

Effective field theory analysis of rare charm decays

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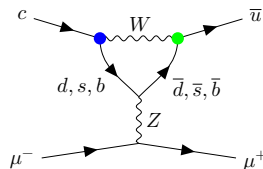
Annual meeting of the German LHCb groups and affiliated theory community



Rare charm decays

Why rare charm decays?

- Unique probe of Flavor-Changing-Neutral-Currents for up-quarks
- Complementary to down-type decays ($s \rightarrow d\mu^+\mu^-$, $b \rightarrow s\mu^+\mu^-$)
- Strong GIM and CKM suppression in $c \rightarrow u\mu^+\mu^-$
- Dominated by resonances whose theoretical prediction is challenging **BUT nulltests remain!**



$$\begin{aligned} \mathcal{A}(c \rightarrow u) &\propto \frac{1}{16\pi^2} V_{cs}^* V_{us} \left(f\left(\frac{m_s^2}{m_W^2}\right) - f\left(\frac{m_d^2}{m_W^2}\right) \right) \\ &+ \frac{1}{16\pi^2} \underbrace{V_{cb}^* V_{ub}}_{\mathcal{O}(\lambda^5)} \left(f\left(\frac{m_b^2}{m_W^2}\right) - f\left(\frac{m_d^2}{m_W^2}\right) \right) \end{aligned}$$

Compare New Physics(NP) constraints from

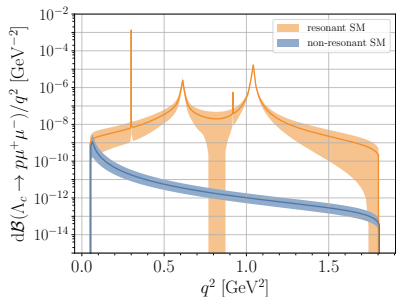
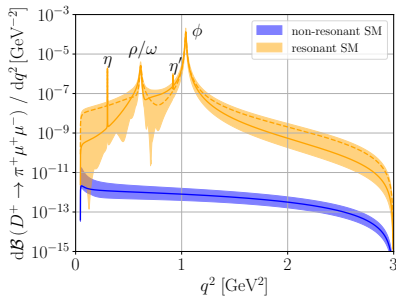
$$\begin{aligned} D^0 &\rightarrow \mu^+\mu^-, D^+ \rightarrow \pi^+\mu^+\mu^-, \\ \Lambda_c^+ &\rightarrow p\mu^+\mu^-, D^0 \rightarrow \pi^+\pi^-\mu^+\mu^- \end{aligned}$$

$$V_{cd}^* V_{ud} + V_{cs}^* V_{us} + V_{cb}^* V_{ub} = 0$$

Resonances

$$D^+ \rightarrow \pi^+ \mu^+ \mu^-$$

[Bause et al. 2020]

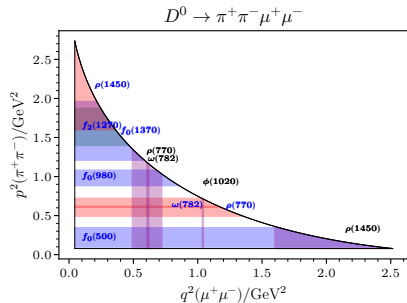
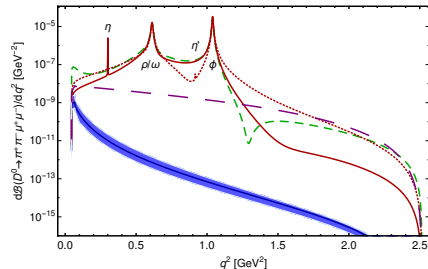


$$\Lambda_c^+ \rightarrow p \mu^+ \mu^-$$

[Golz, Hiller, and Magorschi 2021]

$$D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-$$

[De Boer and Hiller 2018]



Weak effective field theory (WET)

