

Study of the QCD Phase Structure

- Recent Results from RHIC BES Program

Nu Xu

Outline

1) Introduction

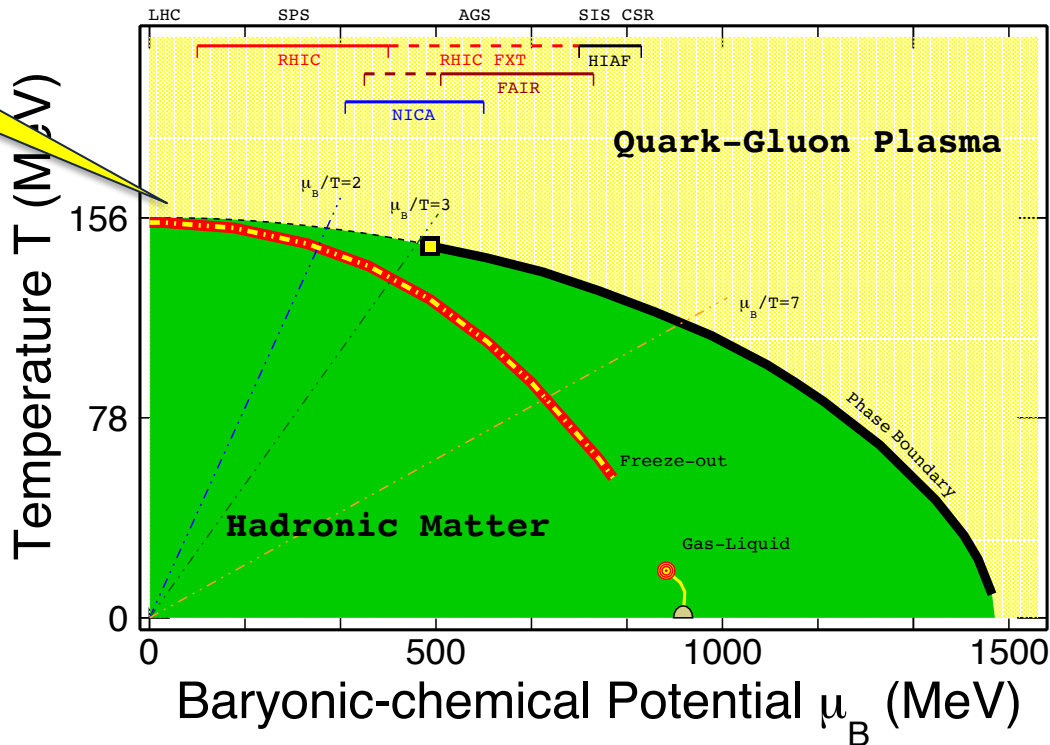
2) Selected Results

- Collectivity
- Baryon Correlations and Hyper-Nuclei Productions
- Criticality from BES-II (collider energy $7.7 \leq \sqrt{s_{NN}} \leq 27 \text{ GeV}$)

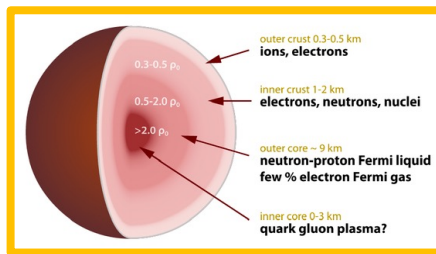
3) Summary and Outlook

Nuclear Collisions and QCD Phase Diagram

Early Universe



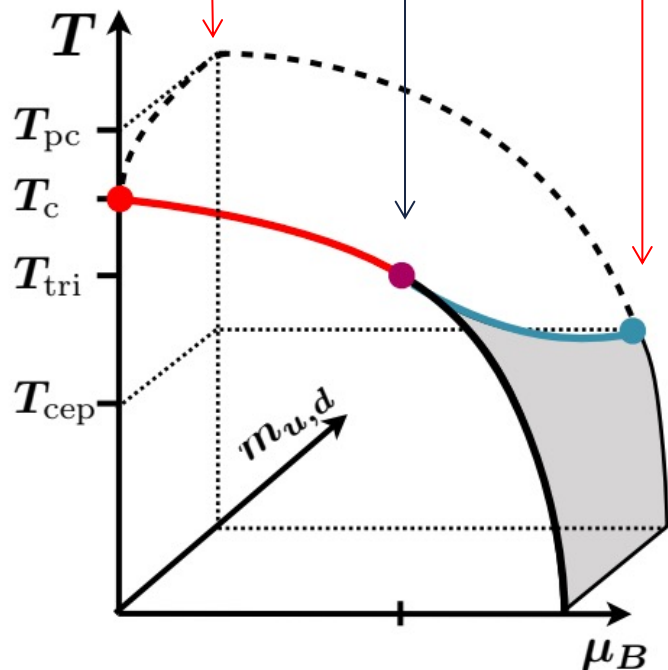
High baryon density:
Inner structure of compact stars



- 1) RHIC BES: → search for 1st-order phase transition and **QCD critical point**;
- 2) Baryon interactions (e.g. $N - N$, $Y - N$) → inner structure of compact stars

LGT: QCD Phase Structure

T_C^0 T_{PC} T^{TC} T^{CEP}



F. Karsch *et al.*, 2020

1) QCD transition temperature:

$$T_{PC} = 156.5 \pm 1.5 \text{ MeV}$$

2) Chiral crossover line

$$T_{PC}(\mu_B) = T_{PC}^0 \left[1 - \kappa_2 \left(\frac{\mu_B}{T_{PC}^0} \right)^2 - \kappa_4 \left(\frac{\mu_B}{T_{PC}^0} \right)^4 \right]$$

$$\kappa_2 = 0.012(4), \quad \kappa_4 = 0.00(4)$$

3) Chiral transition temperature:

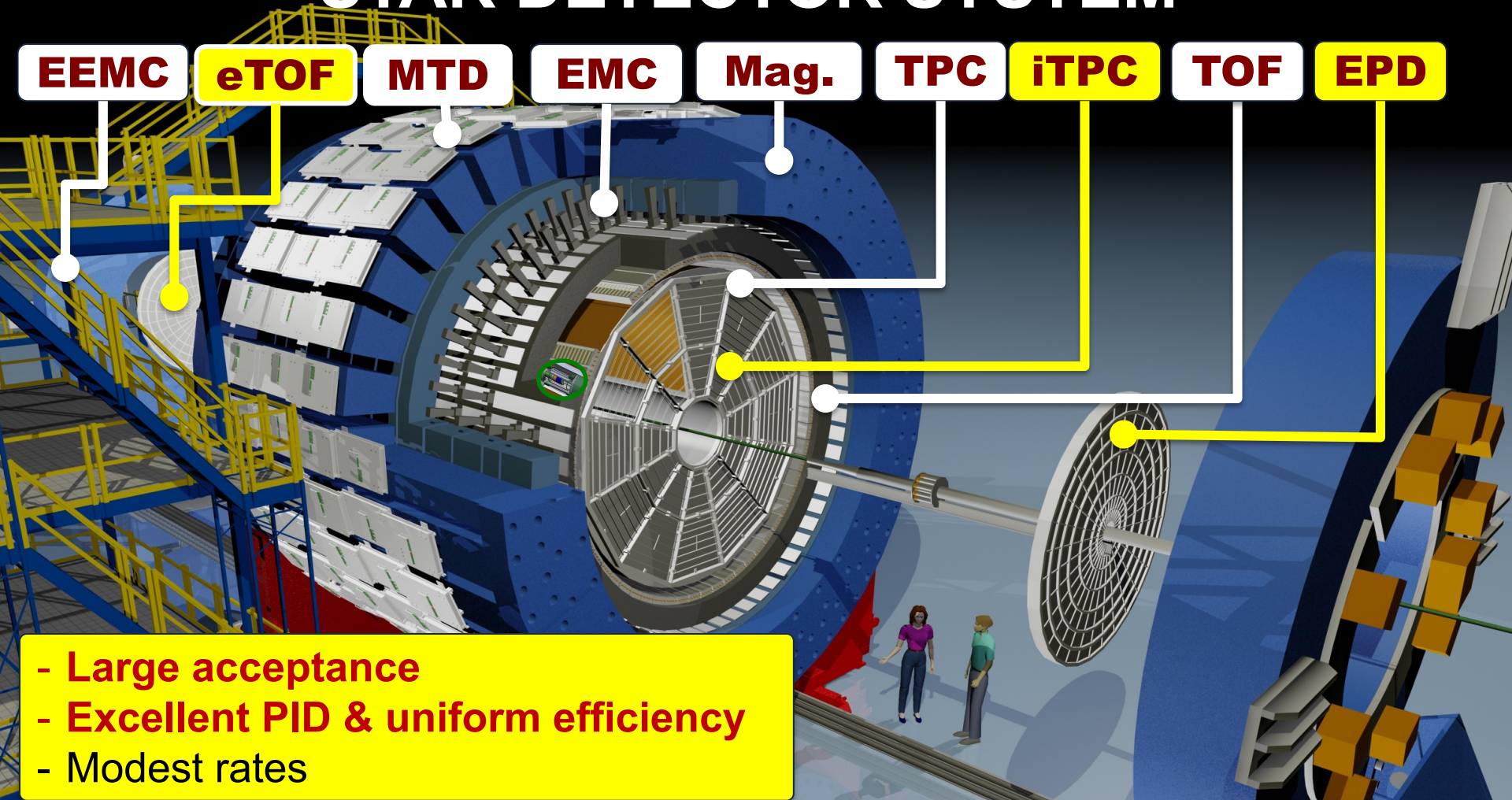
$$T_C = 132_{-6}^{+3} \text{ MeV}$$

4) QCD critical end point:

$$T^{CEP} < T_C, \quad \mu_B^{CEP} \gtrsim 3T_C$$

HotQCD: Phys.Lett.**B795**, 15(2019);
Phys. Rev. Lett. **123**, 062002(2019)

STAR DETECTOR SYSTEM



EEMC

eTOF

MTD

EMC

Mag.

