



# Towards a possible solution to the Hubble tension with Horndeski gravity



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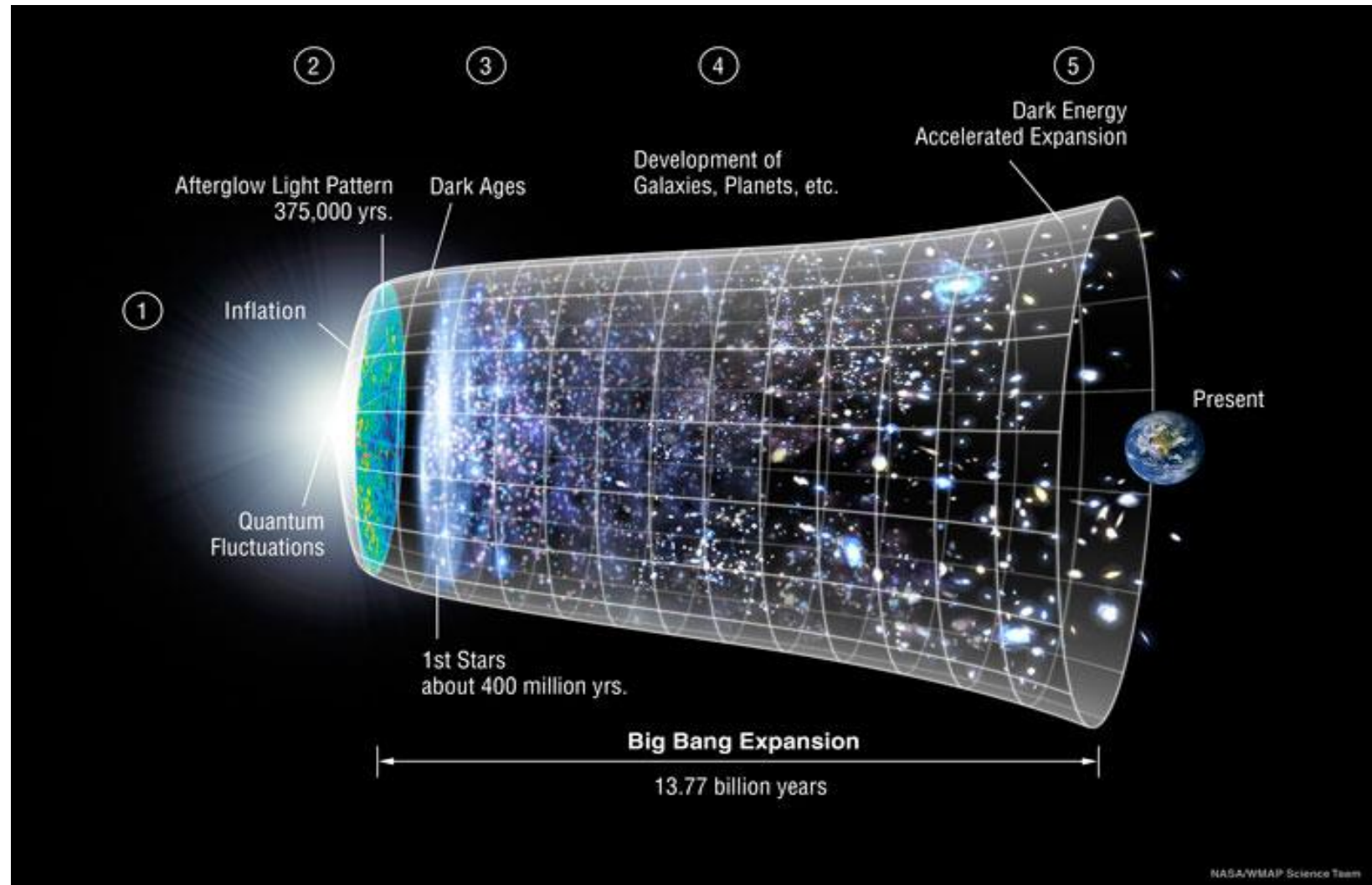
**Frontiers in Particle Physics 2024**

Centre for High Energy Physics, Indian Institute of Science, Bangalore

# Outline

- The Standard Model of Cosmology
- Hubble Tension
- Resolution: Dynamical Dark Energy
- Hints of dynamical dark energy : DESI
- Dark Energy in Horndeski gravity
- Constraints from Observations
- Conclusion and Future Prospects

# Present understanding of the universe



*Image Credit:* NASA/  
LAMBDA Archive / WMAP  
Science Team

# Present understanding of the universe: $\Lambda$ CDM model

Cosmological Principle + General Relativity



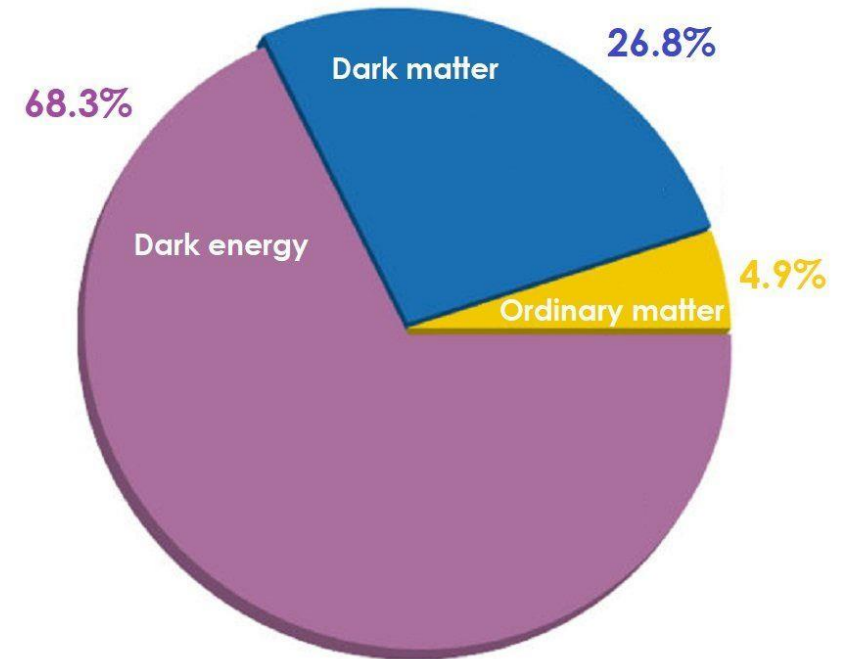
$$ds^2 = -dt^2 + a(t)^2 d\bar{x}^2, \quad R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} = 8\pi GT_{\mu\nu}$$



Friedmann Equation  $\longleftarrow H^2 = \left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3}\rho \longrightarrow$  Total energy density

