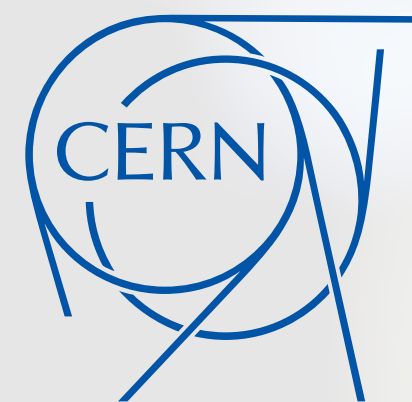


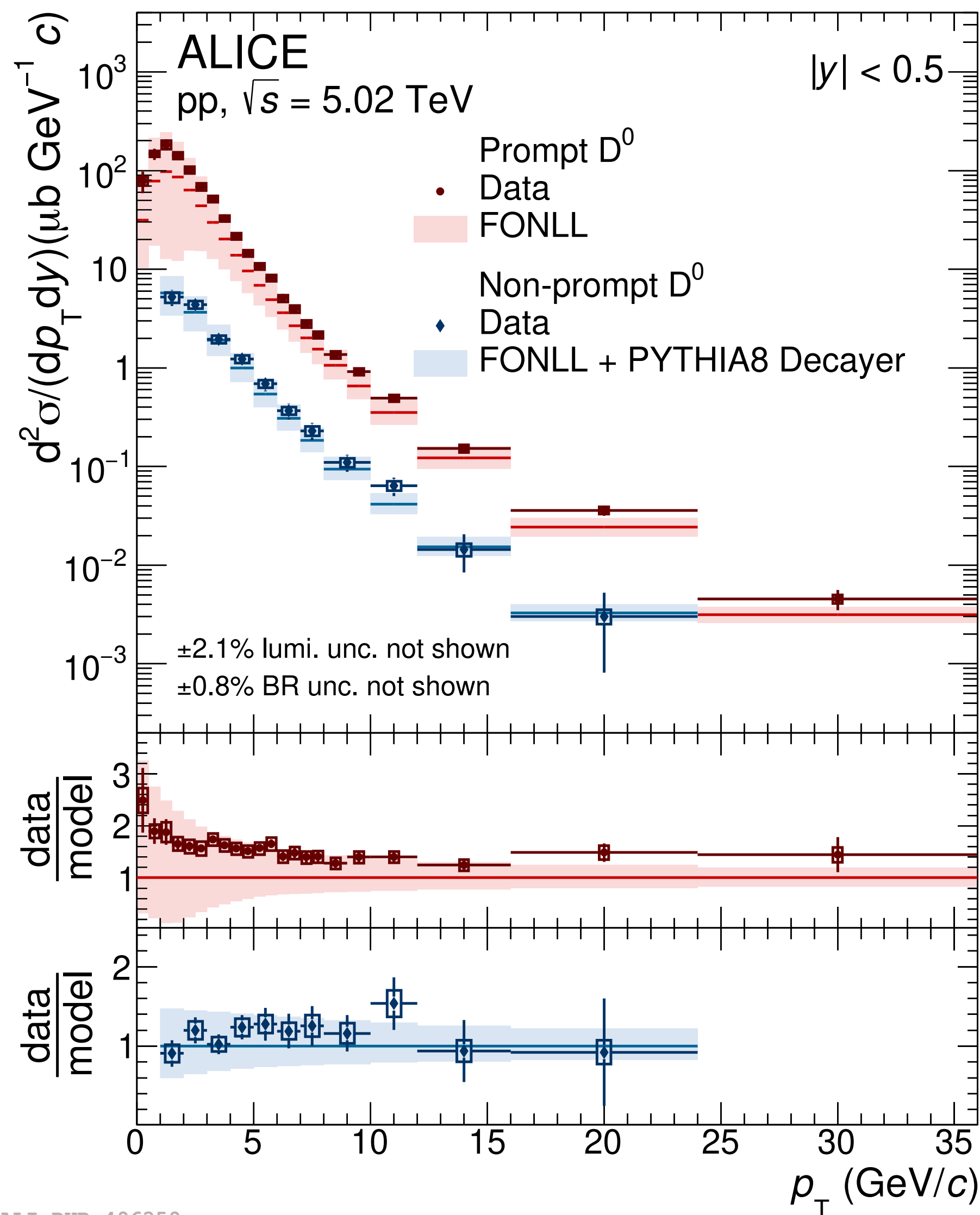
Probing the quark–gluon plasma with heavy-flavour hadrons



Fabrizio Grosa
CERN

Advances, Innovations, and Future Perspectives in High-Energy Nuclear Physics

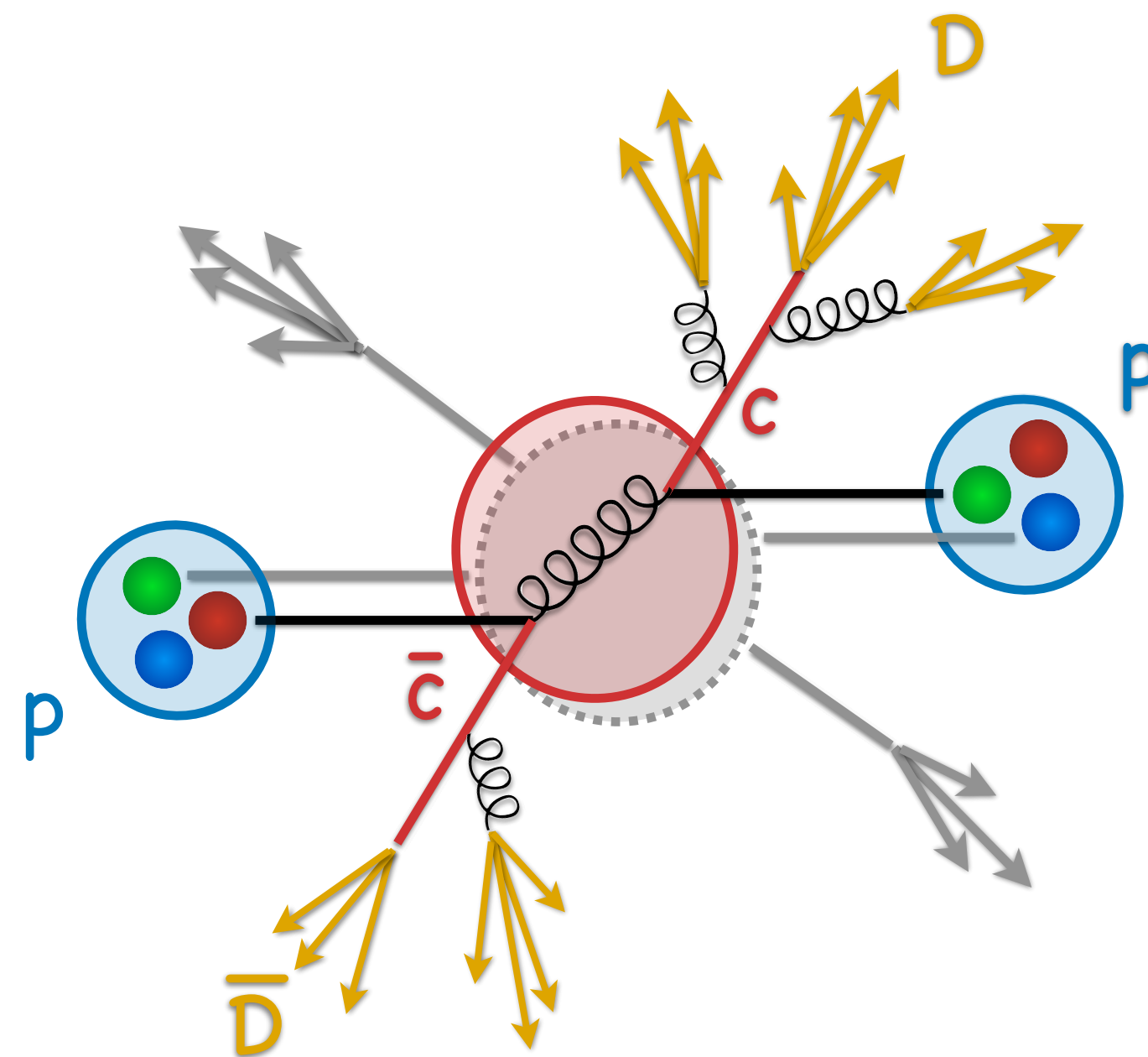
Wuhan | 19–24/10/2024



ALI-PUB-496359

ALICE, JHEP 05 (2021) 220

- Charm and beauty quarks are produced in hard-scattering processes
- perturbative QCD calculations based on the factorisation theorem



$$\sigma_{hh \rightarrow Hh} = \text{PDF}(x_a, Q^2) \text{PDF}(x_b, Q^2) \otimes \sigma_{ab \rightarrow q\bar{q}} \otimes D_{q \rightarrow h}(z_q, Q^2)$$

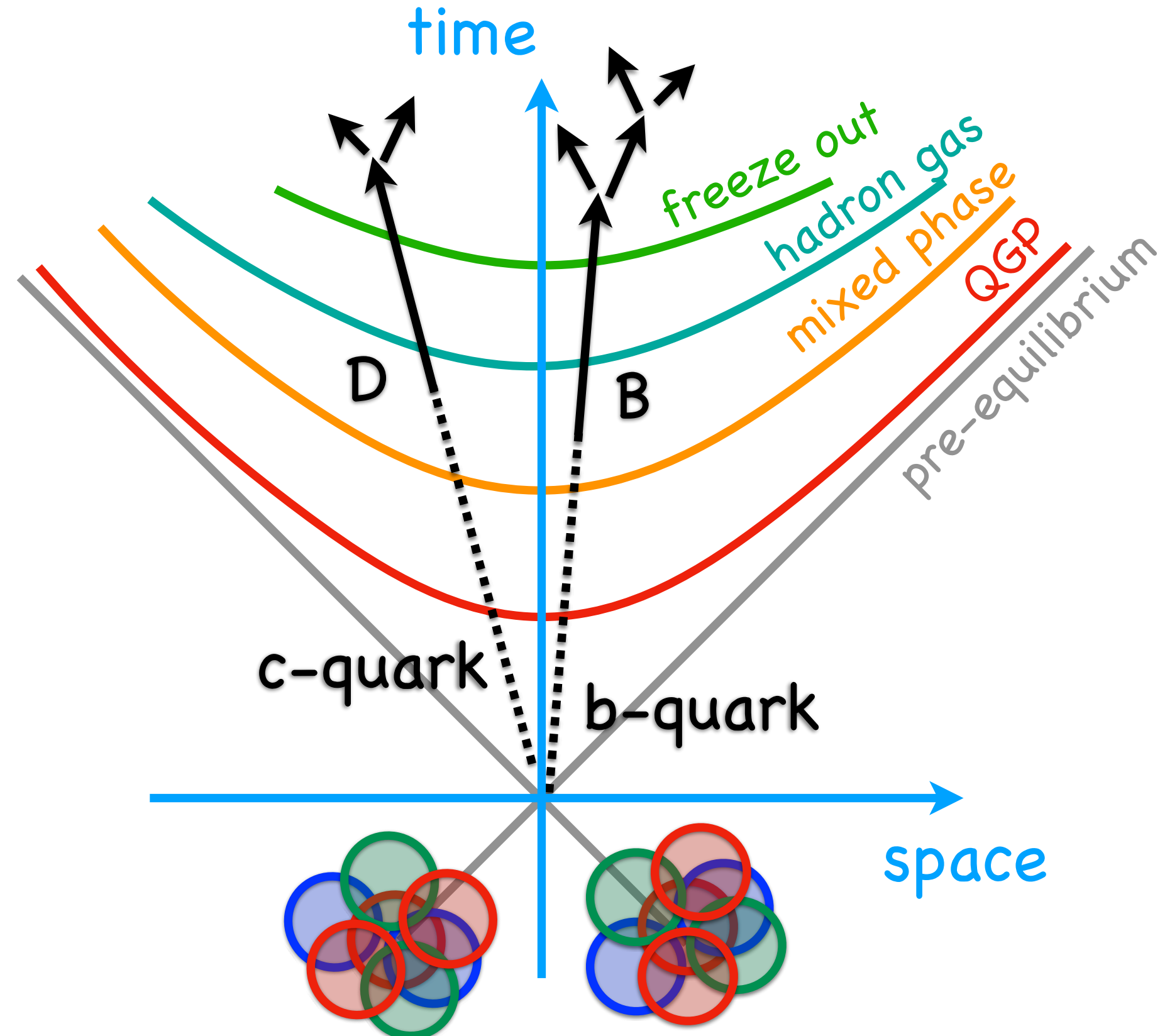
Parton distribution functions
(non perturbative)

Partonic cross section
(perturbative)

Fragmentation functions
(non perturbative)

- Heavy quarks: produced in shorter time scales than the quark–gluon plasma formation (QGP)
 - $\tau_{\text{HF}} \approx \hbar/m \approx 0.05\text{-}0.1 \text{ fm}/c$ depending on p_{T}
 - $\tau_{\text{QGP form (LHC)}} \approx 0.3 \text{ fm}/c$

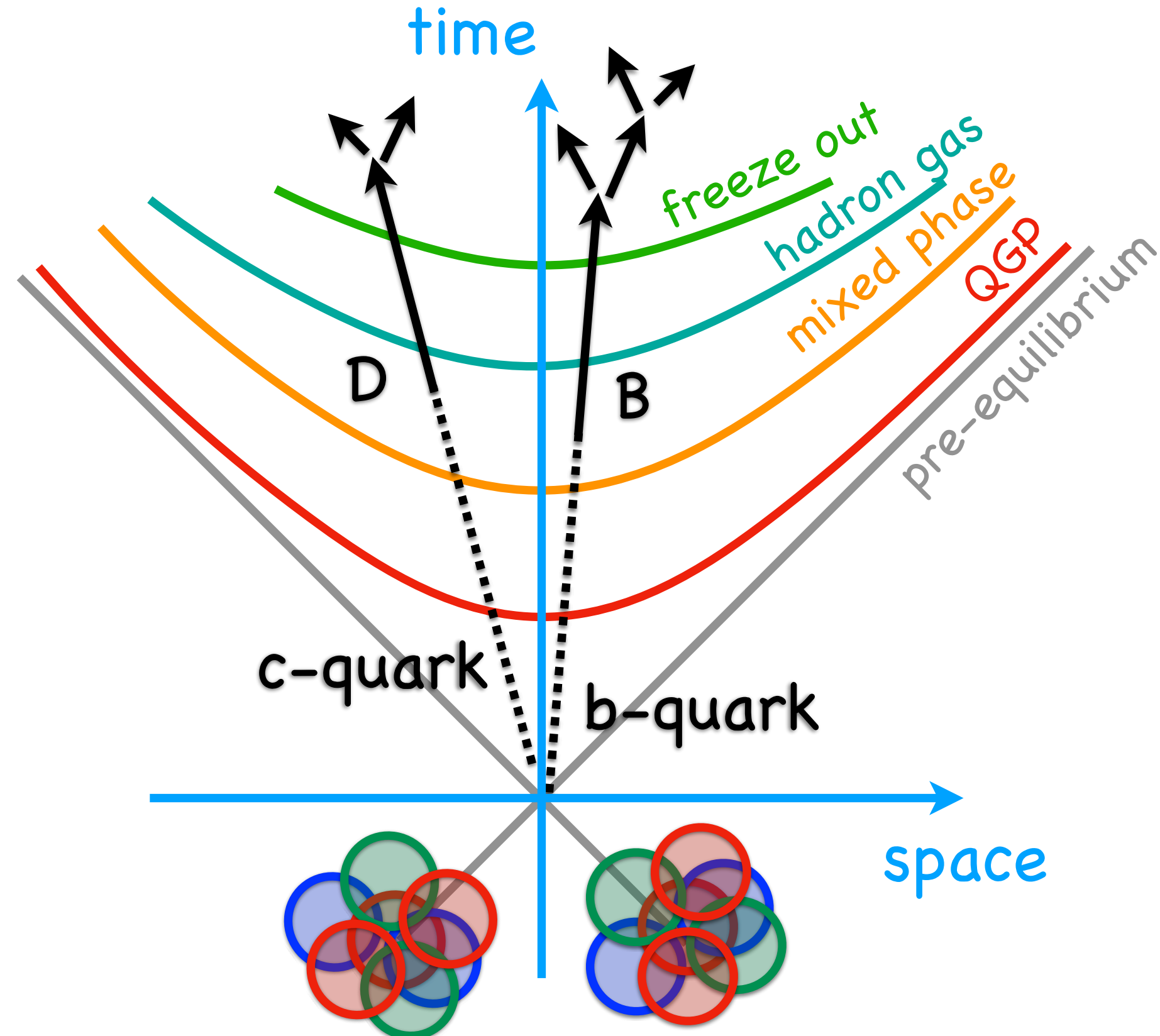
PRC 89 (2014) 034906



- Low- p_{T} : multiple elastic collisions with the medium constituents
 - Diffusion motion and possible (partial) thermalisation in the medium
- High- p_{T} : radiative energy loss (gluon emission)
 - Study properties of in-medium energy loss
- Momentum and angular distributions of HF hadrons
 - Study interactions of heavy-quarks with the medium
- Hydrochemistry: baryons and strange hadrons
 - Study hadronisation from the medium
- Vector meson polarisation:
 - Study initial strong magnetic fields
- Strong interaction of heavy-flavour hadrons with light hadrons:
 - Study the impact of hadronic phase on heavy-ion observables
- Small systems: heavy-ion like effects
 - Flow, baryons-to-meson ratio modification

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PRC 89 (2014) 034906



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- Small systems: heavy-ion like effects
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- Models based on the heavy-quark transport on a hydrodynamically expanding QGP
 - Typical momentum transfers in scatterings between heavy quarks and medium constituents (heat bath) are small
 - Heavy quarks undergo soft and incoherent collisions → Brownian motion
 - Boltzmann equation can be reduced to a Langevin or Fokker-Plank equation in the limit of small momentum exchange

$$\frac{\partial}{\partial t} f_Q(t, \mathbf{p}) = \frac{\partial}{\partial p^i} \left\{ A^i(\mathbf{p}) \cdot f_Q(t, \mathbf{p}) + \frac{\partial}{\partial p^j} [B^{ij}(\mathbf{p}) \cdot f_Q(t, \mathbf{p})] \right\}$$

- In case of a medium in thermal equilibrium
 - $A^i(\mathbf{p}) = A(p)p_i$ friction
 - $B^{ij}(\mathbf{p}) = B_0(p) \cdot P_{ij}^\perp(\mathbf{p}) + B_1(p) \cdot P_{ij}^\parallel(\mathbf{p})$
momentum broadening

- Brownian motion of heavy quarks in QGP governed by the coupling of heavy quarks to the medium
 - Spatial diffusion coefficient

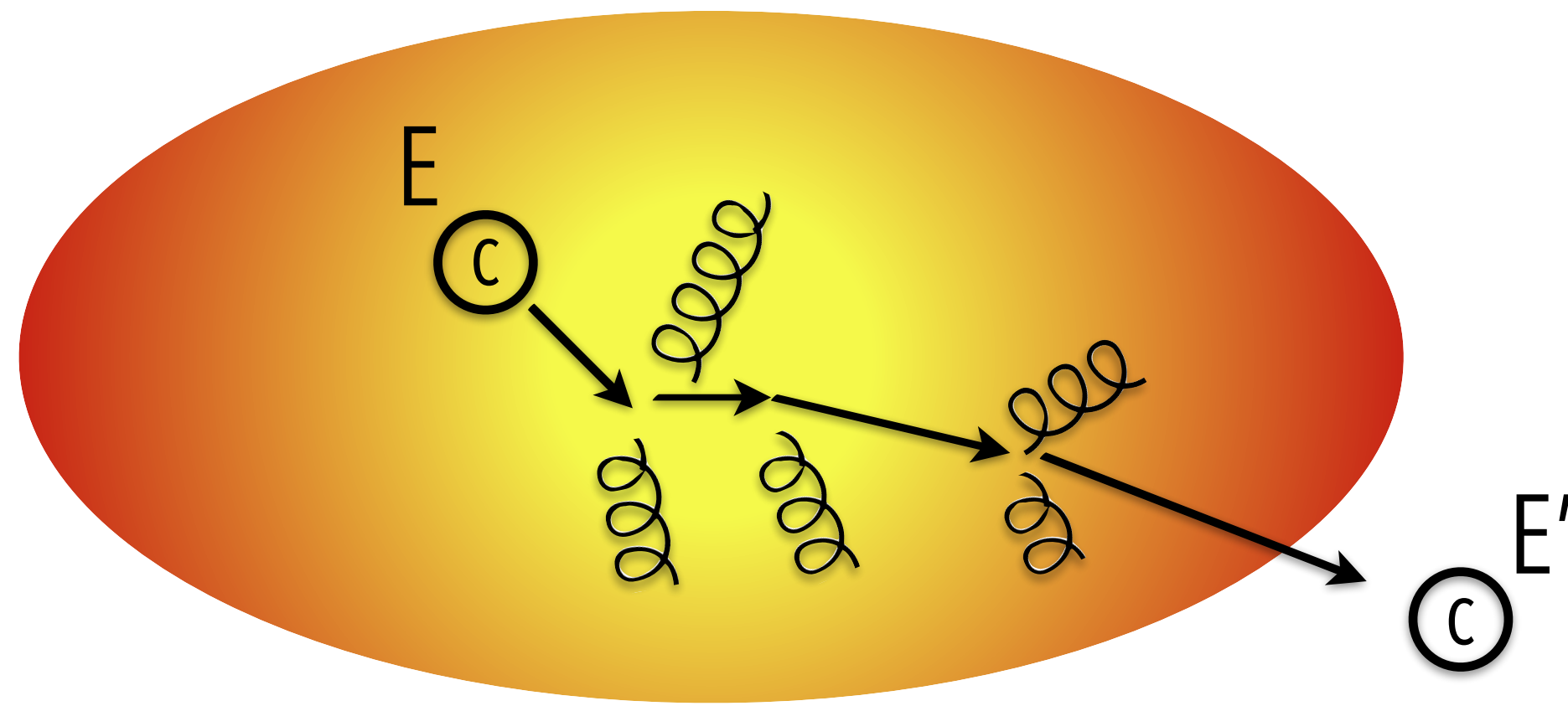
$$D_s = \frac{T}{m_{\text{HQ}} A(p=0)}$$

