

Manimala Chakraborti  
University of Southampton

# A 95 GeV Higgs boson within a 2-Higgs Doublet Model

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BASED ON : JHEP 05 (2024) 209

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WITH A. BELYAEV, R. BENBRIK, M. BOUKIDI, S. MORETTI, S. SEMLALI

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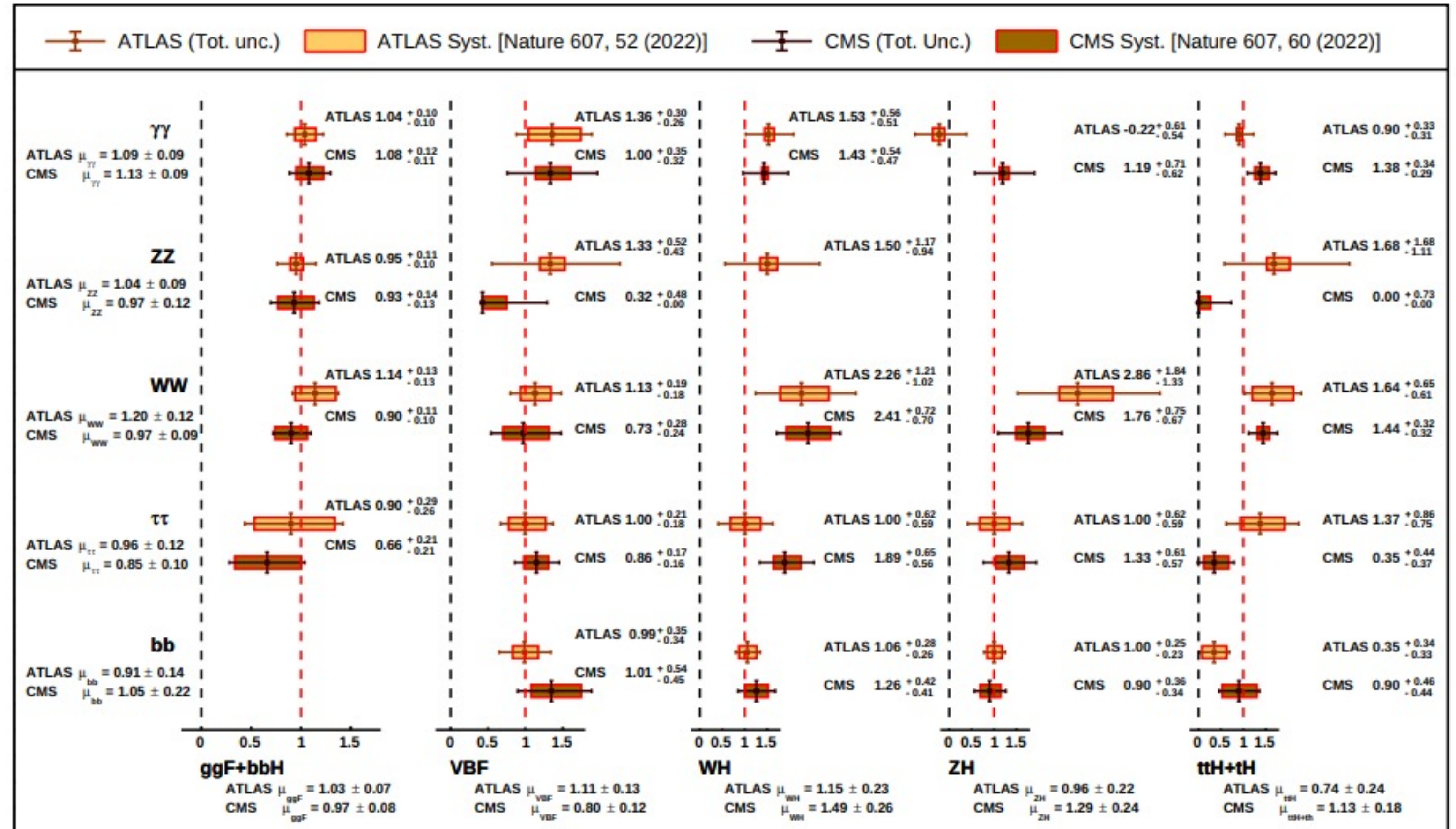
# Outline

- ◆ Introduction
- ◆ Evidence for a light Higgs boson
- ◆ Possible model interpretation
- ◆ Future prospects
- ◆ Conclusion

# Introduction

$\sigma \cdot BR$  (Normalised to SM)

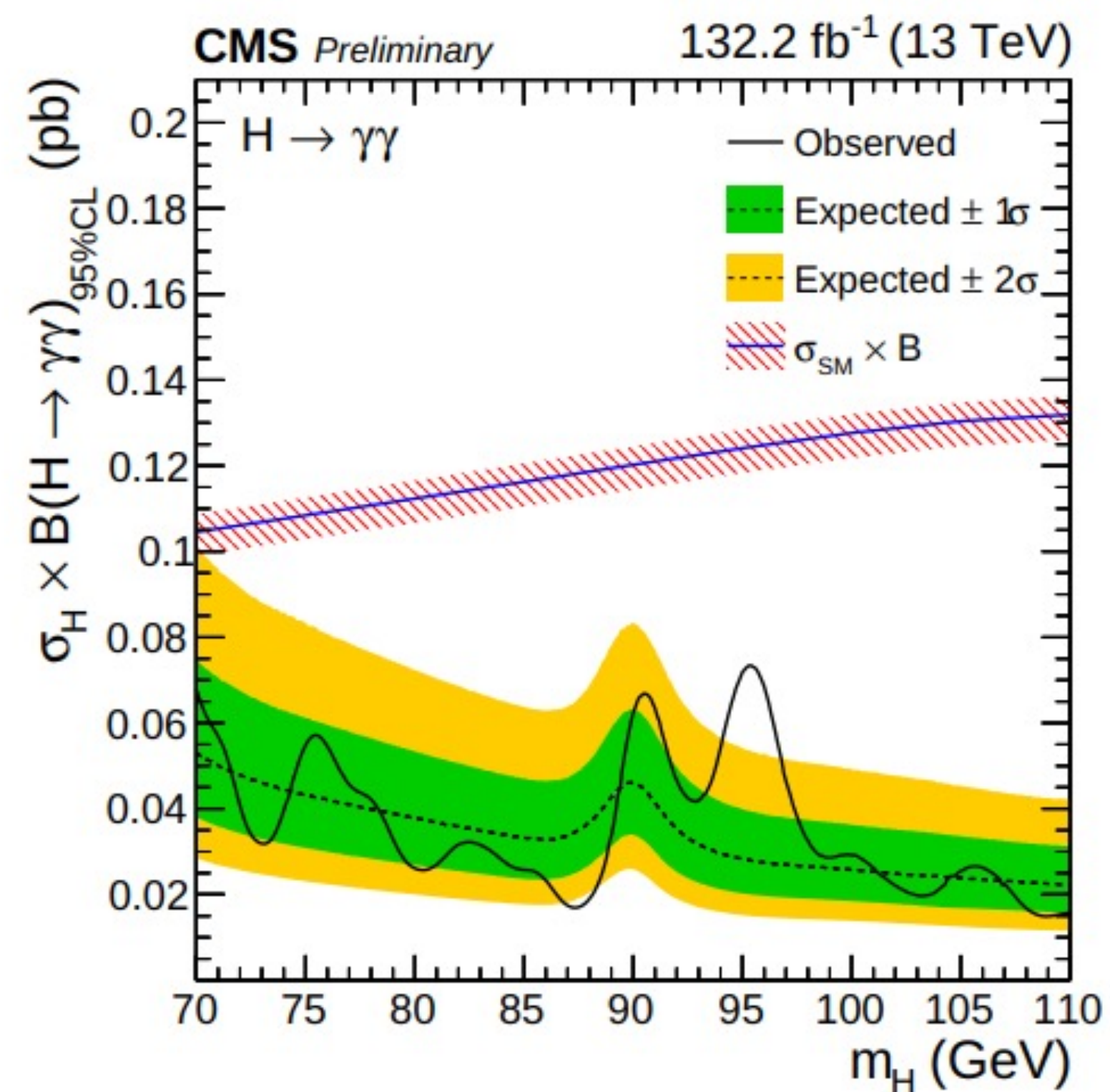
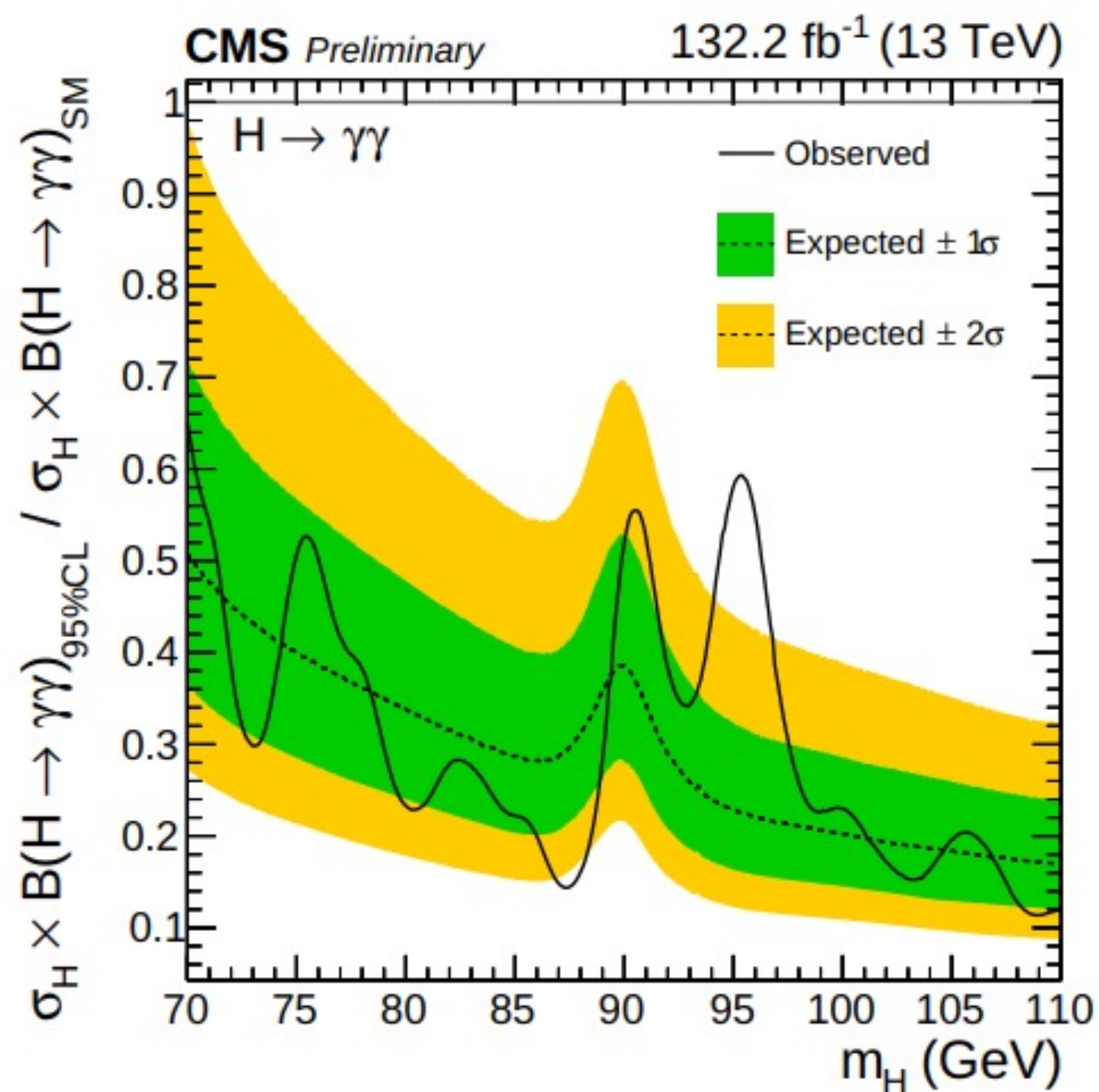
- ◆ 125 GeV Higgs properties are consistent with SM
- ◆ More scalars to come ?
- ◆ Where to look ?
  - ◆ Above and Below 125 GeV



