

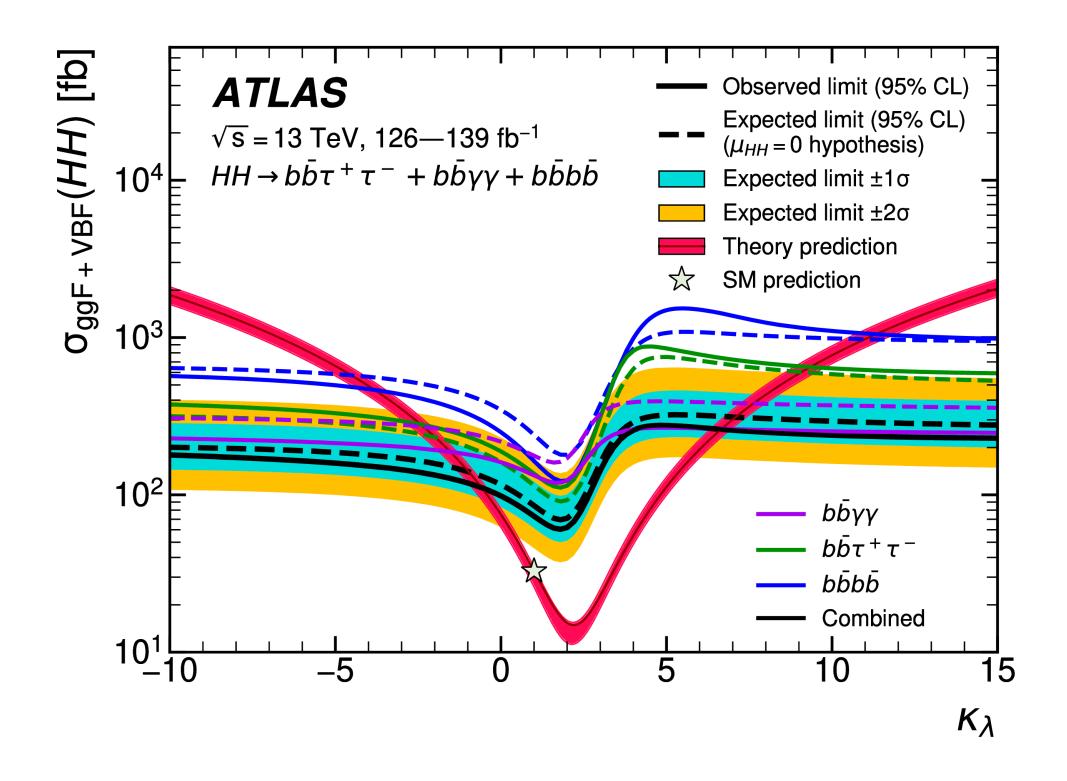
# Higgs Symmetry Breaking and HHH at LHC

### Osama Karkout

Working with Jorinde van de Vis, Marieke Postma, Andreas Papaefstathiou, Gilberto Tetlalmatzi, Tristan du Pree



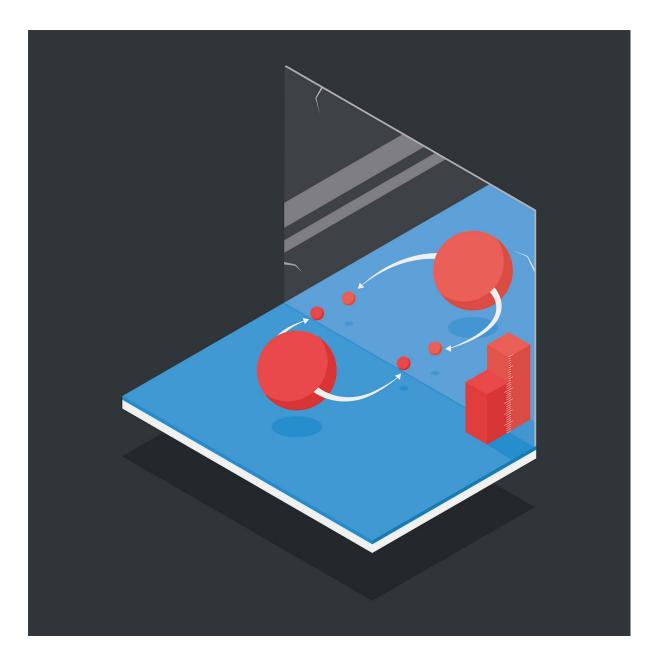
## Project: ATLAS Higgs results $\rightarrow$ matter-antimatter asymmetry



Nik hef Mul

MultiHiggs production and EWSB

?



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### matter-antimatter asymmetry

### Cosmic rays: $\bar{p}/p = 10^{-4}$ = no ambient antiprotons ( $\bar{p}$ )

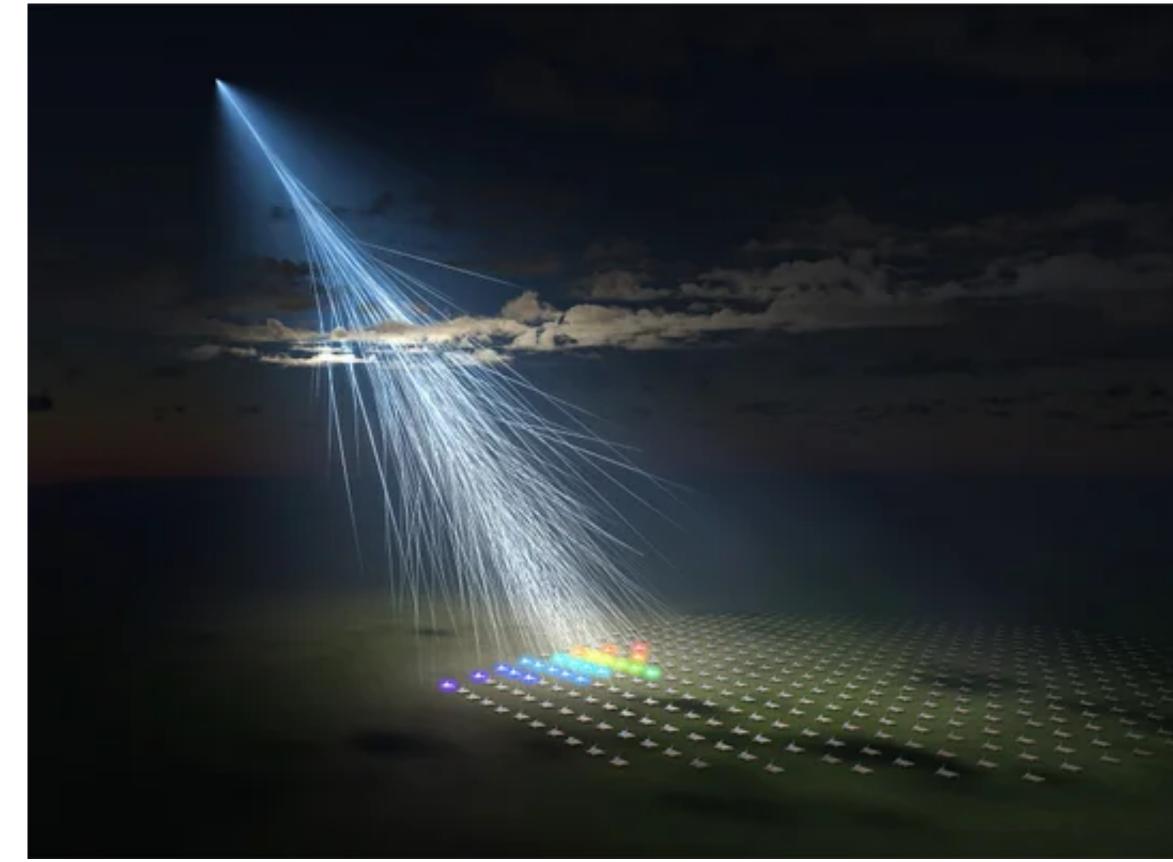
#### **BIG DEAL!**

Lorentz invariance + Hermitian Hamiltonian (physical observables are real) = matter-antimatter symmetry (CPT) is conserved!

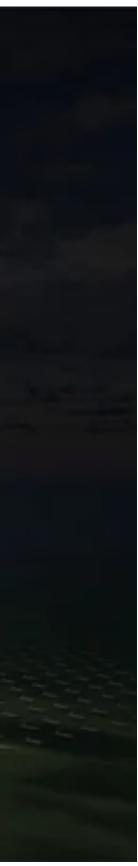
True in SM and any BSM!!!!



MultiHiggs production and EWSB



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# Baryogenesis (matter-antimatter asymmetry)

Problem: we exist :(

(CPT) is conserved => need for **dynamical** mechanism to generate matter-antimatter asymmetry.

Sakharov conditions:

- Baryon number violation
- Loss of thermal equilibrium
- Break C and CP symmetries

In SM: all related to the Higgs field

https://arxiv.org/pdf/hep-ph/0609145.pdf

https://arxiv.org/pdf/2301.05197.pdf http://www.laine.itp.unibe.ch/cosmology/lec09.pdf BARYOGENESIS

James M. Cline



MultiHiggs production and EWSB



Osama Karkout



#### **Baryon number violation**

In SM: left handed B+L violated!



MultiHiggs production and EWSB

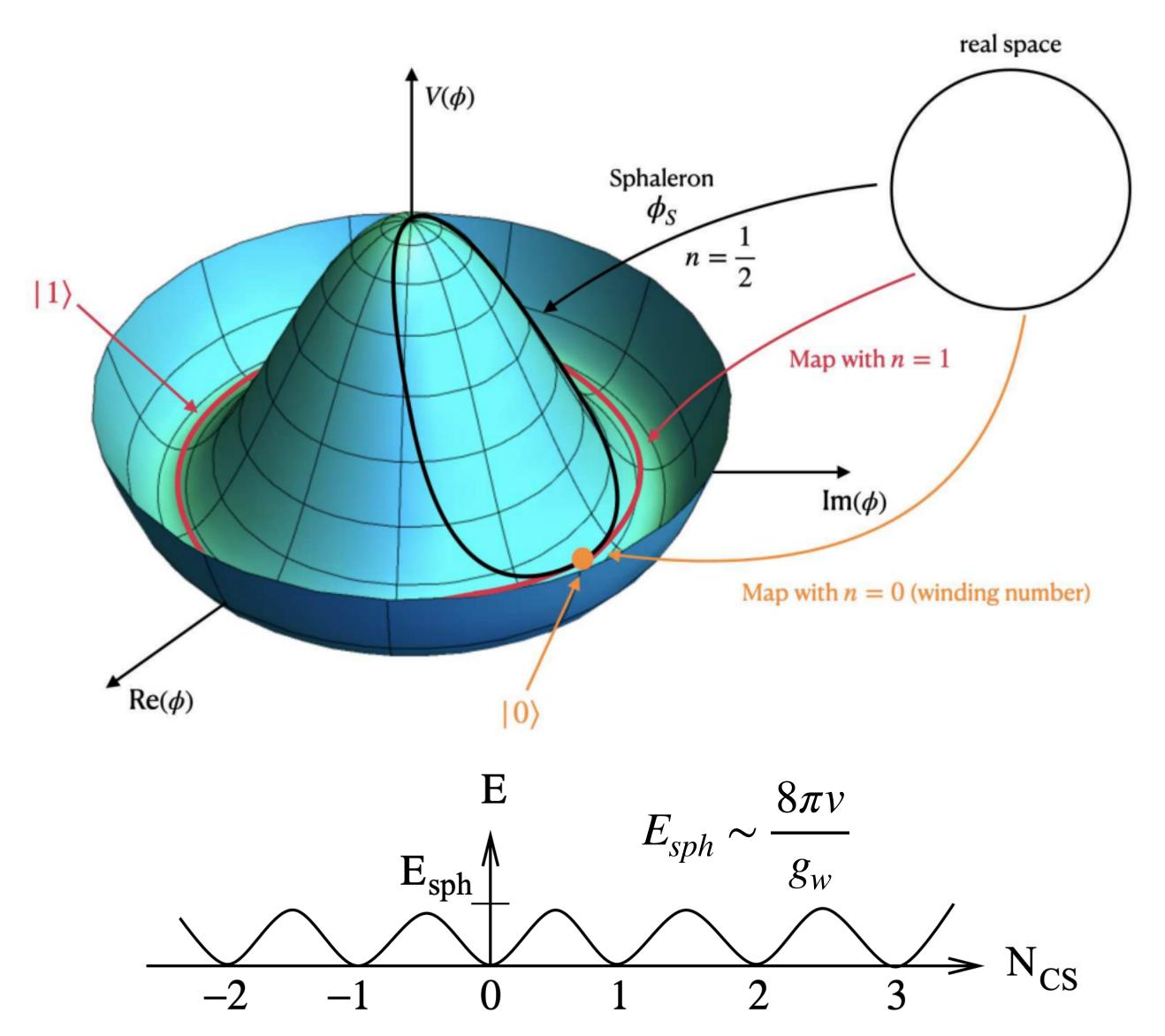


Fig. 8. Energy of gauge field configurations as a function of Chern-Simons number.

*v* is the Higgs VEV

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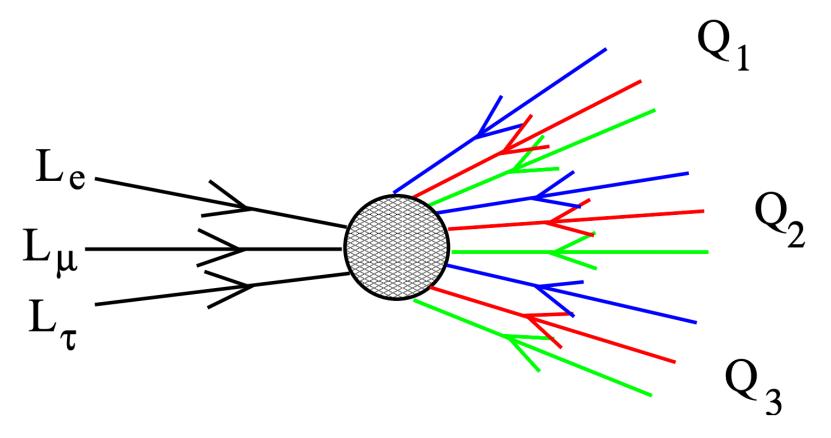
#### **Baryon number violation**

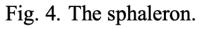
In SM: left handed B+L violated!

$$\partial_{\mu}J^{\mu}_{B_{L}+L_{L}} = \frac{3g^{2}}{32\pi^{2}}\epsilon_{\alpha\beta\gamma\delta}W^{\alpha\beta}_{a}W^{\gamma\delta}_{a}$$

where  $W_a^{\alpha\beta}$  is the SU(2) field strength.

$$\Delta B = \Delta L = \pm 3 \tag{2.2}$$







#### MultiHiggs production and EWSB

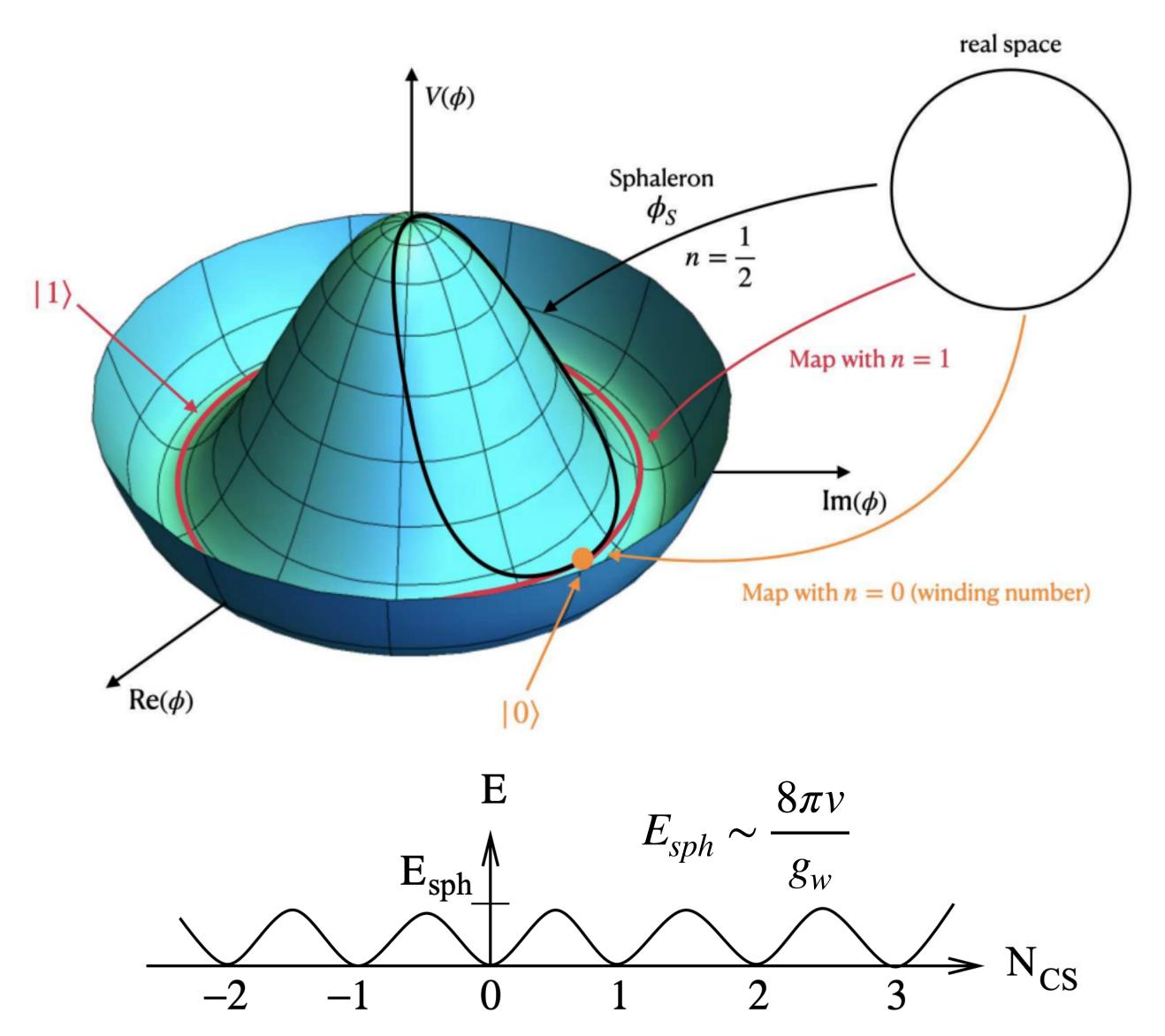


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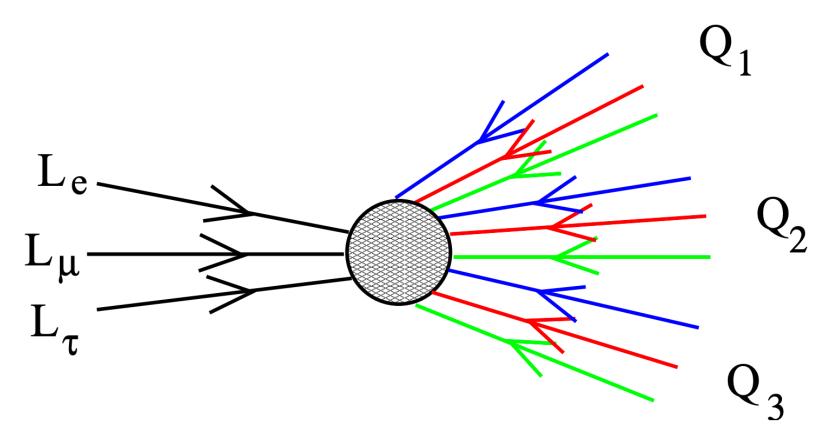
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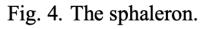
Rate of tunnelling to another vacuum:

$$\Gamma_{sph}(T) \sim e^{-E_{sph}/T} \sim e^{-v/T}$$

 $\Delta B = \Delta L = \pm 3$ 

(2.2)







#### MultiHiggs production and EWSB

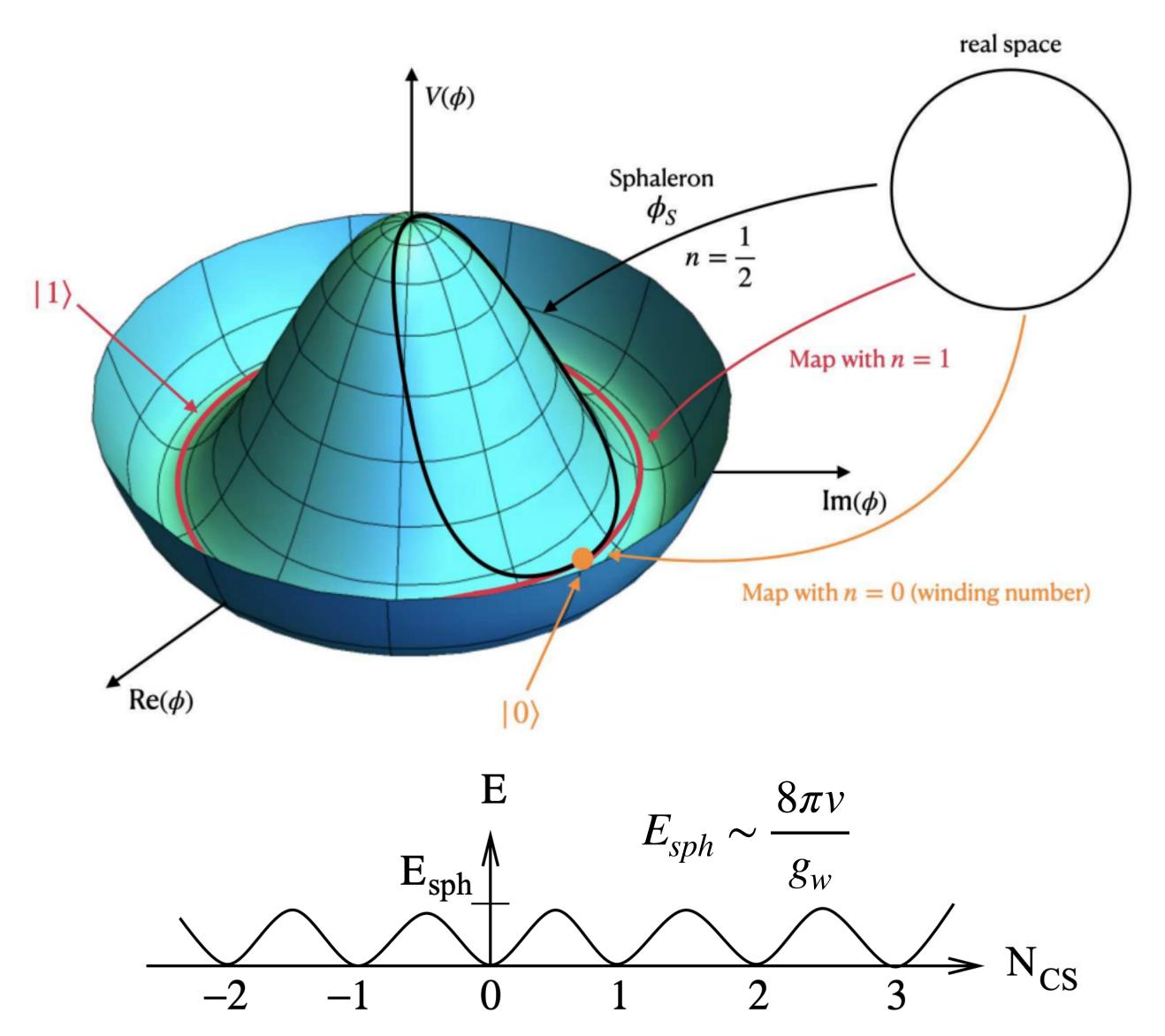


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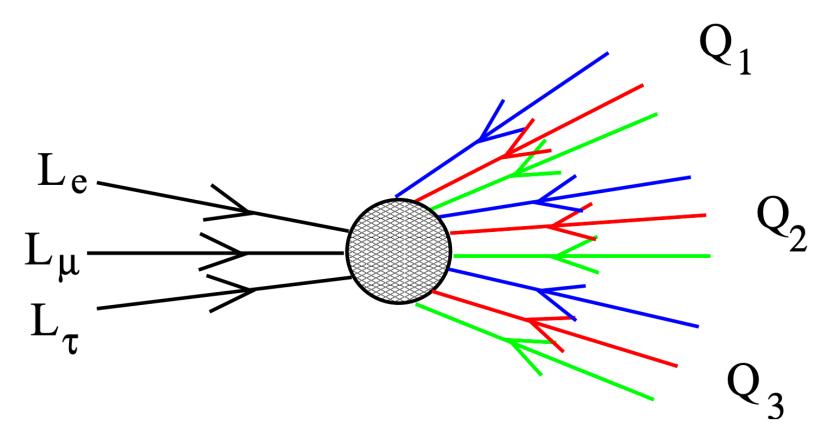
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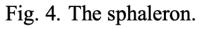
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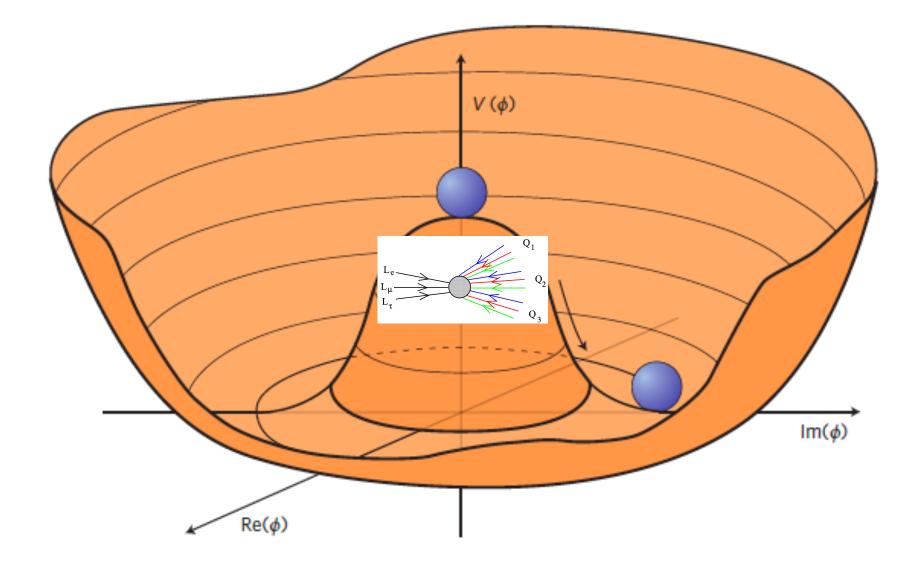
(2.2)







#### MultiHiggs production and EWSB



If EW symmetry is restored (VEV=0) Sphalerons everywhere!