→ Related to the thermalisation time of the heavy quark quark

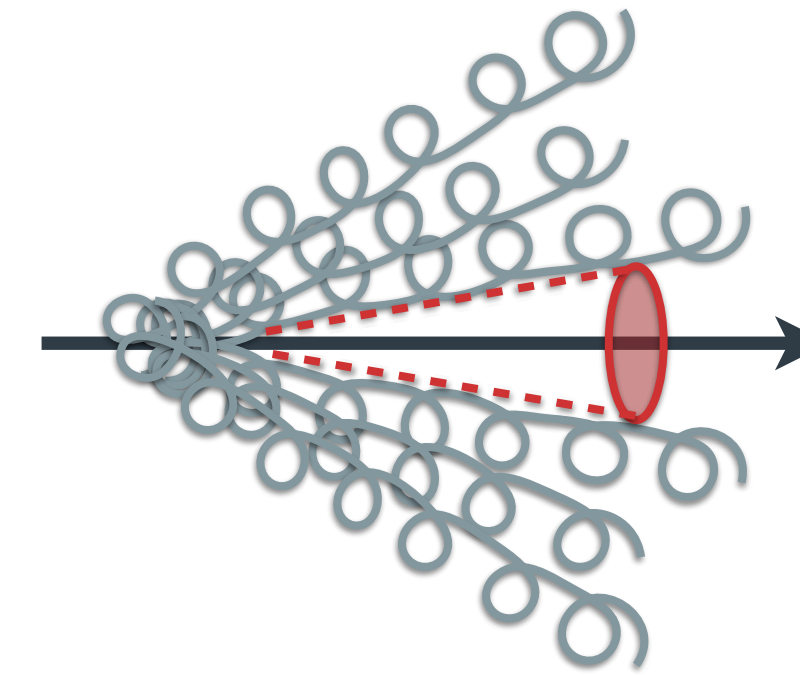
→ Approximately $A(p=0) \propto 1/m_{\text{HQ}}$

$$\tau_{\text{HQ}} = (m_{\text{HQ}}/T) \cdot D_s$$

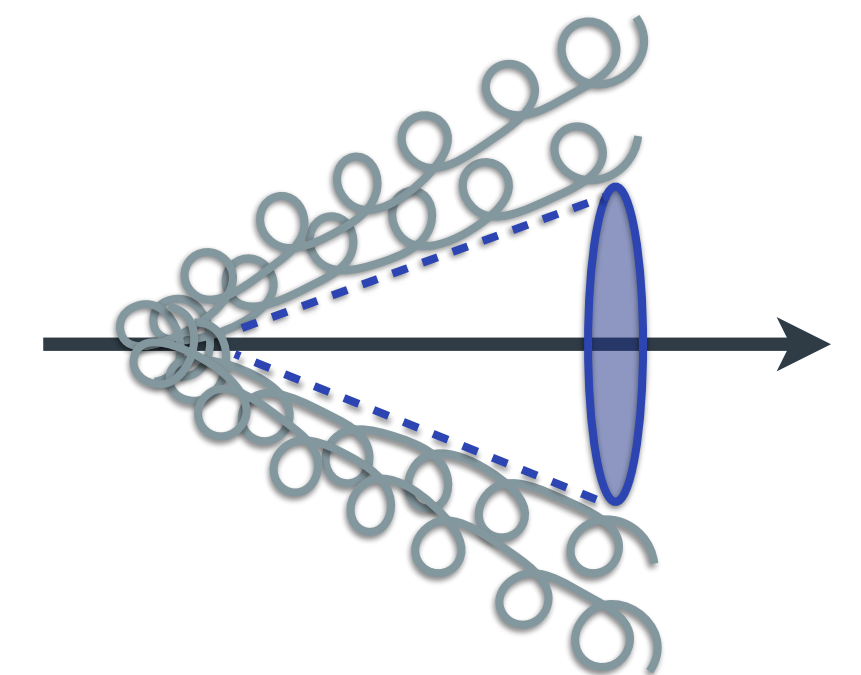
- Dominant effect: energy loss of charm and beauty quarks in the medium
- Goal: study the **colour-charge** and **quark-mass dependence** of the in-medium energy loss



small parton mass



large parton mass



Dead cone effect: gluon radiation suppressed at angles smaller than $\vartheta < m/E$

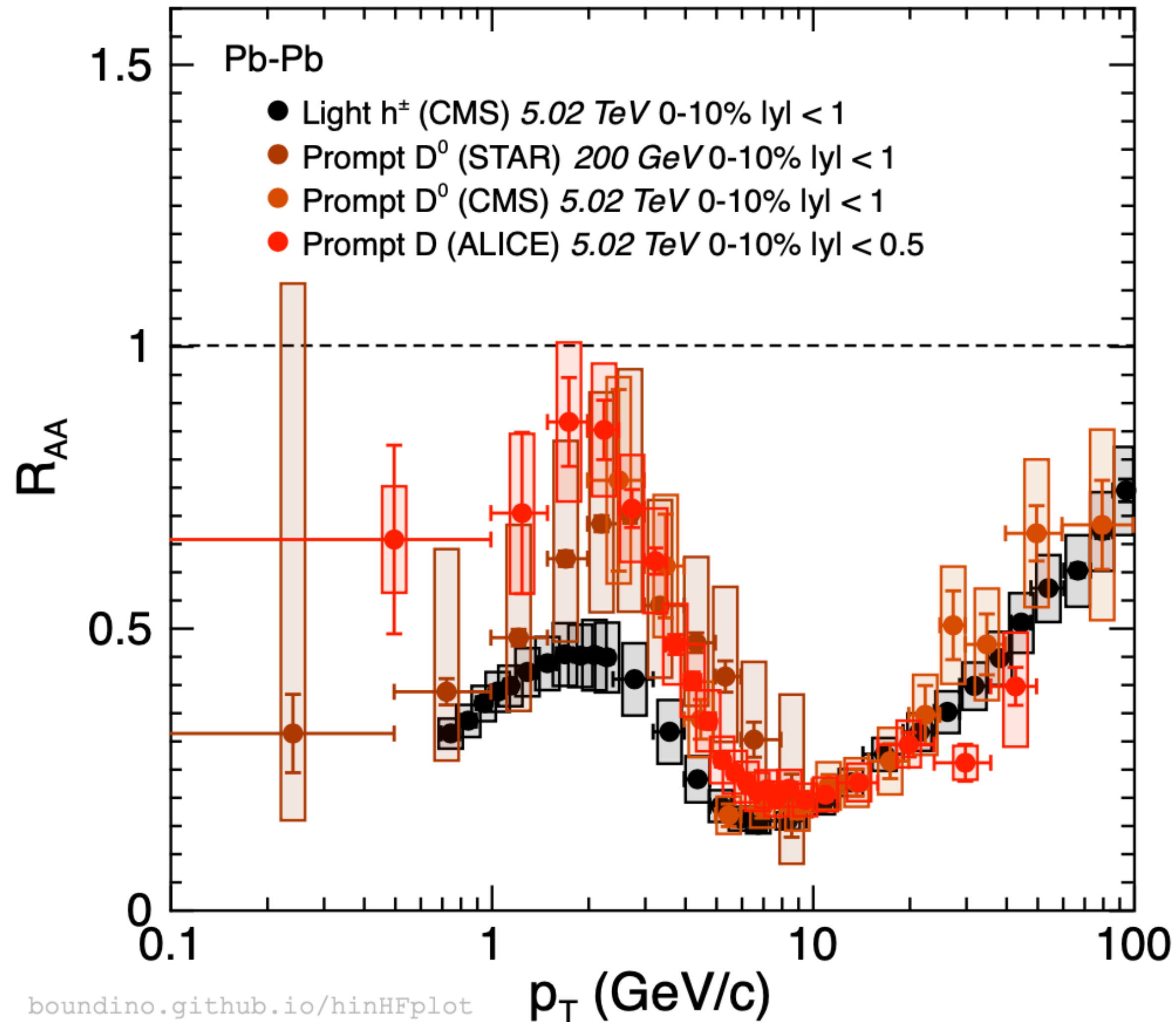
$$\langle \Delta E \rangle \propto \alpha_s C_R \hat{q} L^2$$

→ Path traversed in the medium

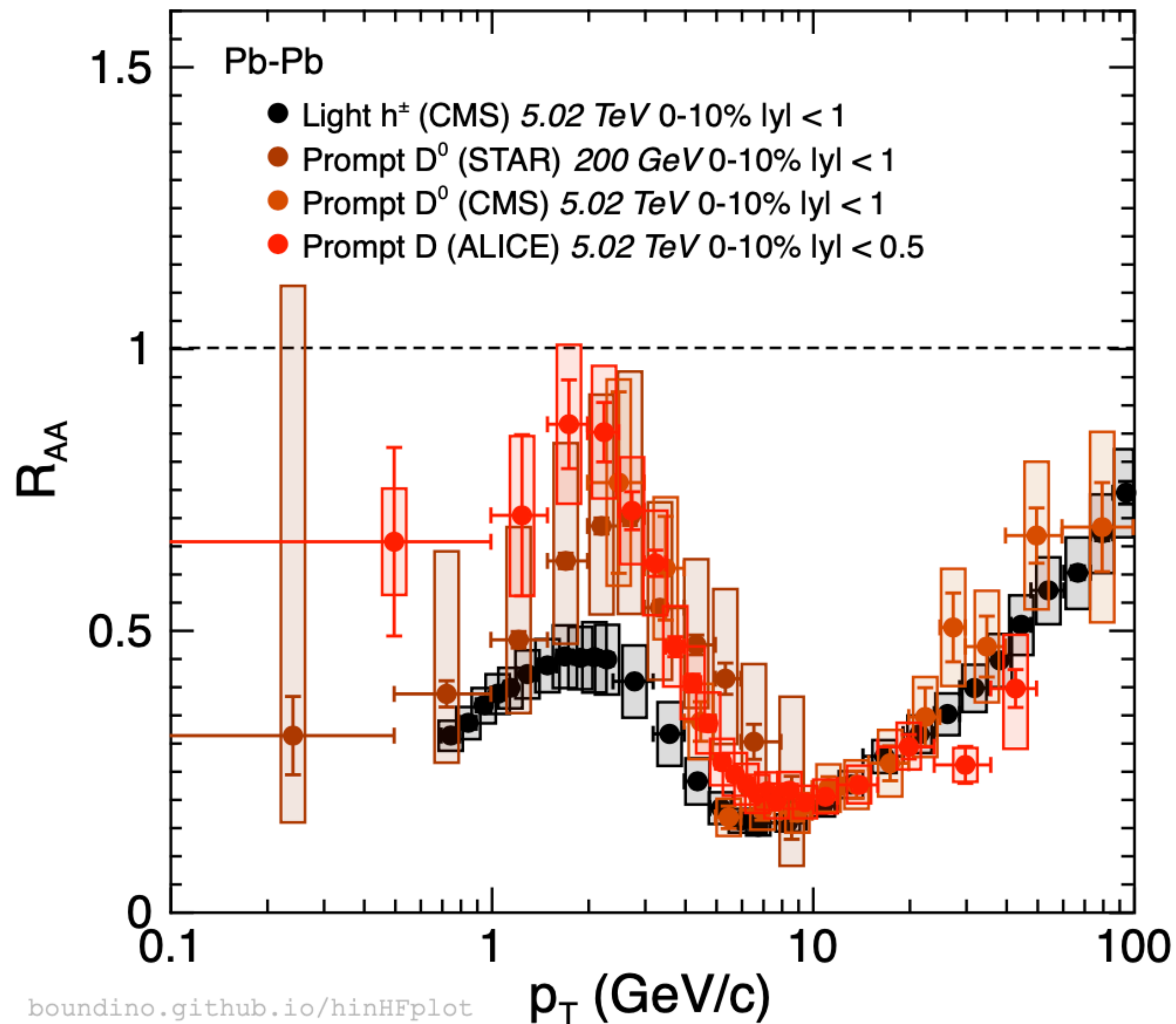
Strong coupling constant

Transport coefficient (average of the square of the transverse momentum exchanged with the QGP per unit mean free path)

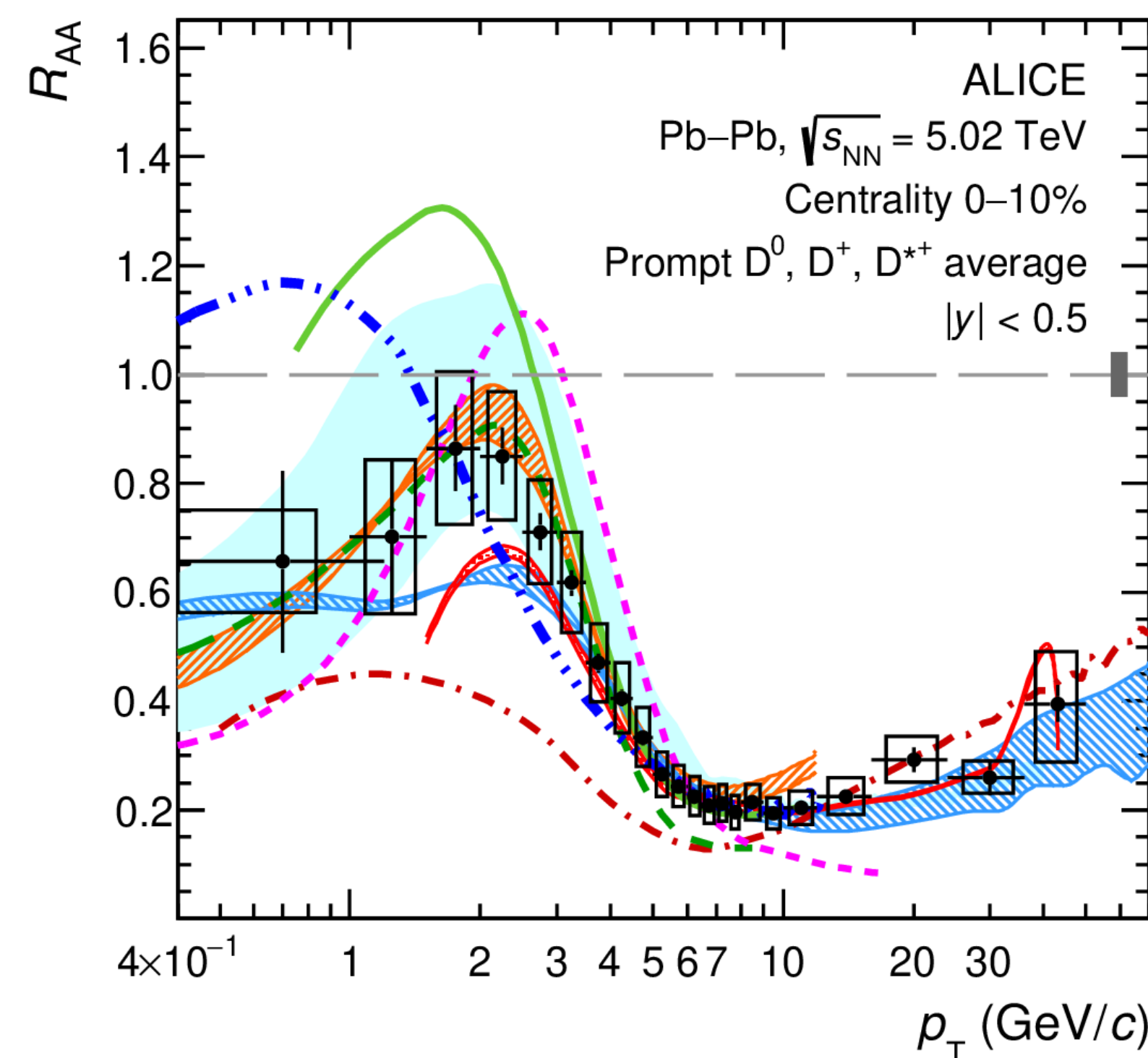
Casimir factor = 3 for gluons and 4/3 for quarks



- $p_T < 6-8$ GeV/c: $R_{AA}(D) > R_{AA}(\pi^\pm)$
 - Nuclear PDFs
 - Radial flow
 - Collisional energy loss
 - Hadronisation via recombination
- $p_T > 8$ GeV/c: $R_{AA}(D) \approx R_{AA}(\pi^\pm)$ → Radiative energy loss



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ALICE, JHEP 01 (2022) 174

Reasonably described by models implementing the heavy-quark transport in a hydrodynamically expanding QGP