# Motivation - I

“Excess” at  $\sim 95.4$  GeV with local (global) significance  $\sim 2.9$  (1.3)  $\sigma$

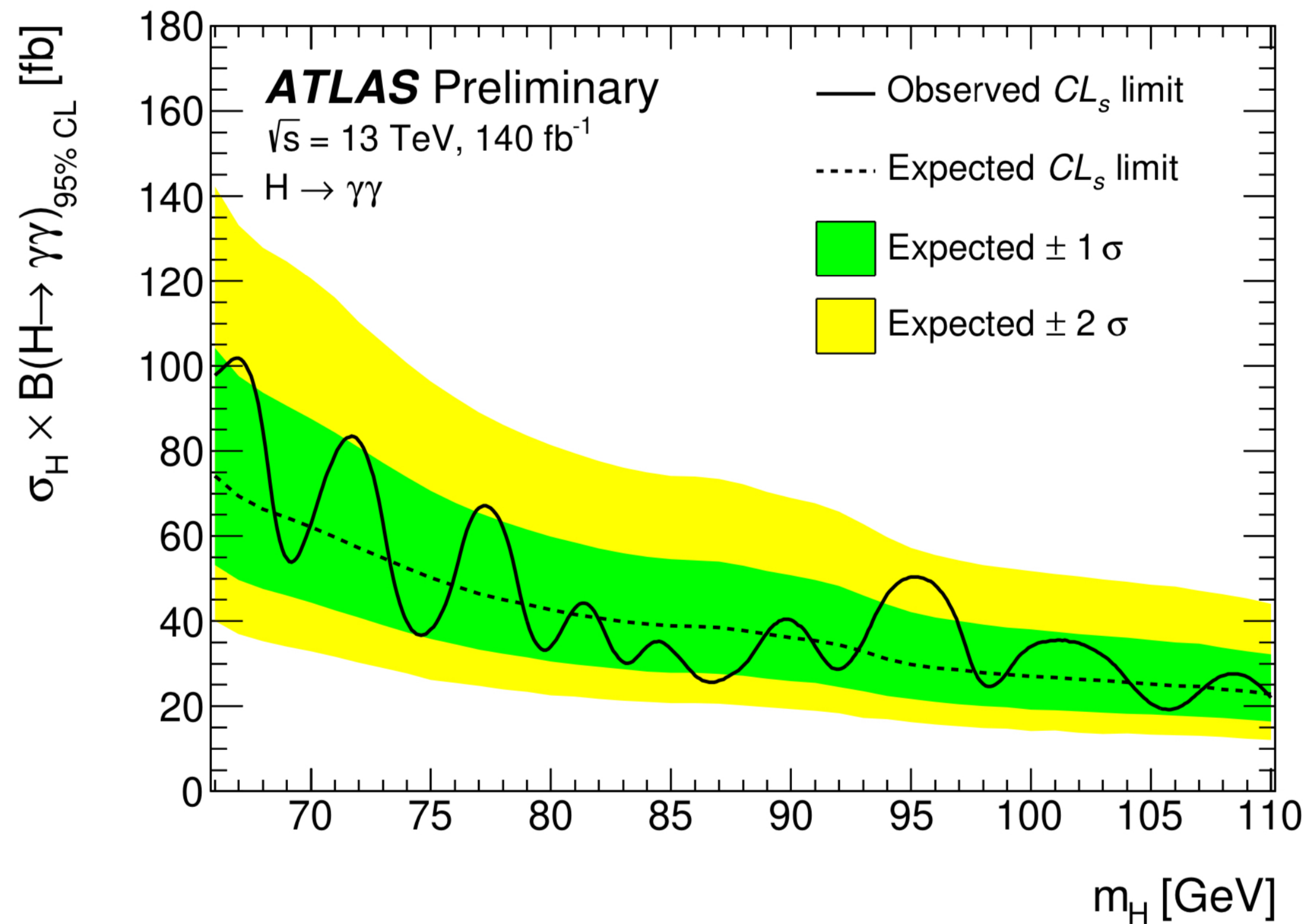
CMS-PAS-HIG-20-002



$$\mu_{\gamma\gamma}^{CMS} = \frac{\sigma^{\text{exp}}(pp \rightarrow \phi \rightarrow \gamma\gamma)}{\sigma^{\text{SM}}(pp \rightarrow H \rightarrow \gamma\gamma)} = 0.33_{-0.12}^{+0.19}$$

# Motivation - II : ATLAS results

A scan over different  $m_X$  hypotheses is performed in the range 66 to 110 GeV.