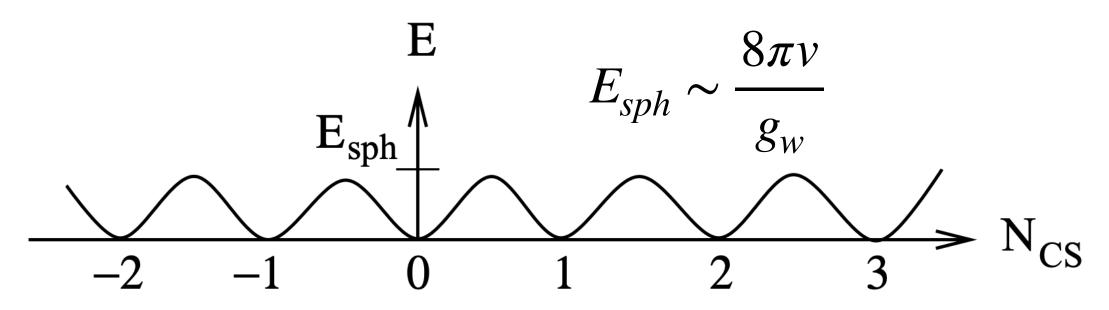


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*v* is the Higgs VEV

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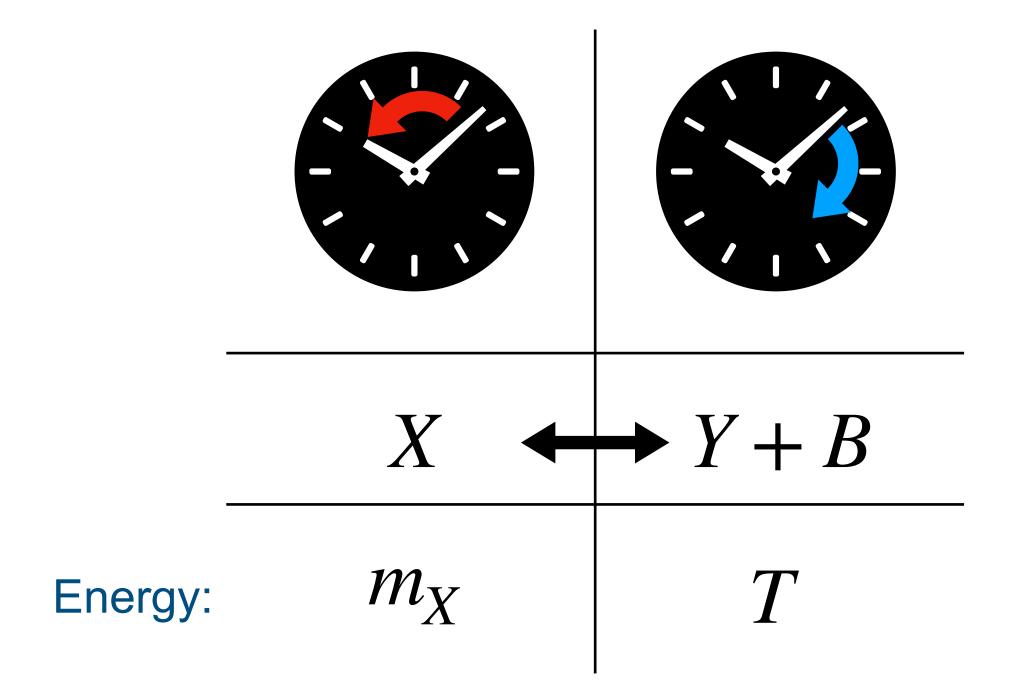
#### Out of thermal equilibrium

In thermal equilibrium: any process that generates some extra B  $X \rightarrow Y + B$ comes with the inverse process at the same rate  $Y + B \rightarrow X$ 

Out of thermal equilibrium if for example  $T < m_X$  $Y + B \rightarrow X$  surpassed by  $e^{-m_X/T}$ 



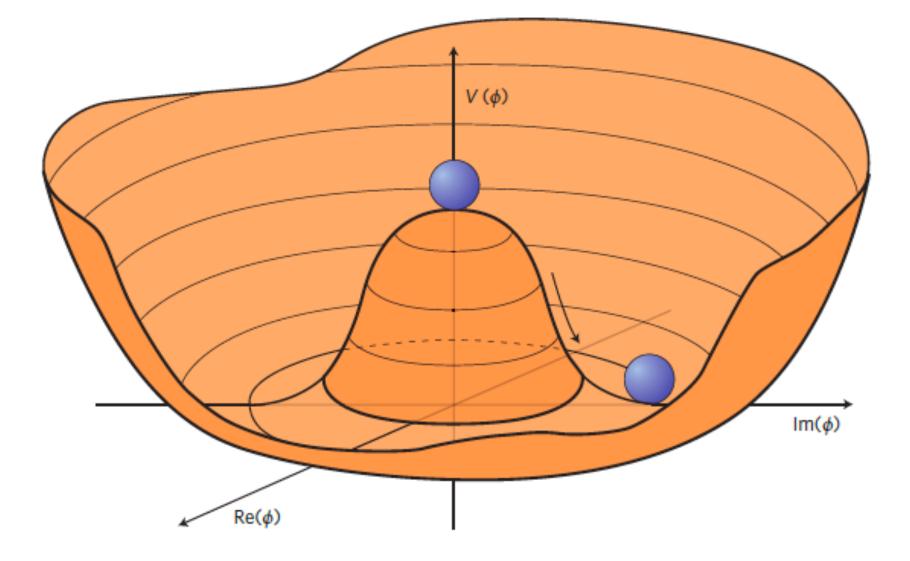
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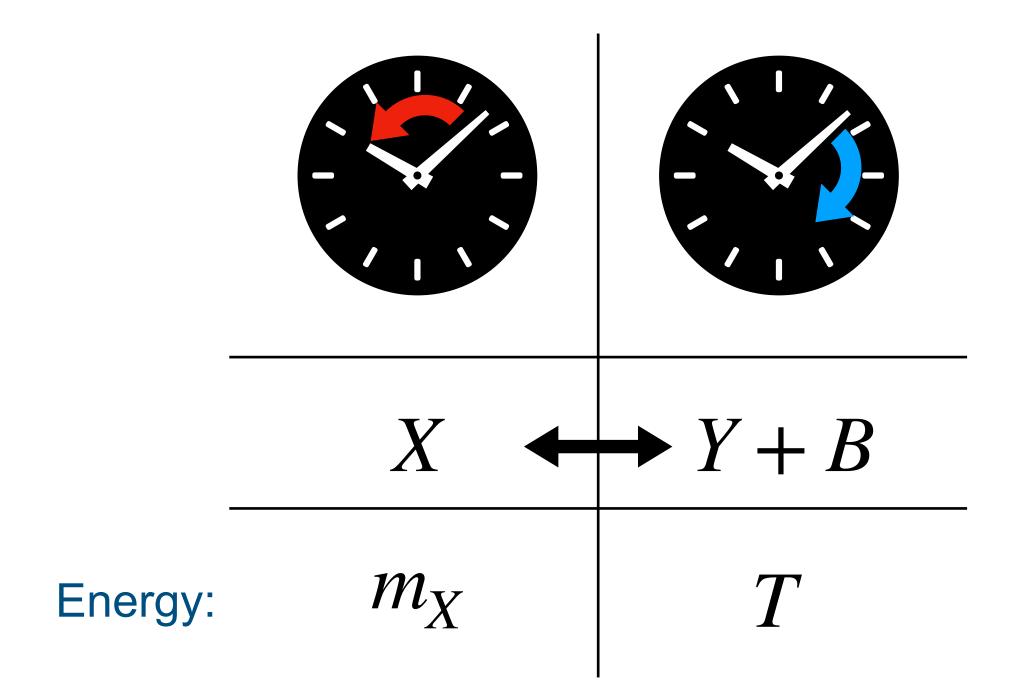
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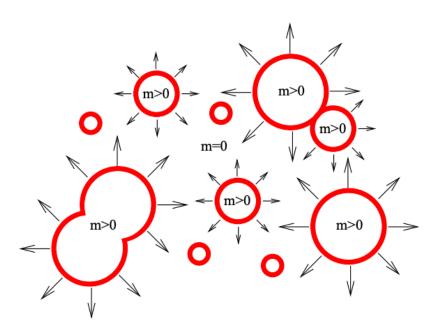


Electroweak symmetry breaking (EWSB) is a phase transition! It can cause loss of thermal equilibrium if it is a First Order Phase Transition (FOPT)



MultiHiggs production and EWSB





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Charge and Charge+Parity symmetries (C and CP violation)

Under C conservation:  $X \to Y + B$  comes with  $\bar{X} \to \bar{Y} + \bar{B}$ 

 $\Gamma(\bar{X} \to \bar{Y} + \bar{B}) = \Gamma$ 

The net rate of baryon production goes like the difference of these rates,

$$\frac{dB}{dt} \propto \Gamma(\bar{X} \to \bar{Y} + t)$$

CP violation is a longer story but also needed



MultiHiggs production and EWSB

 $\begin{array}{cc} C: & q_L \to \bar{q}_L \\ CP: & q_L \to \bar{q}_R \end{array}$ 

$$(X \to Y + B)$$

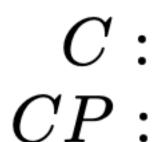
 $\bar{B}$ ) –  $\Gamma(X \to Y + B)$ 

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**Charge and Charge+Parity symmetries (C and CP violation)** 



In SM: CP violation in CKM matrix. Not enough though! BSM CP violation is more than welcomed.

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} c_1 & | -s_1c_3 & | -s_1s_3 \\ \hline s_1c_2 & | & c_1c_2c_3 & | & c_1c_2s_3 \\ \hline s_1s_2 & | & -s_2s_3e^{i\delta} & | & +s_2c_3e^{i\delta} \\ \hline s_1s_2 & | & c_1s_2c_3 & | & c_2s_2s_3 \\ \hline s_1s_2 & | & -c_2c_3e^{i\delta} & | & -c_2c_3e^{i\delta} \end{pmatrix}$$



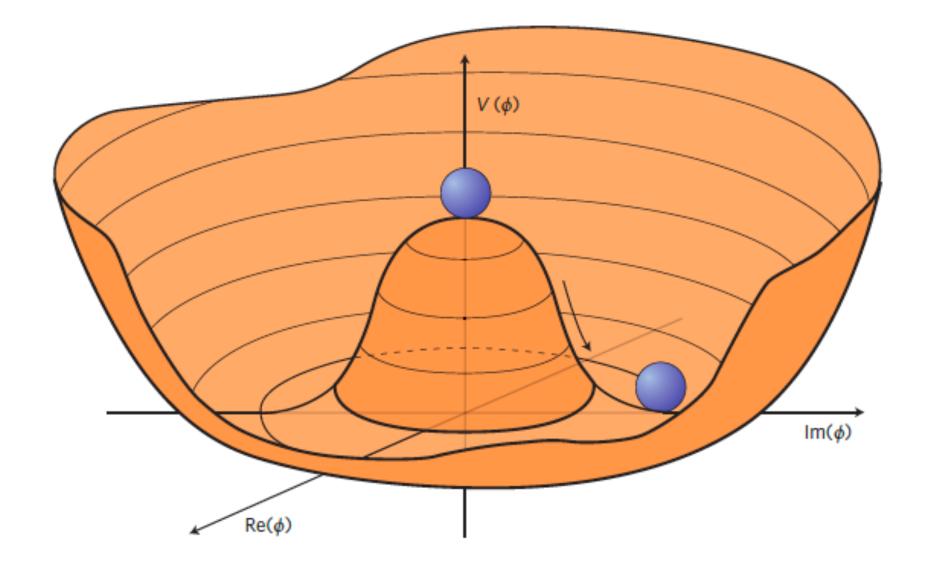
MultiHiggs production and EWSB

$$\begin{array}{l} q_L \to \bar{q}_L \\ q_L \to \bar{q}_R \end{array}$$

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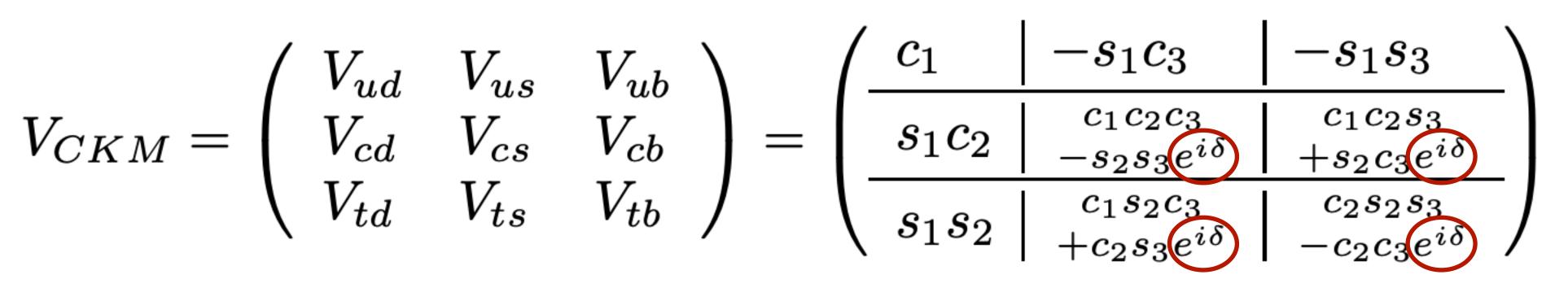


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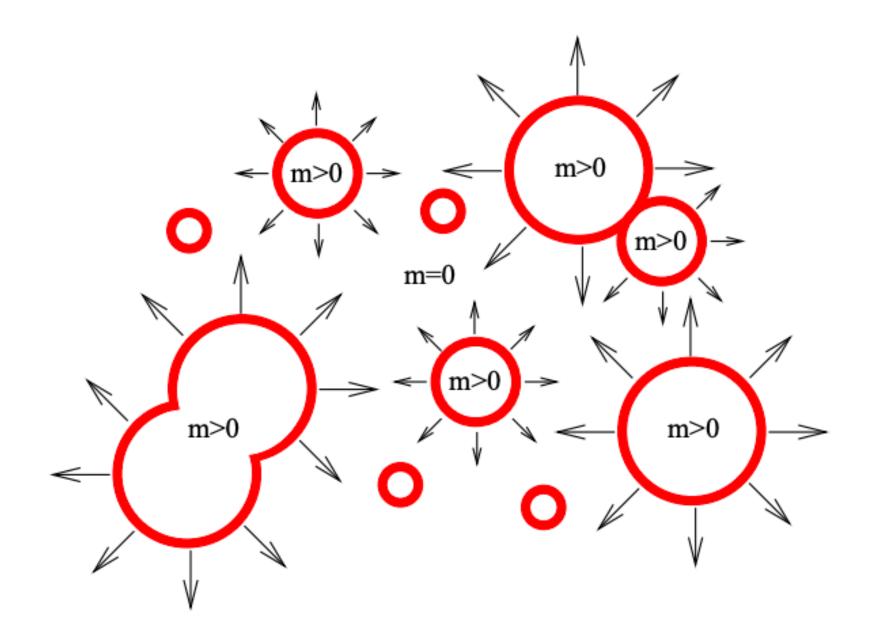


MultiHiggs production and EWSB



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First Order Phase Transition (FOPT)



MultiHiggs production and EWSB

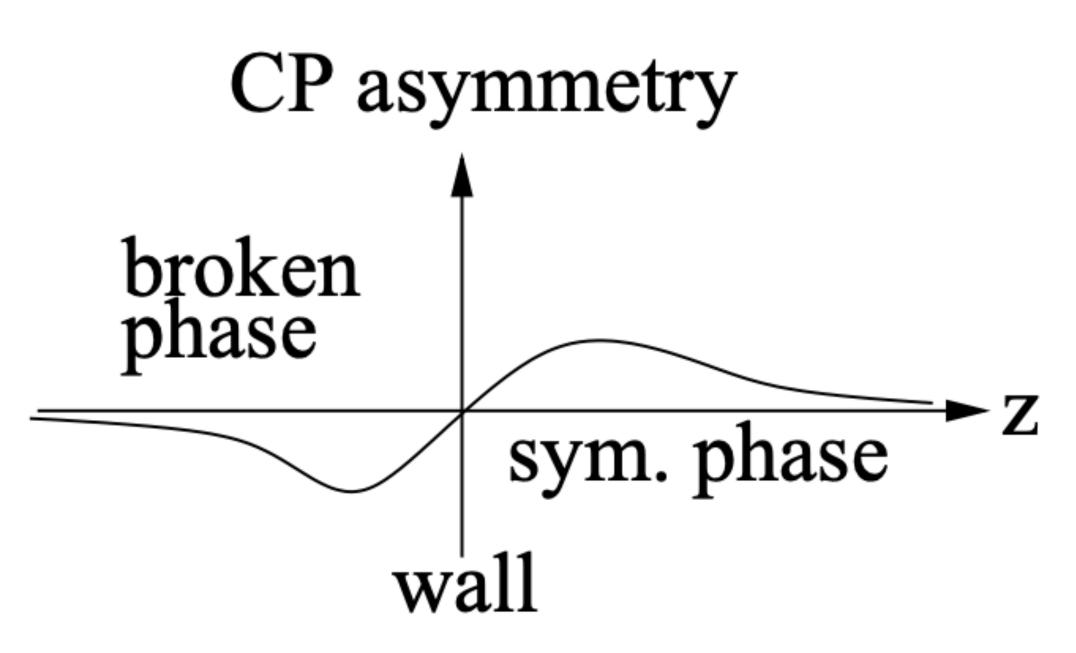
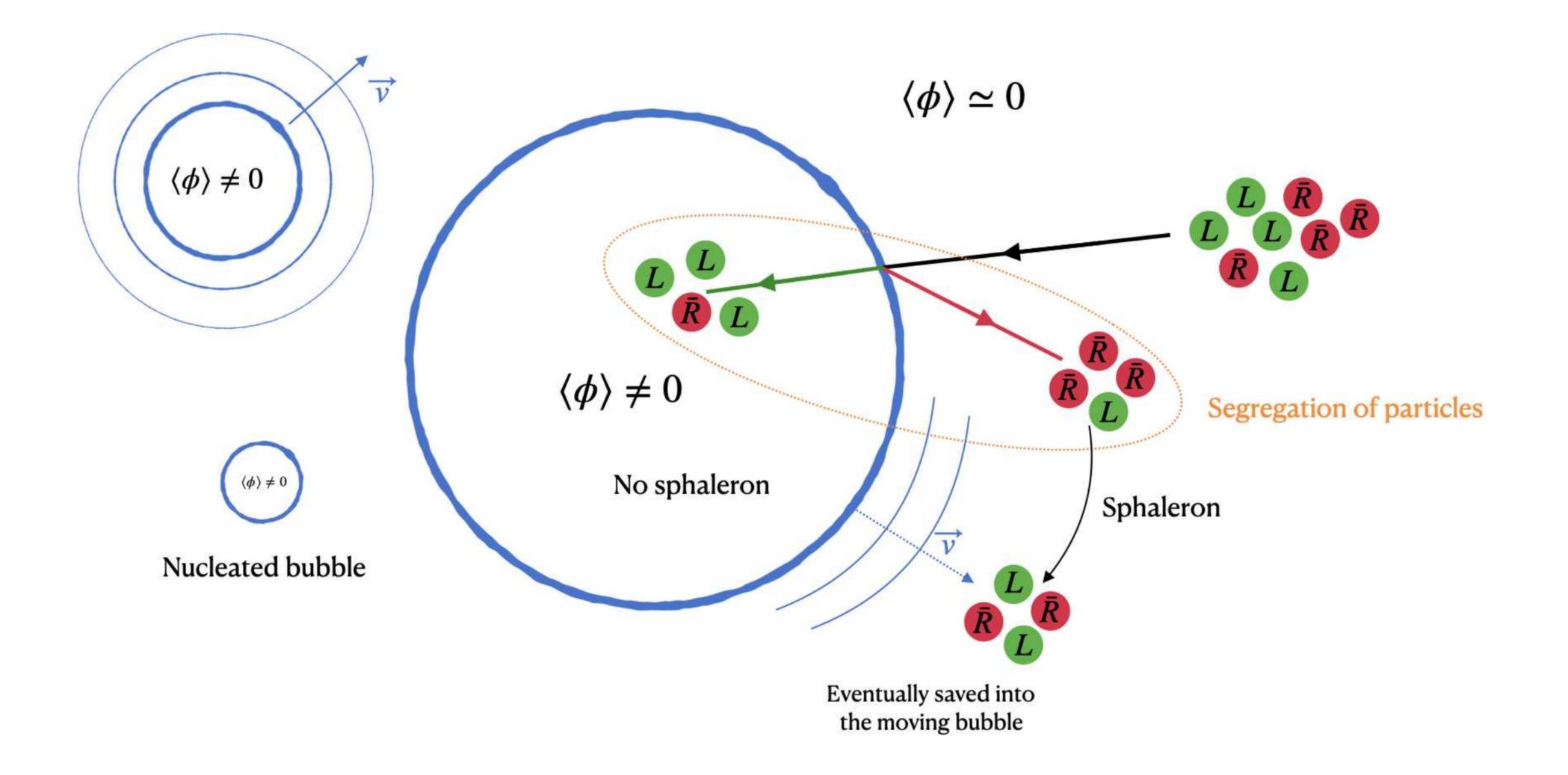


Fig. 13. The CP asymmetry which develops near the bubble wall.