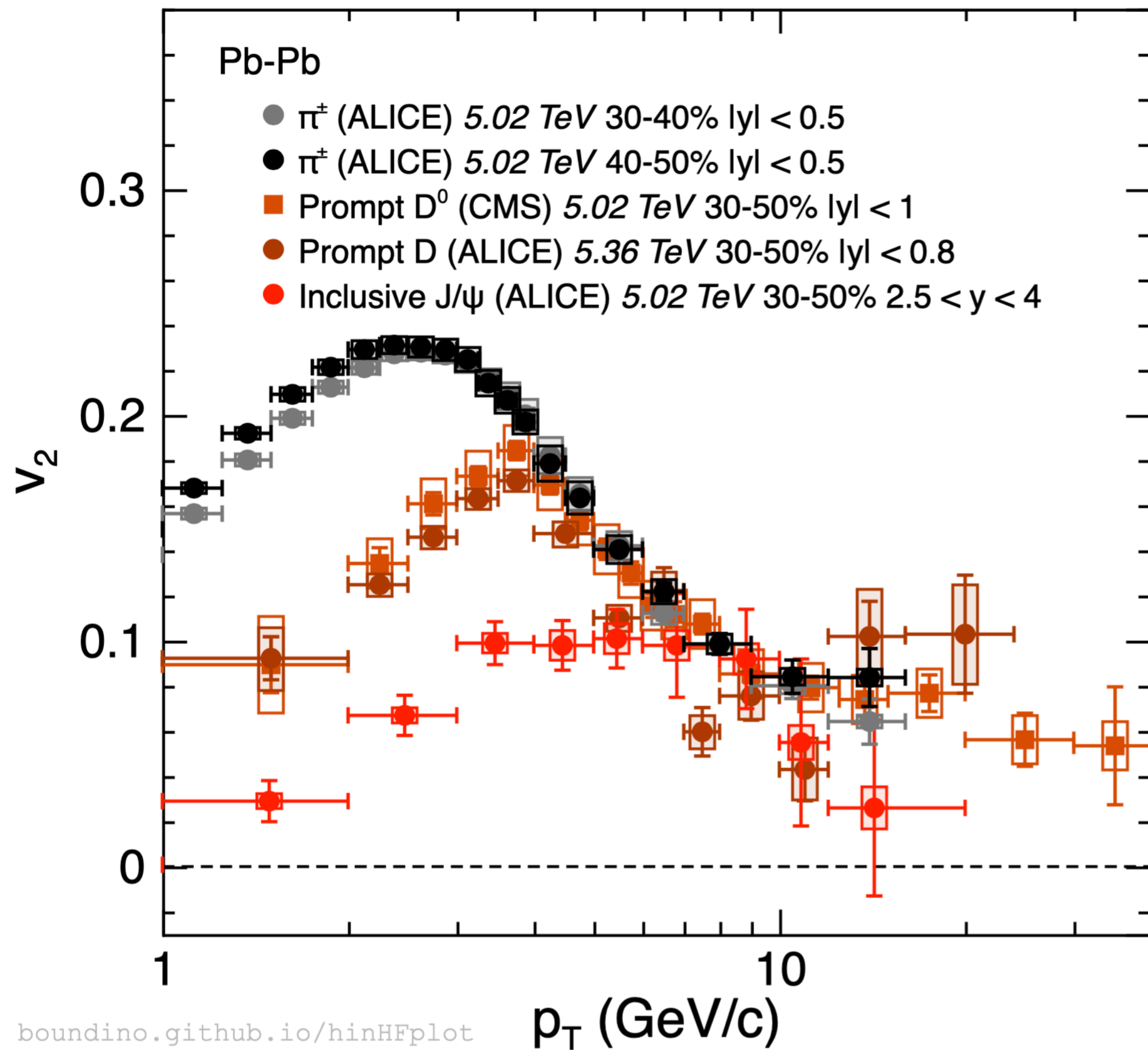
CMS, JHEP 04 (2017) 039

ALICE, JHEP 01 (2022) 174

CMS, PLB 782 (2018) 474

STAR, PRC 99 (2019) 034908

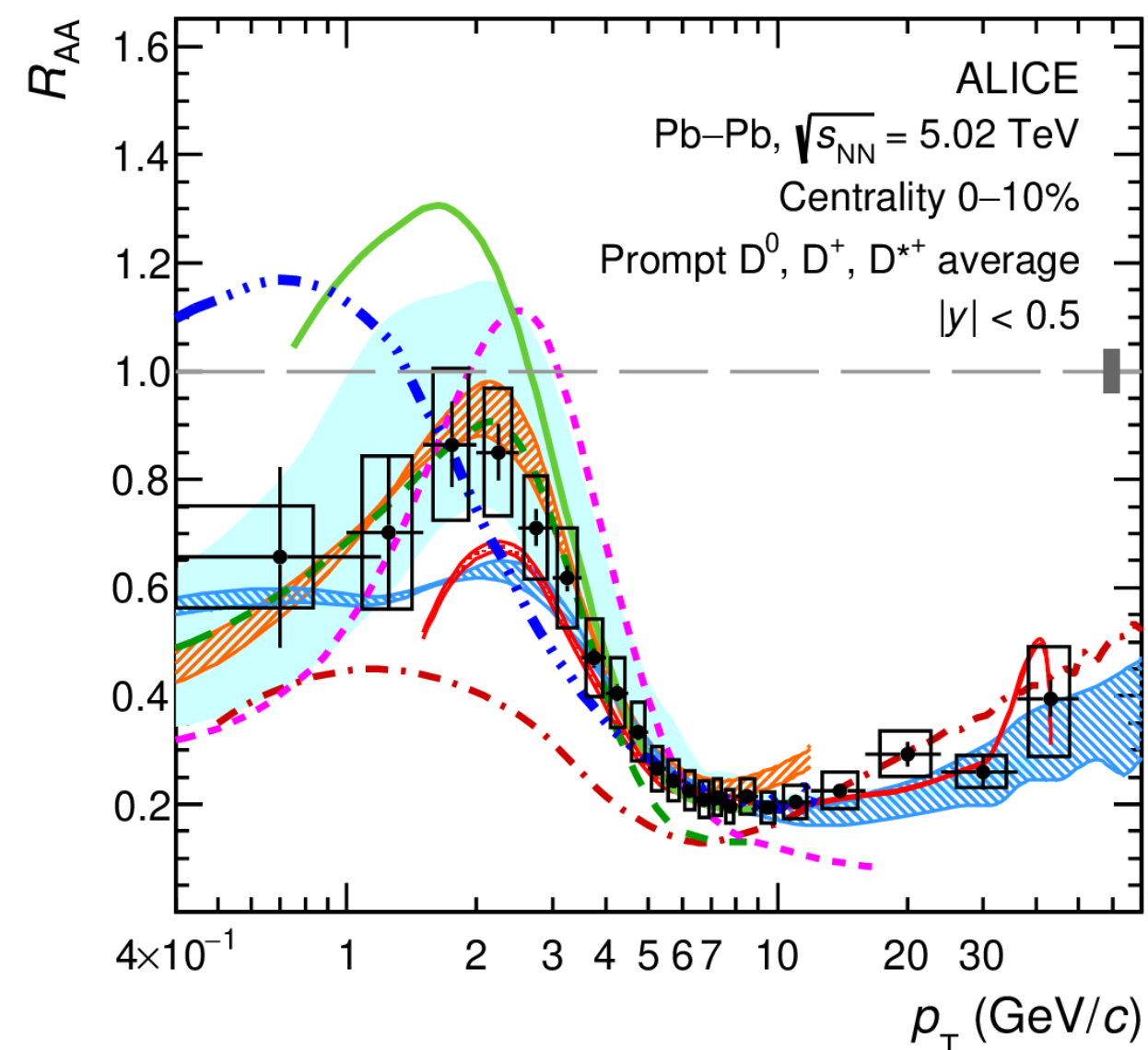
ALI-PUB-501952



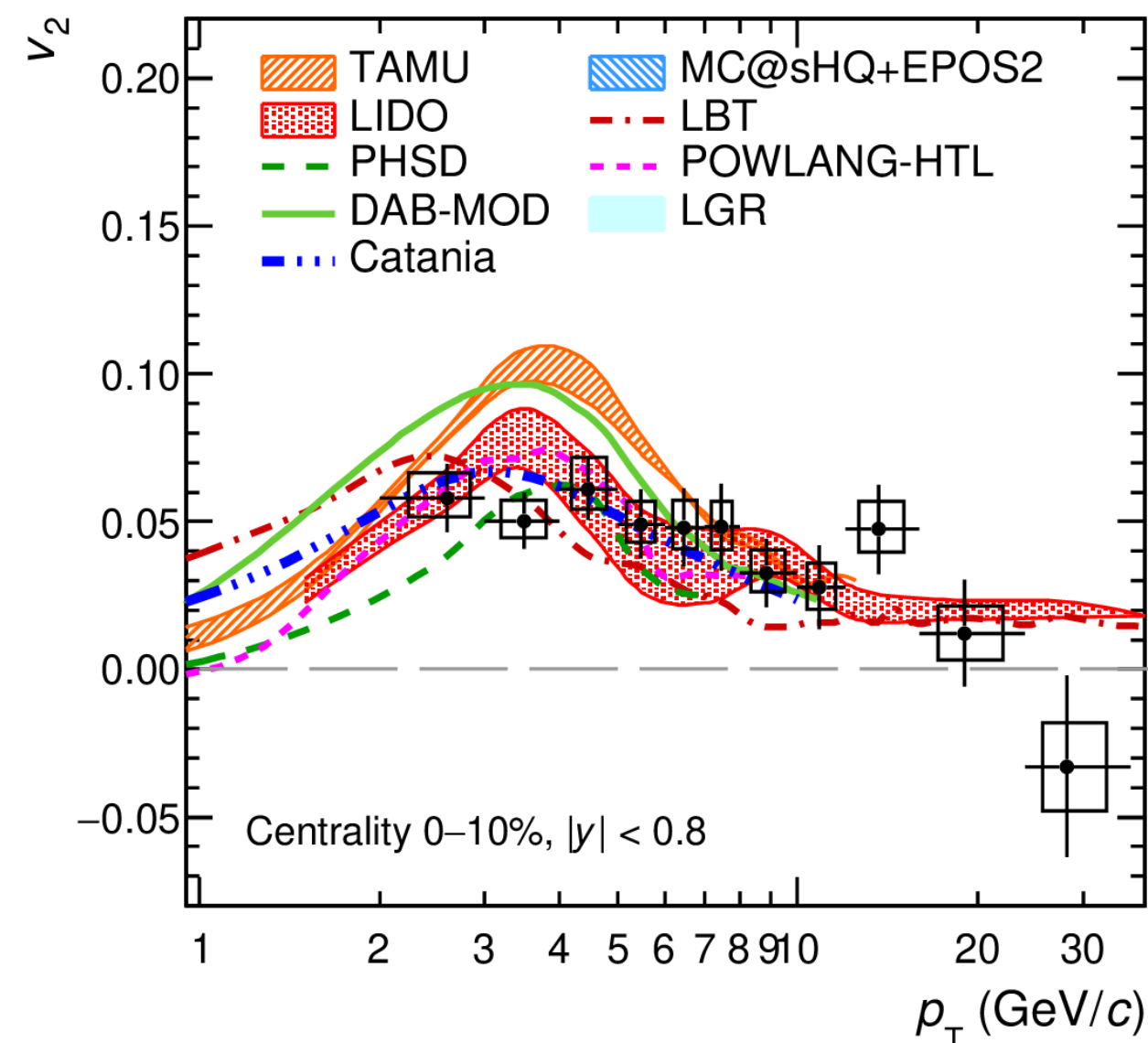
- $p_T < 3$ GeV/c: $v_2(\pi^\pm) > v_2(D) > v_2(J/\psi)$
 - ➔ mass hierarchy due to hydrodynamic expansion indicates that the charm quark is likely to reach at least a partial thermalisation in the QGP
- $3 < p_T < 6$ GeV/c: $v_2(\pi^\pm) \approx v_2(D) > v_2(J/\psi)$
 - ➔ elliptic flow of D mesons similar to that of pions due to the hadronisation via recombination with light quarks from the medium
- $p_T > 6$ GeV/c: $v_2(\pi^\pm) \approx v_2(D) \approx v_2(J/\psi)$
 - ➔ elliptic flow originates from path-length dependent energy loss in the medium

More about J/ψ

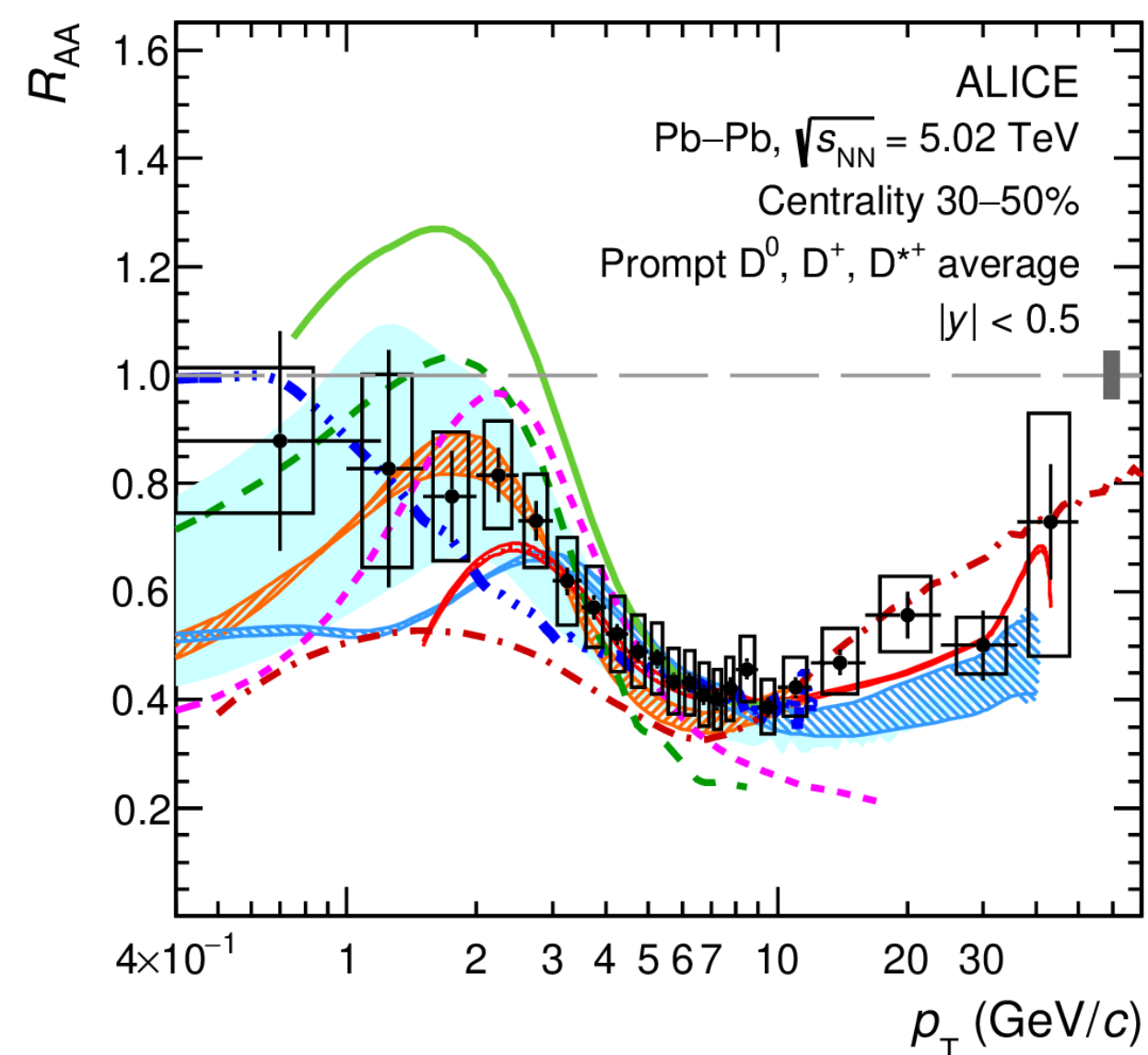
➔ elliptic flow in talk by X. Bai



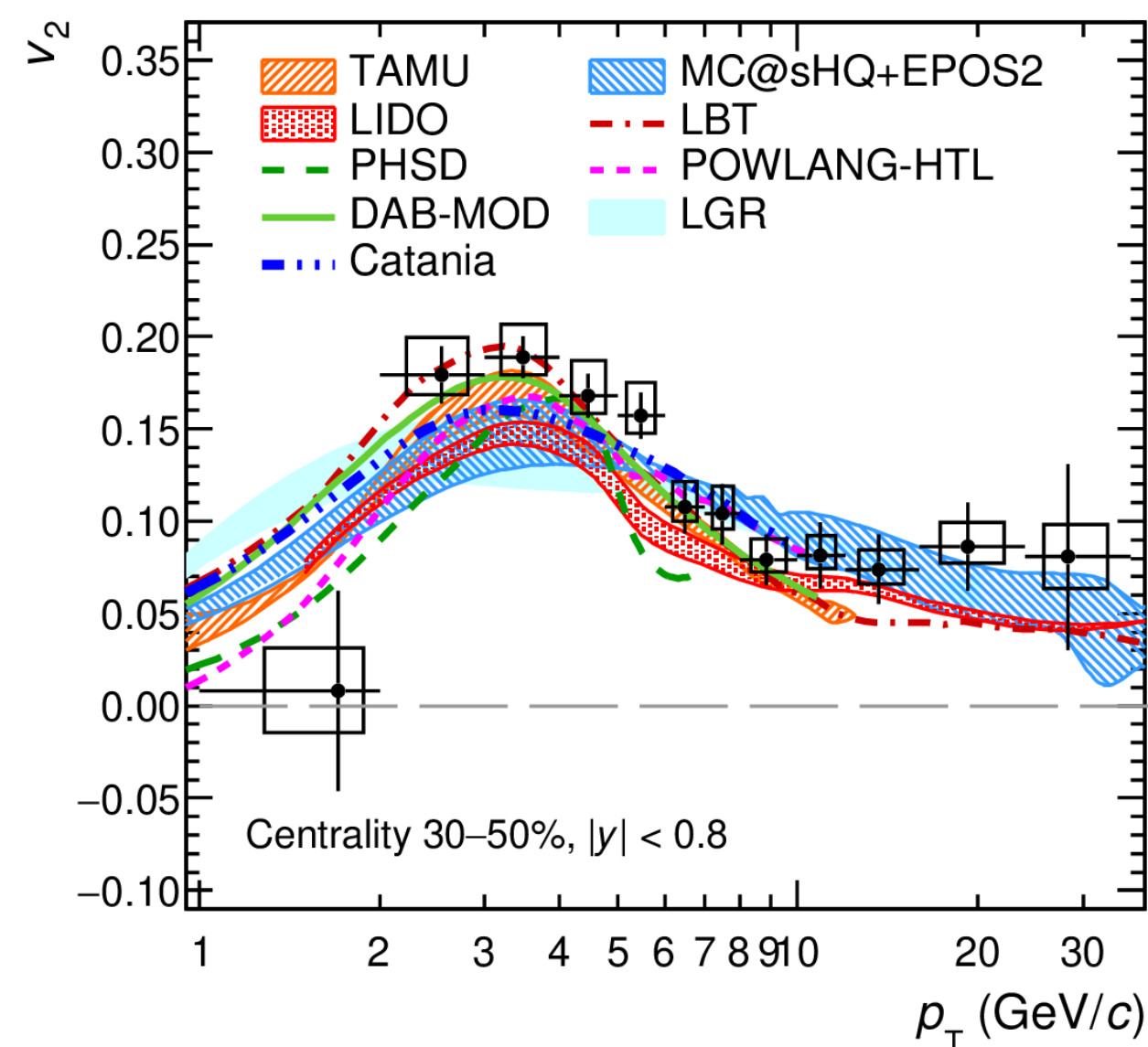
ALI-PUB-501952



- Models based on the charm-quark transport describe reasonably well the measured elliptic and triangular flow of D mesons
 - By selecting those that provide a better agreement with data (in terms of χ^2/ndf) it is possible to constrain the charm-quark spatial diffusion coefficient D_s in the QGP



