

ODDERON EXCHANGE

OBSERVATION AND PROPERTIES

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Intro to Odderon exchange

Model independent results:

Significance at least 6.26σ

Model dependent results:

Significance at least 7.08σ

New results at 8 TeV

1: $H(x)$ scaling

2: ReBB Model vs ATLAS and TOTEM

Summary



Universe 2024, 10(6),264;

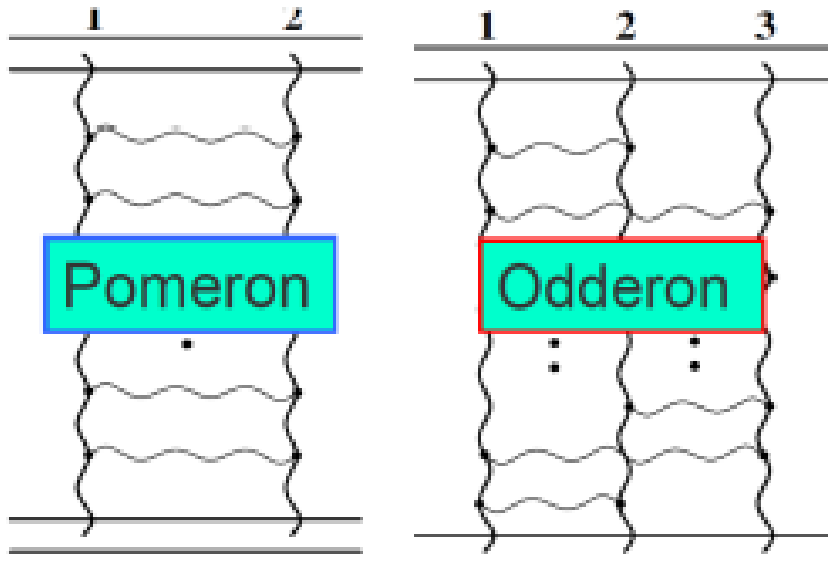
<https://doi.org/10.3390/universe10060264>

[arXiv:2405.06733](https://arxiv.org/abs/2405.06733) [hep-ph]

Odderon: 48 years old scientific puzzle

Odderon: L. Lukaszuk, B. Nicolescu,
Lett. Nuovo Cim. 8, 405 (1973)
Received: 31 July 1973

Odderon is an odd component of
elastic scattering:
Changes sign for crossing



СООБЩЕНИЯ
ОБЪЕДИНЕННОГО
ИНСТИТУТА
ЯДЕРНЫХ
ИССЛЕДОВАНИЙ
Дубна



E2-6350

A.V.Efremov, R.Peschanski

EVIDENCE FOR NEW SINGULARITIES
IN REGGE PHENOMENOLOGY

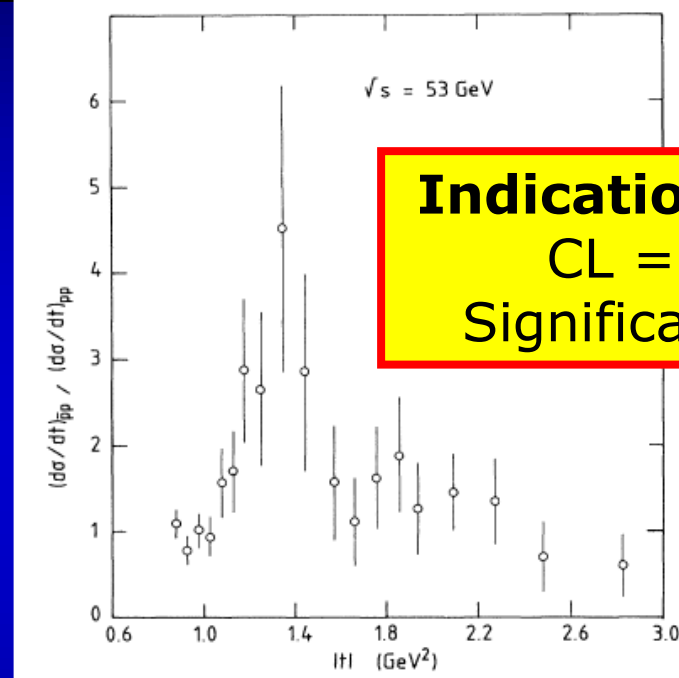
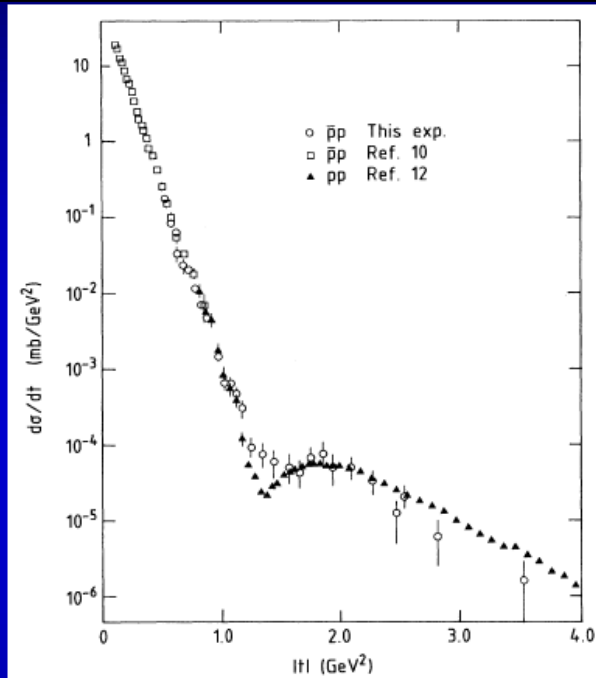
1972

ЛАБОРАТОРИЯ ТЕОРЕТИЧЕСКОЙ ФИЗИКИ

Odderon name coined: D. Joynson, E. Leader, B. Nicolescu, C. Lopez,
Nuovo Cim. 30A, 345 (1975) - Well established in QCD by now !
Honorable mention: A. V. Efremov, R. Peschanski, JINR-E2-6350 (1972)

Odderon: elusive experimentally

Odderon search at ISR: indication but no conclusive result
Breakstone et al, Phys. Rev. Lett. 54, 2180 (**1985**): CL = 99.9 %



Indication of Odderon
CL = 99.9 %,
Significance: 3.35 σ

Terminology for this talk:

Agreement if statistical significance is $< 3 \sigma$

Indication of signal if $3 \sigma \leq \text{significance} < 5 \sigma$

Evidence or observation of signal if $5 \sigma \leq \text{significance}$

Discovery of signal if $5 \sigma \leq \text{significance}$ **for the first time.**

Accepted discovery if [Clay Mathematical Institute \(CMI\) criteria](#) satisfied.

Miscovery if [CMI criteria for Millenium Prize Problems](#) are **not** satisfied.

Odderon: first observation with $> 5 \sigma$




EPJ Web of Conf. (2020) 235: 06005


<https://doi.org/10.1051/epjconf/202023506002>

Proton Holography -- Discovering Odderon from Scaling Properties of Elastic Scattering #4

T. Csorgo (Wigner RCP, Budapest and Eszterhazy Karoly U., Eger), T. Novák (EKU KRC, Gyongyos), R. Pasechnik (Lund U. and Rez, Nucl. Phys. Inst.), A. Sziget (Wigner RCP, Budapest), J. Szanyi (Wigner RCP, Budapest and Eotvos U.) (Apr 15, 2020)

Published in: *EPJ Web Conf.* 235 (2020) 06002 • Contribution to: ISMD 2019 • e-Print: 2004.07095 [hep-ph]

 pdf  DOI  cite

 1 citation

First publication of an at least 5.0σ (6.26σ) odderon effect:

May 11, 2020,

EPJ Web of Conf. 235 (2020) 06002

in an **anonymously refereed / peer reviewed** conference proceedings.

(Proc. ISMD 2019, Santa Fe, USA)

First journal publications, Odderon $> 5 \sigma$

Evidence of Odderon-exchange from scaling properties of elastic scattering at TeV energies #5

T. Csörgő (Wigner RCP, Budapest and CERN), T. Novák (Unlisted, HU), R. Pasechnik (Lund U., Dept. Theor. Phys.), A. Szei (Wigner RCP, Budapest), J. Szanyi (Wigner RCP, Budapest) (Dec 26, 2019)

Published in: *Eur.Phys.J.C* 81 (2021) 2, 180 • e-Print: 1912.11968 [hep-ph]

Online attention



26 tweeters
15 news outlets
3 Mendeley
4 blogs
4 Wikipedia page
2 Facebook pages

This article is in the 98th percentile (ranked 6,037th) of the 428,075 tracked articles of a similar age in all journals and the 99th percentile (ranked 1st) of the 231 tracked articles of a similar age in *The European Physical Journal C*

Published in: *Eur.Phys.J.C* 81 (2021) 7, 611 • e-Print: 2005.14319 [hep-ph]

Online attention



3 tweeters
1 Mendeley
1 Wikipedia page

Hungarian-Swedish team:

Eur. Phys. J. C (2021) **81**: 180, Published: 23 February 2021
<https://doi.org/10.1140/epjc/s10052-021-08867-6>

a real extended Bialas–Bzdak model study #2

J. Szanyi (Eotvos U. and Wigner RCP, Budapest) (May 28, 2020)

Hungarian team, model of Polish origin:

Eur. Phys. J. C (2021) **81**:611, Published: 13 July 2021
<https://doi.org/10.1140/epjc/s10052-021-09381-5>

6 citations

Odderon Exchange from Elastic Scattering Differences between $p\bar{p}$ from pp Forward Scattering Measurements

TOTEM and D0 Collaborations • V.M. Abazov (Dubna, JINR) et al. (Dec 7, 2020)

Published in: *Phys.Rev.Lett.* 127 (2021) 6, 062003 • e-Print: 2012.03401 [hep-ph]

pdf links DOI cite



SUMMARY	News	Blogs	Twitter	Wikipedia	Dimensions citations
Title	Odderon Exchange from Elastic Scattering Differences between pp and pp̄ Data at 1.96 TeV and from pp Forward Scattering Measurements				
Published in	Physical Review Letters, August 2021				
DOI	10.1103/PhysRevLett.127.062003				
Pubmed ID	34420229				
Authors	V. M. Abazov, B. Abbott, B. S. Acharya, M. Adams, T. Adams, J. P. Aghew, G. D. Alexeev, G. Alkhalzov, ... [show]				
TWITTER DEMOGRAPHICS					
MENDELEY READERS					

D0 and TOTEM Collaborations:

Phys. Rev. Lett. **127** (2021) 6, 062003, Published: 4 August 2021
<https://doi.org/10.1103/PhysRevLett.127.062003>

Hungarian-Swedish team, Odderon $> 6.26 \sigma$

Evidence of Odderon-exchange from scaling properties of elastic scattering at TeV energies

#5

T. Csörgő (Wigner RCP, Budapest and CERN), T. Novák (Unlisted, HU), R. Pasechnik (Lund U., Dept. Theor. Phys.), A. Ster (Wigner RCP, Budapest), J. Szanyi (Wigner RCP, Budapest) (Dec 26, 2019)

