

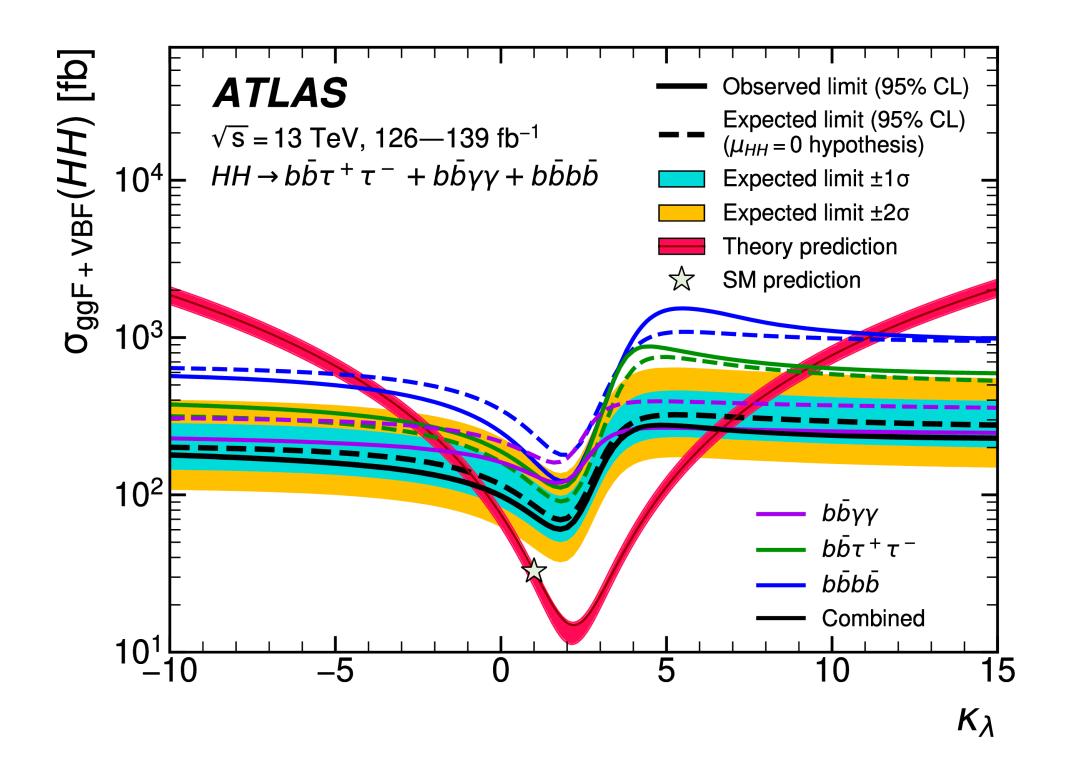
Higgs Symmetry Breaking and HHH at LHC

Osama Karkout

Working with Jorinde van de Vis, Marieke Postma, Andreas Papaefstathiou, Gilberto Tetlalmatzi, Tristan du Pree



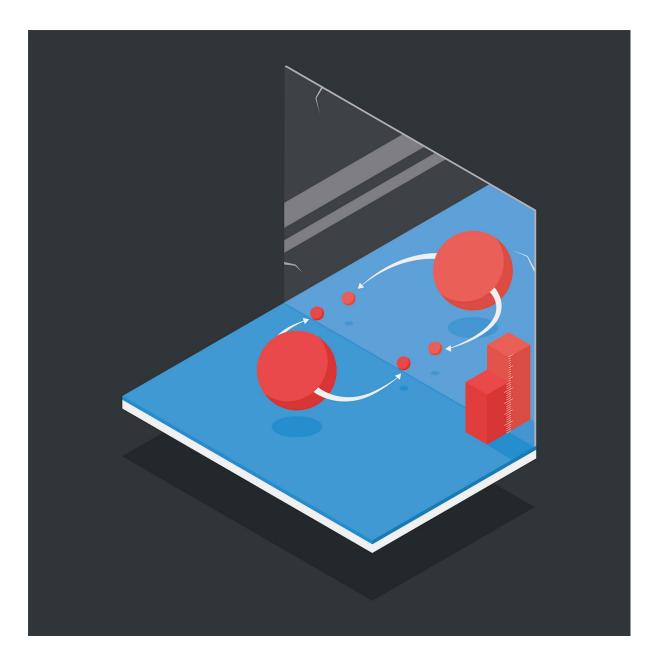
Project: ATLAS Higgs results \rightarrow matter-antimatter asymmetry



Nik hef Mul

MultiHiggs production and EWSB

?



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matter-antimatter asymmetry

Cosmic rays: $\bar{p}/p = 10^{-4}$ = no ambient antiprotons (\bar{p})

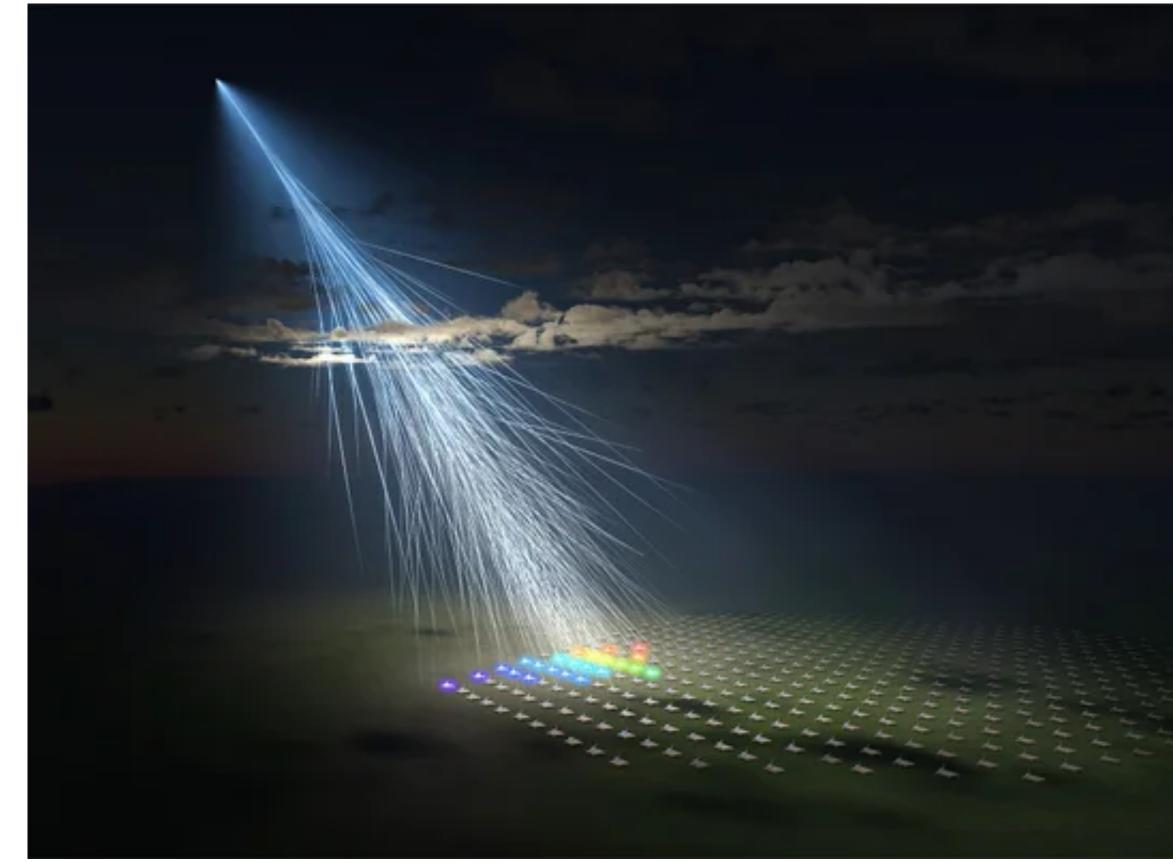
BIG DEAL!

Lorentz invariance + Hermitian Hamiltonian (physical observables are real) = matter-antimatter symmetry (CPT) is conserved!

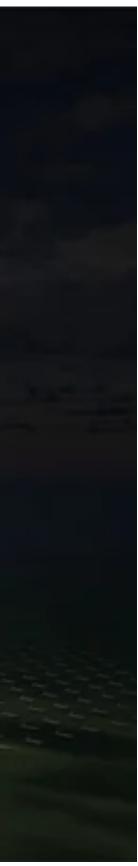
True in SM and any BSM!!!!



MultiHiggs production and EWSB



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Baryogenesis (matter-antimatter asymmetry)

Problem: we exist :(

(CPT) is conserved => need for **dynamical** mechanism to generate matter-antimatter asymmetry.

Sakharov conditions:

- Baryon number violation
- Loss of thermal equilibrium
- Break C and CP symmetries

In SM: all related to the Higgs field

https://arxiv.org/pdf/hep-ph/0609145.pdf

https://arxiv.org/pdf/2301.05197.pdf http://www.laine.itp.unibe.ch/cosmology/lec09.pdf BARYOGENESIS

James M. Cline



MultiHiggs production and EWSB



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Baryon number violation

In SM: left handed B+L violated!



MultiHiggs production and EWSB

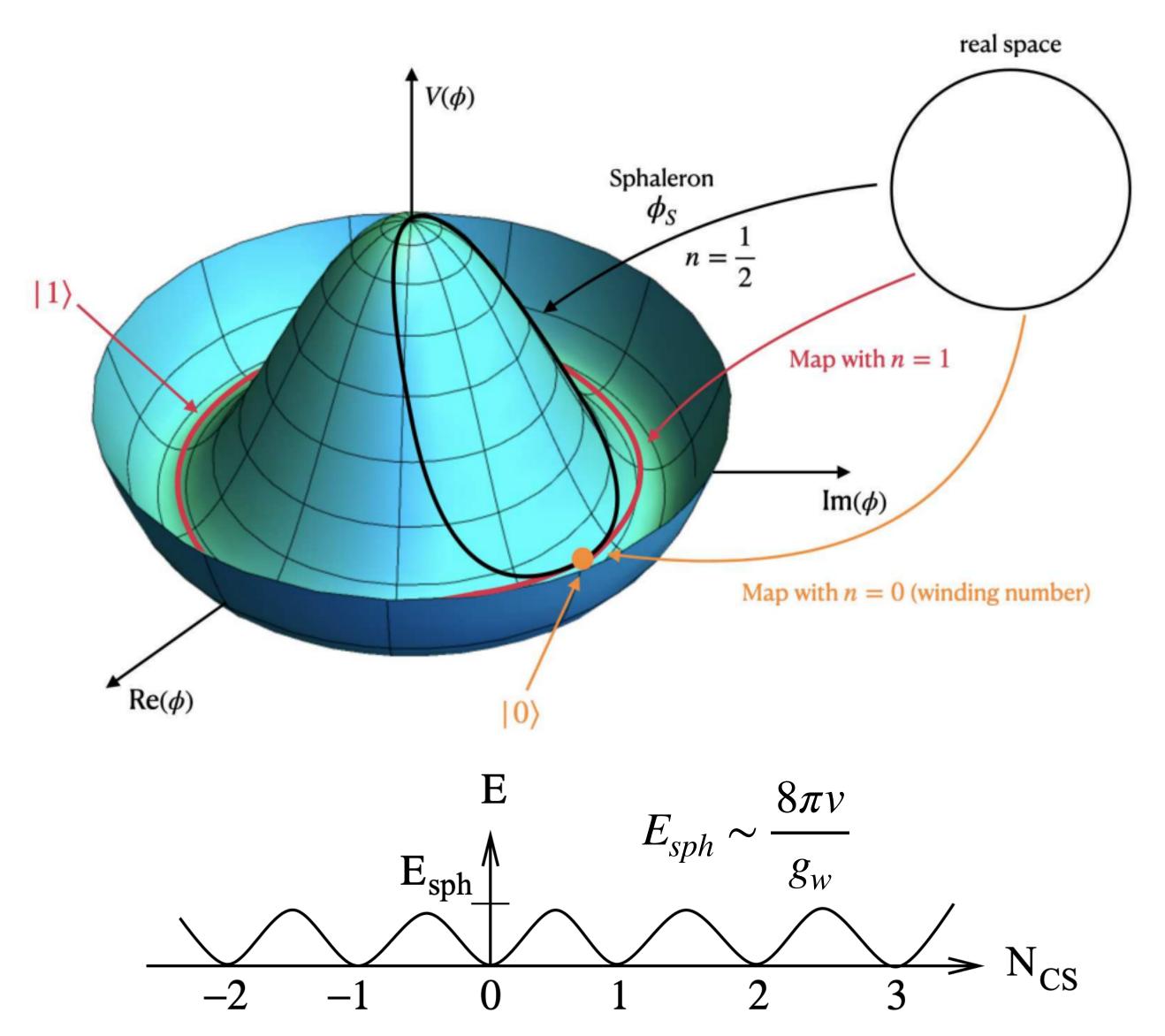


Fig. 8. Energy of gauge field configurations as a function of Chern-Simons number.

v is the Higgs VEV

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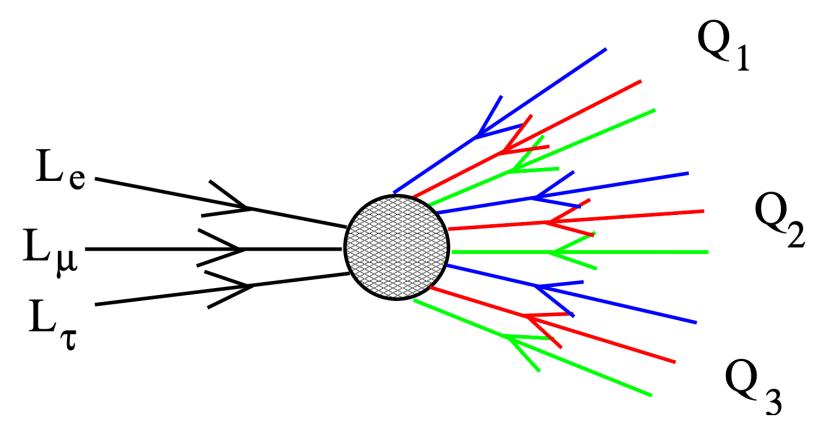
Baryon number violation

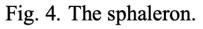
In SM: left handed B+L violated!

$$\partial_{\mu}J^{\mu}_{B_{L}+L_{L}} = \frac{3g^{2}}{32\pi^{2}}\epsilon_{\alpha\beta\gamma\delta}W^{\alpha\beta}_{a}W^{\gamma\delta}_{a}$$

where $W_a^{\alpha\beta}$ is the SU(2) field strength.

$$\Delta B = \Delta L = \pm 3 \tag{2.2}$$







MultiHiggs production and EWSB

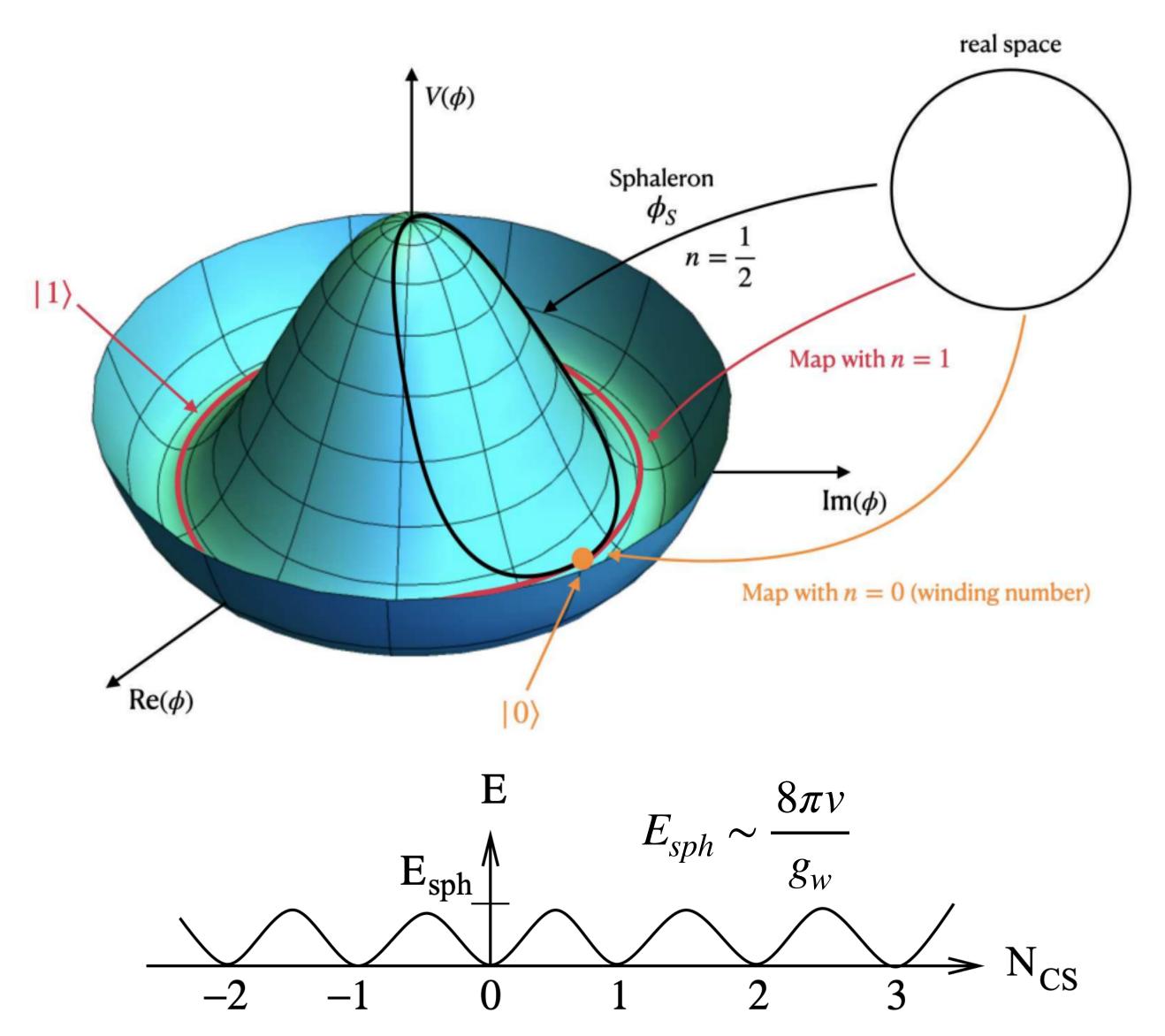


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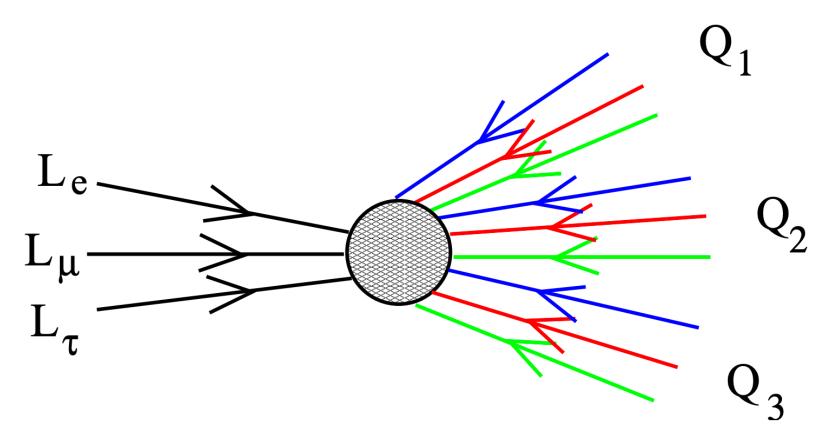
Baryon number violation

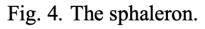
Rate of tunnelling to another vacuum:

$$\Gamma_{sph}(T) \sim e^{-E_{sph}/T} \sim e^{-v/T}$$

 $\Delta B = \Delta L = \pm 3$

(2.2)







MultiHiggs production and EWSB

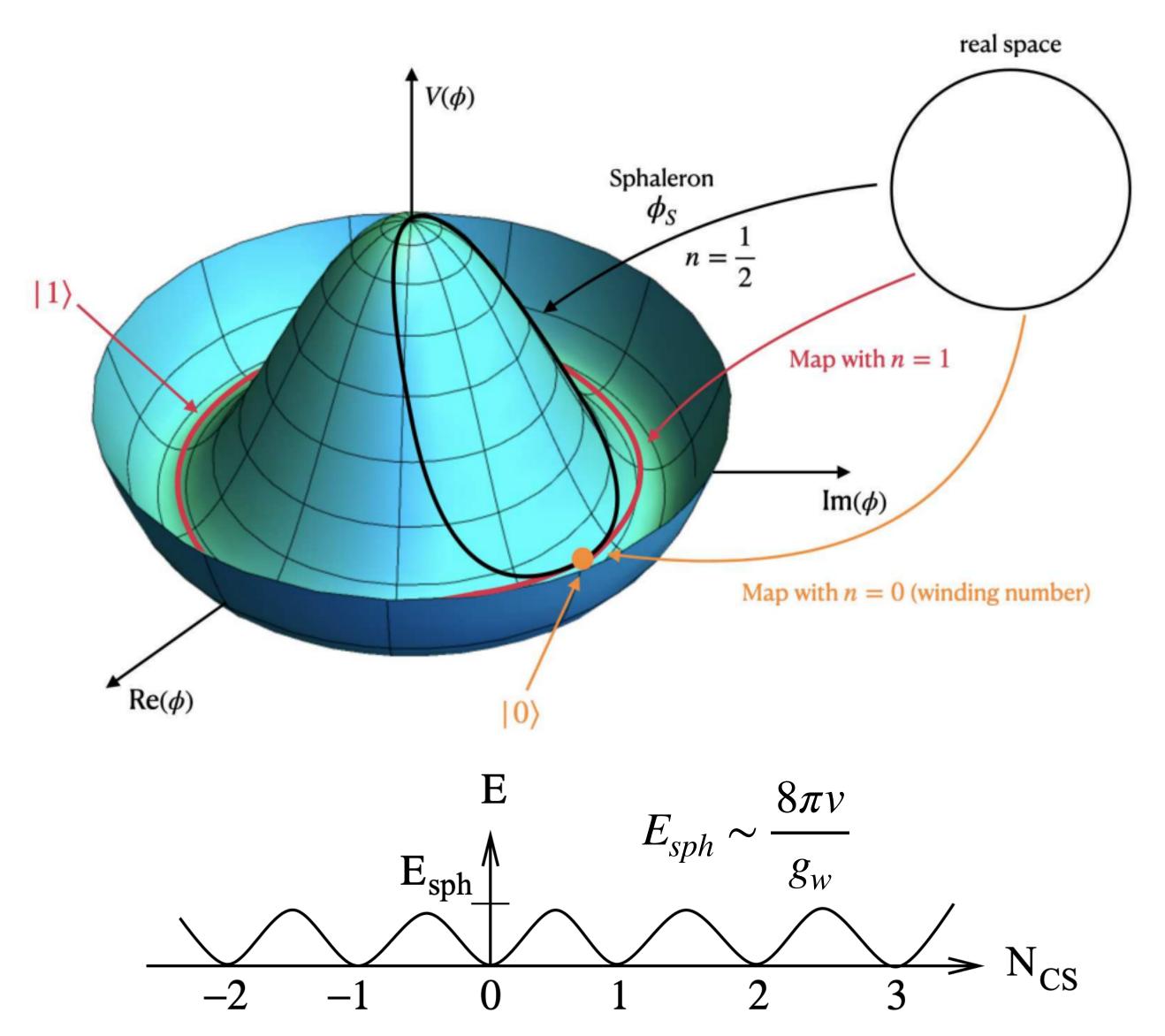


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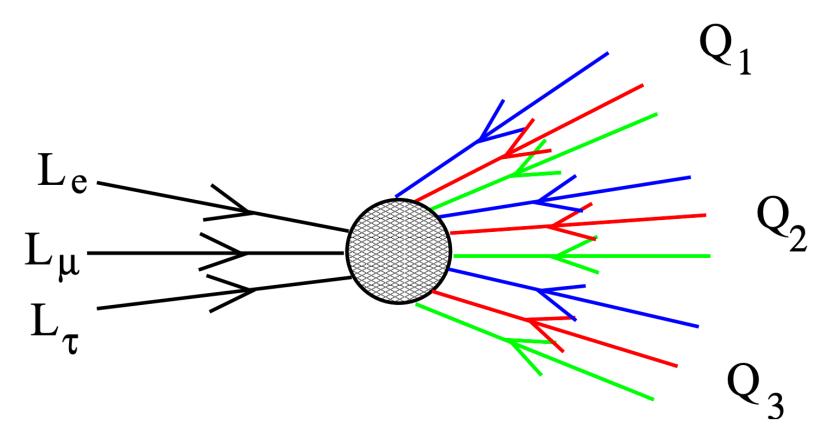
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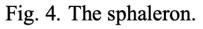
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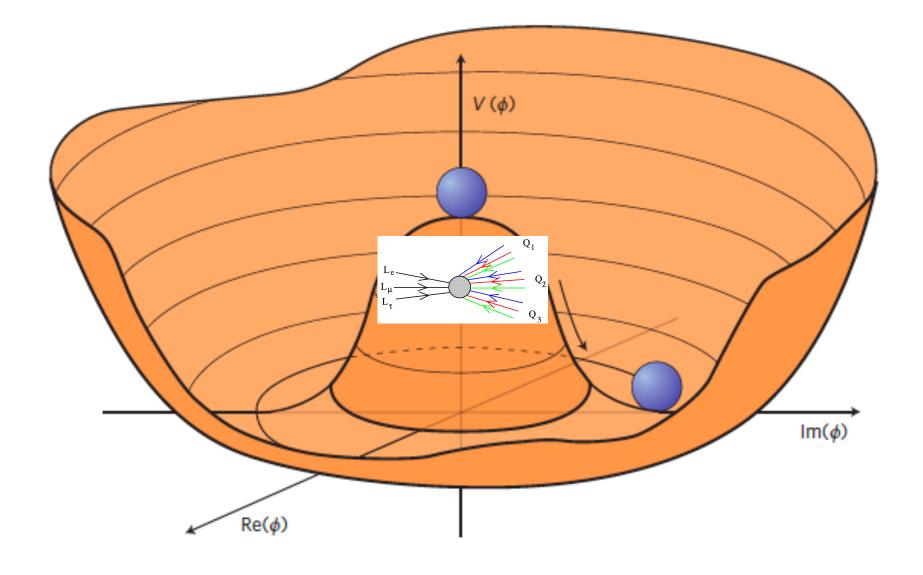
(2.2)







MultiHiggs production and EWSB



If EW symmetry is restored (VEV=0) Sphalerons everywhere!