ALI-PUB-501956



ALICE, JHEP 01 (2022) 174

TAMU: PRL 124 (2020) 042301

MC@sHQ+EPOS2: PRC 89 (2014) 014905

LGR: EPJC, 80 7 (2020) 671

LIDO: PRC 98 (2018) 064901

POWLANG: EPJC (2019) 79:494

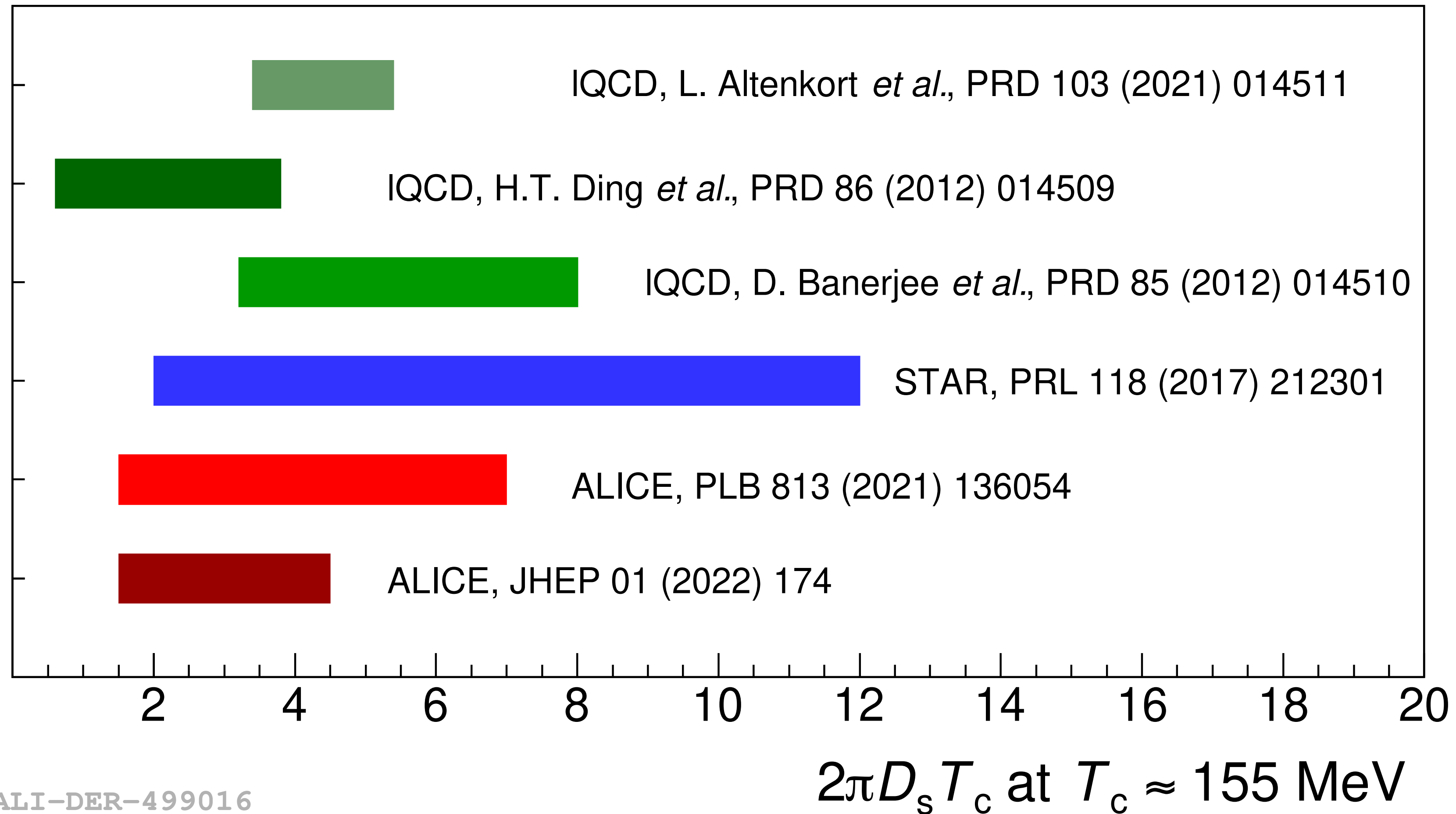
PHSD: PRC 93 (2016) 034906

LBT: PRC 94 (2016) 014909

Catania: PLB 805 (2020) 135460

DAB-MOD: PRC 102 (2020) 024906

ALICE, JHEP 01 (2022) 174

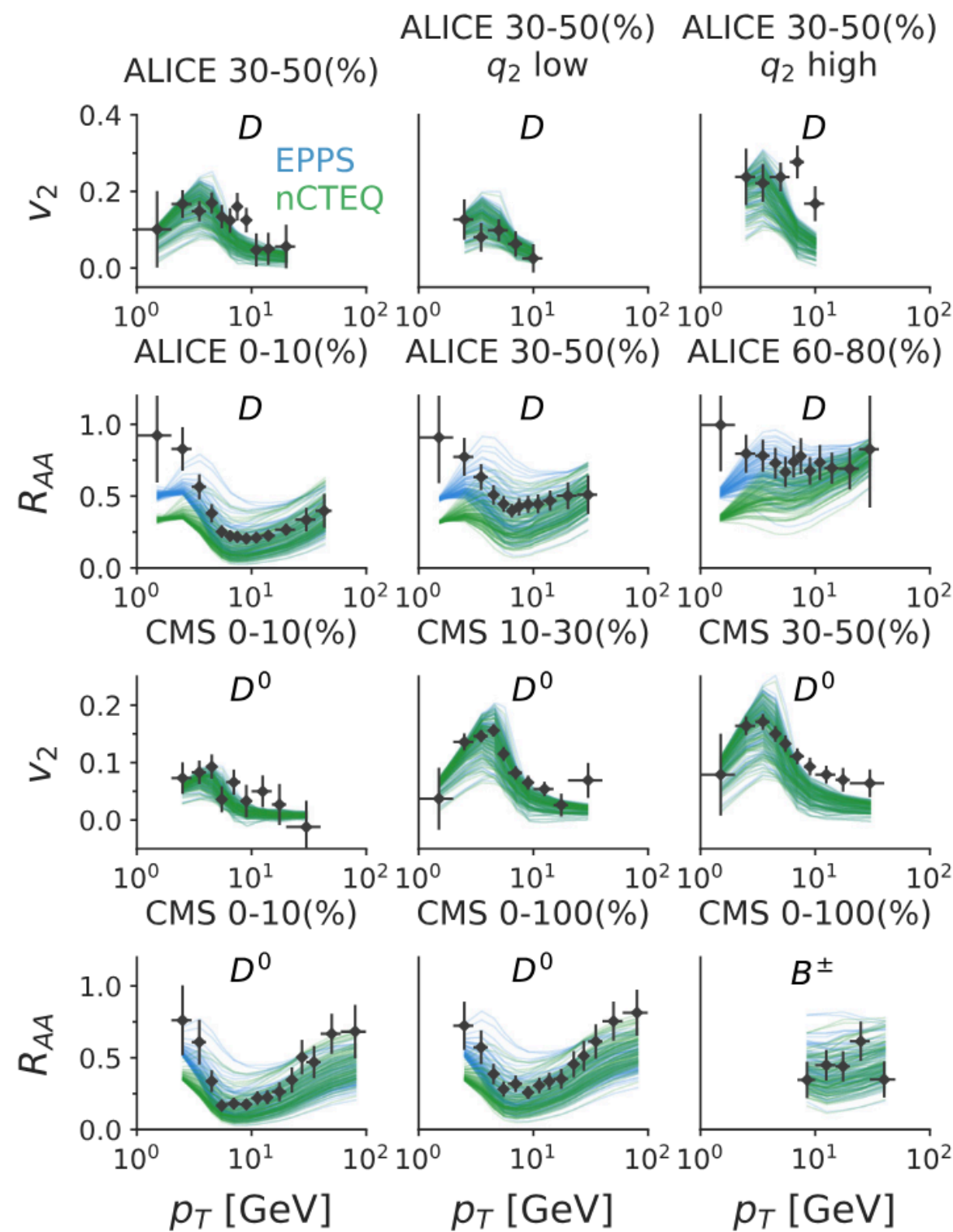


ALI-DER-499016

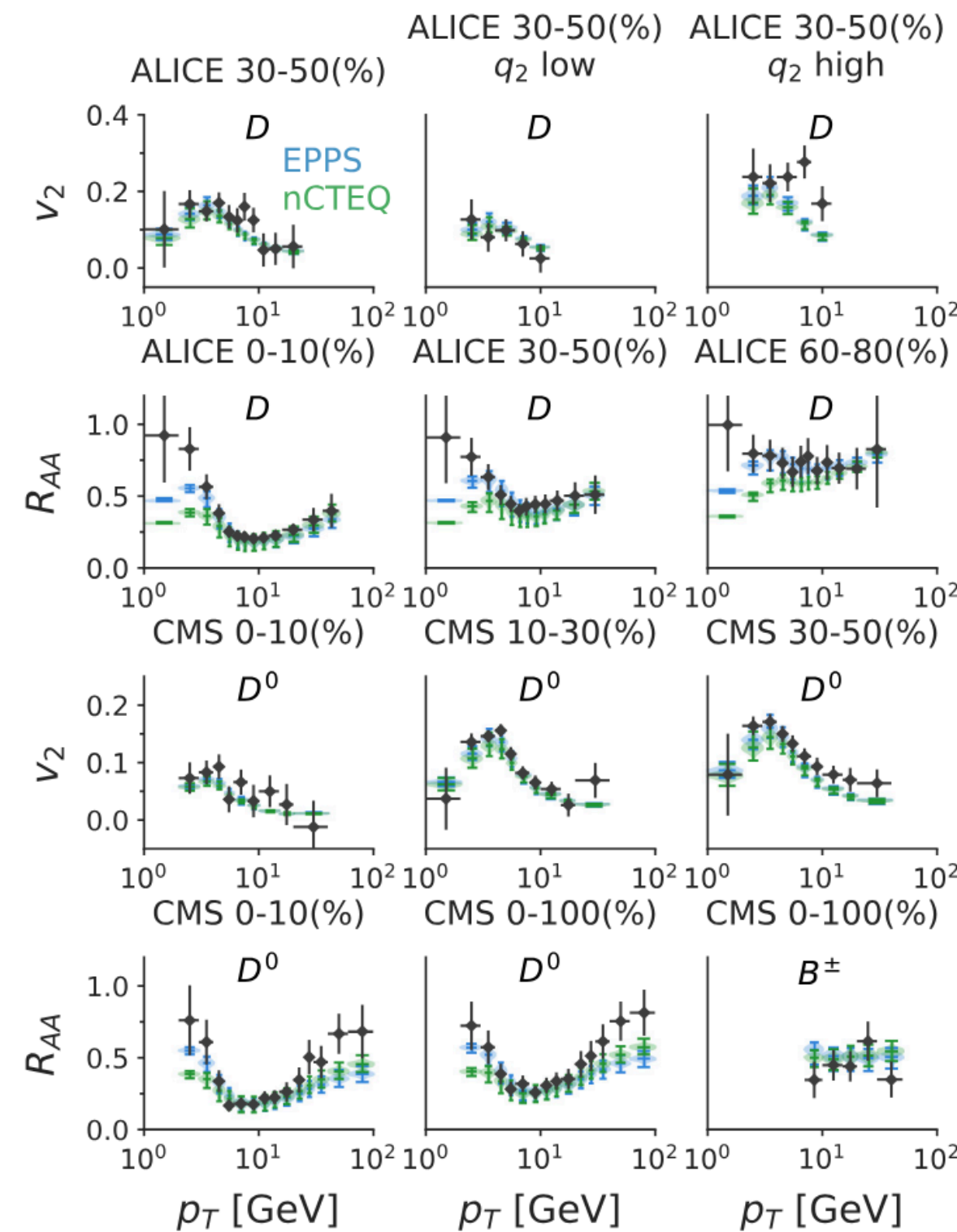
- Interval of spatial diffusion coefficient obtained by considering the values used in the transport models that reproduce the data
 - $1.5 < 2\pi D_s T_c < 4.5$ which corresponds to $2 < \tau_{\text{charm}} < 6$ fm/c
 - Indicates a thermalisation time of the charm quark comparable with the QGP lifetime
 - Compatible with values obtained with QCD calculations on lattice

● Caveat: the spatial diffusion coefficient is not the only parameter that influences the R_{AA} and v_n observables!

Prior distributions



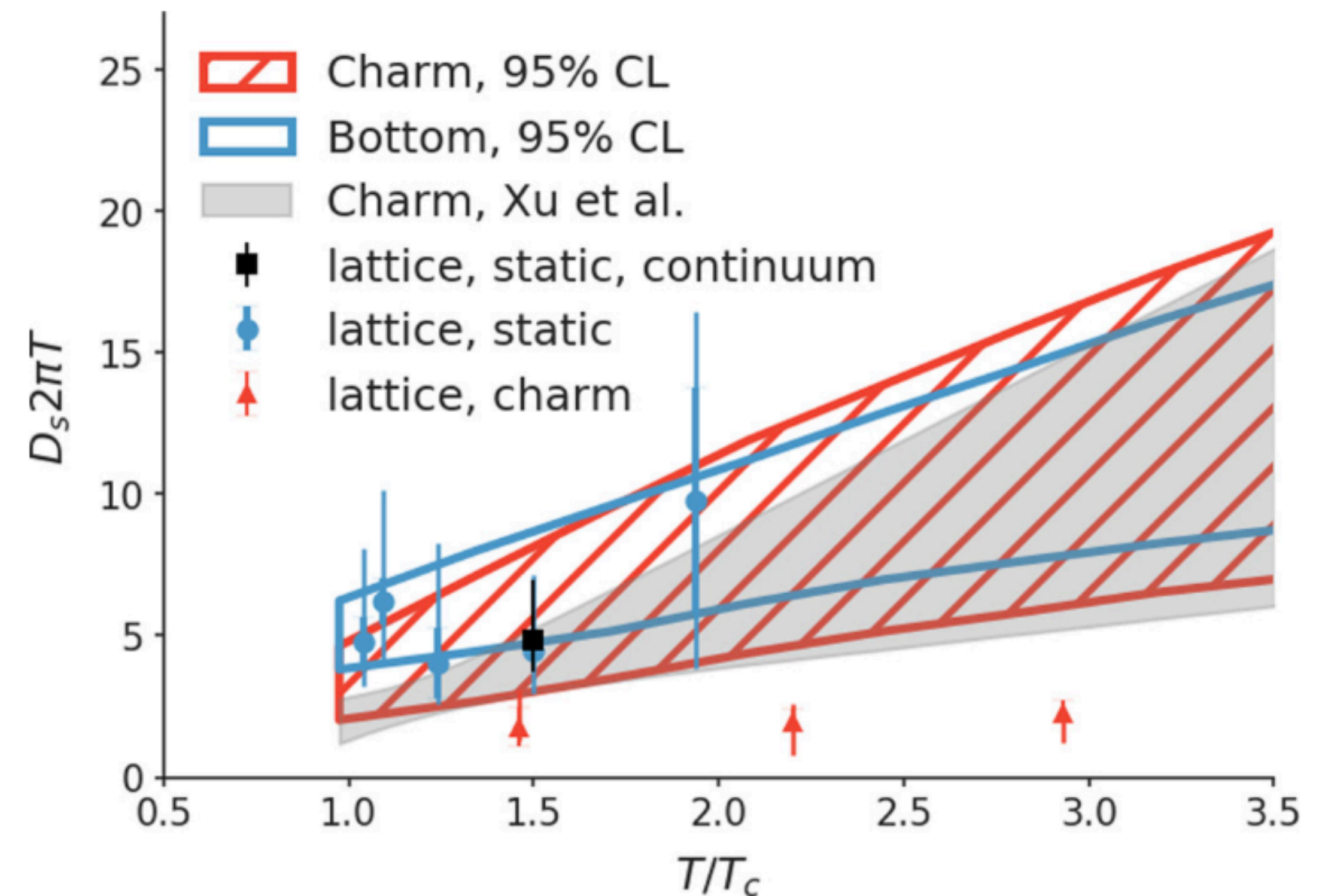
Posterior distributions

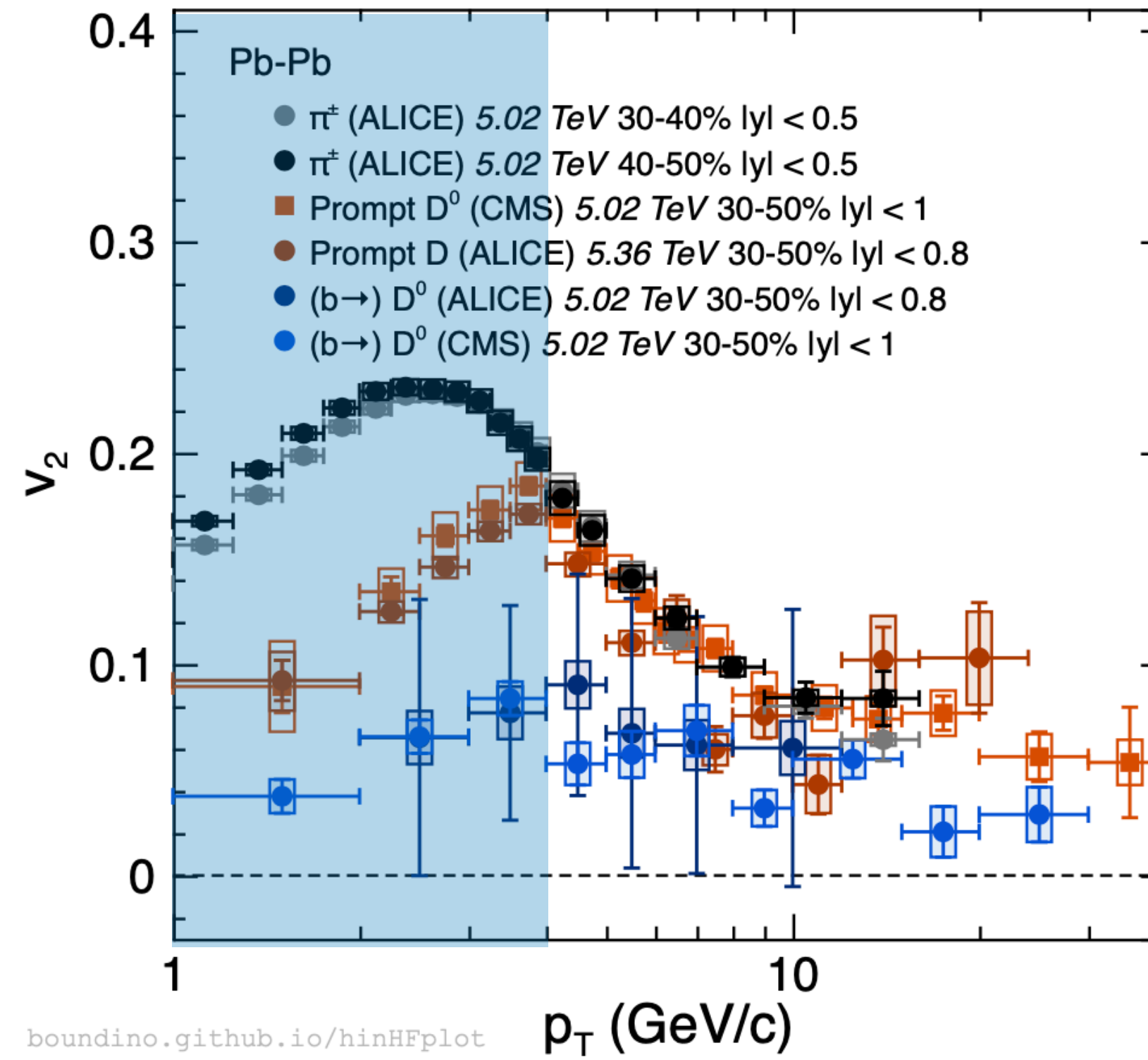
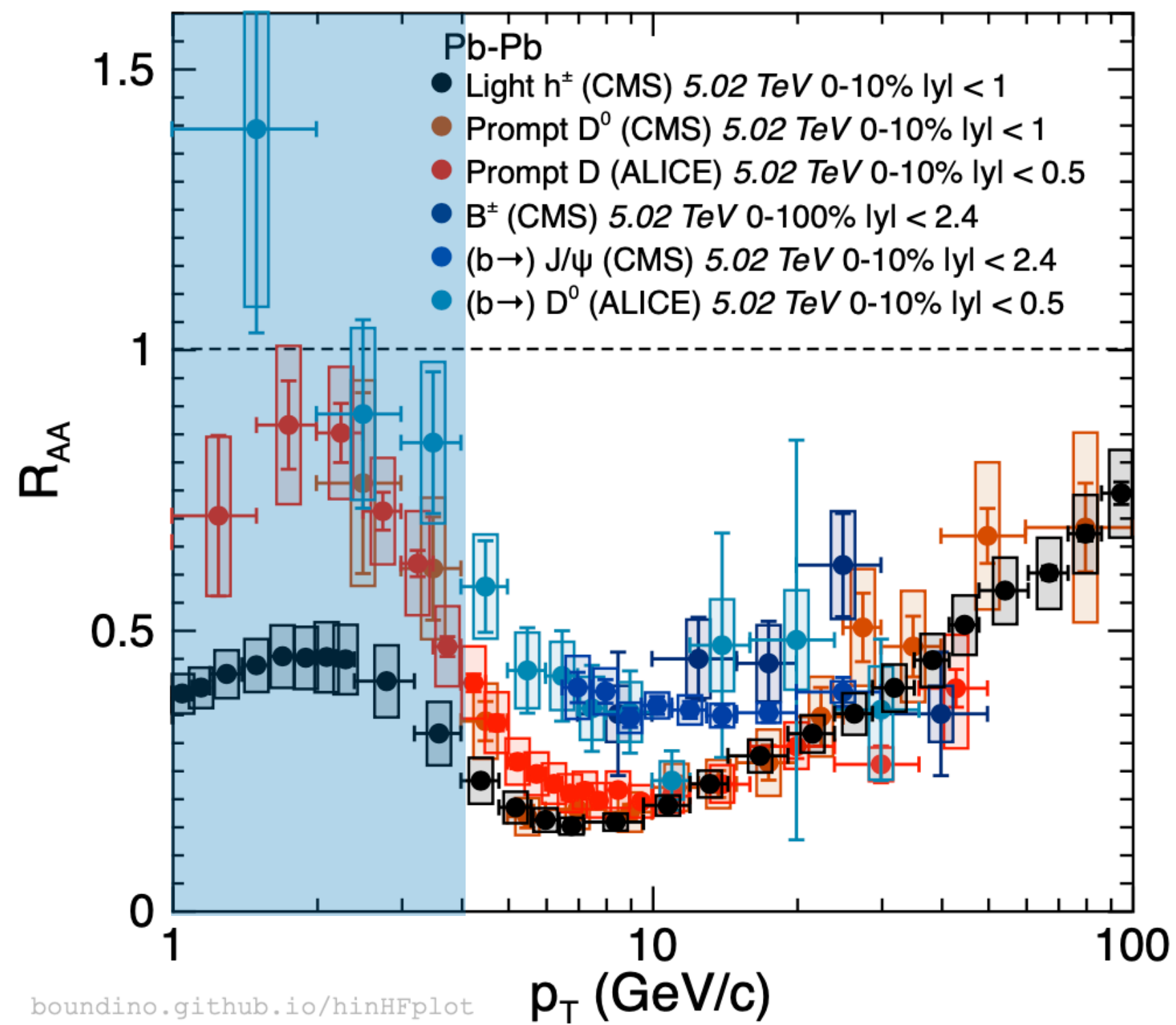


W. Ke et al, PRC 98 (2018) no.6, 064901

- To have a proper determination of the spatial diffusion coefficient, a **global (e.g. bayesian) analysis** of several measurements is needed

- Posterior distribution of the heavy-quark spatial diffusion coefficient
 - ➔ Compatible between charm and beauty
 - ➔ Still large uncertainty (beauty ~ charm even if many less and less precise observables) ➔ **beauty crucial to constrain D_s**





● $p_T < 3-4$ GeV/c:

→ $R_{AA}(B) \approx R_{AA}(D) > R_{AA}(\pi^\pm)$

→ $v_2(B) < v_2(D) < v_2(\pi^\pm)$

📖 CMS, JHEP 04 (2017) 039

📖 CMS, PLB 782 (2018) 474

📖 ALICE, JHEP 01 (2022) 174

📖 CMS, PRL 119 (2017) 152301

📖 CMS, EPJC 78 (2018) 509

📖 ALICE, JHEP 12 (2022) 126

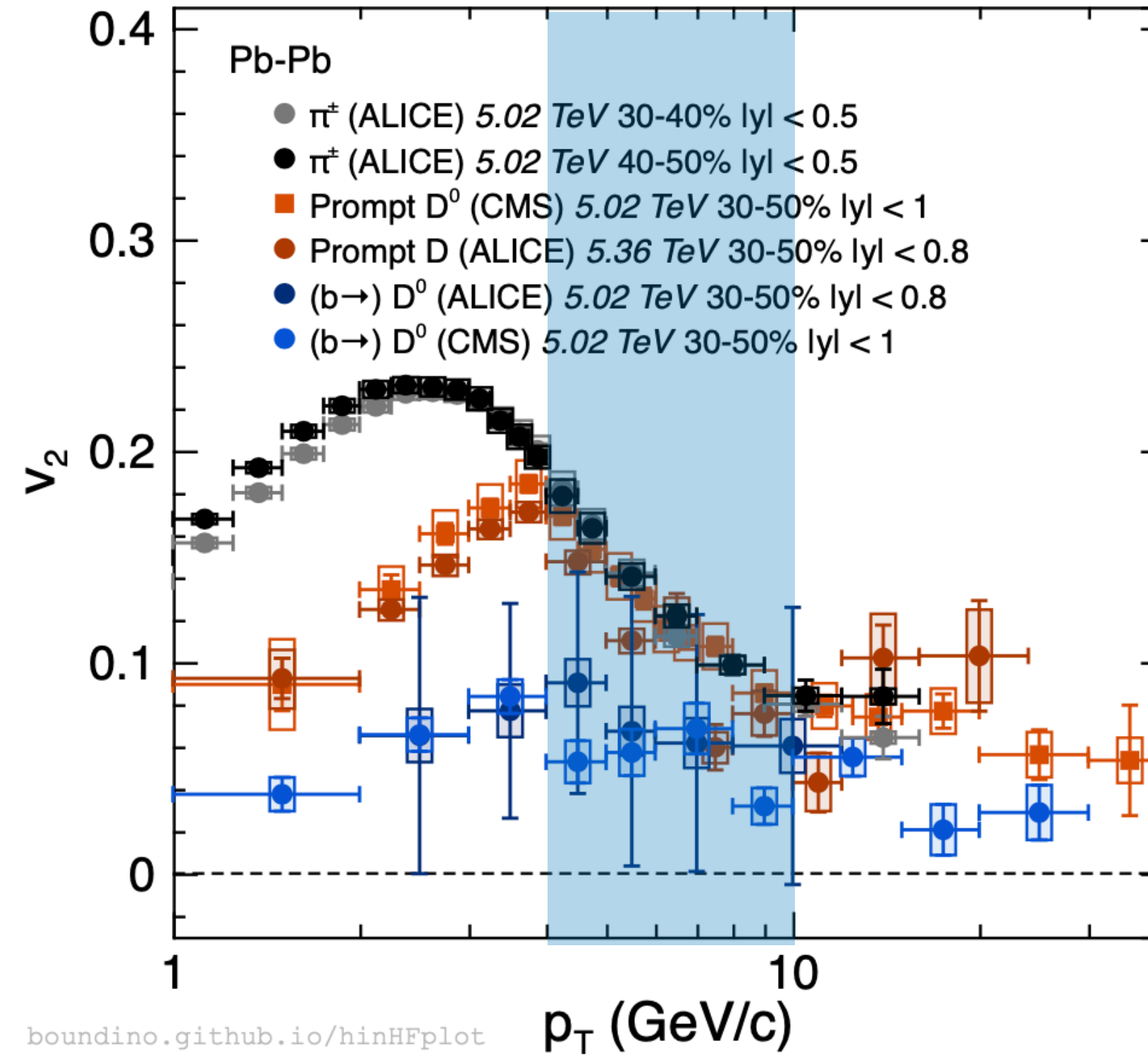
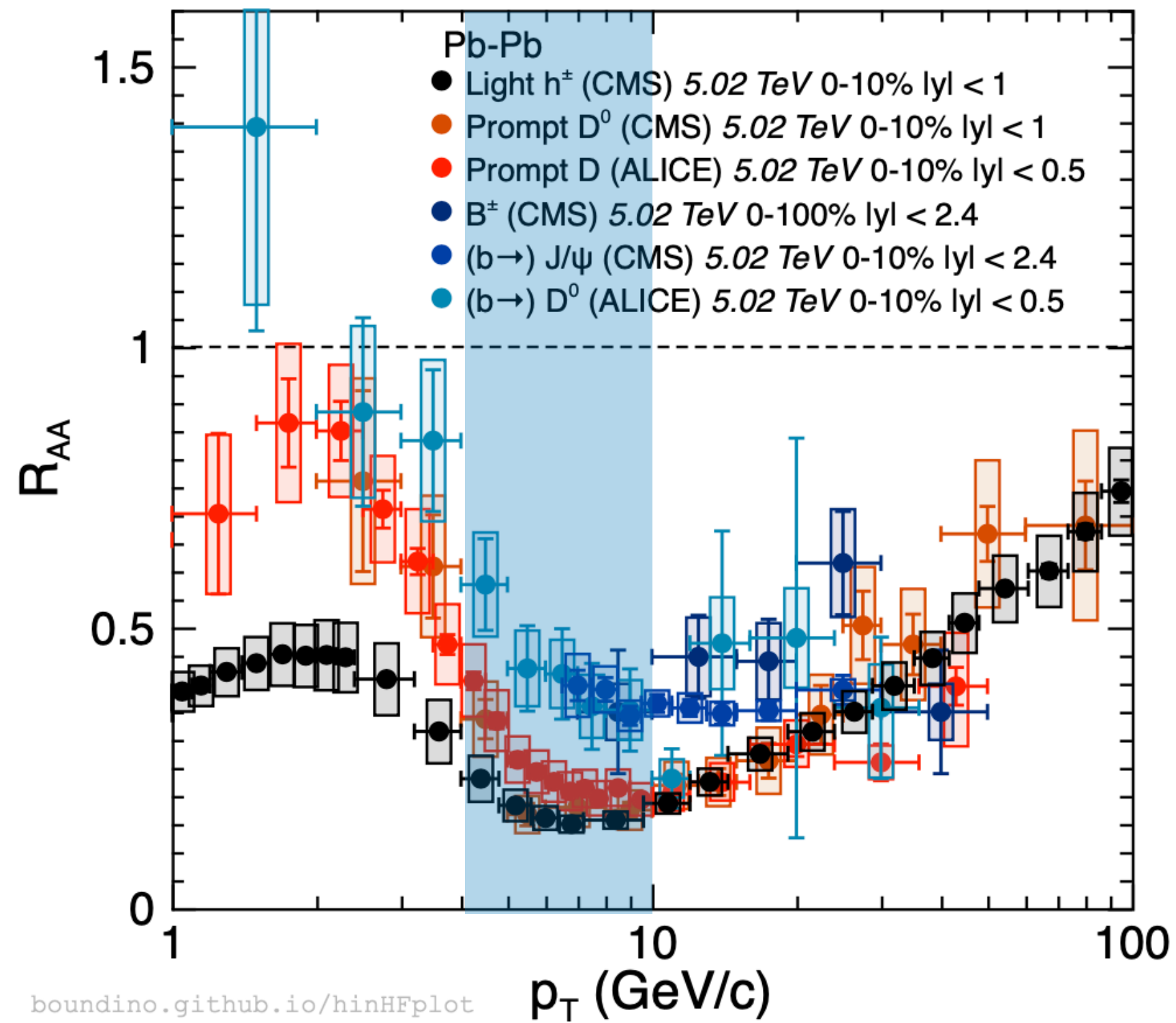
📖 ALICE, JHEP 09 (2018) 006