Small “excess” at  $\sim 95 \text{ GeV}$  with local  
 $\sim 1.7 \sigma$

$$\mu_{\gamma\gamma}^{ATLAS} = 0.18 \pm 0.10 \quad (1.7\sigma)$$

$$\mu_{\gamma\gamma}^{ATLAS+CMS} = 0.24_{-0.08}^{+0.09} \quad (3.1\sigma)$$

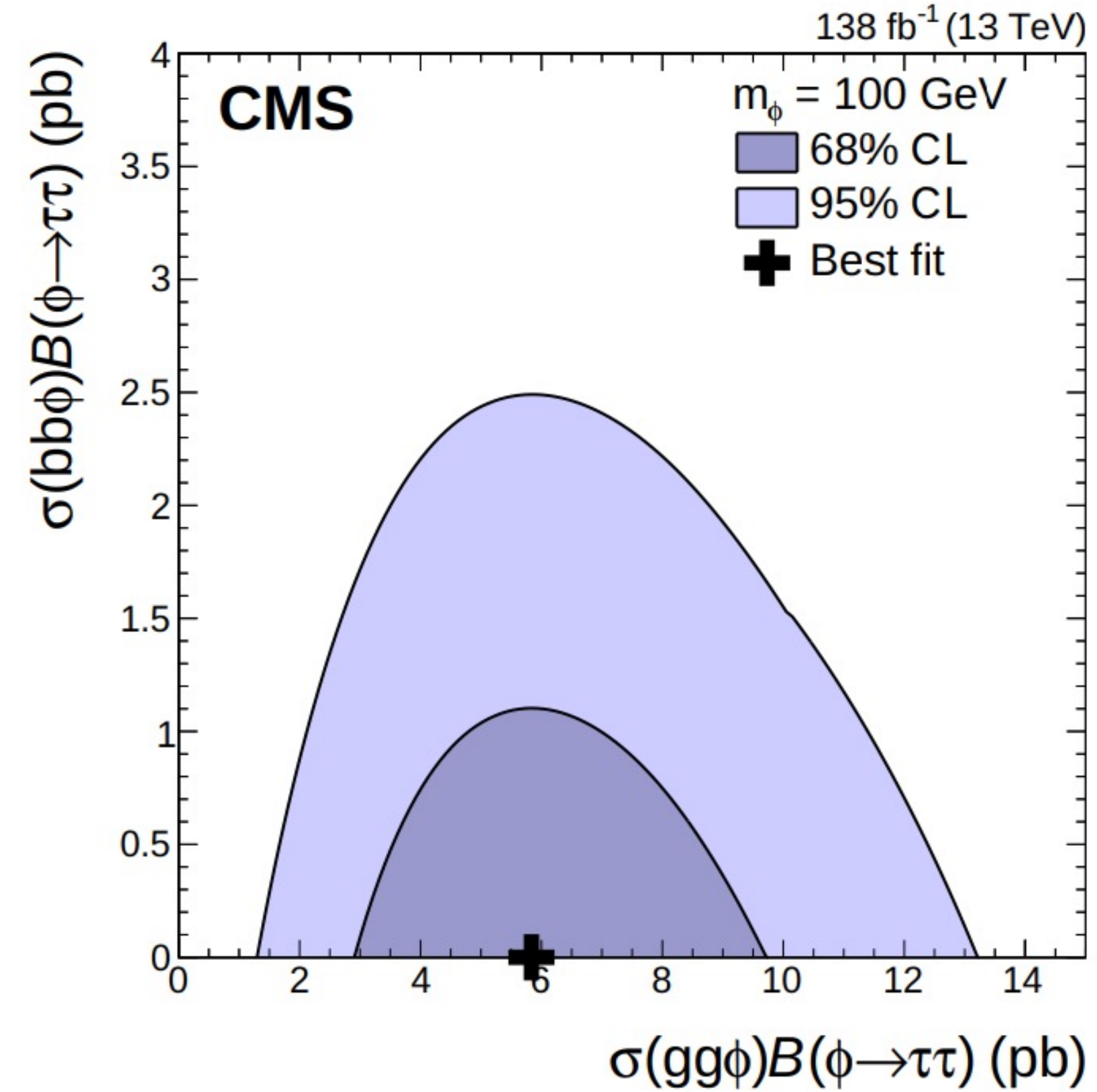
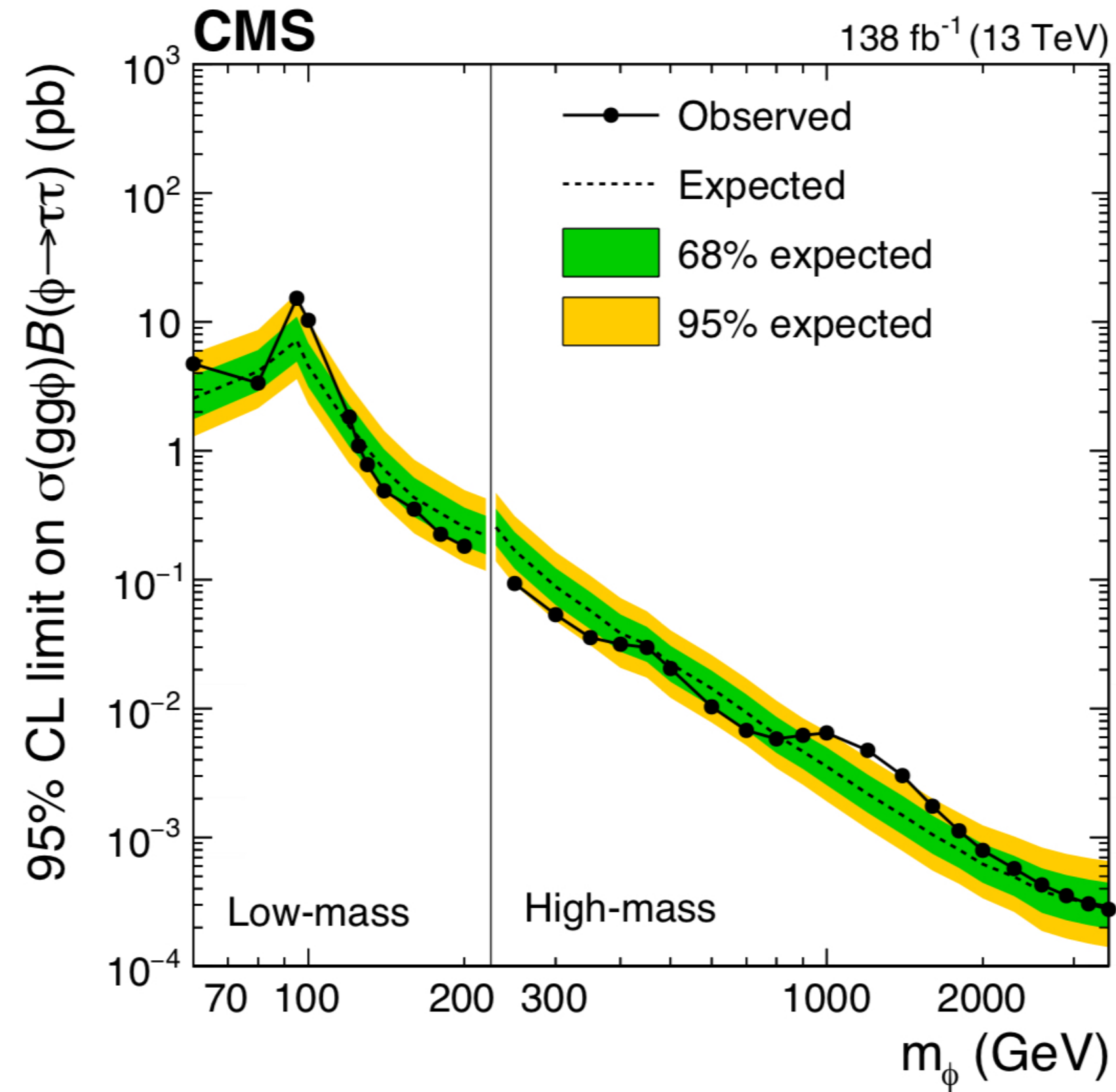
[T. Biekotter, S. Heinemeyer, G. Weiglein 2306.03889]

• [https://indico.cern.ch/event/1281604/attachments/2660420/4608571/LHCseminarArcangeletti\\_final.pdf](https://indico.cern.ch/event/1281604/attachments/2660420/4608571/LHCseminarArcangeletti_final.pdf)

# Motivation - III

◆ Excess at  $\sim 100$  GeV with local  $\sim 3 \sigma$

CMS 2208.02717

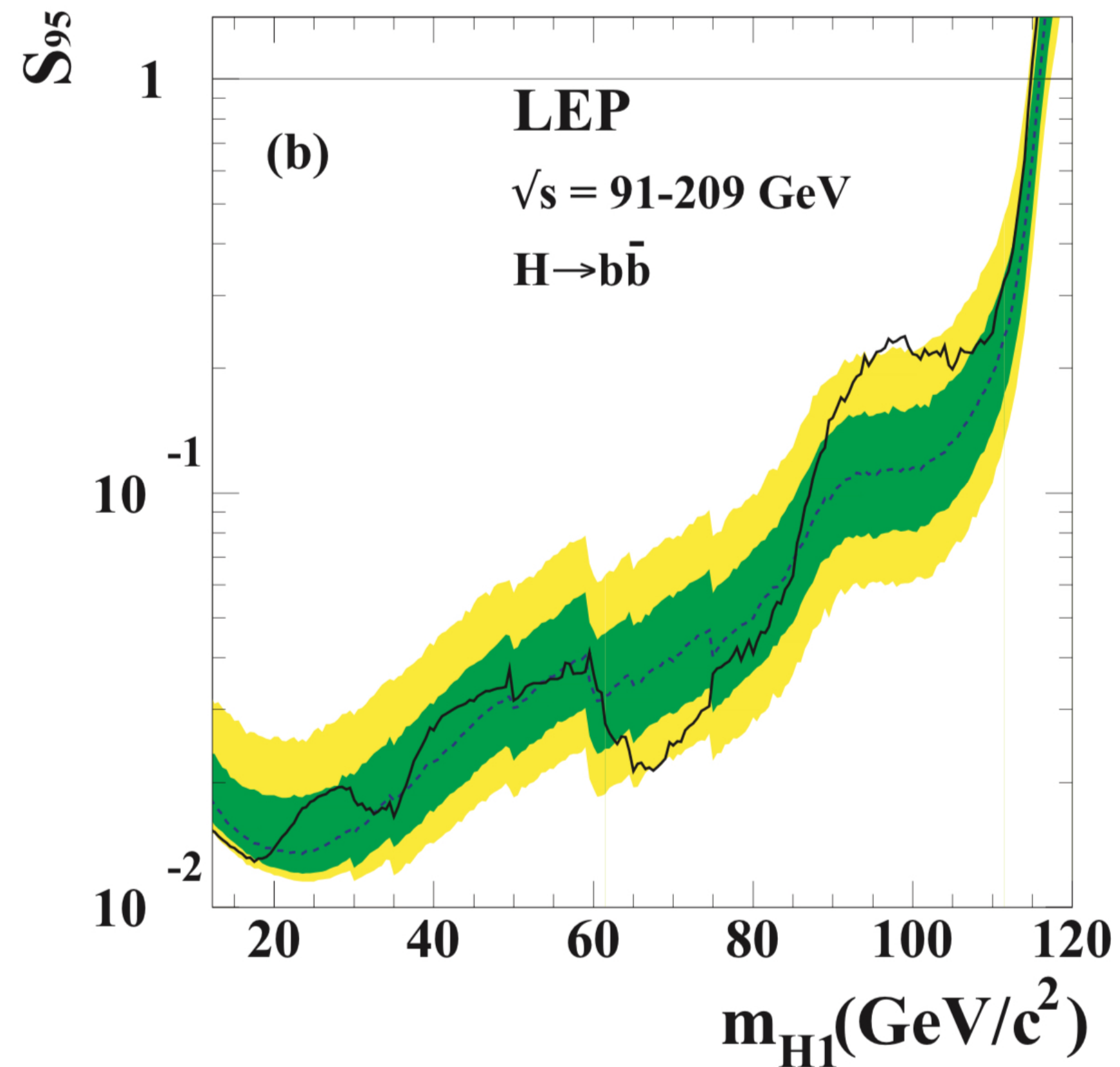


$$\mu_{\tau\tau}^{\text{exp}} = \frac{\sigma^{\text{exp}}(gg \rightarrow \phi \rightarrow \tau^+\tau^-)}{\sigma^{\text{SM}}(gg \rightarrow H \rightarrow \tau^+\tau^-)} = 1.2 \pm 0.5$$