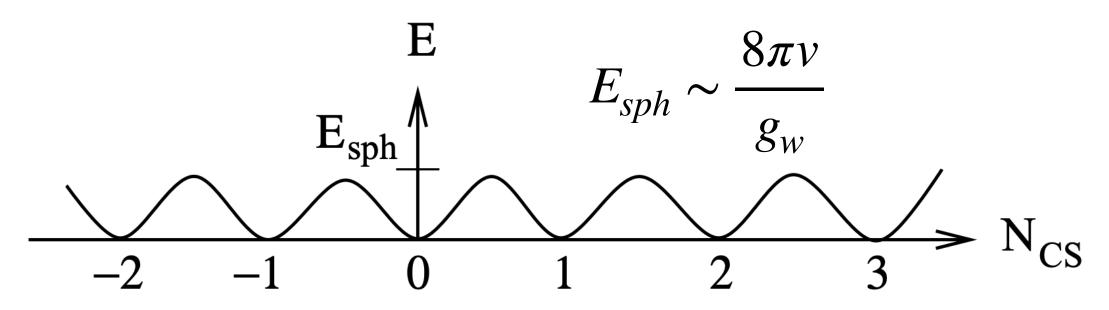


Fig. 8. Energy of gauge field configurations as a function of Chern-Simons number.

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v is the Higgs VEV

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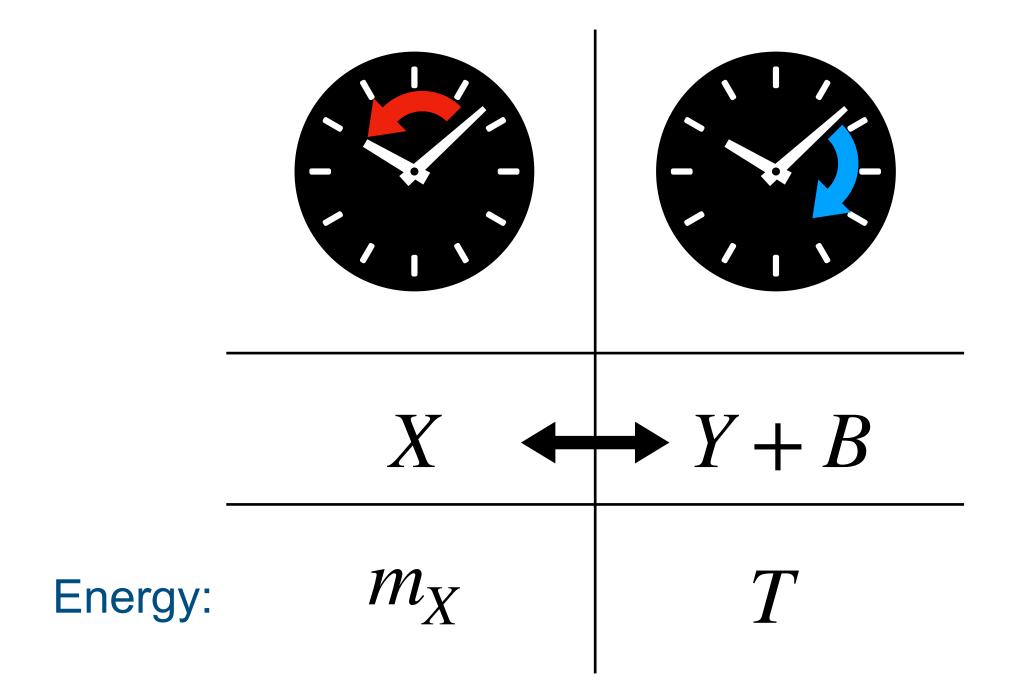
Out of thermal equilibrium

In thermal equilibrium: any process that generates some extra B $X \rightarrow Y + B$ comes with the inverse process at the same rate $Y + B \rightarrow X$

Out of thermal equilibrium if for example $T < m_X$ $Y + B \rightarrow X$ surpassed by $e^{-m_X/T}$



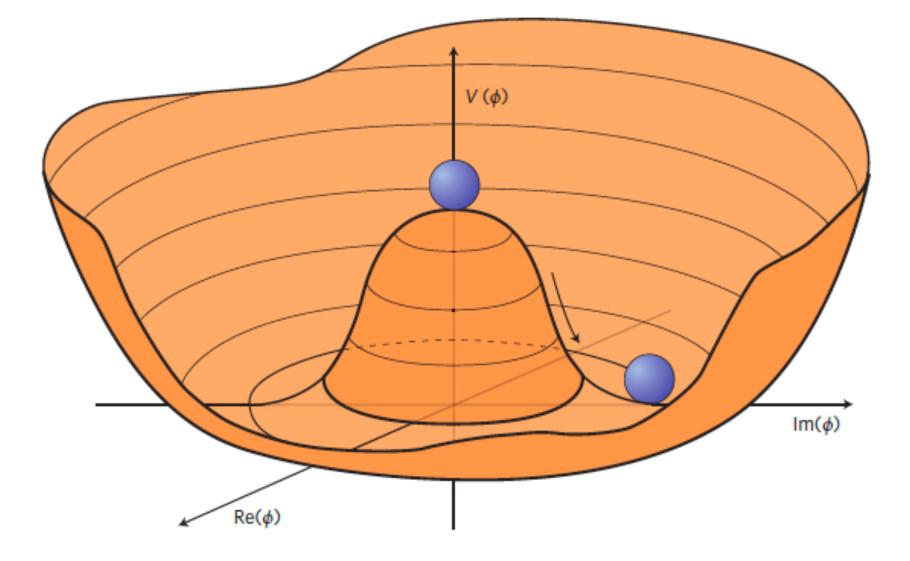
MultiHiggs production and EWSB



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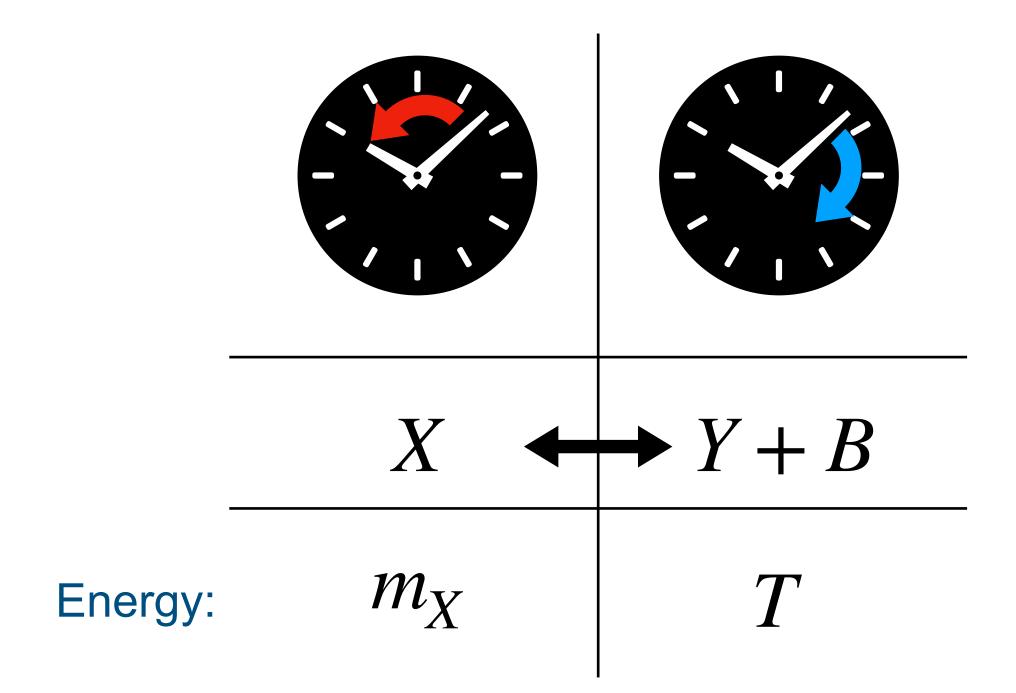
Out of thermal equilibrium

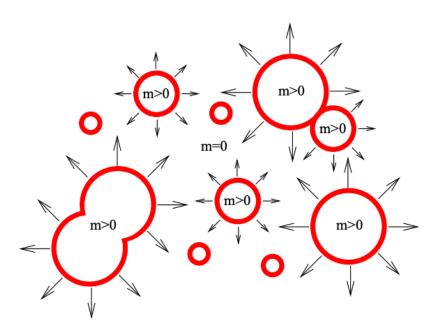


Electroweak symmetry breaking (EWSB) is a phase transition! It can cause loss of thermal equilibrium if it is a First Order Phase Transition (FOPT)



MultiHiggs production and EWSB





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Charge and Charge+Parity symmetries (C and CP violation)

Under C conservation: $X \to Y + B$ comes with $\bar{X} \to \bar{Y} + \bar{B}$

 $\Gamma(\bar{X} \to \bar{Y} + \bar{B}) = \Gamma$

The net rate of baryon production goes like the difference of these rates,

$$\frac{dB}{dt} \propto \Gamma(\bar{X} \to \bar{Y} + t)$$

CP violation is a longer story but also needed



MultiHiggs production and EWSB

 $\begin{array}{cc} C: & q_L \to \bar{q}_L \\ CP: & q_L \to \bar{q}_R \end{array}$

$$(X \to Y + B)$$

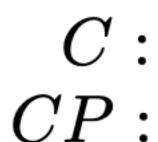
 \bar{B}) – $\Gamma(X \to Y + B)$

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Charge and Charge+Parity symmetries (C and CP violation)



In SM: CP violation in CKM matrix. Not enough though! BSM CP violation is more than welcomed.

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} c_1 & | -s_1c_3 & | -s_1s_3 \\ \hline s_1c_2 & | & c_1c_2c_3 & | & c_1c_2s_3 \\ \hline s_1s_2 & | & -s_2s_3e^{i\delta} & | & +s_2c_3e^{i\delta} \\ \hline s_1s_2 & | & c_1s_2c_3 & | & c_2s_2s_3 \\ \hline s_1s_2 & | & -c_2c_3e^{i\delta} & | & -c_2c_3e^{i\delta} \end{pmatrix}$$



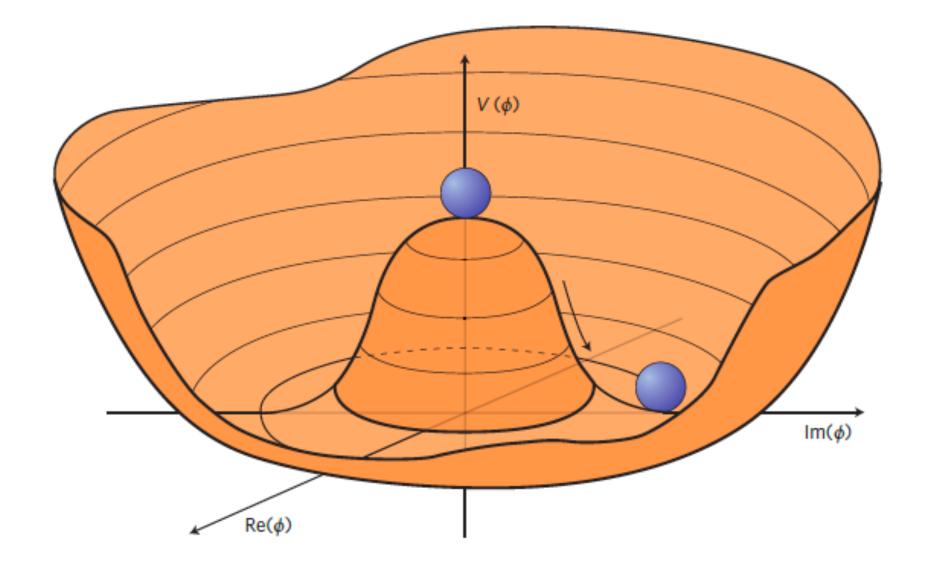
MultiHiggs production and EWSB

$$\begin{array}{l} q_L \to \bar{q}_L \\ q_L \to \bar{q}_R \end{array}$$

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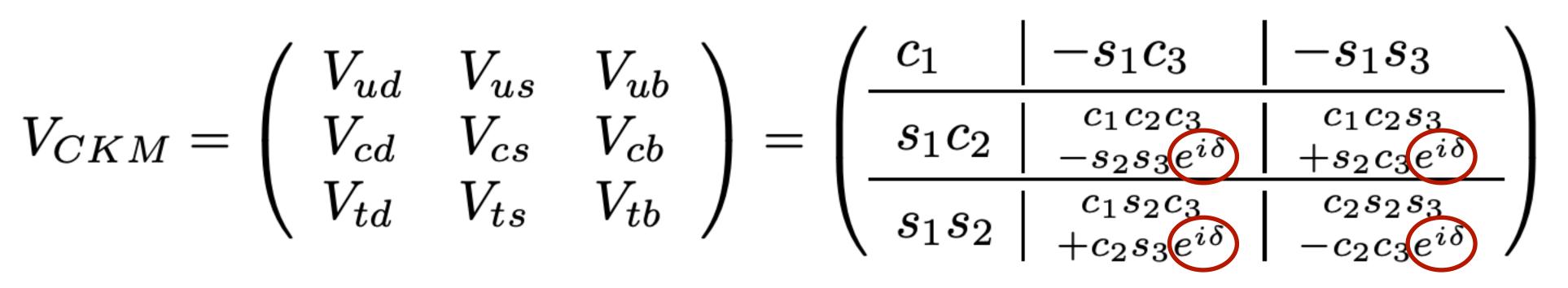


Charge and Charge+Parity symmetries (C and CP violation)



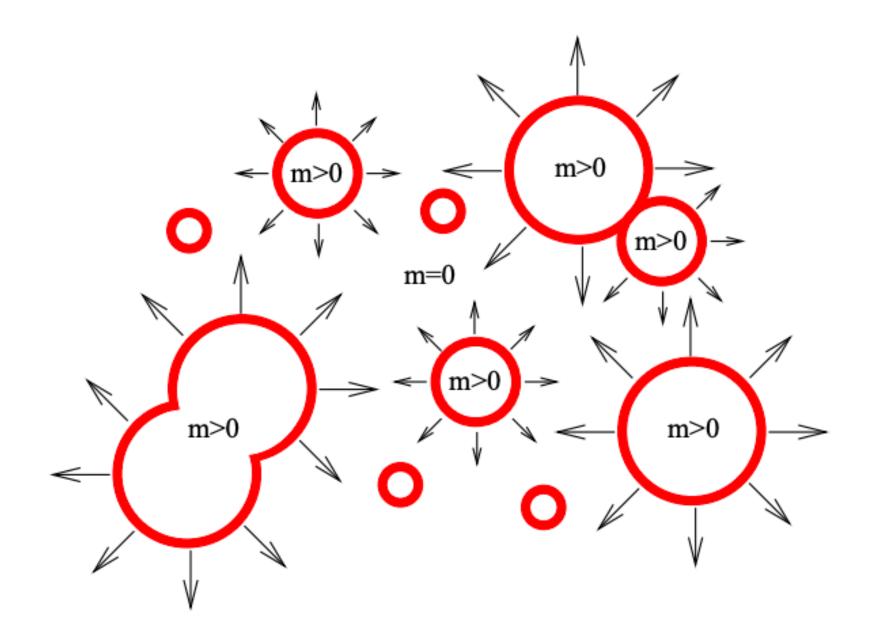


MultiHiggs production and EWSB



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First Order Phase Transition (FOPT)



MultiHiggs production and EWSB

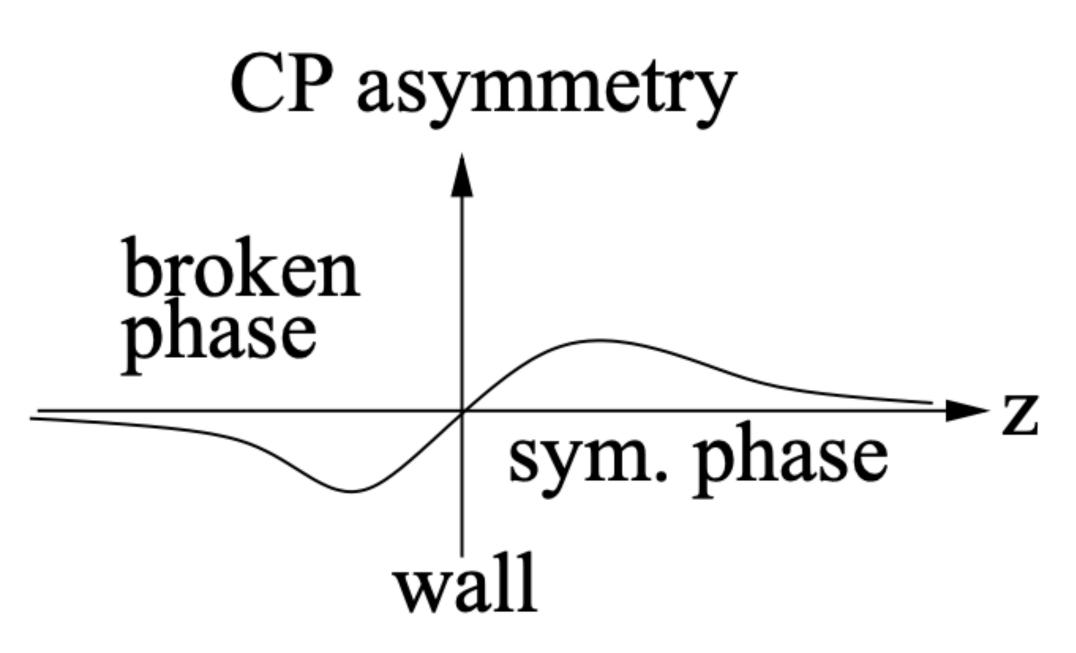
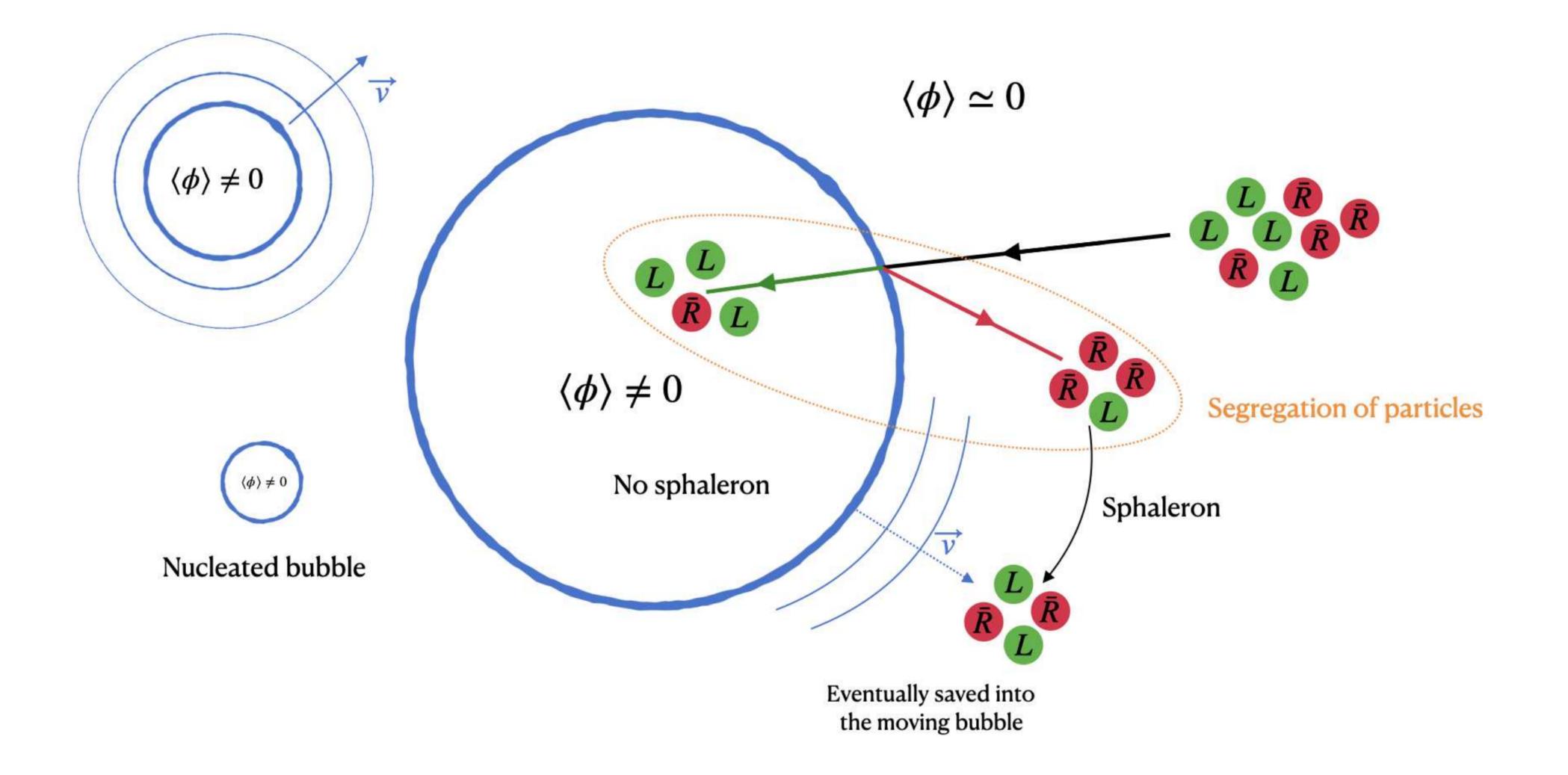


Fig. 13. The CP asymmetry which develops near the bubble wall.