► Effective Hamiltonian

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} \frac{\alpha_e}{4\pi} \left[\sum_{i \neq T, T_5} \left(c_i(\mu) \mathcal{O}_i(\mu) + \overbrace{c'_i(\mu) \mathcal{O}'_i(\mu)}^{c'_i \mathcal{O}_i |_{L(R) \rightarrow R(L)}} \right) + \sum_{i=T, T_5} c_i(\mu) \mathcal{O}_i(\mu) \right]$$

$$\begin{aligned} \mathcal{O}_7 &= \frac{m_c}{e} (\bar{u}_L \sigma_{\mu\nu} c_R) F^{\mu\nu}, & \mathcal{O}_9 &= (\bar{u}_L \gamma_\mu c_L) (\bar{\ell} \gamma^\mu \ell), & \mathcal{O}_{10} &= (\bar{u}_L \gamma_\mu c_L) (\bar{\ell} \gamma^\mu \gamma_5 \ell), \\ \mathcal{O}_{S(P)} &= (\bar{u}_L c_R) (\bar{\ell} (\gamma_5) \ell), & \mathcal{O}_{T(T_5)} &= \frac{1}{2} (\bar{u} \sigma_{\mu\nu} c) (\bar{\ell} \sigma^{\mu\nu} (\gamma_5) \ell). \end{aligned}$$

► SM Wilson coefficients negligible

$$|\mathcal{C}_9^{\text{eff}}(q^2)| \lesssim 0.01, \quad |\mathcal{C}_7^{\text{eff}}(q^2)| \simeq \mathcal{O}(0.001) \quad [\text{De Boer and Hiller 2018}]$$

► all others vanish and create **null test** opportunities

$$\mathcal{C}_{10, S, P, T, T_5}^{\text{SM}} = \mathcal{C}'_{7, 9, 10, S, P}{}^{\text{SM}} = 0 \Rightarrow \mathcal{C}_i \equiv \mathcal{C}_i^{\text{NP}}$$

Experimental status

	$D^0 \rightarrow \mu^+ \mu^-$	$D^+ \rightarrow \pi^+ \mu^+ \mu^-$	$\Lambda_c^+ \rightarrow p \mu^+ \mu^-$	$D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-$
upper limits BR	✓	full- q^2 , (low- q^2 , high- q^2)	low- q^2 , high- q^2 , combined, full- q^2	high- q^2
resonant BR	$< 4 \cdot 10^{-11}$	\mathcal{B}_ϕ , narrow-width approx. (NWA)	$\frac{\mathcal{B}_{\omega\text{-region}}}{\mathcal{B}_{\phi\text{-region}}}, \frac{\mathcal{B}_{\rho\text{-region}}}{\mathcal{B}_{\phi\text{-region}}},$ NWA	$\mathcal{B}_{\omega/\rho\text{-region}}, \mathcal{B}_{\phi\text{-region}}$ $\left(\frac{d\Gamma}{dm_{\mu^+\mu^-}}, \frac{d\Gamma}{dm_{\pi^+\pi^-}} \right)$
angular obs.	—	not measured	not measured	CP-sym./CP-asym. $\langle S_{2-9} \rangle, \langle A_{2-9} \rangle$

- ▶ Angular observables include **null tests** sensitive to NP
- ▶ For this we need to fix resonance parameters as best as we can from available measurements

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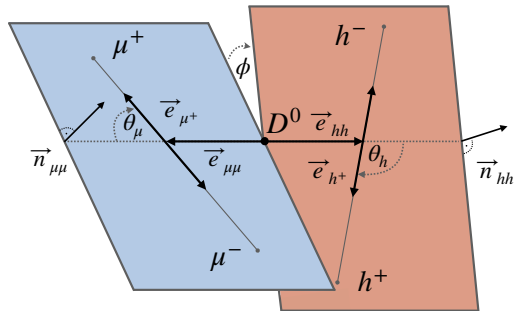
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$$D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-$$

► 5-differential distribution:

[Cappiello, Cata, and D'Ambrosio 2013, De Boer and Hiller 2018]

$$\frac{d^5 \Gamma}{dq^2 dp^2 d \cos \theta_{P_1} d \cos \theta_\ell d \phi} = \frac{1}{2\pi} \sum_{i=1}^9 c_i(\theta_\ell, \phi) I_i(q^2, p^2, \cos \theta_{P_1})$$



[LHCb, arXiv: 2111.03327]

► Integrating $\cos \theta_{P_1}, p^2$ and different q^2 bins

$$\langle I_{2,3,6,9} \rangle_{[q_{\min}^2, q_{\max}^2]} = \frac{1}{\Gamma_{[q_{\min}^2, q_{\max}^2]}} \int dq^2 dp^2 \int_{-1}^1 d \cos \theta_{P_1} I_{2,3,6,9},$$

