

GMVFN scheme implementations with Subtraction and Residual PDFs for processes at hadron colliders

Marco Guzzi

with

Pavel Nadolsky, Laura Reina, Doreen Wackerroth, Keping Xie

Based on e-Print: [2410.03876](https://arxiv.org/abs/2410.03876) [hep-ph] To appear on Phys. Rev. D



Motivations 1

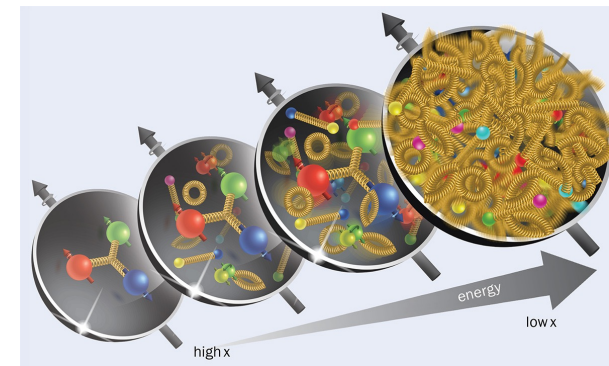
➤ We developed the theory framework to extend ACOT-like GMVFN schemes to PP collisions.

This effort is connected to many areas of investigations in global CTEQ analyses:

- HQ effects
- NNLO- \rightarrow N³LO transition
- DGLAP evolution @N³LO
- Intrinsic HQ in the proton
- Constrain HQ PDFs

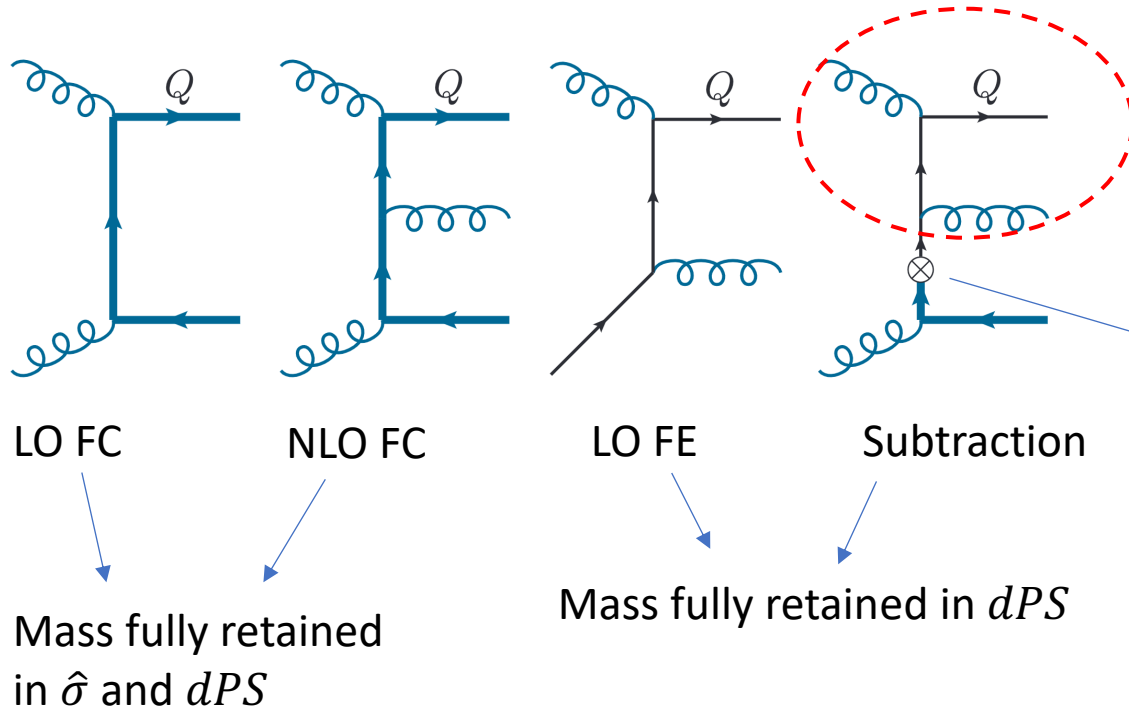
Motivations 2

- Modern Parton Distribution Function (PDF) analyses: extend on wide range of collision energies. Sensitive to mass effects, e.g., phase space suppression, large radiative corrections to collinear $Q\bar{Q}$ production. **Magnitude comparable to NNLO and N³LO corrections.**
- Natural to evaluate all fitted cross sections in a factorization (GMVFN) scheme, which assumes that the number of (nearly) massless quark flavors varies with energy, and at the same time includes dependence on heavy-quark masses in relevant kinematical regions.



Main idea behind ACOT/S-ACOT/S-ACOT-MPS

Inclusive production of a HQ as an example



The subtraction term avoids double counting and cancels enhanced collinear contributions from FC when $\hat{s} \gg m_Q^2$ or $p_T \gg m_Q$

Collinear splitting $gg \rightarrow Q\bar{Q}$

$$\sigma = \text{FC} + \text{FE} - \text{SB.} \quad \text{Subtraction well defined also in the } p_T \rightarrow 0 \text{ limit}$$

FE and Subtraction \rightarrow facilitated by introducing Residual PDF: $\delta f_Q(x, \mu^2) = f_Q(x, \mu^2) - \underbrace{\frac{\alpha_s}{2\pi} \log\left(\frac{\mu^2}{m_Q^2}\right) f_Q(x, \mu^2) \otimes P_{Q \leftarrow g}(x)}_{\text{Subtraction PDF}}$

allows us to get (FE-Subtraction) in one step

More details in: K. Xie, "Massive elementary particles in the standard model and its supersymmetric triplet higgs extension."

https://scholar.smu.edu/hum_sci_physics_etds/7, 2019. PhD Thesis

Subtraction PDF

Subtraction and Residual PDFs

Subtraction and Residual PDFs consist of convolutions between PDFs and universal operator matrix elements (OMEs). They are process independent.

(See J. Blümlein's talk for recent progress on OMEs computation)

Subtraction and Residual PDFs are provided in the form of LHAPDF6 grids for phenomenology applications: <https://sacotmps.hepforge.org/>

The new CTEQ fitting code will be equipped by a module specifically designed for this task

GMVFN Theory framework

The differential cross section for $p_A p_B \rightarrow F + X$ where F contains at least one HQ, can be written

$$\frac{d\sigma(A + B \rightarrow F + X)}{d\mathcal{X}} = \sum_{i,j} \int_{x_A}^1 d\xi_A \int_{x_B}^1 d\xi_B f_{i/A}(\xi_A, \mu) f_{j/B}(\xi_B, \mu) \frac{d\hat{\sigma}(i + j \rightarrow F + X)}{d\mathcal{X}}$$

After UV renormalization on $d\sigma/d\mathcal{X}$, we identify its infrared-safe part $d\hat{\sigma}/d\mathcal{X}$ by factoring out parton-level PDFs

$$G_{ij} \equiv \frac{d\sigma(i + j \rightarrow F + X)}{d\mathcal{X}} \text{ after UV renormalization,}$$

$$H_{km} \equiv \frac{d\hat{\sigma}(k + m \rightarrow F + X)}{d\mathcal{X}},$$

$$G_{ij}(x_A, x_B) = \sum_{k,m} \int_{x_A}^1 d\xi_A \int_{x_B}^1 d\xi_B f_{k/i}(\xi_A) f_{m/j}(\xi_B) H_{km}(\hat{x}_A, \hat{x}_B)$$

$$\equiv [f_{k/i} \triangleright H_{km} \triangleleft f_{m/j}](x_A, x_B).$$

$$\hat{x}_i \equiv x_i/\xi_i$$

Convolution product with two variables

$$[f \triangleright H](x_A, x_B) \equiv \int_{x_A}^1 \frac{d\xi_A}{\xi_A} f(\xi_A) H(\hat{x}_A, x_B),$$

$$[H \triangleleft f](x_A, x_B) \equiv \int_{x_B}^1 \frac{d\xi_B}{\xi_B} H(x_A, \hat{x}_B) f(\xi_B).$$

Convolution product with one variable

$$\int_x^1 \frac{d\xi}{\xi} f(\xi) g\left(\frac{x}{\xi}\right) = [f \triangleright g](x) = [g \triangleleft f](x)$$

