

# EICでの物理（実験）

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THE UNIVERSITY OF TOKYO



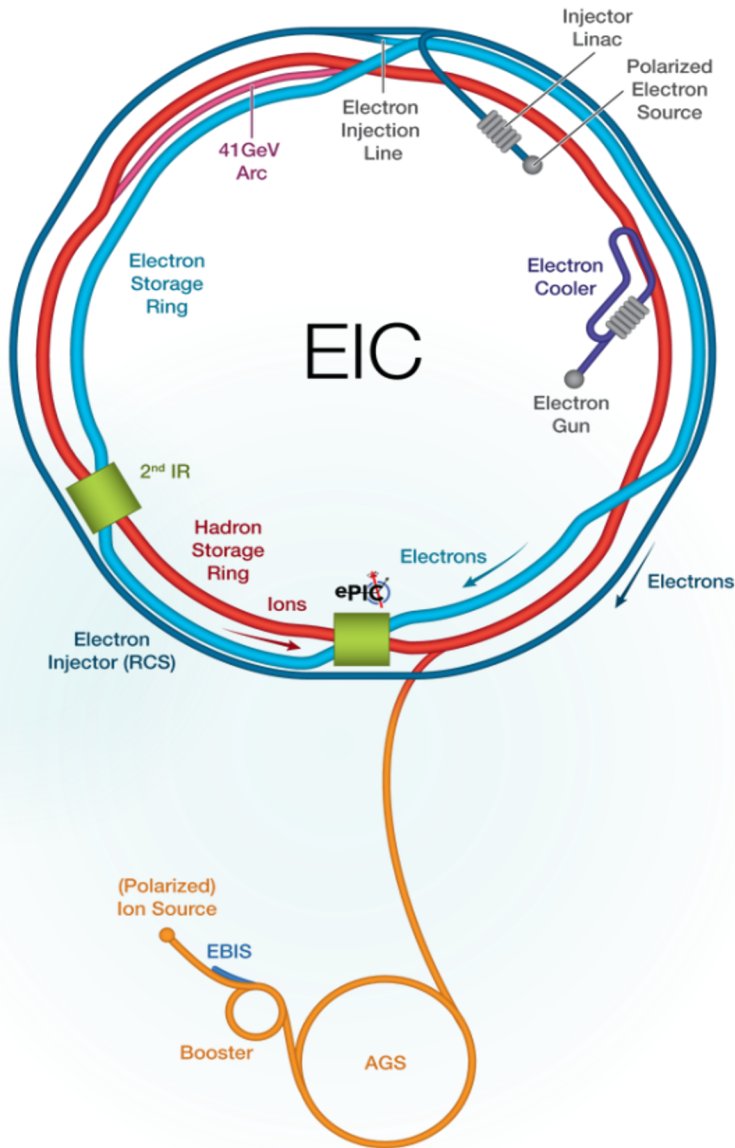
# Outline

- ▶ **What is EIC and Why EIC is so important (my personal view)?**
- ▶ **High-Energy QCD Physics**
- ▶ **DIS and Parton distribution**
- ▶ **Physics topics at the EIC**
  - ▶ **3D parton structure**
  - ▶ **spin, mass, pressure**
  - ▶ **gluon saturation, hadronization**
- ▶ **Experiment**
- ▶ **Summary**

**What is EIC and why EIC is so important (my personal view)?**

# Electron-Ion Collider

4



**EIC = a machine that will unlock the secrets of the strongest force in Nature**

- the major US project in the field of nuclear physics
- the world's first collider for polarized electron and polarized proton (and light ions) and electron-nucleus collisions

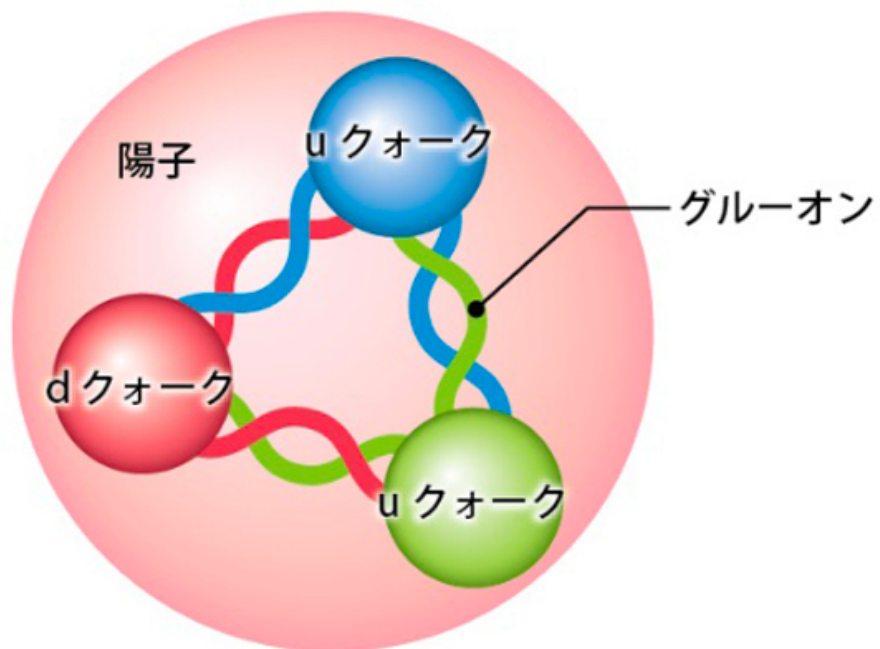
- EIC hosted at Brookhaven National Laboratory
- 80% polarized electrons from 5-18 GeV
- 70% polarized protons from 40-275 GeV
- Ions from 40-110 GeV/u
- Polarized light ions 40 -184 GeV ( $\text{He}^3$ )
- 100-1000 x HERA luminosities:  $10^{33}$ - $10^{34} \text{ cm}^{-2}\text{s}^{-1}$
- CMS energies:  $\sqrt{s} = 29$ – $140 \text{ GeV}$
- foreseen to start operation in early 2030's

# Electron-Ion Collider

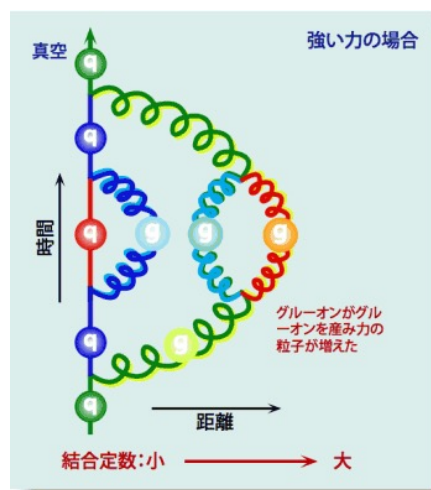
## Internal structure of nucleon and nucleus

教科書的には

3 valence quarks

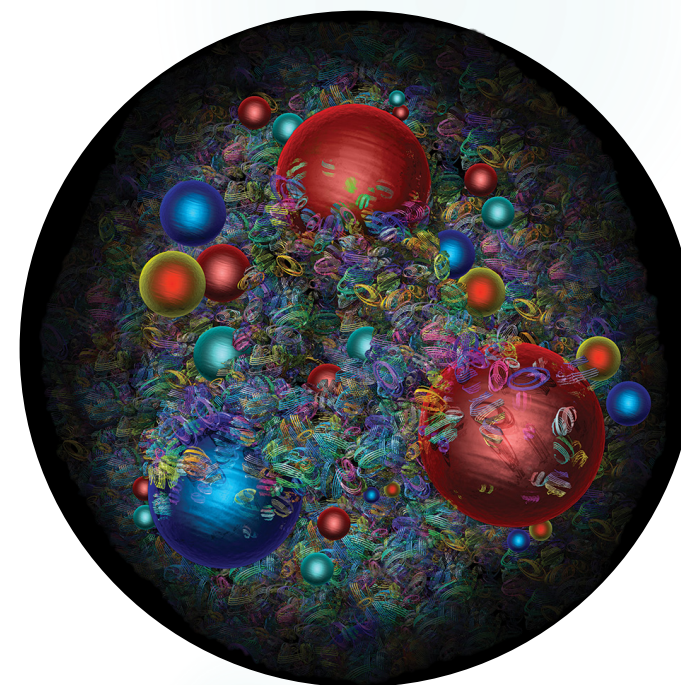


quantum fluctuation

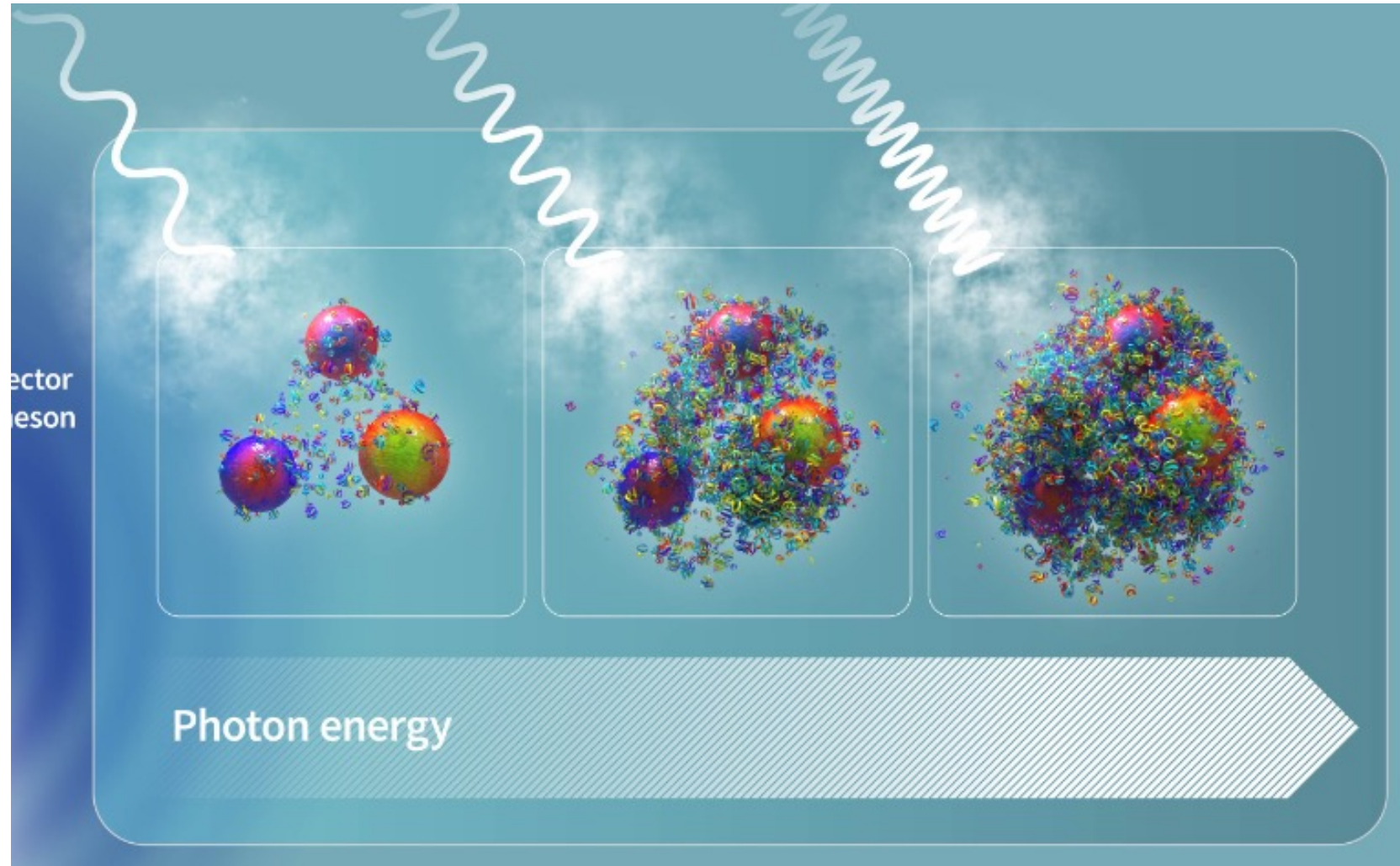
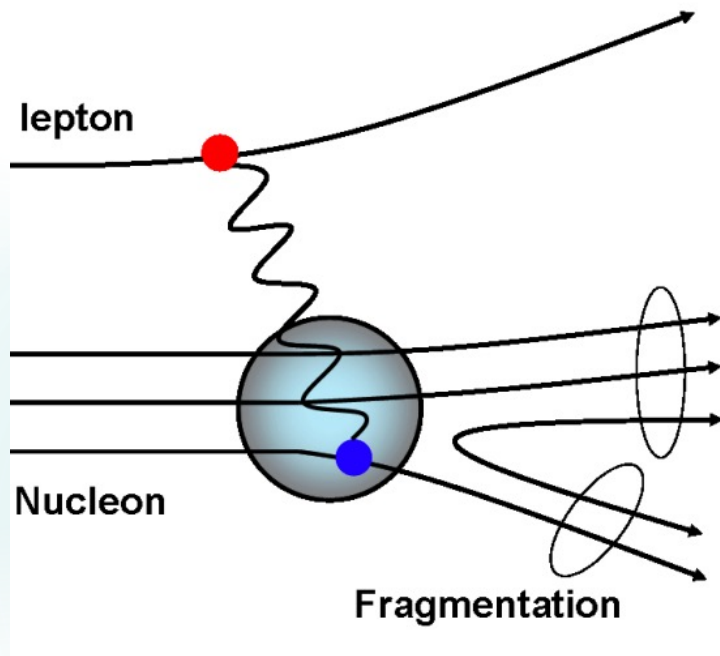


実際は

Dense quark & anti-quark pairs and gluons

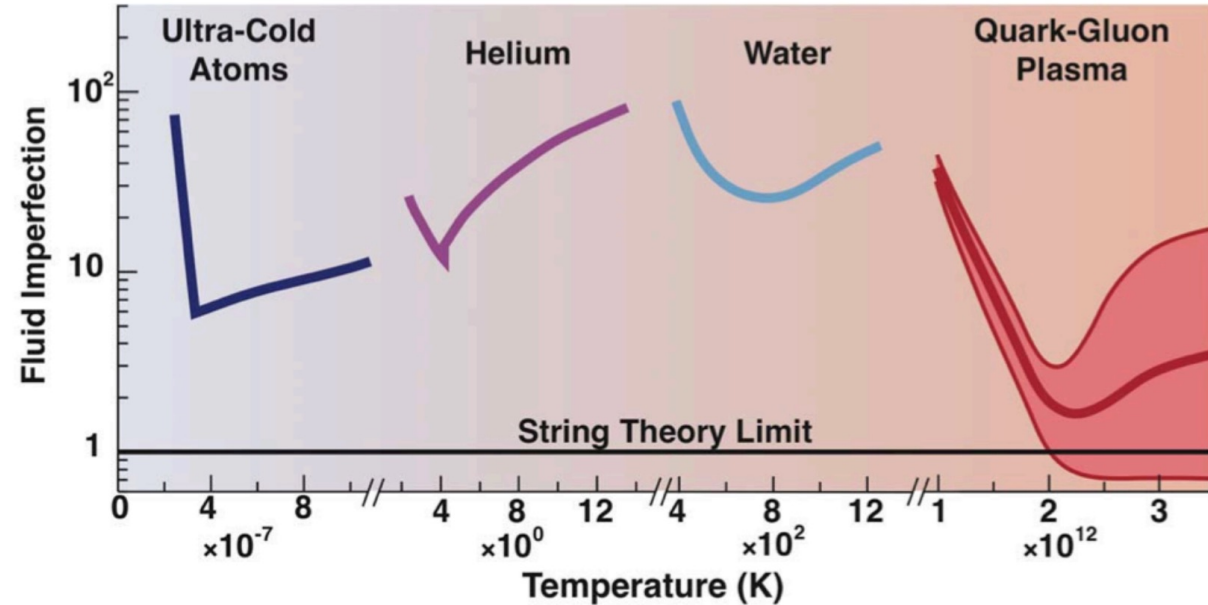
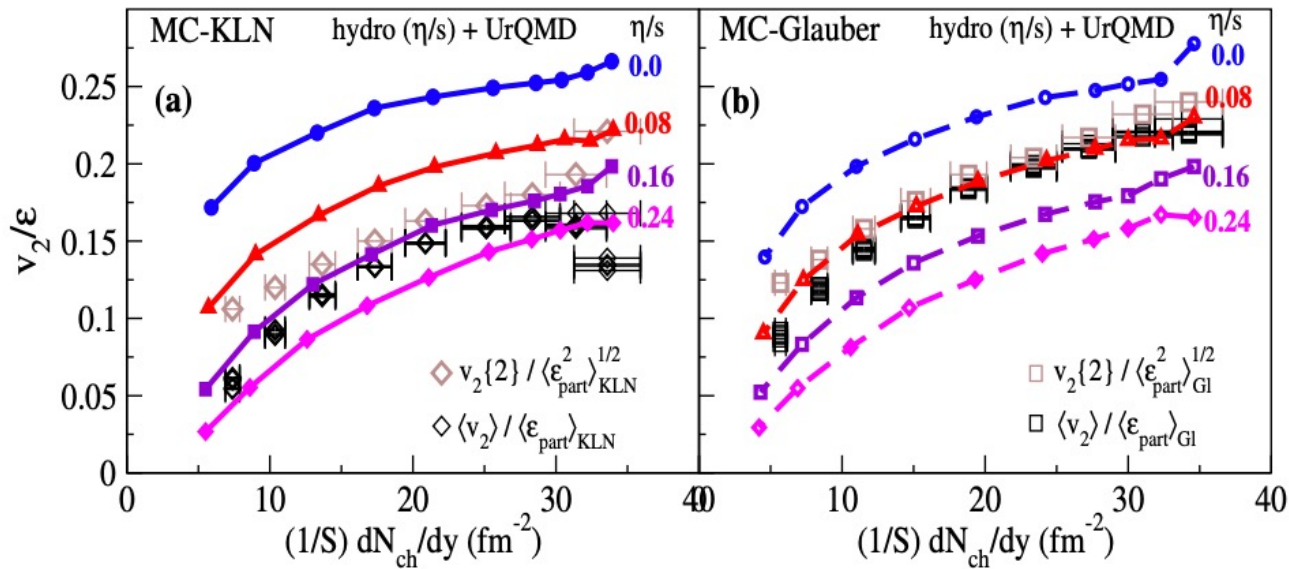


# Electron-Ion Collider



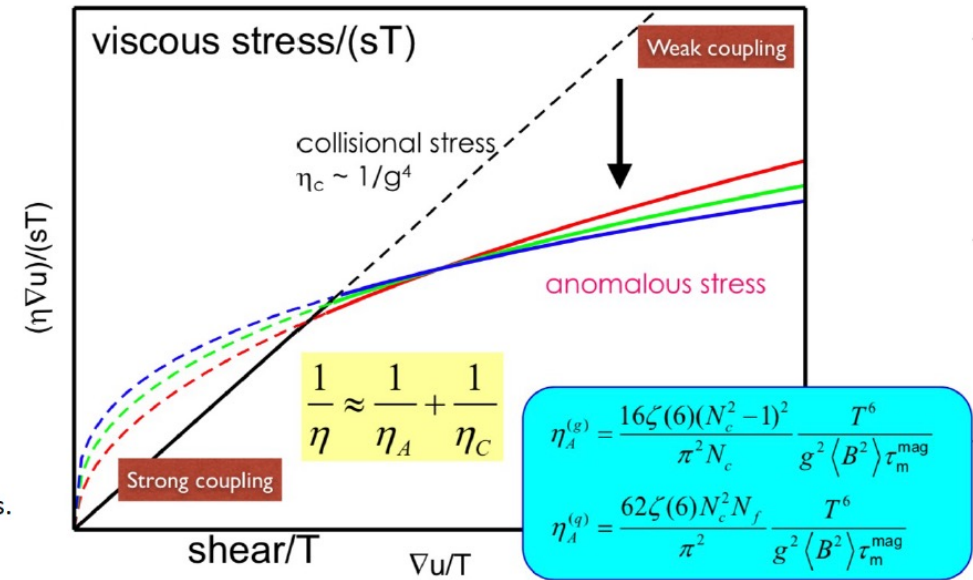
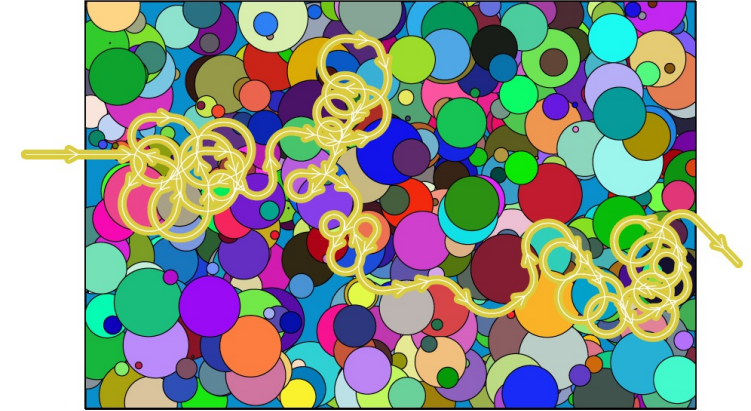
# Why EIC is so important?

- ▶ To understand QGP properties more precisely
  - ▶ Initial conditions and early dynamics



# Why EIC is so important?

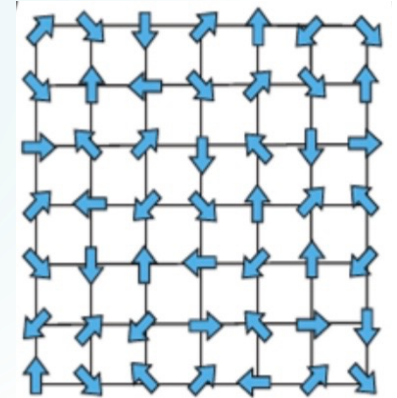
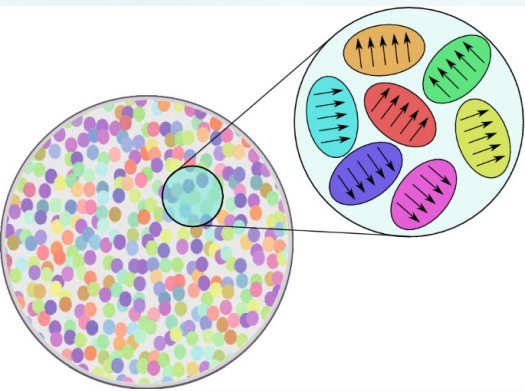
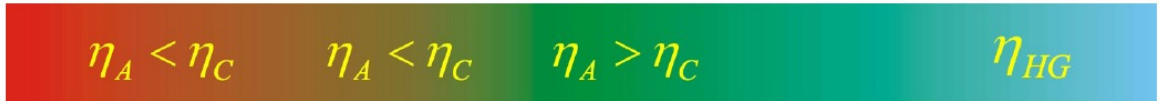
- ▶ **Characterization of gluonic matter**
  - ▶ unique matter composed of Gauge bosons
  - ▶ Anomalous viscosity in glasma?
    - ▶ Soft color fields generate anomalous transport coefficients
  - ▶ Synergies with spin-glass?



$$\frac{1}{\eta} = \frac{1}{\eta_A} + \frac{1}{\eta_C}$$

M. Asakawa, S.A. Bass & B. Mueller: Phys. Rev. Lett. 96: 252301 (2006)

temperature evolution:

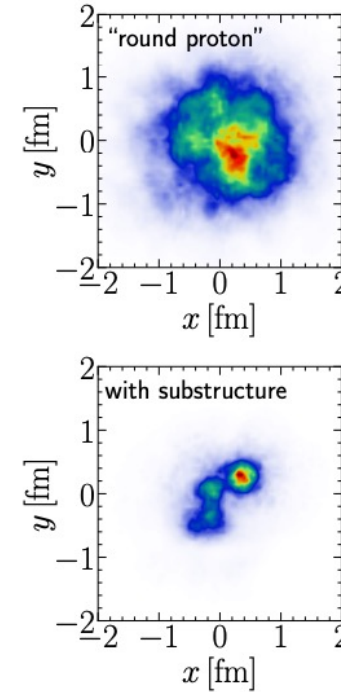
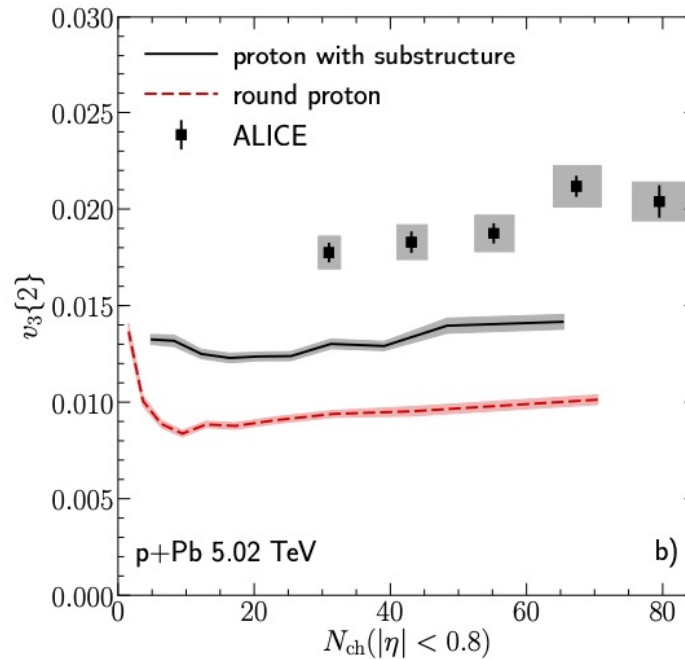
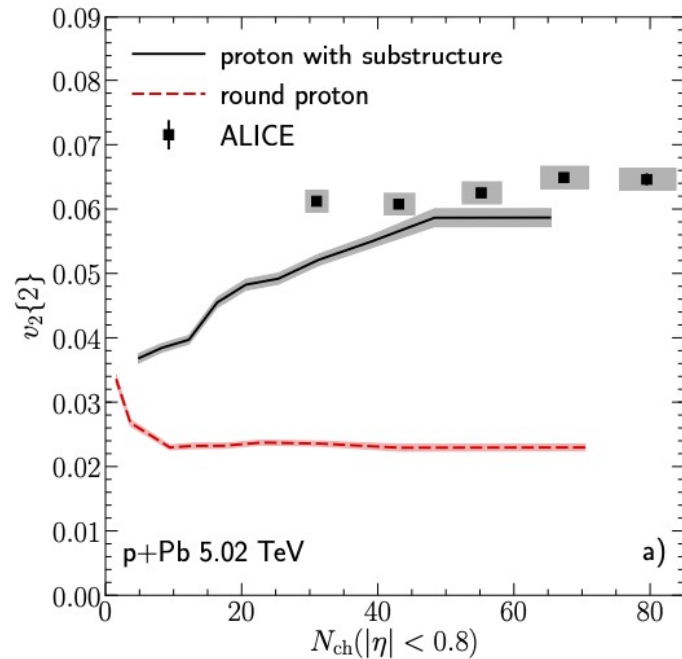




# Why EIC is so important?

- ▶ Origin of collectivity in small systems -> quantum fluctuations (“eccentric” proton)

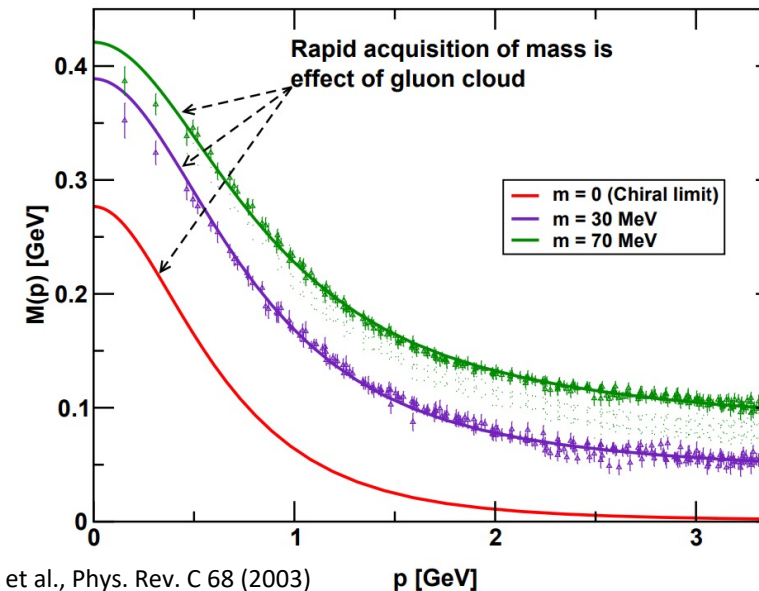
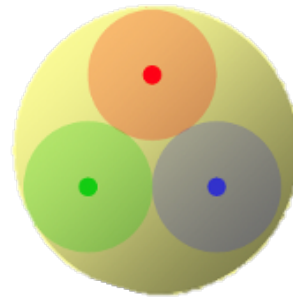
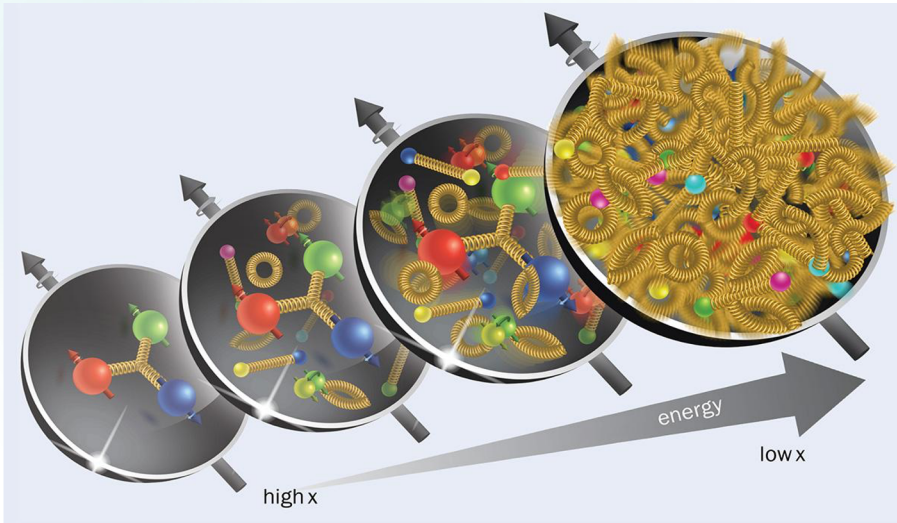
arXiv:2102.11189



**Quantum fluctuations in protons at very short time scale**  
**Dynamical structure of protons (fluctuations in parton distribution functions)**

# Why EIC is so important?

- ▶ Why proton and nucleus has so high toughness?
  - ▶ What mechanisms keep mass and spin constant?
  - ▶ Mechanisms of emergence of effective degree of freedom (localization)? -> Connection to condensed matter physics
    - ▶ Strongly correlated electrons, Heavy-fermions, superconductors, Mott-insulator



# High-Energy QCD Physics

# 11 Science Questions in 21 century

12



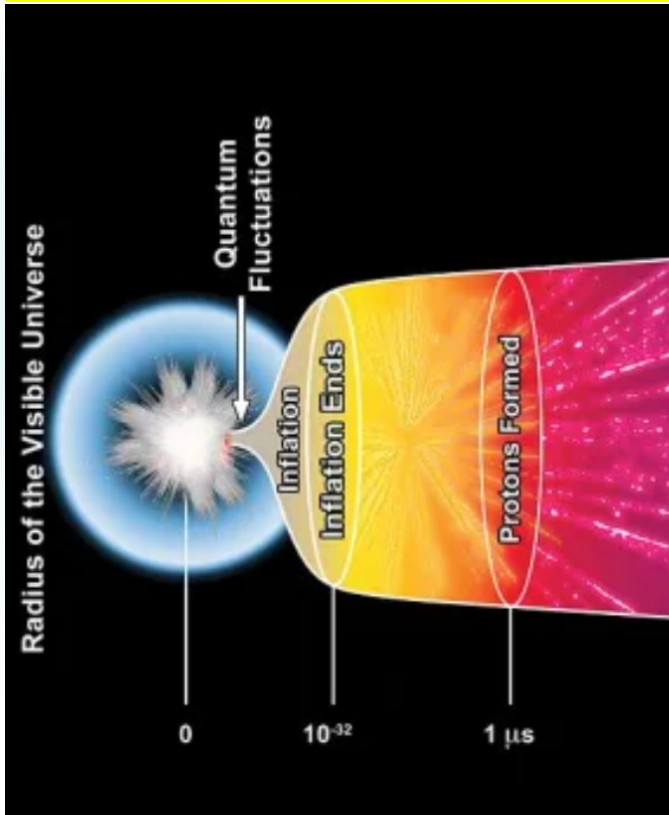
1. What is dark matter?
2. What is dark energy?
3. How were the heavy elements from Iron to Uranium made?
4. Do neutrinos have a mass?
5. Where do ultra-high energy particles come from?
6. Is a new theory of light and matter needed to explain what happens at very high energies and temperatures?
7. Are there new states of matter at ultra-high temperatures and densities?
8. Are protons unstable?
9. What is gravity?
10. Are there additional dimensions?
11. How did the Universe begin?

# 11 Science Questions in 21 century

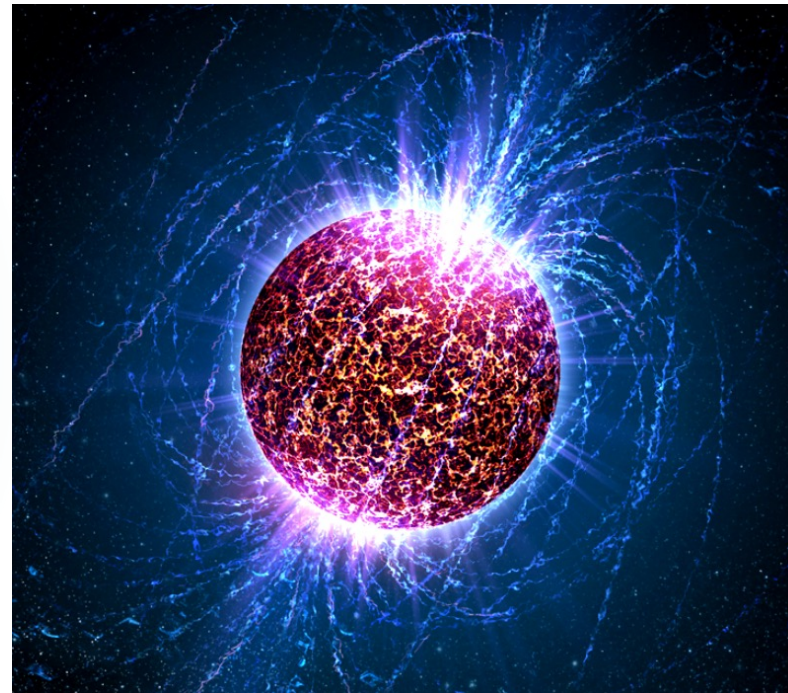
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7. Are there new states of matter at ultra-high temperatures and densities?

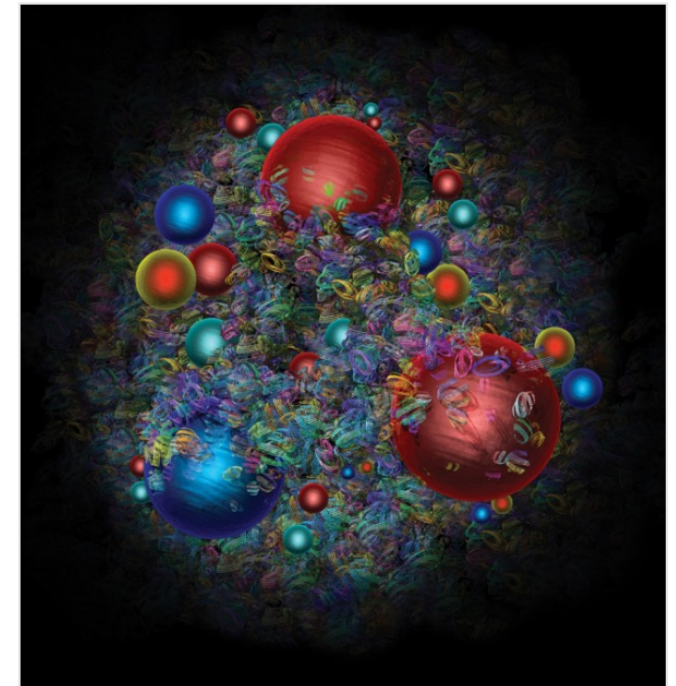
Very early universe ( $T > 100$  MeV,  $t < 10 \mu\text{sec}$ )



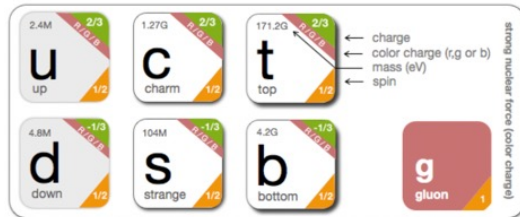
Neutron stars ( $\rho > 10^{15} \text{ g/cm}^3$ )



Dense partonic structure inside high energy proton/nuclei



## 学術振興の「ビジョン」



- 様々な状況で現れるQCDの複雑性・創発性・多様性を統一的に理解
  - 高温・高密度クォーク・グルーオン物質や核物質の相構造と物性
  - 高エネルギー核子内部の高密度クォーク・グルーオン状態
  - クォーク・グルーオン凝縮に伴うQCD真空構造とその相転移

- 素粒子物理学・物性物理学をつなぐ普遍的な自然法則を探求
- 次世代のQCD物理学を創生（例、素粒子物性物理学）

$$\mathcal{L} = \frac{1}{4g^2} G_{\mu\nu}^a G_{\mu\nu}^a + \sum_f \bar{q}_i (i\gamma^\mu D_\mu + m_f) q_i$$

where  $G_{\mu\nu}^a \equiv \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + gf_{bc}^a A_\mu^b A_\nu^c$   
and  $D_\mu = \partial_\mu + it^a A_\mu^a$   
That's it!

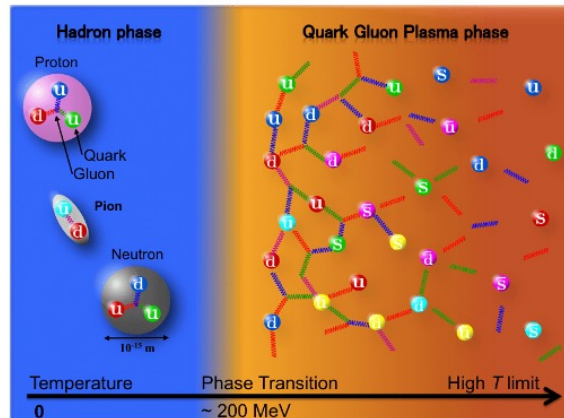
Quantum chromodynamics is conceptually simple. Its realization in nature, however, is usually very complex. But not always.

Frank Wilczek

[http://frankwilczek.com/Wilczek\\_Easy\\_Pieces/298\\_QCD\\_Made\\_Simple.pdf](http://frankwilczek.com/Wilczek_Easy_Pieces/298_QCD_Made_Simple.pdf)

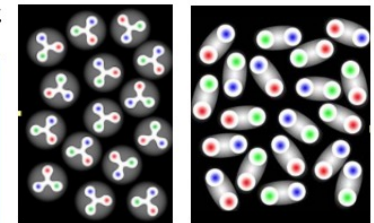
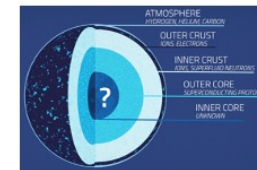
### 高温QCD

初期宇宙の物質創生  
クォークグルーオンプラズマの物性  
QCD相転移



### 高密度・ストレンジネスQCD

中性子星内部構造  
ストレンジネス核物質～カラー超伝導相  
QCD相転移



### 高エネルギーQCD



核子内パートン構造  
グルーオン飽和  
質量の起源  
摂動的QCD真空

# 未来の学術構想2022

国際高エネルギー量子科学フロンティア：海外施設で展開するQCD研究

## 計画：海外施設で展開する国際共同実験

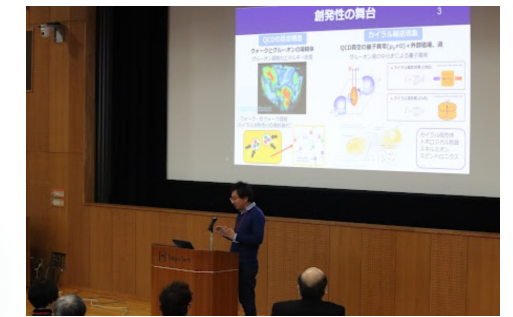


# 核談70周年記念シンポジウム

<https://indico.rcnp.osaka-u.ac.jp/event/2286/>



11:00	ニイタカヤマノボレ・ナンブヤマノボレ	延與 秀人	10:55 - 11:20
	高エネルギーオーク核物理の将来：さらなる高みへ *私見に基づく	郡司 卓	11:20 - 11:45
	KEK-PSで始めた高エネルギー核物理	田中 万博	11:45 - 12:10
12:00	ストレンジネス核物理の展開	今井 憲一	12:10 - 12:35
	J-PARCでのハドロン・ハイパー核物理の進展と展望	三輪 浩司	12:35 - 13:00





## 高エネルギーQCD研究の目標

2

クォークとグルーオン多体系の創発性を通じて、  
(非摂動領域の) QCDを究める

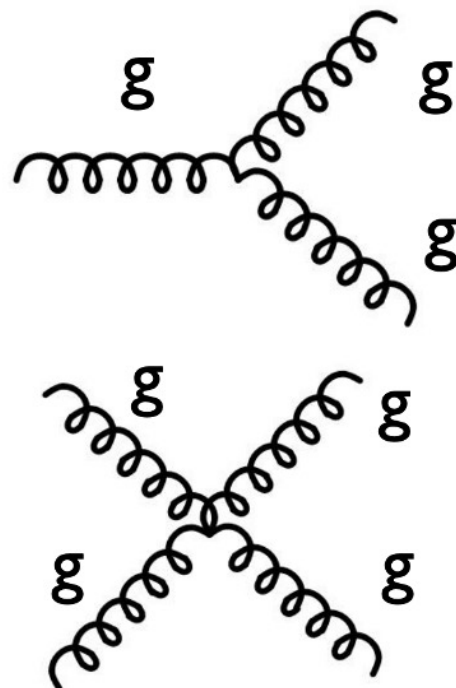
## グルーオンの自己相互作用

$$\mathcal{L} = \frac{1}{4g^2} G_{\mu\nu}^a G_{\mu\nu}^a + \sum_j \bar{q}_j (i\gamma^\mu D_\mu + m_j) q_j$$

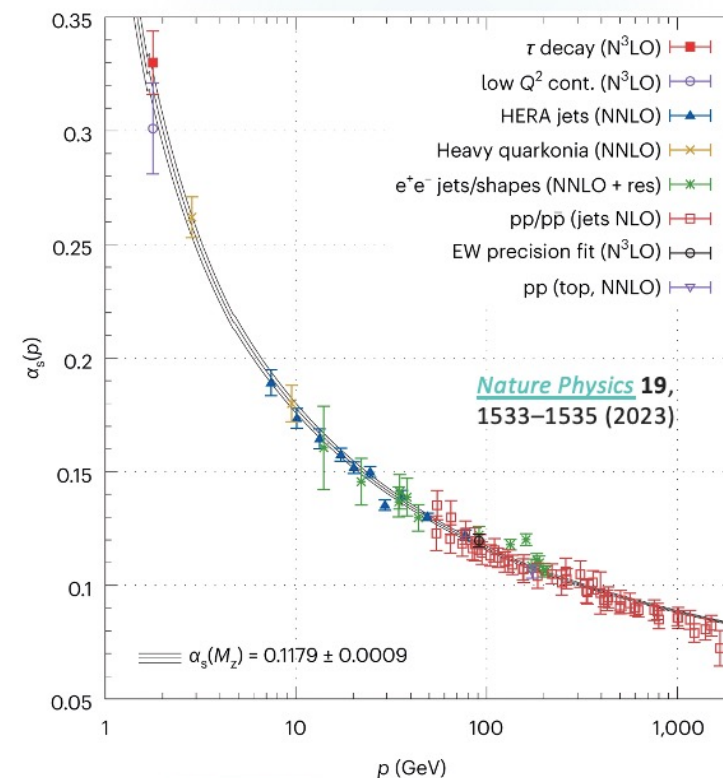
where  $G_{\mu\nu}^a \equiv \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + if_{bc}^a A_\mu^b A_\nu^c$   
and  $D_\mu \equiv \partial_\mu + it^a A_\mu^a$

That's it!

[http://frankwilczek.com/Wilczek\\_Easy\\_Pieces/298\\_QCD\\_Made\\_Simple.pdf](http://frankwilczek.com/Wilczek_Easy_Pieces/298_QCD_Made_Simple.pdf)



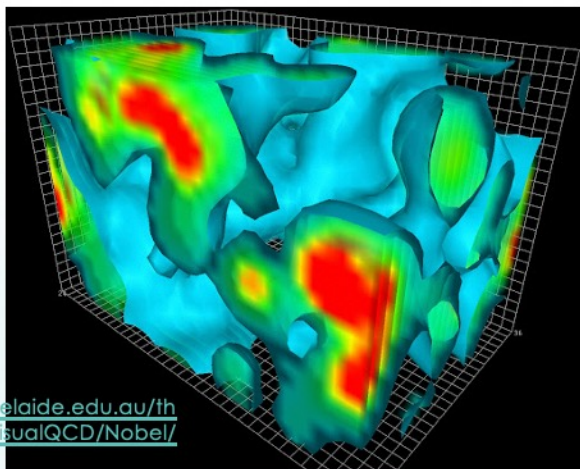
## 漸近的自由性



# 創発性の舞台

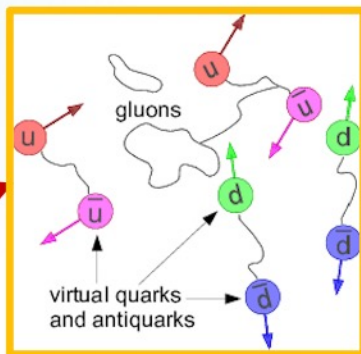
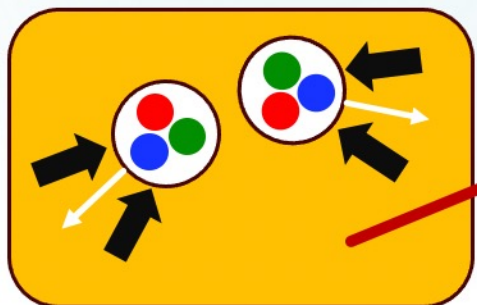
## QCDの真空構造

クォークとグルーオンの凝縮体  
グルーオン凝縮のエネルギー密度



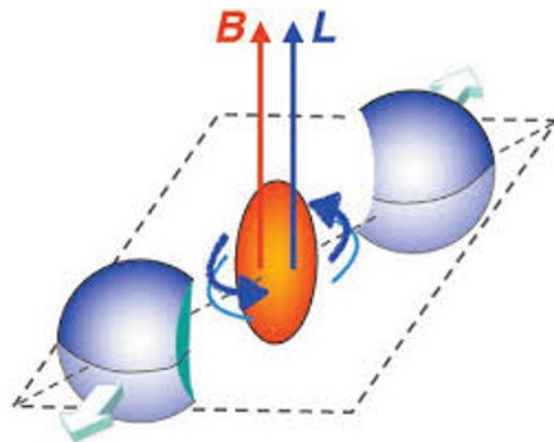
<http://www.physics.adelaide.edu.au/theory/staff/leinweber/VisualQCD/Nobel/>

クォーク・反クォーク凝縮  
(カイラル対称性の自発的破れ)



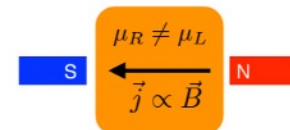
## カイラル輸送現象

QCD真空の量子異常( $\mu_5 \neq 0$ ) + 外部磁場、渦  
グルーオン場のゆらぎによる量子異常



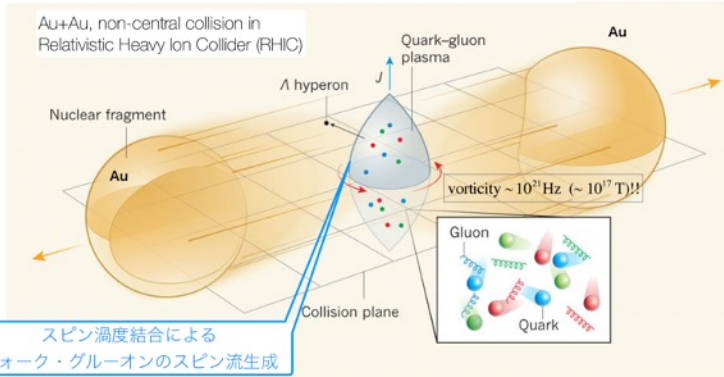
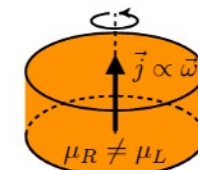
◆ カイラル磁気効果 (CME) [Fukushima et al.2008, Vilenkin 1980]

$$\vec{j} = \frac{e\mu_5}{2\pi^2} \vec{B}$$



◆ カイラル渦効果 (CVE) [Erdmenger et al. 2008, Son-Surowka 2009]

$$\vec{j} = \frac{\mu\mu_5}{2\pi^2} \vec{\omega}$$



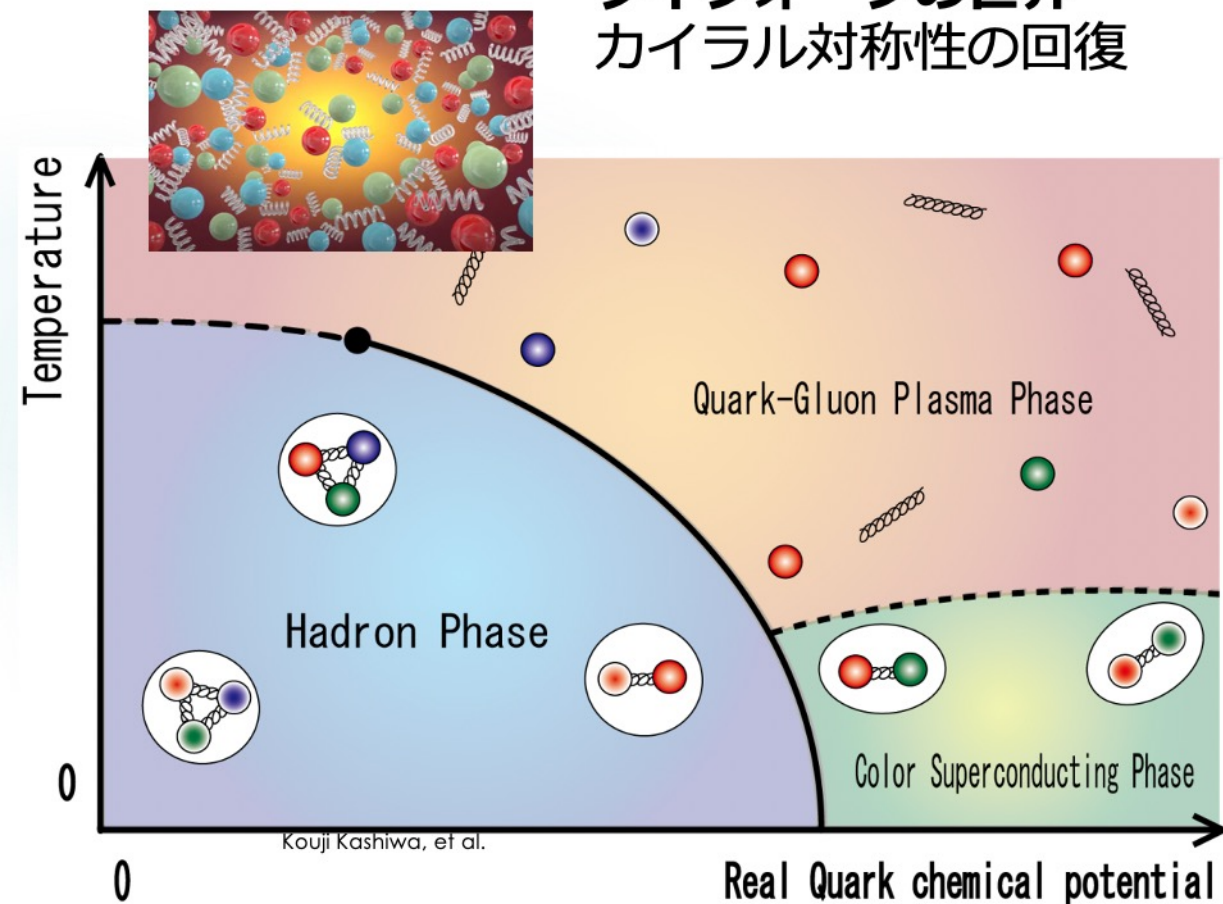
スピン渦度結合による  
クォーク・グルーオンのスピン流生成

カイラル磁性体  
トポロジカル物質  
スキルミオン  
スピントロニクス  
...

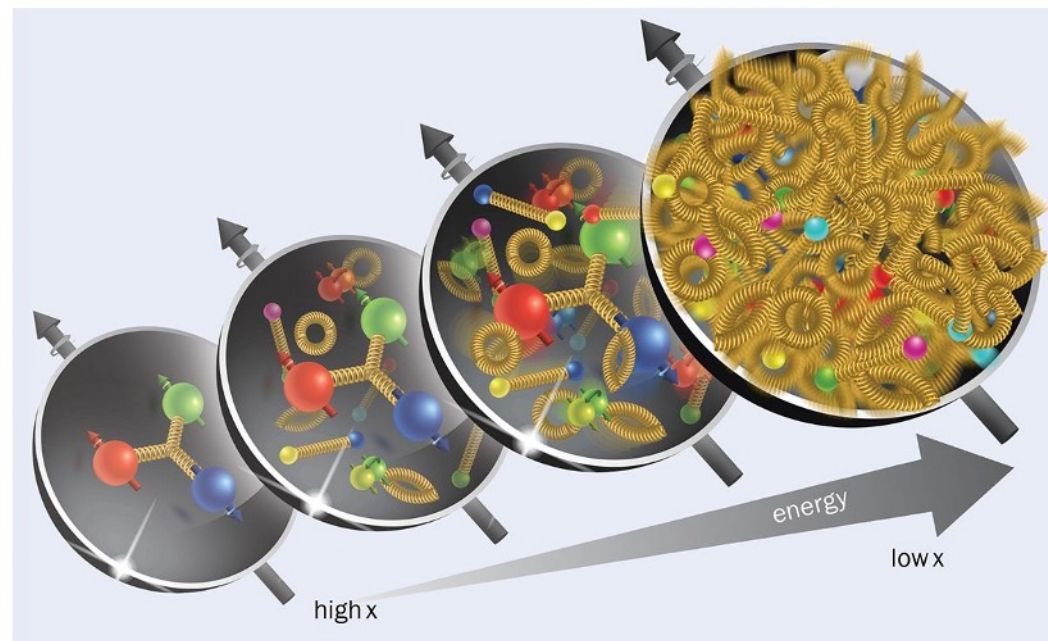
# 創発性の舞台

## QCD物質の相構造

クォーク・反クォークの世界  
ダイクォークの世界  
カイラル対称性の回復

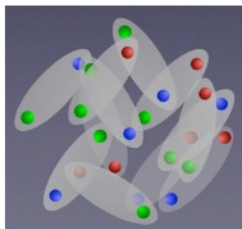


## 核子と原子核の内部構造・核スピン

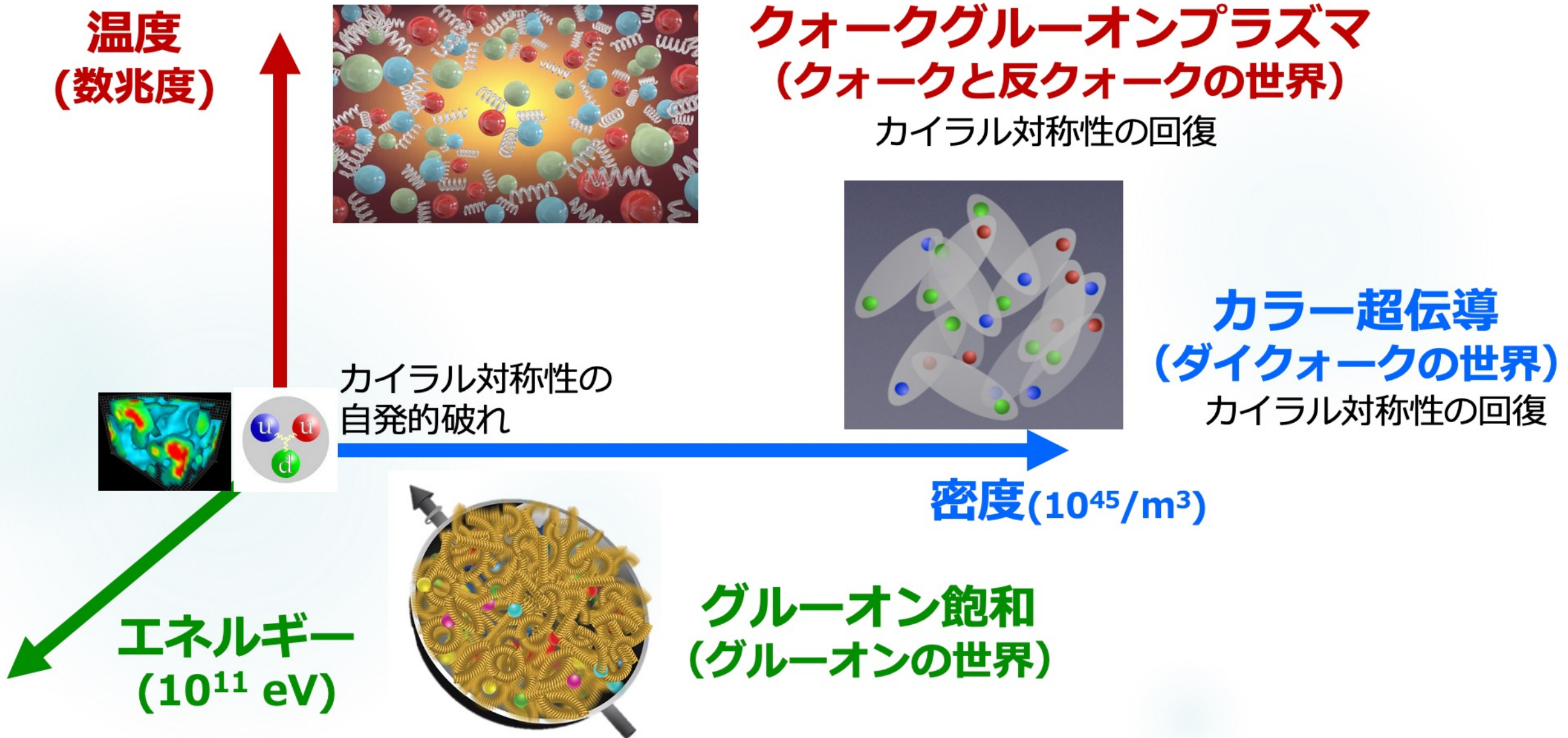


## 高密度グルーオンの世界

真空の揺らぎ  
クォークとグルーオン相互作用の平衡状態  
核子の質量・スピンの起源・閉じ込め

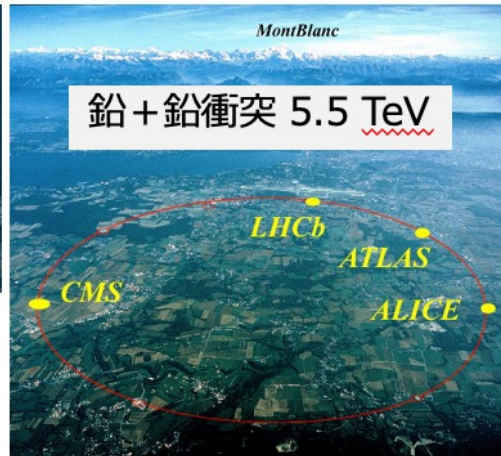
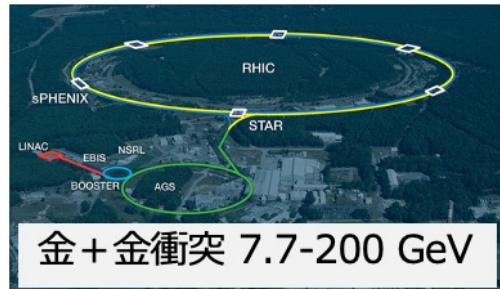


# 創発性の舞台



# 創発性を探る実験の舞台

温度  
(数兆度)

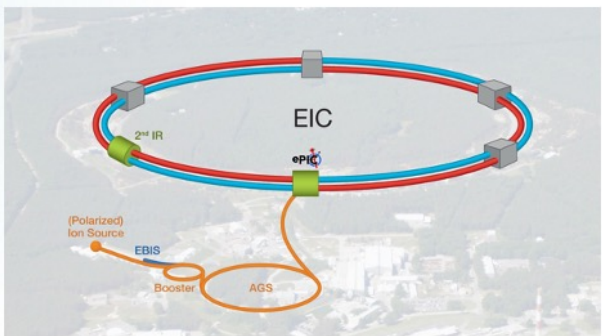


**RHIC(米)**  
**LHC(欧州)** **稼働中**

**FAIR (独)** **2028-**  
**J-PARC-HI (日)**



エネルギー  
( $10^{11}$  eV)



電子+陽子、電子+金: 29-140 GeV

密度( $10^{45}/m^3$ )

**EIC (米)** **2030-**  
アメリカ原子核業界の最優先計画。RHICの次の大型計画（世界で唯一建設が決まっている加速器）

# EIC workshop

22

<https://indico3.cns.s.u-tokyo.ac.jp/event/315/>

## 研究会「EICで展開する新たな原子核・素粒子物理」

28-30 May 2024  
University of Tokyo  
Asia/Tokyo timezone

Enter your search term

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- My Conference
- My Contributions
- Registration
- Participant List

### 連絡先

✉ [eic\\_workshop\\_2024@...](mailto:eic_workshop_2024@...)