TPC

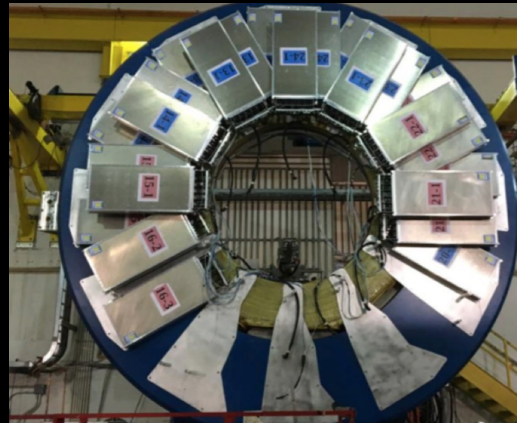
iTPC

TOF

EPD

- Large acceptance
- Excellent PID & uniform efficiency
- Modest rates

Major Upgrades for BES-II



iTPC:

- Improves dE/dx
- Extends η coverage from 1.0 to 1.6
- Lowers p_T cut-in from 125 to 60 MeV/c
- Ready in 2019

eTOF:

- Forward rapidity coverage
- PID at $\eta = 0.9$ to 1.6
- **Borrowed from CBM-FAIR**
- Ready in 2019

EPD:

- Improves trigger
- Better centrality & event plane measurements
- Ready in 2018

- 1) Enlarge rapidity acceptance
- 2) Improve particle identification
- 3) Enhance centrality/event plane resolution

iTPC: <https://drupal.star.bnl.gov/STAR/starnotes/public/sn0619>
eTOF: STAR and CBM eTOF group, arXiv: 1609.05102
EPD: J. Adams, et al. NIM [A968](#), 163970 (2020)

STAR BES Data Sets

Au+Au Collisions at RHIC											
Collider Runs						Fixed-Target Runs					
	$\sqrt{s_{NN}}$ (GeV)	#Events	μ_B	y_{beam}	run		$\sqrt{s_{NN}}$ (GeV)	#Events	μ_B	y_{beam}	run
1	200	380 M	25 MeV	5.3	Run-10, 19	1	13.7 (100)	50 M	280 MeV	-2.69	Run-21
2	62.4	46 M	75 MeV		Run-10	2	11.5 (70)	50 M	320 MeV	-2.51	Run-21
3	54.4	1200 M	85 MeV		Run-17	3	9.2 (44.5)	50 M	370 MeV	-2.28	Run-21
4	39	86 M	112 MeV		Run-10	4	7.7 (31.2)	260 M	420 MeV	-2.1	Run-18, 19, 20
5	27	585 M / 220	156 MeV	3.36	Run-11, 18	5	7.2 (26.5)	470 M	440 MeV	-2.02	Run-18, 20
6	19.6	595 M / 270 M	206 MeV	3.1	Run-11, 19	6	6.2 (19.5)	120 M	490 MeV	1.87	Run-20
7	17.3	256 M / 116 M	230 MeV		Run-21	7	5.2 (13.5)	100 M	540 MeV	-1.68	Run-20
8	14.6	340 M / 145 M	262 MeV		Run-14, 19	8	4.5 (9.8)	110 M	590 MeV	1.52	Run-20
9	11.5	257 M / 110 M	316 MeV		Run-10, 20	9	3.9 (7.3)	120 M	633 MeV	-1.37	Run-20
10	9.2	160 M / 78 M	372 MeV		Run-10, 20	10	3.5 (5.75)	120 M	670 MeV	-1.2	Run-20
11	7.7	104 M / 45 M	420 MeV		Run-21	11	3.2 (4.59)	200 M	699 MeV	-1.13	Run-19
						12	3.0 (3.85)	260 + 2000 M	760 MeV	-1.05	Run-18, 21

Most precise data to map the QCD phase diagram

$$3 < \sqrt{s_{NN}} < 200 \text{ GeV}; \quad 760 > \mu_B > 25 \text{ MeV}$$

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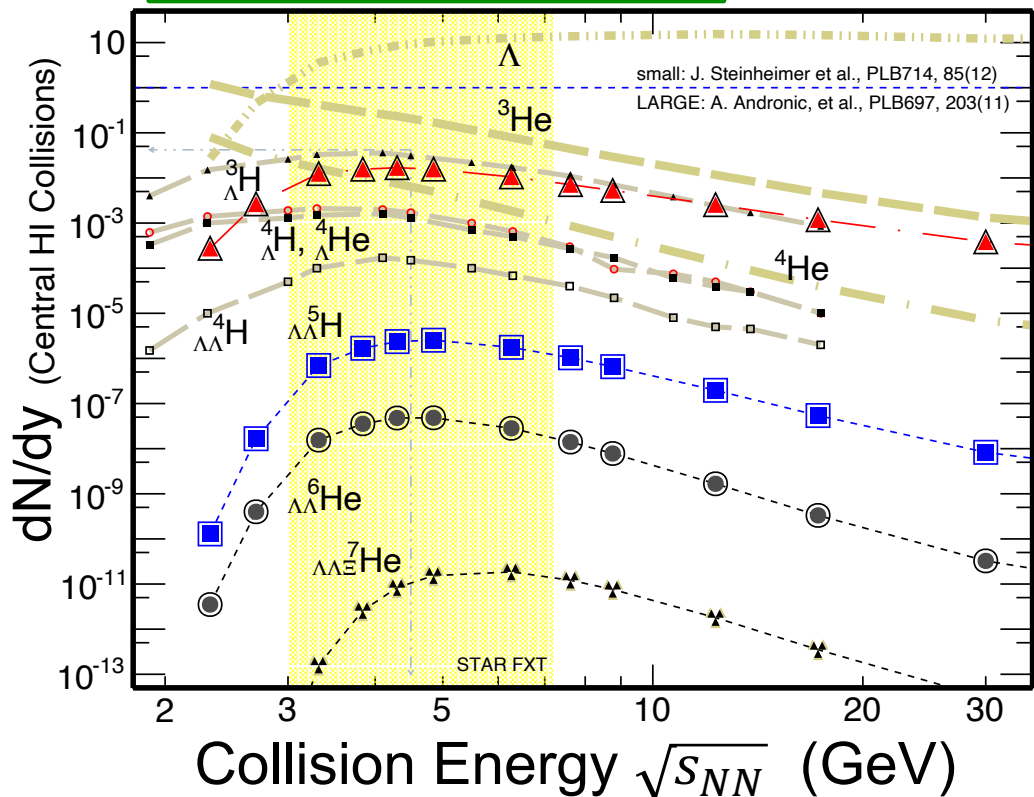
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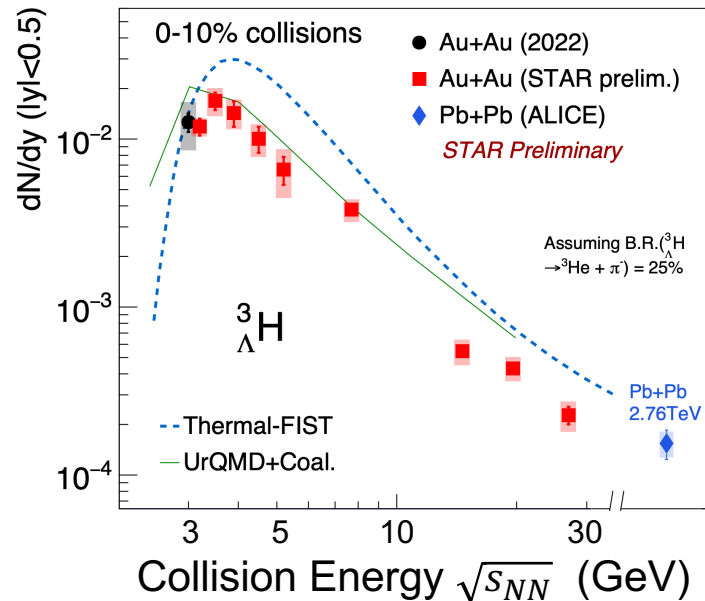
3) Summary and Outlook

STAR FXT and High Baryon Density Region

A. Andronic *et al.* PLB697, 203(2011);
J. Steinheimer *et al.* PLB714, 85(2012)



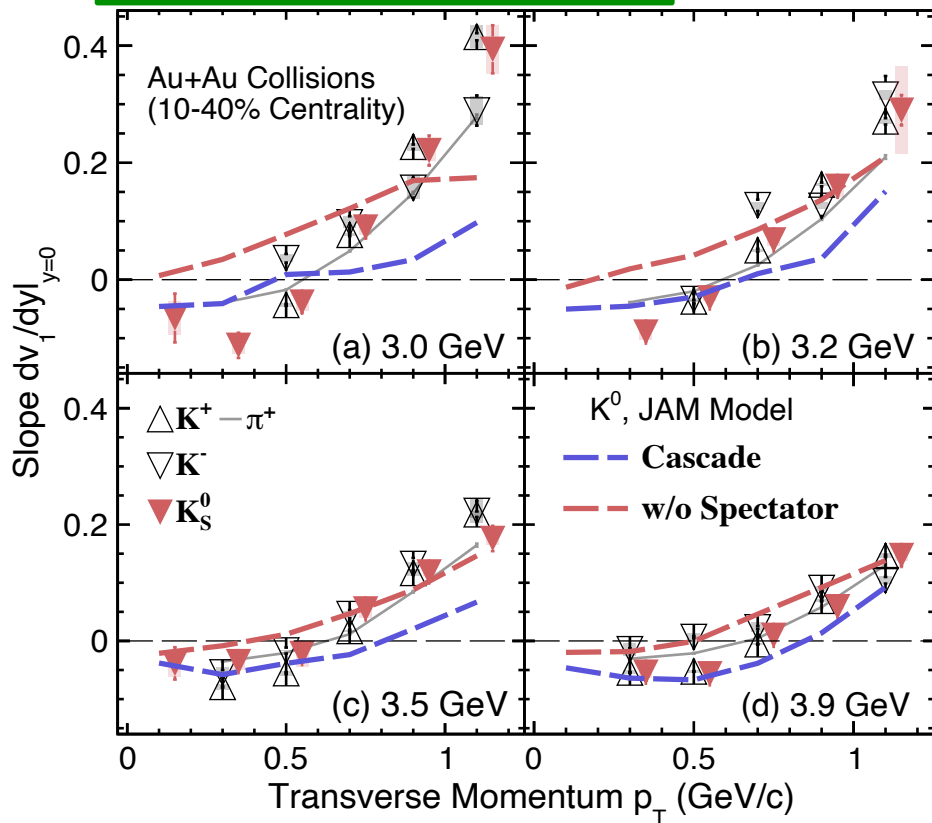
STAR: CPOD2024, SQM2024



- 1) Hypernucleus: ${}^3_{\Lambda}\text{H}$ yields versus energy: peaks at 3.2 GeV;
- 2) For $\sqrt{s_{NN}} < 10$ GeV, calculations from coalescence more consistent with data