GMVFN Theory framework

The perturbative expansion of terms leads to

$$\begin{aligned}
 G_{i,b}(x_A, x_B) &= G_{i,b}^{(0)}(x_A, x_B) + a_s G_{i,b}^{(1)}(x_A, x_B) + a_s^2 G_{i,b}^{(2)}(x_A, x_B) + \dots, \\
 H_{i,a}(\hat{x}_A, \hat{x}_B) &= H_{i,a}^{(0)}(\hat{x}_A, \hat{x}_B) + a_s H_{i,a}^{(1)}(\hat{x}_A, \hat{x}_B) + a_s^2 H_{i,a}^{(2)}(\hat{x}_A, \hat{x}_B) + \dots, \\
 f_{a/b}(\xi) &= \delta_{ab} \delta(1 - \xi) + a_s A_{ab}^{(1)}(\xi) + a_s^2 A_{ab}^{(2)}(\xi) + a_s^3 A_{ab}^{(3)}(\xi) + \dots,
 \end{aligned}$$

$$\hat{x} = x/\xi.$$

$$A_{ab}^{(k)} \quad (k = 0, 1, 2, \dots) \quad \text{OMEs}$$

$$A_{hg}^{(1)}(\xi) = 2P_{hg}^{(1)}(\xi) \ln(\mu^2/m_h^2)^* \text{ for } g \rightarrow Q\bar{Q}$$

Substituting these in the previous formula for G and solving for $H^{(k)}$ order by order in a_s one obtains

$$H_{ij}^{(0)}(x_A, x_B) = G_{ij}^{(0)}(x_A, x_B),$$

$$H_{ij}^{(1)}(x_A, x_B) = G_{ij}^{(1)}(x_A, x_B) - [A_{ki}^{(1)} \triangleright H_{kj}^{(0)}](x_A, x_B) - [H_{im}^{(0)} \triangleleft A_{mj}^{(1)}](x_A, x_B)$$

$$\begin{aligned}
 H_{ij}^{(2)}(x_A, x_B) &= G_{ij}^{(2)}(x_A, x_B) - [A_{ki}^{(1)} \triangleright H_{kj}^{(1)}](x_A, x_B) - [H_{im}^{(1)} \triangleleft A_{mj}^{(1)}](x_A, x_B) \\
 &\quad - [A_{ki}^{(2)} \triangleright H_{kj}^{(0)}](x_A, x_B) - [H_{im}^{(0)} \triangleleft A_{mj}^{(2)}](x_A, x_B) \\
 &\quad - [A_{ki}^{(1)} \triangleright H_{km}^{(0)} \triangleleft A_{mj}^{(1)}](x_A, x_B),
 \end{aligned}$$

$$\begin{aligned}
 H_{ij}^{(3)}(x_A, x_B) &= G_{ij}^{(3)}(x_A, x_B) - [A_{ki}^{(1)} \triangleright H_{kj}^{(2)}](x_A, x_B) - [H_{im}^{(2)} \triangleleft A_{mj}^{(1)}](x_A, x_B) \\
 &\quad - [A_{ki}^{(2)} \triangleright H_{kj}^{(1)}](x_A, x_B) - [H_{im}^{(1)} \triangleleft A_{mj}^{(2)}](x_A, x_B) \\
 &\quad - [A_{ki}^{(3)} \triangleright H_{kj}^{(0)}](x_A, x_B) - [H_{im}^{(0)} \triangleleft A_{mj}^{(3)}](x_A, x_B) \\
 &\quad - [A_{ki}^{(1)} \triangleright H_{km}^{(1)} \triangleleft A_{mj}^{(1)}](x_A, x_B) \\
 &\quad - [A_{ki}^{(2)} \triangleright H_{km}^{(0)} \triangleleft A_{mj}^{(1)}](x_A, x_B) - [A_{ki}^{(1)} \triangleright H_{km}^{(0)} \triangleleft A_{mj}^{(2)}](x_A, x_B).
 \end{aligned}$$

....

Two forms for the OMEs

$$\left\{ \begin{aligned}
 A_{ij}^{(n)}(\xi, \mu^2) &= \sum_{l=1}^n \left(\frac{1}{\epsilon}\right)^l P_{ij}^{(n,l)}(\xi) + \sum_{l=0}^n \ln^l \left(\frac{\mu^2}{\mu_{\text{IR}}^2}\right) P_{ij}'^{(n,l)}(\xi) \\
 A_{Qj}^{(n)}\left(\xi, \frac{\mu^2}{m_Q^2}\right) &= \sum_{l=0}^n \ln^l \left(\frac{\mu^2}{m_Q^2}\right) a_{Qj}^{(n,l)}(\xi)
 \end{aligned} \right.$$

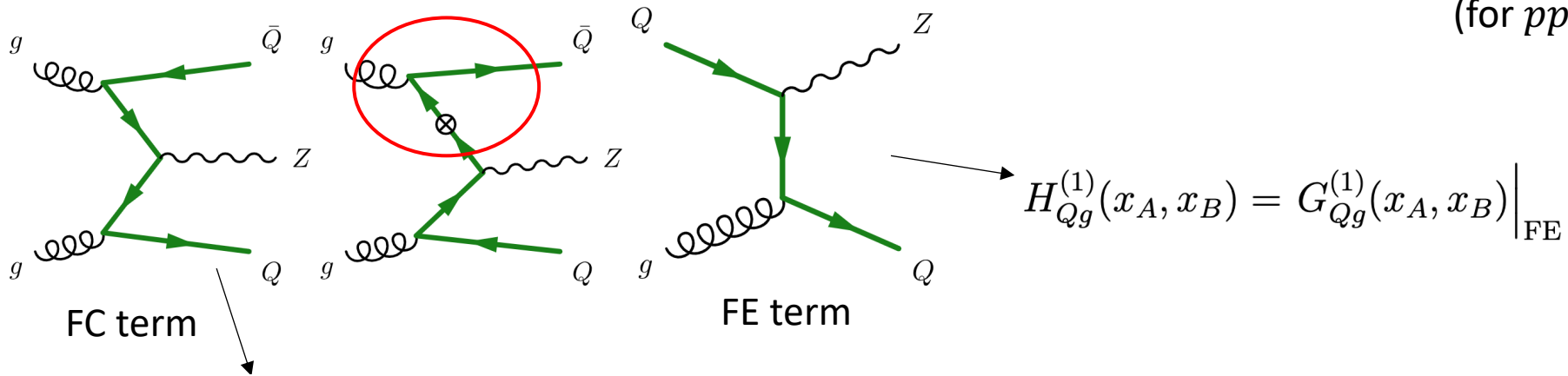
*Our convention for the splitting functions

$$P_{ij}(x, a_s) = a_s P_{ij}^{(1)}(x) + a_s^2 P_{ij}^{(2)}(x) + a_s^3 P_{ij}^{(3)}(x) + \dots$$

Let us apply this GM theory framework to
a physical process of interest at the LHC: $pp \rightarrow Z + Q + X$
with $Q = b$ -quark

Cancellation pattern at the lowest order ($pp \rightarrow Z+Q+X$)

(for $pp \rightarrow Z + Q + X$ this is $O(\alpha_s^2)$)



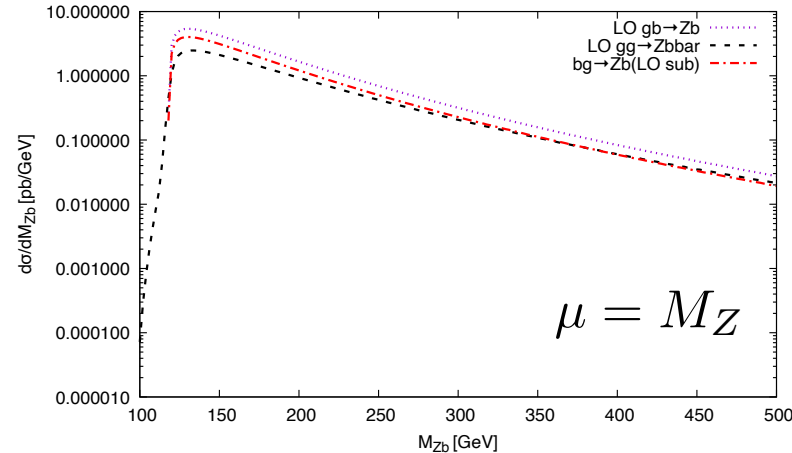
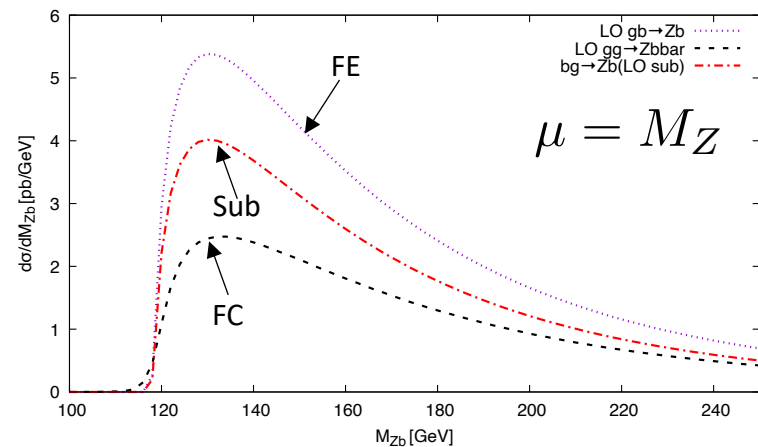
$$H_{gg}^{(2)}(x_A, x_B) = G_{gg}^{(2)}(x_A, x_B) \Big|_{\text{FC}} - \left[A_{Qg}^{(1)} \triangleright H_{Qg}^{(1)} \right] (x_A, x_B) - \left[H_{gQ}^{(1)} \triangleleft A_{Qg}^{(1)} \right] (x_A, x_B)$$