2020年に行われたKEK研究会「素粒子・原子核コライダー物理の交点」を受けて、今回は、米国の次期大型計画EIC (Electron-Ion Collider) に焦点を置き、EICが今後の素粒子物理学と原子核物理学にどのような新しい展開をもたらすかを議論したいと思います。

EICはアメリカ原子核物理の最優先計画であり、ブルックヘブン国立研究所に建設される世界初の偏極電子+偏極陽子及び原子核衝突型加速器です。EIC計画は現在アメリカエネルギー省から計画実行段階への権限を与えられ、次の施設建設段階へ、そして2032年頃の建設完了に向けて、順調に進んでいます。

EICは今後10年程度で実現する新たなコライダーとしては唯一のものとなる可能性もあり、原子核物理分野と素粒子物理分野が協力して推進することを目指したいと思います。

3日間の研究会を予定しています。初日の午後は、EICの物理に関する簡単なスクールを実施します。2-3日目に議論を行います。素粒子物理、高エネルギーQCD物理、ハドロン物理、原子核物理の観点から、EICでの展望を議論します。また、EICにおける加速器技術、先端的な半導体測定器技術やデータ収集や処理技術に関する議論も行い、分野を超えた共同研究の可能性を議論したいと思います。



10:00	基調講演: The Electron-Ion Collider: the ultimate electron microscope Koshiba-hall, University of Tokyo	Prof. Gordon Baym 09:45 - 10:35
	coffee break Koshiba-hall, University of Tokyo	10:35 - 10:55
11:00	RHICスピンの発展 Koshiba-hall, University of Tokyo	Yuji Goto 10:55 - 11:20
	ePIC Experiment Overview Koshiba-hall, University of Tokyo	Yano Satoshi 11:20 - 11:45
12:00	Lunch Koshiba-hall, University of Tokyo	11:45 - 13:15
13:00	Studies of exotic-hadron candidates in high-energy reactions Koshiba-hall, University of Tokyo	13:40 - 14:00
	Study of internal structure of baryons using hadron beam Koshiba-hall, University of Tokyo	14:00 - 14:35
14:00	Searching for Lepton Flavor Violation at EIC Koshiba-hall, University of Tokyo	Kaori Fuyuto 14:05 - 14:35
	Workshop photo II coffee break Koshiba-hall, University of Tokyo	14:35 - 14:55
15:00	Recent trend of timing silicon detectors and development plan for future colliders Koshiba-hall, University of Tokyo	Koji Nakamura 14:55 - 15:20
	MAPS (TBD) Koshiba-hall, University of Tokyo	Katsuro Nakamura 15:20 - 15:45
	Streaming readout DAQ development and standardization by SPADI Alliance Koshiba-hall, University of Tokyo	Prof. Shinsuke OTA 15:45 - 16:10
16:00	coffee break Koshiba-hall, University of Tokyo	16:10 - 16:30
	基調講演: Status of Collinear PDFs and the impact of the EIC de Koshiba-hall, University of Tokyo	Enrico Tassi 16:30 - 17:20
17:00	Measurement of Hadron Mass in nuclei Koshiba-hall, University of Tokyo	Megumi Naruki 17:20 - 17:45
	ハドロンの重力形状因子と質量分解 Koshiba-hall, University of Tokyo	Kazuhiro Tanaka 17:45 - 18:10
18:00		

09:00	The color entanglement in TMD-factorization Koshiba-hall, University of Tokyo	Christine Aidala 09:00 - 09:25
	EIC Physics from Lattice QCD: The Nucleon Mass and Spin Decomposition (zoom) Koshiba-hall, University of Tokyo	Raza Sufian 09:25 - 09:50
10:00	格子QCDの量子計算に向けて Koshiba-hall, University of Tokyo	Arata Yamamoto 09:50 - 10:15
	coffee break Koshiba-hall, University of Tokyo	10:15 - 10:35
	Introduction to TMD and higher twist frameworks and their expected role in EIC Koshiba-hall, University of Tokyo	Shinsuke Yoshida 10:35 - 11:00
11:00	Fragmentation functions for nucleon structure measurements Koshiba-hall, University of Tokyo	Ralf Seidl 11:00 - 11:25
	Initial and final state effects on QGP in relativistic heavy-ion collision Koshiba-hall, University of Tokyo	Shingo Sakai 11:25 - 11:50
12:00	Lunch Koshiba-hall, University of Tokyo	11:50 - 13:00
13:00	cluster and SRC を含む原子核物理の最近のトピック (TBD) Koshiba-hall, University of Tokyo	13:00 - 13:30
14:00	hadron spectroscopy from Belle to EIC Koshiba-hall, University of Tokyo	14:00 - 14:30
	Hadron structure studies with antiproton beam at J-PARC Koshiba-hall, University of Tokyo	14:30 - 15:00
	coffee break Koshiba-hall, University of Tokyo	15:00 - 15:15
	kaon-nucleus bound systems Koshiba-hall, University of Tokyo	15:15 - 15:40
15:00	cSeaQuest実験・COMPASS実験で何が分かったのか? ~陽子のフレーバー&スピン構造~ Koshiba-hall, University of Tokyo	Yoshiyuki Miyachi 15:15 - 15:40
	Measurements of Generalized Parton Distribution functions using lepton and hadron beam Koshiba-hall, University of Tokyo	Natsuki Tomida 15:40 - 16:05
16:00	coffee break Koshiba-hall, University of Tokyo	16:05 - 16:25
	議論 Koshiba-hall, University of Tokyo	16:25 - 17:05
17:00	Closing Koshiba-hall, University of Tokyo	Yuji Goto 17:05 - 17:15

entanglement

Lattice, QC

Spin

technologies

TMD

QGP

Hadron structure

Nuclear cluster

BSM

Hadron structure

technologies

Hadron cluster

PDF

Spin, GPD

mass

# JPS symposium

23

16日 B132会場 16pB132 13:30~16:45

実験核物理領域, 素粒子論領域, 素粒子実験領域, 理論核物理領域  
電子-イオン衝突型加速器EICが展開する新たな原子核・素粒子物理

- 1 (一般シンポジウム講演) EICとePIC実験の現状  
東大CNS  
郡司卓
- 2 (一般シンポジウム講演) EICへの理論からの期待とグルーオン飽和の物理  
東大理  
福嶋健二
- 3 (一般シンポジウム講演) EICで明らかにするハドロン物理と質量起源  
広島大先進理工  
八野哲
- 4 (一般シンポジウム講演) 原子核の多次元量子イメージとハドロンの発現機構  
成蹊大理工  
渡邊和宏

休憩 (15:15~15:30)

- 5 (一般シンポジウム講演) 低エネルギー原子核物理  
理研  
久保田悠樹
- 6 (一般シンポジウム講演) 素粒子物理の観点  
信大理  
川出健太郎
- 7 (一般シンポジウム講演) ePIC実験の技術と波及  
奈良女子大理  
蜂谷崇

# DIS and Parton distribution

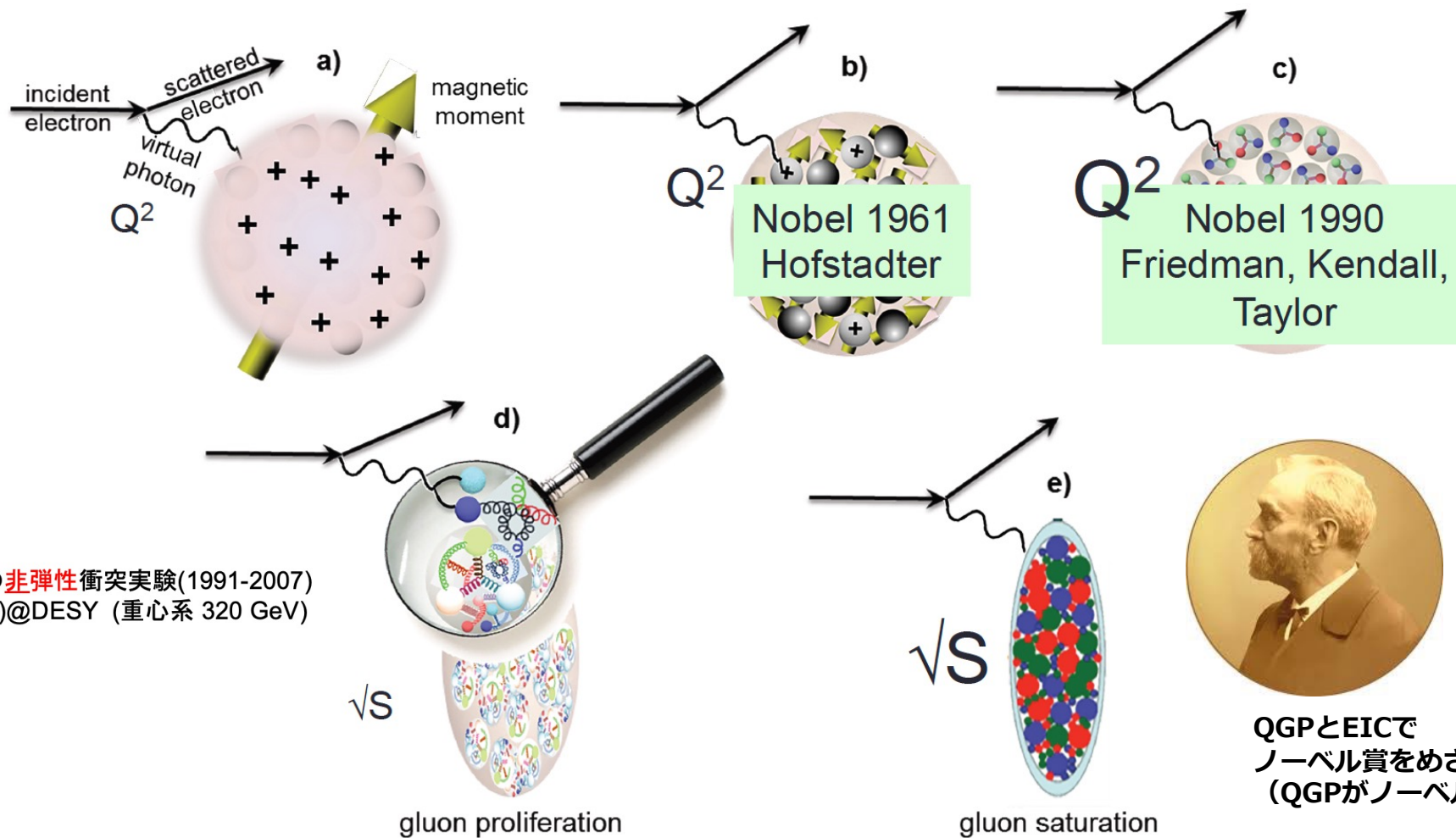


# Deep inelastic scattering

原子核の電荷分布の発見 (Lyman-Hanson-Scott)  
電子と原子核の弾性散乱実験 (1951)  
ベータトロン@イリノイ (15.7MeV)

核子構造の発見 (Hofstadter) → Nobel Prize (1961)  
電子と核子の弾性散乱実験(1956)  
リニアック@スタンフォード (187 MeV)

クォークの発見 (Kendall-Friedman-Taylor)  
電子と核子の非弾性散乱実験(1967-1973)  
リニアック@SLAC (-20 GeV)



## 核子の1次元構造

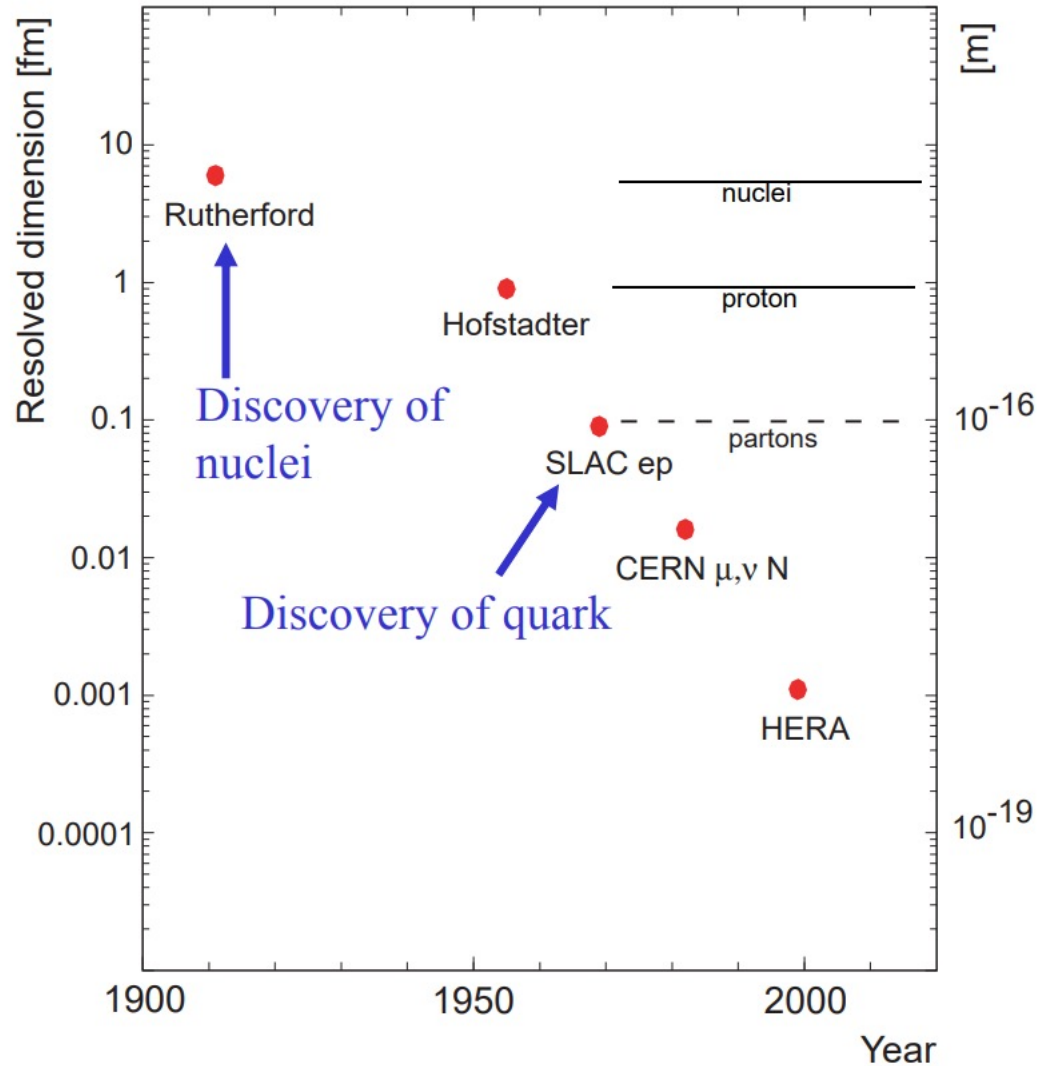
電子/陽電子 と陽子の非弾性衝突実験(1991-2007)  
HERA(シンクロトロン)@DESY (重心系 320 GeV)



QGPとEICで  
ノーベル賞をめざしましょう  
(QGPがノーベル賞にならないのは何故か?)

# Resolution power

26



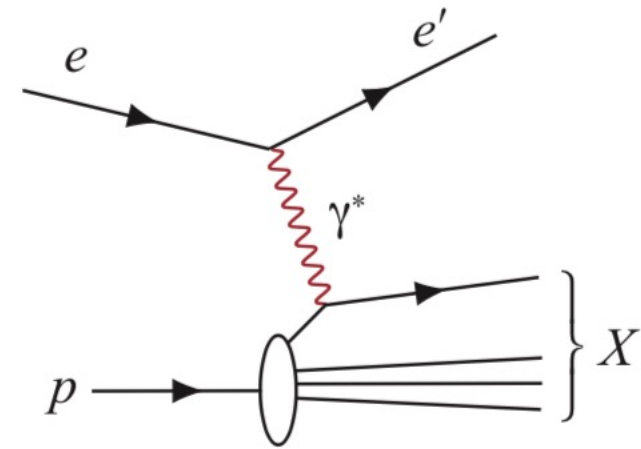
$$\lambda = \frac{h}{p} = \frac{h}{\sqrt{Q^2}}$$

HERA:  
(27.5 GeV e vs 920 GeV p)

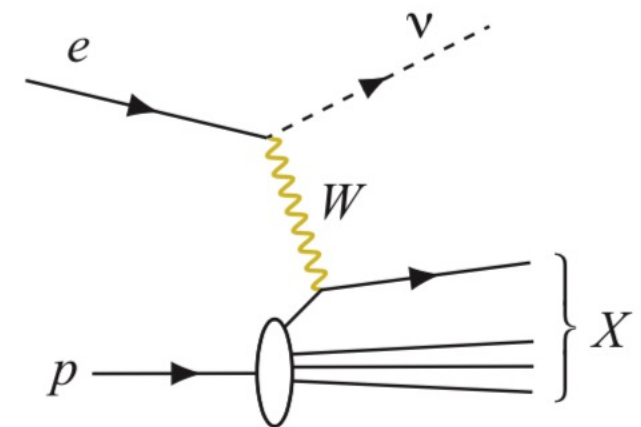
$$Q^2_{\max} = s = 4E_e E_p \sim 10000 \text{ GeV}^2$$

# Reactions to be measured in DIS

**Neutral-current Inclusive DIS:**  $e + p/A \rightarrow e' + X$ ;  
for this process, it is essential to detect the scattered electron,  $e'$ , with high precision. All other final state particles ( $X$ ) are ignored. The scattered electron is critical for all processes to determine the event kinematics.

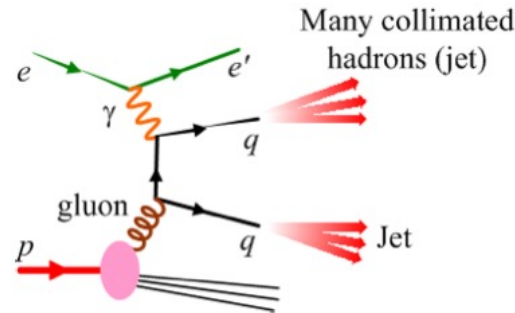


**Charged-current Inclusive DIS:**  $e + p/A \rightarrow \nu + X$ ;  
at high enough momentum transfer  $Q^2$ , the electron-quark interaction is mediated by the exchange of a  $W^\pm$  gauge boson instead of the virtual photon. In this case the event kinematic cannot be reconstructed from the scattered electron, but needs to be reconstructed from the final state particles.

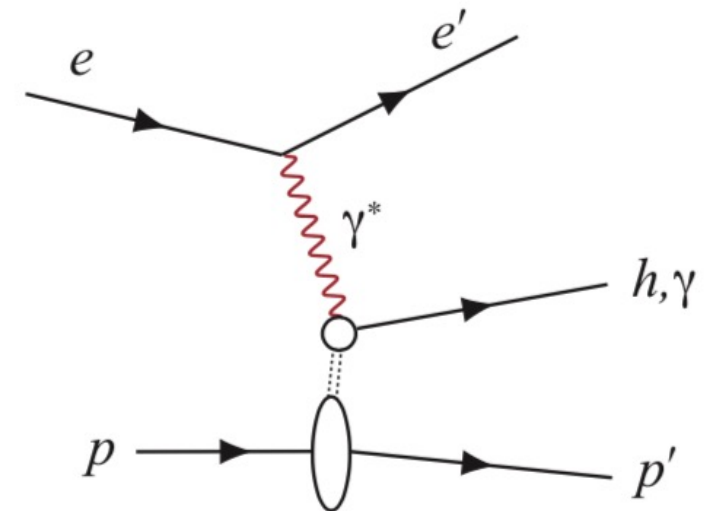
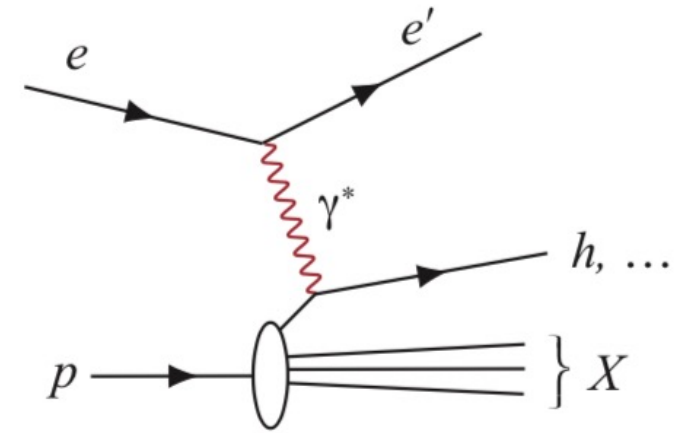


# Reactions to be measured in DIS

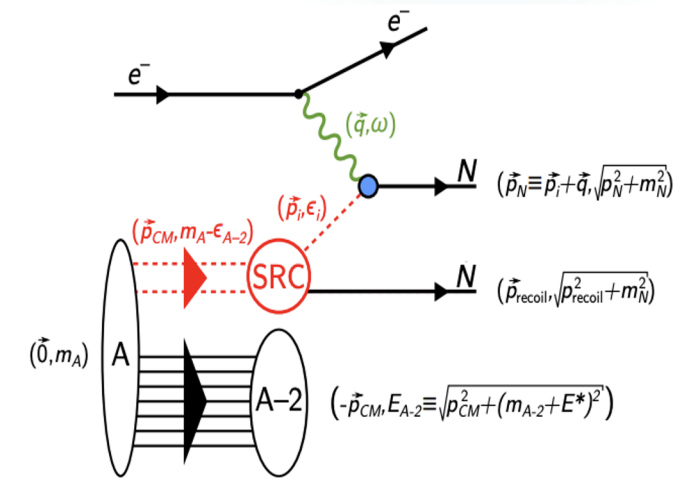
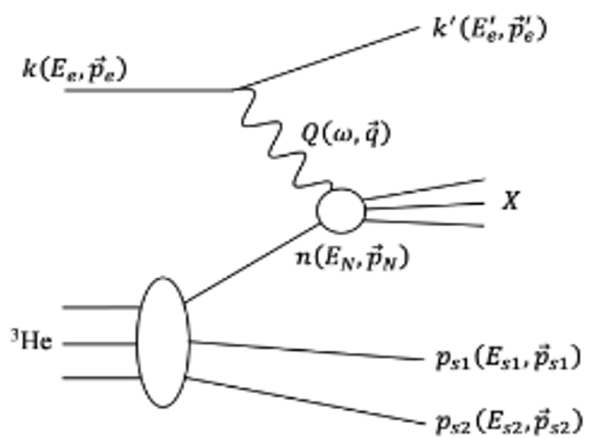
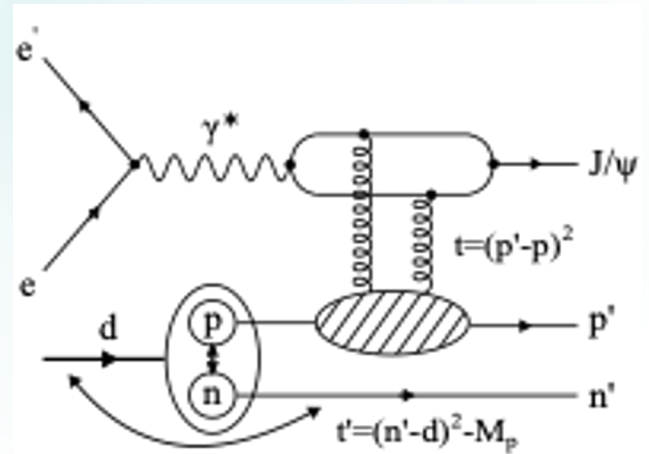
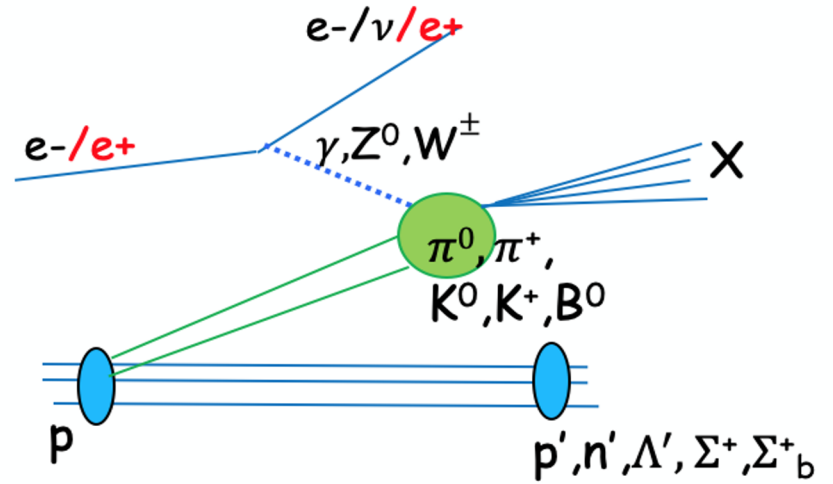
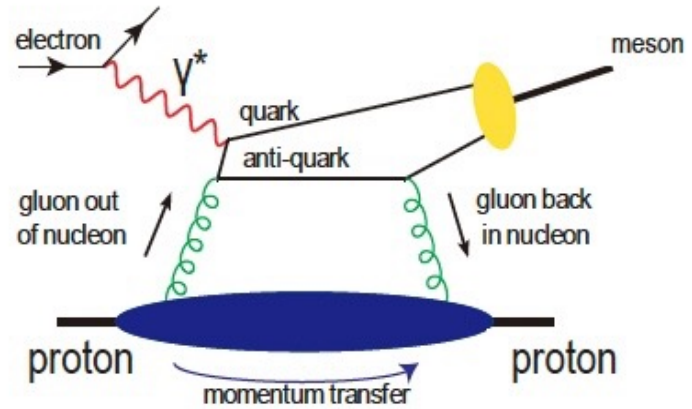
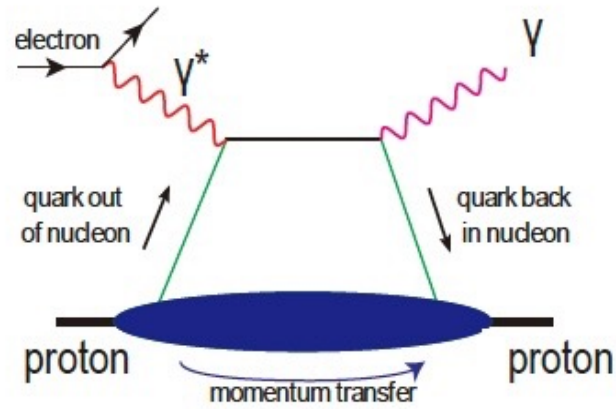
**Semi-inclusive DIS:**  $e + p/A \longrightarrow e' + h^{\pm,0} + X$ , which requires measurement of *at least one* identified hadron in coincidence with the scattered electron.



**Exclusive DIS:**  $e + p/A \longrightarrow e' + p'/A' + \gamma/h^{\pm,0}/VM$ , which require the measurement of *all* particles in the event with high precision.

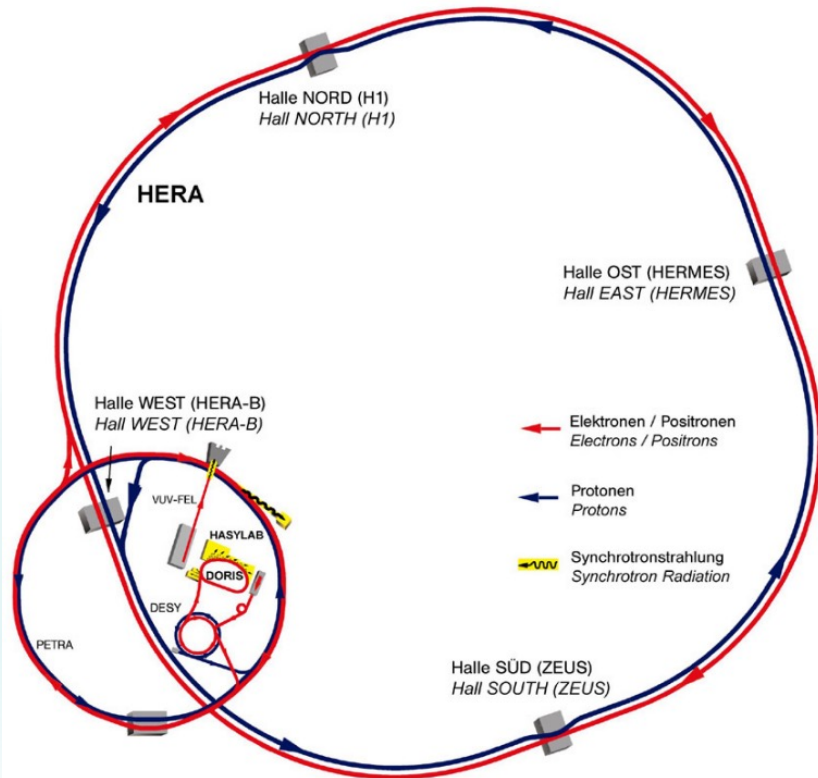


# Reactions to be measured in DIS



# HERA @ DESY

30



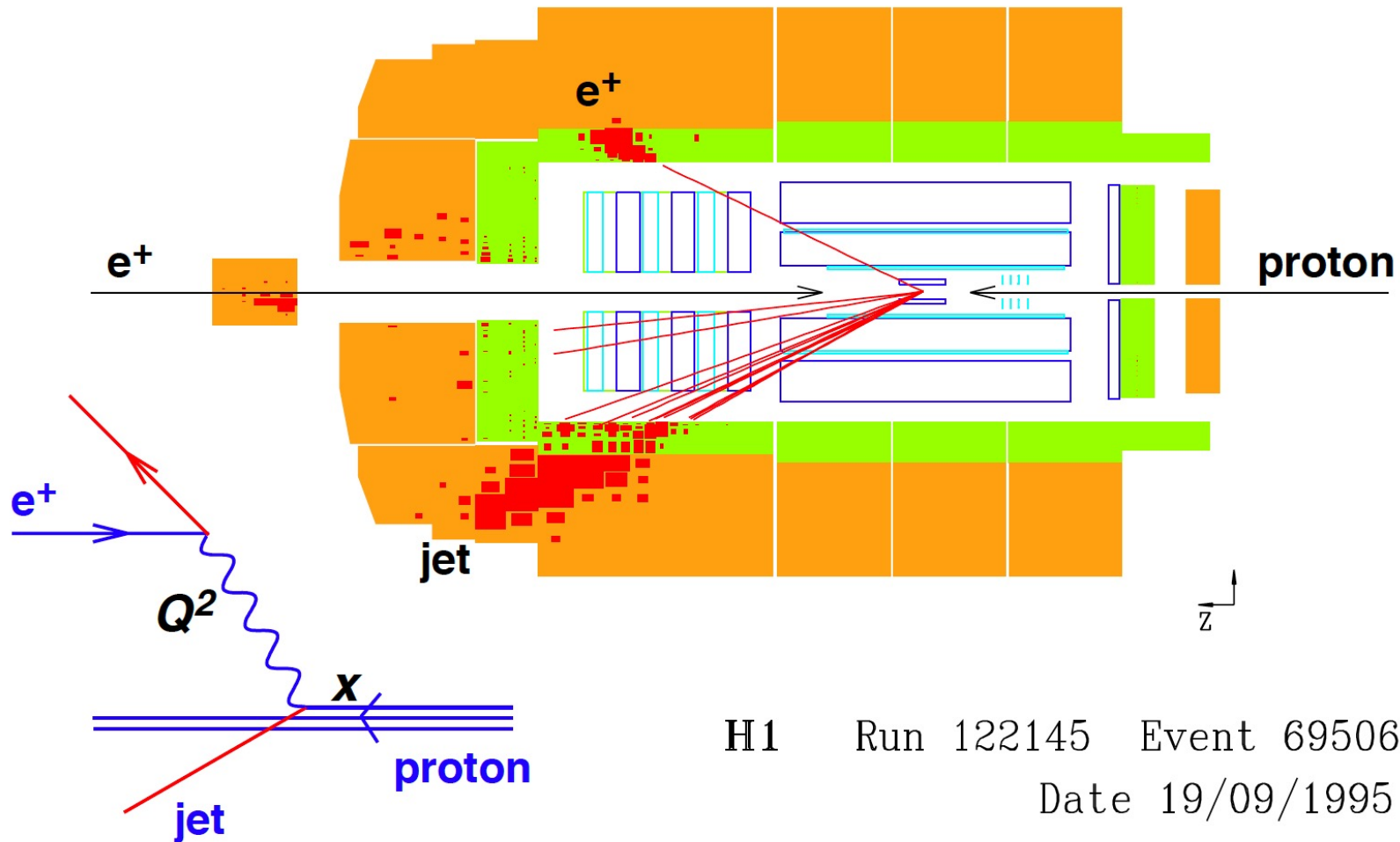
- At Hamburg in Germany
- 6.3 km circumference

- proton beam = 920 GeV
- electron beam = 27.5 GeV
- $\sqrt{s} = 318$  GeV

# HERA @ DESY

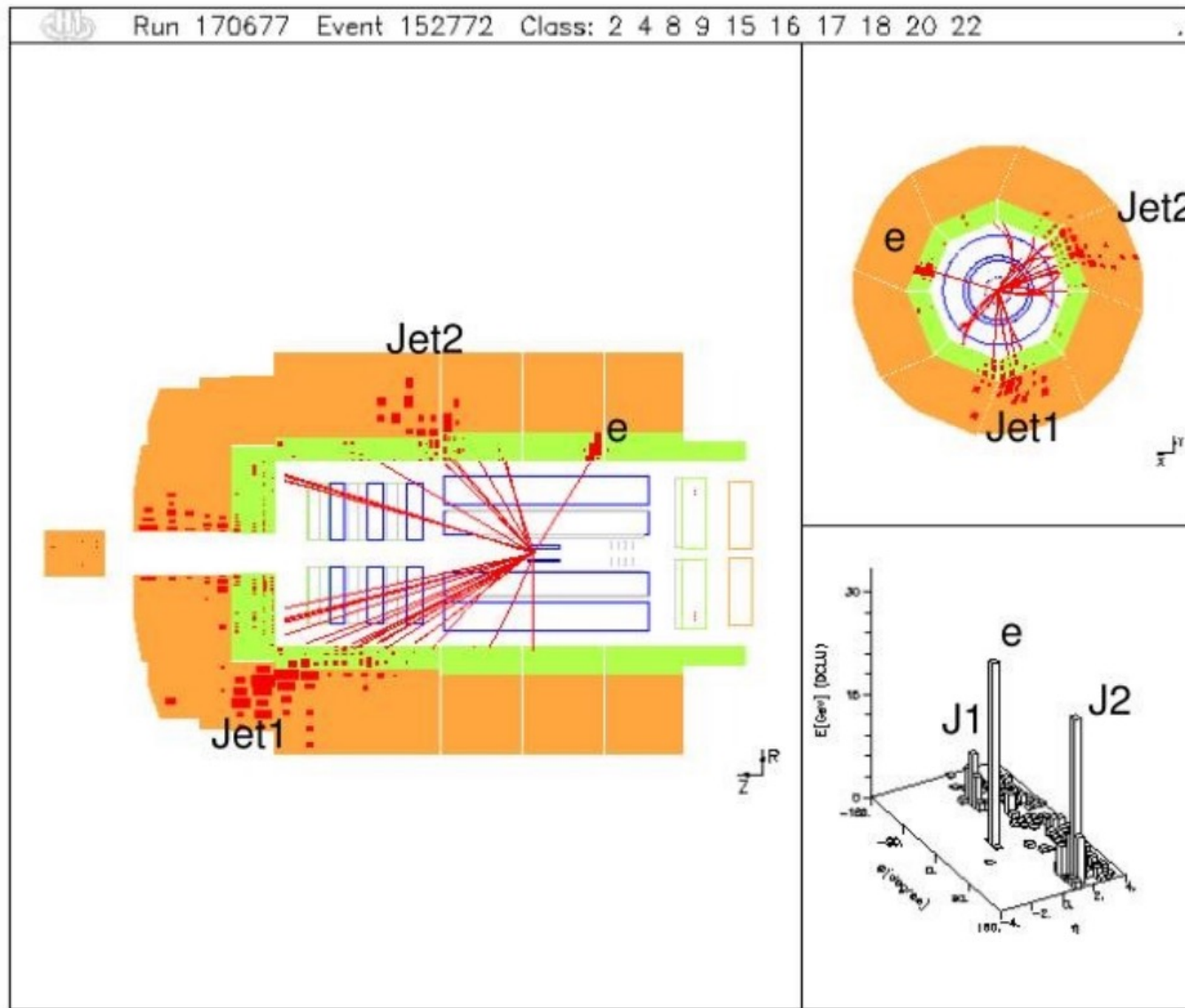
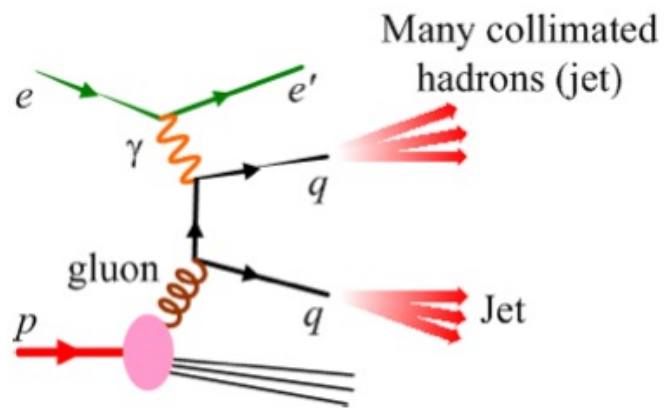


$Q^2 = 25030 \text{ GeV}^2$ ;  $y = 0.56$ ;  $x=0.50$



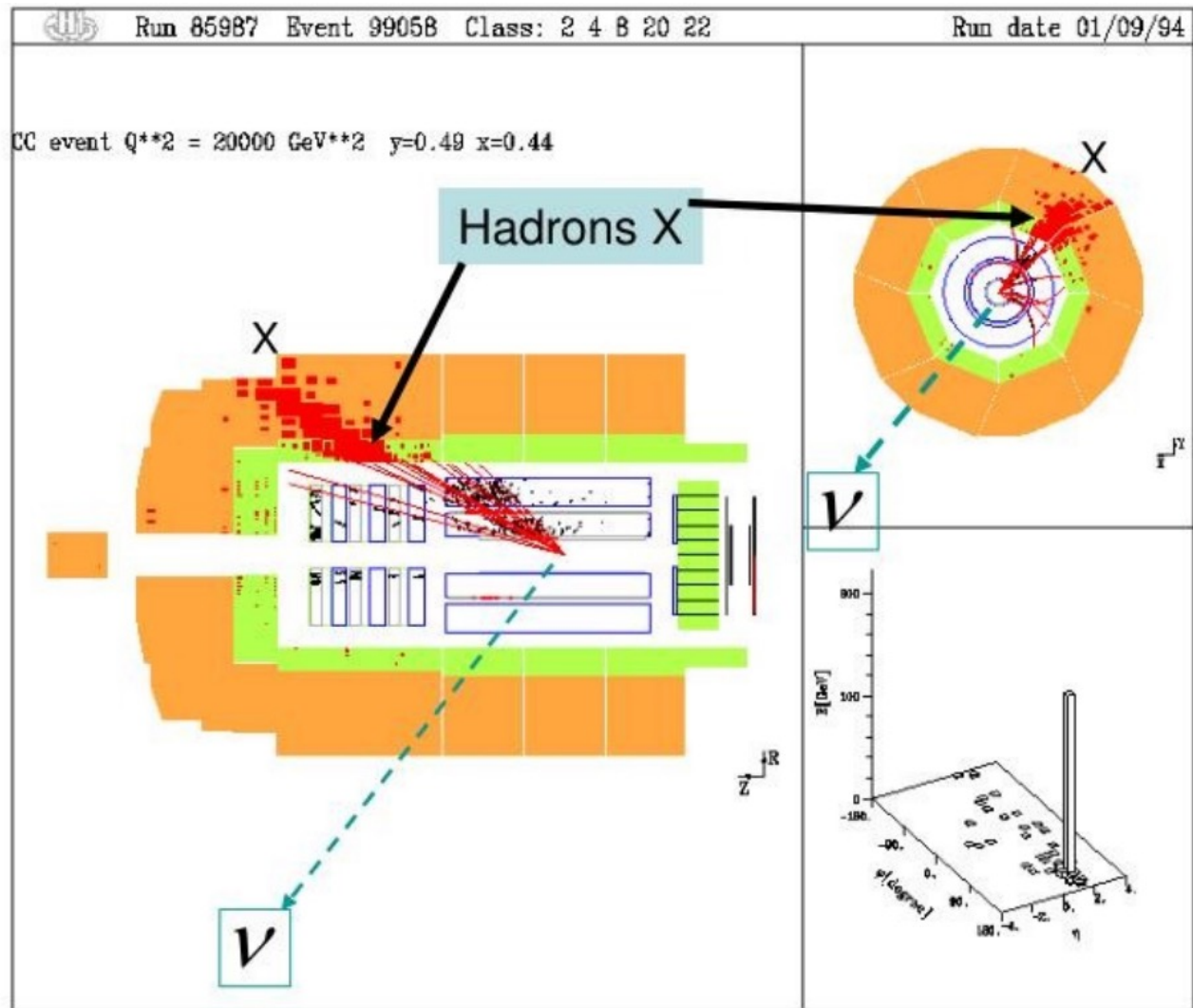
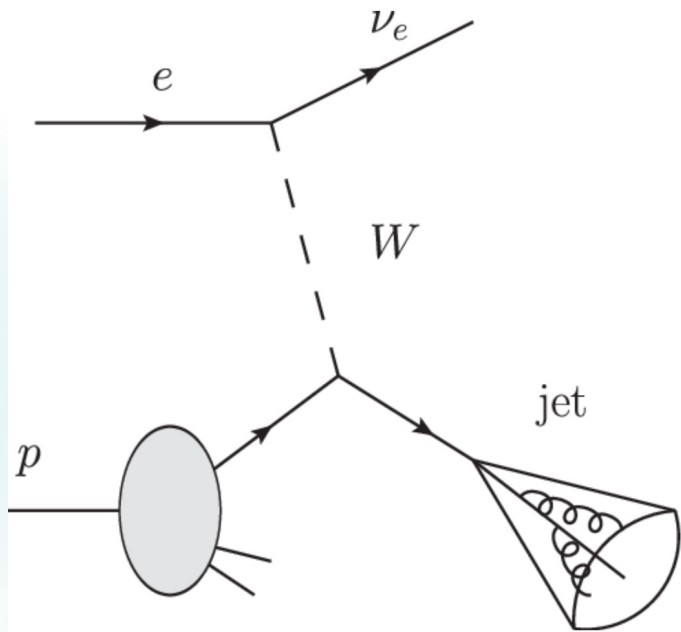
H1 Run 122145 Event 69506  
Date 19/09/1995

# HERA @ DESY



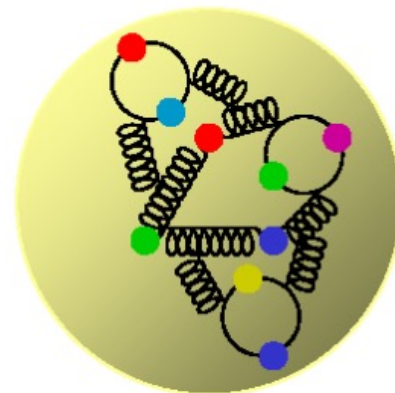
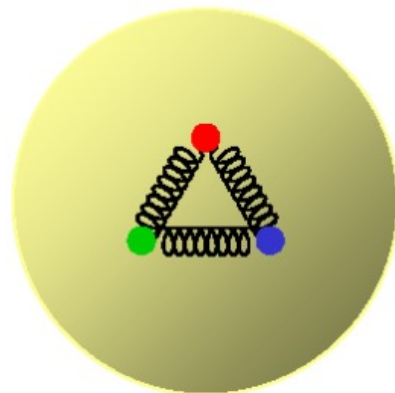
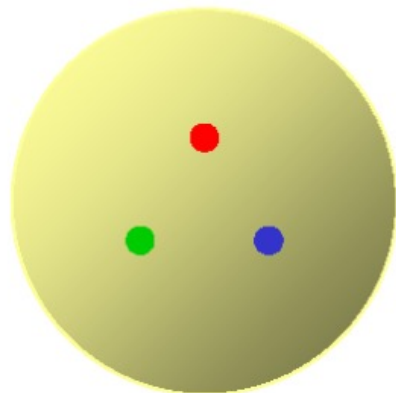
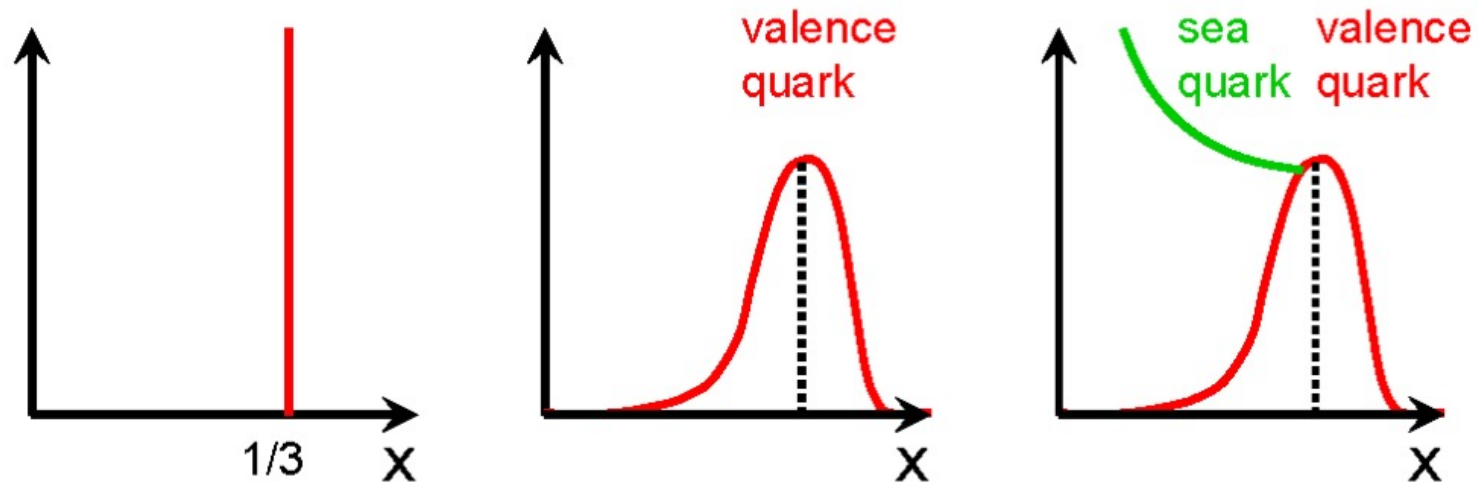


# HERA @ DESY

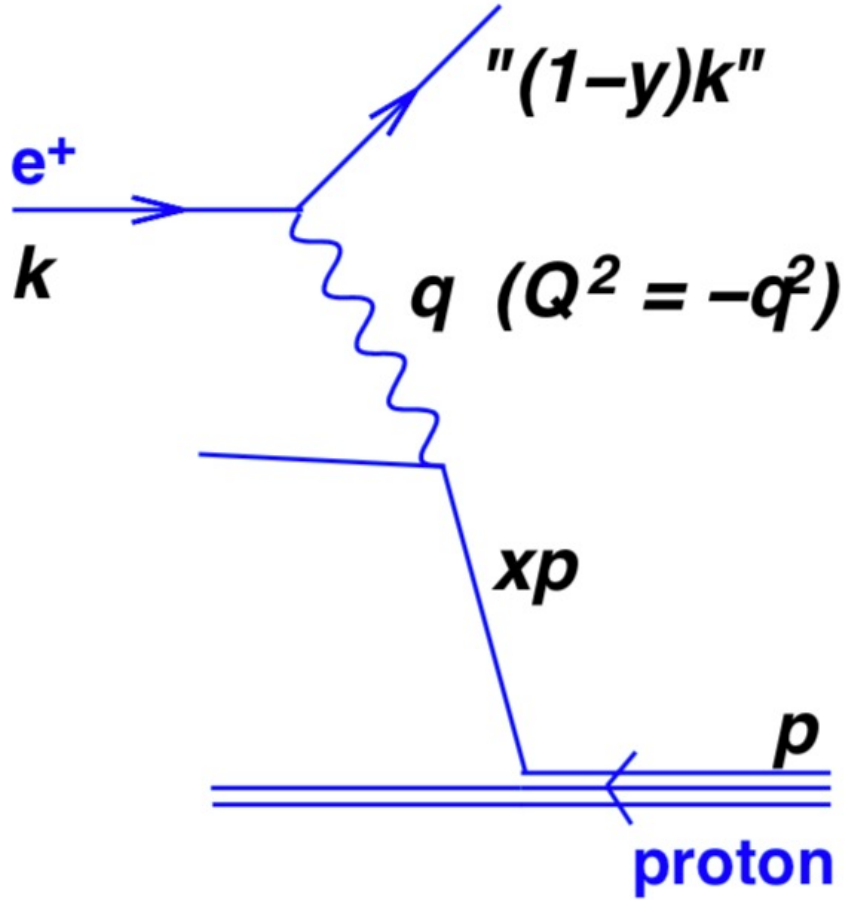


# Parton Distribution Function

The probability of a parton of type  $i$  having a fraction  $x$  of the proton energy



# Kinematics of DIS



Kinematic relations:

$$x = \frac{Q^2}{2p \cdot q}; \quad y = \frac{p \cdot q}{p \cdot k}; \quad Q^2 = xys$$

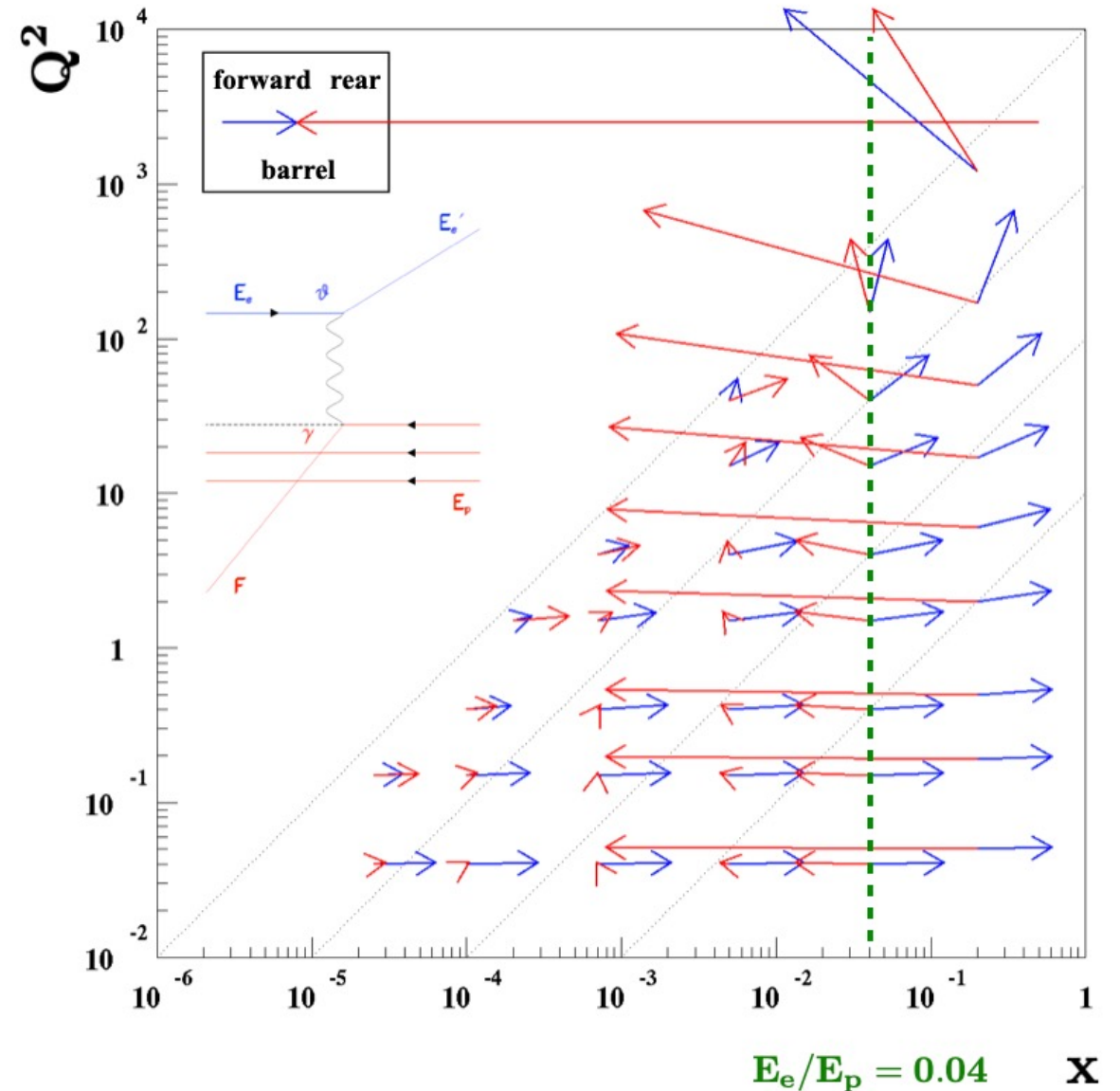
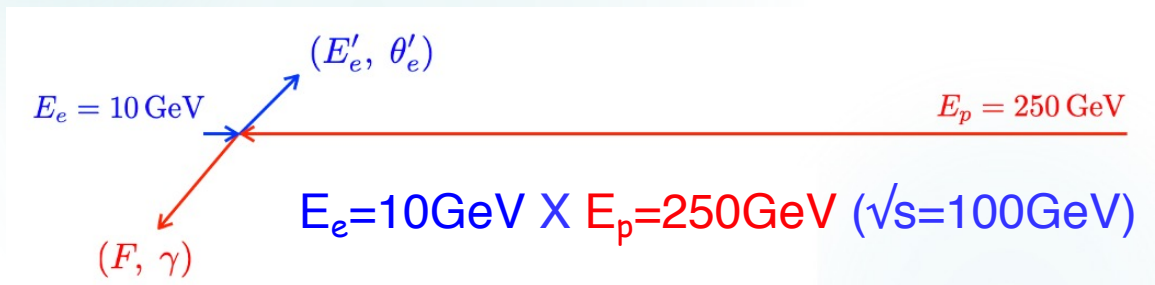
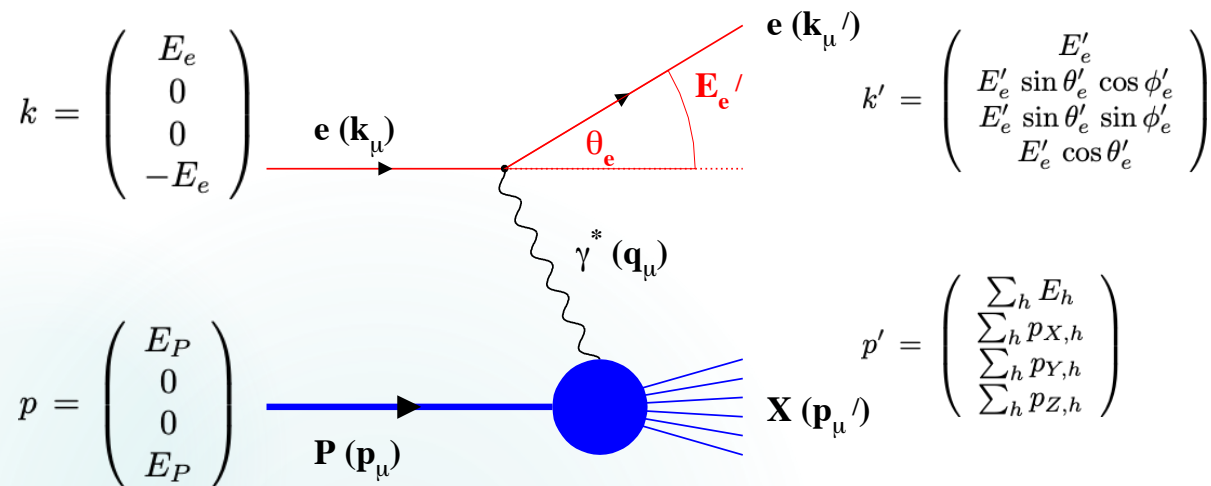
$\sqrt{s}$  = c.o.m. energy

- ▶  $Q^2$  = photon virtuality  $\leftrightarrow$  *transverse resolution* at which it probes proton structure
- ▶  $x$  = *longitudinal momentum fraction* of struck parton in proton
- ▶  $y$  = momentum fraction lost by electron (in proton rest frame)

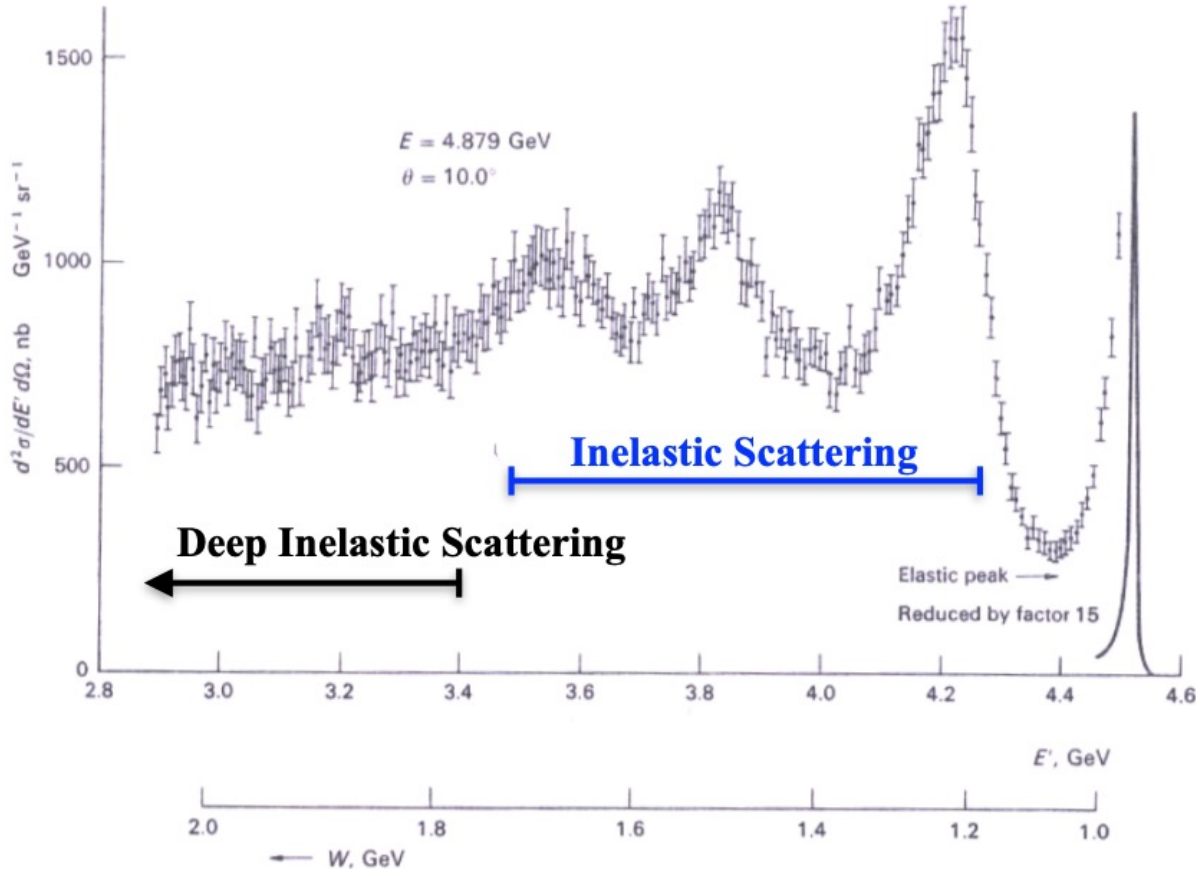
$y=0$ : small scattering angle limit

$y=1$ : backscattering i.e. total momentum transfer to the hadronic system

# Deep inelastic scattering (again)



# $e+p \rightarrow e+X$



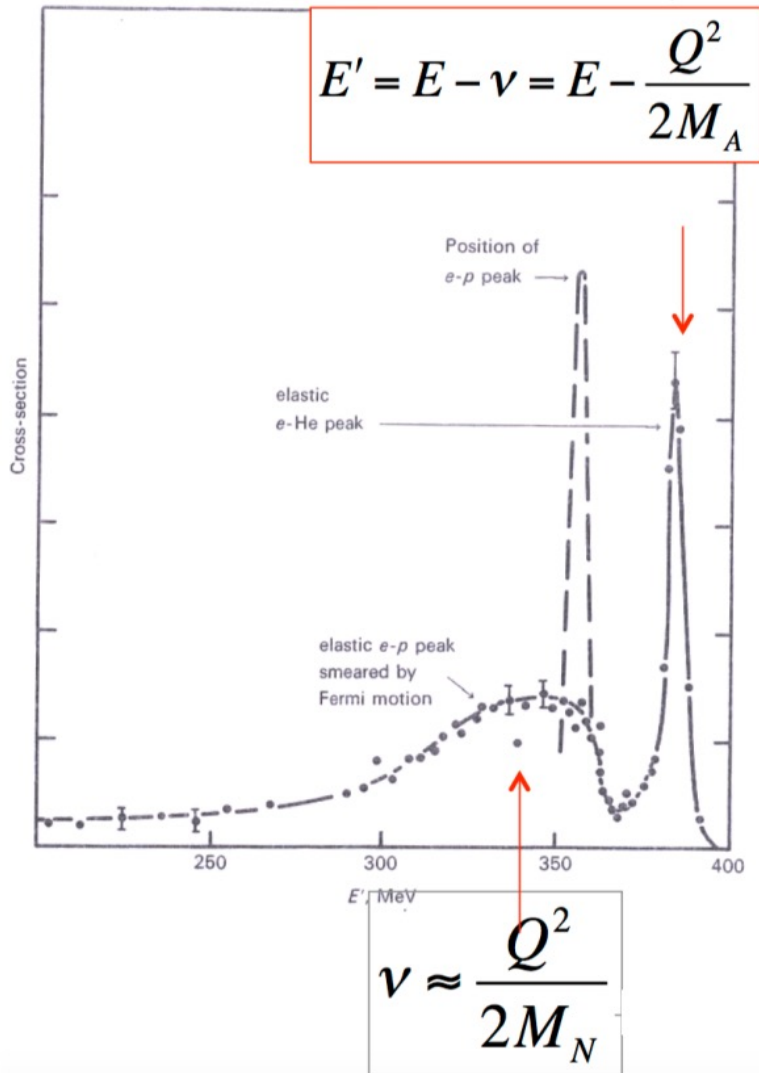
- Elastic peak at  $x=1$  ( $Q^2=2Mv$ )
- Inelastic scattering at larger  $q^2$  : the peaks correspond to “excited states” of the proton, e.g.  $\Delta^+(1232)$ , ...
- Deep Inelastic Scattering: proton breaks up resulting in many particles final state (large  $W$ )

$W^2=(P+q)^2$ : invariant mass of the hadronic final state

Scattering of 4.879 GeV electron from proton at rest

- Detector at 10 deg. w.r.t the beam, and measure the energy of the scattered electron
- Kinematics fully determined from the electron energy and the angle

# $e+A \rightarrow e+X$



- Elastic peak at high value of  $E'$  (low value of  $Q^2$ )
- The broader peak at larger  $q^2$  corresponds to quasi-elastic scattering on single nucleons
  - If nucleons were free, we would have a single narrow peak at  $\nu \approx Q^2 / (2M_N)$
  - Nucleons are in a potential well of radius  $R \sim 1 \text{ fm}$ , so they have a Fermi momentum  $p_F \sim 1/R \sim 200 \text{ MeV}$  which broaden the elastic peak:
    - $\Delta\nu/\nu = \pm p_F/M_N \sim 10\%$

# Structure function

Write DIS X-section to zeroth order in  $\alpha_s$  ('quark parton model'):

$$\frac{d^2\sigma^{em}}{dx dQ^2} \simeq \frac{4\pi\alpha^2}{xQ^4} \left( \frac{1 + (1-y)^2}{2} F_2^{em} + \mathcal{O}(\alpha_s) \right)$$

$\propto F_2^{em}$  [structure function]

$$F_2(x) = \sum_i e_i^2 x f_i(x)$$

e-p scattering

$$\frac{1}{x} F_2^{ep} = \left(\frac{2}{3}\right)^2 (u^p + \bar{u}^p) + \left(\frac{1}{3}\right)^2 (d^p + \bar{d}^p) + \left(\frac{1}{3}\right)^2 (s^p + \bar{s}^p)$$

e-n scattering  
(from e-d  
scattering)

$$\frac{1}{x} F_2^{en} = \left(\frac{2}{3}\right)^2 (u^n + \bar{u}^n) + \left(\frac{1}{3}\right)^2 (d^n + \bar{d}^n) + \left(\frac{1}{3}\right)^2 (s^n + \bar{s}^n),$$

# Structure function

e-p scattering  $\frac{1}{x} F_2^{ep} = \left(\frac{2}{3}\right)^2 (u^p + \bar{u}^p) + \left(\frac{1}{3}\right)^2 (d^p + \bar{d}^p) + \left(\frac{1}{3}\right)^2 (s^p + \bar{s}^p)$

e-n scattering  
(from e-d scattering)  $\frac{1}{x} F_2^{en} = \left(\frac{2}{3}\right)^2 (u^n + \bar{u}^n) + \left(\frac{1}{3}\right)^2 (d^n + \bar{d}^n) + \left(\frac{1}{3}\right)^2 (s^n + \bar{s}^n),$

exchanging an up quark for a down turns basically a proton into a neutron (iso-spin symmetry)

the three lightest quark flavors (u,d,s) occur with equal probability in the sea:

$$u := u_v + u_s = u^p = d^n$$

$$d := d_v + d_s = d^p = u^n.$$

$$S := u_s = \bar{u}_s = d_s = \bar{d}_s = s_s = \bar{s}_s.$$

$$\frac{1}{x} F_2^{ep} = \frac{1}{9}(4u_v + d_v) + \frac{4}{3}S$$
$$\frac{1}{x} F_2^{en} = \frac{1}{9}(4d_v + u_v) + \frac{4}{3}S.$$



# Structure function

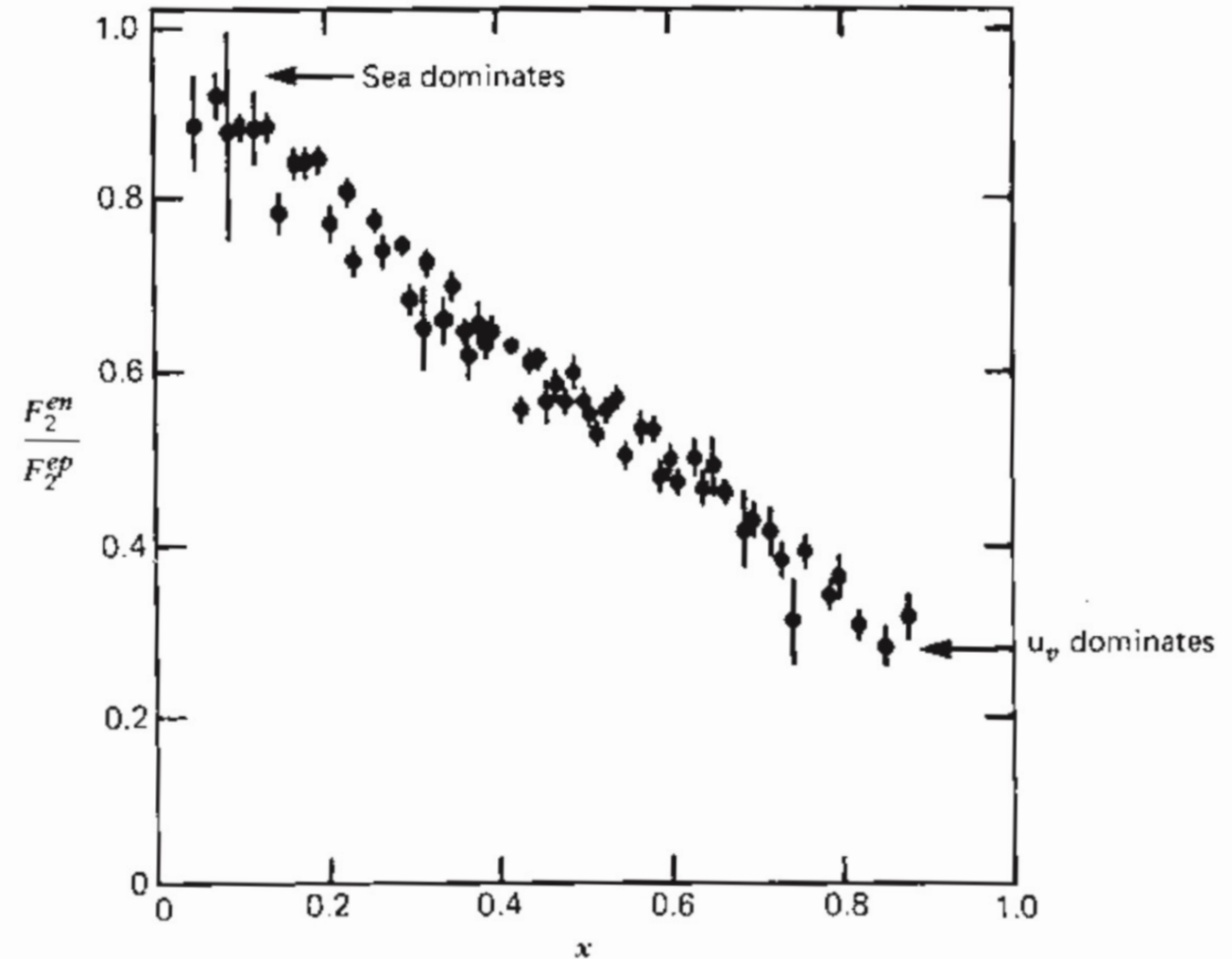
$$\frac{1}{x} F_2^{ep} = \frac{1}{9} (4u_v + d_v) + \frac{4}{3} S$$
$$\frac{1}{x} F_2^{en} = \frac{1}{9} (4d_v + u_v) + \frac{4}{3} S.$$

At small momentum fractions ( $x \approx 0$ ) the structure function is dominated by low-momentum  $q\bar{q}$ -pairs constituting the “sea”.

$$\frac{F_2^{en}}{F_2^{ep}} \rightarrow 1,$$

for  $x \approx 1$  the valence quarks dominate

$$\frac{F_2^{en}}{F_2^{ep}} \rightarrow \frac{1}{4}.$$



# Gluons

Summing the measured momenta of the partons give the proton momentum.

$$\int_0^1 dx x(u + \bar{u} + d + \bar{d} + s + \bar{s}) = 1 - \varepsilon_g,$$

$$\int_0^1 dx F_2^{ep} = \frac{4}{9}\varepsilon_u + \frac{1}{9}\varepsilon_d = 0.18,$$

$$\int_0^1 dx F_2^{en} = \frac{1}{9}\varepsilon_u + \frac{4}{9}\varepsilon_d = 0.12.$$

$$\varepsilon_u = 0.36$$

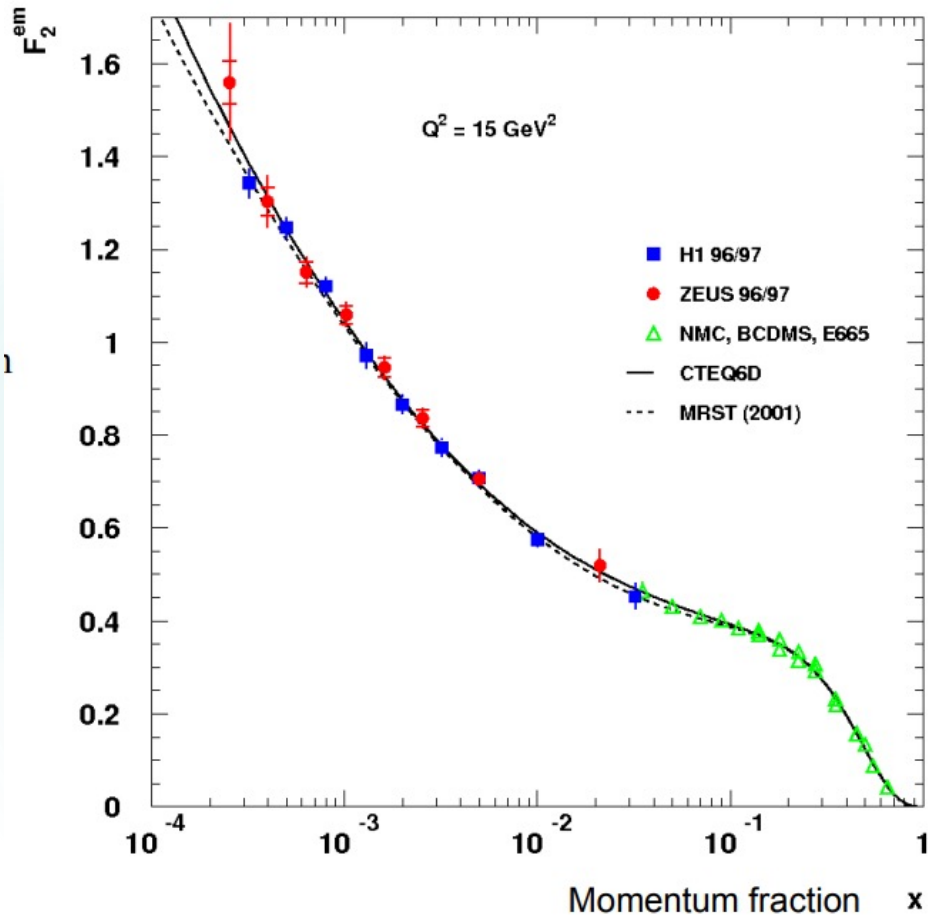
$$\varepsilon_d = 0.18,$$

$$\varepsilon_g = 1 - \varepsilon_u - \varepsilon_d = 0.46.$$

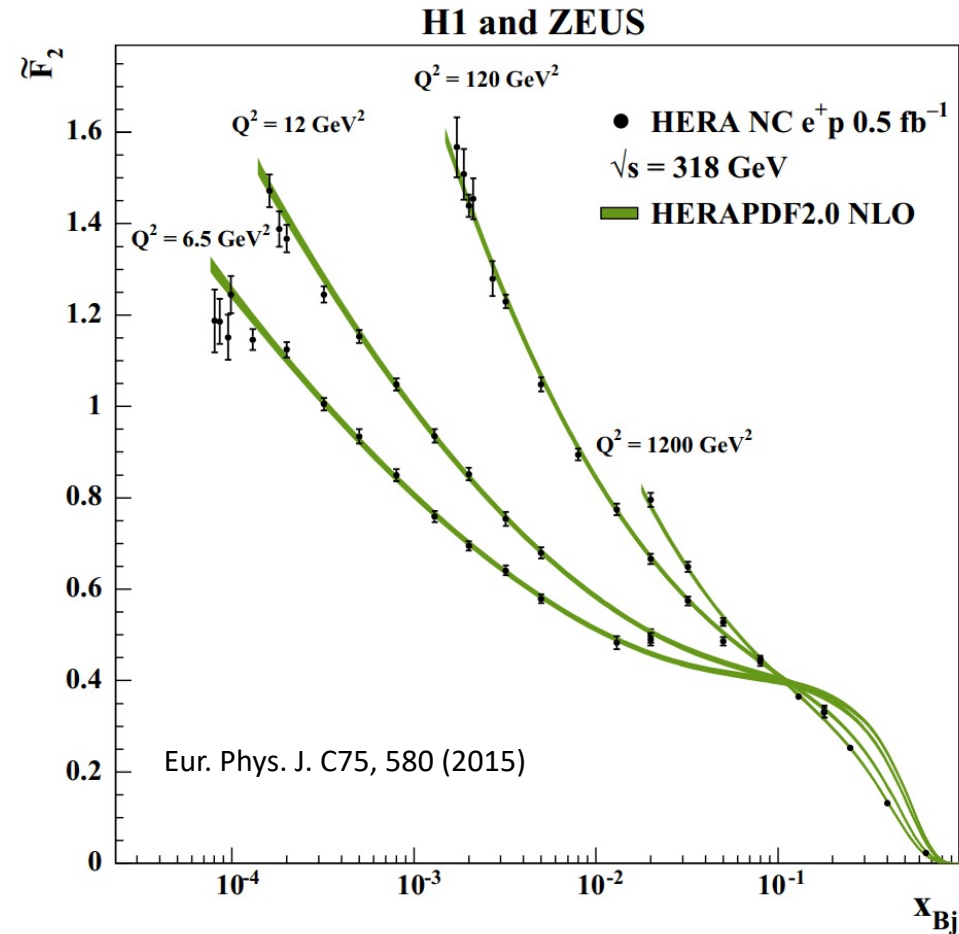
Almost half of the proton momentum is carried by gluons