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MultiHiggs production and EWSB

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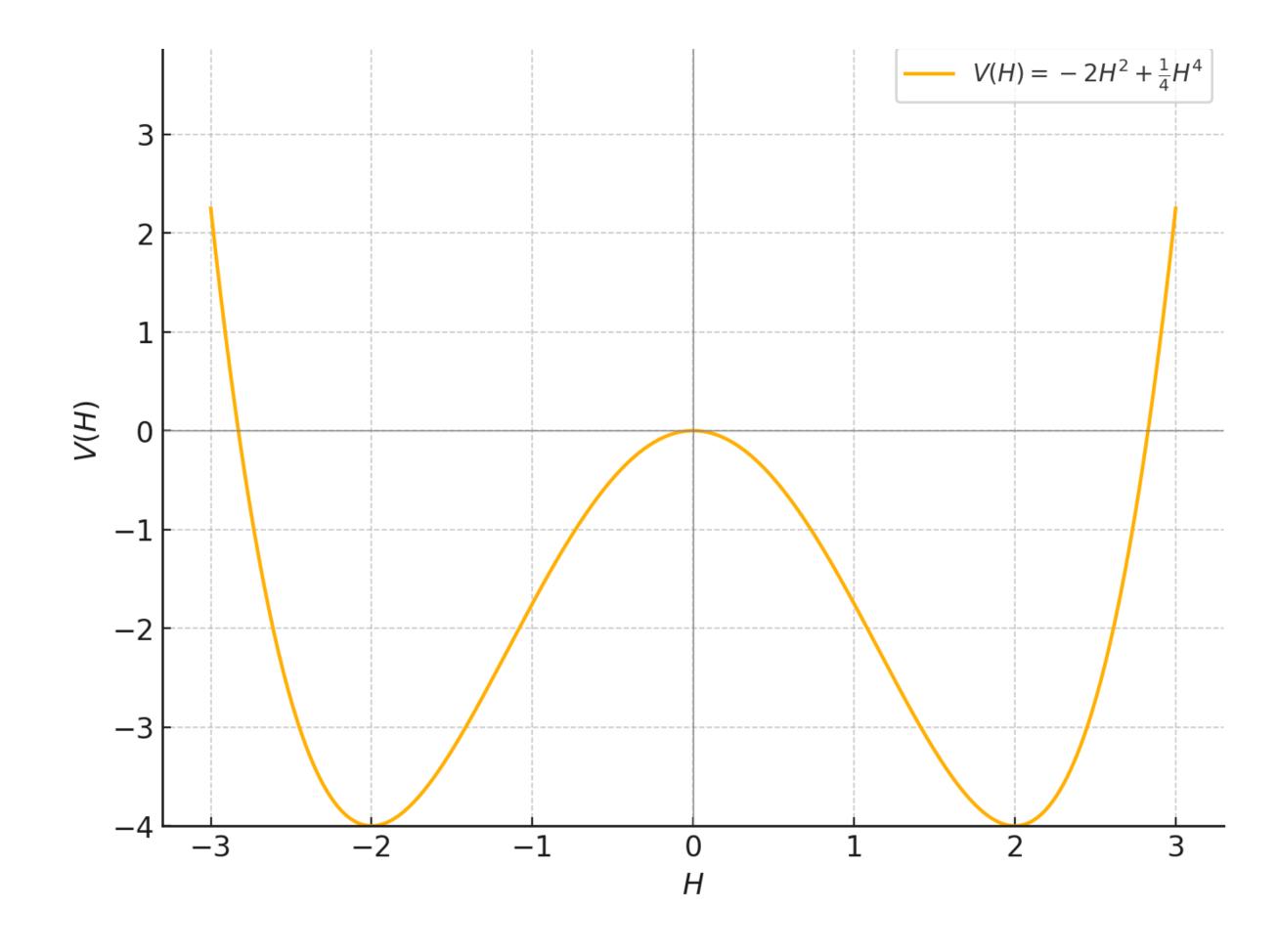


Before symmetry breaking, Higgs potential is:

$$V(H) = -\frac{1}{2}\mu^2 H^2 + \frac{1}{4}\lambda H^4$$



MultiHiggs production and EWSB



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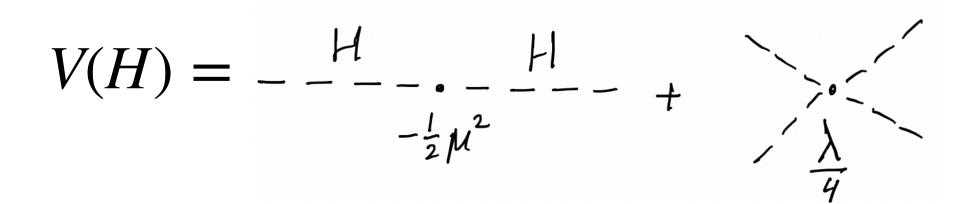




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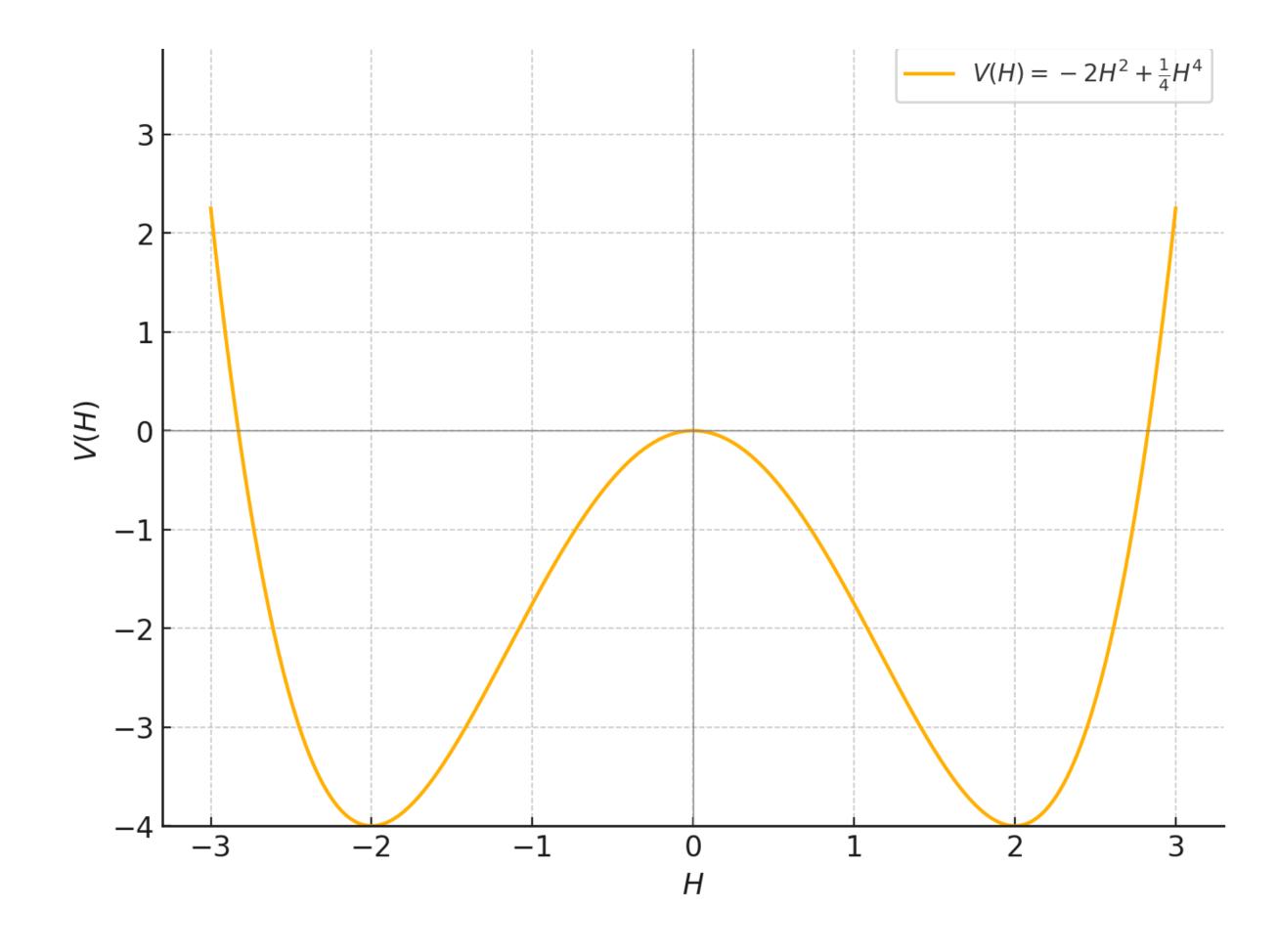
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In Feynman diagrams:





MultiHiggs production and EWSB



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Before symmetry breaking, Higgs potential is:

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In Feynman diagrams:

$$V(H) = - \frac{H}{-\frac{1}{2}\mu^2} + \frac{H}{\frac{1}{2}\mu^2} + \frac{1}{\frac{1}{4}\mu^2}$$

Higgs field is coupled to a thermal bath of fields. at LO, this looks like:

$$-\frac{H}{\sim T^2} - O_2 - \frac{H}{\sim T^2} - O_2$$

$$V_{eff}(H,T) = -\frac{1}{2}\mu^2 H^2 + \frac{1}{4}\lambda H^4 + \frac{\alpha}{2}T^2 H^2$$



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$$V(H) = -\frac{1}{2}\mu^2 H^2 + \frac{1}{4}\lambda H^4$$

In Feynman diagrams:

$$V(H) = -\frac{H}{-\frac{1}{2}\mu^2} + \frac{H}{-\frac{1}{2}\mu^2} + \frac{\lambda}{\frac{\lambda}{4}}$$

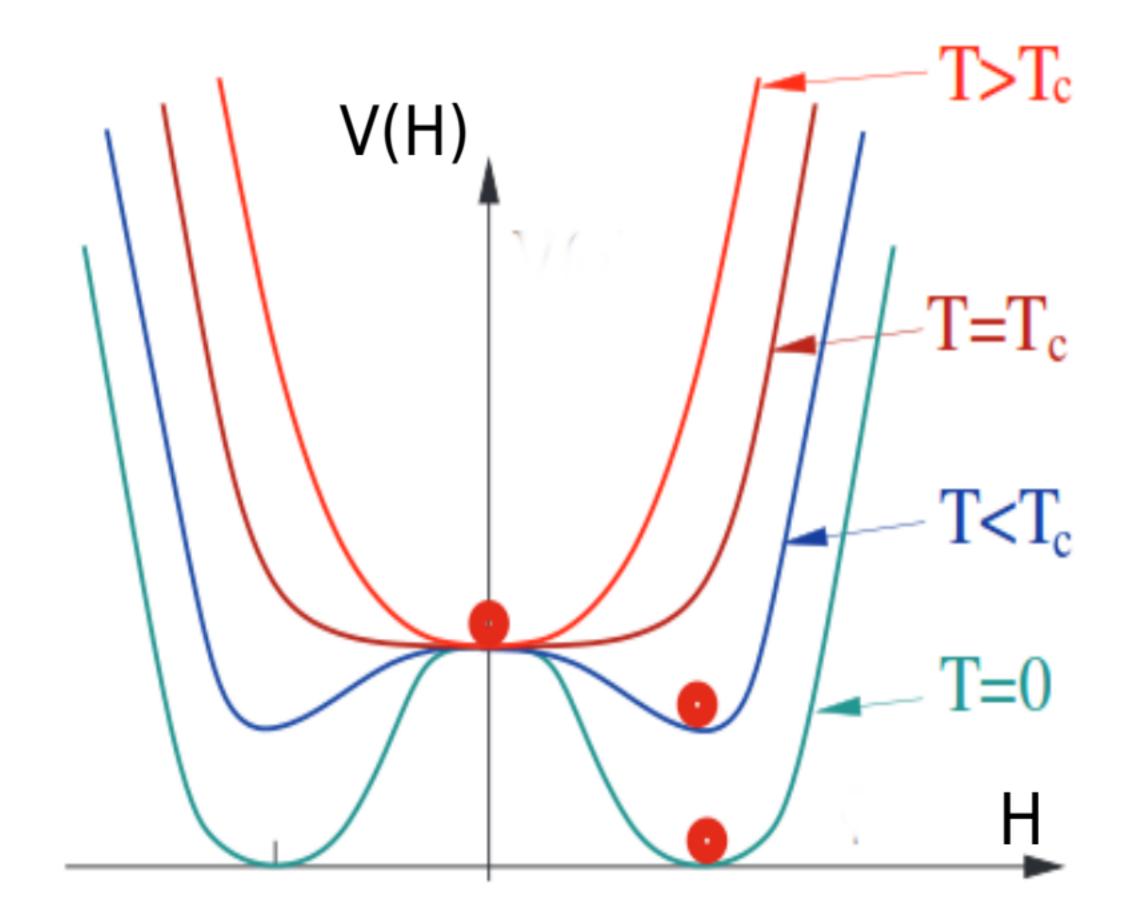
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## **Electroweak Phase Transition**

at NLO, the effective potential gets a cubic term  $V_{eff}(H,T) = \frac{1}{2}(-\mu^2 + \alpha T^2)H^2 - \beta T(-\mu^2 + \gamma H^2)^{3/2} + \frac{1}{4}\lambda H^4$ 

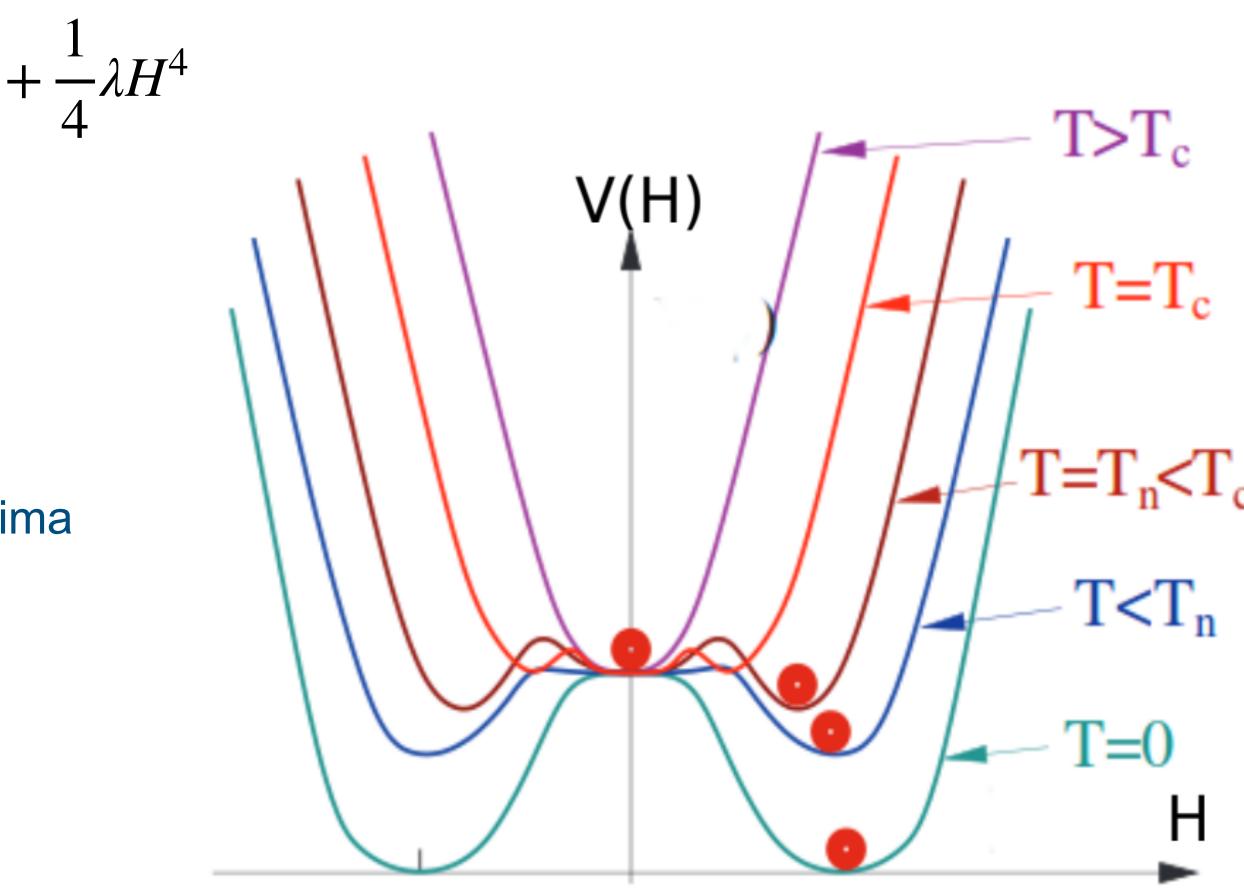
The values of  $(\alpha, \beta, \gamma)$  depend on your theory

If you're lucky, you can get a barrier between two minima at some critical temperature  $T_c$ 

Then at some random point in space, the VEV tunnels a bubble forms around it and expands!



MultiHiggs production and EWSB



 $T_n$  = temperature of bubble nucleation

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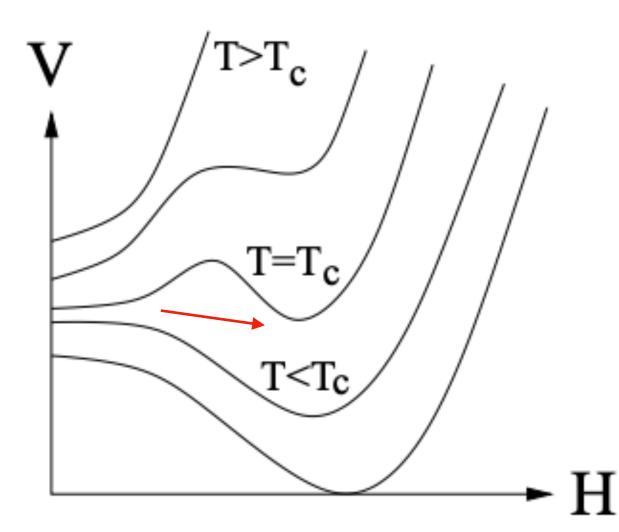




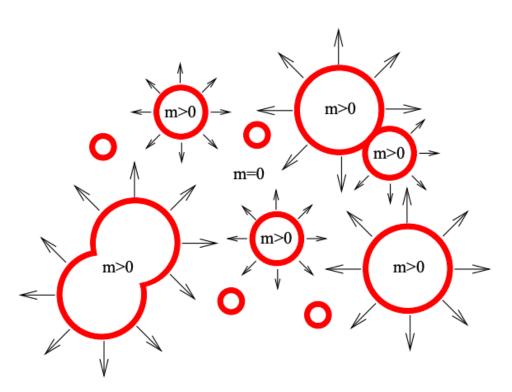


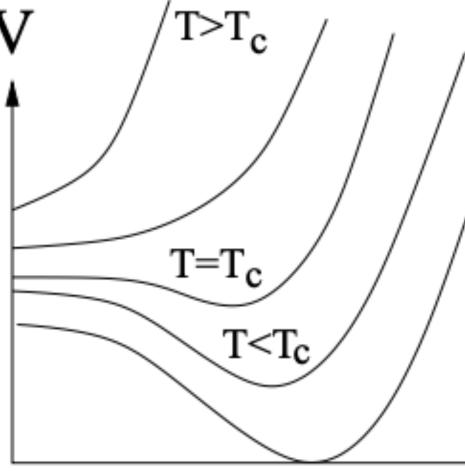


# **Electroweak Phase Transition**



first order phase transition FOPT





second order phase transition SOPT (or crossover)



MultiHiggs production and EWSB

 $V_{eff}(H,T) = \bigcirc + \{\bigcirc + \bigoplus \} + \dots$  $\sim \frac{1}{2}(-m^2 + \alpha T^2)H^2 - \beta TH^3 + \frac{1}{4}\lambda H^4$ 

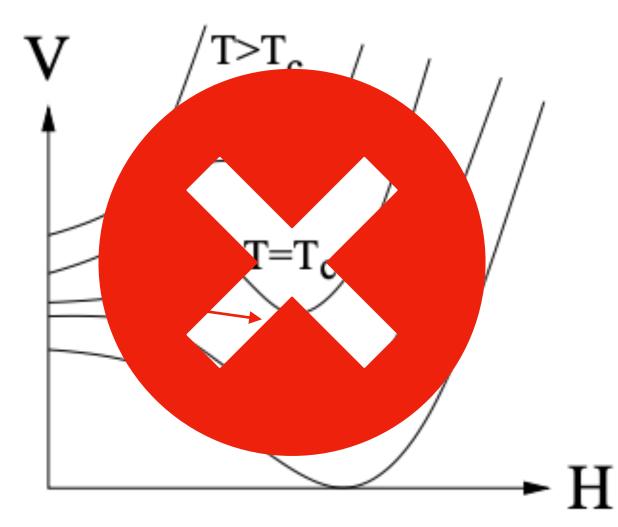
#### WE WANT TO BE FIRST!!!

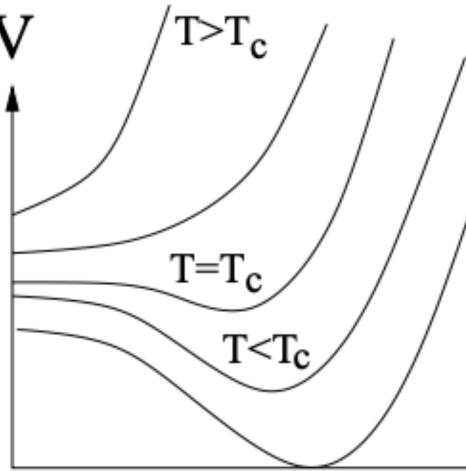


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# **Electroweak Phase Transition: SM**





second order phase transition SOPT (or crossover)

# No first order phase transition in SM

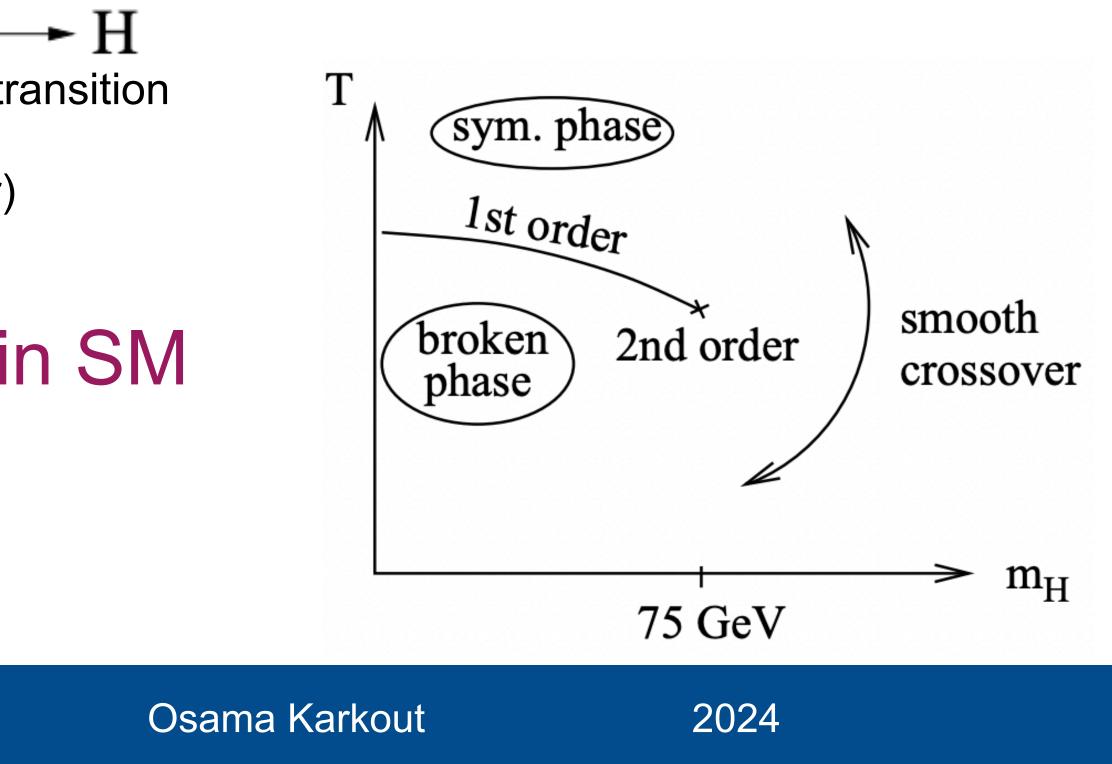


MultiHiggs production and EWSB

 $V_{eff}(H,T) = \bigcirc + \{\bigcirc + \bigoplus \} + \dots$  $\sim \frac{1}{2}(-m^2 + \alpha T^2)H^2 - \beta TH^3 + \frac{1}{4}\lambda H^4$ 

#### WE WANT TO BE FIRST!!!

But we're not...