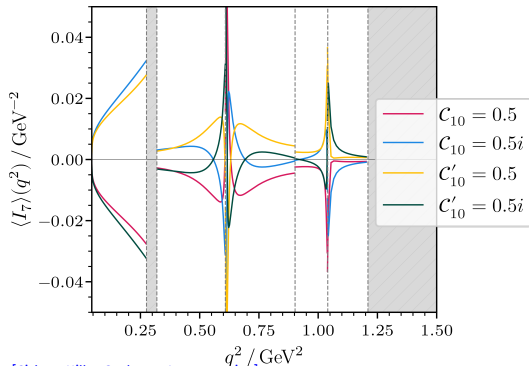
$$\langle I_{4,5,7,8} \rangle_{[q_{\min}^2, q_{\max}^2]} = \frac{1}{\Gamma_{[q_{\min}^2, q_{\max}^2]}} \int dq^2 dp^2 \left[\int_0^1 d \cos \theta_{P_1} - \int_{-1}^0 d \cos \theta_{P_1} \right] I_{4,5,7,8},$$

$$D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-$$

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[Gisbert, Hiller, Suelmann In preparation]

► Integrating $\cos \theta_{P_1}, p^2$ and different q^2 bins

Null tests: $\langle I_{5,6,7} \rangle + \text{CP-asymmetries}$

$$\langle I_{2,3,6,9} \rangle_{[q_{\min}^2, q_{\max}^2]} = \frac{1}{\Gamma_{[q_{\min}^2, q_{\max}^2]}} \int dq^2 dp^2 \int_{-1}^1 d \cos \theta_{P_1} I_{2,3,6,9},$$

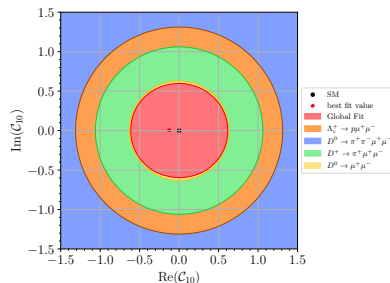
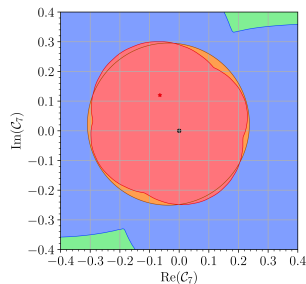
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Fits of Wilson coefficients

- ▶ Compare upper limits from branching ratios and null tests
- ▶ Upper limits from $D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-$ are the weakest
 - ▶ strong phases in charm (main source of uncertainty)
 - ▶ experimental sensitivity not there yet
 - ▶ Theory prediction more challenging than 3-body decays
- ▶ Best constrains for \mathcal{C}_{10} from $D^0 \rightarrow \mu^+ \mu^-$
- ▶ Best constrains for \mathcal{C}_7 from low- q^2 of $\Lambda_c^+ \rightarrow p \mu^+ \mu^-$

Future directions

- ▶ Should focus on NP potential in hadronic simpler decays
- ▶ $\Lambda_c \rightarrow p \mu^+ \mu^-$ with null test for \mathcal{C}_{10}



[Gisbert, Hiller, Suelmann In preparation]

- ▶ Double differential distribution

depends on: $f_i(q^2)$, $c_9^{\mathcal{R}}$, c_i^{NP}

$$\frac{d^2\Gamma}{dq^2 d\cos\theta_\ell} = \frac{3}{2} (K_{1ss}(q^2) \sin^2\theta_\ell + K_{1cc}(q^2) \cos^2\theta_\ell + K_{1c}(q^2) \cos\theta_\ell) .$$

- ▶ Long-distance contribution modeled with ansatz

$$c_9^{\mathcal{R}}(q^2) = \frac{\mathbf{a}_\rho e^{i\delta_\rho}}{q^2 - m_\rho^2 + i m_\rho \Gamma_\rho} + \frac{\mathbf{a}_\omega e^{i\delta_\omega}}{q^2 - m_\omega^2 + i m_\omega \Gamma_\omega} + \frac{\mathbf{a}_\phi e^{i\delta_\phi}}{q^2 - m_\phi^2 + i m_\phi \Gamma_\phi} ,$$