Lambda Cold Dark Matter ( $\Lambda$ CDM) Model : Simplest Scenario

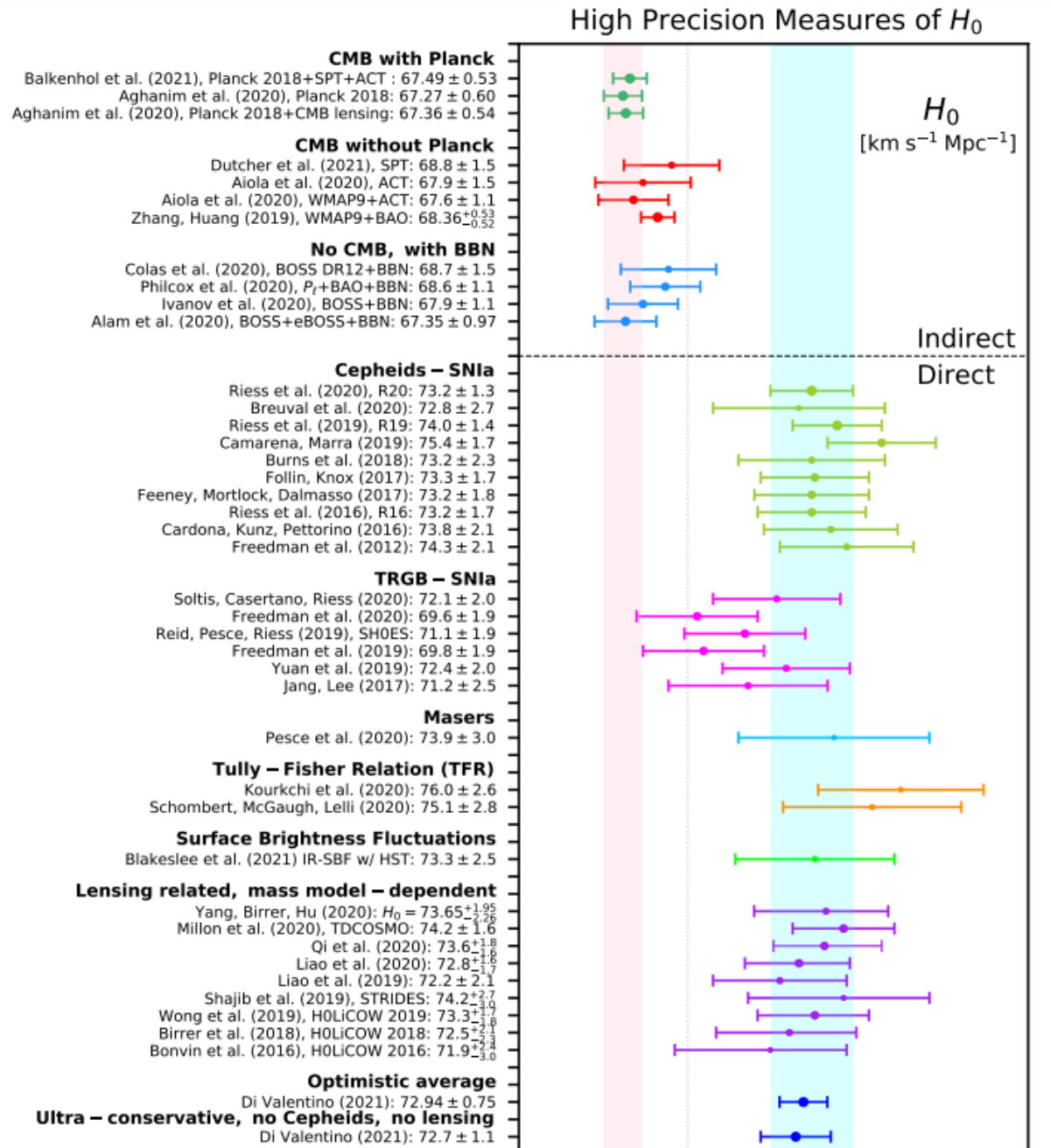
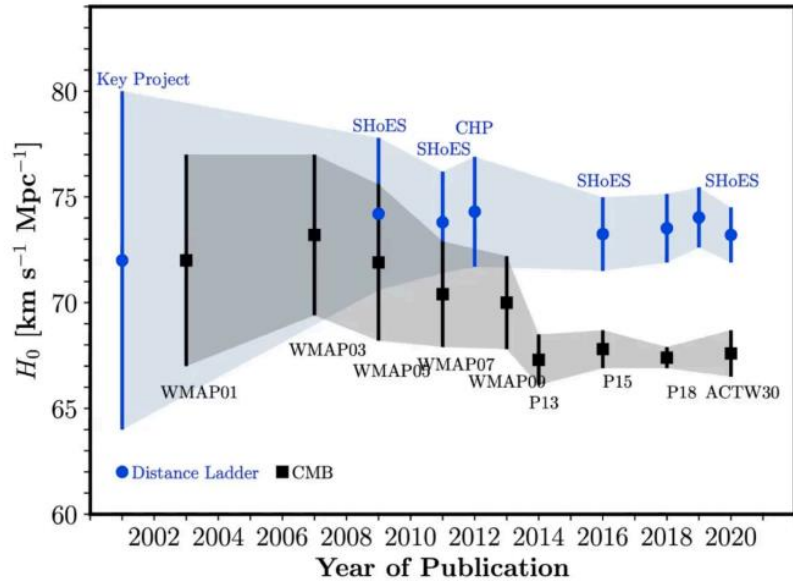
$$H(z) = H_0 \sqrt{\Omega_{r0}(1+z)^4 + \Omega_{m0}(1+z)^3 + \Omega_{\Lambda}}$$



Here it is assumed that universe is spatially flat i.e.  $\Omega_k=0$ . Thanks to inflation!

# The Hubble Trouble

5 $\sigma$  tension at present!

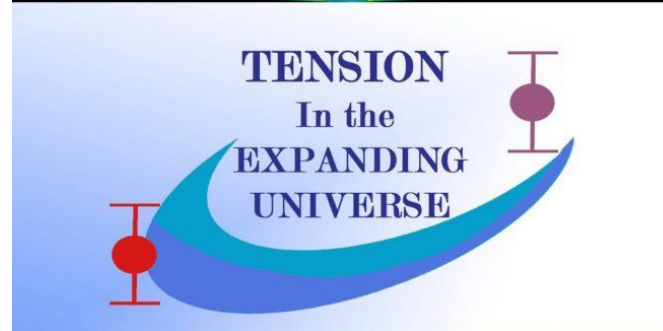
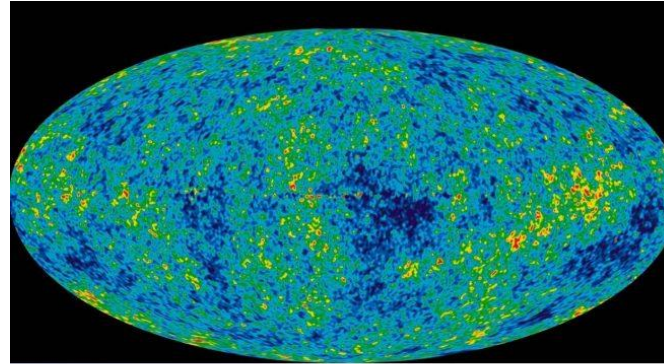


(Di Valentino et al 2021)