Kaon Anti-Flow at High Baryon Density Region

STAR: CPOD2024, SQM2024



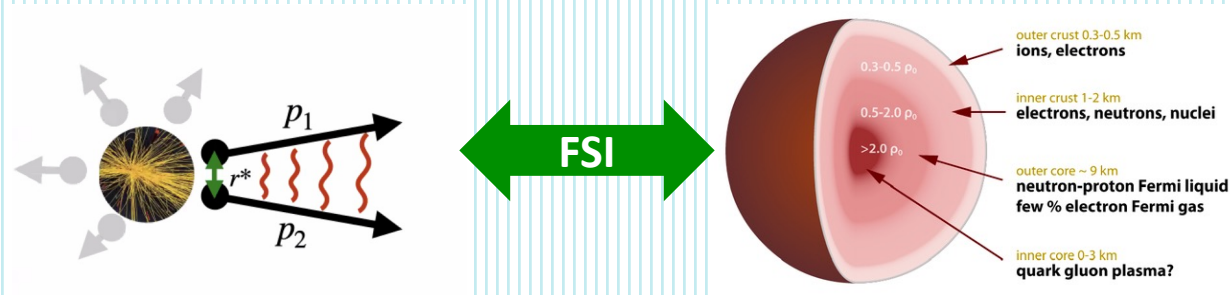
- 1) A systematic analysis of the p_T dependence of the neutral- and charged-Kaon v_1 from Au+Au collisions at $\sqrt{s_{NN}} = 3.0 - 3.9$ GeV;
- 2) At $p_T < 0.6$ GeV, all mid-rapidity v_1 slopes are negative. Kaon potential was proposed to explain the data, ref.[1,2];
- 3) JAM model calculations suggest that spectator shadowing, similar to the case of elliptical v_2 , plays important role for the negative v_1 slope parameter.

→ **Spectator shadowing**
 → **No Kaon potential is needed**

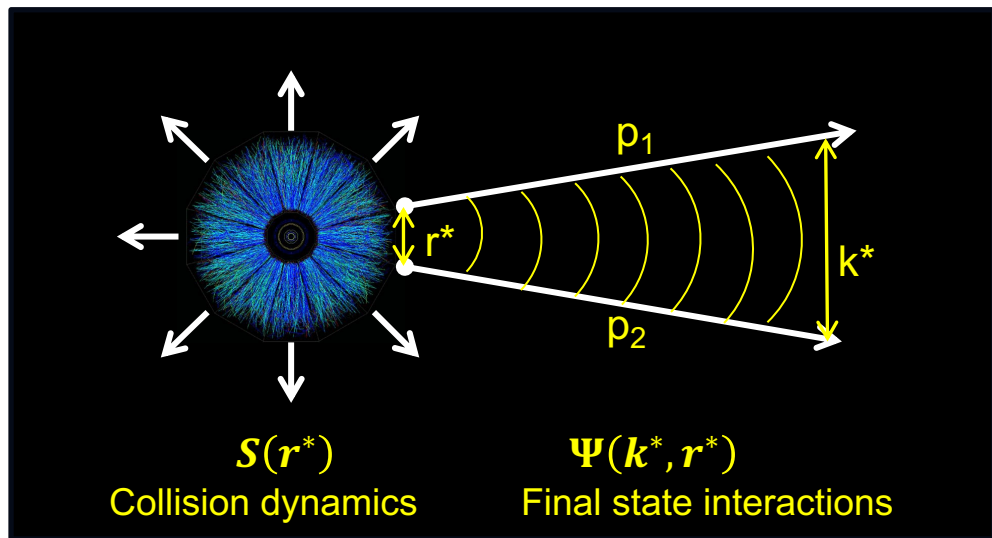
References:

- (1) P. Chung *et al.* (E895), PRL **85**, 940(2000);
- (2) G.-Q. Li, C. M. Ko, and B.-A. Li, PRL **74**, 235 (1995) and S. Pal, C. M. Ko, Z.-W. Lin, and B. Zhang, PR **C62**, 061903(2000)

Baryon Correlations



Baryon Correlation Functions



STAR:

(1) Meson HBT: $\pi - \pi$, $K - K$;

(2) Baryon Correlations:

$p - p$	reference	
$p - \Lambda$, $p - \Xi^-$, $p - \Omega$	Y-N	
$p - \phi$		
$\Lambda - \Lambda$	Y-Y	
$p - d$, $d - d$	N-N-N	
$d - \Lambda$	Y-N-N	

Source

$$C_{the}(k^*) = \frac{1}{4\pi} \int d^3 r^* S(r^*) |\Psi(r^*, k^*)|^2$$

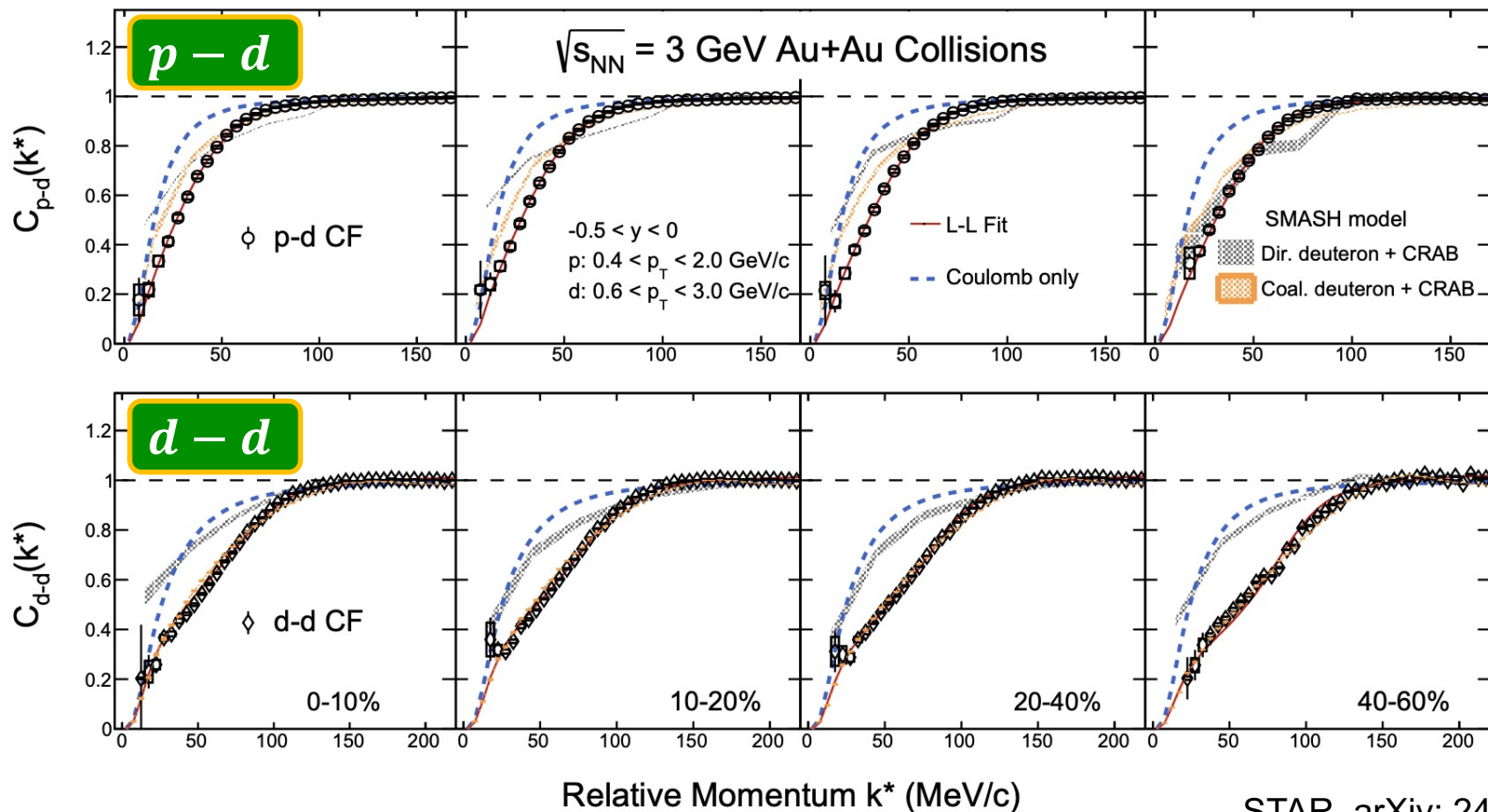
$$k^* = \frac{1}{2} |p_1^* - p_2^*|$$

$$C_{exp}(k^*) = \lambda \frac{N_{same}(p_1, p_2)}{N(p_1)N(p_2)} \rightarrow \text{Source and FSI}$$

Final State Interactions:

(1) Quantum statistics; (2) Coulomb; (3) Strong interaction

$p - d, d - d$ Correlation Functions

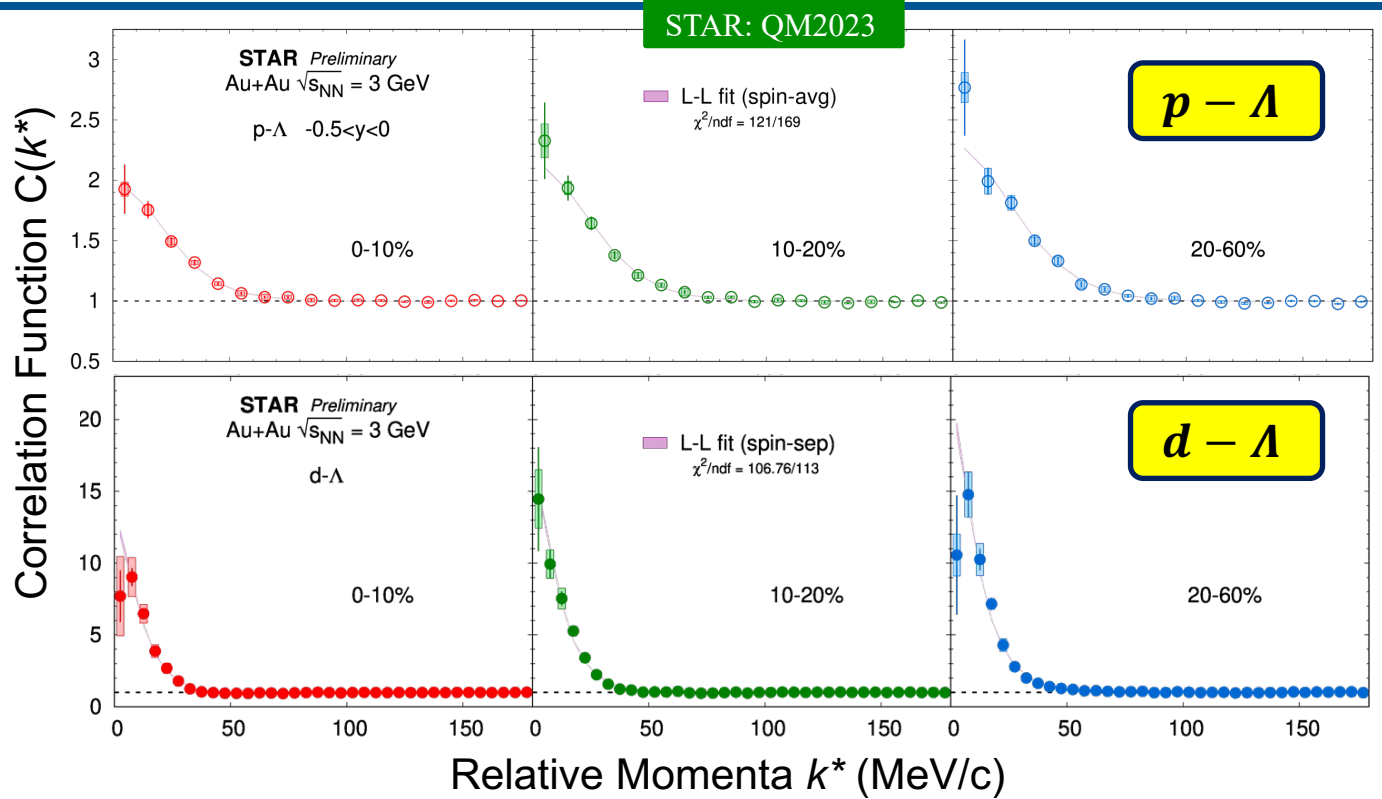


STAR, arXiv: 2410.03436

$p - d$, $d - d$ Correlation Functions

- 1) Both $p - d$ and $d - d$ CFs can be reproduced by calculations of transport model (SMASH) plus coalescence after-burner. Consistent with the coalescence procedure for deuteron production;
- 2) LL calculations are used to extract FSI parameters:
 - $f_0 < 0$ is observed
 - *no collision centrality dependence is observed*

$p - \Lambda$, $d - \Lambda$ Correlation Functions



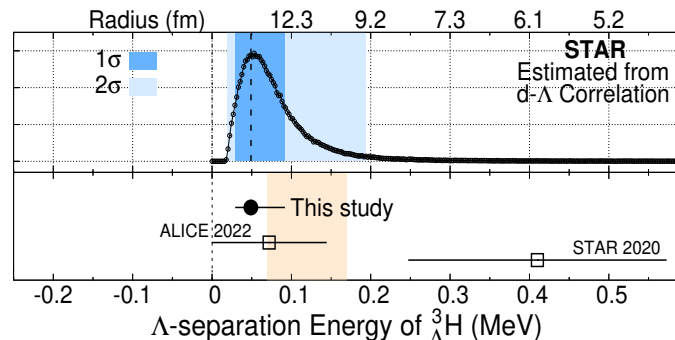
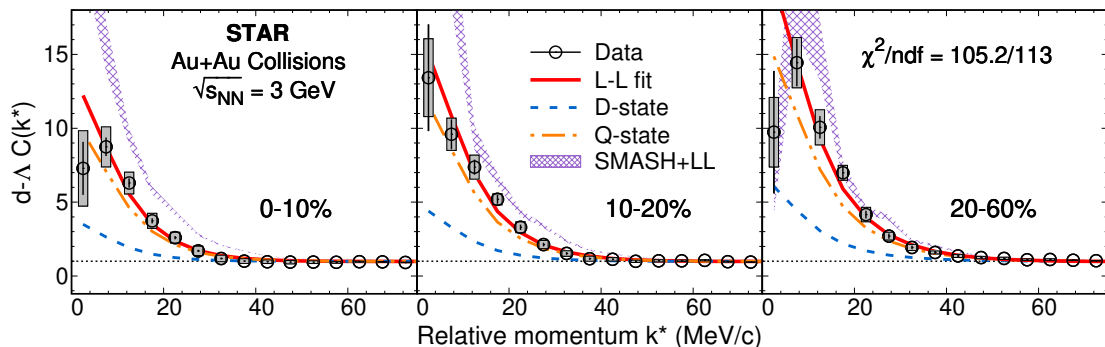
Corrections:

- 1) Track merging;
- 2) Track splitting;
- 3) Resonance decays;
- 4) Purity;
- 5) Momentum smearing;
- 6) Contribution of ${}^3\Lambda H$

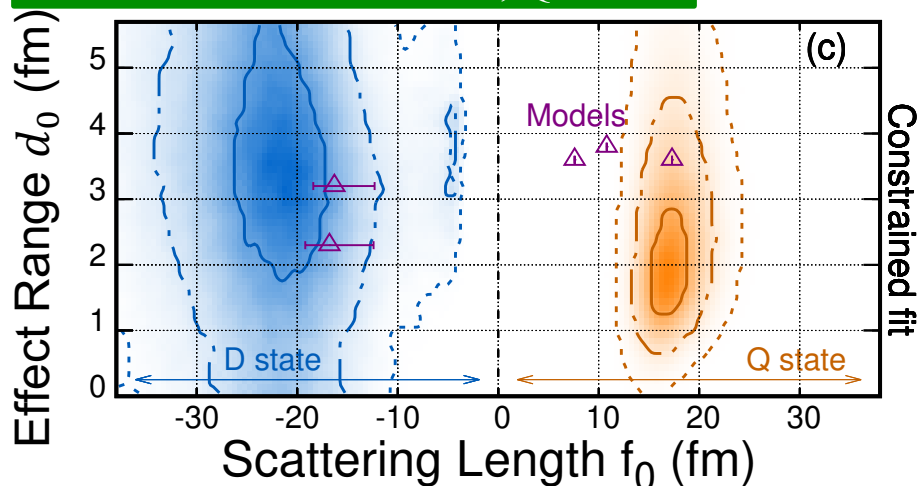
Acceptance:

- All: $0.5 < y < 0$;
- **p**: $0.25 < p_T < 2$ (GeV/c);
- **d**: $0.25 < p_T < 3$ (GeV/c);
- **Λ** : $0.25 < p_T < 2$ (GeV/c)

$d - \Lambda$ Correlation Functions 3.0 GeV



STAR: CPOD2024, QM2023



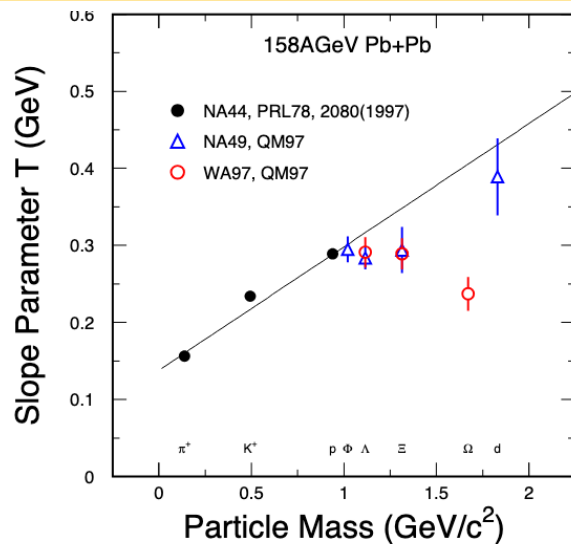
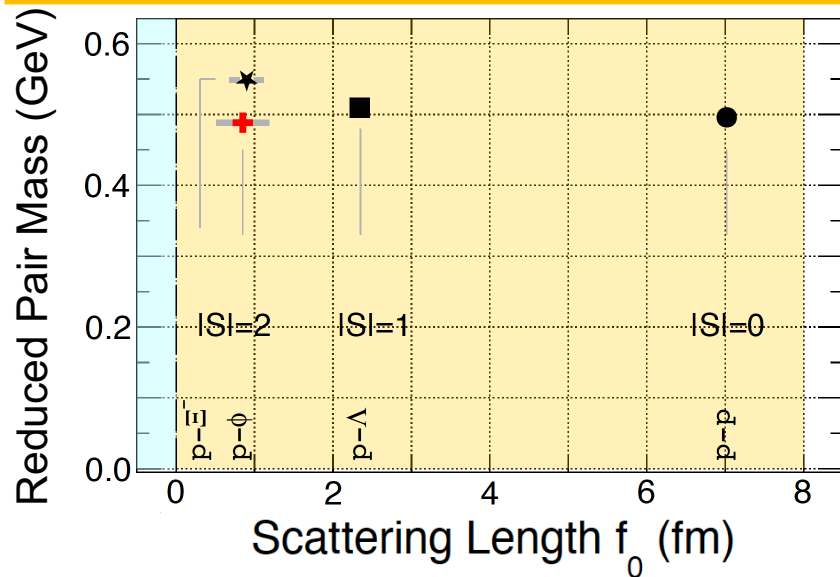
- 1) Centrality dependence of the $d - \Lambda$ correlation functions from 3.0 GeV Au+Au collisions;
- 2) For the first time, spin dependent states, D and Q , identified experimentally!

