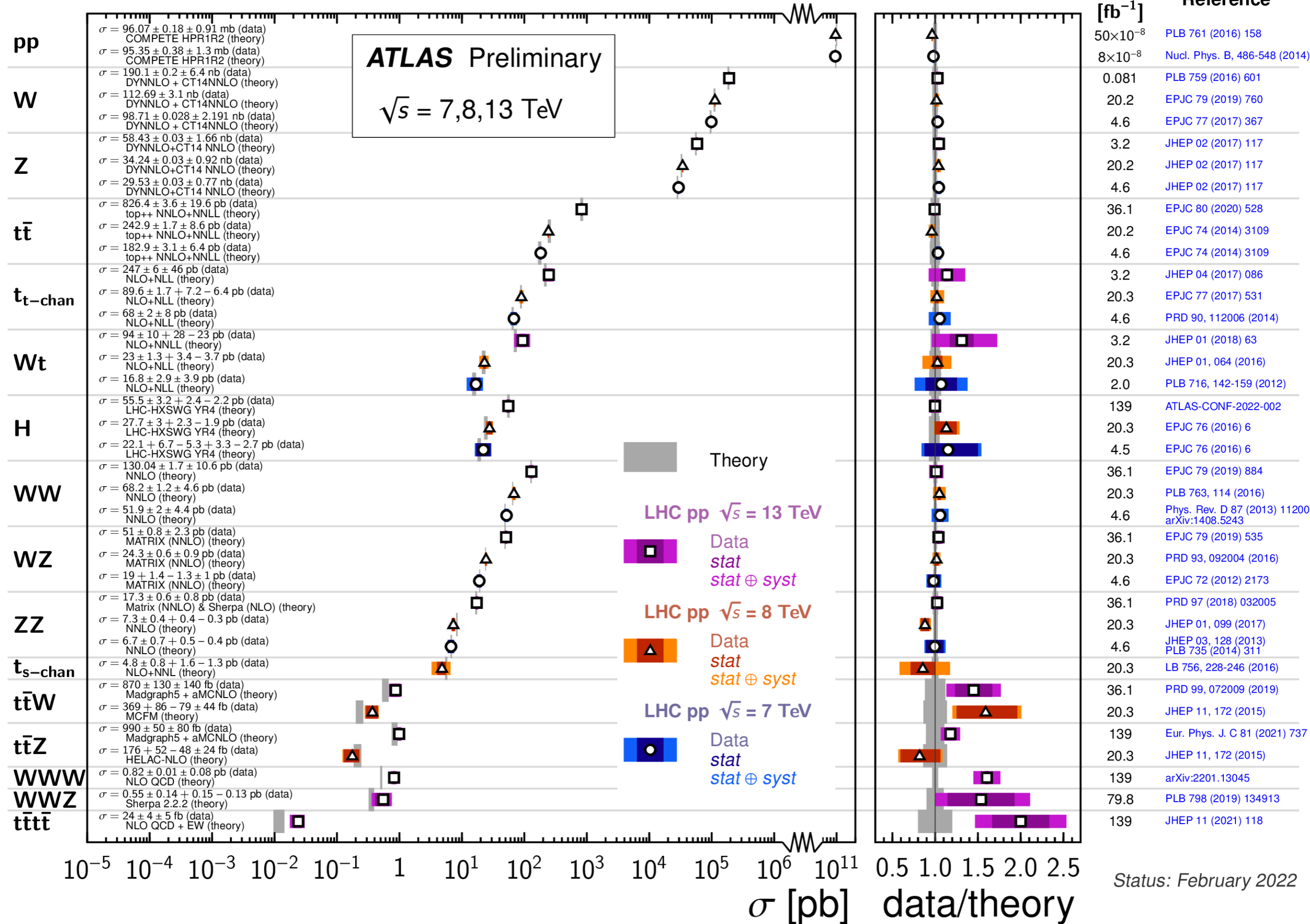
UK Research
and Innovation

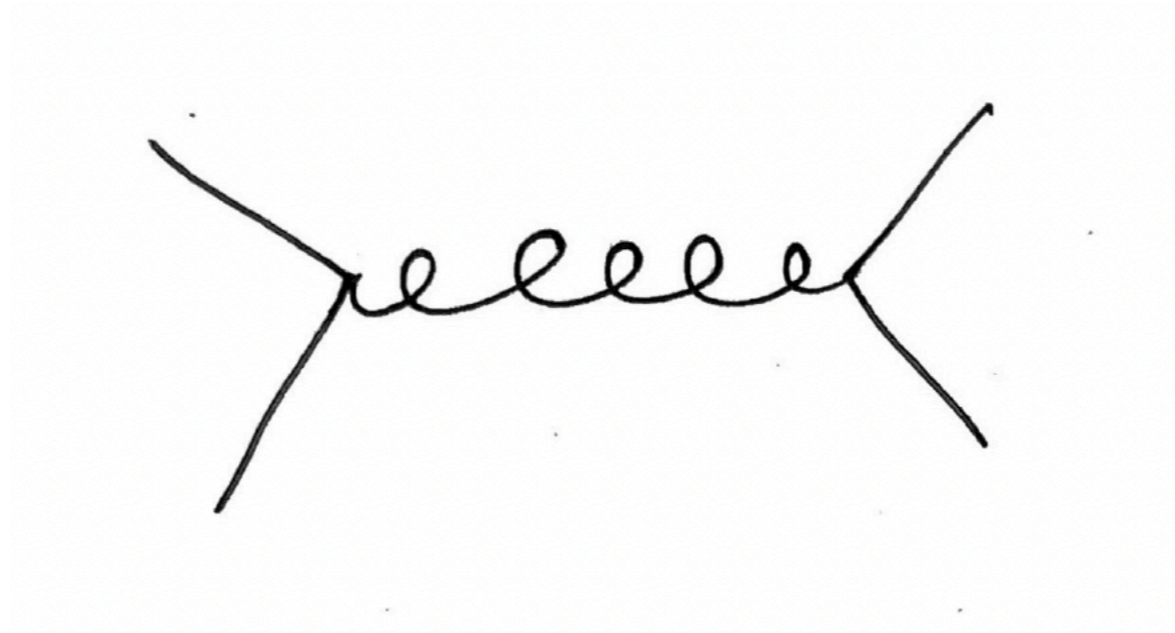
BUILDING BETTER EVENT GENERATORS FOR THE LHC

MATTHEW A. LIM

NEXT MEETING 2024, KING'S COLLEGE
LONDON

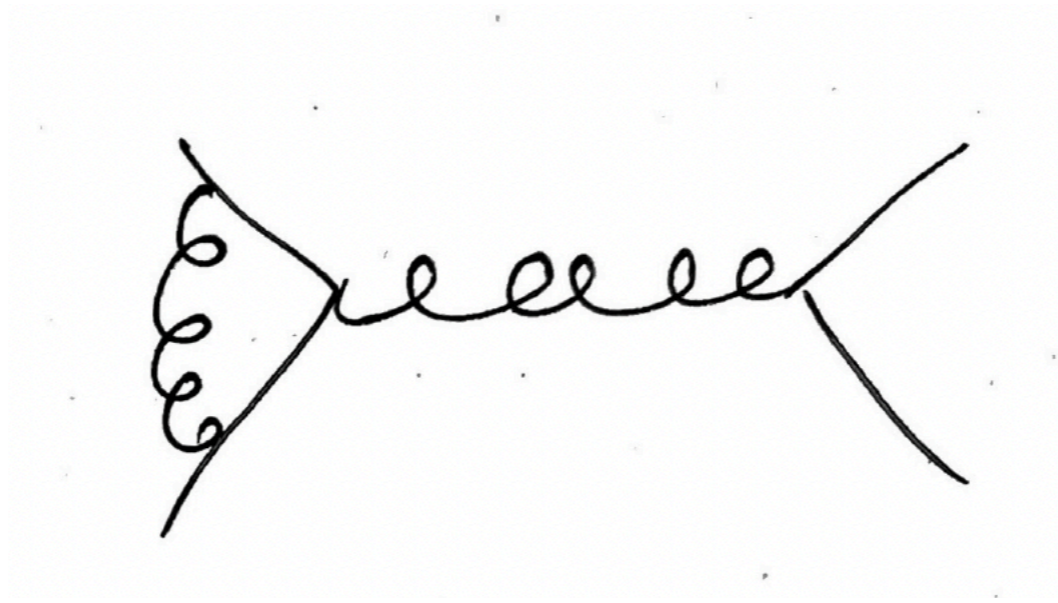
Standard Model Total Production Cross Section Measurements



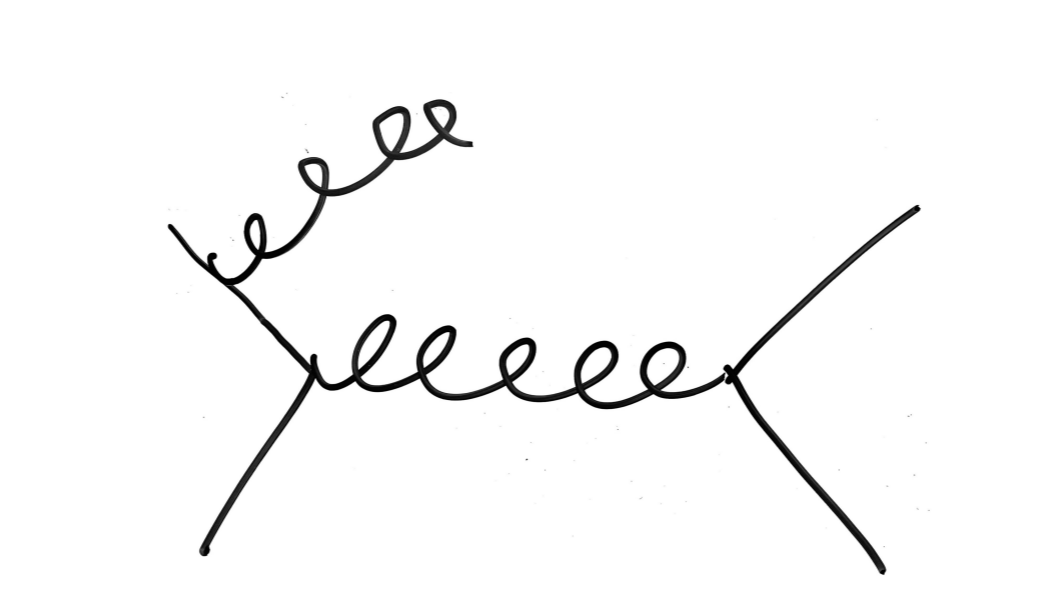


LEADING ORDER (LO)

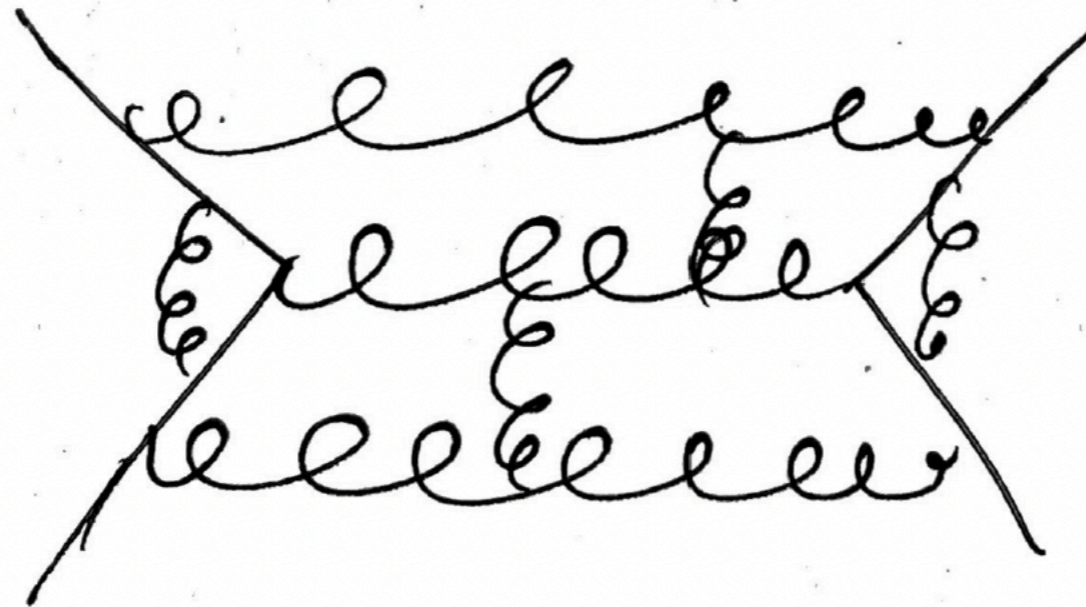
VIRTUAL



REAL



NEXT-TO-LEADING ORDER (NLO)

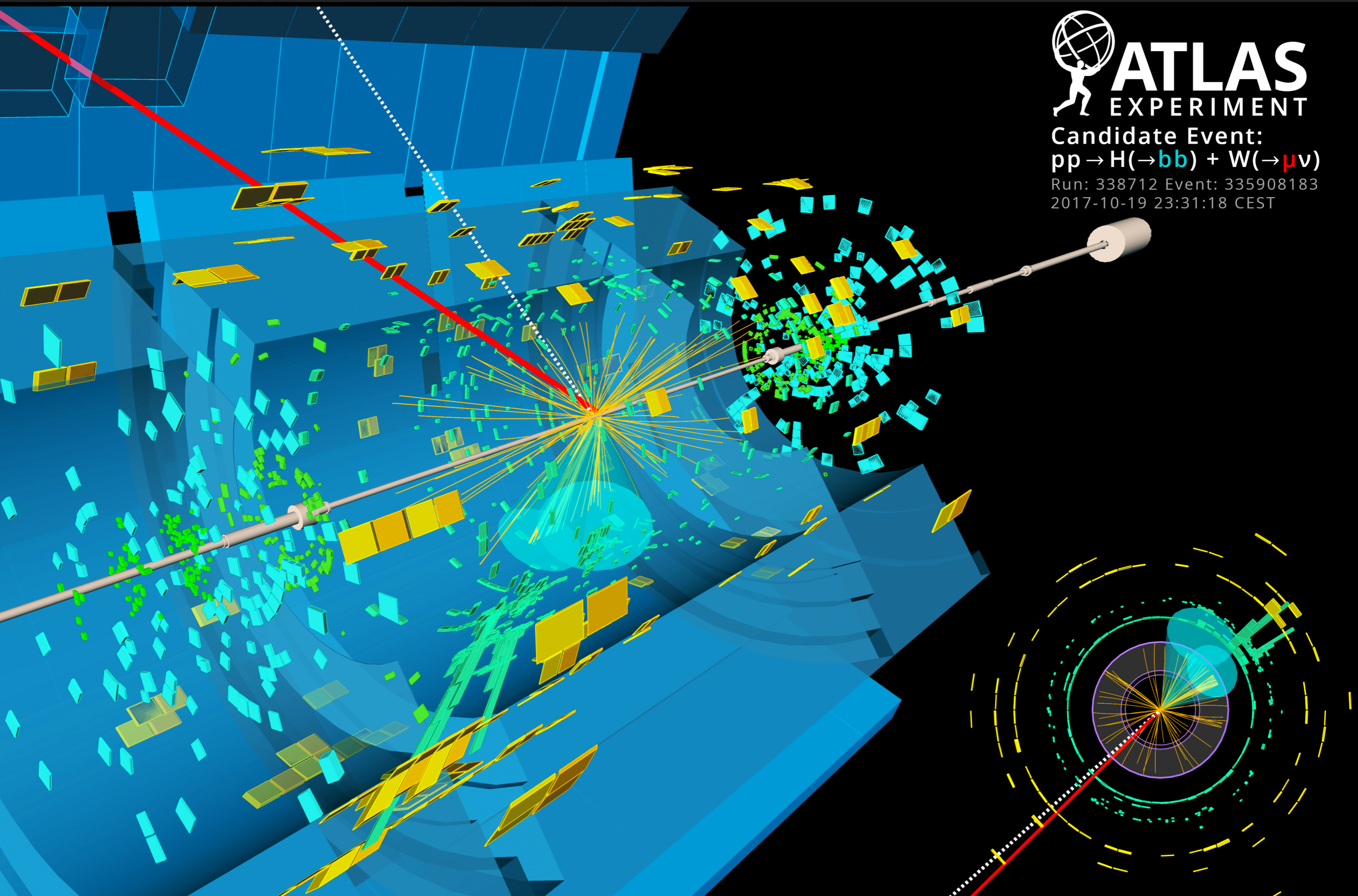


NEXT-TO-NEXT-TO-... LEADING ORDER (N^NLO)

