



TECHNISCHE
UNIVERSITÄT
WIEN

FWF Österreichischer
Wissenschaftsfonds

$\int dk \Pi$

Doktoratskolleg
Particles and Interactions

Pre-hydrodynamic jet momentum broadening beyond the jet quenching parameter

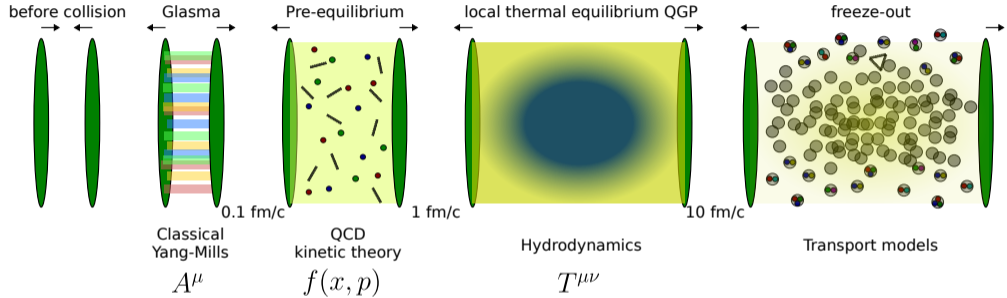
2303.12595 & 2312.00447 with K. Boguslavski, A. Kurkela, T. Lappi, J. Peuron
and based on work in preparation with Alois Altenburger & Kirill Boguslavski,

Florian Lindenbauer

TU Wien

15.11.2024, Light ion collisions at the LHC, CERN

Time-evolution of the QGP in heavy-ion collisions



- Different stages in time evolution¹

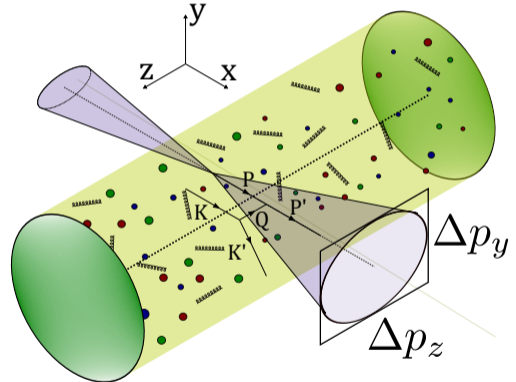
- Light-ion collisions

→ **Pre-equilibrium/pre-hydrodynamic stages more important**

¹[Rev.Mod.Phys. 93 (2021) [Berges, Heller, Mazeliauskas, Venugopalan]]

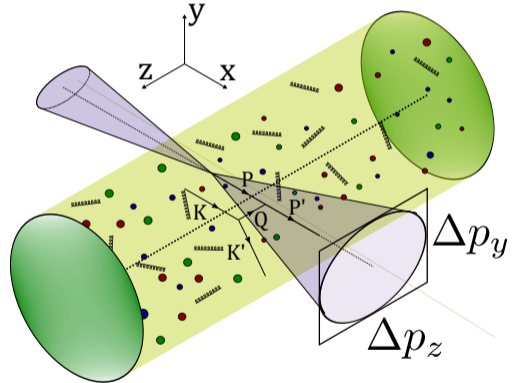
Hard probes to study pre-hydrodynamic evolution

- Study pre-hydrodynamic evolution
→ very **energetic** or **heavy** probes
- Here depicted: **jets**



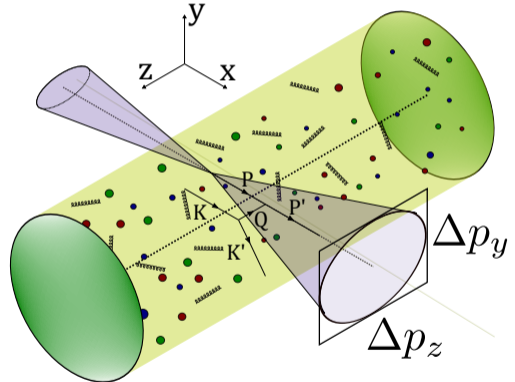
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→ then measured in the detectors
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 - Imprints of **medium interactions**
- Probe physics of **nonequilibrium QCD**



Motivation summary

Light ions

- System initially very out of equilibrium
- Smaller medium → **shorter hydrodynamic stage**
- Opportunity for studying **QCD out of equilibrium**

Why jets?