# Structure functions at HERA

Contribution of sea quarks  
Contribution increases as smaller-x



Sea quarks dynamically created at high  $Q^2$



# Dynamical picture of evolution

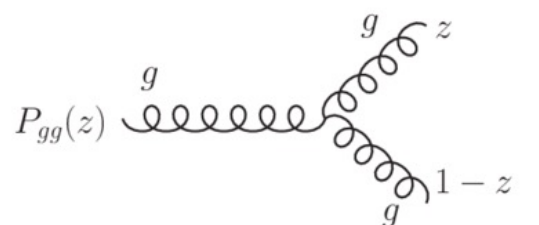
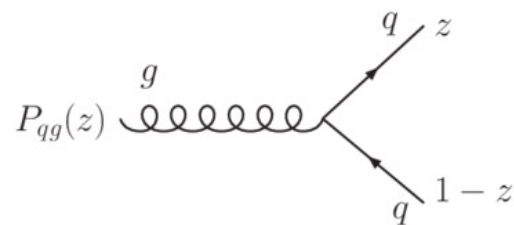
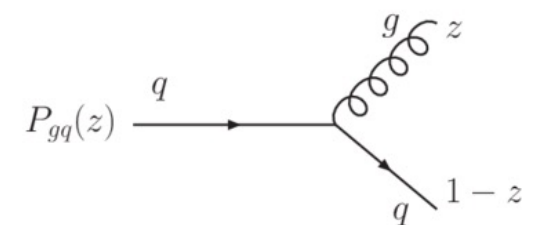
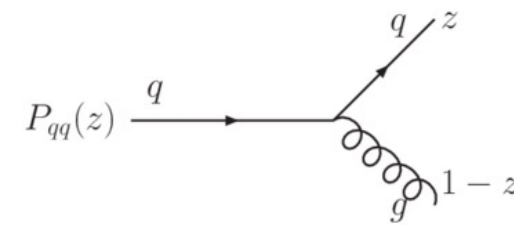
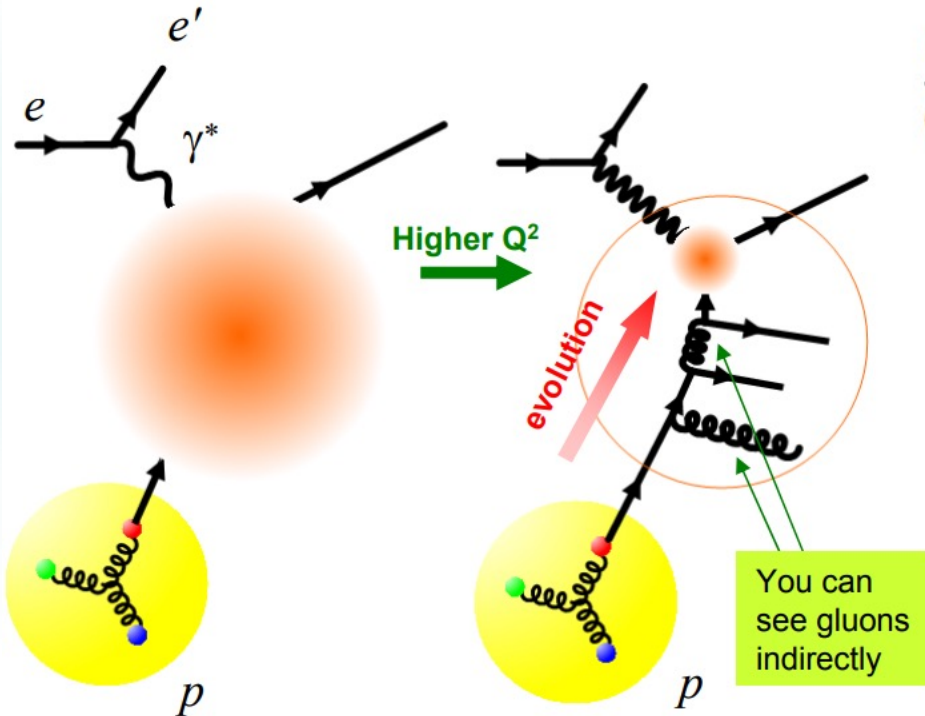
Increased spatial resolution  $Q^2 \rightarrow$  Shorter interaction time  $\tau_i$  ( $\tau_i = 1/Q^2$ )

- **Quantum fluctuations** : Gluon splits into a pair of quark and anti-quark, and in turn recombines back to gluon later.
- With EM interaction (e-p scattering via  $\gamma$ ), gluon cannot be seen directly (gluons cannot directly interact with  $\gamma$ ), but is indirectly seen as “increase of quarks with smaller  $x$  as  $Q^2$  gets higher”

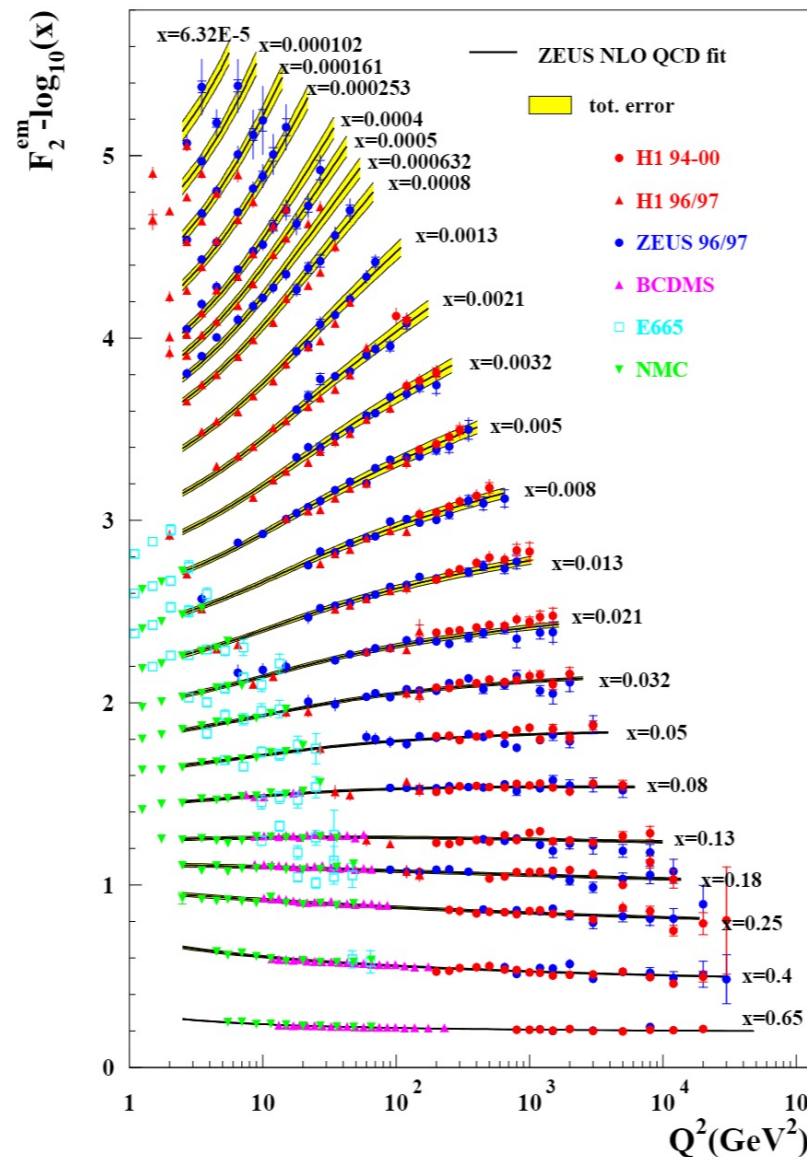
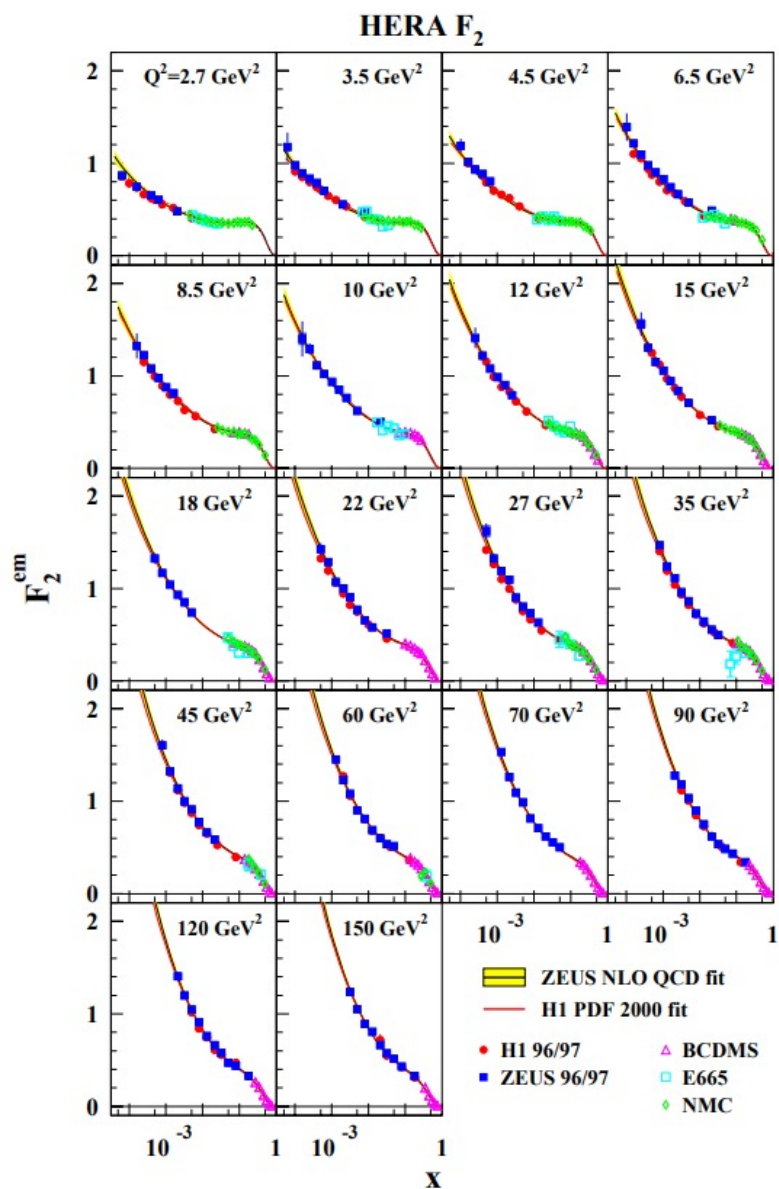
## Dokshitzer-GribovLipatov-Altarelli-Parisi (DGLAP) evolution equation

$$\frac{\partial}{\partial t} \begin{pmatrix} q_i(x, t) \\ g(x, t) \end{pmatrix} = a_s(t) \sum_{j=1}^{2n_f} \int_x^1 \frac{dz}{z} \begin{pmatrix} P_{q_i q_j} \left( \frac{x}{z}, a_s(t) \right) & P_{q_i g} \left( \frac{x}{z}, a_s(t) \right) \\ P_{g q_j} \left( \frac{x}{z}, a_s(t) \right) & P_{g g} \left( \frac{x}{z}, a_s(t) \right) \end{pmatrix} \begin{pmatrix} q_j(z, t) \\ g(z, t) \end{pmatrix},$$

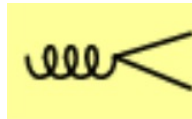
$t = \ln Q^2,$



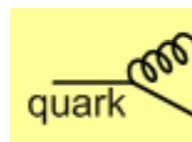
# Structure functions at HERA



Small-x

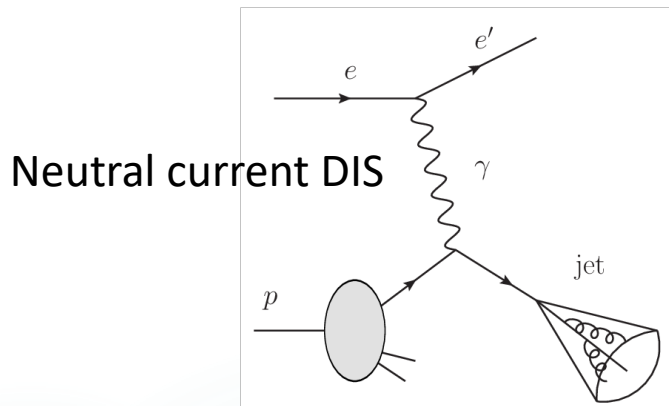


DGLAP evolution describes well



Large-x

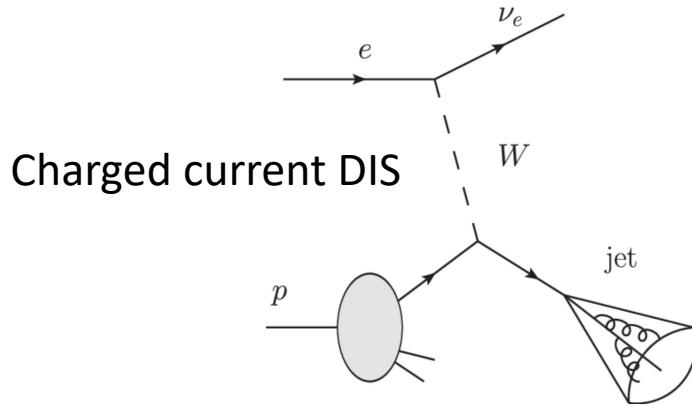
# Structure functions at HERA



Neutral current DIS

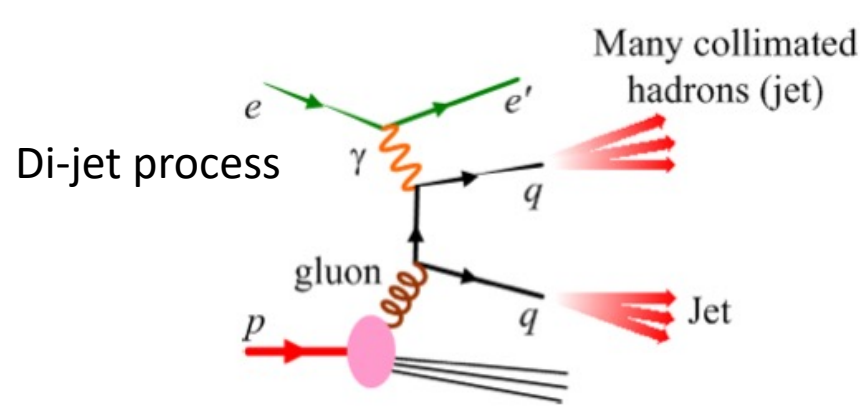
$\gamma, Z^0 \rightarrow F_2 \propto \sum x(q + \bar{q})$   
Sea + valence quark

$$\frac{\partial F_2}{\partial \ln Q^2} \propto xg \quad \text{gluon}$$



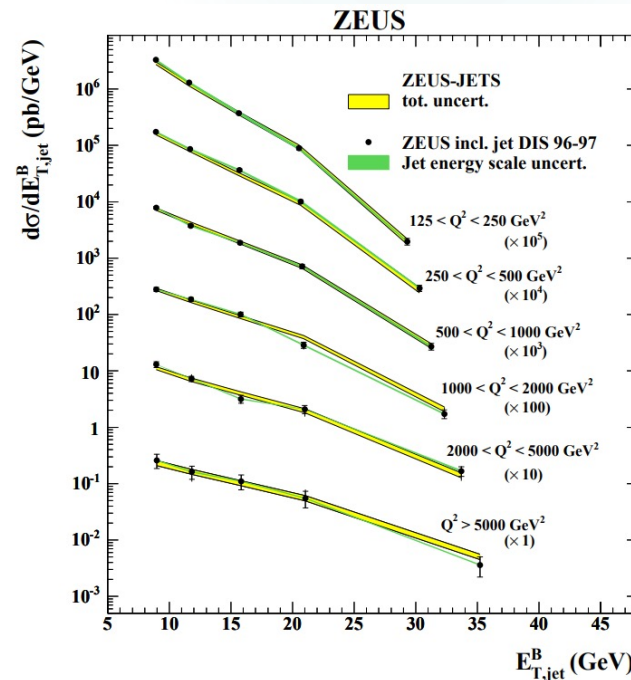
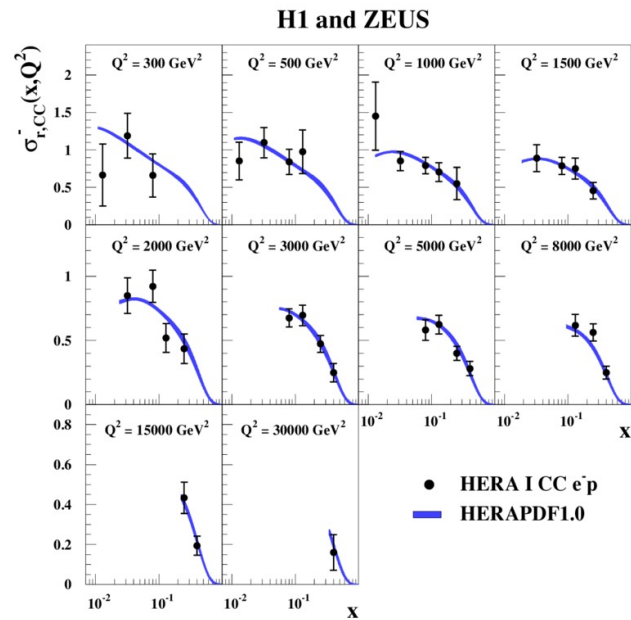
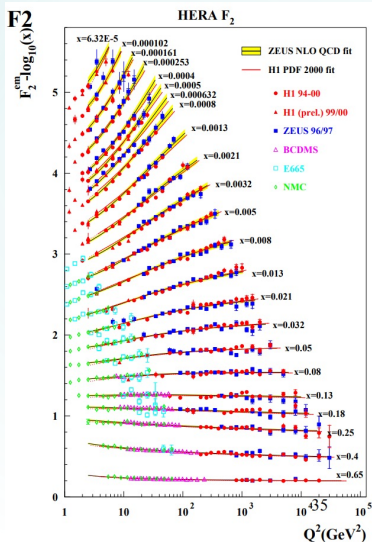
Charged current DIS

Charge selective interaction  
 $e^- : u \text{ quark} \quad e^+ : d \text{ quark}$



Di-jet process

Directly sensitive to gluon density



# PDF Parameterization for global fit

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## PDF Parameterization

u-valence ( $xu_v$ )	$A_{uv} x^{b_{uv}} (1-x)^{c_{uv}} (1+d_{uv}x)$
d-valence ( $xd_v$ )	$A_{dv} x^{b_{dv}} (1-x)^{c_{dv}} (1+d_{dv}x)$
Sea ( $xS$ )	$A_S x^{b_S} (1-x)^{c_S}$
gluon ( $xg$ )	$A_g x^{b_g} (1-x)^{c_g} (1+d_gx)$
dbar-ubar ( $x\Delta$ )	$0.27 x^{0.5} (1-x)^{c_\Delta}$

### Constraints

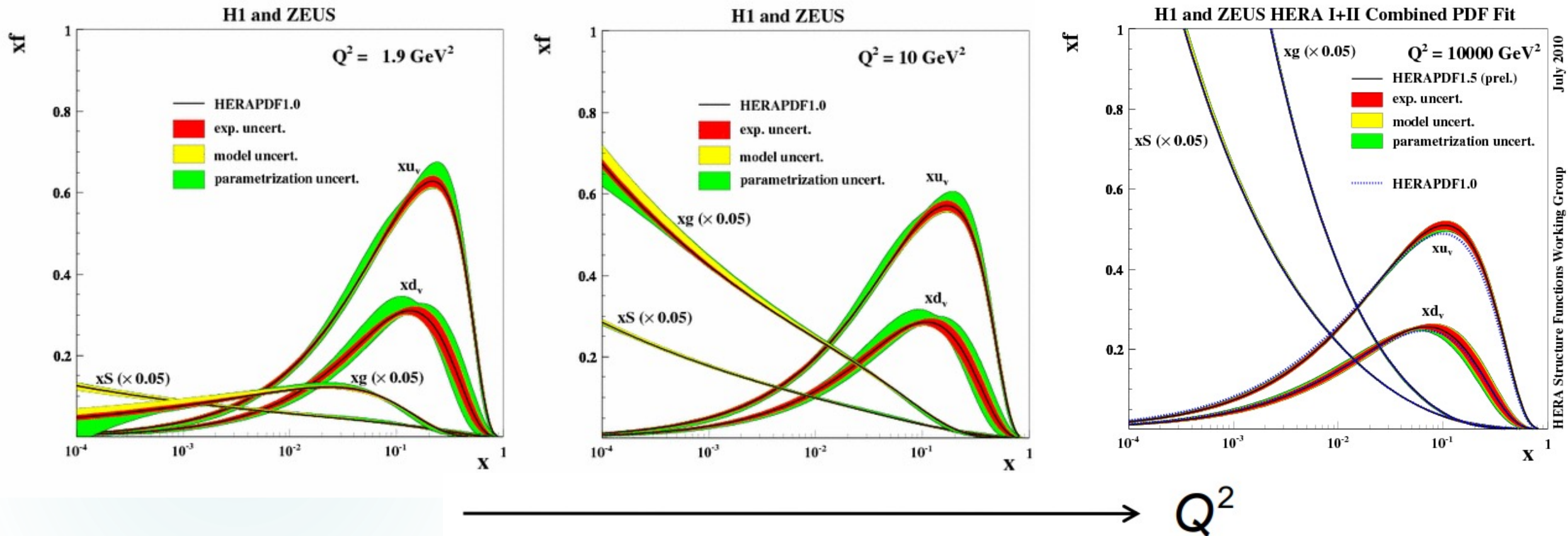
- Momentum and number sum rule
- Equal behaviour of  $u_v$  and  $d_v$  at low  $x$
- $\Delta$  : consistent with Gottfried sum rule and Drell Yan

11 free parameters

$$F_2(x) = \sum_i e_i^2 x f_i(x)$$

# Parton distribution function

[JHEP 1001:109\(2010\)](#)



The most dramatic of these experimental consequences, that the protons viewed at ever higher resolution would appear more and more as field energy (soft gluons), was only clearly verified at HERA ... F. Wilczek [Nobel Prize 2004]



# Polarized PDF

## Unpolarized PDF

$$f(x) \equiv f^\uparrow(x) + f^\downarrow(x)$$

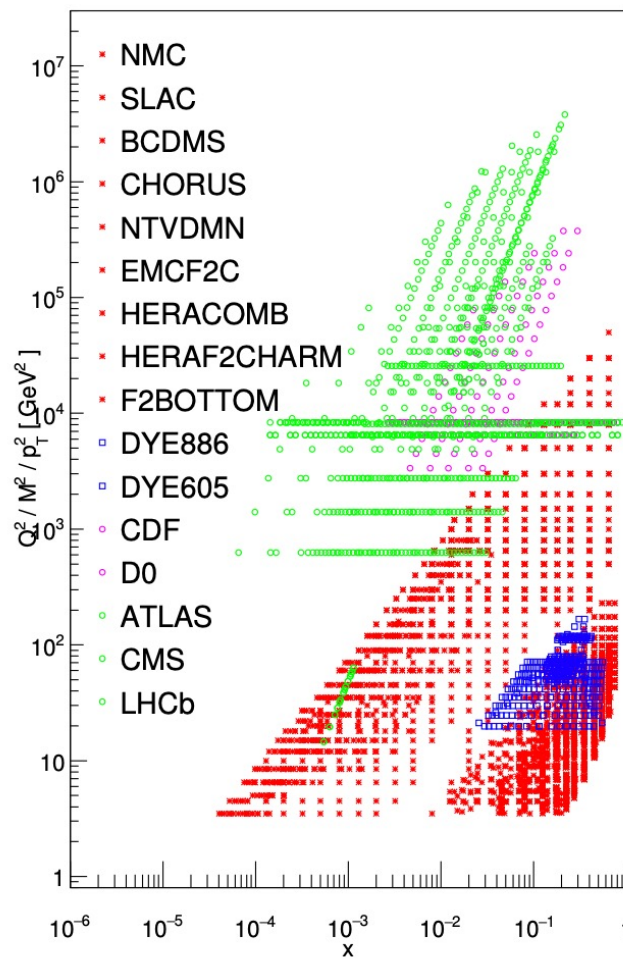


## Polarized PDF

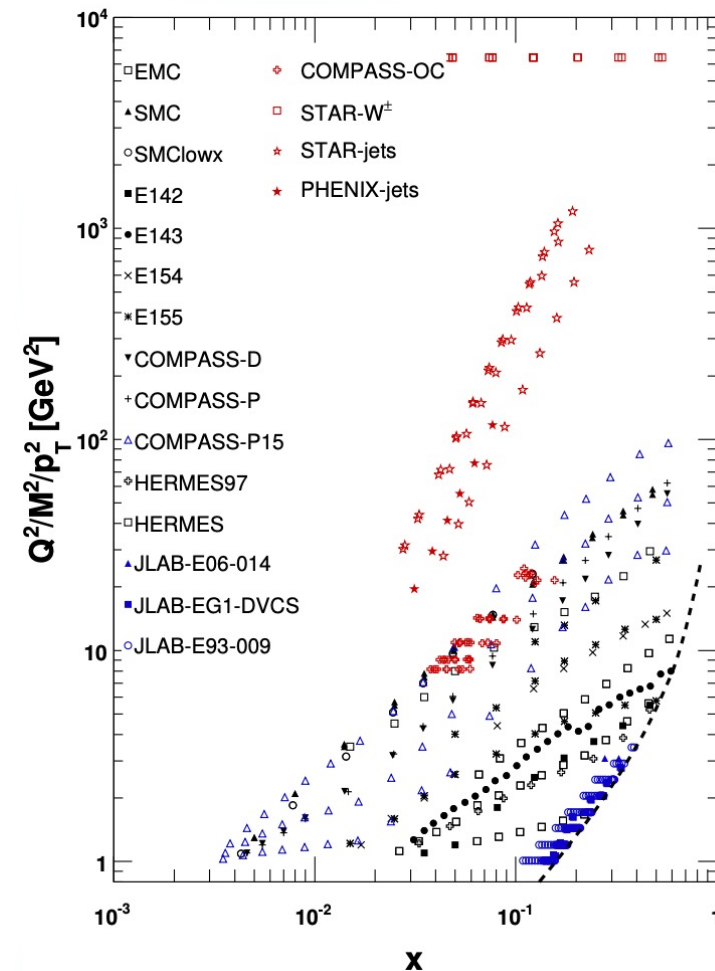
$$\Delta f(x) \equiv f^\uparrow(x) - f^\downarrow(x)$$



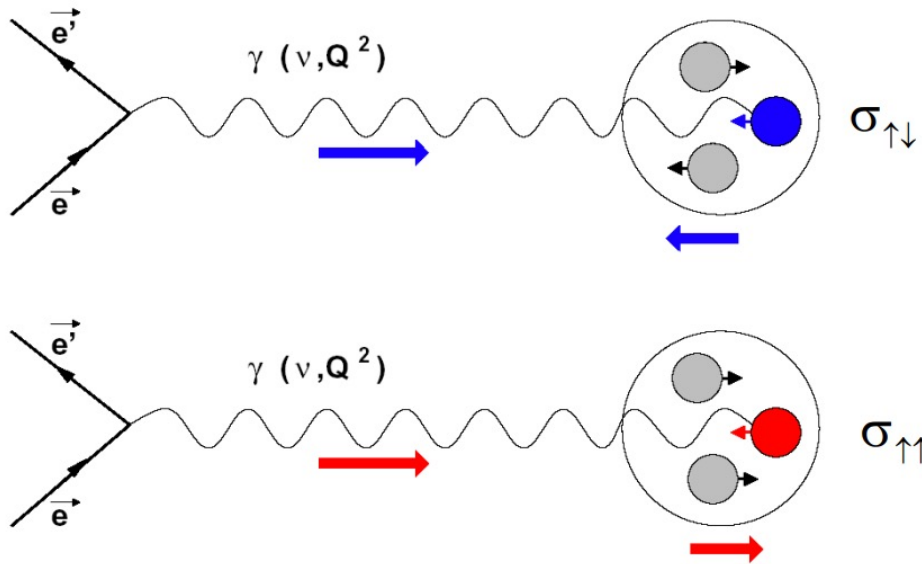
## Unpolarized PDF



## Polarized PDF



# Asymmetry (DIS)

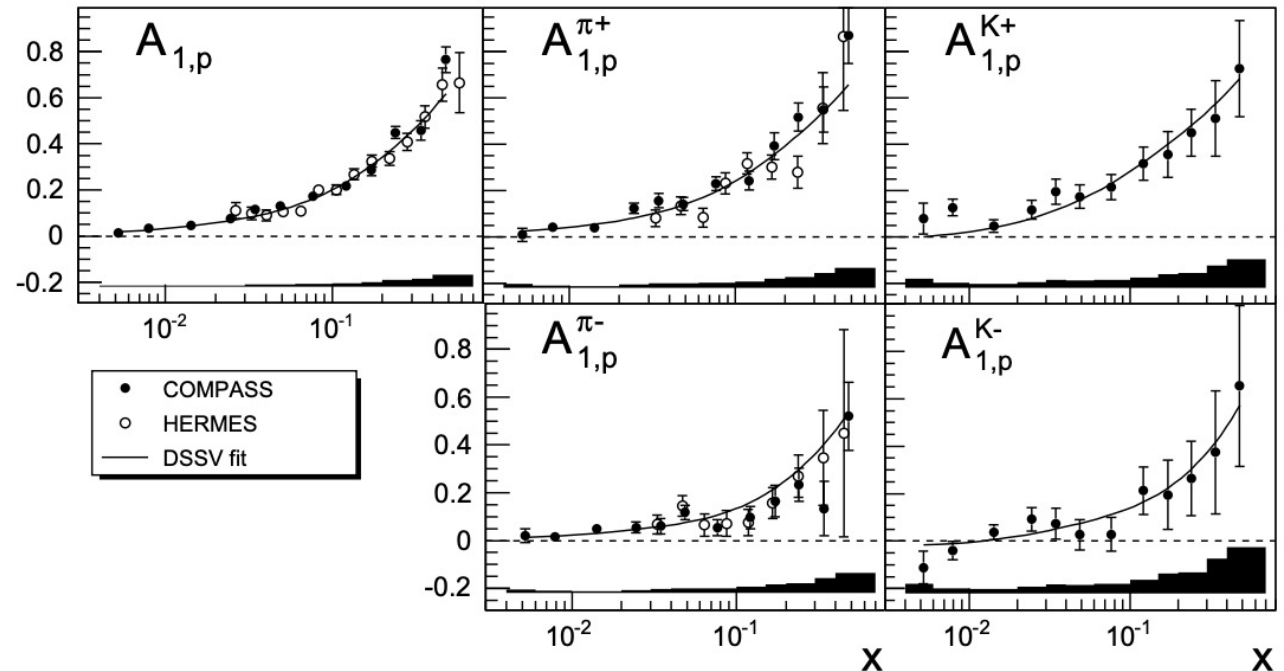
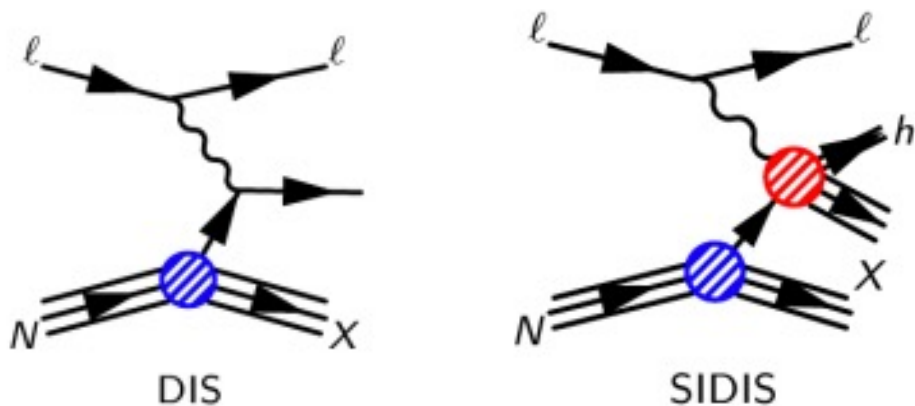


Inclusive DIS

$$A_1(x, Q^2) = \frac{\sigma_{\uparrow\downarrow} - \sigma_{\uparrow\uparrow}}{\sigma_{\uparrow\downarrow} + \sigma_{\uparrow\uparrow}} \approx \frac{\sum_q e_q^2 \Delta q(x, Q^2)}{\sum_q e_q^2 q(x, Q^2)}$$

Semi-Inclusive DIS

$$A_1^h(x, z, Q^2) = \frac{\sigma_{\uparrow\downarrow}^h - \sigma_{\uparrow\uparrow}^h}{\sigma_{\uparrow\downarrow}^h + \sigma_{\uparrow\uparrow}^h} \approx \frac{\sum_q e_q^2 \Delta q(x, Q^2) D_q^h(z, Q^2)}{\sum_q e_q^2 q(x, Q^2) D_q^h(z, Q^2)}$$



# Asymmetry (pp)

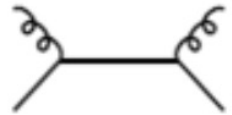
RHIC polarized p+p collisions

dijets

$$\bar{g}\bar{g} \rightarrow gg$$

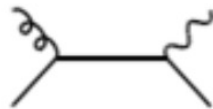


$$\bar{q}\bar{g} \rightarrow qg$$



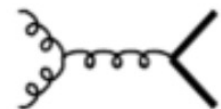
prompt photon

$$\bar{q}\bar{g} \rightarrow \gamma q$$



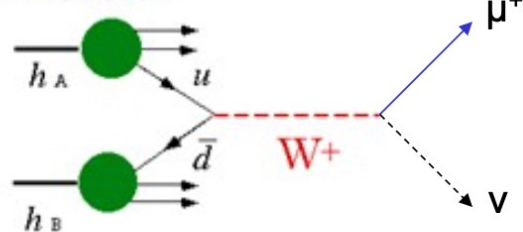
charm/bottom

$$\bar{g}\bar{g} \rightarrow c\bar{c}$$

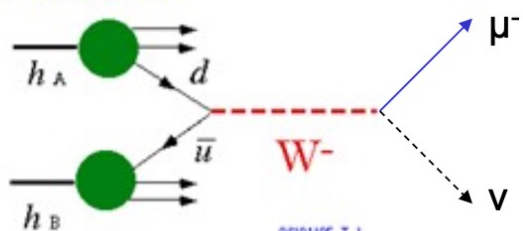


$$\bar{g}\bar{g} \rightarrow b\bar{b}$$

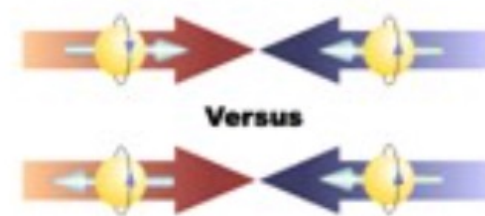
W<sup>+</sup> Production



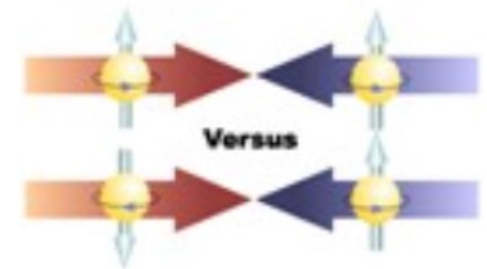
W<sup>-</sup> Production



$$A_{LL} = \frac{\sigma(++)-\sigma(+ -)}{\sigma(++)+\sigma(+ -)}$$



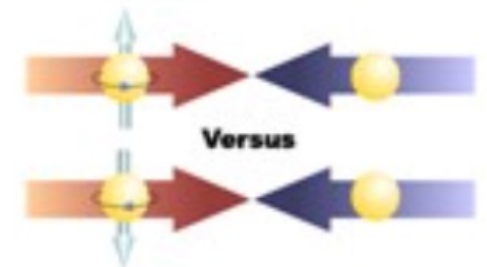
$$A_{TT} = \frac{\sigma(\uparrow\uparrow)-\sigma(\uparrow\downarrow)}{\sigma(\uparrow\uparrow)+\sigma(\uparrow\downarrow)}$$



$$A_L = \frac{\sigma(+)-\sigma(-)}{\sigma(+)+\sigma(-)}$$

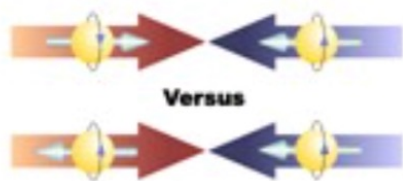


$$A_T = \frac{\sigma(\uparrow)-\sigma(\downarrow)}{\sigma(\uparrow)+\sigma(\downarrow)}$$



# Asymmetry measured at RHIC

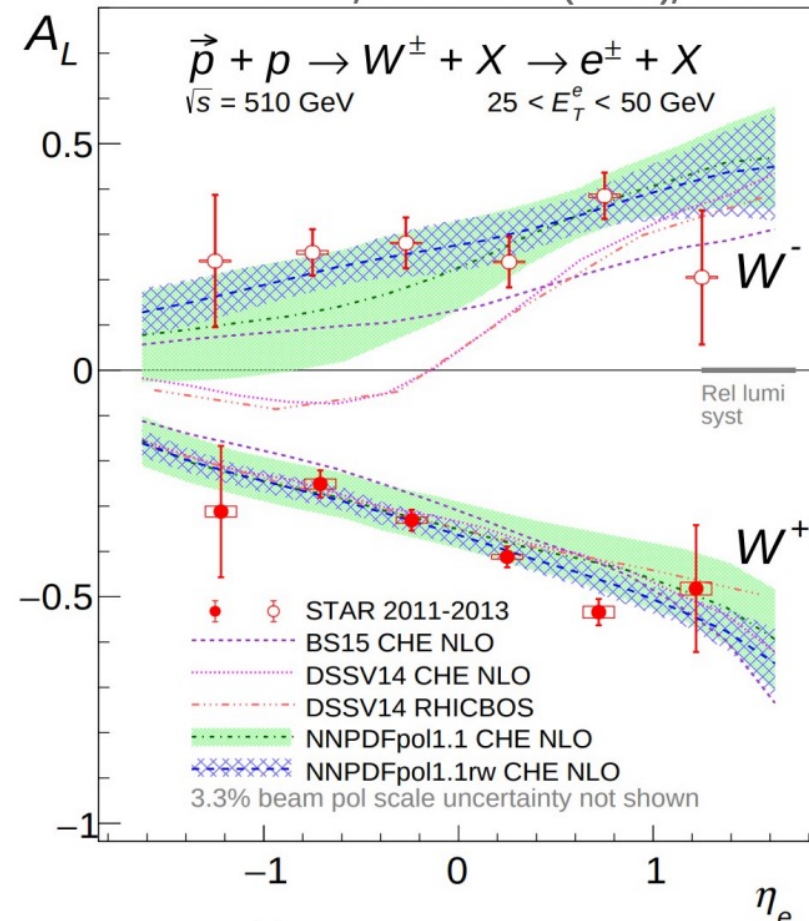
$$A_{LL} = \frac{\sigma(++)-\sigma(+-)}{\sigma(++)+\sigma(+-)}$$



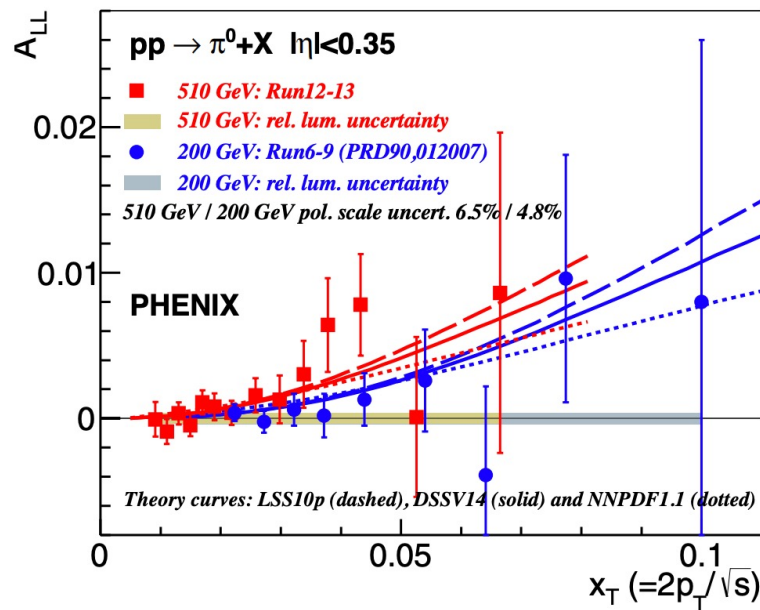
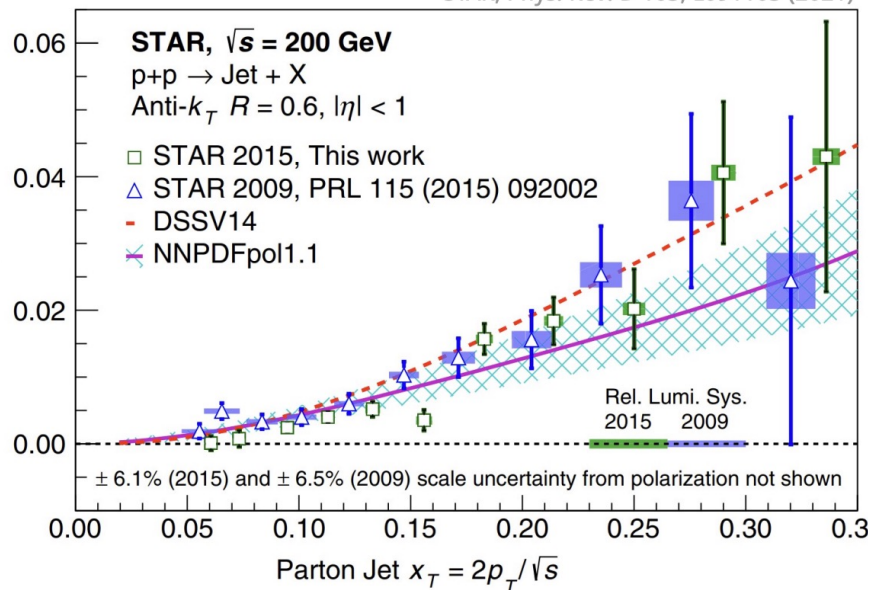
$$A_L = \frac{\sigma(+)-\sigma(-)}{\sigma(+)+\sigma(-)}$$



STAR, PRD RC 99 (2019), 051102



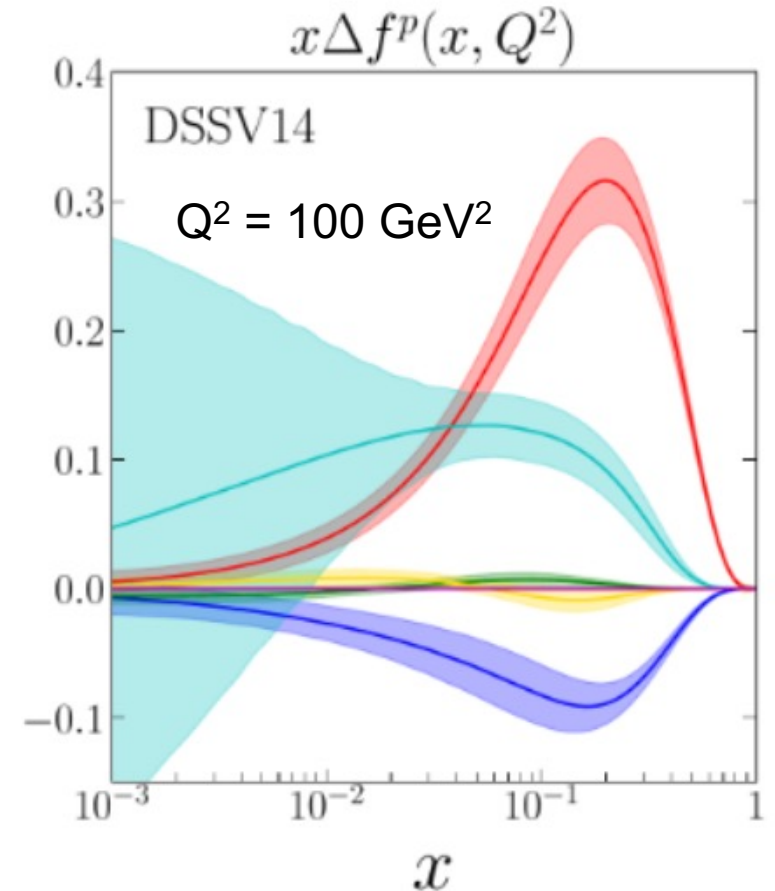
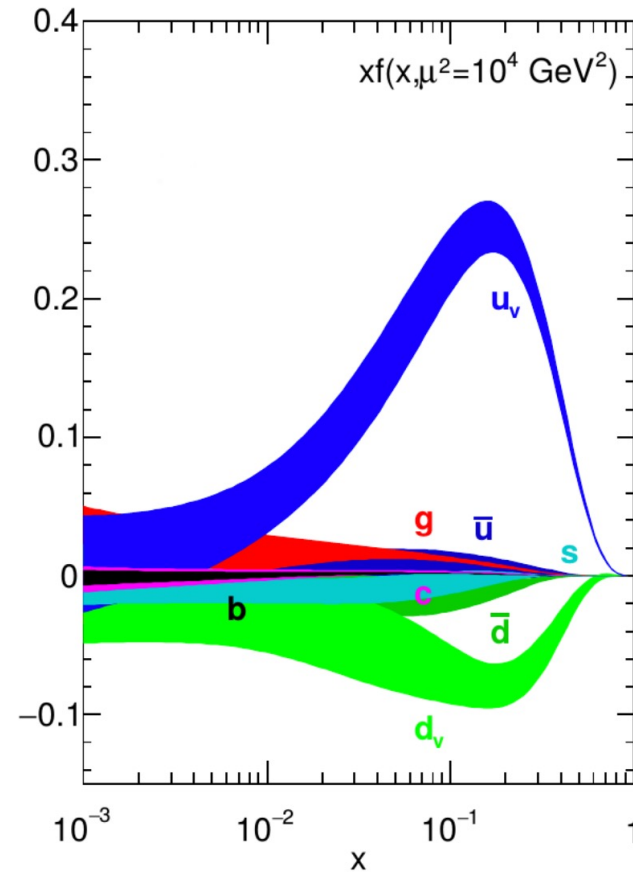
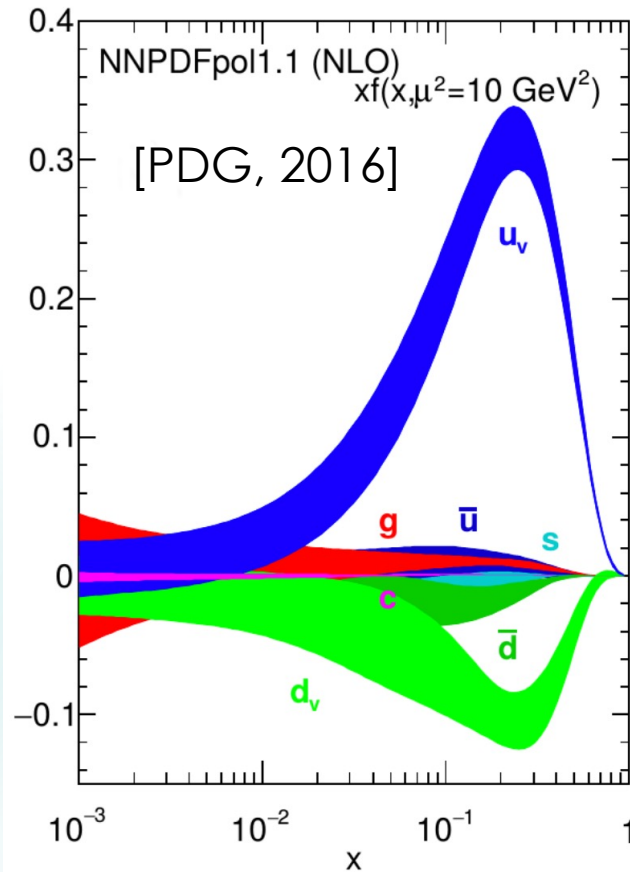
STAR, Phys. Rev. D 103, L091103 (2021)



# Global Fit for Polarized PDF

arXiv:1711.07916

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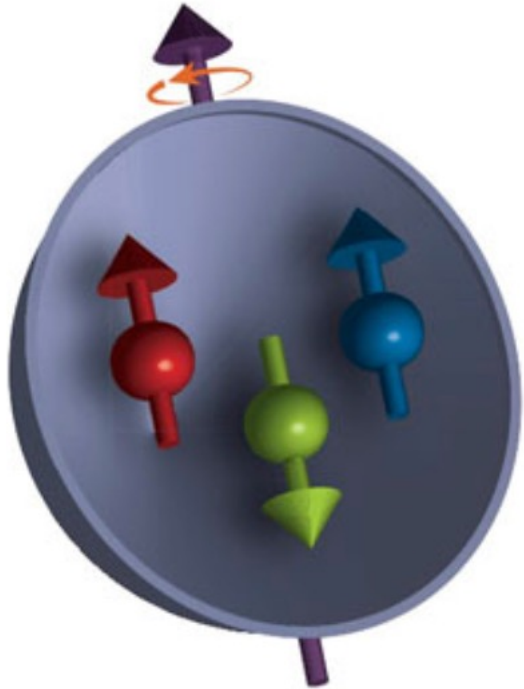


The most recent analyses of polarized PDFs are DSSV14[29] and NNPDFpol1.1[18]. Motivated by the interest in assessing the impact of RHIC proton-proton data, they upgrade the corresponding previous analyses, DSSV08[[19], [222]] and NNPDFpol1.0[227], with data respectively on double-spin asymmetries for inclusive jet production[228] and  $\pi^0$  production[229] (DSSV14<sup>9</sup>), and on double-spin asymmetries for high- $p_T$  inclusive jet production[[228], [230], [231]] and single-spin asymmetries for  $W^\pm$  production[232] (NNPDFpol1.1). The new data have been included in NNPDFpol1.1 by means of Bayesian reweighting[233], and in DSSV14 by means of a full refit.

Overall, both the DSSV14 and NNPDFpol1.1 PDF determinations are state-of-the-art in the inclusion of the available experimental information. The data sets in the two analyses differ between each other only in fixed-target SIDIS and RHIC  $\pi^0$  production measurements, included in DSSV14, but not in NNPDFpol1.1. The information brought in by these data is complementary to that provided by RHIC  $W^\pm$  production and inclusive jet production data respectively, although fraught with larger theoretical uncertainties related to fragmentation.

# Nucleon spin

- ▶ **Constitute Quark model : spin is 100% from constituent quarks**



$$|p \uparrow\rangle = \sqrt{\frac{1}{2}} (p_S \chi(M_S) + p_A \chi(M_A))$$

$$P(M_S) = \frac{1}{\sqrt{6}} [(ud + du)u - 2uud]$$

$$P(M_A) = \frac{1}{\sqrt{2}} (ud - du)u$$

$$\chi(M_S) = \frac{1}{\sqrt{6}} (\uparrow\downarrow\uparrow + \downarrow\uparrow\uparrow - 2\uparrow\uparrow\downarrow)$$

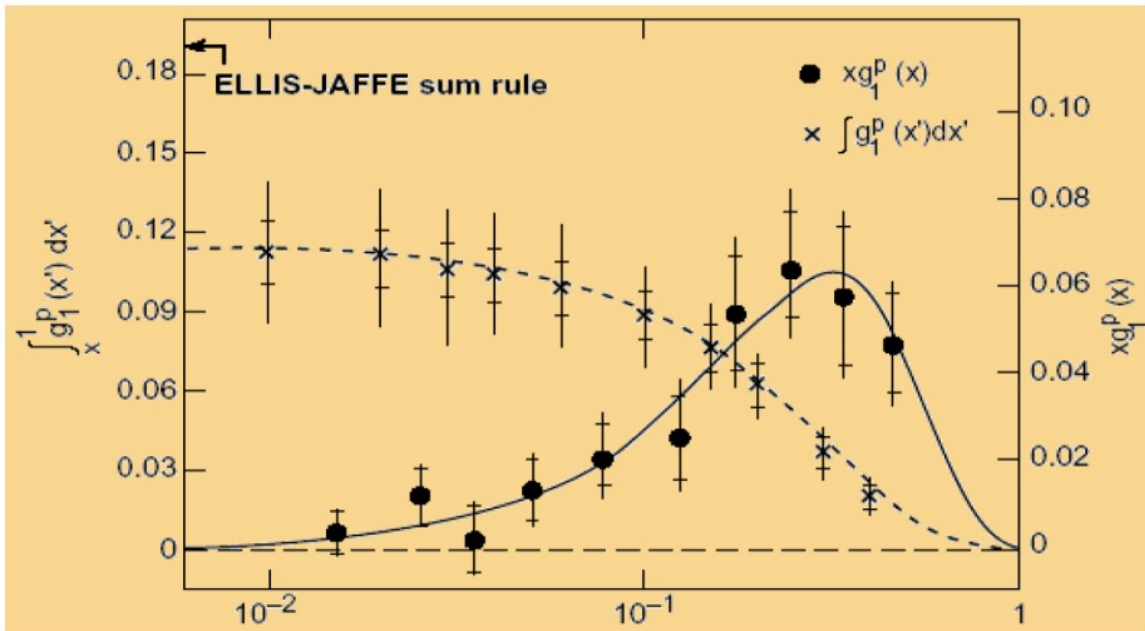
$$\chi(M_A) = \frac{1}{\sqrt{2}} (\uparrow\downarrow\uparrow - \downarrow\uparrow\uparrow)$$

$$\frac{1}{2} = \frac{1}{2} \Delta \Sigma$$

$$\Delta \Sigma \equiv \Delta u + \Delta d + \Delta s$$

# Nucleon spin

- ▶ Discovered by EMC experiment at CERN (polarized muon + polarized proton) Confirmed by SMC, SLAC, HERMES: Quark contribution is ~25% (“Spin Crisis”)



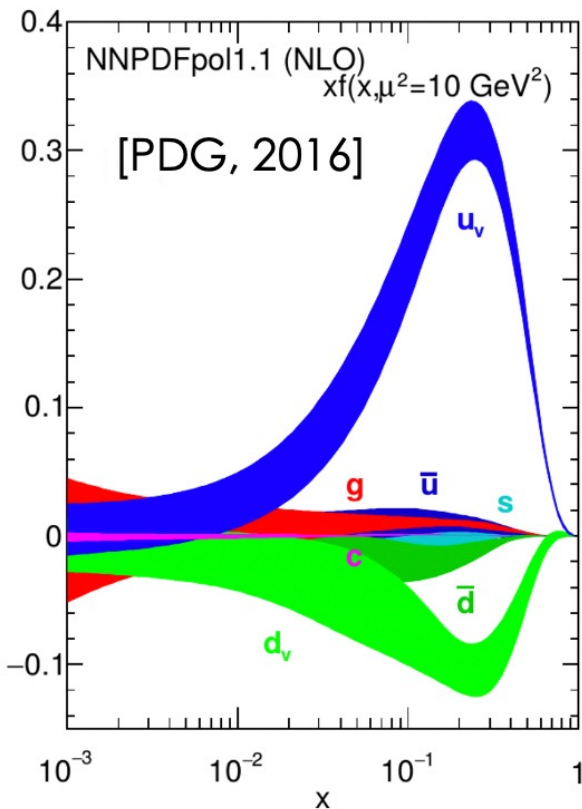
$$g_1(x) = \frac{1}{2} \sum_q e_q^2 [\Delta q(x) + \Delta \bar{q}(x)]$$

$$\int_0^1 g_1^p(x) dx = 0.126 \pm 0.018$$

$$\Delta\Sigma = \sum_q [\Delta q + \Delta \bar{q}] = 0.12 \pm 0.17$$

# Nucleon spin

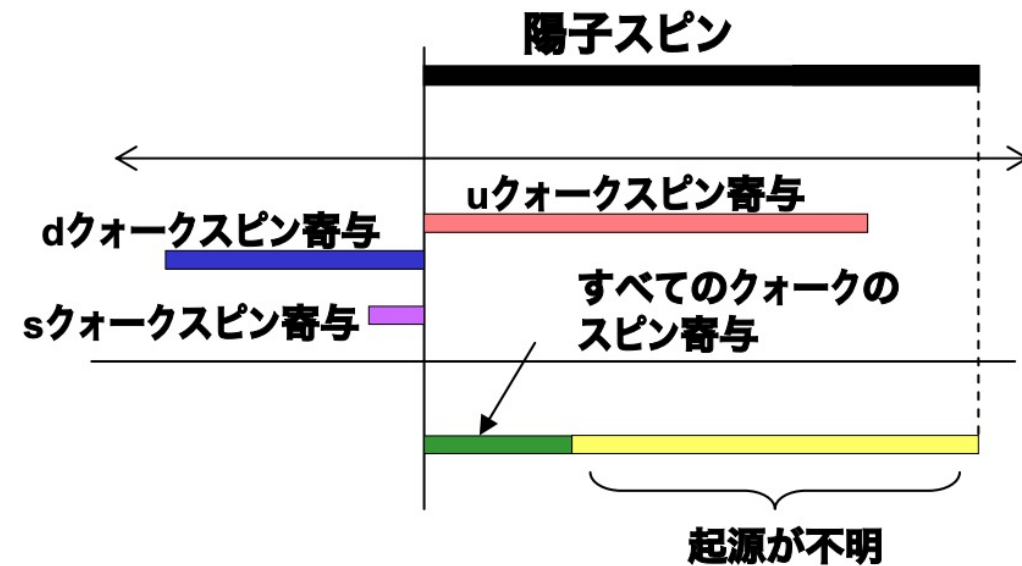
- ▶ Discovered by EMC experiment at CERN (polarized muon + polarized proton) Confirmed by SMC, SLAC, HERMES: Quark contribution is ~25% (“Spin Crisis”)



$$\Delta u = 0.82 \pm 0.02$$

$$\Delta d = -0.43 \pm 0.02$$

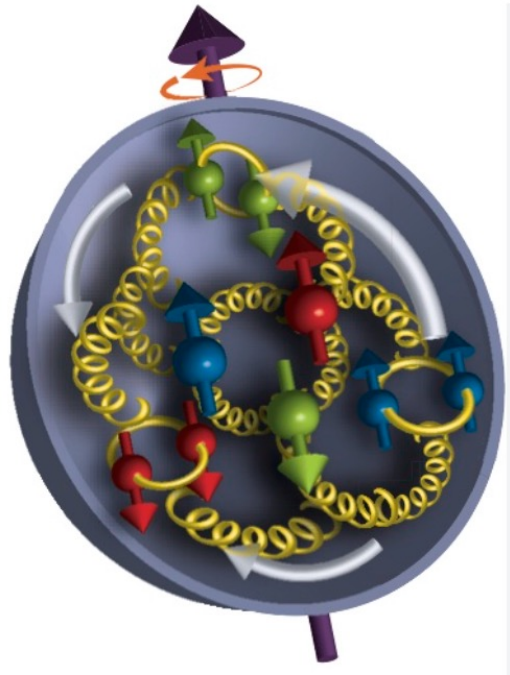
$$\Delta s = -0.10 \pm 0.02$$





# Nucleon spin

## ▶ Current picture of spin composition



$$\frac{1}{2} = \frac{1}{2} \Delta \Sigma + \Delta G + (L_q + L_g)$$

Gluon spin

Angular momentum of all quarks and gluons



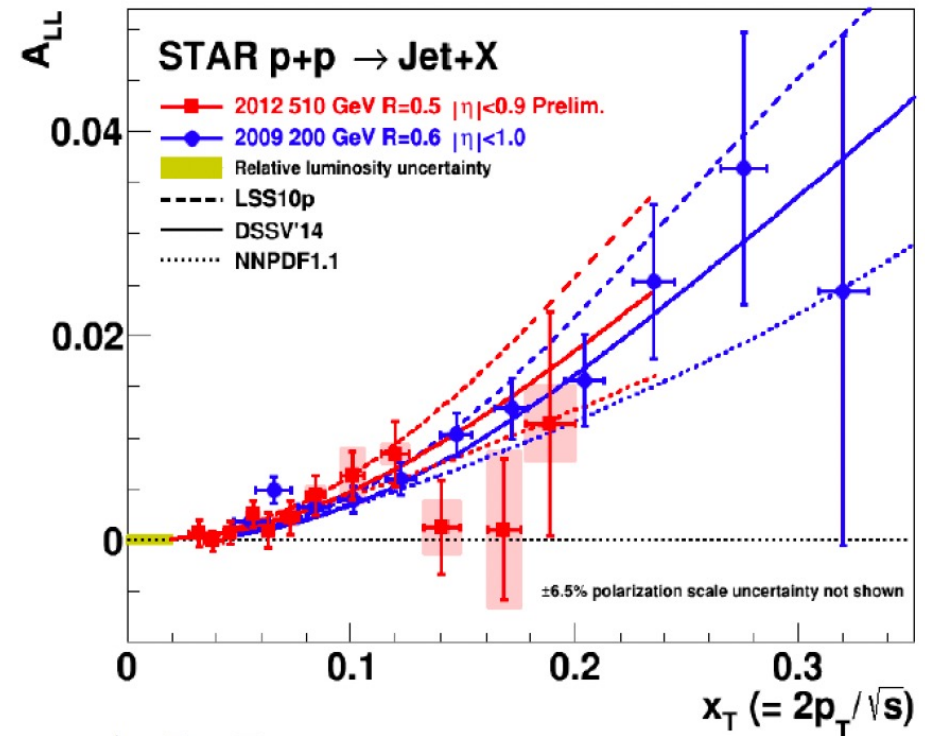
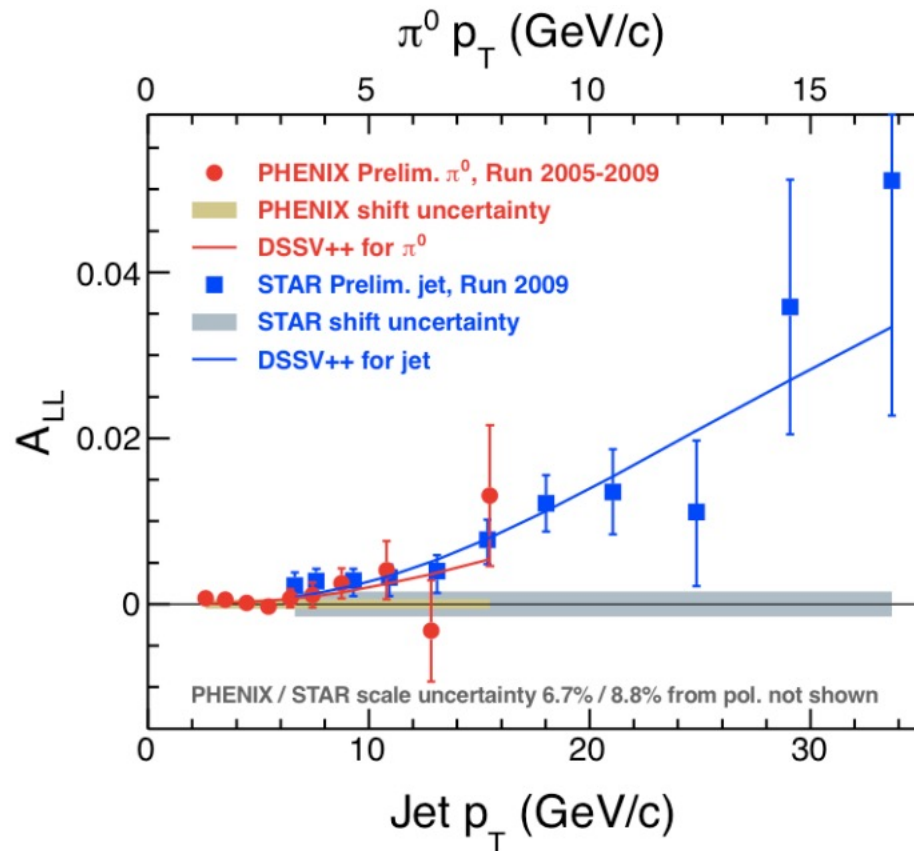
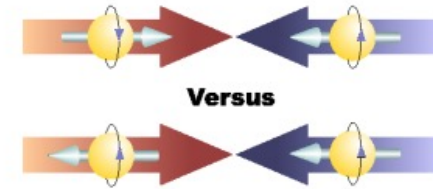
RHIC spin program (polarized proton)