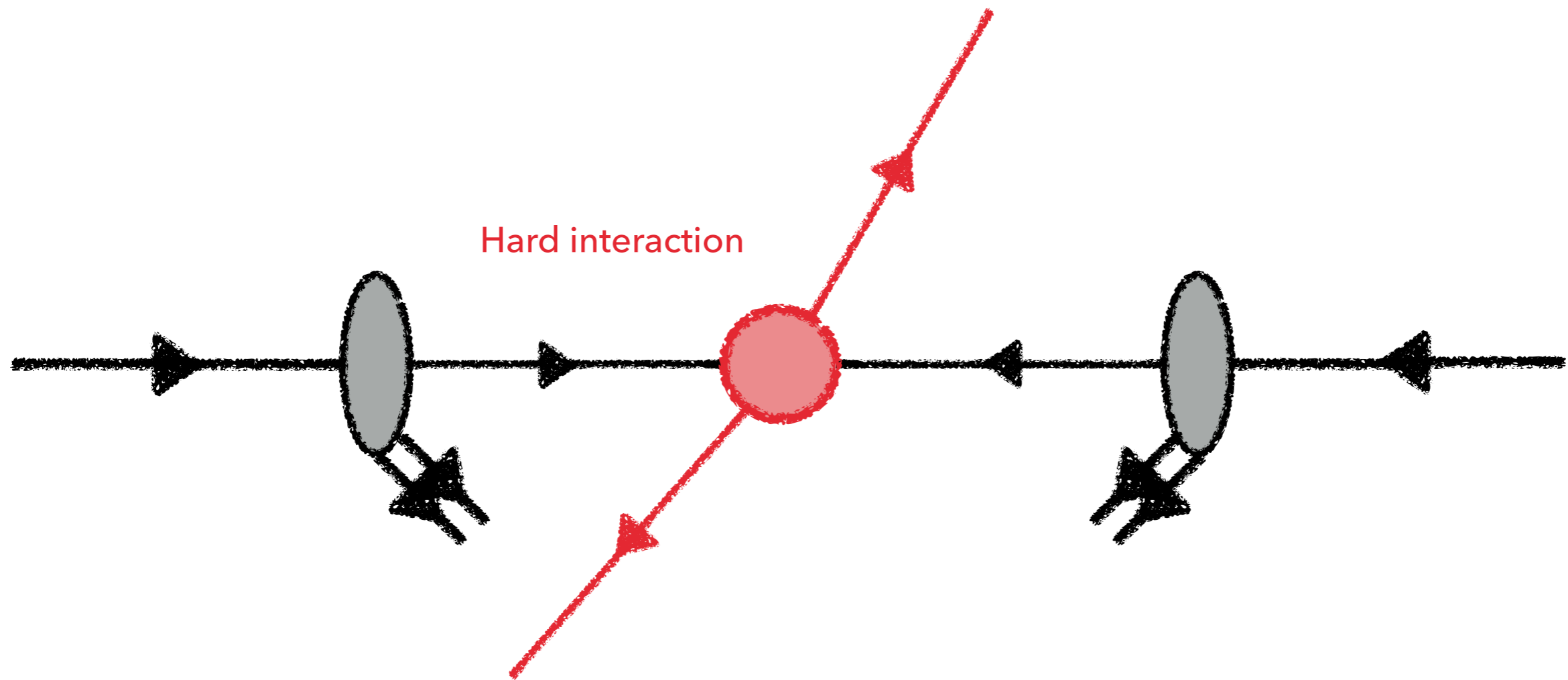


Candidate Event:
 $pp \rightarrow H(\rightarrow bb) + W(\rightarrow \mu\nu)$

Run: 338712 Event: 335908183
2017-10-19 23:31:18 CEST

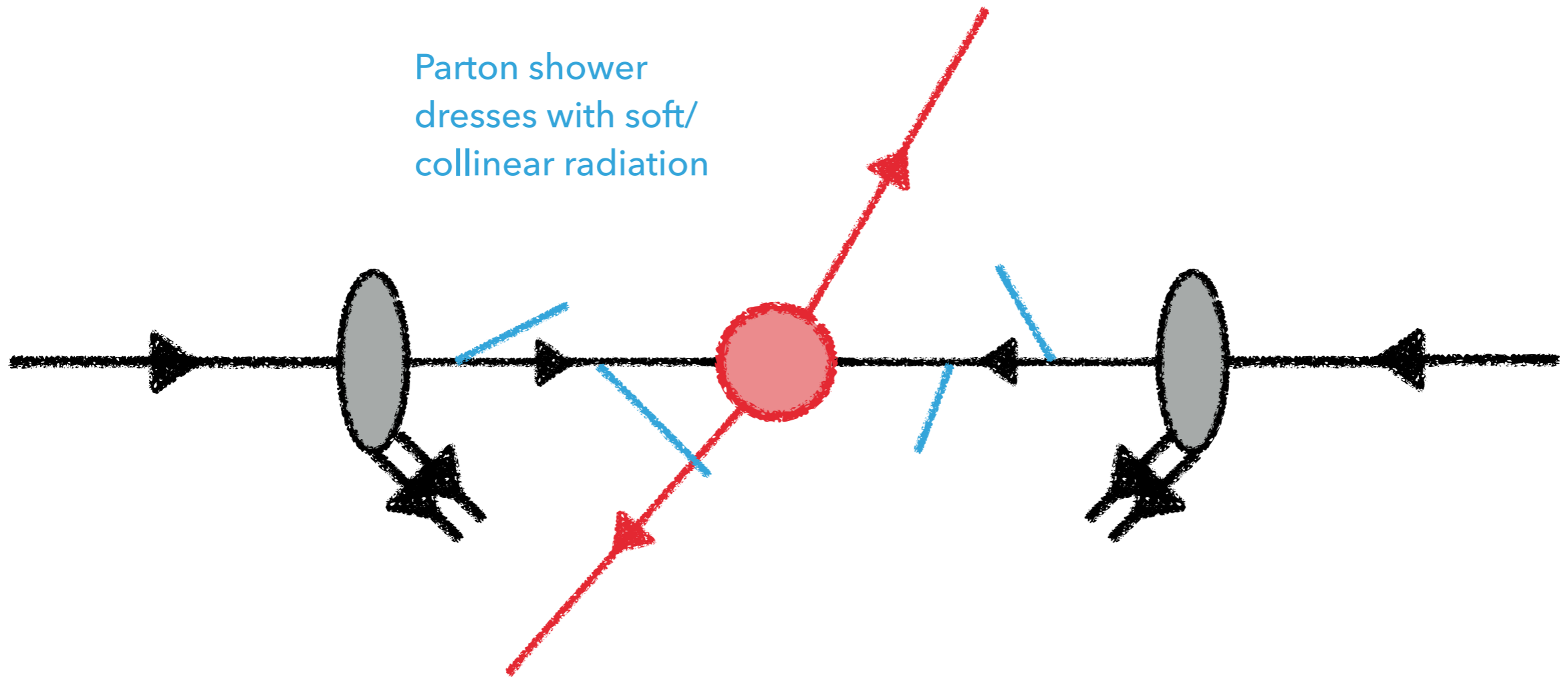


MONTE CARLO EVENT GENERATORS



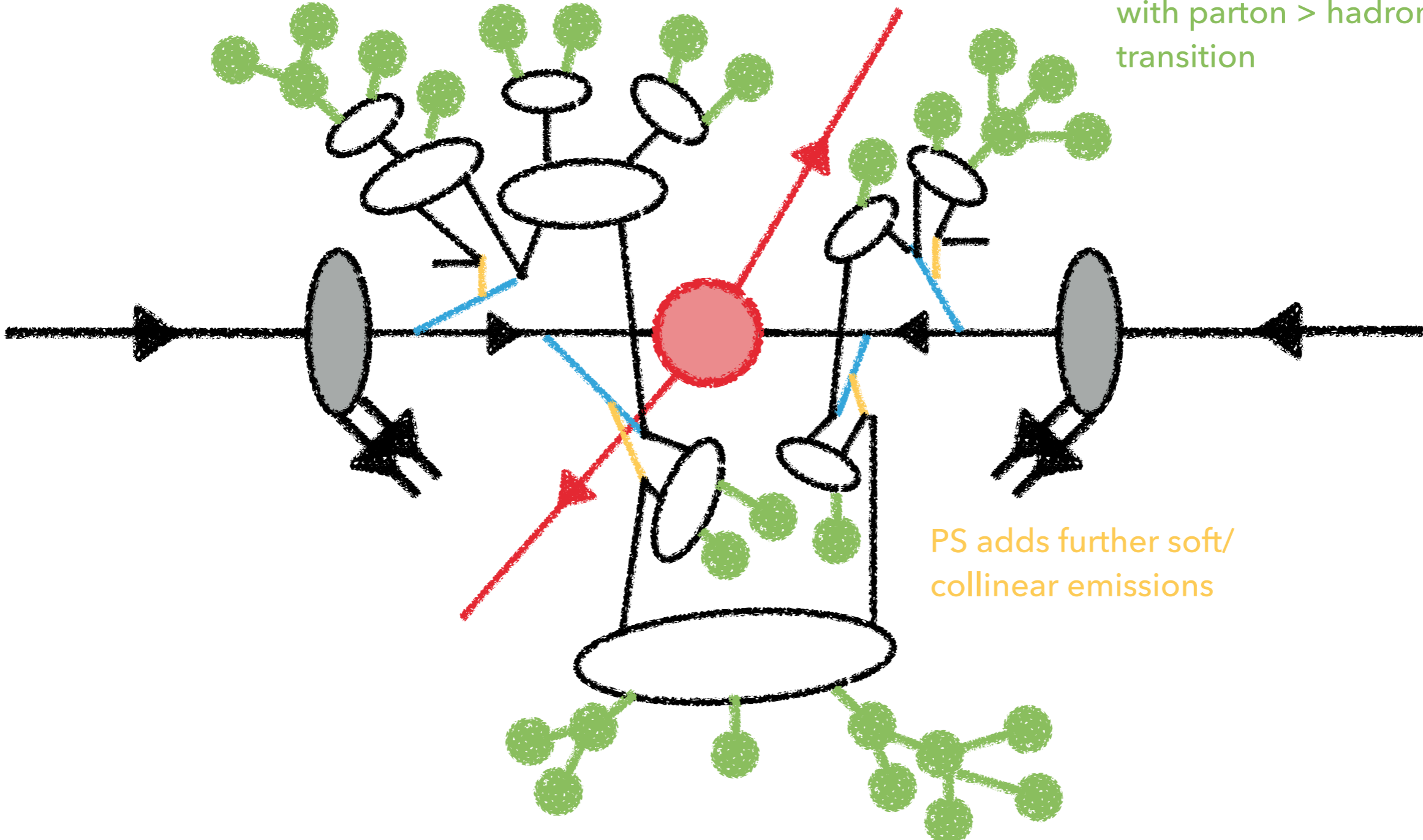
MONTE CARLO EVENT GENERATORS

Parton shower
dresses with soft/
collinear radiation



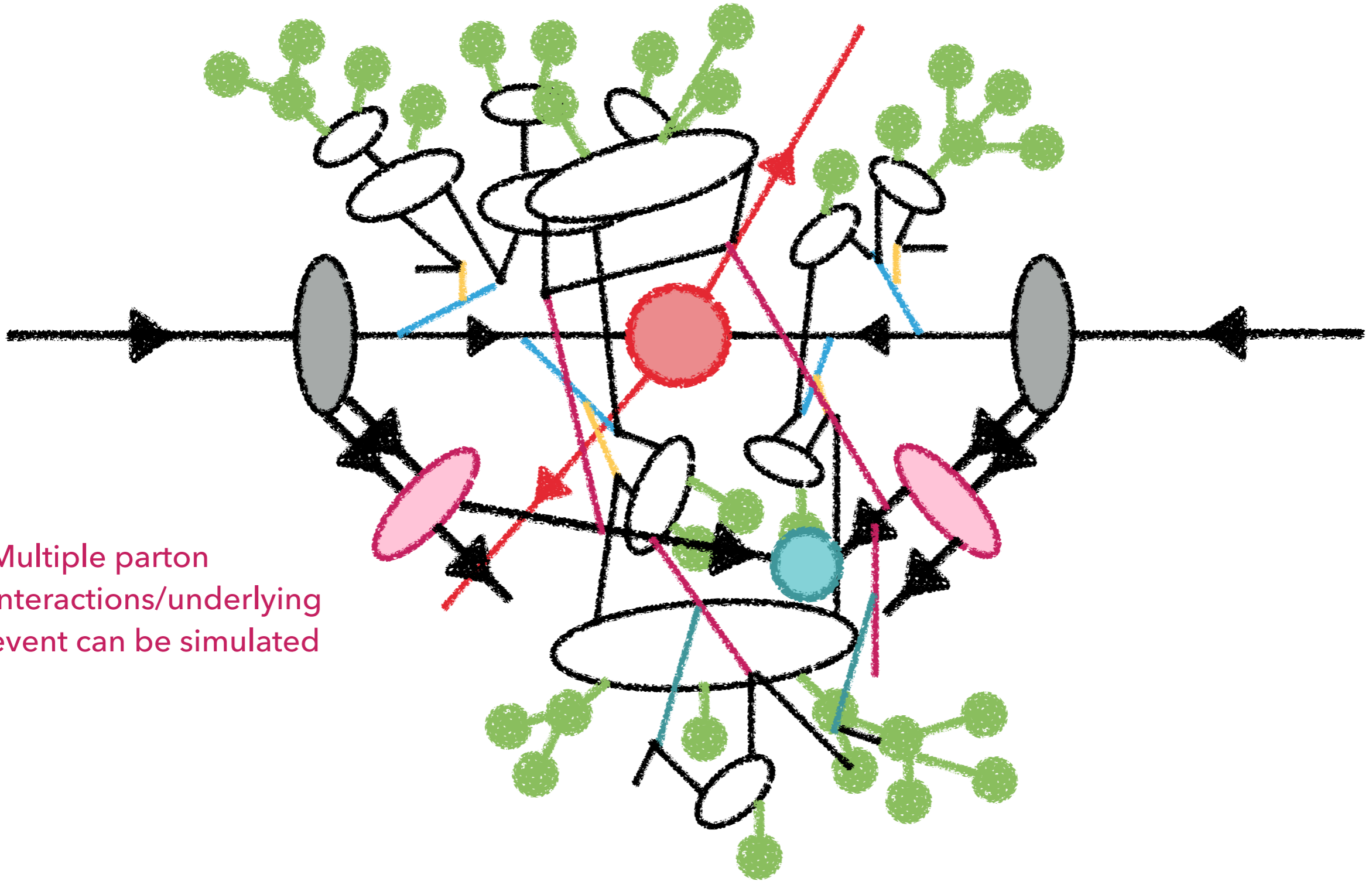
MONTE CARLO EVENT GENERATORS

Hadronisation model deals with parton > hadron transition



PS adds further soft/collinear emissions

MONTE CARLO EVENT GENERATORS



Multiple parton interactions/underlying event can be simulated

IMPROVING EVENT GENERATOR ACCURACY

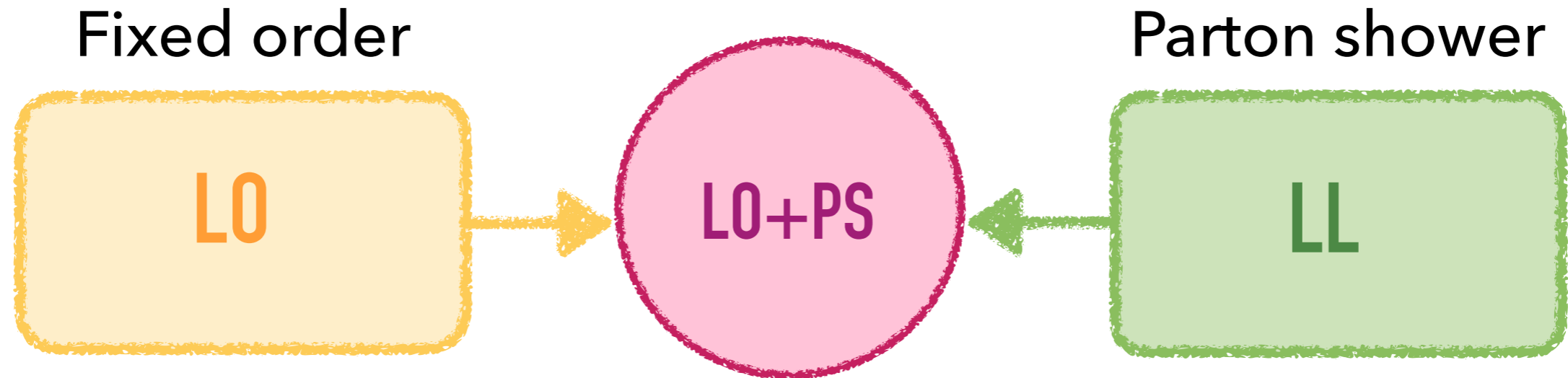
Fixed order



Parton shower



IMPROVING EVENT GENERATOR ACCURACY

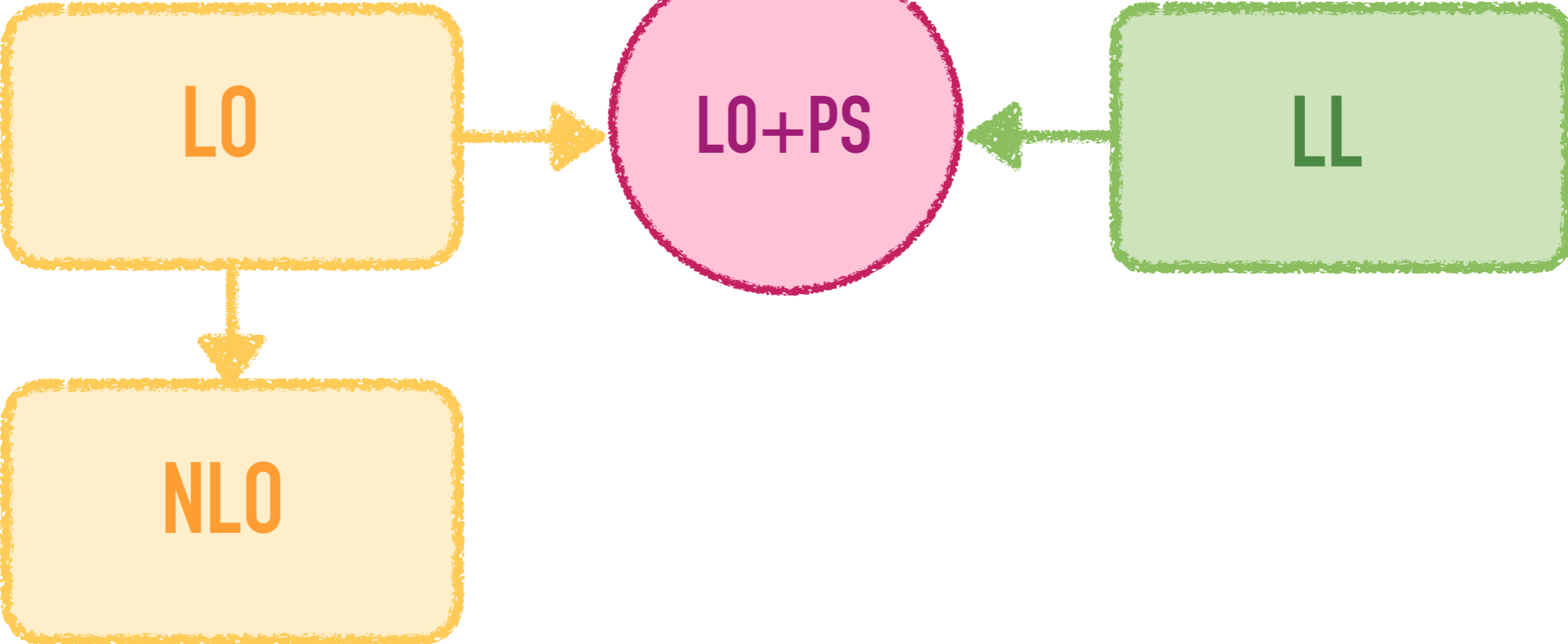


IMPROVING EVENT GENERATOR ACCURACY

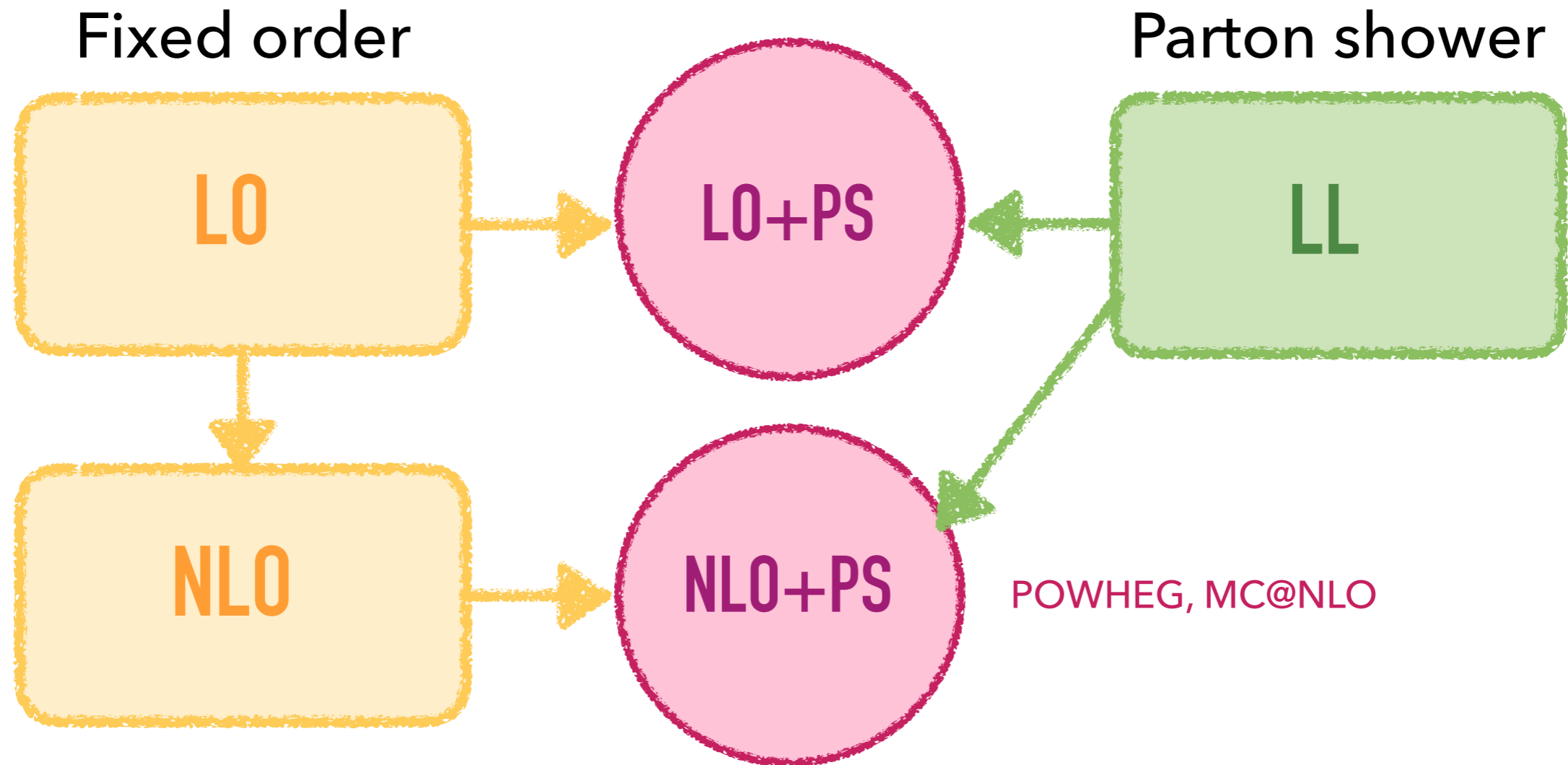
Fixed order



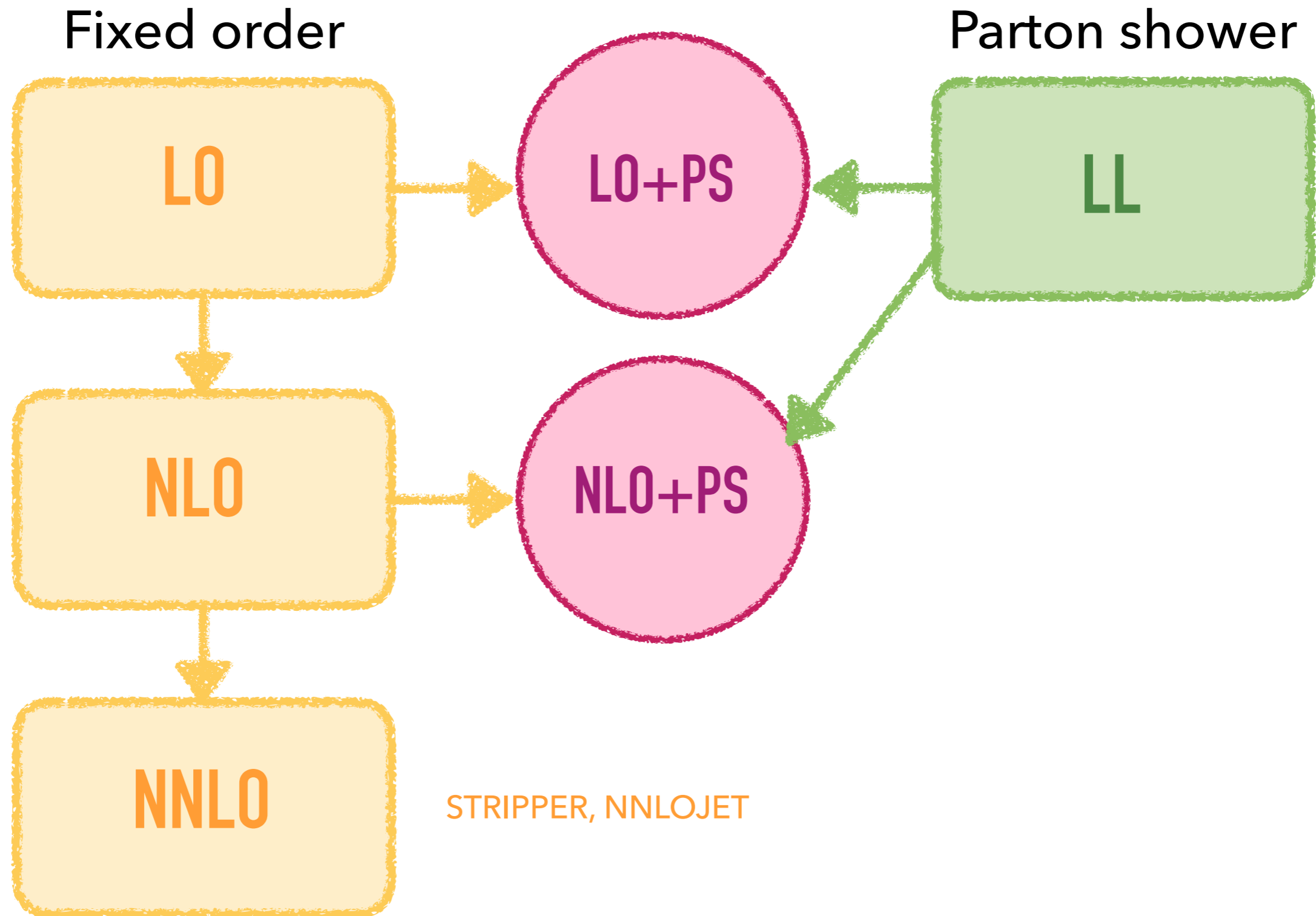
Parton shower



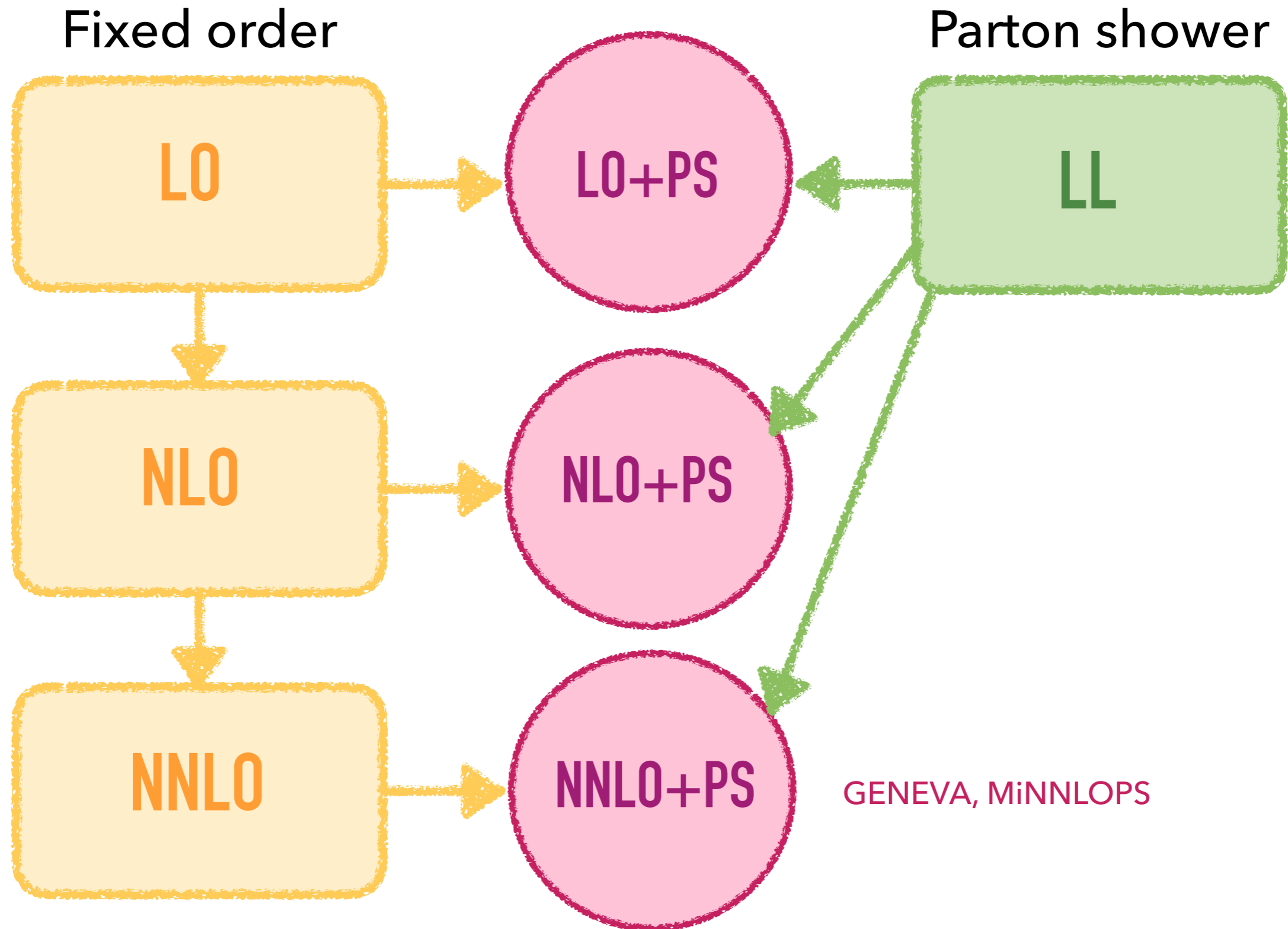
IMPROVING EVENT GENERATOR ACCURACY



