

## aN3LO PDFs for Run3 & YR5

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# WG1 ggF: Current Tasks

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## Run 3 Update **(Now)**

**Goal:** Update ggF Cross Section for Run 3

**Timeline:** End of Summer 2024

**Location:** <https://github.com/bmistlbe/InclusiveHXSUpdate> (currently template)

N<sup>3</sup>LO QCD HTL [Dulat, Lazopoulos, Mistlberger 18](#)

NNLO QCD Quark Mass Corrections [Czakon et al. 21, 23](#)

Mixed QCD-EW Corrections [Becchetti et al 20](#)

PDF Uncertainties

## Yellow Report 5 **(Next)**

**Goal:** Update ggF Cross Section for Run 3 & HL-LHC + Boosted Higgs + ...

**Timeline:** General Assembly 2025

**Location:** <https://scipost.org/SciPostPhysCommunityRep> (currently empty)

**Room for other topics of exp/th interest — please propose them!**

# Parameter Choices

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**Most parameters fixed:** (thanks to Karlberg, Mistlberger, Malcles, Di Nardo)

<https://twiki.cern.ch/twiki/bin/view/LHCPhysics/LHCHWG136TeVxsec>

Each group asked if they can produce full or reduced scan

Each group asked if  $m_H \neq 125$  BSM scan is possible

## Additional parameters/choices:

Central Scale set to  $\mu_0 = \frac{m_H}{2}$

Requested 7-point scale variation

**No omissions/ambiguities yet identified in above settings**

# 1. iHixs2 Run 3 Parameter Update

**Old:**  $\delta\sigma_{PP \rightarrow H+X} = \delta(\text{PDF} + \alpha_s) + \delta(\text{theory}) = [\delta(\text{PDF} + \alpha_s)] + [\delta(\text{scale}) + \delta(\text{EWK}) + \delta(t, b, c) + \delta(1/m_t) + \delta(\text{PDF} - \text{TH})]$

**New:**  $\delta\sigma_{PP \rightarrow H+X} = \delta(\text{PDF} + \alpha_s) + \delta(\text{theory}) + \delta(\text{PDF} - \text{TH}) = [\delta(\text{PDF} + \alpha_s)] + [\delta(\text{scale}) + \delta(\text{EWK}) + \delta(t, b, c) + \delta(1/m_t)] + [\delta(\text{PDF} - \text{TH})]$

Running iHixs2 with recommended parameters:

$\sqrt{s}$ [TeV]	$M_H$ [GeV]	$\sigma$ [pb]	$\delta(\text{theory})$	$\delta(\text{scale})$	$\delta(\text{EWK})$	$\delta(t, b, c)$	$\delta(1/m_t)$	$\delta(\text{PDF} + \alpha_s)$	$\delta(\text{PDF})$	$\delta(\alpha_s)$	$\delta(\text{PDF} - \text{TH})$
13.6	120.00	56.03	+3.16% -5.42%	+0.31% -2.57%	±1.00%	±0.85%	±1.00%	+2.67% -2.27%	+1.65% +1.65%	+2.11% -1.56%	±1.21%
13.6	122.00	54.40	+3.14% -5.37%	+0.30% -2.53%	±1.00%	±0.84%	±1.00%	+2.67% -2.26%	+1.65% +1.65%	+2.10% -1.55%	±1.20%
13.6	124.00	52.87	+3.12% -5.33%	+0.29% -2.50%	±1.00%	±0.83%	±1.00%	+2.67% -2.26%	+1.64% +1.64%	+2.10% -1.55%	±1.18%
13.6	124.60	52.43	+3.11% -5.32%	+0.28% -2.49%	±1.00%	±0.83%	±1.00%	+2.67% -2.26%	+1.64% +1.64%	+2.10% -1.54%	±1.18%
13.6	124.80	52.28	+3.11% -5.32%	+0.28% -2.49%	±1.00%	±0.83%	±1.00%	+2.67% -2.26%	+1.64% +1.64%	+2.10% -1.54%	±1.18%
13.6	125.00	52.13	+3.11% -5.31%	+0.28% -2.48%	±1.00%	±0.83%	±1.00%	+2.67% -2.25%	+1.64% +1.64%	+2.10% -1.54%	±1.18%
13.6	125.09	52.07	+3.11% -5.31%	+0.28% -2.48%	±1.00%	±0.83%	±1.00%	+2.67% -2.25%	+1.64% +1.64%	+2.10% -1.54%	±1.18%
13.6	125.20	51.99	+3.11% -5.31%	+0.28% -2.48%	±1.00%	±0.83%	±1.00%	+2.67% -2.25%	+1.64% +1.64%	+2.10% -1.54%	±1.18%
13.6	125.30	51.92	+3.10% -5.30%	+0.28% -2.48%	±1.00%	±0.83%	±1.00%	+2.66% -2.25%	+1.64% +1.64%	+2.10% -1.54%	±1.18%
13.6	125.38	51.86	+3.10% -5.30%	+0.28% -2.48%	±1.00%	±0.83%	±1.00%	+2.66% -2.25%	+1.64% +1.64%	+2.10% -1.54%	±1.18%
13.6	125.60	51.70	+3.10% -5.30%	+0.28% -2.47%	±1.00%	±0.82%	±1.00%	+2.66% -2.25%	+1.64% +1.64%	+2.10% -1.54%	±1.17%
13.6	126.00	51.41	+3.10% -5.29%	+0.27% -2.47%	±1.00%	±0.82%	±1.00%	+2.66% -2.25%	+1.64% +1.64%	+2.10% -1.54%	±1.17%
13.6	128.00	50.00	+3.07% -5.24%	+0.26% -2.43%	±1.00%	±0.81%	±1.00%	+2.66% -2.25%	+1.64% +1.64%	+2.09% -1.54%	±1.16%
13.6	130.00	48.65	+3.05% -5.19%	+0.25% -2.39%	±1.00%	±0.80%	±1.00%	+2.66% -2.24%	+1.64% +1.64%	+2.09% -1.53%	±1.15%

**Note:** Numbers here do not include  $(t, b, c)$  or (EWK) update

c.f. previous extrapolated numbers: (differences: PDF4LHC 15 → 21)

2	ggF (N3LO QCD + NLO EW)								
3	MH	XS	Uncertainty						
4		Interpolation	Theory			PDF+ $\alpha_s$	PDF	$\alpha_s$	
5	[GeV]	[pb]	pos [%]	neg [%]	Gauss [%]	[%]	[%]	[%]	
6	120.00	5.611E+01	+4.7	-6.9	±4.0	±3.2	±1.9	±2.6	
24	125.00	5.223E+01	+4.6	-6.7	±3.9	±3.2	±1.9	±2.6	
25	125.09	5.217E+01	+4.6	-6.7	±3.9	±3.2	±1.9	±2.6	
26	125.10	5.216E+01	+4.6	-6.7	±3.9	±3.2	±1.9	±2.6	
43	130.00	4.875E+01	+4.5	-6.6	±3.8	±3.2	±1.8	±2.6	

## 2. Estimate for PDF-TH & aN<sup>3</sup>LO PDFs

numbers for  $\sqrt{s} = 13.6 \text{ TeV}$  &  $M_H = 125.09 \text{ GeV}$

**baseline:** 
$$\delta(\text{PDF-TH}) = \pm \frac{1}{2} \left| \sigma_{PP \rightarrow H+X}^{(2), \text{EFT}, \text{NNLO}} - \sigma_{PP \rightarrow H+X}^{(2), \text{EFT}, \text{NLO}} \right|$$

PDF4LHC21 — no NLO set available

⇒ switch to PDF4LHC15 *just* for  $\delta(\text{PDF-TH})$  estimate

↪ PDF4LHC15  $\pm 1.18 \%$

Robust w.r.t. PDF var.