# Measurement at RHIC

- ▶ Longitudinal spin asymmetry :  $A_{LL}$
- observation of non-zero  $A_{LL}$  associated with non-zero  $\Delta G$  ( $\sim 0.3$ )

$$A_{LL} = \frac{\sigma(++)-\sigma(+-)}{\sigma(++)+\sigma(+-)}$$

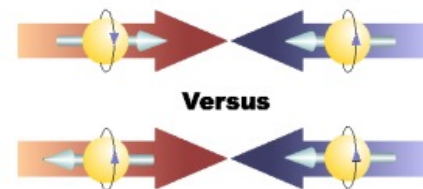


# Gluon contribution to spin

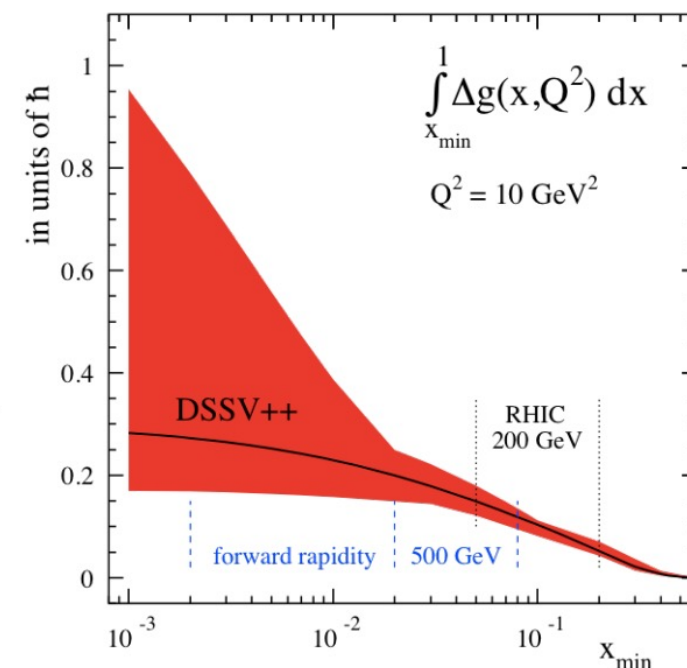
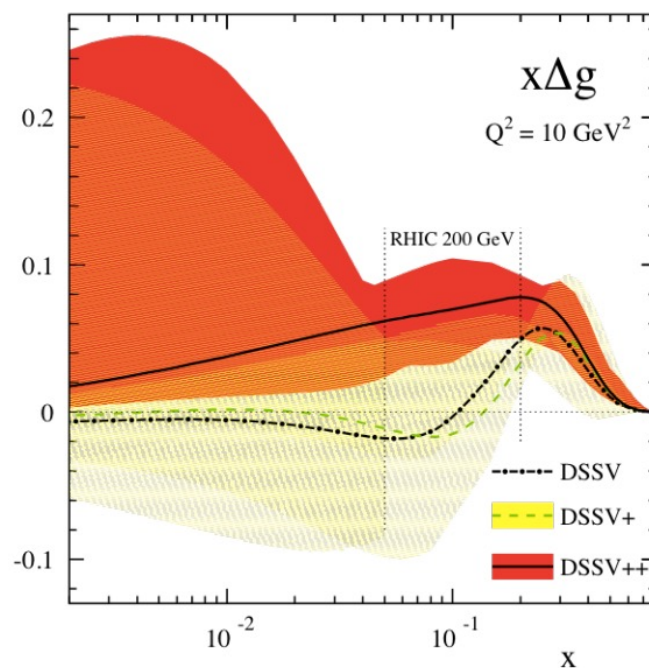
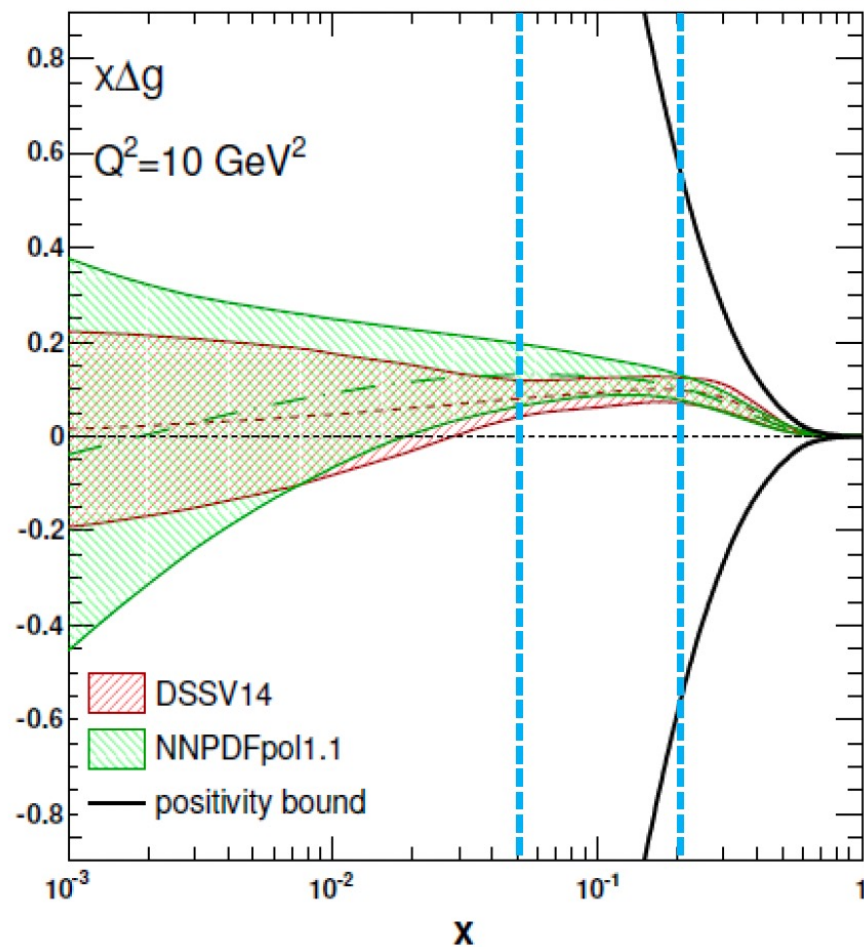
$$A_{LL} = \frac{\sigma(++)-\sigma(+-)}{\sigma(++)+\sigma(+-)}$$

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## ▶ Longitudinal spin asymmetry : $A_{LL}$



arXiv:1503.03518



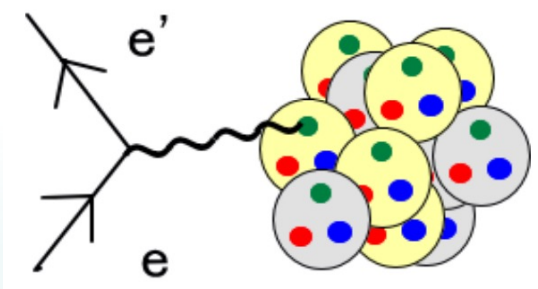
$$Q^2 = 10 \text{ GeV}^2 \quad \int_{0.05}^{0.2} dx \Delta g(x, Q^2)$$

NNPDFpol1.1	$+0.15 \pm 0.06$
DSSV14	$0.10^{+0.06}_{-0.07}$

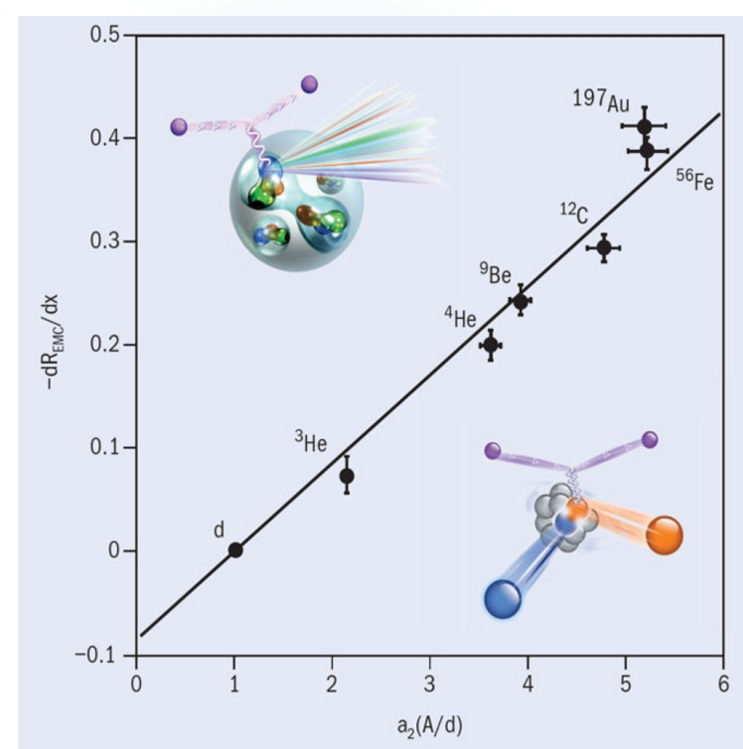
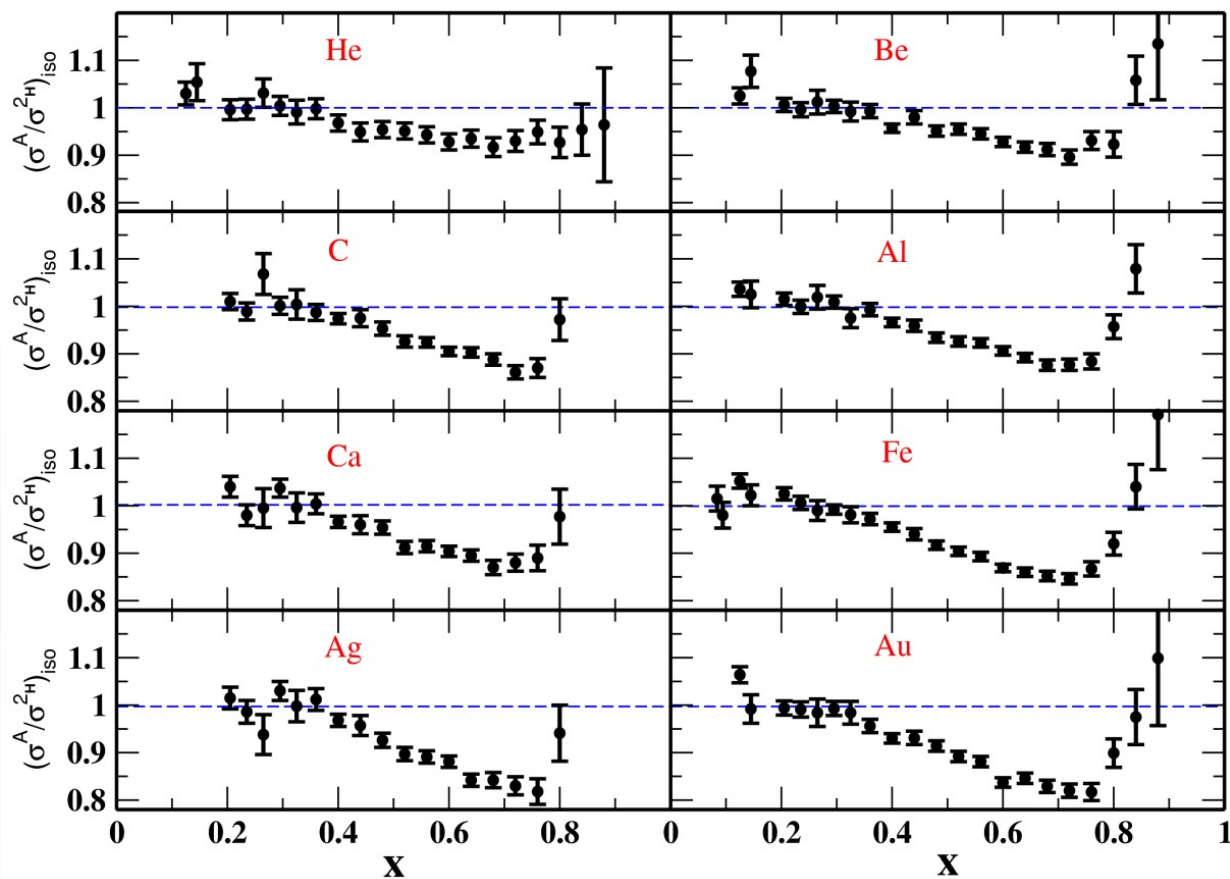
# PDF in nuclei ( $x > 0.3$ )

► Proton bound in the nucleus is different from a free proton?

Phys. Rev. D 49, 4348 (1994)



Naïve expectation was nuclear effects in DIS would be small since DIS energy is much larger than binding energy.



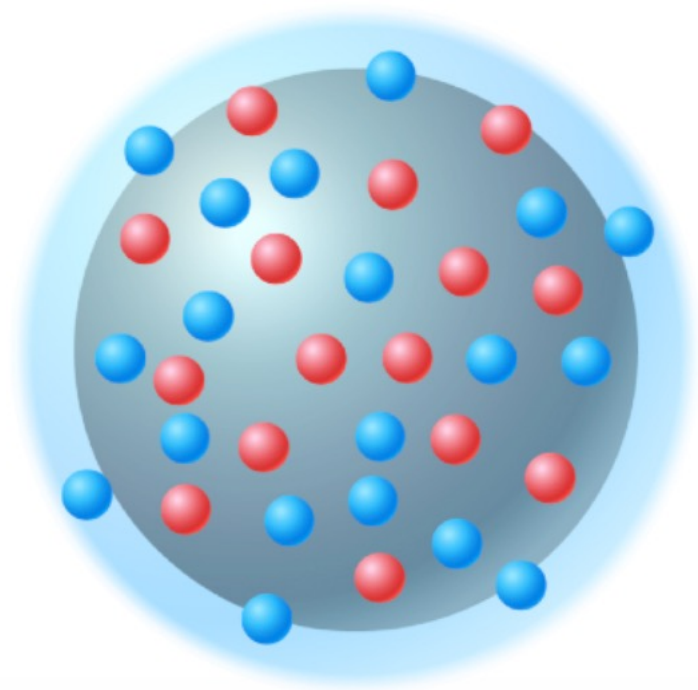
**DIS off a bound nucleon  $\neq$  DIS off a free nucleon (EMC effect)**

# Clusters in nuclei

## ► Modern view of atomic nucleus

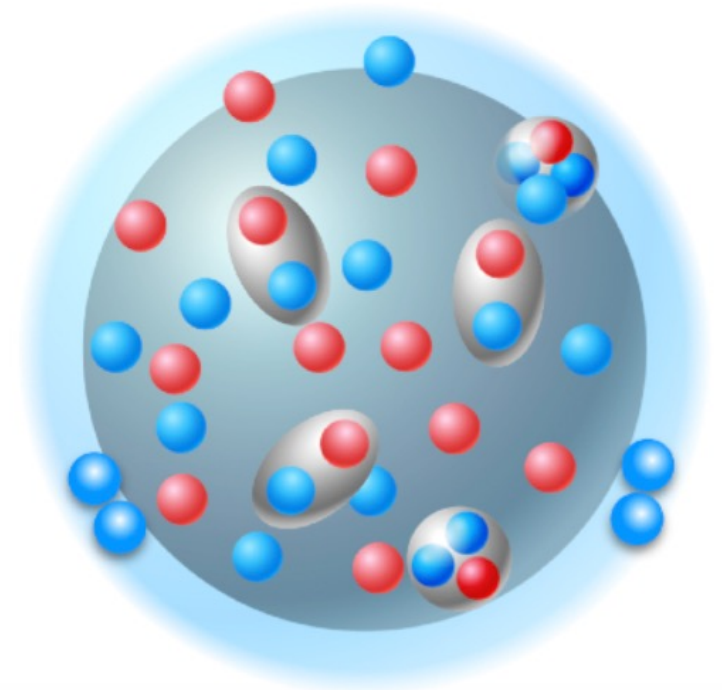
### Conventional picture

Uniform nuclei formed by independent neutrons and protons



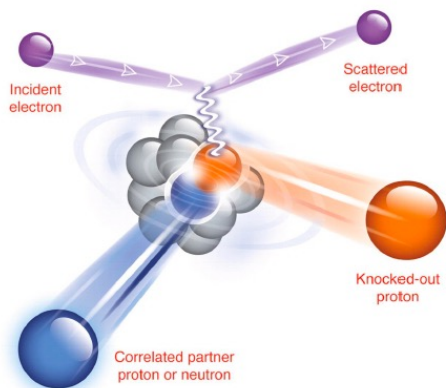
### Modern picture

Various clusters ( $d$ ,  $t$ ,  ${}^3\text{He}$ ,  $\alpha$ , ...) develop in all nuclei

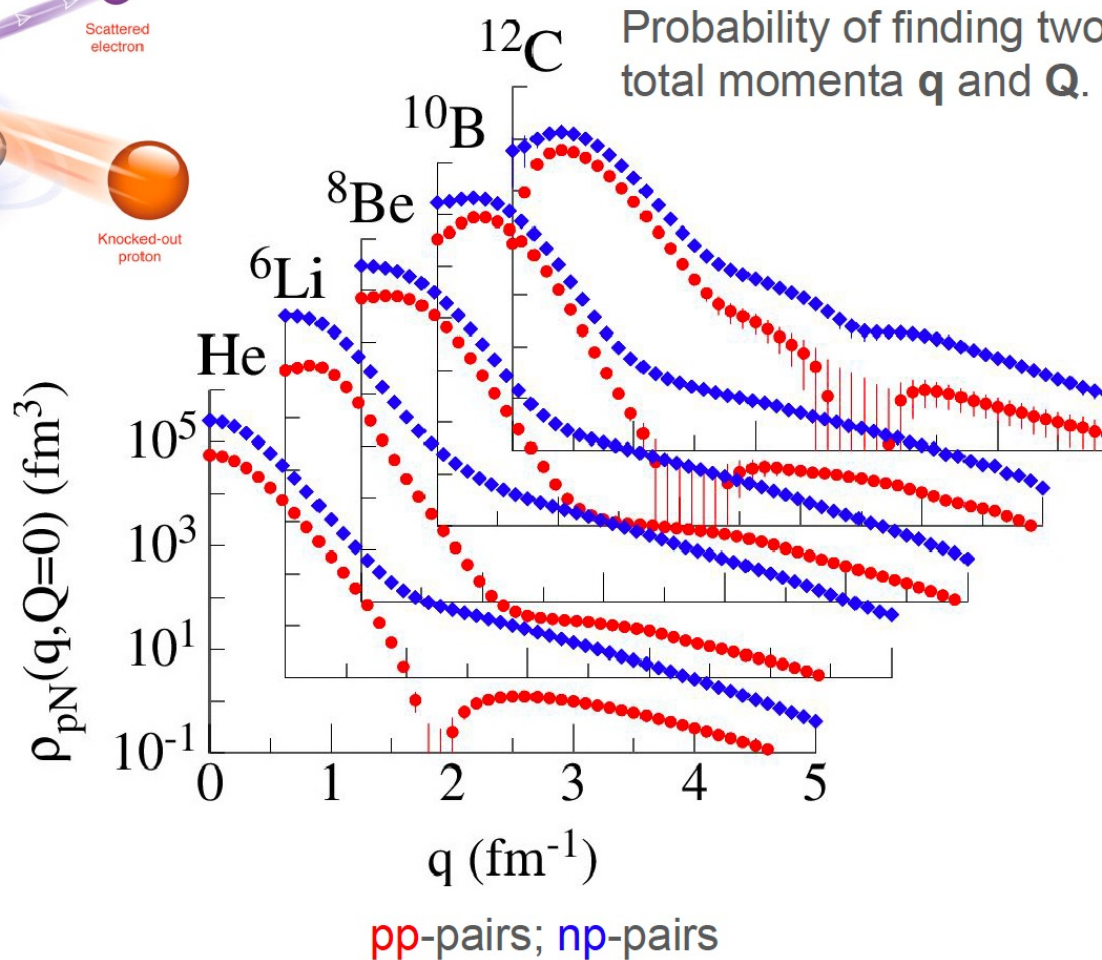


# Clusters in nuclei

## Two-nucleon correlations & momentum distributions



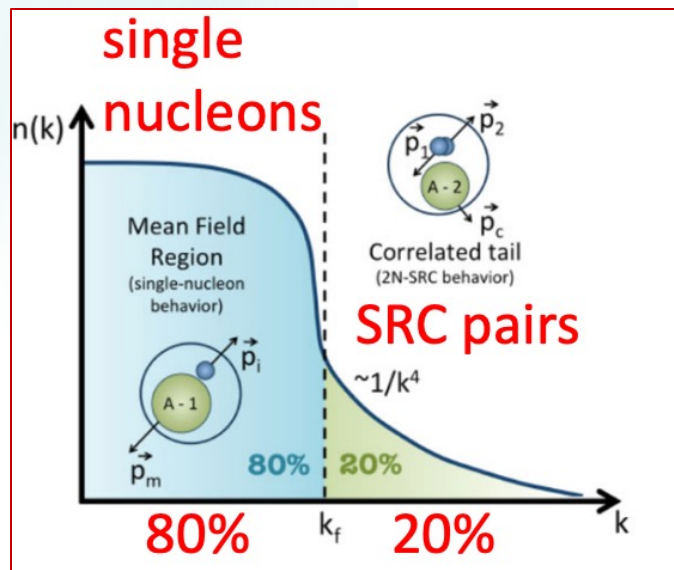
Probability of finding two nucleons with relative and total momenta  $q$  and  $Q$ .



Tensor correlations lead to large differences in the  $np$  versus  $pp$  distributions.

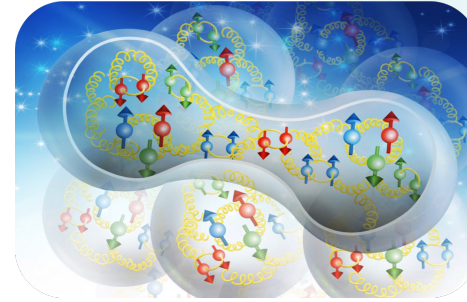
These differences are observed in  $A(e, e'np)$  and  $A(e, e'pp)$  reactions.

Schiavilla Carlson Wiringa Pieper PRL98(2007) & PRC89(2014)

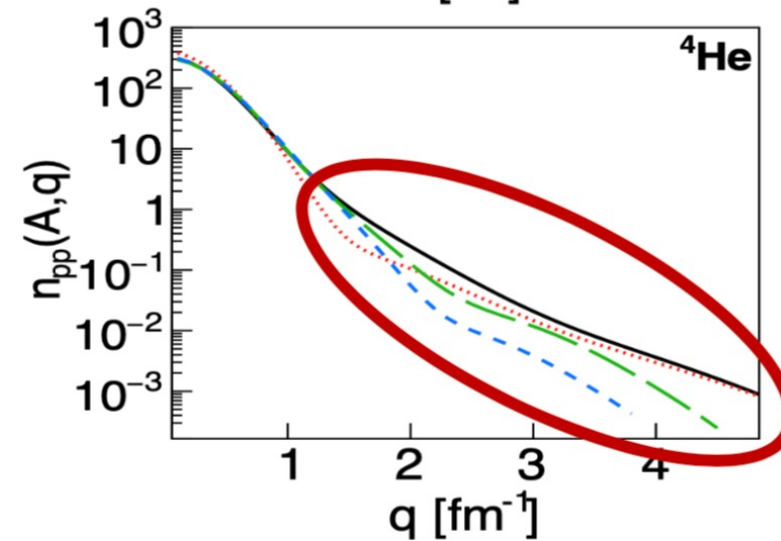
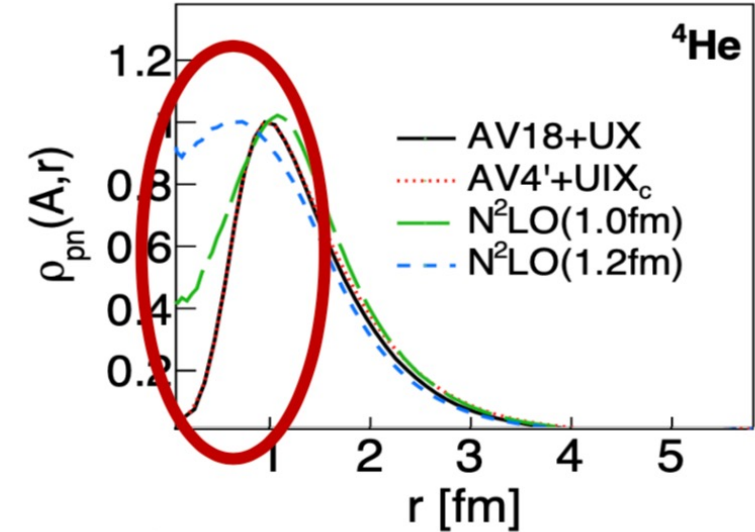
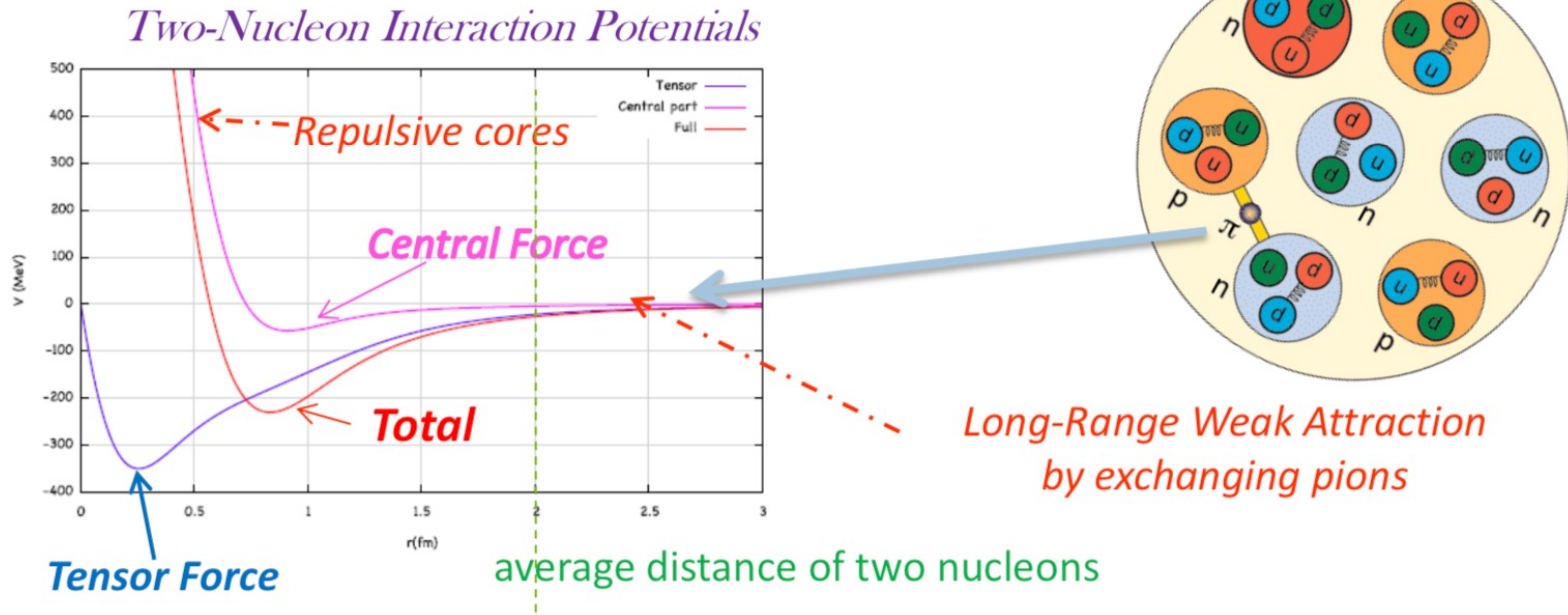


# Short range correlation

NN Short-range correlation



## Realistic Nucleon-Nucleon Interactions:



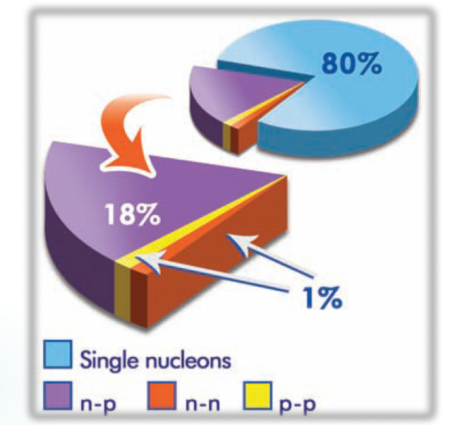
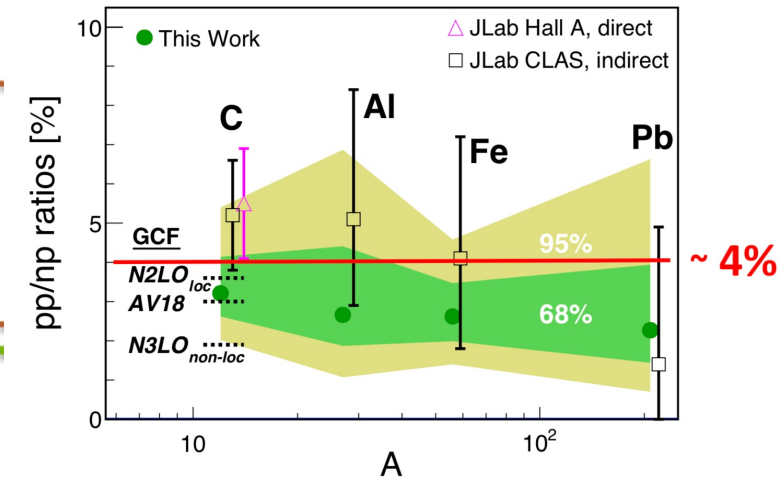
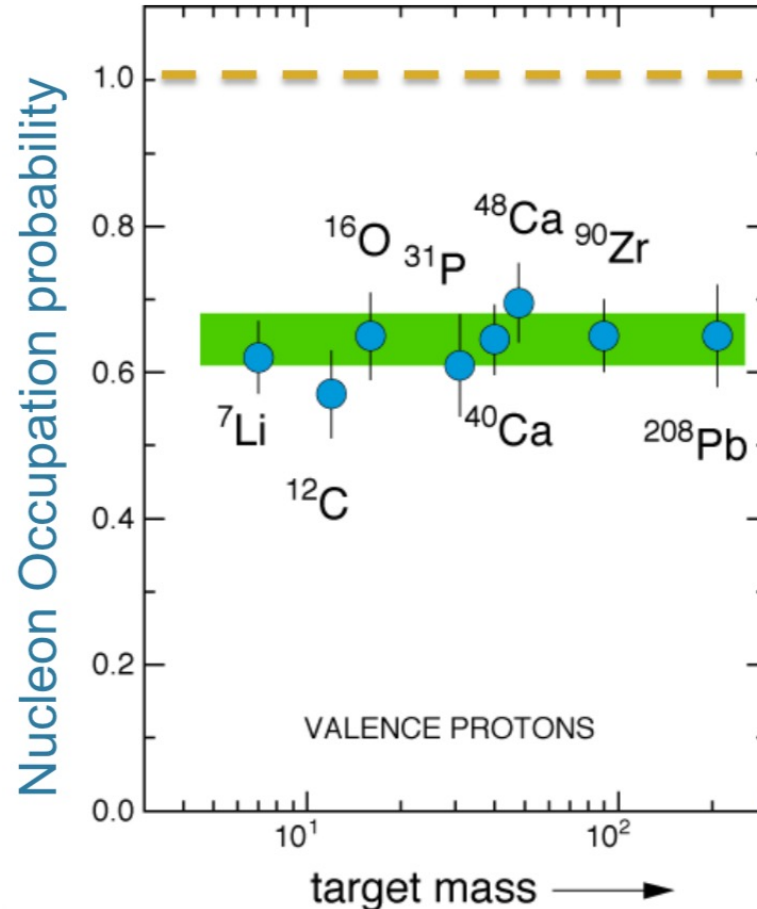
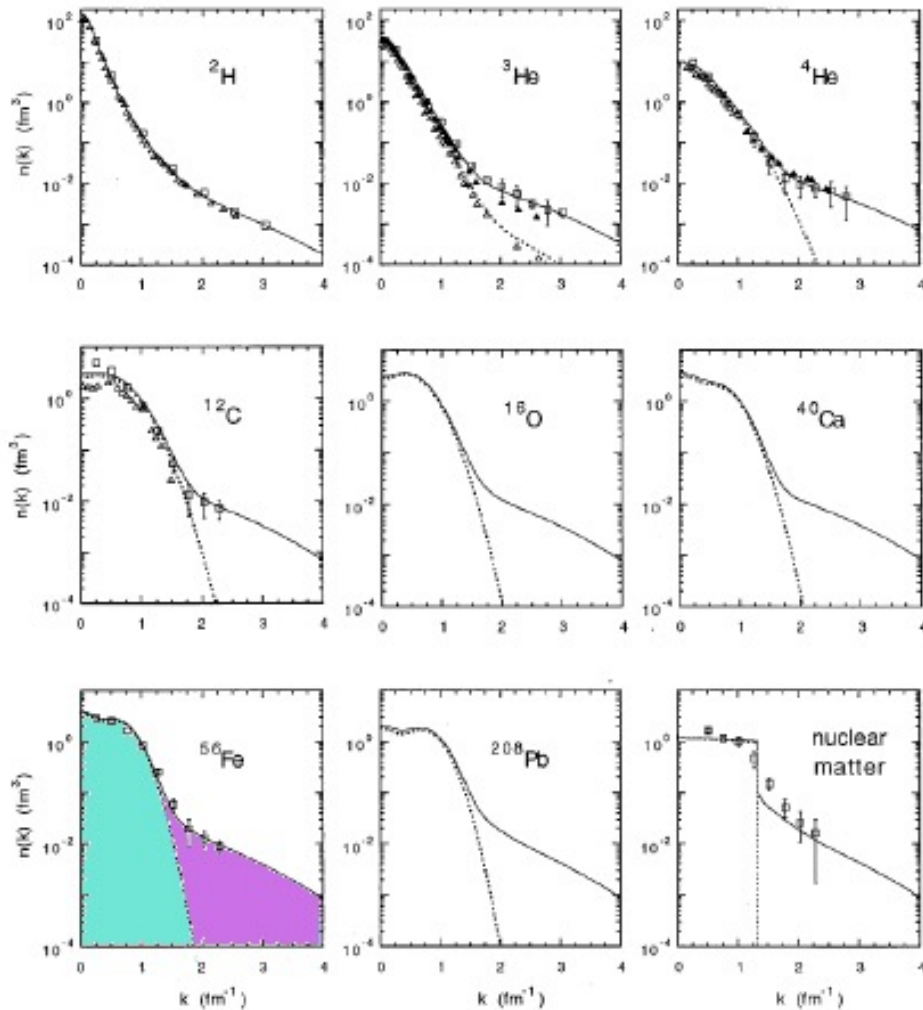
Large model dependence at short-distance / high-momentum

# Short range correlation

L. Lapiks, Nuclear Physics A 553, 297 (1993)

65% for naive shell model calculations. Fraction reaches 80% in more modern calculations

## NN Short-range correlation

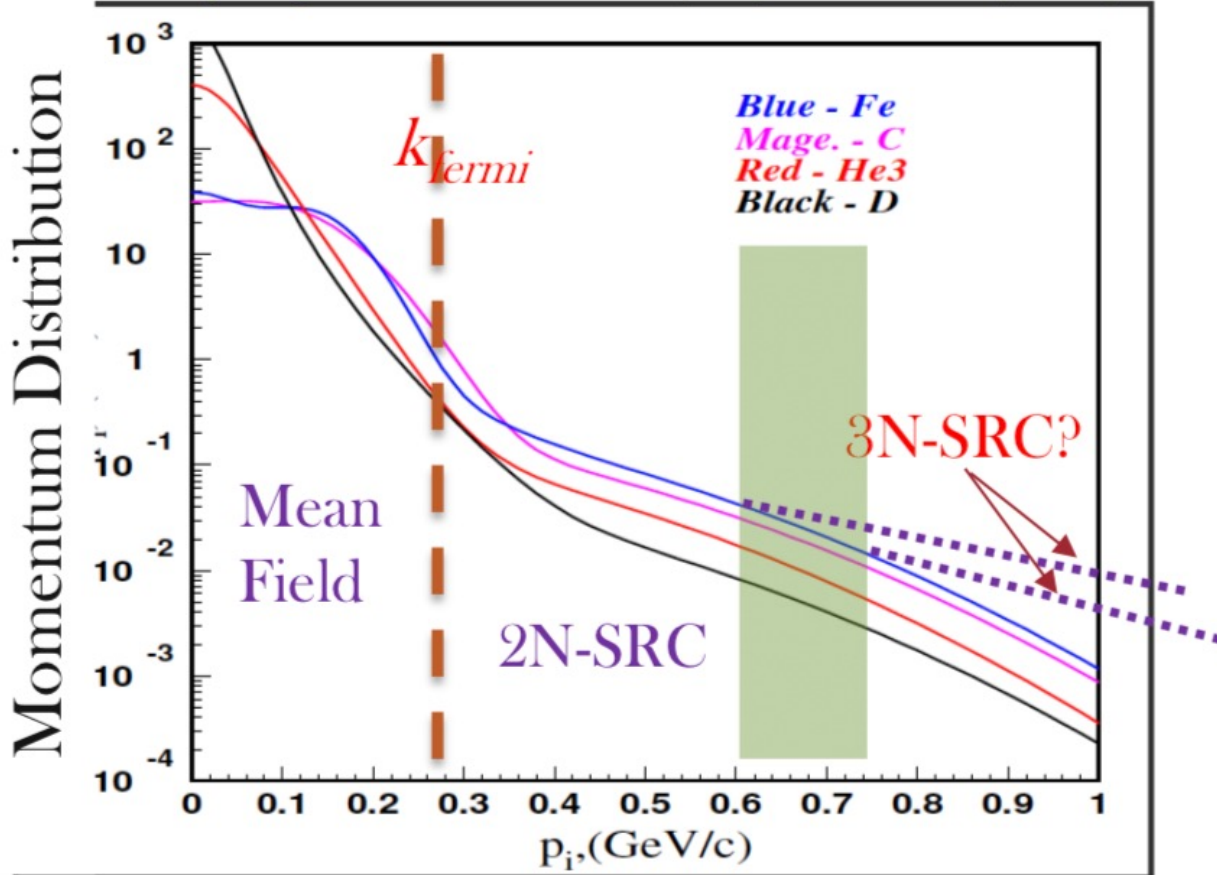




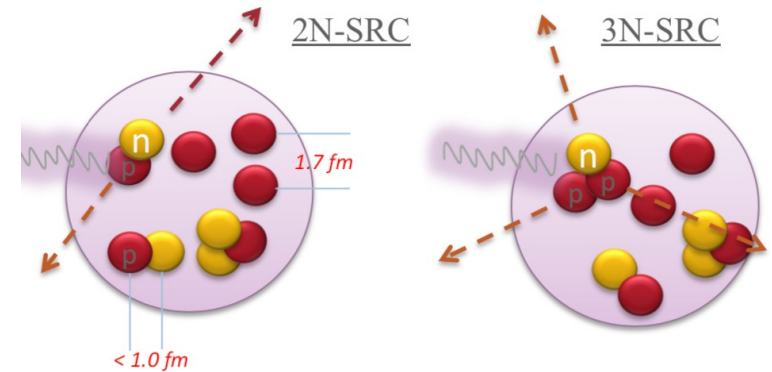
# Short range correlation

NN Short-range correlation:  
From 2-nucleons (2N-SRC) to 3-nucleons/4-nucleons(alpha?)-SRC

C. Ciofi degli Atti and S. Simula, Phys. Rev. C 53 (1996).

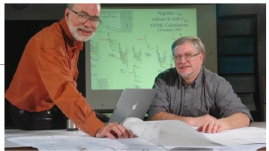
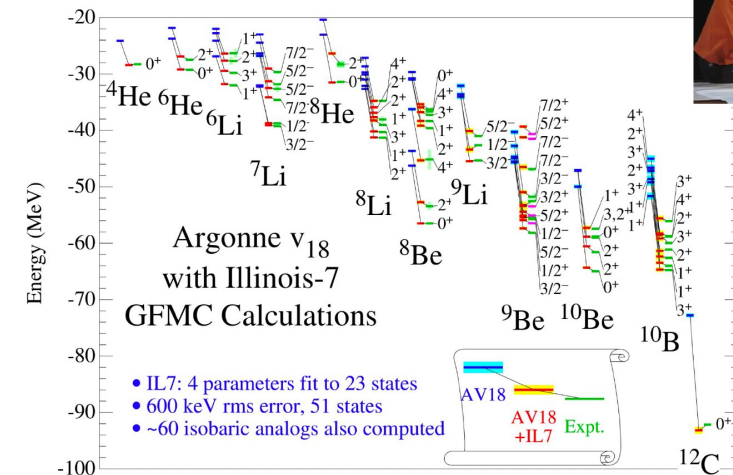


Zhihong Ye, iHIC2018



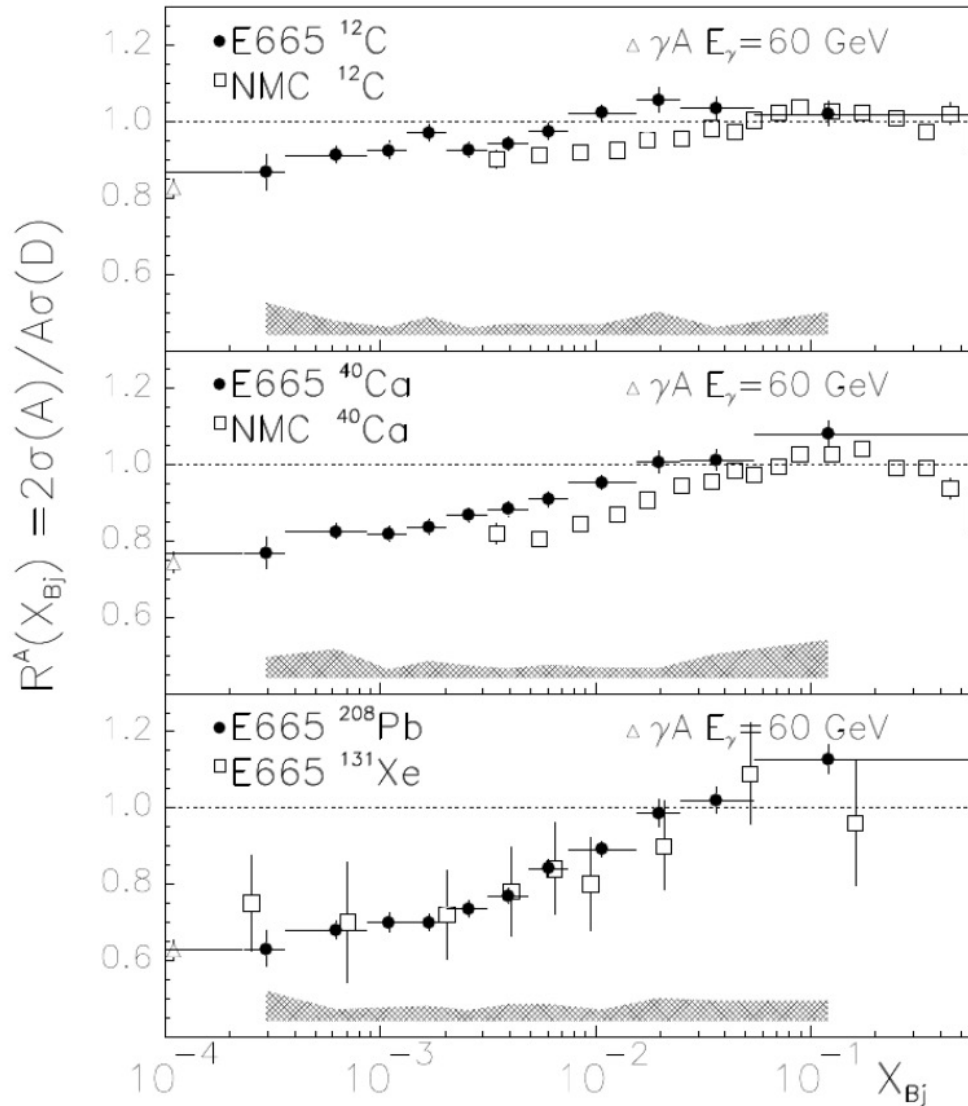
- 重い原子核における2N-SRC, 3N-SRC, 4N-SRC  
→ deuteron, 3H/3He, alpha cluster?  
→ 高密度原子核物質へ(EMC effects, 中性子星EOS)

Spectra of light nuclei with AV18+IL7

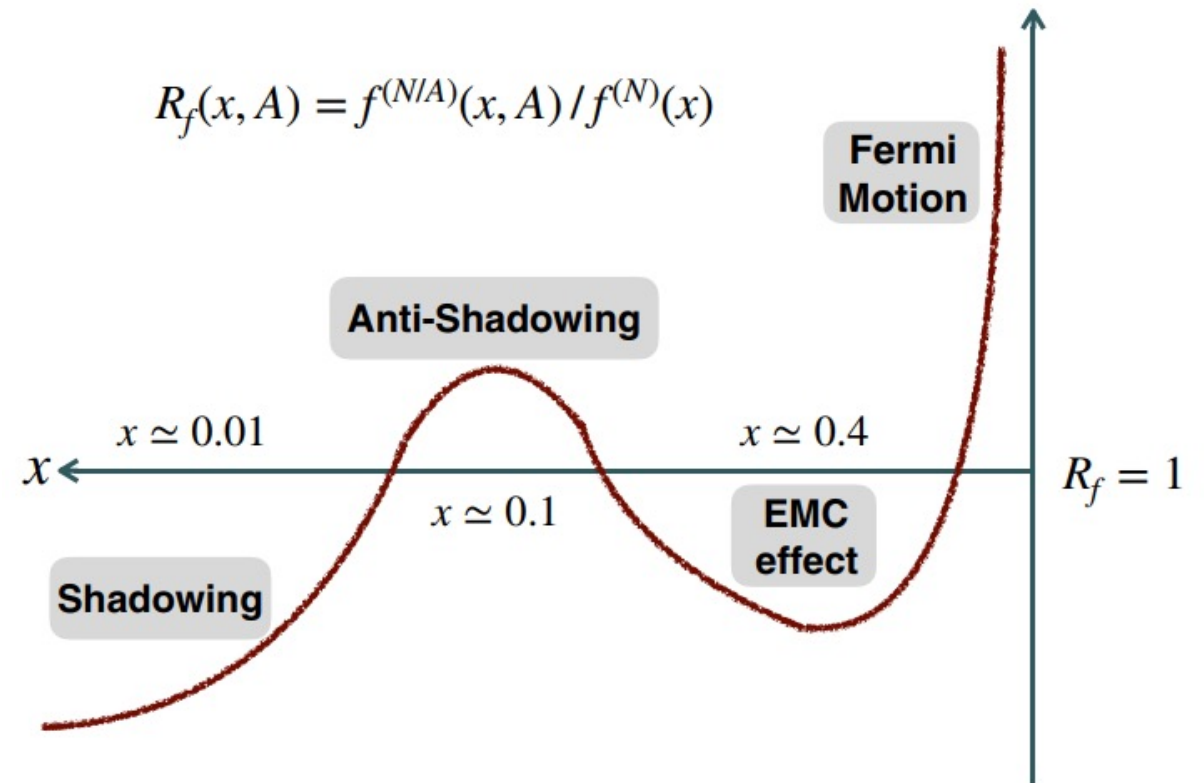


# PDF in nuclei ( $x < 0.3$ )

Phys. Rev. Lett. 68 (1992) 3266

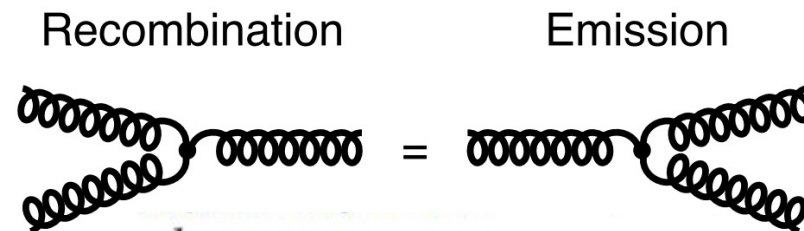


► Reduction of PDF in small- $x$  ( $x < 0.3$ ) called “shadowing”.



# Gluon Saturation

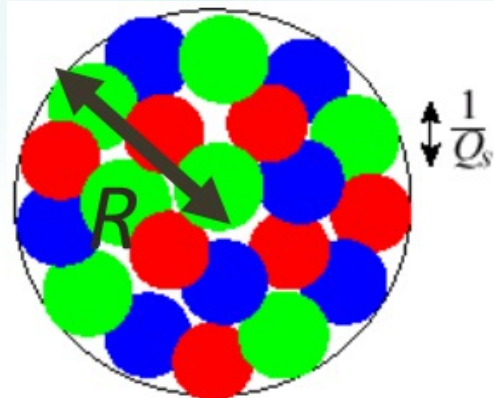
- ▶ We know that at small- $x$ , gluons are dominated in proton and nuclei.
- ▶ When the density of gluons becomes high, they start to interact with each other and gluons are saturated.



$$\frac{d}{dt}N(t) = \kappa [N(t) - N(t)^2]$$

- ▶ Saturation scale =  $Q_s(x, A)$  : Typical transverse momentum carried by gluons

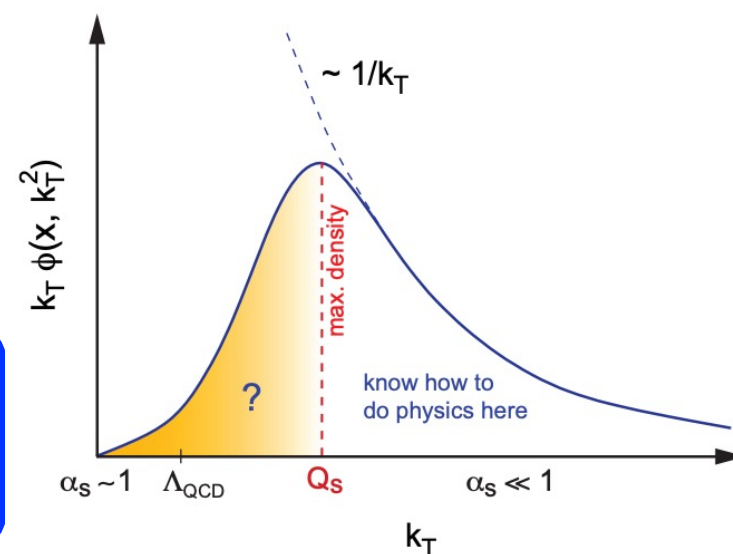
Gluons fill the transverse area of hadron ( $\pi R^2$ )



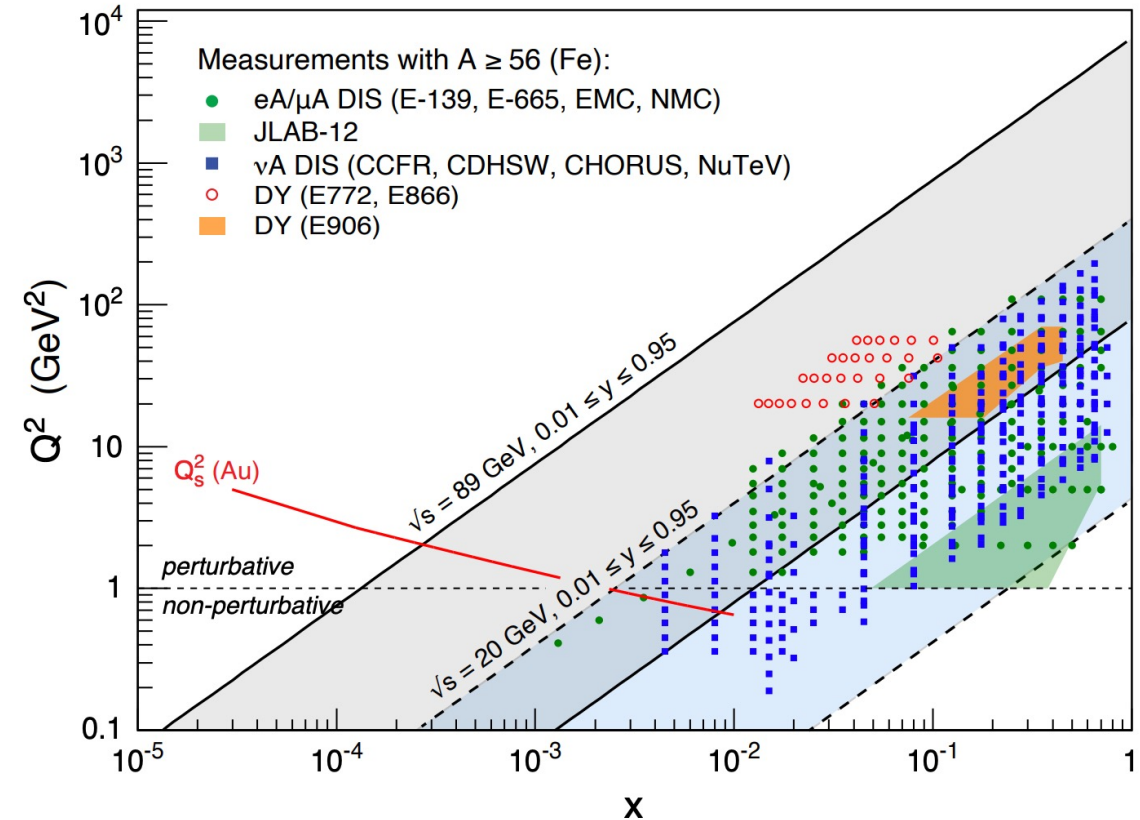
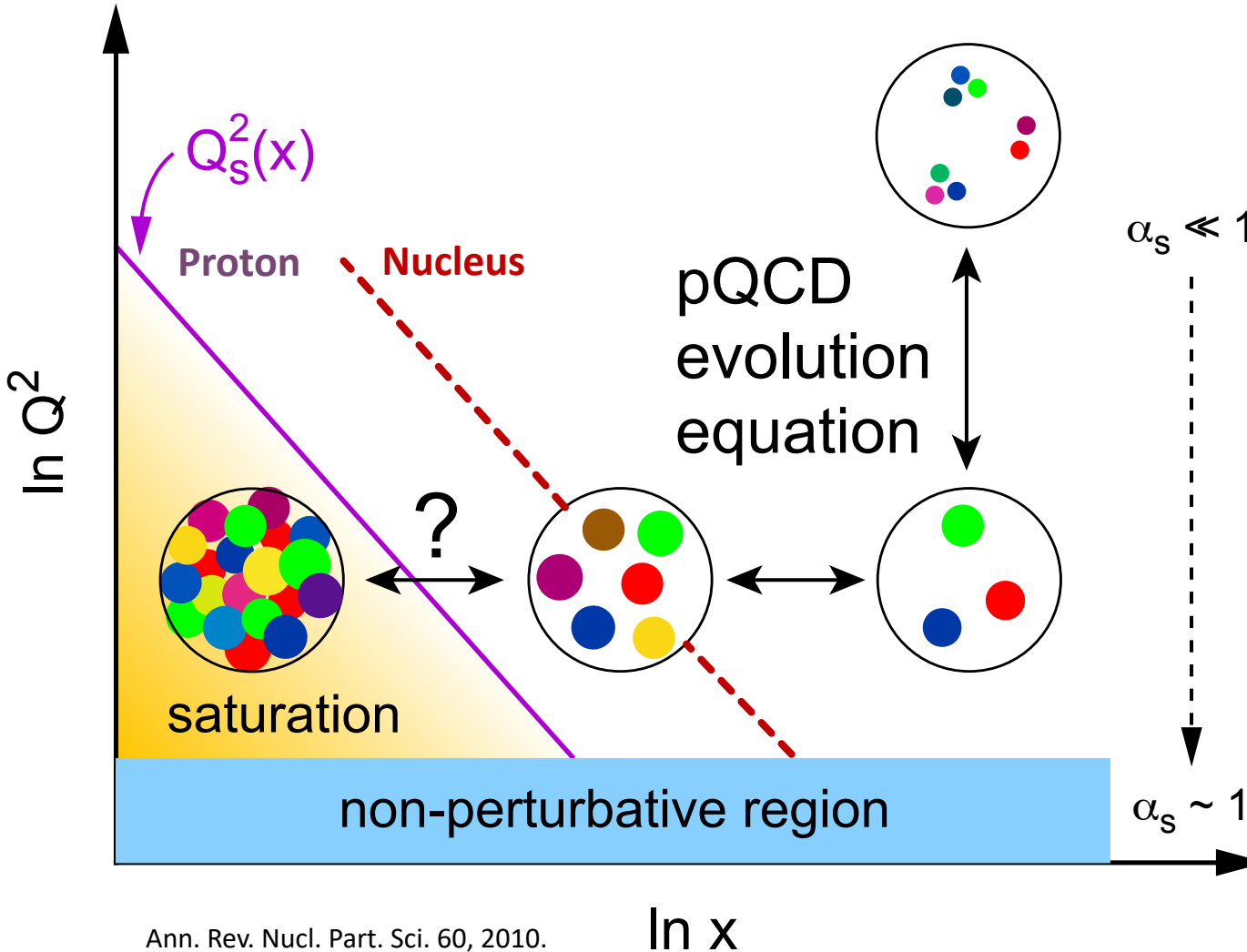
$$\frac{\alpha_s}{Q^2} \cdot xG(x, Q^2) = \pi R^2$$

Size of gluons      Number of gluons

$$Q_s(x, A) = A^{1/3} x^{-\lambda}$$

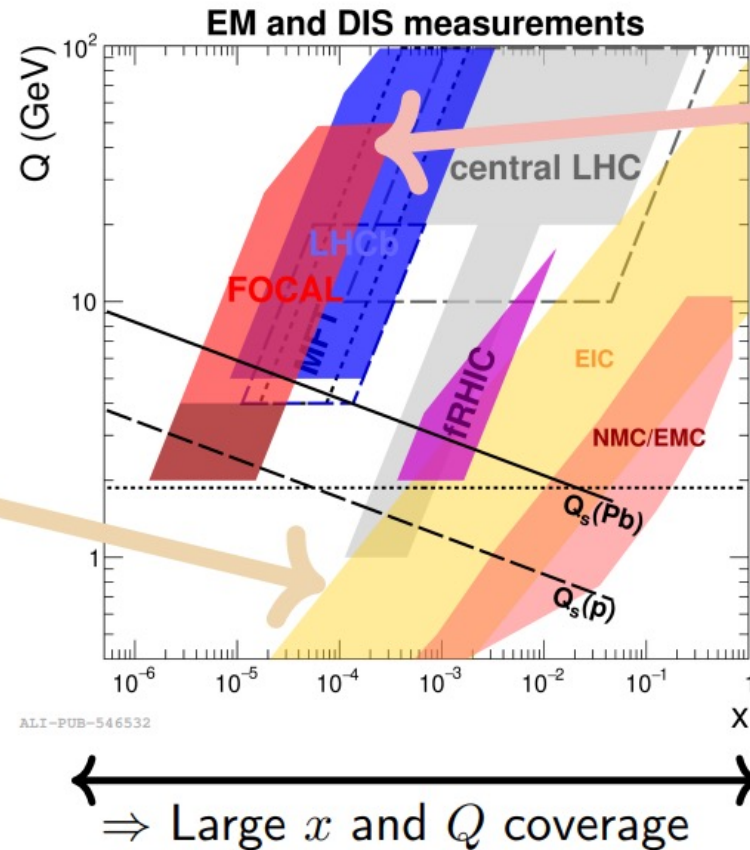
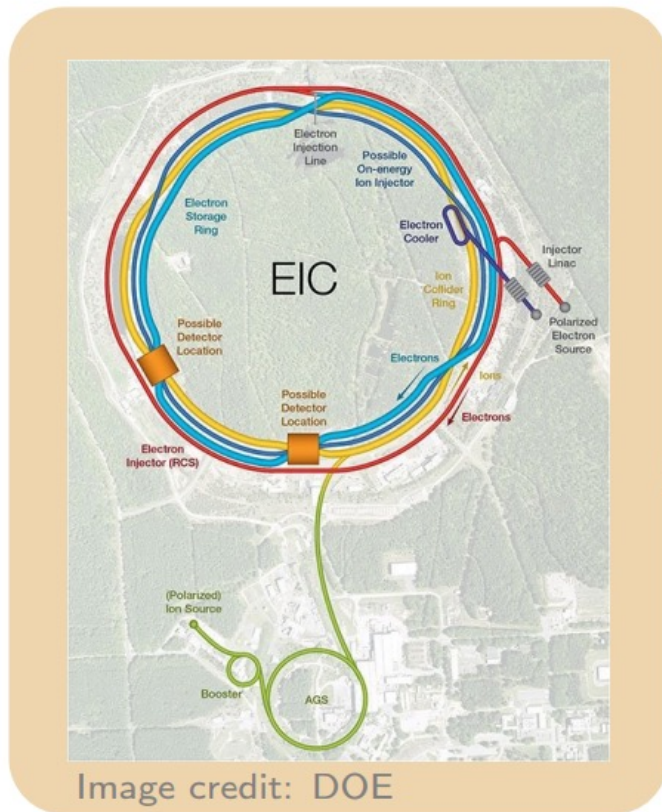


# Phase diagram of proton and nucleus

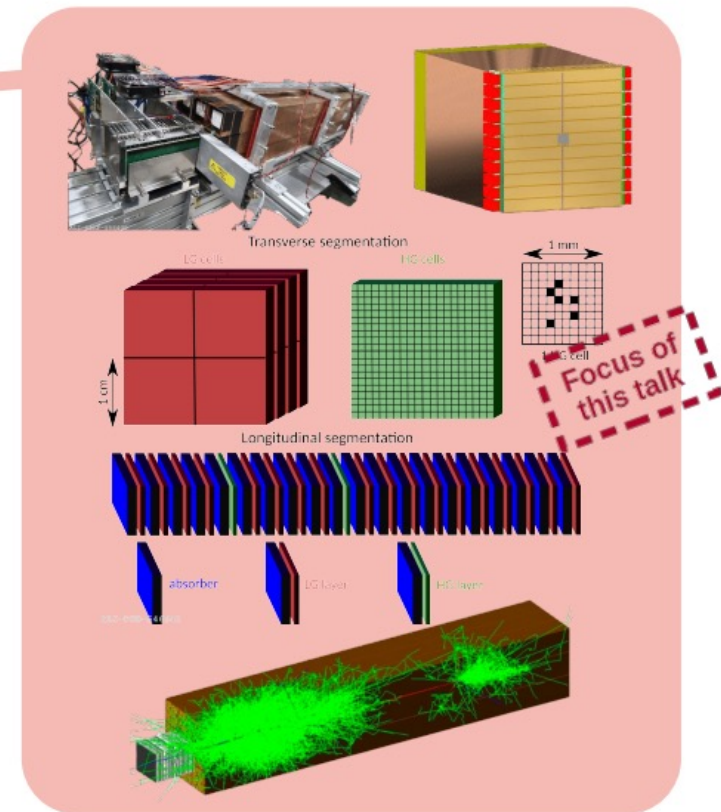


# Phase diagram of proton and nucleus

## DIS in e-A collisions: The Electron-Ion Collider

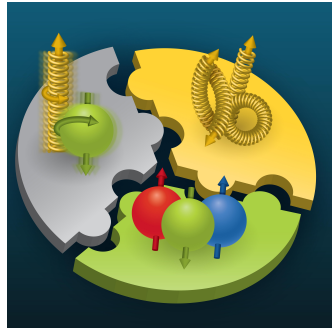


## Forward p+A collisions: The ALICE FoCal



# Main Physics at the EIC

# Science Goal of EIC



SPIN is one of the fundamental properties of matter. All elementary particles, but the Higgs carry spin. Spin cannot be explained by a static picture of the proton. It is the interplay between the intrinsic properties and interactions of quarks and gluons

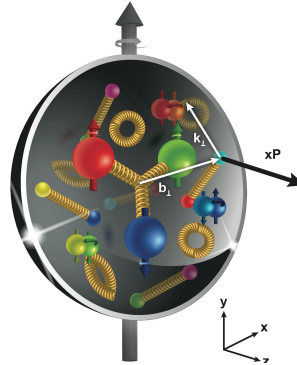
The EIC will unravel the different contribution from the quarks, gluons and orbital angular momentum.



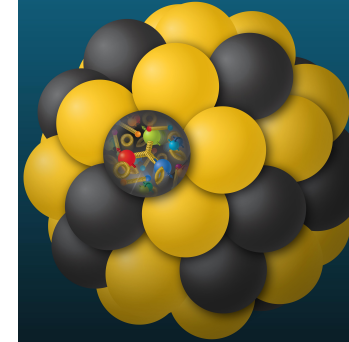
Does the mass of visible matter emerge from quark-gluon interactions?

Atom: Binding/Mass = 0.00000001  
 Nucleus: Binding/Mass = 0.01  
 Proton: Binding/Mass = 100

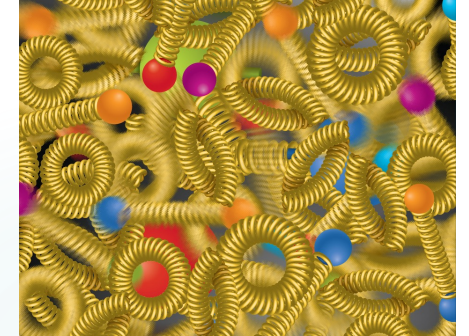
For the proton the EIC will determine an important term contributing to the proton mass, the so-called "QCD trace anomaly"



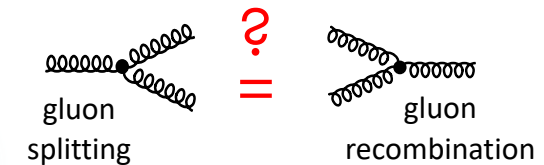
How are the quarks and gluon distributed in space and momentum inside the nucleon & nuclei?  
 How do the nucleon properties emerge from them and their interactions?  
 How can we understand their dynamical origin in QCD?  
 What is the relation to Confinement?



Is the structure of a free and bound nucleon the same?  
 How do quarks and gluons, interact with a nuclear medium?  
 How do the confined hadronic states emerge from these quarks and gluons?  
 How do the quark-gluon interactions create nuclear binding?

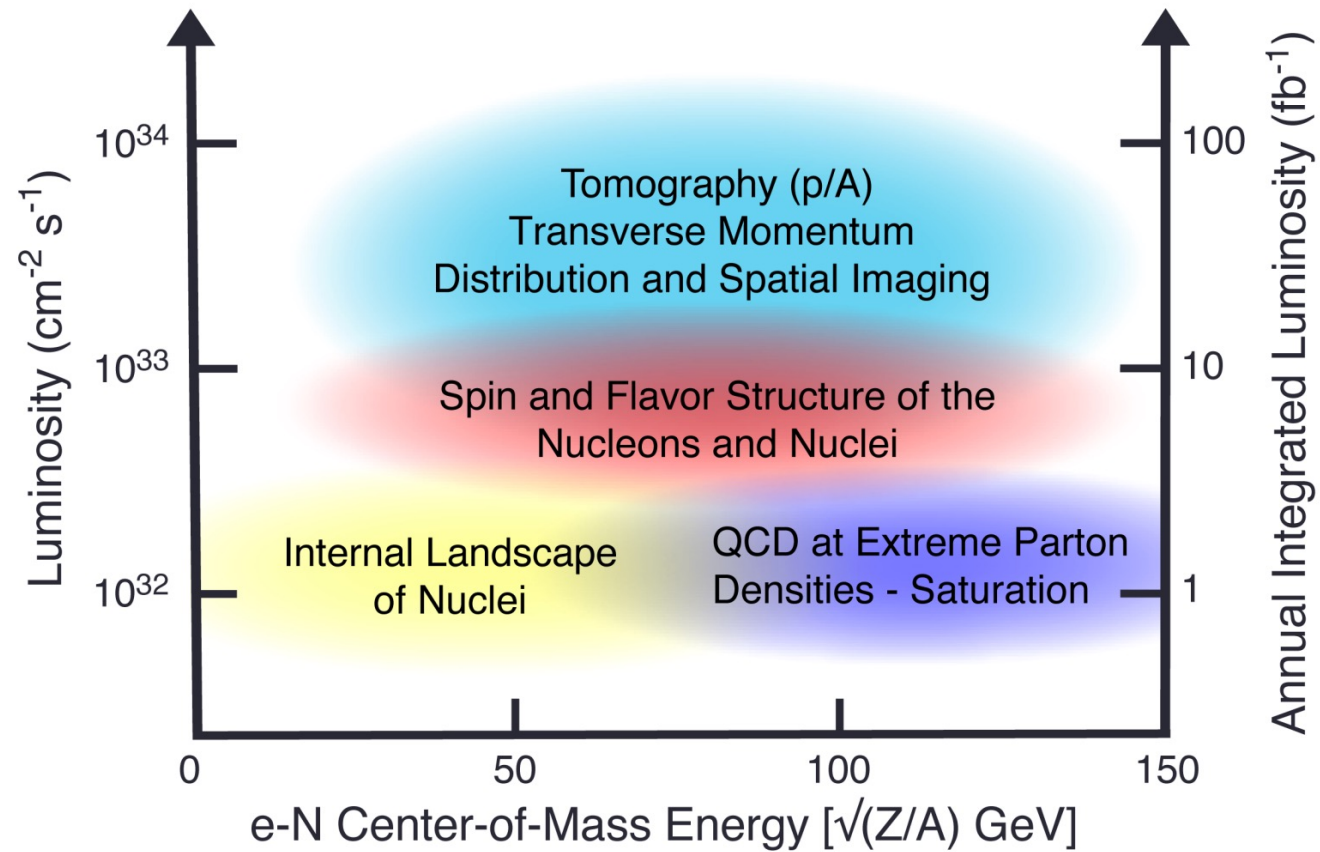
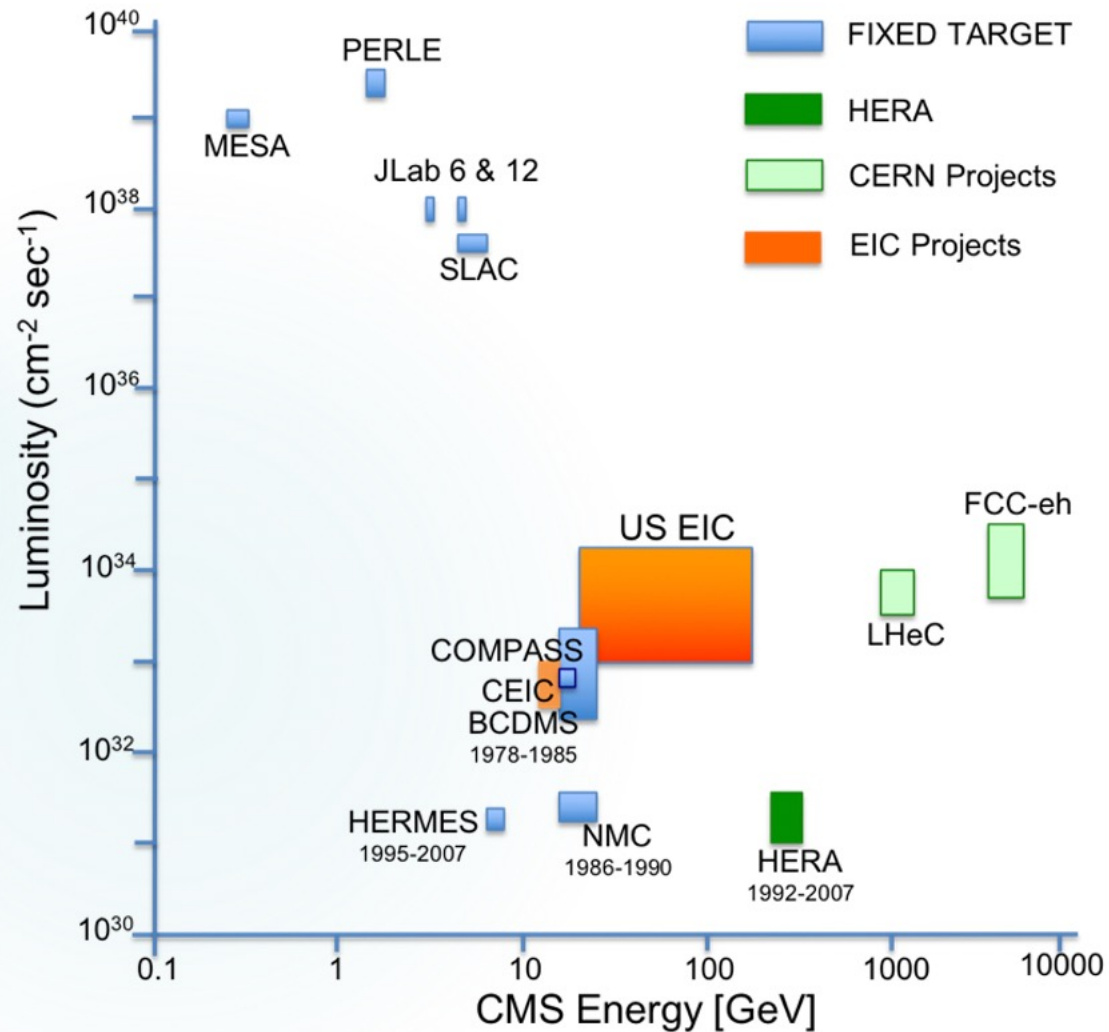


How many gluons can fit in a proton?  
 How does a dense nuclear environment affect the quarks and gluons, their correlations, and their interactions?  
 What happens to the gluon density in nuclei? Does it saturate at high energy?