📖 CMS, PLB 816 (2021) 136253

📖 ALICE Preliminary

📖 CMS, PLB 850 (2024) 138389

📖 ALICE, EPJC 83 (2023) 1123



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📄 CMS, JHEP 04 (2017) 039

📄 CMS, PLB 782 (2018) 474

📄 ALICE, JHEP 01 (2022) 174

📄 CMS, PRL 119 (2017) 152301

📄 CMS, EPJC 78 (2018) 509

📄 ALICE, JHEP 12 (2022) 126

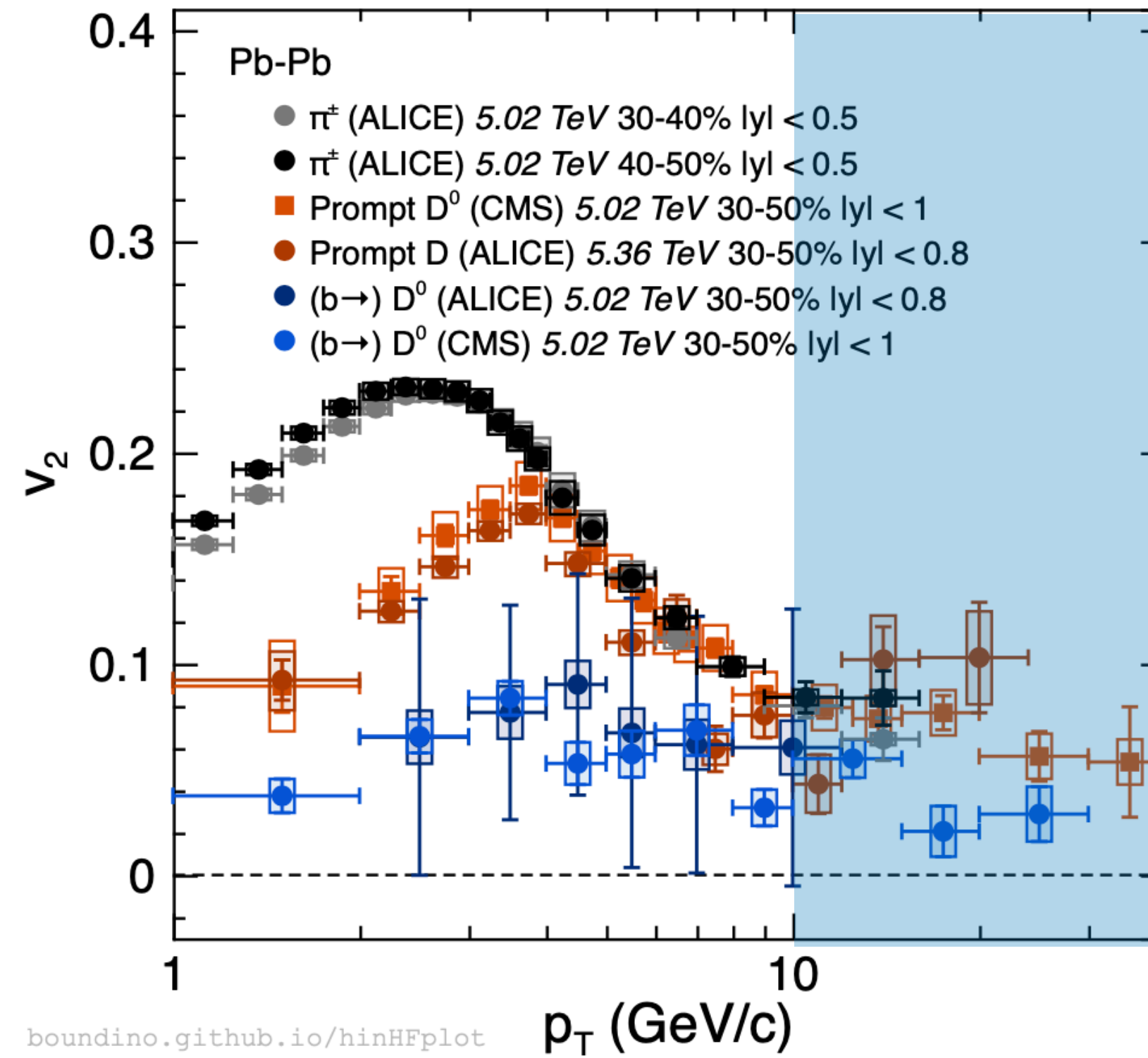
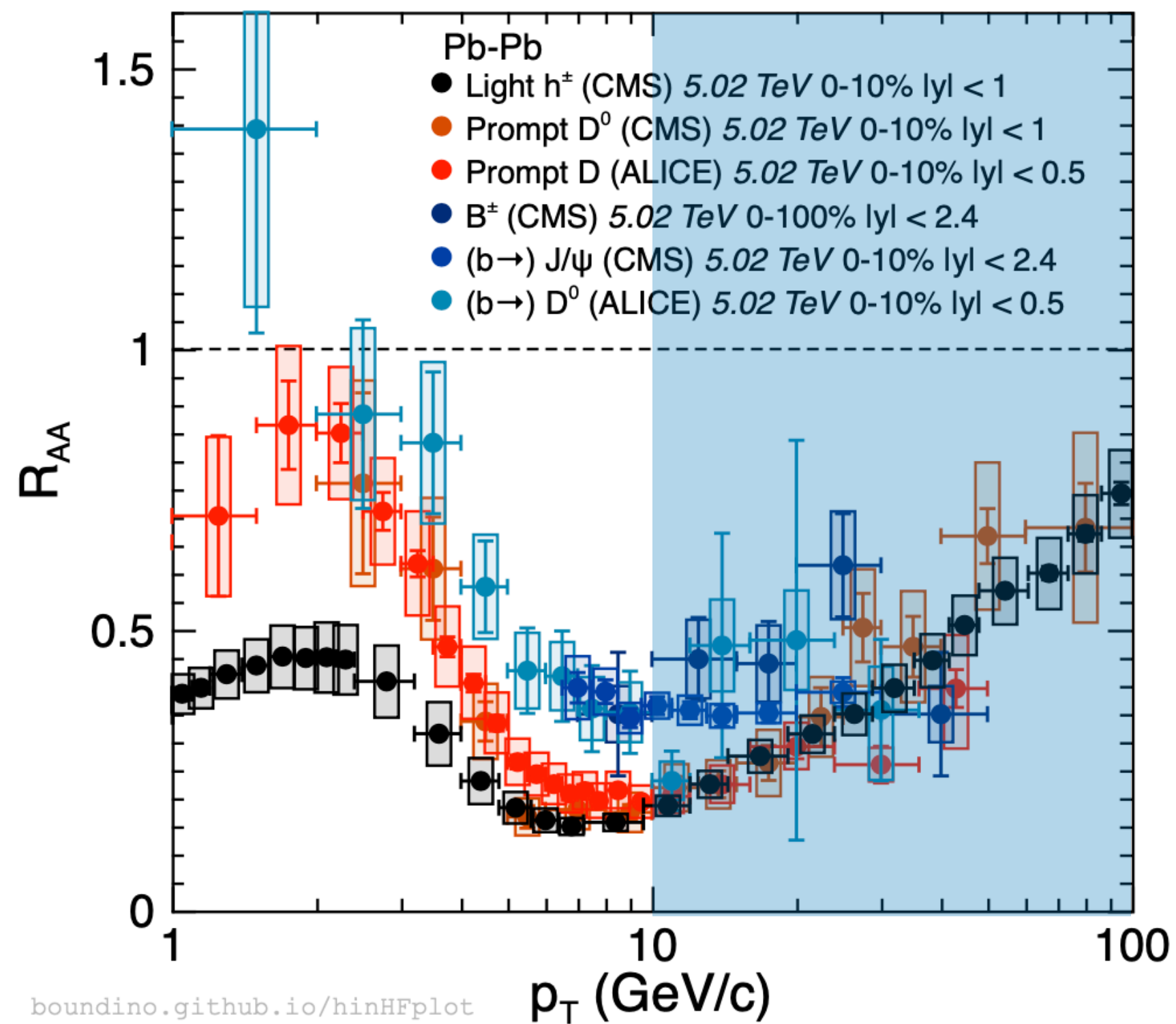
📄 ALICE, JHEP 09 (2018) 006

📄 CMS, PLB 816 (2021) 136253

📄 ALICE Preliminary

📄 CMS, PLB 850 (2024) 138389

📄 ALICE, EPJC 83 (2023) 1123



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📖 CMS, JHEP 04 (2017) 039

📖 CMS, PLB 782 (2018) 474

📖 ALICE, JHEP 01 (2022) 174

📖 CMS, PRL 119 (2017) 152301

📖 CMS, EPJC 78 (2018) 509

📖 ALICE, JHEP 12 (2022) 126

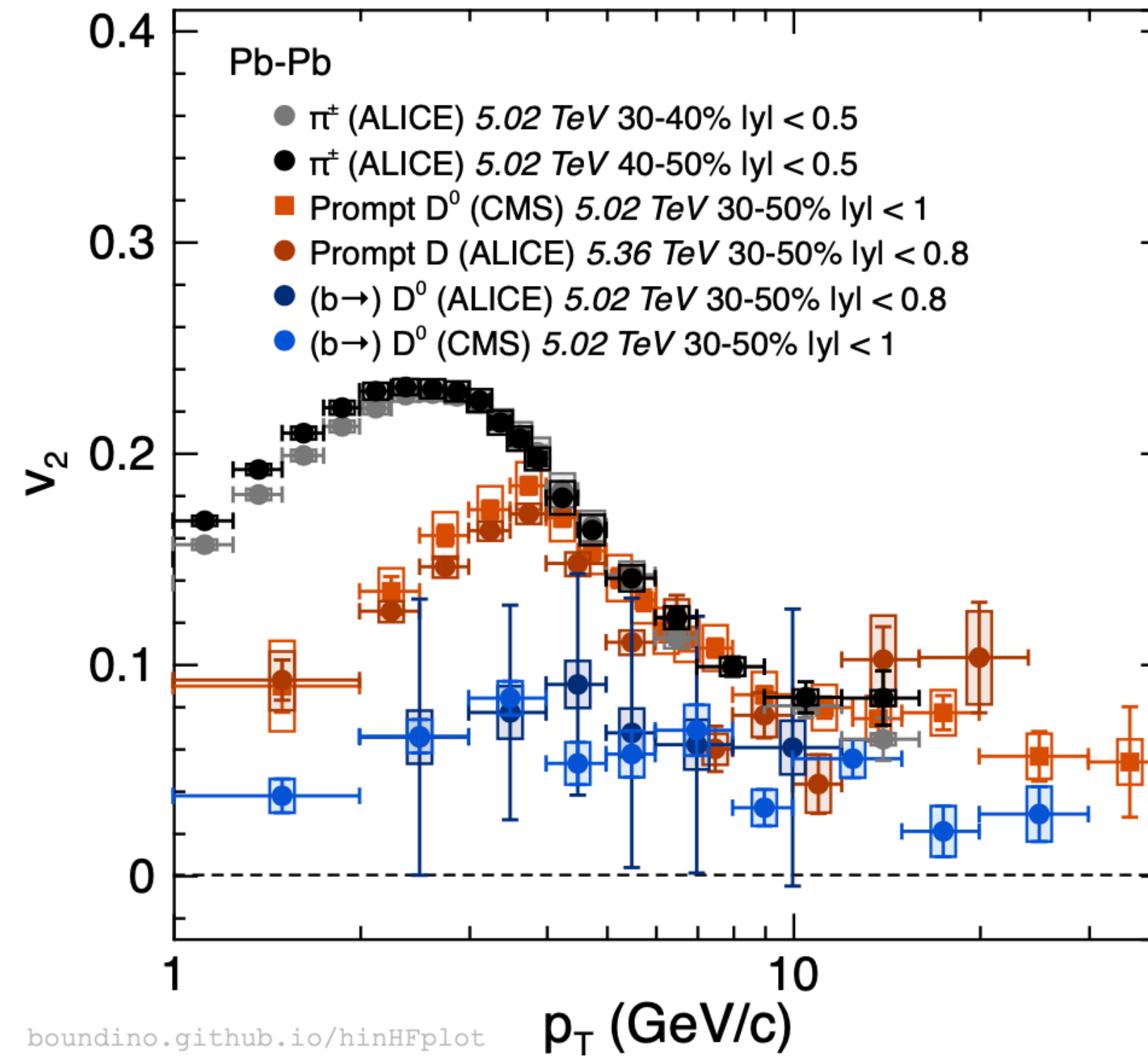
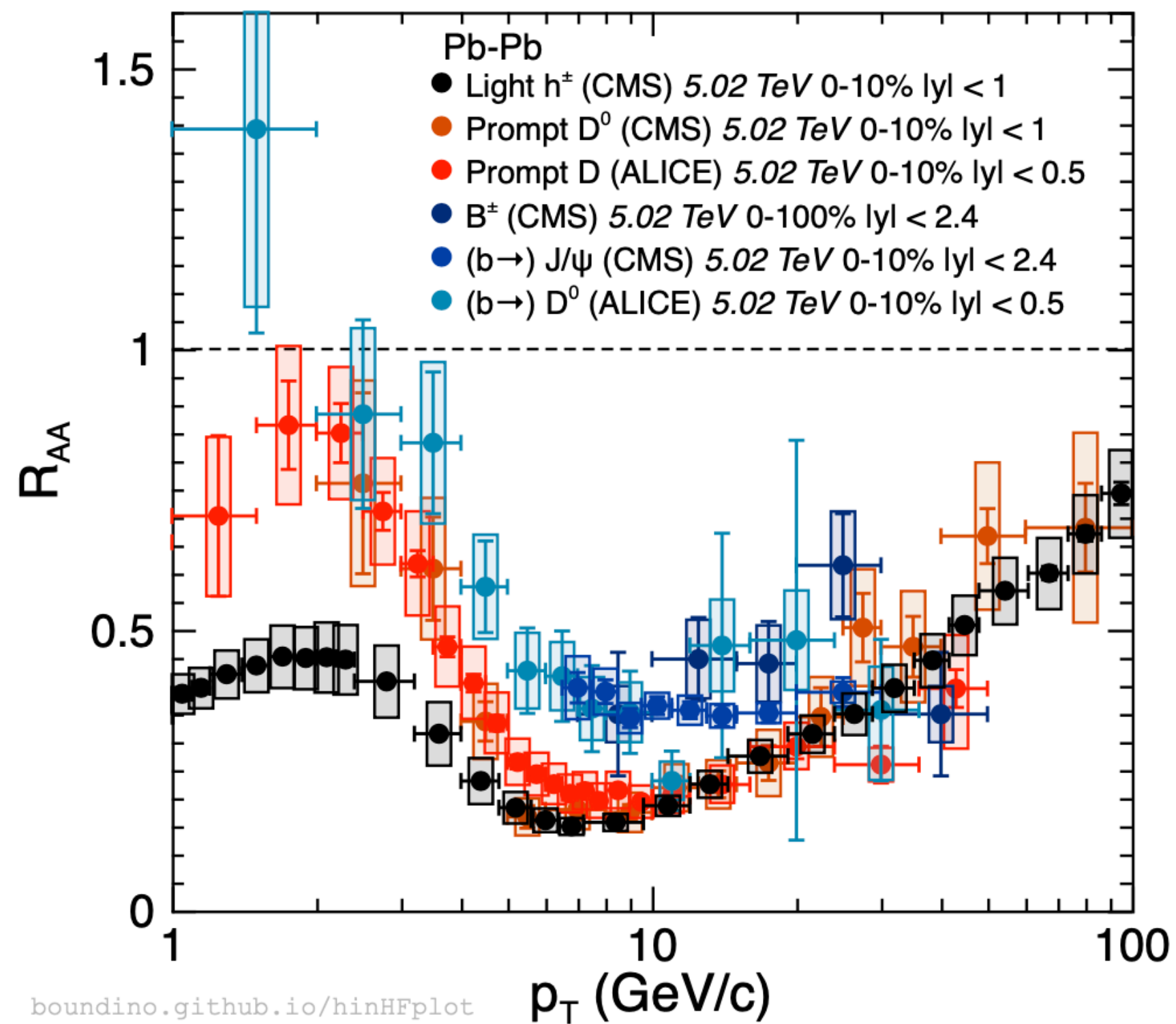
📖 ALICE, JHEP 09 (2018) 006

📖 CMS, PLB 816 (2021) 136253

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📖 ALICE, EPJC 83 (2023) 1123