- Created early
→ **sensitive to out-of-equilibrium** medium

Jet energy loss through medium-induced radiation

- Energy loss dominated by gluon radiation

- **Energy loss** dominated by **gluon radiation**
- Depends on effective propagator
Input: **dipole cross section**

$$C(\mathbf{b}) = \int \frac{d^2\mathbf{q}_\perp}{(2\pi)^2} C(\mathbf{q}_\perp) \left(1 - e^{i\mathbf{b}\cdot\mathbf{q}_\perp}\right)$$

$$C(\mathbf{q}_\perp) = (2\pi)^2 \frac{d\Gamma^{\text{el}}}{d^2\mathbf{q}_\perp}$$

See also JHEP 07 (2020) [Andres, Apolinário, Dominguez], JHEP 10 (2021) [Moore, Schlichting, Schlusser, Soudi], PRD 105 (2022) [Schlichting, Soudi]

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- **Harmonic approximation**: (small b limit)
Dependence on single medium parameter \hat{q}

$$C(\mathbf{b}) \approx \frac{1}{4} \hat{q} \mathbf{b}^2 + \dots$$

“**Jet quenching parameter**”

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- Quantifies **momentum broadening**

$$\hat{q} = \frac{d\langle p_\perp^2 \rangle}{dL} = \frac{d\langle p_\perp^2 \rangle}{dt} = \int d^2q_\perp q_\perp^2 \frac{d\Gamma^{\text{el}}}{d^2q_\perp}$$

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$$\hat{q} = \hat{q}^{yy} + \hat{q}^{zz}$$

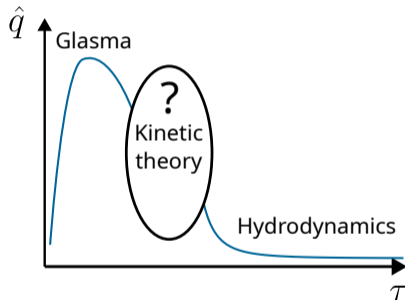
- Most jet implementations:
based on static media.
- Recent generalization to non-static systems²

²Phys.Rev.D 104 (2021) [Sadofyev, Sievert, Vitev], Phys.Rev.D 108 (2023) [Barata, Mayo López, Sadofyev, Salgado]

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[Avramescu, Baran, Greco, Ipp, Müller, Ruggieri]]

- Most jet implementations: based on static media.
- Recent generalization to non-static systems²
- **Medium input:** \hat{q} (or $C(\mathbf{b})$)
- Recent studies in the initial Glasma stage: \hat{q} very large³
- **Goal:** \hat{q} during hydrodynamization
→ between Glasma and hydro

Schematic \hat{q} evolution

²Phys.Rev.D 104 (2021) [Sadofyev, Sievert, Vitev], Phys.Rev.D 108 (2023) [Barata, Mayo López, Sadofyev, Salgado]

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Effective kinetic theory description of the QGP

- Gluons with **distribution function** $f(t, \mathbf{p})$

⁴[JHEP 01 (2003) [Arnold, Moore, Yaffe], Int.J.Mod.Phys.E 16 (2007) [Arnold]] 

Effective kinetic theory description of the QGP

- Gluons with **distribution function** $f(t, \mathbf{p})$
- Time evolution described by **Boltzmann equation** at leading-order⁴

$$(\partial_t + \mathbf{v} \cdot \nabla) f = \underbrace{\left| \begin{array}{c} \text{[Feynman diagram: two red lines merging into one with a red wavy line loop]} \end{array} \right|^2 + \left| \begin{array}{c} \text{[Feynman diagram: one red line passing through a blue rectangular box with a red wavy line loop]} \end{array} \right|^2}_{\text{Collision term}}$$

- Azimuthal symmetry around beam axis \hat{z} ,
Bjorken expansion, homogeneous in transverse plane

⁴[JHEP 01 (2003) [Arnold, Moore, Yaffe], Int.J.Mod.Phys.E 16 (2007) [Arnold]]