↪ MSHT20  $\pm 1.43 \%$

↪ CT18  $\pm 1.03 \%$

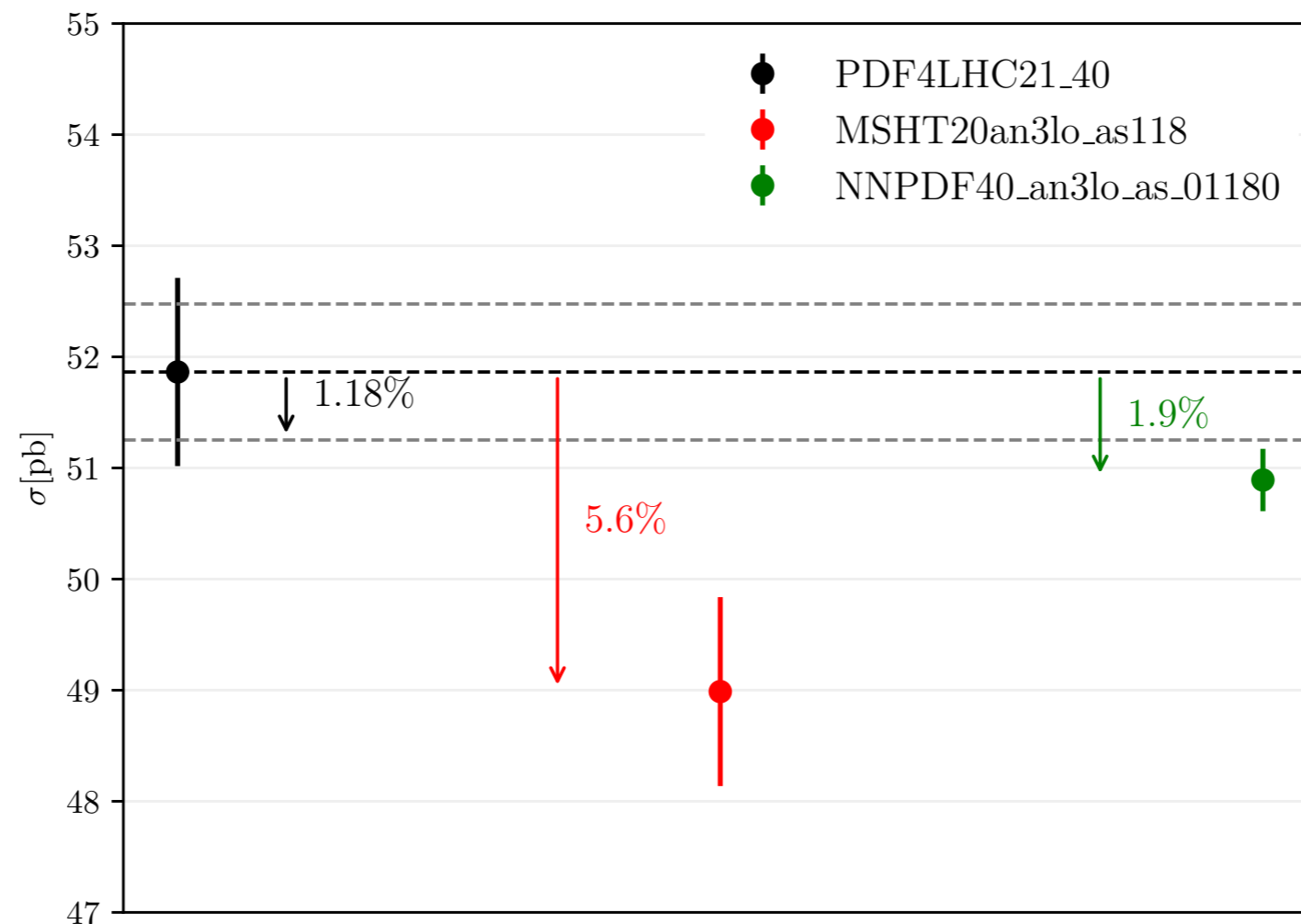
↪ NNPDF3.1  $\pm 0.92 \%$

↪ NNPDF4  $\pm 0.18 \%$

## 2. Estimate for PDF-TH & aN<sup>3</sup>LO PDFs

numbers for  $\sqrt{s} = 13.6 \text{ TeV}$  &  $M_H = 125.09 \text{ GeV}$

**alternative:**  $\delta(\text{PDF} - \text{TH}) = \left| \sigma_{PP \rightarrow H+X}^{(3),\text{EFT},\text{aN}^3\text{LO}} - \sigma_{PP \rightarrow H+X}^{(3),\text{EFT},\text{NNLO}} \right|$