# Luminosity

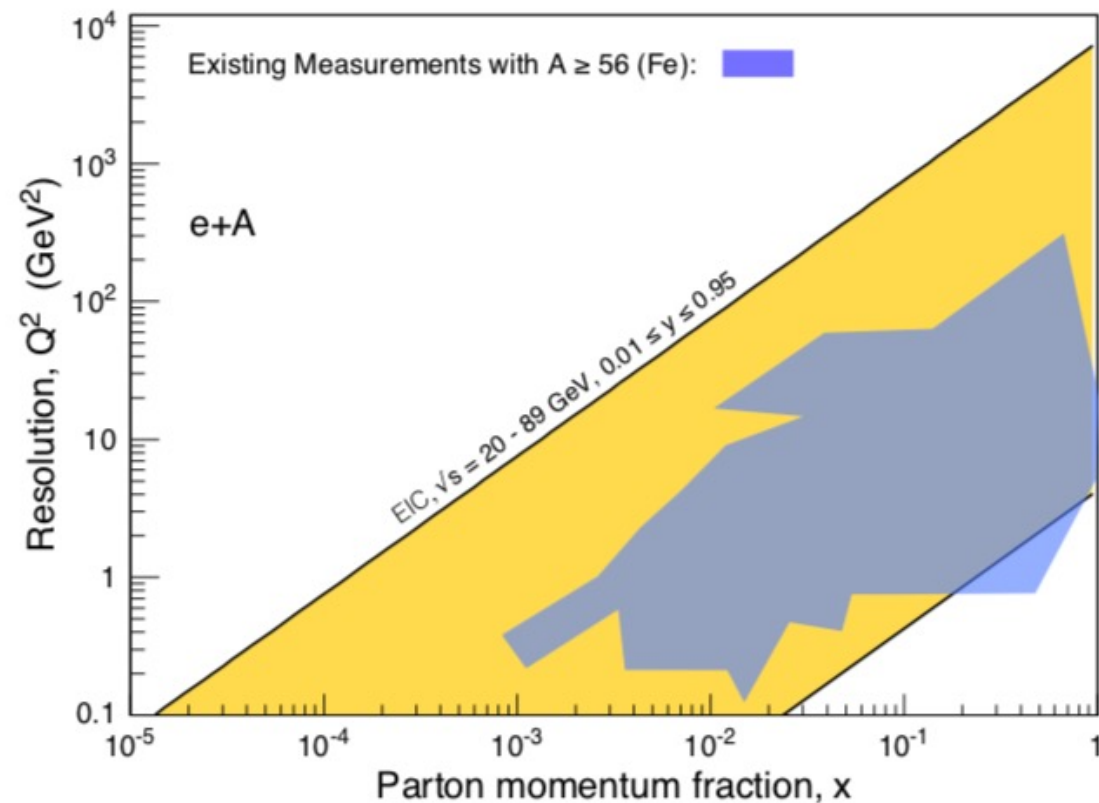
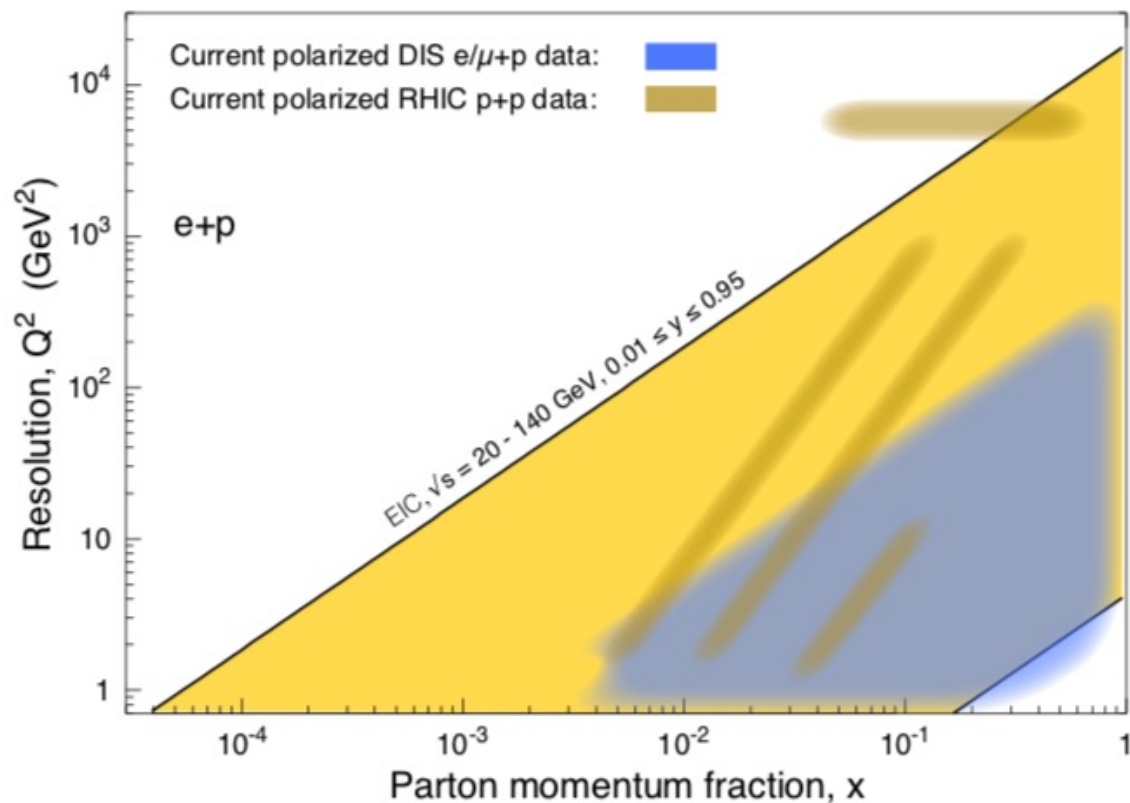
72





# (x, Q<sup>2</sup>) coverage

73



# Further understanding of PDF by EIC

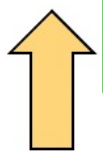
$$W(x, \vec{k}_\perp, \vec{b}_\perp) = \int \frac{d^2 \Delta_\perp}{(2\pi)^2} e^{i\vec{b}_\perp \cdot \vec{\Delta}_\perp} \int \frac{dz^- d^2 z_\perp}{16\pi^3} e^{ixP^+ z^- - i\vec{k}_\perp \cdot \vec{z}_\perp} \langle P - \frac{\Delta}{2} | \bar{q}(-z/2) \gamma^+ q(z/2) | P + \frac{\Delta}{2} \rangle$$

ウィグナー分布関数

5次元

EIC! 21世紀

横運動量 パarton分布  $f(x, \vec{k}_\perp)$       一般化 パarton分布  $f(x, \vec{b}_\perp)$       3次元



$$\int d\vec{k}_\perp$$

$$\int d\vec{b}_\perp$$

$$\int dx$$

20世紀

$$f(x)$$

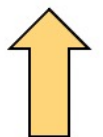
$$F(\vec{b}_\perp)$$

1次元

パarton分布

形状因子

2次元



19世紀

$$\int dx$$

$$Q$$

$$\int d\vec{b}_\perp$$

電荷

0次元

# 3D parton distribution

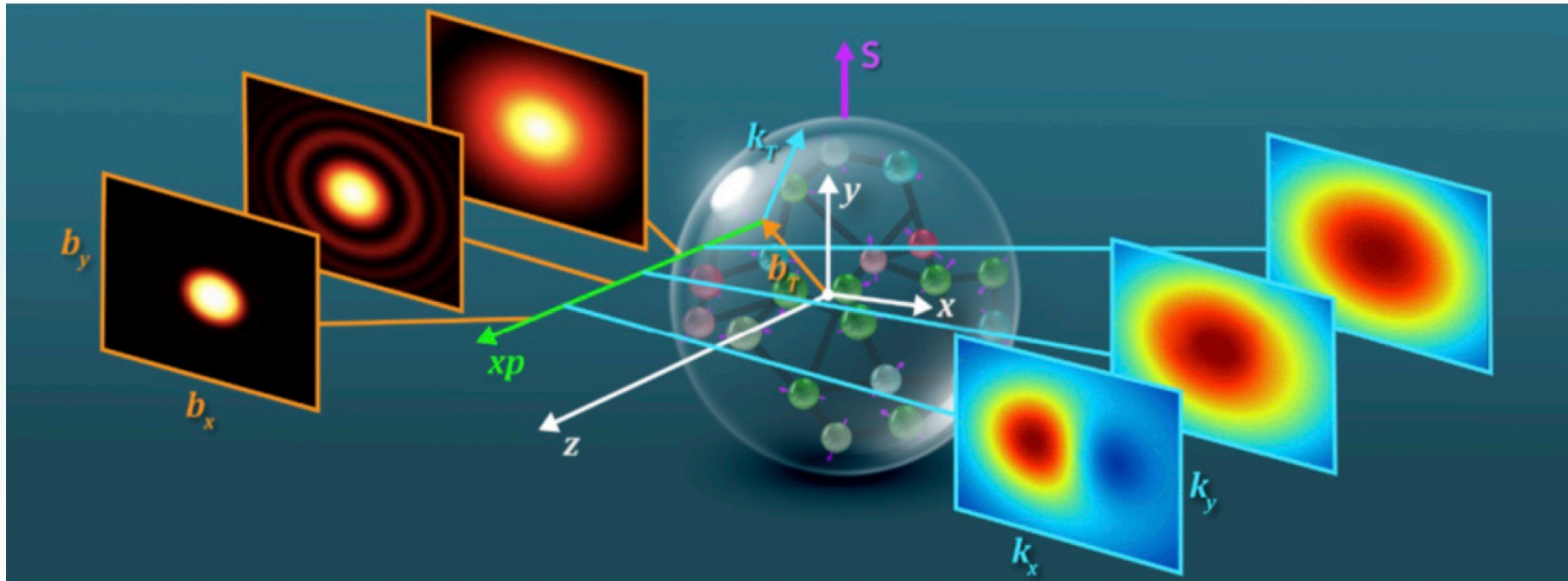
75

## ▶ Generalized Parton Distributions (GPDs)

- ▶ Transverse position & longitudinal momentum fraction of partons

## ▶ Transverse Momentum Dependent Parton Distributions (TMDs)

- ▶ Transverse momentum & longitudinal momentum fraction of partons



# TMD Handbook (>400 pages!)

76

<https://arxiv.org/pdf/2304.03302>



Preprints: JLAB-THY-23-3780, LA-UR-21-20798, MIT-CTP/5386

## TMD Handbook

Renaud Boussarie<sup>1</sup>, Matthias Burkardt<sup>2</sup>, Martha Constantinou<sup>3</sup>, William Detmold<sup>4</sup>, Markus Ebert<sup>4,5</sup>, Michael Engelhardt<sup>6</sup>, Sean Fleming<sup>6</sup>, Leonard Gamberg<sup>7</sup>, Xiangdong Ji<sup>8</sup>, Zhong-Bo Kang<sup>9</sup>, Christopher Lee<sup>10</sup>, Keh-Fei Liu<sup>11</sup>, Simonetta Liuti<sup>12</sup>, Thomas Mehen<sup>13</sup>, Andreas Metz<sup>3</sup>, John Negele<sup>4</sup>, Daniel Pitonyak<sup>14</sup>, Alexei Prokudin<sup>7,16</sup>, Jian-Wei Qiu<sup>16,17</sup>, Abha Rajan<sup>12,18</sup>, Marc Schlegel<sup>2,19</sup>, Phiala Shanahan<sup>4</sup>, Peter Schweitzer<sup>20</sup>, Iain W. Stewart<sup>4</sup>, Andrey Tarasov<sup>21,22</sup>, Raju Venugopalan<sup>18</sup>, Ivan Vitev<sup>10</sup>, Feng Yuan<sup>23</sup>, Yong Zhao<sup>24,4,18</sup>

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### Abstract

This handbook provides a comprehensive review of transverse-momentum-dependent parton distribution functions and fragmentation functions, commonly referred to as transverse momentum distributions (TMDs). TMDs describe the distribution of partons inside the proton and other hadrons with respect to both their longitudinal and transverse momenta. They provide unique insight into the internal momentum and spin structure of hadrons, and are a key ingredient in the description of many collider physics cross sections. Understanding TMDs requires a combination of theoretical techniques from quantum field theory, nonperturbative calculations using lattice QCD, and phenomenological analysis of experimental data. The handbook covers a wide range of topics, from theoretical foundations to experimental analyses, as well as recent developments and future directions. It is intended to provide an essential reference for researchers and graduate students interested in understanding the structure of hadrons and the dynamics of partons in high energy collisions.



## TMD Handbook

A modern introduction to the physics of  
Transverse Momentum Dependent distributions

April 6, 2023

Renaud Boussarie  
Matthias Burkardt  
Martha Constantinou  
William Detmold  
Markus Ebert  
Michael Engelhardt  
Sean Fleming  
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Raju Venugopalan  
Ivan Vitev  
Feng Yuan  
Yong Zhao

\* - Editors



(全く読めていません)  
勉強不足ですみません

arXiv:2304.03302v1 [hep-ph] 6 Apr 2023

# A lot of TMDs ...

Leading Quark TMDPDFs  Nucleon Spin  Quark Spin

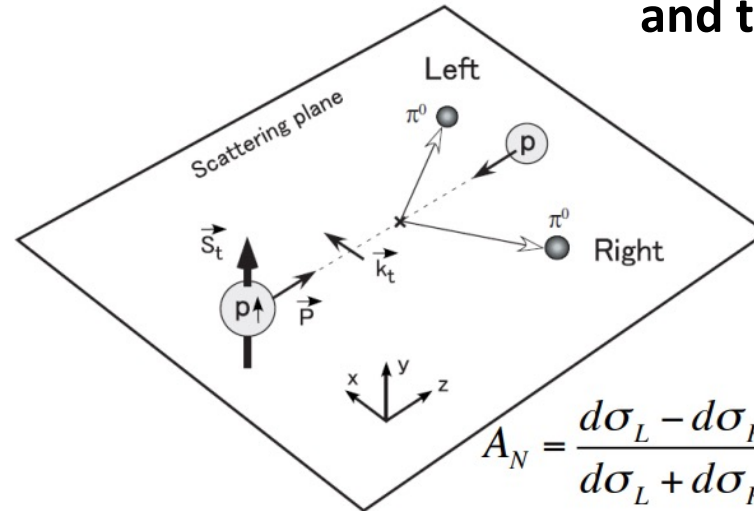
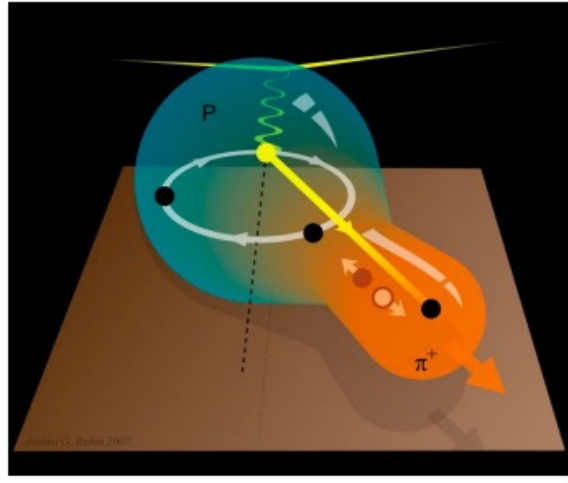
		Quark Polarization		
		Un-Polarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	$f_1 = \text{Unpolarized}$		$h_1^\perp = \text{Boer-Mulders}$
	L		$g_1 = \text{Helicity}$	$h_{1L}^\perp = \text{Worm-gear}$
	T	$f_{1T}^\perp = \text{Sivers}$	$g_{1T}^\perp = \text{Worm-gear}$	$h_{1T} = \text{Transversity}$ $h_{1T}^\perp = \text{Pretzelosity}$

Leading Gluon TMDPDFs  Nucleon Spin  Gluon Operator Helicities

		Gluon Operator Polarization		
		Un-Polarized	Helicity 0 antisymmetric	Helicity 2
Nucleon Polarization	U	$f_1^g = \text{Unpolarized}$		$h_1^{\perp g} = \text{Linearly Polarized}$
	L		$g_{1L}^g = \text{Helicity}$	$h_{1L}^{\perp g} = \text{Helicity 2}$
	T	$f_{1T}^{\perp g} = \text{Sivers}$	$g_{1T}^{\perp g} = \text{Worm-gear}$	$h_{1T}^g = \text{Transversity}$ $h_{1T}^{\perp g} = \text{Pretzelosity}$

# Sivers effect and TSA

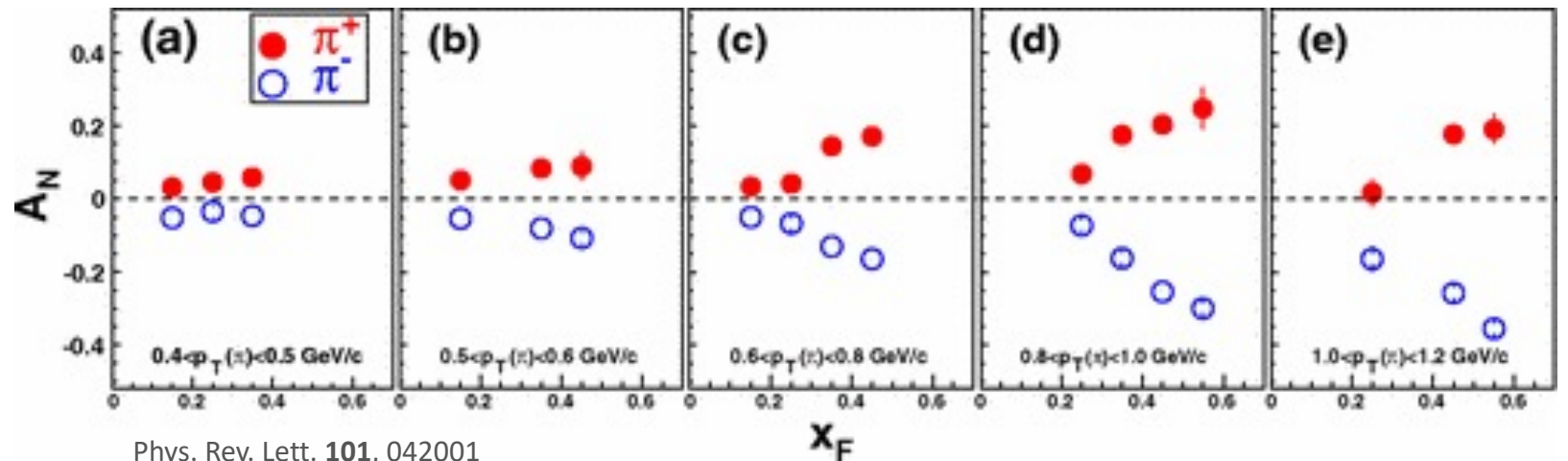
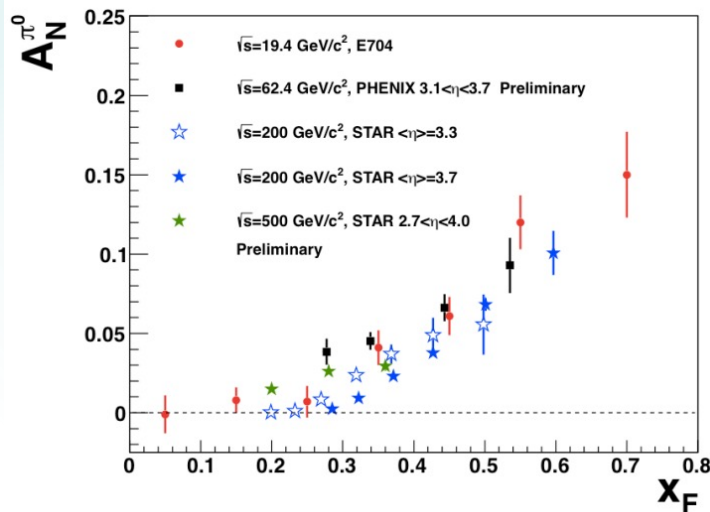
## ► RHIC: Transverse Spin Asymmetry ( $A_N$ )



### Sivers effect

Correlation between nucleon transverse spin and transverse momentum of partons

Non-zero  $A_N$  and charge dependent  
 -> opposite spin- $k_T$  properties of valence u and d quarks

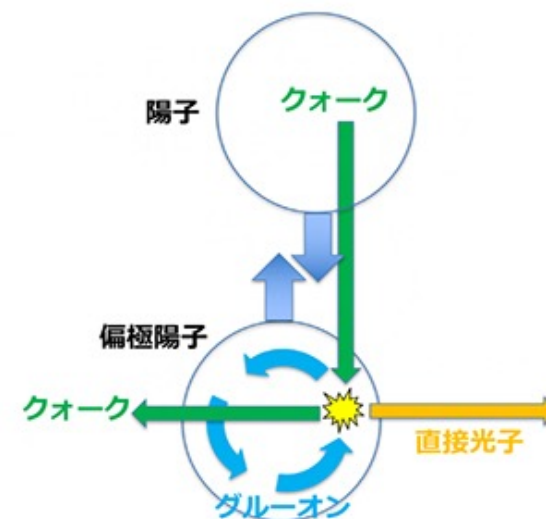
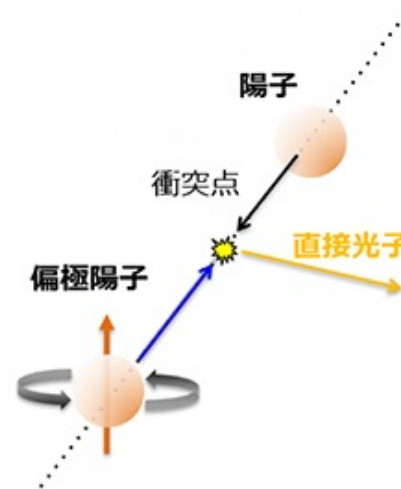
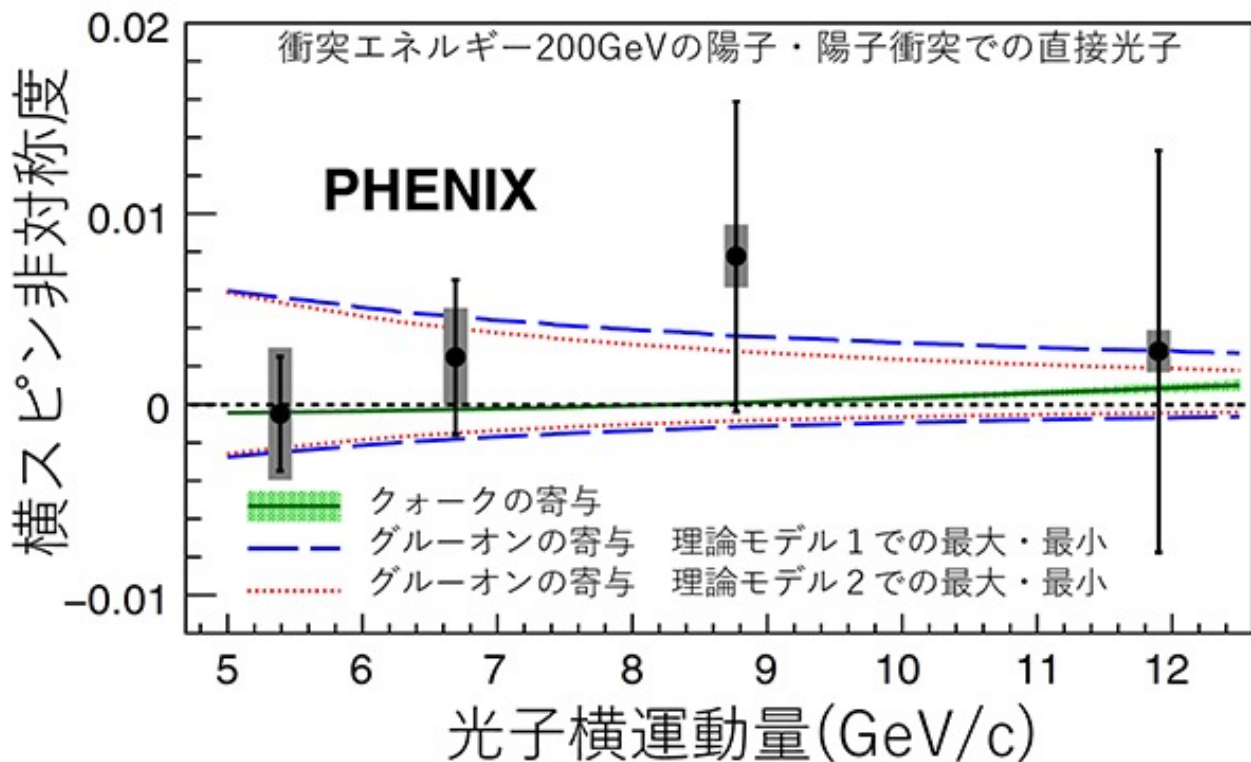
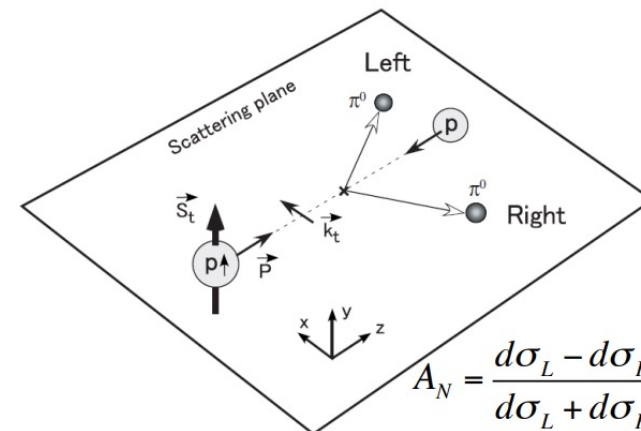


# Sivers effect and TSA

## ► RHIC: Transverse Spin Asymmetry ( $A_N$ )

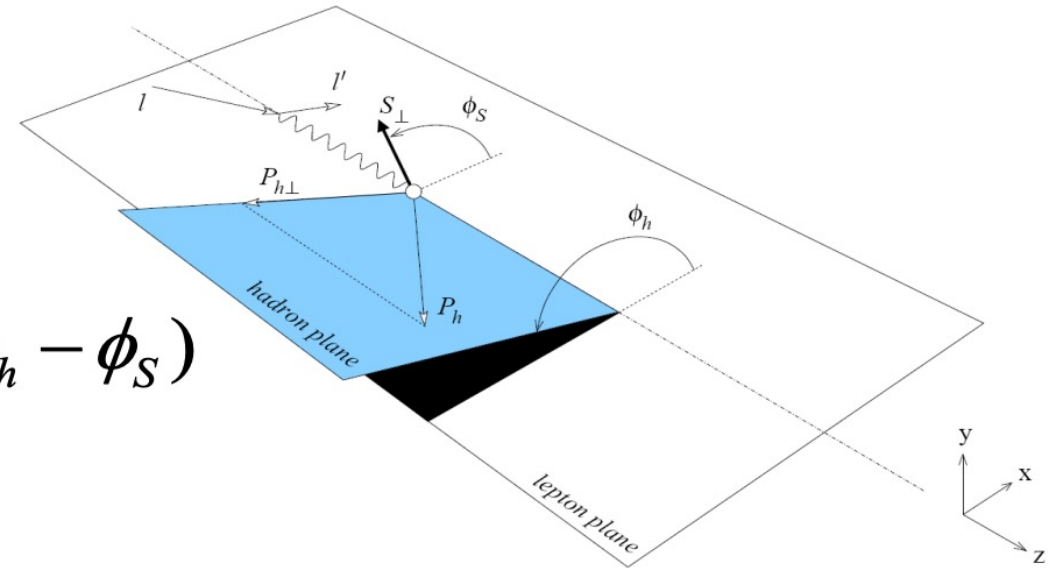
[https://www.riken.jp/press/2021/20211015\\_1/index.html](https://www.riken.jp/press/2021/20211015_1/index.html)

Direct photon  $A_N$  sensitive to gluon angular momentum



# TMD at EIC through SI-DIS

$$\begin{aligned}
 A_{UT}(\varphi_h^l, \varphi_S^l) &= \frac{1}{P} \frac{N^\uparrow - N^\downarrow}{N^\uparrow + N^\downarrow} \\
 &= A_{UT}^{\text{Collins}} \sin(\varphi_h + \varphi_S) + A_{UT}^{\text{Sivers}} \sin(\varphi_h - \varphi_S) \\
 &+ A_{UT}^{\text{Pretzelosity}} \sin(3\varphi_h - \varphi_S)
 \end{aligned}$$



$$A_{UT}^{\text{Collins}} \propto \langle \sin(\varphi_h + \varphi_S) \rangle_{UT} \propto h_1 \otimes H_1^\perp$$

$$A_{UT}^{\text{Sivers}} \propto \langle \sin(\varphi_h - \varphi_S) \rangle_{UT} \propto f_{1T}^\perp \otimes D_1$$

$$A_{UT}^{\text{Pretzelosity}} \propto \langle \sin(3\varphi_h - \varphi_S) \rangle_{UT} \propto h_{1T}^\perp \otimes H_1^\perp$$

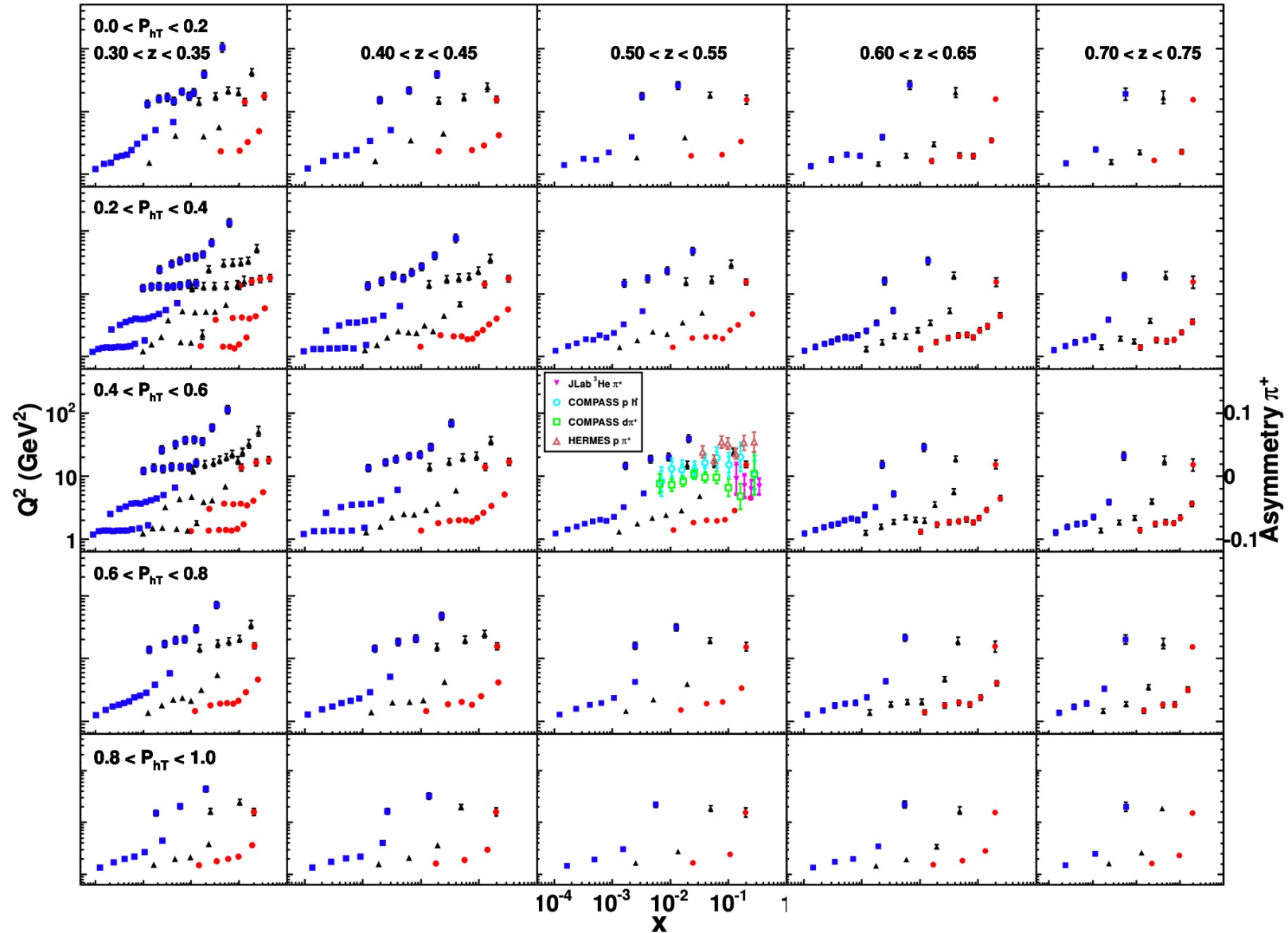


# TMD at EIC through SI-DIS

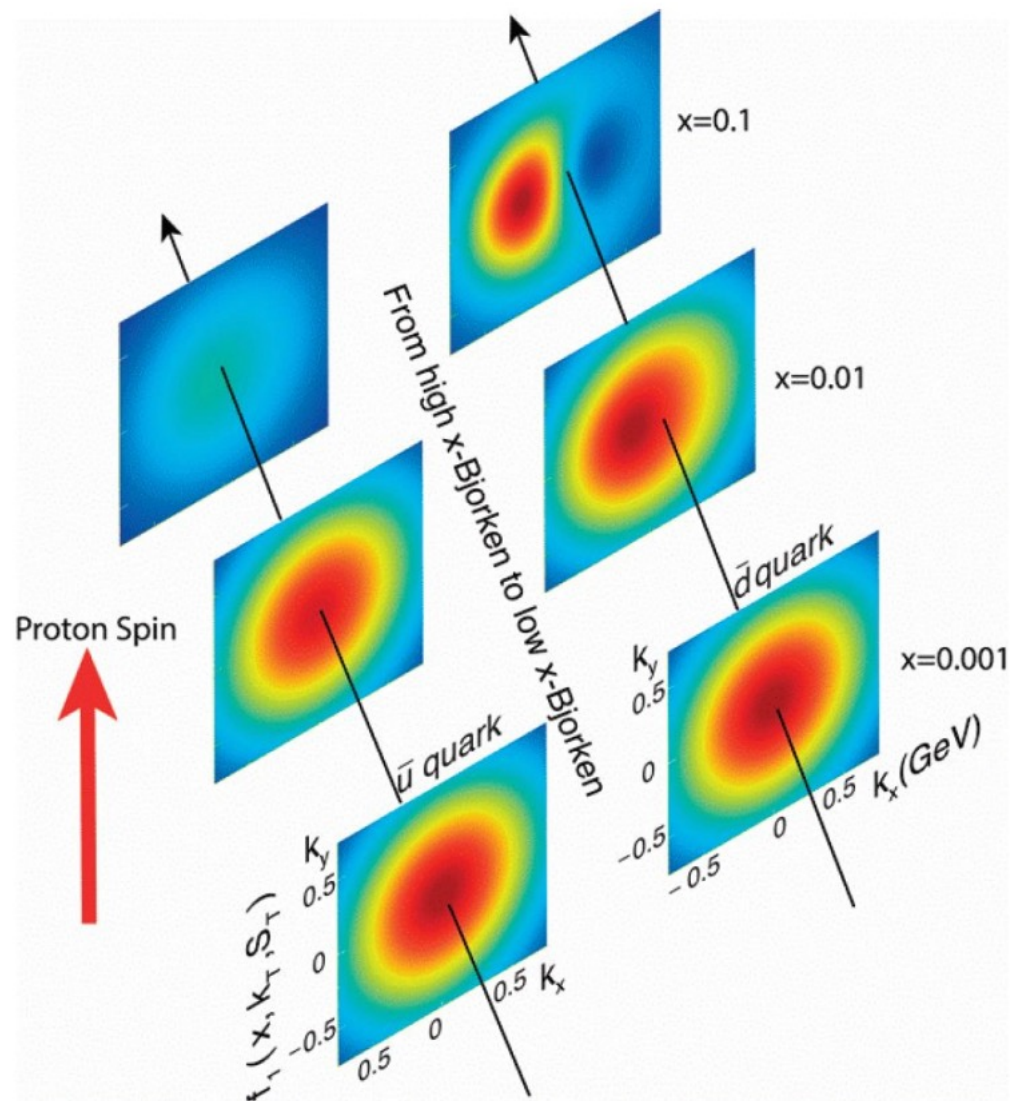
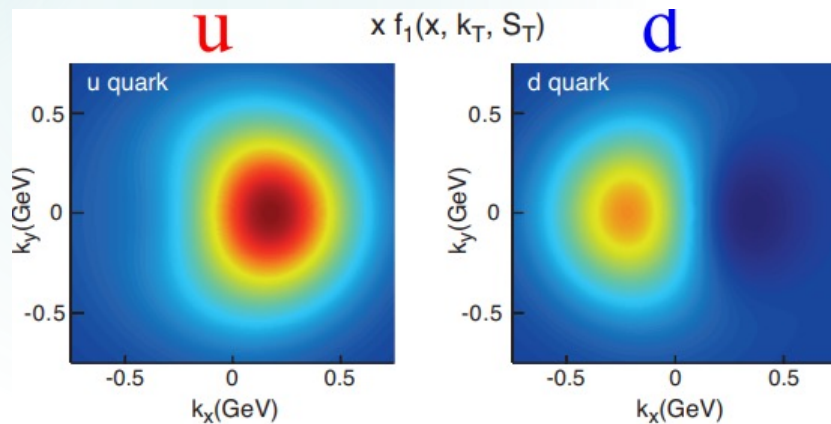
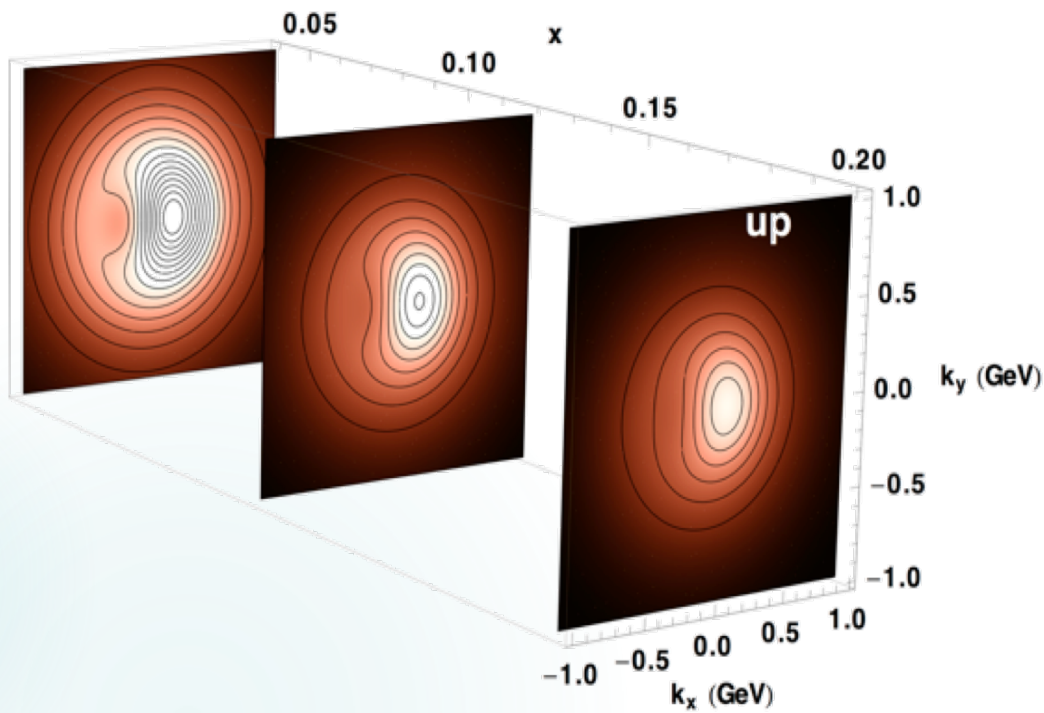
$\sqrt{s} = 140 \text{ GeV}$

$\sqrt{s} = 45 \text{ GeV}$

$\sqrt{s} = 15 \text{ GeV}$



# Momentum imaging



# Generalized Parton Distributions

83

About 200 pages...



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PHYSICS REPORTS

Physics Reports 388 (2003) 41–277

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## Generalized parton distributions

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Accepted 6 August 2003  
editor: W. Weise

### Abstract

We give an overview of the theory for generalized parton distributions. Topics covered are their general properties and physical interpretation, the possibility to explore the three-dimensional structure of hadrons at parton level, their potential to unravel the spin structure of the nucleon, their role in small- $x$  physics, and efforts to model their dynamics. We review our understanding of the reactions where generalized parton distributions occur, to leading power accuracy and beyond, and present strategies for phenomenological analysis. We emphasize the close connection between generalized parton distributions and generalized distribution amplitudes, whose properties and physics we also present. We finally discuss the use of these quantities for describing soft contributions to exclusive processes at large energy and momentum transfer.

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PACS: 13.60.-r; 13.88.+e; 14.20.Dh

Keywords: Nucleon structure; Parton distributions; Hard exclusive processes

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3.3.2. Symmetry properties	55
3.3.3. Sum rules and polynomiality	57
3.4. Parton interpretation and the light-cone	60
3.5. Helicity structure	64

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PHYSICS REPORTS

Physics Reports 418 (2005) 1–387

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## Unraveling hadron structure with generalized parton distributions

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Accepted 8 June 2005

editor: W. Weise

Dedicated to Anatoly V. Efremov on occasion of his 70th anniversary

### Abstract

The generalized parton distributions, introduced nearly a decade ago, have emerged as a universal tool to describe hadrons in terms of quark and gluonic degrees of freedom. They combine the features of form factors, parton densities and distribution amplitudes—the functions used for a long time in studies of hadronic structure. Generalized parton distributions are analogous to the phase-space Wigner quasi-probability function of nonrelativistic quantum mechanics which encodes full information on a quantum-mechanical system. We give an extensive review of main achievements in the development of this formalism. We discuss physical interpretation and basic properties of generalized parton distributions, their modeling and QCD evolution in the leading and next-to-leading orders. We describe how these functions enter a wide class of exclusive reactions, such as electro- and photo-production of photons, lepton pairs, or mesons. The theory of these processes requires and implies full control over diverse corrections and thus we outline the progress in handling higher-order and higher-twist effects. We catalogue corresponding results and present diverse techniques for their derivations. Subsequently, we address observables that are sensitive to different characteristics of the nucleon structure in terms of generalized parton distributions. The ultimate goal of the GPD approach is to provide a three-dimensional spatial picture of the nucleon, direct measurement of the quark orbital angular momentum, and various inter- and multi-parton correlations.

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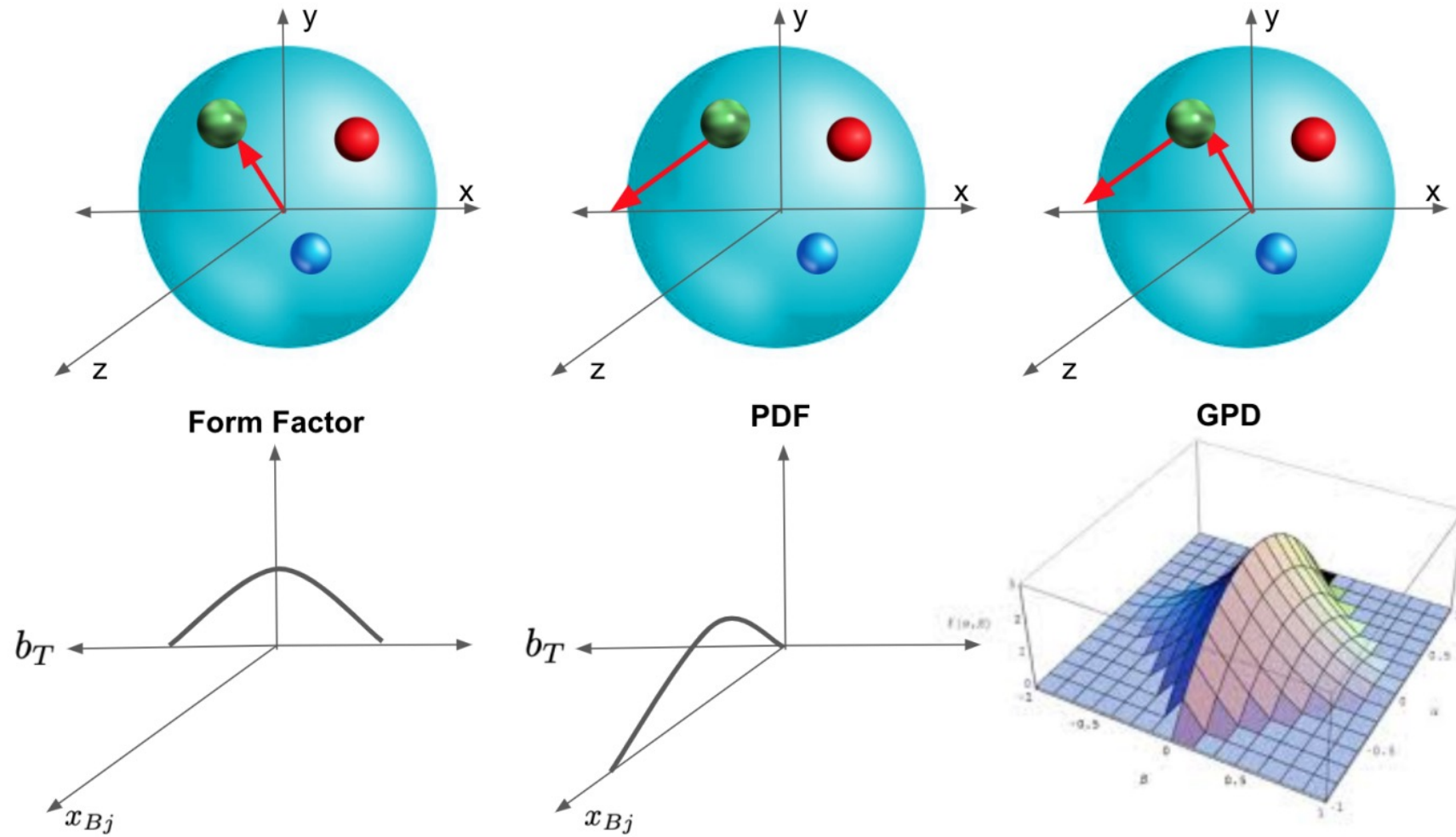
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doi:10.1016/j.physrep.2005.06.002



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# Generalized Parton Distributions

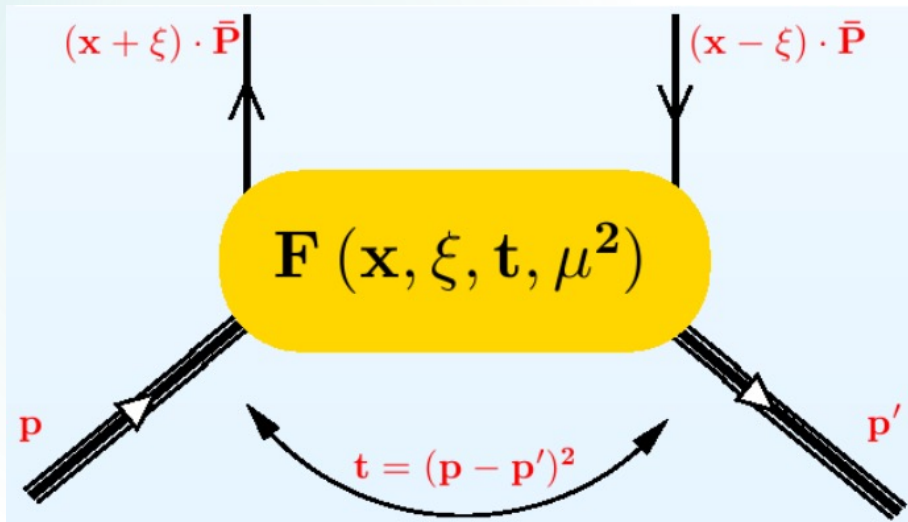


# Generalized Parton Distributions

The nucleon (spin-1/2) has four quark and gluon GPDs. Like usual PDFs, GPDs are non-perturbative functions defined via the **off-forward matrix elements** of well-defined parton operators:

異なる運動量を持つ初期状態と終状態の核子間のクォーク演算子の行列要素

$$\begin{aligned}
 F^q &= \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ix\bar{P}^+z^-} \langle p' | \bar{q}(-\frac{1}{2}z) \gamma^+ q(\frac{1}{2}z) | p \rangle |_{z^+=0, \mathbf{z}=0} \\
 &= \frac{1}{2\bar{P}^+} \left[ H^q(x, \xi, t, \mu^2) \bar{u}(p') \gamma^+ u(p) + E^q(x, \xi, t, \mu^2) \bar{u}(p') \frac{i\sigma^{+\alpha} \Delta_\alpha}{2m_N} u(p) \right]
 \end{aligned}$$



$$\Delta = p' - p$$

$$t = (p' - p)^2$$

$$\bar{P}^+ = (p' + p)/2$$

$$x \pm \xi$$

$$\mu^2$$

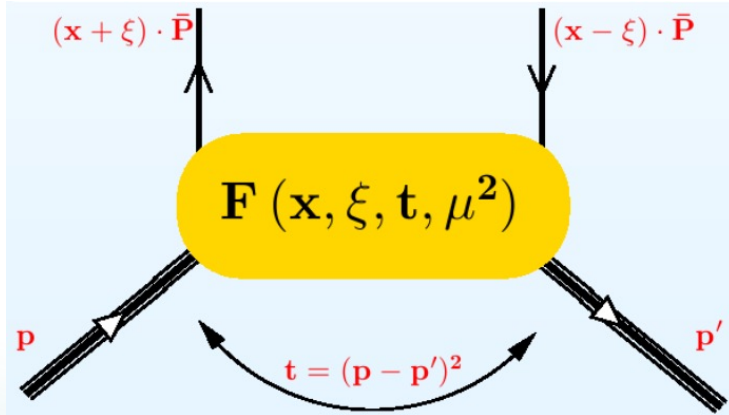
$$\xi = x_B / (2 - x_B)$$

-- long. mom. fractions

-- factorization scale

-- fixed

# Basic Properties of GPD

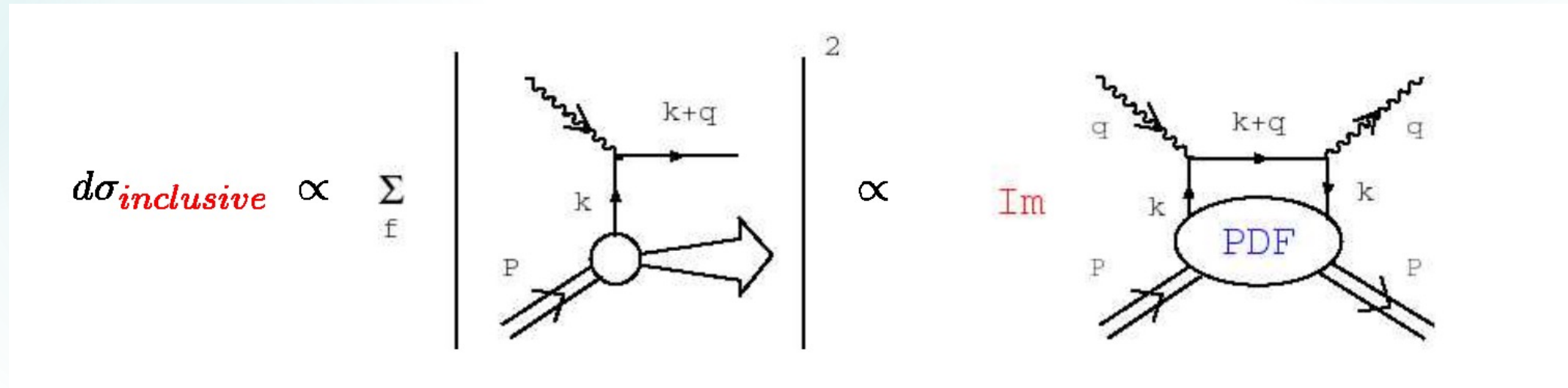


Forward Limit

$\xi \rightarrow 0, t \rightarrow 0$ : 1D parton distribution (PDFs)

$H^q(x, 0, 0) = q(x)$  Unpolarized

$\tilde{H}^q(x, 0, 0) = \Delta q(x)$  Polarized

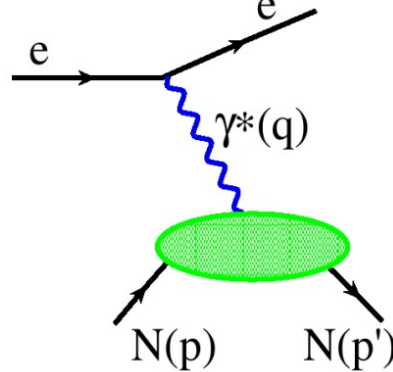


# Basic Properties of GPD

Connection to elastic Form Factors  
(charge radius and magnetic radius)

$$\int_0^1 dx H^q(x, \xi, t, \mu^2) = F_1^q(t)$$

$$\int_0^1 dx E^q(x, \xi, t, \mu^2) = F_2^q(t)$$



$$\langle N(p') | J^\mu(0) | N(p) \rangle = \bar{u}(p') \left[ F_1(q^2) \gamma^\mu + F_2(q^2) \frac{i\sigma^{\mu\nu} q_\nu}{2m_N} \right] u(p)$$

Dirac form factor

Pauli form factor

$$F_1^p(0) = 1$$

$$F_1^n(0) = 0$$

$$F_2^p(0) = \kappa^p = 1.79$$

$$F_2^n(0) = \kappa^n = -1.91$$

$$G_E(q^2) = F_1(q^2) + \frac{q^2}{4m_N^2} F_2(q^2)$$

$$G_M(q^2) = F_1(q^2) + F_2(q^2)$$

$$\int_{-1}^1 dx x H(x, \xi, t) = \boxed{M_2^Q(t)} + \frac{4}{5} \boxed{d^Q(t)} \xi^2$$

Mass                      Pressure

Connection to spin, mass, pressure

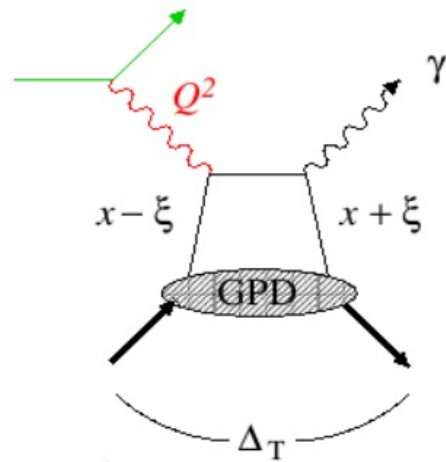
$$\frac{1}{2} \int_0^1 dx x [H^q(x, \xi, t=0, \mu^2) + E^q(x, \xi, t=0, \mu^2)] = J^q(\mu^2)$$

$$\frac{1}{2} \int_0^1 dx x [H^g(x, \xi, t=0, \mu^2) + E^g(x, \xi, t=0, \mu^2)] = J^g(\mu^2)$$

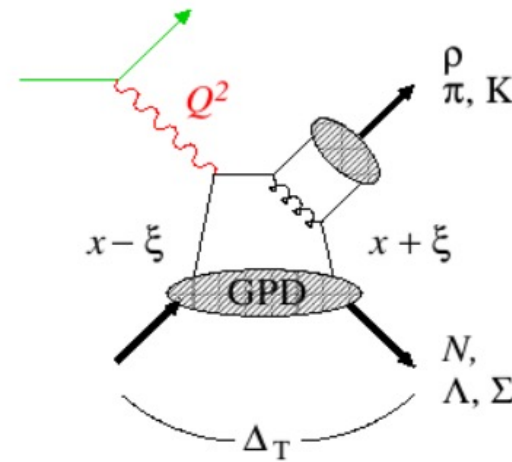
$$\sum_q J^q + J^g = \frac{1}{2} \quad \begin{array}{l} J^q = S^q + L^q \\ J^g = \Delta G + L^g \end{array}$$

# Measurement of GPD

► Deeply Virtual Compton Scattering and Deeply Virtual Meson Production



Deeply virtual Compton scattering



(e) Deeply virtual meson production

$$\mathcal{A}_{DVCS}(\xi, t, Q^2) \propto \sum_q e_q^2 \int_0^1 dx \frac{2x}{x^2 - \xi^2} H^q(x, \xi, t, Q^2) + \text{other GPDs}$$

Perturbative

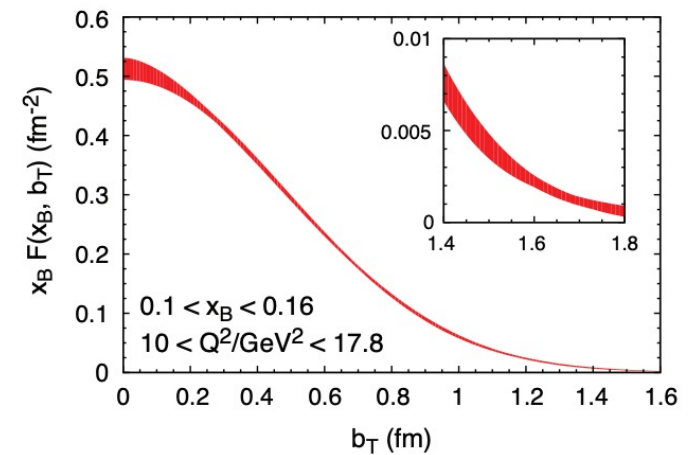
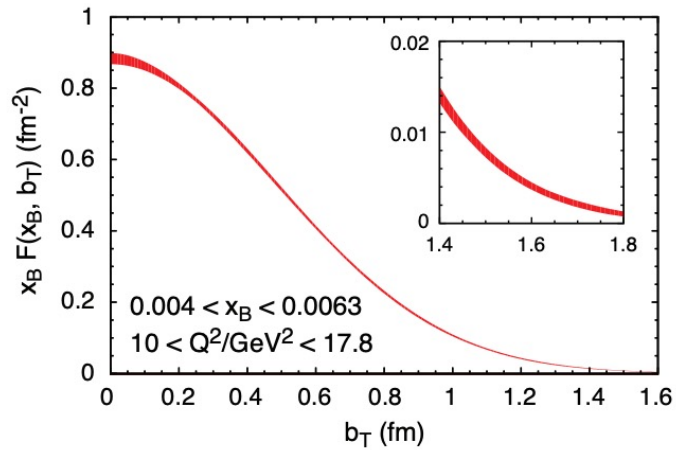
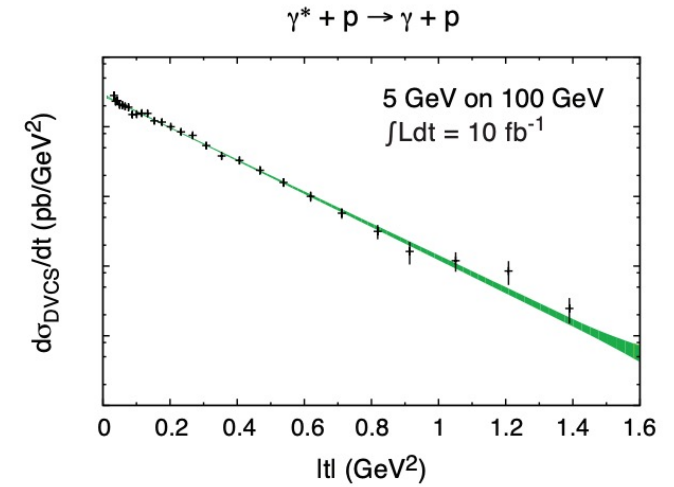
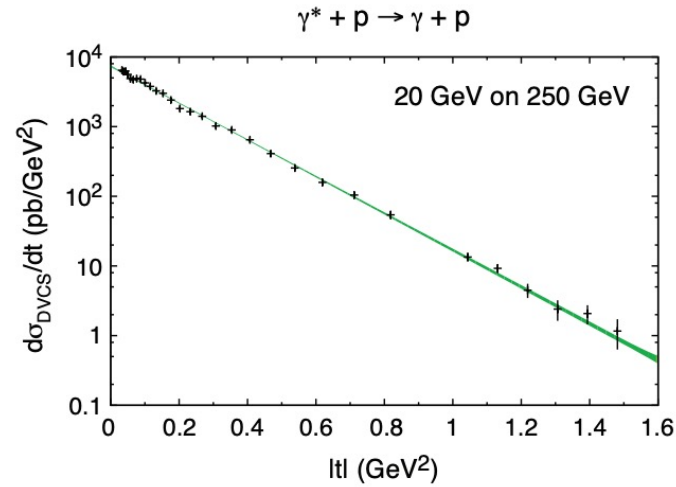
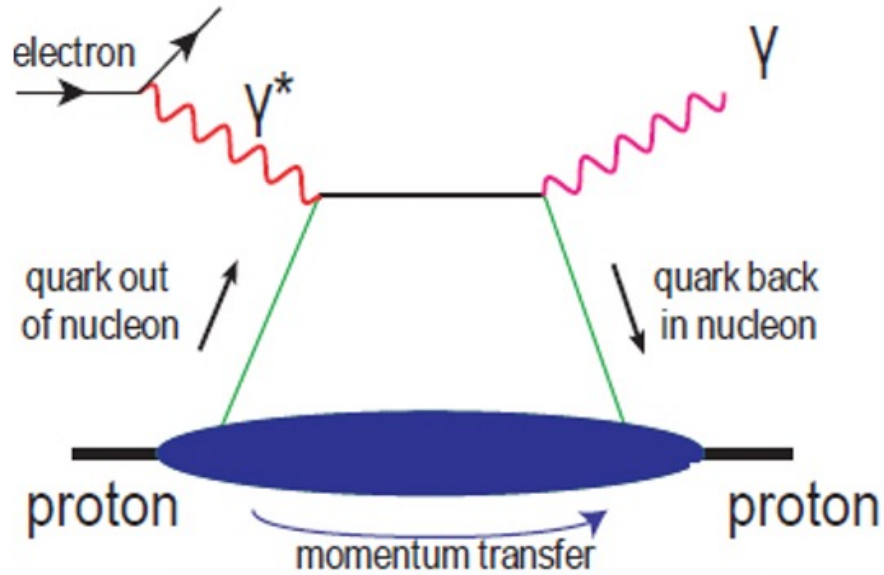
GPDs



# 3D tomography of nucleons (GPD)

## ▶ Deeply Virtual Compton Scattering

Fourier transform of momentum transferred= $(p-p')$   $\rightarrow$  Spatial distribution

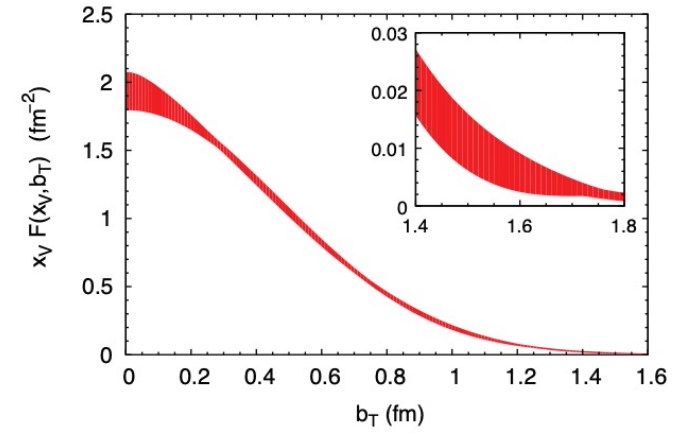
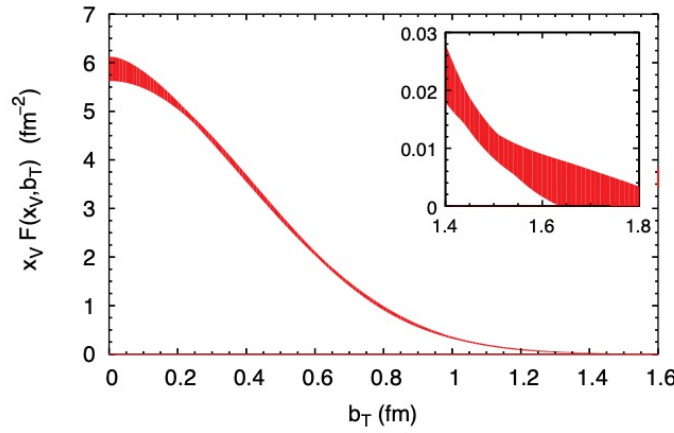
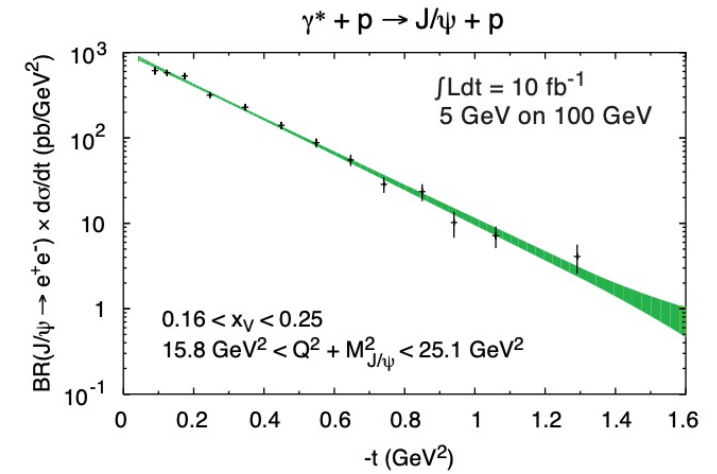
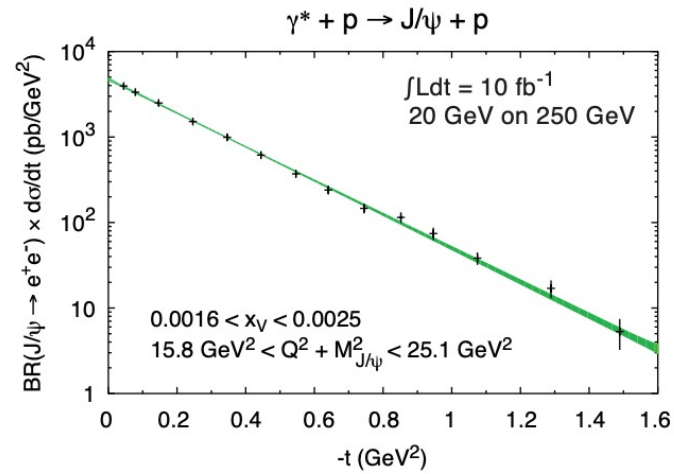
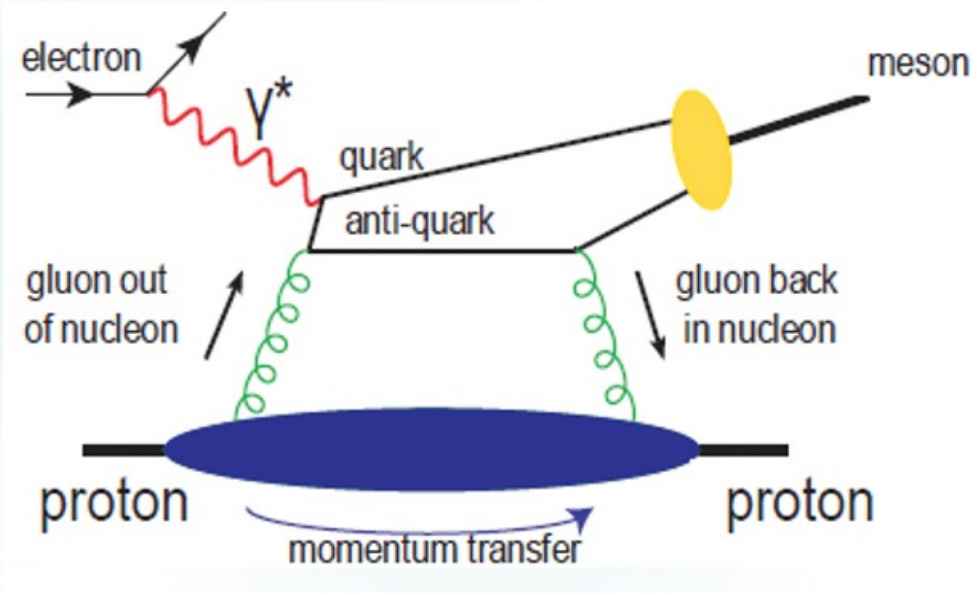


Proton radius of quarks (x)!