# Understanding Hubble Tension

## Early measurements

- Based on observations of cosmic microwave background coming from last scattering surface (redshift  $\sim 1100$ , 13.76 Gyr back).
- Assumes  $\Lambda$ CDM model to calculate  $H_0$ .
- Planck, WMAP
- $H_0 = 67.37 \pm 0.54$  km/sec/Mpc

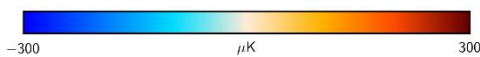
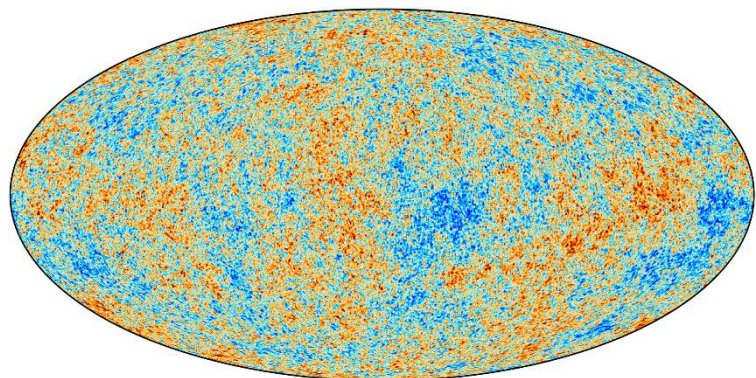


## Late measurements

- Based on astrophysics of stars: observing standard candles in the nearby universe.
- Model independent measurement.
- SHOES, CHP
- $H_0 = 73.3 \pm 1.04$  km/sec/Mpc



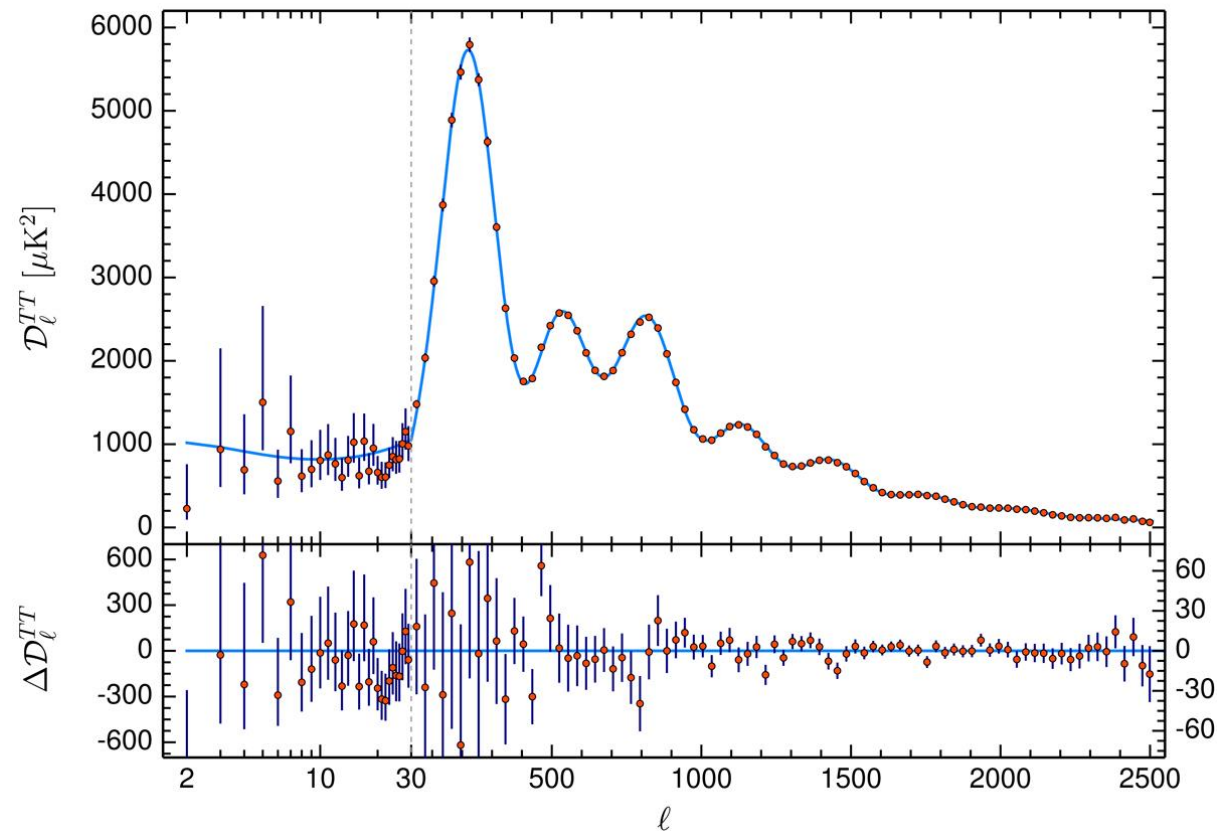
# Measurement of $H_0$ from early Universe



six independent parameters of **ΛCDM** model.

Parameter	Combined
$\Omega_b h^2$ .....	$0.02233 \pm 0.00015$
$\Omega_c h^2$ .....	$0.1198 \pm 0.0012$
$100\theta_{MC}$ .....	$1.04089 \pm 0.00031$
$\tau$ .....	$0.0540 \pm 0.0074$
$\ln(10^{10} A_s)$ .....	$3.043 \pm 0.014$
$n_s$ .....	$0.9652 \pm 0.0042$
$\Omega_m h^2$ .....	$0.1428 \pm 0.0011$
$H_0$ [ km s <sup>-1</sup> Mpc <sup>-1</sup> ] ...	$67.37 \pm 0.54$
$\Omega_m$ .....	$0.3147 \pm 0.0074$
Age [Gyr] .....	$13.801 \pm 0.024$
$\sigma_8$ .....	$0.8101 \pm 0.0061$
$S_8 \equiv \sigma_8(\Omega_m/0.3)^{0.5}$ ..	$0.830 \pm 0.013$
$z_{re}$ .....	$7.64 \pm 0.74$
$100\theta_*$ .....	$1.04108 \pm 0.00031$
$r_{drag}$ [Mpc] .....	$147.18 \pm 0.29$