Error bars:  $\delta(\text{PDF})$

**Proposal:** stick with baseline using PDF4LHC15, report numbers for aN<sup>3</sup>LO set(s)?

# Summary

14:00	→ 14:10	ggF Overview	🕒 10m	✎
14:15	→ 14:35	MSHT (Thomas Cridge) Speaker: Thomas Cridge (DESY)	🕒 20m	✎
14:50	→ 15:10	NNPDF (Giacomo Magni) Speaker: Giacomo Magni (Nikhef, VU Amsterdam)	🕒 20m	✎
15:25	→ 15:45	ABM (Sasha Zenaiev)	🕒 20m	✎
16:00	→ 16:15	Break	🕒 15m	
16:15	→ 16:35	CT (Marco Guzzi) Speaker: Marco Guzzi (Kennesaw State University)	🕒 20m	✎
16:50	→ 17:05	Splitting Functions (Sven-Olaf Moch) Speakers: Giulio Falcioni, Sven-Olaf Moch, Sven-Olaf Moch	🕒 15m	✎
17:10	→ 17:25	Splitting Functions (Tongzhi Yang) Speakers: Thomas Kurt Gehrman (University of Zurich (CH)), Tongzhi Yang	🕒 15m	✎
17:40	→ 18:00	Summary & Discussion	🕒 20m	✎

## Goals of Meeting:

- 1) Decide path to producing a contribution (text and/or plots) to be presented alongside the Run 3 recommendations regarding PDF-TH uncertainties
- 2) Brainstorm/kick-off YR5 activities surrounding the latest PDFs

**Finally:** Please join the new\* ggF mailing list for future meetings/updates:

[lhc-higgs-ggf@cern.ch](mailto:lhc-higgs-ggf@cern.ch) (via <http://cern.ch/egroups>)

# Backup

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**Warning: The following slides are from from GA 2023 and are partially outdated**



# Inclusion of NNLO $m_t$

**iHixs:**

$$\hat{\sigma}_{ij} = R_{\text{LO}} C^2 \left[ \sigma_{ij}^{\text{LO, EFT}} + \sigma_{ij}^{\text{NLO, EFT}} + \sigma_{ij}^{\text{NNLO, EFT}} + \sigma_{ij}^{\text{N}^3\text{LO, EFT}} \right] + \delta\sigma_{ij}^{\text{LO, (t,b,c)}} + \delta\sigma_{ij}^{\text{NLO, (t,b,c)}} + \delta\sigma_{ij}^{\text{NNLO, (t)}} + R_{\text{LO}} C^2 \delta\sigma_{ij}^{\text{Res}}.$$

- start with iHixs prediction and systematically incorporate new results
- exact top mass at NNLO [Czakon, Harlander, Klappert, Niggetiedt 21](#)

$$\delta\sigma_{ij}^{\text{NNLO, (t)}} = \boxed{\sigma_{ij}^{\text{NNLO, approx.}}} - \left[ C_{\text{QCD}}^2 R_{\text{LO}} \sigma_{ij}^{\text{EFT}} \right]_{\alpha_S^4} \quad \text{for } (ij) \in \{(gg), (gq)\}$$

iHixs gives access to each part:

↪ substitution  $\sigma_{ij}^{\text{NNLO, approx.}} \rightarrow \sigma_{ij}^{\text{NNLO, exact}}$  straightforward

(computation of "exact" already as a difference to EFT ↗ compatibility checks)