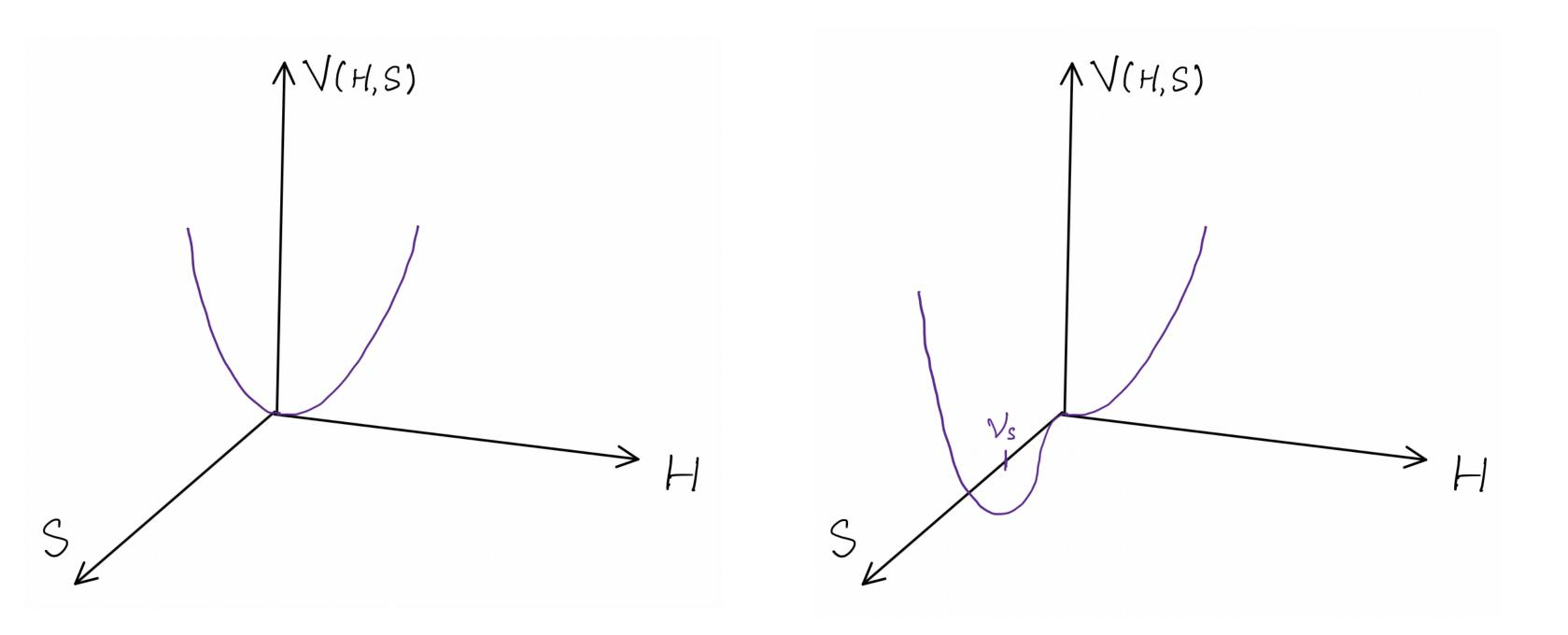




# **Electroweak Phase Transition: BSM**

Idea:

- 1. add a scalar field S which couples to the Higgs.
- 2. This scalar field also has a phase transition! Going to a VEV for S





#### MultiHiggs production and EWSB

 $V(H) = -\frac{1}{2}\mu^2 H^2 + \frac{1}{4}\lambda H^4 + V(H,S)$ 

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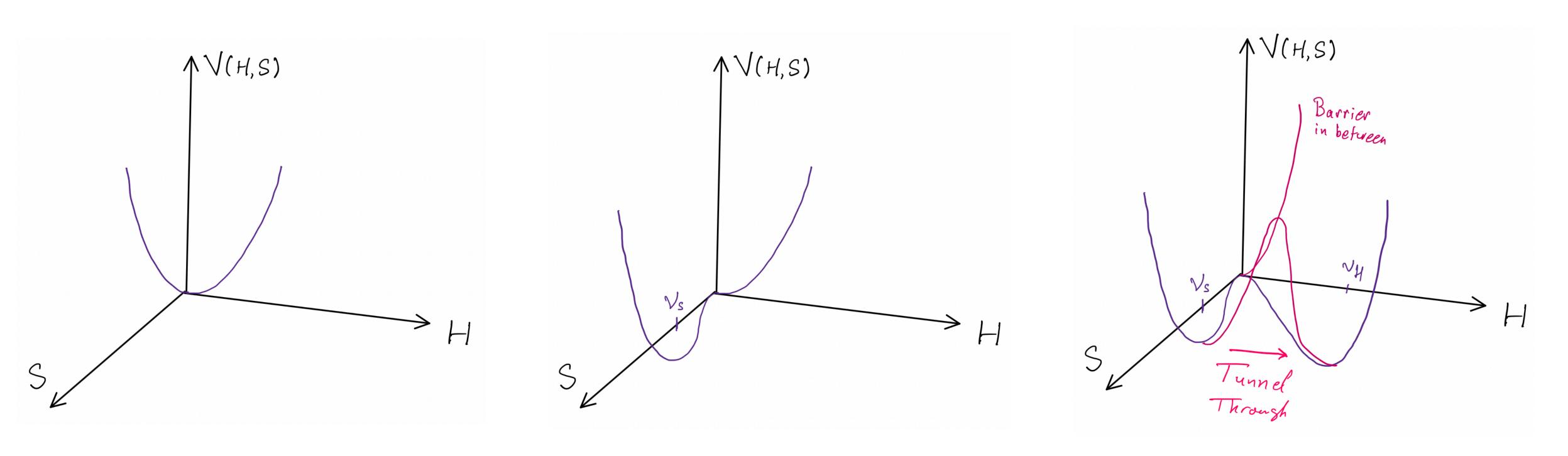




# **Electroweak Phase Transition: BSM**

Idea:

- 1. add a scalar field S which couples to the Higgs.
- 2. This scalar field also has a phase transition! Going to a VEV for S
- 3. Form a potential barrier between the VEV of S and the VEV of H
- 4. Tunnel to the VEV of H: This is FOPT





#### MultiHiggs production and EWSB

 $V(H) = -\frac{1}{2}\mu^2 H^2 + \frac{1}{4}\lambda H^4 + V(H,S)$ 

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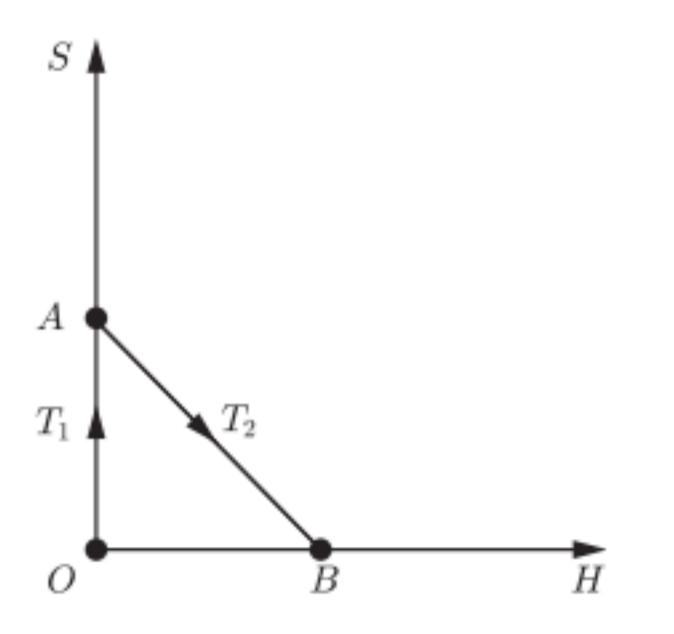


## **Electroweak Phase Transition: BSM**

Adding a scalar field can make a two-step FOPT!

$$V = -\frac{1}{2}\mu_h^2 h^2 + \frac{1}{4}\lambda_h h^4 + \frac{1}{2}\mu_s^2 s^2 + \frac{1}{4}\lambda_s s^4 + \frac{1}{4}\mu_m sh^2 + \frac{1}{4}\lambda_m s^2 h^2 + \mu_1^3 s + \frac{1}{4}\lambda_m s^2 h^2 + \frac{1}{4}$$

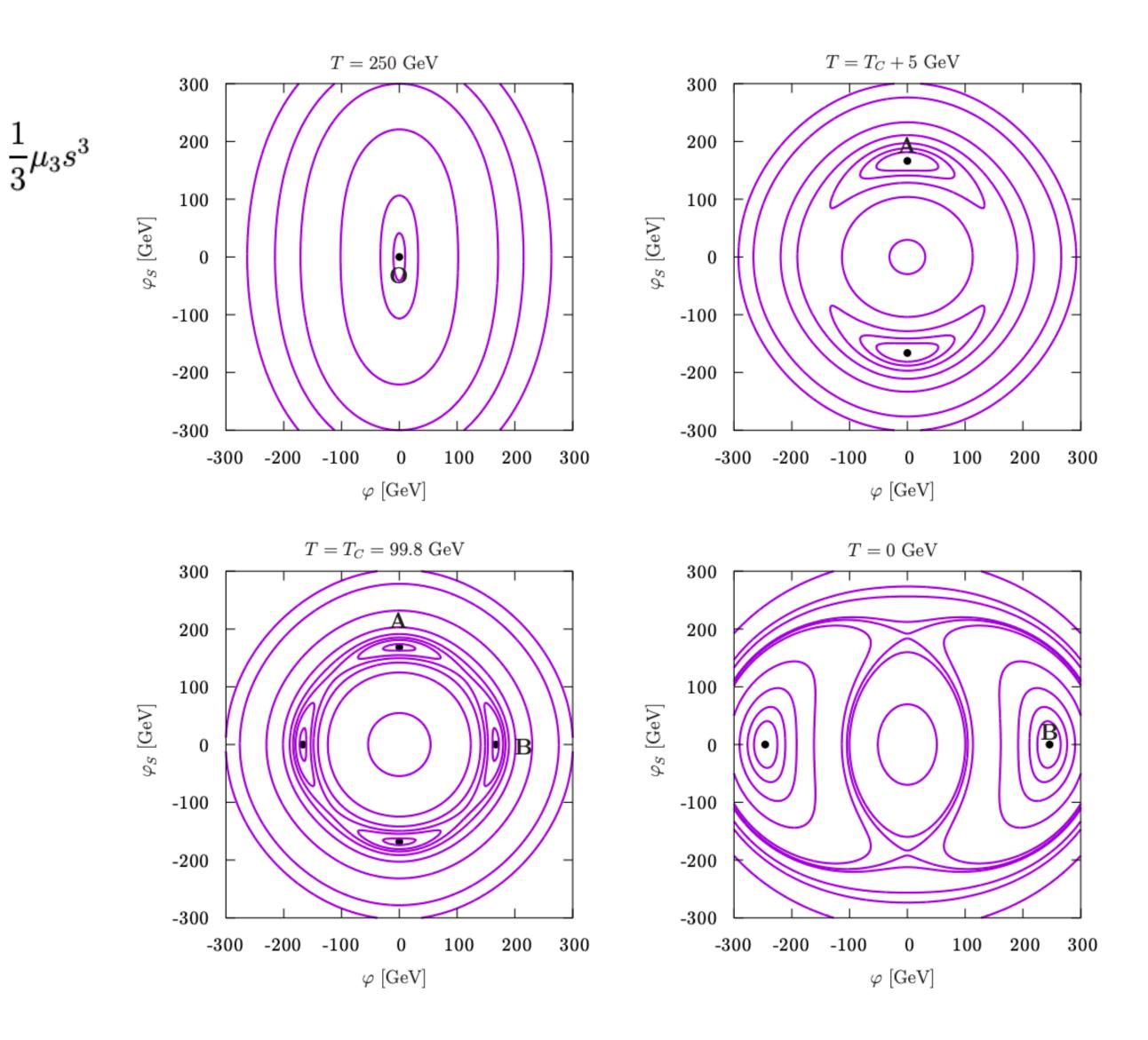
 $V^{\text{high-}T}(\varphi,\varphi_S;T) = V_0(\varphi,\varphi_S) + \frac{1}{2}(\Sigma_H \varphi^2 + \frac{1}{2}\Sigma_S \varphi_S^2)T^2$ 



Cheng-Wei Chiang,<sup>1,2,3,4,\*</sup> Michael J. Ramsey-Musolf,<sup>5,6,†</sup> and Eibun Senaha<sup>1,7,‡</sup>



#### MultiHiggs production and EWSB



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**ATLAS** Observed limit (95% CL) Expected limit (95% CL)  $\sqrt{s} = 13 \text{ TeV}, 126 - 139 \text{ fb}^{-1}$  $(\mu_{HH} = 0 \text{ hypothesis})$  $\sigma_{ggF+VBF}^{SM}(HH) = 32.7^{+2.1}_{-7.2}$  fb Expected limit  $\pm 1\sigma$ Expected limit ±20 Theory prediction Obs. Exp. 130 180 bbγγ  $b\bar{b}\tau^+\tau^-$ 140 110 bbbb 160 240 73 85 Combined-20 50 200 500 1000 2000 100  $\sigma_{ggF+VBF}(HH)$  [fb] HS > H

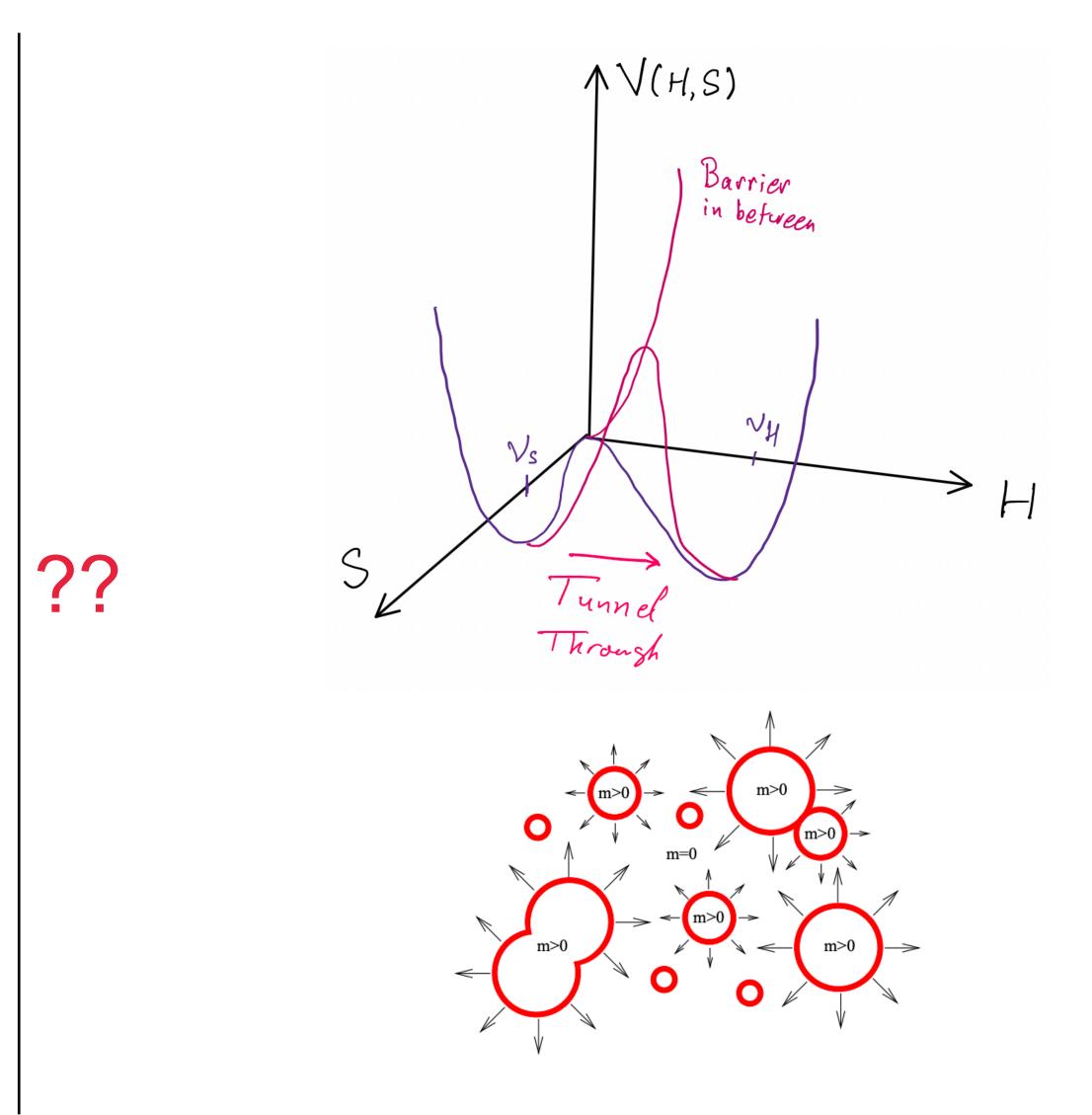
hef

Nik

explored for one added scalar, answer will come

MultiHiggs production and EWSB

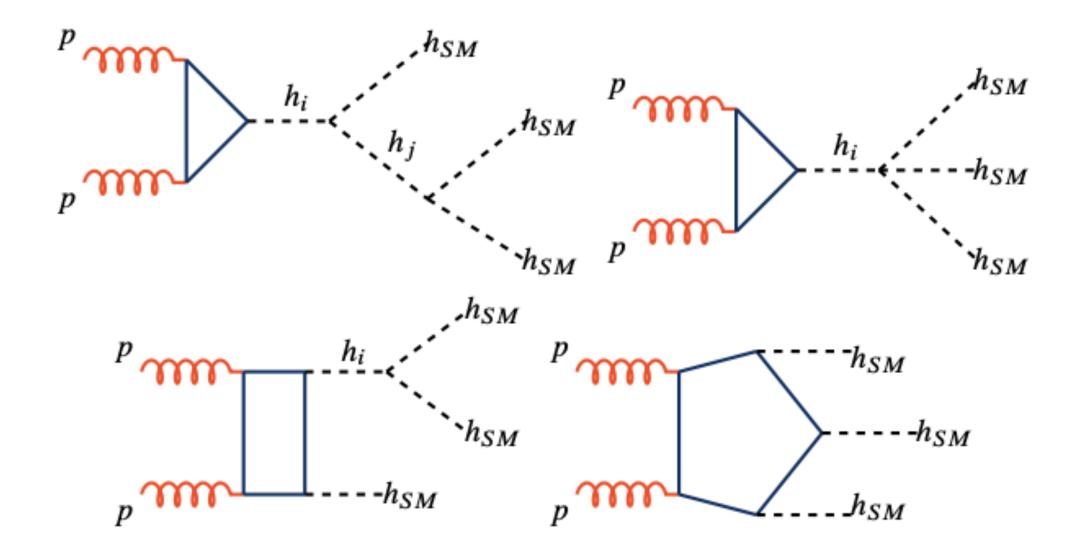
### ATLAS Higgs results $\rightarrow$ Higgs phase transition



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Maybe we will see enhancement of HHH production!

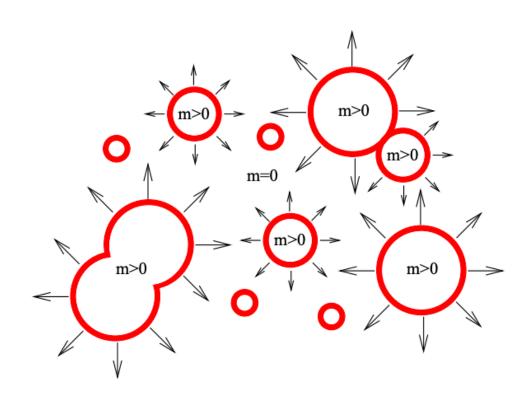




MultiHiggs production and EWSB

### ATLAS Higgs results $\rightarrow$ Higgs phase transition





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Simplified BSM model predicting large HHH: **TRSM**.

SM + two singlets coupling to the Higgs.

$$V = \mu_{\Phi}^2 \Phi^{\dagger} \Phi + \lambda_{\Phi} (\Phi^{\dagger} \Phi)^2 + \mu_S^2 S^2 + \lambda_S S^4 + \mu_X^2 X^2 + \lambda_X X^4 + \lambda_{\Phi S} \Phi^{\dagger} \Phi S^2 + \lambda_{\Phi X} \Phi^{\dagger} \Phi X^2 + \lambda_{SX} S^2 X^2 .$$



MultiHiggs production and EWSB

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Scalars get VEVs!  $\rightarrow$  Mixing:

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$$\Phi = \begin{pmatrix} 0\\ \frac{\phi_h + v}{\sqrt{2}} \end{pmatrix}, \quad S = \frac{\phi_S + v_S}{\sqrt{2}}, \quad X = \frac{\phi_X + v_X}{\sqrt{2}}$$
$$\begin{pmatrix} h_1\\ h_2\\ h_3 \end{pmatrix} = R \begin{pmatrix} \phi_h\\ \phi_S\\ \phi_X \end{pmatrix}$$

h1 can be our scalar particle of 125 GeV Tania Robens,<sup>1,\*</sup> Tim Stefaniak,<sup>2,†</sup> and Jonas Wittbrodt<sup>2,‡</sup>

MultiHiggs production and EWSB

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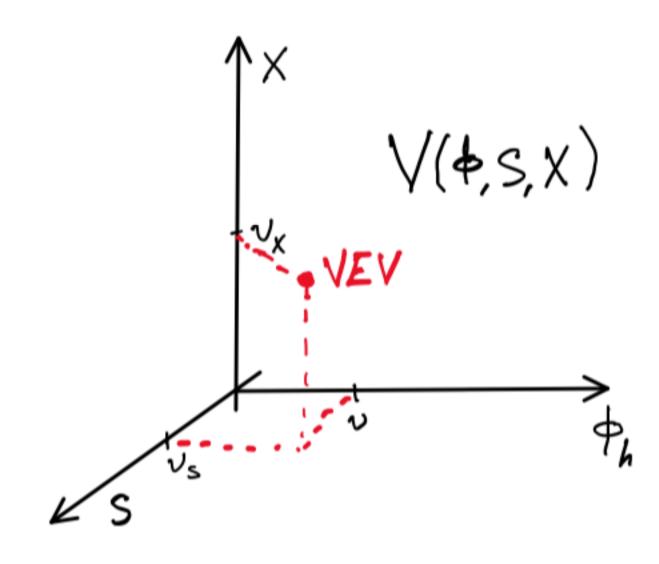
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MultiHiggs production and EWSB



## Remember: Mixing requires nonzero VEV For added scalars

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hef

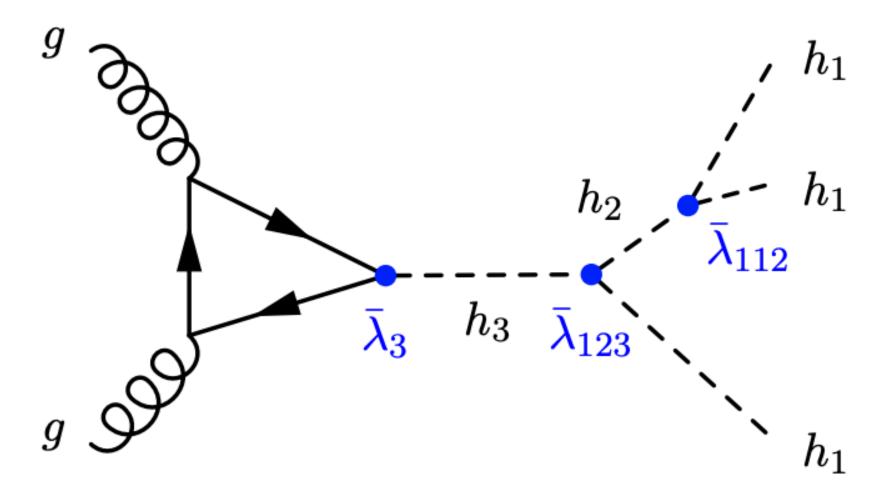
Nik

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MultiHiggs production and EWSB

HHH production is enhanced through **resonance** xsec ~ 30 fb (~ HH production in SM)



We updated this conclusion using better theoretical bounds (perturbativity) and newest experimental bounds!

Osama Karkout,<sup>1</sup> Andreas Papaefstathiou,<sup>2</sup> Marieke Postma,<sup>1,3</sup> Gilberto Tetlalmatzi-Xolocotzi,<sup>4,5</sup> Jorinde van de Vis,<sup>6</sup> Tristan du Pree<sup>1</sup> https://arxiv.org/pdf/2404.12425





Simplified BSM model predicting large HHH: **TRSM**.