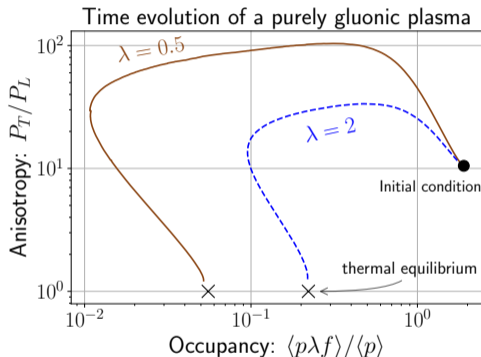
Bottom-up thermalization in heavy-ion collisions

- Initial condition⁵, with $\lambda = g^2 N_C$

$$f(p_{\perp}, p_z) = \frac{2A}{\lambda} \frac{\langle p_T \rangle}{\sqrt{p_{\perp}^2 + \xi_0^2 p_z^2}} \times \exp\left(\frac{-2}{3\langle p_T \rangle^2} (p_{\perp}^2 + \xi_0^2 p_z^2)\right)$$

$\xi_0 \sim$ anisotropy, $\langle p_T \rangle = 1.8Q_s$,

$Q_s \sim$ saturation scale



⁵[Phys.Rev.Lett. 115 (2015) [Kurkela, Zhu]]

⁶[Phys.Lett.B 502 (2001) [Baier, Mueller, Schiff, Son]]

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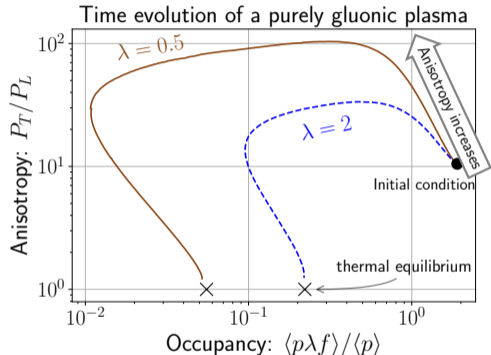
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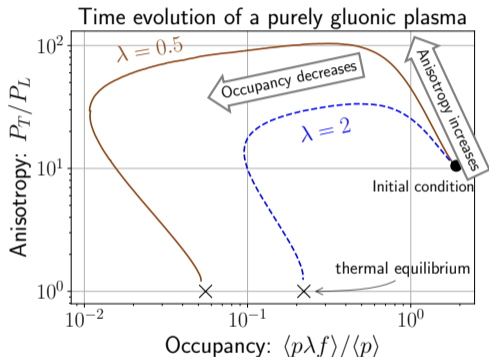
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- Phase 1:** Anisotropy increases
- Phase 2:** Occupancy decreases



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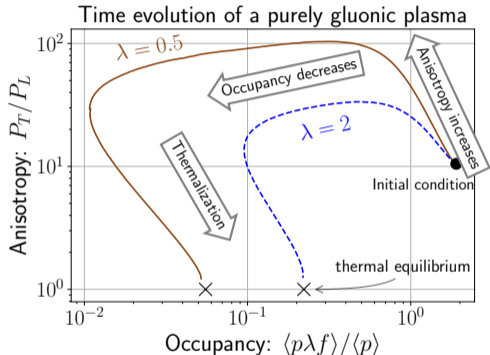
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- Phase 1:** Anisotropy increases
- Phase 2:** Occupancy decreases
- Phase 3:** System thermalizes at

$$\text{time}^6 \tau_{\text{BMSS}} = \left(\frac{\lambda}{12\pi}\right)^{-13/5} / Q_s$$



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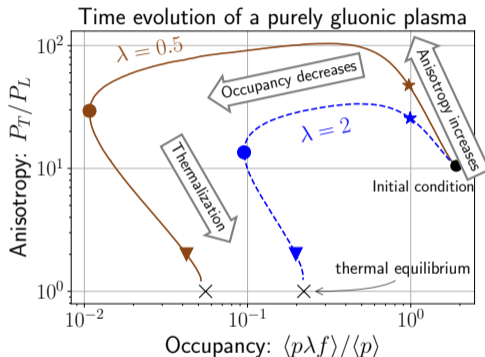
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Markers represent **different stages**

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- From $f(\mathbf{k})$ we obtain:

Jet momentum broadening in kinetic theory

- From $f(\mathbf{k})$ we obtain: Outgoing plasma particle

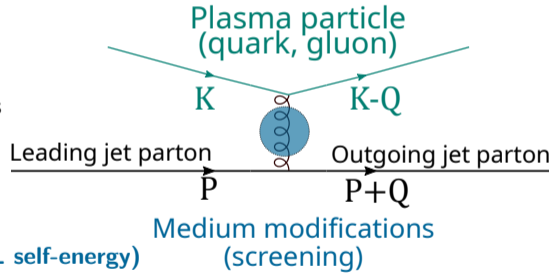
$$\hat{q}^{ij} = \int_{\substack{q_{\perp} < \Lambda \\ p \rightarrow \infty}} d\Gamma_{\text{PS}} q^i q^j |\mathcal{M}|^2 f(\mathbf{k}) (1 + f(\mathbf{k}'))$$

Incoming plasma particles
with momentum k

Matrix element
with medium corrections (HTL self-energy)

appropriate phase-space measure

Matrix element



Jet momentum broadening in kinetic theory

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$$C(\mathbf{q}_\perp) = \int_{p \rightarrow \infty} d\Gamma_{\text{PS}}$$

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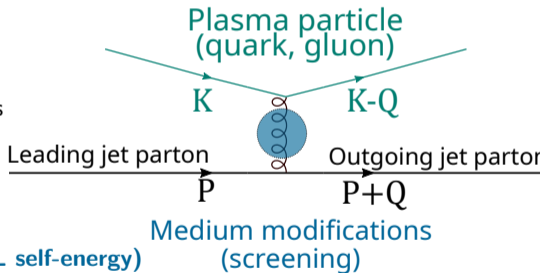
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- Logarithmic cutoff Λ_{\perp} dependence⁷

$$\hat{q}^{xx}(\Lambda_{\perp} \gg T_{\varepsilon}) \simeq a_x \ln \frac{\Lambda_{\perp}}{Q_s} + b_x$$

(and similar for \hat{q}^{yy})

⁷[Values available at <https://zenodo.org/records/10419537>]

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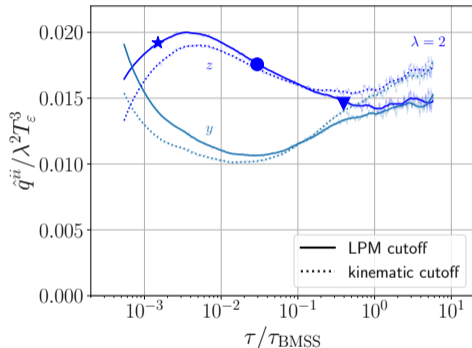
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- Cutoff models for dependence on jet energy and effective temperature

- $\Lambda_{\perp}^{\text{LPM}}(E, T_{\varepsilon}) = \zeta^{\text{LPM}} g \times (ET_{\varepsilon}^3)^{1/4}$

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[Phys.Lett.B 850 (2024) [Boguslavski, Kurkela, Lappi, FL, Peuron]]

Plot for $E = 100 \text{ GeV}$

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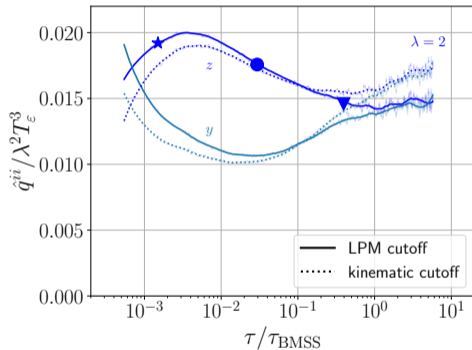
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→ **Enhanced broadening along beam axis**

- Similar results for both cutoffs



[Phys.Lett.B 850 (2024) [Boguslavski, Kurkela, Lappi, FL, Peuron]]