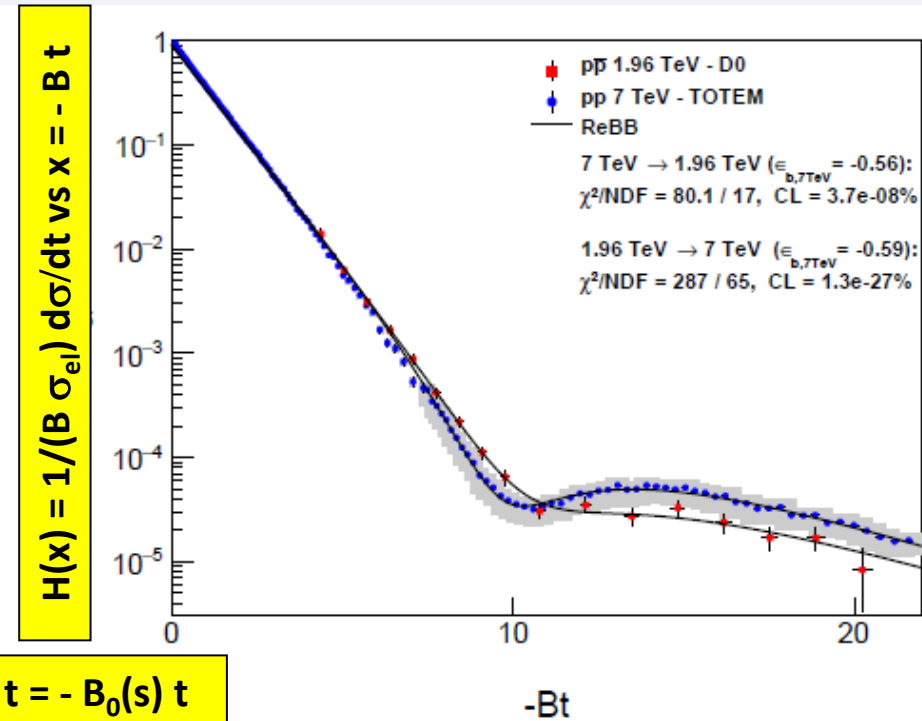
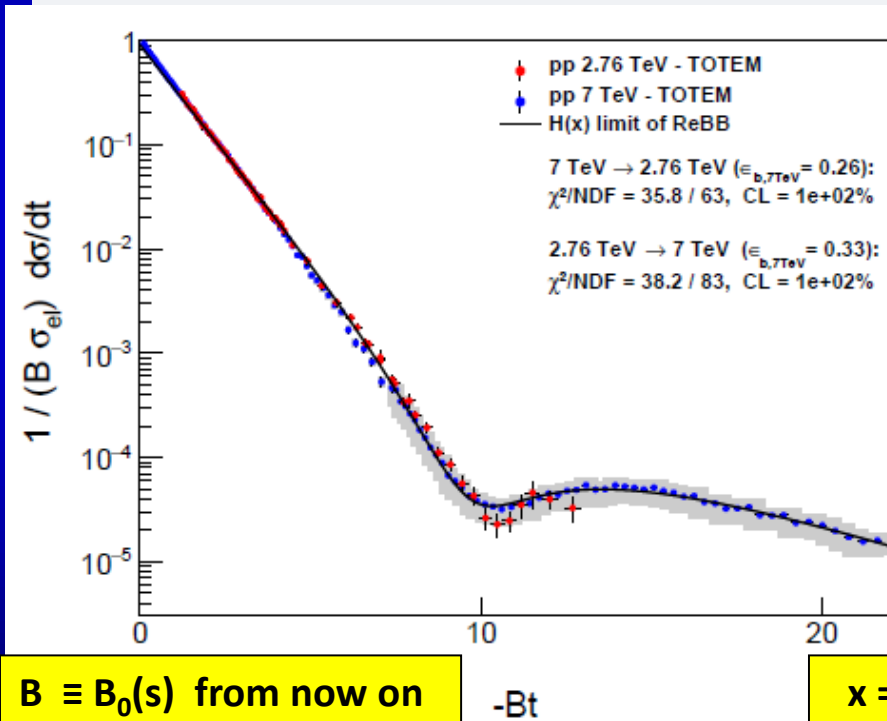
Published in: *Eur.Phys.J.C* 81 (2021) 2, 180 • e-Print: 1912.11968 [hep

Eur. Phys. J. C (2021) 81: 180, published February 2021

<https://doi.org/10.1140/epjc/s10052-021-08867-6>

pdf DOI cite

15 citations



S: Model independent Odderon significance $\geq 6.26 \sigma$

C1: All D0 and TOTEM published data at 1.96, 2.76 and 7.0 TeV

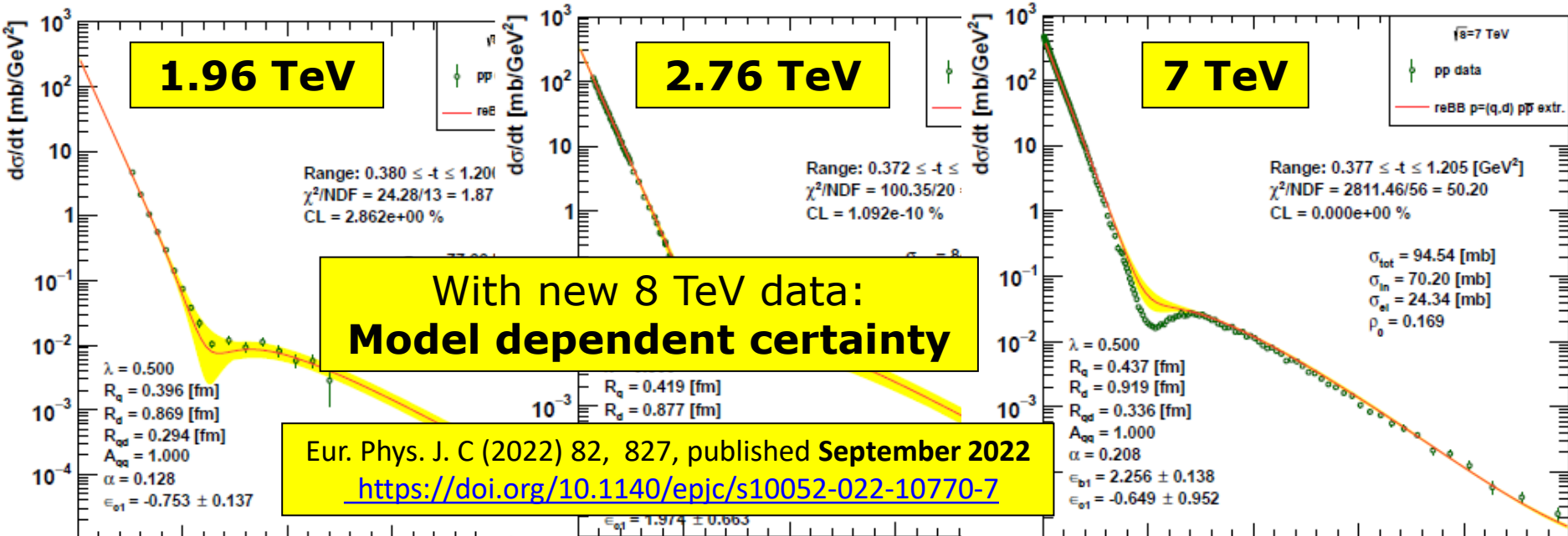
C2: domain of validity is still determined model dependently.

Hungarian team, Polish model, Odderon $> 7.08 \sigma$

Observation of Odderon Effects at LHC energies -- A Real Extended Bialas-Bzdak Model Study #2

T. Csorgo (Wigner RCP, Budapest and EKI KRC, Gyongyos), I. Szanyi (E...)
e-Print: 2005.14319 [hep-ph]

Eur. Phys. J. C (2021) 81:611, published July 2021
<https://doi.org/10.1140/epjc/s10052-021-09381-5>



S: Model dependent Odderon significance $\geq 7.08 \sigma$

C1: All D0 and TOTEM published data at 1.96, 2.76, and 7.0 TeV

C2: domain of validity extended to both pp and pbarp

But **limited to** $0.37 \leq -t \leq 1.2 \text{ GeV}^2$ and $0.546 \leq \sqrt{s} \leq 7 \rightarrow 8 \text{ TeV}$

Model dependent, Real Extended Bialas-Bzdak theory results, Odderon significance $\geq 7.08 \sigma$, from 1.96 and 2.76 TeV data only

2023-24: new 0 observations with $> 5 \sigma$

Model-independent Odderon Results Based on TOTEM data on Elastic Proton-Proton Scattering at 8 TeV #2

T. Csörgő (Wigner RCP, Budapest and Karoly Robert U. Coll.), T. Novák (Karoly Robert U. Coll.), R. Pasechnik (Lund U.), A. Ster (Wigner RCP, Budapest), I. Szanyi (Wigner RCP, Budapest and Karoly Robert U. Coll. and Eotvos U.) (Feb 9, 2023)

Published in: *Acta Phys.Polon.Supp.* 16 (2023) 5, 2 • Contribution to: Diffflowx2022, 2, Diffflowx2022 • e-Print: 2302.04930 [hep-ex]

Hungarian – Swedish team, new TOTEM data at 8 TeV:
Model-independent $H(x)$ scaling method
Proc. Diffraction and Low-x 2022 by T. Csörgő
8 TeV data confirm and strengthen the Odderon signal

Model-independent Odderon results based on new TOTEM data on elastic pp collisions at 8 TeV #1

T. Csörgő (Budapest, RMKI and Karoly Robert U. Coll.), T. Novák (Karoly Robert U. Coll. and Budapest, Tech. U.), R. Pasechnik (Lund U.), A. Ster (Budapest, RMKI), I. Szanyi (Budapest, RMKI and Karoly Robert U. Coll. and Eotvos U.) (May 10, 2024)

Contribution to: ISMD23 • e-Print: 2405.06733 [hep-ph]

Hungarian – Swedish team, scaling method:
New TOTEM 8 TeV data vs $H(x)$ scaling:
MDPI Universe (2024) 10(6), 264;
Detailed peer reviewed paper, see talk of A. Ster

Universe 2024, 10(6),264;

<https://doi.org/10.3390/universe10060264>

[arXiv:2405.06733](https://arxiv.org/abs/2405.06733) [hep-ph]

What about domain of validity, model independently?
-- stay tuned... coming soon

Looking for Crossing-Odd(eron) effects

$$\begin{aligned}T_{\text{el}}^{PP}(s,t) &= T_{\text{el}}^+(s,t) - T_{\text{el}}^-(s,t), \\T_{\text{el}}^{P\bar{P}}(s,t) &= T_{\text{el}}^+(s,t) + T_{\text{el}}^-(s,t), \\T_{\text{el}}^+(s,t) &= T_{\text{el}}^P(s,t) + T_{\text{el}}^f(s,t), \\T_{\text{el}}^-(s,t) &= T_{\text{el}}^O(s,t) + T_{\text{el}}^\omega(s,t).\end{aligned}$$

$$\begin{aligned}T_{\text{el}}^P(s,t) &= \frac{1}{2} \left(T_{\text{el}}^{PP}(s,t) + T_{\text{el}}^{P\bar{P}}(s,t) \right) \\T_{\text{el}}^O(s,t) &= \frac{1}{2} \left(T_{\text{el}}^{P\bar{P}}(s,t) - T_{\text{el}}^{PP}(s,t) \right)\end{aligned}$$

for $\sqrt{s} \geq 1 \text{ TeV}$,

Three simple consequences:

$$T_{\text{el}}^O(s,t) = 0 \implies \frac{d\sigma^{pp}}{dt} = \frac{d\sigma^{p\bar{p}}}{dt} \quad \text{for } \sqrt{s} \geq 1 \text{ TeV}$$

$$\frac{d\sigma^{pp}}{dt} = \frac{d\sigma^{p\bar{p}}}{dt} \quad \text{for } \sqrt{s} \geq 1 \text{ TeV} \not\Rightarrow T_{\text{el}}^O(s,t) = 0.$$

$$\frac{d\sigma^{pp}}{dt} \neq \frac{d\sigma^{p\bar{p}}}{dt} \quad \text{for } \sqrt{s} \geq 1 \text{ TeV} \implies T_{\text{el}}^O(s,t) \neq 0$$

9

Scaling in the diffractive cone region

$$\frac{d\sigma}{dt} = A(s) \exp [B(s)t]$$

$$A(s) = B(s) \sigma_{\text{el}}(s) = \frac{1 + \rho_0^2(s)}{16\pi} \sigma_{\text{tot}}^2(s),$$

$$\frac{1}{B(s)\sigma_{\text{el}}(s)} \frac{d\sigma}{dt} = \exp [tB(s)]$$

$$H(x) \equiv \frac{1}{B(s)\sigma_{\text{el}}(s)} \frac{d\sigma}{dt},$$
$$x = -tB(s).$$

Advantages:

- 1) $H(x) \sim \exp(-x)$ in the diffractive cone
- 2) Start from a place that you know
- 3) Measurable both for pp and pbarp