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MultiHiggs production and EWSB

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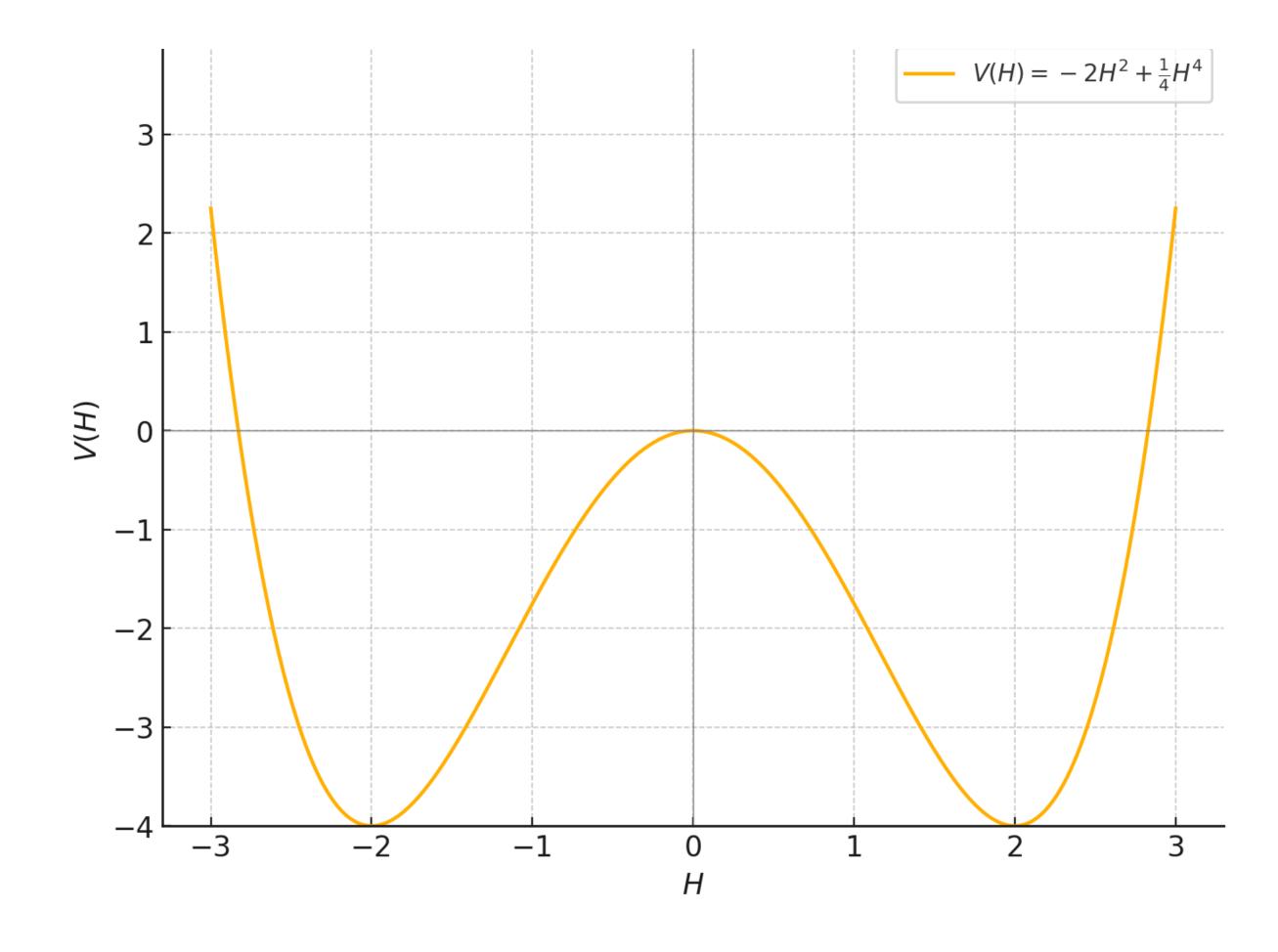


Before symmetry breaking, Higgs potential is:

$$V(H) = -\frac{1}{2}\mu^2 H^2 + \frac{1}{4}\lambda H^4$$



MultiHiggs production and EWSB



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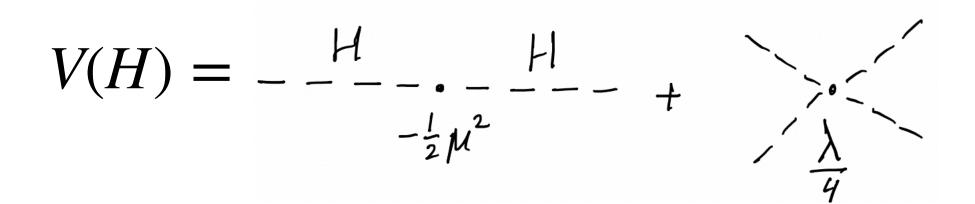




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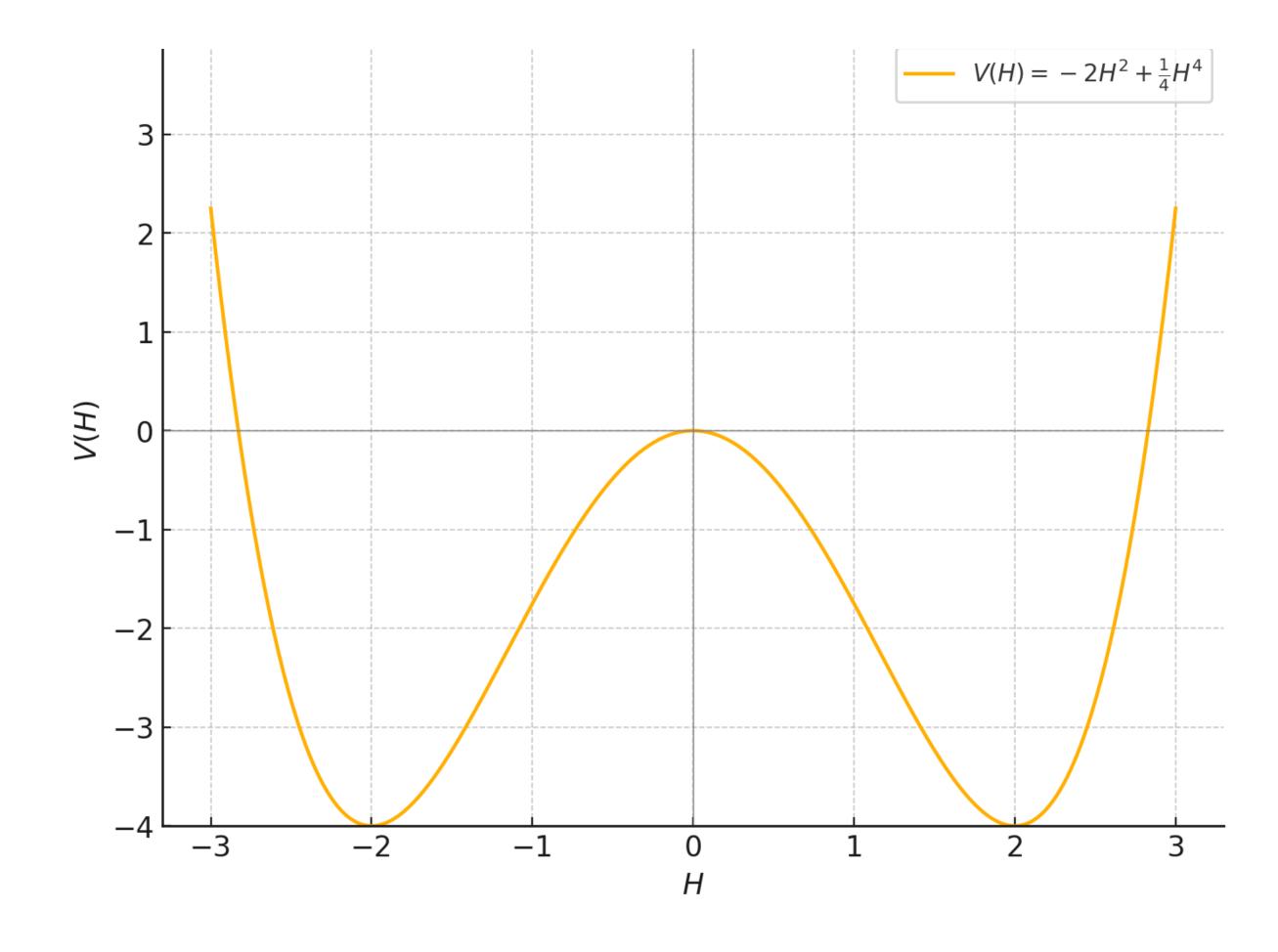
$$V(H) = -\frac{1}{2}\mu^2 H^2 + \frac{1}{4}\lambda H^4$$

In Feynman diagrams:





MultiHiggs production and EWSB



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Before symmetry breaking, Higgs potential is:

$$V(H) = -\frac{1}{2}\mu^2 H^2 + \frac{1}{4}\lambda H^4$$

In Feynman diagrams:

$$V(H) = - \frac{H}{-\frac{1}{2}\mu^2} + \frac{H}{\frac{1}{2}\mu^2} + \frac{1}{\frac{1}{4}\mu^2}$$

Higgs field is coupled to a thermal bath of fields. at LO, this looks like:

$$-\frac{H}{\sim T^2} - O_2 - \frac{H}{\sim T^2} - O_2$$

$$V_{eff}(H,T) = -\frac{1}{2}\mu^2 H^2 + \frac{1}{4}\lambda H^4 + \frac{\alpha}{2}T^2 H^2$$



MultiHiggs production and EWSB

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Before symmetry breaking, Higgs potential is:

$$V(H) = -\frac{1}{2}\mu^2 H^2 + \frac{1}{4}\lambda H^4$$

In Feynman diagrams:

$$V(H) = -\frac{H}{-\frac{1}{2}\mu^2} + \frac{H}{-\frac{1}{2}\mu^2} + \frac{\lambda}{\frac{\lambda}{4}}$$

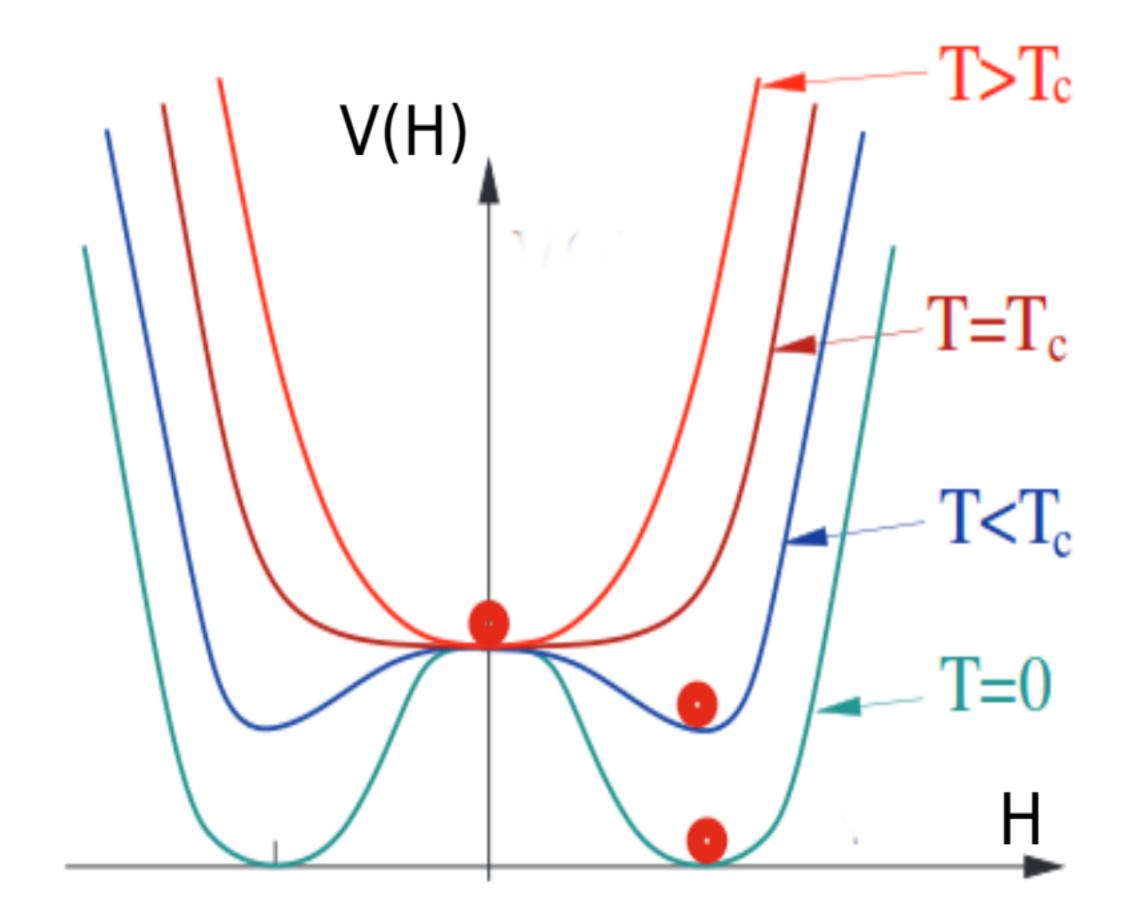
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MultiHiggs production and EWSB



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Electroweak Phase Transition

at NLO, the effective potential gets a cubic term $V_{eff}(H,T) = \frac{1}{2}(-\mu^2 + \alpha T^2)H^2 - \beta T(-\mu^2 + \gamma H^2)^{3/2} + \frac{1}{4}\lambda H^4$

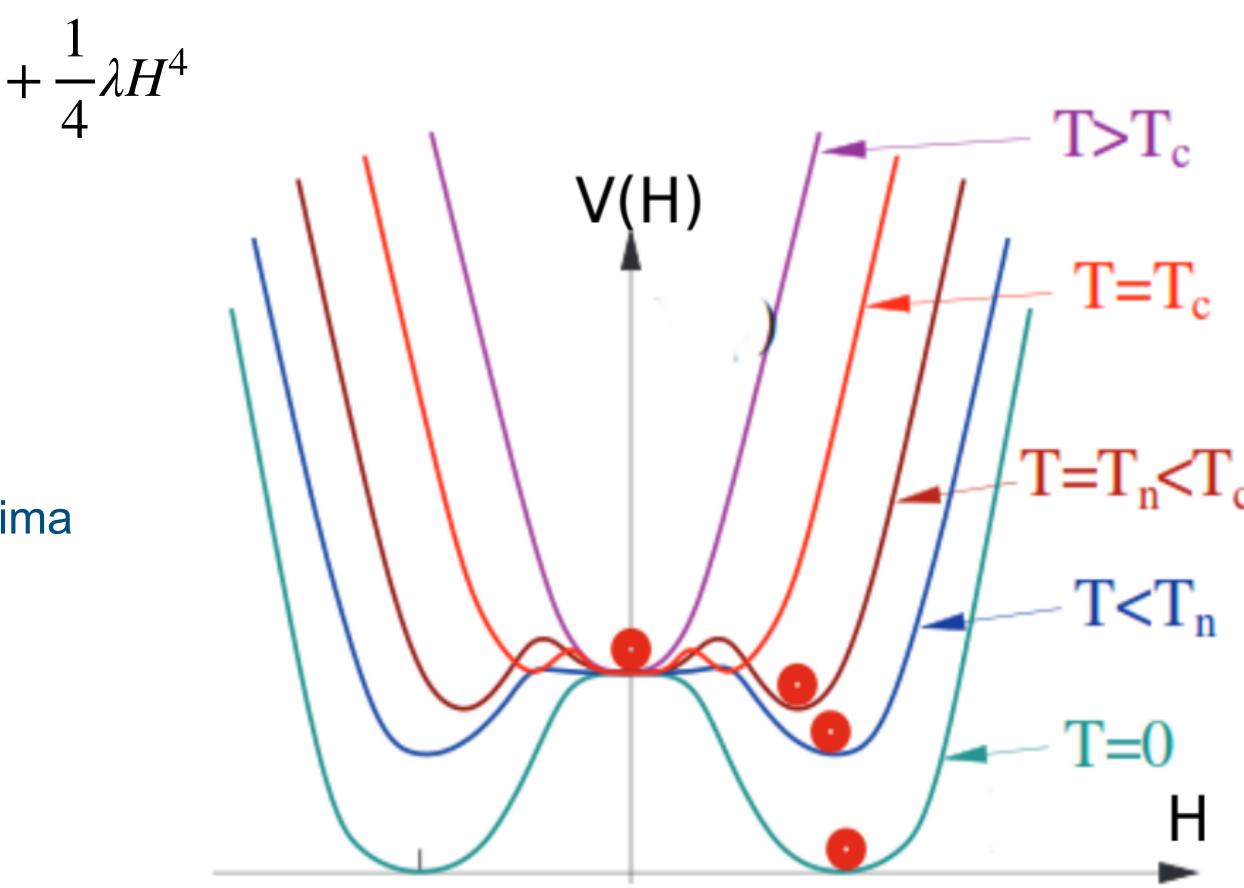
The values of (α, β, γ) depend on your theory

If you're lucky, you can get a barrier between two minima at some critical temperature T_c

Then at some random point in space, the VEV tunnels a bubble forms around it and expands!



MultiHiggs production and EWSB



 T_n = temperature of bubble nucleation

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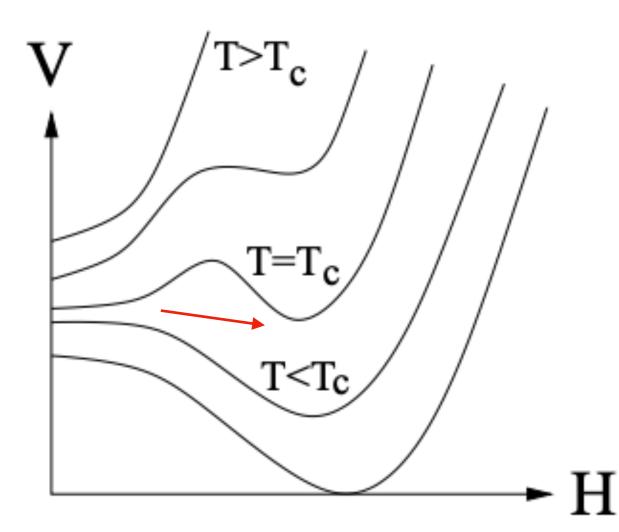




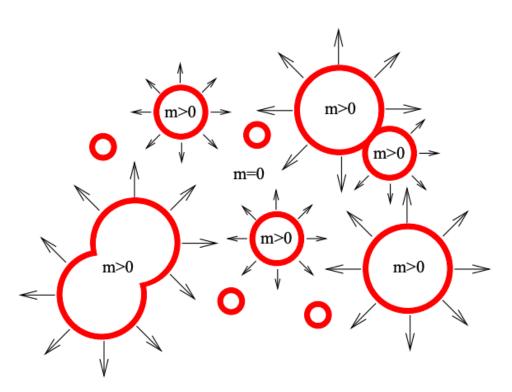


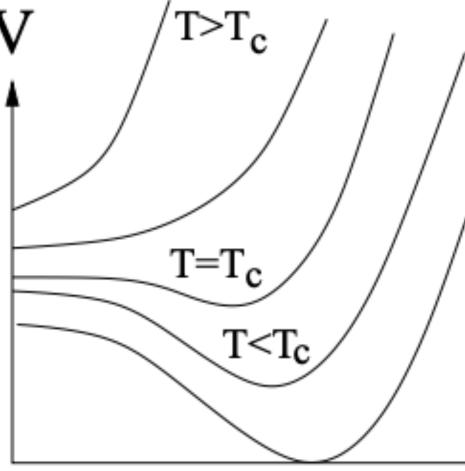


Electroweak Phase Transition



first order phase transition FOPT





second order phase transition SOPT (or crossover)



MultiHiggs production and EWSB

 $V_{eff}(H,T) = \bigcirc + \{\bigcirc + \bigoplus \} + \dots$ $\sim \frac{1}{2}(-m^2 + \alpha T^2)H^2 - \beta TH^3 + \frac{1}{4}\lambda H^4$

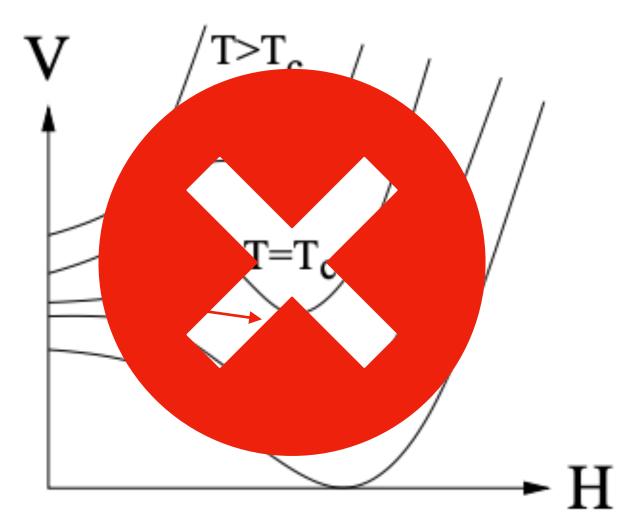
WE WANT TO BE FIRST!!!

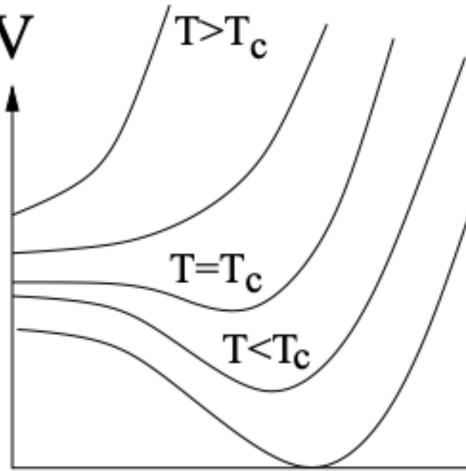


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Electroweak Phase Transition: SM





second order phase transition SOPT (or crossover)

No first order phase transition in SM

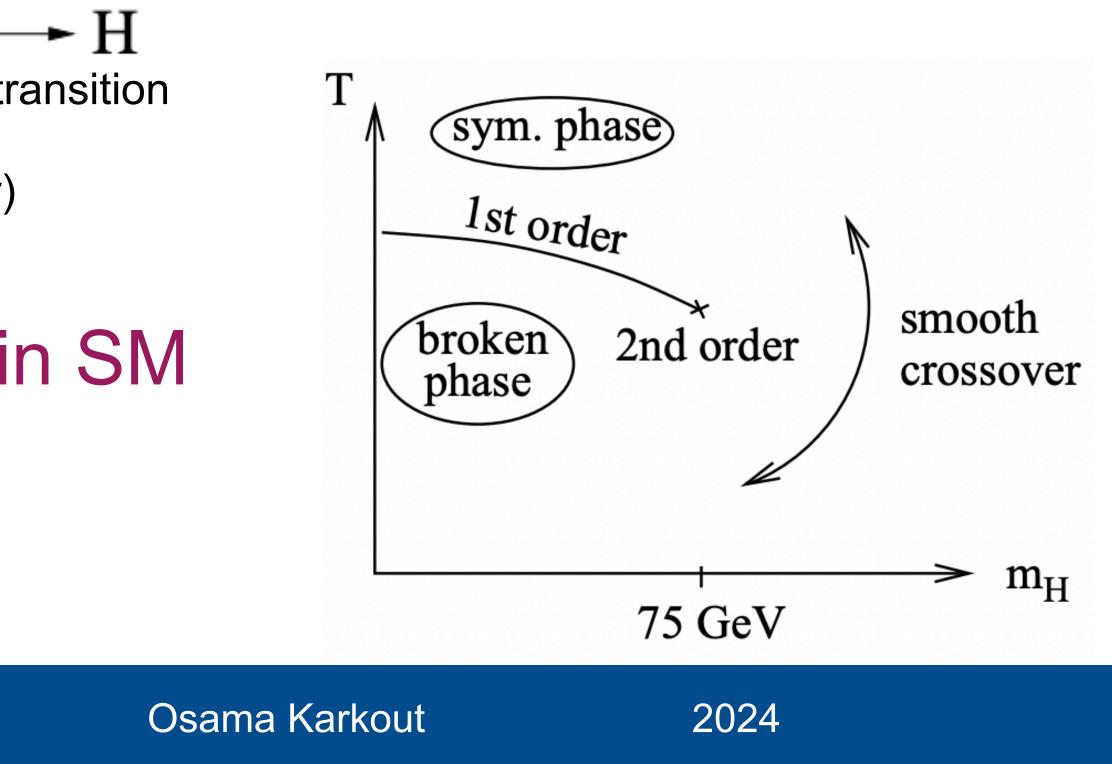


MultiHiggs production and EWSB

 $V_{eff}(H,T) = \bigcirc + \{\bigcirc + \bigoplus \} + \dots$ $\sim \frac{1}{2}(-m^2 + \alpha T^2)H^2 - \beta TH^3 + \frac{1}{4}\lambda H^4$

WE WANT TO BE FIRST!!!

But we're not...