$$a_s H^{(1)} + a_s^2 H^{(2)} = a_s H_{Qg}^{(1)}(x_A, x_B) + a_s^2 H_{gg}^{(2)}(x_A, x_B) + a_s^2 H_{q\bar{q}}^{(2)}(x_A, x_B)$$

$$d\sigma = \sum_{i,j} f_{i/A} \triangleright \left[a_s H^{(1)} + a_s^2 H^{(2)} \right]_{ij} \triangleleft f_{j/B}$$

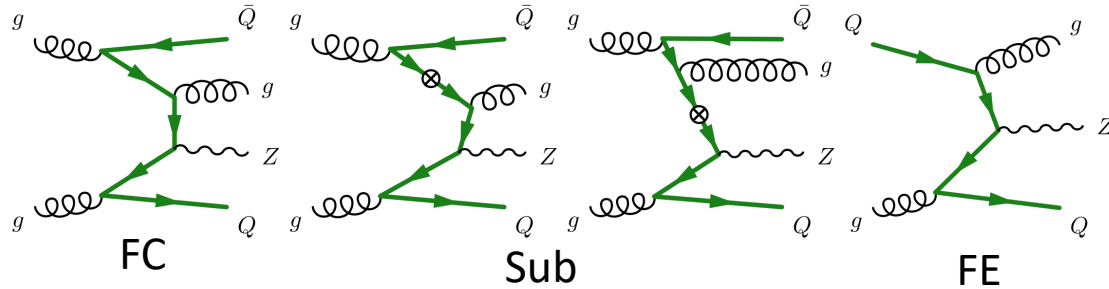
Subtraction

$$-d\sigma_{\text{sub}} = -a_s^2 \left[g \triangleright A_{Qg}^{(1)} \triangleright H_{Qg}^{(1)} \right] \triangleleft g + (\text{exch.})$$

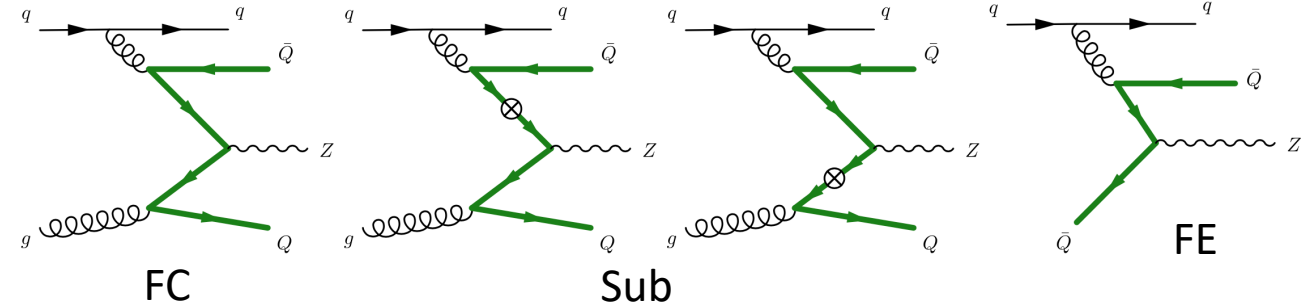


Cancellation pattern at NLO ($pp \rightarrow Z+Q+X$)

(for $pp \rightarrow Z + b + X$ this is $O(\alpha_s^3)$)



gg-channel



qg-channel

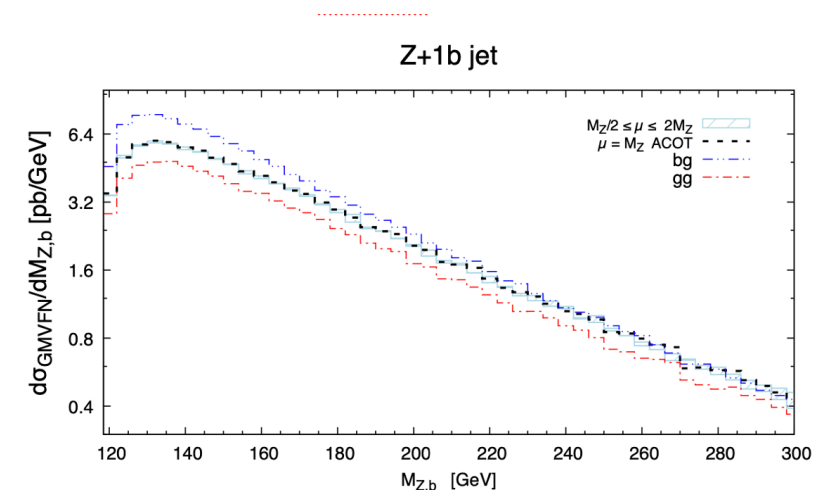
$$H_{Qi}^{(2)}(x_A, x_B) = \widehat{G}_{Qi}^{(2)}(x_A, x_B) \Big|_{\text{FE}} \quad \text{for } i = g, q, \bar{q};$$

$$H_{ij}^{(3)}(x_A, x_B) = \widehat{G}_{ij}^{(3)}(x_A, x_B) \Big|_{\text{FC}} - [A_{Qi}^{(1)} \triangleright H_{Qj}^{(2)}](x_A, x_B) - [H_{iQ}^{(2)} \triangleleft A_{Qj}^{(1)}](x_A, x_B) \\ - [A_{Qi}^{(2)} \triangleright H_{Qj}^{(1)}](x_A, x_B) - [H_{iQ}^{(1)} \triangleleft A_{Qj}^{(2)}](x_A, x_B) \quad \text{for } i, j = g, q, \bar{q};$$

$$H_{q\bar{q}}^{(3)}(x_A, x_B) = \widehat{G}_{q\bar{q}}^{(3)}(x_A, x_B) \Big|_{\text{FC}}.$$

$$a_s H^{(1)} + a_s^2 H^{(2)} + a_s^3 H^{(3)} = a_s H_{Qg}^{(1)}(x_A, x_B) + a_s^2 H_{gg}^{(2)}(x_A, x_B) + a_s^2 H_{q\bar{q}}^{(2)}(x_A, x_B) \\ + a_s^2 H_{Qg}^{(2)}(x_A, x_B) + a_s^2 H_{Qq}^{(2)}(x_A, x_B) \\ + a_s^3 H_{gg}^{(3)}(x_A, x_B) + a_s^3 H_{qg}^{(3)}(x_A, x_B) + a_s^3 H_{q\bar{q}}^{(3)}(x_A, x_B)$$

Virtual diagrams are not shown here, but are included in the calculation.