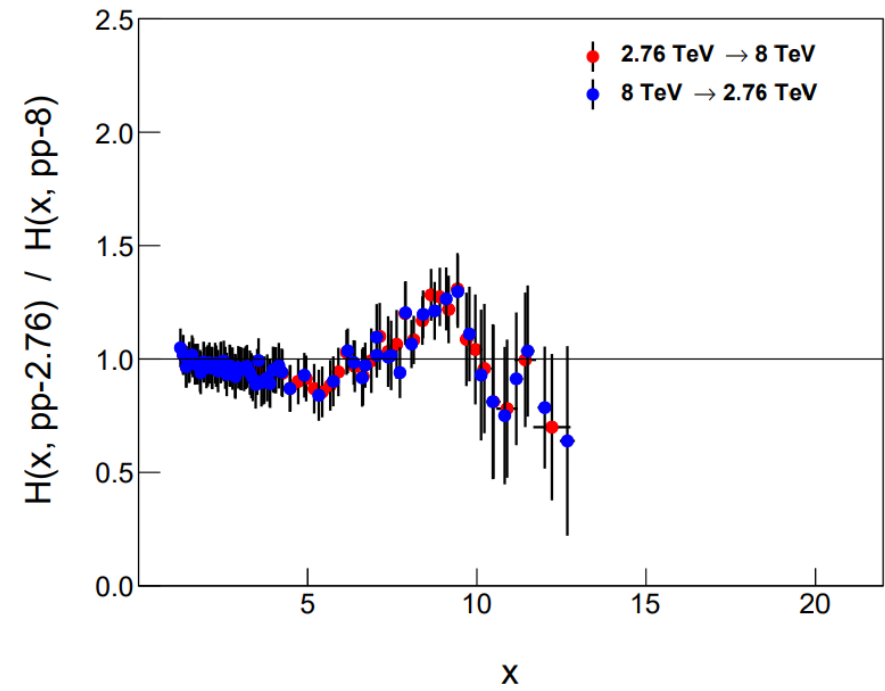
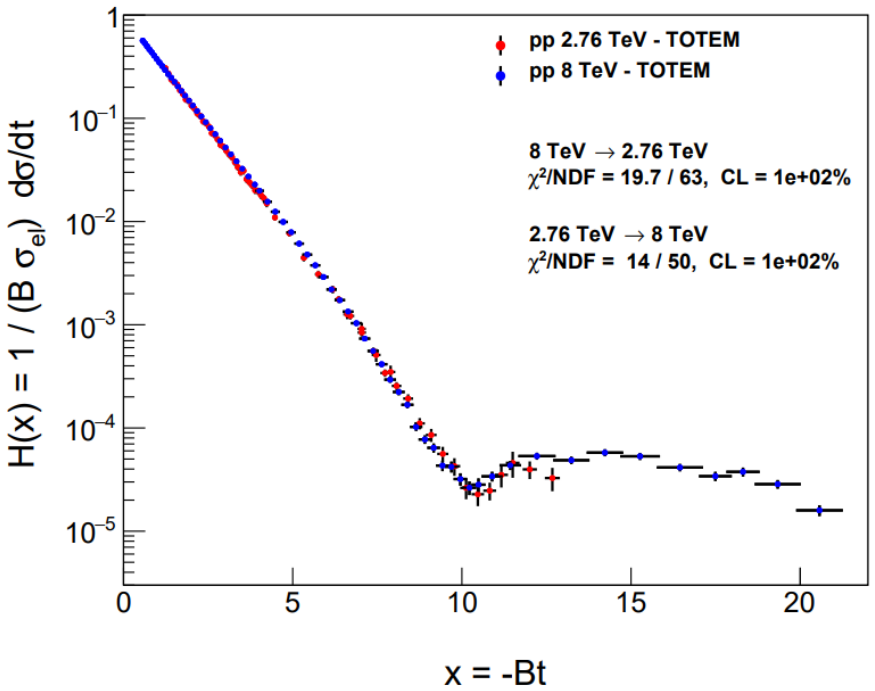
NEW RESULTS 1

H(x) SCALING, USING 8 TeV

Test of H(x) scaling: 8 vs 2.76 TeV

$$H(x) \equiv \frac{1}{B(s)\sigma_{el}(s)} \frac{d\sigma}{dt},$$

$$x = -tB(s).$$



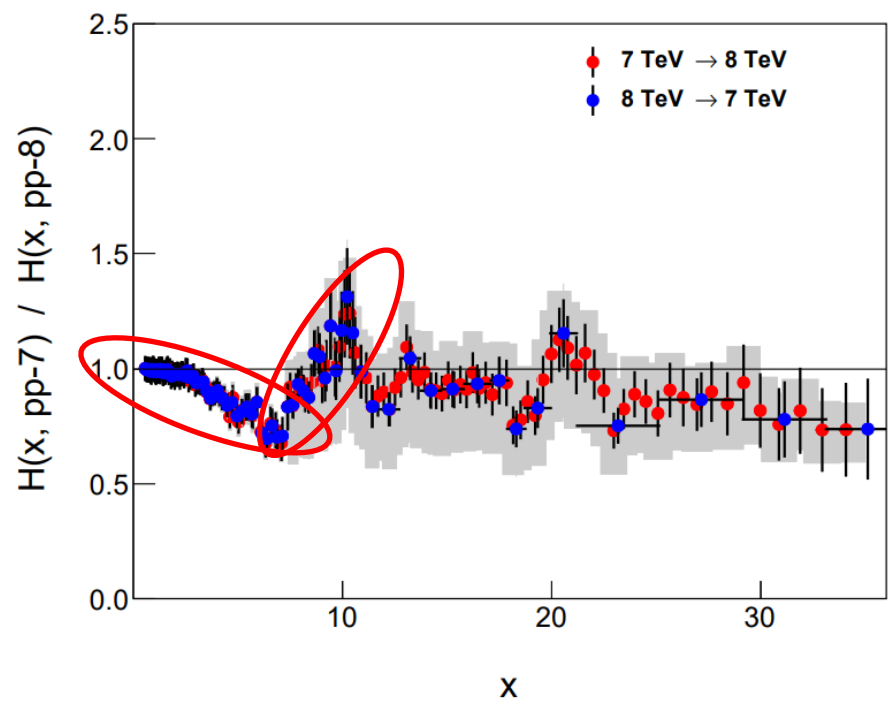
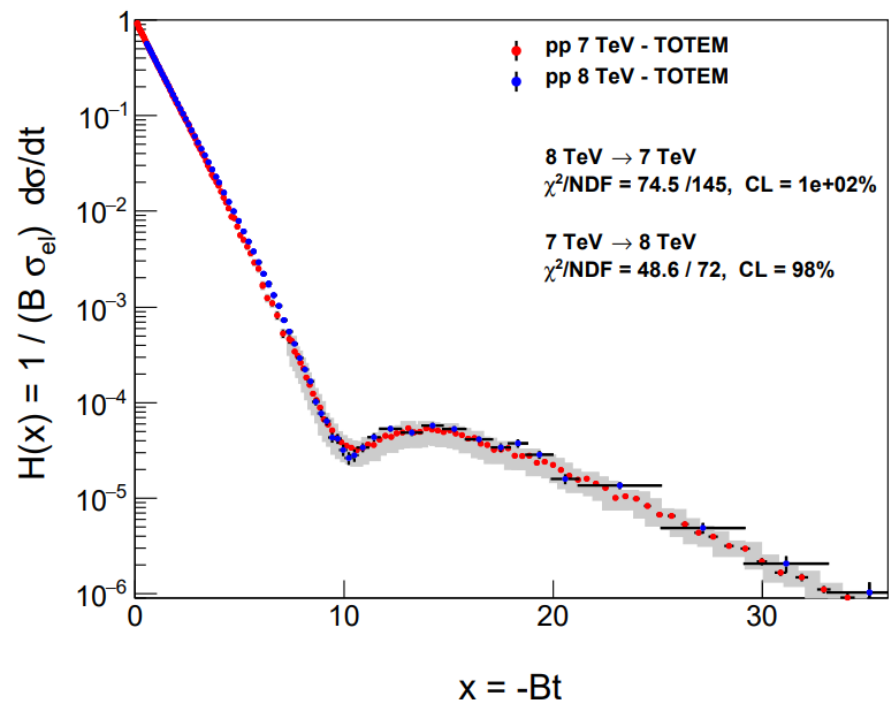
Between 2.76 and 8 TeV, H(x) scaling observed!

Hungarian-Swedish team, e-Print: [2405.06733](https://arxiv.org/abs/2405.06733) [hep-ph],

Test of H(x) scaling: 8 vs 7 TeV TOTEM

$$H(x) \equiv \frac{1}{B(s)\sigma_{el}(s)} \frac{d\sigma}{dt},$$

$$x = -tB(s).$$



Between 7 and 8 TeV, H(x) scaling observed, but ...

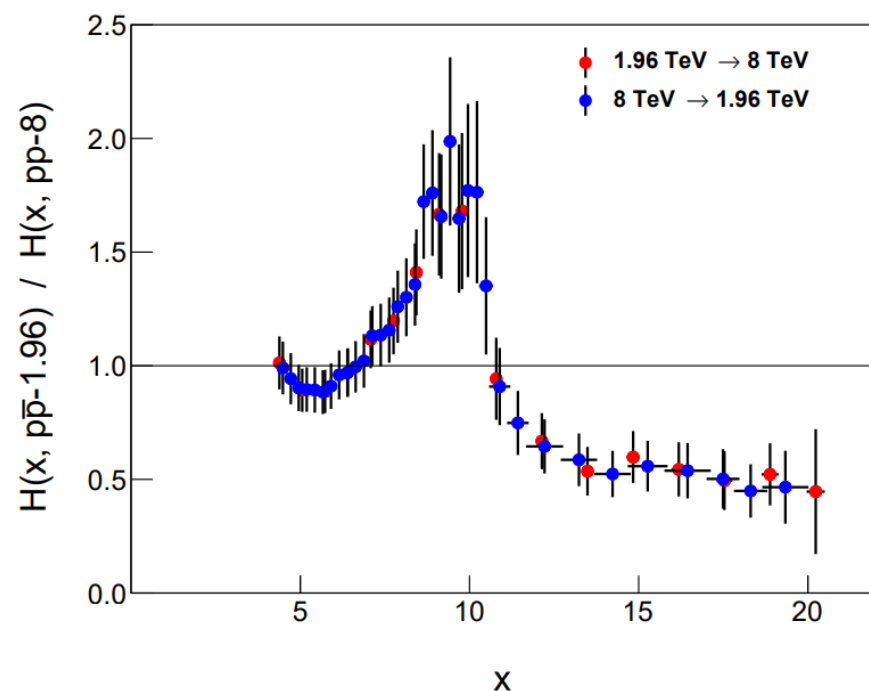
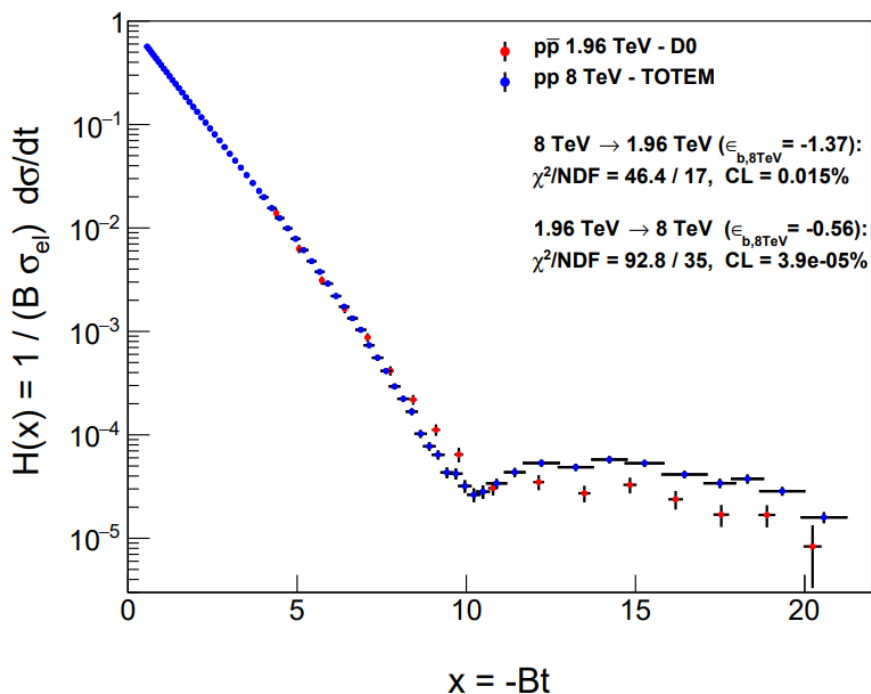
Hungarian-Swedish team, e-Print: [2405.06733](https://arxiv.org/abs/2405.06733) [hep-ph],

MDPI Universe 2024, 10(6), 264

Odderon of $H(x)$ scaling: 8 vs 1.96 TeV

$$H(x) \equiv \frac{1}{B(s)\sigma_{\text{el}}(s)} \frac{d\sigma}{dt},$$

$$x = -tB(s).$$



Between 1.96 and 8 TeV, $H(x|s,pp)$ and $H(x|s,p\bar{p})$ are clearly different, with $3 < 3.79 < 5 \sigma$

Hungarian-Swedish team, e-Print: [2405.06733](https://arxiv.org/abs/2405.06733) [hep-ph],

Odderon significances from $H(x)$ scaling

\sqrt{s} (TeV)	χ^2	NDF	CL	significance (σ)
1.96 vs. 2.76	3.85	11	9.74×10^{-1}	0.03
1.96 vs. 7	80.1	17	3.681×10^{-10}	6.26
1.96 vs. 8	46.4	17	1.502×10^{-4}	3.79

\sqrt{s} (TeV)	χ^2	NDF	CL	χ^2/NDF method	combined σ Stouffer's method
1.96 vs 2.76 & 8	50.25	28	6.064×10^{-3}	2.74	2.70
1.96 vs 2.76 & 7	83.95	28	1.698×10^{-7}	5.22	4.44
1.96 vs 2.76 & 7 & 8	130.35	45	2.935×10^{-10}	6.30	5.81
1.96 vs 7 & 8	126.5	34	1.415×10^{-12}	7.08	7.10

If 1.96, 2.76, 7 and 8 TeV data are combined, $H(x)$ significances on all data results in $5 < 5.8 \sigma$
If 1.96, 7 and 8 TeV data are combined, at least 7.08 σ .