# 3D tomography of nucleons (GPD)

## Deeply Virtual Compton Scattering

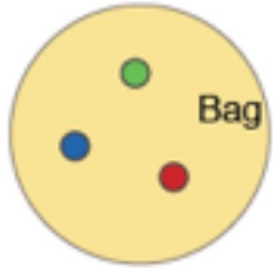
Fourier transform of momentum transferred  $= (p-p') \rightarrow$  Spatial distribution



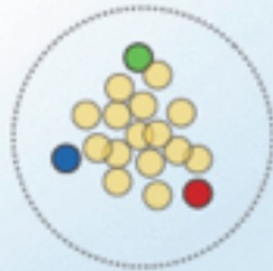
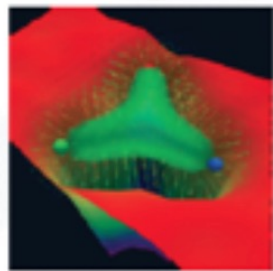
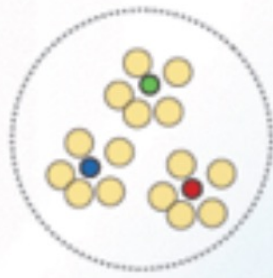
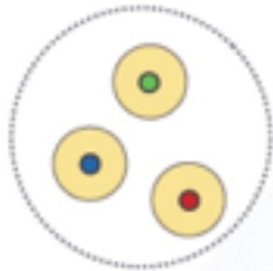
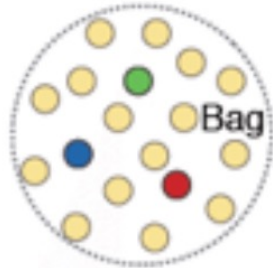
Proton radius of gluons (x)!

# 3D tomography of nucleons (GPD)

Static



Boosted



Bag Model:

- Gluon field distribution is wider than the fast moving quarks.
- **Gluon radius > Charge Radius**

Constituent Quark Model:

- Gluons and sea quarks hide inside massive quarks.
- **Gluon radius ~ Charge Radius**

Lattice Gauge theory (with slow moving quarks),

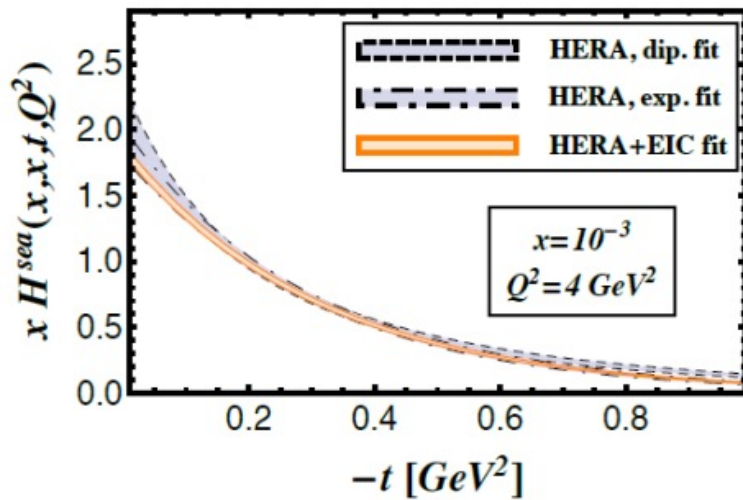
- gluons more concentrated inside the quarks:
- **Gluon radius < Charge Radius**

**Need transverse images of the quarks and gluons in protons**

# GPD at EIC

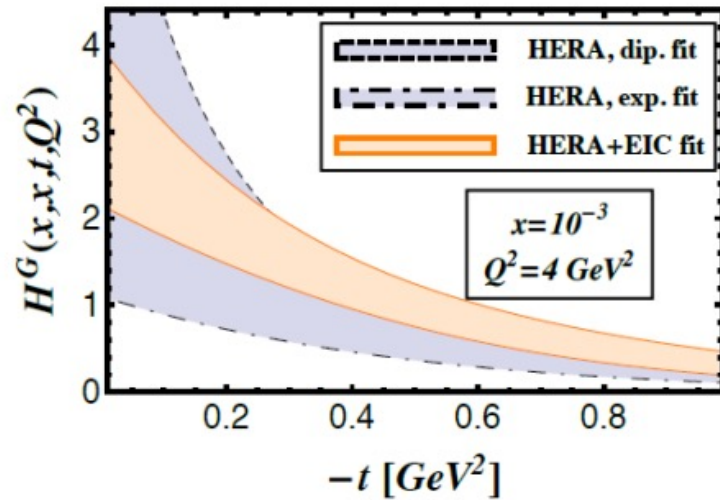
- DVCS in wider phase space  $\Rightarrow$  valence and sea quarks
- DVMP of heavy meson ( $J/\psi, Y$ ), light vector and pseudoscalar meson  $\Rightarrow$  gluon @ low  $x$ , flavor separation

sea quark H



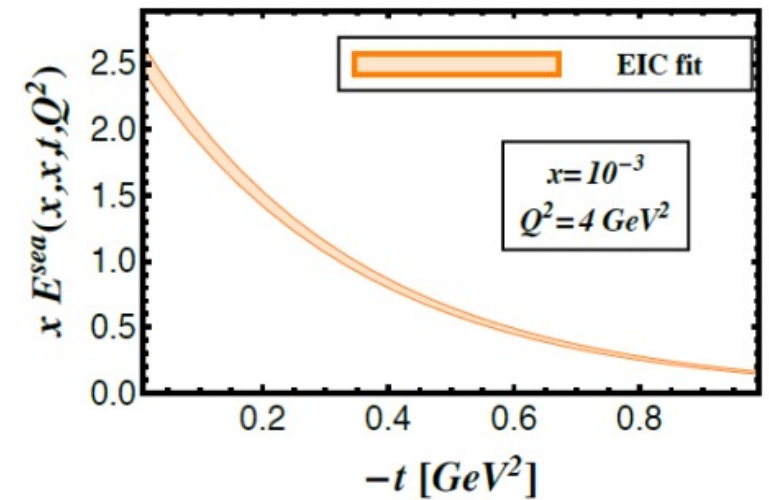
current data

gluon



EIC pseudodata

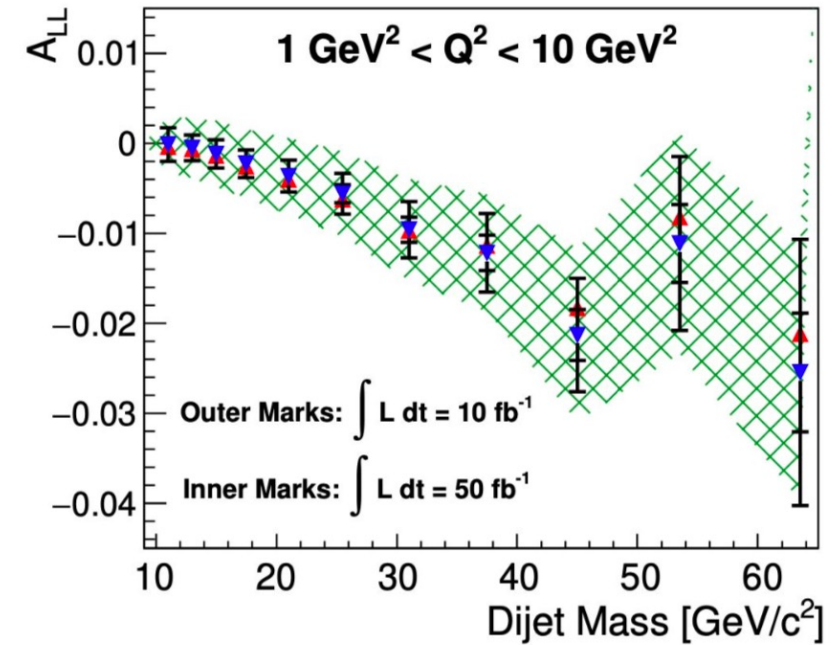
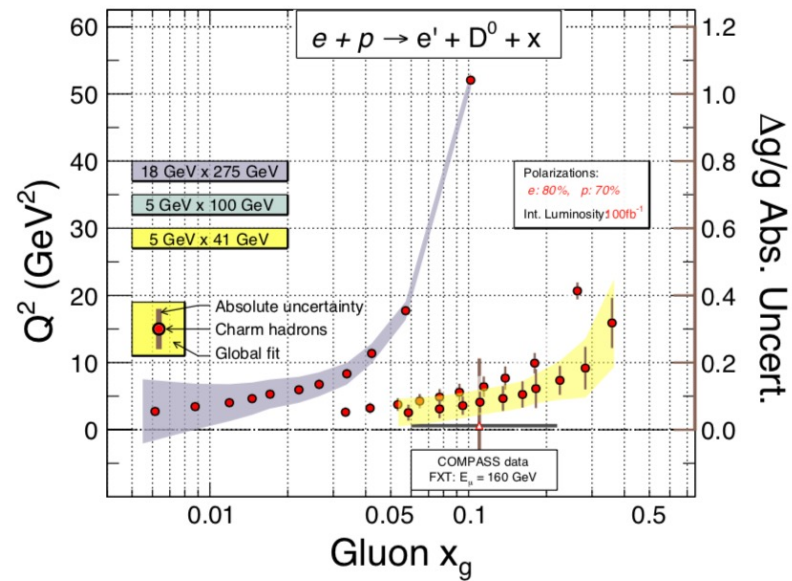
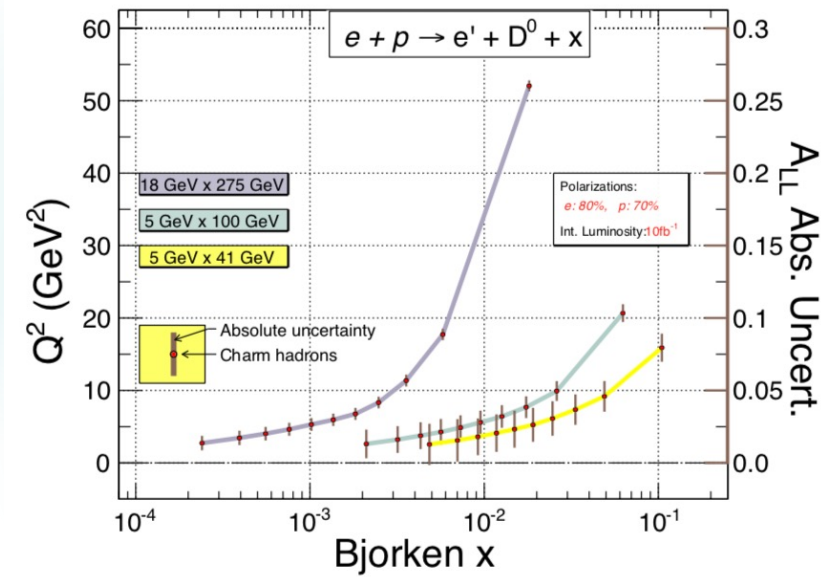
sea quark E



EIC Yellow Paper(2021)

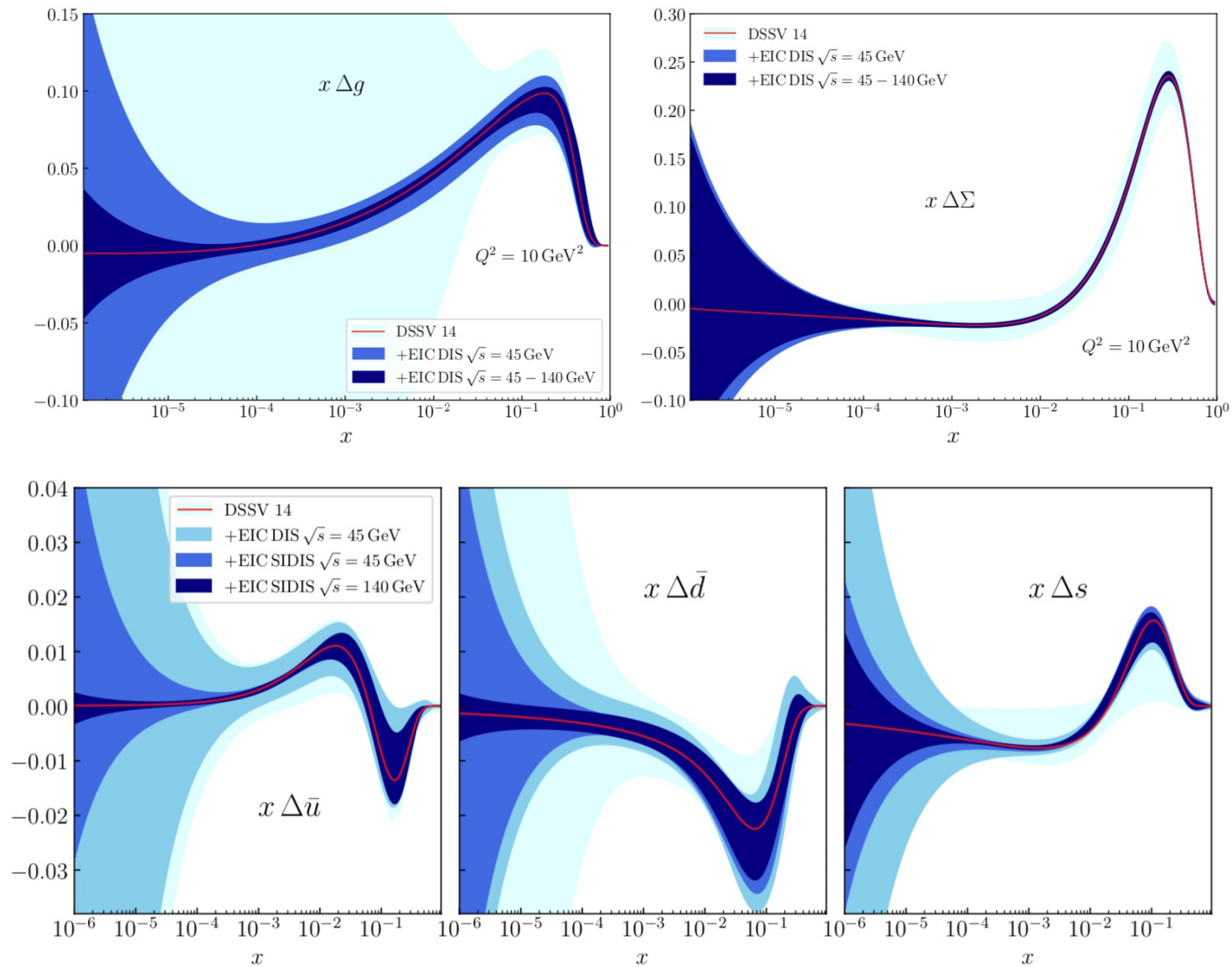
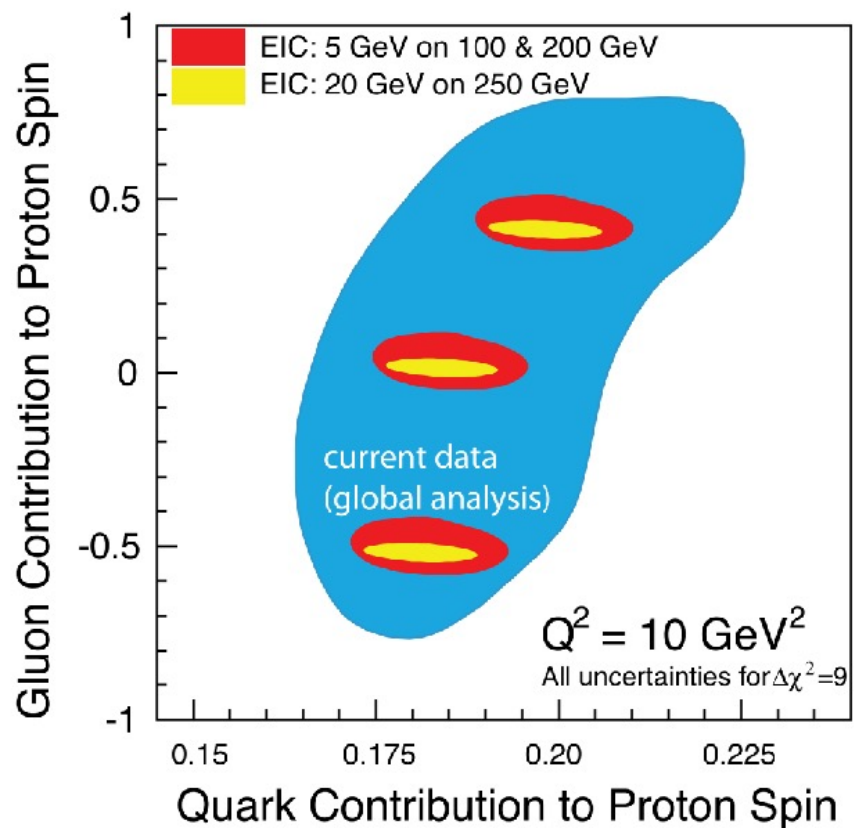
# Spin: $A_{LL}$ and Polarized PDF at EIC

- ▶ Polarized PDF from  $A_{LL}$  measurements at the EIC
  - ▶ SIDIS, charm
  - ▶ dijets



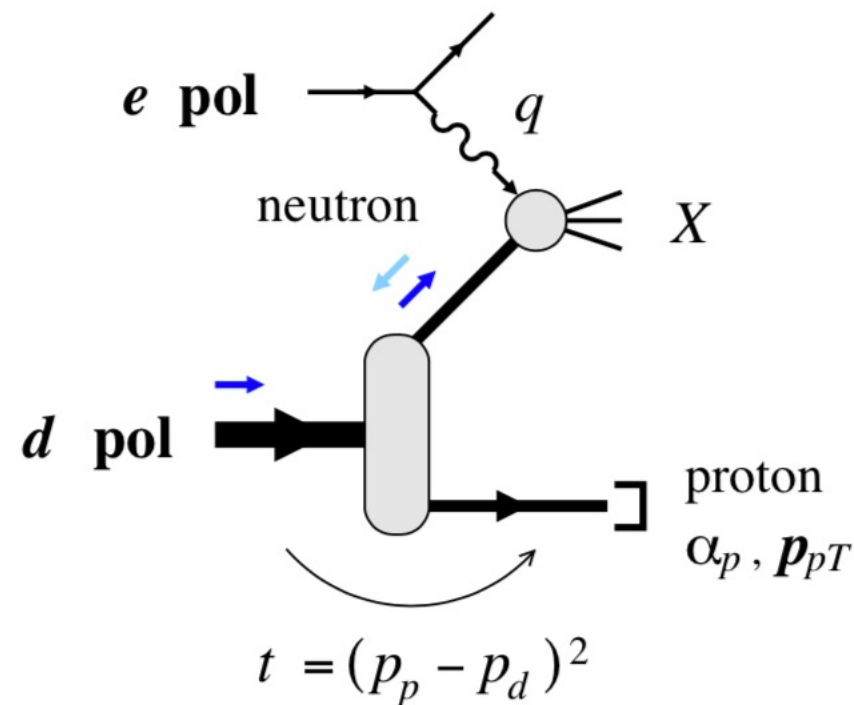
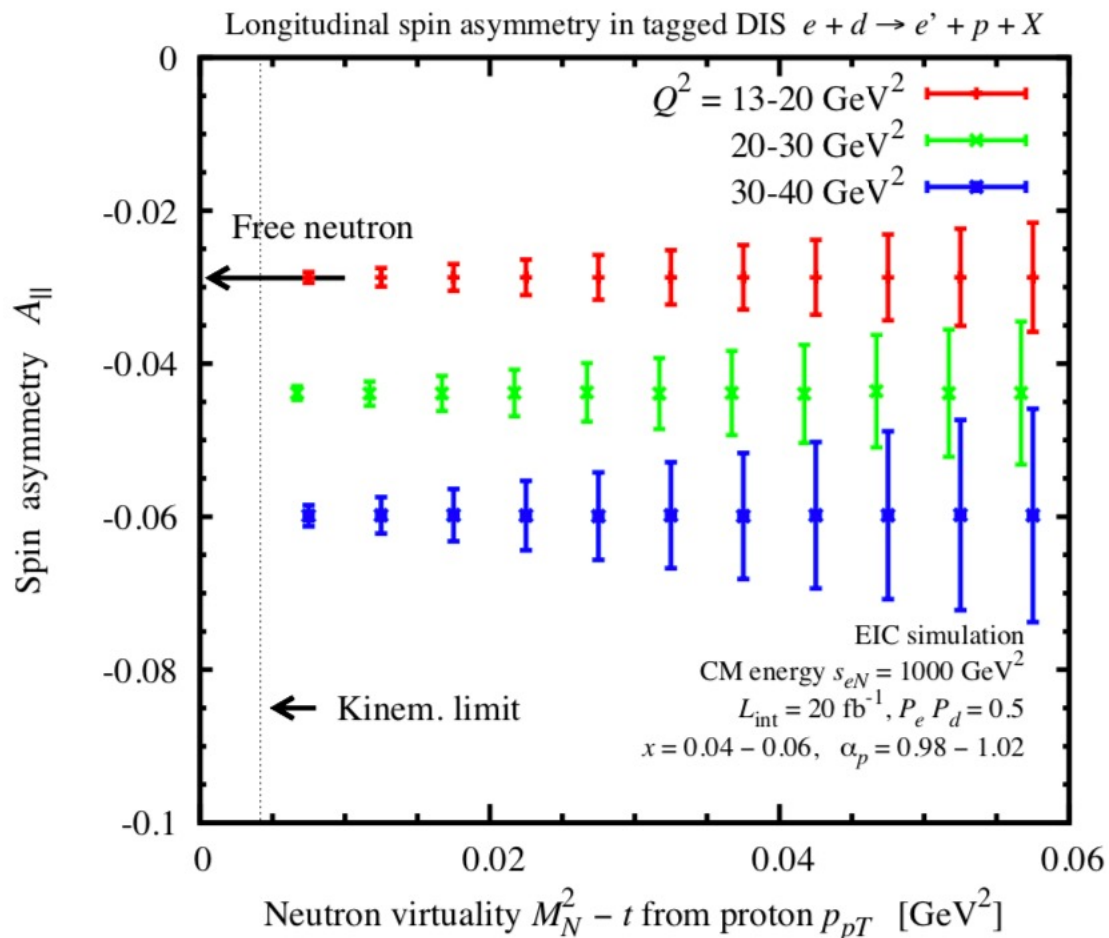
# Spin: $A_{LL}$ and Polarized PDF at EIC

## ► Polarized PDF from $A_{LL}$ measurements at the EIC



# Spin: $A_{LL}$ and Polarized PDF at EIC

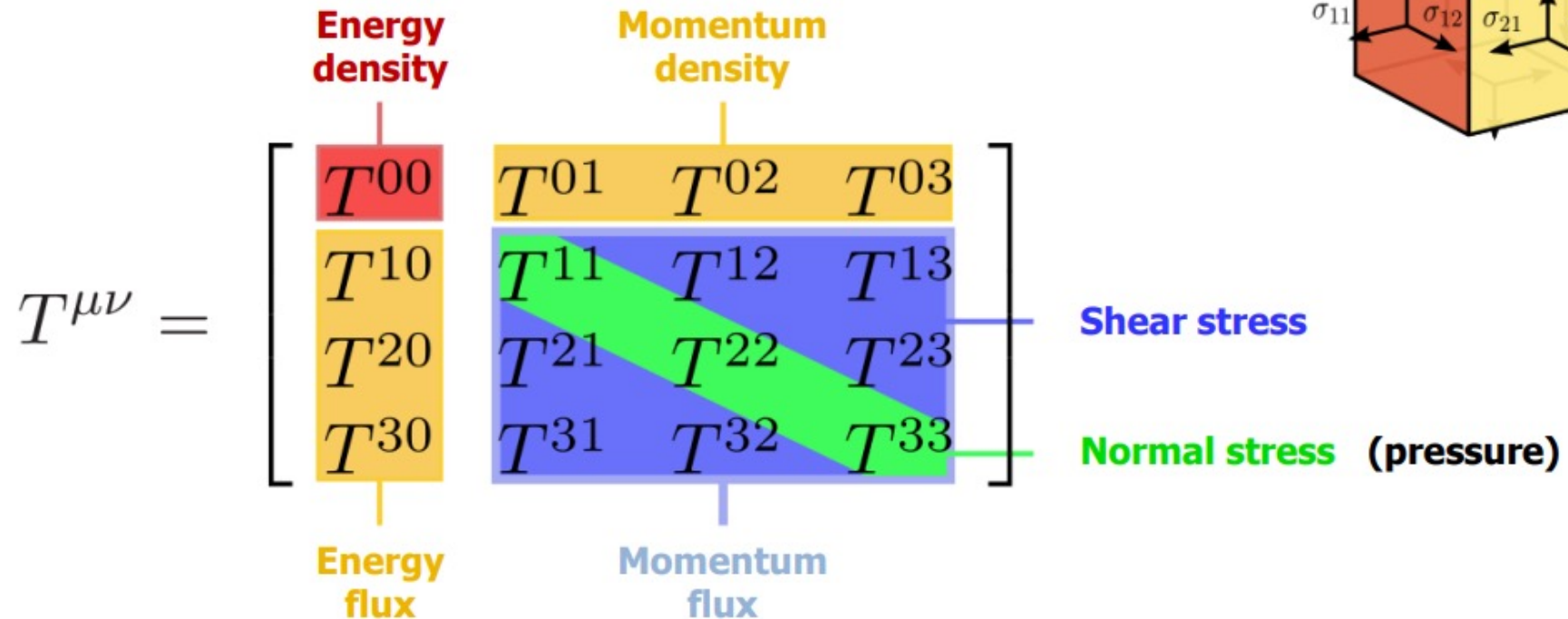
► New: neutron spin structure from  $e+d$  and  $e+^3\text{He}$



# Energy Momentum Tensor

EMT is a key fundamental object.

Mass, spin, and pressure are all encoded in the ETM.





# ETM and GPD (GFF)

Gravitational form factors (GFFs) encode information in the ETM

$$\langle p' | T_i^{\mu\nu} | p \rangle = \bar{u}(p') \left[ A_i(t) \frac{P^\mu P^\nu}{M} + D_i(t) \frac{\Delta^\mu \Delta^\nu - \Delta^2 g^{\mu\nu}}{4M} + J_i(t) \frac{P^{\{\mu} i\sigma^{\nu\}\alpha} \Delta_\alpha}{2M} + \bar{c}_i(t) M g^{\mu\nu} \right] u(p)$$

- $A_q(0) + A_g(0) = 1$ ,  $J(t) = \frac{1}{2} [A(t) + B(t)]$ ,  $B_q(0) + B_g(0) = 0$ , and  $\bar{c}_q(t) + \bar{c}_g(t) = 0$
- Related to mass and angular momentum distributions, and pressure and shear forces

GFFs are related to GPDs (i = quark, gluons)

$$\int_{-1}^1 dx [x H_i(x, \xi, t), x E_i(x, \xi, t)] = [A_i(t) + \xi^2 D_i(t), B_i(t) - \xi^2 D_i(t)]$$

Forward limit:

$$\langle p | T_i^{\mu\nu} | p \rangle = 2 [A_i(0) p^\mu p^\nu + \bar{c}_i(0) M^2 g^{\mu\nu}], \quad \langle p | T_{i\mu}^\mu | p \rangle = 2 M^2 [A_i(0) + 4 \bar{c}_i(0)], \quad \langle p | T_\mu^\mu | p \rangle = 2 M^2$$

- Any hadron mass decomposition should depend on at most two quantities

# ETM from QCD

## QCD's Energy-Momentum Tensor (EMT)

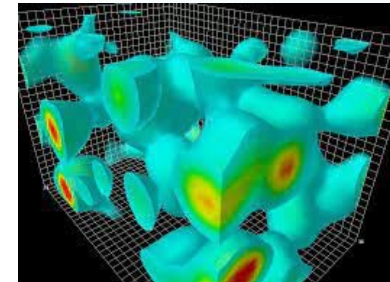
$$T^{\mu\nu} = \frac{1}{2} \bar{\psi} i D^{(\mu} \gamma^{\nu)} \psi + \frac{1}{4} g^{\mu\nu} F^2 - F^{\mu\alpha} F_{\alpha}^{\nu}, \quad T^{\mu\nu} = T^{\nu\mu}, \quad \partial_{\mu} T^{\mu\nu} = 0,$$

In the chiral limit ( $m \rightarrow 0$ ) classical EMT is traceless

QCD is scale invariant if EMT is traceless — scale-invariant theories can only have massless states

**QCD has a trace anomaly, which** breaks scale invariance and is therefore responsible for hadron masses

$$T^{\mu}_{\mu} = m_q \bar{\psi}_q \psi_q + \gamma_m m_q \bar{\psi}_q \psi_q + \frac{\tilde{\beta}(g)}{2g} F^2$$



**This trace anomaly gives trace decomposition (ex, Ji's mass decomposition)**

$$M = \frac{\langle p | \int d^3x T^{00}(0, \mathbf{x}) | p \rangle}{\langle p | p \rangle} \Big|_{\text{at rest}} = \underbrace{M_q + M_g}_{\text{quark \& gluon energies}} + \underbrace{M_m}_{\text{quark mass}} + \underbrace{M_a}_{\text{trace anomaly}}$$
$$M_q = \frac{3}{4} (a - b) M, \quad M_g = \frac{3}{4} (1 - a) M, \quad M_m = b M, \quad M_a = \frac{1}{4} (1 - b) M,$$

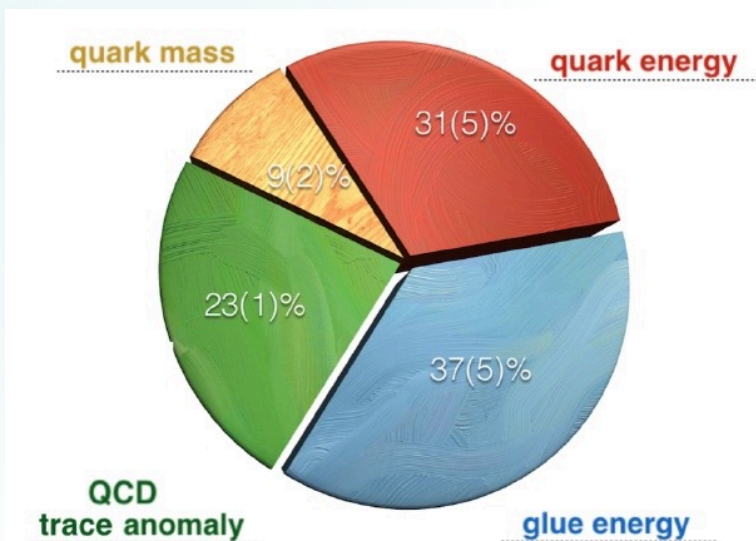
# Proton mass decomposition

## ▶ Mass Decomposition

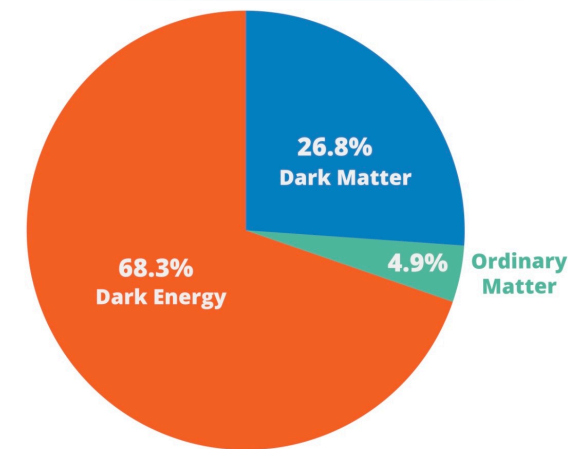
$$M = \frac{\langle p | \int d^3x T^{00}(0, \mathbf{x}) | p \rangle}{\langle p | p \rangle} \Big|_{\text{at rest}} = \underbrace{M_q + M_g}_{\text{quark \& gluon energies}} + \underbrace{M_m}_{\text{quark mass}} + \underbrace{M_a}_{\text{trace anomaly}}$$

[X.D. Ji, Phys. Rev. Lett. 74, 1071 (1995); X. D. Ji, Phys. Rev. D 52, 271 (1995)]

陽子のエネルギー分解



宇宙のエネルギー分解



クォーク ⇔ バリオン  
 グルーオン ⇔ ダークマター  
 真空のひずみ ⇔ ダークエネルギー

# Proton mass decomposition

????

$$\langle p | T_i^{\mu\nu} | p \rangle = 2 [A_i(0) p^\mu p^\nu + \bar{c}_i(0) M^2 g^{\mu\nu}], \quad \langle p | T_{i\mu}^\mu | p \rangle = 2 M^2 [A_i(0) + 4 \bar{c}_i(0)], \quad \langle p | T_\mu^\mu | p \rangle = 2 M^2$$

- Any hadron mass decomposition should depend on at most two quantities

$$M = \frac{\langle p | \int d^3x T^{00}(0, \mathbf{x}) | p \rangle}{\langle p | p \rangle} \Big|_{\text{at rest}} = \underbrace{M_q + M_g}_{\text{quark \& gluon energies}} + \underbrace{M_m}_{\text{quark mass}} + \underbrace{M_a}_{\text{trace anomaly}}$$

K. Tanaka@EIC workshop, 本郷

[https://indico3.cns.s.u-tokyo.ac.jp/event/315/contributions/2724/attachments/945/1627/utokyo24\\_05\\_29\\_tanaka.pdf](https://indico3.cns.s.u-tokyo.ac.jp/event/315/contributions/2724/attachments/945/1627/utokyo24_05_29_tanaka.pdf)

$$M = \underbrace{M_q}_{0.4} + \underbrace{M_g}_{0.6}$$

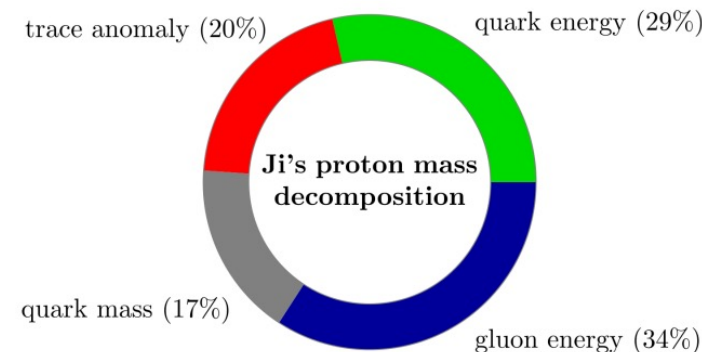
$$M_{q,g} = \left( \underbrace{A_{q,g}(0)}_{0.6, 0.4} + \underbrace{\bar{C}_{q,g}(0)}_{-0.2, 0.2} \right) M$$

$$M = \left( \underbrace{M_q}_{0.3} - \underbrace{M_m}_{0.1} \right) + \underbrace{M_m}_{0.1} + \underbrace{M_g}_{0.6}$$

$$M_m = \left\langle \int d^3x m \bar{\psi} \psi \right\rangle = \frac{\sigma_{\pi N} + \sigma_s}{M} M$$

$$M = \left( \underbrace{M_q}_{0.3} - \underbrace{M_m}_{0.1} - \underbrace{\Delta M_q}_{0.2} \right) + \underbrace{M_m}_{0.1} + \left( \underbrace{M_g}_{0.4} - \underbrace{\Delta M_g}_{0.2} \right) + \left( \underbrace{\Delta M_q}_{0.2} + \underbrace{\Delta M_g}_{0.2} \right)$$

$$\underbrace{\Delta M_q + \Delta M_g}_{0.2} = \frac{1}{4} \left\langle \int d^3x \left( \frac{\beta(g)}{2g} F^2 + \gamma_m(g) m \bar{\psi} \psi \right) \right\rangle = \frac{1}{4} (M - M_m)$$



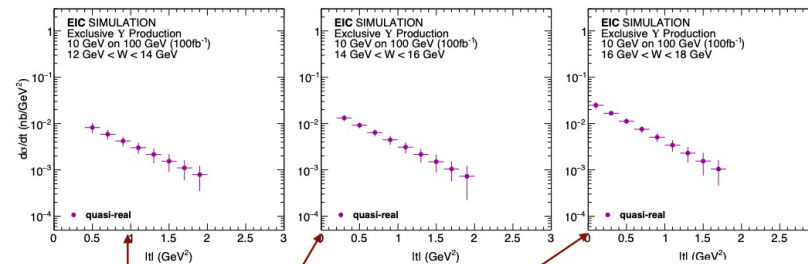
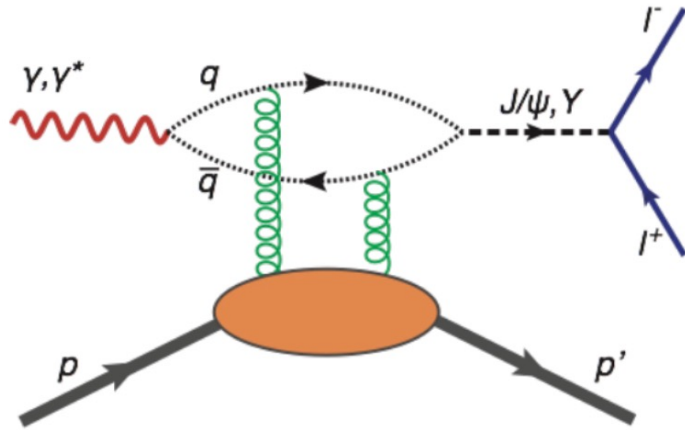
# Proton mass decomposition

$$M = \frac{\langle p | \int d^3x T^{00}(0, \mathbf{x}) | p \rangle}{\langle p | p \rangle} \Big|_{\text{at rest}} = \underbrace{M_q + M_g}_{\text{quark \& gluon energies}} + \underbrace{M_m}_{\text{quark mass}} + \underbrace{M_a}_{\text{trace anomaly}}$$

$$M_q = \frac{3}{4} \left( a - \frac{b}{1 + \gamma_m} \right) M, \quad M_g = \frac{3}{4} (1 - a) M,$$

$$M_m = \frac{4 + \gamma_m}{4(1 + \gamma_m)} b M, \quad M_a = \frac{1}{4} (1 - b) M$$

a = quark momentum fraction, b = QCD trace anomaly parameter

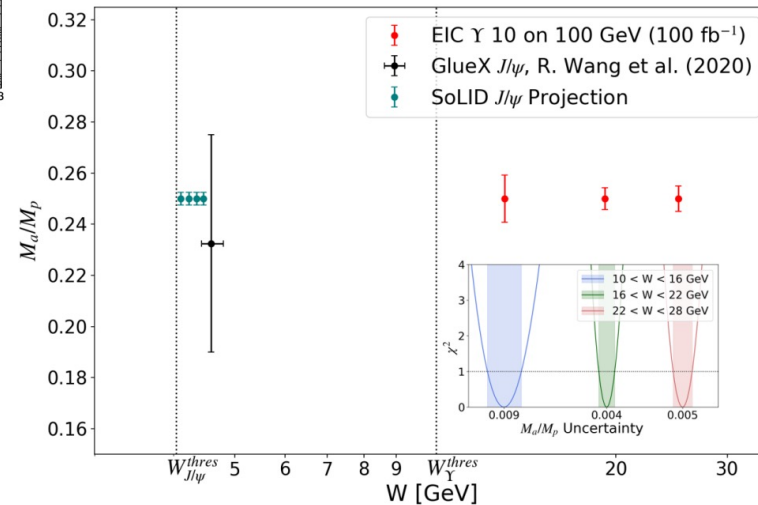
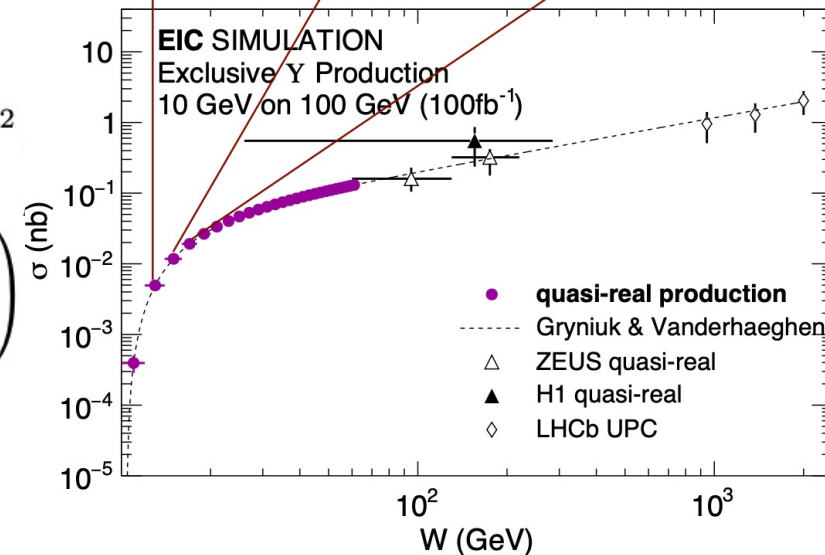


$$\left. \frac{d\sigma_{J/\psi N \rightarrow J/\psi N}}{dt} \right|_{t=0} = \frac{1}{64\pi} \frac{1}{m_{J/\psi}^2 (\lambda^2 - m_N^2)} |F_{J/\psi N}|^2$$

$$F_{J/\psi N} \simeq r_0^3 d_2 \frac{2\pi^2}{27} \left( 2M_N^2 - \left\langle N \left| \sum_{i=u,d,s} m_i \bar{q}_i q_i \right| N \right\rangle \right)$$

$$\simeq r_0^3 d_2 \frac{2\pi^2}{27} (2M_N^2 - 2bM_N^2)$$

$$\simeq r_0^3 d_2 \frac{2\pi^2}{27} 2M_N^2 (1 - b)$$



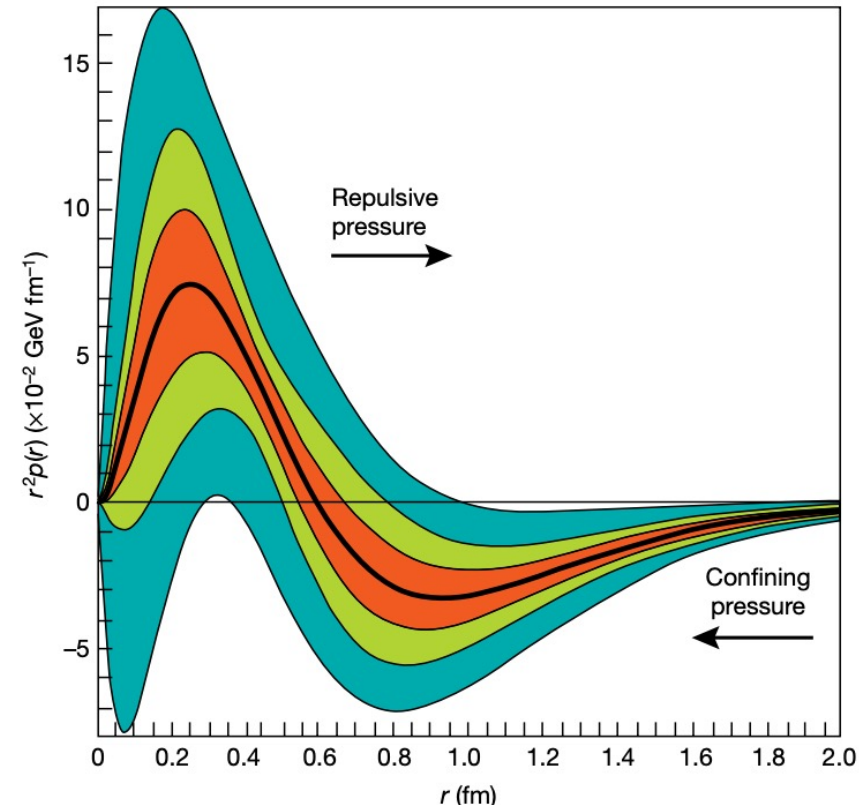
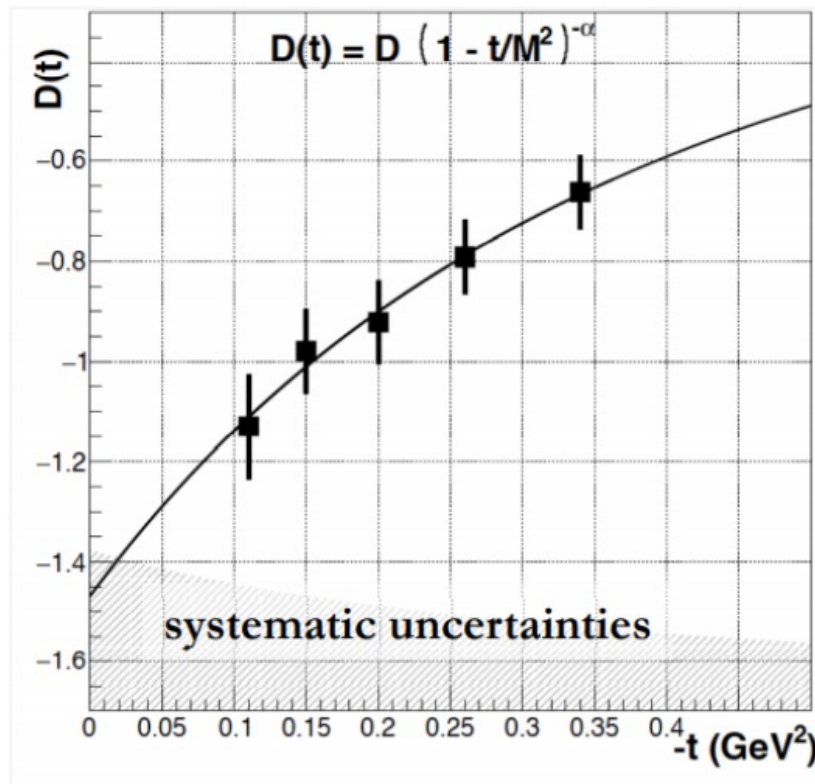
# Pressure

$$\langle p' | T_i^{\mu\nu} | p \rangle = \bar{u}(p') \left[ A_i(t) \frac{P^\mu P^\nu}{M} + D_i(t) \frac{\Delta^\mu \Delta^\nu - \Delta^2 g^{\mu\nu}}{4M} + J_i(t) \frac{P^{\{\mu} i\sigma^{\nu\}\alpha} \Delta_\alpha}{2M} + \bar{c}_i(t) M g^{\mu\nu} \right] u(p)$$

$$\int_{-1}^1 dx [x H_i(x, \xi, t), x E_i(x, \xi, t)] = [A_i(t) + \xi^2 D_i(t), B_i(t) - \xi^2 D_i(t)]$$

DVCS from JLab [Nature](#) volume 557, pages396–399 (2018)

$$p(r) = \int_0^\infty d\sqrt{-t} \sqrt{-t} J_0(r\sqrt{-t}) d(t).$$



# Pressure

Phys. Rev. Lett. 122, 072003

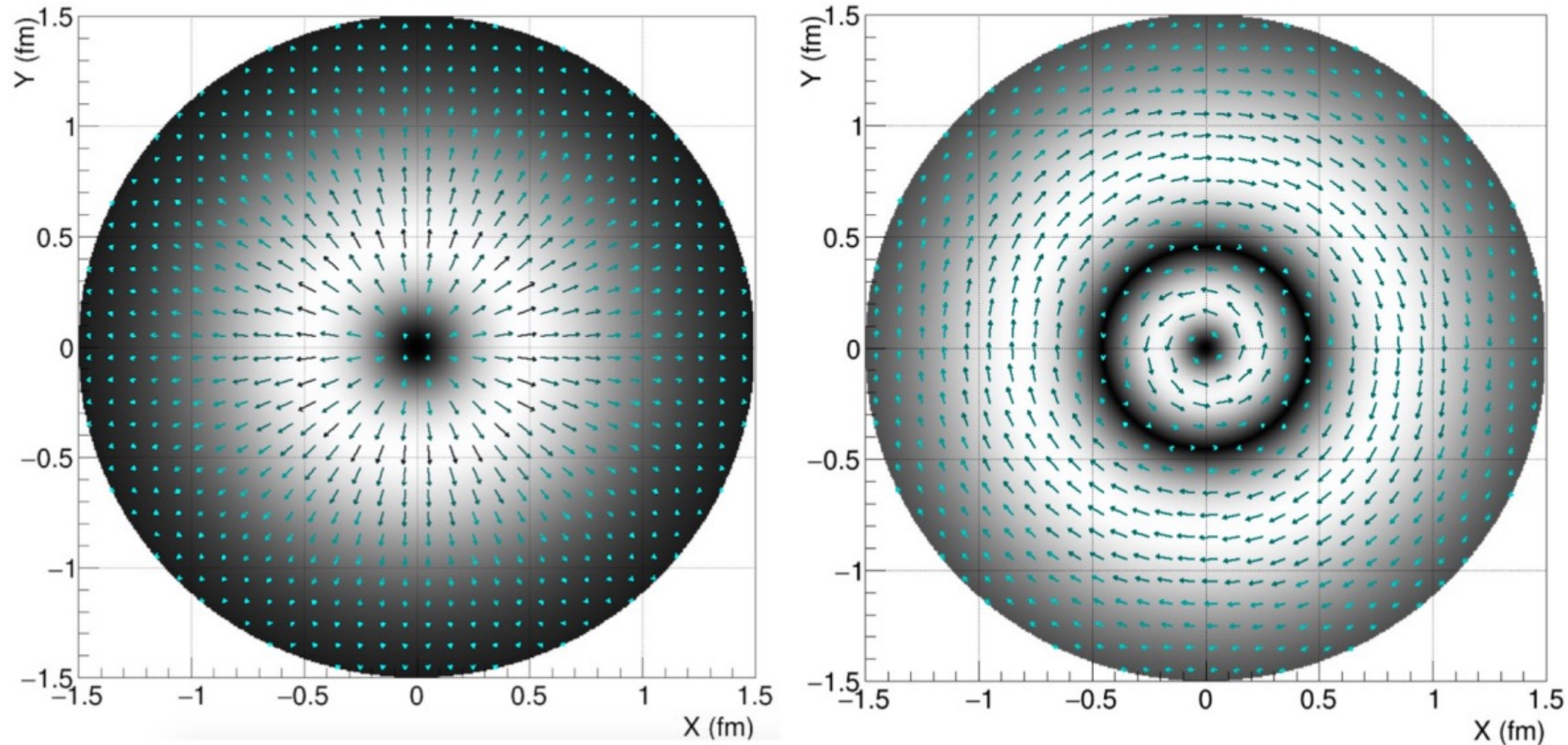
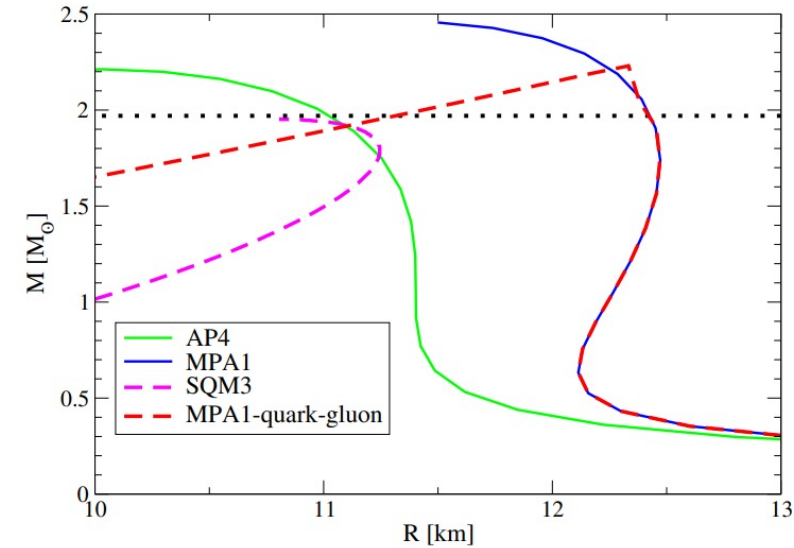
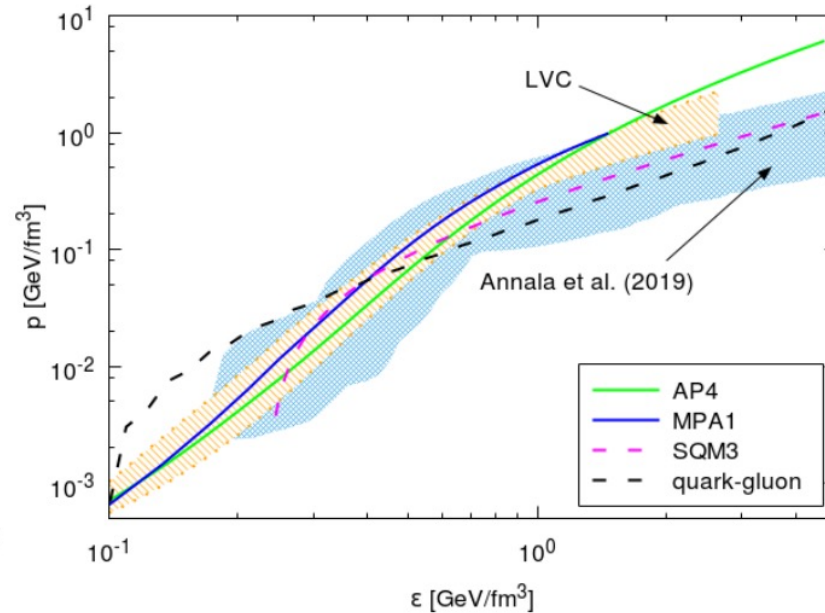
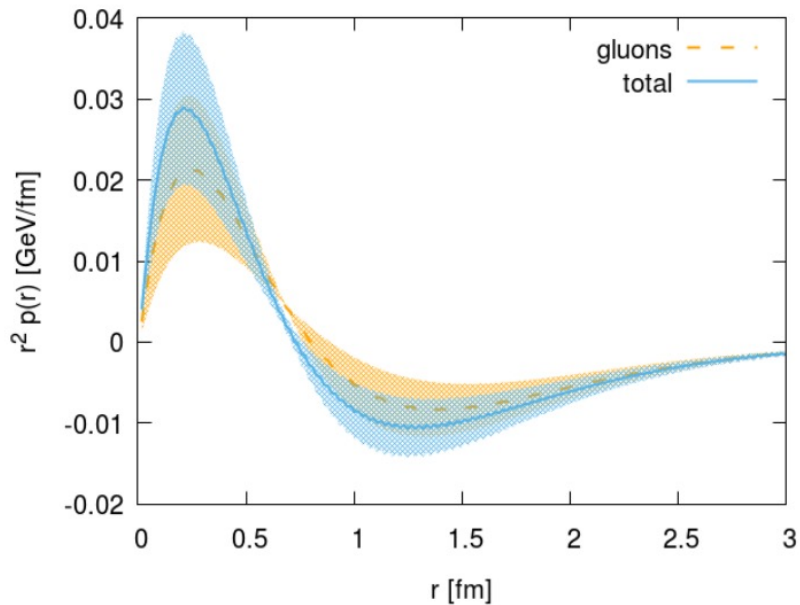


FIG. 14 2D display of the quark contribution to the distribution of forces in the proton as a function of the distance from the proton's center (Burkert et al., 2021b). The light gray shading and longer arrows indicate areas of stronger forces, the dark shading and shorter arrows indicate areas of weaker forces. Left panel: Normal forces as a function of distance from the center. The arrows change magnitude and point always radially outwards. Right panel: Tangential forces as a function of distance from the center. The forces change direction and magnitude as indicated by the direction and lengths of the arrows. They change sign near 0.4 fm from the proton center.

# EoS for neutron star

<https://arxiv.org/pdf/1812.01479>



$$\varepsilon_{q,g}(r) = \int \frac{d^2 \Delta_T}{(2\pi)^2} e^{i\Delta_T \cdot \mathbf{b}} A_2^{q,g}(t),$$

$$p_{q,g}(r) = \int \frac{d^2 \Delta_T}{(2\pi)^2} e^{i\Delta_T \cdot \mathbf{b}} \frac{t}{M^2} \underline{C_2^{q,g}(t)}.$$

**D(t)**

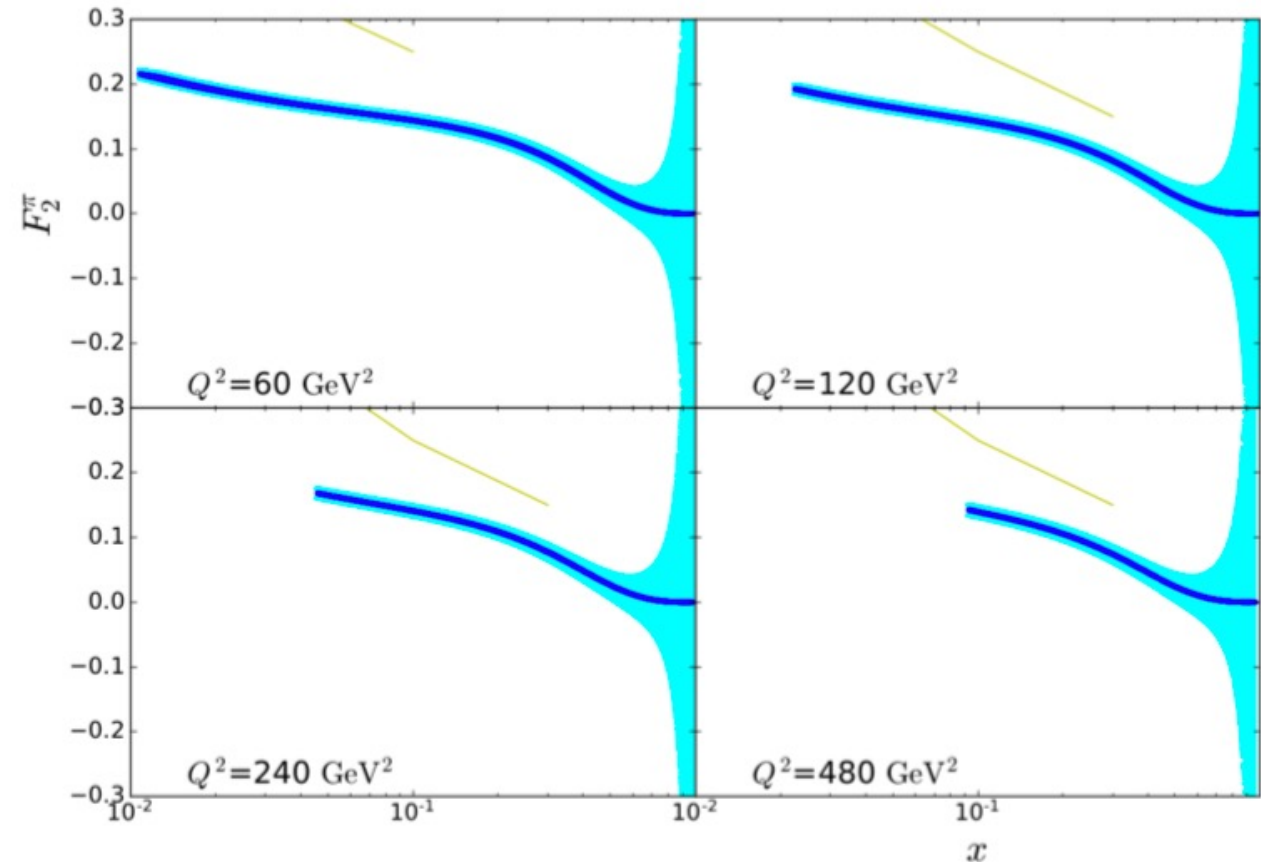
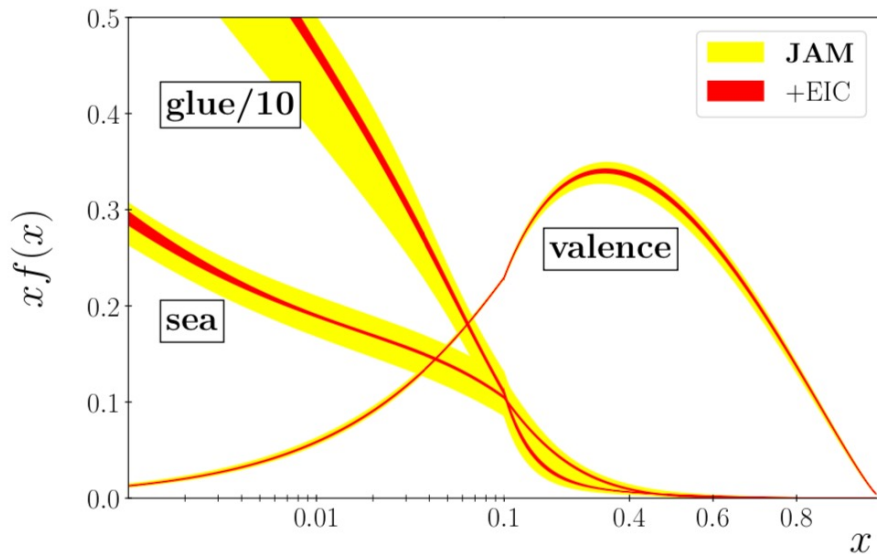
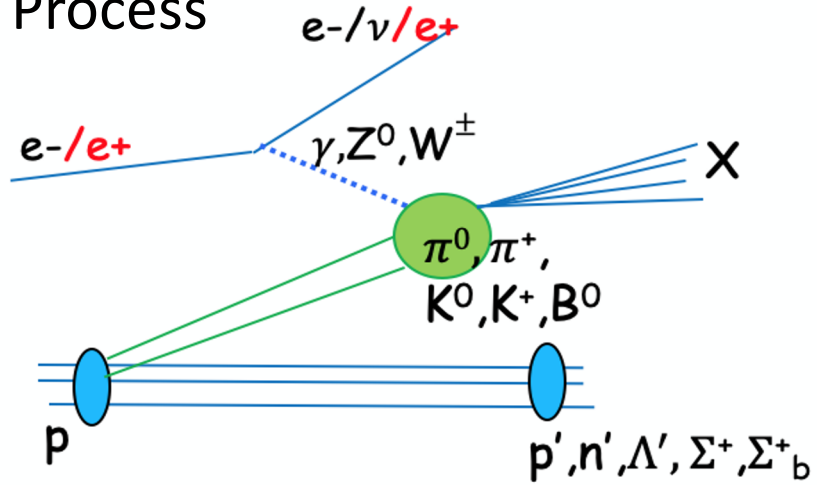
*Our main result is that the EoS obtained from the EMT is dominated by the gluon contribution, the quark contribution being largely suppressed*

*the EoS of dense matter in QCD can be obtained from first principles, using ab initio calculations for both quark and gluon degrees of freedom. Gluons, in particular, dominate the EoS, and provide a trend in the high density regime which is consistent with the constraint from LIGO*



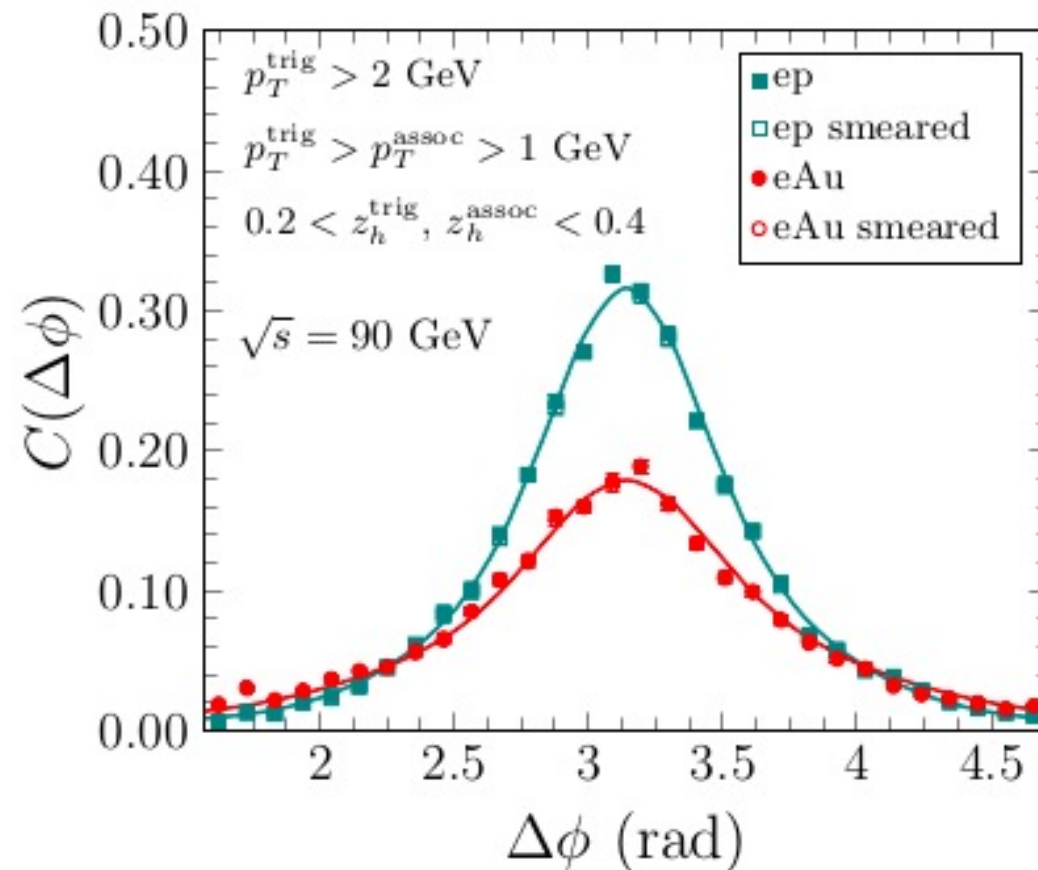
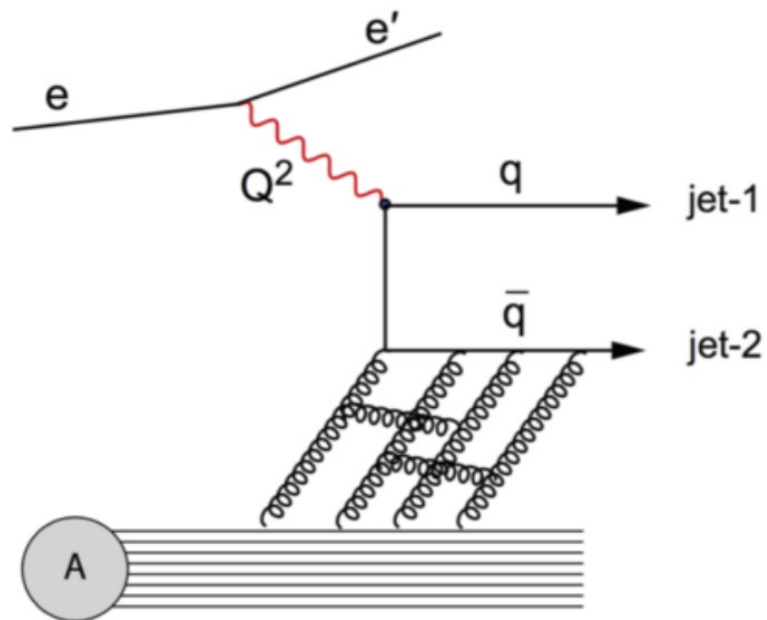
# Pion and Kaon structure

Sullivan Process



# Gluon Saturation

Measure back-to-back hadron(jet) - hadron or hadron(jet) - photon correlations  
Suppression of away peak as indication for saturation



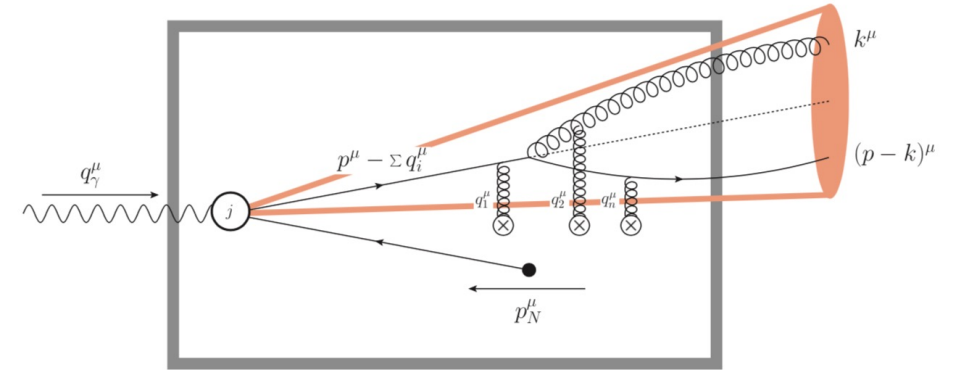
Other signatures: vector meson production in diffractive processes.