Subtraction PDFs

Once the $H_{ij}^{(k)}$ functions are determined, the hadronic cross section can be written as

$$d\sigma = \sum_{i,j} f_{i/A} \triangleright [a_s H^{(1)} + a_s^2 H^{(2)} + a_s^3 H^{(3)} + \dots]_{ij} \triangleleft f_{j/B}$$

Then, the various subtraction (“sub”) terms can be collected as follows:

$$-d\sigma_{\text{sub}} = -a_s^2 \left[g \triangleright A_{Qg}^{(1)} \triangleright H_{Qg}^{(1)} \right] \triangleleft g - a_s^3 \left[\sum_{i,j=g,q,\bar{q}} f_i \triangleright A_{Qi}^{(2)} \triangleright H_{Qj}^{(1)} \right] \triangleleft f_j$$

$$- a_s^3 \left[\sum_{i,j=g,q,\bar{q}} f_i \triangleright A_{Qi}^{(1)} \triangleright H_{Qj}^{(2)} \right] \triangleleft f_j + (\text{exch.}),$$

At this point we can define subtraction HQ PDFs $\tilde{f}_Q^{(1)} = a_s [A_{Qg}^{(1)} \triangleleft g]$, $\tilde{f}_Q^{(2)} = a_s^2 \sum_{i=g,q,\bar{q}} [A_{Qi}^{(2)} \triangleleft f_i]$

$$\tilde{f}_Q^{(\text{NLO})}(x, \mu) \equiv \tilde{f}_Q^{(1)} + \tilde{f}_Q^{(2)}$$

$$-d\sigma_{\text{sub}} = -a_s \tilde{f}_Q^{(\text{NLO})} \triangleright H_{Qg}^{(1)} \triangleleft g - a_s^2 \sum_{i=g,q,\bar{q}} \tilde{f}_Q^{(1)} \triangleright H_{Qi}^{(2)} \triangleleft f_i$$

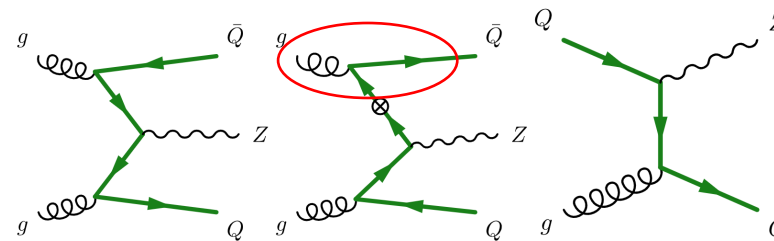
Residual PDFs

$$\delta f_Q^{(1)} = f_Q - \tilde{f}_Q^{(1)}, \quad \delta f_Q^{(\text{NLO})} = f_Q - \tilde{f}_Q^{(\text{NLO})}$$

$$d\sigma_{\text{FE}} - d\sigma_{\text{sub}} = a_s (f_Q - \tilde{f}_Q^{(\text{NLO})}) \triangleright H_{Qg}^{(1)} \triangleleft g$$

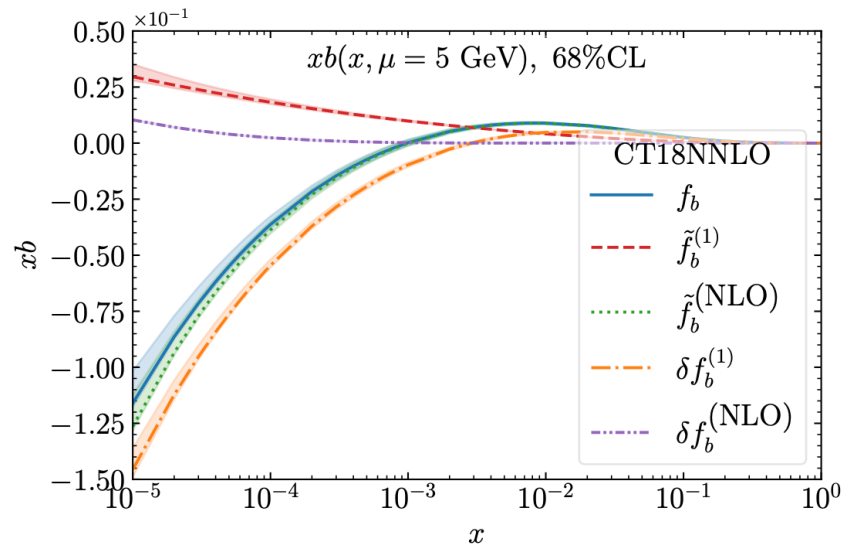
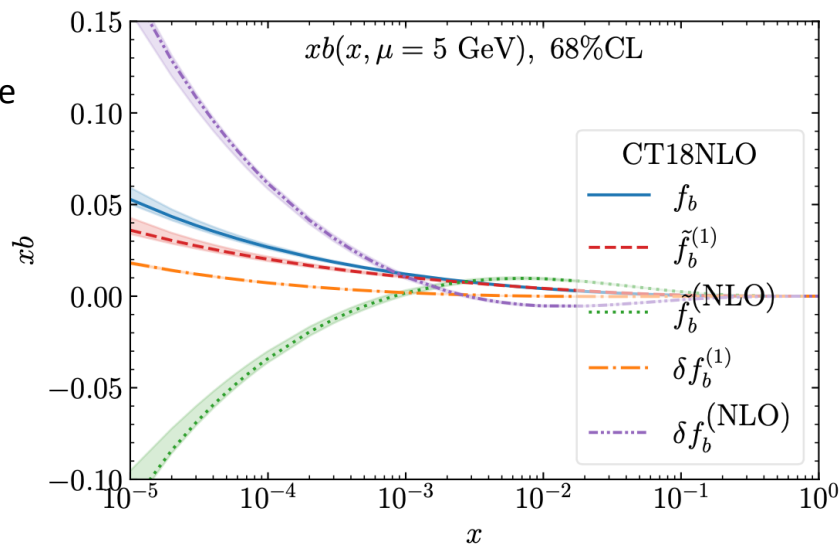
$$+ a_s^2 (f_Q - \tilde{f}_Q^{(1)}) \triangleright \left[H_{Qg}^{(2)} \triangleleft g + \sum_{i=q,\bar{q}} H_{Qq}^{(2)} \triangleleft f_i \right] + (\text{exch.})$$

$$= a_s \delta f_Q^{(\text{NLO})} \triangleright H_{Qg}^{(1)} \triangleleft g + a_s^2 \delta f_Q^{(1)} \triangleright \left[H_{Qg}^{(2)} \triangleleft g + \sum_{i=q,\bar{q}} H_{Qq}^{(2)} \triangleleft f_i \right]$$



FE and SUB share the same matrix elements and can be combined in one piece in terms of residual PDFs!

HQ, Subtraction and Residual PDFs near the b-quark threshold



GMVFN scheme hadronic cross section

$$\begin{aligned}
 d\sigma_{\text{FC}}^{\text{NLO}} &= f_g \triangleright \left[a_s^2 d\hat{\sigma}_{gg \rightarrow ZQ\bar{Q}}^{(2)} + a_s^3 d\hat{\sigma}_{gg \rightarrow ZQ\bar{Q}(g)}^{(3)} \right] \triangleleft f_g \\
 &+ \sum_{i=q,\bar{q}} f_i \triangleright \left[a_s^2 d\hat{\sigma}_{q\bar{q} \rightarrow ZQ\bar{Q}}^{(2)} + a_s^3 d\hat{\sigma}_{q\bar{q} \rightarrow ZQ\bar{Q}(g)}^{(3)} \right] \triangleleft f_i \\
 &+ a_s^3 \sum_{i=q,\bar{q}} \left[f_g \triangleright d\hat{\sigma}_{gq \rightarrow ZQ\bar{Q}(q)}^{(3)} \triangleleft f_i + f_i \triangleright d\hat{\sigma}_{qg \rightarrow ZQ\bar{Q}(q)}^{(3)} \triangleleft f_g \right]
 \end{aligned}$$

$$\begin{aligned}
 d\sigma_{\text{FE}}^{\text{NLO}} &= f_g \triangleright \left[a_s d\hat{\sigma}_{gQ \rightarrow ZQ}^{(1)} + a_s^2 d\hat{\sigma}_{gQ \rightarrow ZQ(g)}^{(2)} \right] \triangleleft f_Q \\
 &+ a_s^2 \sum_{i=q,\bar{q}} f_i \triangleright d\hat{\sigma}_{qQ \rightarrow ZQ(q)}^{(2)} \triangleleft f_Q + (\text{exch.});
 \end{aligned}$$

$$\begin{aligned}
 d\sigma_{\text{sub}}^{\text{NLO}} &= a_s f_g \triangleright d\hat{\sigma}_{gQ \rightarrow ZQ}^{(1)} \triangleleft \tilde{f}_Q^{(\text{NLO})} + a_s^2 f_g \triangleright d\hat{\sigma}_{gQ \rightarrow ZQ(g)}^{(2)} \triangleleft \tilde{f}_Q^{(1)} \\
 &+ a_s^2 \sum_{i=q,\bar{q}} f_i \triangleright d\hat{\sigma}_{qQ \rightarrow ZQ(q)}^{(2)} \triangleleft \tilde{f}_Q^{(1)} + (\text{exch.});
 \end{aligned}$$