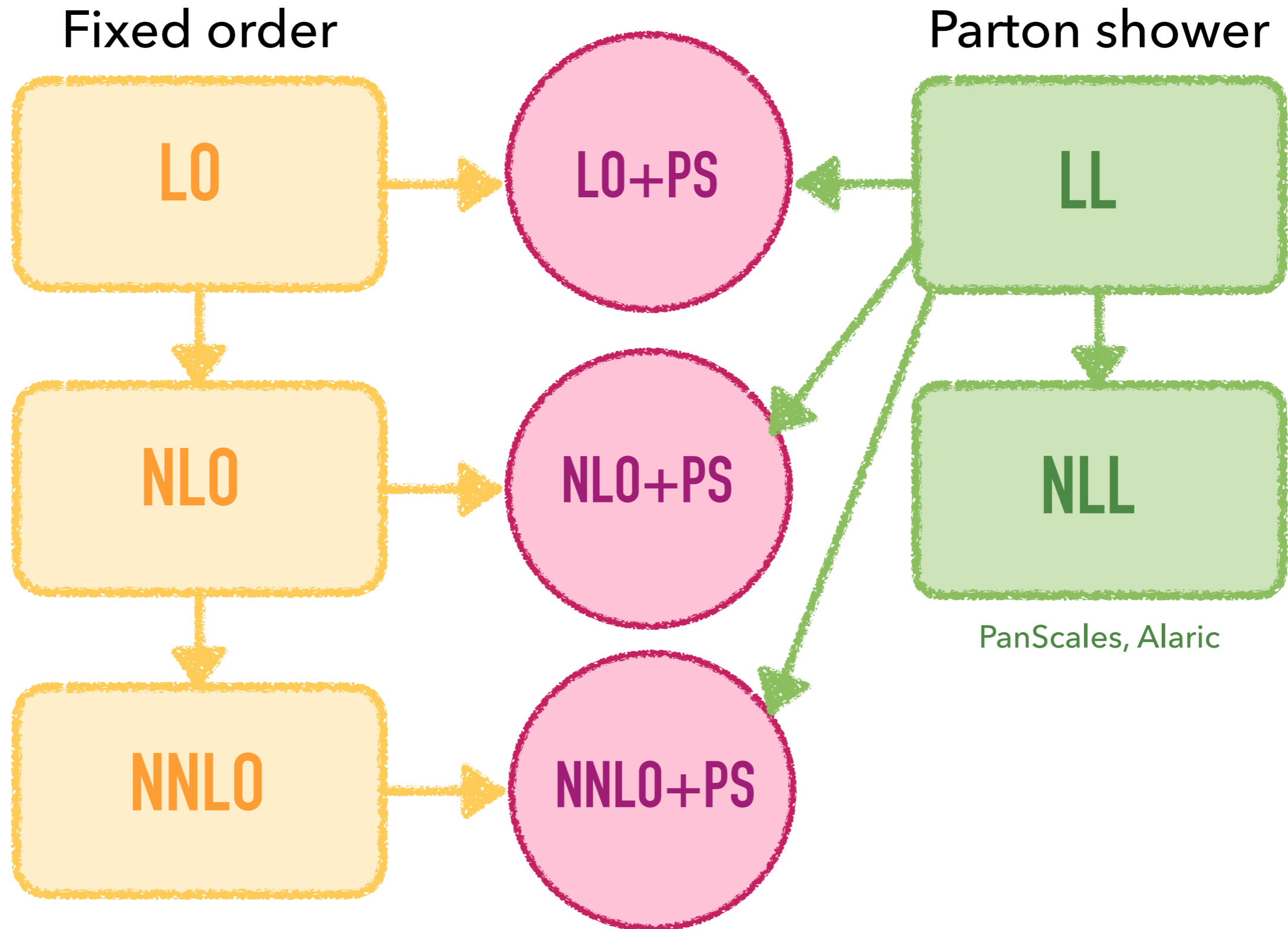
IMPROVING EVENT GENERATOR ACCURACY



IMPROVING EVENT GENERATOR ACCURACY

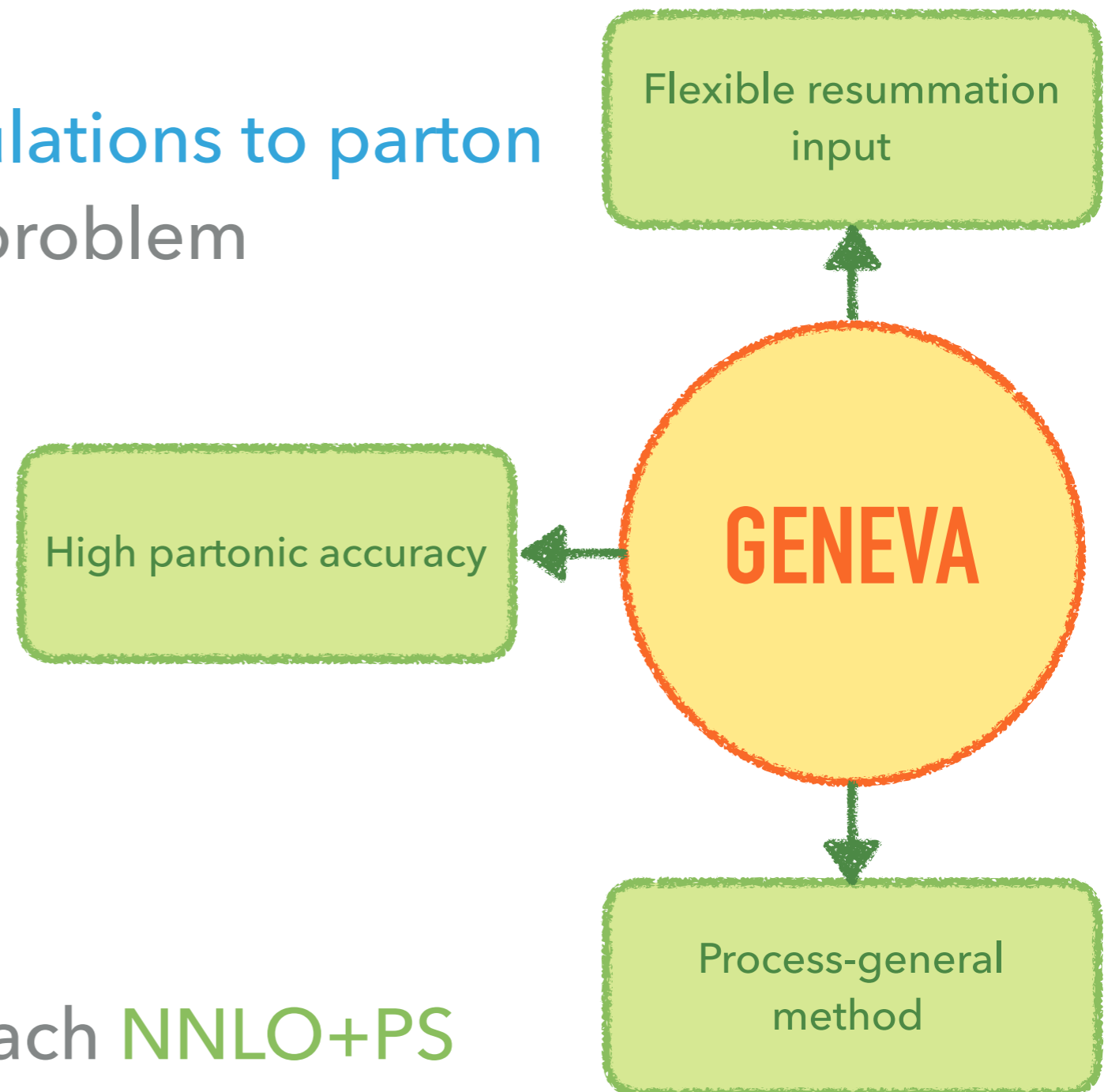


IMPROVING EVENT GENERATOR ACCURACY



HIGHER ORDER MONTE CARLO EVENT GENERATORS

- ▶ Matching fixed order calculations to parton showers is a well-studied problem
- ▶ At NLO, several successful methods available - POWHEG, MC@NLO, KrkNLO, multiplicative-accumulative...
- ▶ **GENEVA** is a method to reach NNLO+PS accuracy



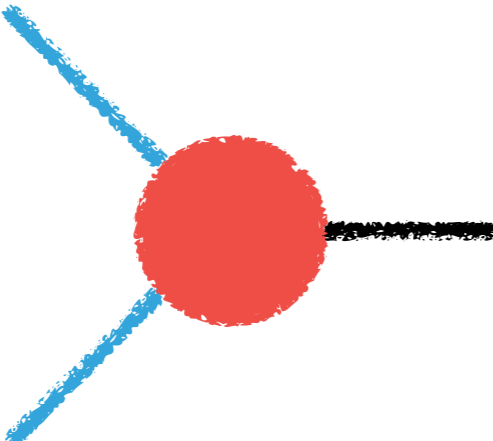
CALCULATIONS BEYOND LEADING ORDER

$$\sigma^{\text{NLO}}(X) = \int d\Phi_N [B_N(\Phi_N) + V_N^C(\Phi_N)] M_X(\Phi_N) + \int d\Phi_{N+1} \left\{ B_{N+1}(\Phi_{N+1}) M_X(\Phi_{N+1}) - \sum_m C_{N+1}^m(\Phi_{N+1}) M_X[\hat{\Phi}_N^m(\Phi_{N+1})] \right\}$$

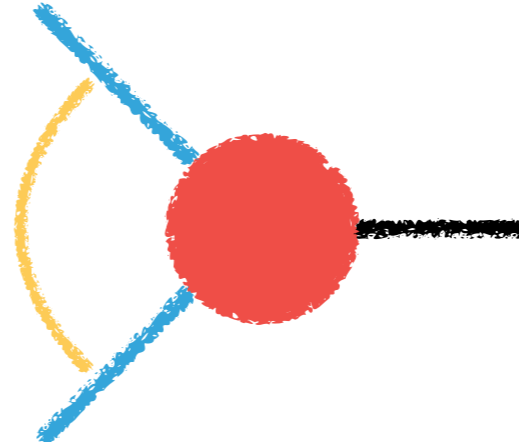
- ▶ Calculations beyond leading order suffer from **infrared divergences**
- ▶ Happens when particles become indistinguishable - soft (low-energy) or collinear
- ▶ Divergences cancel between matrix elements with different numbers of final-state particles