Hungarian-Swedish team, e-Print: [2405.06733](https://arxiv.org/abs/2405.06733) [hep-ph],

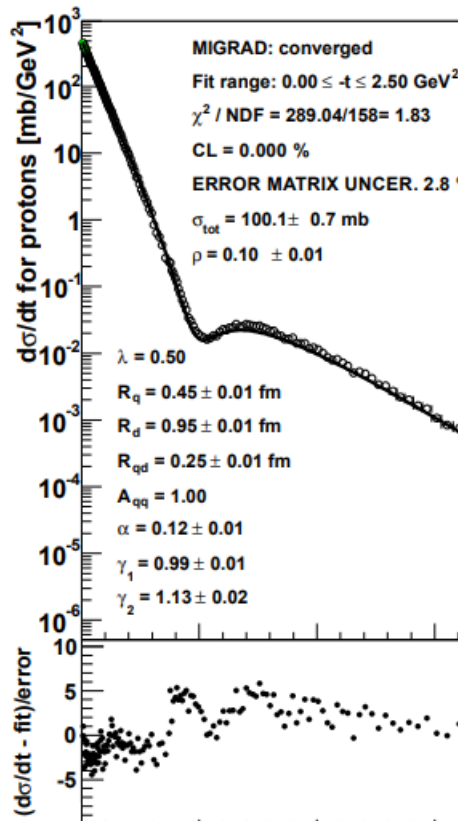
MDPI Universe **2024**, *10*(6), 264

NEW RESULTS 2

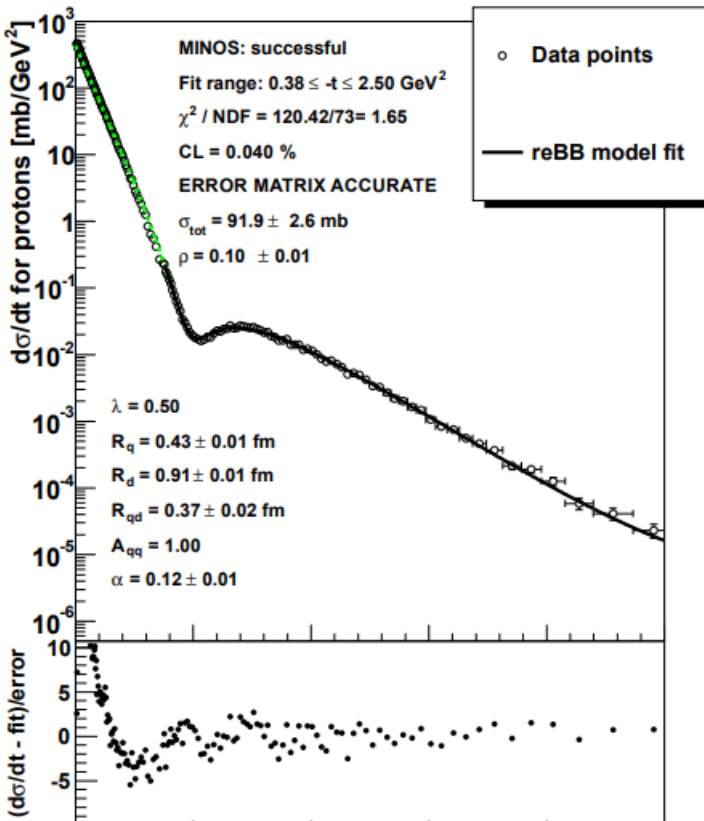
**Low- t extension of ReBB
7 and 8 TeV pp
(cross-check, without Levy)**

Statement of the problem, with old chi2

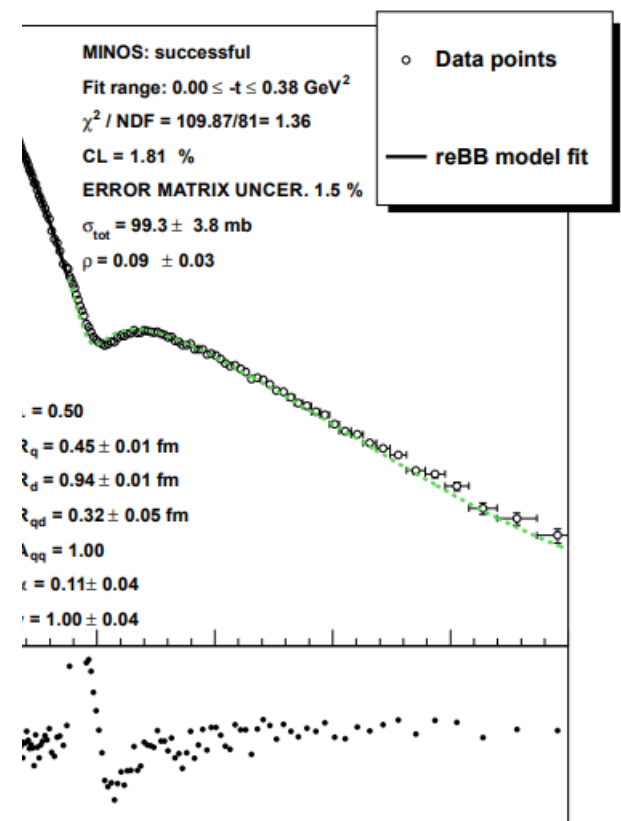
p+p → p+p, diquark as a single entity



p+p → p+p, diquark as a single entity at $\sqrt{s}=7000.0 \text{ GeV}$



+p, diquark as a single entity at $\sqrt{s}=7000.0 \text{ GeV}$



Excitation function of elastic pp scattering from a unitarily extended Bialas–Bzdak model

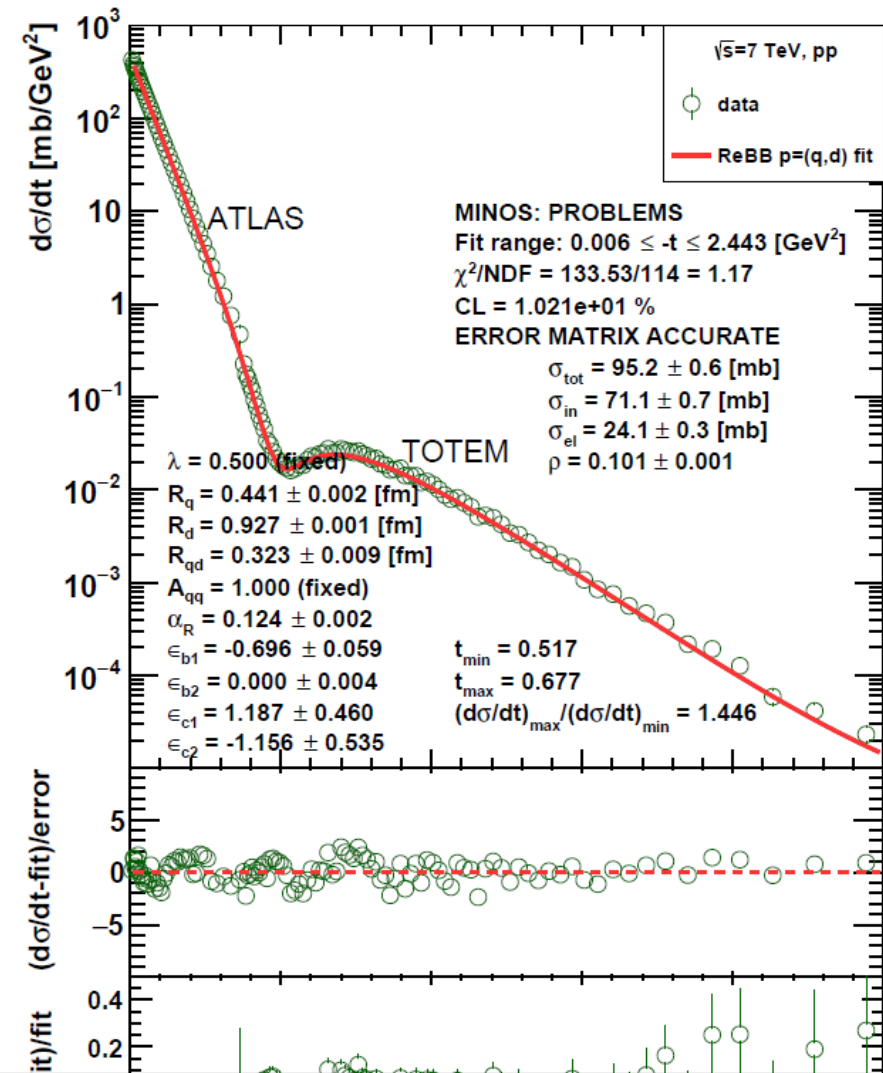
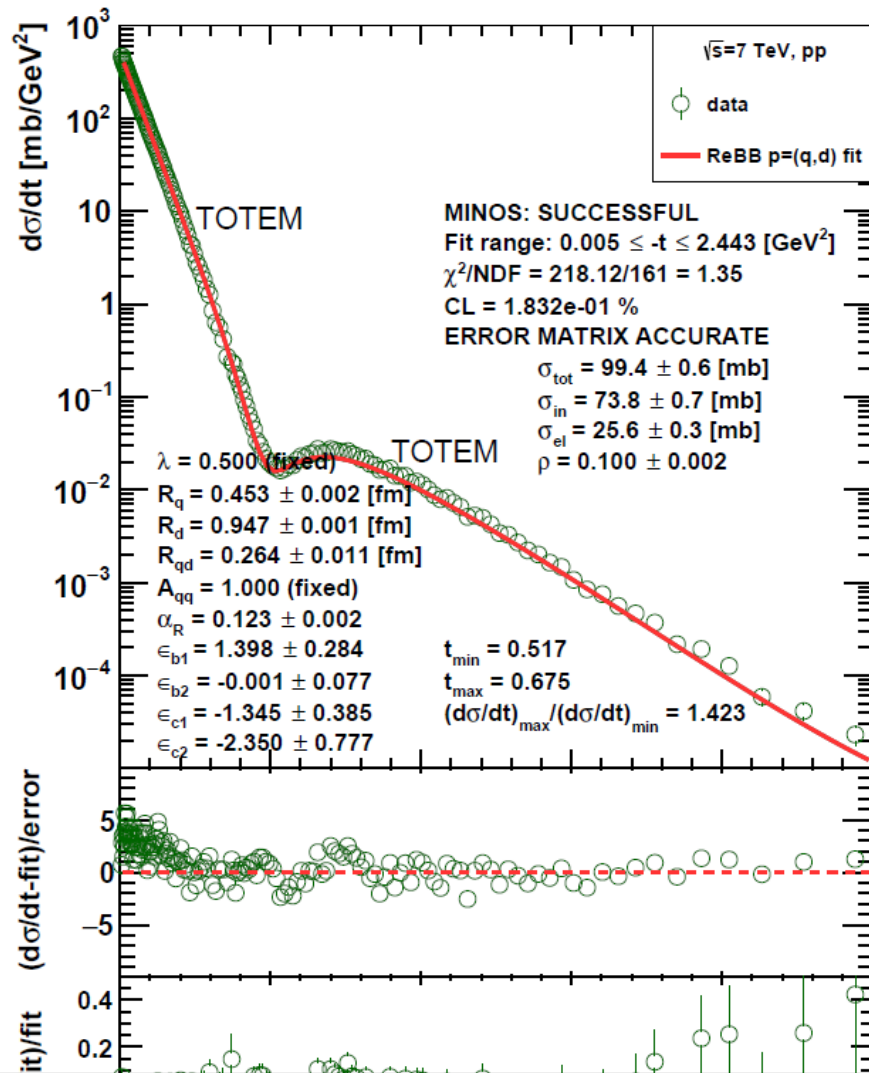
#1