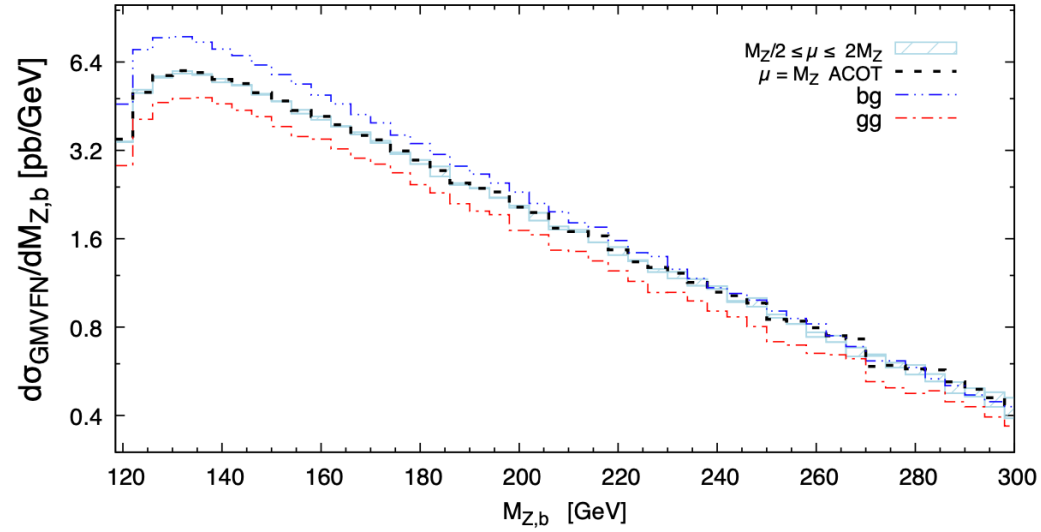
Equivalently, with the $d\sigma_{\text{FE}} - d\sigma_{\text{sub}}$ reorganized in terms of HQ PDF residuals we obtain a very simple form

$$\begin{aligned}
 d\sigma_{\text{GMVFN}}^{\text{NLO}} &= d\sigma_{\text{FC}}^{\text{NLO}} + a_s f_g \triangleright \left[d\hat{\sigma}_{gQ \rightarrow ZQ}^{(1)} \right] \triangleleft \delta f_Q^{(\text{NLO})} \\
 &+ a_s^2 f_g \triangleright \left[d\hat{\sigma}_{gQ \rightarrow ZQ(g)}^{(2)} \right] \triangleleft \delta f_Q^{(1)} + a_s^2 \sum_{i=q,\bar{q}} f_i \triangleright \left[d\hat{\sigma}_{qQ \rightarrow ZQ(q)}^{(2)} \right] \triangleleft \delta f_Q^{(1)} + (\text{exch.})
 \end{aligned}$$

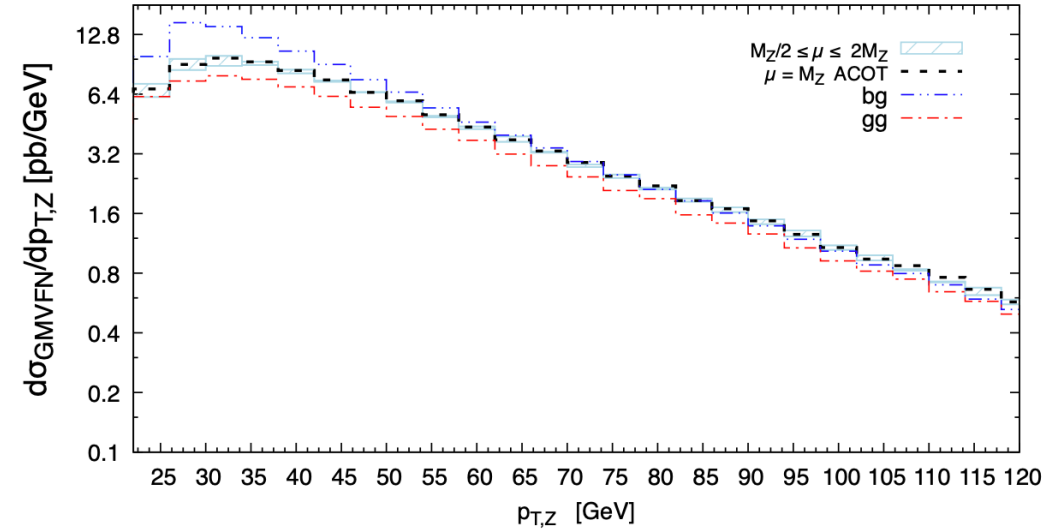
Lowest mandatory order" (LMO) representation at NLO in that it retains only the unambiguous terms up to order a_s^3 required by order-by-order factorization and scale invariance. Any ACOT-like scheme must contain such terms.

Results: Z+b differential distributions (gg channel)