# Inclusion of NNLO $m_t$

**Predictions from** Czakon, Harlander, Klappert, Niggetiedt 21 + Tom Schellenberger, Felix Eschment

channel	$\sigma_{\text{HEFT}}^{\text{NNLO}}$ [pb]			$(\sigma_{\text{exact}}^{\text{NNLO}} - \sigma_{\text{HEFT}}^{\text{NNLO}})$ [pb]	
	$\mathcal{O}(\alpha_s^2)$	$\mathcal{O}(\alpha_s^3)$	$\mathcal{O}(\alpha_s^4)$	$\mathcal{O}(\alpha_s^3)$	$\mathcal{O}(\alpha_s^4)$
$\sqrt{s} = 13.6 \text{ TeV}$					
$gg$	+17.114	+20.750(5)	+9.216(23)	+0.0238	+0.2644(6)
$qg$		+1.613(2)	+0.916(6)	-0.4034	-0.0004(47)
$qq$		+0.026(1)	+0.109(1)	+0.0335	-0.0551(1)
total	+17.114	+22.389(6)	+10.241(23)	-0.3461	+0.2090(47)

- predictions employ the **pole mass scheme**
  - $\leftrightarrow$  default so far:  **$\overline{\text{MS}}$  scheme**
  - $\hookrightarrow$  numerical impact? need to include as **uncertainty**?
- predictions  $\forall \sqrt{s}$  (7, 8, 13, 13.6, 14 TeV)
  - $\leftrightarrow$  single Higgs mass  **$M_{\text{H}}^{\text{ref}} \equiv 125.09 \text{ GeV}$**
  - $\hookrightarrow$  how to extrapolate? what are the **uncertainties**?

# Inclusion of NNLO $m_t$

## $m_t$ scheme dependence (pole v.s. $\overline{MS}$ ) [%]

$M_H$ [GeV]	7 TeV	8 TeV	13 TeV	13.6 TeV	14 TeV
120	0.168	0.164	0.128	0.115	0.115
122	0.165	0.159	0.164	0.165	0.166
124	0.159	0.155	0.154	0.150	0.148
124.60	0.157	0.155	0.147	0.143	0.142
124.80	0.157	0.155	0.145	0.142	0.141
125	0.156	0.154	0.143	0.141	0.140
125.09	0.156	0.154	0.143	0.140	0.139
125.20	0.155	0.152	0.142	0.139	0.139
125.30	0.155	0.151	0.133	0.132	0.128
125.38	0.155	0.151	0.133	0.132	0.128
125.60	0.154	0.151	0.133	0.132	0.127
126	0.154	0.150	0.132	0.130	0.130
128	0.147	0.142	0.127	0.125	0.121
130	0.139	0.137	0.123	0.121	0.119

- scheme dependence  
 $\sim 0.15\%$   
 $\leftrightarrow$  c.f.  $\delta(1/m_t) = 1\%$   
 (negligible before)  
 $\hookrightarrow$  matters now:  
 new uncertainty

- new default: pole mass scheme in iHixs2

# Inclusion of NNLO $m_t$

## $M_H$ extrapolation

- use  $M_H$  dependence of HTL to extrapolate

$M_H$ [GeV]	13.6 TeV	13.6 TeV
120	0.984	1.038
122	0.985	1.037
124	0.985	1.036
124.60	0.985	1.035
124.80	0.985	1.035
125	0.984	1.035
125.09	0.984	1.035
125.20	0.984	1.035
125.30	0.984	1.035
125.38	0.984	1.035
125.60	0.984	1.035
126	0.984	1.034
128	0.984	1.033
130	0.984	1.032

- very stable ratio  $\leftrightarrow$  use extrapolation

$$\frac{\delta\sigma^{\text{HTL}}(M_H) \Big|_{\mathcal{O}(\alpha_s^4)}}{\delta\sigma^{\text{HTL}}(M_H^{\text{ref}}) \Big|_{\mathcal{O}(\alpha_s^4)}} \times \delta\sigma^{\text{exact}}(M_H^{\text{ref}}) \Big|_{\mathcal{O}(\alpha_s^4)}$$