# Evidence - IV

LEP hep-ex/ 0602042, 0306033

“Excess” at  $\sim 98$  GeV with local  $\sim 2.3 \sigma$



Particle with production cross section  
 $\sim 10\%$  of the SM

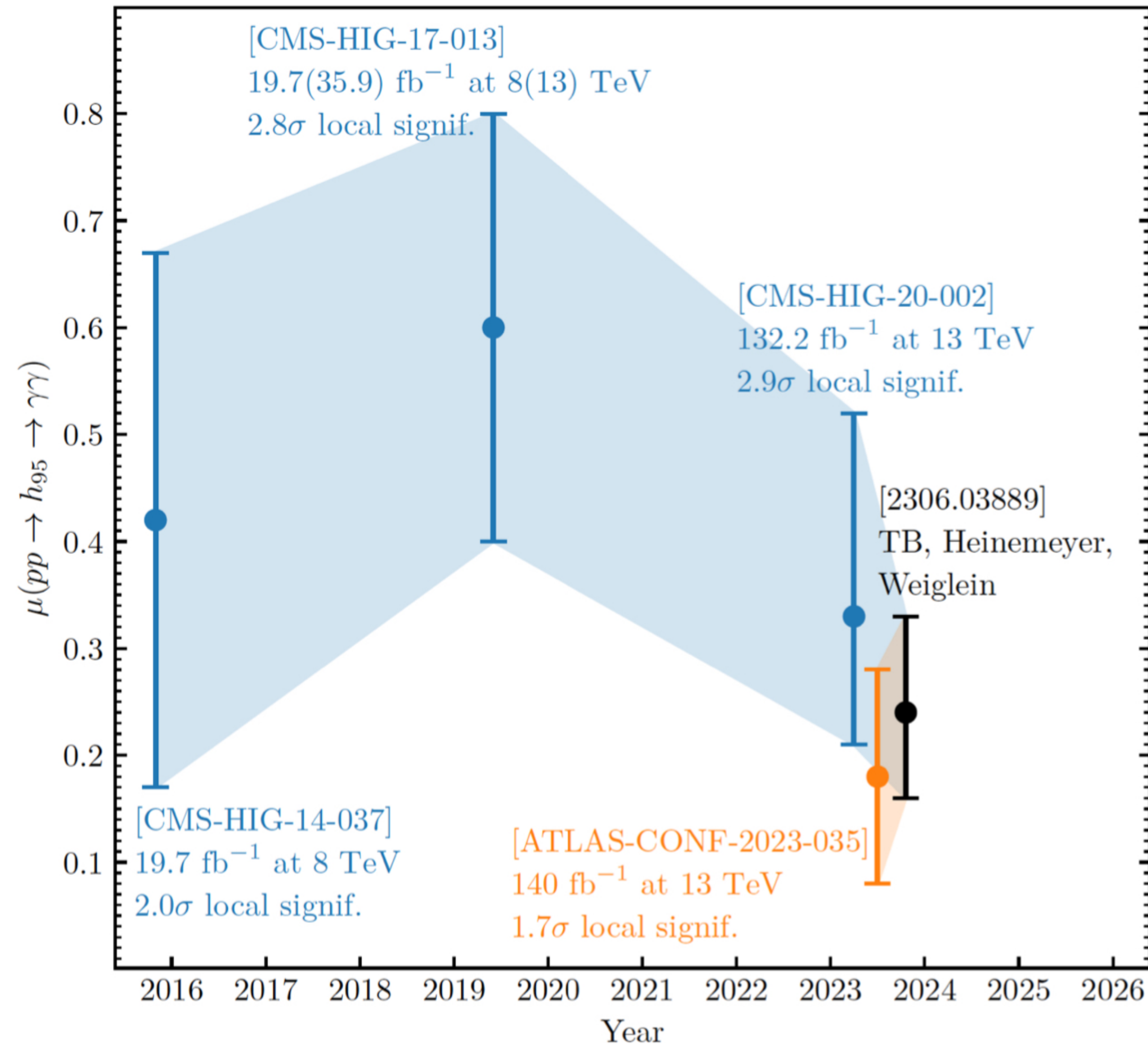
→ Suppressed VV coupling

Same origin ?

$$\mu_{bb}^{\text{exp}} = \frac{\sigma^{\text{exp}}(e^+e^- \rightarrow Z\phi \rightarrow Zb\bar{b})}{\sigma^{\text{SM}}(e^+e^- \rightarrow ZH \rightarrow Zb\bar{b})} = 0.117 \pm 0.057$$

arXiv : 1612.08522

# Diphoton over time



$$\mu_{\gamma\gamma}^{ATLAS} = 0.18 \pm 0.10 \quad (1.7\sigma)$$

$$\mu_{\gamma\gamma}^{ATLAS+CMS} = 0.24^{+0.09}_{-0.08} \quad (3.1\sigma)$$

[T. Biekotter, S. Heinemeyer, G. Weiglein 2306.03889]



# 2HDM

The most general scalar potential of the 2HDM :

$$\begin{aligned} V(\Phi_1\Phi_2) = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - [m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}] \\ & + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) \\ & + \left\{ \frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 + [\lambda_6 (\Phi_1^\dagger \Phi_1) + \lambda_7 (\Phi_2^\dagger \Phi_2)] \Phi_1^\dagger \Phi_2 + \text{h.c.} \right\} \end{aligned}$$

◆ CP conserving scenario : 10 free parameters  $m_{11}^2, m_{22}^2, m_{12}^2, \lambda_{1,\dots,7}$

◆ After EWSB  $\Phi_{1,2} = \begin{pmatrix} \phi_{1,2}^+ + i\varphi_{1,2}^+ \\ \frac{1}{\sqrt{2}} (v_{1,2} + \rho_{1,2} + i\eta_{1,2}) \end{pmatrix}$

◆ Minimization conditions and  $v_1^2 + v_2^2 = v^2$   $m_h, m_H, m_A, m_{H^\pm}, \sin(\beta - \alpha), \tan \beta, m_{12}^2$

◆ Physical states :  $h, H$  (CP-even),  $A$  (CP-odd),  $H^\pm$  (Charged)

# 2HDM

$$\mathcal{L}_{\text{Yukawa}}^{2\text{HDM}} = - \sum_{f=u,d,\ell} \frac{m_f}{v} \left( \xi_h^f \bar{f} f h + \xi_H^f \bar{f} f H - i \xi_A^f \bar{f} \gamma_5 f A \right) - \left\{ \frac{\sqrt{2} V_{ud}}{v} \bar{u} (m_u \xi_A^u P_L + m_d \xi_A^d P_R) d H^+ + \frac{\sqrt{2} m_\ell \xi_A^\ell}{v} \bar{\nu}_L \ell_R H^+ + \text{H.c.} \right\}$$

Discreet  $Z_2$  to forbid tree FCNC

$$\Phi_1 \rightarrow \Phi_1, \Phi_2 \rightarrow -\Phi_2$$

	$u$ -type	$d$ -type	leptons
type I	$\Phi_2$	$\Phi_2$	$\Phi_2$
type II	$\Phi_2$	$\Phi_1$	$\Phi_1$
(lepton-specific)	$\Phi_2$	$\Phi_2$	$\Phi_1$
type IV (flipped)	$\Phi_2$	$\Phi_1$	$\Phi_2$

Allowed fermion couplings

	Type I	Type II	Lepton-specific	Flipped
$\xi_h^u$	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$
$\xi_h^d$	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$
$\xi_h^\ell$	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$	$-\sin \alpha / \cos \beta$	$\cos \alpha / \sin \beta$

# Requirements to fit excesses

$$m_h = 95 \text{ GeV} \quad m_H = 125 \text{ GeV}$$

$C_{hVV}$  □ must be **strongly suppressed**

$$\mu_{b\bar{b}}^{\text{exp}} = 0.117 \pm 0.057$$

$C_{hb\bar{b}}$  □ must be **suppressed** to enhance  $BR(h \rightarrow \gamma\gamma)$

$$\mu_{\gamma\gamma}^{\text{exp}} = \mu_{\gamma\gamma}^{\text{ATLAS+CMS}} = 0.24_{-0.08}^{+0.09}$$

$C_{ht\bar{t}}$  □ must **not** be strongly **suppressed**

$$\mu_{\tau\tau}^{\text{exp}} = 1.2 \pm 0.5$$

$C_{h\tau\bar{\tau}}$  □ must **not** be **suppressed**

	Type I	Type II	Lepton-specific	Flipped
$\xi_h^u$	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$
$\xi_h^d$	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$
$\xi_h^\ell$	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$	$-\sin \alpha / \cos \beta$	$\cos \alpha / \sin \beta$

□ Type-II and flipped : tension between STU parameter measurements and  $b \rightarrow s\gamma$