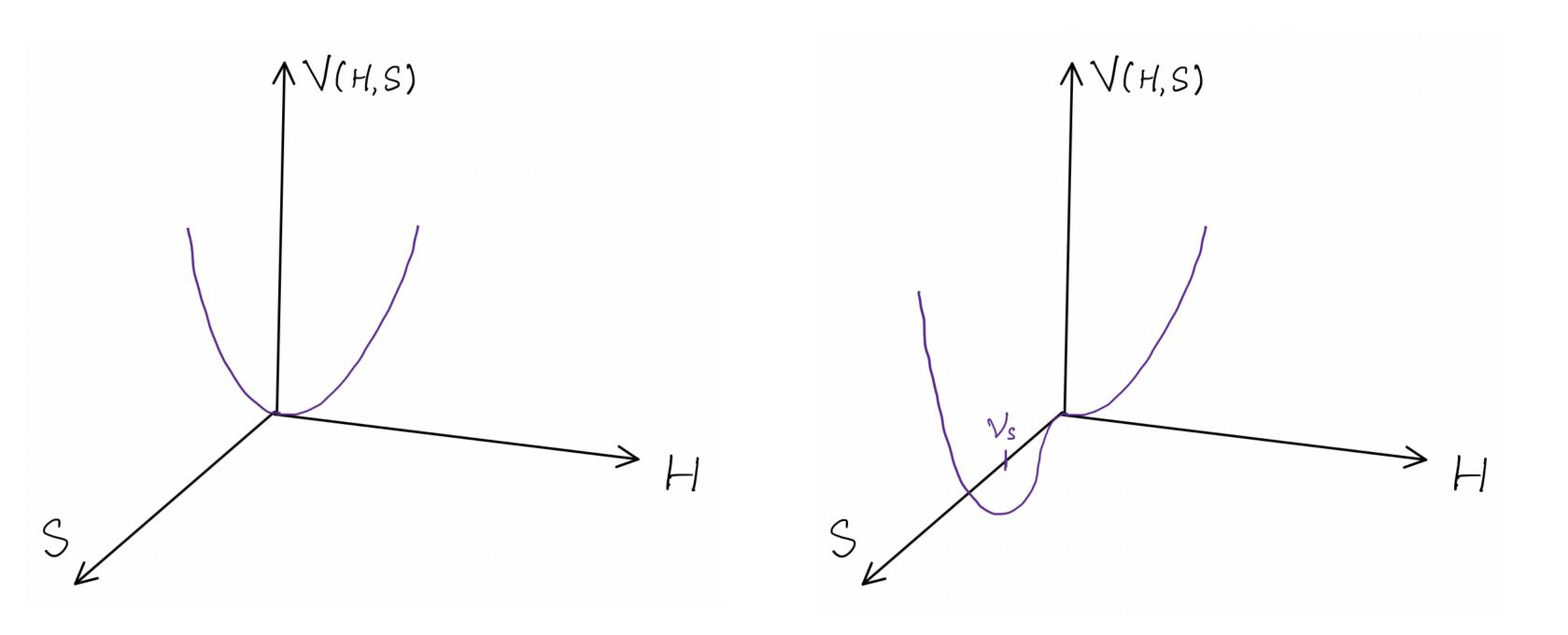




Electroweak Phase Transition: BSM

Idea:

- 1. add a scalar field S which couples to the Higgs.
- 2. This scalar field also has a phase transition! Going to a VEV for S





MultiHiggs production and EWSB

 $V(H) = -\frac{1}{2}\mu^2 H^2 + \frac{1}{4}\lambda H^4 + V(H,S)$

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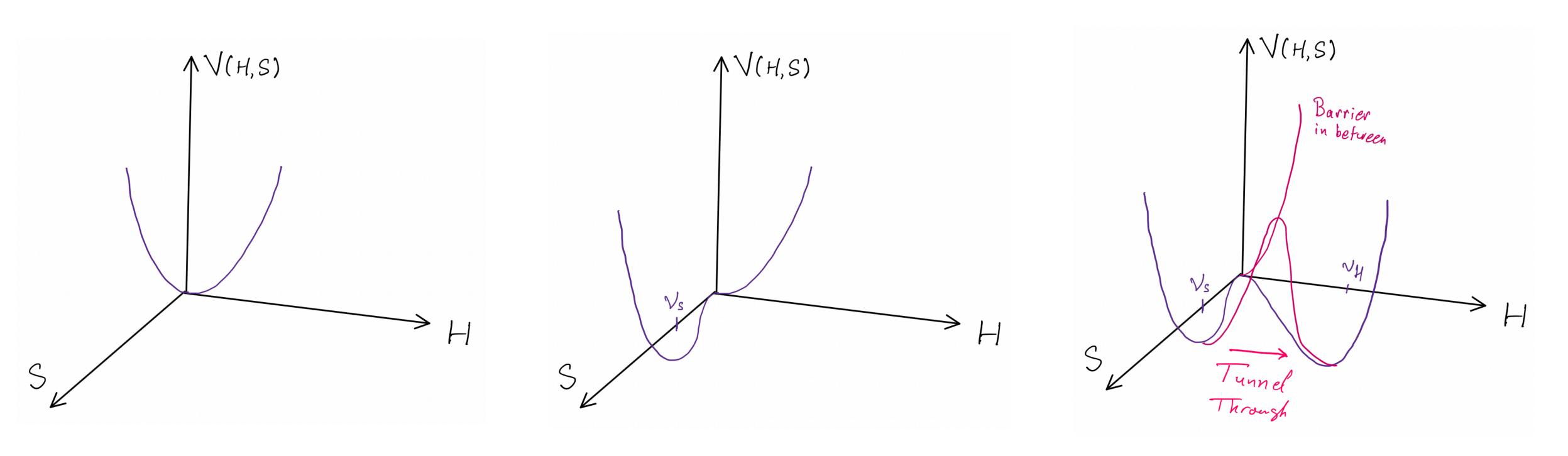




Electroweak Phase Transition: BSM

Idea:

- 1. add a scalar field S which couples to the Higgs.
- 2. This scalar field also has a phase transition! Going to a VEV for S
- 3. Form a potential barrier between the VEV of S and the VEV of H
- 4. Tunnel to the VEV of H: This is FOPT





MultiHiggs production and EWSB

 $V(H) = -\frac{1}{2}\mu^2 H^2 + \frac{1}{4}\lambda H^4 + V(H,S)$

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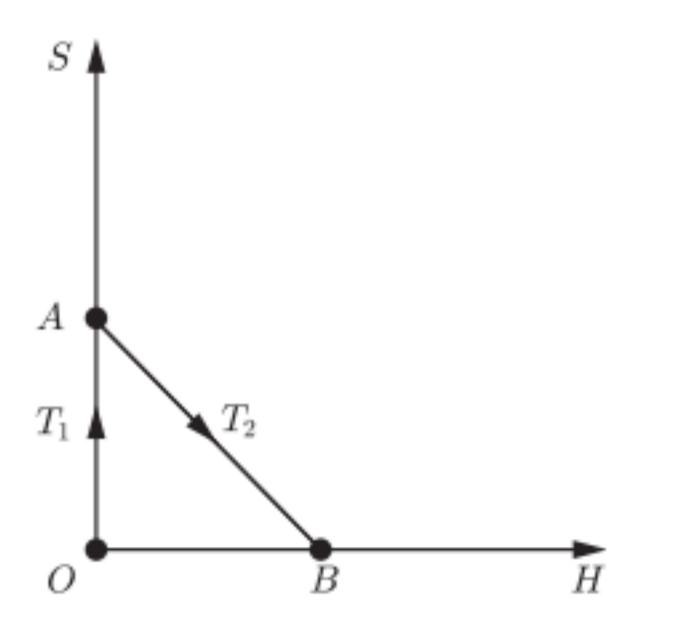


Electroweak Phase Transition: BSM

Adding a scalar field can make a two-step FOPT!

$$V = -\frac{1}{2}\mu_h^2 h^2 + \frac{1}{4}\lambda_h h^4 + \frac{1}{2}\mu_s^2 s^2 + \frac{1}{4}\lambda_s s^4 + \frac{1}{4}\mu_m sh^2 + \frac{1}{4}\lambda_m s^2 h^2 + \mu_1^3 s + \frac{1}{4}\lambda_m s^2 h^2 + \frac{1}{4}$$

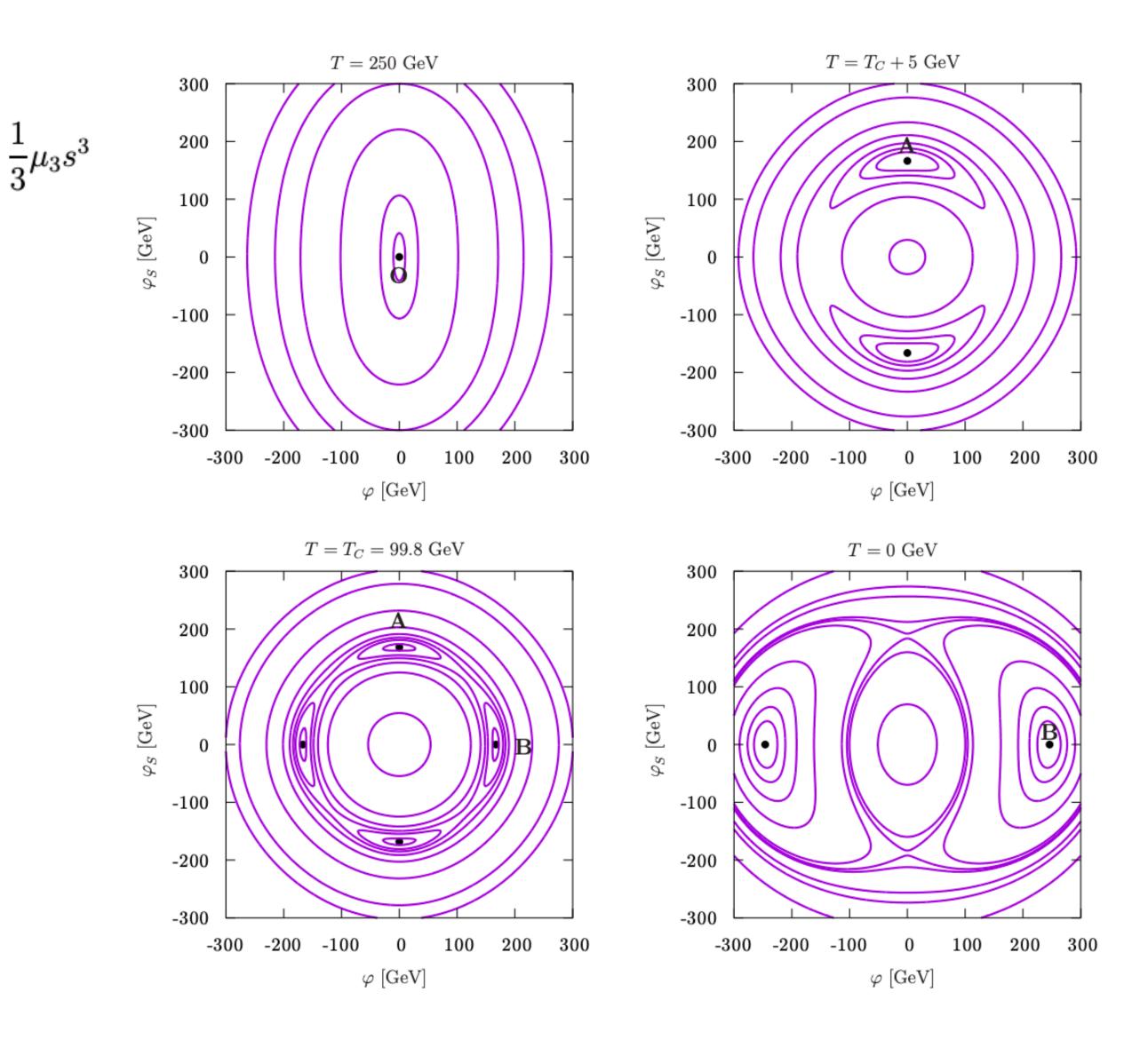
 $V^{\text{high-}T}(\varphi,\varphi_S;T) = V_0(\varphi,\varphi_S) + \frac{1}{2}(\Sigma_H \varphi^2 + \frac{1}{2}\Sigma_S \varphi_S^2)T^2$



Cheng-Wei Chiang,^{1,2,3,4,*} Michael J. Ramsey-Musolf,^{5,6,†} and Eibun Senaha^{1,7,‡}



MultiHiggs production and EWSB



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ATLAS Observed limit (95% CL) Expected limit (95% CL) $\sqrt{s} = 13 \text{ TeV}, 126 - 139 \text{ fb}^{-1}$ $(\mu_{HH} = 0 \text{ hypothesis})$ $\sigma_{ggF+VBF}^{SM}(HH) = 32.7^{+2.1}_{-7.2}$ fb Expected limit $\pm 1\sigma$ Expected limit ±20 Theory prediction Obs. Exp. 130 180 bbγγ $b\bar{b}\tau^+\tau^-$ 140 110 bbbb 160 240 73 85 Combined-20 50 200 500 1000 2000 100 $\sigma_{ggF+VBF}(HH)$ [fb] HS > H

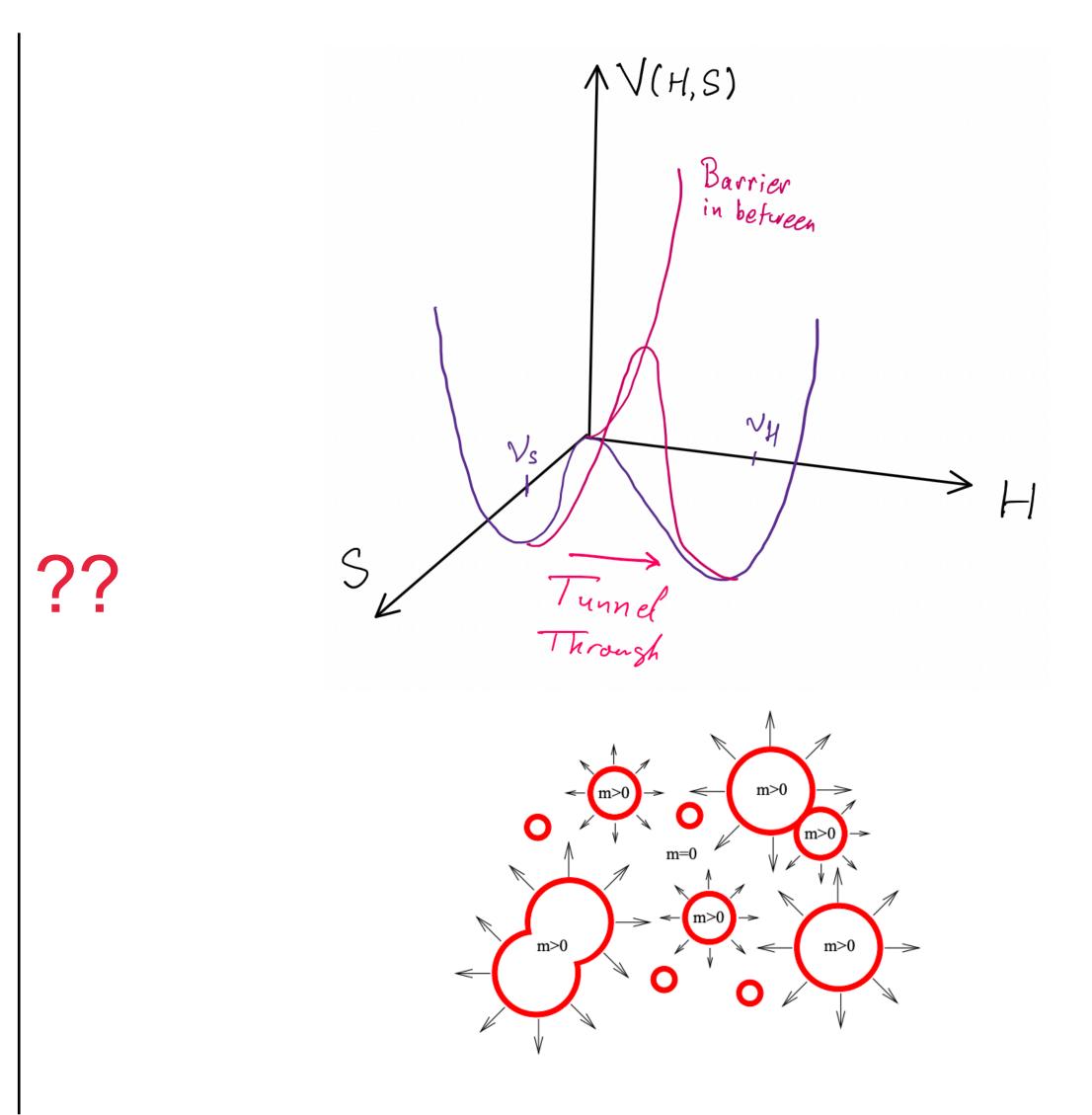
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Nik

explored for one added scalar, answer will come

MultiHiggs production and EWSB

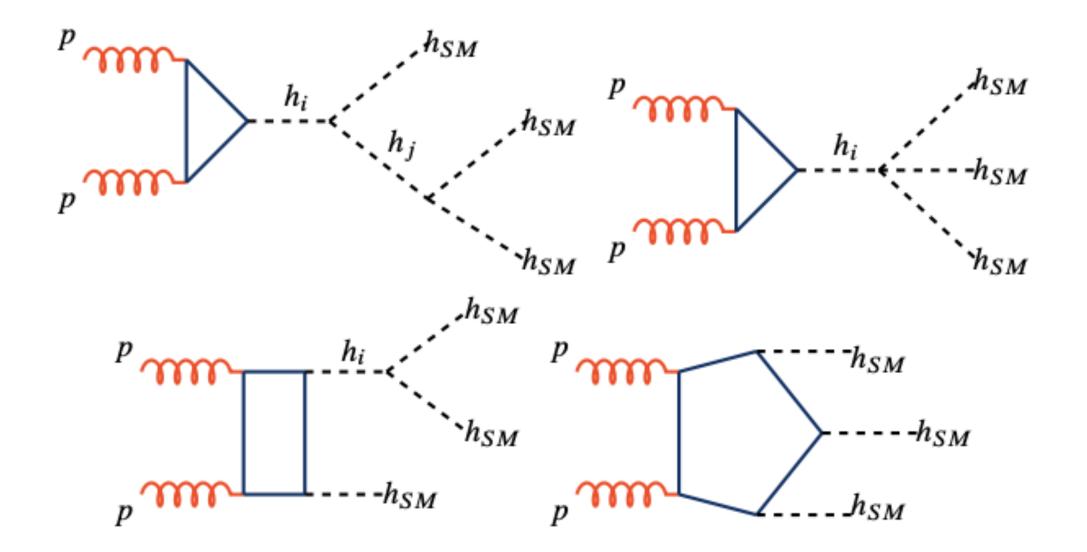
ATLAS Higgs results \rightarrow Higgs phase transition



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Maybe we will see enhancement of HHH production!

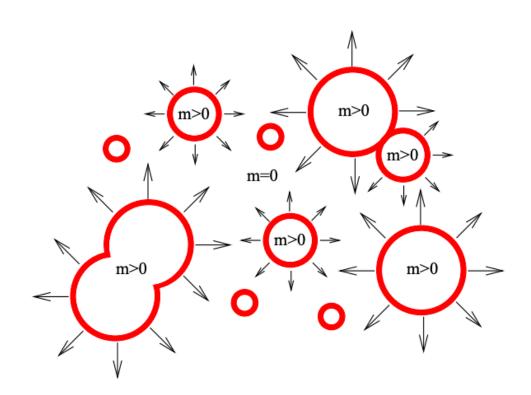




MultiHiggs production and EWSB

ATLAS Higgs results \rightarrow Higgs phase transition





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Simplified BSM model predicting large HHH: **TRSM**.

SM + two singlets coupling to the Higgs.

$$V = \mu_{\Phi}^2 \Phi^{\dagger} \Phi + \lambda_{\Phi} (\Phi^{\dagger} \Phi)^2 + \mu_S^2 S^2 + \lambda_S S^4 + \mu_X^2 X^2 + \lambda_X X^4 + \lambda_{\Phi S} \Phi^{\dagger} \Phi S^2 + \lambda_{\Phi X} \Phi^{\dagger} \Phi X^2 + \lambda_{SX} S^2 X^2 .$$



MultiHiggs production and EWSB

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Scalars get VEVs! \rightarrow Mixing:

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$$\Phi = \begin{pmatrix} 0\\ \frac{\phi_h + v}{\sqrt{2}} \end{pmatrix}, \quad S = \frac{\phi_S + v_S}{\sqrt{2}}, \quad X = \frac{\phi_X + v_X}{\sqrt{2}}$$
$$\begin{pmatrix} h_1\\ h_2\\ h_3 \end{pmatrix} = R \begin{pmatrix} \phi_h\\ \phi_S\\ \phi_X \end{pmatrix}$$

h1 can be our scalar particle of 125 GeV Tania Robens,^{1,*} Tim Stefaniak,^{2,†} and Jonas Wittbrodt^{2,‡}

MultiHiggs production and EWSB

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Simplified BSM model predicting large HHH: **TRSM**.

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$$V = \mu_{\Phi}^2 \Phi^{\dagger} \Phi + \lambda_{\Phi} (\Phi^{\dagger} \Phi)^2 + \mu_S^2 S^2 + \lambda_S S^4 + \mu_X^2 X^2 + \lambda_X X^4 + \lambda_{\Phi S} \Phi^{\dagger} \Phi S^2 + \lambda_{\Phi X} \Phi^{\dagger} \Phi X^2 + \lambda_{SX} S^2 X^2 .$$

Scalars get VEVs! \rightarrow Mixing:

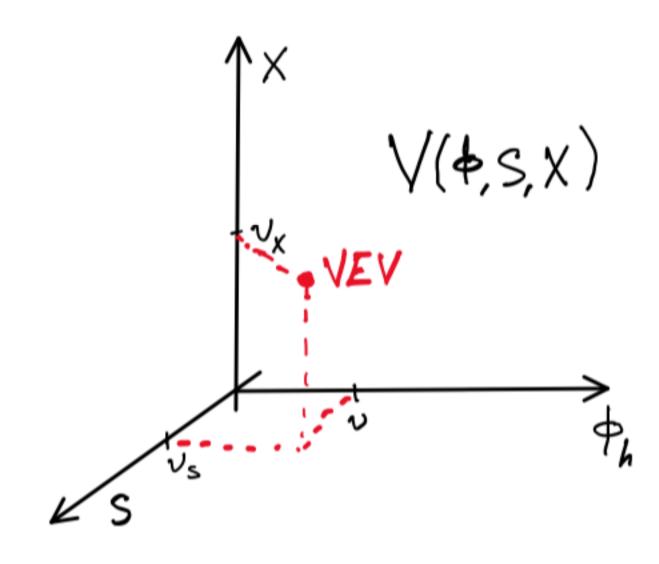
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Nik

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MultiHiggs production and EWSB



Remember: Mixing requires nonzero VEV For added scalars

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Simplified BSM model predicting large HHH: **TRSM**.

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$$V = \mu_{\Phi}^2 \Phi^{\dagger} \Phi + \lambda_{\Phi} (\Phi^{\dagger} \Phi)^2 + \mu_S^2 S^2 + \lambda_S S^4 + \mu_X^2 X^2 + \lambda_X X^4 + \lambda_{\Phi S} \Phi^{\dagger} \Phi S^2 + \lambda_{\Phi X} \Phi^{\dagger} \Phi X^2 + \lambda_{SX} S^2 X^2 .$$

Scalars get VEVs! \rightarrow Mixing:

hef

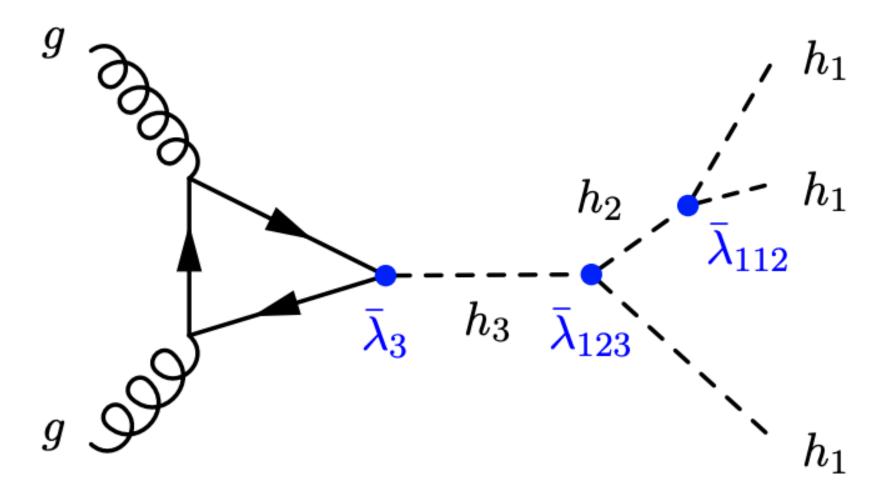
Nik

$$\Phi = \begin{pmatrix} 0\\ \frac{\phi_h + v}{\sqrt{2}} \end{pmatrix}, \quad S = \frac{\phi_S + v_S}{\sqrt{2}}, \quad X = \frac{\phi_X + v_X}{\sqrt{2}}$$
$$\begin{pmatrix} h_1\\ h_2\\ h_3 \end{pmatrix} = R \begin{pmatrix} \phi_h\\ \phi_S\\ \phi_X \end{pmatrix}$$

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MultiHiggs production and EWSB

HHH production is enhanced through **resonance** xsec ~ 30 fb (~ HH production in SM)



We updated this conclusion using better theoretical bounds (perturbativity) and newest experimental bounds!