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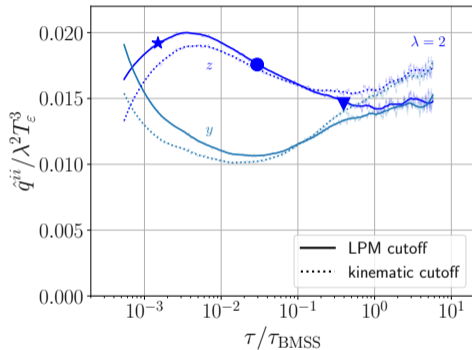
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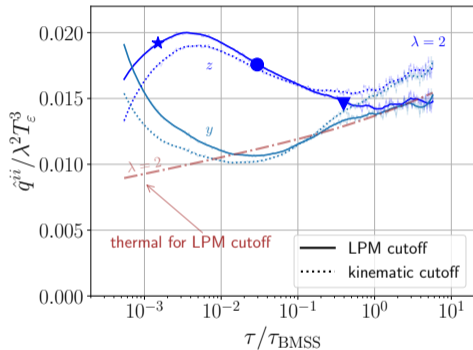
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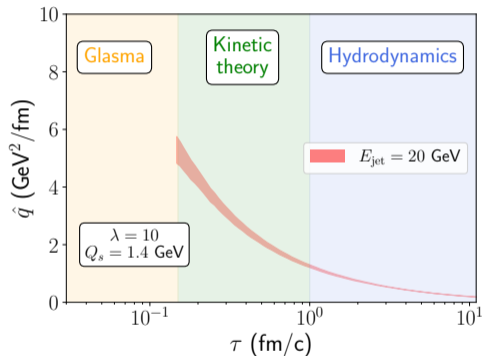


[Phys.Lett.B 850 (2024) [Boguslavski, Kurkela, Lappi, FL, Peuron]]

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Time evolution of jet quenching parameter

- Model cutoff variation for fixed jet energy
- Dependence on initial conditions and cutoff (bands)

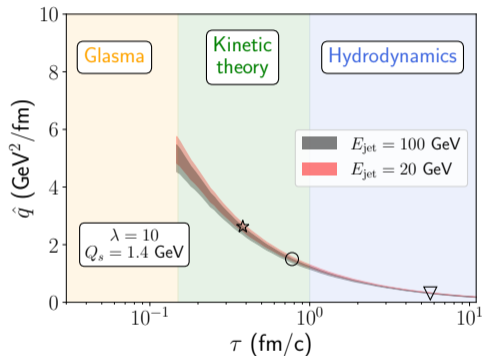


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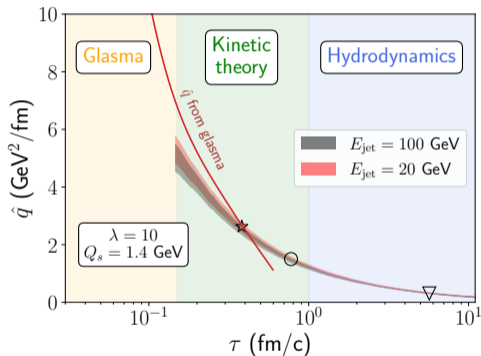


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Time evolution of jet quenching parameter

- Model cutoff variation for fixed jet energy
- Dependence on initial conditions and cutoff (bands)
- Little jet energy dependence
- Supports **large values** from **Glasma**⁷ and lower values in hydrodynamic stage



[Phys.Lett.B 850 (2024) [Boguslavski, Kurkela, Lappi, FL, Peuron]]

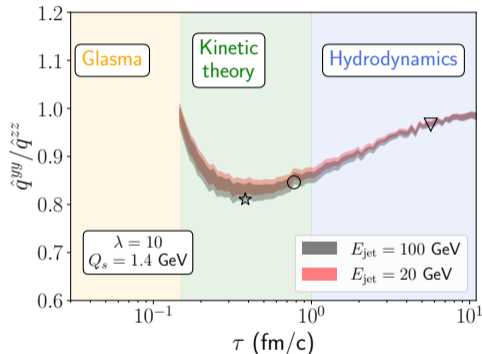
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Time evolution of jet quenching parameter

- Model cutoff variation for fixed jet energy
- Dependence on initial conditions and cutoff (bands)
- Little jet energy dependence
- Broadening **anisotropy** up to 15 %
- Possible impact on polarization⁷, azimuthal and spin observables⁸

⁷[JHEP 08 (2023) [Hauksson, Iancu]]