DEFINING IR-FINITE EVENTS

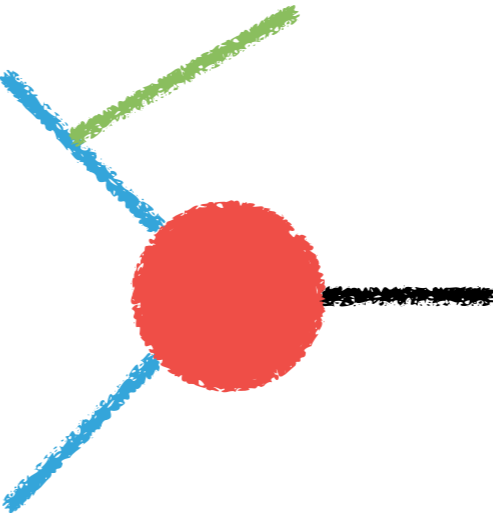
BORN



0-JET



VIRTUAL

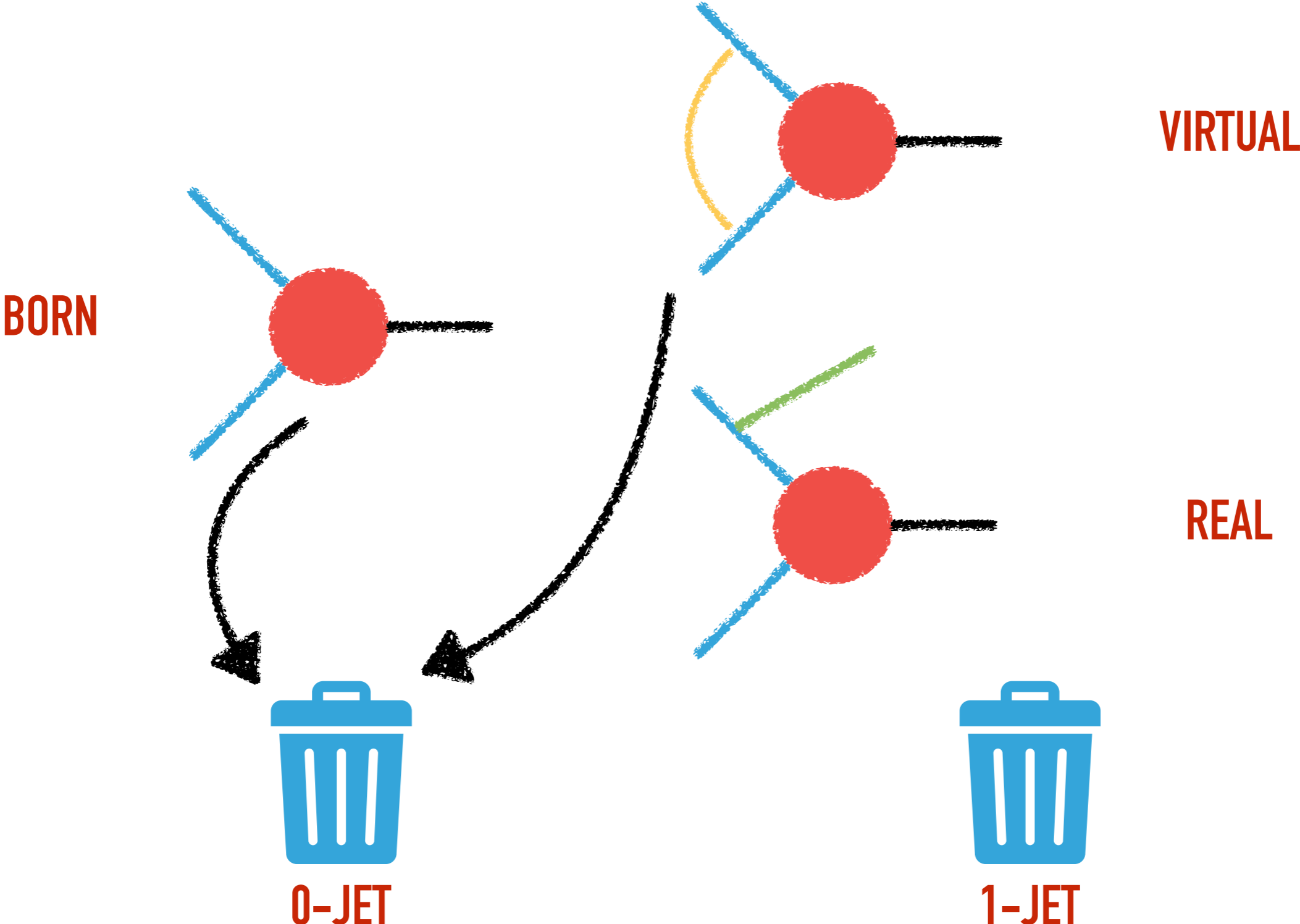


REAL

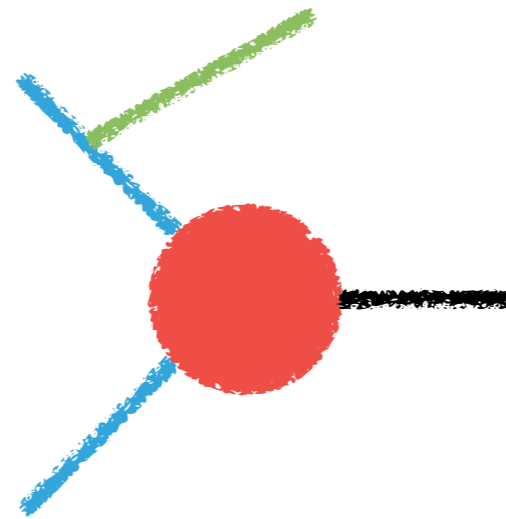


1-JET

DEFINING IR-FINITE EVENTS



DEFINING IR-FINITE EVENTS



REAL



0-JET

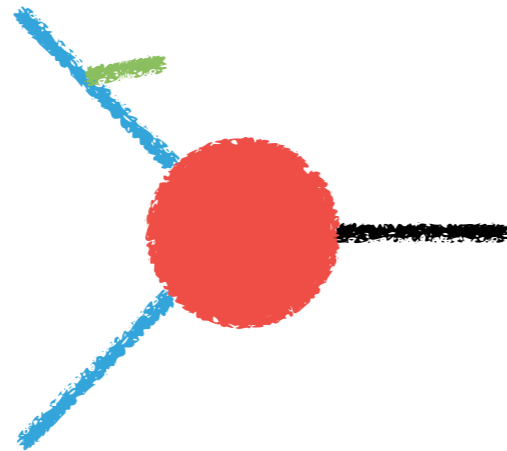


1-JET

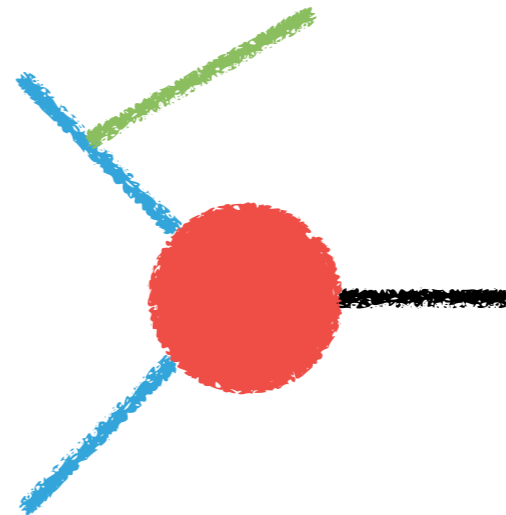
DEFINING IR-FINITE EVENTS

SOFT/COLL. REAL

$$r_0 < r_0^{\text{cut}}$$



0-JET



1-JET

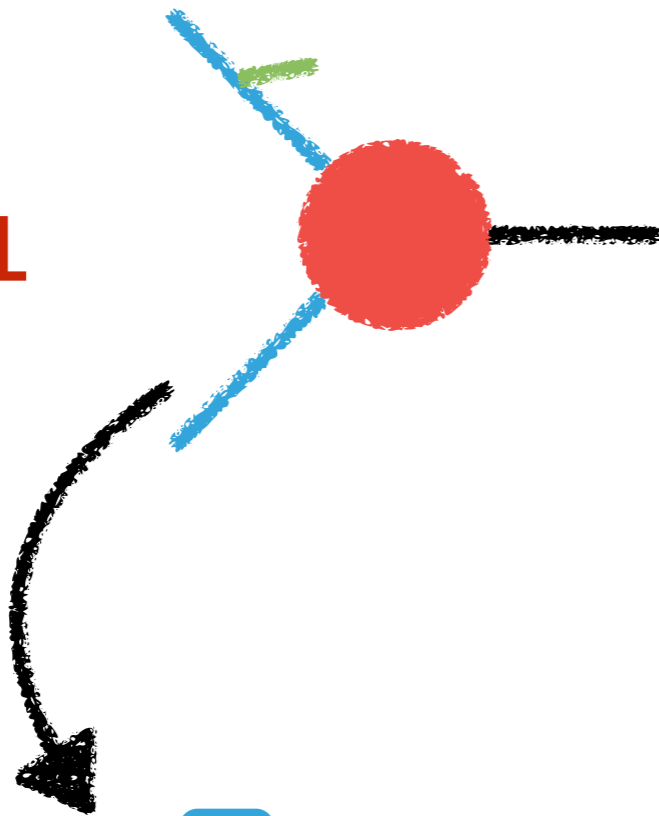
HARD REAL

$$r_0 > r_0^{\text{cut}}$$

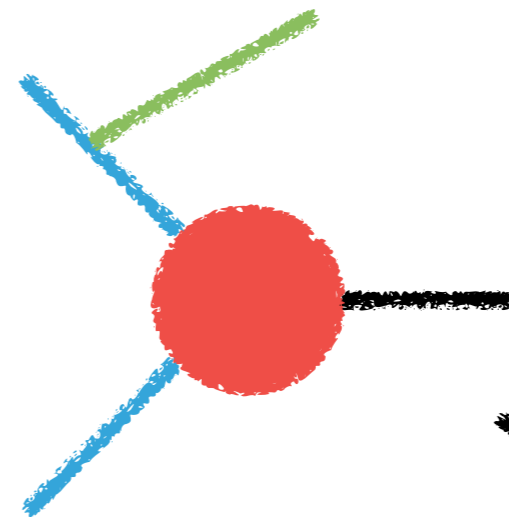
DEFINING IR-FINITE EVENTS

SOFT/COLL. REAL

$$r_0 < r_0^{\text{cut}}$$



0-JET

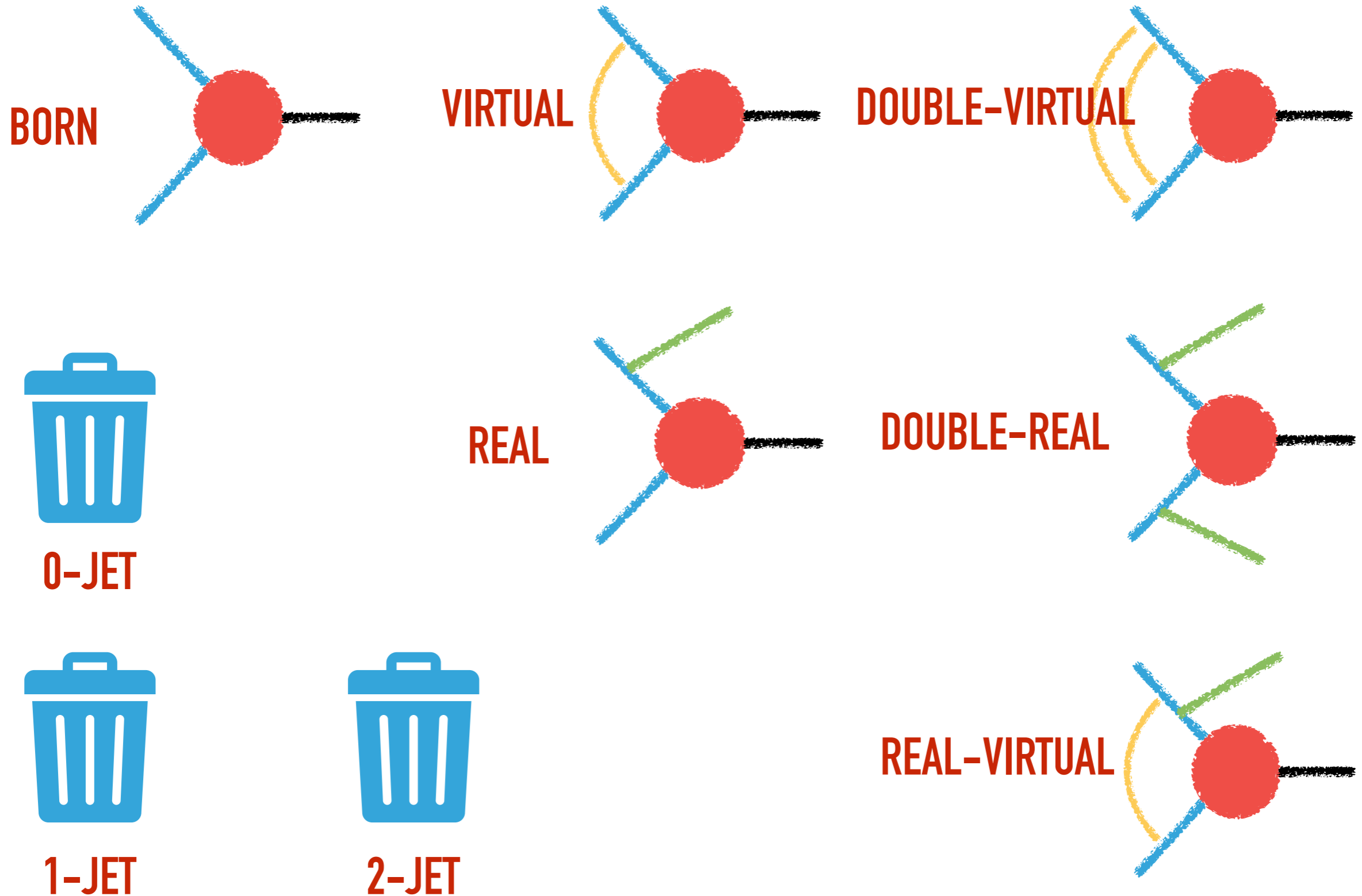


1-JET

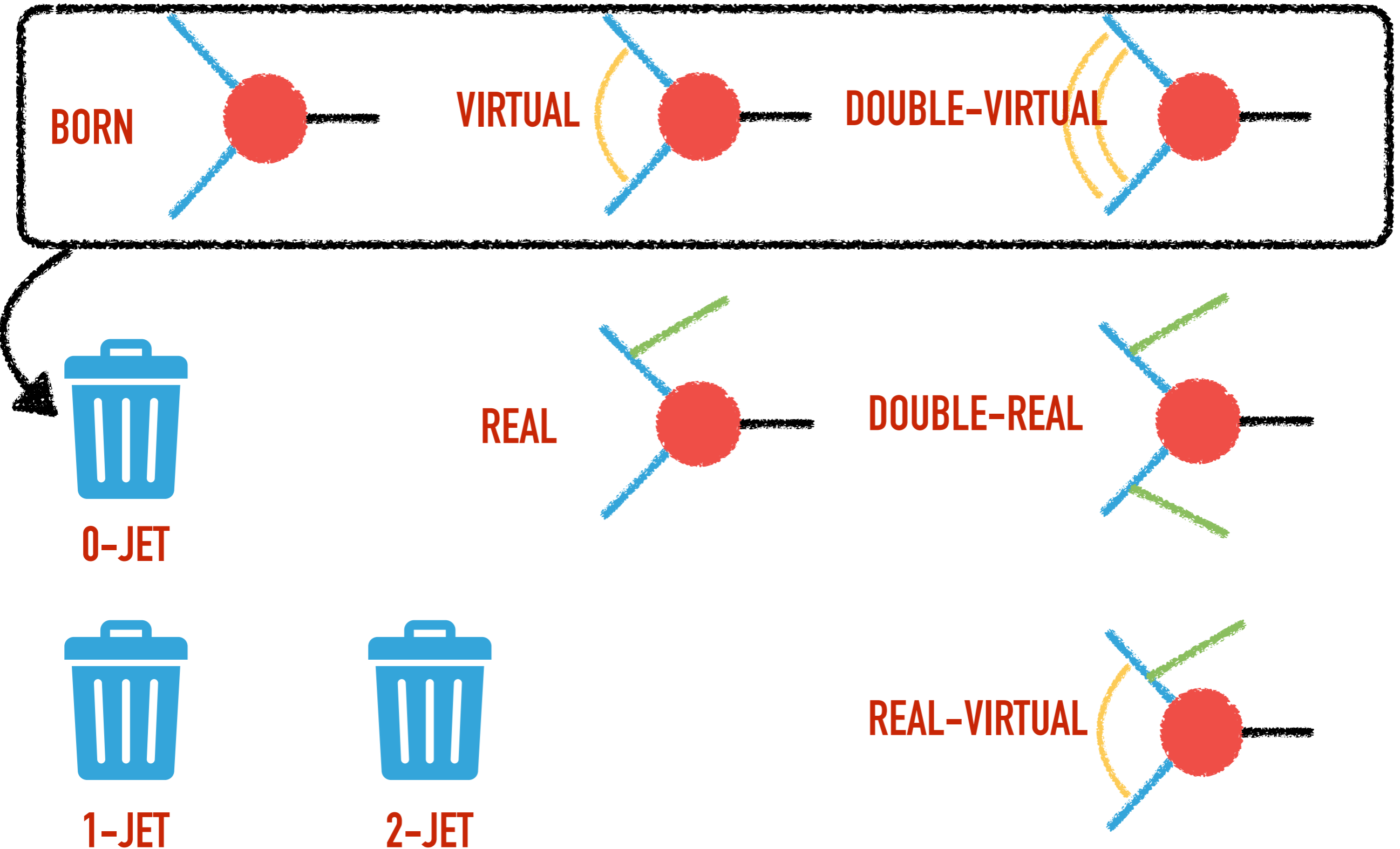
HARD REAL

$$r_0 > r_0^{\text{cut}}$$

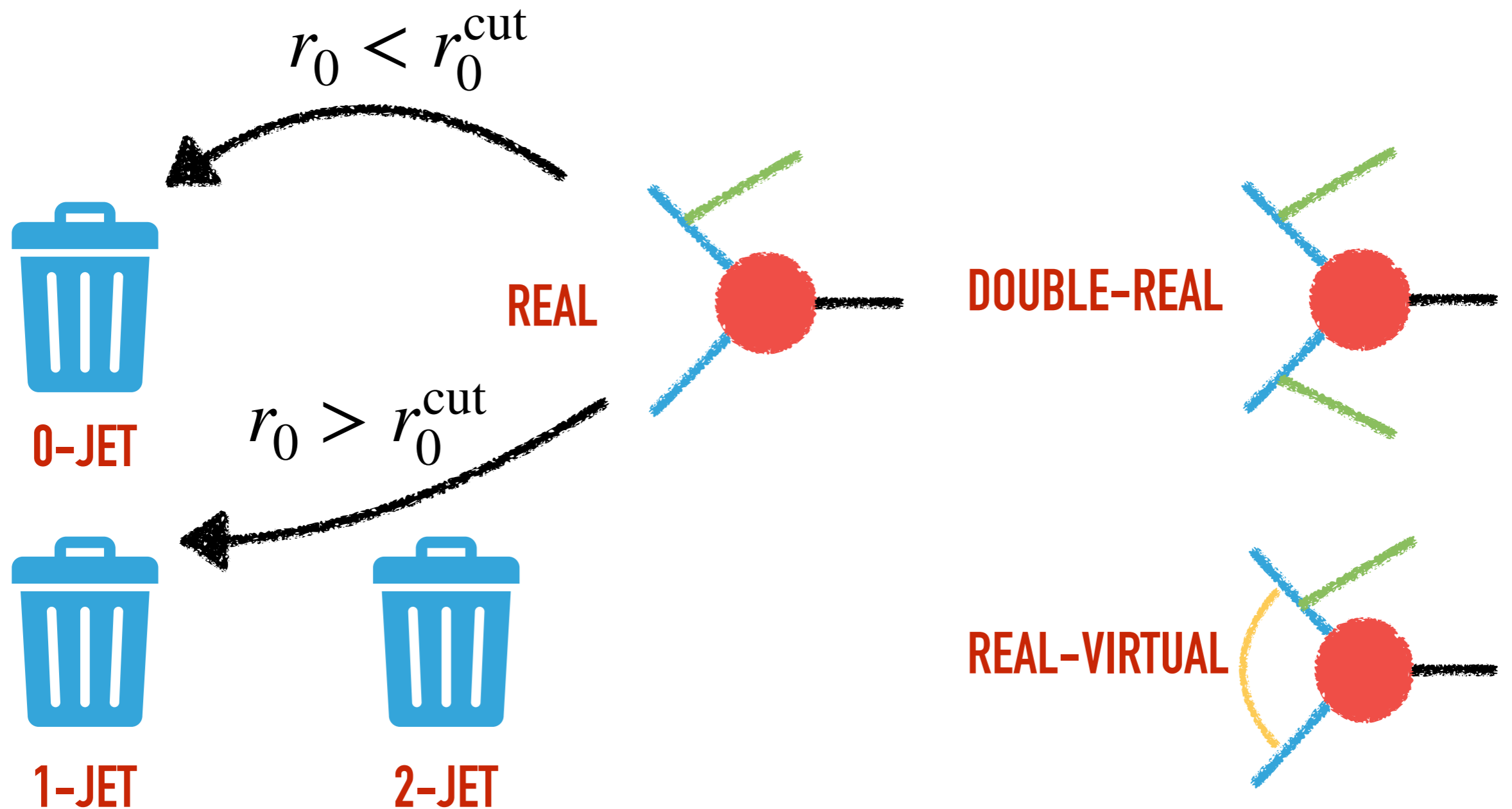
DEFINING IR-FINITE EVENTS



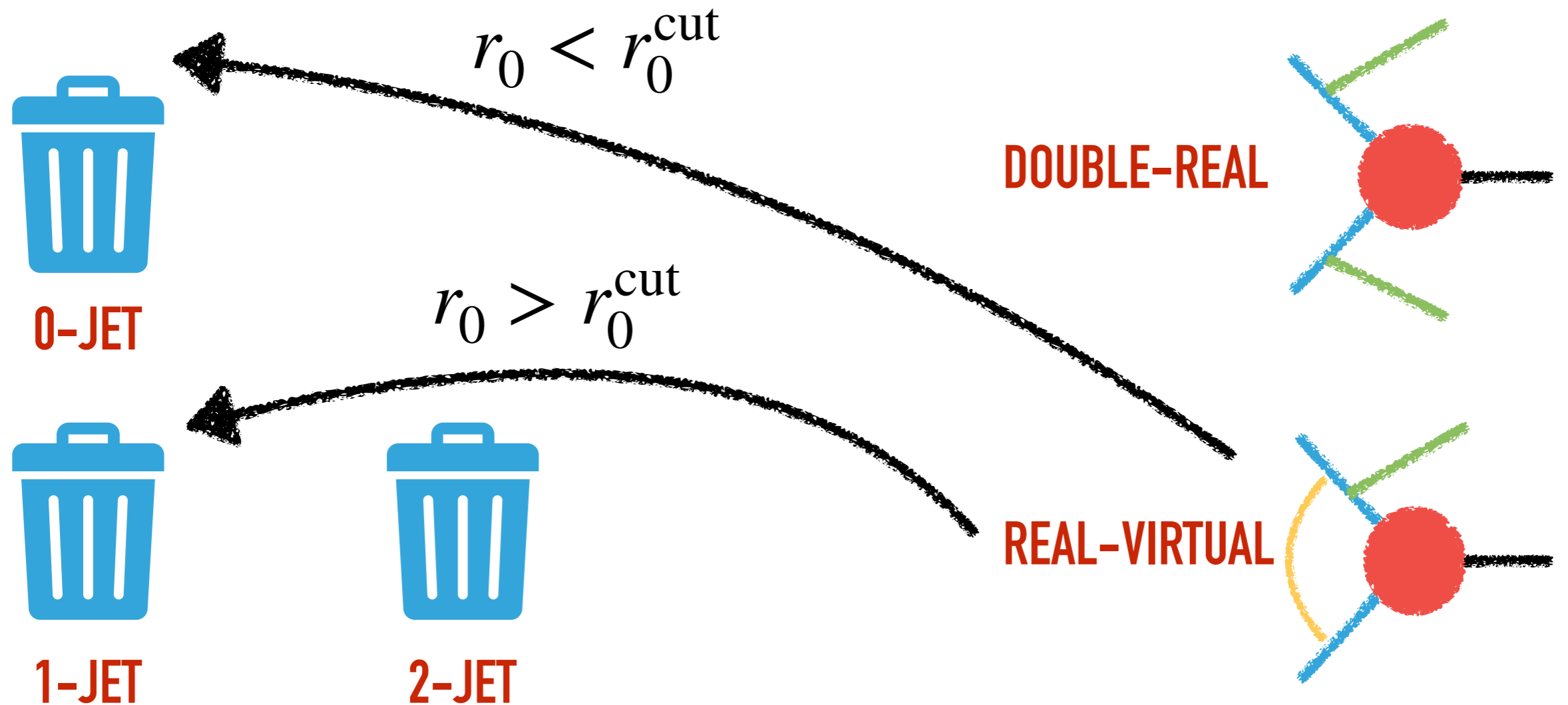
DEFINING IR-FINITE EVENTS



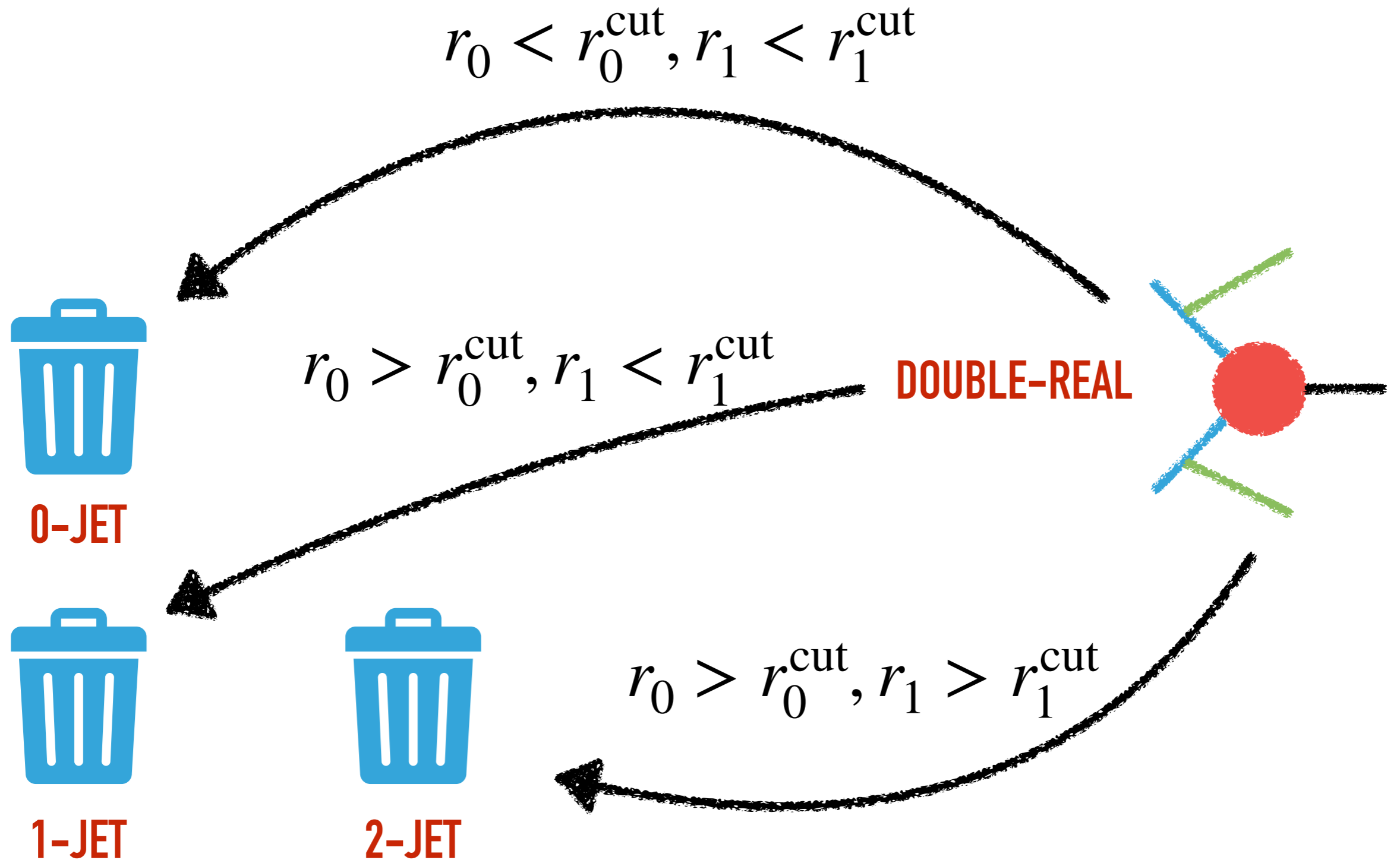
DEFINING IR-FINITE EVENTS



DEFINING IR-FINITE EVENTS



DEFINING IR-FINITE EVENTS



DEFINING IR-FINITE EVENTS

- ▶ Defining events this way introduced a **projection** from a higher multiplicity to a lower multiplicity phase space
- ▶ Results are only (N)NLO accurate up to **power corrections** in r_0^{cut} - **as $r_0^{\text{cut}} \rightarrow 0$** , exact fixed order result is recovered
- ▶ Causes **large logarithms** to appear which spoil perturbative convergence!