Osama Karkout,¹ Andreas Papaefstathiou,² Marieke Postma,^{1,3} Gilberto Tetlalmatzi-Xolocotzi,^{4,5} Jorinde van de Vis,⁶ Tristan du Pree¹ https://arxiv.org/pdf/2404.12425





Simplified BSM model predicting large HHH: **TRSM**.

SM + two singlets coupling to the Higgs.

$$V = \mu_{\Phi}^2 \Phi^{\dagger} \Phi + \lambda_{\Phi} (\Phi^{\dagger} \Phi)^2 + \mu_S^2 S^2 + \lambda_S S^4 + \mu_X^2 X^2 + \lambda_X X^4 + \lambda_{\Phi S} \Phi^{\dagger} \Phi S^2 + \lambda_{\Phi X} \Phi^{\dagger} \Phi X^2 + \lambda_{SX} S^2 X^2 .$$

Scalars get VEVs! \rightarrow Mixing:

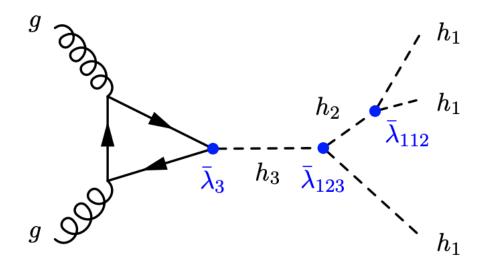
hef

Nik

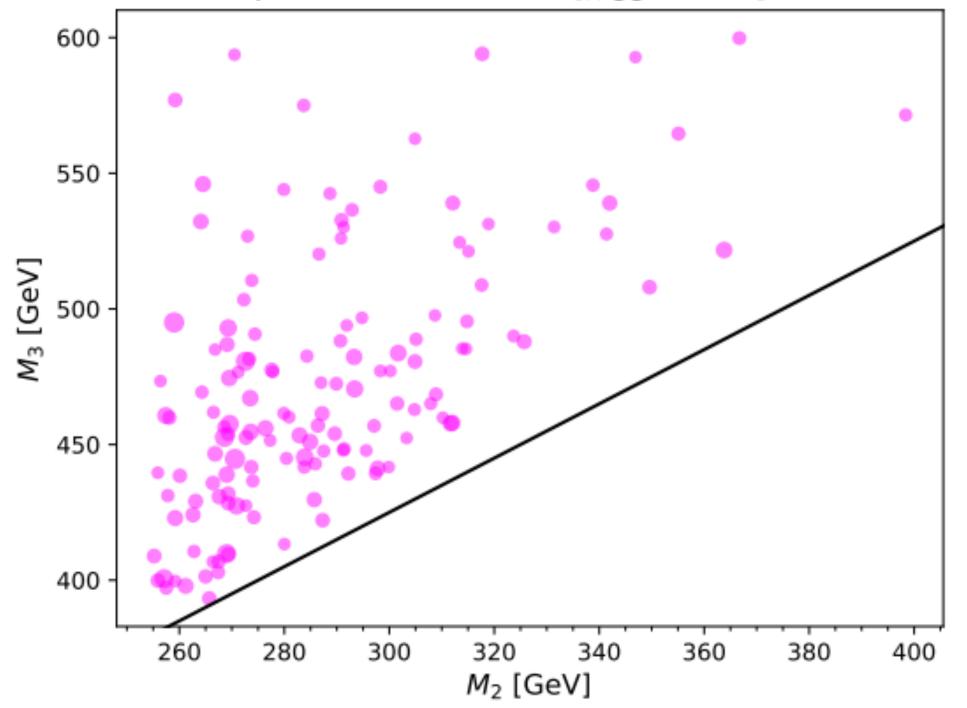
$$\Phi = \begin{pmatrix} 0\\ \frac{\phi_h + v}{\sqrt{2}} \end{pmatrix}, \quad S = \frac{\phi_S + v_S}{\sqrt{2}}, \quad X = \frac{\phi_X + v_X}{\sqrt{2}}$$
$$\begin{pmatrix} h_1\\ h_2\\ h_3 \end{pmatrix} = R \begin{pmatrix} \phi_h\\ \phi_S\\ \phi_X \end{pmatrix}$$

h1 can be our scalar particle of 125 GeV Tania Robens,^{1,*} Tim Stefaniak,^{2,†} and Jonas Wittbrodt^{2,‡}

MultiHiggs production and EWSB



Viable points with $\sigma > 100 \times \sigma_{SM}(gg \rightarrow hhh)@13.6 \text{ TeV}$



Osama Karkout,¹ **Andreas Papaefstathiou**,² **Marieke Postma**,^{1,3} **Gilberto Tetlalmatzi-Xolocotzi**,^{4,5} **Jorinde van de Vis**,⁶ **Tristan du Pree**¹ https://arxiv.org/pdf/2404.12425

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Electroweak Phase Transition: TRSM

$$V = \mu_{\Phi}^2 \Phi^{\dagger} \Phi + \lambda_{\Phi} (\Phi^{\dagger} \Phi)^2 + \mu_S^2 S^2 + \lambda_S S^4 + \mu_X^2 X^2 + \lambda_X + \lambda_{\Phi S} \Phi^{\dagger} \Phi S^2 + \lambda_{\Phi X} \Phi^{\dagger} \Phi X^2 + \lambda_{SX} S^2 X^2 .$$

Mixing:

Nik hef

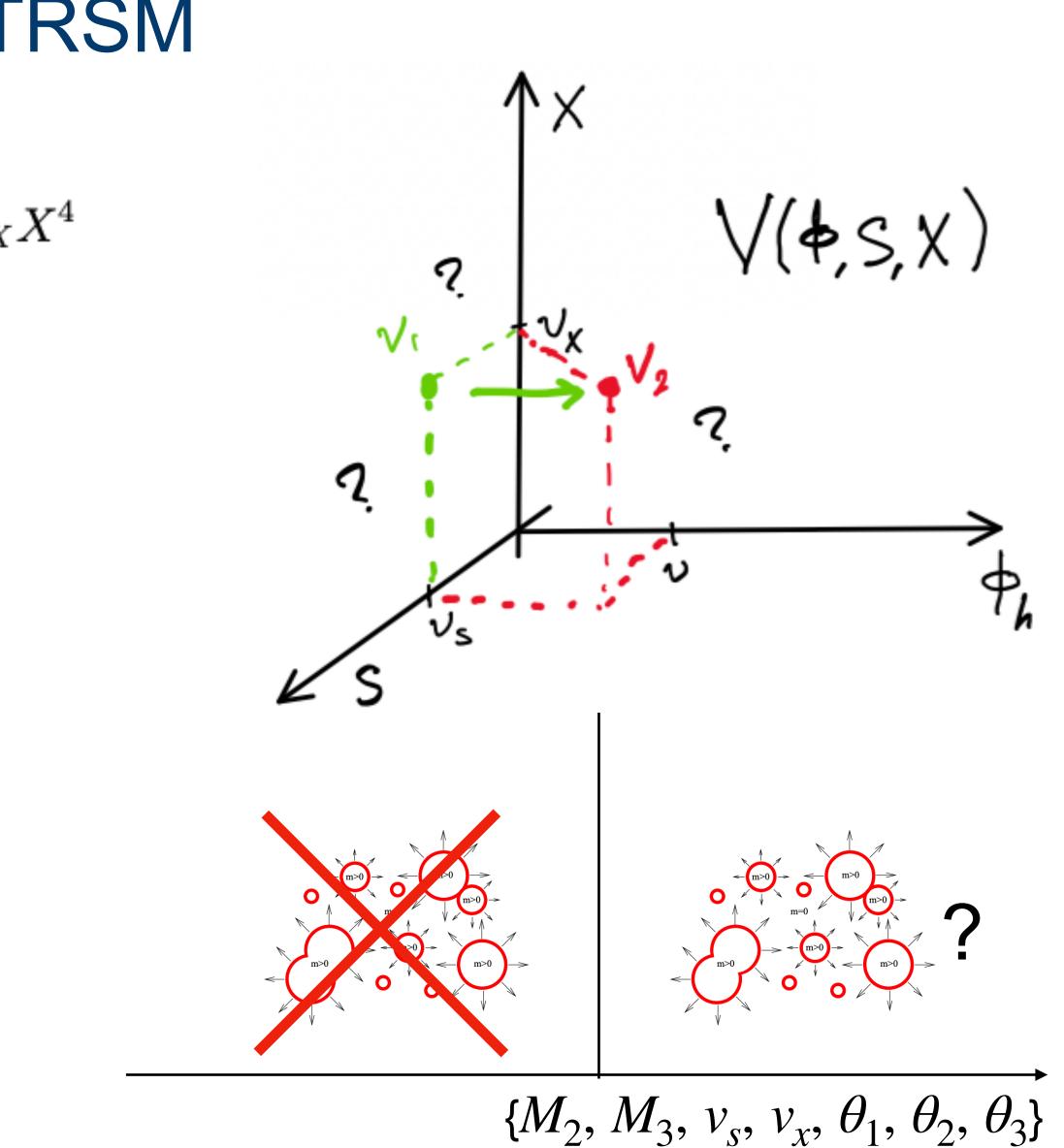
$$\Phi = \begin{pmatrix} 0\\ \frac{\phi_h + v}{\sqrt{2}} \end{pmatrix}, \quad S = \frac{\phi_S + v_S}{\sqrt{2}}, \quad X = \frac{\phi_X + v_X}{\sqrt{2}} \qquad \begin{pmatrix} h_1\\ h_2\\ h_3 \end{pmatrix} = R \begin{pmatrix} \phi_h\\ \phi_S\\ \phi_X \end{pmatrix}$$

Physical parameter space: $\{M_2, M_3, v_s, v_x, \theta_1, \theta_2, \theta_3\}$

 $M_1 = 125 \ GeV, v = 246 \ GeV$

Can we have First-Order Phase Transition (FOPT)? For which parameters? Does it come with HHH enhancement?

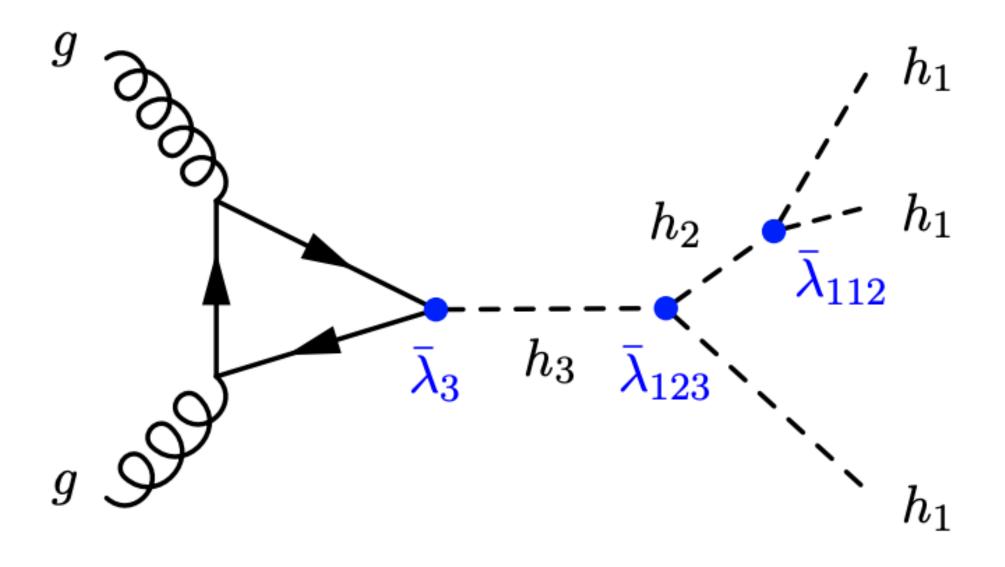




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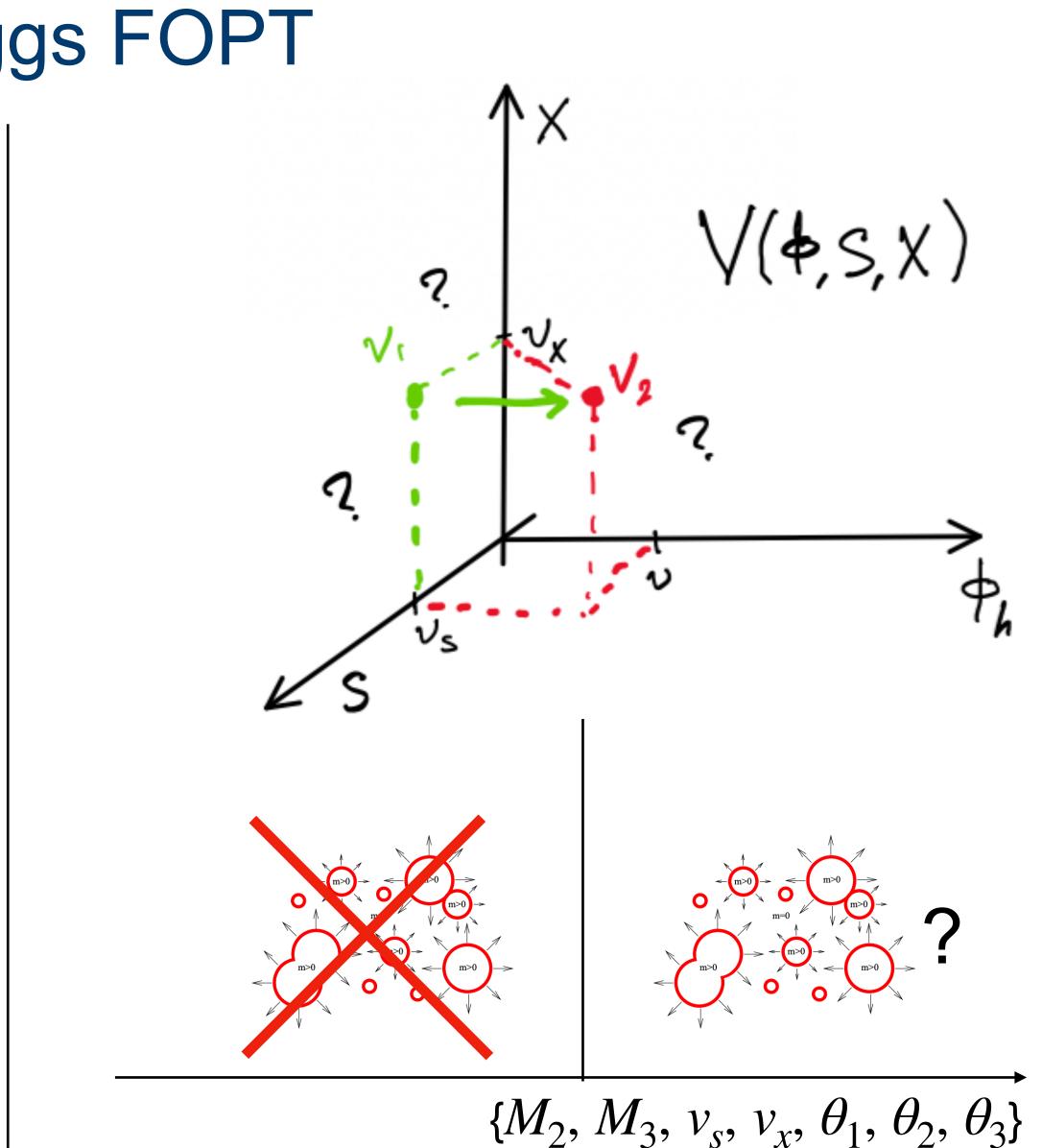
TRSM: HHH production and Higgs FOPT



nonzero VEV for two added scalars for double resonance



MultiHiggs production and EWSB

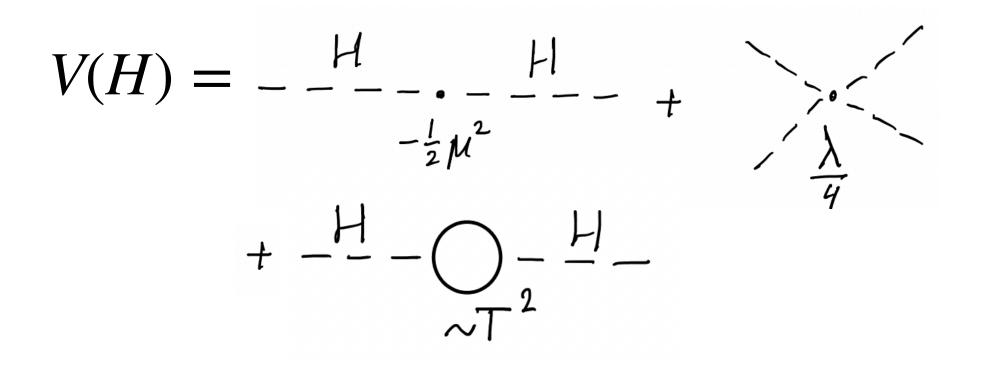


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PT in TRSM: start with thermal QFT

At LO: only masses get T contribution



$$\begin{split} m_1^2(T) &= -\mu_1^2 + \frac{T^2}{48} \left(3g_1^2 + 9g_2^2 + 2(6y_t^2 + 12\lambda_1 + \lambda_{12} + \lambda_{13}) \right), \\ m_2^2(T) &= -\mu_2^2 + \frac{T^2}{24} \left(4\lambda_{12} + \lambda_{23} + 6\lambda_2 \right), \\ m_3^2(T) &= -\mu_3^2 + \frac{T^2}{24} \left(4\lambda_{13} + \lambda_{23} + 6\lambda_3 \right), \end{split}$$

resulting in an *effective* finite-temperature potential:

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$$V_{\text{eff,LO}}(\phi_i, T) = \frac{1}{2} \sum_i m_i^2(T) \phi_i^2 + \frac{1}{4} \sum_{i \le j} \lambda_{ij} \phi_i^2 \phi_j^2.$$

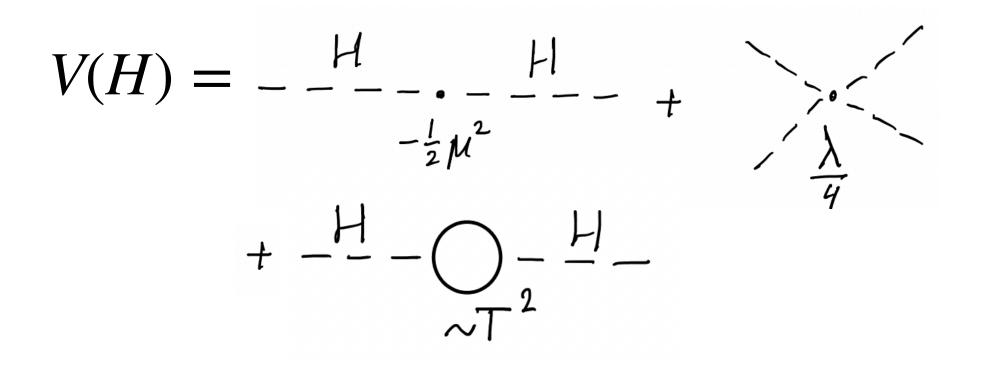
MultiHiggs production and EWSB

Osama Karkout



PT in TRSM: start with thermal QFT

At LO: only masses get T contribution



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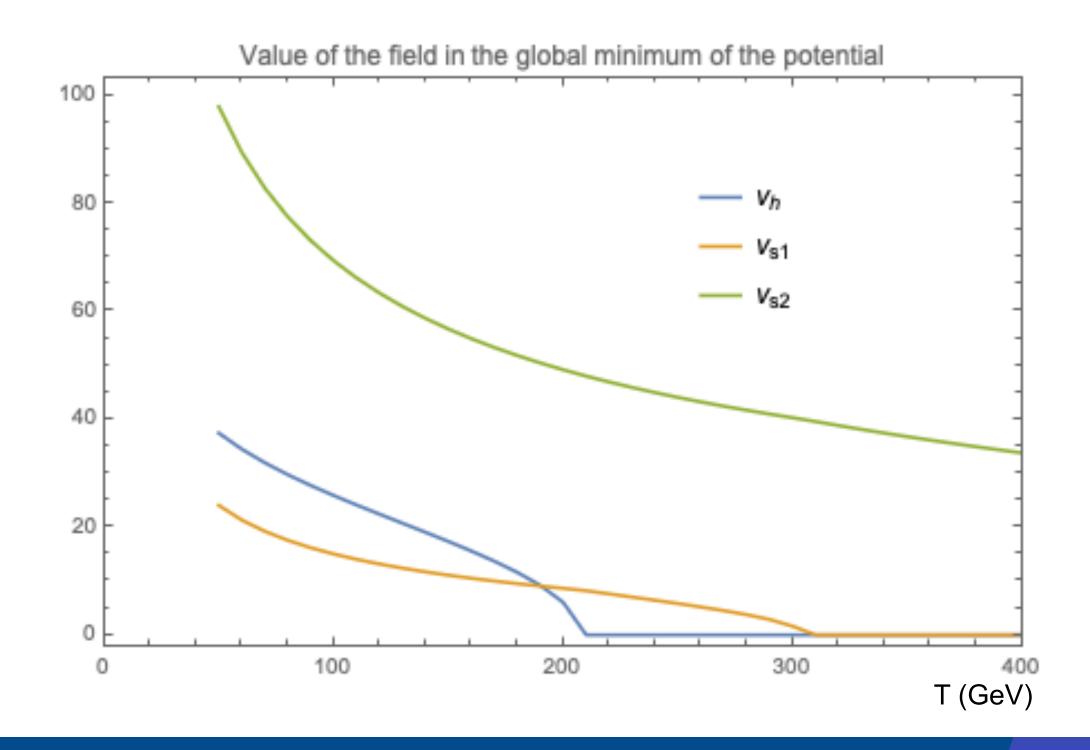
$$V_{\text{eff,LO}}(\phi_i, T) = \frac{1}{2} \sum_i m_i^2(T) \phi_i^2 + \frac{1}{4} \sum_{i \le j} \lambda_{ij} \phi_i^2 \phi_j^2.$$

MultiHiggs production and EWSB

Started using Mathematica to numerically solve RGEs (differential equations as a function of T)

We tried points with large HHH xsec: No FOPT!