F. Nemes (CERN and Wigner RCP, Budapest), T. Csörgő (Wigner RCP, Budapest and Unlisted, HU), M. Csanád (Eotvos U.) (Apr 16, 2015)

Published in: *Int.J.Mod.Phys.A* 30 (2015) 14, 1550076 • e-Print: 1505.01415 [hep-ph]

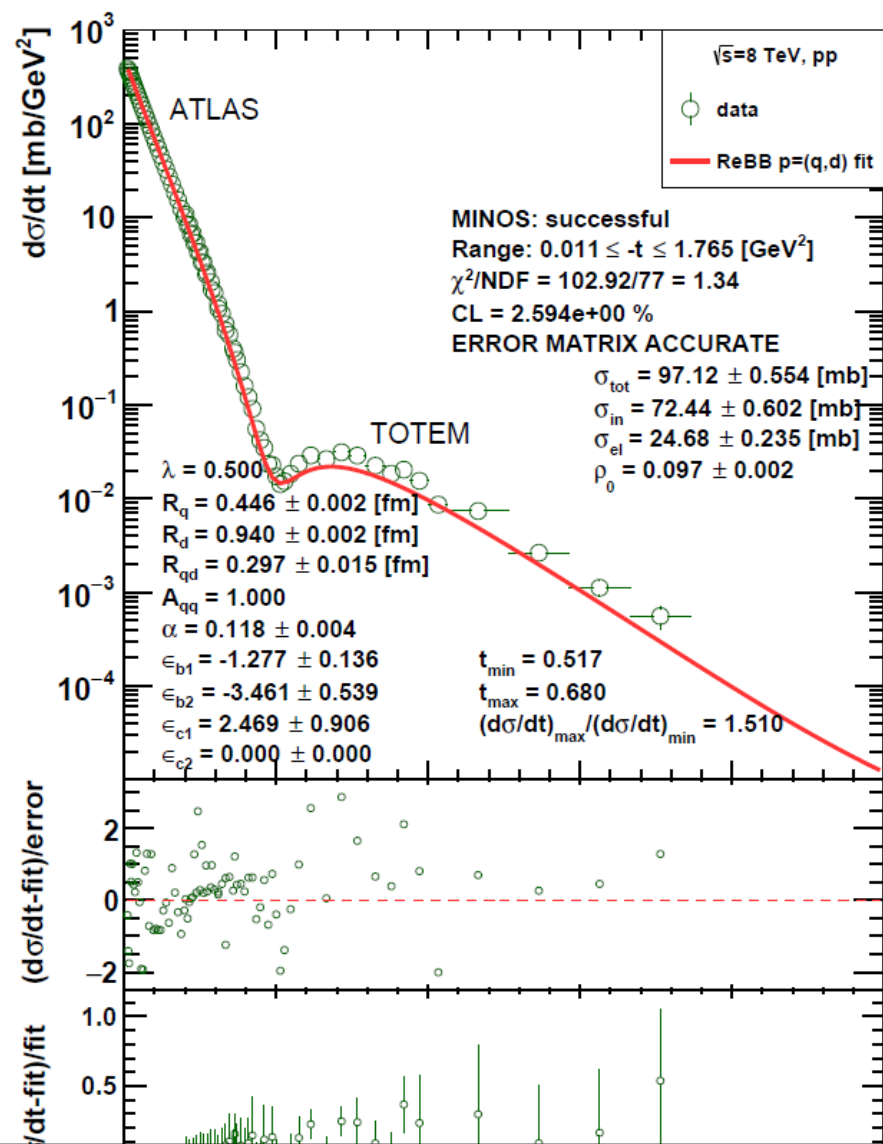
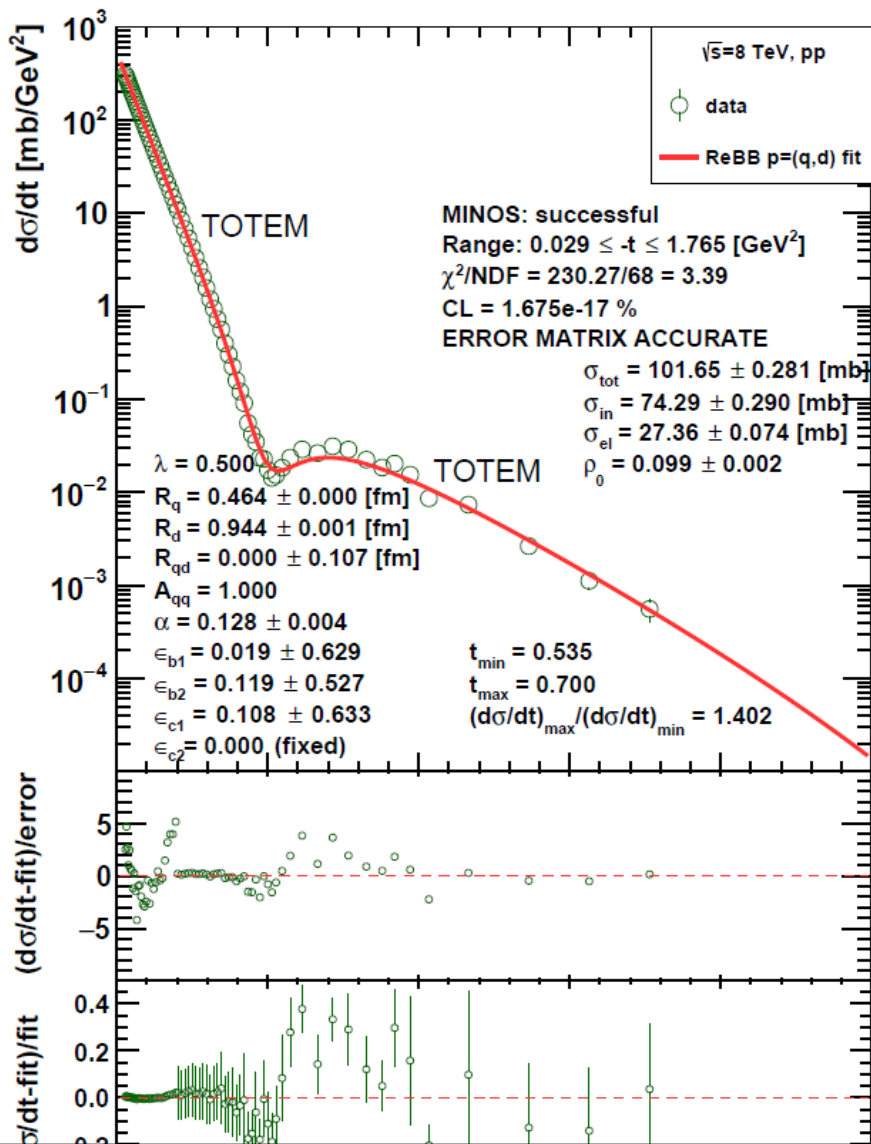
**TOTEM low-t vs TOTEM-large-t fit acceptable at 7 TeV, but
 The two datasets could not be ReBB fitted without a PHENIX method !**

ReBB model extension to low $-t$, 7 TeV



TOTEM low- t vs TOTEM-large- t fit acceptable at 7 TeV, using using PHENIX method of covariance diagonalization, but ...
ATLAS low- t vs TOTEM-large- t fit successful at 7 TeV !

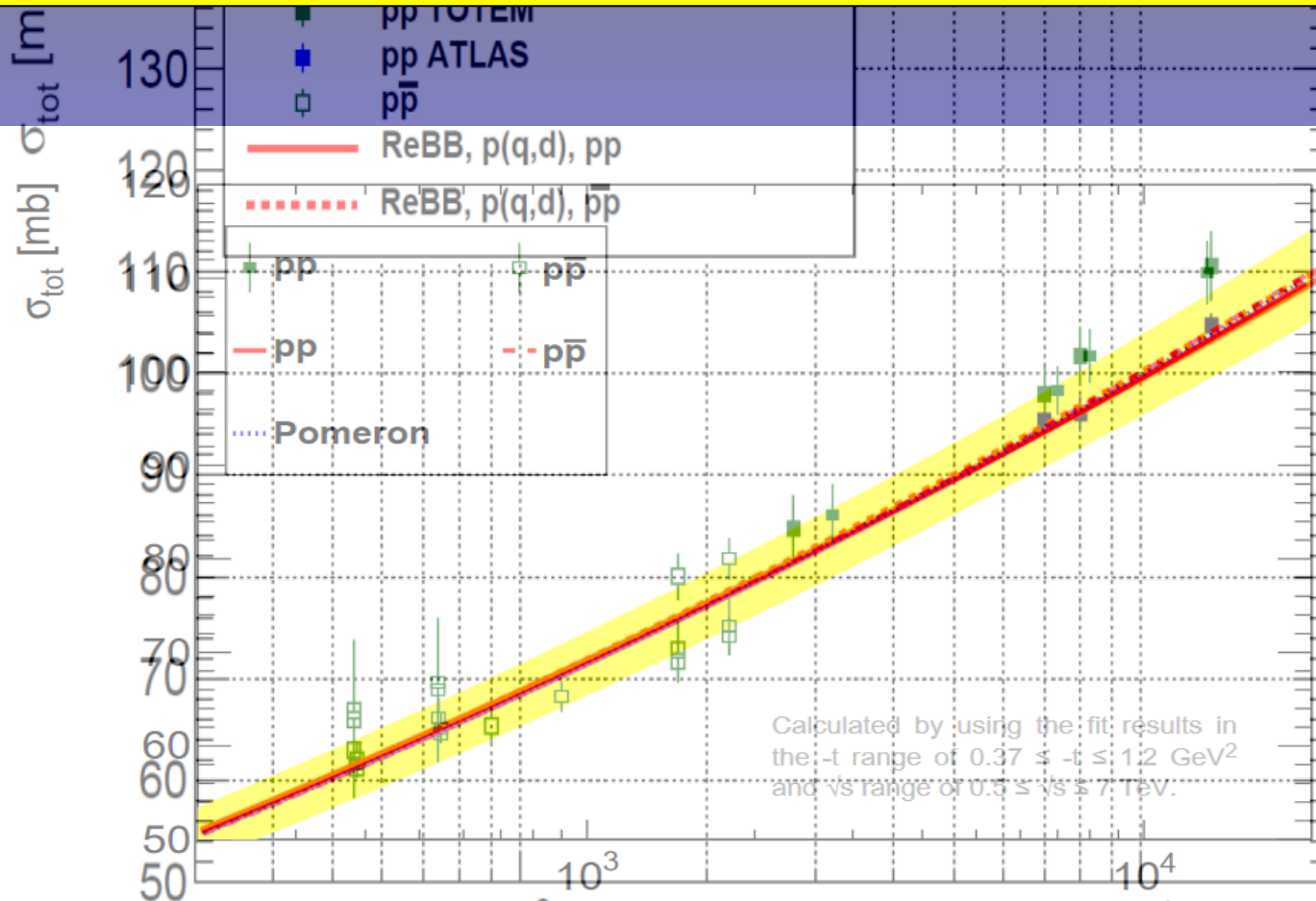
ReBB model extension to low $-t$, 8 TeV



TOTEM low- t vs TOTEM-large- t fit FAILS at 8 TeV, but ...
ATLAS low- t vs TOTEM-large- t fit SUCCESSFUL at 8 TeV !

ReBB at low $-t$ vs ATLAS and TOTEM σ_{tot}

ReBB prediction vs ATLAS and TOTEM data at low $-t$:



T. Csörgő and I. Szanyi, *Eur.Phys.J.C* 81 (2021) 7, 611 • e-Print: [2005.14319](https://arxiv.org/abs/2005.14319) [hep-ph]

Fig. 27 Excitation function of the total cross-section for elastic pp , $p\bar{p}$ collisions and for the amplitude of Pomeron exchange, as evaluated from the log-linear excitation functions of the opacity parameters $\alpha^{PP}(s)$ and $\alpha^{P\bar{P}}(s)$ as well as that of the scale parameters, $R_q(s)$, $R_d(s)$, $R_{qd}(s)$, corresponding to Table 2. The yellow band indicates our conservative estimates on the systematic errors of the total cross-section of the Pomeron exchange.

Detailed Summary and Conclusions

New 8 TeV TOTEM data strengthen
Odderon signal using $H(x)$ scaling method

New 8 TeV TOTEM data strengthen
Odderon signal using ReBB model

ReBB fit range can be extended to low $-t$ at 8 TeV, if ATLAS data
are used instead of TOTEM low $-t$ data

THANK YOU !

QUESTIONS?