SM + two singlets coupling to the Higgs.

$$V = \mu_{\Phi}^2 \Phi^{\dagger} \Phi + \lambda_{\Phi} (\Phi^{\dagger} \Phi)^2 + \mu_S^2 S^2 + \lambda_S S^4 + \mu_X^2 X^2 + \lambda_X X^4 + \lambda_{\Phi S} \Phi^{\dagger} \Phi S^2 + \lambda_{\Phi X} \Phi^{\dagger} \Phi X^2 + \lambda_{SX} S^2 X^2 .$$

Scalars get VEVs!  $\rightarrow$  Mixing:

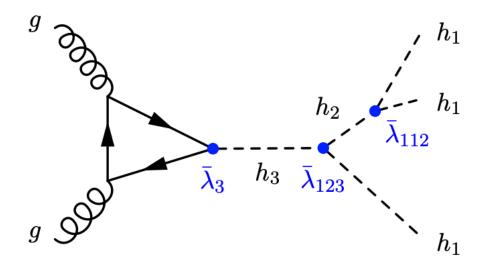
hef

Nik

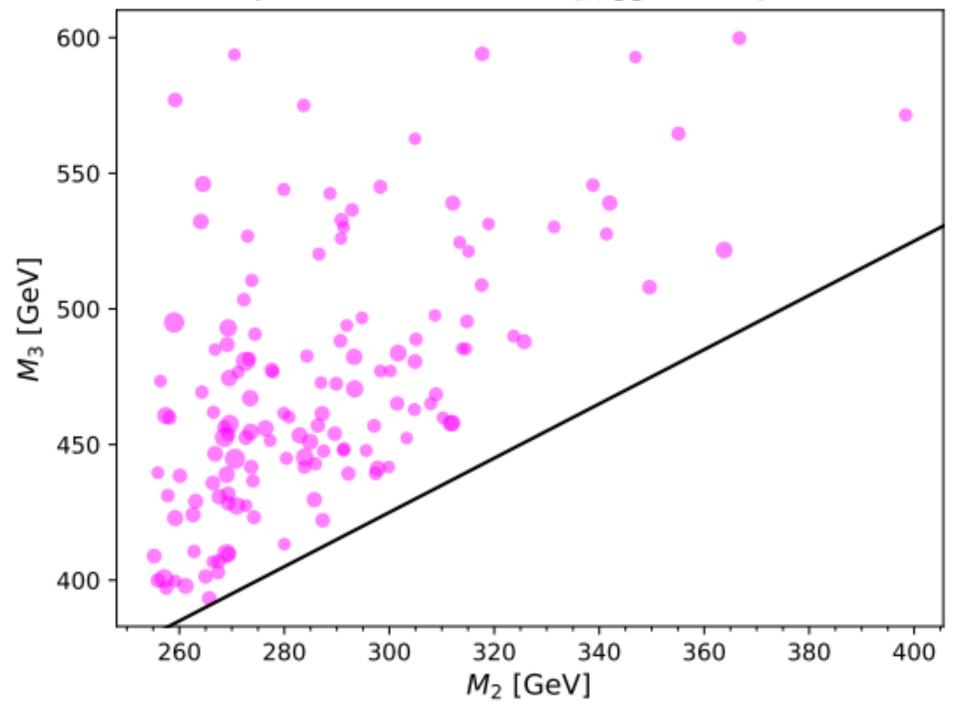
$$\Phi = \begin{pmatrix} 0\\ \frac{\phi_h + v}{\sqrt{2}} \end{pmatrix}, \quad S = \frac{\phi_S + v_S}{\sqrt{2}}, \quad X = \frac{\phi_X + v_X}{\sqrt{2}}$$
$$\begin{pmatrix} h_1\\ h_2\\ h_3 \end{pmatrix} = R \begin{pmatrix} \phi_h\\ \phi_S\\ \phi_X \end{pmatrix}$$

h1 can be our scalar particle of 125 GeV Tania Robens,<sup>1,\*</sup> Tim Stefaniak,<sup>2,†</sup> and Jonas Wittbrodt<sup>2,‡</sup>

MultiHiggs production and EWSB



Viable points with  $\sigma > 100 \times \sigma_{SM}(gg \rightarrow hhh)@13.6 \text{ TeV}$ 



**Osama Karkout**,<sup>1</sup> **Andreas Papaefstathiou**,<sup>2</sup> **Marieke Postma**,<sup>1,3</sup> **Gilberto Tetlalmatzi-Xolocotzi**,<sup>4,5</sup> **Jorinde van de Vis**,<sup>6</sup> **Tristan du Pree**<sup>1</sup> https://arxiv.org/pdf/2404.12425

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#### Osama Karkout



### **Electroweak Phase Transition: TRSM**

$$V = \mu_{\Phi}^2 \Phi^{\dagger} \Phi + \lambda_{\Phi} (\Phi^{\dagger} \Phi)^2 + \mu_S^2 S^2 + \lambda_S S^4 + \mu_X^2 X^2 + \lambda_X + \lambda_{\Phi S} \Phi^{\dagger} \Phi S^2 + \lambda_{\Phi X} \Phi^{\dagger} \Phi X^2 + \lambda_{SX} S^2 X^2 .$$

Mixing:

Nik hef

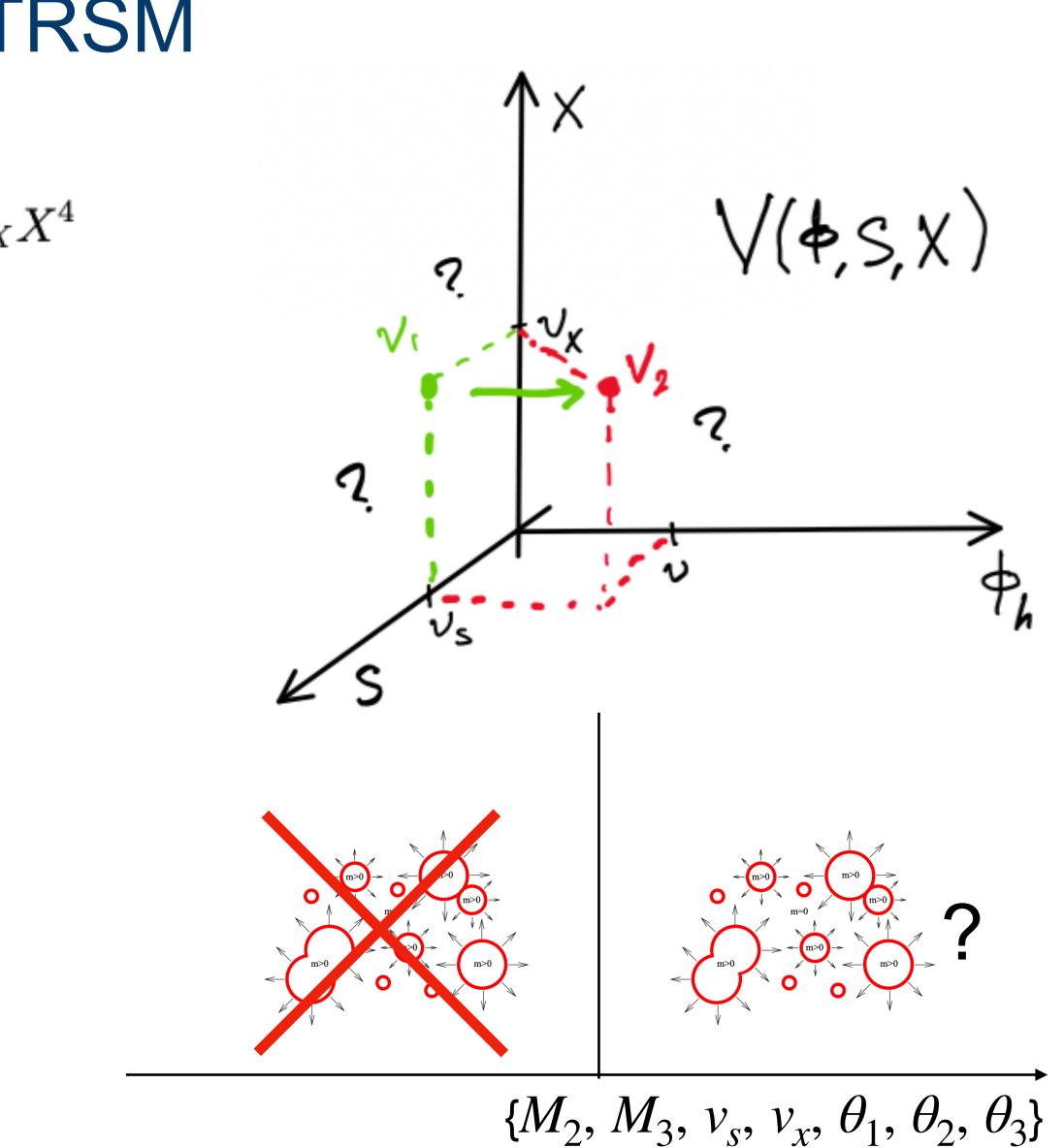
$$\Phi = \begin{pmatrix} 0\\ \frac{\phi_h + v}{\sqrt{2}} \end{pmatrix}, \quad S = \frac{\phi_S + v_S}{\sqrt{2}}, \quad X = \frac{\phi_X + v_X}{\sqrt{2}} \qquad \begin{pmatrix} h_1\\ h_2\\ h_3 \end{pmatrix} = R \begin{pmatrix} \phi_h\\ \phi_S\\ \phi_X \end{pmatrix}$$

Physical parameter space:  $\{M_2, M_3, v_s, v_x, \theta_1, \theta_2, \theta_3\}$ 

 $M_1 = 125 \ GeV, v = 246 \ GeV$ 

Can we have First-Order Phase Transition (FOPT)? For which parameters? Does it come with HHH enhancement?

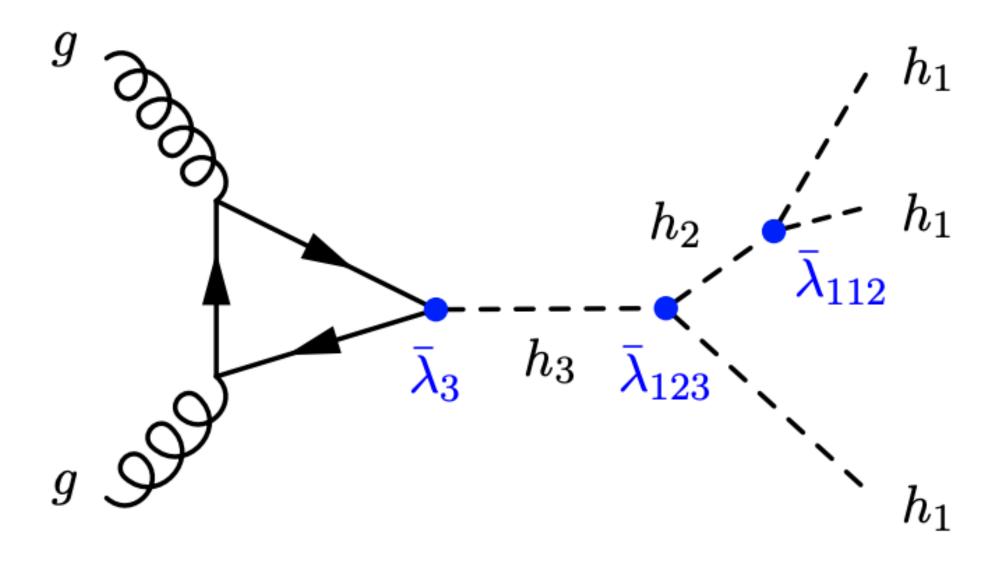




Osama Karkout



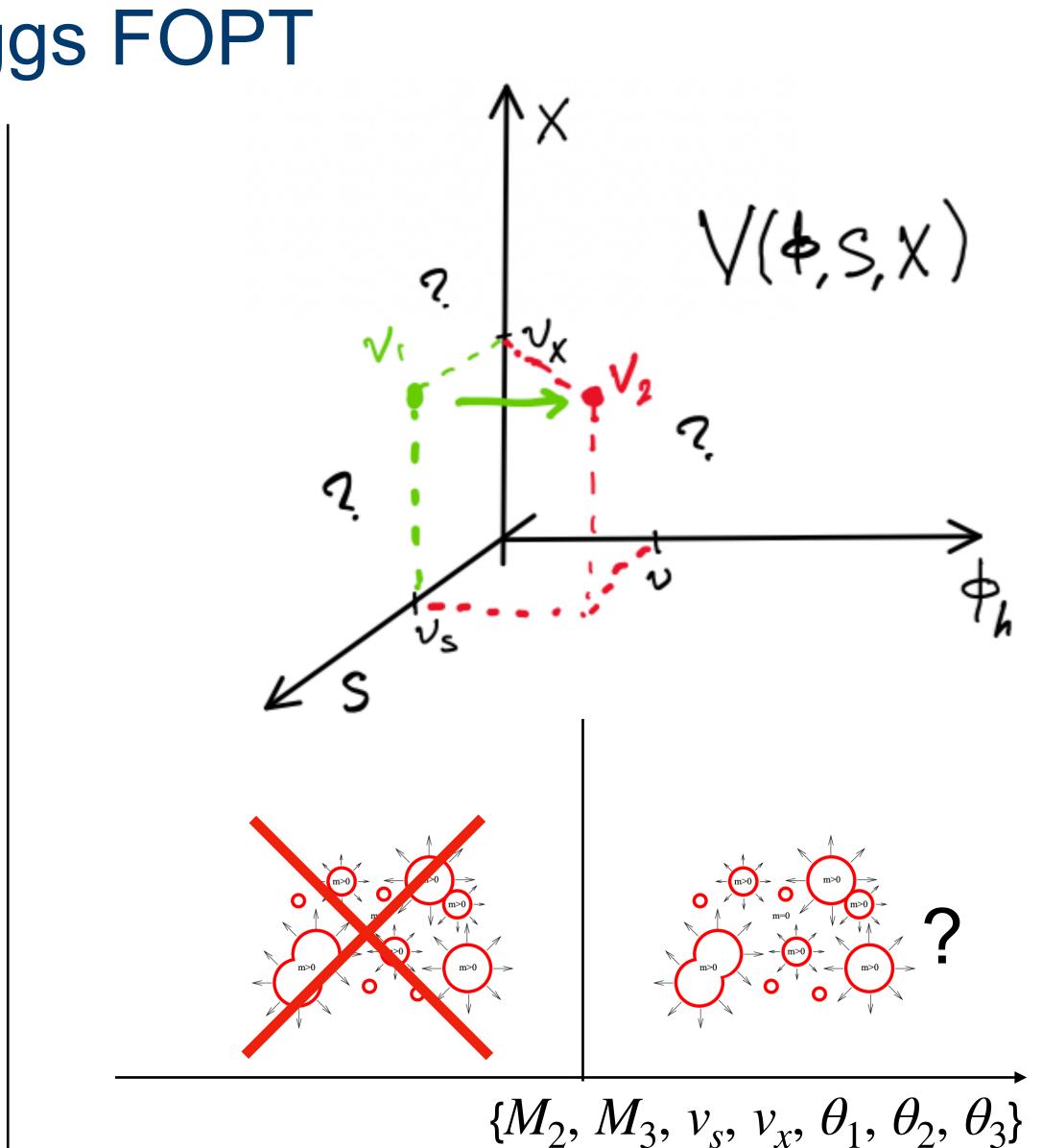
# TRSM: HHH production and Higgs FOPT



## nonzero VEV for two added scalars for double resonance



MultiHiggs production and EWSB

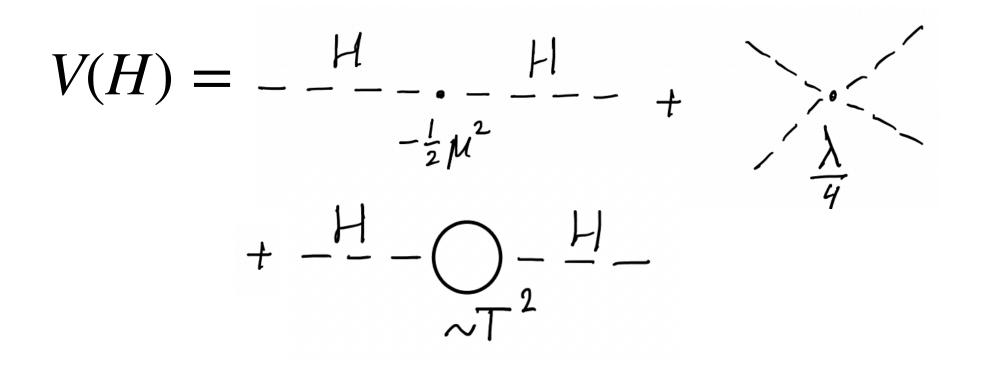


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# PT in TRSM: start with thermal QFT

At LO: only masses get T contribution



$$\begin{split} m_1^2(T) &= -\mu_1^2 + \frac{T^2}{48} \left( 3g_1^2 + 9g_2^2 + 2(6y_t^2 + 12\lambda_1 + \lambda_{12} + \lambda_{13}) \right), \\ m_2^2(T) &= -\mu_2^2 + \frac{T^2}{24} \left( 4\lambda_{12} + \lambda_{23} + 6\lambda_2 \right), \\ m_3^2(T) &= -\mu_3^2 + \frac{T^2}{24} \left( 4\lambda_{13} + \lambda_{23} + 6\lambda_3 \right), \end{split}$$

resulting in an *effective* finite-temperature potential:

Nik hef

$$V_{\text{eff,LO}}(\phi_i, T) = \frac{1}{2} \sum_i m_i^2(T) \phi_i^2 + \frac{1}{4} \sum_{i \le j} \lambda_{ij} \phi_i^2 \phi_j^2.$$

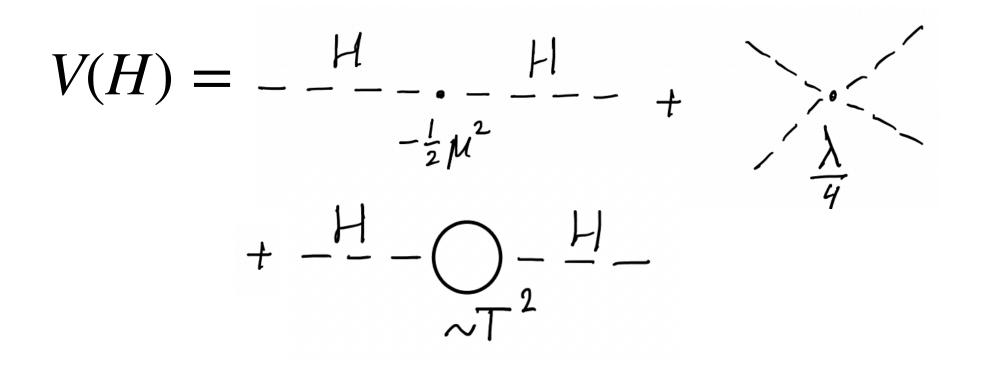
MultiHiggs production and EWSB

#### Osama Karkout



# PT in TRSM: start with thermal QFT

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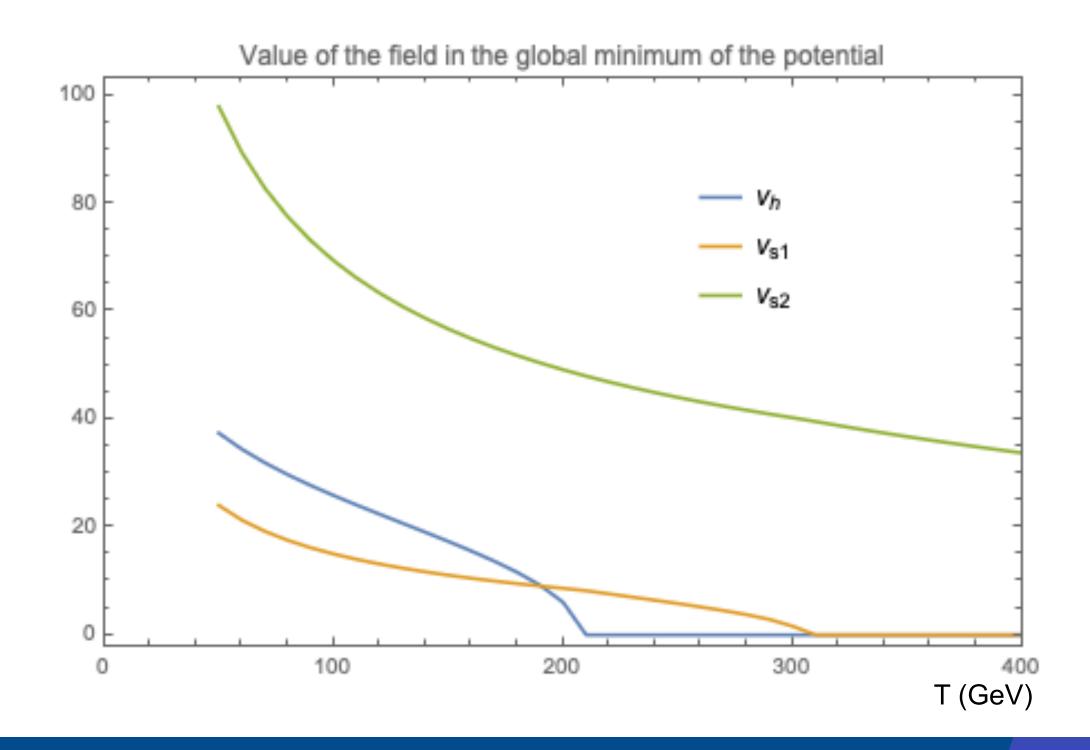
$$V_{\text{eff,LO}}(\phi_i, T) = \frac{1}{2} \sum_i m_i^2(T) \phi_i^2 + \frac{1}{4} \sum_{i \le j} \lambda_{ij} \phi_i^2 \phi_j^2.$$

MultiHiggs production and EWSB

Started using Mathematica to numerically solve RGEs (differential equations as a function of T)

We tried points with large HHH xsec: No FOPT!

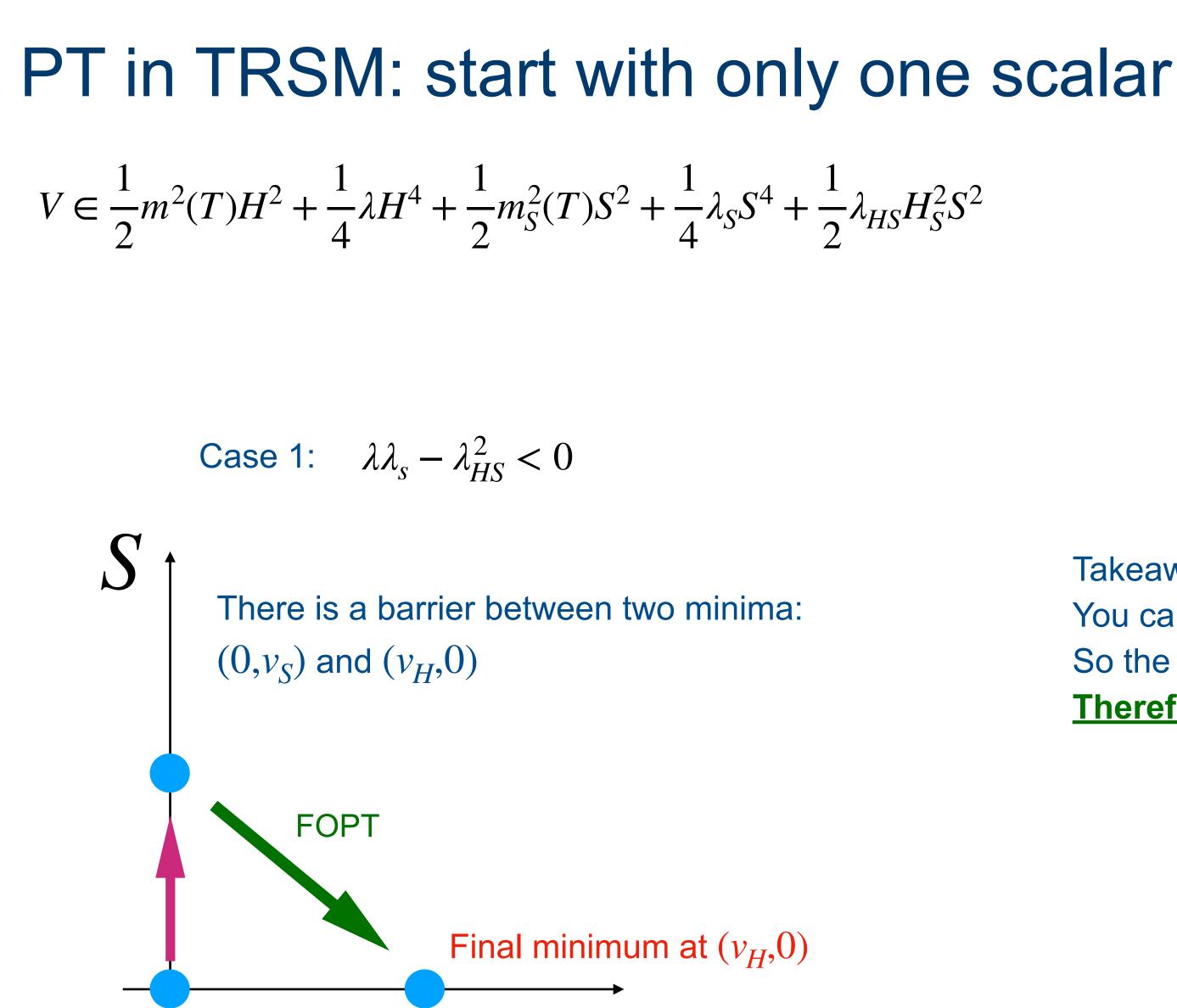
Intuition: I don't think there will be FOPT... Can we prove it?