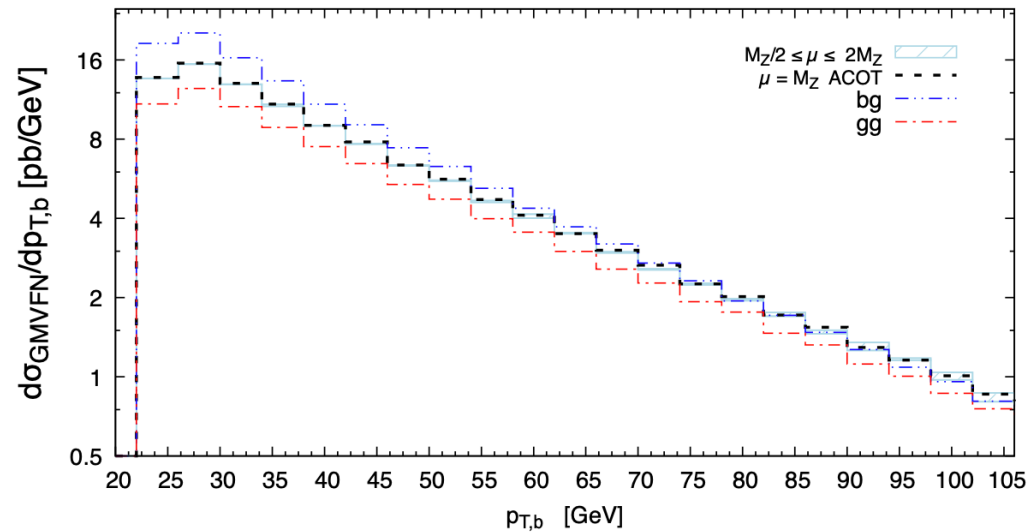
Z+1b jet



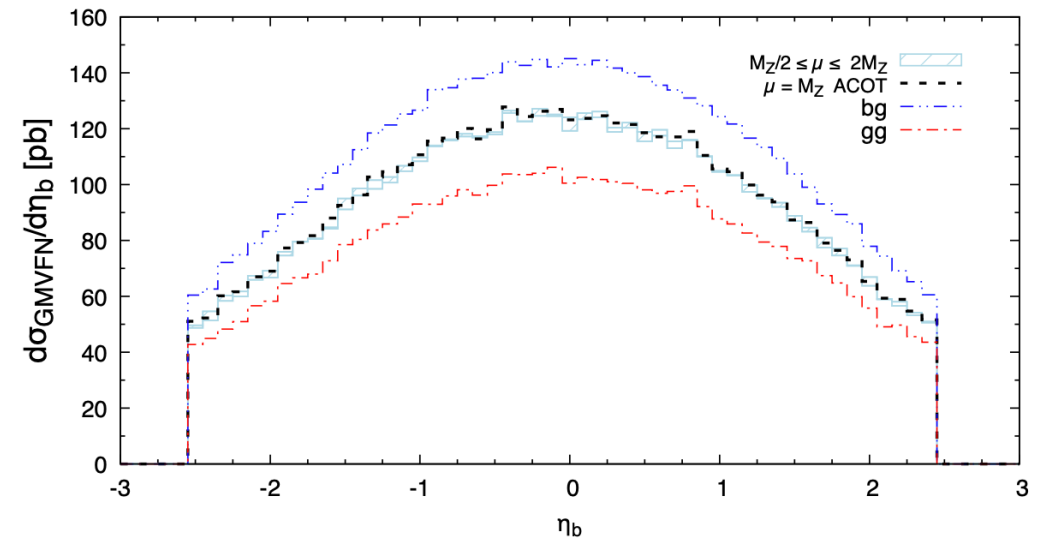
Z+1b jet



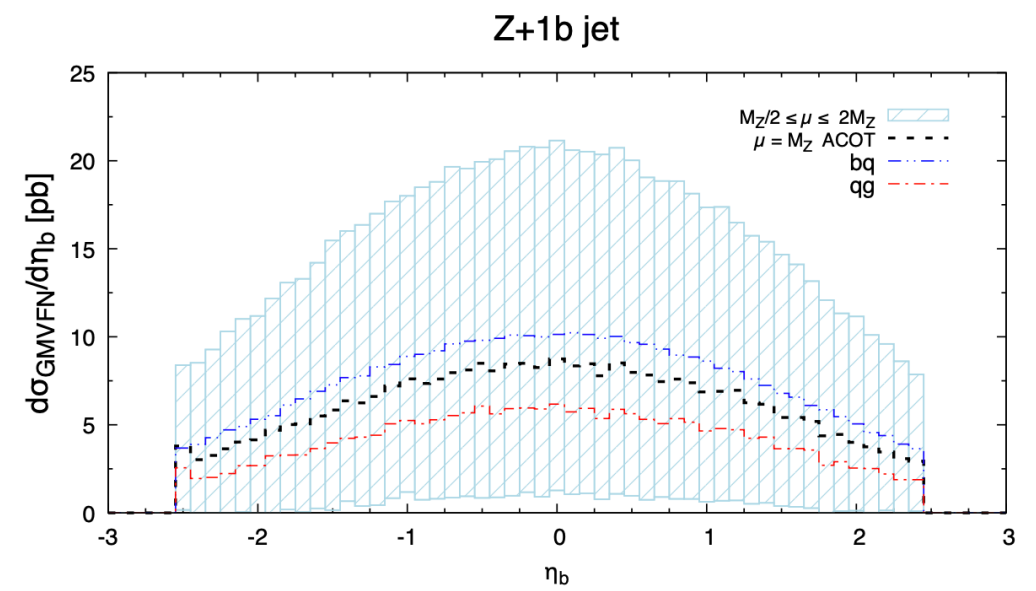
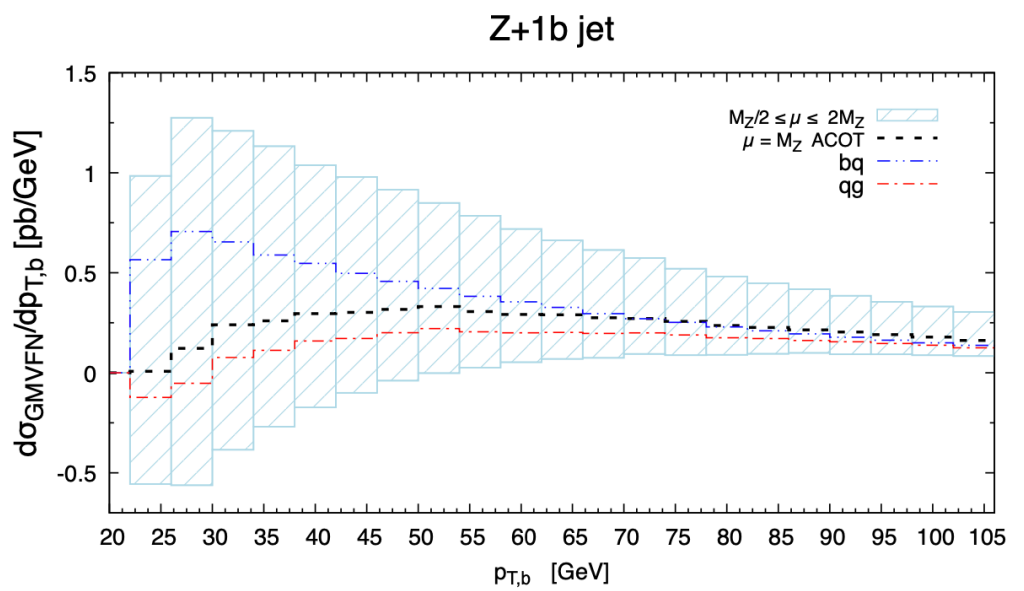
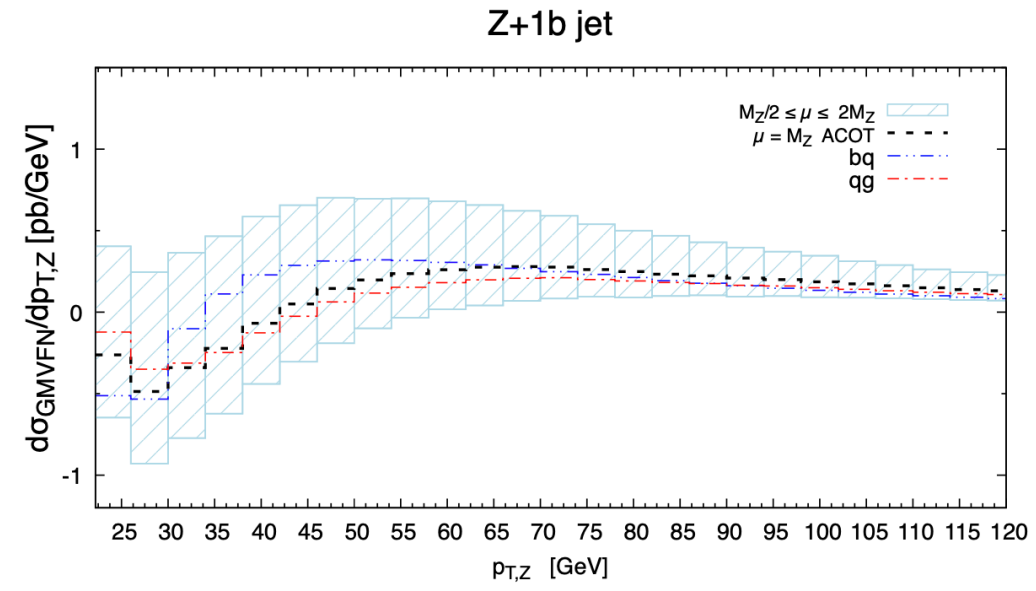
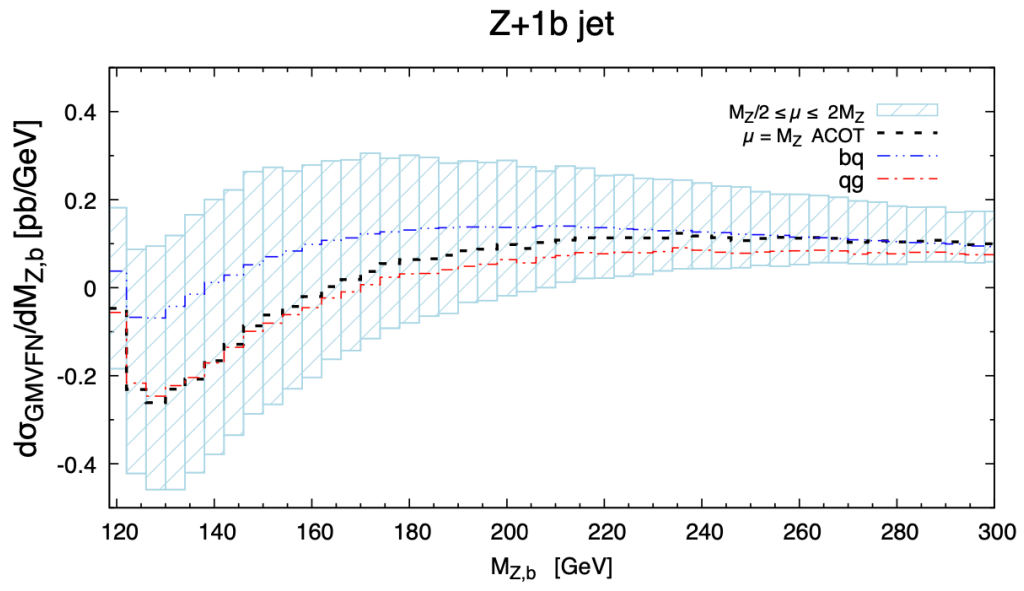
Z+1b jet