$\hookrightarrow$  uncertainty: conservative 100%  
 $\lesssim 0.03\%$

$$\delta^{\text{extrap}}(M_H) = \left| 1 - \frac{\delta\sigma^{\text{HTL}}(M_H) \Big|_{\mathcal{O}(\alpha_s^4)}}{\delta\sigma^{\text{HTL}}(M_H^{\text{ref}}) \Big|_{\mathcal{O}(\alpha_s^4)}} \right|$$

$$\frac{\delta\sigma^{\text{exact}}(M_H) \Big|_{\mathcal{O}(\alpha_s^3)}}{\delta\sigma^{\text{HTL}}(M_H) \Big|_{\mathcal{O}(\alpha_s^3)}}$$

$$\frac{\delta\sigma^{\text{approx.}}(M_H) \Big|_{\mathcal{O}(\alpha_s^4)}}{\delta\sigma^{\text{HTL}}(M_H) \Big|_{\mathcal{O}(\alpha_s^4)}}$$

# Inclusion of NNLO $m_t$

## Final impact from NNLO $m_t$

$\sqrt{s}$ [TeV]	$M_H$ [GeV]	$\sigma$ [pb]	$\delta(\text{scale})$	$\delta(\text{EWK})$	$\delta(\text{t, b, c})$	$\delta\Sigma(m_t)$	$\delta(\text{theory})$
13.6	120.00	55.90	+0.56% -3.32%	$\pm 1.00\%$	$\pm 0.85\%$	$\pm 0.15\%$	+2.56% -1.32%
13.6	122.00	54.31	+0.56% -3.31%	$\pm 1.00\%$	$\pm 0.84\%$	$\pm 0.19\%$	+2.59% -1.28%
13.6	124.00	52.79	+0.56% -3.31%	$\pm 1.00\%$	$\pm 0.83\%$	$\pm 0.16\%$	+2.55% -1.32%
13.6	124.60	52.35	+0.56% -3.31%	$\pm 1.00\%$	$\pm 0.83\%$	$\pm 0.15\%$	+2.53% -1.33%
13.6	124.80	52.20	+0.56% -3.31%	$\pm 1.00\%$	$\pm 0.83\%$	$\pm 0.14\%$	+2.53% -1.33%
13.6	125.00	52.06	+0.56% -3.31%	$\pm 1.00\%$	$\pm 0.83\%$	$\pm 0.14\%$	+2.53% -1.34%
13.6	125.09	51.99	+0.56% -3.31%	$\pm 1.00\%$	$\pm 0.83\%$	$\pm 0.14\%$	+2.52% -1.34%
13.6	125.20	51.91	+0.56% -3.31%	$\pm 1.00\%$	$\pm 0.83\%$	$\pm 0.14\%$	+2.52% -1.34%
13.6	125.30	51.84	+0.56% -3.30%	$\pm 1.00\%$	$\pm 0.83\%$	$\pm 0.13\%$	+2.52% -1.34%
13.6	125.38	51.78	+0.56% -3.30%	$\pm 1.00\%$	$\pm 0.83\%$	$\pm 0.13\%$	+2.52% -1.34%
13.6	125.60	51.62	+0.55% -3.30%	$\pm 1.00\%$	$\pm 0.83\%$	$\pm 0.14\%$	+2.52% -1.34%
13.6	126.00	51.33	+0.55% -3.30%	$\pm 1.00\%$	$\pm 0.82\%$	$\pm 0.14\%$	+2.51% -1.34%
13.6	128.00	49.94	+0.55% -3.29%	$\pm 1.00\%$	$\pm 0.81\%$	$\pm 0.14\%$	+2.51% -1.33%
13.6	130.00	48.60	+0.55% -3.28%	$\pm 1.00\%$	$\pm 0.80\%$	$\pm 0.15\%$	+2.51% -1.33%

- linearly add **uncertainties** from ( $m_t$  scheme dependence) + (extrapolation)
  - $\leftrightarrow$  dominant piece: scheme dependence
  - $\hookrightarrow$  net effect: previous **1%** reduced to  $\sim$  **0.15%**
- full set of numbers in "table\_comp.pdf" (attachment on indico)