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**Continuous transition** 

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MultiHiggs production and EWSB



Osama Karkout,<sup>1</sup> Andreas Papaefstathiou,<sup>2</sup> Marieke Postma,<sup>1,3</sup> Gilberto Tetlalmatzi-Xolocotzi,<sup>4,5</sup> Jorinde van de Vis,<sup>6</sup> Tristan du Pree<sup>1</sup> https://arxiv.org/pdf/2404.12425

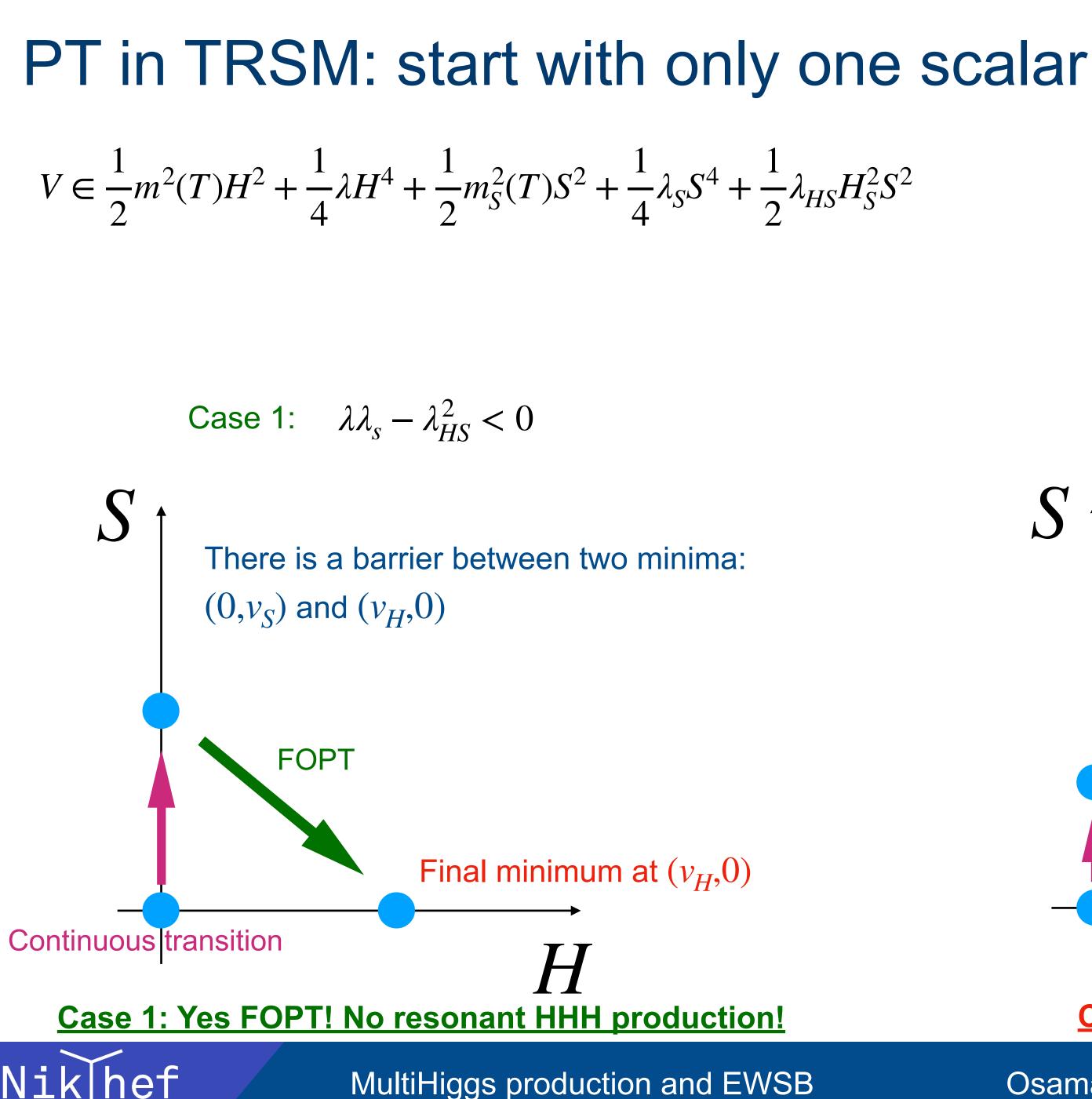
**Extrema at:**  $\partial_H V = 0$ ,  $\partial_S V = 0$ 

Takeaway: Since there is a barrier between the two axes (fields) You cannot put a minimum there! So the field S must end up with a zero VEV **Therefor: No Mixing! No resonant HHH production!** 

Osama Karkout

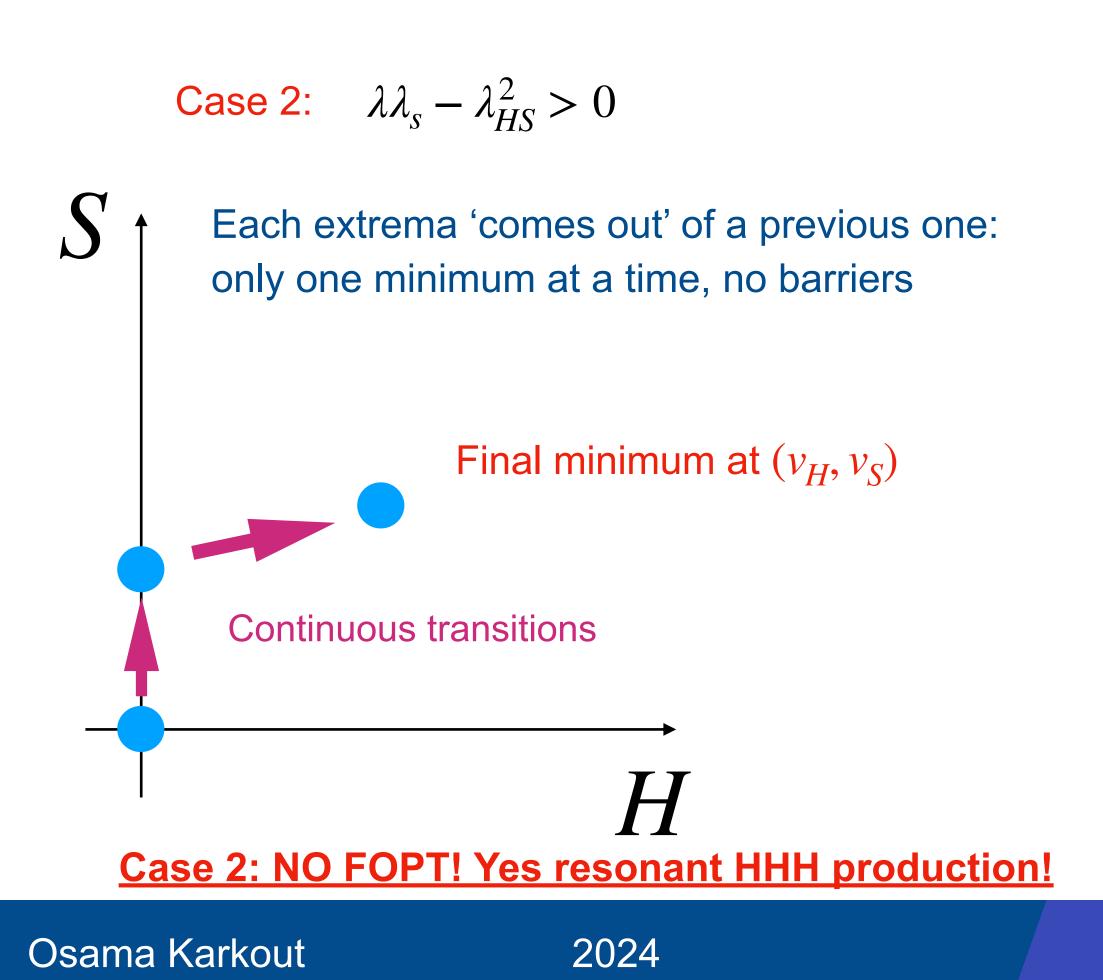






Osama Karkout,<sup>1</sup> Andreas Papaefstathiou,<sup>2</sup> Marieke Postma,<sup>1,3</sup> Gilberto Tetlalmatzi-Xolocotzi,<sup>4,5</sup> Jorinde van de Vis,<sup>6</sup> Tristan du Pree<sup>1</sup> https://arxiv.org/pdf/2404.12425

**Extrema at:**  $\partial_H V = 0$ ,  $\partial_S V = 0$ 





#### Call the fields $x_i$

$$V(x_1,x_2,x_3) = rac{1}{2}\sum_i m_i^2 x_i^2 + rac{1}{4}\sum_{i,j} c_{ij} x_i^2 x_j^2,$$

Find all extrema by taking  $\partial_i V = 0$ 

- Origin:  $\mathbf{x}_0 \equiv (0, 0, 0)$ .
- Axial extremum  $\mathbf{x}_1 \equiv (x_1, 0, 0)$  with

$$x_1 = \sqrt{-m_1^2/c_{11}}.$$

• Planar extremum  $\mathbf{x}_{12} \equiv (x_1, x_2, 0)$  with

$$x_1 = \sqrt{rac{c_{12}m_2^2 - c_{22}m_1^2}{c_{11}c_{22} - c_{12}^2}}, \quad x_2 = \sqrt{rac{c_{12}m_1^2 - c_{11}m_2^2}{c_{11}c_{22} - c_{12}^2}},$$

• Bulk extremum  $\mathbf{x}_{123} \equiv (x_1, x_2, x_3)$  with

$$\begin{split} x_1 &= \frac{\sqrt{(c_{23}^2 - c_{22}c_{33})m_1^2 + (c_{12}c_{33} - c_{13}c_{23})m_2^2 + (c_{13}c_{22} - c_{12}c_{23})m_3^2}}{\sqrt{D}},\\ x_2 &= \frac{\sqrt{(c_{12}c_{33} - c_{13}c_{23})m_1^2 + (c_{13}^2 - c_{11}c_{33})m_2^2 + (c_{11}c_{23} - c_{12}c_{13})m_3^2}}{\sqrt{D}},\\ x_3 &= \frac{\sqrt{(c_{13}c_{22} - c_{12}c_{23})m_1^2 + (c_{11}c_{23} - c_{12}c_{13})m_2^2 + (c_{12}^2 - c_{11}c_{22})m_3^2}}{\sqrt{D}}, \end{split}$$

where

Nik

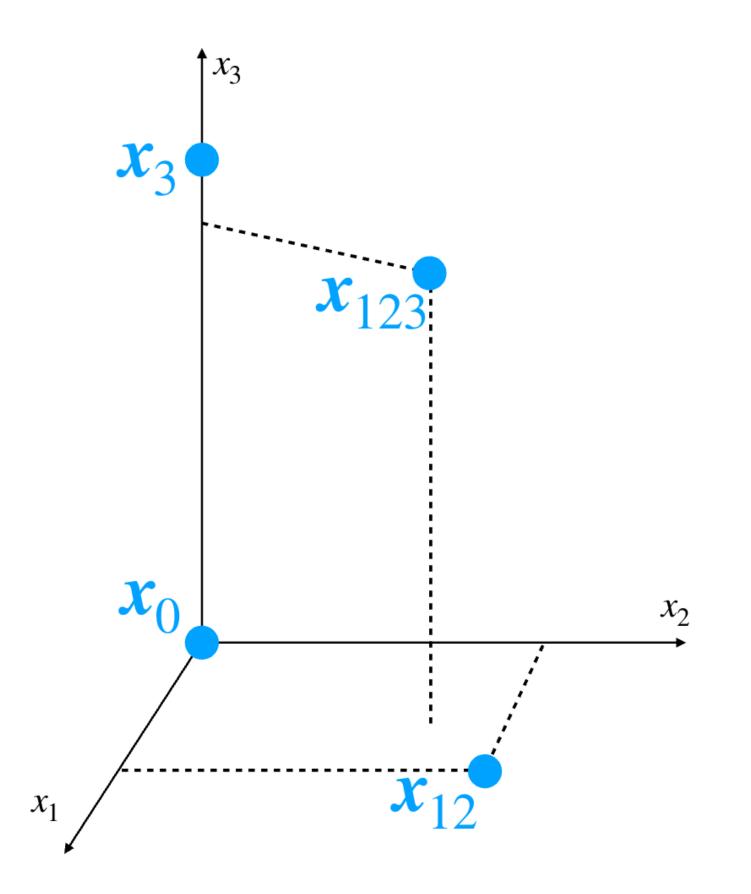
$$D = c_{11}c_{22}c_{33} + 2c_{12}c_{13}c_{23} - c_{13}^2c_{22} - c_{11}c_{23}^2 - c_{12}^2c_{33},$$

is the determinant of  $c_{ij}$ .

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#### MultiHiggs production and EWSB

**Osama Karkout**,<sup>1</sup> **Andreas Papaefstathiou**,<sup>2</sup> **Marieke Postma**,<sup>1,3</sup> **Gilberto Tetlalmatzi-Xolocotzi**,<sup>4,5</sup> **Jorinde van de Vis**,<sup>6</sup> **Tristan du Pree**<sup>1</sup> https://arxiv.org/pdf/2404.12425



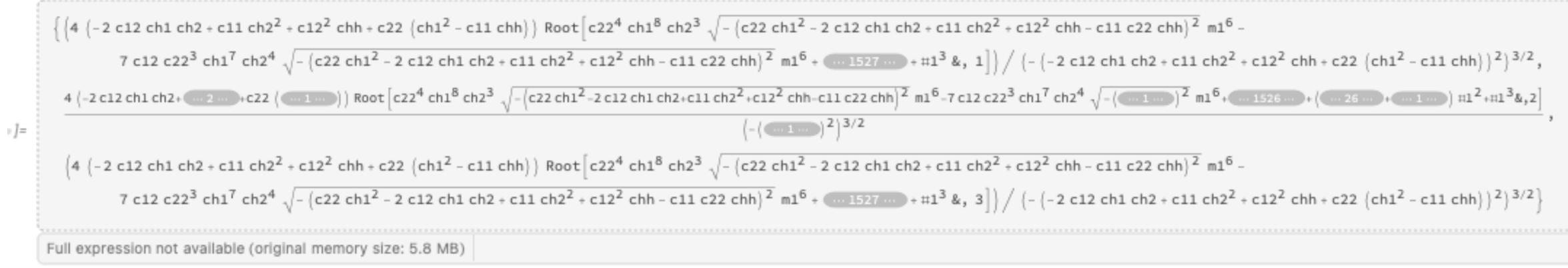
Osama Karkout



The extremum is a minimum if the eigenvalues of the Hessian of the potential  $h_{kl}$ , i.e. the mass matrix, evaluated at the extremum are all positive, with

 $h_{kl}(x_1, x_2, x_3) \equiv \partial_{x_k} \partial_{x_l} V(x_1, x_2, x_3)$ 

l= curve = Simplify[Eigenvalues[Simplify[hessian /. Solutions[16]]]]



### Not even mathematica could help... insight needed.



MultiHiggs production and EWSB

**Osama Karkout**,<sup>1</sup> **Andreas Papaefstathiou**,<sup>2</sup> **Marieke Postma**,<sup>1,3</sup> **Gilberto Tetlalmatzi-Xolocotzi**,<sup>4,5</sup> **Jorinde van de Vis**,<sup>6</sup> **Tristan du Pree**<sup>1</sup> https://arxiv.org/pdf/2404.12425

$$x_3) = (m_k^2 + \sum_i c_{ik} x_i^2) \delta_{kl} + 2c_{kl} x_k x_l.$$
(4.16)

Osama Karkout





$$V(x_1, x_2, x_3) = \frac{1}{2} \sum_{i} m_i^2 x_i^2 + \frac{1}{4} \sum_{i,j} c_{ij} x_i^2 x_j^2,$$

Insights:

- $Z_2$  symmetry:  $(x \rightarrow -x)$  does not change the potential! I can focus on the positive  $x_i$  and generalise.

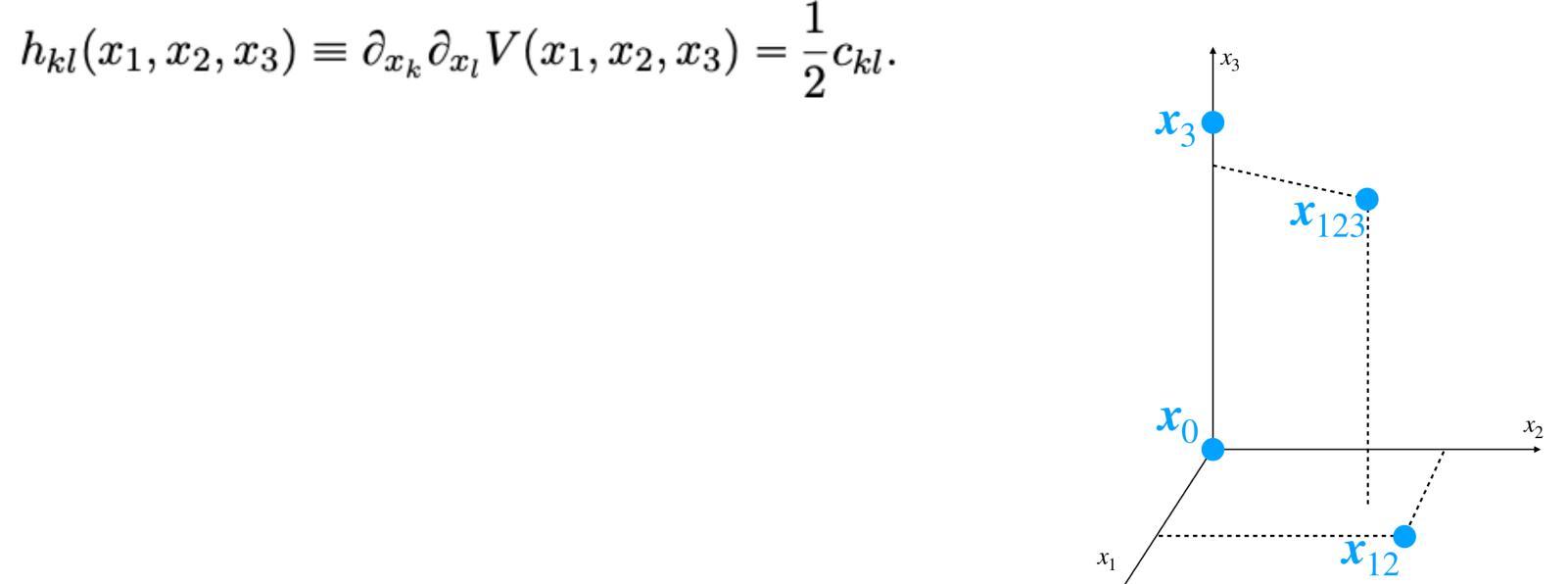
Now the Hessian is simple:



MultiHiggs production and EWSB

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The shape of the potential (whether an extremum is minimum) does not change if I scale the axes:  $x^2 \rightarrow x$ 



**Osama Karkout** 



$$V(x_1, x_2, x_3) = \frac{1}{2} \sum_{i} m_i^2 x_i^2 + \frac{1}{4} \sum_{i,j} c_{ij} x_i^2 x_j^2,$$

Insights:

- $Z_2$  symmetry:  $(x \rightarrow -x)$  does not change the potential! I can focus on the positive  $x_i$  and generalise.

Now the Hessian is simple:  $h_{kl}(x_1, x_2, x_3) \equiv \partial_{x_k} \partial_{x_l}$ For resonant HHH:

We demand that  $\mathbf{x}_{123}$  is today's vacuum. The eigenvalues of the rescaled Hessian should then be positive. Sylvester's criterion, stating that a square Hermitian matrix is positive definite if and only if all the leading principal minors are positive, then gives

$$c_{ii} > 0$$
, &  $C_{ij} \equiv c_{ii}c_{jj} - c_{ij}^2 > 0$ , &

where

hef

$$D = c_{11}c_{22}c_{33} + 2c_{12}c_{13}c_{23} - c_{13}^2c_{22} - c_{11}c_{23}^2 - c_{12}^2$$

is the determinant of  $c_{ij}$ .

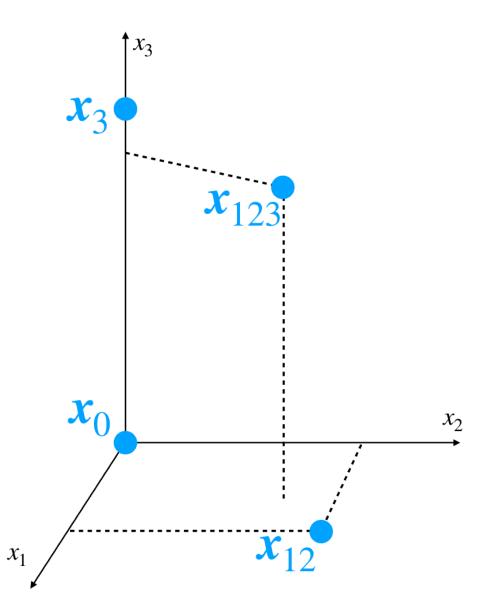
MultiHiggs production and EWSB

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The shape of the potential (whether an extremum is minimum) does not change if I scale the axes:  $x^2 \rightarrow x$ 

$$V(x_1, x_2, x_3) = rac{1}{2}c_{kl}$$

$$D > 0,$$
 (4.18)



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 $_{2}c_{33}$ ,

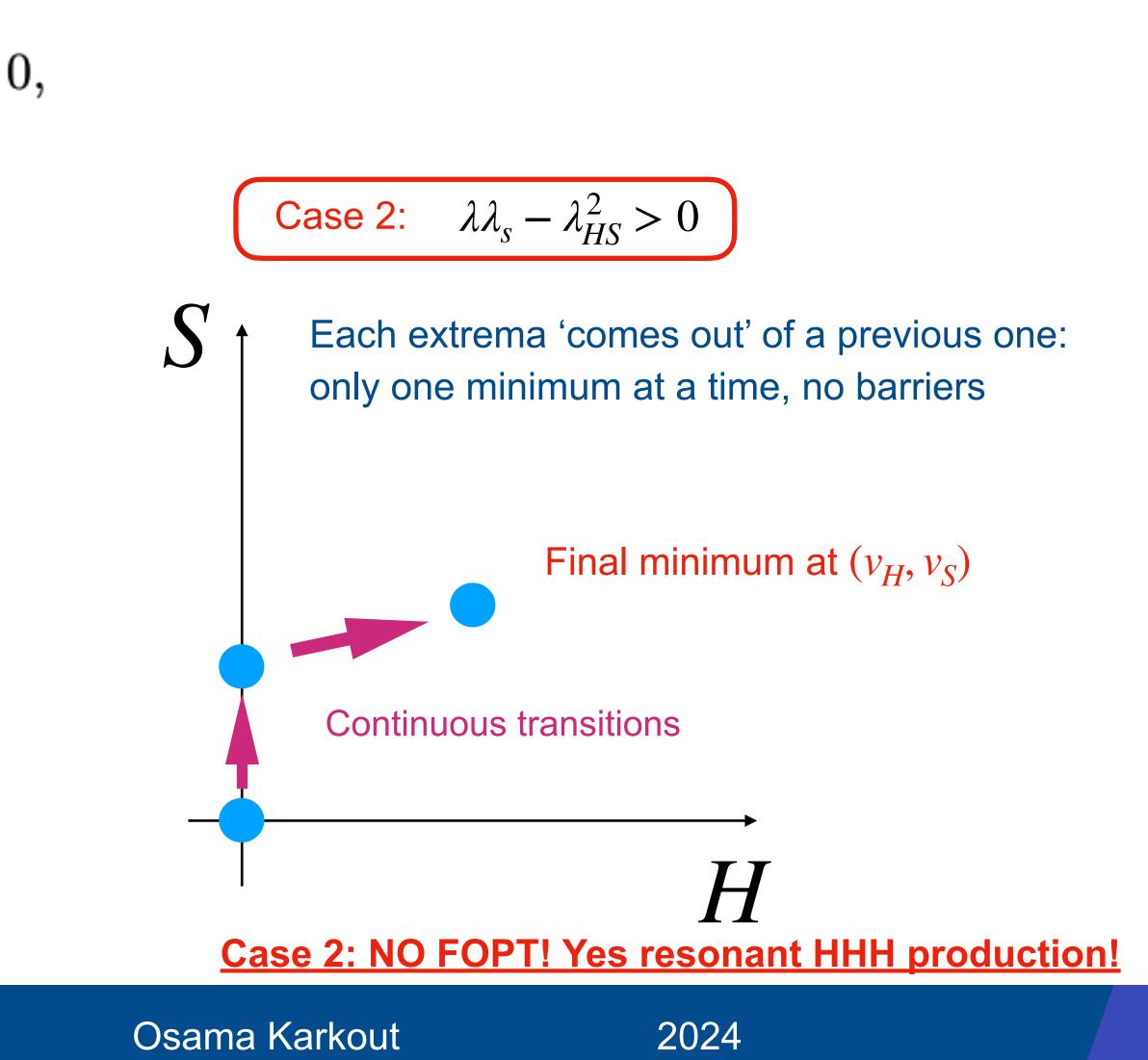


$$egin{aligned} V(x_1,x_2,x_3) &= rac{1}{2} \sum_i m_i^2 x_i^2 + rac{1}{4} \sum_{i,j} c_{ij} x_i^2 x_j^2, \ c_{ii} &> 0, \quad \& \quad C_{ij} \equiv c_{ii} c_{jj} - c_{ij}^2 > 0, \quad \& \quad D > 0 \end{aligned}$$