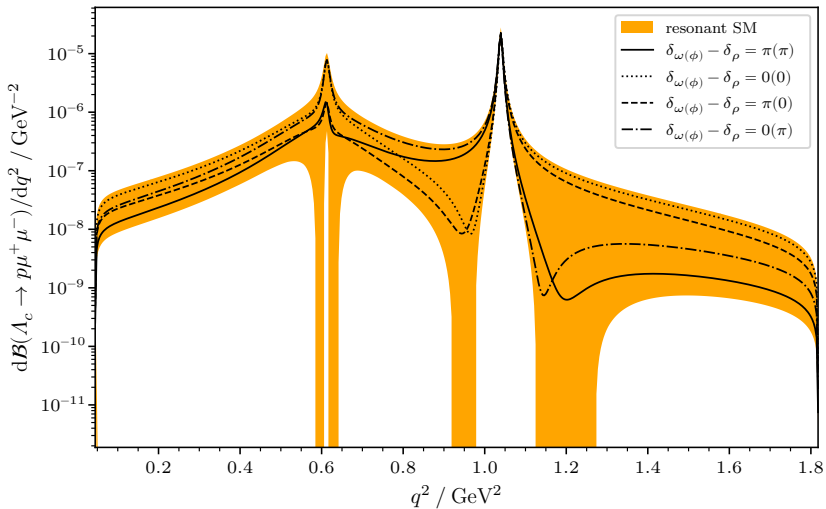
- ▶ Take **Lattice QCD form factors** [Meinel 2018] and $\mathcal{B}(\Lambda_c^+ \rightarrow p \mu^+ \mu^-)$ data [LHCb, arXiv: 2407.11474]

$$\langle p(k, s_p) | \bar{u} \gamma^\mu c | \Lambda_c(p, s_{\Lambda_c}) \rangle = \bar{u}_p(k, s_p) \left[\mathbf{f}_0(q^2) (m_{\Lambda_c} - m_p) \frac{q^\mu}{q^2} + \dots \right] u_{\Lambda_c}(p, s_{\Lambda_c})$$

- ▶ Fit parameters $\mathbf{a}_{\mathcal{R}}$, but **relative phases unconstrained!** measure: high- q^2 & between m_ρ^2 and m_ϕ^2

$$\mathbf{a}_\phi = 0.108_{-0.008}^{+0.008} , \mathbf{a}_\omega = 0.074_{-0.015}^{+0.012} , \mathbf{a}_\rho = 0.50_{-0.06}^{+0.06} ,$$

$$\Lambda_c^+ \rightarrow p\mu^+\mu^-$$



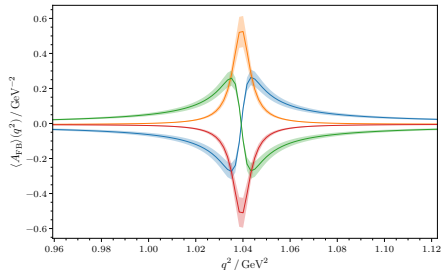
[Gisbert, Hiller, Suelmann In preparation]

Future improvements with $\Lambda_c^+ \rightarrow p\mu^+\mu^-$ null tests

- ▶ Forward-backward asymmetry of the lepton pair

$$\langle A_{\text{FB}} \rangle(q^2) = \frac{1}{\langle \Gamma \rangle} \left[\int_0^1 - \int_{-1}^0 \right] \frac{d^2\Gamma}{dq^2 d \cos \theta_l} d \cos \theta_l$$
$$\propto \text{Re} \{ \mathcal{C}_9^{\mathcal{R}} \mathcal{C}_{10}^* \}$$

- ▶ Strongly depends on an overall strong phase of $\mathcal{C}_9^{\mathcal{R}}$
- ▶ Binning is important around resonances