Z+1b jet

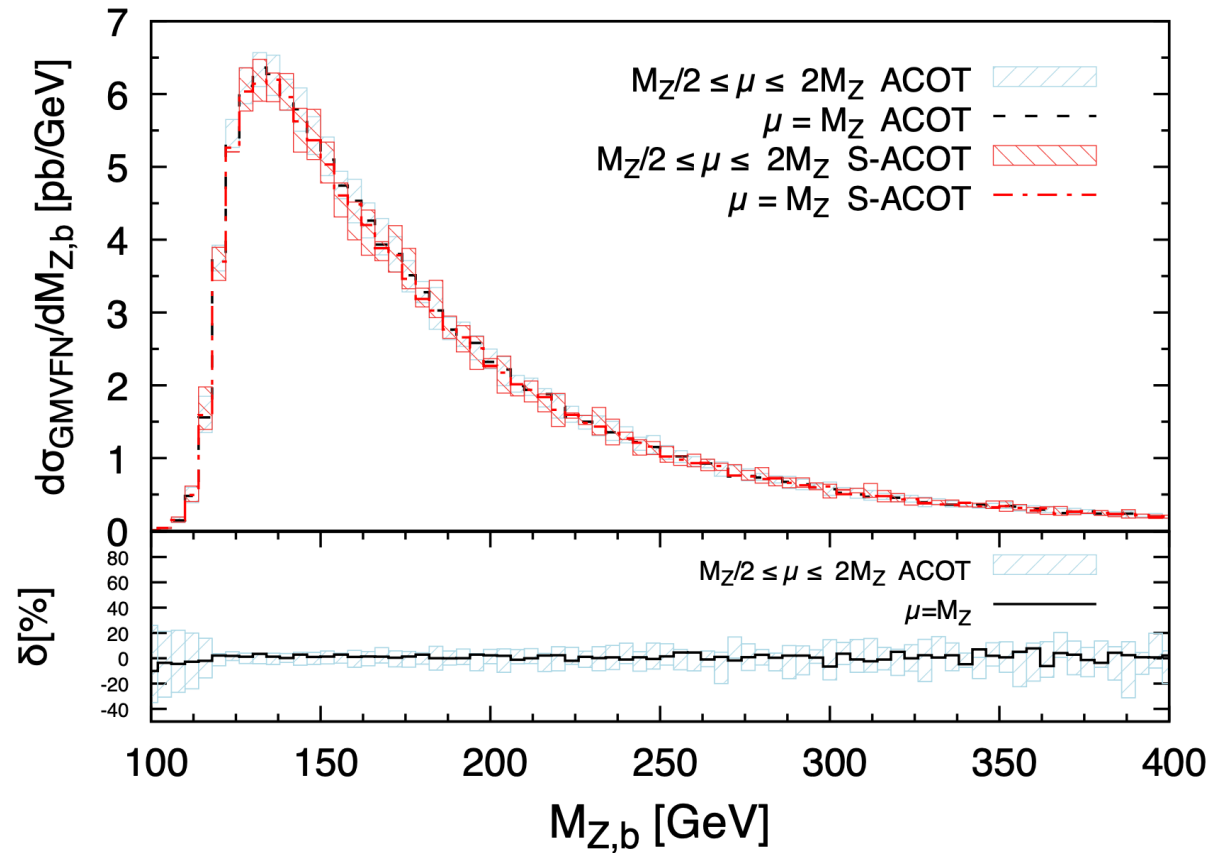


Results: Z+b differential distributions (qg channel)

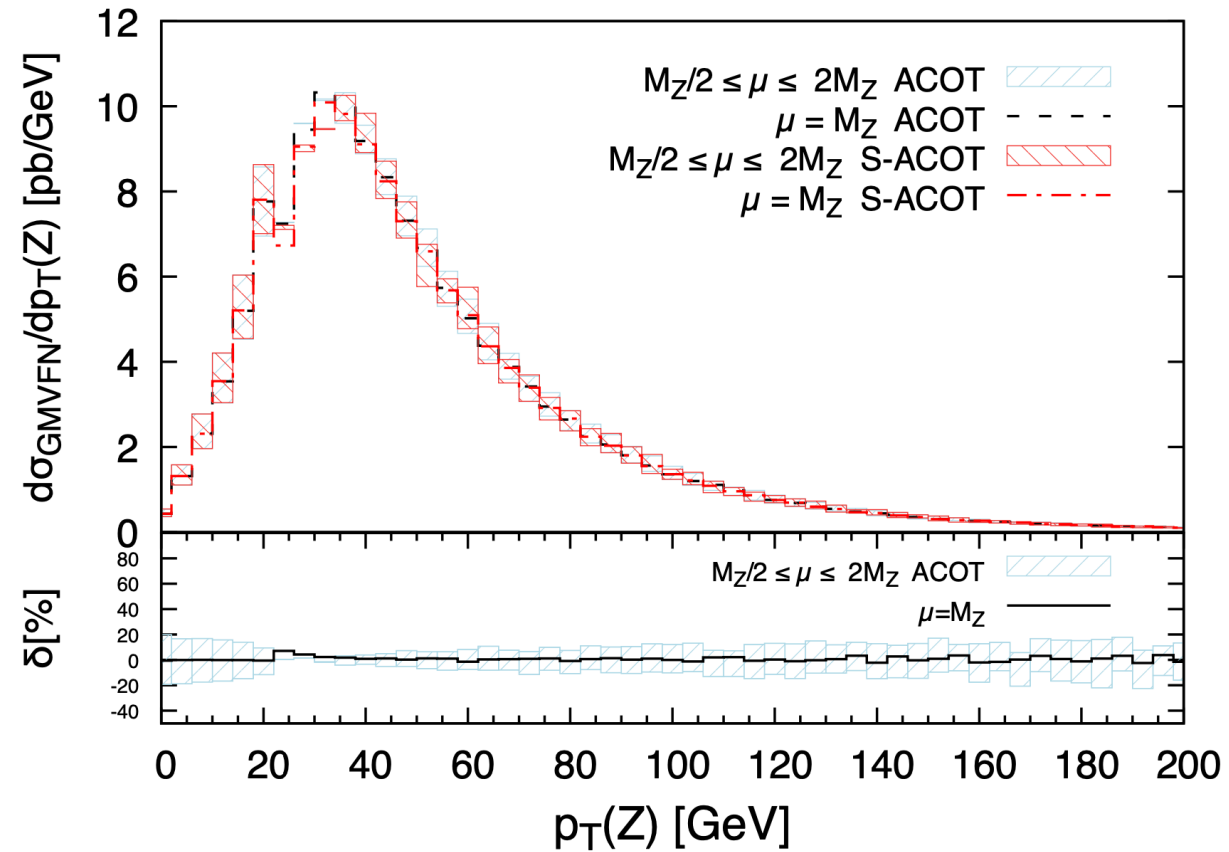


Z+b: ACOT vs S-ACOT

Z+1b jet




Z+1b jet



Further simplifications in ACOT-type schemes

$$\begin{aligned}
 d\sigma_{\text{GMVFN}}^{\text{NLO}} &= d\sigma_{\text{FC}}^{\text{NLO}} + a_s f_g \triangleright \left[d\hat{\sigma}_{gQ \rightarrow ZQ}^{(1)} \right] \triangleleft \delta f_Q^{(\text{NLO})} \\
 &+ a_s^2 f_g \triangleright \left[d\hat{\sigma}_{gQ \rightarrow ZQ(g)}^{(2)} \right] \triangleleft \delta f_Q^{(1)} + a_s^2 \sum_{i=q, \bar{q}} f_i \triangleright \left[d\hat{\sigma}_{qQ \rightarrow ZQ(q)}^{(2)} \right] \triangleleft \delta f_Q^{(1)} + (\text{exch.})
 \end{aligned}$$

$\delta f_Q^{(\text{NLO})}?$


Lowest mandatory order" (LMO) representation at NLO in that it retains only the unambiguous terms up to order a_s^3 required by order-by-order factorization and scale invariance. Any ACOT-like scheme must contain such terms.

Further simplifications in ACOT-type schemes

One generally can augment $d\sigma_{\text{GMVFN}}^{\text{NLO}}$ with extra radiative contributions from higher orders with the goal to improve consistency with the specific GMVFN scheme adopted in the fit of the used PDFs. The GMVFN scheme assumed for determination of CTEQ-TEA PDFs with up to 5 active flavors is closely matched with the following additional choices:

1. Evolve $\alpha_s(\mu)$ and PDFs $f_i(\xi, \mu)$ with $N_f = 5$ at $\mu \geq m_b$. The hard cross sections are also evaluated with $N_f = 5$ in virtual loops both for massive and massless channels. If the virtual contributions are obtained in the $N_f = 4$ scheme, they should be converted to the $N_f = 5$ scheme by adding known terms to the hard cross sections
2. The sums over initial-state light quarks and antiquarks in $d\sigma_{\text{GMVFN}}^{\text{NLO}}$ are extended to also include the b-quark PDF via the introduction of the singlet PDF $\Sigma \equiv \sum_{i=1}^5 (f_i + \bar{f}_i)$
3. replace $\tilde{f}_Q^{(1)}$ in $d\sigma_{\text{sub}}^{\text{NLO}}$ and $\delta f_Q^{(1)}$ in $d\sigma_{\text{GMVFN}}^{\text{NLO}}$ by $f^{(\text{NLO})}$ and $\delta f^{(\text{NLO})}$, respectively.
4. The α_s and PDFs must be evolved at least at NLO, although evolution at NNLO is acceptable or even desirable in some contexts.
5. In the hard cross sections inside $d\sigma_{\text{FE}} - d\sigma_{\text{sub}}$, dependence on the HQ mass can be eliminated altogether or simplified, producing a difference only in higher-order terms.