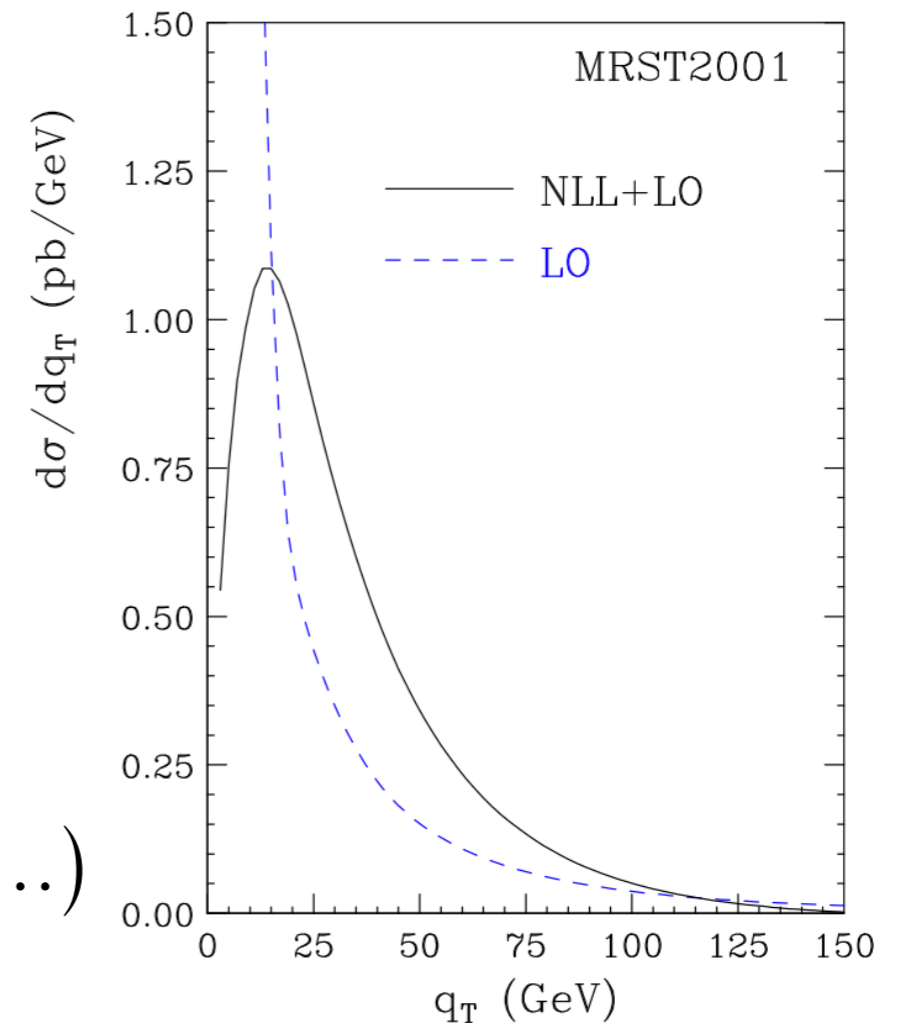
$$L = \log(Q/r_0^{\text{cut}}) \text{ becomes large...}$$

RESUMMATION – THE CURE FOR LARGE LOGS

- ▶ Large logs signal the **breakdown of the perturbative series** in the coupling, leading term $\alpha L^2 \sim 1 \Rightarrow \alpha L \ll 1$
- ▶ **Reordering the series** to expand in a genuinely small parameter cures behaviour

$$d\sigma = C(\alpha_s) \exp \left(Lg_1(\alpha_s L) + g_2(\alpha_s L) + \alpha_s g_3(\alpha_s L) + \dots \right)$$

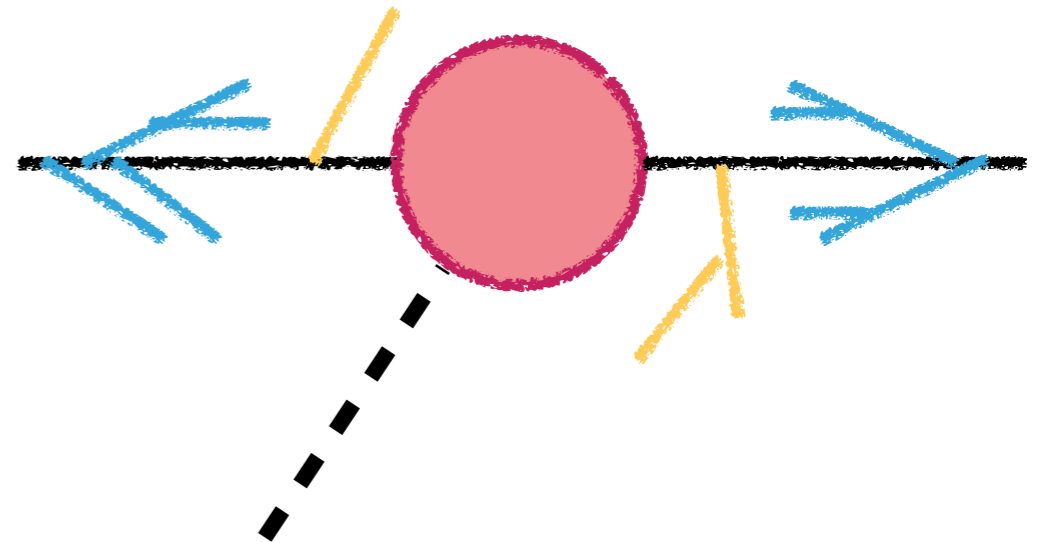
- ▶ Different formalisms available to achieve this: parton branching, **soft-collinear effective theory**



RESUMMATION FROM EFFECTIVE FIELD THEORIES

- ▶ Soft-Collinear effective theory formalism - an **EFT with QCD as its UV limit**
- ▶ QCD Lagrangian split into low-energy modes
- ▶ For $r_0 \ll Q$, the partonic cross section typically factorises:

$$\frac{d\hat{\sigma}}{dr_0} \approx H(Q, \mu_H) B_i(r_0, \mu_B) \otimes B_j(r_0, \mu_B) \otimes S(r_0, \mu_S)$$



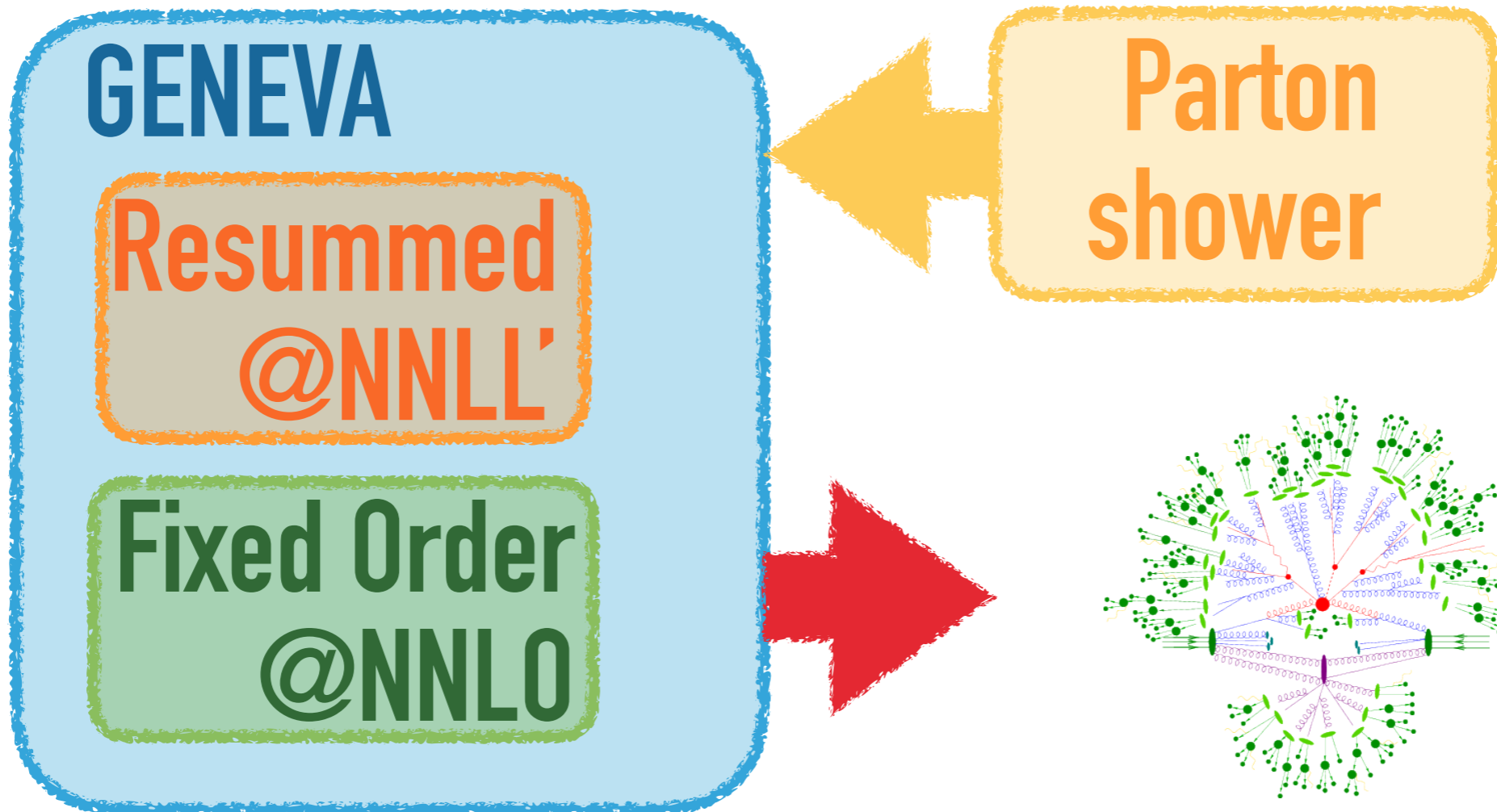
SOFT-COLLINEAR EFFECTIVE THEORY

- ▶ **Beam** and **soft** functions correspond to matrix elements of **collinear/soft** SCET modes, **hard function** gives **matching** onto full QCD (Wilson coefficient)
- ▶ **Each component** of factorisation theorem is **evaluated at its own scale** \implies no large logs! Evolution to common scale via **double-log RGE** resums large log terms.

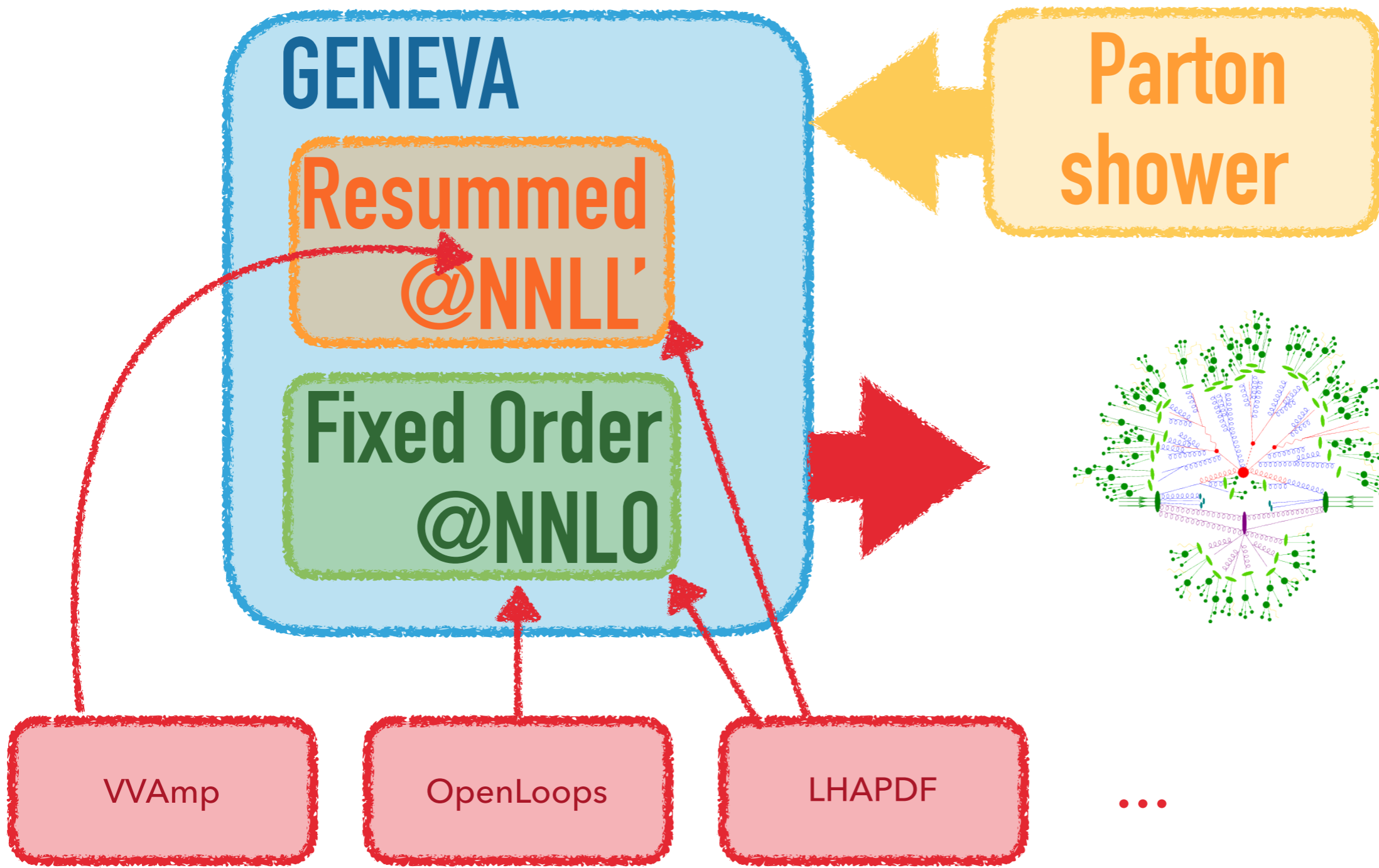
$$\frac{d}{d \ln \mu} \ln H(\Phi_0, \mu) = \Gamma_{\text{cusp}} \ln \frac{\mu_H^2}{\mu^2} + \gamma_H$$

- ▶ **Accuracy improvable** by going to higher loop orders

COMBINING RESUMMED AND FIXED ORDER CALCULATIONS IN GENEVA



COMBINING RESUMMED AND FIXED ORDER CALCULATIONS IN GENEVA



COMBINING RESUMMED AND FIXED ORDER CALCULATIONS IN GENEVA

GENEVA

Parton

COMBINES ADVANTAGES OF
RESUMMED, FIXED ORDER AND
PARTON SHOWER!