⁸[arXiv:2407.04774 [Barata, Salgado, Silva]]



[Phys.Lett.B 850 (2024) [Boguslavski, Kurkela, Lappi, FL, Peuron]]

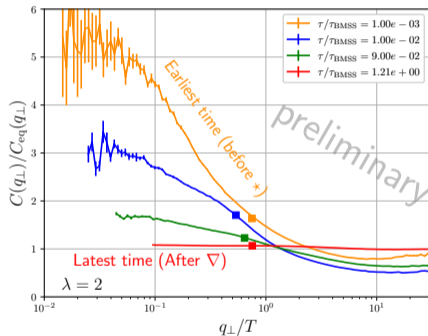
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Normalize using (Landau-matched) thermal kernel, with small q_\perp form⁹

$$C_{\text{equ}}(q_\perp \ll T) = \frac{C_R g^2 T m_D^2}{q_\perp^2 (q_\perp^2 + m_D^2)}$$



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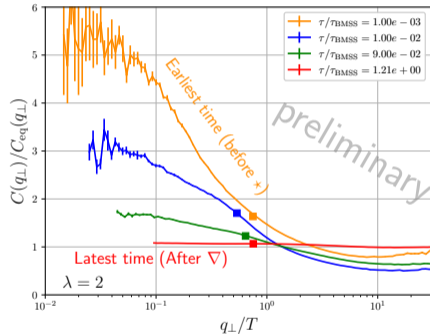
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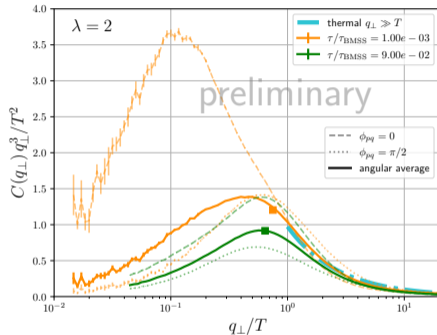
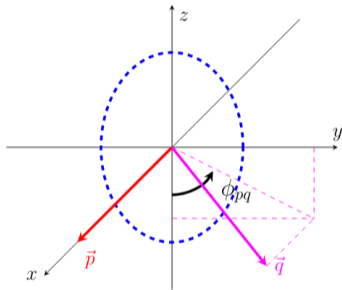
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- Momentum transfer of soft momenta enhanced
- Late times (red curve): Thermal

⁹[JHEP 05 (2002) [Aurenche, Gelis, Zaraket]]



Angular dependence and contribution to \hat{q}



- Contribution to $\hat{q} = \int d^2\mathbf{q}_\perp q_\perp^2 C(\mathbf{q}_\perp)/(2\pi)$
- **Peaked at Debye mass** ■ for later times
- Along beam ($\phi_{pq} = 0$): Much larger and different form at early times

Conclusions and outlook

- Out-of-equilibrium plasma described by kinetic theory
→ important for light-ion collisions
- Studied **momentum broadening of jets**
→ \hat{q} and $C(\mathbf{q}_\perp)$ during initial stages in heavy-ion collisions
→ input for jet quenching simulations
- Values of \hat{q} within $\sim 20\%$ of thermal estimate
- More momentum broadening along the beam axis ($\hat{q}^{zz} > \hat{q}^{yy}$)
- $C(\mathbf{q}_\perp)$ at small \mathbf{q}_\perp is enhanced compared to thermal (especially along beam)

Outlook

- Obtain gluon emission spectrum from pre-equilibrium \hat{q} (with Barata, Sadofyev)
- Inclusion of quarks in plasma background (with Mazeliauskas, Takaçs, Zhou)

Thank you very much for your attention!