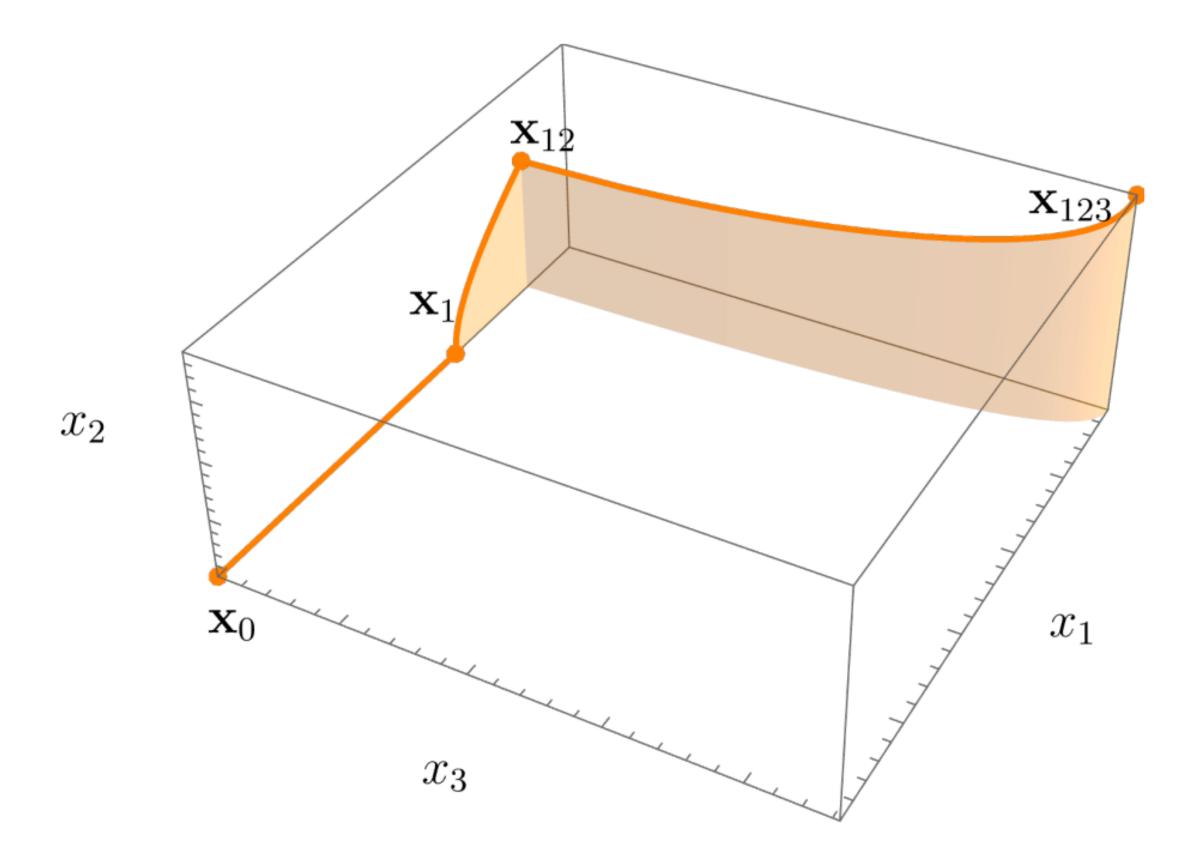
MultiHiggs production and EWSB

**Osama Karkout**,<sup>1</sup> **Andreas Papaefstathiou**,<sup>2</sup> **Marieke Postma**,<sup>1,3</sup> **Gilberto Tetlalmatzi-Xolocotzi**,<sup>4,5</sup> **Jorinde van de Vis**,<sup>6</sup> **Tristan du Pree**<sup>1</sup> https://arxiv.org/pdf/2404.12425





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#### MultiHiggs production and EWSB

**Osama Karkout**,<sup>1</sup> **Andreas Papaefstathiou**,<sup>2</sup> **Marieke Postma**,<sup>1,3</sup> **Gilberto Tetlalmatzi-Xolocotzi**,<sup>4,5</sup> **Jorinde van de Vis**,<sup>6</sup> **Tristan du Pree**<sup>1</sup> https://arxiv.org/pdf/2404.12425



Each extrema 'comes out' of a previous one: only one minimum at a time, no barriers

Final minimum at  $(v_H, v_S, v_x)$ 

Continuous transitions

**Case 2: NO FOPT! Yes resonant HHH production!** 





$$V(x_1, x_2, x_3) = \frac{1}{2} \sum_i m_i^2 x_i^2 + \frac{1}{4} \sum_{i,j} c_{ij} x_i^2 x_j^2,$$
  
 $c_{ii} > 0, \quad \& \quad C_{ij} \equiv c_{ii} c_{jj} - c_{ij}^2 > 0, \quad \& \quad D < 0$ 

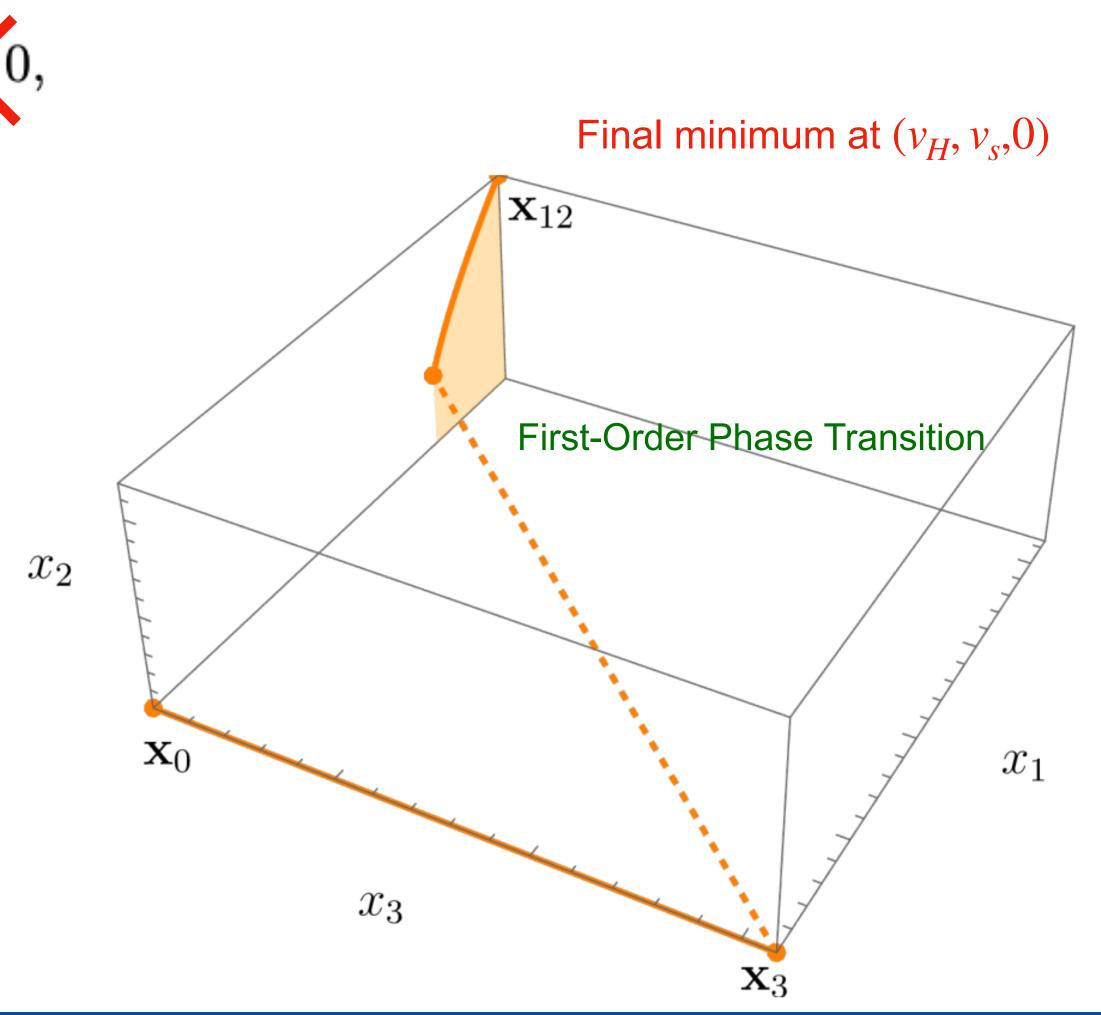
#### **Case 1: Yes FOPT! No resonant HHH production!**

hef

Nik



**Osama Karkout**,<sup>1</sup> **Andreas Papaefstathiou**,<sup>2</sup> **Marieke Postma**,<sup>1,3</sup> **Gilberto Tetlalmatzi-Xolocotzi**,<sup>4,5</sup> **Jorinde van de Vis**,<sup>6</sup> **Tristan du Pree**<sup>1</sup> https://arxiv.org/pdf/2404.12425



Osama Karkout



$$V(x_1, x_2, x_3) = \frac{1}{2} \sum_{i} m_i^2 x_i^2 + \frac{1}{4} \sum_{i,j} c_{ij} x_i^2 x_j^2,$$
  
$$c_{ii} > 0, \quad \& \quad C_{ij} \equiv c_{ii} c_{jj} - c_{ij}^2 > 0, \quad \& \quad D < 0$$
  
$$D < 0$$

# Nightmare! If we want FOPT, we cannot detect it with HHH

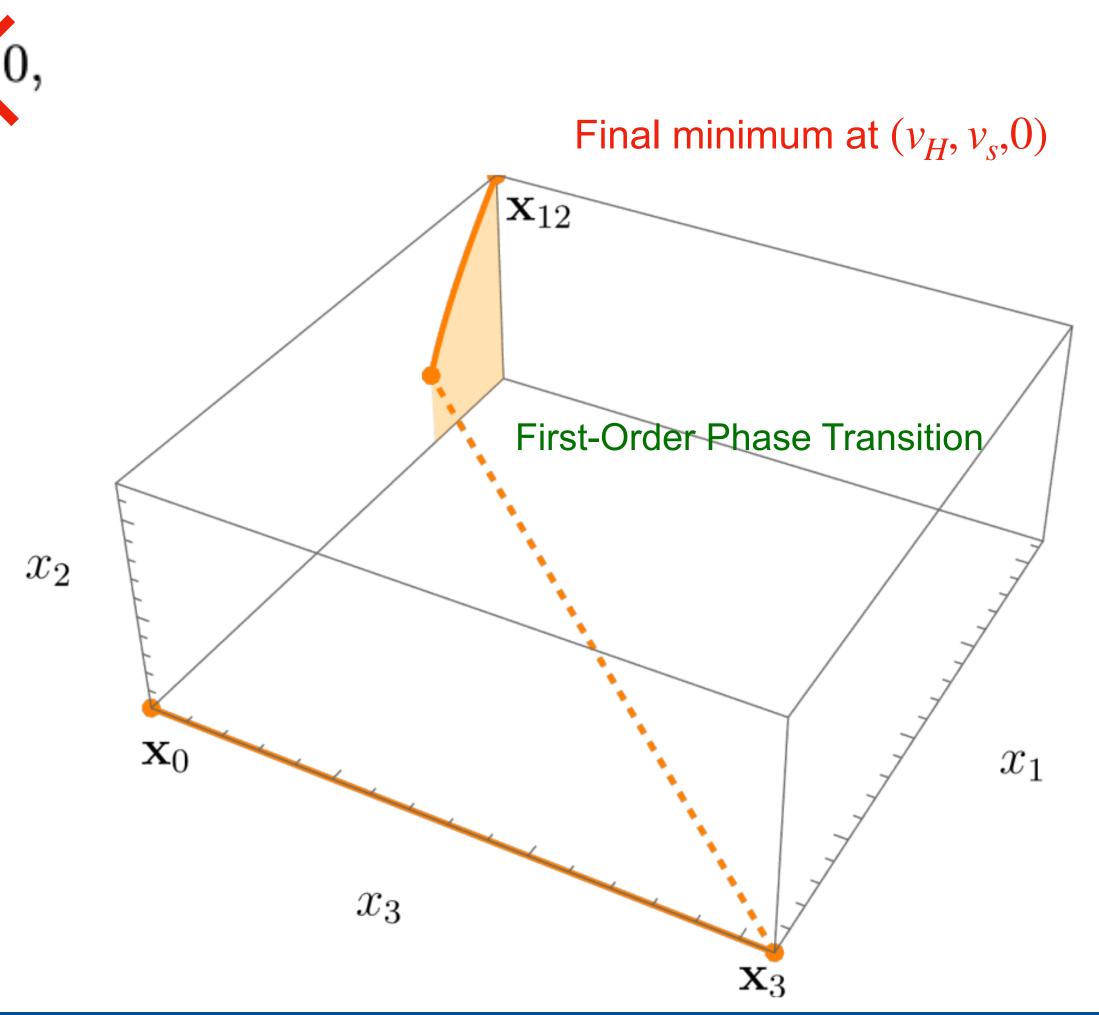
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hef

Nik

MultiHiggs production and EWSB

**Osama Karkout**,<sup>1</sup> **Andreas Papaefstathiou**,<sup>2</sup> **Marieke Postma**,<sup>1,3</sup> **Gilberto Tetlalmatzi-Xolocotzi**,<sup>4,5</sup> **Jorinde van de Vis**,<sup>6</sup> **Tristan du Pree**<sup>1</sup> https://arxiv.org/pdf/2404.12425



Osama Karkout



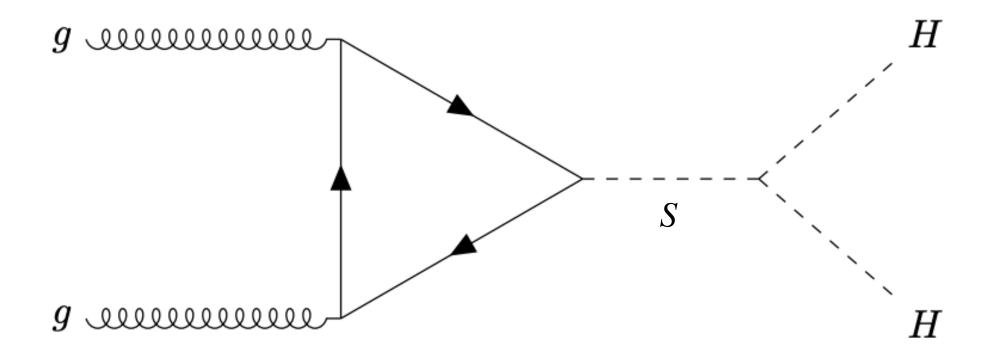
$$V(x_1, x_2, x_3) = \frac{1}{2} \sum_{i} m_i^2 x_i^2 + \frac{1}{4} \sum_{i,j} c_{ij} x_i^2 x_j^2,$$

$$c_{ii} > 0, \quad \& \quad C_{ij} \equiv c_{ii} c_{jj} - c_{ij}^2 > 0, \quad \& \quad D < 0$$

$$D < 0$$

# Silver lining:

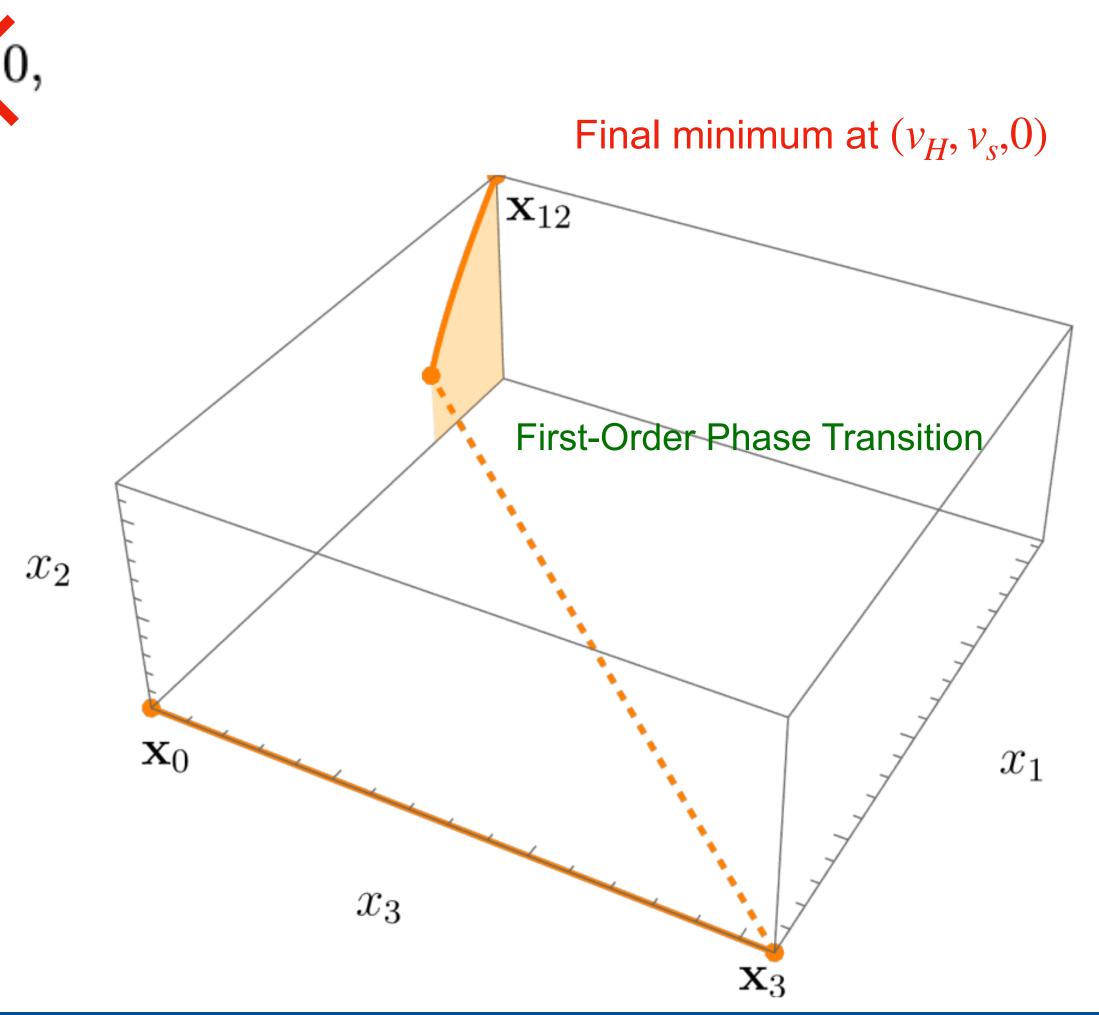
Final minimum at  $(v_H, v_s, 0) \rightarrow$  resonant HH production!!





MultiHiggs production and EWSB

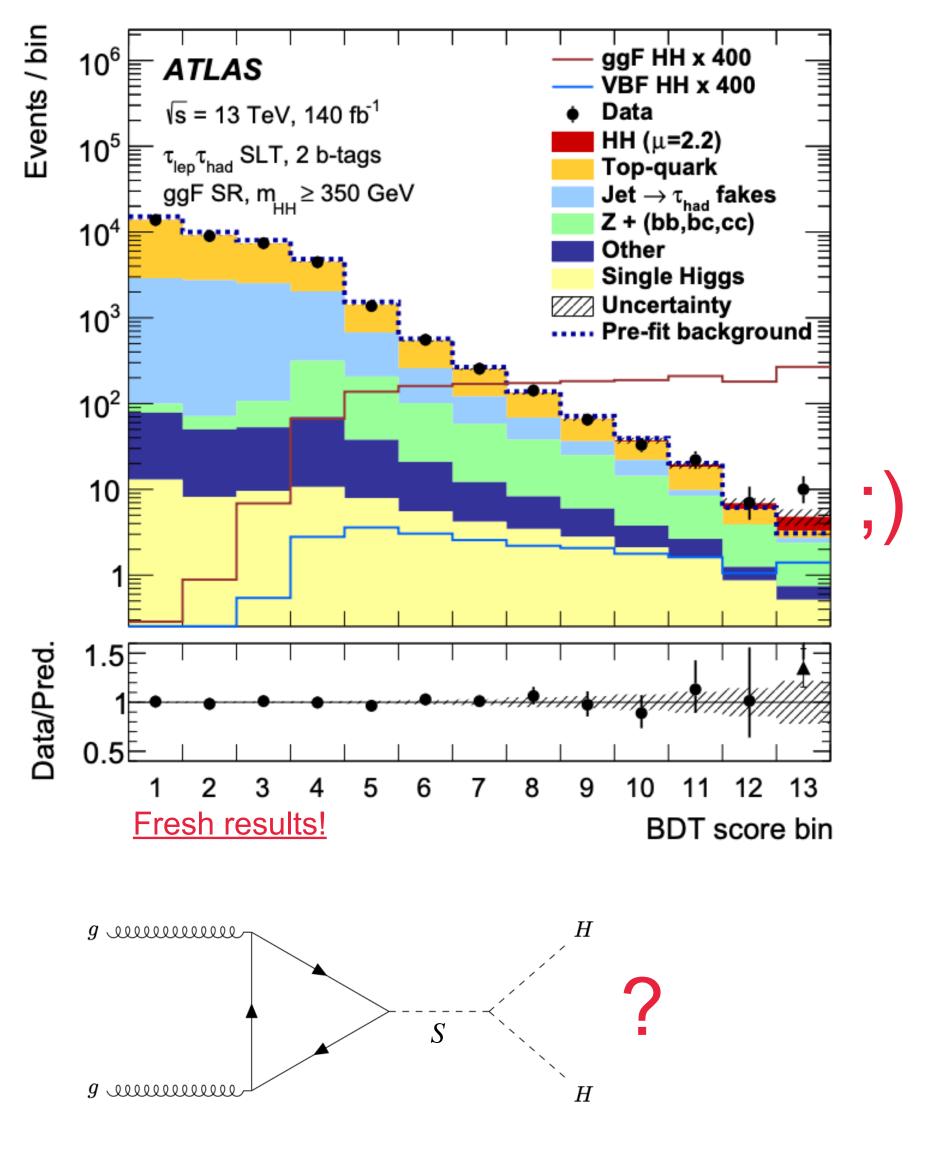
**Osama Karkout**,<sup>1</sup> **Andreas Papaefstathiou**,<sup>2</sup> **Marieke Postma**,<sup>1,3</sup> **Gilberto Tetlalmatzi-Xolocotzi**,<sup>4,5</sup> **Jorinde van de Vis**,<sup>6</sup> **Tristan du Pree**<sup>1</sup> https://arxiv.org/pdf/2404.12425