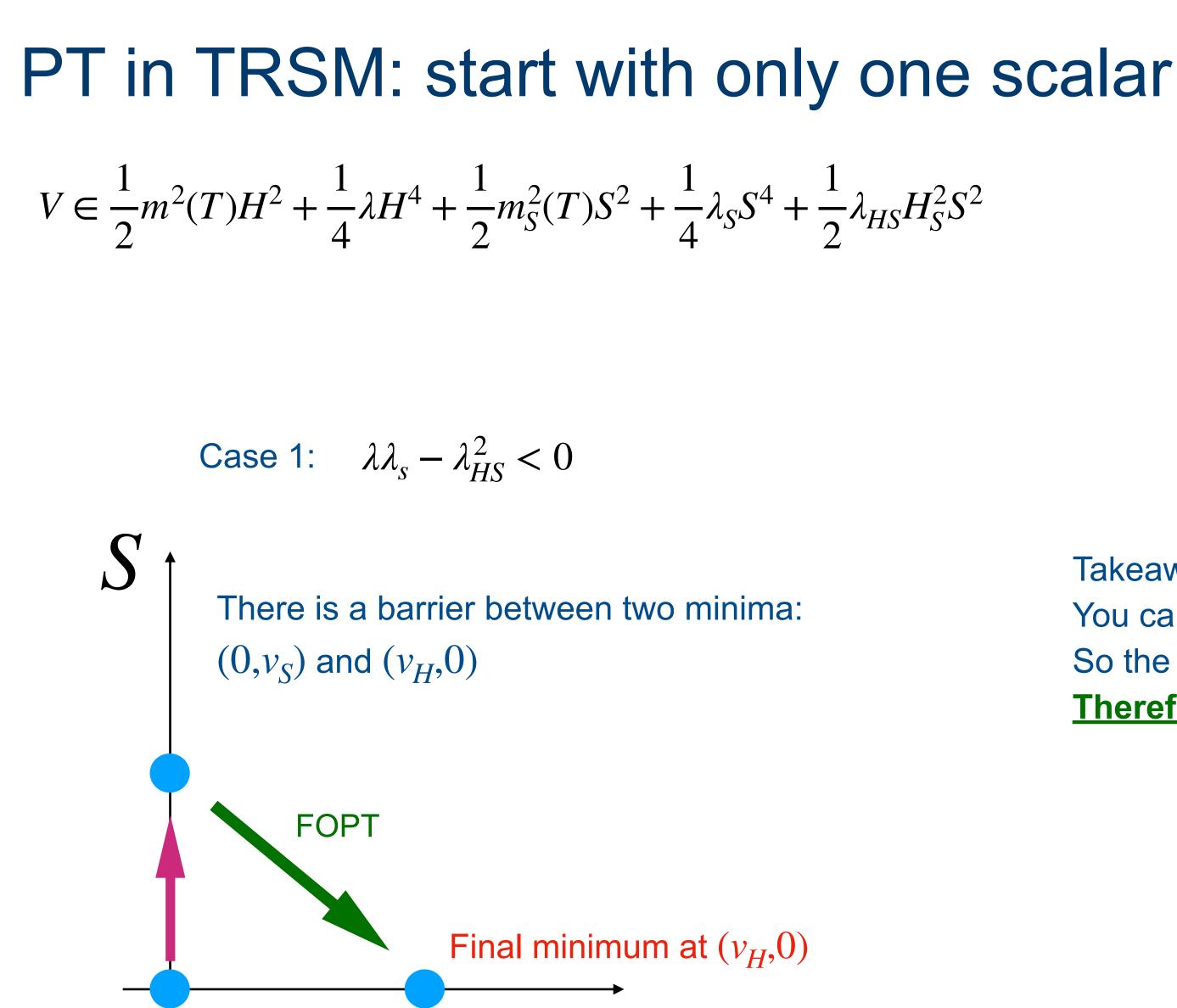
Intuition: I don't think there will be FOPT... Can we prove it?



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Continuous transition

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MultiHiggs production and EWSB



Osama Karkout,¹ Andreas Papaefstathiou,² Marieke Postma,^{1,3} Gilberto Tetlalmatzi-Xolocotzi,^{4,5} Jorinde van de Vis,⁶ Tristan du Pree¹ https://arxiv.org/pdf/2404.12425

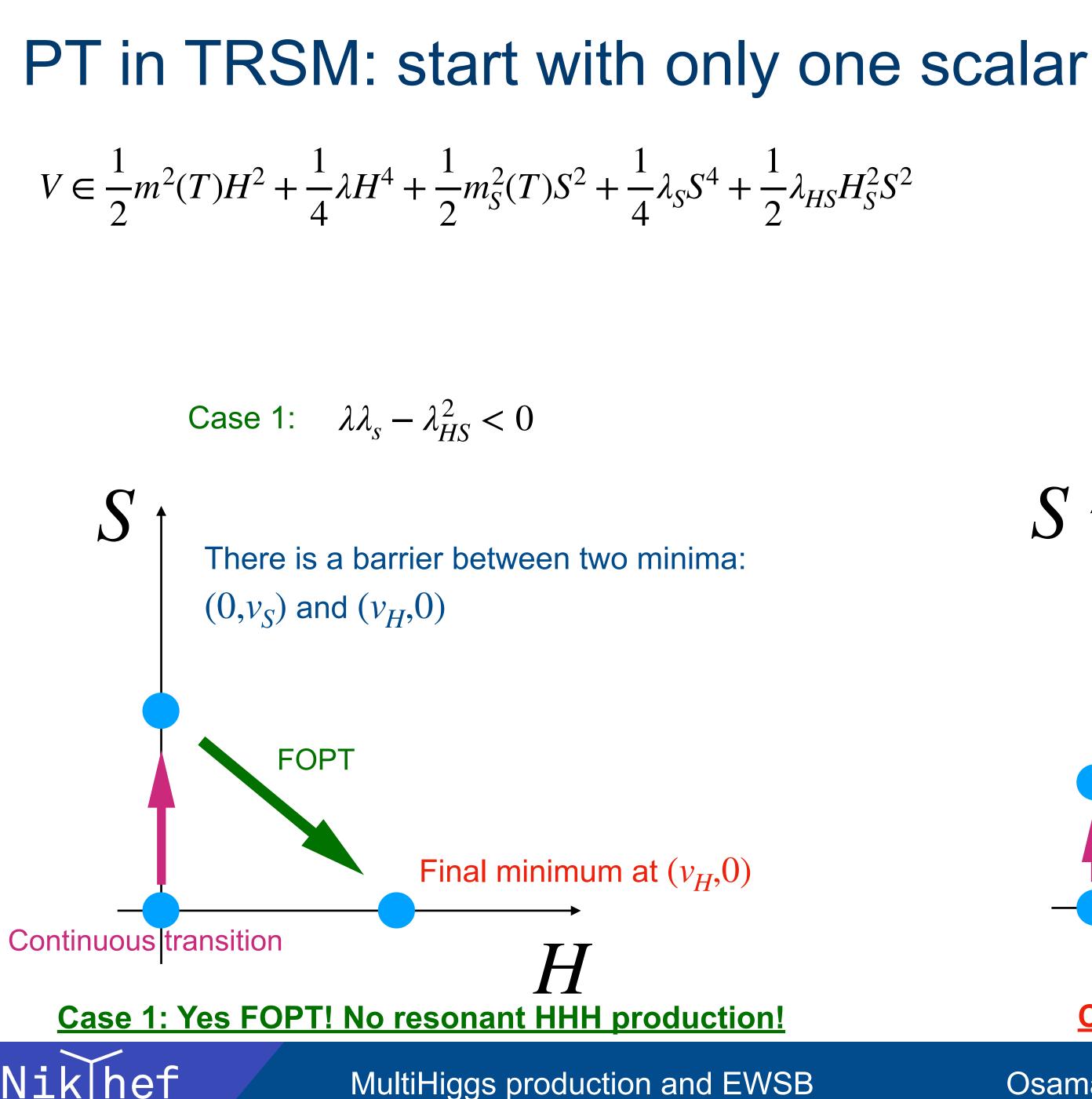
Extrema at: $\partial_H V = 0$, $\partial_S V = 0$

Takeaway: Since there is a barrier between the two axes (fields) You cannot put a minimum there! So the field S must end up with a zero VEV **Therefor: No Mixing! No resonant HHH production!**

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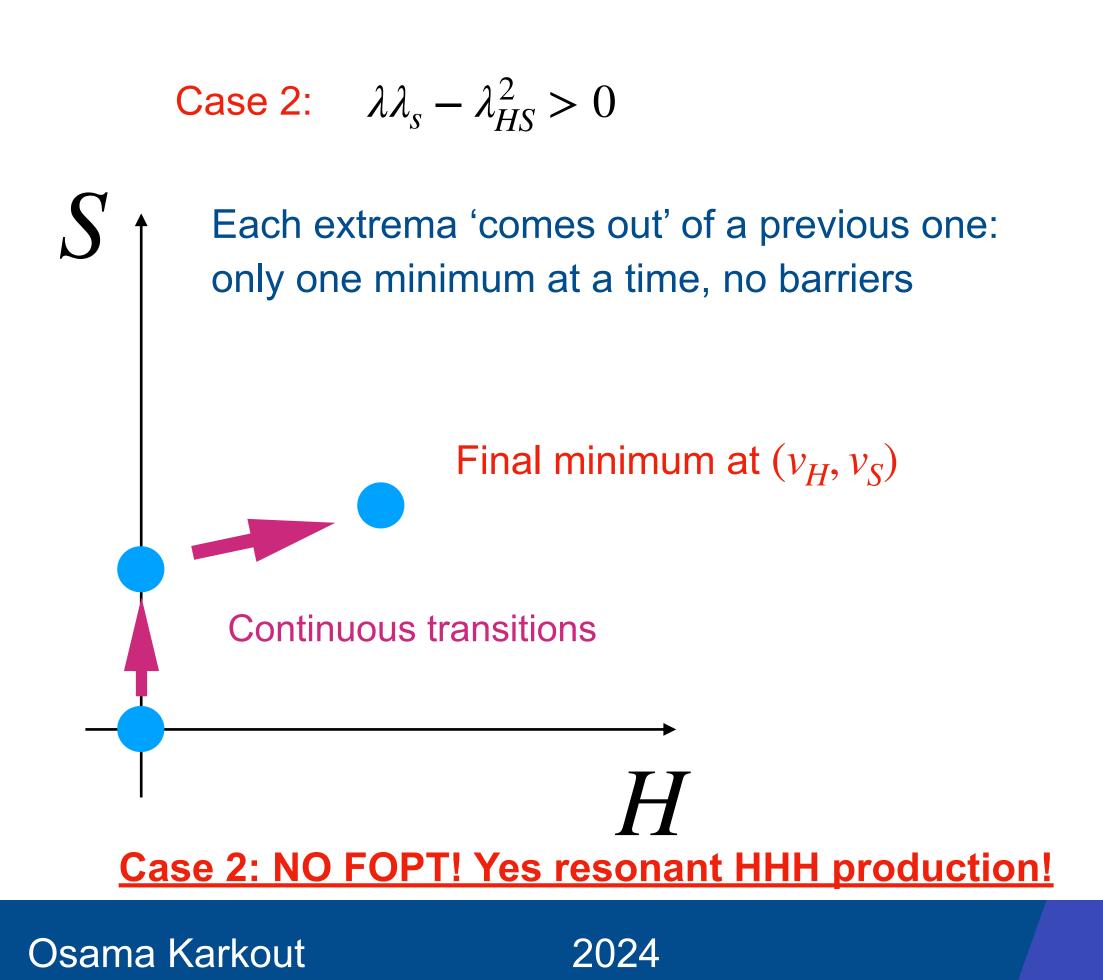






Osama Karkout,¹ Andreas Papaefstathiou,² Marieke Postma,^{1,3} Gilberto Tetlalmatzi-Xolocotzi,^{4,5} Jorinde van de Vis,⁶ Tristan du Pree¹ https://arxiv.org/pdf/2404.12425

Extrema at: $\partial_H V = 0$, $\partial_S V = 0$





Call the fields x_i

$$V(x_1,x_2,x_3) = rac{1}{2}\sum_i m_i^2 x_i^2 + rac{1}{4}\sum_{i,j} c_{ij} x_i^2 x_j^2,$$

Find all extrema by taking $\partial_i V = 0$

- Origin: $\mathbf{x}_0 \equiv (0, 0, 0)$.
- Axial extremum $\mathbf{x}_1 \equiv (x_1, 0, 0)$ with

$$x_1 = \sqrt{-m_1^2/c_{11}}.$$

• Planar extremum $\mathbf{x}_{12} \equiv (x_1, x_2, 0)$ with

$$x_1 = \sqrt{rac{c_{12}m_2^2 - c_{22}m_1^2}{c_{11}c_{22} - c_{12}^2}}, \quad x_2 = \sqrt{rac{c_{12}m_1^2 - c_{11}m_2^2}{c_{11}c_{22} - c_{12}^2}},$$

• Bulk extremum $\mathbf{x}_{123} \equiv (x_1, x_2, x_3)$ with

$$\begin{split} x_1 &= \frac{\sqrt{(c_{23}^2 - c_{22}c_{33})m_1^2 + (c_{12}c_{33} - c_{13}c_{23})m_2^2 + (c_{13}c_{22} - c_{12}c_{23})m_3^2}}{\sqrt{D}},\\ x_2 &= \frac{\sqrt{(c_{12}c_{33} - c_{13}c_{23})m_1^2 + (c_{13}^2 - c_{11}c_{33})m_2^2 + (c_{11}c_{23} - c_{12}c_{13})m_3^2}}{\sqrt{D}},\\ x_3 &= \frac{\sqrt{(c_{13}c_{22} - c_{12}c_{23})m_1^2 + (c_{11}c_{23} - c_{12}c_{13})m_2^2 + (c_{12}^2 - c_{11}c_{22})m_3^2}}{\sqrt{D}}, \end{split}$$

where

Nik

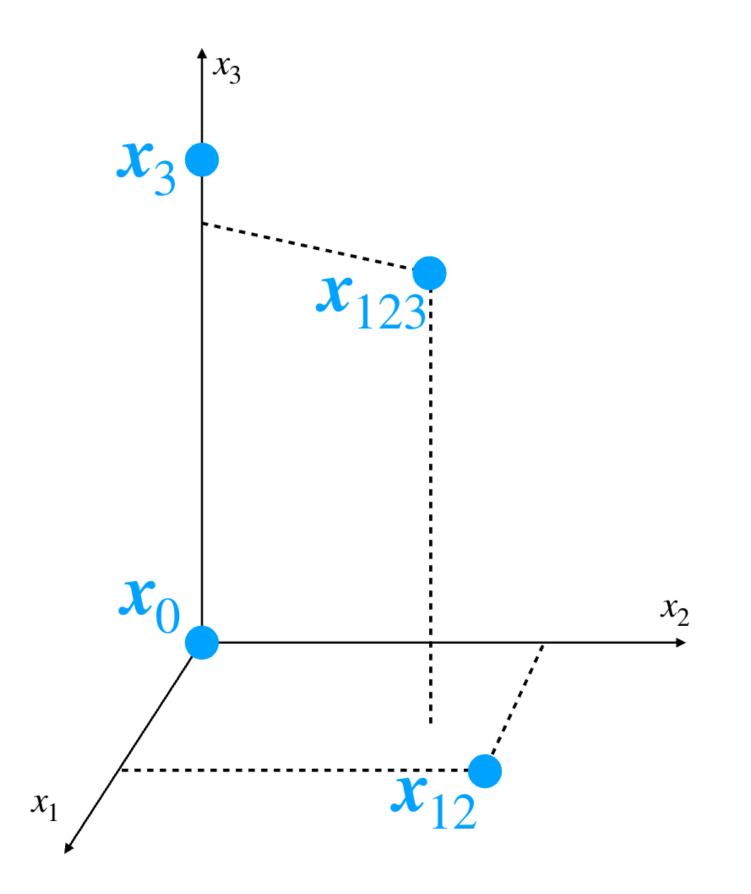
$$D = c_{11}c_{22}c_{33} + 2c_{12}c_{13}c_{23} - c_{13}^2c_{22} - c_{11}c_{23}^2 - c_{12}^2c_{33},$$

is the determinant of c_{ij} .

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MultiHiggs production and EWSB

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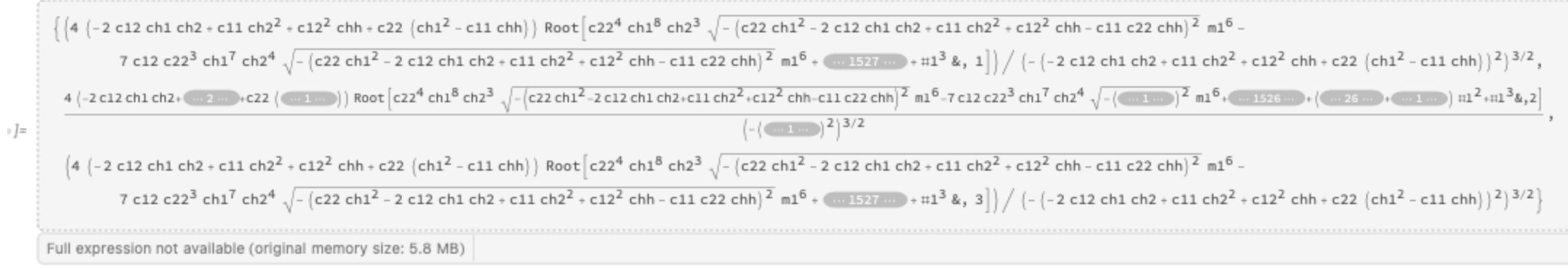
Osama Karkout



The extremum is a minimum if the eigenvalues of the Hessian of the potential h_{kl} , i.e. the mass matrix, evaluated at the extremum are all positive, with

 $h_{kl}(x_1, x_2, x_3) \equiv \partial_{x_k} \partial_{x_l} V(x_1, x_2, x_3)$

l= curve = Simplify[Eigenvalues[Simplify[hessian /. Solutions[16]]]]



Not even mathematica could help... insight needed.



MultiHiggs production and EWSB

Osama Karkout,¹ **Andreas Papaefstathiou**,² **Marieke Postma**,^{1,3} **Gilberto Tetlalmatzi-Xolocotzi**,^{4,5} **Jorinde van de Vis**,⁶ **Tristan du Pree**¹ https://arxiv.org/pdf/2404.12425

$$x_3) = (m_k^2 + \sum_i c_{ik} x_i^2) \delta_{kl} + 2c_{kl} x_k x_l.$$
(4.16)

Osama Karkout





$$V(x_1, x_2, x_3) = \frac{1}{2} \sum_{i} m_i^2 x_i^2 + \frac{1}{4} \sum_{i,j} c_{ij} x_i^2 x_j^2,$$

Insights:

- Z_2 symmetry: $(x \rightarrow -x)$ does not change the potential! I can focus on the positive x_i and generalise.

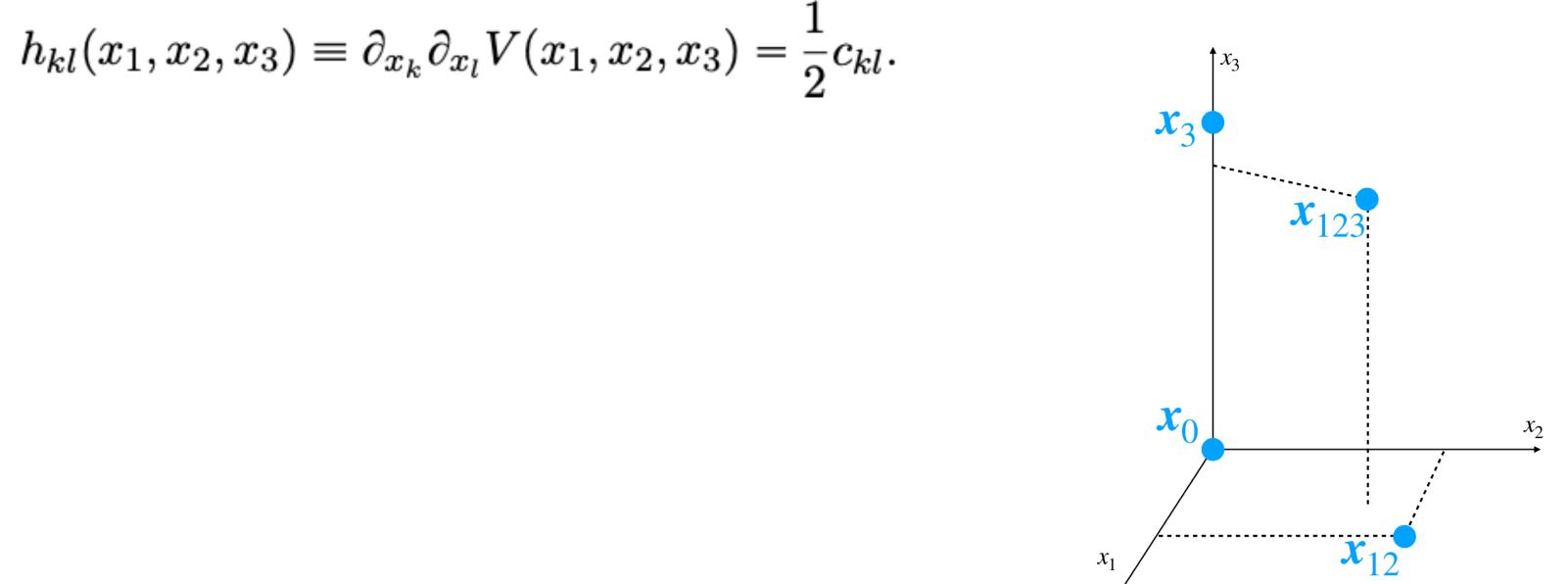
Now the Hessian is simple:



MultiHiggs production and EWSB

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The shape of the potential (whether an extremum is minimum) does not change if I scale the axes: $x^2 \rightarrow x$



Osama Karkout



$$V(x_1, x_2, x_3) = \frac{1}{2} \sum_{i} m_i^2 x_i^2 + \frac{1}{4} \sum_{i,j} c_{ij} x_i^2 x_j^2,$$

Insights:

- Z_2 symmetry: $(x \rightarrow -x)$ does not change the potential! I can focus on the positive x_i and generalise.

Now the Hessian is simple: $h_{kl}(x_1, x_2, x_3) \equiv \partial_{x_k} \partial_{x_l}$ For resonant HHH:

We demand that \mathbf{x}_{123} is today's vacuum. The eigenvalues of the rescaled Hessian should then be positive. Sylvester's criterion, stating that a square Hermitian matrix is positive definite if and only if all the leading principal minors are positive, then gives

$$c_{ii} > 0$$
, & $C_{ij} \equiv c_{ii}c_{jj} - c_{ij}^2 > 0$, &

where

hef

$$D = c_{11}c_{22}c_{33} + 2c_{12}c_{13}c_{23} - c_{13}^2c_{22} - c_{11}c_{23}^2 - c_{12}^2$$

is the determinant of c_{ij} .