# Type-III 2HDM

$$-\mathcal{L}_Y = \bar{Q}_L Y_1^u U_R \tilde{\Phi}_1 + \bar{Q}_L Y_2^u U_R \tilde{\Phi}_2 + \bar{Q}_L Y_1^d D_R \Phi_1 + \bar{Q}_L Y_2^d D_R \Phi_2 \\ + \bar{L} Y_1^\ell \ell_R \Phi_1 + \bar{L} Y_2^\ell \ell_R \Phi_2 + \text{H.c.},$$

- ◆ Generic Yukawa couplings, no discrete symmetry
- ◆ Specific Yukawa texture : **Must reproduce observed fermion masses and mixings**

$$M_l = \begin{pmatrix} 0 & C_l & 0 \\ C_l^* & 0 & B_l \\ 0 & B_l^* & A_l \end{pmatrix} \quad A_l \simeq m_3, B_l \simeq \sqrt{m_2 m_3} \text{ and } C_l \simeq \sqrt{m_1 m_2}$$

- ◆ FCNC effects  $\sim \sqrt{m_i m_j} / m_W$

**Cheng, Sher PRD'1987**

See Hernandez-Sanchez, Moretti, Noriega-Papaqui, Rosado  
1212.6818

# Type-III 2HDM

After EWSB

$$\begin{aligned}
 -\mathcal{L}_Y^{\text{III}} = & \sum_{f=u,d,\ell} \frac{m_j^f}{v} \times \left( (\xi_h^f)_{ij} \bar{f}_{Li} f_{Rj} h + (\xi_H^f)_{ij} \bar{f}_{Li} f_{Rj} H - i(\xi_A^f)_{ij} \bar{f}_{Li} f_{Rj} A \right) \\
 & + \frac{\sqrt{2}}{v} \sum_{k=1}^3 \bar{u}_i \left[ (m_i^u (\xi_A^{u*})_{ki} V_{kj} P_L + V_{ik} (\xi_A^d)_{kj} m_j^d P_R) \right] d_j H^+ \\
 & + \frac{\sqrt{2}}{v} \bar{\nu}_i (\xi_A^\ell)_{ij} m_j^\ell P_R \ell_j H^+ + \text{H.c.},
 \end{aligned}$$

Type-III 2HDM Yukawa couplings

$\phi$	$(\xi_\phi^u)_{ij}$	$(\xi_\phi^d)_{ij}$	$(\xi_\phi^\ell)_{ij}$
$h$	$\frac{c_\alpha}{s_\beta} \delta_{ij} - \frac{c_{\beta-\alpha}}{\sqrt{2}s_\beta} \sqrt{\frac{m_i^u}{m_j^u}} \chi_{ij}^u$	$-\frac{s_\alpha}{c_\beta} \delta_{ij} + \frac{c_{\beta-\alpha}}{\sqrt{2}c_\beta} \sqrt{\frac{m_i^d}{m_j^d}} \chi_{ij}^d$	$-\frac{s_\alpha}{c_\beta} \delta_{ij} + \frac{c_{\beta-\alpha}}{\sqrt{2}c_\beta} \sqrt{\frac{m_i^\ell}{m_j^\ell}} \chi_{ij}^\ell$
$H$	$\frac{s_\alpha}{s_\beta} \delta_{ij} + \frac{s_{\beta-\alpha}}{\sqrt{2}s_\beta} \sqrt{\frac{m_i^u}{m_j^u}} \chi_{ij}^u$	$\frac{c_\alpha}{c_\beta} \delta_{ij} - \frac{s_{\beta-\alpha}}{\sqrt{2}c_\beta} \sqrt{\frac{m_i^d}{m_j^d}} \chi_{ij}^d$	$\frac{c_\alpha}{c_\beta} \delta_{ij} - \frac{s_{\beta-\alpha}}{\sqrt{2}c_\beta} \sqrt{\frac{m_i^\ell}{m_j^\ell}} \chi_{ij}^\ell$
$A$	$\frac{1}{t_\beta} \delta_{ij} - \frac{1}{\sqrt{2}s_\beta} \sqrt{\frac{m_i^u}{m_j^u}} \chi_{ij}^u$	$t_\beta \delta_{ij} - \frac{1}{\sqrt{2}c_\beta} \sqrt{\frac{m_i^d}{m_j^d}} \chi_{ij}^d$	$t_\beta \delta_{ij} - \frac{1}{\sqrt{2}c_\beta} \sqrt{\frac{m_i^\ell}{m_j^\ell}} \chi_{ij}^\ell$

◆ Free parameters

$$m_h, m_H, m_A, m_{H^\pm}, \sin(\beta - \alpha), \tan \beta, m_{12}^2, \chi_{ij}$$

# Explaining the excesses

$$m_h = 95 \text{ GeV} \quad m_H = 125 \text{ GeV}$$

$$\mu_{b\bar{b}} = \frac{\sigma_{2\text{HDM}}(e^+e^- \rightarrow Z\phi)}{\sigma_{\text{SM}}(e^+e^- \rightarrow Zh_{\text{SM}})} \times \frac{\mathcal{BR}_{2\text{HDM}}(\phi \rightarrow b\bar{b})}{\mathcal{BR}_{\text{SM}}(h_{\text{SM}} \rightarrow b\bar{b})} = |c_{\phi ZZ}|^2 \times \frac{\mathcal{BR}_{2\text{HDM}}(\phi \rightarrow b\bar{b})}{\mathcal{BR}_{\text{SM}}(h_{\text{SM}} \rightarrow b\bar{b})}$$

$$\mu_{\tau\tau} = \frac{\sigma_{2\text{HDM}}(gg \rightarrow \phi)}{\sigma_{\text{SM}}(gg \rightarrow h_{\text{SM}})} \times \frac{\mathcal{BR}_{2\text{HDM}}(\phi \rightarrow \tau\tau)}{\mathcal{BR}_{\text{SM}}(h_{\text{SM}} \rightarrow \tau\tau)} = |c_{\phi tt}|^2 \times \frac{\mathcal{BR}_{2\text{HDM}}(\phi \rightarrow \tau\tau)}{\mathcal{BR}_{\text{SM}}(h_{\text{SM}} \rightarrow \tau\tau)}$$

$$\mu_{\gamma\gamma} = \frac{\sigma_{2\text{HDM}}(gg \rightarrow \phi)}{\sigma_{\text{SM}}(gg \rightarrow h_{\text{SM}})} \times \frac{\mathcal{BR}_{2\text{HDM}}(\phi \rightarrow \gamma\gamma)}{\mathcal{BR}_{\text{SM}}(h_{\text{SM}} \rightarrow \gamma\gamma)} = |c_{\phi tt}|^2 \times \frac{\mathcal{BR}_{2\text{HDM}}(\phi \rightarrow \gamma\gamma)}{\mathcal{BR}_{\text{SM}}(h_{\text{SM}} \rightarrow \gamma\gamma)}$$

$$\chi_{\gamma\gamma, \tau\tau, b\bar{b}}^2 = \frac{\left(\mu_{\gamma\gamma, \tau\tau, b\bar{b}} - \mu_{\gamma\gamma, \tau\tau, b\bar{b}}^{\text{exp}}\right)^2}{\left(\Delta\mu_{\gamma\gamma, \tau\tau, b\bar{b}}^{\text{exp}}\right)^2}$$

$$\chi_{\gamma\gamma + \tau\tau + b\bar{b}}^2 = \chi_{\gamma\gamma}^2 + \chi_{\tau\tau}^2 + \chi_{b\bar{b}}^2$$

See Benbrik, Boukidi, Moretti 2405.02899 for **CP-odd contributions**

# Numerical analysis

2HDMC-1.8.0

## Theoretical constraints

- Unitarity : tree 2-to-2 scattering matrix eigenvalues  $|e_i| < 8\pi$
- Perturbativity  $|\lambda_i| < 8\pi$
- Vacuum stability

$$\lambda_1 > 0, \quad \lambda_2 > 0, \quad \lambda_3 > -\sqrt{\lambda_1 \lambda_2},$$
$$\lambda_3 + \lambda_4 - |\lambda_5| > -\sqrt{\lambda_1 \lambda_2}.$$

## Experimental constraints

- EWPO.  $S = 0.05 \pm 0.08$ ,  $T = 0.09 \pm 0.07$ ,  $\rho_{ST} = 0.92$  (for  $U = 0$ )
- SM-like Higgs boson constraints  
HiggsSignals-3 via HiggsTools
- Non-SM-like Higgs constraints  
HiggsBounds-6 via HiggsTools
- B-physics observables  
(mainly  $B \rightarrow X_s \gamma$ ,  $B_{s,d} \rightarrow \mu^+ \mu^-$  and  $B_s \rightarrow \tau \nu$ )

SuperIso\_v4.1

$m_h$	$m_H$	$m_A$	$m_{H^\pm}$	$s_{\beta-\alpha}$	$\tan \beta$	$m_{12}^2$	$\chi_{ij}^{f,\ell}$
[94; 97]	125.09	[80; 300]	[160; 200]	[-0.5; 0]	[1; 30]	$m_h^2 \tan \beta / (1 + \tan^2 \beta)$	[-3; 3]