2022 observations of Odderon with $> 5 \sigma$

Characterisation of the dip-bump structure observed in proton-proton elastic scattering at $\sqrt{s} = 8 \text{ TeV}$ #1

TOTEM Collaboration • G. Antchev (Pilsen U.) et al. (Nov 23, 2021)

Published in: *Eur.Phys.J.C* 82 (2022) 3, 263 • e-Print: 2111.11991 [hep-ex]

Online attention



This article is in the 1st percentile (ranked 279,419th) of the 343,918 tracked articles of a similar age in all journals and the 1st percentile (ranked 73rd) of the 114 tracked articles of a similar age in *The European Physical Journal C*

TOTEM Collaboration:

8 TeV: EPJ C (2022) 82, 263 (2022). **Published: March 26, 2022**
<https://doi.org/10.1140/epjc/s10052-022-10065-x>
Publishes final data for D0-TOTEM PRL published in 2021

The ReBB model and its H(x) scaling version at 8 TeV: Odderon exchange is a certainty #1

I. Szanyi (Eotvos U. and Wigner RCP, Budapest and Karoly Robert U. Coll.), T. Csörgő (Wigner RCP, Budapest and Karoly Robert U. Coll.) (Apr 21, 2022)

Published in: *Eur.Phys.J.C* 82 (2022) 9, 827, *Eur.Phys.J.C* 82 (2022) 827 • e-Print: 2204.10094 [hep-ph]

Online attention



This article is in the 64th percentile (ranked 57,525th) of the 166,532 tracked articles of a similar age in all journals and the 99th percentile (ranked 1st) of the 1 tracked articles of a similar age in *The European Physical Journal C*

Hungarian team, model of Polish origin:

New TOTEM 8 TeV data vs ReBB model predictions:
EPJ C 82 (2022) 9, 827. **Published: Sept 19, 2022**

In the ReBB model, Odderon exchange is a certainty

Presented at Zimányi'22 by I. Szanyi

What about model independent results?

NEW RESULTS 3

Simple Levy fits at small $-t$
(For details, see talk of I. Szanyi)

Review: Elastic scattering at small $-t$

$$\frac{d\sigma}{dt}(s, t) \simeq A(s) \exp(tB(s))$$

$$\sigma_{el}(s) = \int_0^\infty d|t| \frac{d\sigma(s)}{dt}$$

$$A(s) = \frac{1}{16\pi} (1 + \rho_0^2(s)) \sigma_{tot}^2(s)$$

$$\sigma_{el}(s) = \frac{1}{16\pi} (1 + \rho_0^2(s)) \frac{\sigma_{tot}^2(s)}{B_0(s)}$$

If Odderon exists: signals possible both at $t = 0$ and at $-t > 0$.
Where the significance of the signal is coming from?

Odderon Search at small -t

$$T_{el}^O(s,t) = \frac{1}{2} \left(T_{el}^{pp\bar{p}}(s,t) - T_{el}^{pp}(s,t) \right) \quad \text{valid for } \sqrt{s} \geq 1 \text{ TeV},$$

Some simple consequences at small -t, Gaussian sources:

$$\frac{d\sigma}{dt}(s,t) \simeq A(s) \exp(tB(s))$$

If any of

$$\begin{aligned} A^{pp}(s) &\neq A^{pp\bar{p}}(s), \\ B^{pp}(s) &\neq B^{pp\bar{p}}(s). \end{aligned}$$

$$\begin{aligned} \rho_0^{pp}(s) &\neq \rho_0^{pp\bar{p}}(s), \\ \sigma_{el}^{pp}(s) &\neq \sigma_{el}^{pp\bar{p}}(s), \\ \sigma_{tot}^{pp}(s) &\neq \sigma_{tot}^{pp\bar{p}}(s). \end{aligned}$$

is statistically significant

$$\text{for } \sqrt{s} \geq 1 \text{ TeV} \implies T_{el}^O(s,0) \neq 0$$

Odderon Search at small $-t$

$$T_{el}^O(s, t) = \frac{1}{2} \left(T_{el}^{pp\bar{p}}(s, t) - T_{el}^{pp}(s, t) \right) \quad \text{valid for } \sqrt{s} \geq 1 \text{ TeV,}$$

Some simple consequences at small $-t$, Levy sources:

If any of

$$a^{pp}(s) \neq a^{pp\bar{p}}(s),$$

$$b^{pp}(s) \neq b^{pp\bar{p}}(s),$$

$$\alpha_L^{pp} \neq \alpha_L^{pp\bar{p}},$$

$$\frac{d\sigma}{dt}(s, t) \simeq a(s) \exp \left[-(tb(s))^{\alpha_L/2} \right]$$

is statistically significant

$$\text{for } \sqrt{s} \geq 1 \text{ TeV} \implies T_{el}^O(s, 0) \neq 0$$

$$\rho_0^{pp}(s) \neq \rho_0^{pp\bar{p}}(s),$$

$$\sigma_{el}^{pp}(s) \neq \sigma_{el}^{pp\bar{p}}(s),$$

$$\sigma_{tot}^{pp}(s) \neq \sigma_{tot}^{pp\bar{p}}(s).$$

Lévy α -Stable Model for the Non-Exponential Low- $|t|$ Proton-Proton Differential Cross-Section #1

Tamás Csörgő (Karoly Robert U. Coll. and Budapest, RMKI), Sándor Hegyi (Budapest, RMKI), István Szanyi (Karoly Robert U. Coll. and Budapest, RMKI and Eotvos U., Dept. Atomic Phys.) (Aug 3, 2023)

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Levy generalized Bialas-Bzdak Model

Simple results at small -t:

$$a(s) = \frac{81}{16} \pi \left(2R_q^{\alpha_L(s)}(s) \right)^{4/\alpha_L} (1 + 4\alpha_R^2(s))$$

$$b(s) = \frac{1}{36} \left(\frac{4}{3} \right)^{2/\alpha_L(s)} \left((2 + 2\alpha_L(s)) R_{qd}^{\alpha_L(s)}(s) + 3\alpha_L(s) \left(2R_d^{\alpha_L(s)}(s) + R_q^{\alpha_L(s)}(s) \right) \right)^{2/\alpha_L(s)}$$

$$\rho_0(s) = 2\alpha_R(s)$$

$$\sigma_{tot}(s) = 9\pi \left(2R_q^{\alpha_L(s)}(s) \right)^{2/\alpha_L(s)}$$

$$\sigma_{el}(s) = \frac{a(s)}{b(s)} \Gamma \left(\frac{2 + \alpha_L(s)}{\alpha_L(s)} \right)$$

From data fits: R_q , R_d , R_{qd} , α_L is same in pp and pbarb
But!

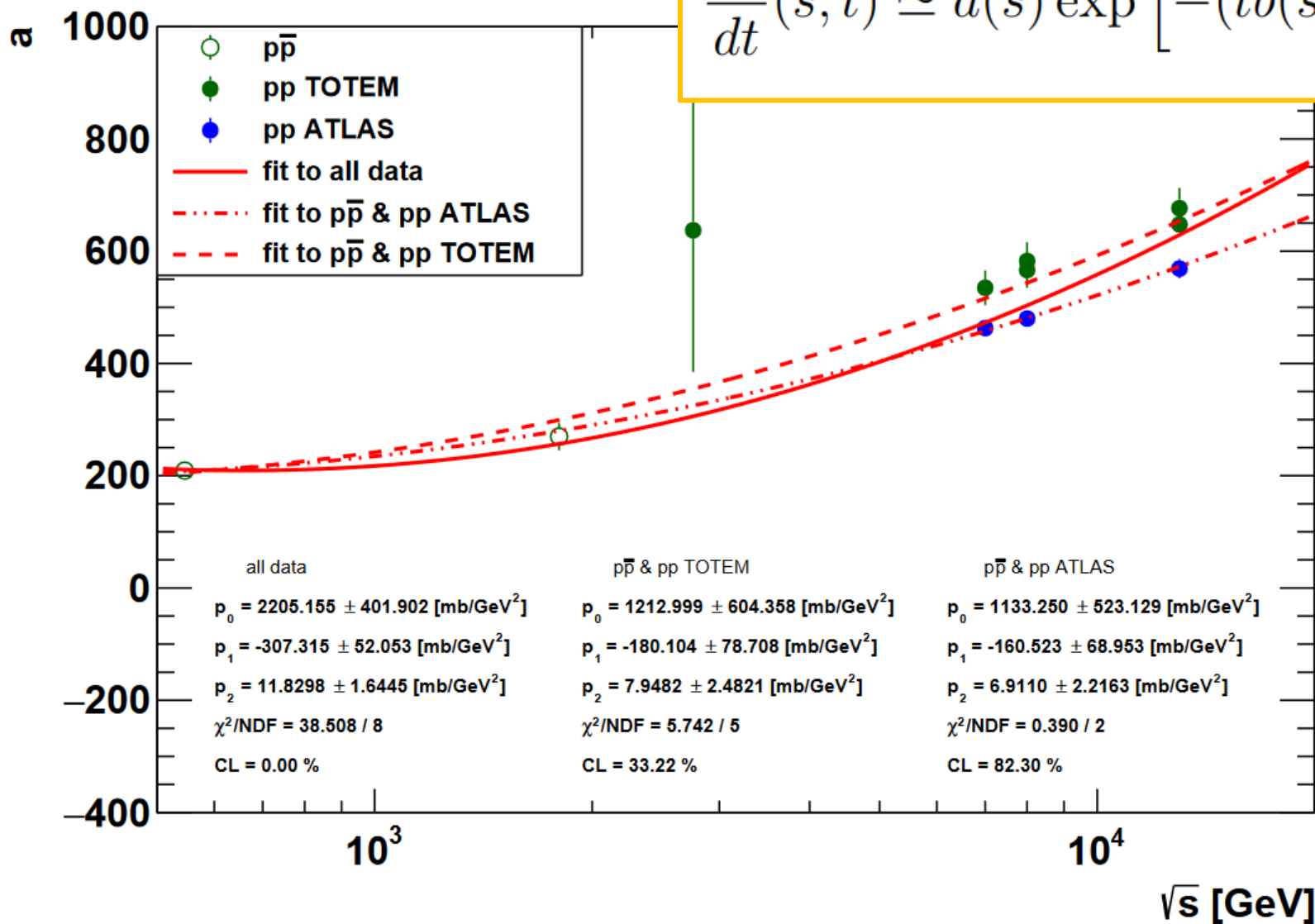
$$\rho_0^{pp}(s) \neq \rho_0^{p\bar{p}}(s),$$

Lévy α -stable model for the non-exponential low- $|t|$ proton-proton differential cross section

T. Csörgő (Karoly Robert U. Coll. and Budapest, RMKI), S. Hegyi, I. Szanyi (Karoly Robert U. Coll. and Budapest, RMKI and Eotvos U., Dept. Atomic Phys.) (Aug 9, 2023)

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$$\frac{d\sigma}{dt}(s, t) \simeq a(s) \exp \left[-(tb(s))^{\alpha_L/2} \right]$$