Derived parameters



**Planck 2018 measurements assuming ΛCDM model give,  $H_0 = 67.37 \pm 0.54$  km/sec/Mpc**

# Measurement of $H_0$ from Late Universe

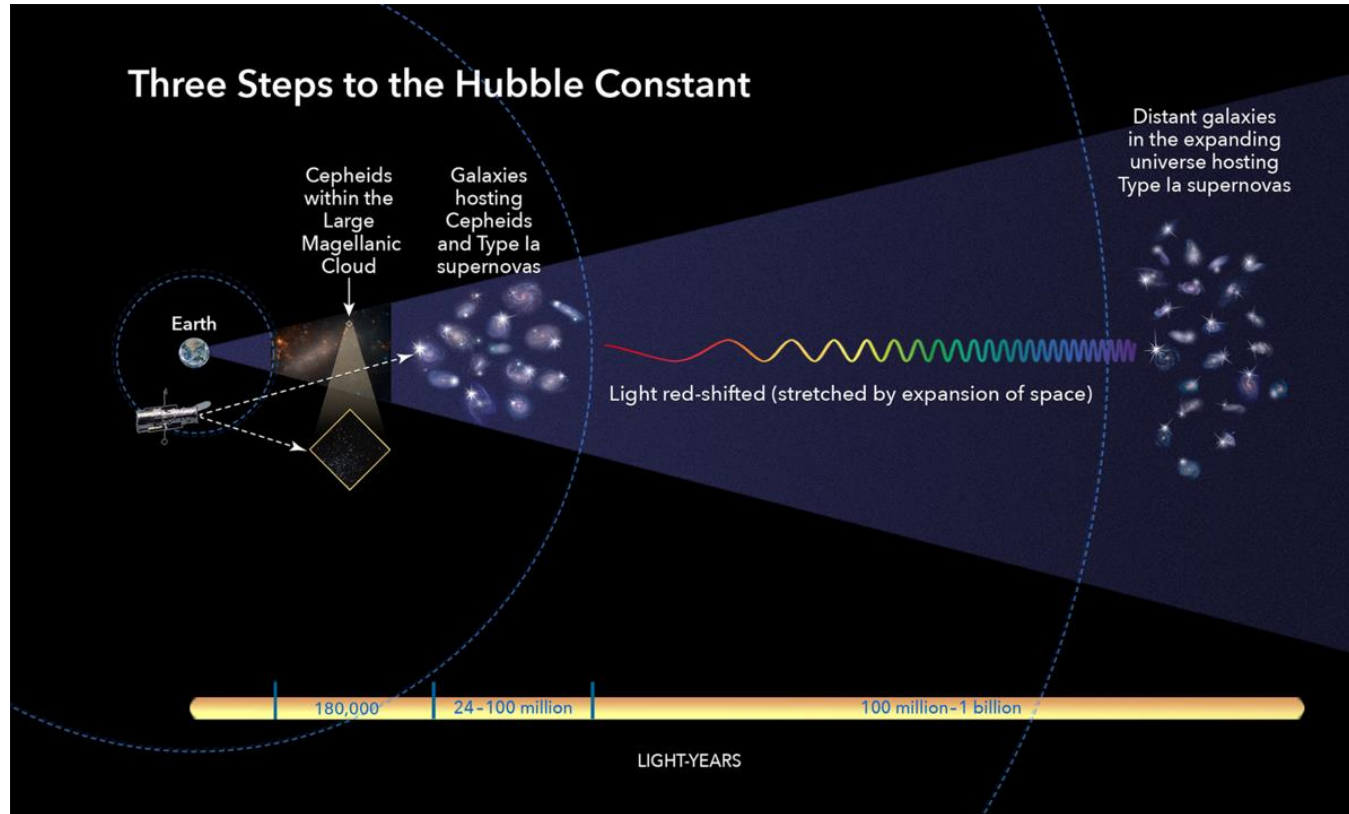


Image Credit: NASA

Cosmic Distance Ladder : calibrating distances to galaxies farther away upto redshift  $\sim 0.1$

- Observing standard candles (Supernovae and Cepheids) to calibrate distances to galaxies and using Hubble's law to calculate  $H_0$ .
- The **SHOES** Program (Supernovae and  $H_0$  for the Equation of State of dark energy) measured  $H_0 = 73.3 \pm 1.04$  km/sec/Mpc (Riess et al 2022).
- This drives the  $H_0$  tension  $\sim 5\sigma$



# Resolving Hubble Tension with a dynamical dark energy

A dark energy field whose equation of state evolves with time  $w(z)$ : But what else?





Physics of the Dark Universe

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## Simultaneously solving the $H_0$ and $\sigma_8$ tensions with late dark energy

Lavinia Heisenberg <sup>a b</sup>  , Hector Villarrubia-Rojo <sup>b</sup> , Jann Zosso <sup>b</sup> 

Conditions which can resolve cosmological tensions without disturbing the CMB observations:

- Phantom crossing
- Variation in Gravitational coupling constant  $G_{eff}$

Phantom equation of state:  $w < -1$   Violation of Strong Energy Condition

# Hints of dynamical dark energy from DESI



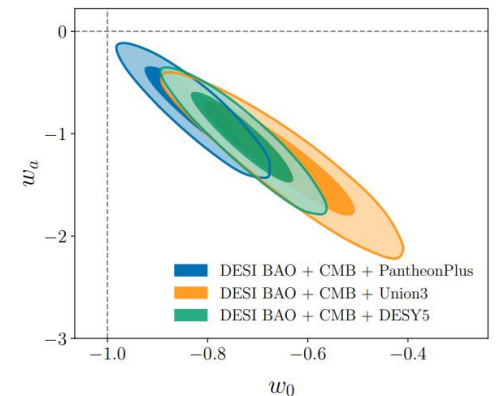
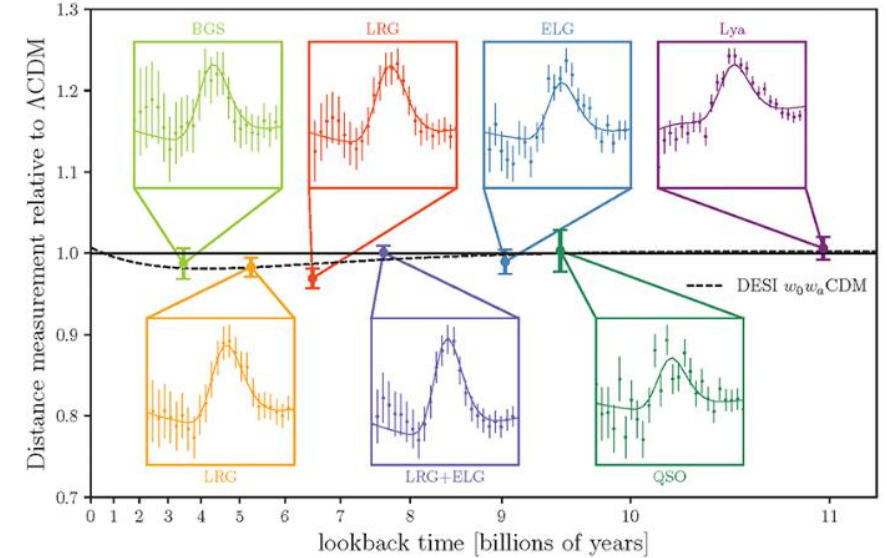
FERMILAB-PUB-24-0154-PPD

PREPARED FOR SUBMISSION TO JCAP

## DESI 2024 VI: Cosmological Constraints from the Measurements of Baryon Acoustic Oscillations

DESI Collaboration: A. G. Adame,<sup>1</sup> J. Aguilar,<sup>2</sup> S. Ahlen<sup>3</sup>,

- DESI BAO favors a **dynamical dark energy** over cosmological constant.
- Signatures of **phantom crossing** in DESI.