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📖 CMS, JHEP 04 (2017) 039

📖 CMS, PLB 782 (2018) 474

📖 ALICE, JHEP 01 (2022) 174

📖 CMS, PRL 119 (2017) 152301

📖 CMS, EPJC 78 (2018) 509

📖 ALICE, JHEP 12 (2022) 126

📖 ALICE, JHEP 09 (2018) 006

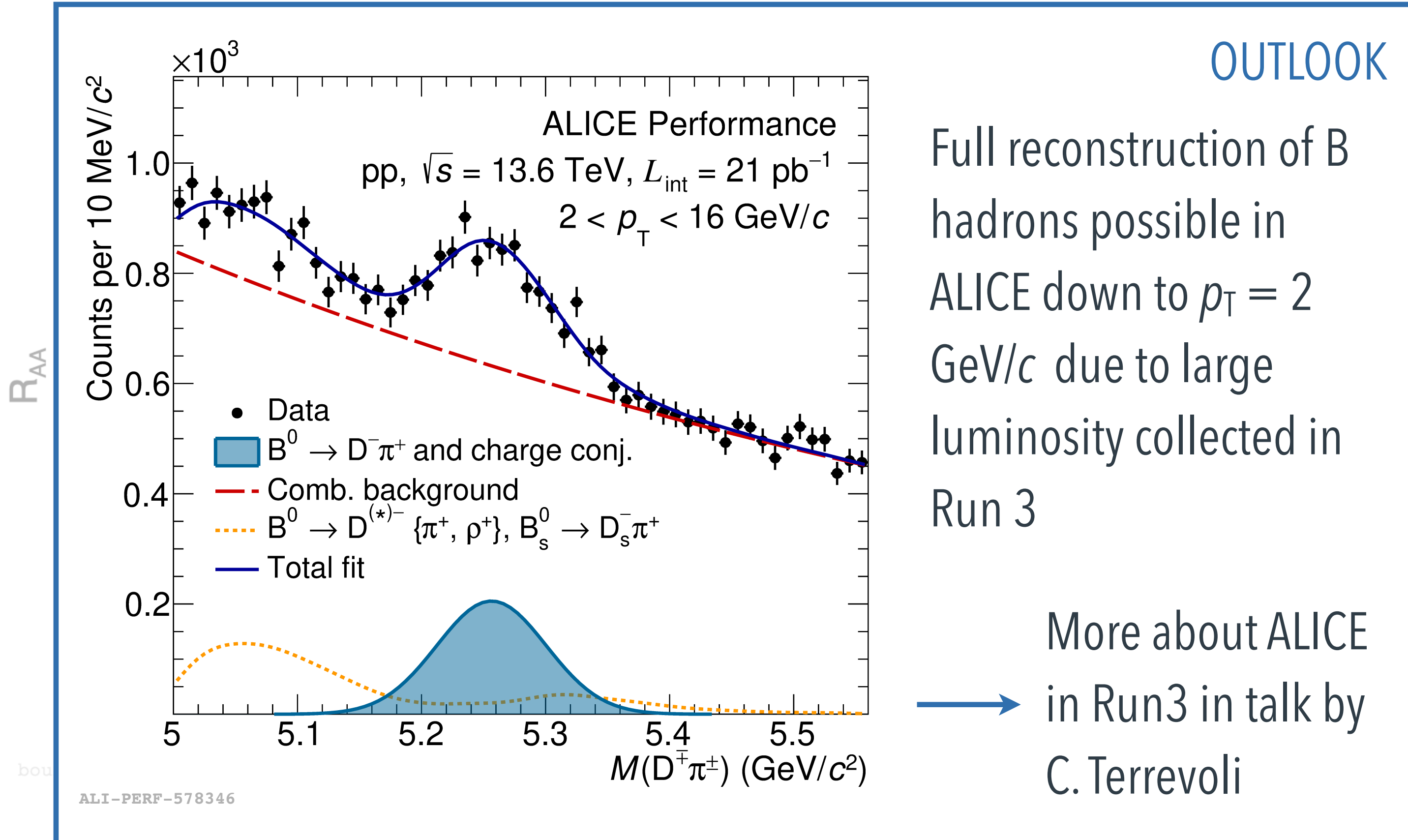
📖 CMS, PLB 816 (2021) 136253

📖 ALICE Preliminary

📖 CMS, PLB 850 (2024) 138389

📖 ALICE, EPJC 83 (2023) 1123

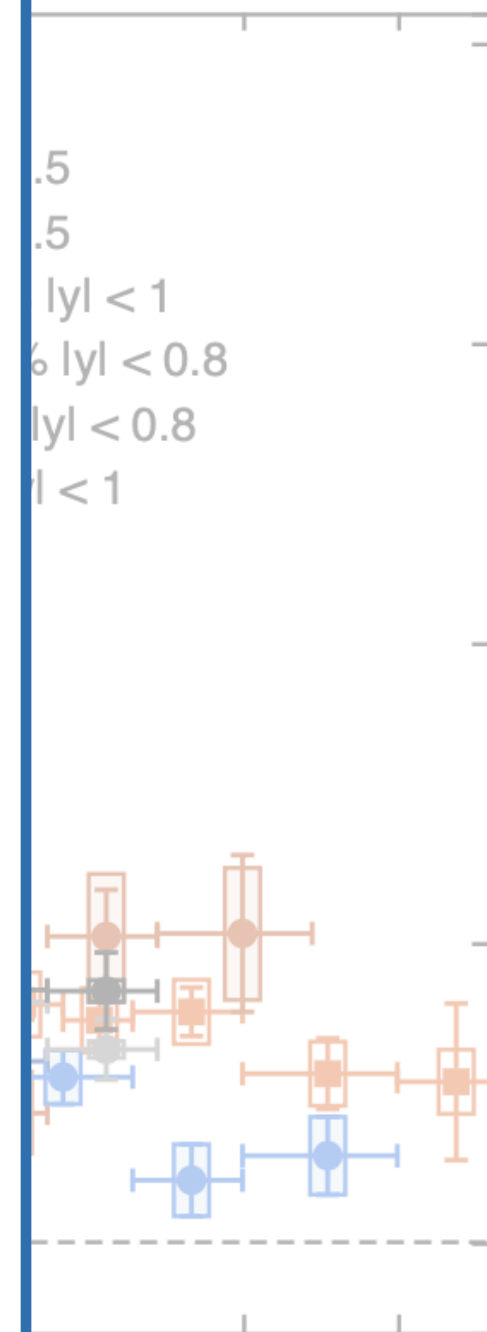
- Most of the measurements related to beauty currently indirect **via non-prompt charm hadrons** (only B fully reconstructed from CMS for $p_T > 7$ GeV/c)
 - Possible effects due to decay kinematics (shift in p_T)
 - Need of properly modelling to extract physics message



OUTLOOK

Full reconstruction of B hadrons possible in ALICE down to $p_T = 2$ GeV/c due to large luminosity collected in Run 3

More about ALICE in Run3 in talk by C. Terrevoli



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CMS, JHEP 04 (2017) 039

CMS, PLB 782 (2018) 474

ALICE, JHEP 01 (2022) 174

CMS, PRL 119 (2017) 152301

CMS, EPJC 78 (2018) 509

ALICE, JHEP 12 (2022) 126

ALICE, JHEP 09 (2018) 006

CMS, PLB 816 (2021) 136253

ALICE Preliminary

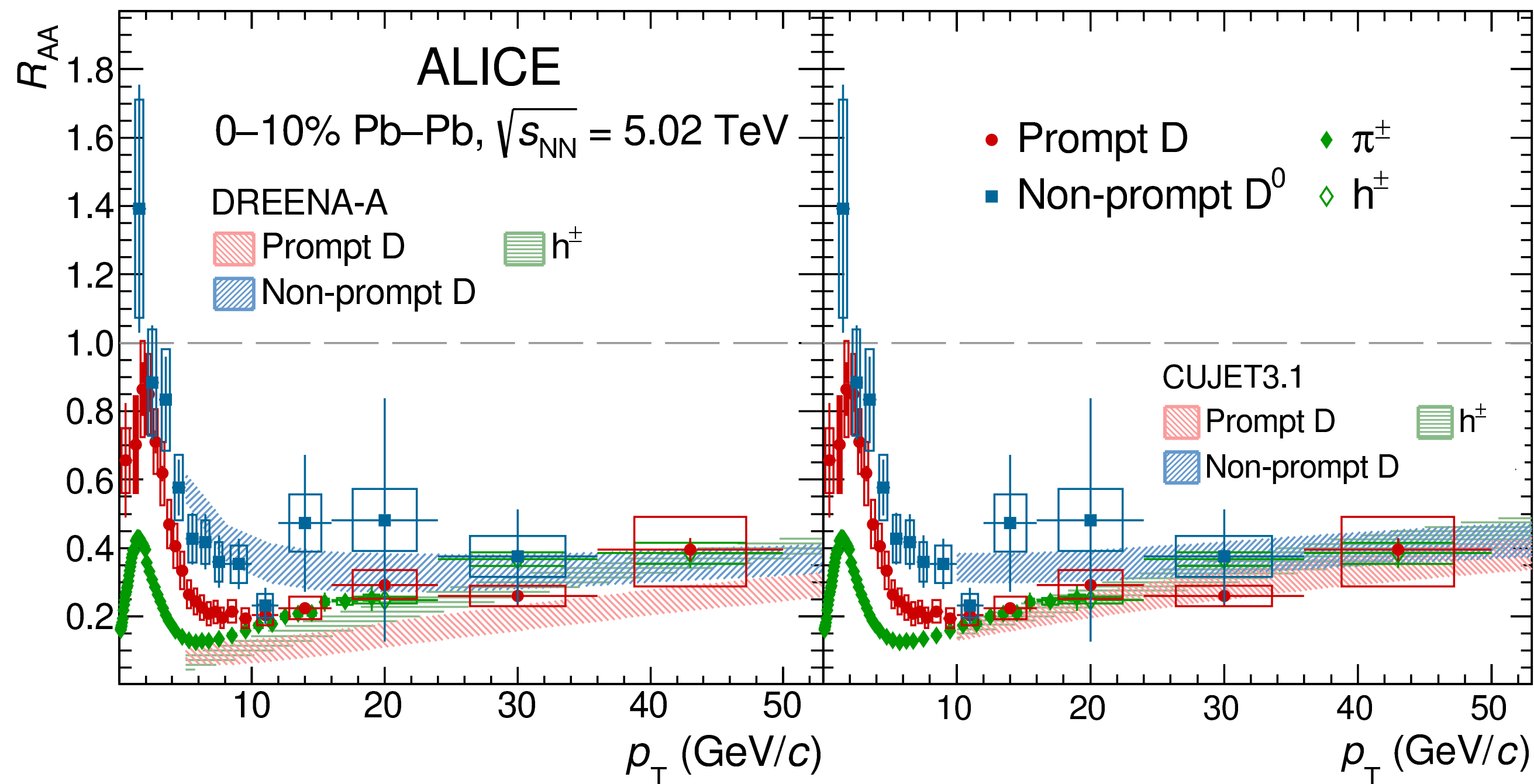
CMS, PLB 850 (2024) 138389

ALICE, EPJC 83 (2023) 1123

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ALICE, EPJC 84 (2024) 813

CMS, arXiv:2409.07258

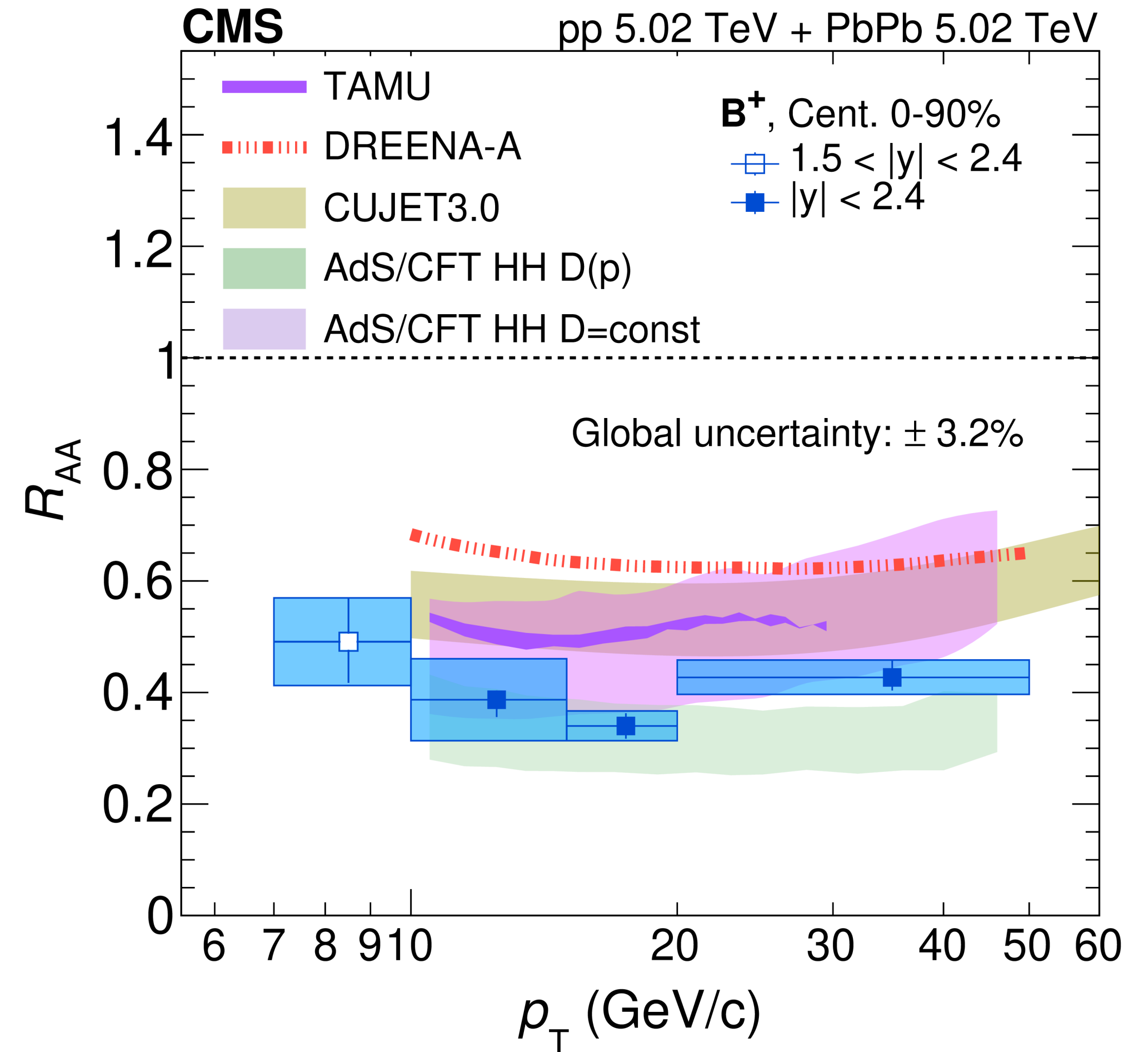


ALI-PUB-531169

- Expected hierarchy from dead-cone effect

$$R_{AA}(B) > R_{AA}(D) \gtrsim R_{AA}(\pi^\pm)$$

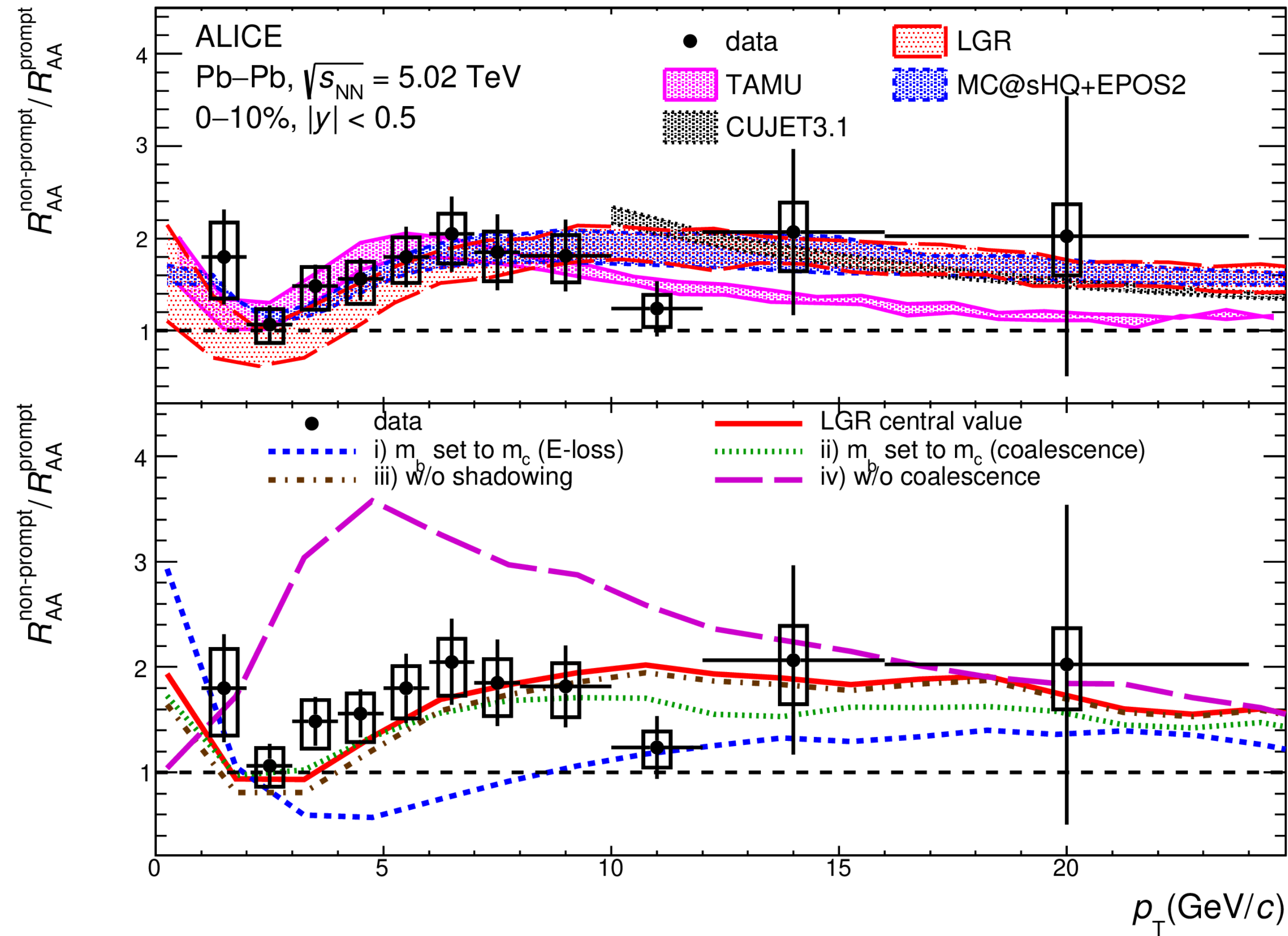
- Constrain pQCD inspired models including energy loss via radiative processes



TAMU: PRL 124 (2020) 042301
CUJET3: CPC 43 (2019) 044101



DREENA-A: Front. Phys. 10 (2022) 957019
Ads/CFT: arXiv:1703.05845

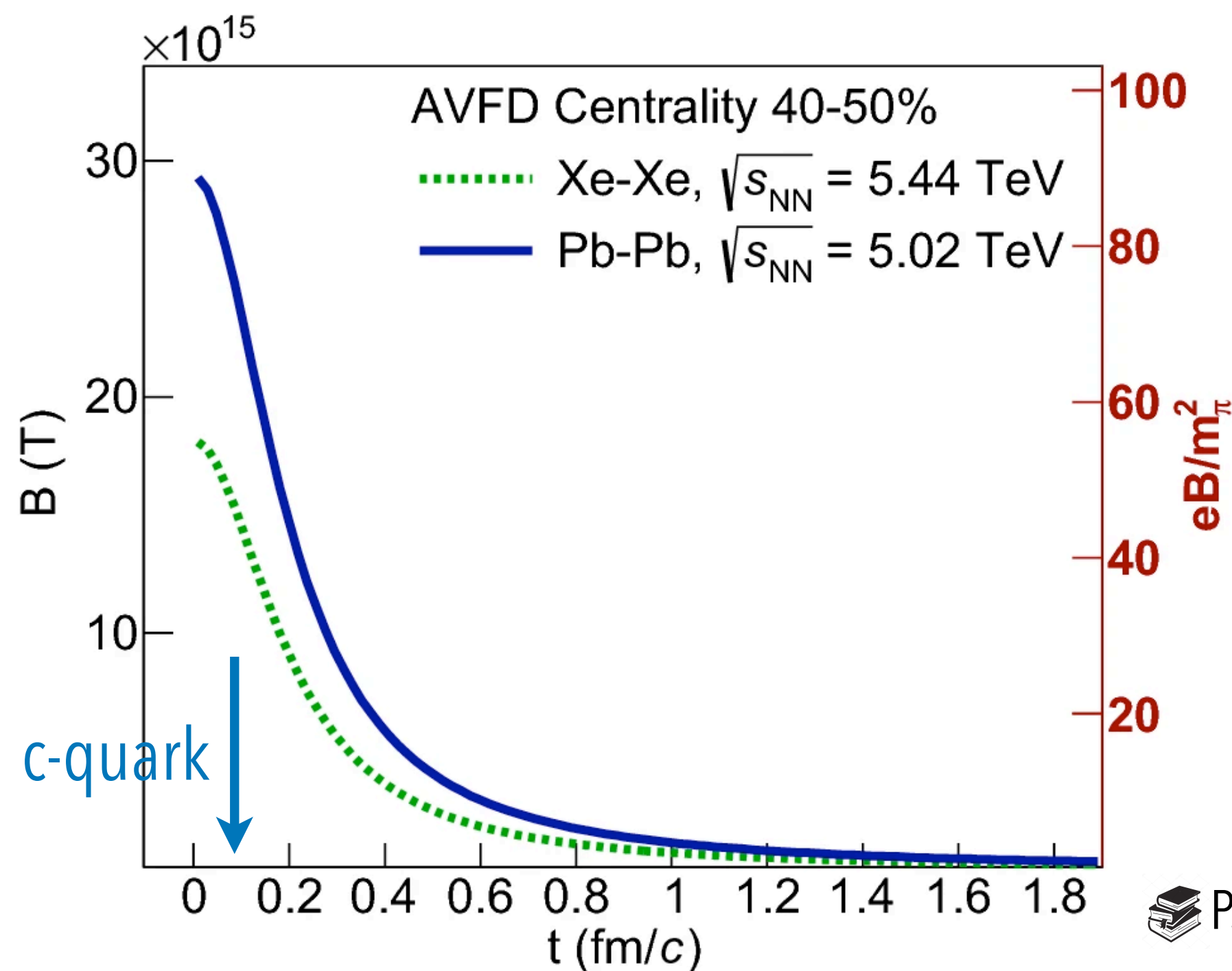
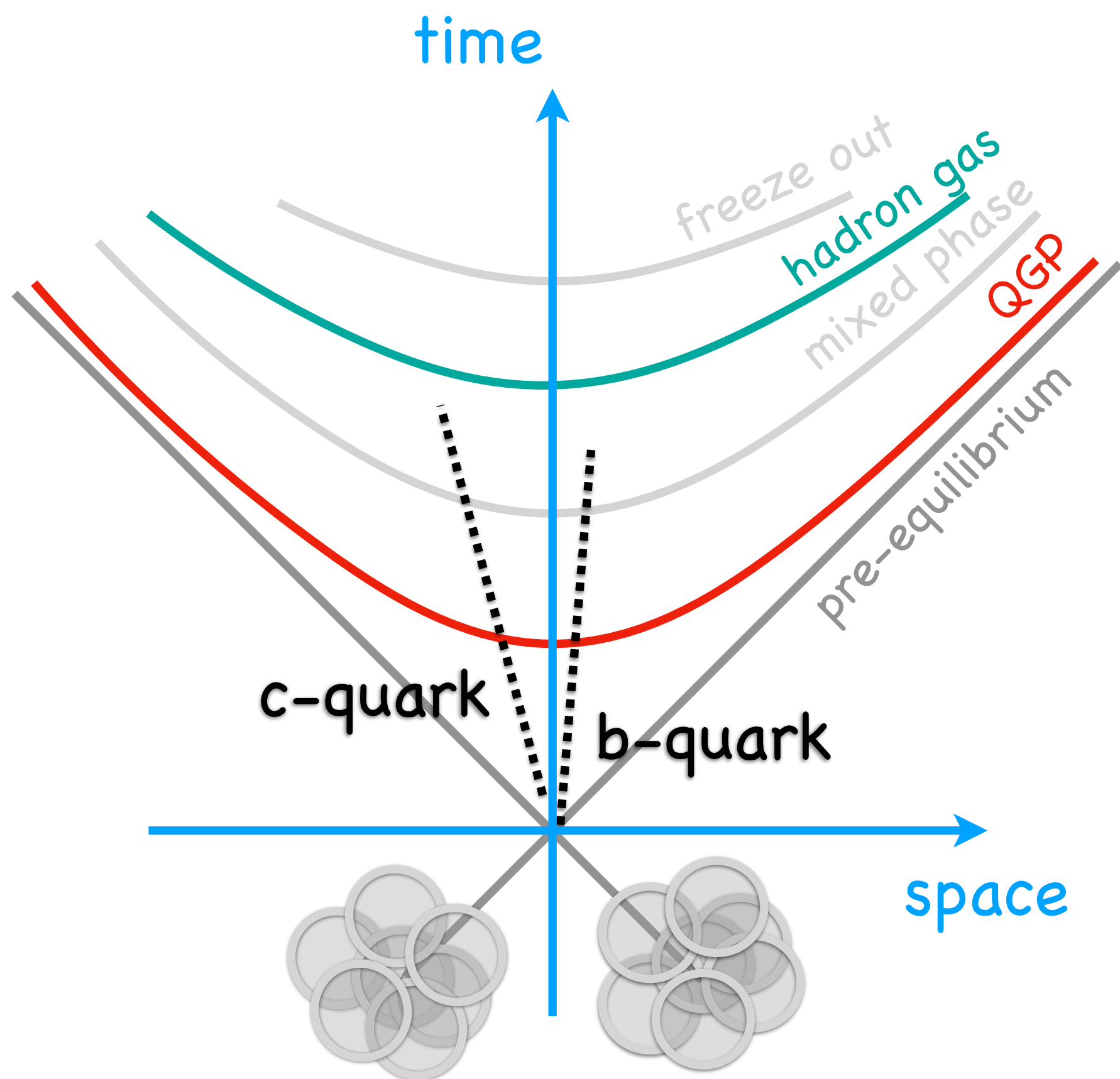
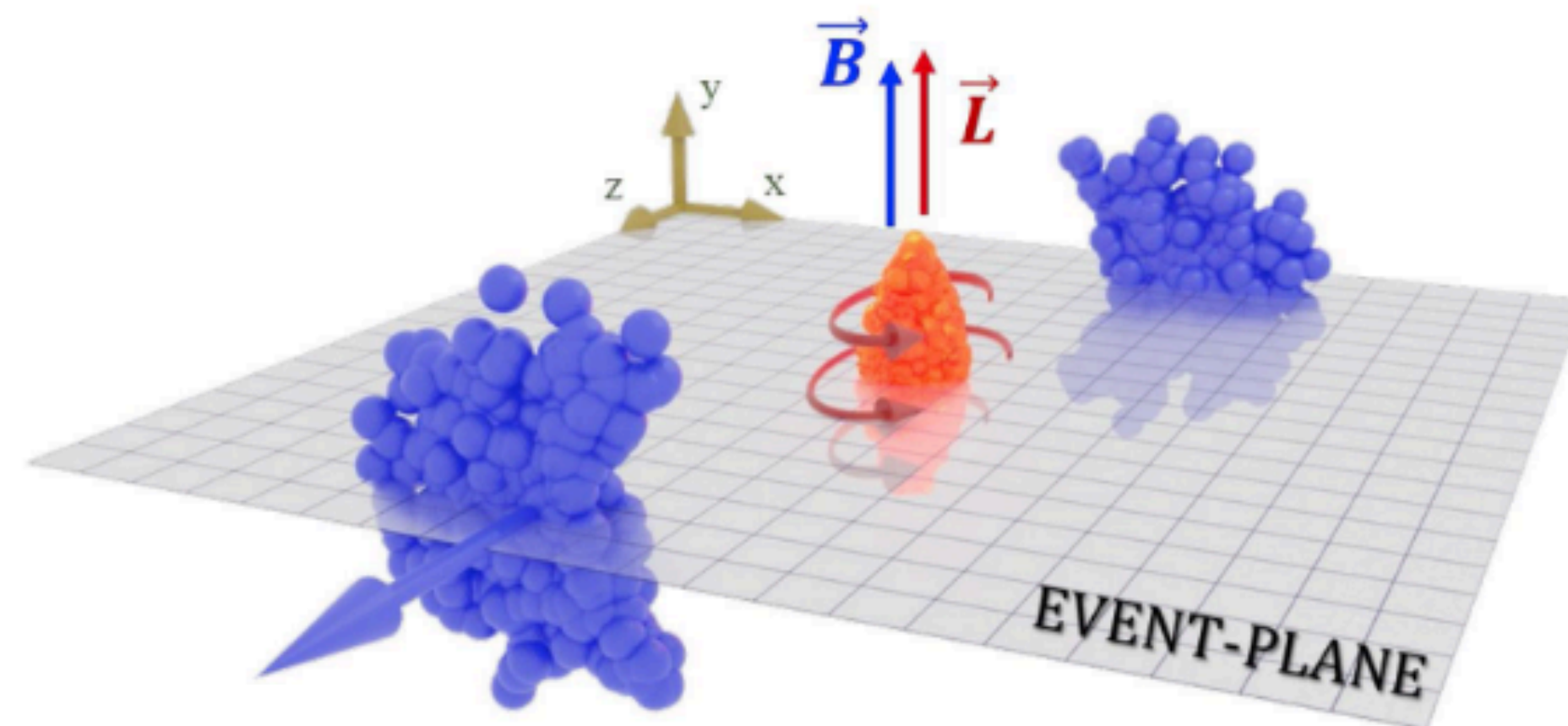
ALICE, JHEP 12 (2022) 126