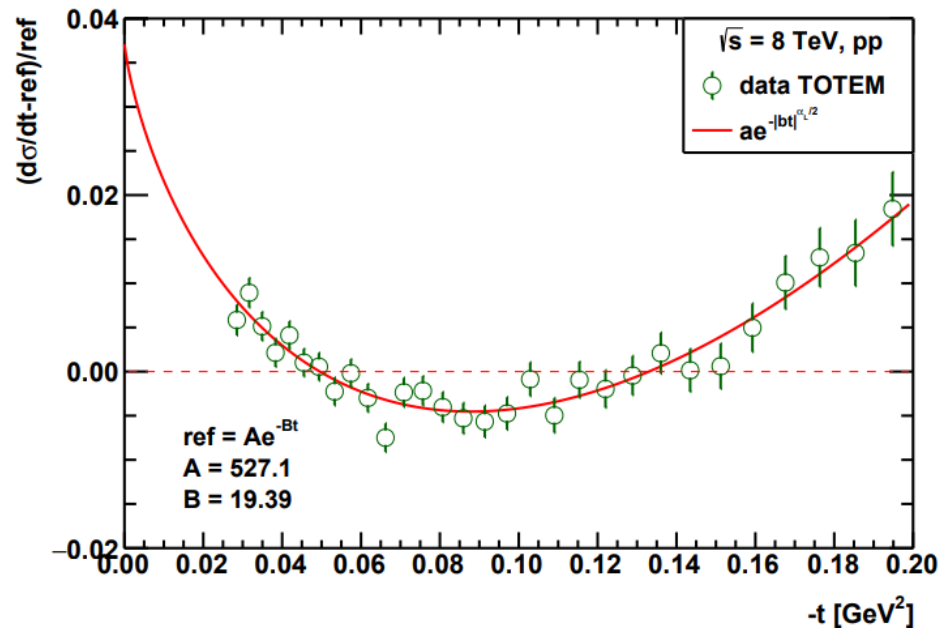
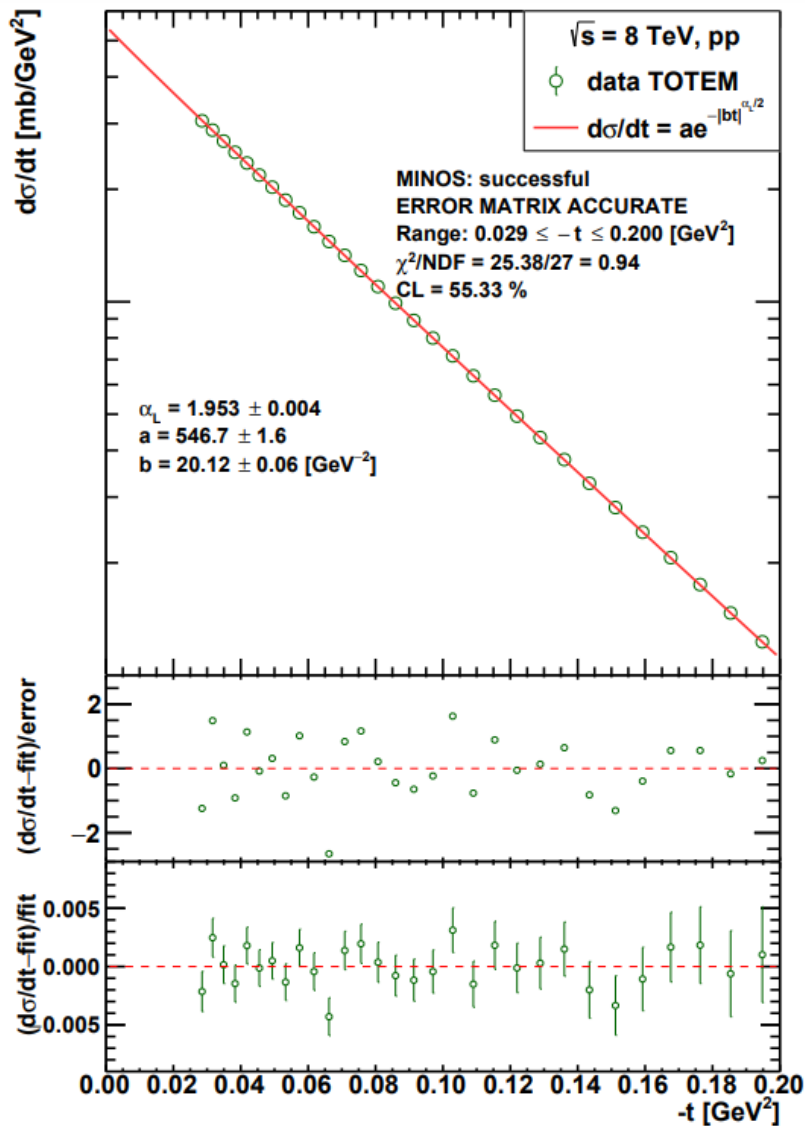


Lévy α -stable model for the non-exponential low- $|t|$ proton-proton differential cross section

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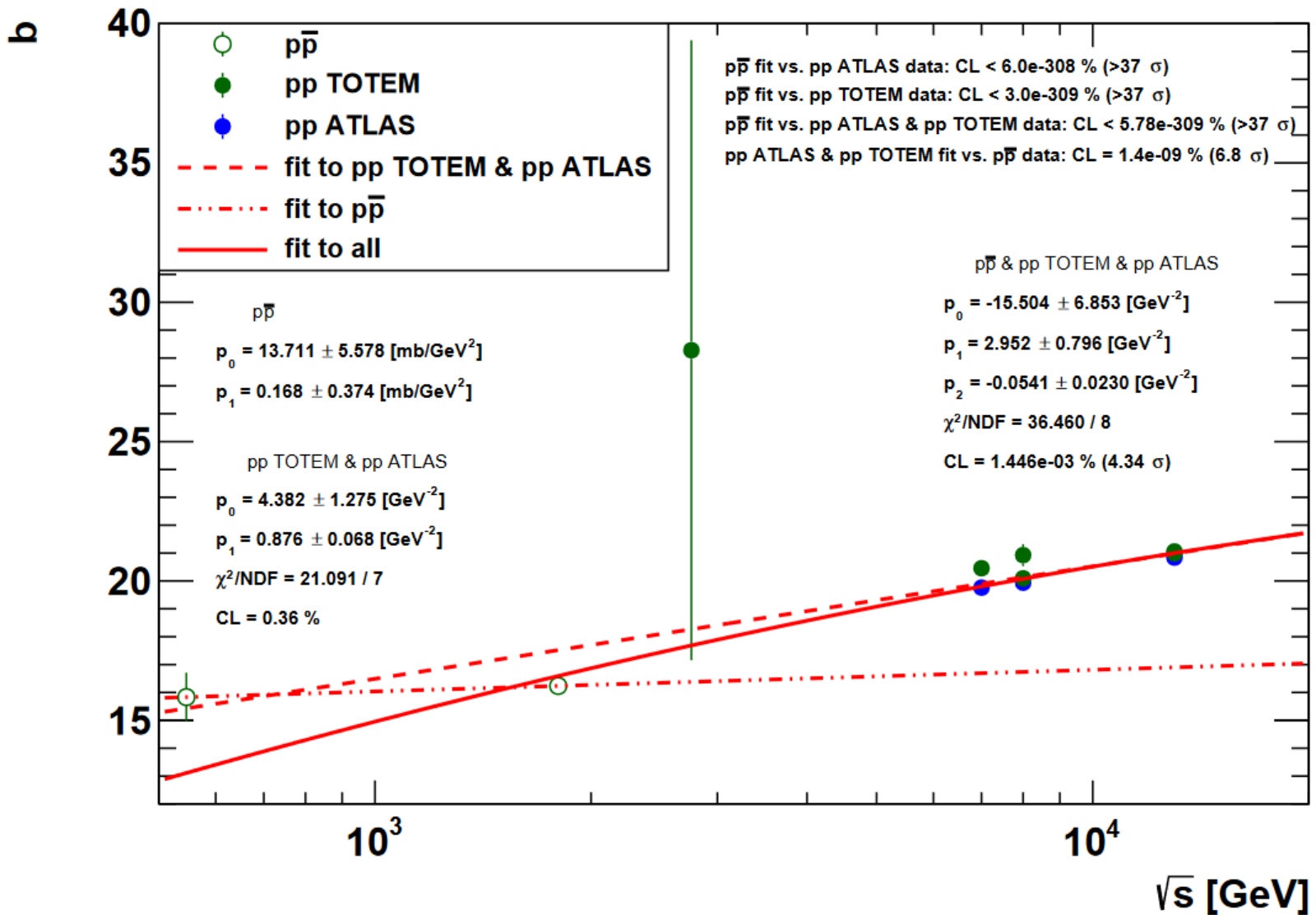
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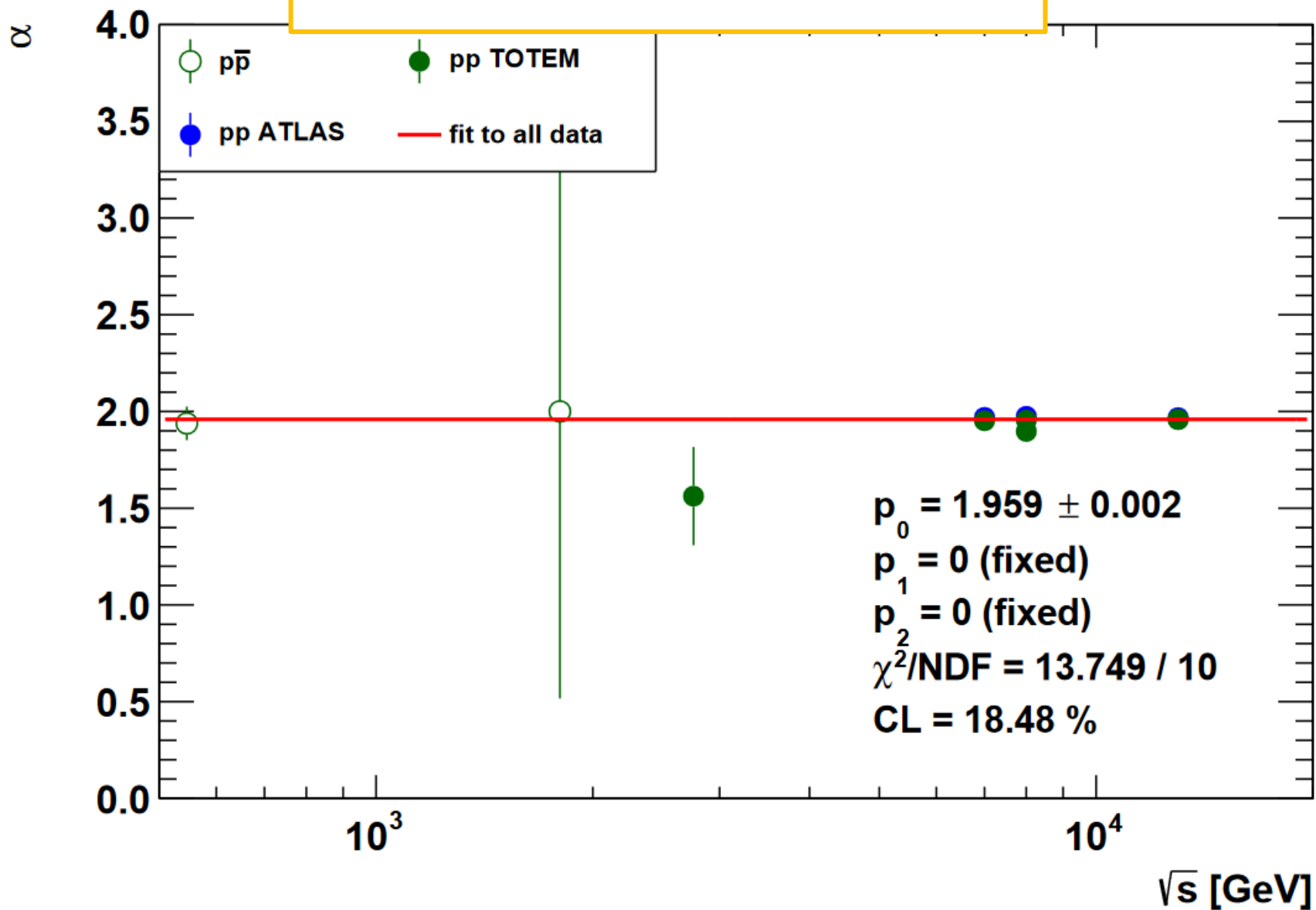
$$\frac{d\sigma}{dt}(s, t) \simeq a(s) \exp \left[-(tb(s))^{\alpha_L/2} \right]$$

From Glauber's theory, $p=(q,d)$
 Good quality fits at 8 TeV and also
 at every low $-t$ dataset for pp, pbarp

$$\frac{d\sigma}{dt}(s, t) \simeq a(s) \exp \left[-(tb(s))^{\alpha_L/2} \right]$$



$$\frac{d\sigma}{dt}(s, t) \simeq a(s) \exp \left[-(tb(s))^{\alpha_L/2} \right]$$