FIXED ORDER
@NNLO



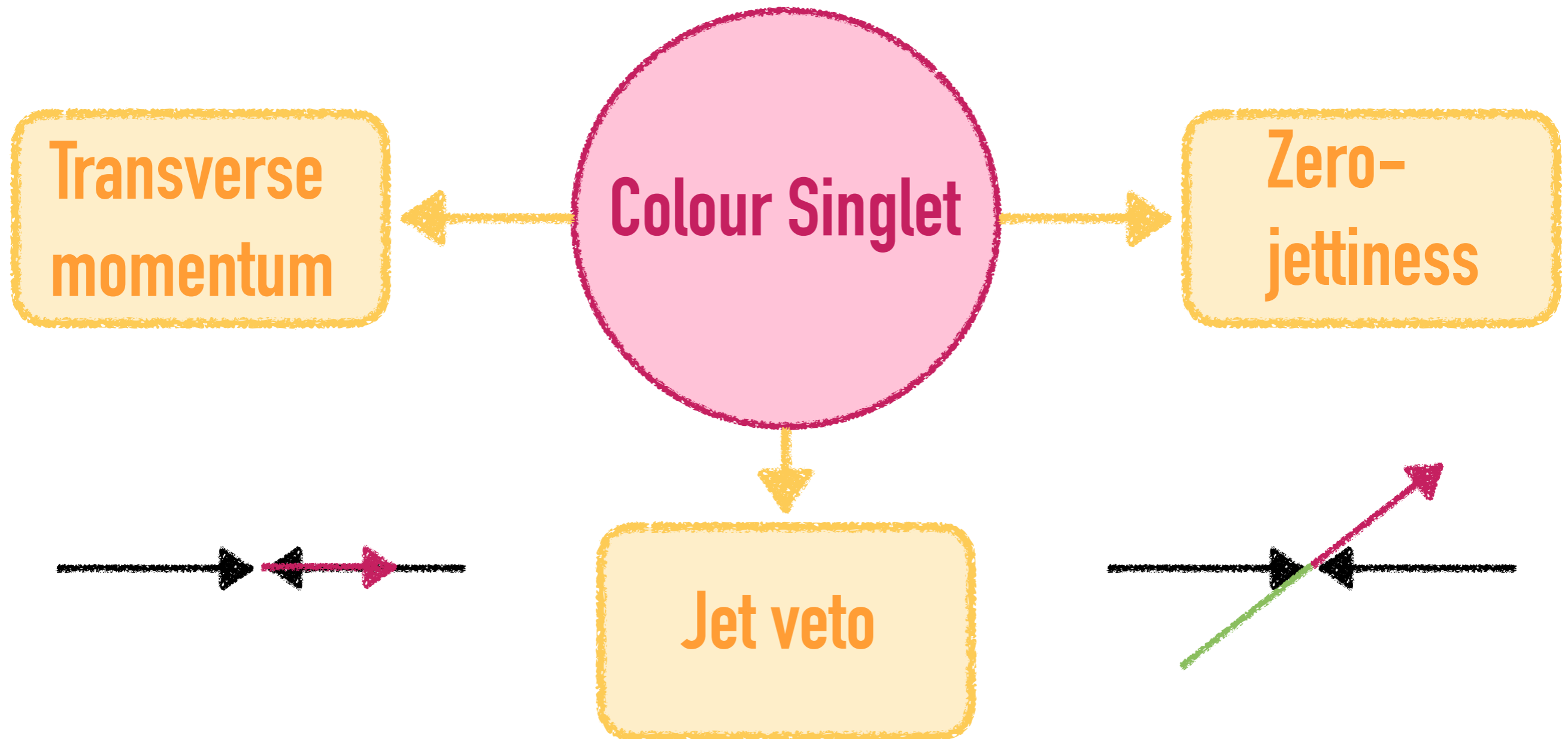
VVAmp

OpenLoops

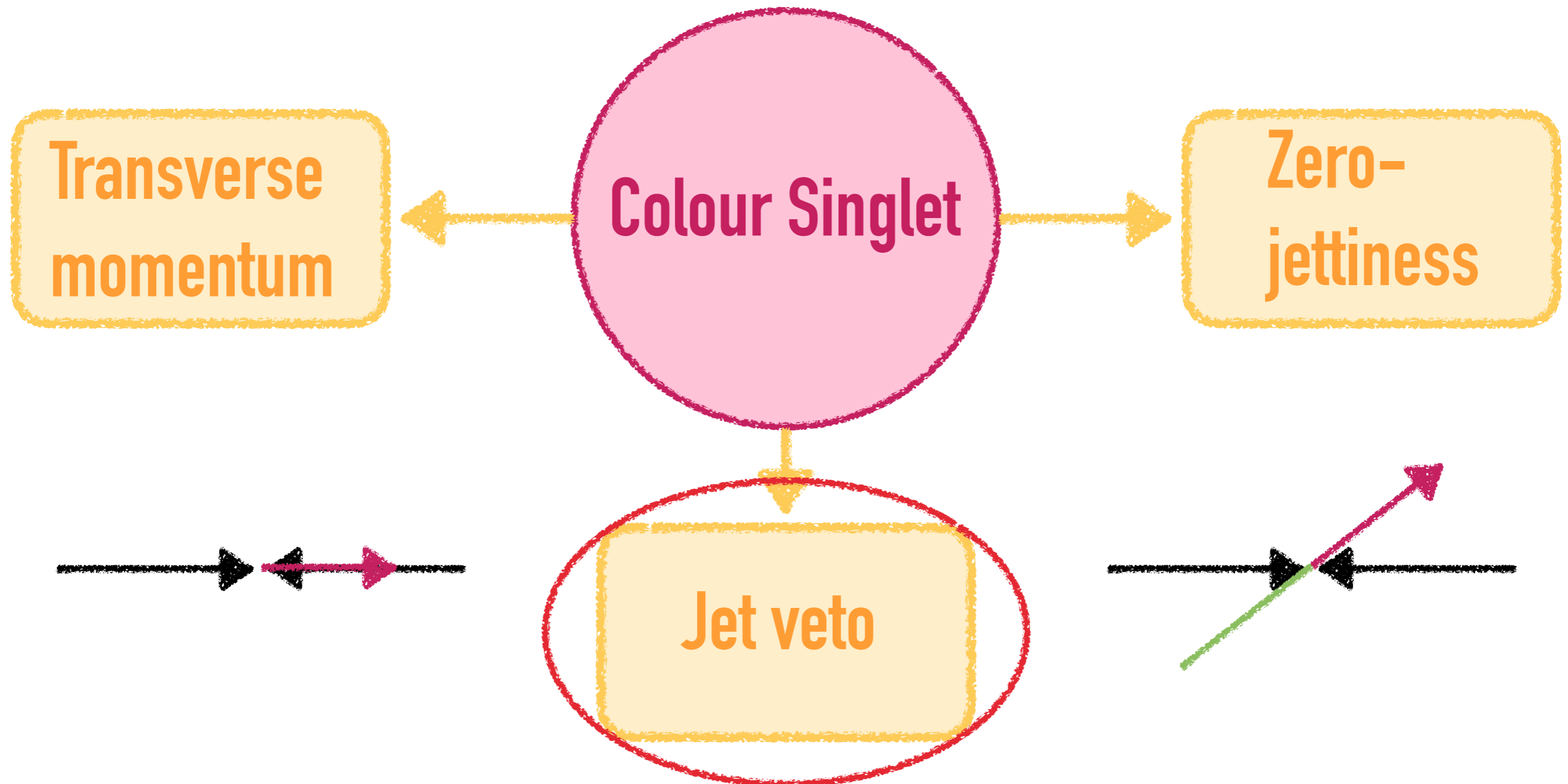
LHAPDF

...

RESOLUTION VARIABLES

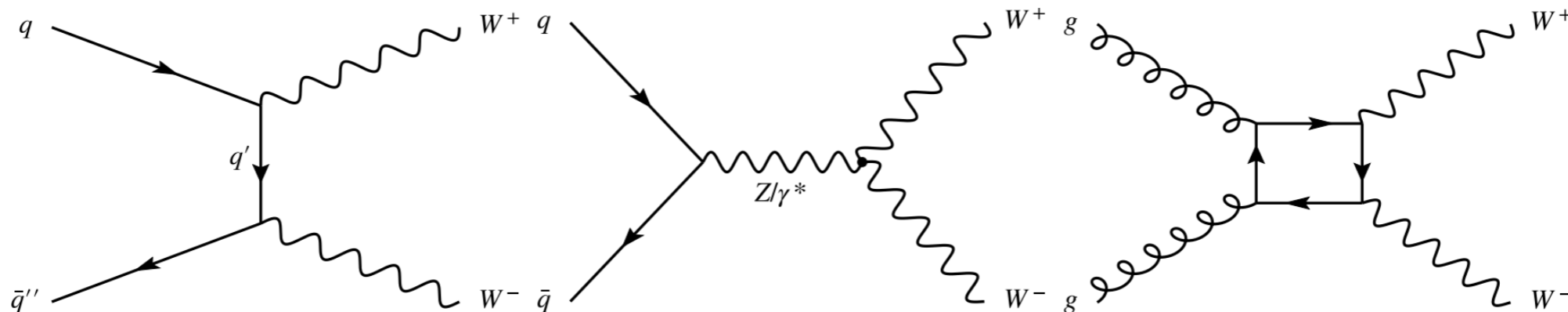


RESOLUTION VARIABLES



GENEVA USING JET VETO RESUMMATION

- ▶ W^+W^- production an interesting case study - jet vetoes used in analyses to reject $t\bar{t}$ background
- ▶ Aim to improve description of jet-vetoed cross section within an NNLO+PS event generator
- ▶ Combine NNLL' resummation for $WW + 0$ jets with NLL' resummation for $WW + 1$ jet to define events at NNLO



FACTORISATION WITH A JET VETO FOR COLOUR SINGLET

- ▶ Consider colour singlet production, vetoing all jets with $p_T > p_T^{\text{veto}}$. Resummation has been studied in both QCD and SCET. T. Becher, M. Neubert, 1205.3806, F. Tackmann, J. Walsh, S. Zuberi, 1206.4312, A. Banfi, G. Salam, G. Zanderighi, 1203.5773, I. Stewart, F. Tackmann, J. Walsh, S. Zuberi, 1307.1808, T. Becher, M. Neubert, L. Rothen, 1307.0025

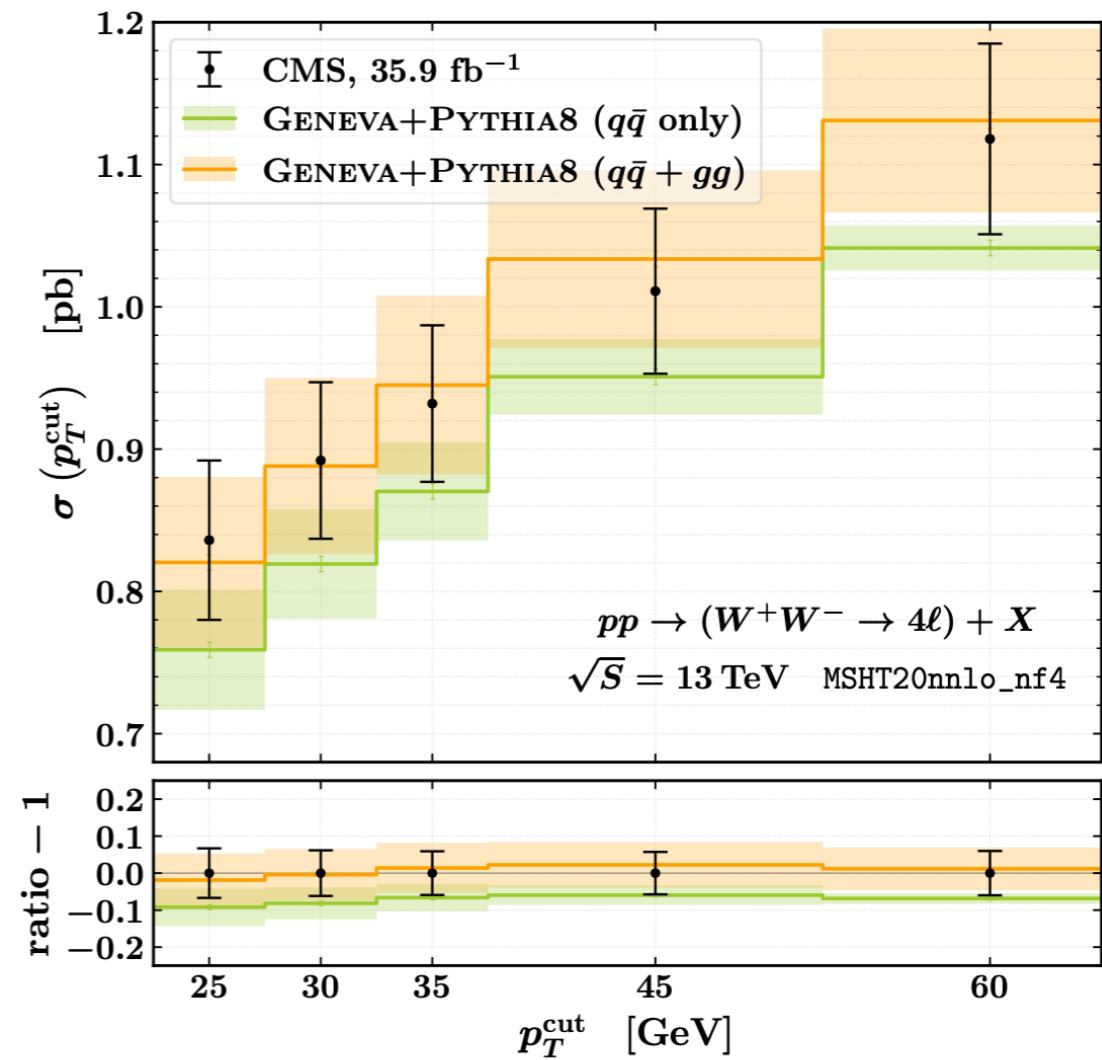
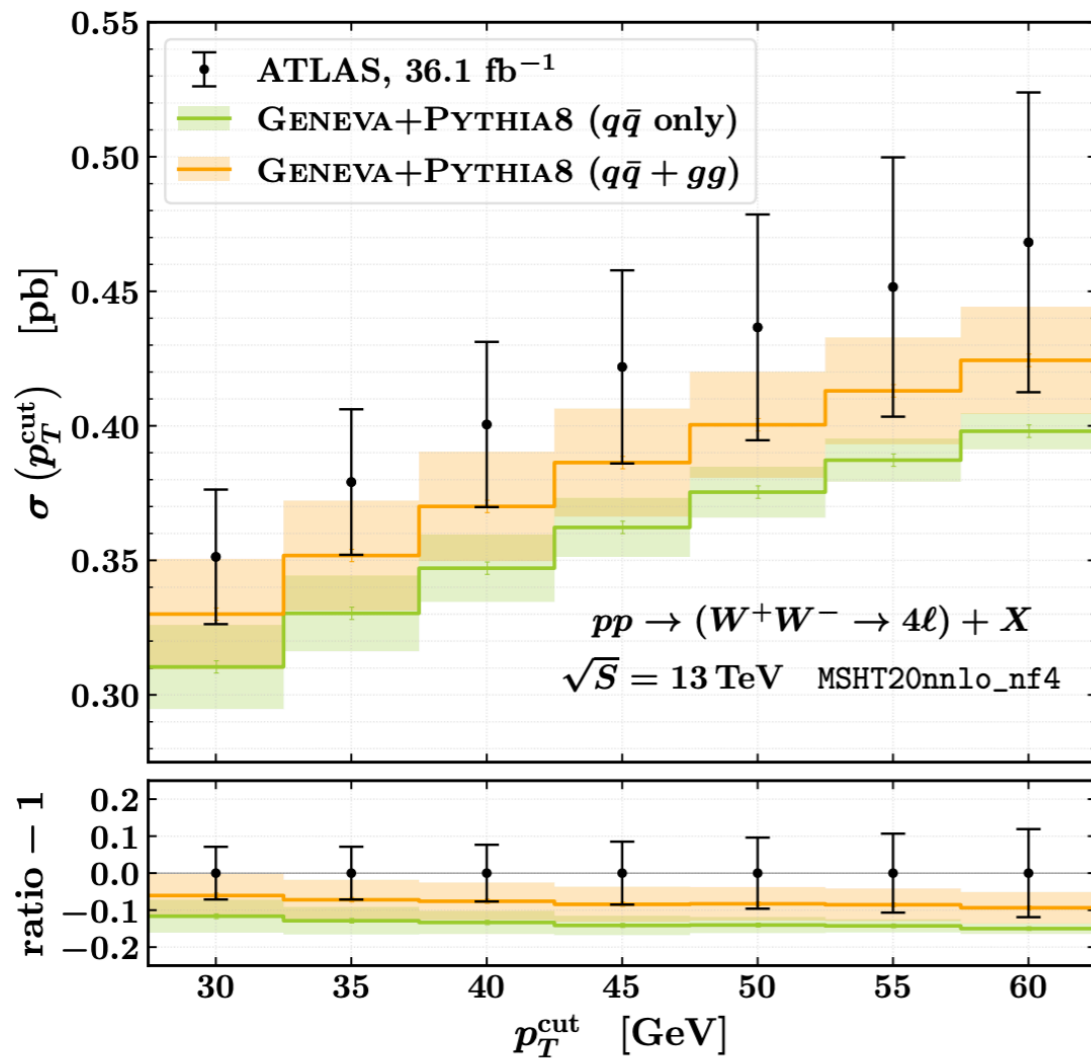
- ▶ Factorisation into hard, beam and soft functions

$$\frac{d\sigma(p_T^{\text{veto}})}{d\Phi_0} = H(\Phi_0, \mu) [B_a \times B_b](p_T^{\text{veto}}, R, x_a, x_b, \mu, \nu) S_{ab}(p_T^{\text{veto}}, R, \mu, \nu)$$

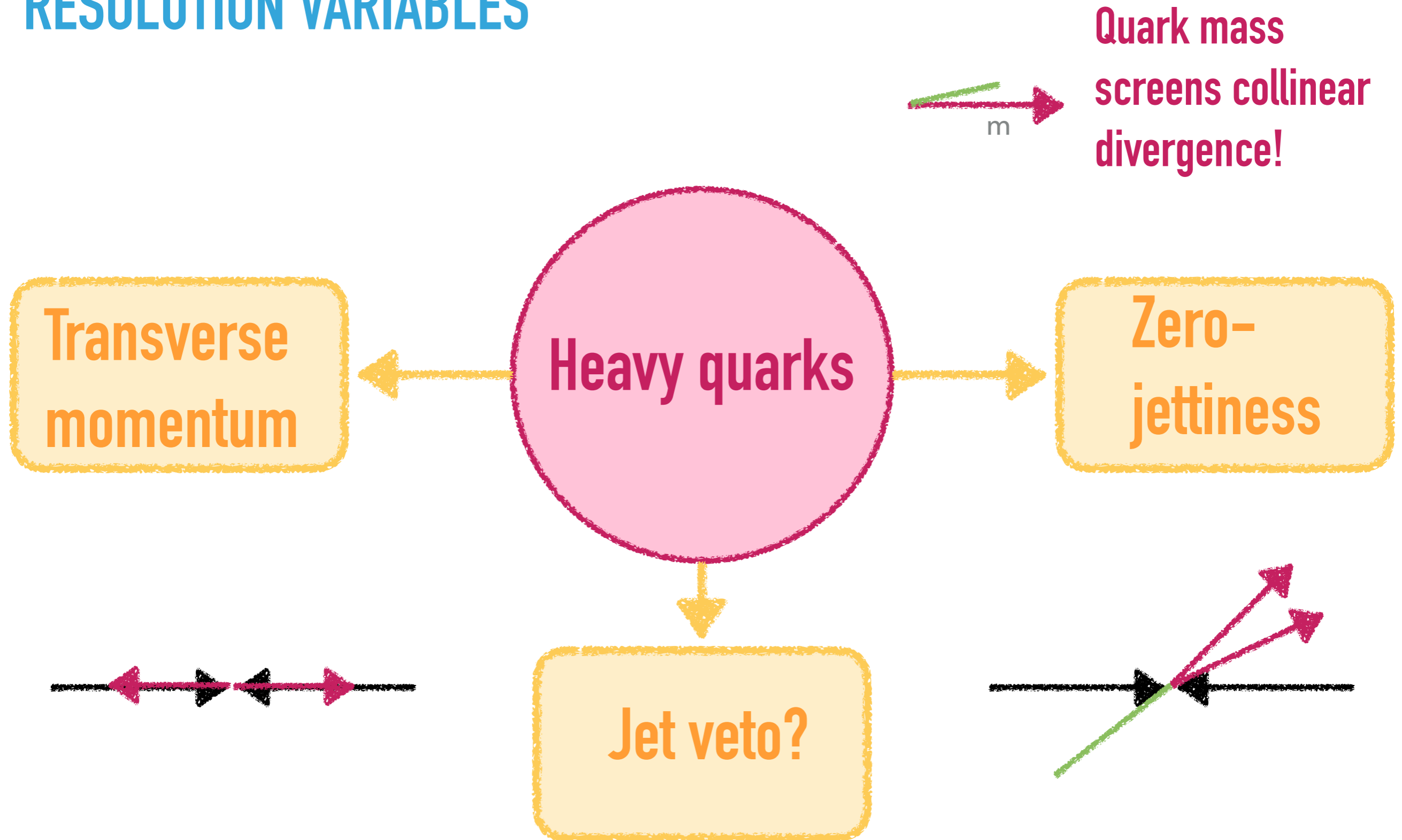
- ▶ Radius of vetoed jets R
- ▶ Additional scale ν necessary to separate soft/collinear modes (SCET II)

COMPARISON TO ATLAS/CMS

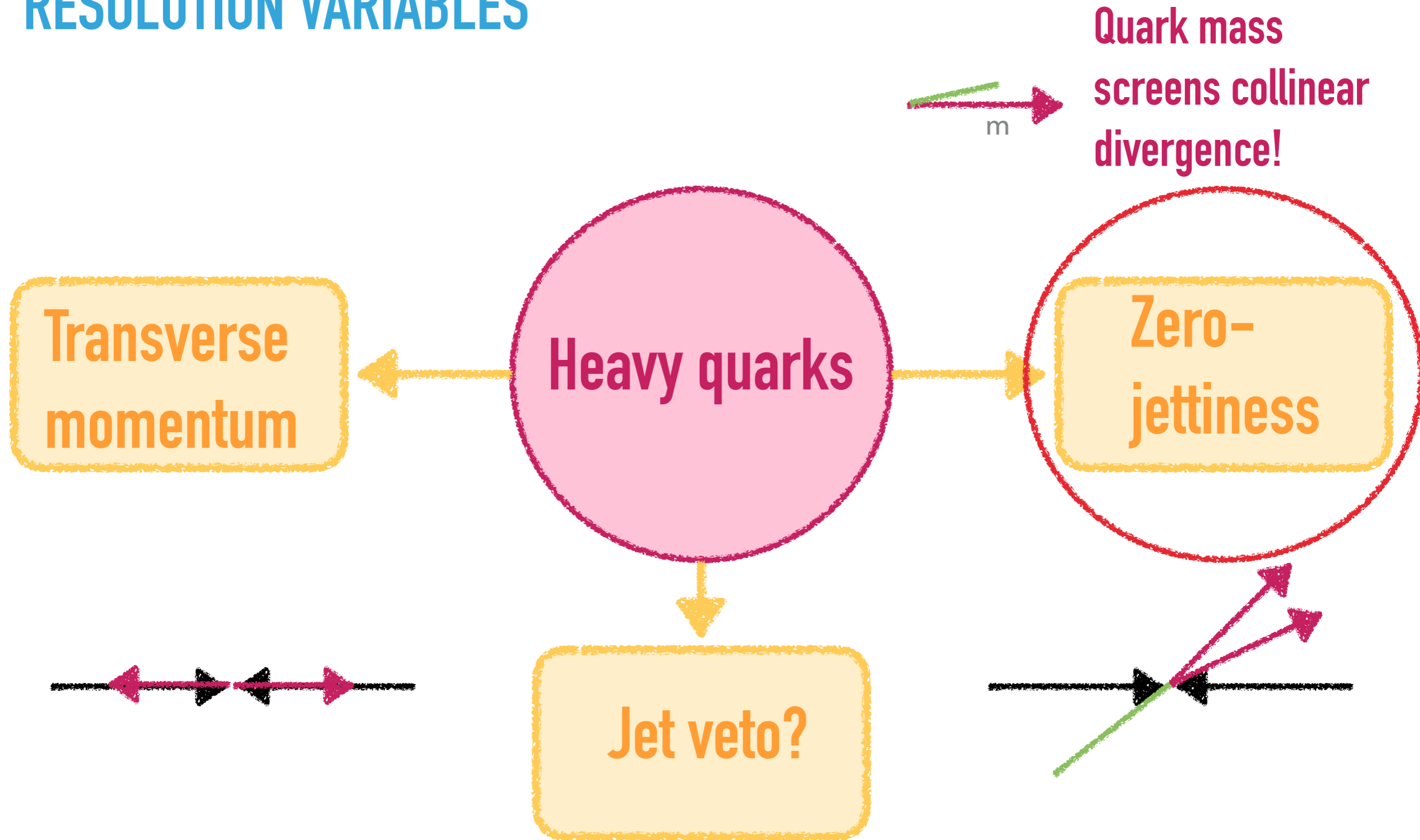
► Vetoed cross section measurements



RESOLUTION VARIABLES



RESOLUTION VARIABLES



ZERO-JETTINESS RESUMMATION FOR HEAVY QUARK PAIRS

SCET allows us to write a factorisation formula as

$$\frac{d\sigma^{\text{resum}}}{d\Phi_0 d\mathcal{T}_0} = \sum_{ij} \int dt_a dt_b \underbrace{B_i(t_a, x_a, \mu_B) B_j(t_b, x_b, \mu_B)}_{\substack{\text{Same as colour singlet} \\ \uparrow}} \text{Tr} \left\{ \underbrace{\mathbf{H}_{ij}(\Phi_0, \mu_H)}_{\substack{\text{Matrices in colour space!} \\ \uparrow}} \underbrace{\mathbf{S} \left(\mathcal{T}_0 - \frac{t_a + t_b}{Q}, \Phi_0, \mu_S \right)}_{\substack{\uparrow}} \right\}$$