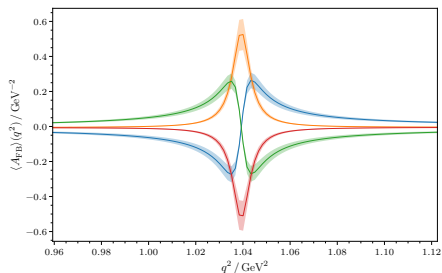
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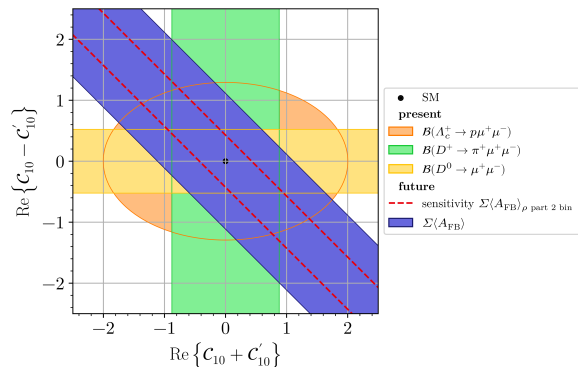
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- ▶ Complementary to limits from BR

[Gisbert, Hiller, Suelmann In preparation]



Rare charm decays are essential to test FCNCs in the up-sector

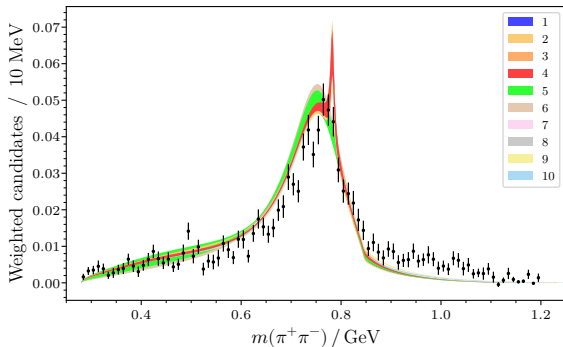
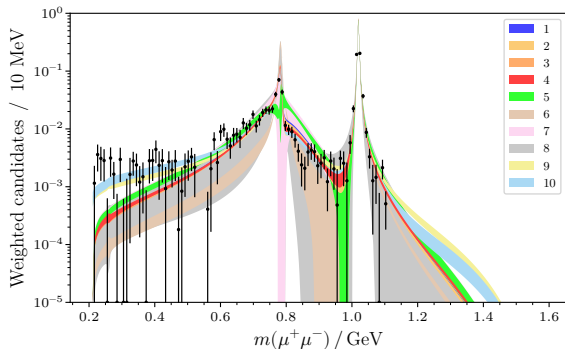
- ▶ Progress in charm is starting, more modes / observables are getting measured
- ▶ present $D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-$ null tests less sensitive than BRs
 - ▶ NP limits weaker due to strong phases
 - ▶ theory prediction more challenging
- ▶ Low- q^2 and high- q^2 BR give stronger bounds, but will reach resonant SM contribution eventually
- ▶ Focus on $\langle A_{\text{FB}} \rangle$ null test in $A_c \rightarrow p \mu^+ \mu^-$
- ▶ More than one mode required for complementarity

Thank you for your attention!

Backup

Fit of resonance parameters

- ▶ $\frac{d\Gamma}{d\sqrt{q^2}}, \frac{d\Gamma}{d\sqrt{p^2}}, \langle S_{2,3,4} \rangle$ and \mathcal{B} for normalization
- ▶ Different scenarios depending on which data to include / assumptions about amplitude
- ▶ Scenario 2 as in [\[Fajfer, Solomonidi, and Vale Silva 2023\]](#)
- ▶ Choosing scenario 4 with lowest likelihood (excluding NPs)



$$D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-$$

[Gisbert, Hiller, Suelmann In preparation]

Some problems with SM fit

- ▶ discrepancy in $\langle S_{2,3,4} \rangle$ data partially in low- q^2
- ▶ $\langle \mathcal{B} \rangle$ in first bin disagrees, no direct data on second bin
- ▶ low- q^2 for $d\Gamma/dq^2$ and high- p^2 for $d\Gamma/dp^2$ disagree
- ▶ $\langle S_9 \rangle_{\text{SM/NP}} = 0$, but $\langle S_9 \rangle = (16.9 \pm 4.4)\%$ for $[0.950-1.02]$ GeV, a local anomaly of 3.8σ

What is the solution?

- ▶ more precise p^2, q^2 binning and double differential
- ▶ for now exclude low- q^2 region
- ▶ null tests limits more conservative & less effected