Further simplifications in ACOT-type schemes

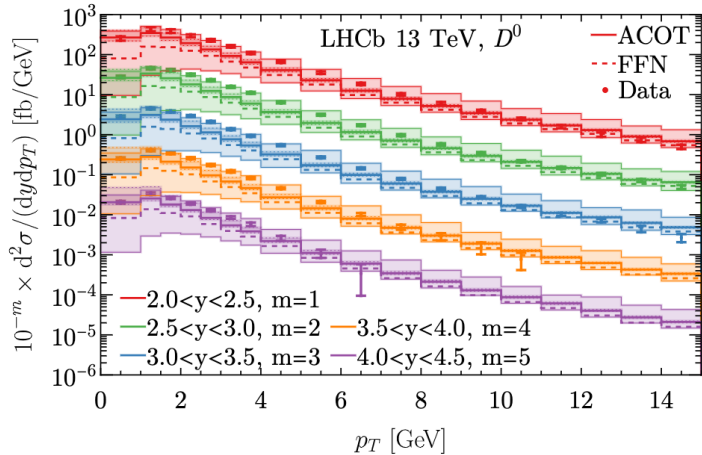
With the simplifications discussed above, we obtain

$$\tilde{f}_Q^{(1)} = a_s \left[A_{Qg}^{S,(1)} \triangleleft g \right], \quad \tilde{f}_Q^{(2)} = a_s^2 \left[A_{Qq}^{\text{PS},(2)} \triangleleft \Sigma + A_{Qg}^{S,(2)} \triangleleft g \right]$$

$$\tilde{f}_Q^{(\text{NLO})}(x, \mu) \equiv \tilde{f}_Q^{(1)} + \tilde{f}_Q^{(2)} \quad \delta f_Q^{(\text{NLO})} = f_Q - \tilde{f}_Q^{(\text{NLO})}$$

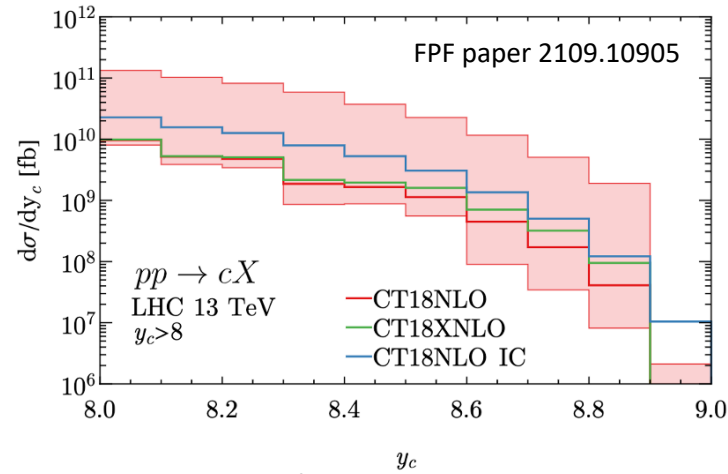
$$\begin{aligned} d\sigma_{\text{ACOT}}^{\text{NLO}} = d\sigma_{\text{FC}}^{\text{NLO}} + & \left(a_s f_g \triangleright d\hat{\sigma}_{gQ \rightarrow ZQ}^{(1)} \right. \\ & \left. + a_s^2 f_g \triangleright d\hat{\sigma}_{gQ \rightarrow ZQ(g)}^{(2)} + a_s^2 \Sigma \triangleright d\hat{\sigma}_{qQ \rightarrow ZQ(q)}^{(2)} \right) \triangleleft \delta f_Q^{(\text{NLO})} + (\text{exch.}). \end{aligned}$$

Other results using ACOT-like schemes



Transverse momentum at central rapidity at LHCb 13TeV (LHCb data from JHEP 03 (2016) 159).

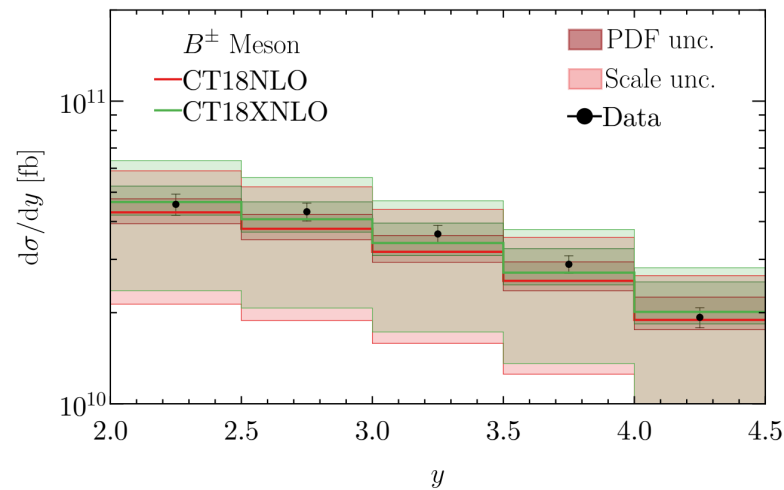
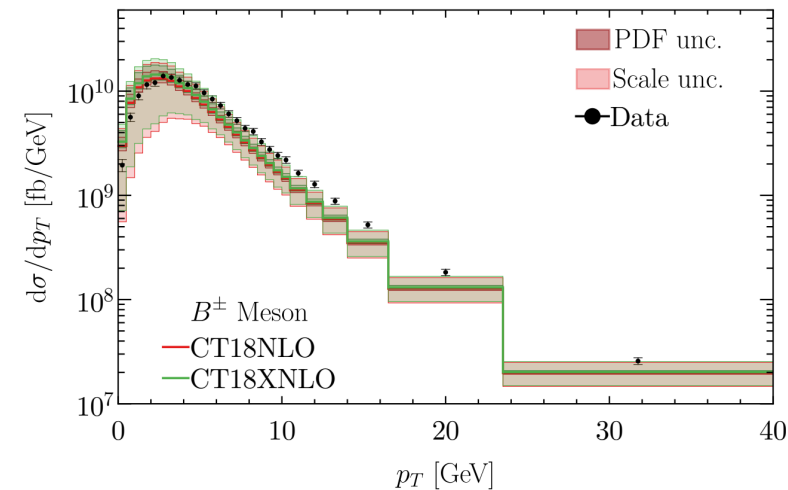
Error bands are scale uncertainties.



Rapidity distributions of prompt charm at the LHC 13 TeV in the very forward region ($y_c > 8$). Error band represents the CT18NLO induced PDF uncertainty at 68% C.L.

Charm hadroproduction and Z + c production at the LHC can constrain the IC contributions. LHCb Z+c data deserve attention as they can potentially discriminate gluon functional forms at $x \geq 0.2$ and improve gluon accuracy.

For small x below 10^{-4} , higher-order QCD terms with $\ln(1/x)$ dependence grow quickly at factorization scales of order 1 GeV. FPF facilities like FASERv will access novel kinematic regimes where both large- x and small- x QCD effects contribute to charm hadroproduction rate.



NLO theory predictions for the p_T and y distributions obtained with CT18NLO and CT18XNLO PDFs compared to B^\pm production data from LHCb 13 TeV [[arXiv:2203.06207](https://arxiv.org/abs/2203.06207)]

Theoretical uncertainties at NLO are large ($O(50\%)$) and mainly ascribed to scale variation. This can be improved by including higher-order corrections which imply an extension of the S-ACOT-MPS scheme to NNLO

Concluding remarks

- We developed the theory framework to extend ACOT-like schemes to pp collisions
- ACOT/S-ACOT used to describe Z+b production differentially at NLO in QCD
- Technically possible to generate predictions within the ACOT-type schemes at NNLO
- Important to constrain heavy-flavor PDFs: direct access to c/b-PDF
- Subtracted PDFs provided in the form of LHAPDF grids to for pheno applications
- Work toward simplifying implementation of GMVFN schemes in (N)NLO QCD calculations using the formalism of subtracted PDFs