→ **New window for studying 3-body interactions in the laboratory**

References:

- (1) J.M. Lattimer and M. Prakash, Science **304**, 536 (2004);
- (2) M. Kohno and H. Kamada, arXiv:2406.13899;
- (3) H. W. Hammer, Nucl. Phys. **A705**, 173 (2002)

Summary: *NY* Correlations



H. van Hecke, H. Sorge
 NX, Phys.Rev.Lett. **81**,
 5764(1998). “Evidence of
 early multi-strange hadron
 freeze-out in high energy
 nuclear collisions”

→ Rescatterings lead to
 collectivity

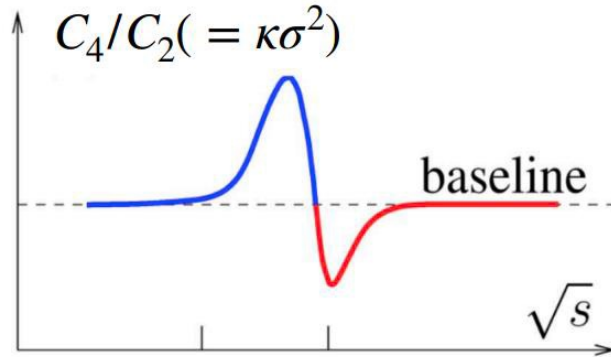
→ Collectivity is reduced
 as the strangeness
 content is increased

Hierarchy of strangeness content: $f_0(|s| = 0) > f_0(|s| = 1) > f_0(|s| = 2) > 0$

- Interaction section is proportional to f_0^2 , the observation implies that the strength of the interaction depends on strangeness;
- Important for understanding EOS of the medium in nuclear collisions and compact stars;
 In case of $f_0 < 0$, important for the search for di-baryons, such as $p\Omega$
 Understand the strangeness hierarchy in QCD calculations?

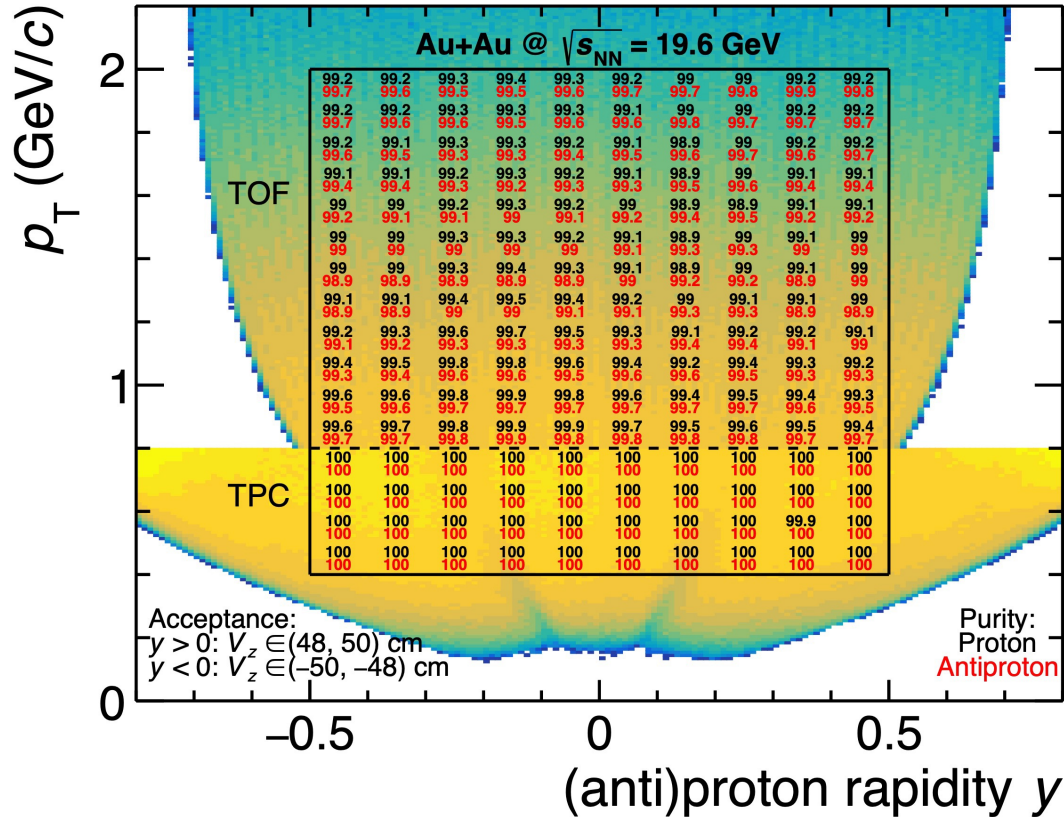
Search for QCD Critical Point

Precision Measurements of (Net-)Proton Number Fluctuations in Au+Au Collisions at RHIC (STAR Collaboration)



Signal for Critical Point:
Non-monotonical energy dependence

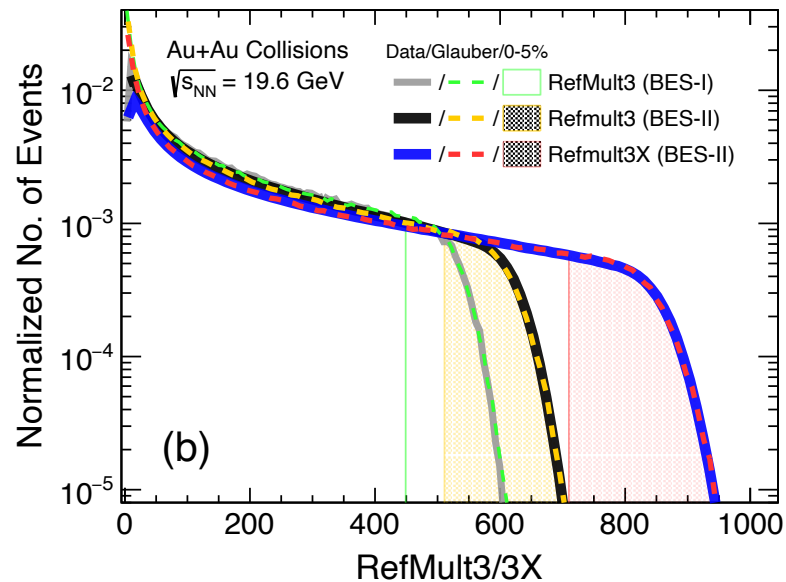
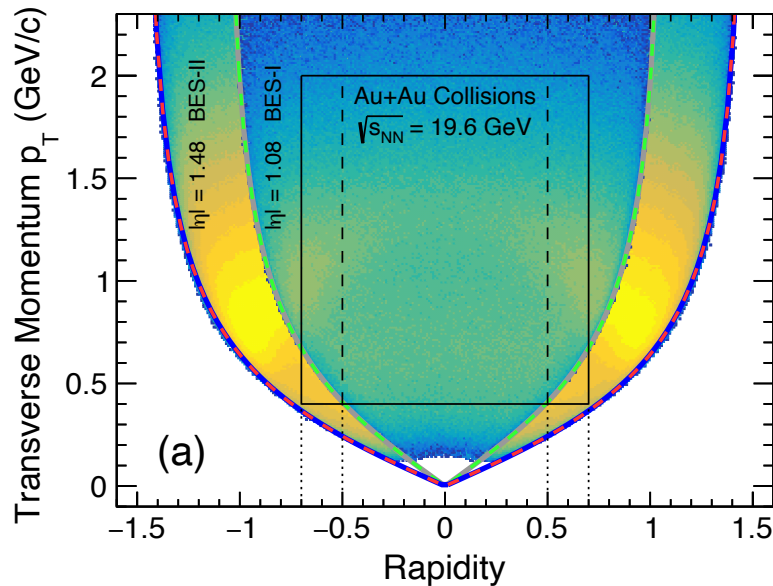
Proton Identification at BES-II



Detector	TPC	TPC+TOF
dE/dx	$ n\sigma < 2$	
$m^2 (\text{GeV}/c^2)^2$	NA	0.6 – 1.2
$p_T (\text{GeV}/c)$	0.4 – 0.8	0.8 – 1.2
rapidity	$ y < 0.5$	

- 1) Uniform acceptance for (anti-) protons $|y| < 0.5$ with $|V_z| < 50$ cm;
- 2) (anti-)protons identified using TPC dE/dx and TOF
- 3) Bin-by-bin purity $> 99\%$ in the full acceptance range and for all energies