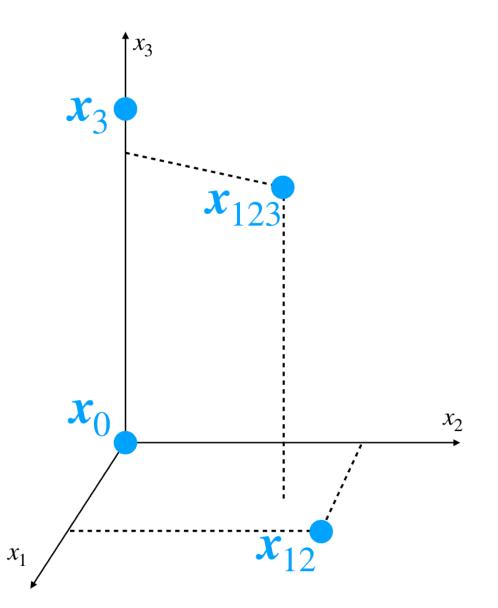
MultiHiggs production and EWSB

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The shape of the potential (whether an extremum is minimum) does not change if I scale the axes: $x^2 \rightarrow x$

$$V(x_1, x_2, x_3) = rac{1}{2}c_{kl}$$

$$D > 0,$$
 (4.18)



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 $_{2}c_{33}$,

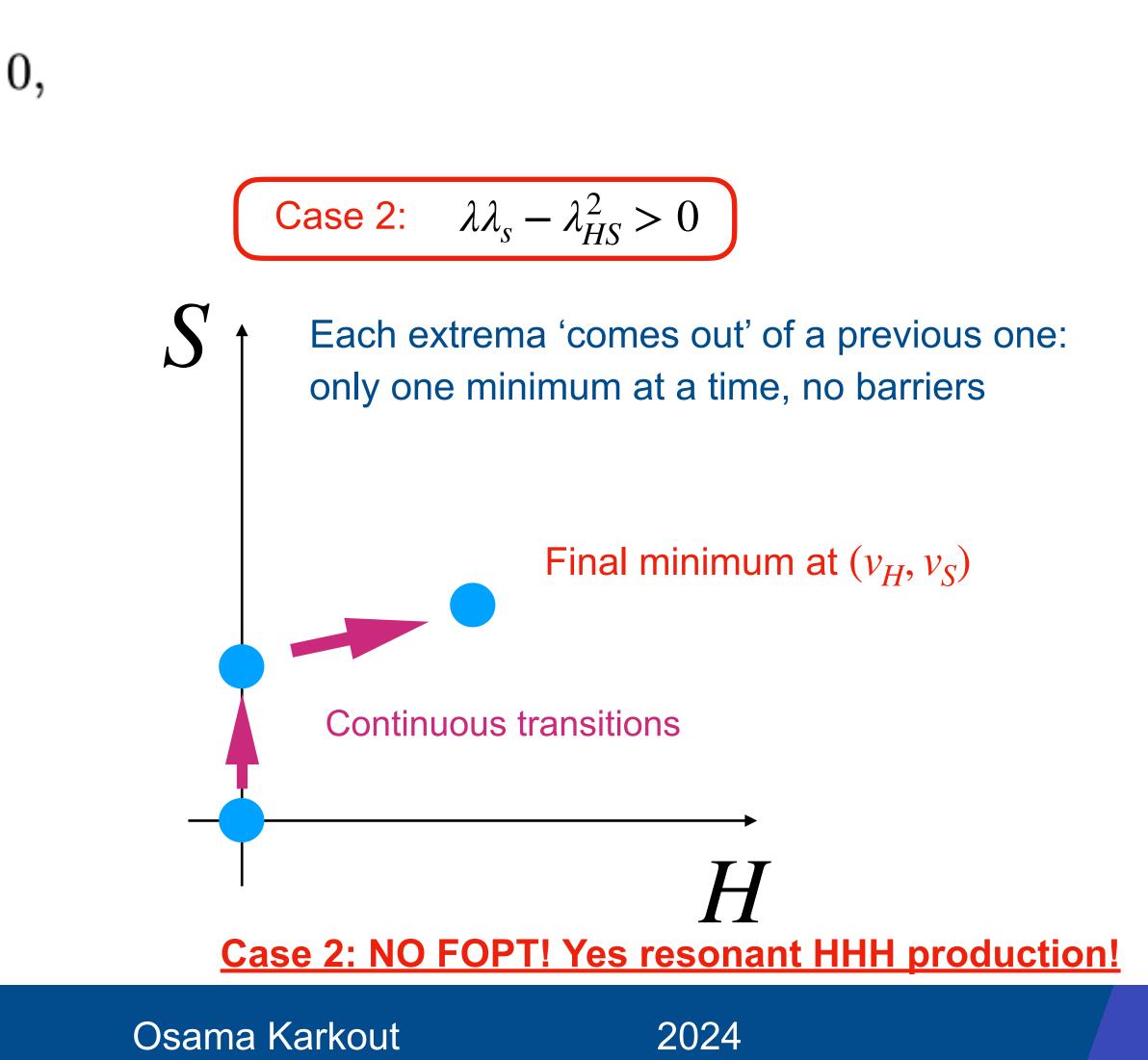


$$egin{aligned} V(x_1,x_2,x_3) &= rac{1}{2} \sum_i m_i^2 x_i^2 + rac{1}{4} \sum_{i,j} c_{ij} x_i^2 x_j^2, \ c_{ii} &> 0, \quad \& \quad C_{ij} \equiv c_{ii} c_{jj} - c_{ij}^2 > 0, \quad \& \quad D > 0 \end{aligned}$$



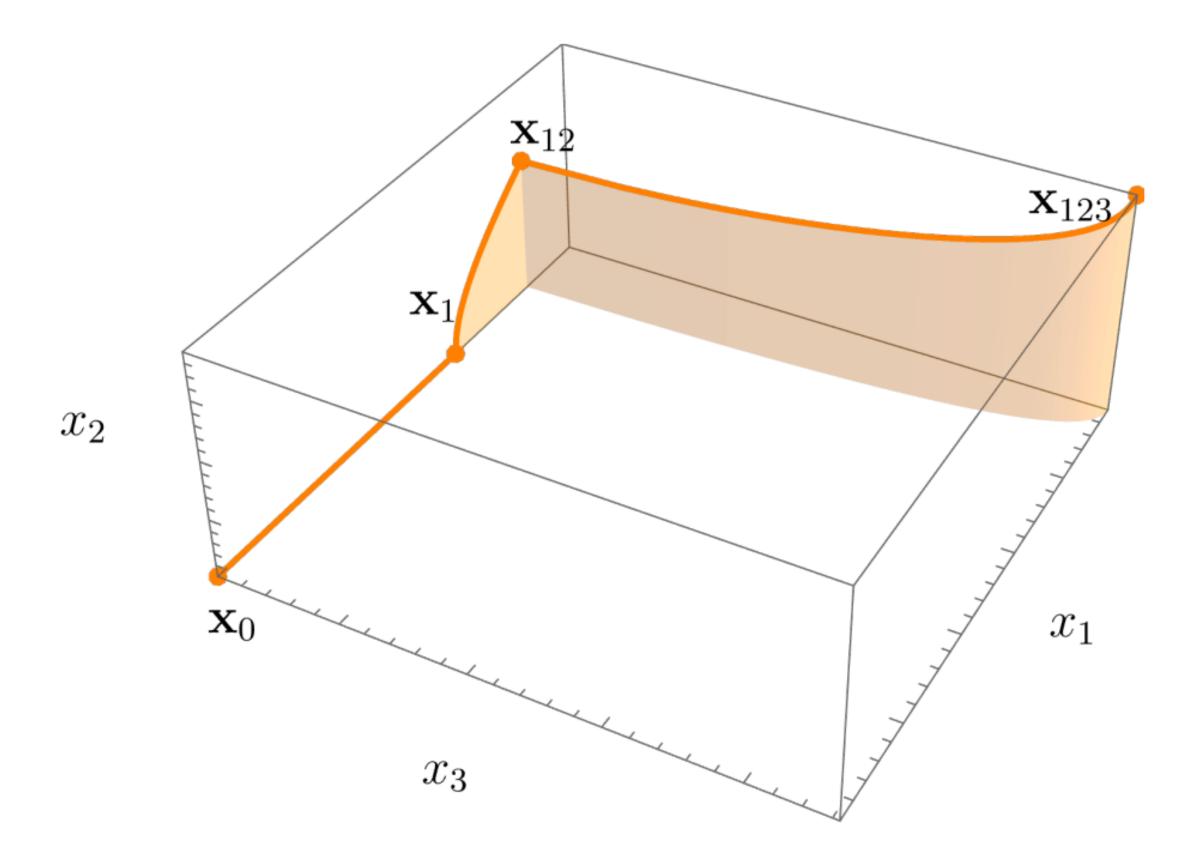
MultiHiggs production and EWSB

Osama Karkout,¹ **Andreas Papaefstathiou**,² **Marieke Postma**,^{1,3} **Gilberto Tetlalmatzi-Xolocotzi**,^{4,5} **Jorinde van de Vis**,⁶ **Tristan du Pree**¹ https://arxiv.org/pdf/2404.12425





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MultiHiggs production and EWSB

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Each extrema 'comes out' of a previous one: only one minimum at a time, no barriers

Final minimum at (v_H, v_S, v_x)

Continuous transitions

Case 2: NO FOPT! Yes resonant HHH production!





$$V(x_1, x_2, x_3) = \frac{1}{2} \sum_i m_i^2 x_i^2 + \frac{1}{4} \sum_{i,j} c_{ij} x_i^2 x_j^2,$$

 $c_{ii} > 0, \quad \& \quad C_{ij} \equiv c_{ii} c_{jj} - c_{ij}^2 > 0, \quad \& \quad D < 0$

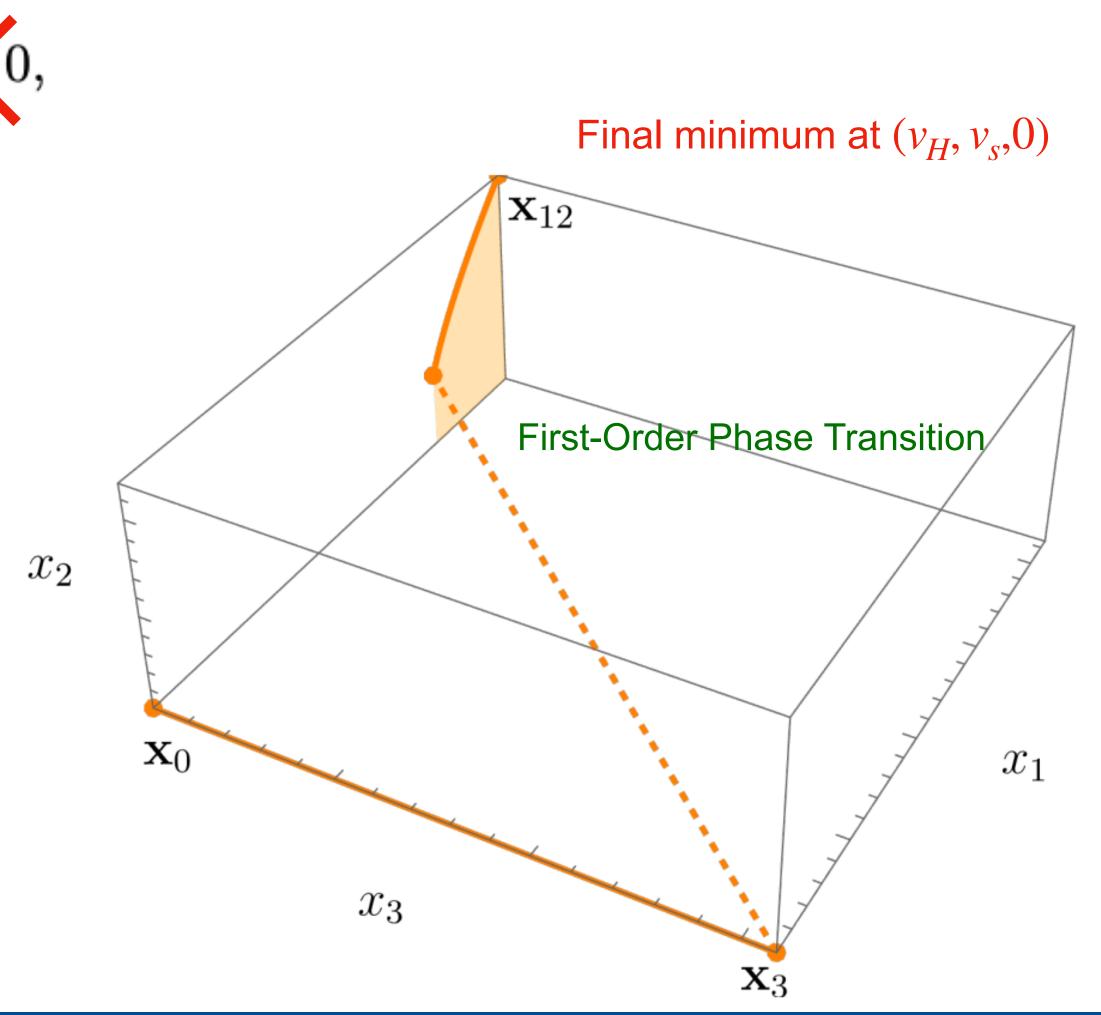
Case 1: Yes FOPT! No resonant HHH production!

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Nik



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Osama Karkout



$$V(x_1, x_2, x_3) = \frac{1}{2} \sum_{i} m_i^2 x_i^2 + \frac{1}{4} \sum_{i,j} c_{ij} x_i^2 x_j^2,$$

$$c_{ii} > 0, \quad \& \quad C_{ij} \equiv c_{ii} c_{jj} - c_{ij}^2 > 0, \quad \& \quad D < 0$$

$$D < 0$$

Nightmare! If we want FOPT, we cannot detect it with HHH

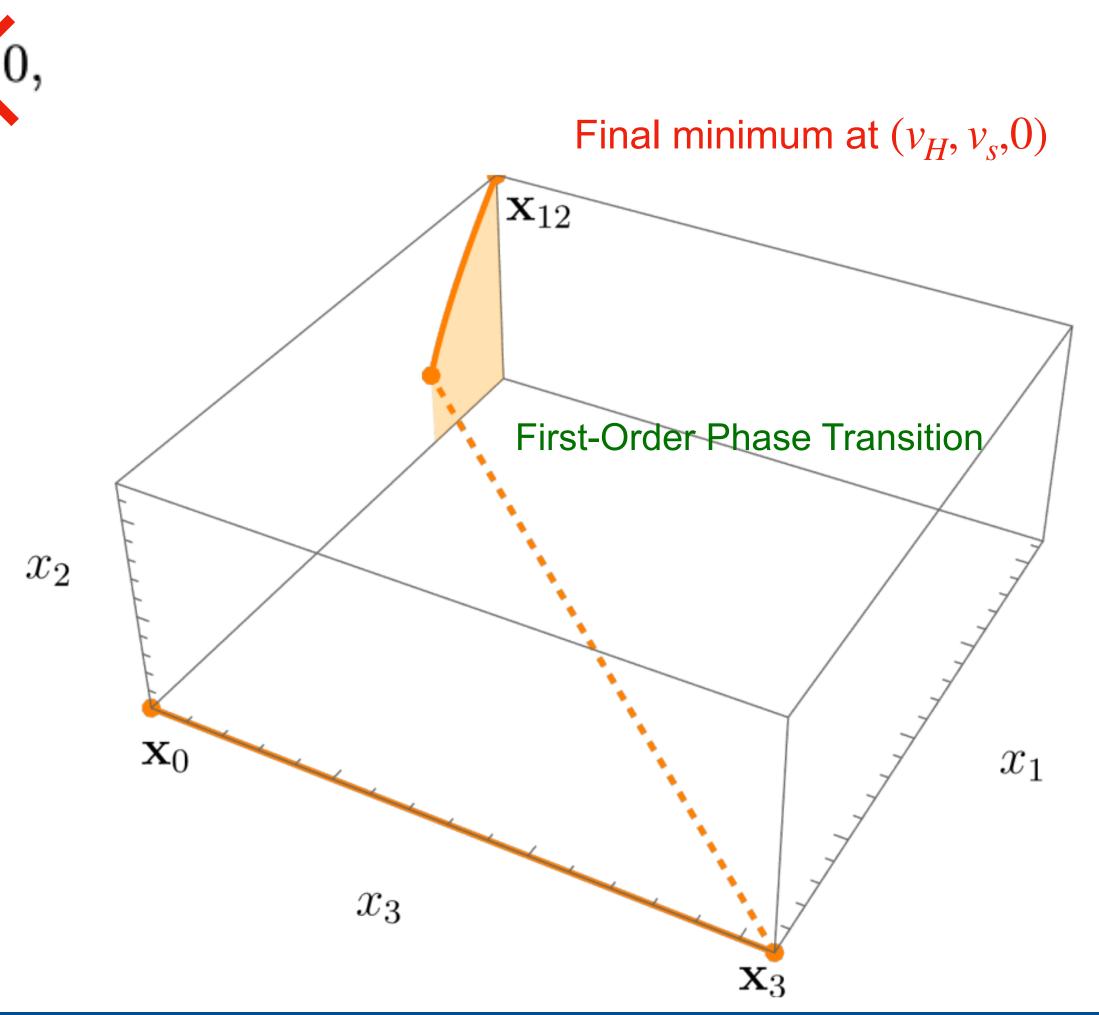
Case 1: Yes FOPT! No resonant HHH production!

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MultiHiggs production and EWSB

Osama Karkout,¹ **Andreas Papaefstathiou**,² **Marieke Postma**,^{1,3} **Gilberto Tetlalmatzi-Xolocotzi**,^{4,5} **Jorinde van de Vis**,⁶ **Tristan du Pree**¹ https://arxiv.org/pdf/2404.12425



Osama Karkout



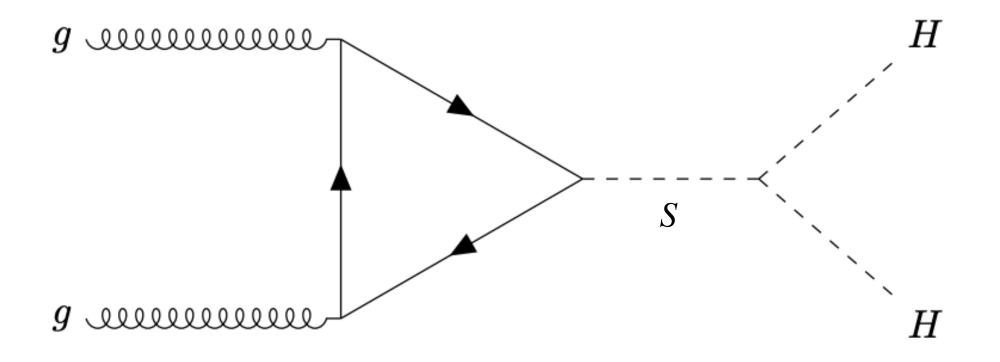
$$V(x_1, x_2, x_3) = \frac{1}{2} \sum_{i} m_i^2 x_i^2 + \frac{1}{4} \sum_{i,j} c_{ij} x_i^2 x_j^2,$$

$$c_{ii} > 0, \quad \& \quad C_{ij} \equiv c_{ii} c_{jj} - c_{ij}^2 > 0, \quad \& \quad D < 0$$

$$D < 0$$

Silver lining:

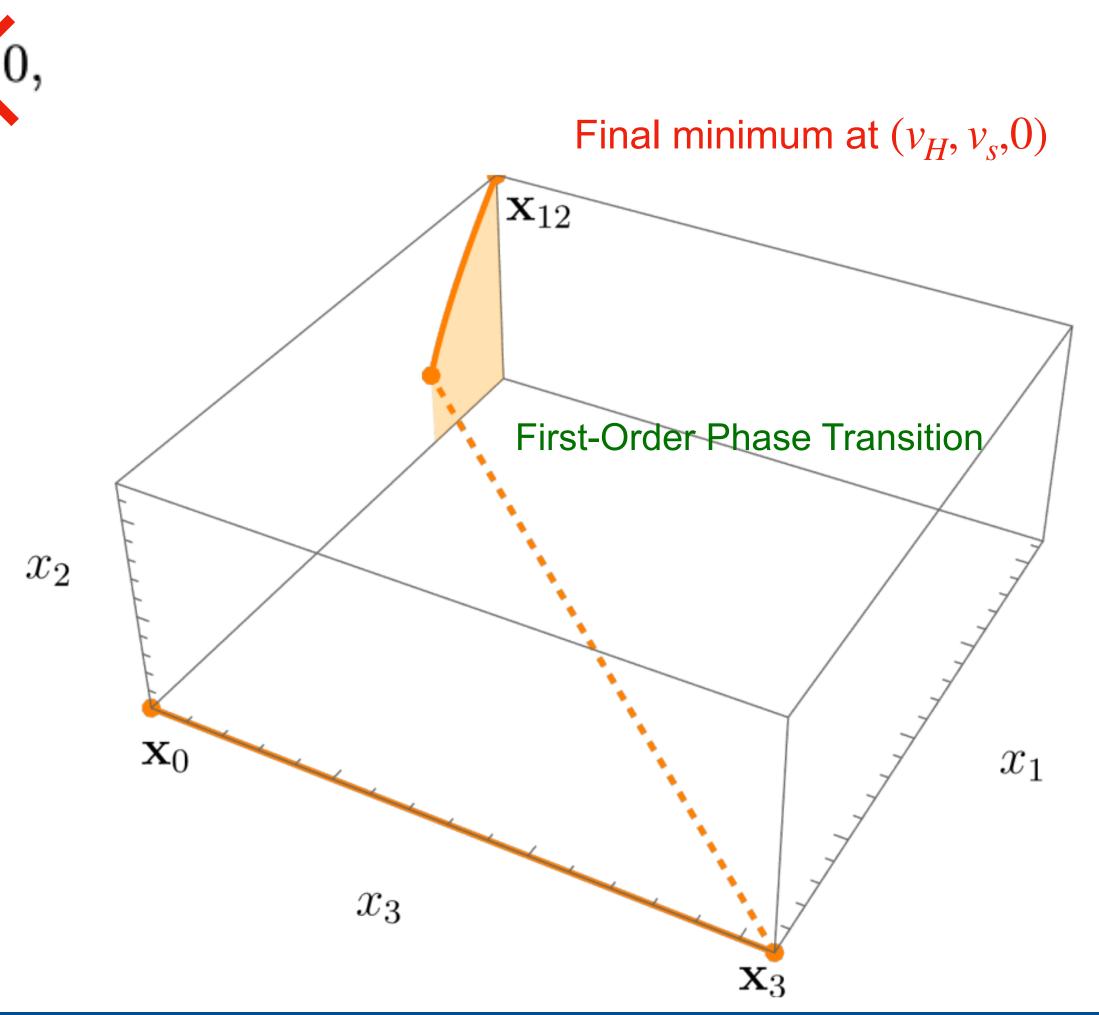
Final minimum at $(v_H, v_s, 0) \rightarrow$ resonant HH production!!





MultiHiggs production and EWSB

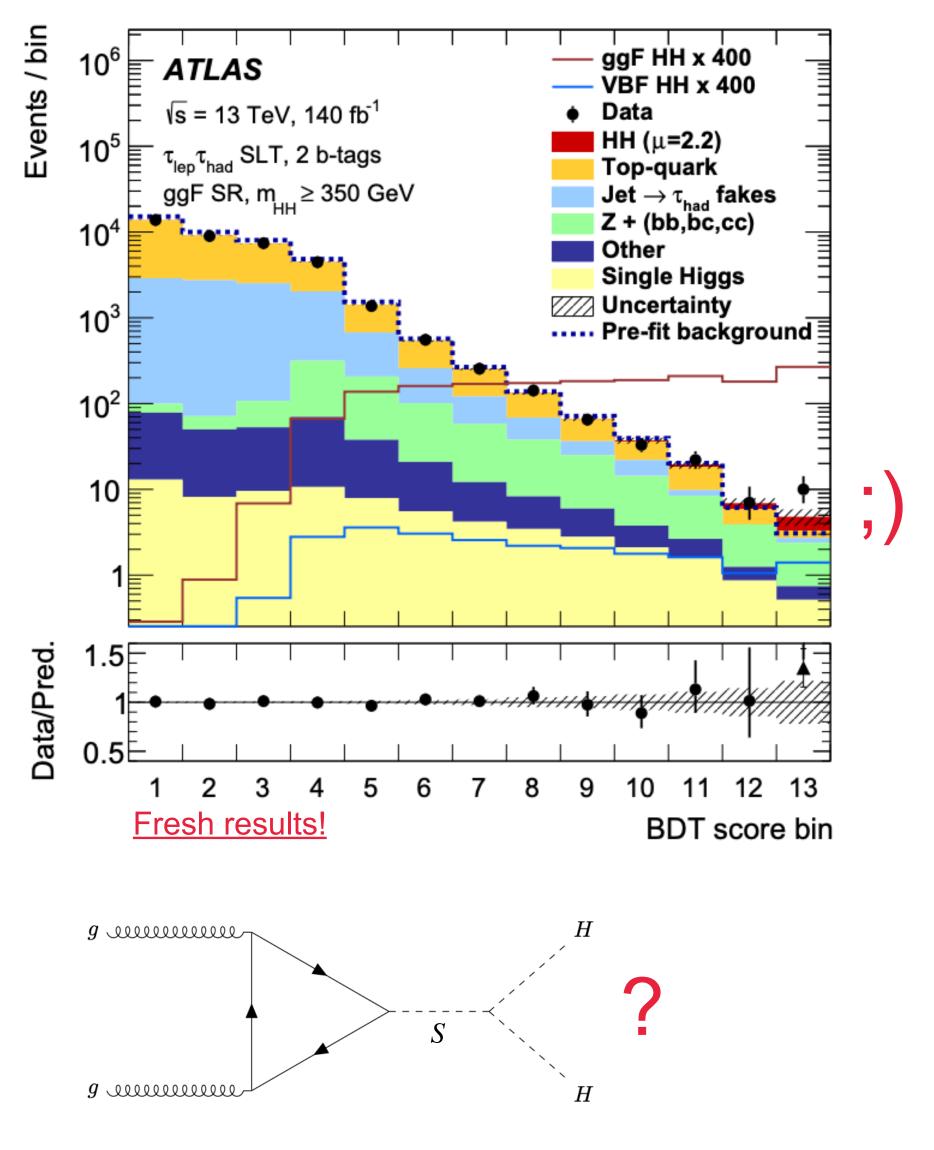
Osama Karkout,¹ **Andreas Papaefstathiou**,² **Marieke Postma**,^{1,3} **Gilberto Tetlalmatzi-Xolocotzi**,^{4,5} **Jorinde van de Vis**,⁶ **Tristan du Pree**¹ https://arxiv.org/pdf/2404.12425



Osama Karkout

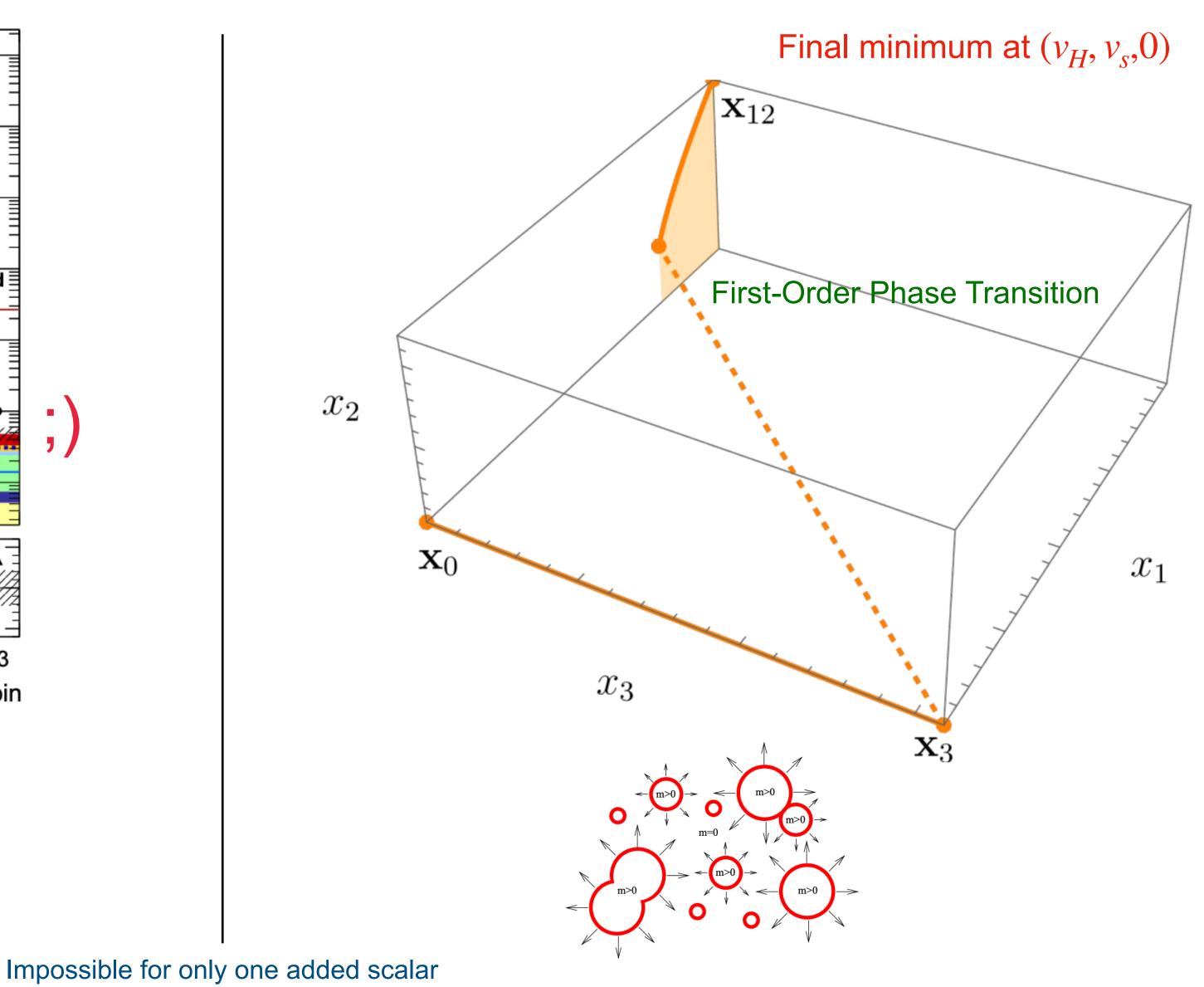


TRSM can accommodate both HH enhancement and FOPT!