- Non-prompt / prompt R_{AA} ratio:
 - ➔ CUJET3.1 describes the measurement at high p_T
 - ➔ Models including both collisional and radiative energy loss (LGR, MC@sHQ+EPOS2) describe the measurement in all the full p_T region
 - ➔ More precision needed to verify necessity of radiative energy loss (not included in TAMU)
- Hadronisation via coalescence needed to describe the intermediate p_T region

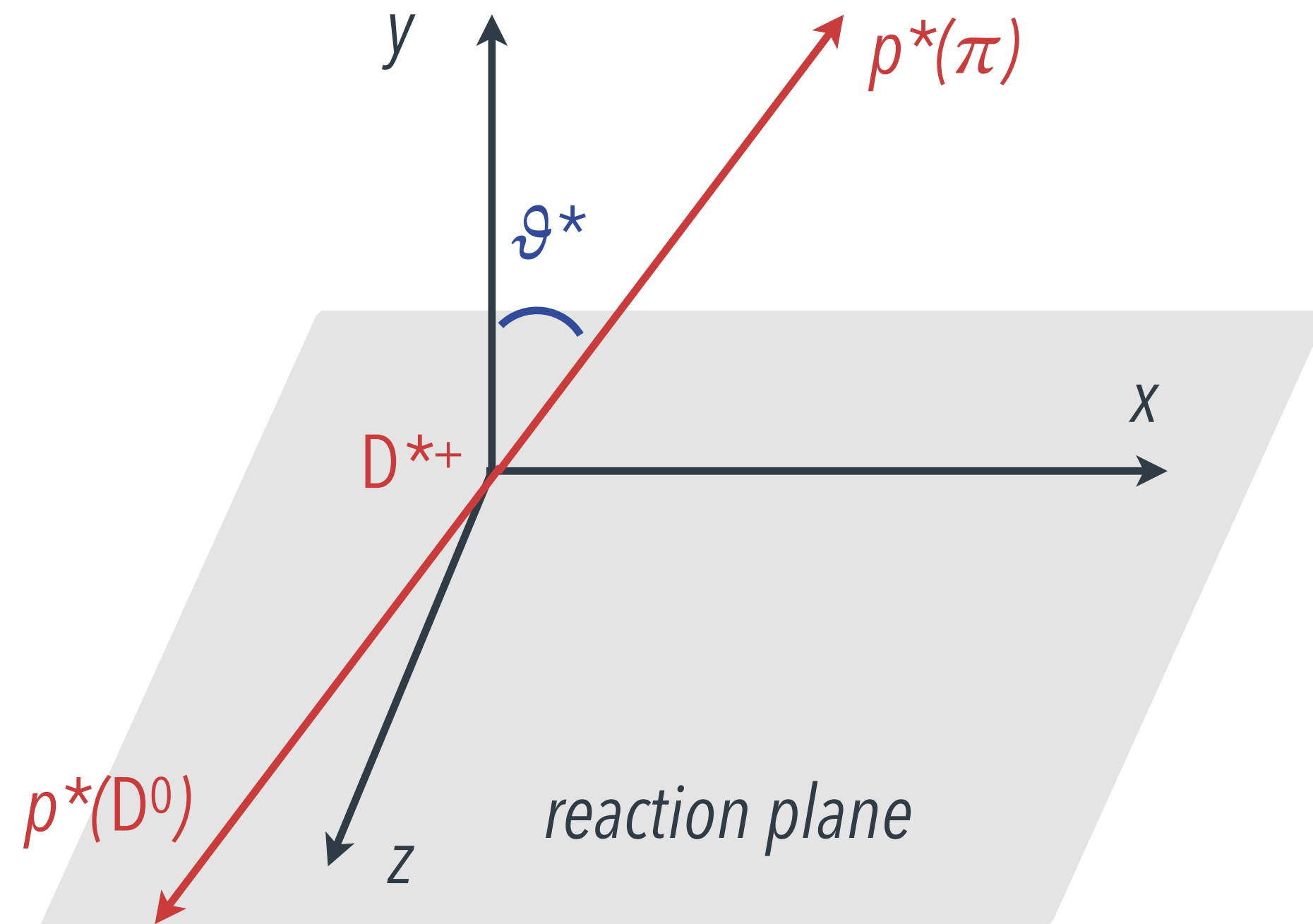
➔ More about HF in hadronisation in talk by A. Rossi

- Non-central heavy-ion collisions
 - ➔ Large angular momentum due to the medium rotation is predicted  Becattini et al, PRC 77 (2008) 024906
 - ➔ Huge initial magnetic field ($B \sim 10^{14}$ T) is expected to be formed  Kharzeev et al, NPA 803 (2008) 227-253



- Charm quarks are produced in the initial stage of the collision and hence are expected to be more sensitive to the magnetic field

- Spin alignment of vector mesons can be studied via the angular distribution of their decay products in the mother rest frame with respect to a quantisation axis



$$\frac{dN}{d \cos \vartheta^*} \propto (1 - \rho_{00}) + (3\rho_{00} - 1)\cos^2 \vartheta^*$$

ρ_{00} is the spin-density matrix element indicating the probability to find the vector meson in the spin 0 state

- $\rho_{00} = 1/3$ no spin alignment
- $\rho_{00} \neq 1/3$ spin alignment

- Quantisation axes:
 - pp collisions: **helicity** (direction of the vector meson momentum in the laboratory reference system) or **production** (orthogonal to helicity and beam axes)
 - Pb–Pb collisions: **normal to the reaction plane** (direction of angular momentum and magnetic field)

- The spin alignment of vector mesons is related to the polarisation of the constituent quarks P_q
 → It also depends on the hadronisation mechanism

Recombination

$$\rho_{00}^{\text{rec}} = \frac{1 - P_q \cdot P_{\bar{q}}}{3 + P_q \cdot P_{\bar{q}}} \begin{cases} > 1/3 \text{ if } P_q \cdot P_{\bar{q}} < 0 \\ < 1/3 \text{ if } P_q \cdot P_{\bar{q}} > 0 \end{cases}$$

* $> 1/3$ for neutral mesons, $< 1/3$ for charged mesons

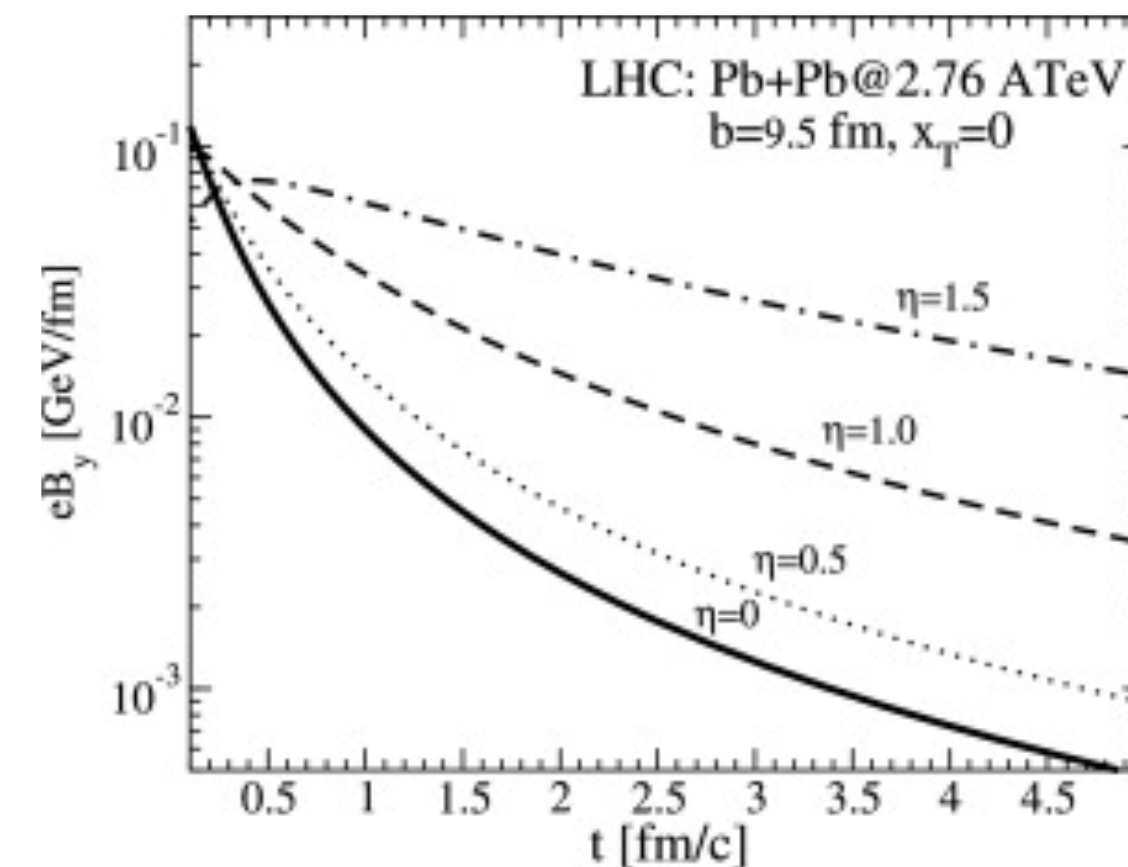
📖 Z.-T. Liang et al, PLB 629:20-26, 2005

Fragmentation

$$\rho_{00}^{\text{frag}} = \frac{1 + \beta \cdot P_q^2}{3 - \beta \cdot P_q^2} > 1/3$$

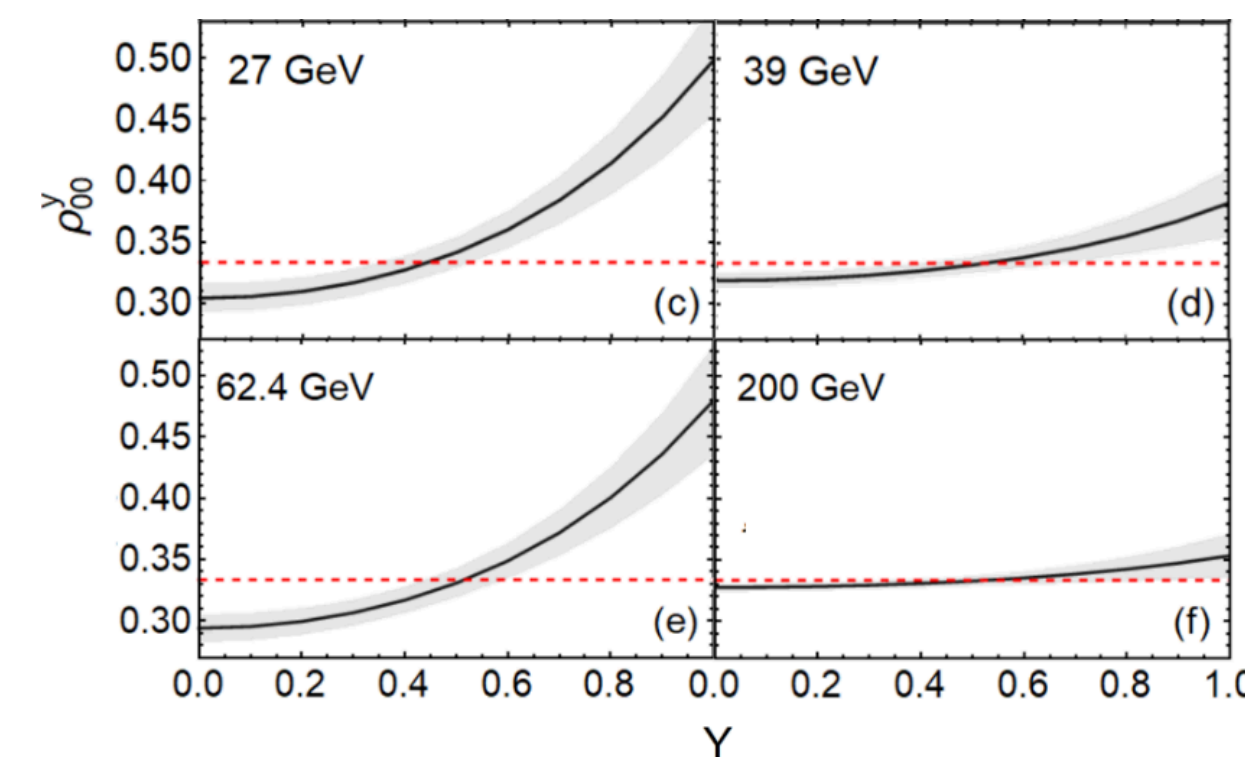
- Increase with p_T also expected because of earlier production for high momentum quarks (magnetic field) and in effective-field theory models which predict a polarisation due to the angular momentum transferred via quark recombination

- rapidity dependence expected:



In case of B-field induced polarisation due to the decrease in time, less steep at forward rapidity

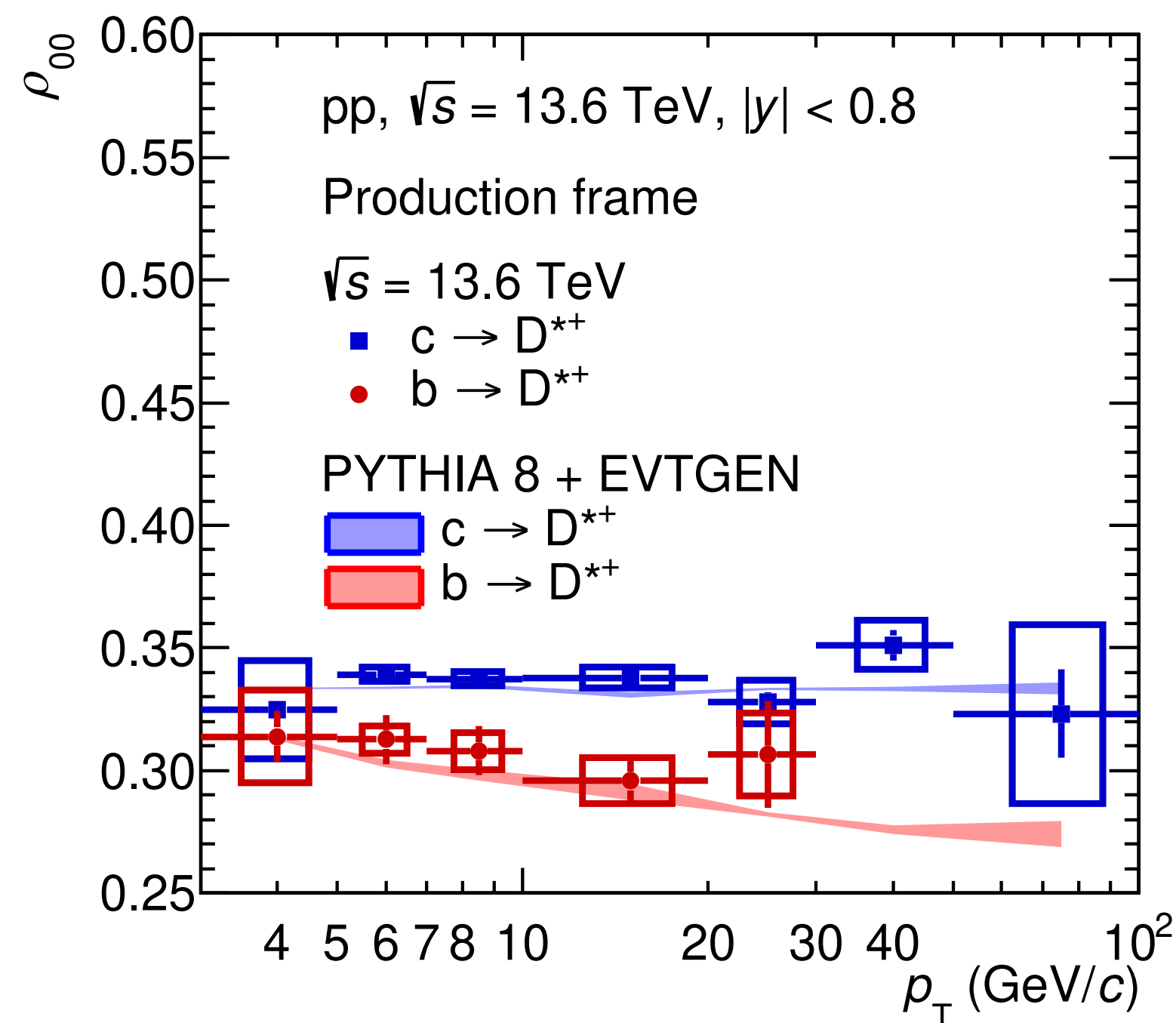
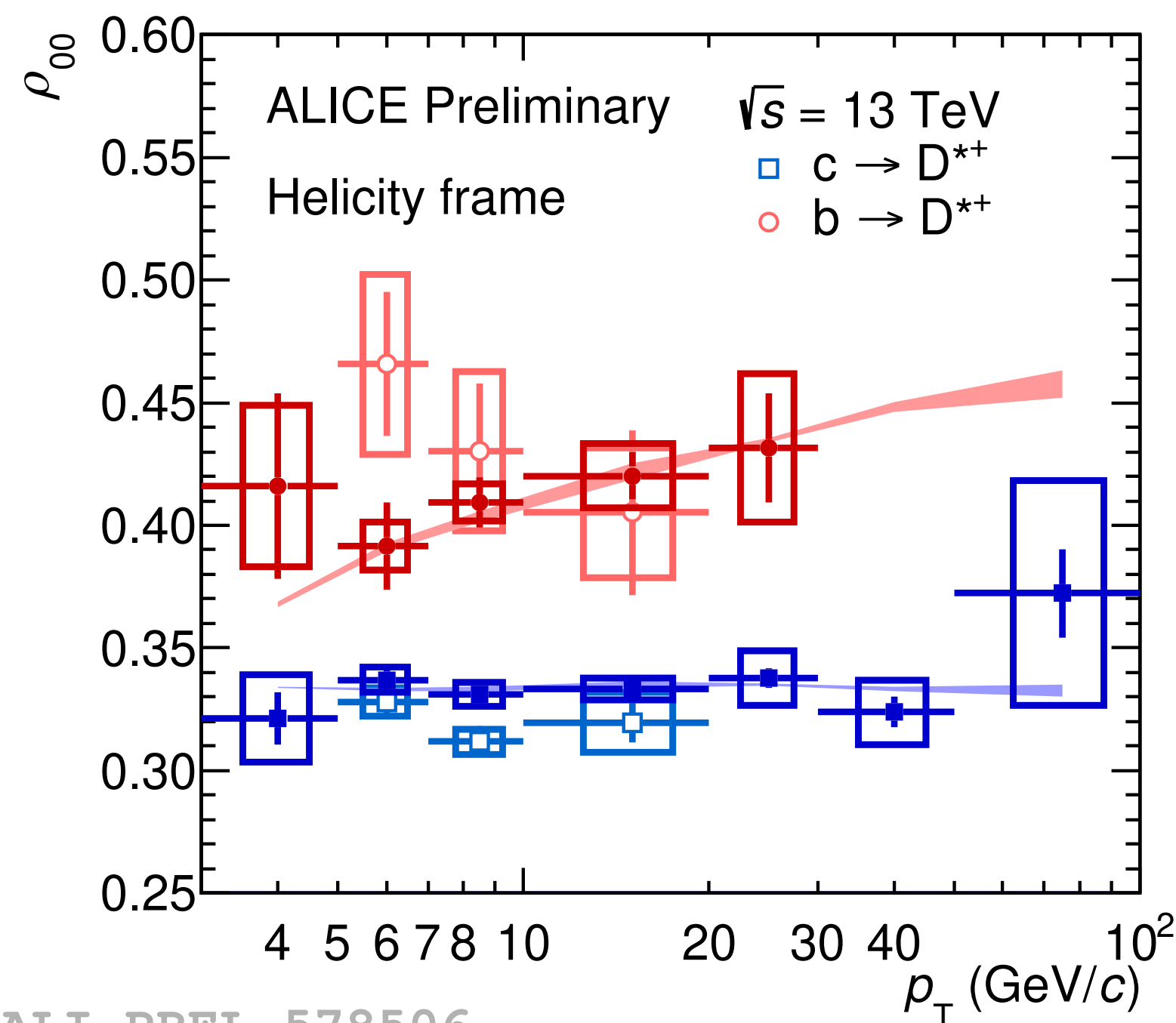
📖 S.K. Das et al, PLB 768 (2017) 260