# Energy loss in gluon matter

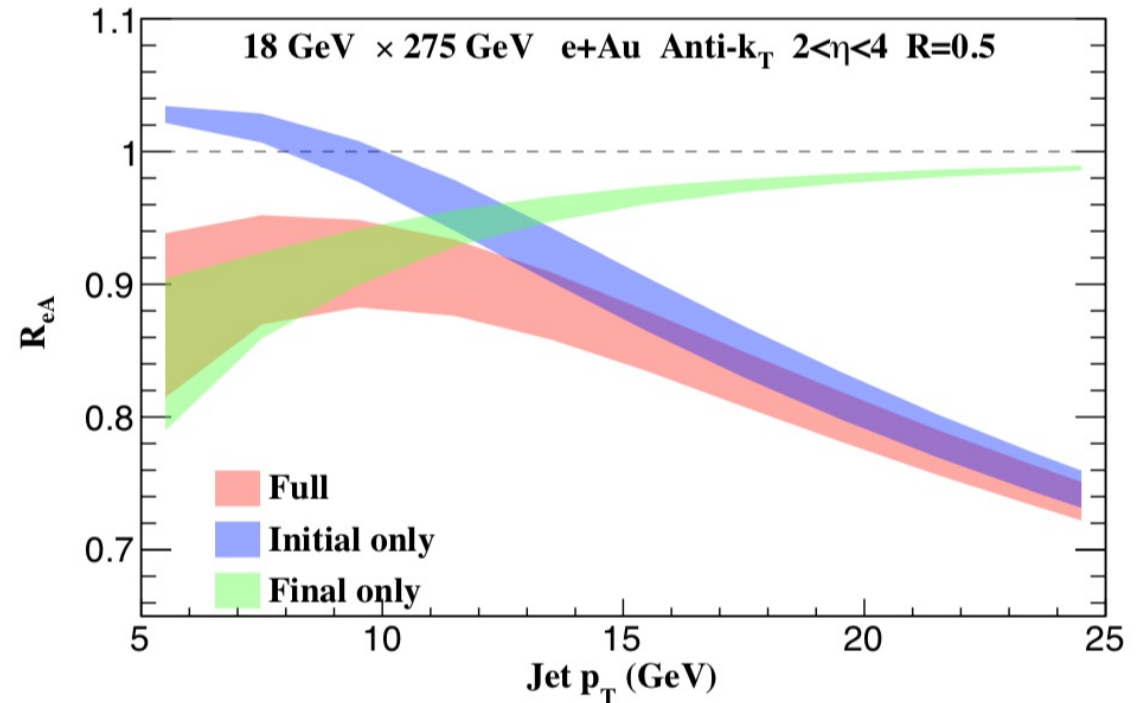
Particle propagation through matter and transport properties of nuclei

Parton showers and energy loss in cold nuclear matter

$$\hat{q} \sim 0.02 - 0.14 \text{ GeV}^2/\text{fm}$$



$$R_{eA}(R) = \frac{1}{A} \frac{\int_{\eta_1}^{\eta_2} d\sigma / d\eta dp_T |_{e+A}}{\int_{\eta_1}^{\eta_2} d\sigma / d\eta dp_T |_{e+p}} .$$



# Energy loss in gluon matter

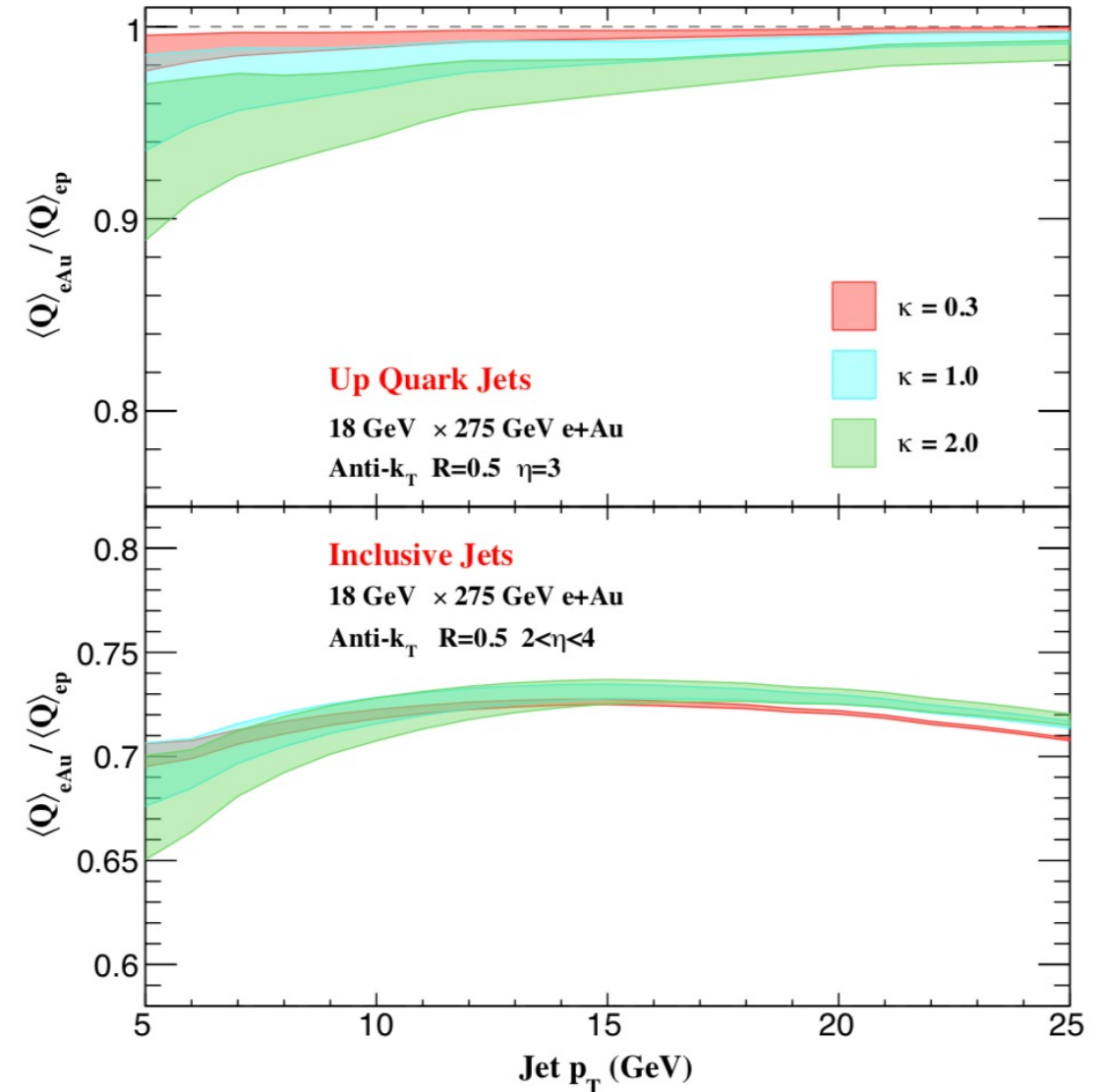
108

Particle propagation through matter and transport properties of nuclei

Parton showers and energy loss in cold nuclear matter

$\hat{q} \sim 0.02 - 0.14 \text{ GeV}^2/\text{fm}$

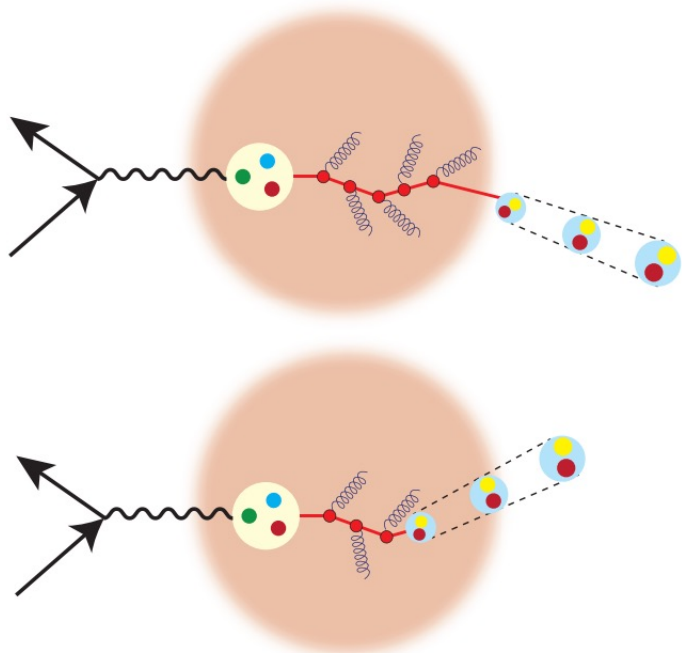
$$Q_{\kappa,\text{jet}} = \frac{1}{\left(p_T^{\text{jet}}\right)^\kappa} \sum_{i \in \text{jet}} Q_i \left(p_T^i\right)^\kappa, \quad \kappa > 0$$



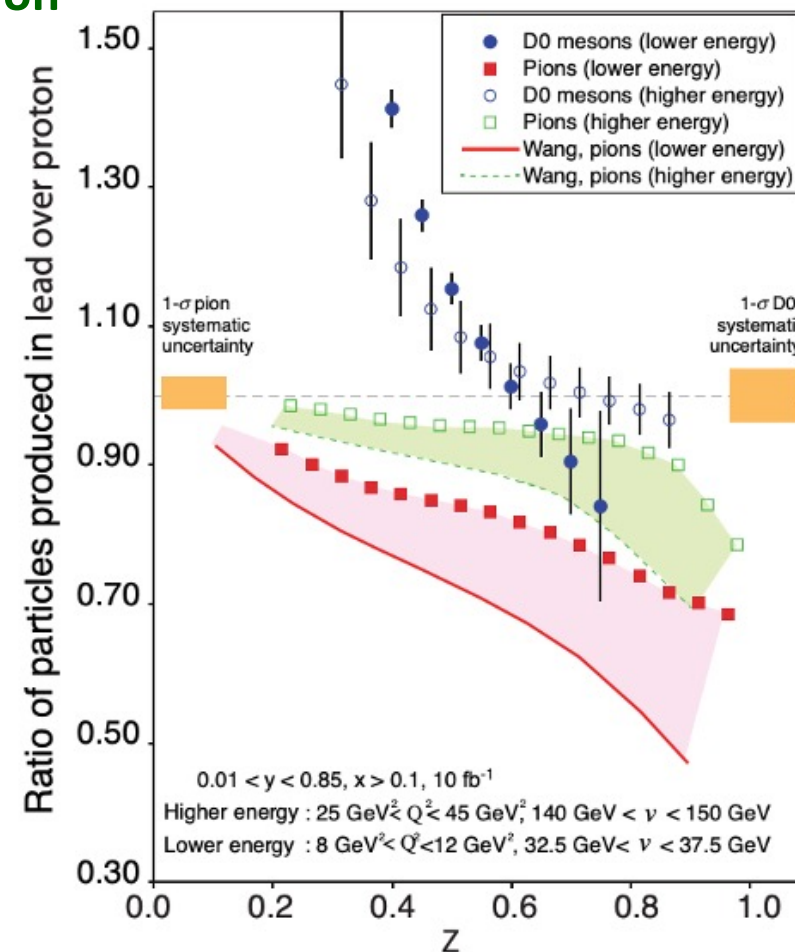
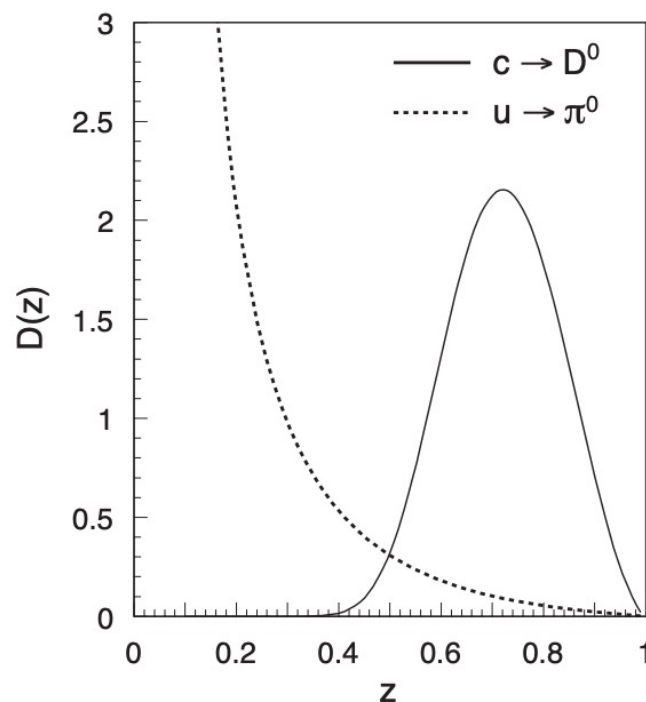
# Hadronization

## ► How Hadrons are Emerged from Quarks and Gluons?

Ions as femtometer sized detectors



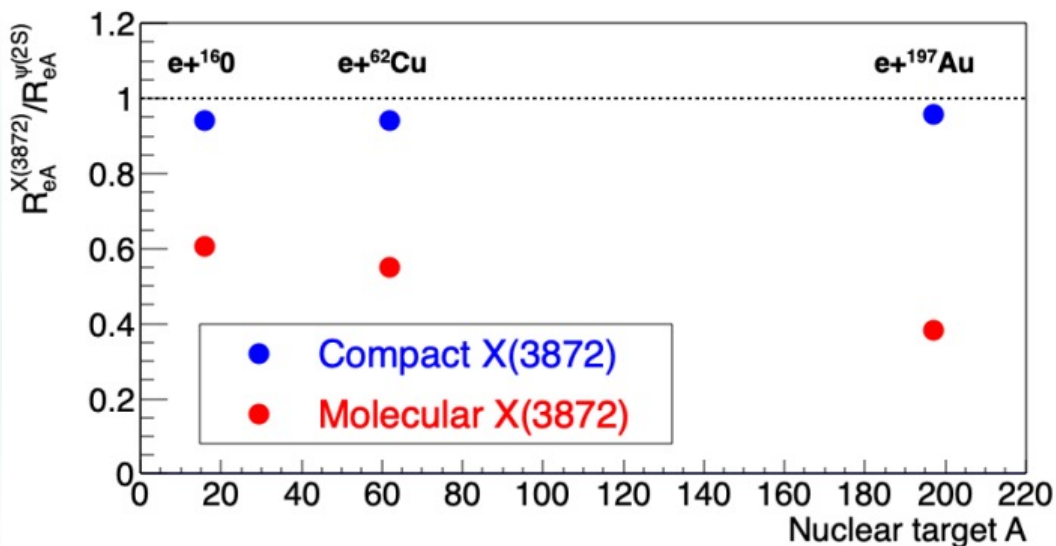
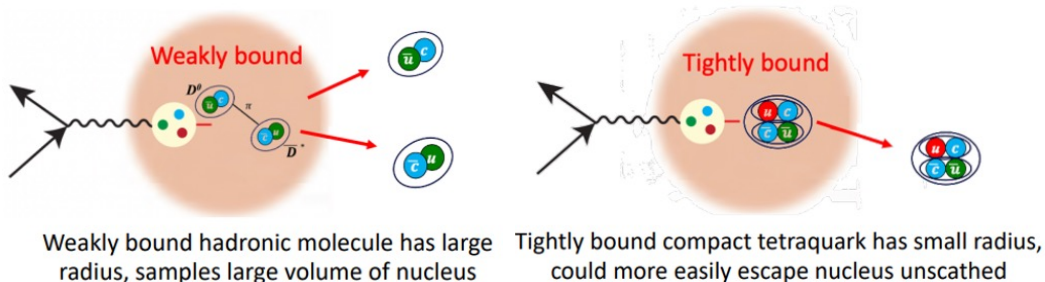
Mass dependence of hadronization



Well controlled hard-scattering kinematics and well known final state  
 Able to go from production inside medium (low-energy) to production outside of medium (high energy)  
 Topics of momentum broadening and color transparency can also be explored

# Exotic hadrons

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Use eA collisions – nucleus as a filter to differentiate between tightly bound (quark) and molecular states

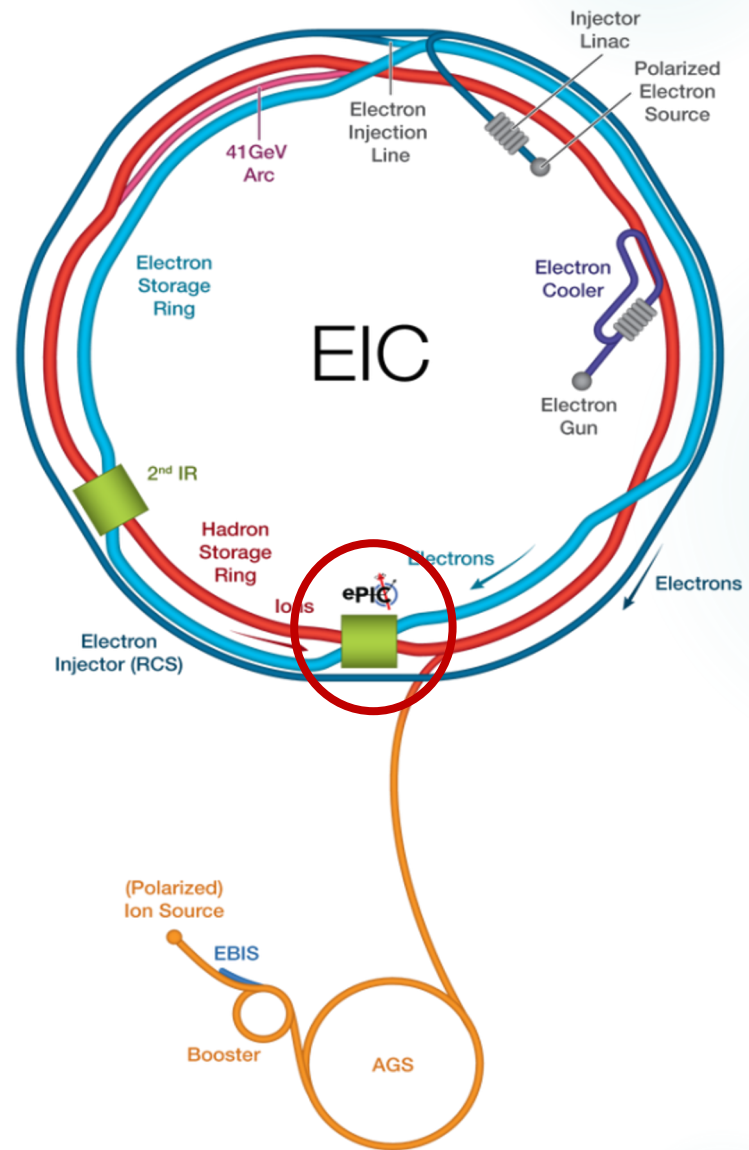
TABLE II: Integrated cross sections (in units of pb) for  $l + p \rightarrow \text{HM} + \text{all}$ , where HM =  $X(3872)$ ,  $Z_c(3900)^{0/+}$ ,  $Z_c(4020)$ , and seven  $P_c$  states. The listed quantum numbers for these

	Constituents	$J^{P(C)}$	COMPASS	EicC	US-EIC
$X(3872)$	$D\bar{D}^*$	$1^{++}$	19(78)	21(89)	216(904)
$Z_c(3900)^0$	$D\bar{D}^*$	$1^{+-}$	$0.3 \times 10^3(1.2 \times 10^3)$	$0.4 \times 10^3(1.3 \times 10^3)$	$3.8 \times 10^3(14 \times 10^3)$
$Z_c(3900)^+$	$D^{*+}\bar{D}^0$	$1^+$	$0.2 \times 10^3(0.9 \times 10^3)$	$0.3 \times 10^3(1.0 \times 10^3)$	$2.7 \times 10^3(9.9 \times 10^3)$
$Z_c(4020)^0$	$D^*\bar{D}^*$	$1^{+-}$	$0.1 \times 10^3(0.5 \times 10^3)$	$0.2 \times 10^3(0.6 \times 10^3)$	$1.7 \times 10^3(6.3 \times 10^3)$
$Z_{cs}^-$	$D^{*0}D_s^-$	$1^+$	8.3(29)	19(69)	253(901)
$Z_{cs}^{*-}$	$D^{*0}D_s^{*-}$	$1^+$	6.2(22)	14(51)	192(679)
$P_c(4312)$	$\Sigma_c\bar{D}$	$\frac{1}{2}^-$	0.8(4.1)	0.8(4.1)	15(73)
$P_c(4440)$	$\Sigma_c\bar{D}^*$	$\frac{3}{2}^-$	0.6(4.3)	0.7(4.7)	11(79)
$P_c(4457)$	$\Sigma_c\bar{D}^*$	$\frac{1}{2}^-$	0.5(2.0)	0.6(2.2)	9.9(36)
$P_c(4380)$	$\Sigma_c^*\bar{D}$	$\frac{3}{2}^-$	1.6(8.0)	1.6(8.4)	30(155)
$P_c(4524)$	$\Sigma_c^*\bar{D}^*$	$\frac{1}{2}^-$	0.8(3.6)	0.8(3.9)	14(67)
$P_c(4518)$	$\Sigma_c^*\bar{D}^*$	$\frac{3}{2}^-$	1.2(6.6)	1.2(6.9)	22(123)
$P_c(4498)$	$\Sigma_c^*\bar{D}^*$	$\frac{5}{2}^-$	1.1(9.3)	1.2(9.8)	21(173)

**+ Charm and bottom hypernuclei (arXiv:2211.15746)**  ${}^AZ(e, e'D^-)_{\Lambda Z}^A$

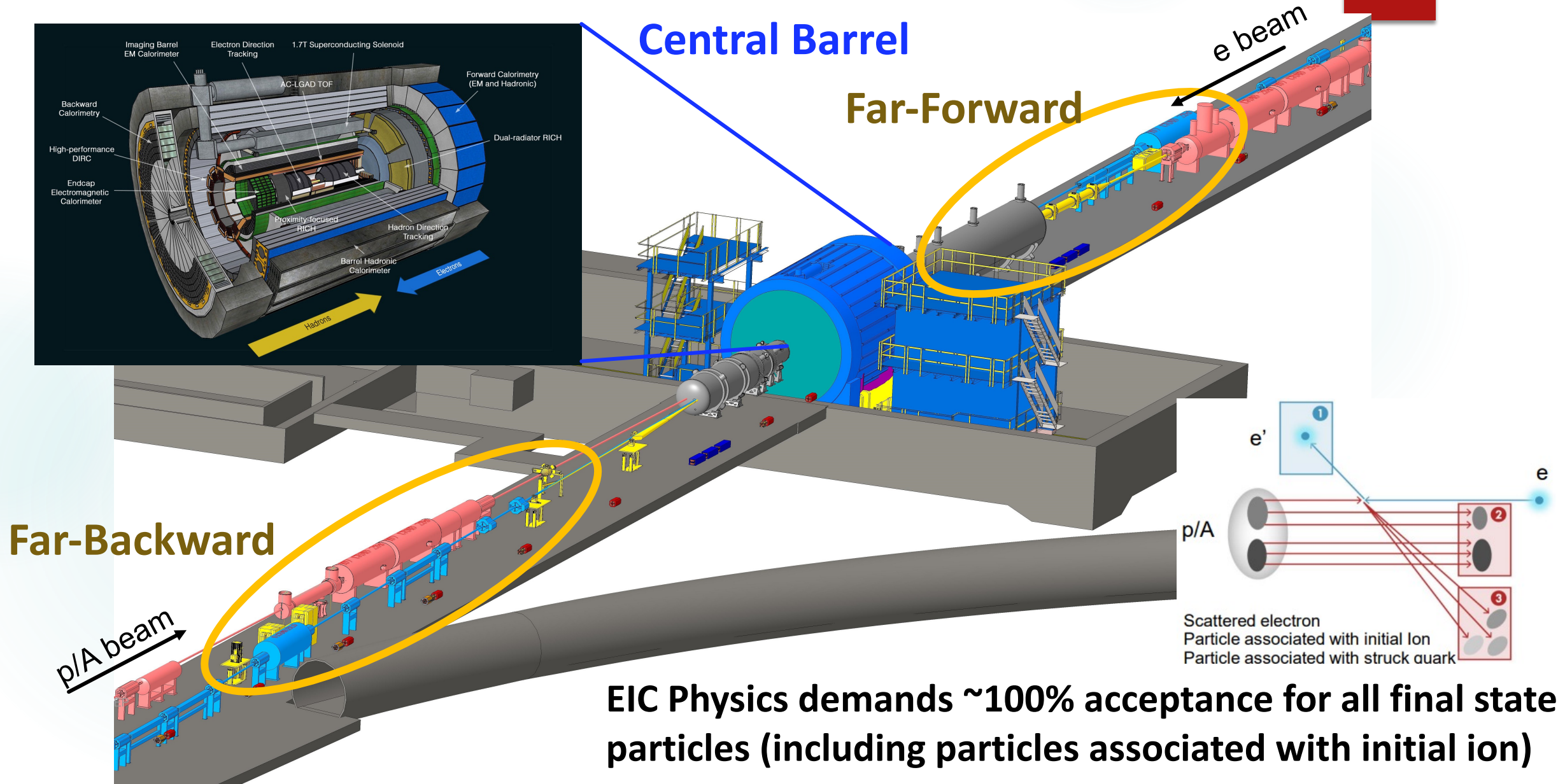
There will be around  $X(3872)$   $4 \times 10^5$  events produced per day at US-EIC. The branching fractions  $B(X(3872) \rightarrow J/\psi\pi\pi) = (3.8 \pm 1.2)\%$ ,  $B(J/\psi \rightarrow l+l^-) = 12\%$  and assuming the detection efficiency to be 50%, then the reconstructed event numbers will be about 1000 per day for US-EIC.

# Experiment



# ePIC experiment

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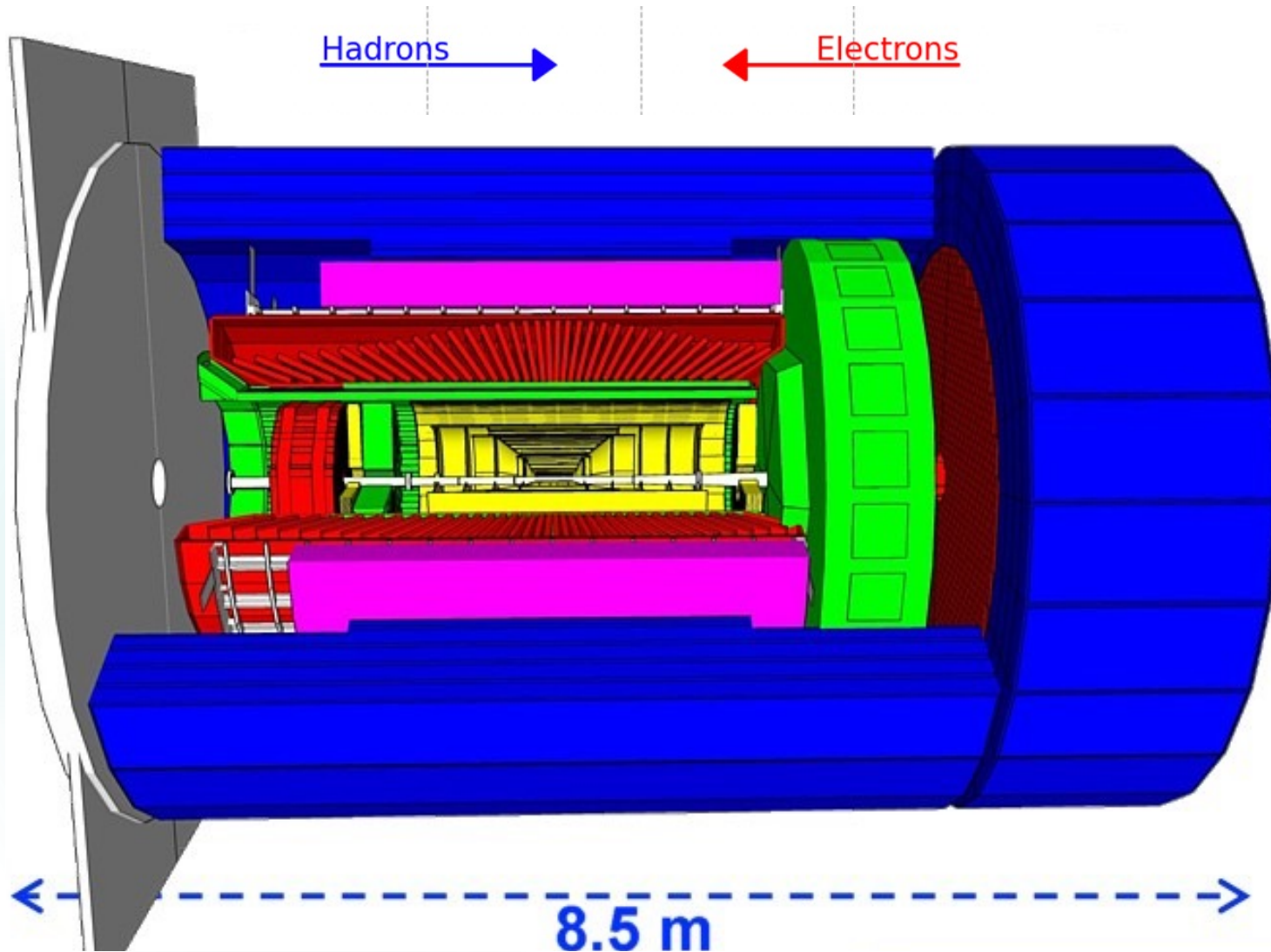


**EIC Physics demands ~100% acceptance for all final state particles (including particles associated with initial ion)**



# ePIC experiment

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hadronic calorimeters

e/m calorimeters

ToF, DIRC, RICH detectors

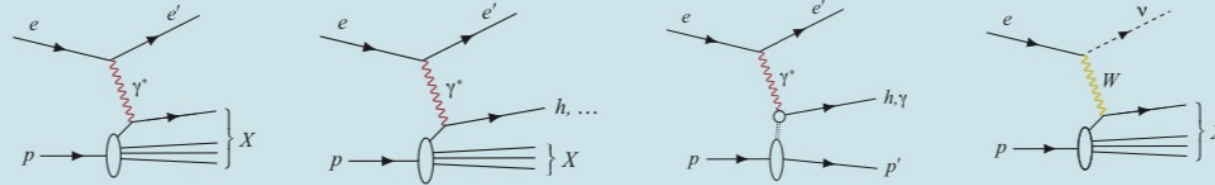
MPG & MAPS trackers

solenoid coils

# ePIC experiment

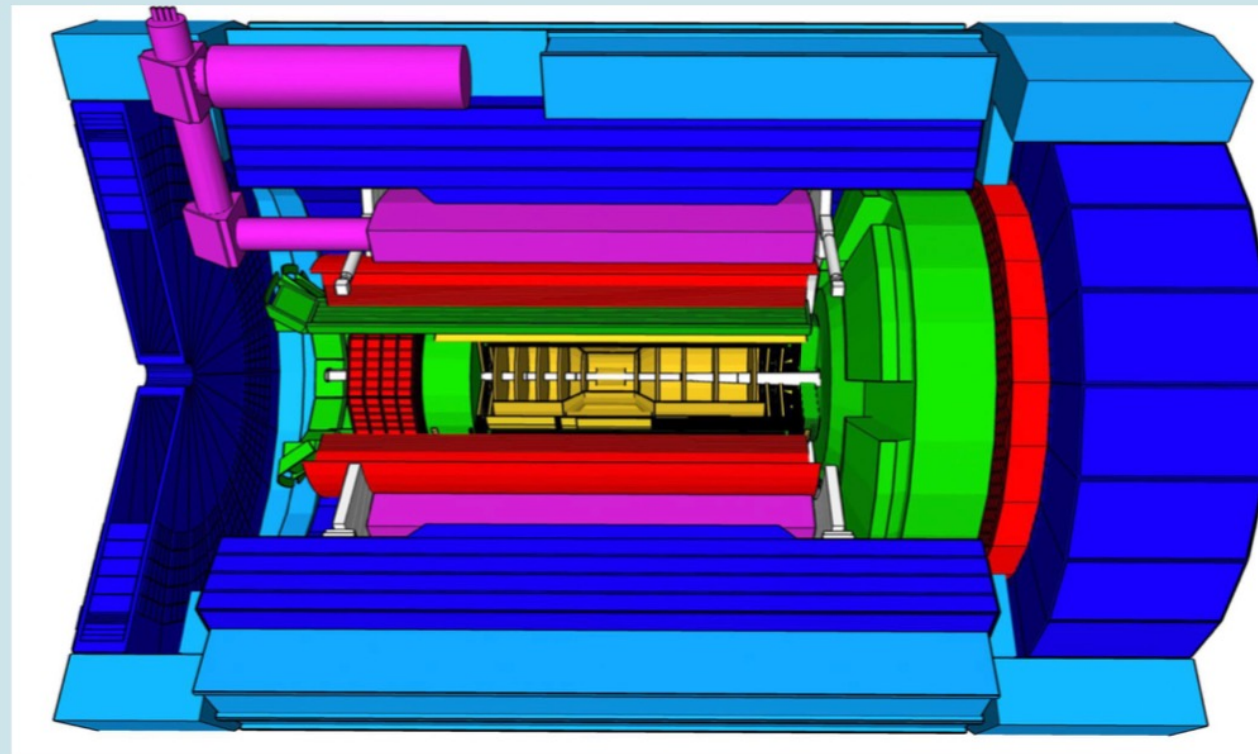
## ePIC Detector Concept

Backward



Forward

Proton/Ion beam



Electron beam

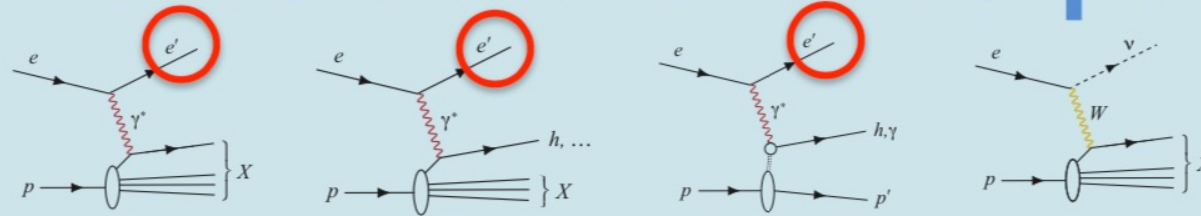
# ePIC experiment

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八野さんのスライドより(EIC研究会)

## ePIC Detector Concept

Backward

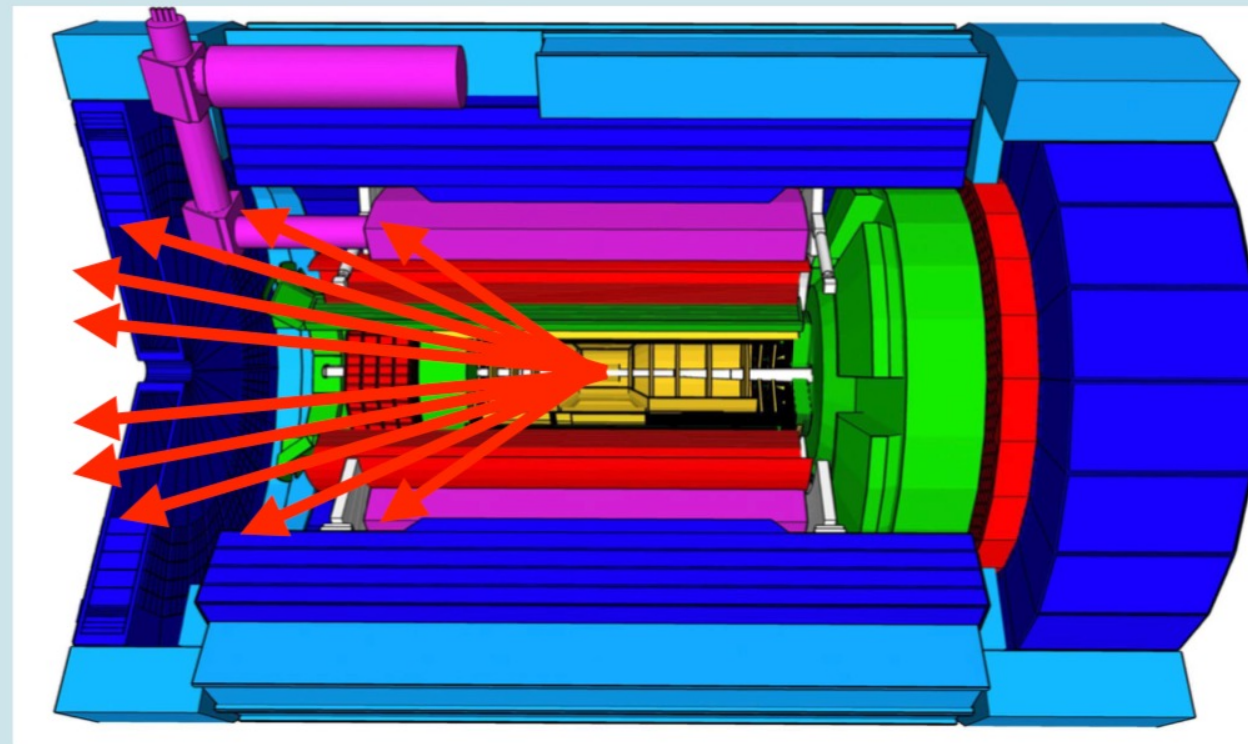


Forward

Scattered electron  
 $\eta < -2.5$  (mostly)

Proton/Ion beam

e-going endcap  
Focus on electron  
measurement

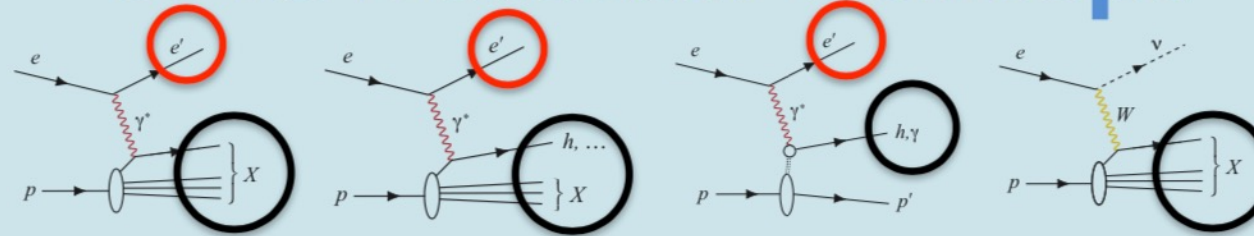


Electron beam

# ePIC experiment

## ePIC Detector Concept

Backward

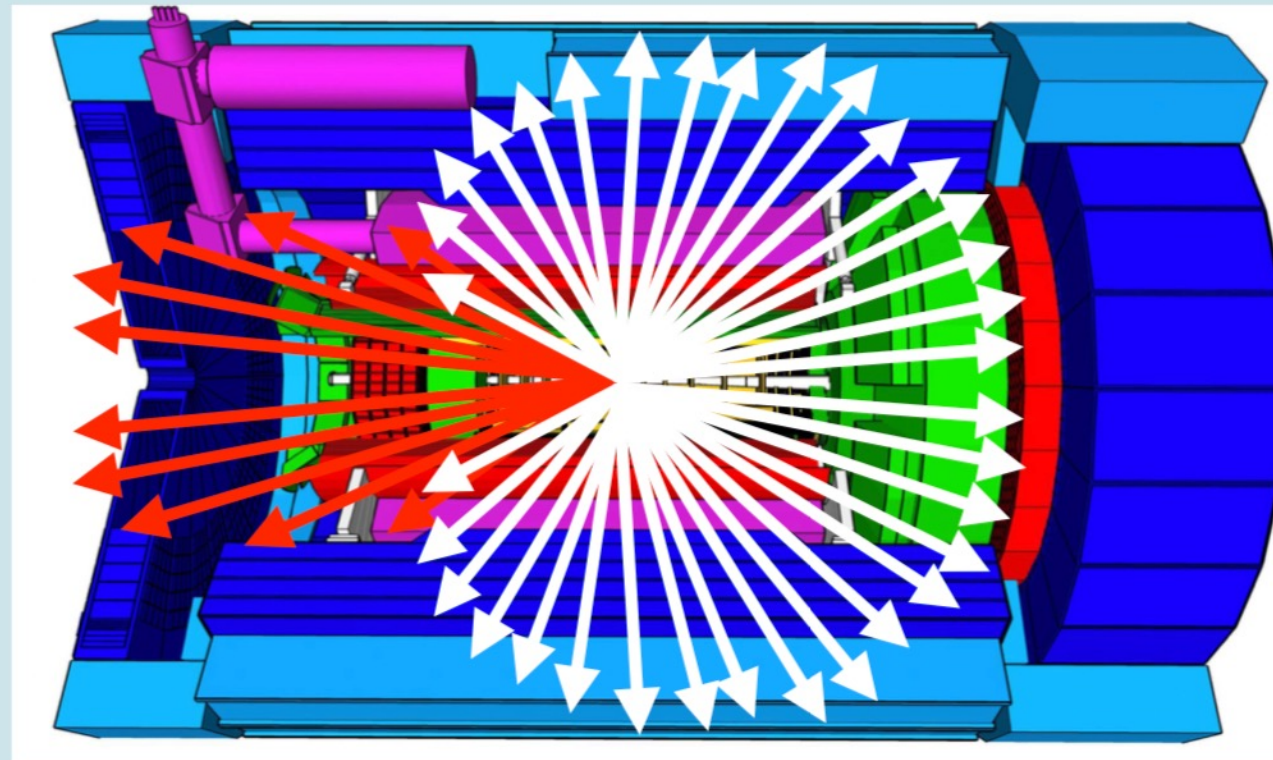


Forward

Scattered electron  
 $\eta < -2.5$  (mostly)

Proton/Ion beam

e-going endcap  
Focus on electron  
measurement



Produced particles  
(incl. jets)  
mid ~ forward  $\eta$

Electron beam

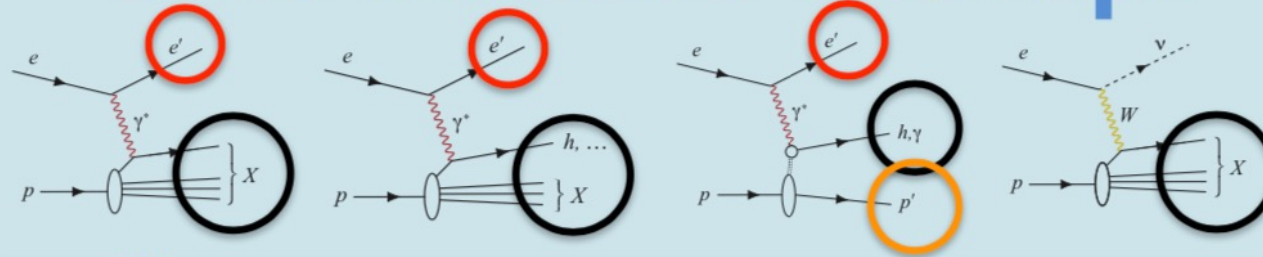
# ePIC experiment

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八野さんのスライドより(EIC研究会)

## ePIC Detector Concept

Backward

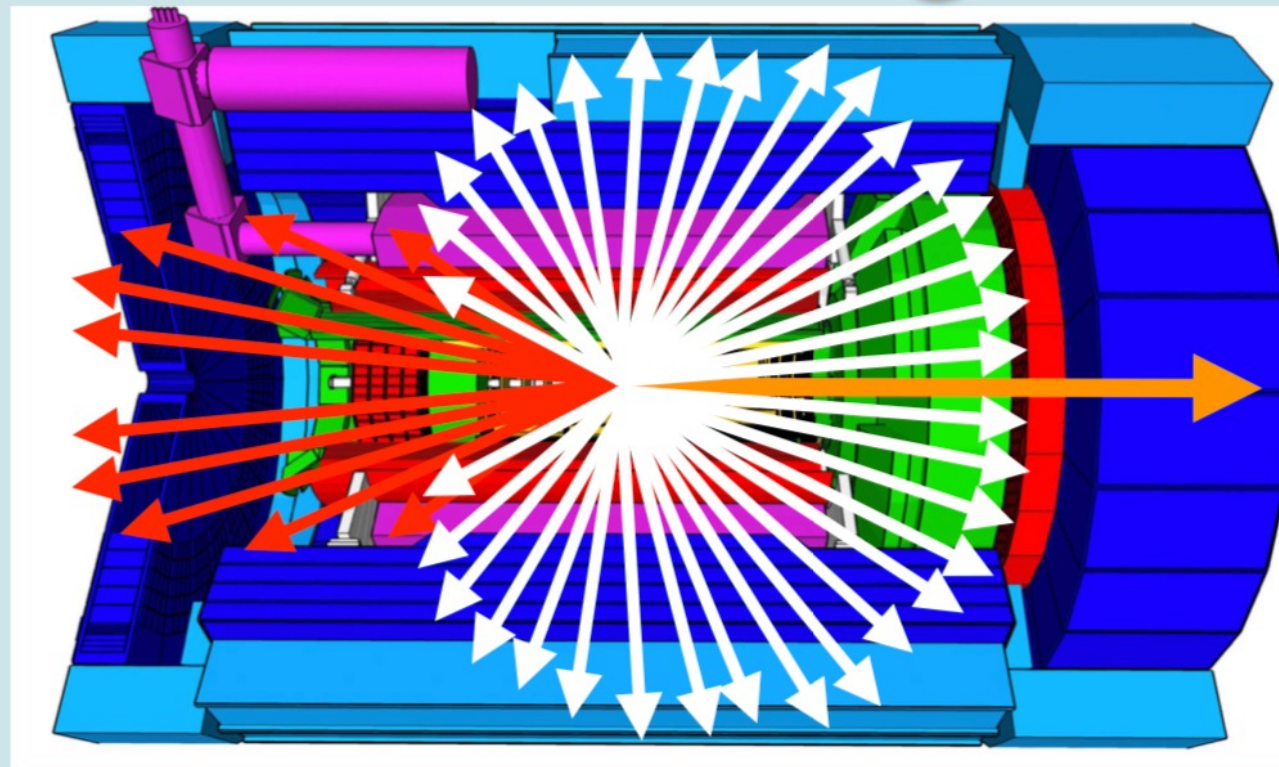


Forward

Scattered electron  
 $\eta < -2.5$  (mostly)

Proton/Ion beam

e-going endcap  
Focus on electron  
measurement



Produced particles  
(incl. jets)  
mid ~ forward  $\eta$

Electron beam

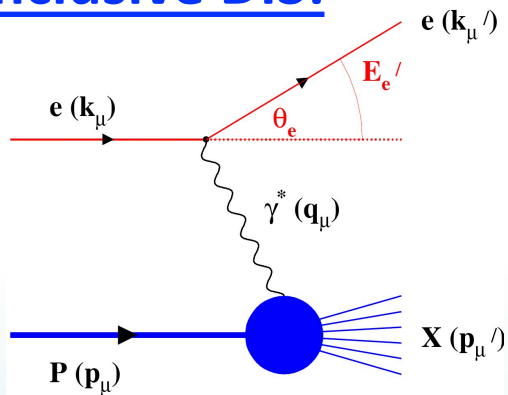
EP hadron beam  
Far-forward  
 $< 2.1^\circ$  ( $\sim 37$  mrad)

# Coverage of ePIC



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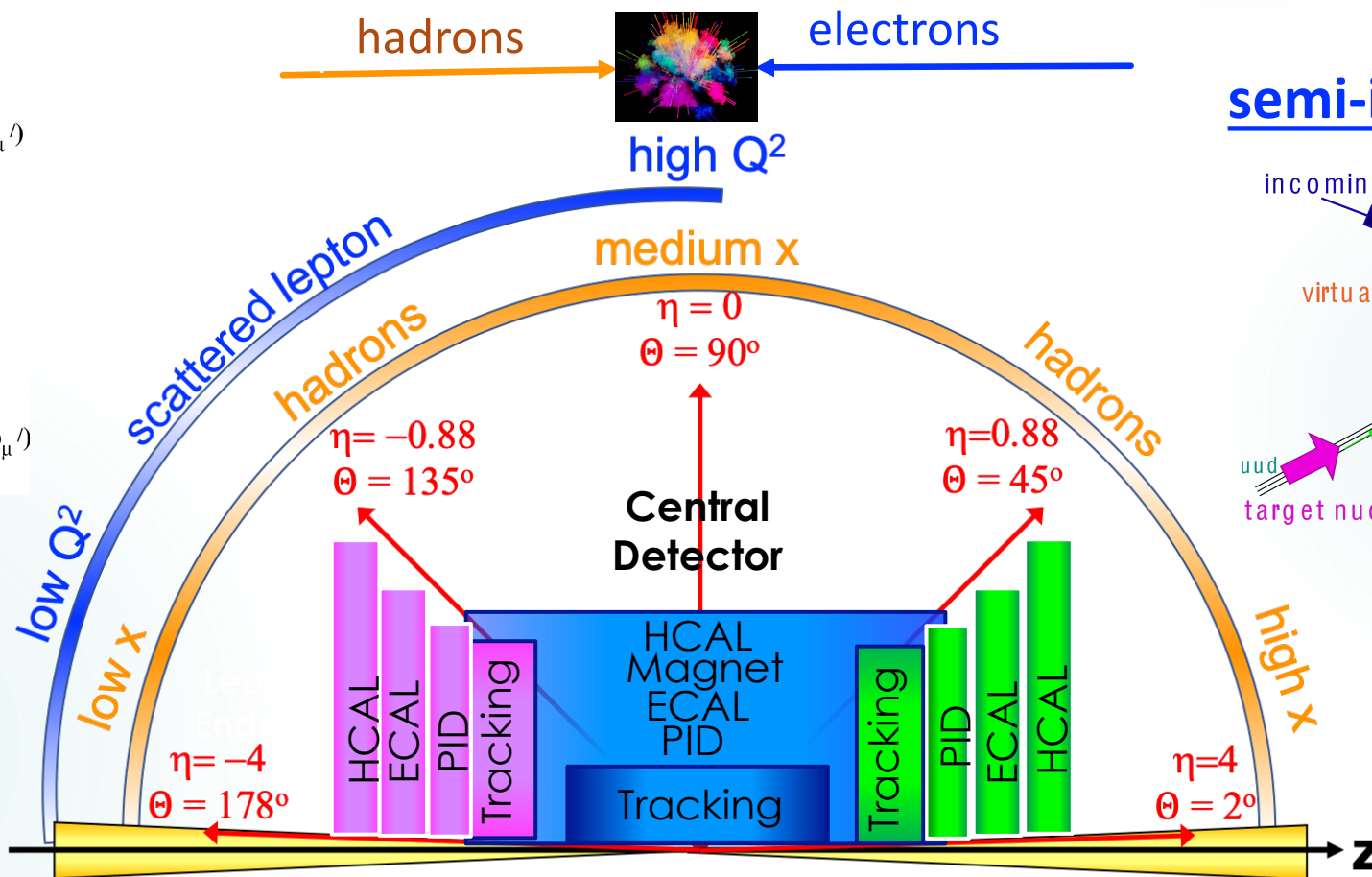
## inclusive DIS:



Detect only the scattered lepton in the detector

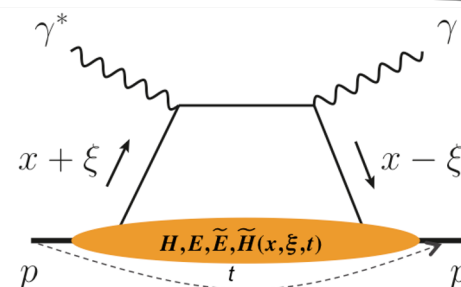
very low  $Q^2$   
scattered lepton  
Bethe-Heitler photons  
for luminosity

Luminosity Detector  
Low  $Q^2$ -Tagger

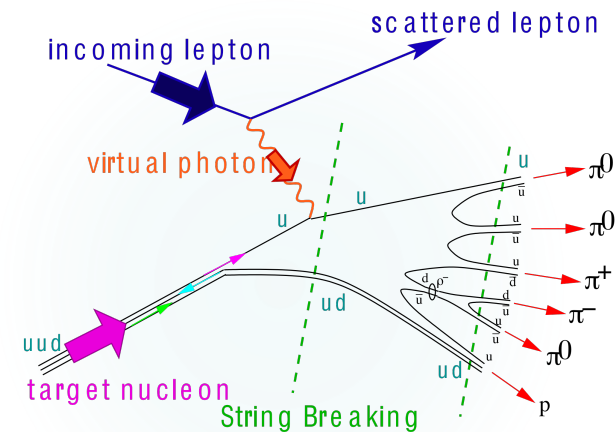


## exclusive DIS

Detect scattered lepton, identify produced hadrons/jets and target remnants



## semi-inclusive DIS



Detect the scattered lepton in coincidence with identified hadrons/jets

particles from nuclear breakup and from diffractive reactions

ZDC  
Forward Tracking

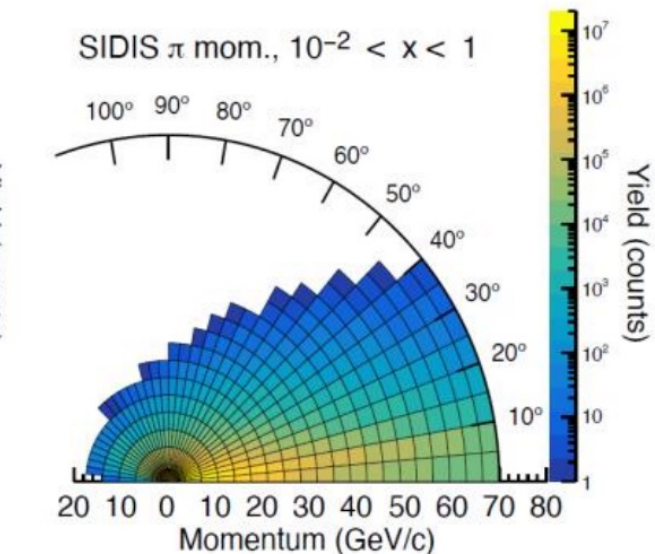
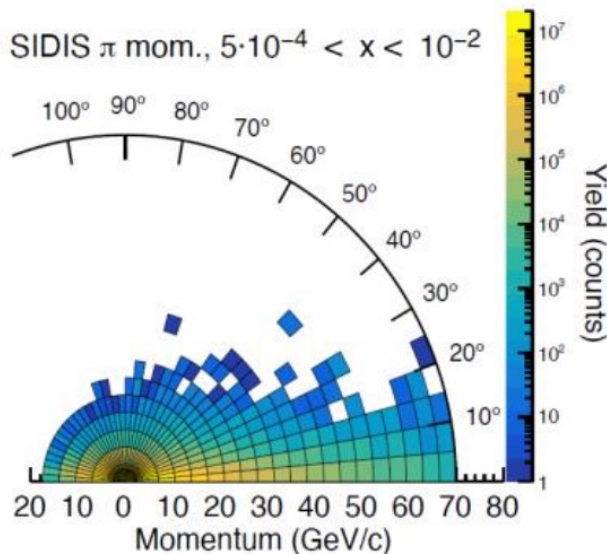
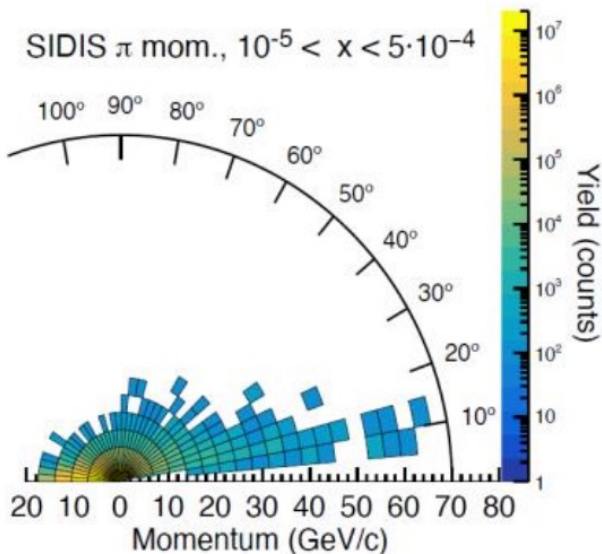
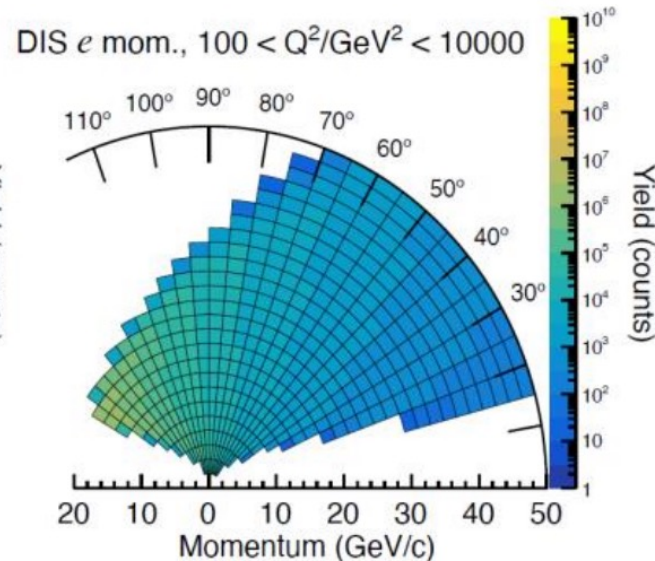
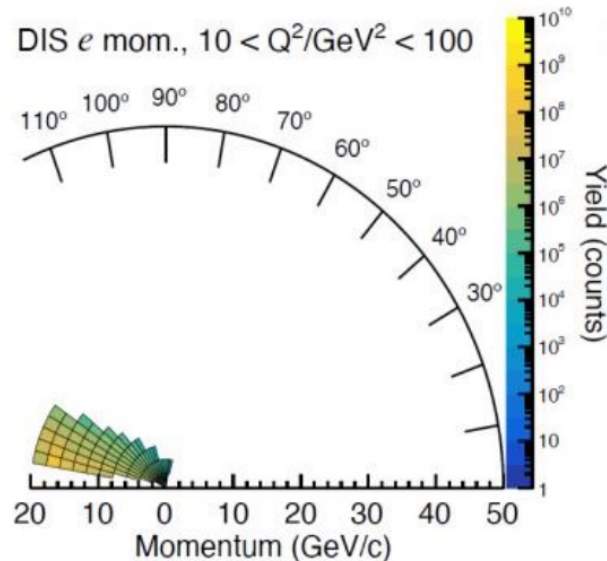
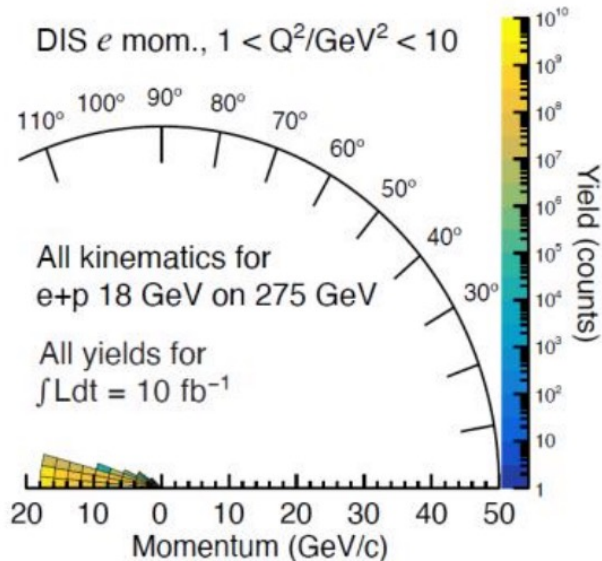
# Coverage of ePIC

hadrons

electrons



119

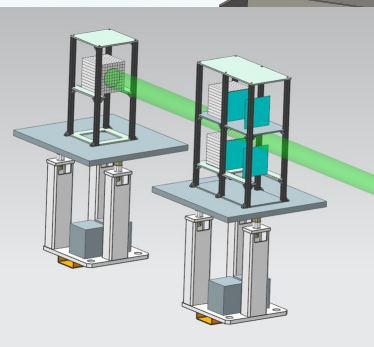


# Far-Forward/Backward

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**Main Function:**  
measure bunch-by-bunch luminosity through Bethe-Heitler process

**Technology:**  
Pair-spectrometer: each with 2 tracking layers of AC-LGAD  
Calorimeter: Tungsten-powder + SciFi SPACAL

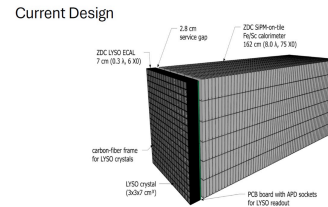


**Luminosity System**

**Main Function:**  
detection of forward scattered neutrons and  $\gamma$

**Technology:**  
EMCAL:  $2 \times 2 \times 20 \text{ cm}^3 \text{ PbWO}_4$  or LYSO  
HCAL: Steel-SiPM-on-Tile

## Zero Degree Calorimeter

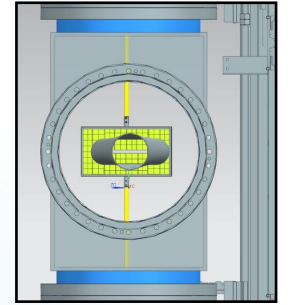


$\rightarrow$  beam

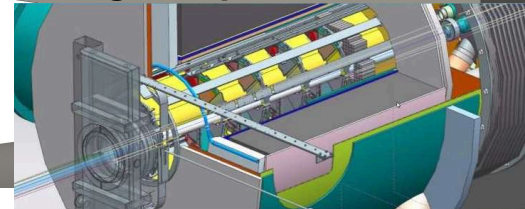
## Roman Pots and Off-Momentum Detectors

**Main Function:**  
detection of forward scattered protons and nuclei

**Technology:**  
2 stations with 2 tracking layers each  
AC-LGAD / EICROC (  $500 \times 500 \mu\text{m}^2$  pixel)



## B0 Magnet Spectrometer

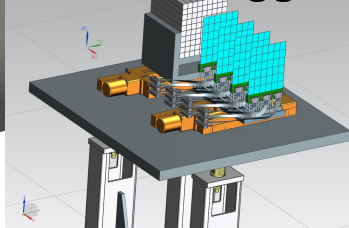


**Main Function:**  
detection of forward scattered protons and  $\gamma$

**Technology:**  
4 tracking layers each  
AC-LGAD / EICROC (  $500 \times 500 \mu\text{m}^2$  pixel)  
Synergy with forward ToF  
EMCAL:  $2 \times 2 \times 20 \text{ cm}^3 \text{ PbWO}_4$  calorimeter

$\rightarrow$  p/A beam

## Low-Q2 Taggers



**Main Function:**  
detection of scattered electrons

**Technology:**  
2 stations with 4 tracking layers each (  $16 \times 18 \text{ cm}^2$  )  
Si / Timepix4  
Calorimeter: Tungsten-powder + SciFi SPACAL

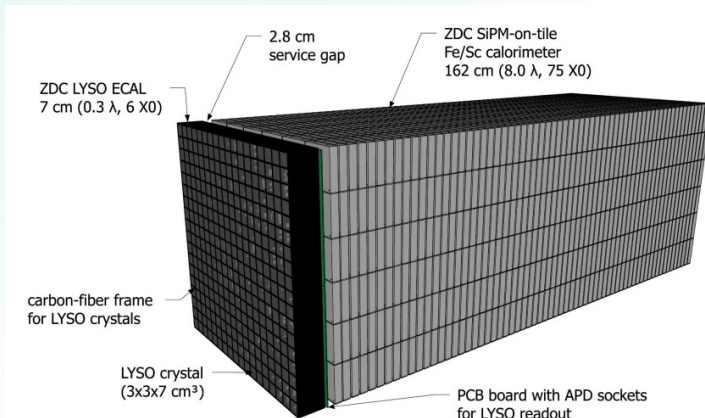
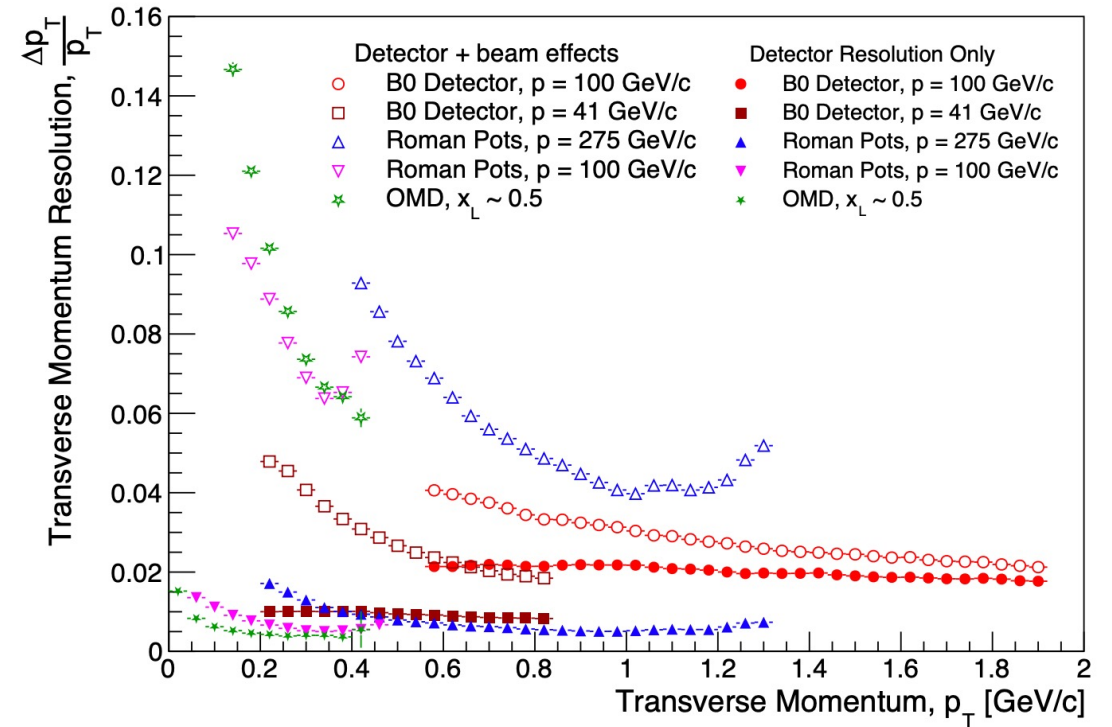
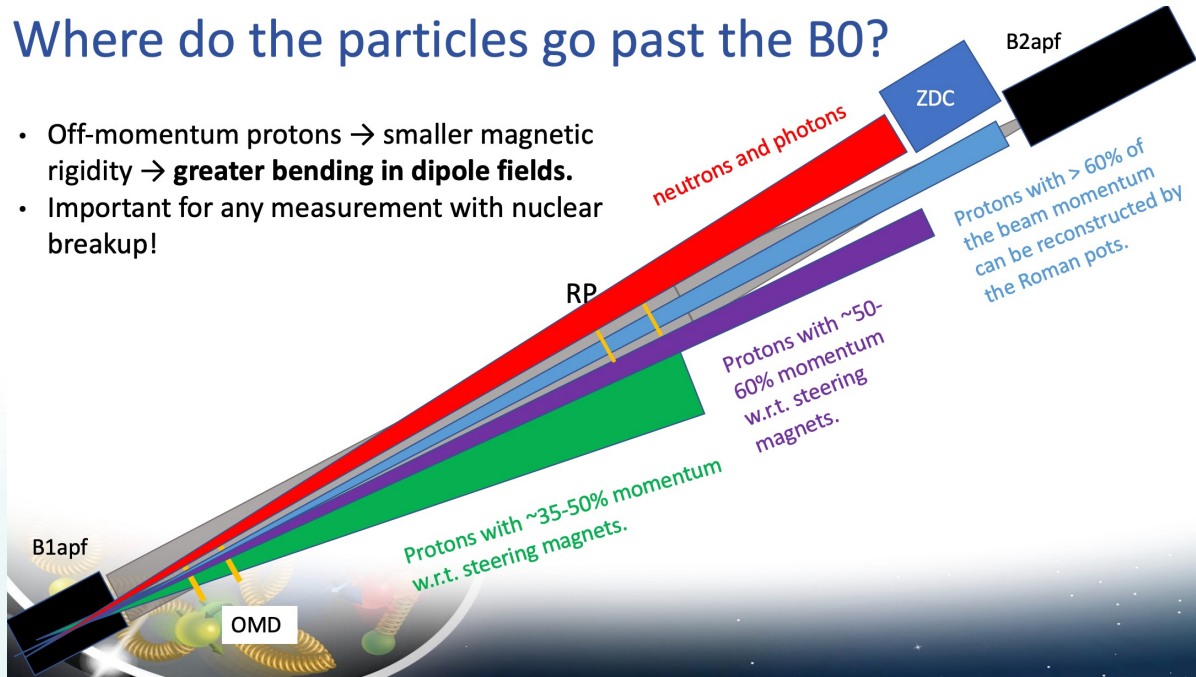
ePIC



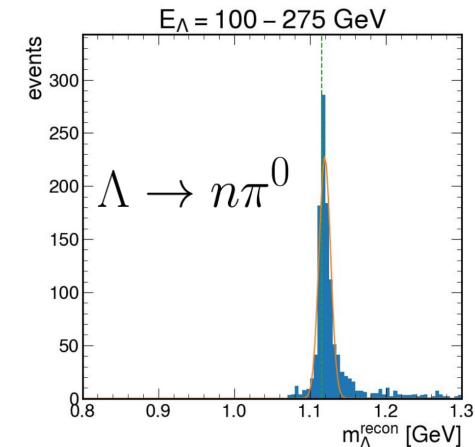
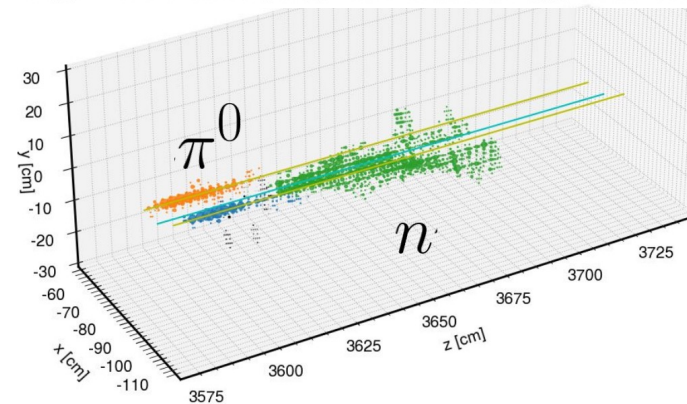
# Far-Forward/Backward

## Where do the particles go past the B0?

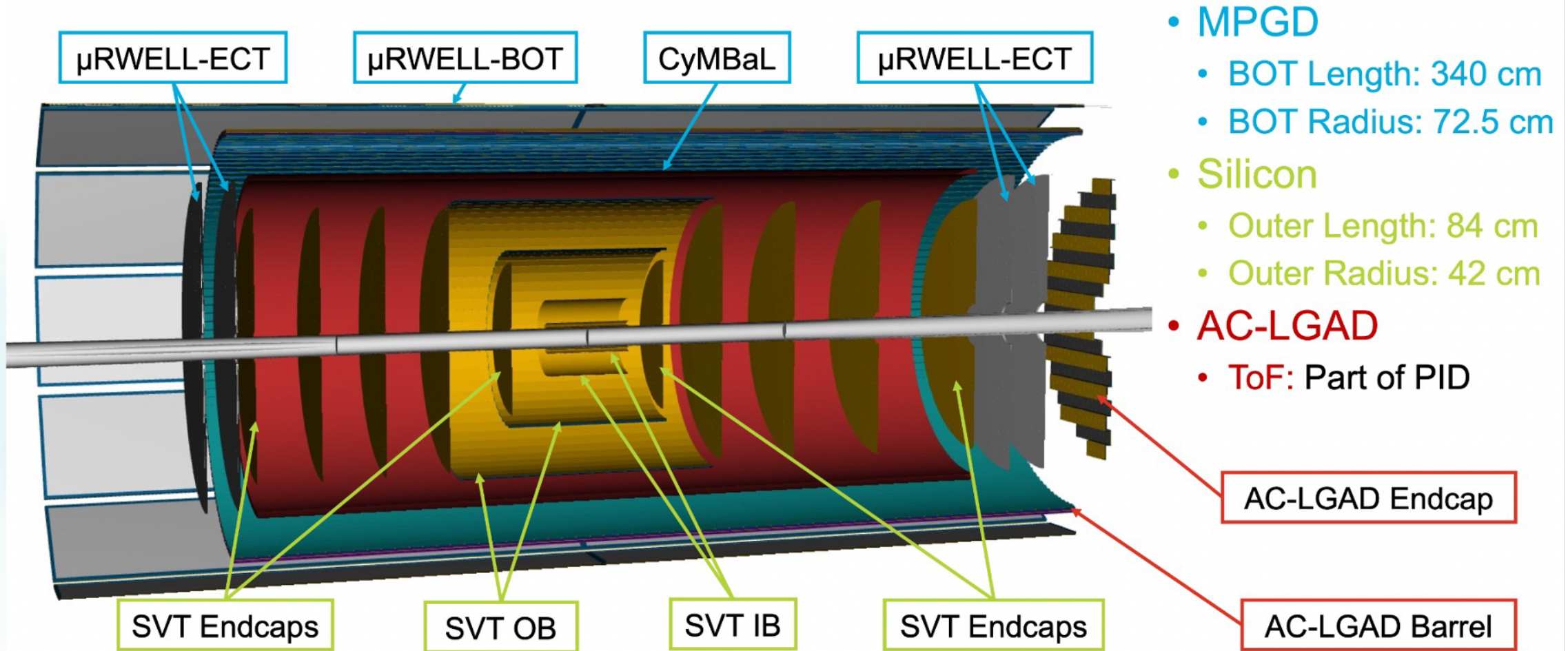
- Off-momentum protons → smaller magnetic rigidity → **greater bending in dipole fields.**
- Important for any measurement with nuclear breakup!