# Our Approach

## Towards a possible solution to the Hubble tension with Horndeski gravity

Yashi Tiwari, Basundhara Ghosh, Rajeev Kumar Jain

Eur. Phys. J. C (2024) 84:220  
<https://doi.org/10.1140/epjc/s10052-024-12577-0>

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Regular Article - Theoretical Physics

### Towards a possible solution to the Hubble tension with Horndeski gravity

Yashi Tiwari<sup>1,a</sup>, Basundhara Ghosh<sup>2,b</sup>, Rajeev Kumar Jain<sup>2,c</sup>

<sup>1</sup> Joint Astronomy Programme, Department of Physics, Indian Institute of Science, CV Raman Road, Bengaluru, Karnataka 560012, India

<sup>2</sup> Department of Physics, Indian Institute of Science, CV Raman Road, Bengaluru, Karnataka 560012, India



# Our Model: A subclass of Horndeski theory

$$\mathcal{L}_\phi = \frac{R}{2} [1 + 2c_3\phi] + \frac{1}{2}\partial_\mu\phi\partial^\mu\phi - V(\phi) - \left[ c_1\phi + \frac{1}{2}c_2\partial_\mu\phi\partial^\mu\phi \right] \partial_\mu\partial^\mu\phi,$$

↓
↓

Non-minimal coupling
Self-interaction (Galileon)

$$\mathcal{L} = \sum_{i=2}^5 \mathcal{L}_i,$$

**Horndeski gravity:** A generalized scalar tensor theory in 4D with second order equations of motion

$$\mathcal{L}_2 = G_2(\phi, X),$$

$$\mathcal{L}_3 = -G_3(\phi, X)\square\phi,$$

$$\mathcal{L}_4 = G_4(\phi, X)R + G_{4,X}(\phi, X) \left[ (\square\phi)^2 - (\nabla_\mu\nabla_\nu\phi)^2 \right],$$

$$\mathcal{L}_5 = G_5(\phi, X)G_{\mu\nu}\nabla^\mu\nabla^\nu\phi - \frac{1}{6}G_{5,X}(\phi, X) \left[ (\square\phi)^3 - 3\square\phi(\nabla_\mu\nabla_\nu\phi)^2 + 2(\nabla_\mu\nabla_\nu\phi)^3 \right],$$

$$G_{i,Y} = \partial G_i / \partial Y$$

$$X = -\frac{1}{2}\partial^\mu\phi\partial_\mu\phi$$

(Kobayashi et al 2011, Kobayashi 2019)

# Background: Previous results

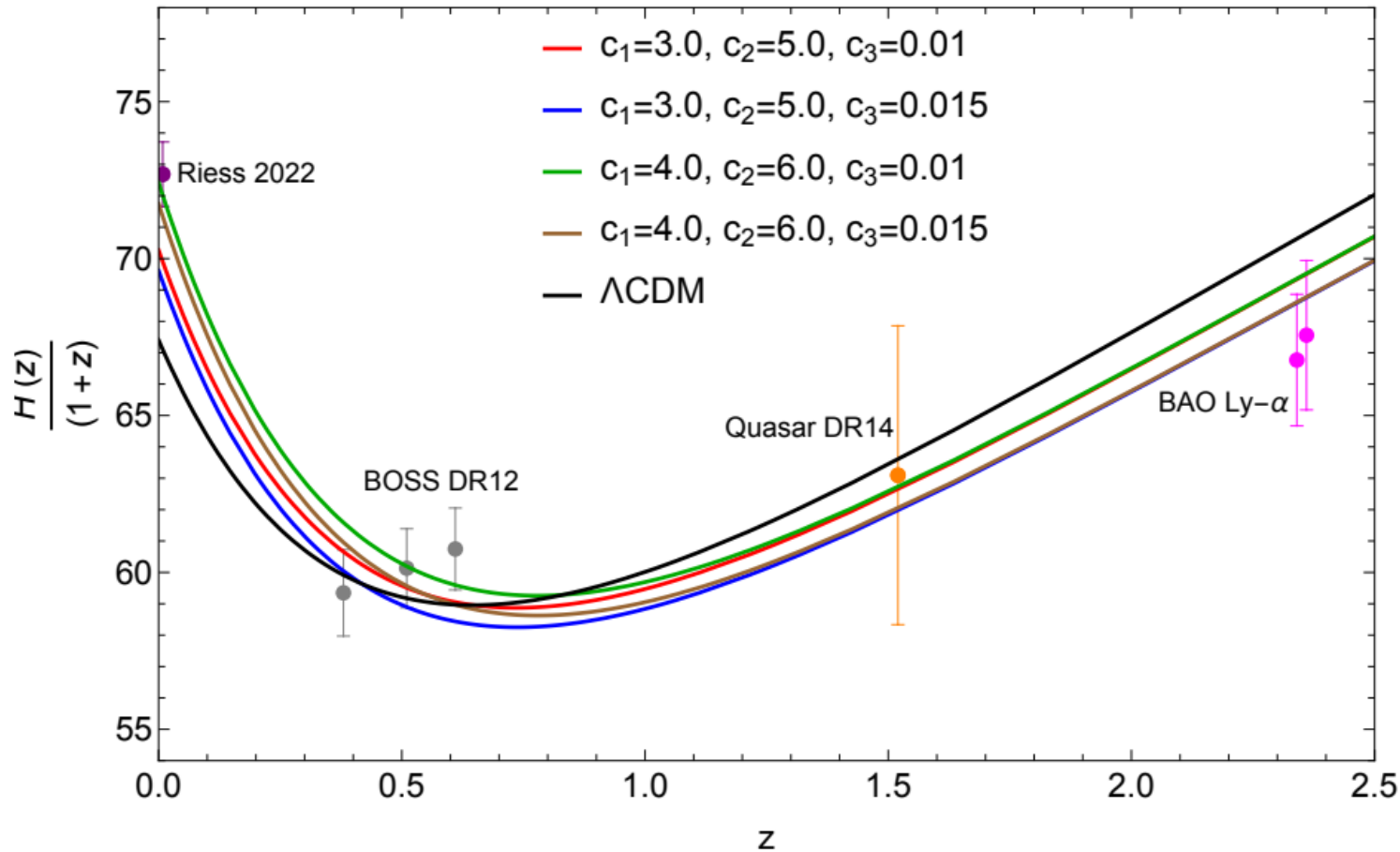


## Towards a possible solution to the Hubble tension with Horndeski gravity

Yashi Tiwari<sup>1,a</sup>, Basundhara Ghosh<sup>2,b</sup>, Rajeev Kumar Jain<sup>2,c</sup>