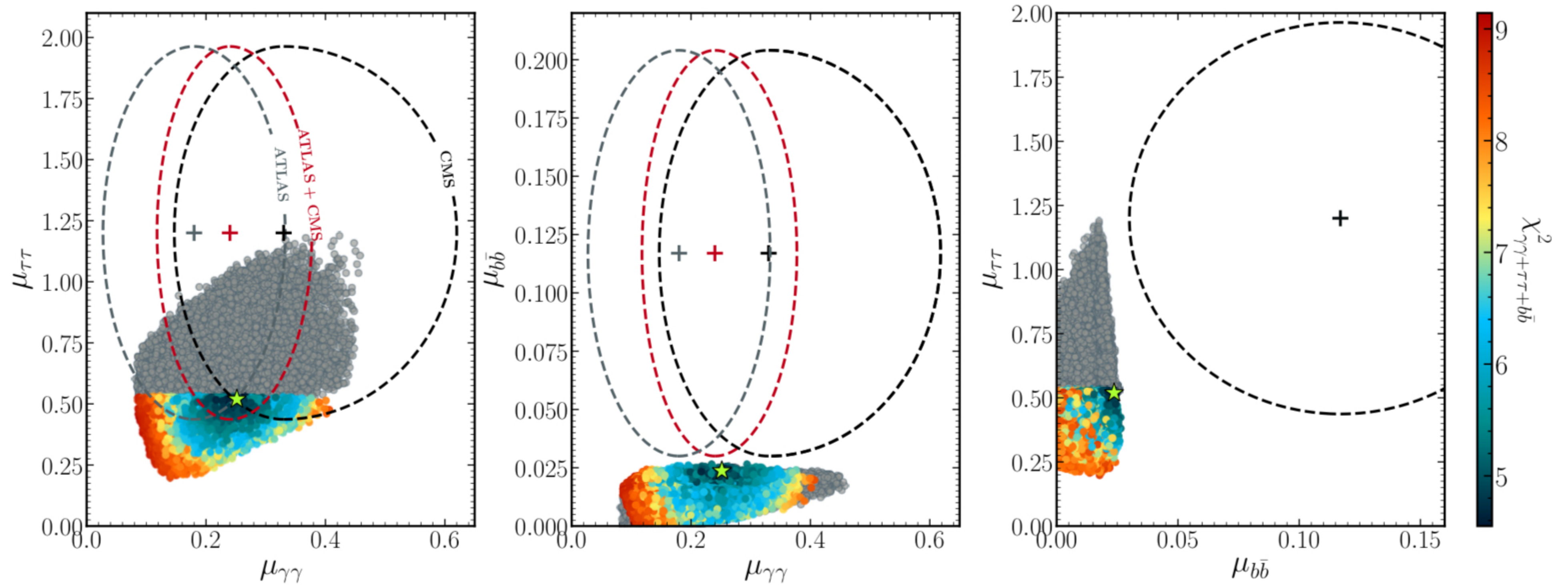
# 2HDM Type-III interpretation

$$\chi_{125}^2 \leq 189.4 \quad (159 \text{ dof})$$

--- 1 $\sigma$  C.L. (2.30) for  $\chi_{x+y}^2$     +  $\mu_{\gamma\gamma, \tau\tau, b\bar{b}}^{\text{exp}}$

★  $\min(\chi_{\gamma\gamma+\tau\tau+b\bar{b}}^2)$

● Excluded by  $\sigma(t\bar{t}\phi) \times \mathcal{BR}(\phi \rightarrow \tau\tau)$  [CMS-PAS-EXO-21-018]

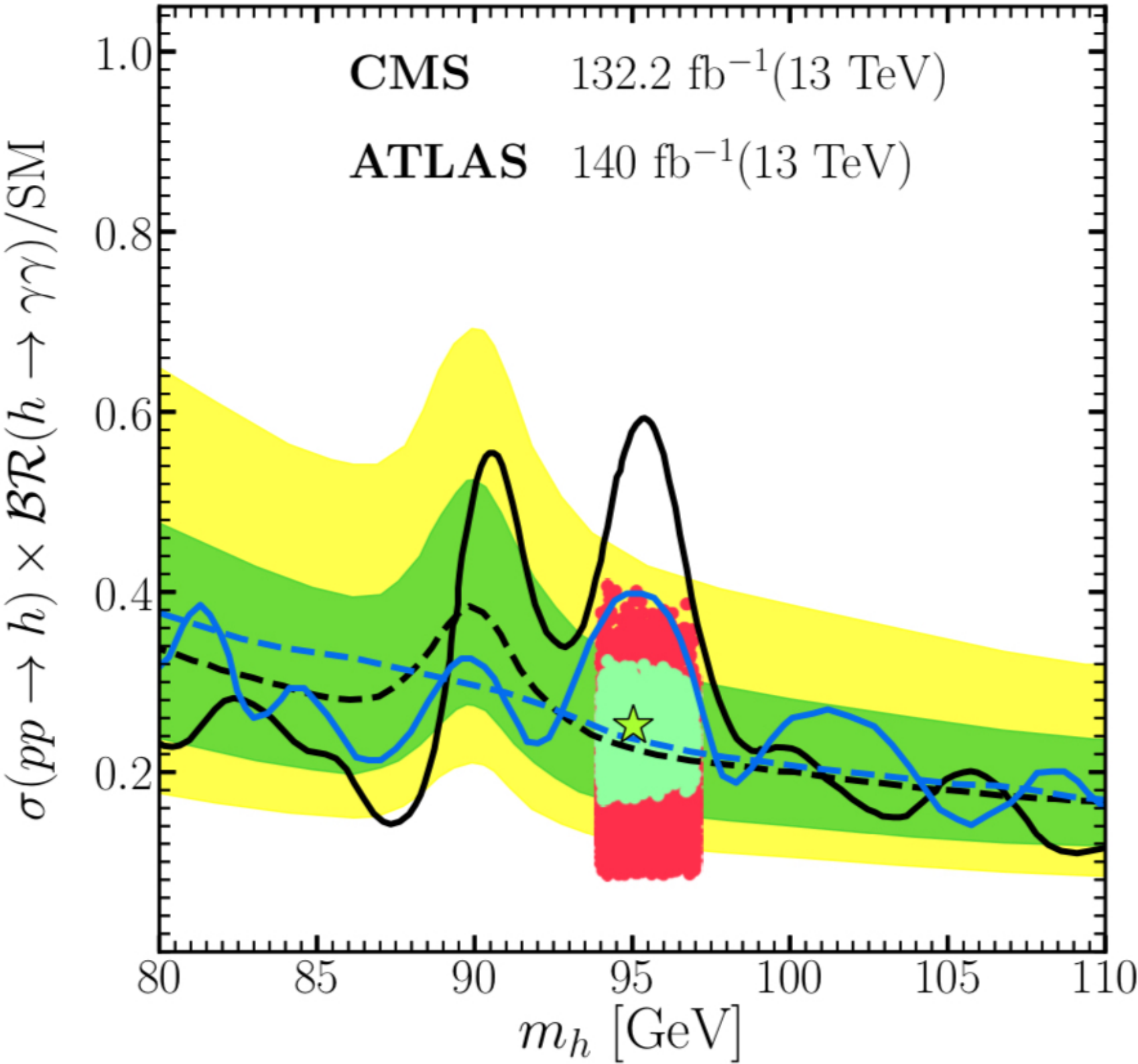


Best fit point :  $\chi_{\gamma\gamma+\tau\tau+b\bar{b}}^2 = 4.55 \sim 1.2\sigma$