$E_\Lambda = 100$  GeV,  $\theta_\Lambda = 1.1$  mrad,  $z_{vtx} = 19.2$  m



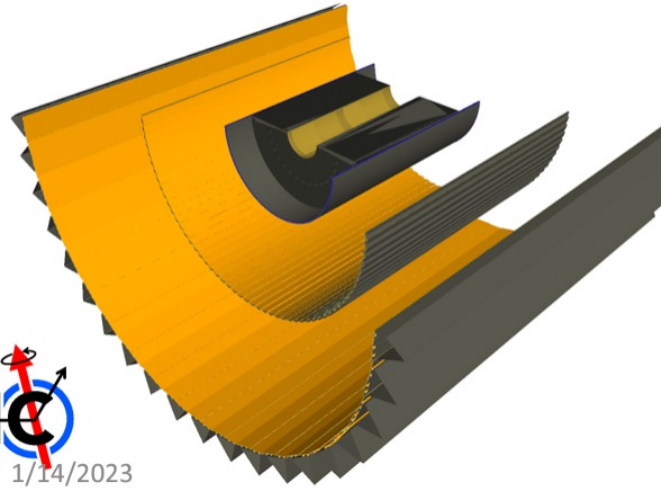
# Tracking



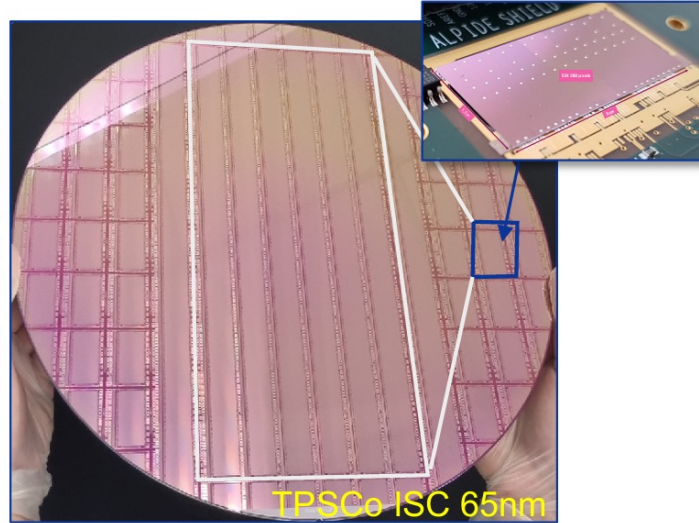
# Tracking : MAPS



1/14/2023



300 mm wafers



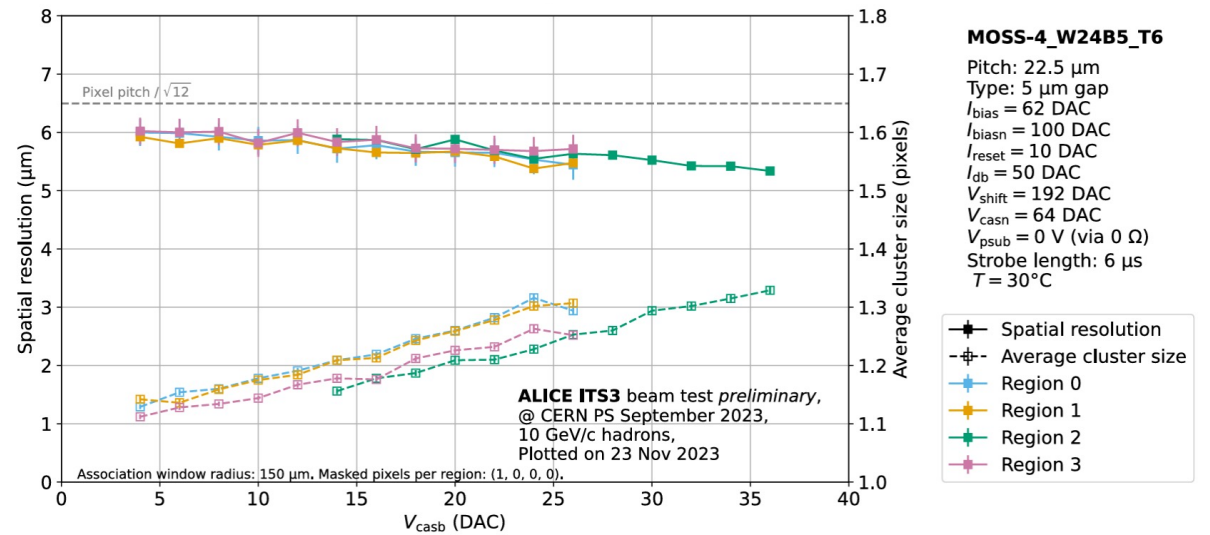
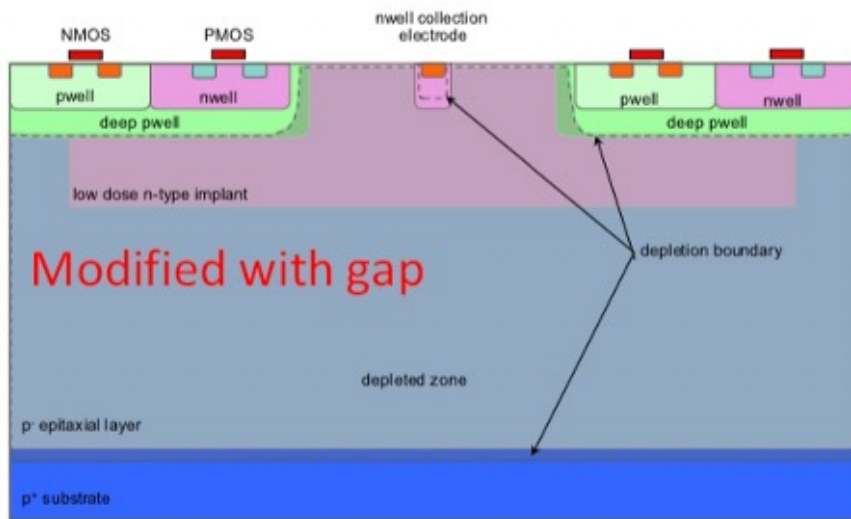
TPSCo ISC 65nm

from reticle-size to wafer-size



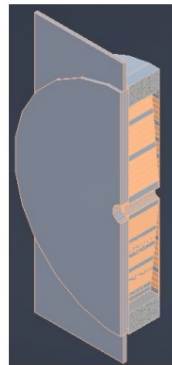
services outside

thin (<50μm CMOS can be curled)

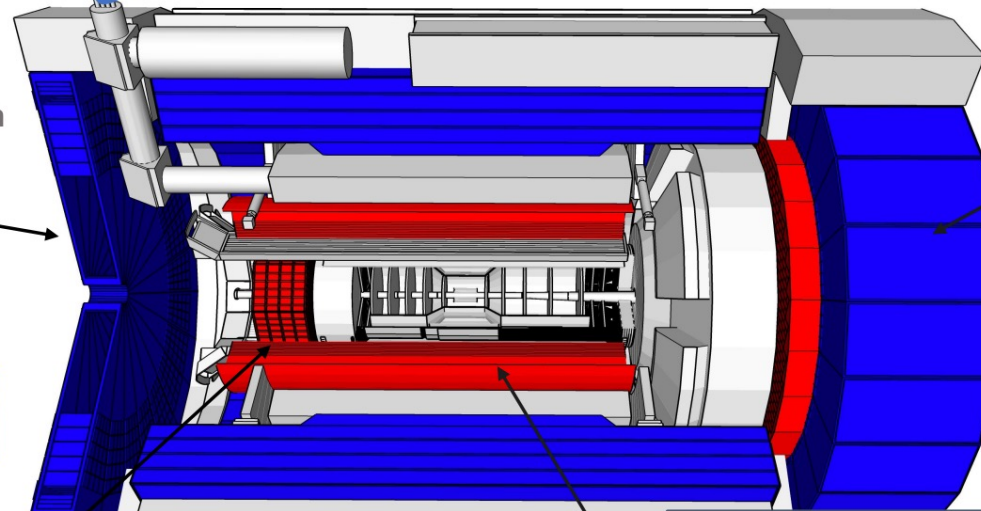


# Calrimeter

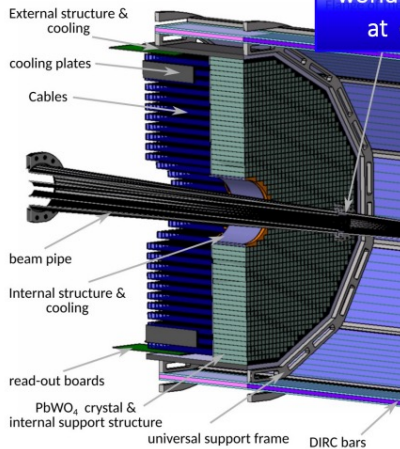
## Calorimetry



Backwards HCAL  
Steel/Sc Sandwich  
tail catcher



world's first  
at ePIC



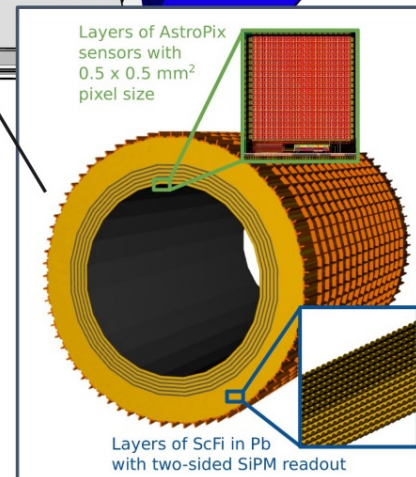
Backwards EMCAL  
PbWO<sub>4</sub> crystals, SiPM  
photosensor

August 4th, 2023

Barrel HCAL  
(sPHENIX re-use)

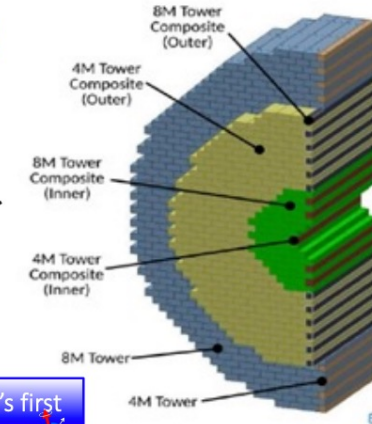


Daniel Brandenburg | ePIC Collaboration



Layers of AstroPix  
sensors with  
0.5 x 0.5 mm<sup>2</sup>  
pixel size

Layers of ScFi in Pb  
with two-sided SiPM readout



world's first  
at ePIC

High granularity  
W/SciFi EMCAL  
Longitudinally separated  
HCAL with high-η insert

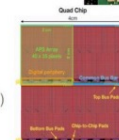
AstroPix v3: Design and Fabrication

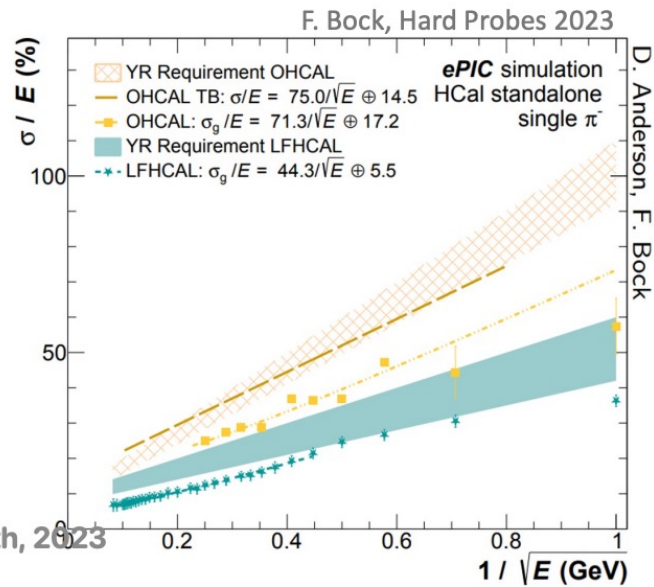
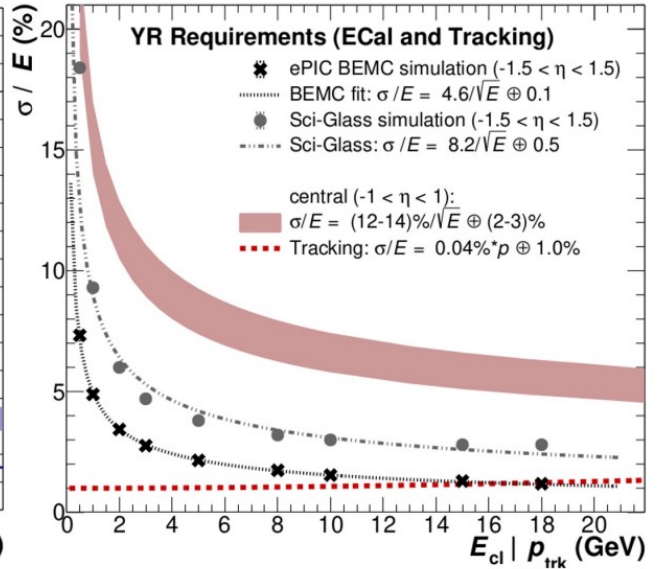
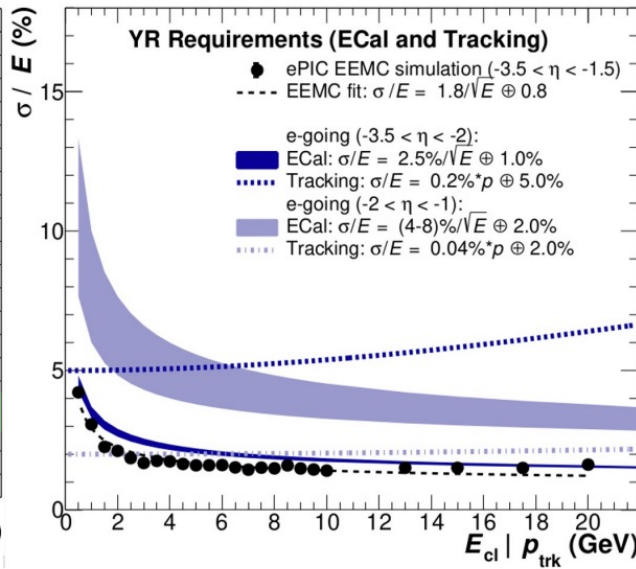
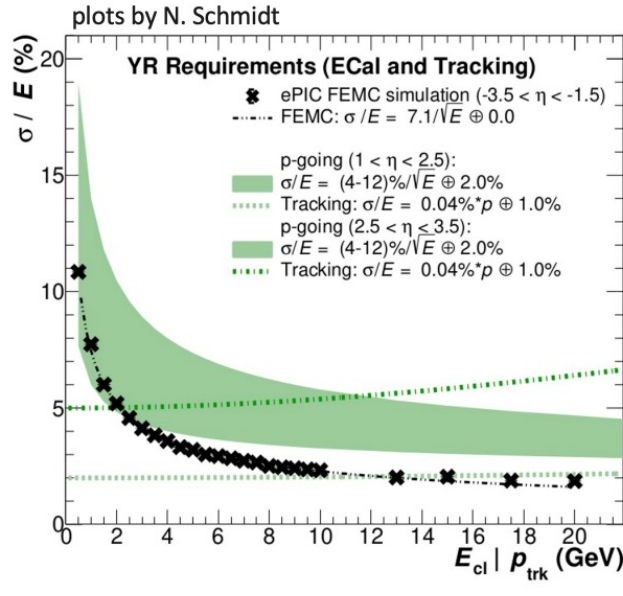
Pixel Matrix:

- 500μm<sup>2</sup> Pixel Pitch, 300μm<sup>2</sup> Pixel Size
- 35 x 35 pixels
- first 3 cols PMOS amplifier others NMOS
- Pixel Comparator Outputs Row/Column OR wired
- Goal:
  - Pixel Dynamic Range 20keV - 700keV
  - Noise Floor 5 keV (2% @ 662keV)

ASTROPiX

world's first  
at ePIC





## Performance on energy resolution and matching

- Technologies fulfill YR requirements on energy resolution
- Ongoing simulation studies related to overlaps between different  $\eta$  regions for calorimetry and reconstruction algorithms

## Ongoing work on Monte-Carlo validation

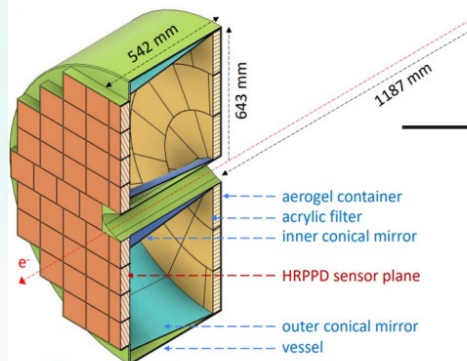
- Validation for high Z absorbers

# Particle identification

## Particle ID

### Proximity Focused (pfRICH)

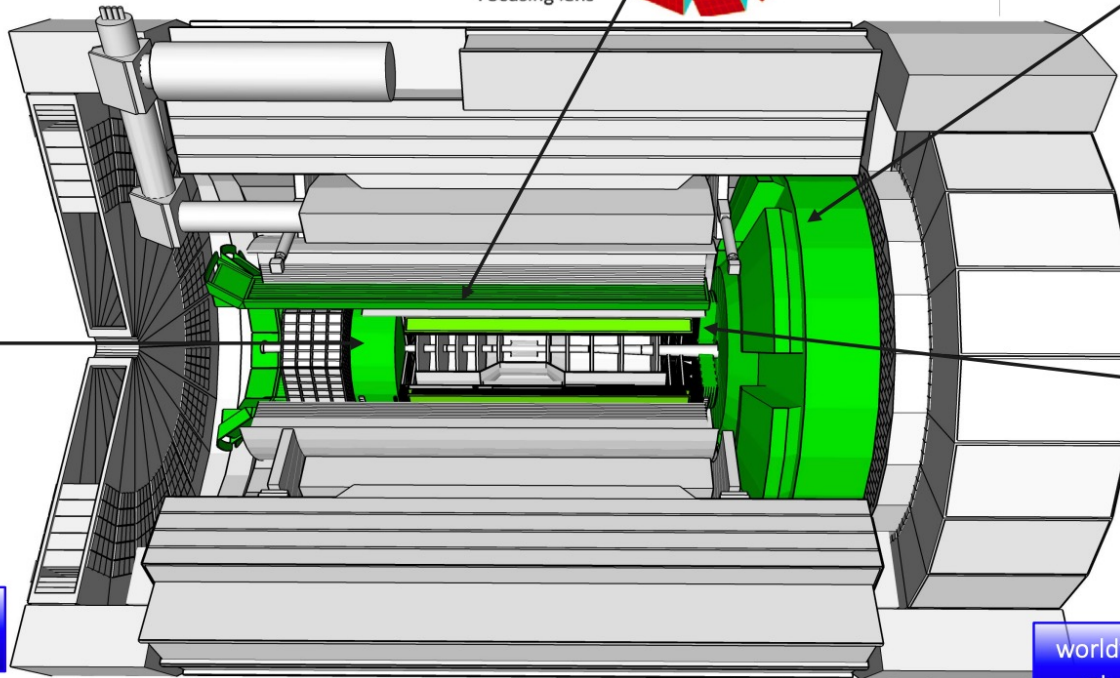
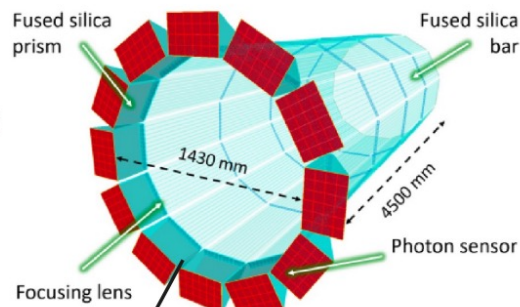
- Long proximity gap (~40 cm)
- Sensor: LAPPDs
- up to 9 GeV/c 36  $\pi$ /K sep.



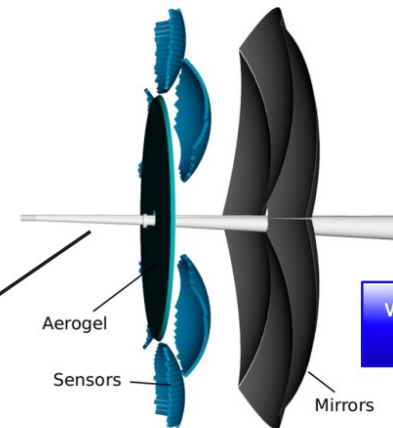
world's first at ePIC

### High-Performance DIRC

- Quartz bar radiator (BaBAR bars)
- light detection with MCP-PMTs
- Fully focused
- $\pi$ /K 3 $\sigma$  separation at 6 GeV/c

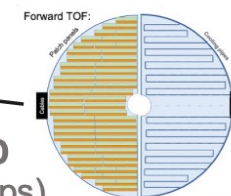


### Dual-Radiator RICH(dRICH)



- C<sub>2</sub>F<sub>6</sub> Gas Volume and Aerogel
- Sensors tiled on spheres (SiPMs)
- $\pi$ /K 3 $\sigma$  sep. at 50 GeV/c

### AC-LGAD TOF (~30ps)



world's first at ePIC

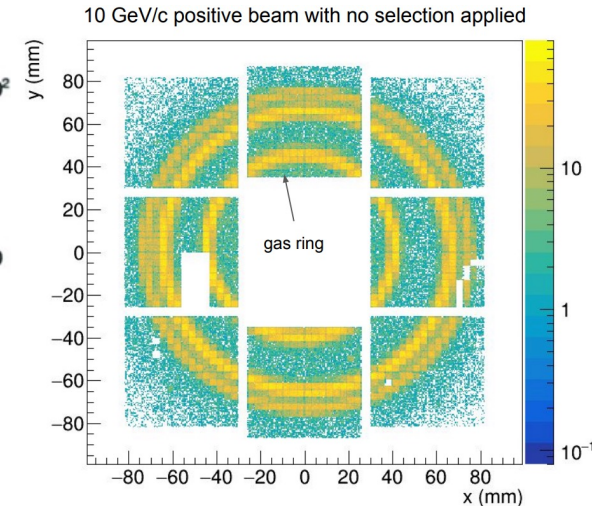
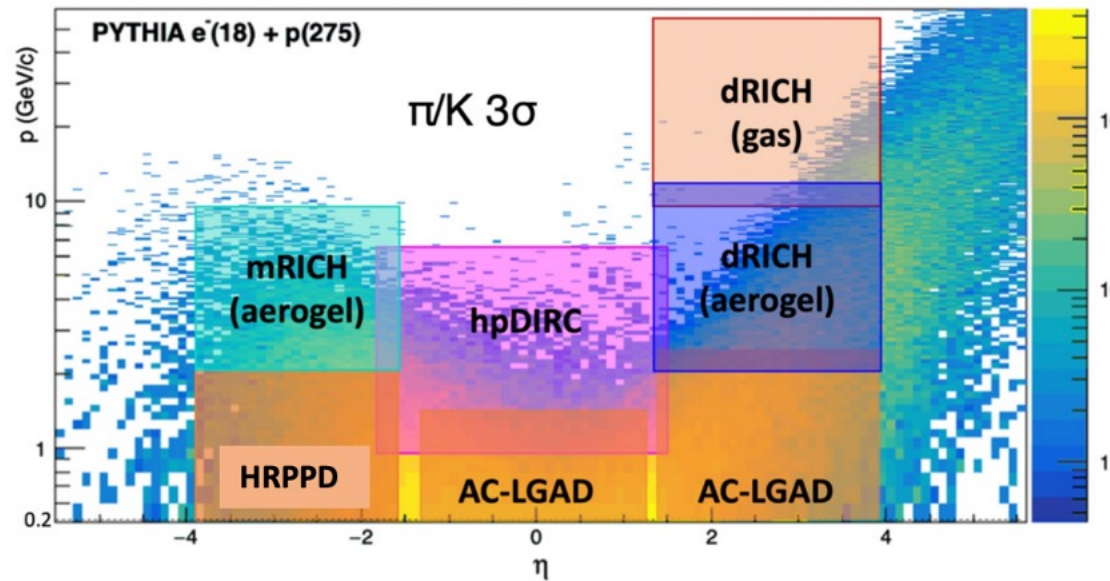
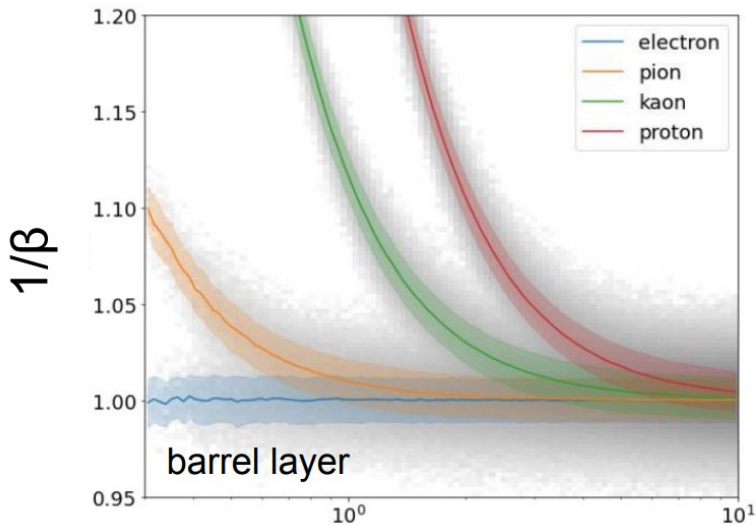
- Accurate space point for tracking forward disk and central barrel

# Particle identification

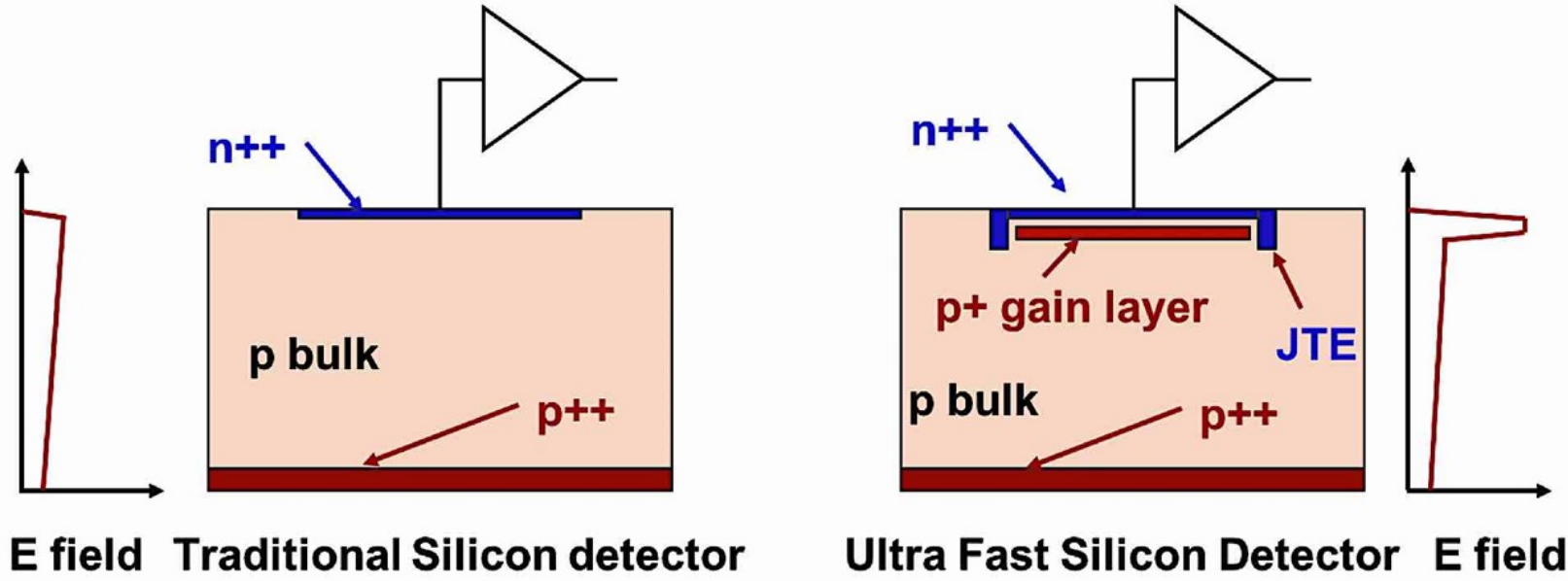
## Particle Identification needs

- Electrons from photons → **4π coverage in tracking**
- Electrons from charged hadrons → **mostly provided by calorimetry and tracking**
- Charged pions, kaons and protons from each other on track level → **Cherenkov detectors**
  - Cherenkov detectors, complemented by ToF

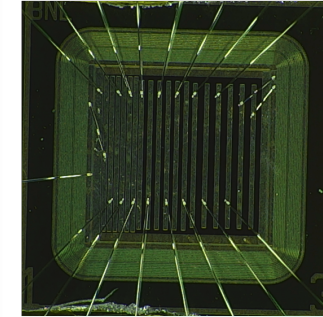
Rapidity	$\pi/K/p$ and $\pi^0/\gamma$	e/h	Min $p_T$ (E)
-3.5 - -1.0	7 GeV/c	18 GeV/c	100 MeV/c
-1.0 - 1.0	8-10 GeV/c	8 GeV/c	100 MeV/c
1.0 - 3.5	50 GeV/c	20 GeV/c	100 MeV/c



# Particle identification : AC-LGAD

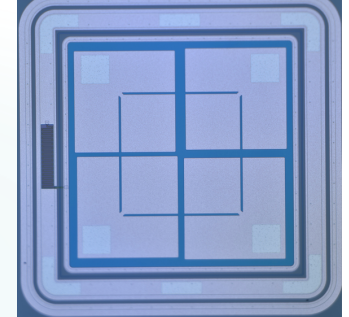


Strip type by BNL      Pad type by HPK



3x3 mm<sup>2</sup>  
Sensor size

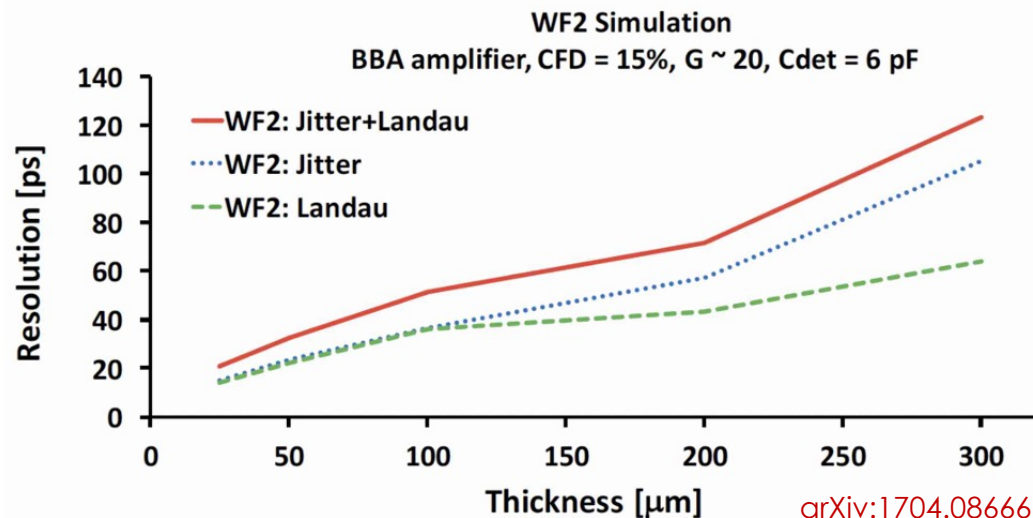
100µm, 150 µm, 200 µm



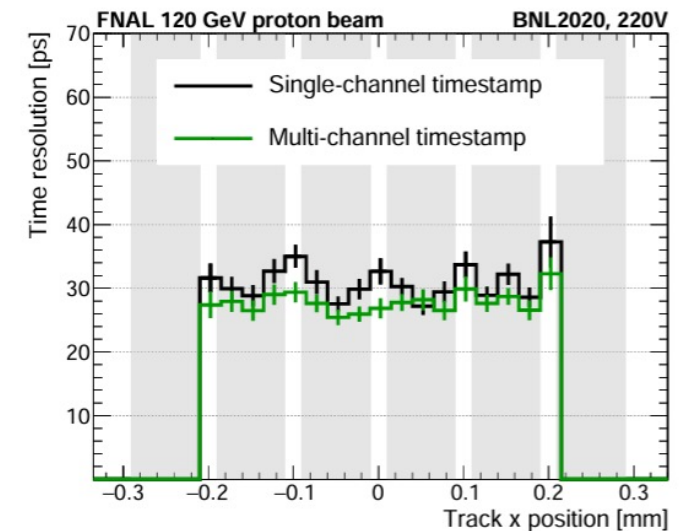
3x3 mm<sup>2</sup>  
Sensor size

Ramo's theorem

$$\frac{di_G}{dt} \propto \frac{G}{d}$$



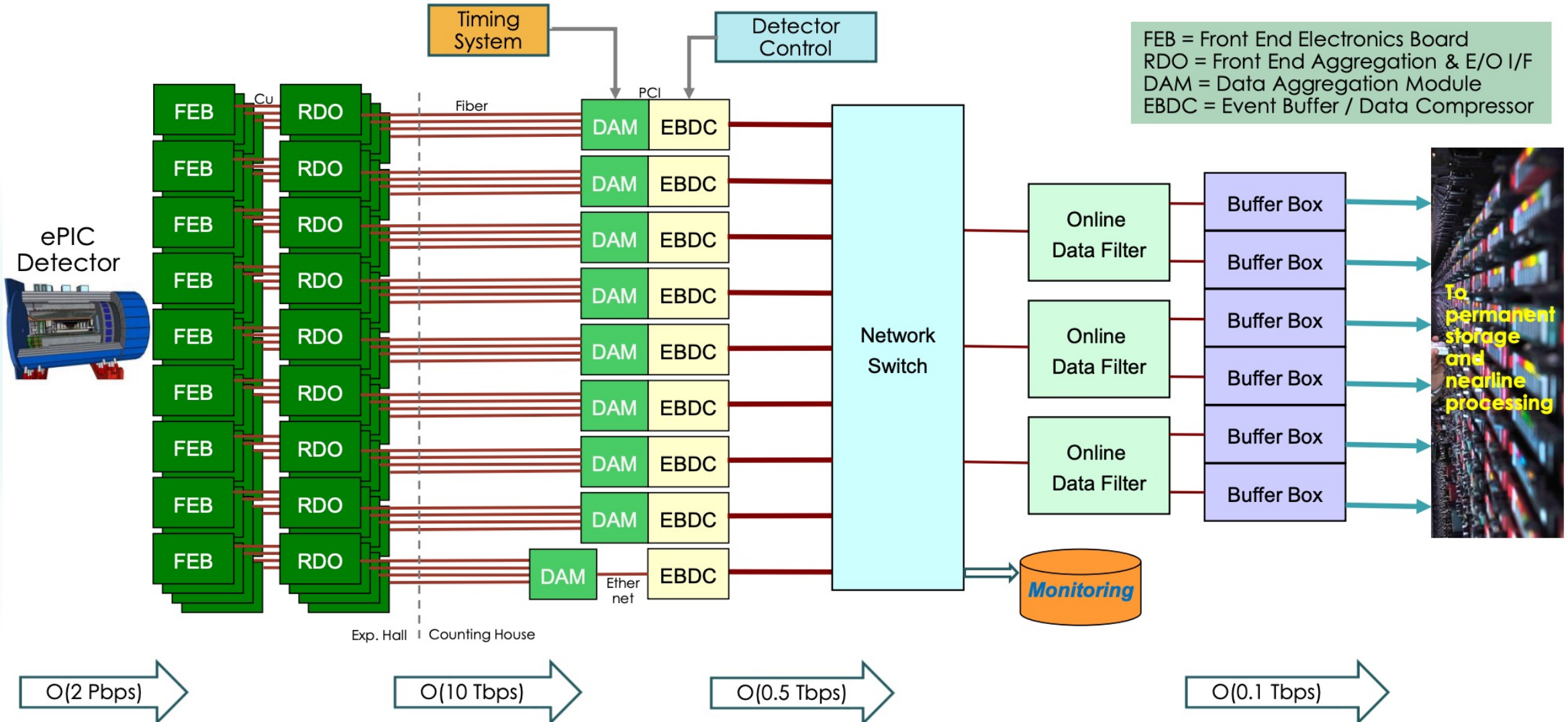
arXiv:1704.08666





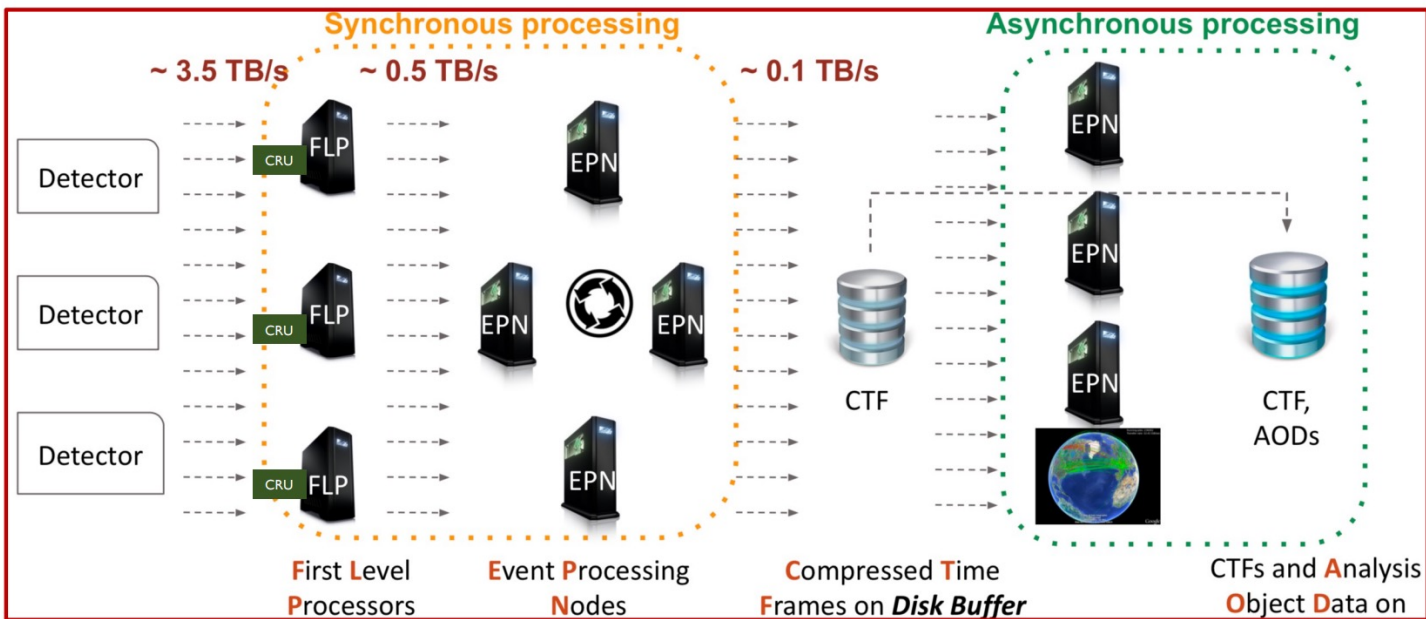
# Streaming DAQ

- No External trigger
- All collision data digitized but aggressively zero suppressed at FEB
- Low / zero deadtime
- Collision data flow is independent and unidirectional-> no global latency requirements
- Avoiding hardware trigger avoids complex custom hardware and firmware
- Data volume is reduced as much as possible at each stage ensuring that biases are controlled
- Integrate AI/ML as close as possible to subdetectors → cognizant Detector

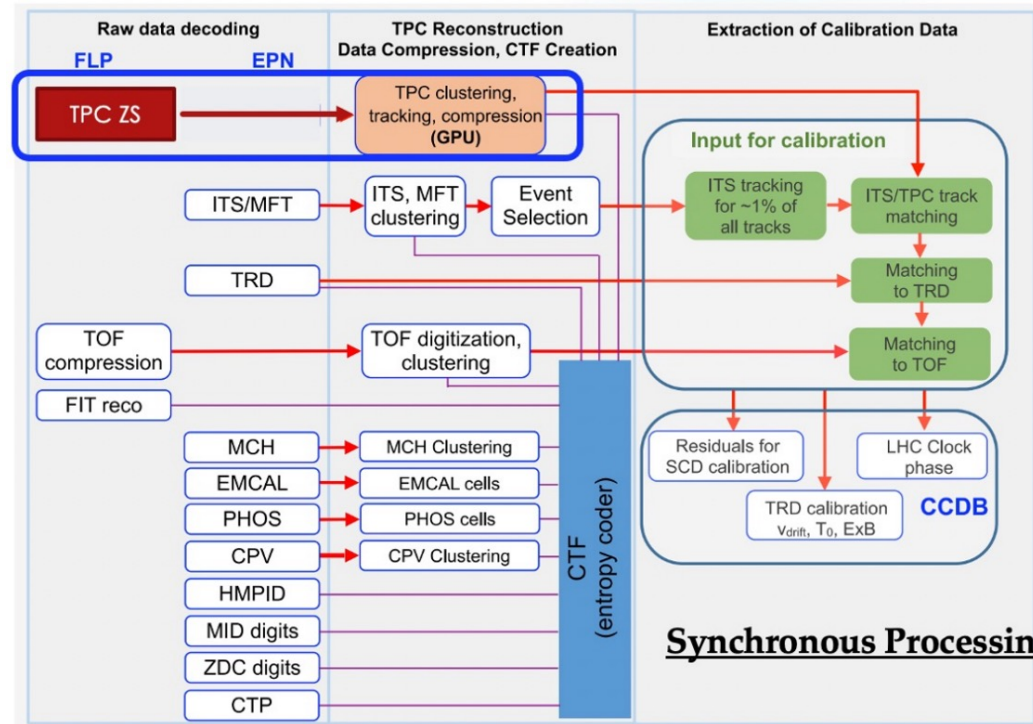


# Streaming DAQ : ALICE case

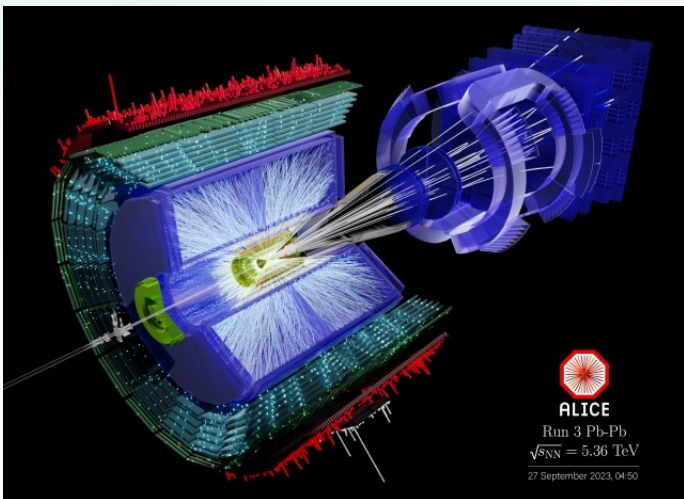
130



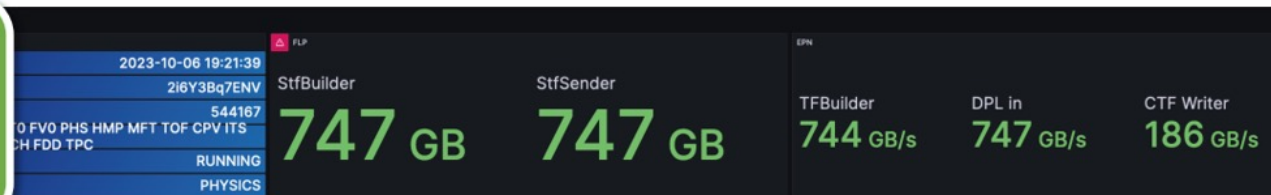
Synchronous processing of TFDData in EPN (250 EPNs, 2000 GPUs)



**Synchronous Processing**



15 detectors  
Data Volume as predicted  
Acquisition with 364  
equivalent MI50 EPNs

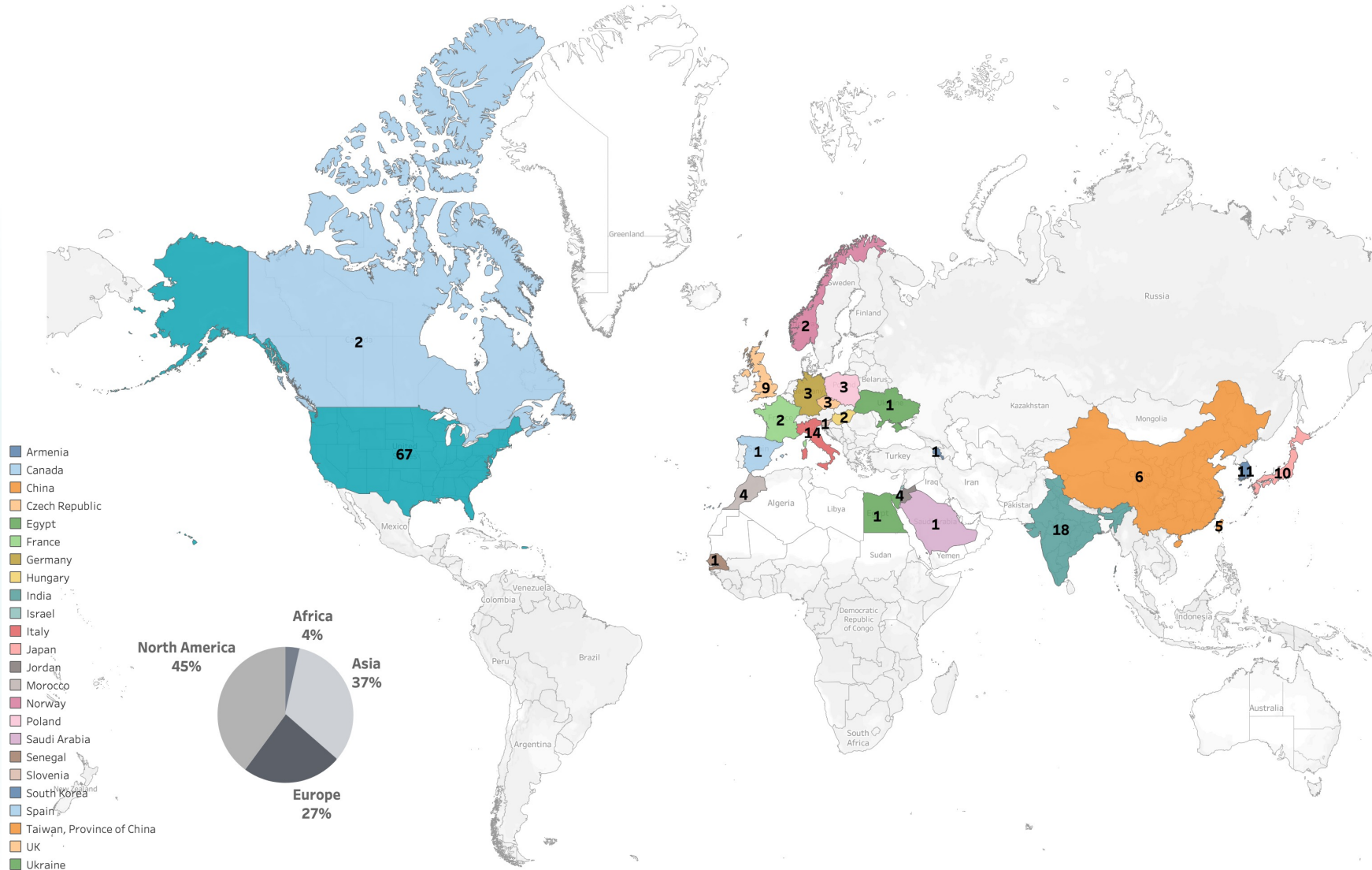


# Japanese Institutes in ePIC

ePIC Institutions  
173

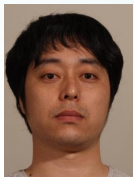
ePIC Countries  
25

ePIC World Region  
4

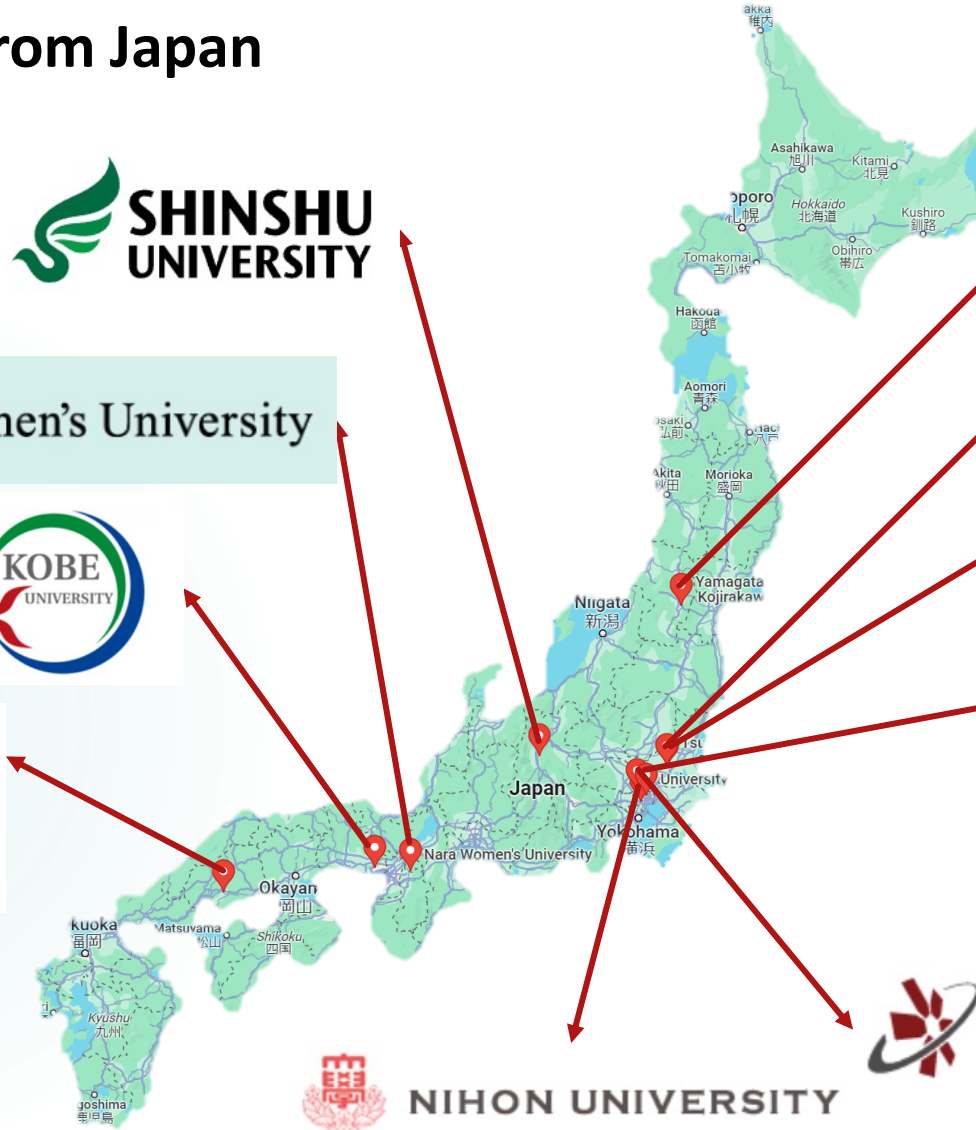


# Japanese Institutes in ePIC

▶ 10 institutes from Japan



S. Yano, TOF-DSC



T. Gunji, Executive Board member

Y. Goto, ZDC DSTC



# Japanese Institutes in ePIC

133

- ▶ Japanese team consists of the institutes with different research backgrounds

**Nucleon structure**  
(COMPASS/AMBER, RHIC, SeaQuest, SpinQuest)



**High-Energy particle physics**  
(ZEUS@HERA, ATLAS@LHC)



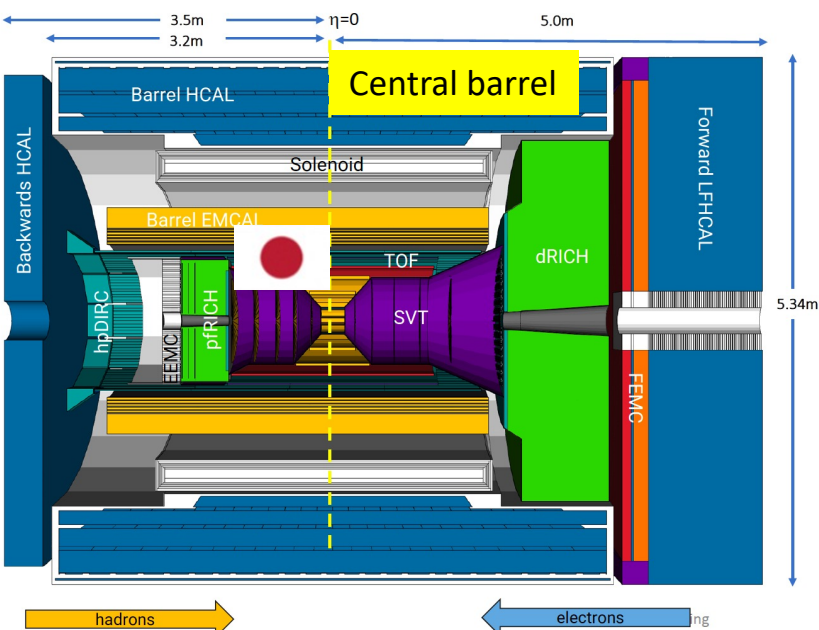
**Heavy-Ion Physics**  
((s)PHENIX@RHIC, ALICE@LHC)



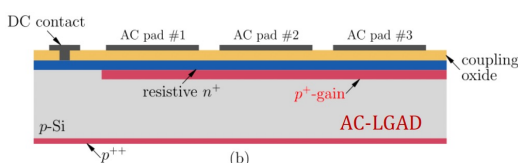
# Japanese contributions

## Japanese contributions

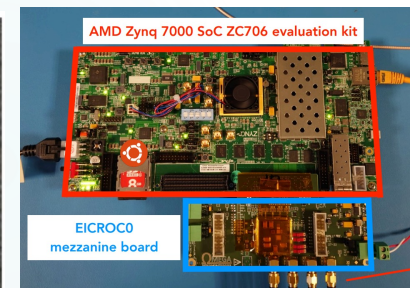
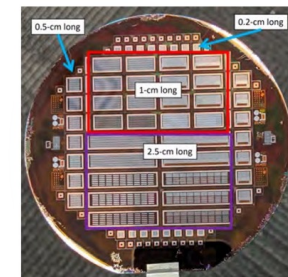
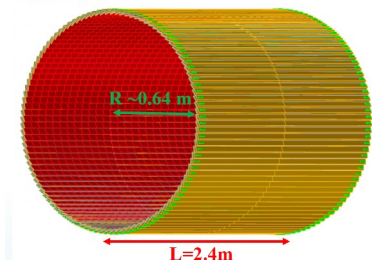
- Barrel AC-LGAD TOF and ZDC R&D and construction
- Streaming DAQ and online data filter



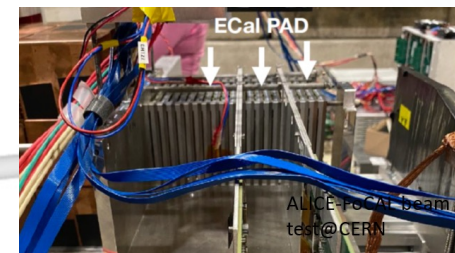
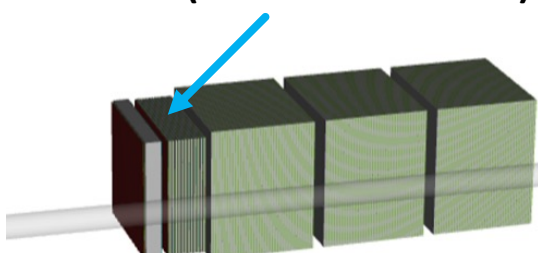
### AC-LGAD R&D



Barrel TOF:



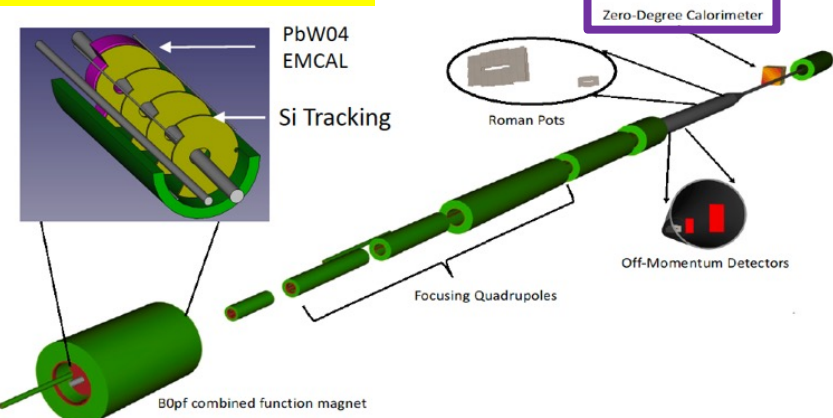
### ZDC R&D (W+Si ALICE-FoCAL)



### Neutron tests at RIKEN

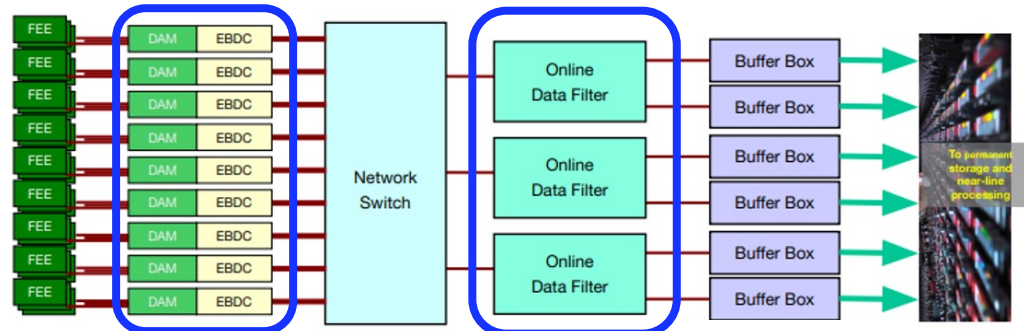
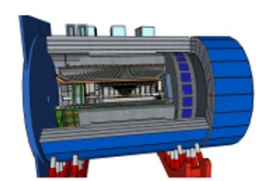


### Far-Forward (h-going)



Streaming DAQ  
online data filter by  
FPGA/GPU/CPU

In collaboration with  
SPADI-Alliance in Japan



- ▶ EICは多くの発見と他分野へ多くの波及をもたらす可能性がある
- ▶ **しかしながら、TMDやGPDをはじめ、EICの物理は難しい...**
- ▶ **定期的に勉強会を開いて、一緒に勉強しませんか？**
- ▶ EICに興味のある人、[eic-japan@ml.riken.jp](mailto:eic-japan@ml.riken.jp)に参加しませんか？
  - ▶ 郡司([gunji@cns.s.u-tokyo.ac.jp](mailto:gunji@cns.s.u-tokyo.ac.jp))と後藤([goto@bnl.gov](mailto:goto@bnl.gov))まで連絡をください
- ▶ EICを契機にして、**クォーク・グルーオン～原子核～原子・分子～生命～宇宙を繋ぎ、クォーク物理・原子核物理・物性物理を融合する「マルチスケール基礎量子科学」を振興したい**
  - ▶ 階層を超えた普遍性の探求、分野を超えた知見を取り入れる
  - ▶ どの階層に進んでも戦える力をつける。多様なキャリアパスの実現。