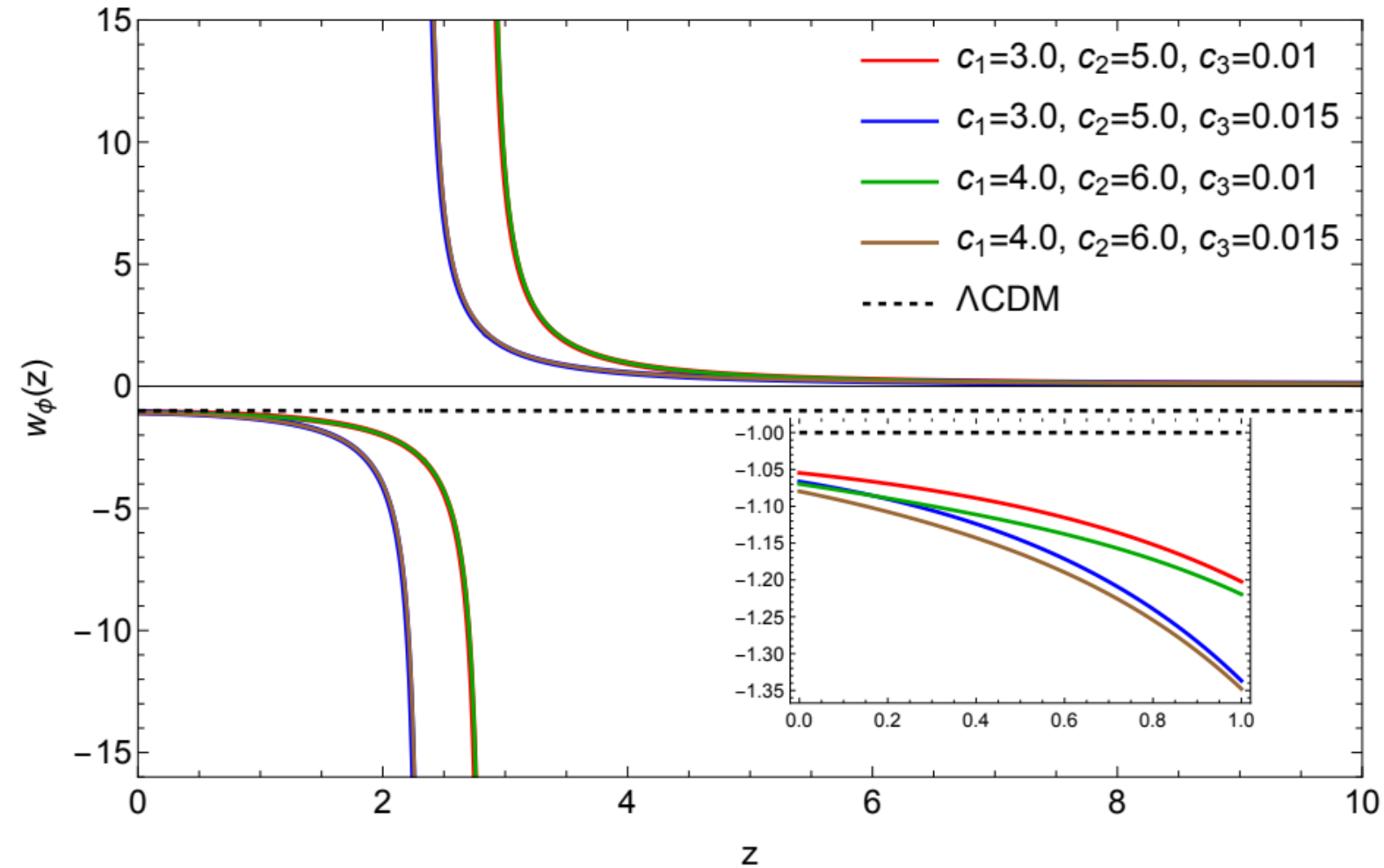
<sup>1</sup> Joint Astronomy Programme, Department of Physics, Indian Institute of Science, CV Raman Road, Bengaluru, Karnataka 560012, India

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# Background: Previous results



The model exhibits phantom divide

Work in progress

Towards a Simultaneous Alleviation of  $H_0$  and  $S_8$  tension with Horndeski gravity

Yashi Tiwari, Ujjwal Upadhyay, Rajeev Kumar Jain



# $S_8$ Tension

$$S_8 = \sigma_8 \left( \frac{\Omega_M}{0.3} \right)^{0.5}$$

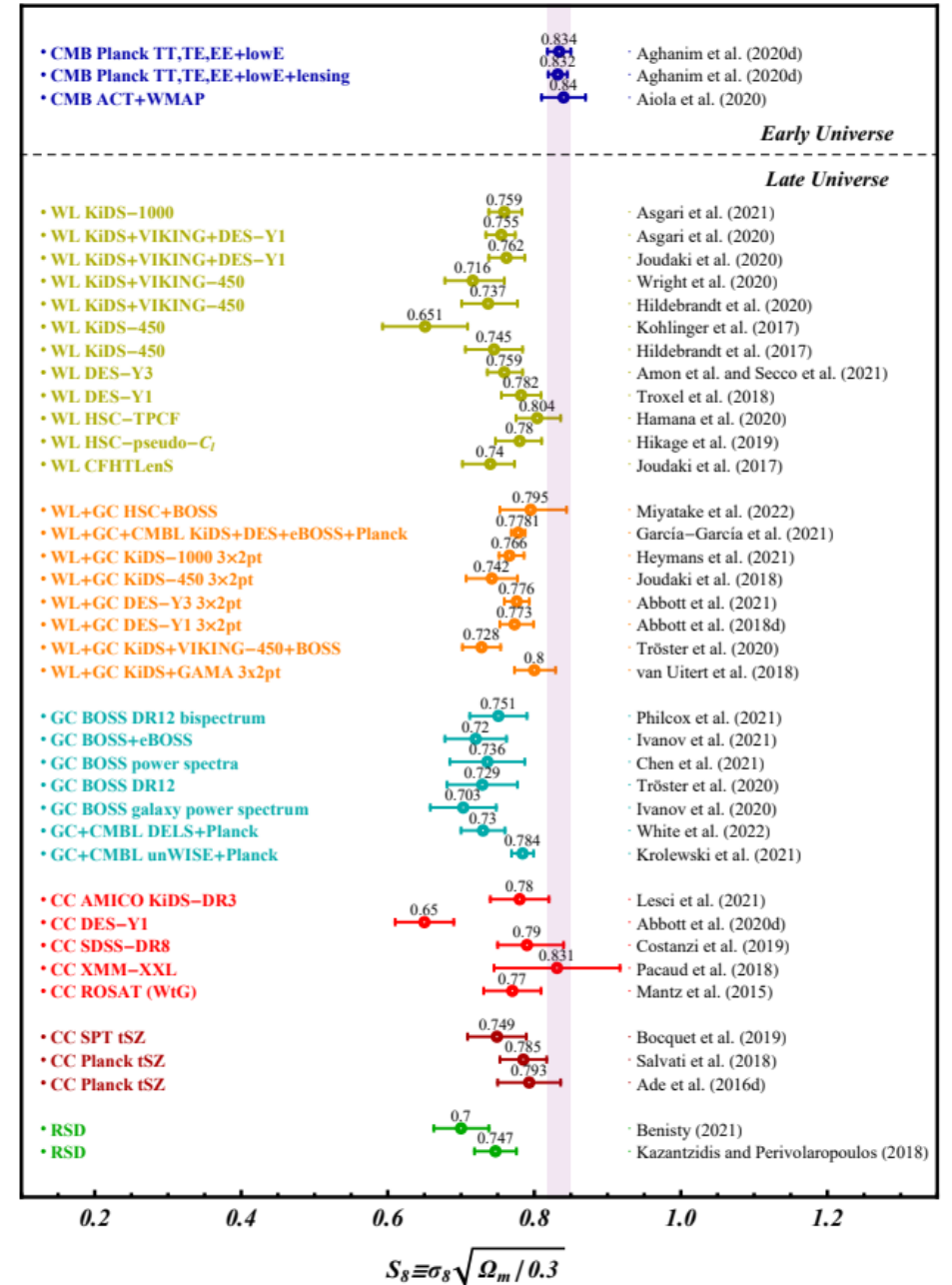


A measure of amplitude of matter clustering in late universe

$\sigma_8$  is the variance of density field smoothed over  $8h^{-1}$  Mpc

2-3 $\sigma$  tension at present

Most of the proposed solutions which resolve Hubble Tension, actually worsen  $S_8$  tension !!!