BES-II: Centrality Determination

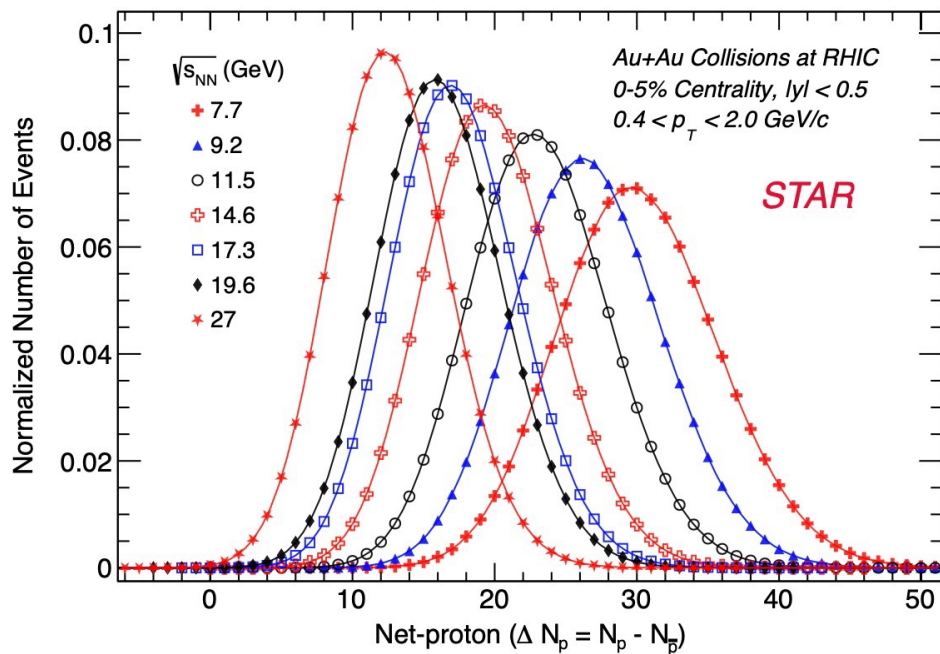


Reference multiplicity measurements **RefMult3**: TPC measured charge particles except (anti-)protons

1) **RefMult3**: ($|\eta| < 1.0$) for both BES-I and BES-II 2) **RefMult3X**: ($|\eta| < 1.6$) for BES-II

→ **Larger acceptance** → **larger multiplicity** → **better centrality resolution**

Net-p from BES-II



- 1) Raw number distributions from BES-II: Uncorrected for detector efficiency;
- 2) Mean increases with decreasing collision energy: Effect of baryon stopping;
- 3) The increase in the width is due to the increase of proton numbers at lower energy

0-5%: C_4/C_2 improvement factor BES-II / BES-I

7.7 GeV		19.6 GeV	
Stat.	Syst.	Stat.	Syst.
4.7	3.2	4.5	4
*Embedding statistics increased by a factor of 5!			

STAR: CPOD2024, SQM2024

Conserved Quantities (B , Q , S)

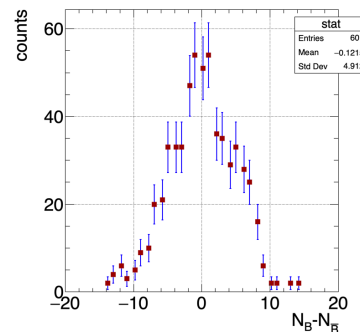
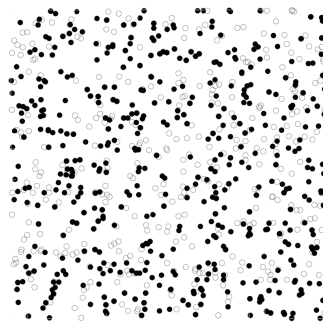
- 1) In strong interactions, baryons (B), charges (Q) and strangeness (S) are conserved;
- 2) Higher order moments/cumulants describe the shape of distributions and quantify fluctuations. They are sensitive to the correlation length ξ , phase structure;
- 3) Direct connection to theoretical calculations of susceptibilities.

$$\begin{aligned} \text{Measured multiplicity } N, & \quad \langle \delta N \rangle = N - \langle N \rangle \\ \text{mean: } M & = \langle N \rangle = C_1 \\ \text{variance: } \sigma^2 & = \langle (\delta N)^2 \rangle = C_2 \\ \text{skewness: } S & = \langle (\delta N)^3 \rangle / \sigma^3 = C_3 / C_2^{3/2} \\ \text{kurtosis: } \kappa & = \langle (\delta N)^4 \rangle / \sigma^3 - 3 = C_4 / C_2^2 \end{aligned}$$

Moments, cumulants and susceptibilities:

$$\begin{aligned} 2^{\text{nd}} \text{ order: } \sigma^2 / M & \equiv C_2 / C_1 = \chi_2 / \chi_1 \\ 3^{\text{rd}} \text{ order: } S \sigma & \equiv C_3 / C_2 = \chi_3 / \chi_2 \\ 4^{\text{th}} \text{ order: } \kappa \sigma^2 & \equiv C_4 / C_2 = \chi_4 / \chi_2 \end{aligned}$$