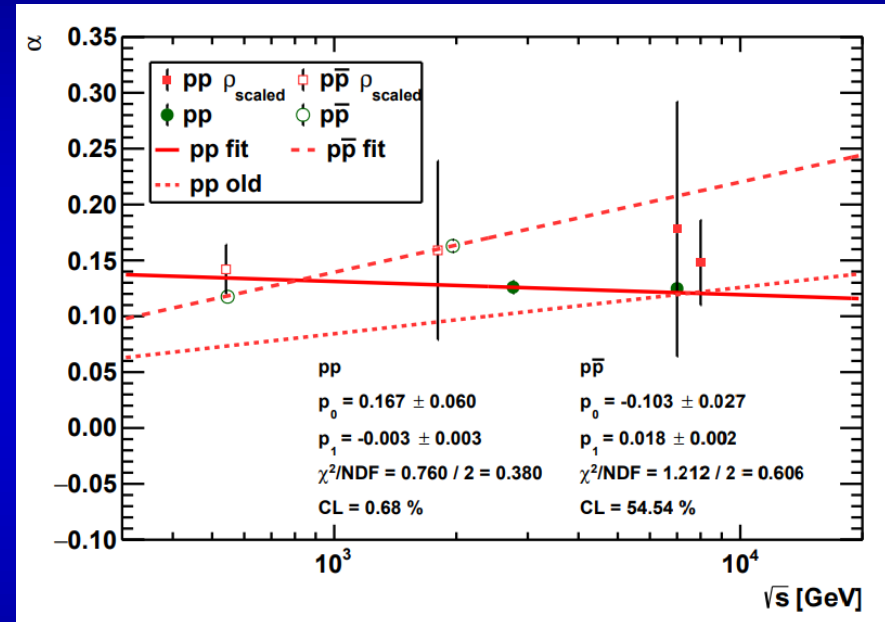
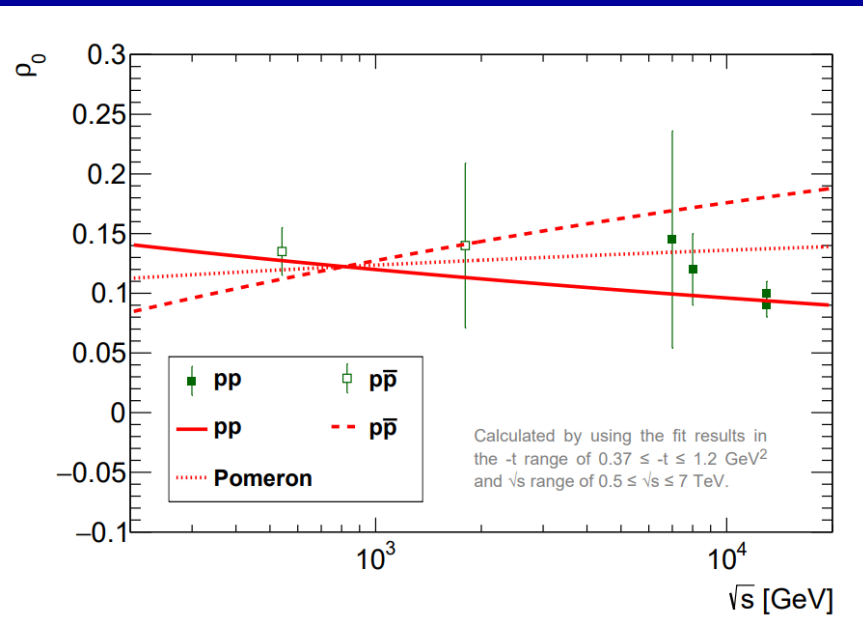


ρ_0 from fits to data

Observation of Odderon effects at LHC energies: a real extended Bialas–Bzdak model study

T. Csorgo (Wigner RCP, Budapest and EKV KRC, Gyongyos), I. Szanyi (Eotvos U. and Wigner RCP, Budapest) (May 28, 2020)

Published in: *Eur.Phys.J.C* 81 (2021) 7, 611 • e-Print: 2005.14319 [hep-ph]



From data fits: R_q, R_d, R_{qd} is the same, but $\alpha \sim \rho$ (opacity) is not the same in pp and pbarb

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$$\rho_0^{pp}(s) \neq \rho_0^{p\bar{p}}(s),$$

Levy + Bialas-Bzdak at small t

Lévy α -Stable Model for the Non-Exponential Low- $|t|$ Proton-Proton Differential Cross-Section

#1

Tamás Csörgő (Karoly Robert U. Coll. and Budapest, RMKI), Sándor Hegyi (Budapest, RMKI), István Szanyi (Karoly Robert U. Coll. and Budapest, RMKI and Eotvos U., Dept. Atomic Phys.) (Aug 3, 2023)

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Easy to fit model, with dramatic consequences

$$\begin{aligned}b^{pp}(s) &= b^{p\bar{p}}(s), \\ \sigma_{tot}^{pp}(s) &= \sigma_{tot}^{p\bar{p}}(s).\end{aligned}$$

**Strong form of Pomeranchuk theorem,
with small signals of odderon exchange in
optical point, ρ and elastic cross-section! Tests are needed...**

$$\begin{aligned}a^{pp}(s) &\neq a^{p\bar{p}}(s), \\ \rho_0^{pp}(s) &\neq \rho_0^{p\bar{p}}(s), \\ \sigma_{el}^{pp}(s) &\neq \sigma_{el}^{p\bar{p}}(s),\end{aligned}$$

Formalism: elastic scattering

$$\frac{d\sigma(s)}{dt} = \frac{1}{4\pi} |T_{el}(s, \Delta)|^2, \quad \Delta = \sqrt{|t|}.$$

$$\sigma_{el}(s) = \int_0^\infty d|t| \frac{d\sigma(s)}{dt}$$

$$A(s) = \lim_{t \rightarrow 0} \frac{d\sigma}{dt}(s, t)$$

$$A(s) = \frac{1}{16\pi} (1 + \rho_0^2(s)) \sigma_{tot}^2(s)$$

$$B(s, t) = \frac{d}{dt} \ln \frac{d\sigma(s)}{dt}$$

$$B(s) \equiv B_0(s) = \lim_{t \rightarrow 0} B(s, t),$$

$$\rho(s, t) \equiv \frac{\text{Re } T_{el}(s, \Delta)}{\text{Im } T_{el}(s, \Delta)}$$

$$\rho(s) \equiv \rho_0(s) = \lim_{t \rightarrow 0} \rho(s, t)$$

$$\sigma_{tot}(s) \equiv 2 \text{Im } T_{el}(\Delta = 0, s)$$

35

Basic problem: $d\sigma/dt$ measures an amplitude, *modulus squared*.
If Odderon exists: signals in elastic scattering at $t = 0$ and at $-t > 0$.

Formalism in b space

$$\frac{d\sigma(s)}{dt} = \frac{1}{4\pi} |T_{el}(s, \Delta)|^2, \quad \Delta = \sqrt{|t|}.$$

$$\begin{aligned} t_{el}(s, b) &= \int \frac{d^2\Delta}{(2\pi)^2} e^{-i\Delta \mathbf{b}} T_{el}(s, \Delta) = \\ &= \frac{1}{2\pi} \int J_0(\Delta b) T_{el}(s, \Delta) \Delta d\Delta, \\ \Delta &\equiv |\mathbf{\Delta}|, \quad b \equiv |\mathbf{b}|. \end{aligned}$$

$$t_{el}(s, b) = i \left[1 - e^{-\Omega(s, b)} \right]$$

$$P(s, b) = 1 - \left| e^{-\Omega(s, b)} \right|^2$$

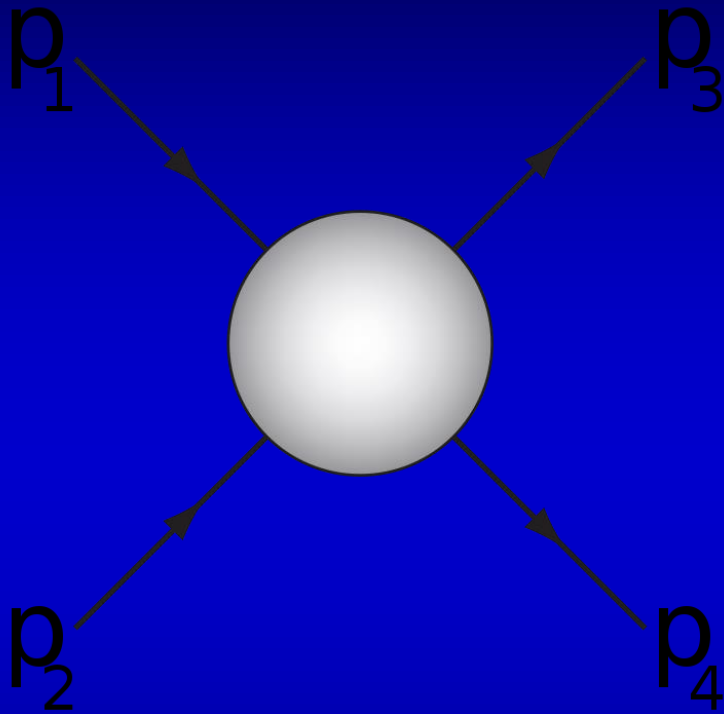
Impact parameter or b space:

elastic scattering interferes with propagation w/o collisions: Genuine quantum physics.

Complex opacity function $\Omega(s, b)$ (eikonal, from unitarity)

$0 \leq P(s, b) \leq 1$: *inelastic* scattering has a probabilistic interpretation

Mandelstam variables



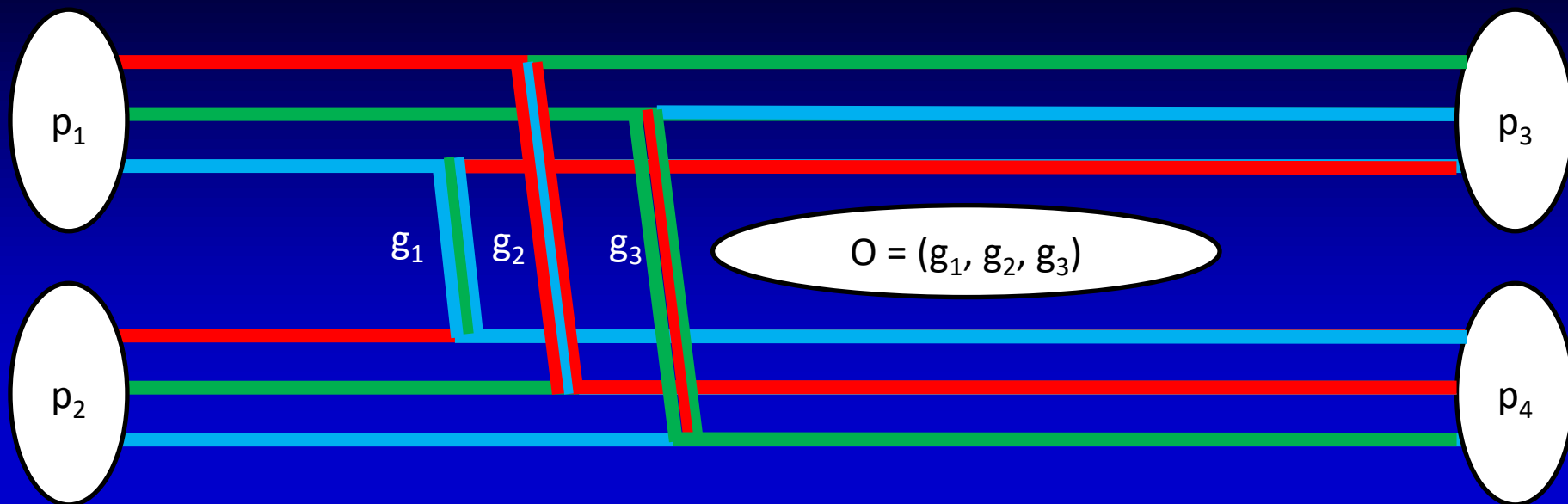
$$s = (p_1 + p_2)^2 = (p_3 + p_4)^2$$
$$t = (p_1 - p_3)^2 = (p_4 - p_2)^2$$
$$u = (p_1 - p_4)^2 = (p_3 - p_2)^2$$

p_1, p_2 : four-momenta
before elastic scattering

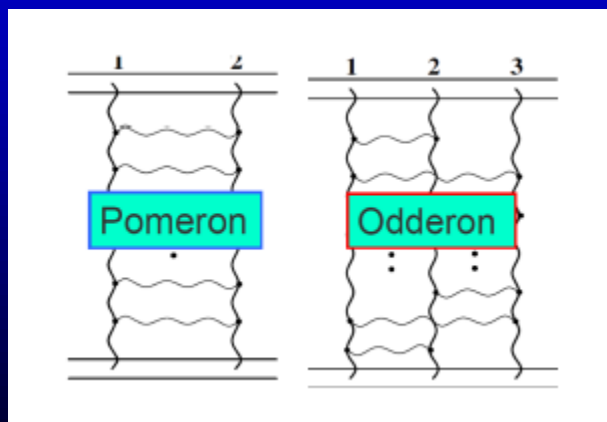
p_3, p_4 : four-momenta
after elastic scattering

s : square of the cms energy
 t : square of four-momentum
transfer

Odderon and QCD in Laymen's Terms



$$g_1 = B\bar{R} + R\bar{B} \quad g_2 = R\bar{G} + G\bar{R} \quad g_3 = G\bar{B} + B\bar{G}$$



Pomeron (2+4+...) gluon in pp:
 (RGB)+(RGB) → (GRB)+(GRB)

Odderon (3+5+... gluon) in pp:
 (RGB)+(RGB) → (GBR)+(BRG)
 Well established in QCD

Odderon and elastic collisions