(Abdalla et al 2022)

# Perturbations: Growth of structures

$$ds^2 = -(1 + 2\Psi)dt^2 + a^2(1 - 2\Phi)d\mathbf{x}^2 \quad \longrightarrow \quad \text{Perturbed metric in Newtonian gauge}$$

In **quasistatic limit** within sub horizon scales the evolution of matter density perturbation follows,

$$\ddot{\delta} + 2H\dot{\delta} - 4\pi G_{\text{eff}}\rho_m\delta \approx 0,$$

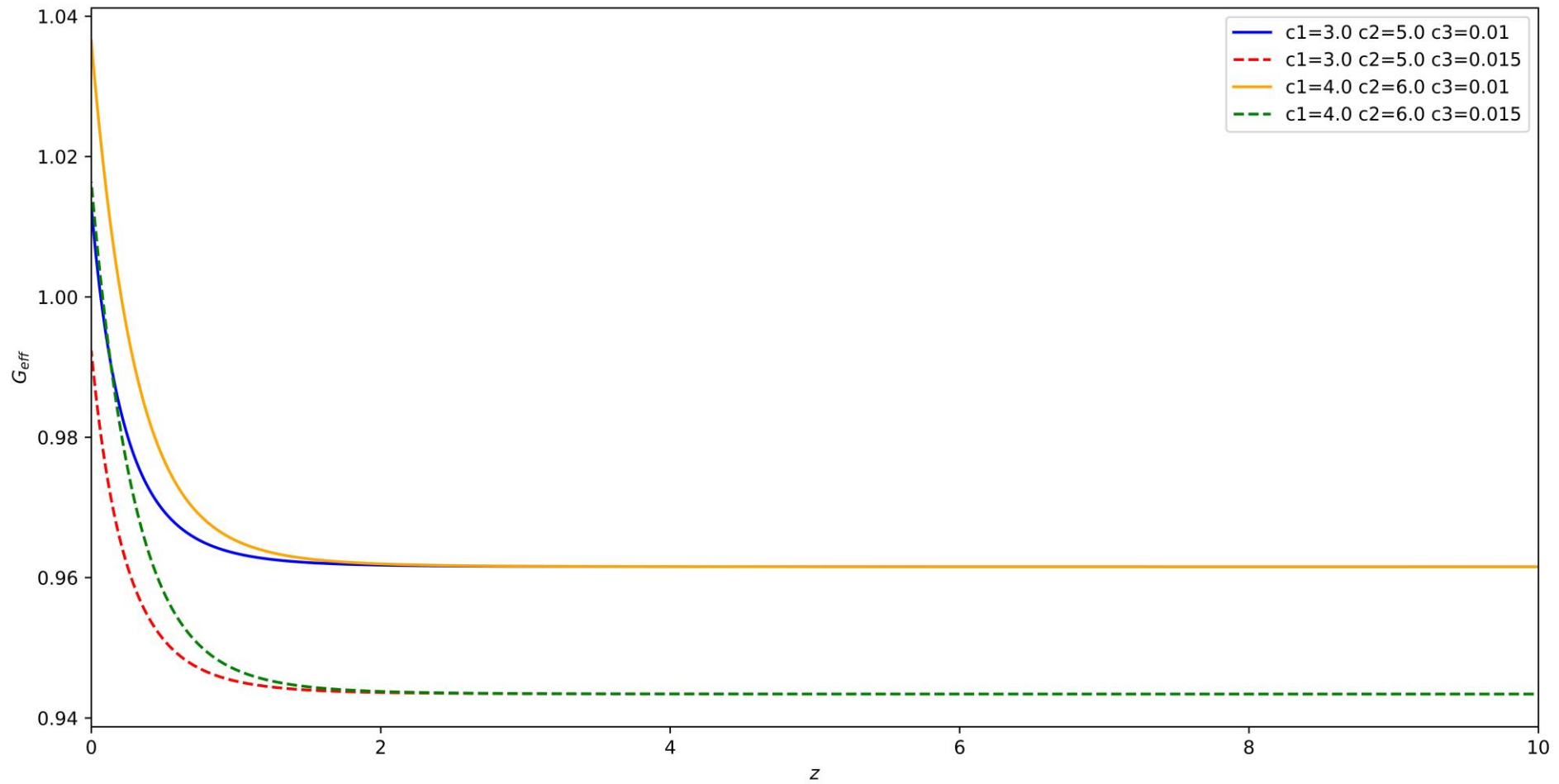
In General Relativity

$$G_{\text{eff}} = G_N$$

In Modified Gravity like Horndeski

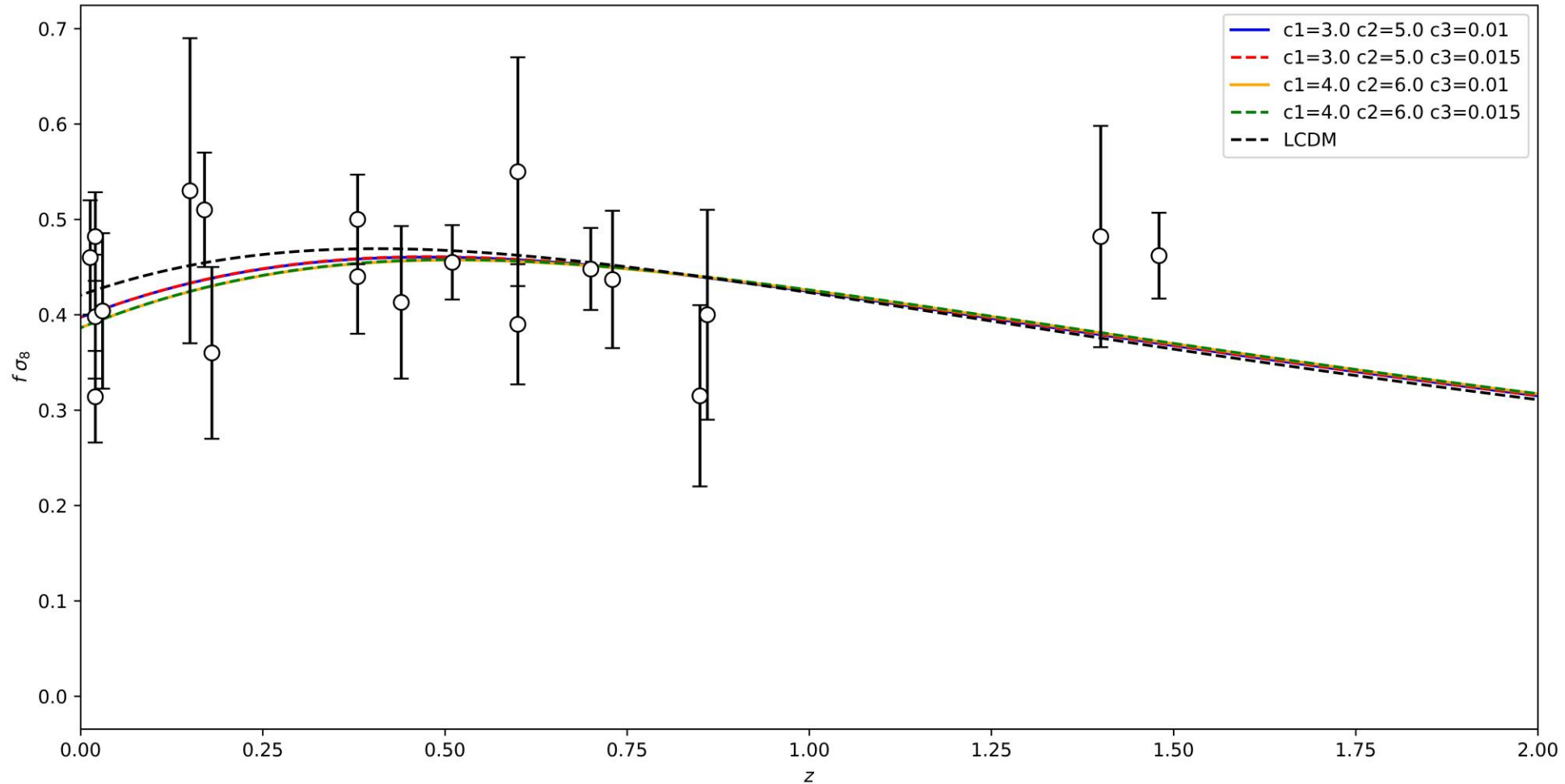
$$G_{\text{eff}} = F(t)$$

# Some preliminary results: $G_{eff}$

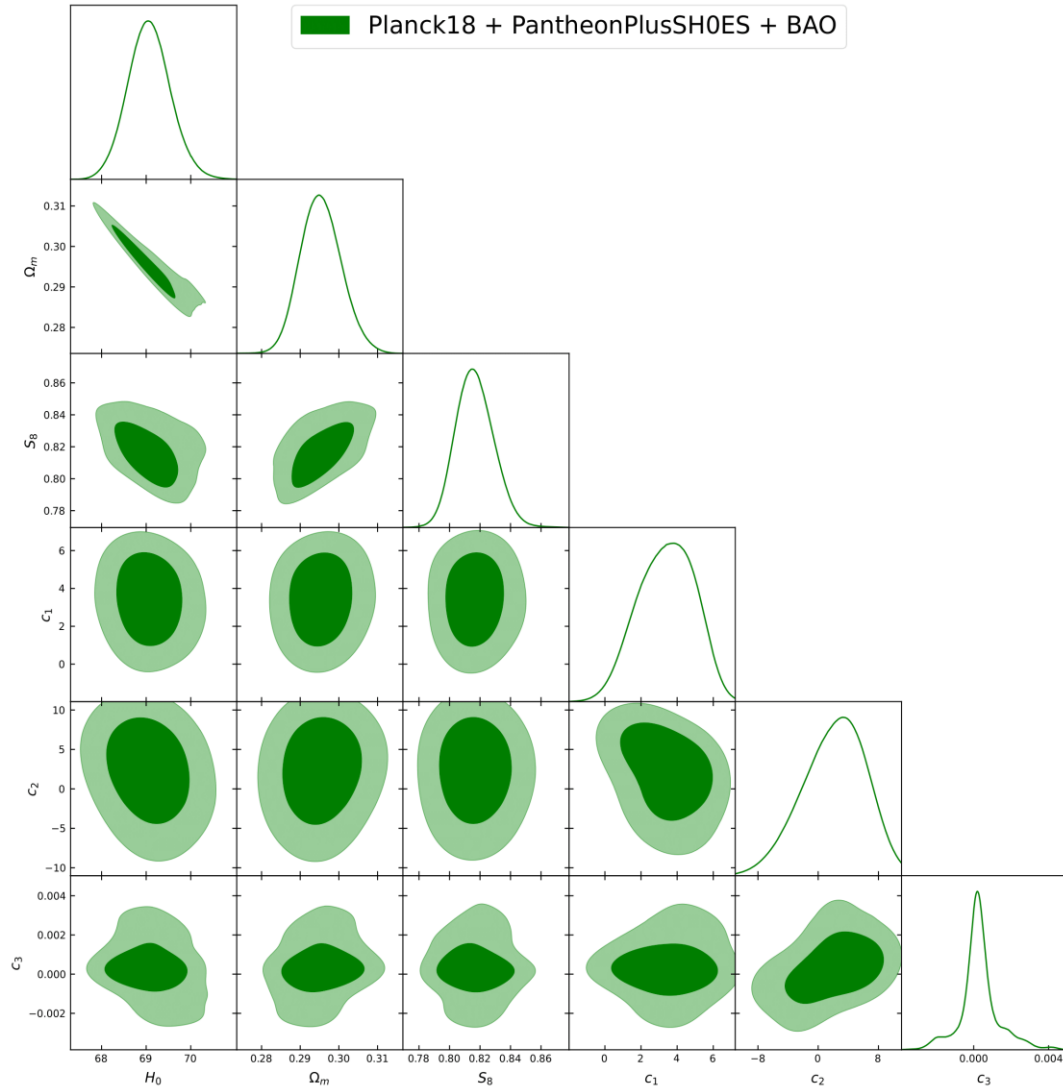




# Some preliminary results: Growth Rate



# Cosmological Parameter Estimation



Parameters	68% limits
$H_0$	$69.06 \pm 0.47$
$\Omega_m$	$0.2953 \pm 0.0052$
$S_8$	$0.8165 \pm 0.0124$
$c_1$	$3.4275 \pm 1.5290$
$c_2$	$2.1895 \pm 3.9560$
$c_3$	$0.0003 \pm 0.0006$

# Conclusion and Future Prospects

- We exploit the phenomenology of Horndeski theory to build dark energy model to resolve cosmological tensions.
- Interesting features like **phantom crossing, variation in gravitational coupling constant** etc., can be obtained in such a setup.
- Constrains are obtained on parameter space by Supernovae, Planck, BAO and SH0ES data.
- We are working on including new DESI data in the analysis.
- We further plan to constrain such MG theories (particularly with nonminimal couplings) with GWs and their cross correlations with galaxy surveys, in a model independent way.

Thank you

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