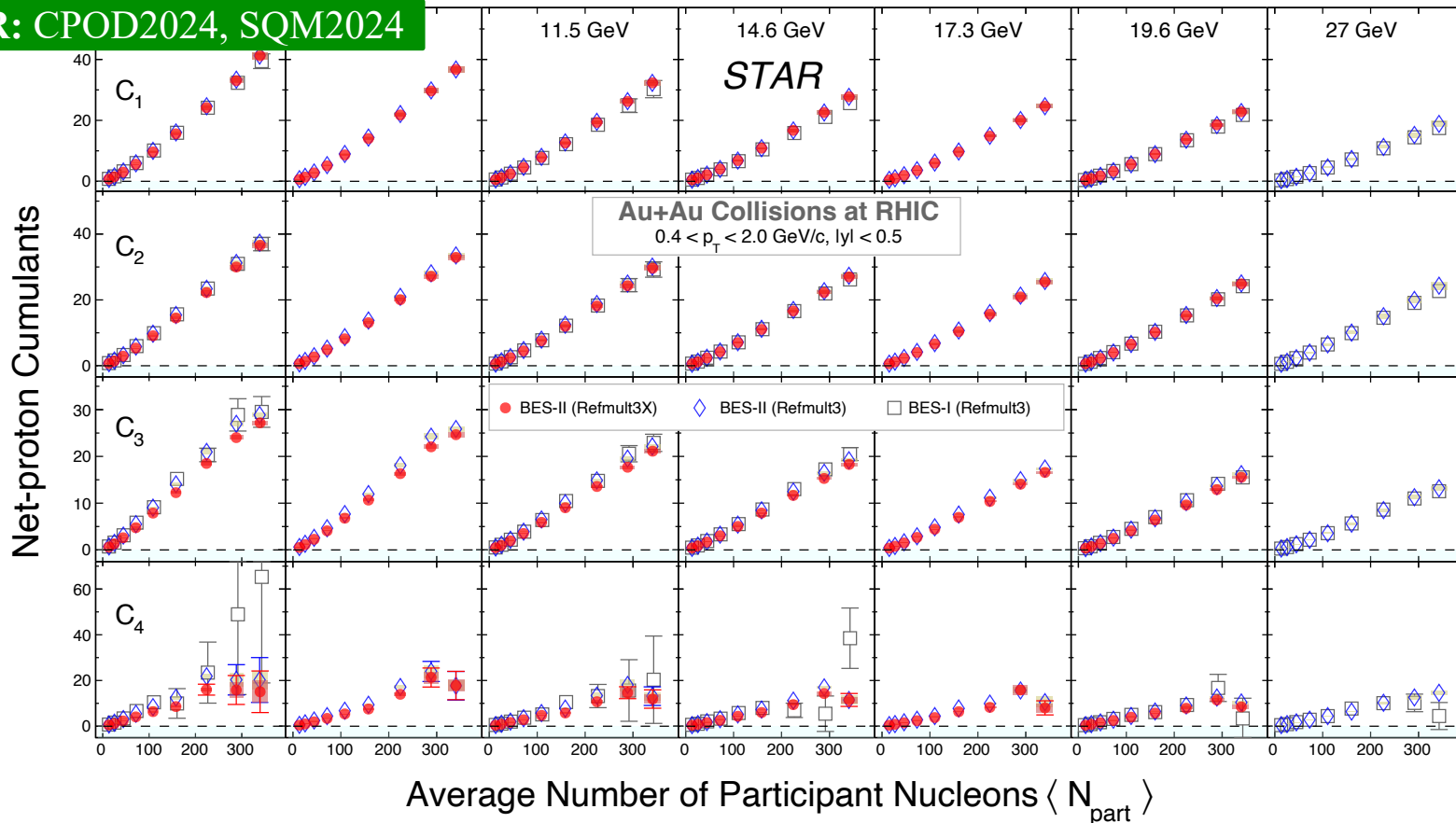
Animation: A.Rustamov



INT 2008-2b : The QCD Critical Point

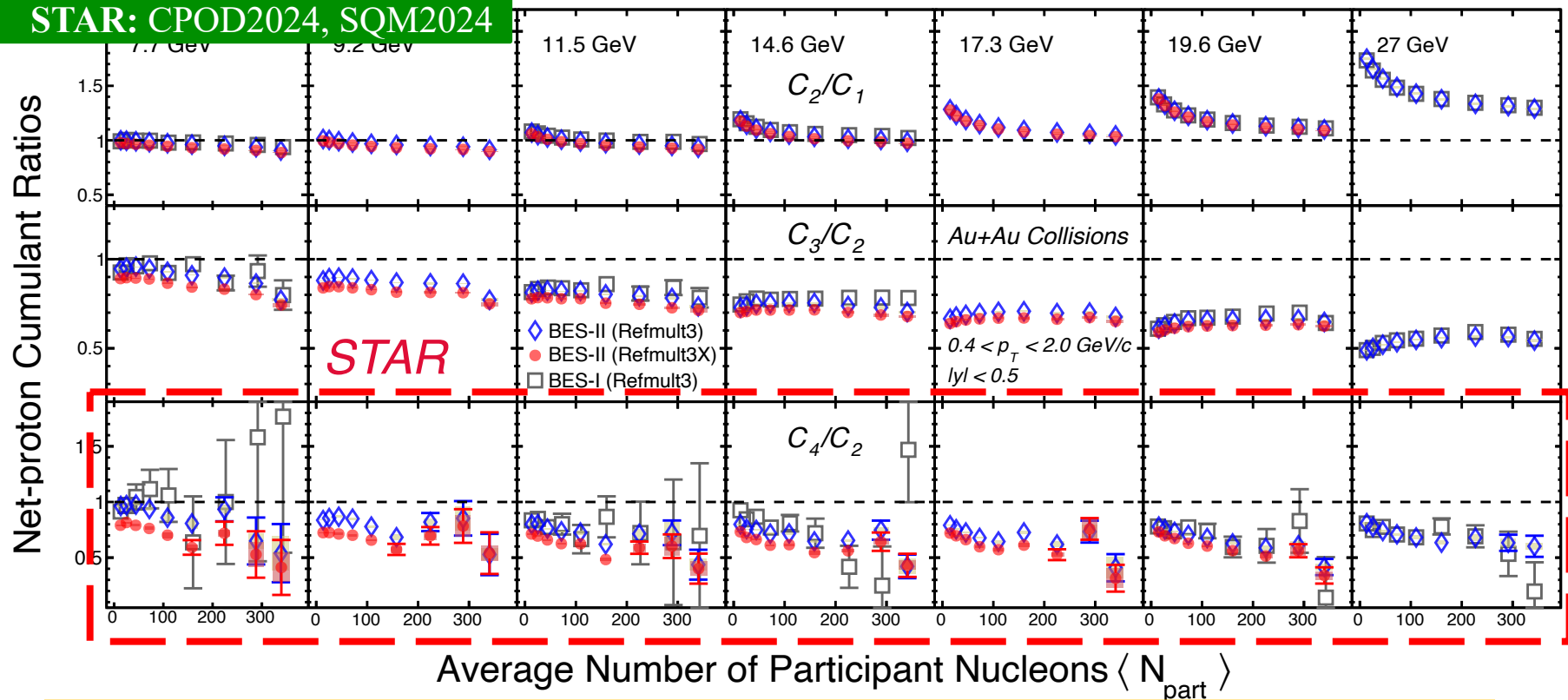
Cumulants of Net-p from BES-II

STAR: CPOD2024, SQM2024



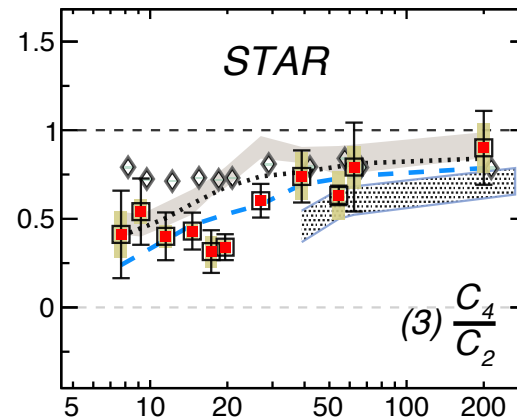
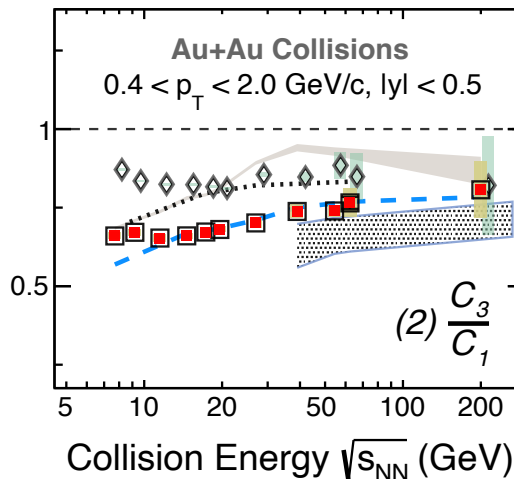
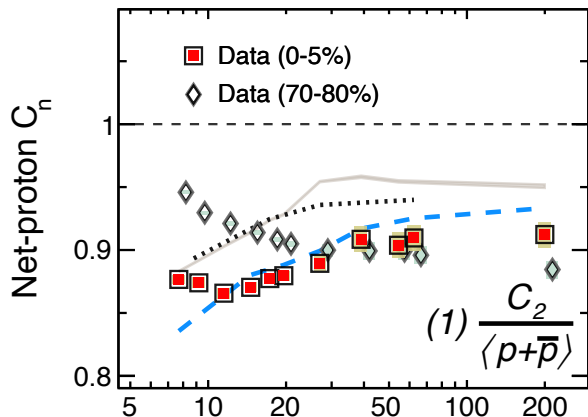
Net-p Cumulant Ratios

STAR: CPOD2024, SQM2024



In 0-5% central collisions, values of C_4/C_2 are consistent among BES-I and BES-II

Energy Dependence of Cumulant Ratios

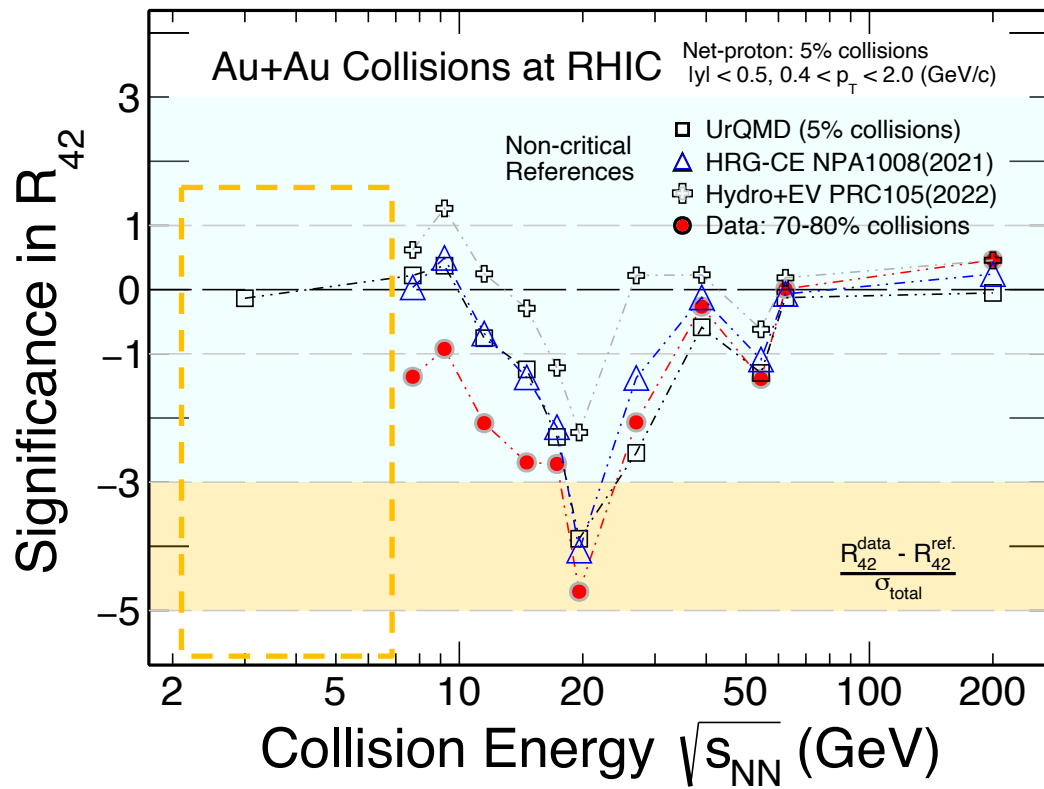


STAR: CPOD2024, SQM2024

- 1) **UrQMD**: hadronic transport and the results are analyzed in the same way as data. S. Bass *et al.*, Prog. Part. Nucl. Phys., **41**, 255 (1998);
- 2) **HRG CE**: P.B. Munzinger *et al.* Nucl. Phys. **A1008**, 122141(2021);
- 3) **Hydro - HRG CE + EV + Collectivity**: V. Vovchenko *et al.*, Phys. Rev. **C105**, 014904 (2022).
- 4) **LQCD GCE**: done for net-baryon A. Bazavov *et al.*, Phys. Rev. D101, 074502 (2020).

Baryon conservations applied in all model calculations except LQCD!

Deviations from Non-CP Models



0-5% central collisions:

1) C_4/C_2 ratios: show minima at 19.6 GeV, 2-5 σ effects, depends on reference;

2) Future data from

- STAR FXT;
- HADES at GSI and
- CBM experiment at FAIR (2028) will cover the energy region $\sqrt{s_{\text{NN}}} = 2.4 - 4.9$ GeV

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- Criticality from BES-II (collider energy $7.7 \leq \sqrt{s_{NN}} \leq 27 \text{ GeV}$)

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Summary

(1) Baryon correlations: Hierarchy of strangeness content in f_0 !