Also possible in case of vector-meson field, for thermalised polarised quarks recombining in the QGP

📖 X.L. Sheng et al, arXiv: 2308.14038

📖 S. Gupta, arXiv:2307.12250

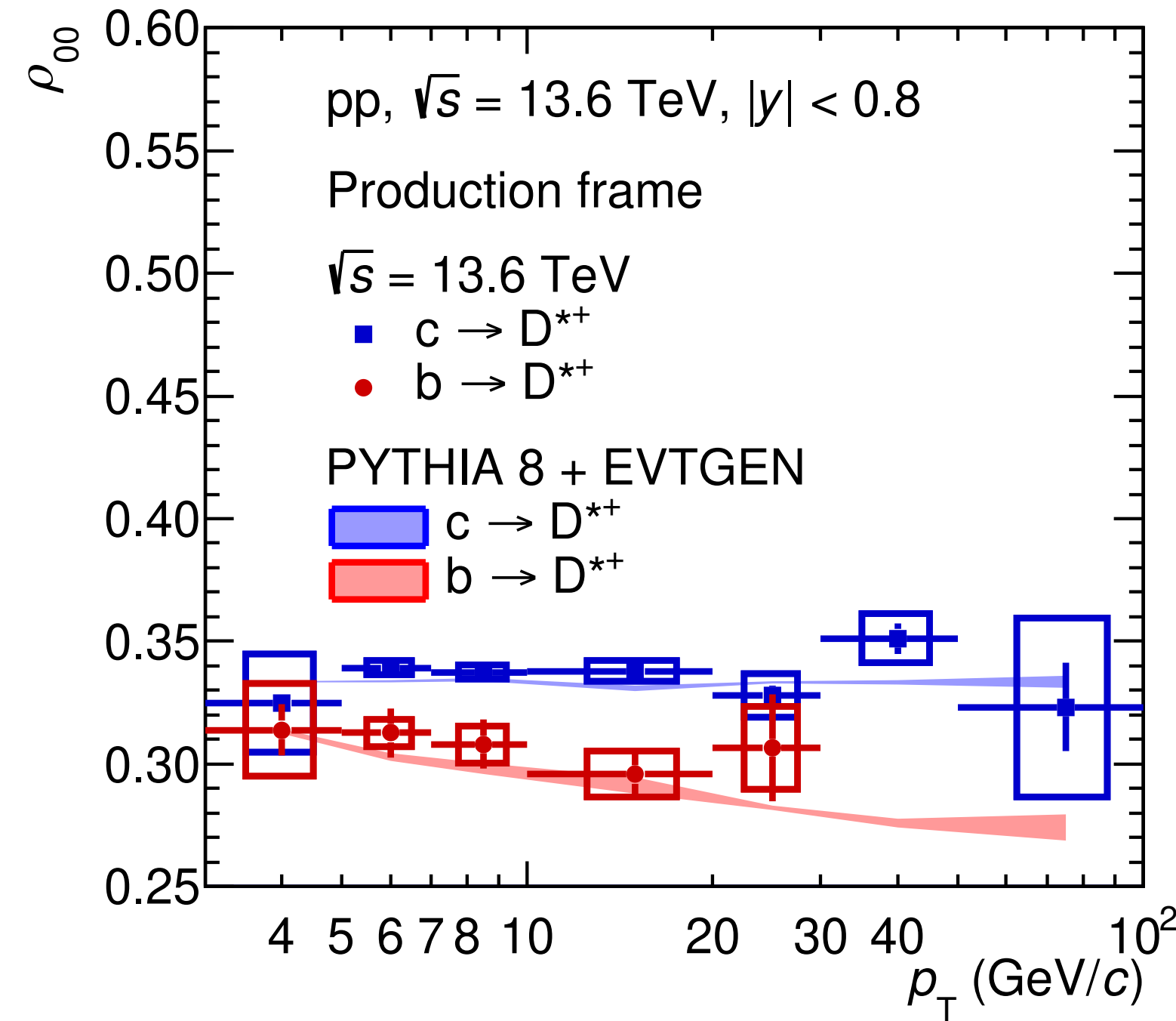
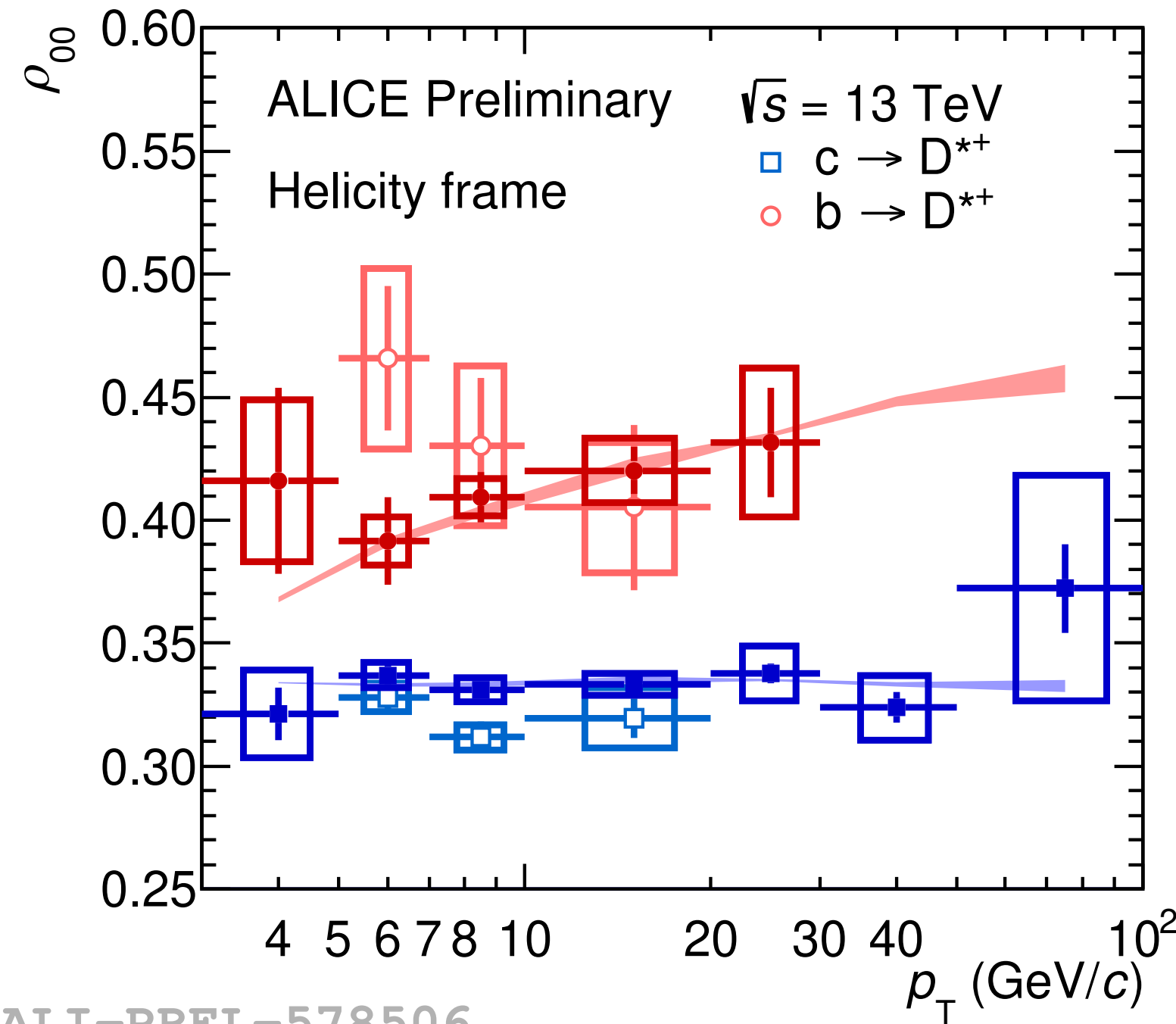


ALICE, PLB 846 (2023) 137920 ALICE Preliminary

PYTHIA8: CPC 191 (2015) 159-177

EVTGEN: NIM A 462 (2001) 152-155

- **Baseline:** spin alignment of prompt and non-prompt charm vector mesons with respect to helicity and production axes in pp collisions
 - Prompt D^{*+} compatible with no polarisation
 - Non-prompt D^{*+} $\rho_{00} > 1/3$ (helicity) $< 1/3$ (production)
 - ▶ helicity conservation in $B \rightarrow D^{*+}X$ decays

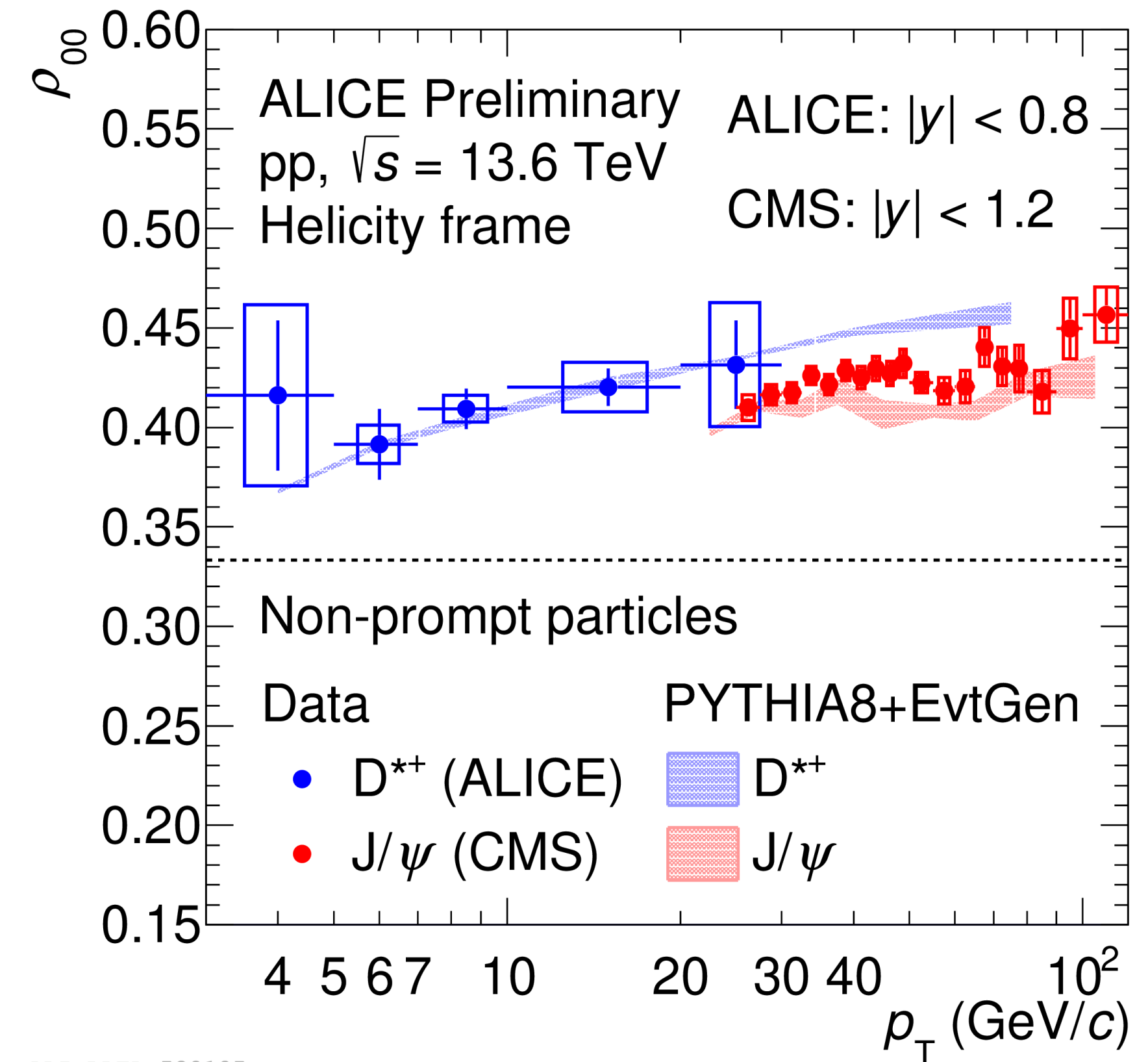


ALICE, PLB 846 (2023) 137920 ALICE Preliminary

PYTHIA8: CPC 191 (2015) 159-177

EVTGEN: NIM A 462 (2001) 152-155

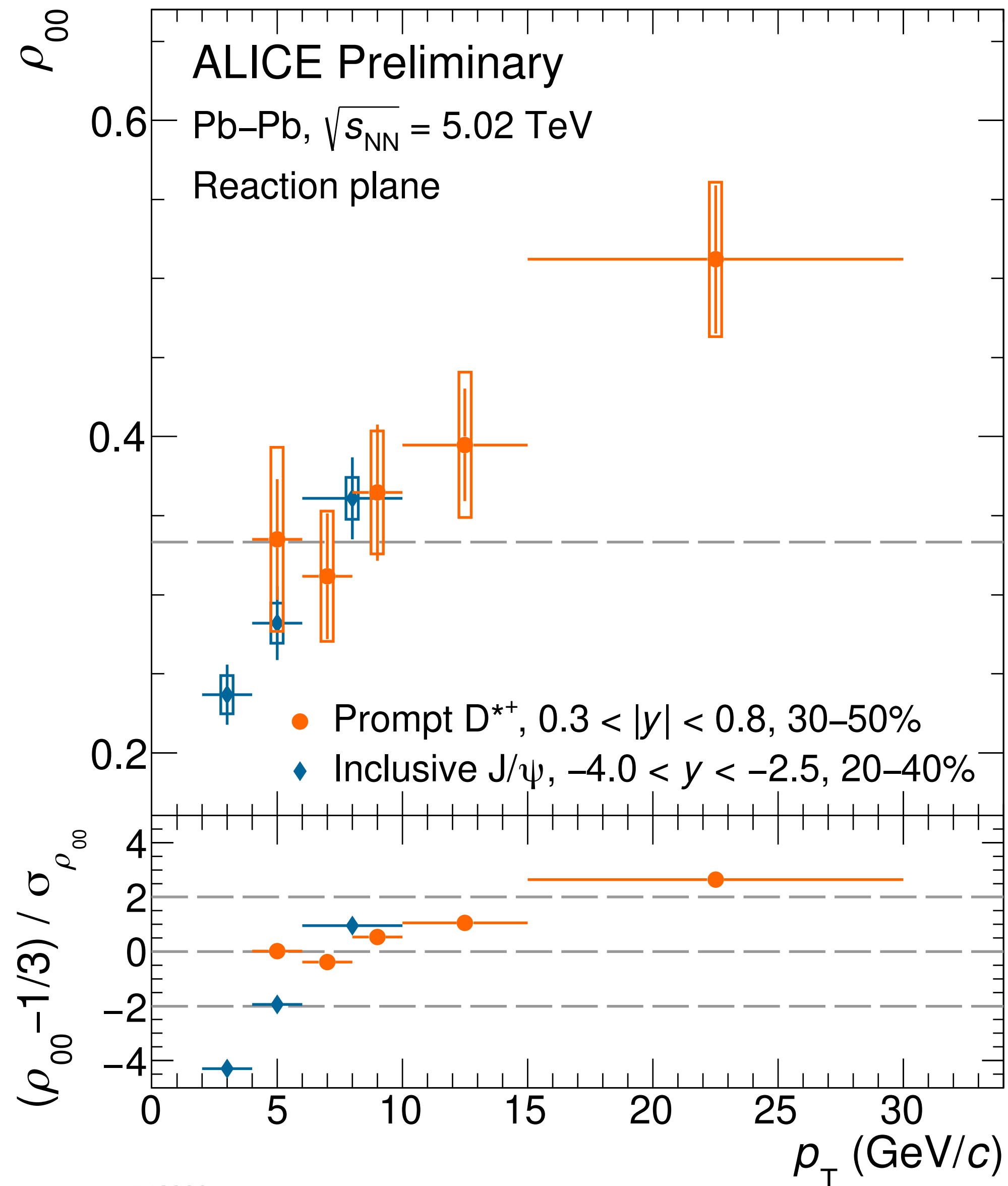
CMS, arXiv:2406.14409



- **Baseline:** spin alignment of prompt and non-prompt charm vector mesons with respect to helicity and production axes in pp collisions

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- Similar ρ_{00} for non-prompt D^{*+} and non-prompt J/ψ



- D^{*+} measurement compatible with polarised charm quarks hadronising via fragmentation
- J/ψ measurement compatible with polarisation due to angular momentum / vector-meson fields and hadronisation via recombination

More about J/ψ

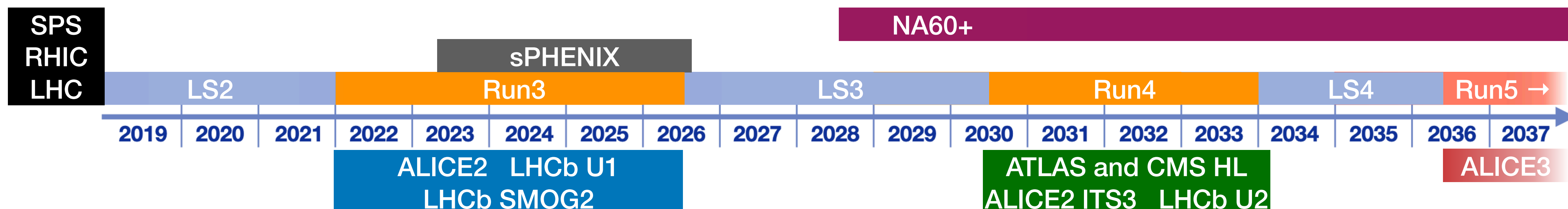
→ polarisation in talk by X. Bai

ALICE, PRL 131 (2023) 042303

ALICE Preliminary

- Hadrons containing **heavy quarks** are excellent probes of the quark–gluon plasma, which allows us to study:
 - **transport coefficients** (i.e. spatial diffusion) and possible **thermal equilibrium**
 - **colour-charge** and **quark-mass** dependence of energy loss
 - **hadronisation** mechanisms
 - Early **magnetic field** and **angular momentum** produced in non-central heavy-ion collisions
- Core of physics programs of current and **future** heavy-ion experiments

→ See presentations by M. Van Leeuwen,
A. Fantoni, A. Marie





ADDITIONAL SLIDES

- Hint of increasing trend with p_T in midcentral Pb–Pb collisions
- Only in the rapidity interval $0.3 < |y| < 0.8 \rightarrow$ need of more precise and more differential (vs y) measurements