FL is a recipient of a DOC Fellowship of the Austrian Academy of Sciences at the University TU Wien. This work is supported by the Austrian Science Fund (FWF) under project DOI 10.55776/P34455 and 10.55776/W1252

Screening in the matrix element of \hat{q}

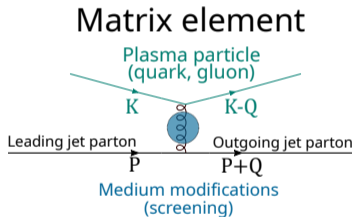
- Scattering matrix element includes **in-medium propagator**
- Receives **self-energy corrections**
- Anisotropic hard thermal loop (HTL) self-energy \rightarrow unstable modes¹⁰
- **Approximation: Use isotropic HTL matrix element**

Similar approximation also in EKT implementations¹¹

¹⁰[Phys.Rev.D 68 (2003) [Romatschke, Strickland]]

¹¹[Phys.Rev.Lett. 115 (2015) [Kurkela, Zhu]; Phys.Rev.Lett. 122 (2019) [Kurkela, Mazeliauskas];

Phys.Rev.D 104 (2021) [Du, Schlichting]]

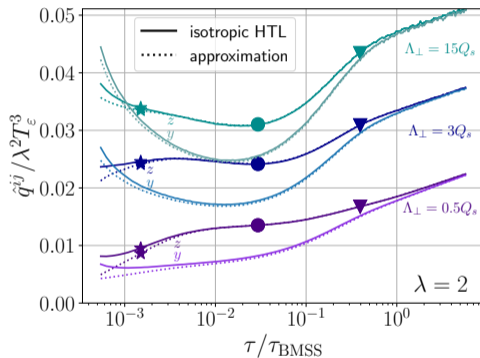


Screening approximation to the matrix element

- Compare with simple screening approximation

$$\frac{(s-u)^2}{t^2} \rightarrow \frac{(s-u)^2}{t^2} \frac{q^4}{(q^2 + \xi_T^2 m_D^2)^2}$$

- Longitudinal¹² $\xi_L = e^{5/6}/\sqrt{8}$
- Transverse broadening:
 $\xi_T = e^{1/3}/2$
- **Good agreement**

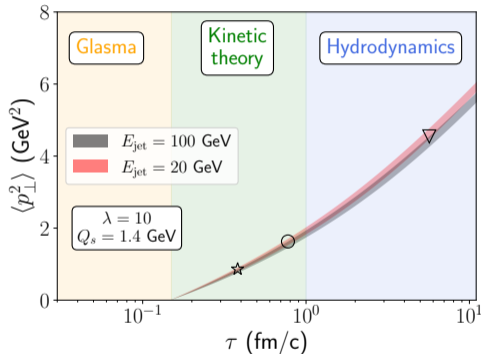


s, u, t : Mandelstam variables

¹²[Phys.Rev.D 89 (2014) [York, Kurkela, Lu, Moore]]

What about total momentum broadening?

- Per definition, $\hat{q} = \frac{d\langle p_{\perp}^2 \rangle}{d\tau}$
- Naively $\Delta p_{\perp}^2 = \int d\tau \hat{q}(\tau)$ over lifetime of jet
- Think of \hat{q} as medium parameter.



Making sense of the cutoff

- Cutoff Λ_{\perp} restricts transverse momentum transfer $q_{\perp} < \Lambda_{\perp}$
(needed in eikonal limit $p \rightarrow \infty$)

$$\hat{q} \sim \int d^2 q_{\perp} q_{\perp}^2 \underbrace{\frac{d\Gamma^{\text{el}}}{d^2 q_{\perp}}}_{1/q_{\perp}^4 \text{ for large } q_{\perp}} \sim \int \frac{dq_{\perp}}{q_{\perp}}$$

Making sense of the cutoff

- Cutoff Λ_{\perp} restricts transverse momentum transfer $q_{\perp} < \Lambda_{\perp}$
(needed in eikonal limit $p \rightarrow \infty$)
- Cutoff should grow with jet energy
- **kinematic cutoff** $\Lambda_{\perp}^{\text{kin}}(E, T) = \zeta^{\text{kin}} g(ET)^{1/2}$
obtained from comparing leading log behavior for large p and Λ_{\perp}
- **LPM cutoff** $\Lambda_{\perp}^{\text{LPM}}(E, T) = \zeta^{\text{LPM}} g(ET^3)^{1/4}$
Estimate for momentum broadening during LPM 'formation time':
 $Q_{\perp}^2 \sim \hat{q} t^{\text{form}}, t^{\text{form}} \sim \sqrt{E/\hat{q}},$ approximately $\hat{q} \sim g^4 T^3$

[arXiv:2312.00447 [Boguslavski, Kurkela, Lappi, FL, Peuron]]