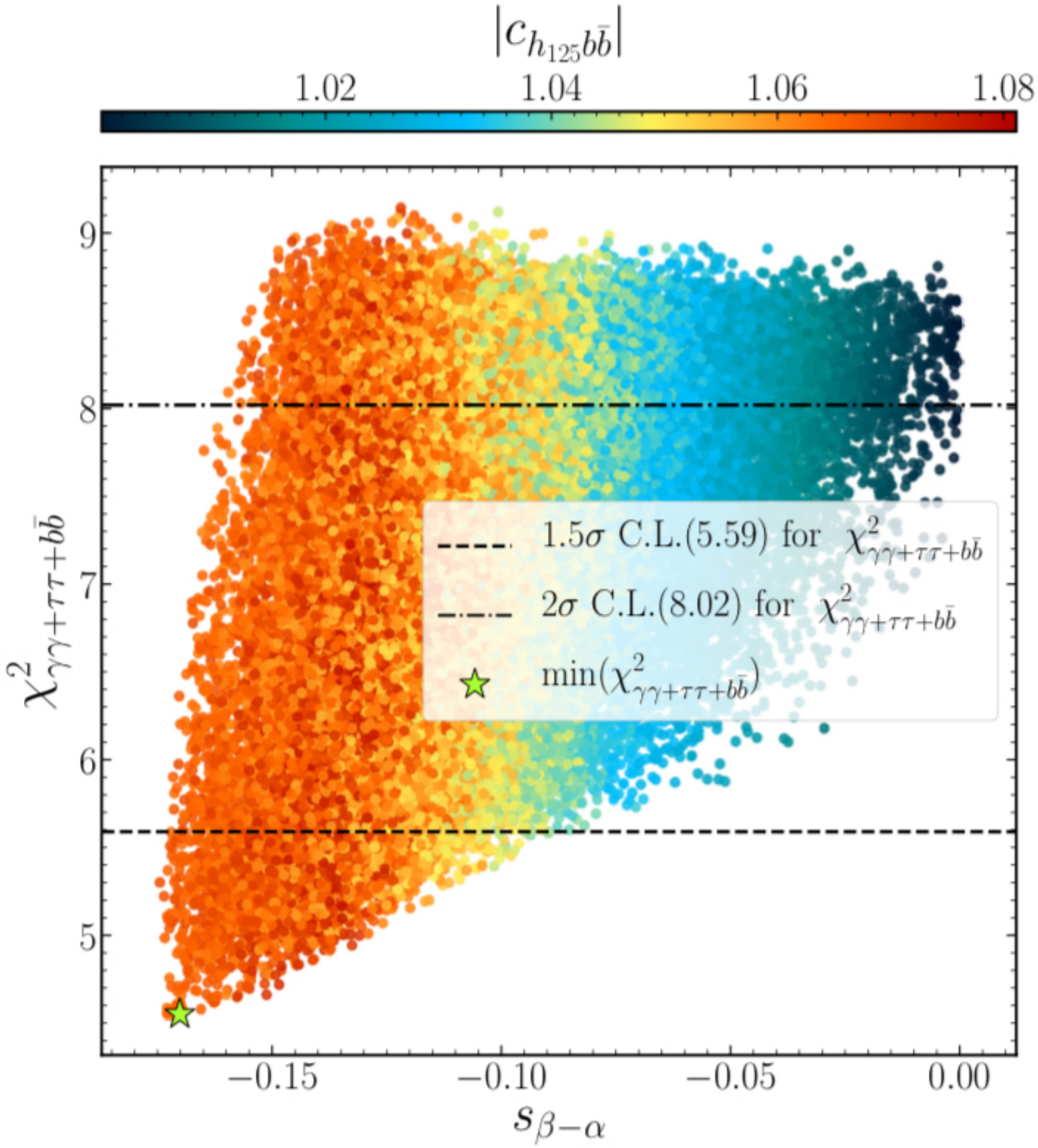
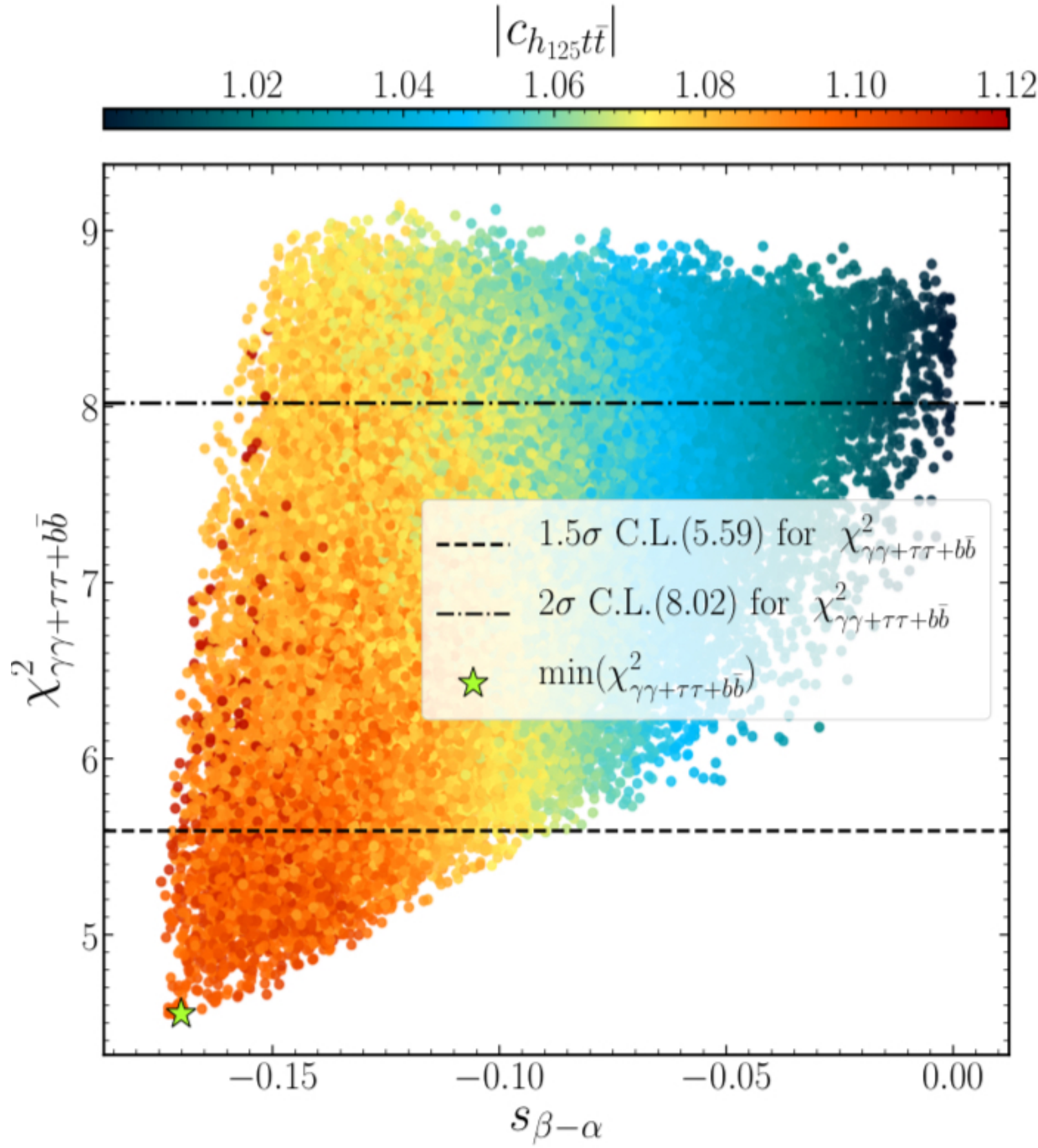


# 2HDM Type-III interpretation

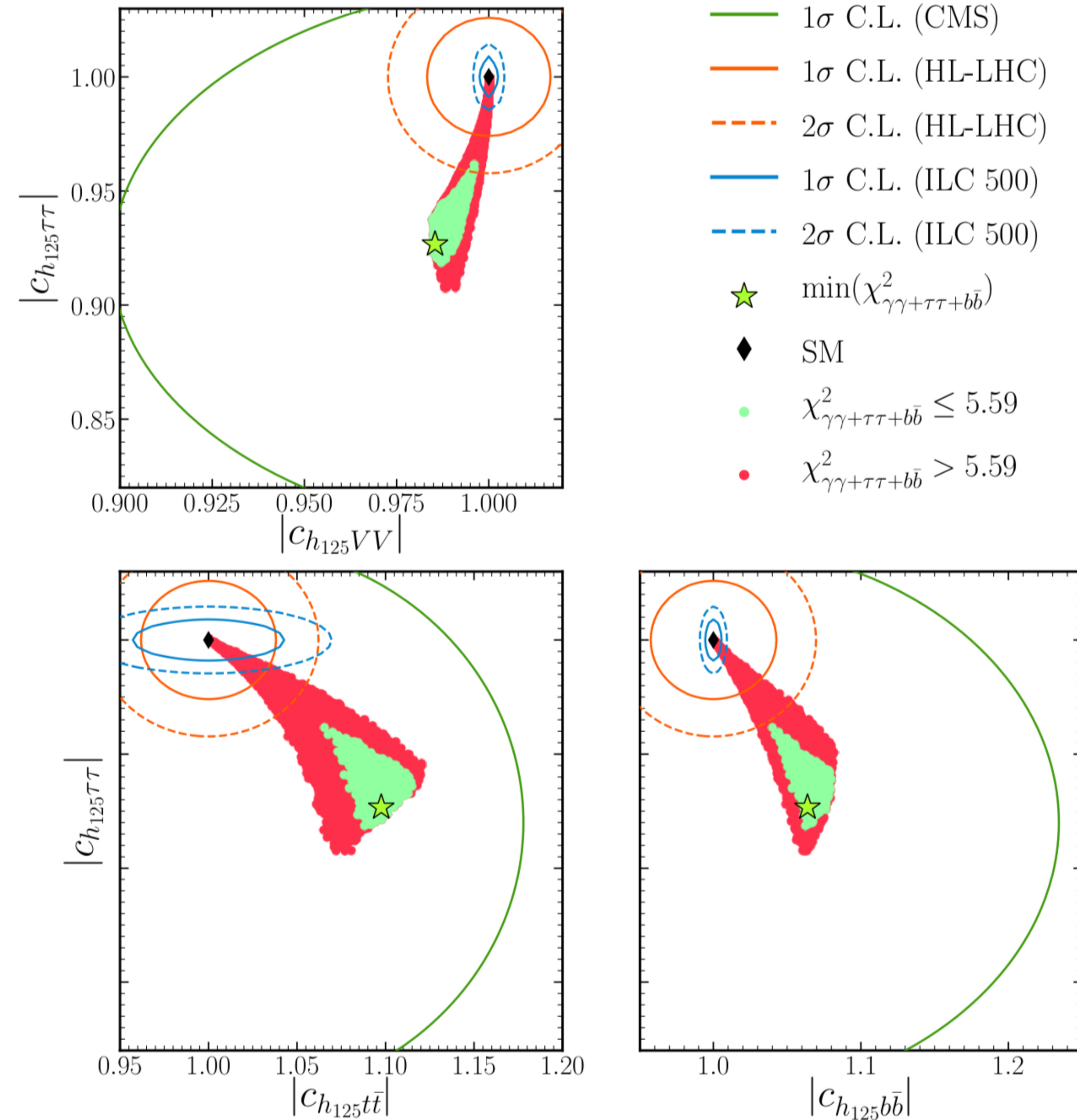
- Observed
- Expected  $\pm 1\sigma$
- Expected  $\pm 2\sigma$
- **ATLAS** obs.
- **ATLAS** exp.
- $\chi^2_{\gamma\gamma+\tau\tau+b\bar{b}} \leq 5.59$  ( $1.5\sigma$  C.L.)
- $\chi^2_{\gamma\gamma+\tau\tau+b\bar{b}} > 5.59$
- ★  $\min(\chi^2_{\gamma\gamma+\tau\tau+b\bar{b}})$