Arises from exchange of soft gluons from heavy quark lines.
Evolution equations more complicated:

$$\mathbf{H}(\Phi_0, \mu) = \mathbf{U}(\Phi_0, \mu, \mu_H) \mathbf{H}(\Phi_0, \mu_H) \mathbf{U}^\dagger(\Phi_0, \mu, \mu_H)$$

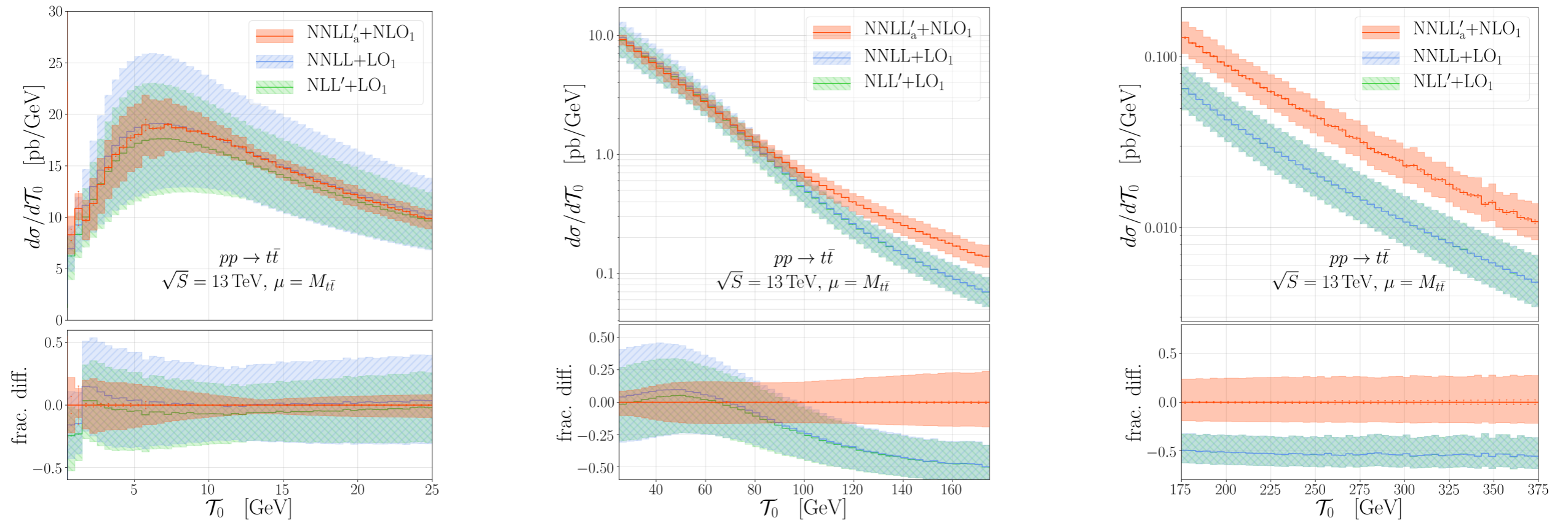
ZERO-JETTINESS RESUMMATION FOR HEAVY QUARK PAIRS

Derived for the first time! **Ingredients partially unknown.**

$$\frac{d\sigma^{\text{resum}}}{d\Phi_0 d\mathcal{T}_0} = \sum_{ij} \int dt_a dt_b \underbrace{B_i(t_a, x_a, \mu_B) B_j(t_b, x_b, \mu_B)}_{\text{Known up to 3-loops}} \text{Tr} \left\{ \underbrace{\mathbf{H}_{ij}(\Phi_0, \mu_H)}_{\text{Known up to 2-loops (in principle)}} \underbrace{\mathbf{S} \left(\mathcal{T}_0 - \frac{t_a + t_b}{Q}, \Phi_0, \mu_S \right)}_{\text{Unknown!}} \right\}$$

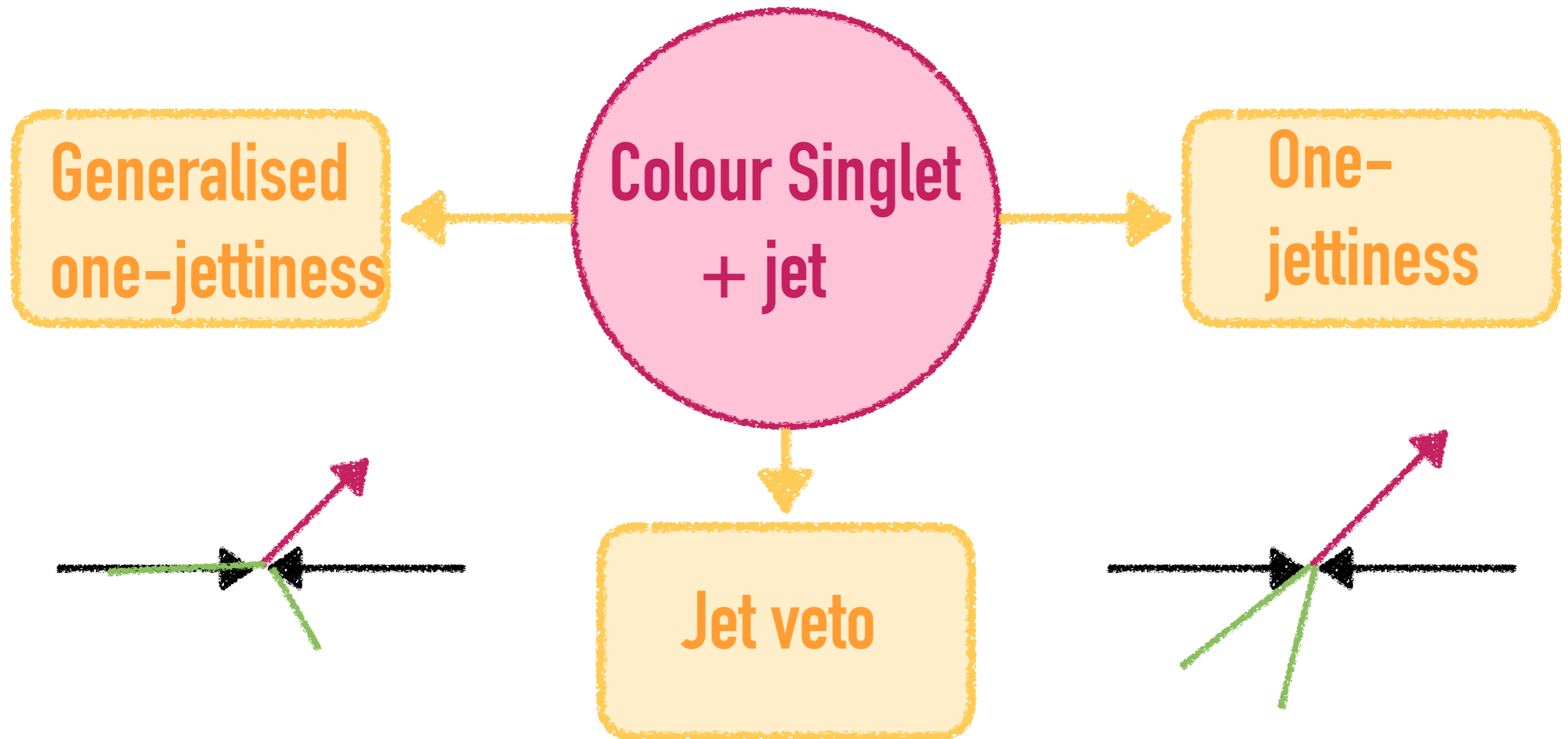
We computed the soft function up to 1-loop. Some 2-loop terms can be obtained via RGE.

ZERO-JETTINESS RESUMMATION FOR TOP-QUARK PAIRS

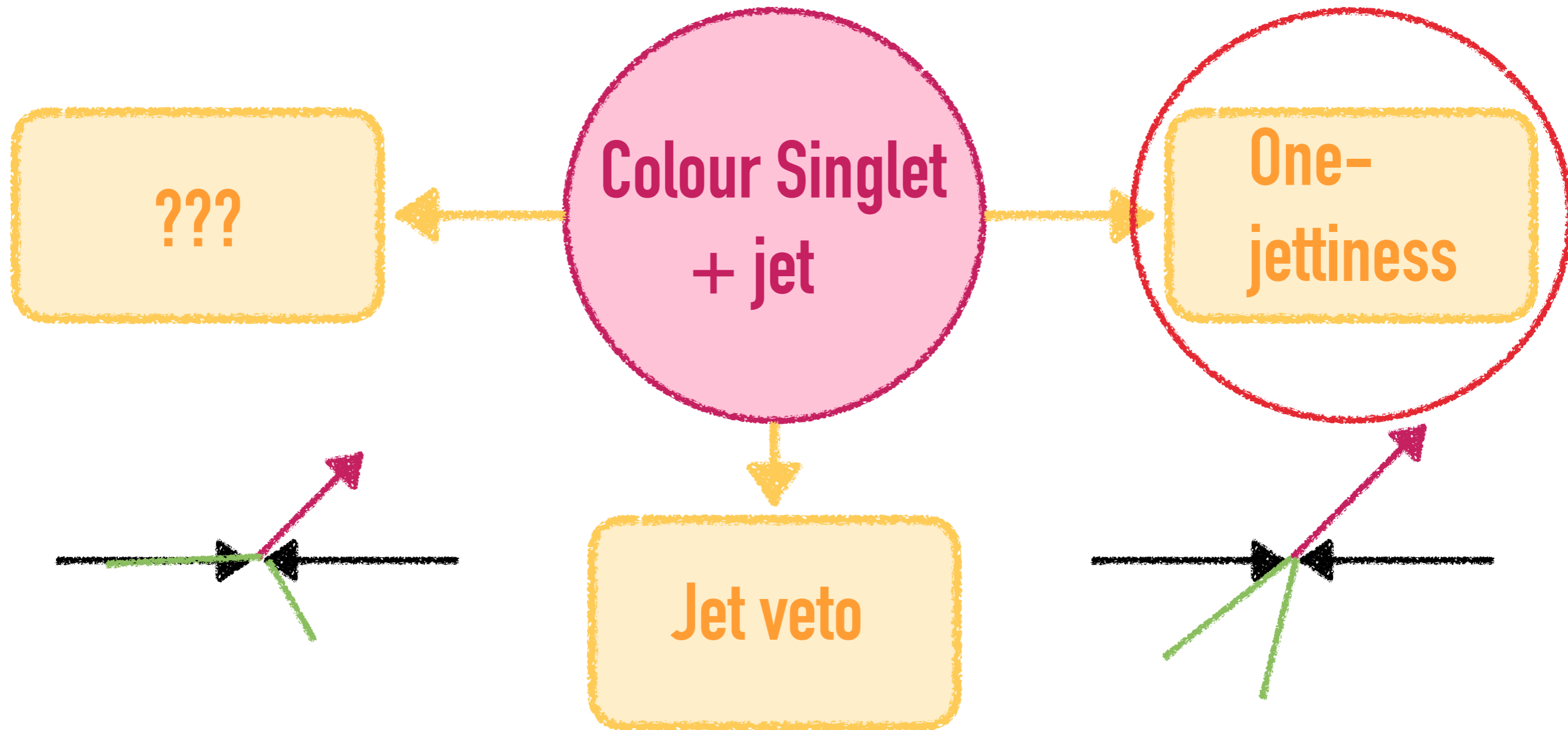


- ▶ Still missing - two-loop hard (not included here) and one piece of the two-loop soft.
- ▶ Allows **approximate NNLL'** accuracy.

RESOLUTION VARIABLES




RESOLUTION VARIABLES



ONE-JETTINESS RESUMMATION FOR COLOUR SINGLET + JET

Similar factorisation to zero-jet case:

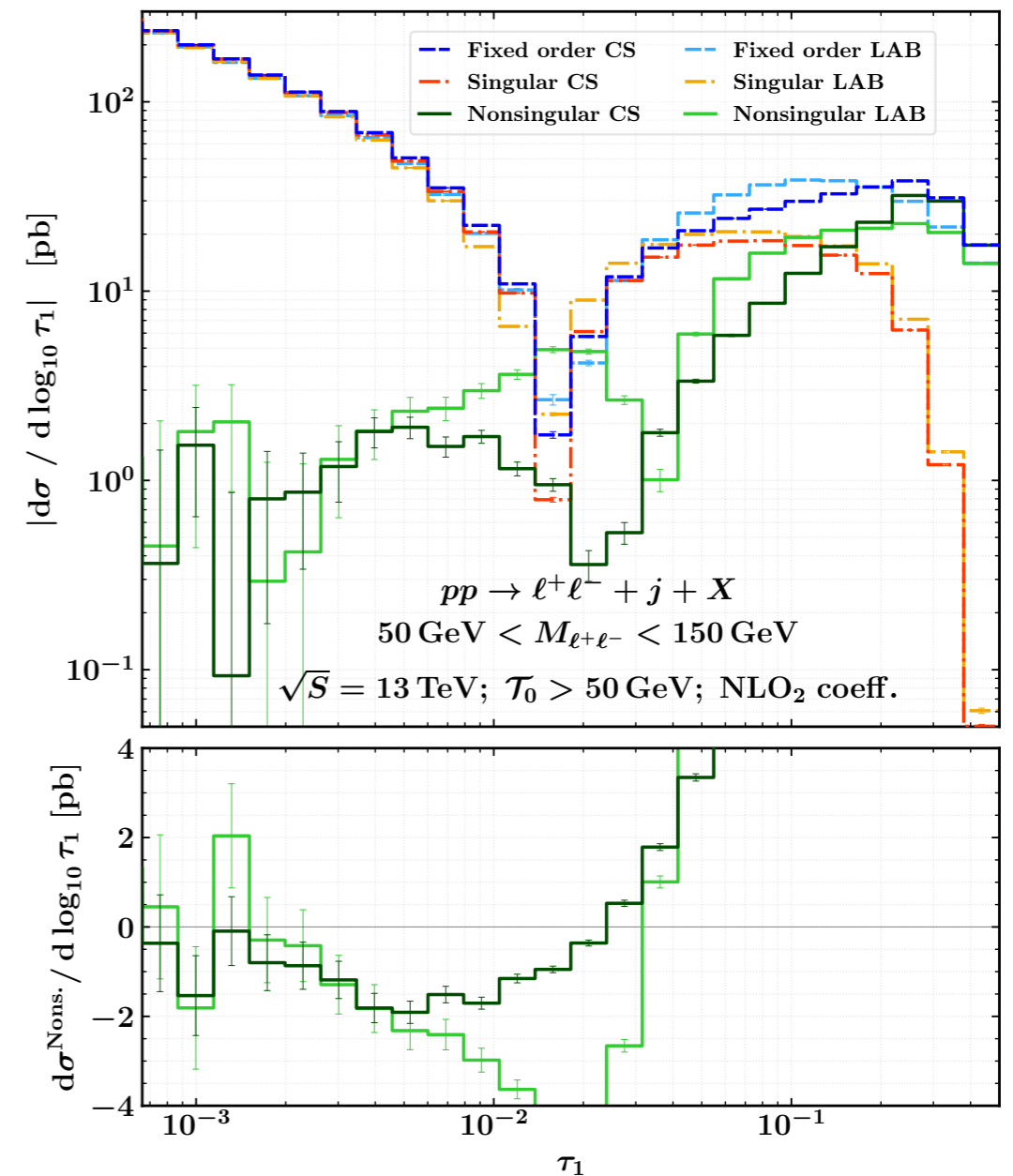
$$\frac{d\sigma^{\text{resum}}}{d\Phi_1 d\mathcal{T}_1} = \sum_{ijk} \int dt_a dt_b ds_J B_i(t_a, x_a, \mu_B) B_j(t_b, x_b, \mu_B) J_k(s_J, \mu_J) \text{Tr} \left\{ \mathbf{H}_{ij}(\Phi_1, \mu_H) \mathbf{S} \left(\mathcal{T}_1 - \frac{t_a}{Q_a} - \frac{t_b}{Q_b} - \frac{s_J}{Q_J}, \Phi_1, \mu_S \right) \right\}$$

New jet function 

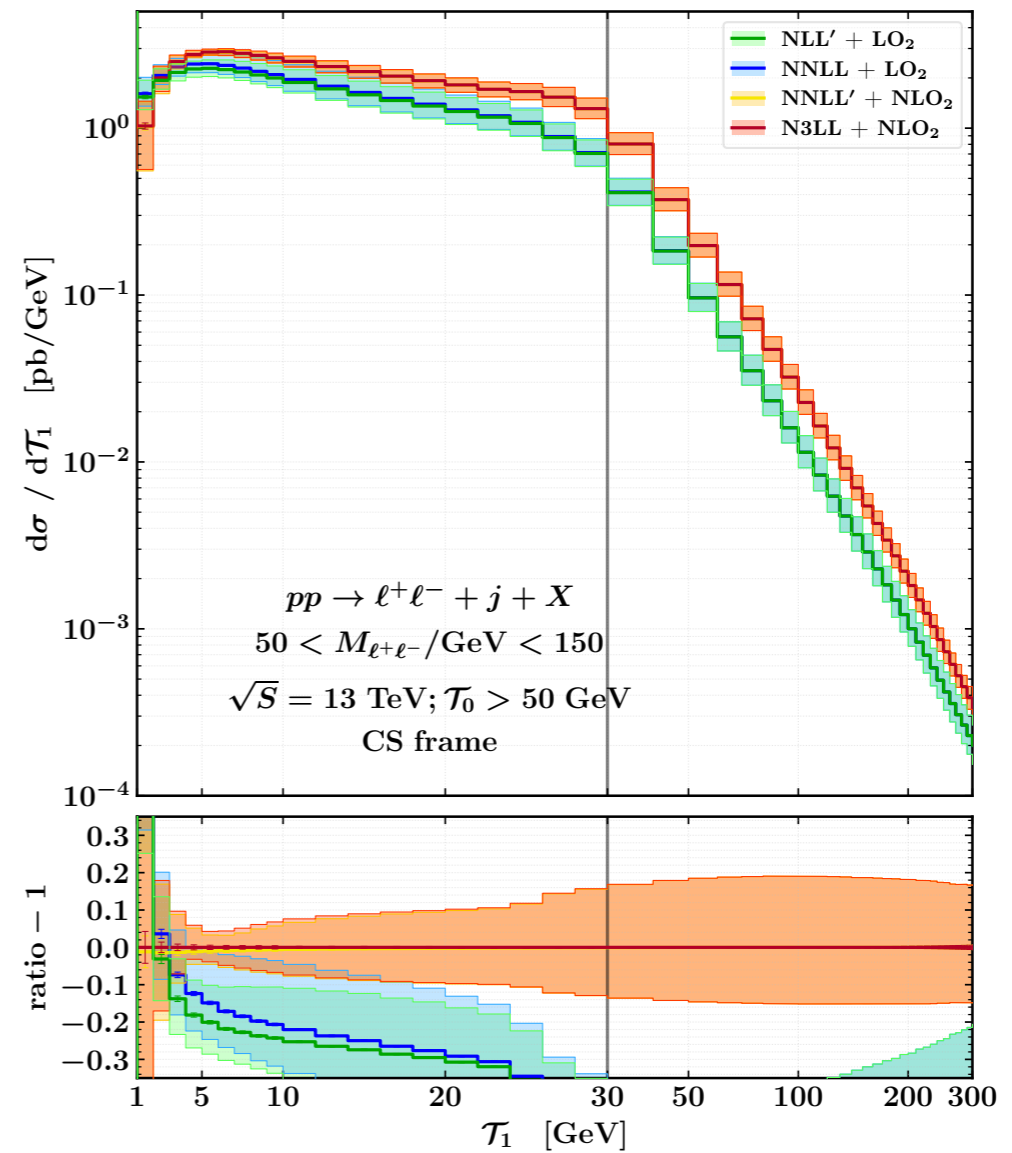
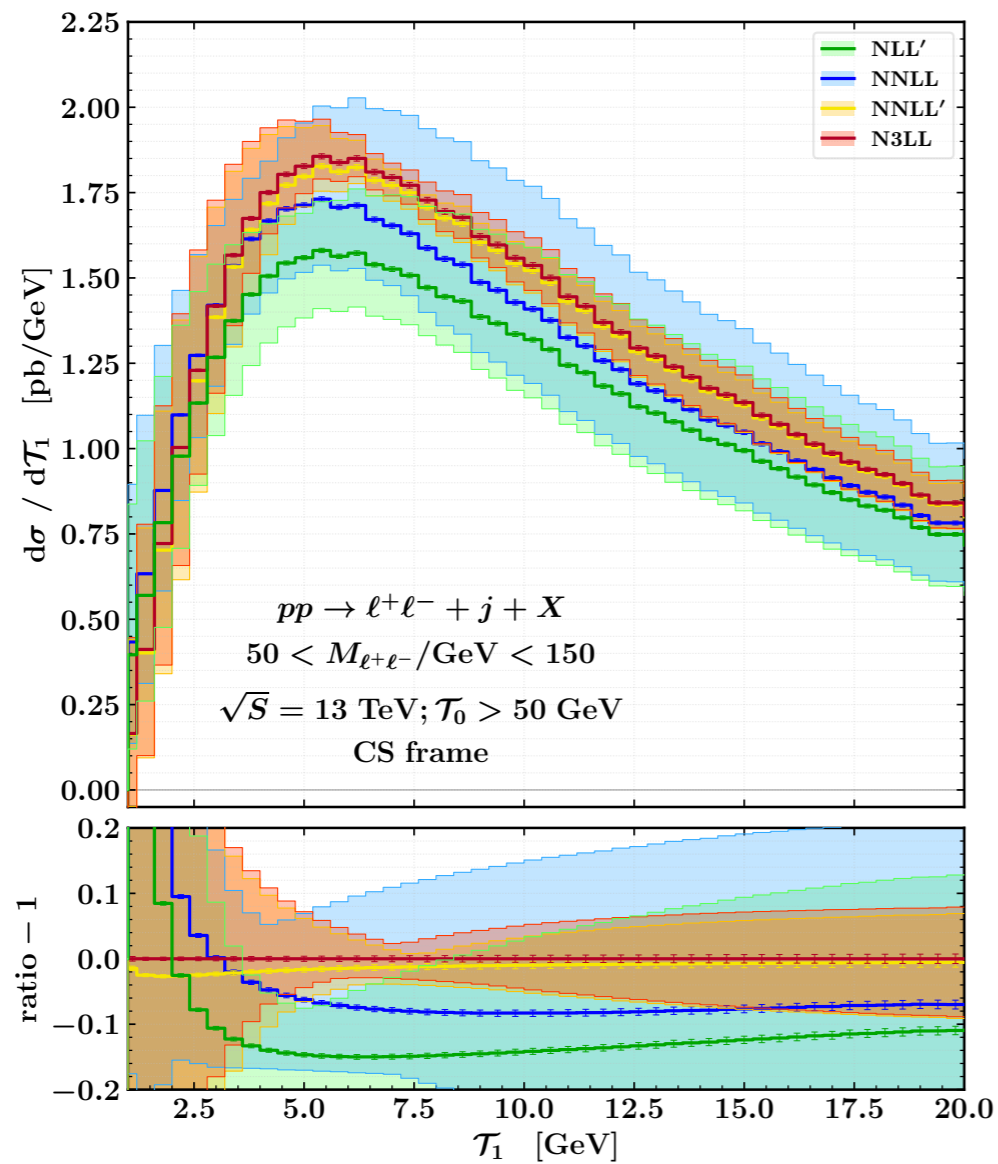
- ▶ Only three coloured legs - colour algebra is diagonal
- ▶ Ingredients for N³LL all known, we use new numerical of two-loop soft function from SoftSERVE
- ▶ One-jettiness definition requires choice of frame - can evaluate energies in lab or in CS centre-of-mass