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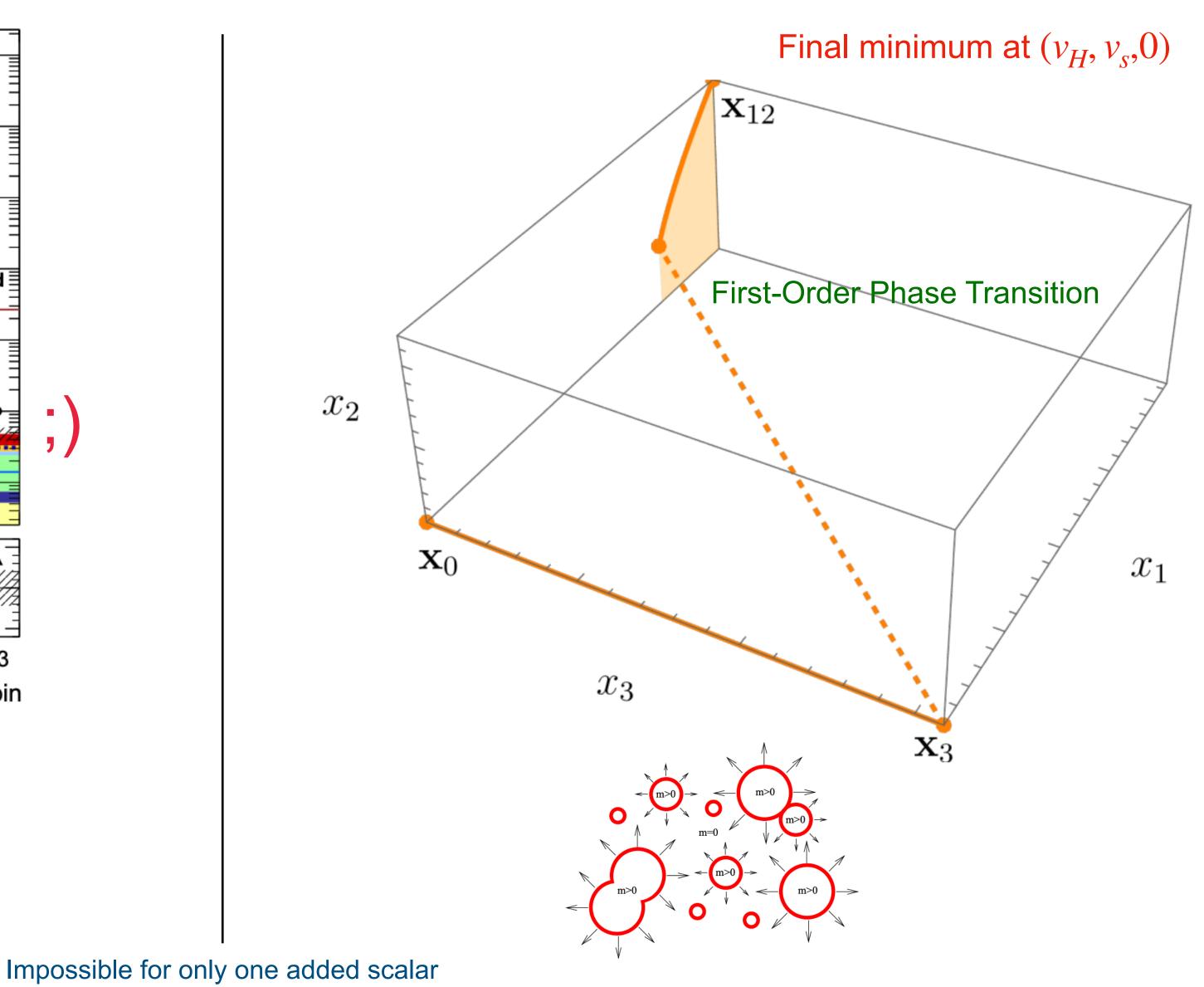


# TRSM can accommodate both HH enhancement and FOPT!



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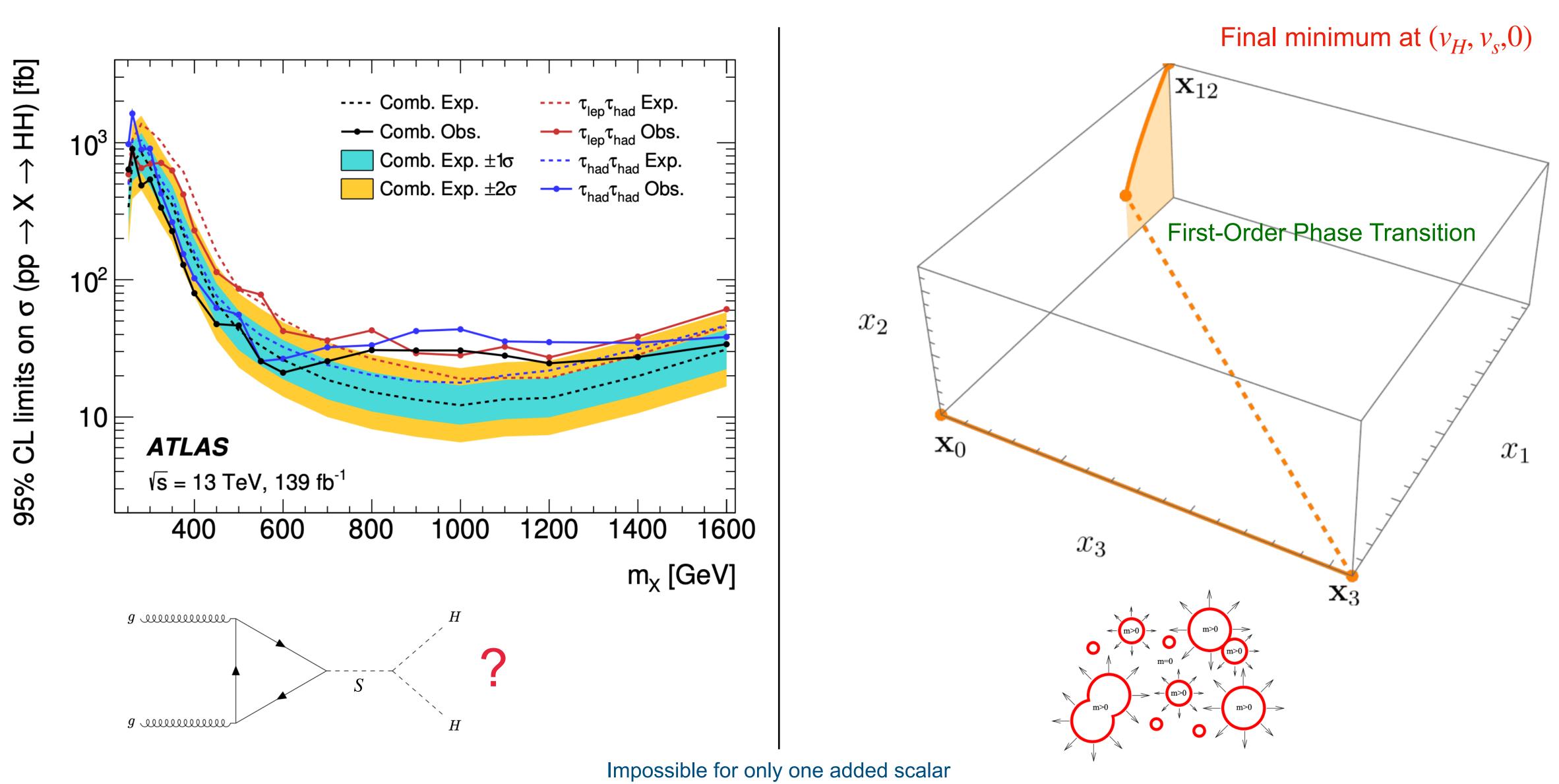
MultiHiggs production and EWSB



Osama Karkout



# TRSM can accommodate both HH enhancement and FOPT!



MultiHiggs production and EWSB

Nik hef

Osama Karkout



# Final notes on HHH and FOPT

- $Z_2$  symmetric TRSM can enhance HHH if both scalars have nonzero VEVs at zero temperature (today)
- Z<sub>2</sub> symmetric TRSM can accommodate First Order Phase Transitions (desired for matter-antimatter asymmetry)
- $Z_2$  symmetric TRSM cannot accommodate both at the same time! Zero scalar VEV required for FOPT



MultiHiggs production and EWSB

**Osama Karkout**,<sup>1</sup> **Andreas Papaefstathiou**,<sup>2</sup> **Marieke Postma**,<sup>1,3</sup> **Gilberto Tetlalmatzi-Xolocotzi**,<sup>4,5</sup> **Jorinde van de Vis**,<sup>6</sup> **Tristan du Pree**<sup>1</sup> https://arxiv.org/pdf/2404.12425

ave nonzero VEVs at zero temperature (today) **se Transitions** (desired for matter-antimatter asymmetry) same time! Zero scalar VEV required for FOPT



# Final notes on HHH and FOPT

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- Z<sub>2</sub> symmetric TRSM can accommodate First Order Phase Transitions (desired for matter-antimatter asymmetry)
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Ideas to achieve both FOPT and HHH:

- Add terms that break  $Z_2$  symmetry
- Add yet another scalar ;)



MultiHiggs production and EWSB

Osama Karkout,<sup>1</sup> Andreas Papaefstathiou,<sup>2</sup> Marieke Postma,<sup>1,3</sup> Gilberto Tetlalmatzi-Xolocotzi,<sup>4,5</sup> Jorinde van de Vis,<sup>6</sup> Tristan du Pree<sup>1</sup> https://arxiv.org/pdf/2404.12425

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# Final notes on HHH and FOPT

- $Z_2$  symmetric TRSM can enhance HHH if both scalars have nonzero VEVs at zero temperature (today)
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Ideas to achieve both FOPT and HHH:

- Add terms that break  $Z_2$  symmetry
- Add yet another scalar;)

presented analytic analysis for LO effective thermal potential. Going to NLO numerically showed us the same conclusion



MultiHiggs production and EWSB

Osama Karkout,<sup>1</sup> Andreas Papaefstathiou,<sup>2</sup> Marieke Postma,<sup>1,3</sup> Gilberto Tetlalmatzi-Xolocotzi,<sup>4,5</sup> Jorinde van de Vis,<sup>6</sup> Tristan du Pree<sup>1</sup> https://arxiv.org/pdf/2404.12425

 $Z_2$  symmetric TRSM can accommodate First Order Phase Transitions (desired for matter-antimatter asymmetry)

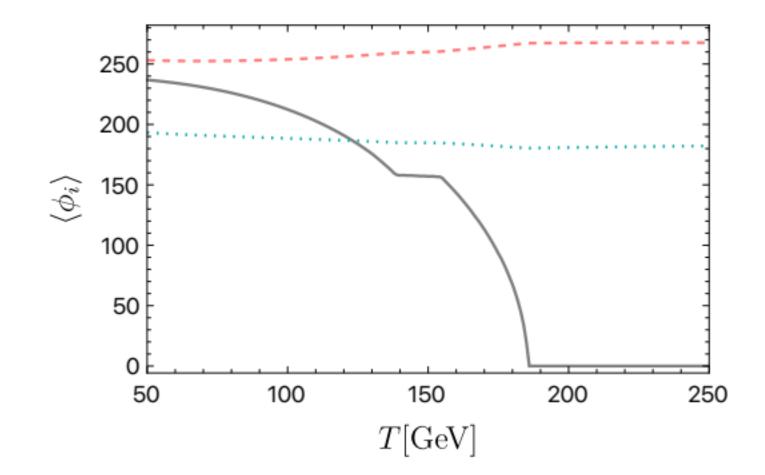


Figure 5: Evolution of the field expectation values in the minimum of the potential for the third BM point in Table 2. The Higgs field is represented by gray solid,  $\phi_2$  by dashed pink, and  $\phi_3$  by dotted cyan.



For the actual scan we have generated 530,000 random points over the phase space defined by  $M_2, M_3, v_2, v_3, \theta_{12}, \theta_{13}, \theta_{23}$ . The ranges considered are as follows:

# $M_2 \in [255, 700] \text{ GeV},$ $v_2 \in [0, 1000]$ GeV,

For the mixing angles  $\theta_{12}, \theta_{13}, \theta_{23}$  we impose the following limits on the scaling factors [38, **68**] of eq. (2.4):



MultiHiggs production and EWSB

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 $M_3 \in [350, 900] \text{ GeV},$  $v_3 \in [50, 1000]$  GeV.

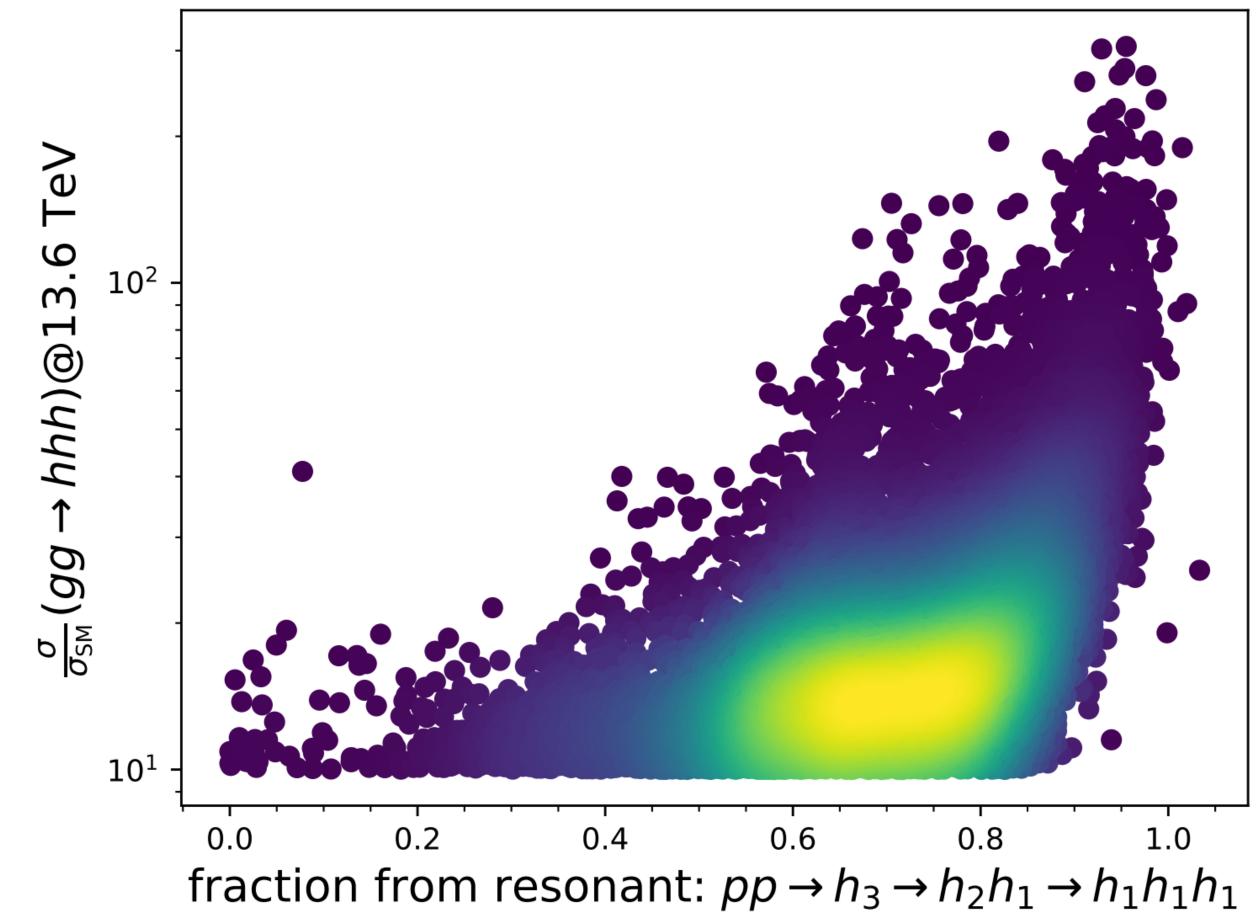
 $0.95 \le \kappa_1 \le 1.00, \quad 0.0 \le \kappa_2 \le 0.25, \quad 0.0 \le \kappa_3 \le 0.25.$ 





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#### **Osama Karkout**,<sup>1</sup> **Andreas Papaefstathiou**,<sup>2</sup> **Marieke Postma**,<sup>1,3</sup> **Gilberto** Viable points with $\sigma > 10 \times \sigma_{SM}(gg \rightarrow hhh)@13.6$ TeV **stan du Pree**<sup>1</sup>



**Figure 2**: Enhancement of the triple Higgs boson production cross section  $\sigma(pp \rightarrow h_1h_1h_1)$  at 13.6 TeV, given in terms of multiples of the SM value, and the resonant fraction contribution from  $pp \rightarrow h_3 \rightarrow h_2h_1 \rightarrow h_1h_1h_1$ . Only points with a factor 10 enhancement or greater are shown. The density of points increases from the dark blue to yellow shade.

MultiHiggs production and EWSB



#### Benchmark points for enhanced triple Higgs production

$M_2$	$M_3$	$v_2$	$v_3$	$ heta_{12}$	$ heta_{13}$	$ heta_{23}$	$rac{\sigma}{\sigma_{SM}}$	Res. Frac.	$\mu_{ m pert}$	$rac{\mu_{ ext{pert}}}{\mu_{ ext{pole}}}$
259.0	495.0	215.8	180.8	6.191	0.163	5.691	306.025	0.955	$2.7 \times 10^2$	7.3
270.6	444.7	122.4	847.2	0.268	0.030	0.522	302.361	0.929	$1.8 \times 10^{2}$	7.3
268.6	452.7	137.8	784.8	0.263	0.023	0.645	275.616	0.954	$2.4  imes 10^2$	7.3
272.6	480.7	928.3	143.7	3.098	2.9	2.375	267.245	0.948	$1.4  imes 10^2$	7.2
269.0	409.8	138.0	599.4	0.244	0.004	0.773	266.439	0.976	$2.4  imes 10^2$	7.2
269.1	486.9	227.5	307.9	0.074	6.149	2.631	157.583	0.956	$4.3  imes 10^2$	8.0
259.2	577.0	289.0	275.6	0.137	6.148	2.324	145.470	0.781	$1.2  imes 10^4$	7.2
283.7	575.0	259.4	330.4	0.137	6.152	2.299	122.546	0.779	$3.0 \times 10^3$	7.2
264.3	469.3	207.3	359.5	0.285	6.277	0.692	119.121	0.999	$5.4 \times 10^{3}$	7.3
266.5	461.9	653.1	229.0	2.889	3.046	1.015	112.794	0.863	$5.3  imes 10^4$	8.0
259.2	399.7	444.5	217.0	2.917	3.046	1.047	103.717	0.973	$1.2 \times 10^5$	8.0

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The one-loop TRSM effective potential at finite temperature is:

$$V_T(\phi_i, T) = V(\phi_i) + V_{CW}(\phi_i) + V_{c.t.}(\phi_i) + V_{T,1-loop}(\phi_i, T),$$

with  $\phi_i$  the field values defined in eq. (2.2) (with  $\phi_i = v_i$  in the vacuum today).  $V(\phi_i)$  is the tree-level potential of eq. (2.1),  $V_{\rm CW}$  the standard zero-temperature one-loop 'Coleman-Weinberg' potential and  $V_{\rm c.t.}$  the corresponding counterterms. The temperature-corrections are captured by  $V_{T, 1-\text{loop}}$ , which is given by

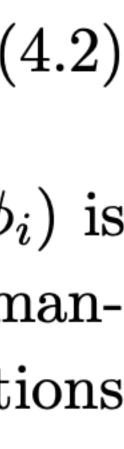
$$V_{T,1-\text{loop}}(\phi,T) = \frac{T^4}{2\pi^2} \left[ \sum_{\alpha=\Phi_i,W,Z} n_\alpha J_B[m_\alpha^2(\phi_i)/T^2] + n_t J_F[m_t^2(\phi_i)/T^2] \right]$$

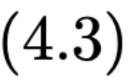


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At temperatures large compared to the  $m_{lpha}^2(\phi_i)/T^2$  as

$$J_B(m_{\alpha}^2/T^2) = -\frac{\pi^4}{45} + \frac{\pi^2}{24}\frac{m_{\alpha}^2}{T^2} - \frac{\pi}{6}\frac{m_{\alpha}^3}{T^3} - \frac{1}{32}\frac{m_{\alpha}^4}{T^4} \left(\log\frac{m_{\alpha}^2}{16\pi^2 T^2} - \frac{3}{2} + 2\gamma_E\right) \cdots,$$
  
$$J_F(m_{\alpha}^2/T^2) = \frac{7\pi^4}{360} - \frac{\pi^2}{24}\frac{m_{\alpha}^2}{T^2} - \frac{1}{32}\frac{m_{\alpha}^4}{T^4} \left(\log\frac{m_{\alpha}^2}{\pi^2 T^2} - \frac{3}{2} + 2\gamma_E\right) \cdots,$$



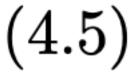
MultiHiggs production and EWSB

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At temperatures large compared to the mass, the functions  $J_{B,F}$  can be expanded in

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#### RGEs $\mathbf{A.3}$

The one-loop RGEs for the quartic couplings are

$$\begin{split} (4\pi)^2 \beta_{\lambda_{11}} &= 24\lambda_{11}^2 + \frac{\lambda_{22}^2}{2} + \frac{\lambda_{33}^2}{2} + \frac{3}{8}g_1^4 + \frac{9}{8}g_2^4 + \frac{3}{4}g_1^2g_2^2 - 6y_t^4 - 4\lambda_{11}\gamma_{\Phi_1}, \\ (4\pi)^2 \beta_{\lambda_{22}} &= 18\lambda_{22}^2 + 2\lambda_{12}^2 + \frac{\lambda_{23}^2}{2}, \\ (4\pi)^2 \beta_{\lambda_{33}} &= 18\lambda_{33}^2 + 2\lambda_{13}^2 + \frac{\lambda_{23}^2}{2}, \\ (4\pi)^2 \beta_{\lambda_{12}} &= 4\lambda_{12}^2 + 12\lambda_{12}\lambda_{11} + 6\lambda_{12}\lambda_{22} + \lambda_{13}\lambda_{23} - 2\lambda_{12}\gamma_{\Phi_1}, \\ (4\pi)^2 \beta_{\lambda_{13}} &= 4\lambda_{13}^2 + 12\lambda_{13}\lambda_{11} + 6\lambda_{13}\lambda_{33} + \lambda_{12}\lambda_{23} - 2\lambda_{13}\gamma_{\Phi_1}, \\ (4\pi)^2 \beta_{\lambda_{23}} &= 4\lambda_{23}^2 + 6\lambda_{23}\lambda_{22} + 6\lambda_{23}\lambda_{33} + 4\lambda_{12}\lambda_{13}, \end{split}$$
(A.5)

with  $\beta_{\lambda} = \mu \partial \lambda / \partial \mu$  and  $\gamma_{\Phi_1} = \left(\frac{3g_1^2}{4} + \frac{9g_2^2}{4} - 3y_t^2\right)$ . The running of the gauge couplings and the top quark is as in the SM

 $(4\pi)^2 \beta_{g_i} = b_i g_i$  $(4\pi)^2 \beta_{y_t} = \frac{9}{2} g_i$ 

with  $b_i = (41/6, -19/6, -7)$  for i = 1, 2, 3.

MultiHiggs production and EWSB



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2024

$$g_i^3,$$
  
 $y_t^3 - y_t(rac{2}{3}g_1^2 + 9g_3^2) - y_t\gamma_{\Phi_1},$  (A.6)



#### How to enhance HHH

$$\mathcal{L} = -\bar{\lambda}_{abc}h_ah_bh_c - \frac{1}{2}\bar{\lambda}_{aab}h_a^2h_b - \frac{1}{3!}\bar{\lambda}_{aaab}h_a^3h_b + \dots , \qquad (2.5)$$

with

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$$\bar{\lambda}_{abc} = (M_a^2 + M_b^2 + M_c^2) \sum_j \frac{R_{aj} R_{bj} R_{cj}}{v_j},$$

$$\bar{\lambda}_{aaab} = (3!) \sum_{ijk} \frac{M_k^2}{v_i v_j} R_{ki}$$

and R the mixing matrix of eq. (A.3). T (up to symmetry factors)

$$\mathcal{A}_1 \sim (\mathcal{A}_{pp \to h_1}^{\mathrm{SM}} \kappa_3) \times \frac{\overline{\lambda}_{321} \overline{\lambda}_{211}}{D_3(p) D_2(p')},$$

The inverse propagators are  $D_a(p) = p^2 - M_a^2 + iM_a\Gamma_a$ , with p the momentum flowing through the propagator, and  $\Gamma_a$  the decay width of  $h_a$ . On resonance, we have  $|p^2 - M_a^2| \ll |M_a\Gamma_a|$ .

MultiHiggs production and EWSB

$$R_{kj}(R_{ai}^2 R_{aj} R_{bj} + R_{ai} R_{bi} R_{aj}^2), \qquad (2.6)$$

and R the mixing matrix of eq. (A.3). The tree-level amplitudes can then be written as

$$\mathcal{A}_{2}^{(a)} \sim (\mathcal{A}_{pp \to h_{1}}^{\text{SM}} \kappa_{a}) \times \frac{\lambda_{a111}}{D_{a}(p)}.$$
 (2.7)

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Baryogenesis (matter-antimatter asymmetry)

# Sakharov is mostly known for his political activism for individual freedom, human rights, civil liberties



MultiHiggs production and EWSB