# 2HDM Type-III interpretation

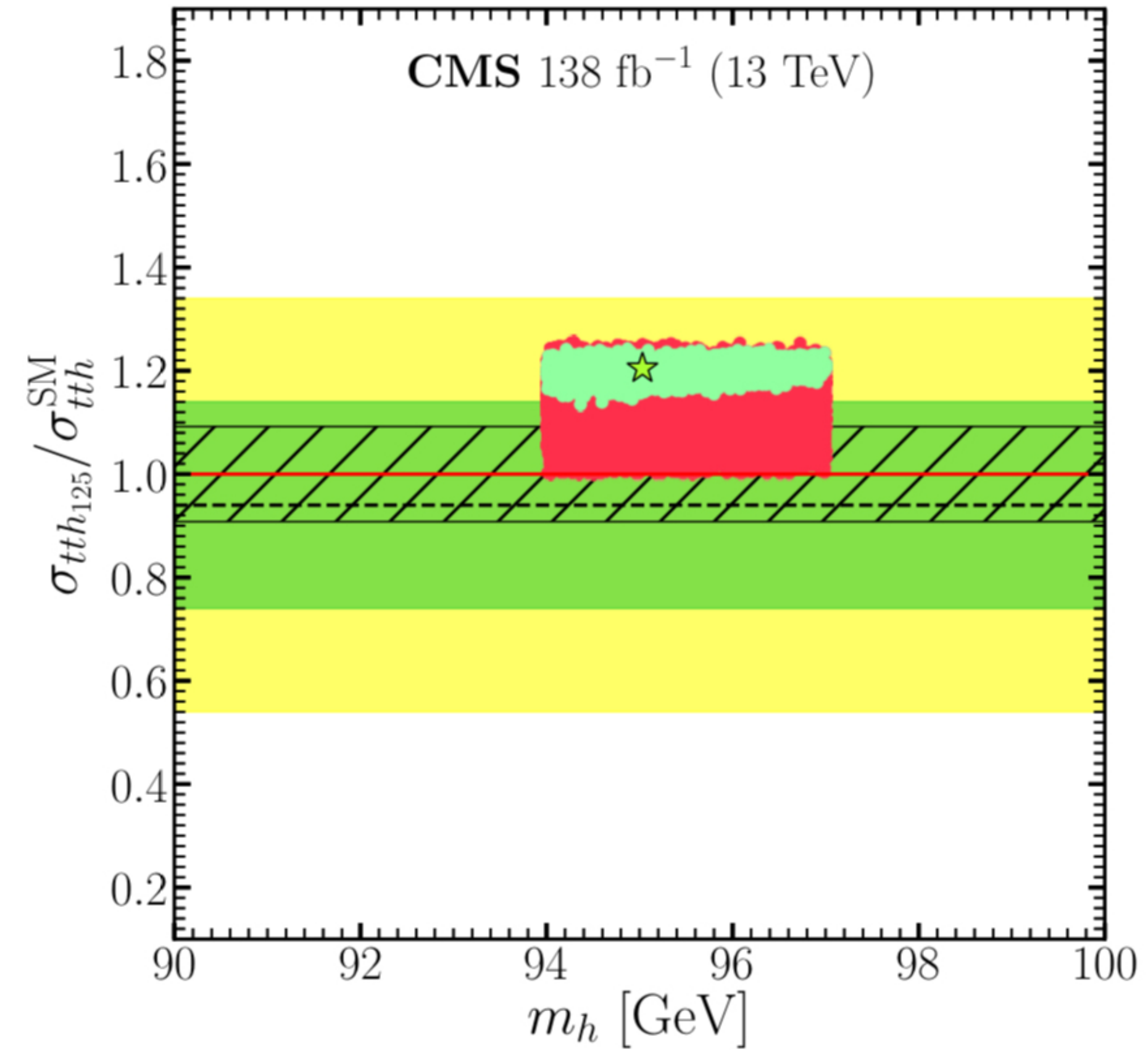


# Correlation between couplings



# Testability in future colliders

-  Observed  $\pm 1\sigma$
-  Observed  $\pm 2\sigma$
-  HL-LHC  $\pm 2\sigma$
-   $\chi^2_{\gamma\gamma+\tau\tau+b\bar{b}} \leq 5.59$  (1.5 $\sigma$  C.L.)
-   $\chi^2_{\gamma\gamma+\tau\tau+b\bar{b}} > 5.59$
-   $\min(\chi^2_{\gamma\gamma+\tau\tau+b\bar{b}})$



# Best-fit point

Parameters	★
(Masses are in GeV)	
$m_h$	95.03
$m_H$	125.09
$m_A$	94.77
$m_{H^\pm}$	162.95
$\tan \beta$	1.74
$\sin(\beta - \alpha)$	-0.17
$\chi_{11}^u$	0.02
$\chi_{22}^u$	0.54
$\chi_{33}^u$	-0.08
$\chi_{11}^d$	-0.41
$\chi_{22}^d$	0.24
$\chi_{33}^d$	1.55
$\chi_{11}^\ell$	-0.06
$\chi_{22}^\ell$	0.33
$\chi_{33}^\ell$	0.97
Effective coupling $c_{h_{125}i\bar{i}}$	
$c_{h_{125}t\bar{t}}$	1.10
$c_{h_{125}b\bar{b}}$	1.06
$c_{h_{125}\tau\tau}$	0.92
Collider signal strength	
$\mu_{\gamma\gamma}$	0.25
$\mu_{\tau\tau}$	0.51
$\mu_{b\bar{b}}$	0.02
Total decay width in MeV	
$\Gamma(h)$	0.27
$\Gamma(H)$	4.73
$\Gamma(A)$	0.66
$\Gamma(H^\pm)$	4.77

$BR(h \rightarrow XY)$ in %	
$BR(h \rightarrow \gamma\gamma)$	0.15
$BR(h \rightarrow gg)$	13.82
$BR(h \rightarrow b\bar{b})$	65.37
$BR(h \rightarrow c\bar{c})$	—
$BR(h \rightarrow s\bar{s})$	0.50
$BR(h \rightarrow \mu^+\mu^-)$	0.67
$BR(h \rightarrow \tau\tau)$	19.33
$BR(h \rightarrow ZZ)$	—
$BR(h \rightarrow W^+W^-)$	0.12
$BR(H \rightarrow XY)$ in %	
$BR(H \rightarrow \gamma\gamma)$	0.16
$BR(H \rightarrow gg)$	8.16
$BR(H \rightarrow b\bar{b})$	64.08
$BR(H \rightarrow c\bar{c})$	3.07
$BR(H \rightarrow \tau\tau)$	4.70
$BR(H \rightarrow ZZ)$	2.19
$BR(H \rightarrow W^+W^-)$	17.48
$BR(A \rightarrow XY)$ in %	
$BR(A \rightarrow \gamma\gamma)$	0.046
$BR(A \rightarrow gg)$	28.70
$BR(A \rightarrow b\bar{b})$	66.95
$BR(A \rightarrow c\bar{c})$	0.40
$BR(A \rightarrow \mu\mu)$	0.16
$BR(A \rightarrow \tau\tau)$	3.53
$BR(H^\pm \rightarrow XY)$ in %	
$BR(H^\pm \rightarrow cs)$	0.11
$BR(H^\pm \rightarrow W^+h)$	33.79
$BR(H^\pm \rightarrow W^+A)$	35.62
$BR(H^\pm \rightarrow \tau\nu)$	0.84
$BR(H^\pm \rightarrow tb)$	29.47

# Summary

- ◆ Interesting set of anomalies around  $\sim 95$  GeV in CMS  $\gamma\gamma, \tau\tau$ , LEP  $b\bar{b}$  channels
- ◆ ATLAS  $\gamma\gamma$  searches also see hints
- ◆ Same origin ?
- ◆ Type-III 2HDM offers explanation with  $m_h \approx 95$  GeV and  $m_H \approx 125$  GeV
- ◆ Stringent constraints on  $\mu_{\tau\tau}$  from CMS  $t\bar{t}h, Zh$  production searches
- ◆ Precision measurement of 125 GeV Higgs couplings @ HL-LHC, ILC can be conclusive

# ALIGNMENT LIMIT

In the Higgs-basis the alignment limit is most clearly exhibited :

$$H_1 = \begin{pmatrix} H_1^+ \\ H_1^0 \end{pmatrix} \equiv \Phi_1 \cos \beta + \Phi_2 \sin \beta, \quad H_2 = \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix} \equiv -\Phi_1 \sin \beta + \Phi_2 \cos \beta$$

$$H_1 = \begin{pmatrix} G^+ \\ (v + S_1 + iG^0) / \sqrt{2} \end{pmatrix}, \quad H_2 = \begin{pmatrix} H^+ \\ (S_2 + iS_3) / \sqrt{2} \end{pmatrix}$$

The 2 physical Higgs states  $h$  et  $H$  are as follows:

$$H = (\sqrt{2}\text{Re}H_1^0 - v)\cos(\beta - \alpha) + \sqrt{2}\text{Re}H_2^0 \sin(\beta - \alpha) \quad (4)$$

$$h = (\sqrt{2}\text{Re}H_1^0 - v)\sin(\beta - \alpha) + \sqrt{2}\text{Re}H_2^0 \cos(\beta - \alpha) \quad (5)$$

- ◆  $\cos(\beta - \alpha) \rightarrow 0$ ,  $h \equiv H_{SM}$  (J. Bernon, J. F. Gunion, H. E. Haber, Y. Jiang and S. Kraml, Phys. Rev. D 92 (2015) no.7, 075004 ) ; standard hierarchy
- ◆  $\sin(\beta - \alpha) \rightarrow 0$ ,  $H \equiv H_{SM}$  (J. Bernon, J. F. Gunion, H. E. Haber, Y. Jiang and S. Kraml, Phys. Rev. D 93 (2016) no.3, 035027 ) ; inverted hierarchy