FIXED-ORDER VALIDATION OF ONE-JETTINESS FACTORISATION

- ▶ Factorisation theorem must reproduce result of fixed order in the **small $\tau_1 = \mathcal{T}_1/Q$ limit**
- ▶ **Size of nonsingular difference** has implications for numerical accuracy of slicing calculations



RESUMMED AND MATCHED ONE-JETTINESS SPECTRA



CONCLUSIONS

- ▶ GENEVA allows matching of NNLO calculations to parton shower algorithms for a range of colour singlet production processes
- ▶ Ongoing work aims to extend this to heavy quark production and processes with jets
- ▶ Main limitation is availability of suitable resummed calculation - SCET allows these to be obtained in a systematic way, different resolution variables to be explored

CONCLUSIONS

- ▶ Recent colour singlet results include **single and double Higgs production using zero-jettiness**, **WW production using jet transverse momentum**
- ▶ **Zero-jettiness for top-quark pair production** also studied
- ▶ Recent work pushes **one-jettiness resummation to N^3LL for $Z + \text{jet}$** , full NNLO+PS generator is work in progress

Thanks for your attention!

BACKUP SLIDES

SCET I VS SCET II

- ▶ 'Simple' SCET problems can be either two- or three-scale, depending on nature of observable
- ▶ Three-scale case: $\mu_S \ll \mu_J \ll \mu_H$, covered by SCET I



$$\mu_H \sim Q$$

$$\mu_J \sim m_J$$

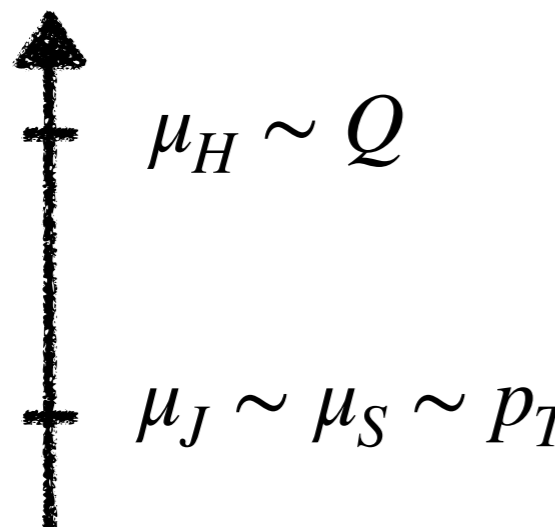
$$\mu_S \sim m_J^2/Q$$

$$d\hat{\sigma} \approx H(Q, \mu) J(m_J, \mu) \otimes S(m_J^2/Q, \mu)$$

$$\ln^2 \frac{Q^2}{m_J^2} = \frac{1}{2} \ln^2 \frac{Q^2}{\mu^2} - \ln^2 \frac{m_J^2}{\mu^2} + \frac{1}{2} \ln^2 \frac{m_J^4}{Q^2 \mu^2}$$

SCET I VS SCET II

- ▶ 'Simple' SCET problems can be either two- or three-scale, depending on nature of observable
- ▶ Two-scale case: $\mu_S \sim \mu_J \ll \mu_H$, covered by SCET II



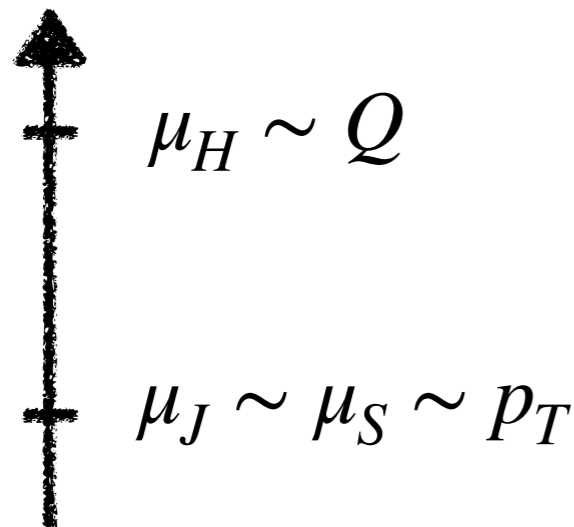
$$d\hat{\sigma} \approx H(Q, \mu) J(p_T, \mu) \otimes S(p_T, \mu)$$

$$\ln^2 \frac{Q^2}{p_T^2} = \ln^2 \frac{Q^2}{\mu^2} - \ln^2 \frac{p_T^2}{\mu^2} + ?$$

- ▶ Jet and soft functions ill-defined in dimensional regularisation

SCET I VS SCET II

- ▶ 'Simple' SCET problems can be either two- or three-scale, depending on nature of observable
- ▶ Two-scale case: $\mu_S \sim \mu_J \ll \mu_H$, covered by SCET II



$$d\hat{\sigma} \approx H(Q, \mu) J(p_T, \mu, Q, \nu) \otimes S(p_T, \mu, Q, \nu)$$

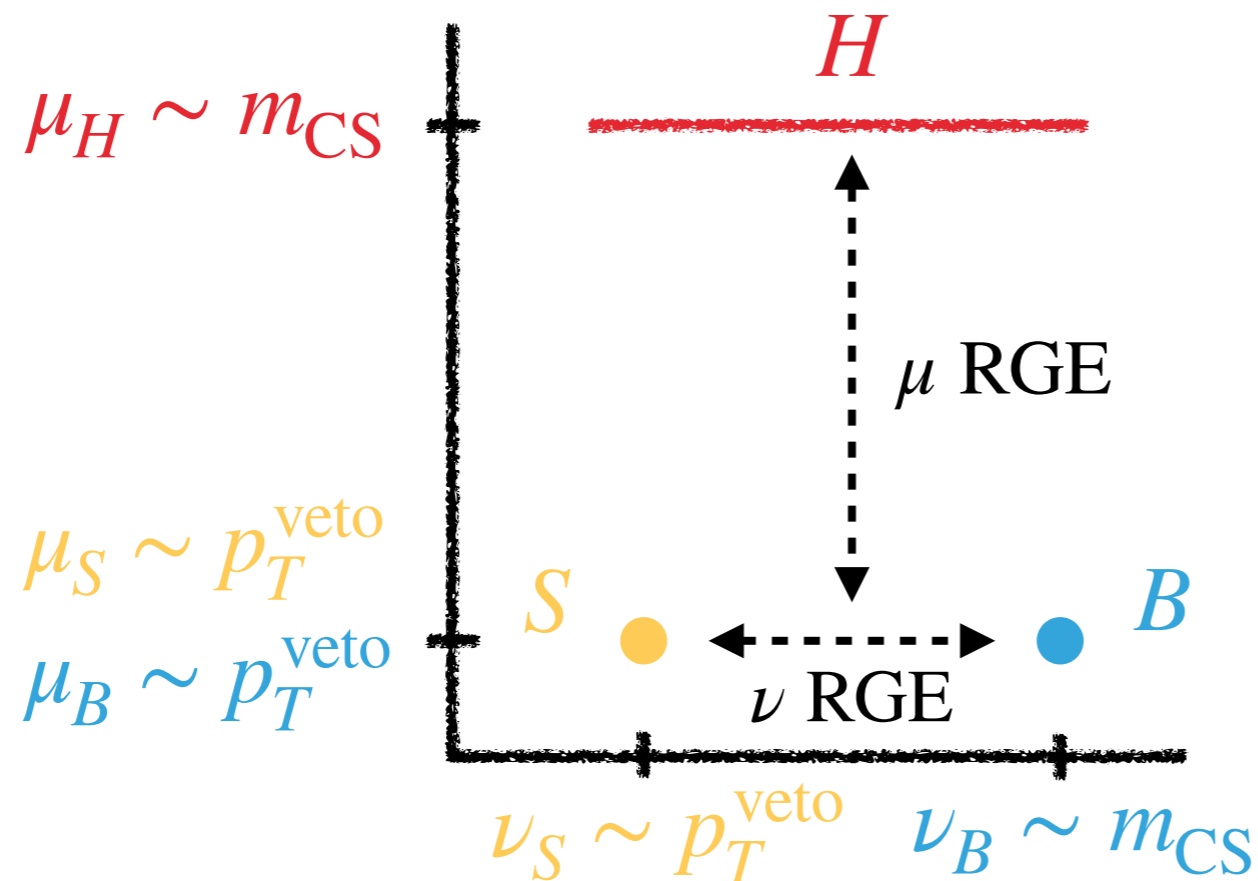
$$\ln^2 \frac{Q^2}{p_T^2} = \ln^2 \frac{Q^2}{\mu^2} - \ln^2 \frac{p_T^2}{\mu^2} - 2 \ln \frac{p_T^2}{\mu^2} \ln \frac{Q^2}{\nu^2} - 2 \ln \frac{p_T^2}{\mu^2} \ln \frac{\nu^2}{p_T^2}$$

- ▶ Introduction of new rapidity scale ν separates soft and collinear modes

RESUMMATION OF JET VETO LOGS FOR COLOUR SINGLET

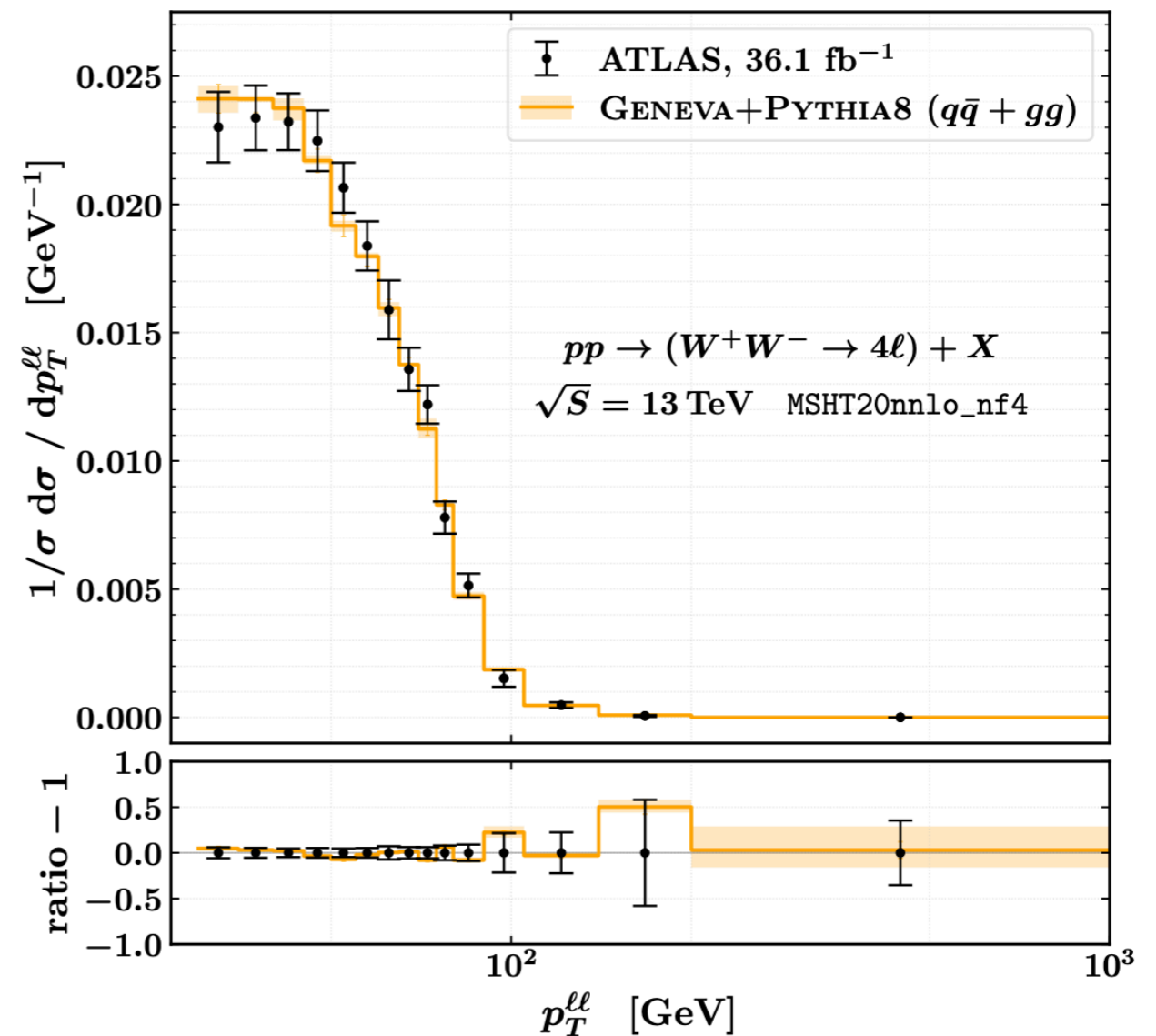
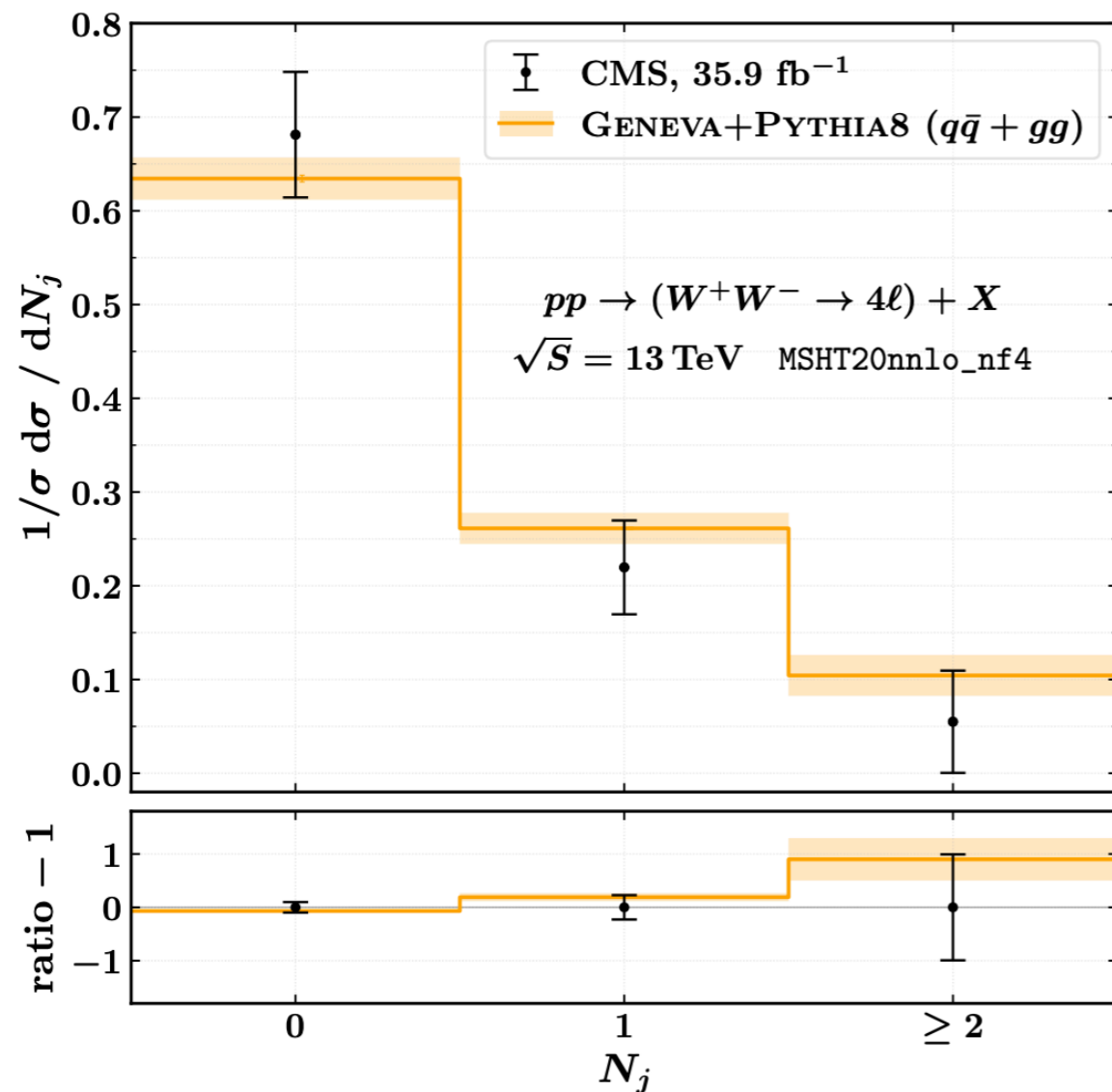
- ▶ Rapidity scale ν requires two-dimensional evolution

$$\frac{d}{d \ln \mu} \ln S(p_T^{\text{cut}}, R, \mu, \nu) = 4\Gamma_{\text{cusp}} \ln \frac{\mu}{\nu} + \gamma_S \quad \frac{d}{d \ln \nu} \ln S(p_T^{\text{cut}}, R, \mu, \nu) = \gamma_\nu$$



COMPARISON TO ATLAS/CMS

- ▶ Compared with ATLAS/CMS measurements



GENERALISED N-JETTINESS

- ▶ The \mathcal{T}_N metric **need not** measure just the invariant **mass**
- ▶ In jet/beam region m , define

$$\mathcal{T}^{(m)} = \sum_{i \in m} f_m(\eta_i, \phi_i) p_{Ti}$$

- ▶ Generic form of \mathcal{T}_N can be **invariant mass-like** or **transverse momentum-like** (latter used in jet substructure)
- ▶ Requires different resummation (SCET-I vs SCET-II)

SHOWERED RESULTS

- Numerically examine effect of shower on accuracy