Nik hef

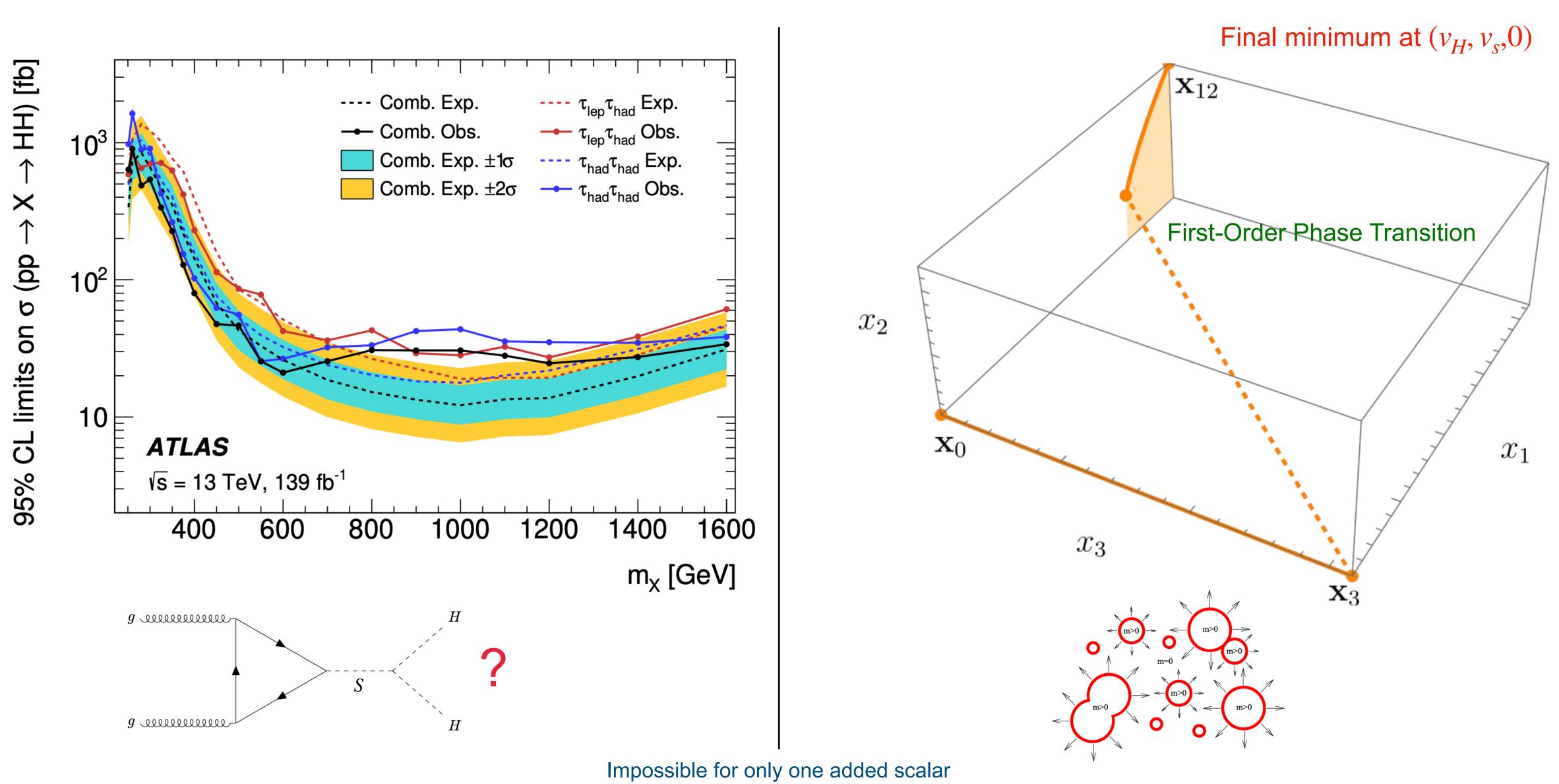
MultiHiggs production and EWSB



Osama Karkout



TRSM can accommodate both HH enhancement and FOPT!



MultiHiggs production and EWSB

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Final notes on HHH and FOPT

- Z_2 symmetric TRSM can enhance HHH if both scalars have nonzero VEVs at zero temperature (today)
- Z₂ symmetric TRSM can accommodate First Order Phase Transitions (desired for matter-antimatter asymmetry)
- Z_2 symmetric TRSM cannot accommodate both at the same time! Zero scalar VEV required for FOPT



MultiHiggs production and EWSB

Osama Karkout,¹ **Andreas Papaefstathiou**,² **Marieke Postma**,^{1,3} **Gilberto Tetlalmatzi-Xolocotzi**,^{4,5} **Jorinde van de Vis**,⁶ **Tristan du Pree**¹ https://arxiv.org/pdf/2404.12425

ave nonzero VEVs at zero temperature (today) **se Transitions** (desired for matter-antimatter asymmetry) same time! Zero scalar VEV required for FOPT



Final notes on HHH and FOPT

- Z_2 symmetric TRSM can enhance HHH if both scalars have nonzero VEVs at zero temperature (today)
- Z₂ symmetric TRSM can accommodate First Order Phase Transitions (desired for matter-antimatter asymmetry)
- Z_2 symmetric TRSM cannot accommodate both at the same time! Zero scalar VEV required for FOPT

Ideas to achieve both FOPT and HHH:

- Add terms that break Z_2 symmetry
- Add yet another scalar ;)



MultiHiggs production and EWSB

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ave nonzero VEVs at zero temperature (today) **se Transitions** (desired for matter-antimatter asymmetry) same time! Zero scalar VEV required for FOPT



Final notes on HHH and FOPT

- Z_2 symmetric TRSM can enhance HHH if both scalars have nonzero VEVs at zero temperature (today)
- Z_2 symmetric TRSM cannot accommodate both at the same time! Zero scalar VEV required for FOPT

Ideas to achieve both FOPT and HHH:

- Add terms that break Z_2 symmetry
- Add yet another scalar;)

presented analytic analysis for LO effective thermal potential. Going to NLO numerically showed us the same conclusion



MultiHiggs production and EWSB

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 Z_2 symmetric TRSM can accommodate First Order Phase Transitions (desired for matter-antimatter asymmetry)

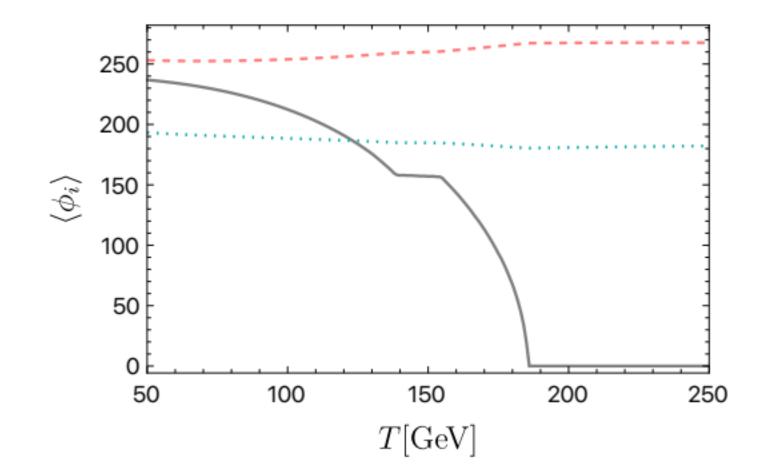


Figure 5: Evolution of the field expectation values in the minimum of the potential for the third BM point in Table 2. The Higgs field is represented by gray solid, ϕ_2 by dashed pink, and ϕ_3 by dotted cyan.



For the actual scan we have generated 530,000 random points over the phase space defined by $M_2, M_3, v_2, v_3, \theta_{12}, \theta_{13}, \theta_{23}$. The ranges considered are as follows:

$M_2 \in [255, 700] \text{ GeV},$ $v_2 \in [0, 1000]$ GeV,

For the mixing angles $\theta_{12}, \theta_{13}, \theta_{23}$ we impose the following limits on the scaling factors [38, **68**] of eq. (2.4):



MultiHiggs production and EWSB

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 $M_3 \in [350, 900] \text{ GeV},$ $v_3 \in [50, 1000]$ GeV.

 $0.95 \le \kappa_1 \le 1.00, \quad 0.0 \le \kappa_2 \le 0.25, \quad 0.0 \le \kappa_3 \le 0.25.$





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Osama Karkout,¹ **Andreas Papaefstathiou**,² **Marieke Postma**,^{1,3} **Gilberto** Viable points with $\sigma > 10 \times \sigma_{SM}(gg \rightarrow hhh)@13.6$ TeV **stan du Pree**¹

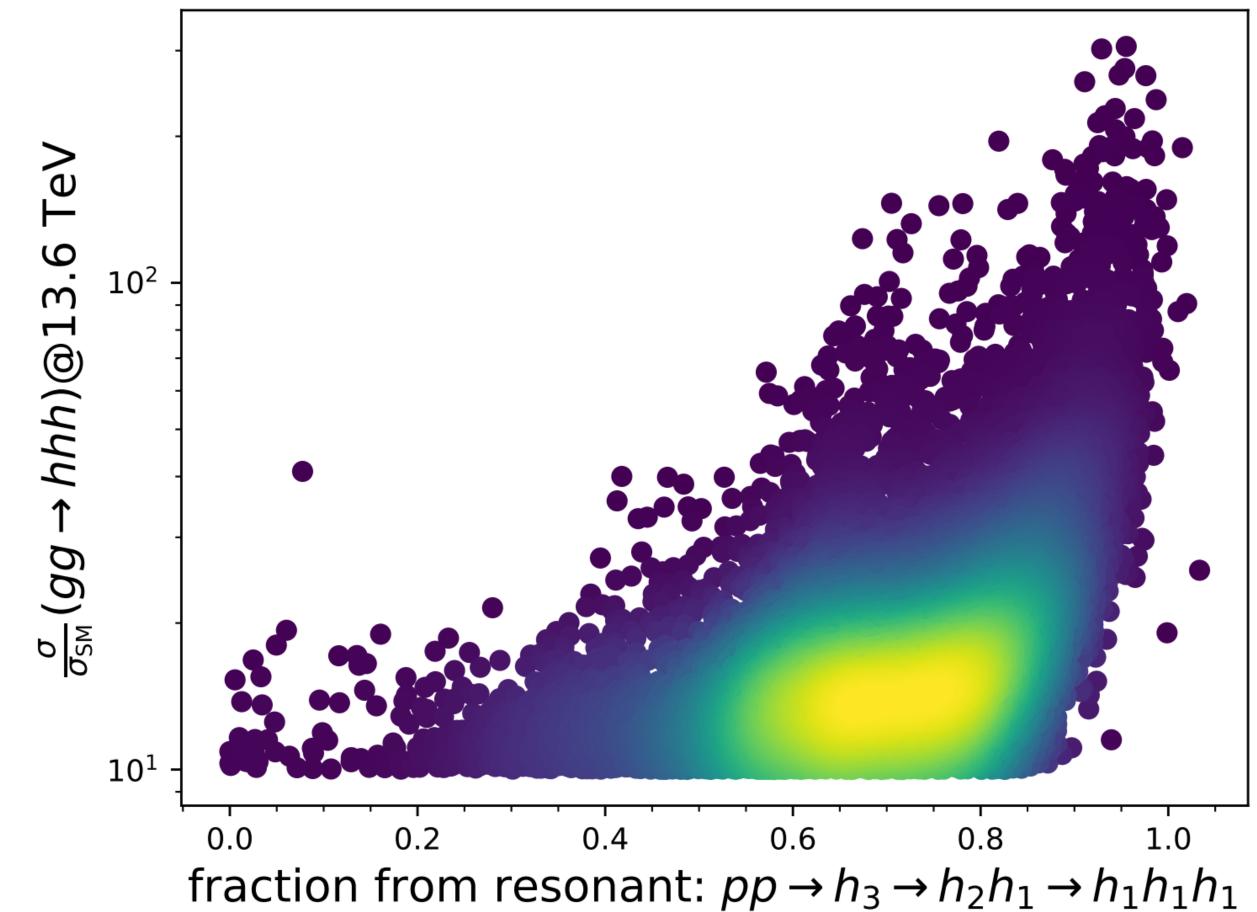


Figure 2: Enhancement of the triple Higgs boson production cross section $\sigma(pp \rightarrow h_1h_1h_1)$ at 13.6 TeV, given in terms of multiples of the SM value, and the resonant fraction contribution from $pp \rightarrow h_3 \rightarrow h_2h_1 \rightarrow h_1h_1h_1$. Only points with a factor 10 enhancement or greater are shown. The density of points increases from the dark blue to yellow shade.

MultiHiggs production and EWSB



Benchmark points for enhanced triple Higgs production

M_2	M_3	v_2	v_3	$ heta_{12}$	$ heta_{13}$	$ heta_{23}$	$rac{\sigma}{\sigma_{SM}}$	Res. Frac.	$\mu_{ m pert}$	$rac{\mu_{ ext{pert}}}{\mu_{ ext{pole}}}$
259.0	495.0	215.8	180.8	6.191	0.163	5.691	306.025	0.955	2.7×10^2	7.3
270.6	444.7	122.4	847.2	0.268	0.030	0.522	302.361	0.929	1.8×10^{2}	7.3
268.6	452.7	137.8	784.8	0.263	0.023	0.645	275.616	0.954	$2.4 imes 10^2$	7.3
272.6	480.7	928.3	143.7	3.098	2.9	2.375	267.245	0.948	$1.4 imes 10^2$	7.2
269.0	409.8	138.0	599.4	0.244	0.004	0.773	266.439	0.976	$2.4 imes 10^2$	7.2
269.1	486.9	227.5	307.9	0.074	6.149	2.631	157.583	0.956	$4.3 imes 10^2$	8.0
259.2	577.0	289.0	275.6	0.137	6.148	2.324	145.470	0.781	$1.2 imes 10^4$	7.2
283.7	575.0	259.4	330.4	0.137	6.152	2.299	122.546	0.779	3.0×10^3	7.2
264.3	469.3	207.3	359.5	0.285	6.277	0.692	119.121	0.999	5.4×10^{3}	7.3
266.5	461.9	653.1	229.0	2.889	3.046	1.015	112.794	0.863	$5.3 imes 10^4$	8.0
259.2	399.7	444.5	217.0	2.917	3.046	1.047	103.717	0.973	1.2×10^5	8.0

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MultiHiggs production and EWSB

Osama Karkout,¹ Andreas Papaefstathiou,² Marieke Postma,^{1,3} Gilberto Tetlalmatzi-Xolocotzi,^{4,5} Jorinde van de Vis,⁶ Tristan du Pree¹

https://arxiv.org/pdf/2404.12425



The one-loop TRSM effective potential at finite temperature is:

$$V_T(\phi_i, T) = V(\phi_i) + V_{CW}(\phi_i) + V_{c.t.}(\phi_i) + V_{T,1-loop}(\phi_i, T),$$

with ϕ_i the field values defined in eq. (2.2) (with $\phi_i = v_i$ in the vacuum today). $V(\phi_i)$ is the tree-level potential of eq. (2.1), $V_{\rm CW}$ the standard zero-temperature one-loop 'Coleman-Weinberg' potential and $V_{\rm c.t.}$ the corresponding counterterms. The temperature-corrections are captured by $V_{T, 1-\text{loop}}$, which is given by

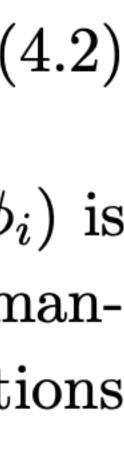
$$V_{T,1-\text{loop}}(\phi,T) = \frac{T^4}{2\pi^2} \left[\sum_{\alpha=\Phi_i,W,Z} n_\alpha J_B[m_\alpha^2(\phi_i)/T^2] + n_t J_F[m_t^2(\phi_i)/T^2] \right]$$

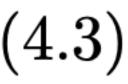


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At temperatures large compared to the $m_{lpha}^2(\phi_i)/T^2$ as

$$J_B(m_{\alpha}^2/T^2) = -\frac{\pi^4}{45} + \frac{\pi^2}{24}\frac{m_{\alpha}^2}{T^2} - \frac{\pi}{6}\frac{m_{\alpha}^3}{T^3} - \frac{1}{32}\frac{m_{\alpha}^4}{T^4} \left(\log\frac{m_{\alpha}^2}{16\pi^2 T^2} - \frac{3}{2} + 2\gamma_E\right) \cdots,$$

$$J_F(m_{\alpha}^2/T^2) = \frac{7\pi^4}{360} - \frac{\pi^2}{24}\frac{m_{\alpha}^2}{T^2} - \frac{1}{32}\frac{m_{\alpha}^4}{T^4} \left(\log\frac{m_{\alpha}^2}{\pi^2 T^2} - \frac{3}{2} + 2\gamma_E\right) \cdots,$$



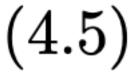
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At temperatures large compared to the mass, the functions $J_{B,F}$ can be expanded in

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RGEs $\mathbf{A.3}$

The one-loop RGEs for the quartic couplings are

$$\begin{split} (4\pi)^2 \beta_{\lambda_{11}} &= 24\lambda_{11}^2 + \frac{\lambda_{22}^2}{2} + \frac{\lambda_{33}^2}{2} + \frac{3}{8}g_1^4 + \frac{9}{8}g_2^4 + \frac{3}{4}g_1^2g_2^2 - 6y_t^4 - 4\lambda_{11}\gamma_{\Phi_1}, \\ (4\pi)^2 \beta_{\lambda_{22}} &= 18\lambda_{22}^2 + 2\lambda_{12}^2 + \frac{\lambda_{23}^2}{2}, \\ (4\pi)^2 \beta_{\lambda_{33}} &= 18\lambda_{33}^2 + 2\lambda_{13}^2 + \frac{\lambda_{23}^2}{2}, \\ (4\pi)^2 \beta_{\lambda_{12}} &= 4\lambda_{12}^2 + 12\lambda_{12}\lambda_{11} + 6\lambda_{12}\lambda_{22} + \lambda_{13}\lambda_{23} - 2\lambda_{12}\gamma_{\Phi_1}, \\ (4\pi)^2 \beta_{\lambda_{13}} &= 4\lambda_{13}^2 + 12\lambda_{13}\lambda_{11} + 6\lambda_{13}\lambda_{33} + \lambda_{12}\lambda_{23} - 2\lambda_{13}\gamma_{\Phi_1}, \\ (4\pi)^2 \beta_{\lambda_{23}} &= 4\lambda_{23}^2 + 6\lambda_{23}\lambda_{22} + 6\lambda_{23}\lambda_{33} + 4\lambda_{12}\lambda_{13}, \end{split}$$
(A.5)

with $\beta_{\lambda} = \mu \partial \lambda / \partial \mu$ and $\gamma_{\Phi_1} = \left(\frac{3g_1^2}{4} + \frac{9g_2^2}{4} - 3y_t^2\right)$. The running of the gauge couplings and the top quark is as in the SM

 $(4\pi)^2 \beta_{g_i} = b_i g_i$ $(4\pi)^2 \beta_{y_t} = \frac{9}{2} g_i$

with $b_i = (41/6, -19/6, -7)$ for i = 1, 2, 3.

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$$g_i^3,$$

 $y_t^3 - y_t(rac{2}{3}g_1^2 + 9g_3^2) - y_t\gamma_{\Phi_1},$ (A.6)



How to enhance HHH

$$\mathcal{L} = -\bar{\lambda}_{abc}h_ah_bh_c - \frac{1}{2}\bar{\lambda}_{aab}h_a^2h_b - \frac{1}{3!}\bar{\lambda}_{aaab}h_a^3h_b + \dots , \qquad (2.5)$$

with

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$$\bar{\lambda}_{abc} = (M_a^2 + M_b^2 + M_c^2) \sum_j \frac{R_{aj} R_{bj} R_{cj}}{v_j},$$

$$\bar{\lambda}_{aaab} = (3!) \sum_{ijk} \frac{M_k^2}{v_i v_j} R_{ki}$$

and R the mixing matrix of eq. (A.3). T (up to symmetry factors)

$$\mathcal{A}_1 \sim (\mathcal{A}_{pp \to h_1}^{\mathrm{SM}} \kappa_3) \times \frac{\overline{\lambda}_{321} \overline{\lambda}_{211}}{D_3(p) D_2(p')},$$

The inverse propagators are $D_a(p) = p^2 - M_a^2 + iM_a\Gamma_a$, with p the momentum flowing through the propagator, and Γ_a the decay width of h_a . On resonance, we have $|p^2 - M_a^2| \ll |M_a\Gamma_a|$.

MultiHiggs production and EWSB

$$R_{kj}(R_{ai}^2 R_{aj} R_{bj} + R_{ai} R_{bi} R_{aj}^2), \qquad (2.6)$$

and R the mixing matrix of eq. (A.3). The tree-level amplitudes can then be written as

$$\mathcal{A}_{2}^{(a)} \sim (\mathcal{A}_{pp \to h_{1}}^{\text{SM}} \kappa_{a}) \times \frac{\lambda_{a111}}{D_{a}(p)}.$$
 (2.7)

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Baryogenesis (matter-antimatter asymmetry)

Sakharov is mostly known for his political activism for individual freedom, human rights, civil liberties



MultiHiggs production and EWSB