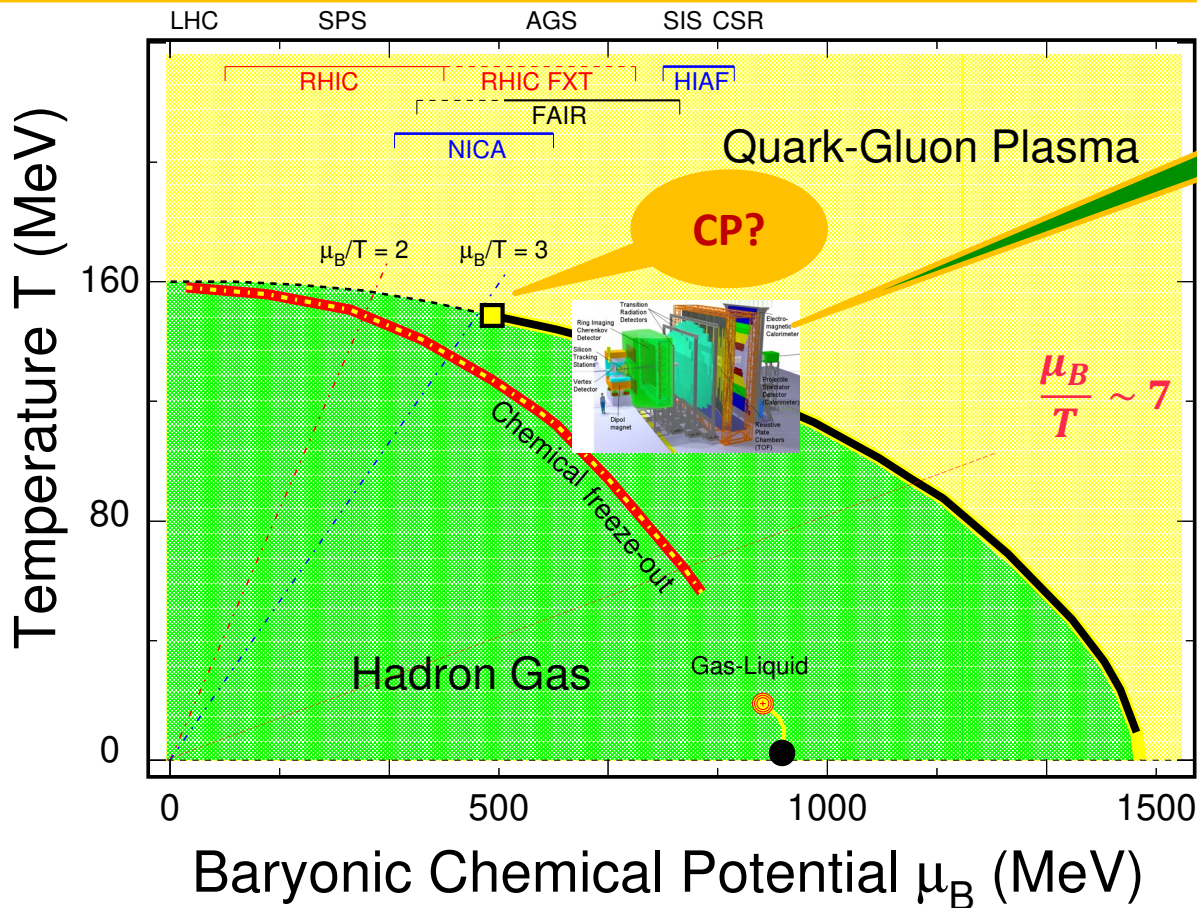
(2) Search for QCD critical point:

- BES-II data offered high statistics, better acceptance, centrality resolution and systematic;
- Known model calculations **Do Not** reproduce the energy dependence ($\sqrt{s_{NN}} = 7.7 - 200$ GeV)

(3) Outlook:

- (i) Transverse momentum p_T and rapidity scan;
- (ii) Higher orders: C_5 , and C_6 analysis;
- (iii) Complete FXT data analysis at $\sqrt{s_{NN}} = 3 - 3.9$ GeV

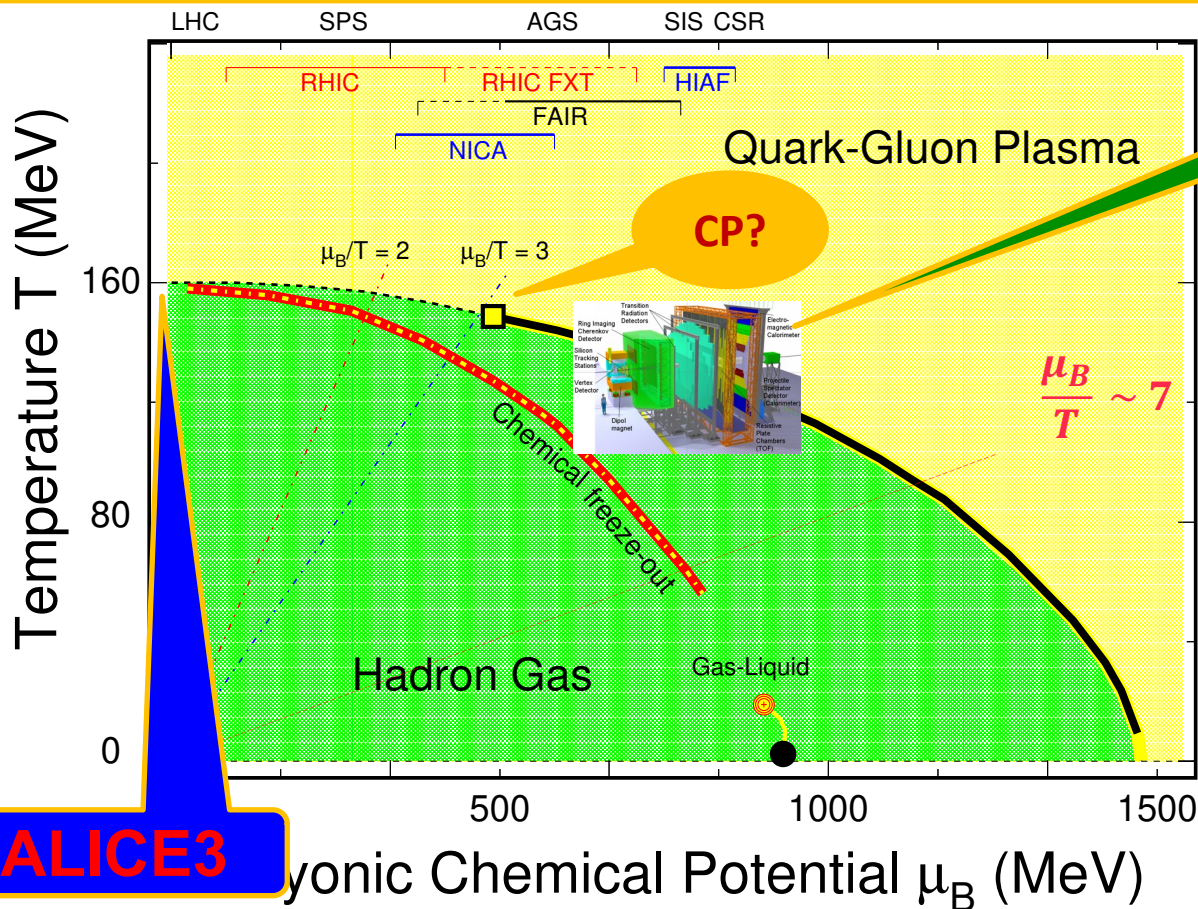
Future Physics Programs at High μ_B



CBM 2028

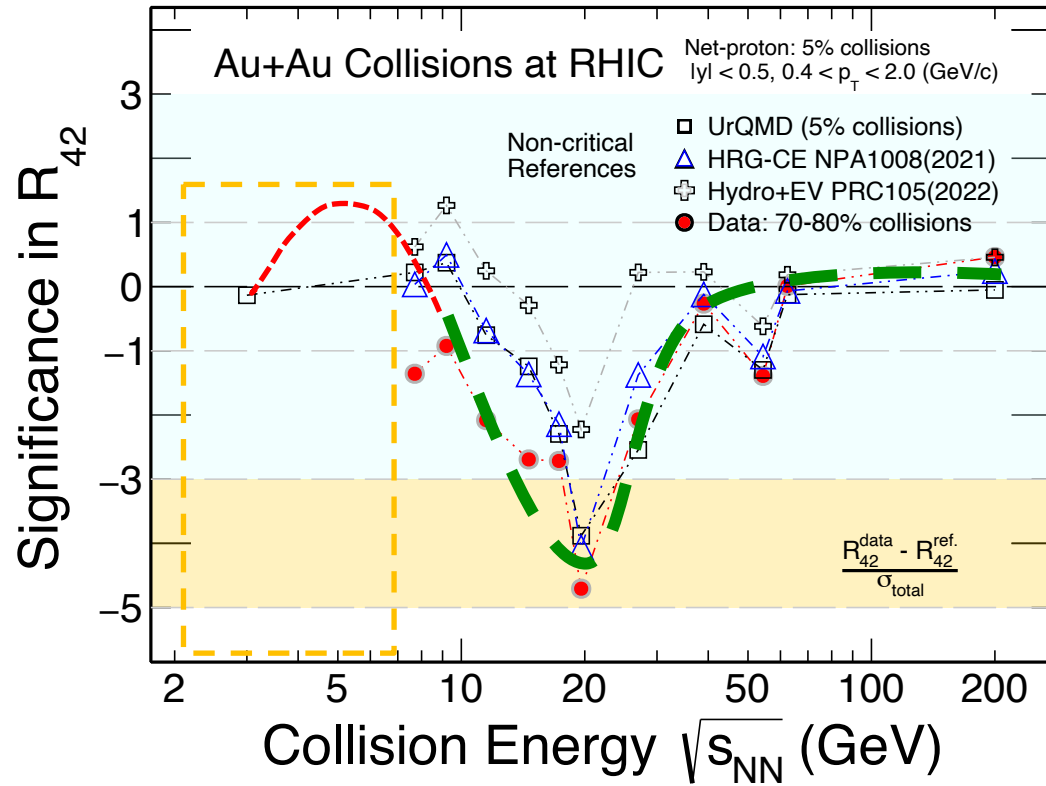
- Critical point and phase boundary;
- Nuclear matter EOS at high baryon density;
- Y-N interactions, inner structure of compact stars

Future Physics Programs at High μ_B



- Critical point and phase boundary;
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- Y-N interactions, inner structure of compact stars

Key Measurements at CBM Experiment



1) CBM covers the key energy region for CP search

$$\sqrt{s_{NN}} = 2.4 - 4.9 \text{ GeV}$$

2) Key measurements at CBM:

- Leptons
- Collective flow
- High moments of proton
- NN and YN correlation
- (m)Hyper-nuclei production

→ The detector must be ready by 2028

Acknowledgements:

RHIC and STAR Experiment

P. Braun-Munzinger, X. Dong, S. Esumi, *Y. Hu*, F. Karsch, *K. Mi*, V. Koch, XF. Luo, B. Mohanty, *A. Pandav*, A. Rustamov, K. Redlich, M. Stephanov, J. Stachel, J. Stroth, V. Vovchenko, *Y. Zhang*

// BLUE: Theory // RED: Exp. //

EMMI/GSI



Thank you for your attention!