# Inclusion of mixed QCD-EW

$$\text{iHixs: } \hat{\sigma}_{ij} = R_{\text{LO}} C^2 \left[ \sigma_{ij}^{\text{LO, EFT}} + \sigma_{ij}^{\text{NLO, EFT}} + \sigma_{ij}^{\text{NNLO, EFT}} + \sigma_{ij}^{\text{N}^3\text{LO, EFT}} \right] \\ + \delta\sigma_{ij}^{\text{LO, (t,b,c)}} + \delta\sigma_{ij}^{\text{NLO, (t,b,c)}} + \delta\sigma_{ij}^{\text{NNLO, (t)}} + R_{\text{LO}} C^2 \delta\sigma_{ij}^{\text{Res}}.$$

- start with iHixs prediction and systematically incorporate new results
- inclusion of EW corrections by [Becchetti, Bonciani, Del Duca, Hirschi, Moriello, Schweitzer 20](#)  
iHixs formula based on *factorization hypothesis*:

$$C = C_{\text{QCD}} + \lambda_{\text{EWK}} \left( 1 + \frac{\alpha_S}{\pi} C_{1w} + \dots \right).$$

↪ iHixs uses  $C_{1w} = 7/6$  as estimated from the  $M_V \rightarrow \infty$  limit

↪ full result gives:  $C_{1w} = -1.7$  ( $\mu_R = M_H/2$ )  $C_{1w} = -2.1$  ( $\mu_R = M_H$ )

**but note:**  $\delta(\text{EW}) \sim \pm 1\%$   $\Leftrightarrow$  vary  $C_{1w}$  by factor in range  $[-3, 6]$

**Initial proposal:** incorporate new result with an additional correction term (1st step)

$$\delta\sigma_{ij}^{\text{EW}} = \sigma_{ij}^{\text{EW}} - \left[ C^2 R_{\text{LO}} \sigma_{ij}^{\text{EFT}} \right]_{\alpha_s^3 \alpha^2}$$

and define error estimates on correction factor (beyond light quarks, gg channel, ...)

# Inclusion of mixed QCD-EW

## Impact from naive replacement $C_{1w} \rightarrow -1.7$

Becchetti, Bonciani, Del Duca,  
Hirschi, Moriello, Schweitzer 20

E [TeV]	$M_H$ [GeV]	$\sigma$ [pb]	$\sigma _{C_{1w} \rightarrow -1.7}$ [pb]	$\Delta$ [%]
7.0	125.09	16.757	16.668	0.530
8.0	125.09	21.326	21.213	0.530
13.0	125.09	48.497	48.240	0.530
13.6	125.09	52.140	51.864	0.529
14.0	125.09	54.611	54.321	0.529

- approx. constant impact  
( $\sqrt{s}$  &  $M_H$  variation)

$\sim 0.5\%$

- well within the  
 $\delta(\text{EWK}) = \pm 1\%$   
uncertainty estimate

- caveats:

$\hookrightarrow$  only gg channel

E [TeV]	$M_H$ [GeV]	$\sigma$ [pb]	$\sigma _{C_{1w} \rightarrow -1.7}$ [pb]	$\Delta$ [%]
13.6	120.00	56.099	55.812	0.512
13.6	122.00	54.494	54.211	0.519
13.6	124.00	52.953	52.675	0.526
13.6	124.60	52.504	52.227	0.528
13.6	124.80	52.355	52.078	0.529
13.6	125.00	52.206	51.930	0.529
13.6	125.09	52.140	51.864	0.529
13.6	125.20	52.059	51.783	0.530
13.6	125.30	51.986	51.710	0.530
13.6	125.38	51.927	51.652	0.530
13.6	125.60	51.766	51.491	0.531
13.6	126.00	51.476	51.202	0.533
13.6	128.00	50.062	49.792	0.539
13.6	130.00	48.706	48.440	0.546

### Current Proposal (for discussion):

- Stick with baseline using  $C_{1w} = 7/6$
- Keep 1% error